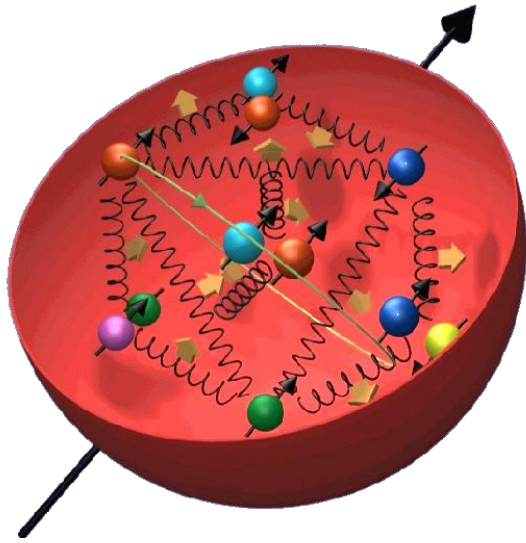




The Nucleon Spin Structure



Gerhard Mallot



Plan

- Lecture I
 - Introduction
 - DIS and structure functions, sum rules
 - Why contribute the quark spin so little?
 - Principle of measurements, experiments

Spin Experiments are Puzzling



Wolfgang Pauli and Niels Bohr, 1954

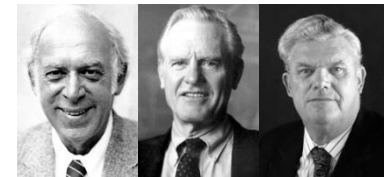
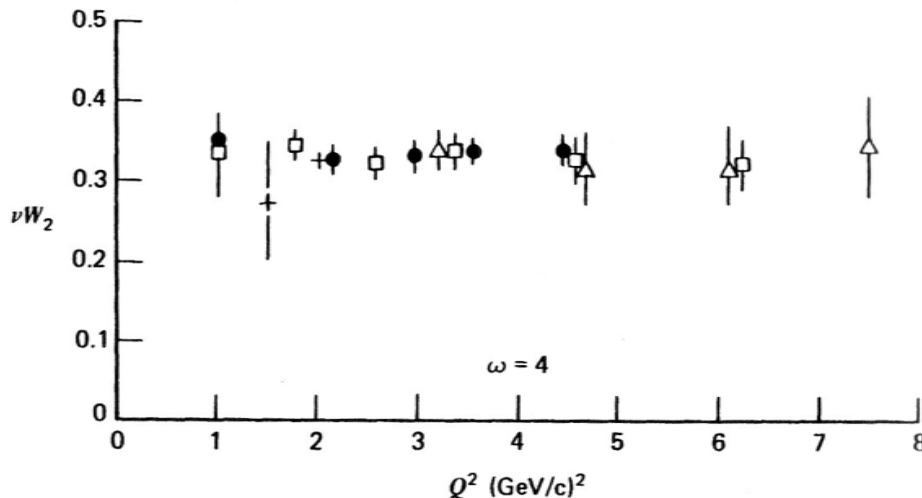
wondering about a tippe top toy

A theory of the nucleon needs to describe the dynamics of quarks and gluons including spin.

Imagine the theory of the atom without spin!

1. Introduction

- electron scattering at SLAC in the late 1960ies revealed **point-like partons** in the nucleon \rightarrow **quarks**
- structure function is Q^2 independent (scaling)



Friedman, Kendall, Taylor



1990

Quark model wave function

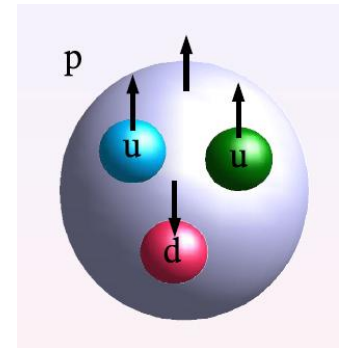
$$SU_{\text{spin}}(2) \times SU_{\text{flavour}}(3)$$

$$|p \uparrow\rangle = \frac{1}{\sqrt{18}} \left\{ 2|u \uparrow u \uparrow d \downarrow\rangle - |u \uparrow u \downarrow d \uparrow\rangle - |u \downarrow u \uparrow d \uparrow\rangle + (u \leftrightarrow d) \right\}$$

$$\Delta u = \langle p \uparrow | N_{u \uparrow} - N_{u \downarrow} | p \uparrow \rangle = \frac{3}{18} (10 - 2) = \frac{4}{3}$$

$$\Delta d = \langle p \uparrow | N_{d \uparrow} - N_{d \downarrow} | p \uparrow \rangle = \frac{3}{18} (2 - 4) = -\frac{1}{3}$$

$$\Delta \Sigma = \Delta u + \Delta d = 1$$



→ up and down quarks carry the nucleon spin!

Weak baryon decays

- weak decay constants are linked to quark polarisations via the axial vector currents matrix elements

$$2MS_\mu\Delta q = \langle P, S | \bar{q}\gamma_\mu\gamma_5 q | P, S \rangle$$

- SU(3) flavour symmetry assumed

Decay $A \rightarrow B\ell\nu$	Rate(10^6 s^{-1})		g_1/f_1 $\ell = e^-$
	$\ell = e^\pm$	$\ell = \mu^-$	
$n \rightarrow p$	1.1291 ± 0.0010		1.2670 ± 0.0030
$\Lambda^0 \rightarrow p$	3.161 ± 0.058	0.60 ± 0.13	0.718 ± 0.015
$\Sigma^- \rightarrow n$	6.88 ± 0.23	3.04 ± 0.27	-0.340 ± 0.017
$\Sigma^- \rightarrow \Lambda^0$	0.387 ± 0.018		
$\Sigma^+ \rightarrow \Lambda^0$	0.250 ± 0.063		
$\Xi^- \rightarrow \Lambda^0$	3.35 ± 0.37	2.1 ± 2.1	0.25 ± 0.05
$\Xi^- \rightarrow \Sigma^0$	0.53 ± 0.10		
$\Xi^0 \rightarrow \Sigma^+$	0.876 ± 0.071	$0.012 \pm 0.007^*$	1.32 ± 0.21

$$\begin{aligned} &\Delta u - \Delta d \\ &2\Delta u - \Delta d - \Delta s \\ &\Delta d - \Delta s \\ &\Delta u + \Delta d - 2\Delta s \\ &\Delta u - \Delta d \\ &\Delta u - \Delta d \end{aligned}$$

From weak baryon decays

Fit to decay data:

$$\Delta u + \Delta d - 2\Delta s = 0.58 \pm 0.03 \quad (\Xi^- \rightarrow \Lambda)$$

assuming $\Delta s = 0$:

$$\Delta\Sigma = \Delta u + \Delta d = 0.58 \pm 0.03$$

→ up and down quarks carry 58% of the nucleon spin!
deviation from 100% due to relativistic motion

Spin puzzle: EMC 1987



$$\Gamma_1 = \int_0^1 g_1(x) dx$$

$$\Delta\Sigma = \Delta u + \Delta d + \Delta s = 0.12 \pm 0.17$$

$$\Delta s = -0.19 \pm 0.06$$

→ quark spin contribution to nucleon spin is consistent with zero! Strange quark polarisation negative.

2. DIS and structure functions

- What did the EMC actually measure?
- How severe is the spin puzzle?
- Can the Quark Model expectation

$$\Delta\Sigma = 0.6$$

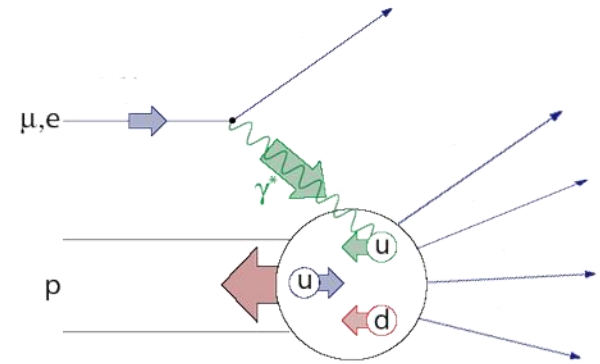
be restored?

Deep inelastic scattering

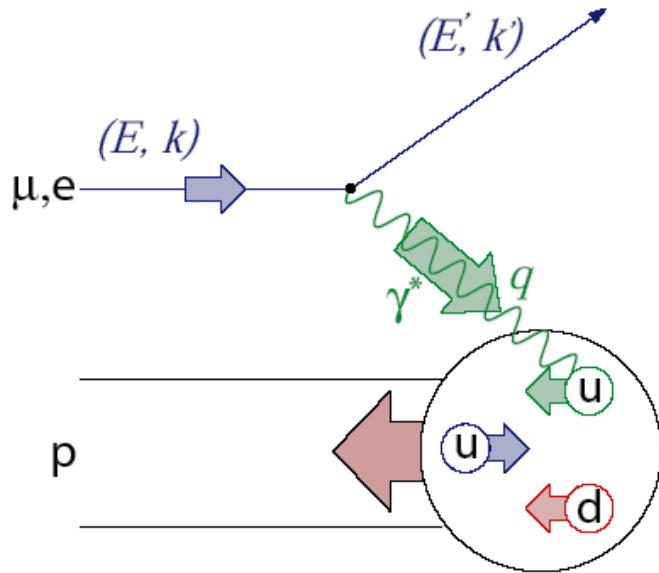
- probing partons

$$\ell N \rightarrow \ell' X$$

- **inclusive** lepton – nucleon scattering
- large **momentum** and **energy** transfer Q^2 and ν
- finite ratio Q^2 / ν
- large **c.m. energy** of the hadronic final state $W > 2 \text{ GeV}$



Deep Inelastic Scattering



$$Q^2 = -(k - k')^2 \stackrel{lab}{=} 4EE' \sin^2 \frac{\vartheta}{2}$$

$$P \cdot q \stackrel{lab}{=} M\nu = M(E - E')$$

$$P \cdot k \stackrel{lab}{=} ME$$

$$x \stackrel{lab}{=} \frac{Q^2}{2M\nu} = \frac{-q^2}{2P \cdot q}$$

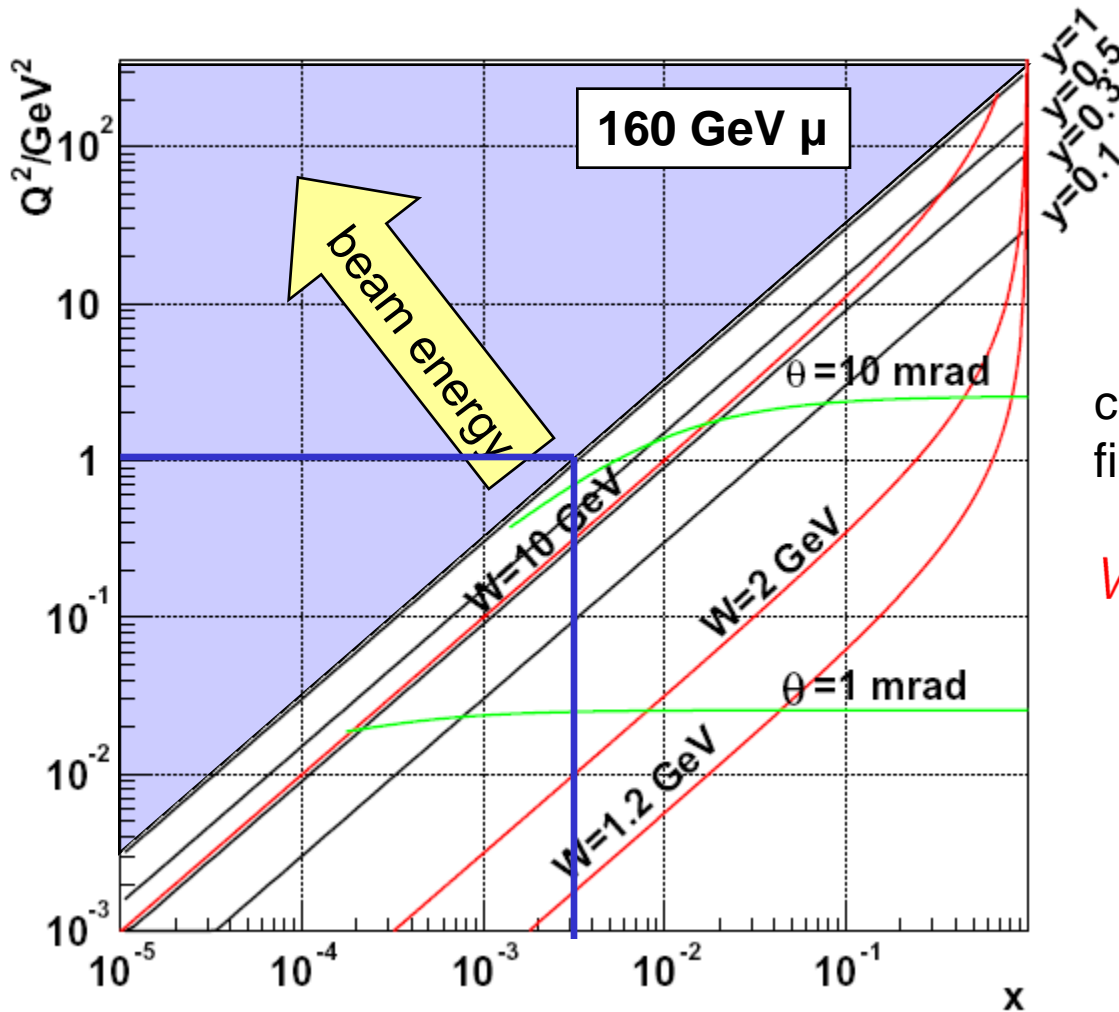
$$y \stackrel{lab}{=} \frac{\nu}{E} = \frac{P \cdot q}{P \cdot k}$$

$$0 \leq x, y \leq 1$$

Bjorken- x : fraction of longitudinal momentum carried by the struck quark in infinite-momentum frame (Breit)



Kinematics



$$y = \frac{\nu}{E}$$

$$x_{min} = \frac{Q^2}{2ME}$$

c.m. energy of hadronic final state, W :

$$W^2 = (q + P)^2$$

$$= \frac{1-x}{x} Q^2 + M^2$$

DIS: $Q^2, W^2 \rightarrow \infty, x$ fix

Distance scales

- longitudinal $1/Mx$
- transverse $1/\sqrt{Q^2}$

- for $x \simeq 0.2$ the longitudinal scale is 1 fm
- for $Q^2 = 1 \text{ (GeV}/c)^2$ the transverse scale is 0.2 fm

DIS cross section

cross section:

lepton

spin

nucleon

$$\frac{d^3\sigma}{dx dy d\phi} = \frac{\alpha^2 y}{Q^4 2} L_{\mu\nu}(k, q, s) W^{\mu\nu}(P, q, S)$$

leptonic tensor $L_{\mu\nu}$: kinematics (QED)

hadronic tensor $W^{\mu\nu}$: nucleon structure

factorise

$$W^{\mu\nu} = - \left(g^{\mu\nu} - \frac{q^\mu q^\nu}{q^2} \right) F_1(x, Q^2) + \left(P^\mu - \frac{P \cdot q}{q^2} q^\mu \right) \left(P^\nu - \frac{P \cdot q}{q^2} q^\nu \right) \frac{1}{P \cdot q} F_2(x, Q^2) - i \epsilon^{\mu\nu\lambda\sigma} q_\lambda \left(\frac{M S_\sigma}{P \cdot q} (g_1(x, Q^2) + g_2(x, Q^2)) - \frac{M(S \cdot q) P_\sigma}{P \cdot q} g_2(x, Q^2) \right)$$

Quark-Parton Model

- in the QPM: $W^{\mu\nu}$ for massless spin-1/2 partons

$$F_1(x) = \frac{1}{2} \sum_i e_i^2 \{ q_i^+(x) + q_i^-(x) \}$$
$$F_2(x) = x \sum_i e_i^2 \{ q_i^+(x) + q_i^-(x) \}$$

unpolarised SF,
momentum distributions

$$g_1(x) = \frac{1}{2} \sum_i e_i^2 \{ q_i^+(x) - q_i^-(x) \}$$
$$g_2(x) = 0$$

polarised SF,
spin distributions

- no Q^2 dependence (scaling)
- Callan-Gross relation $F_2(x) = 2xF_1(x)$
- g_2 twist-3 quark-gluon correlations

Sum rules for g_1

- first moment Γ_1 of g_1 with $\Delta q = \int_0^1 \Delta q(x) dx$

$$\Gamma_1 = \int_0^1 g_1(x) dx \stackrel{\text{proton}}{=} \frac{1}{2} \left\{ \frac{4}{9} \Delta u + \frac{1}{9} \Delta d + \frac{1}{9} \Delta s \right\}$$

$$\Gamma_1^p = \frac{1}{12} \underbrace{(\Delta u - \Delta d)}_{a_3} + \frac{1}{36} \underbrace{(\Delta u + \Delta d - 2\Delta s)}_{\sqrt{3}a_8} + \frac{1}{9} \underbrace{(\Delta u + \Delta d + \Delta s)}_{a_0}$$

Neutron decay
 $a_3 = g_a$

Hyperon decay
 $(3F-D)/3$

$\Delta\Sigma$

From Γ_1 , a_3 and a_8 we obtain $\Delta\Sigma$ without assuming $\Delta s = 0$

Sum Rules

Bjorken
sum rule

PR 148 (1966) 1467

$$\Gamma_1^p - \Gamma_1^n = \frac{1}{6} g_a$$

if wrong \Rightarrow QCD wrong,
"worthless equation", needs
neutron measurement

Ellis-Jaffe
sum rule

PR D9 (1974) 1444

$$\Gamma_1^p = \frac{1}{12} g_a + \frac{5}{36} \sqrt{3} a_8$$

$$\Delta\Sigma \simeq 0.6$$

formulated for $\Delta s=0$,
unpolarised strange quarks

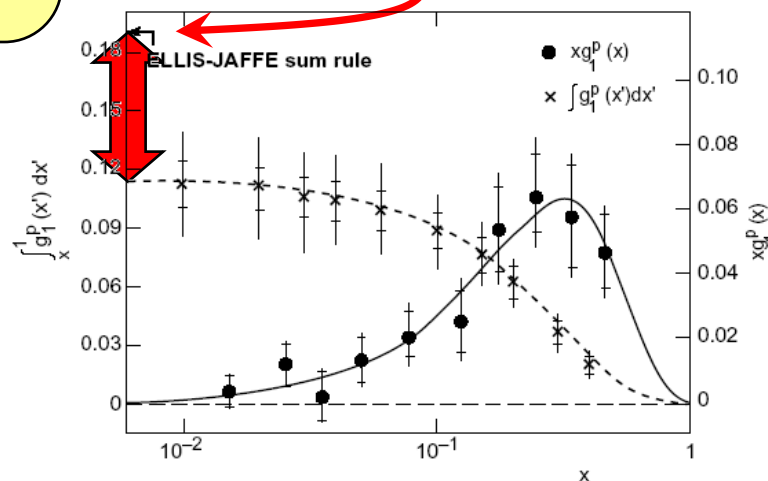
$$+ \frac{1}{3} \Delta s$$

Consequences of violation:

$$\Delta s = -0.19 \pm 0.06$$

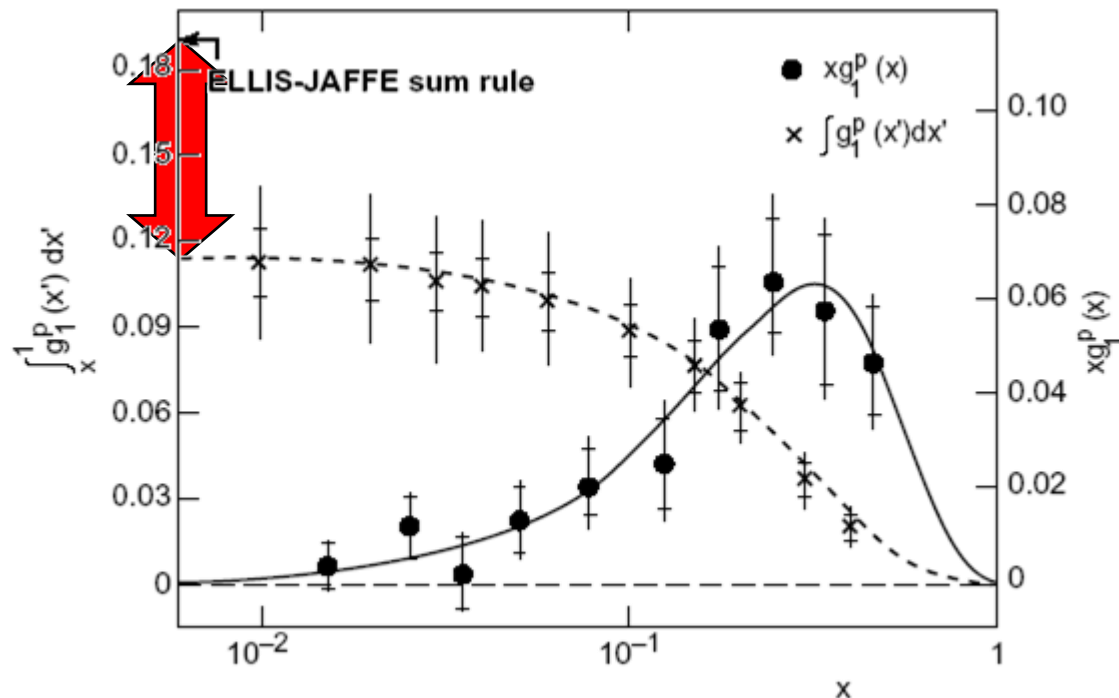
$$\Delta\Sigma = 0.12 \pm 0.17$$

EMC 1987



The First Moment of g_1

- first moment of g_1 $\Gamma_1 = \int_0^1 g_1(x) dx$



“Spin crisis”
EMC 1987

3. Why is $\Delta\Sigma$ so small

(1988)

CHIRAL SYMMETRY AND THE SPIN OF THE PROTON ☆

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PLB 206 (1988) 309

A crisis in the parton model: where, oh where is the proton's spin?

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Received 18 March 1988

ZPC 41 (1988) 239

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E2-88-287

SPIN STRUCTURE OF THE NUCLEON AND TRIANGLE ANOMALY

THE ANOMALOUS GLUON CONTRIBUTION TO POLARIZED LEPTOPRODUCTION

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Received 29 June 1988

PLB 212 (1988) 391

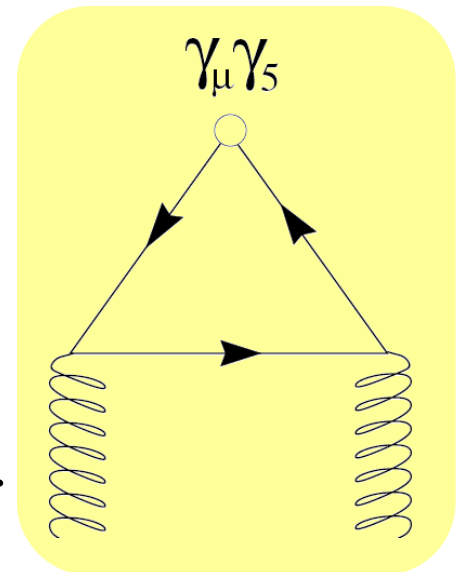
Considered Options

- Skyrmons: model,
all orbital angl. mom. (BEK) **maybe**
- Bjorken sum rule broken?
Measurement wrong? (LA) **no!**
- Large $\Delta G \sim 2-3-6$ at EMC Q^2 could mask
quark spin via **axial anomaly** (ET, AR) **measure
gluon!**

requires fine tuning of cancelation of ΔG and orbital angular momentum (orb. ang. mom. is generated at gluon emission)

Axial anomaly contribution

- The contribution of the quark spins $\Delta\Sigma$ is **NOT** an observable. The observable is a_0 , the **flavour-singlet axial vector** ME.
- The singlet axial vector current is not conserved and receives a gluon contribution via the **axial anomaly** (à la $\pi^0 \rightarrow 2\gamma$). The contribution vanishes for the triplet and octet currents.
- A conserved current can be constructed in next-to-leading order QCD by subtracting the anomalous gluon contribution, however, not in a gauge invariant way.
- The corresponding ME is then independent of Q^2 .



Axial anomaly (continued)

- in the $\overline{\text{MS}}$ renormalisation scheme

$$a_0 = \Delta\Sigma_{\text{MS}}$$

- in the so-called Alder–Bardeen and the jet scheme:

$$a_0 = \Delta\Sigma_{\text{AB}} - n_f \frac{\alpha_s}{2\pi} \Delta G$$

- thus a large gluon polarisation could mask the quark spin contribution to the nucleon spin and the parton model value of 0.6 could be restored by $\Delta\Sigma_{\text{AB}}$

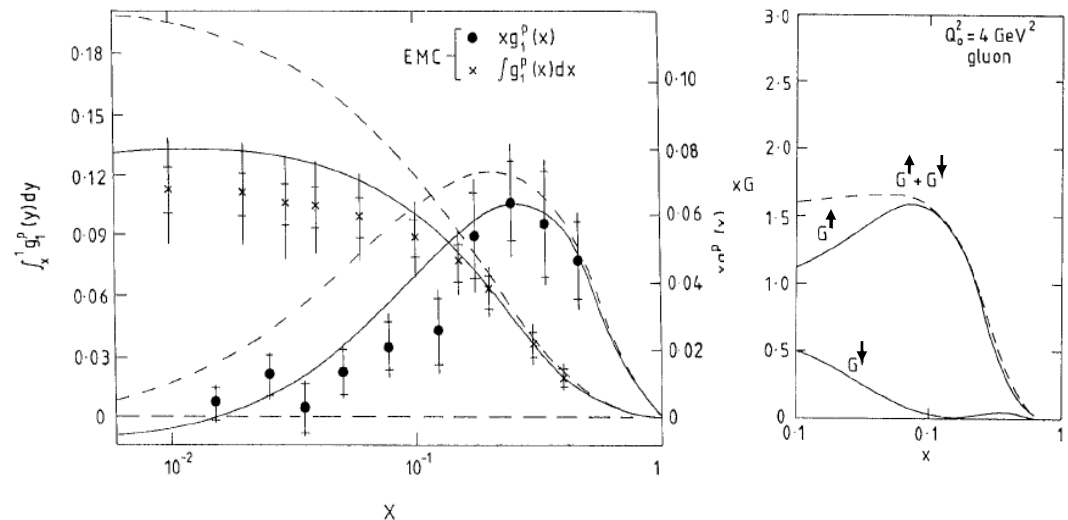
Lepton-Photon 1989

To summarise, let us return to the fit of Fig. 7 and 8. At $Q^2=10\text{GeV}^2$ this corresponds to $\Delta g=6.3$ and so the proton helicity is given by

$$\begin{aligned} \frac{1}{2} &= \frac{1}{2}\Delta\Sigma + \Delta g + L_z \\ &= 0.35 + 6.3 - 6.15 \end{aligned}$$

R.G. Ross 1989

Need $\Delta G \approx 6$ at
 $Q^2 = 10 \text{ GeV}^2$
 for $\Delta\Sigma = 0.7$,
 to be compared to $1/2$
 \Rightarrow measure ΔG

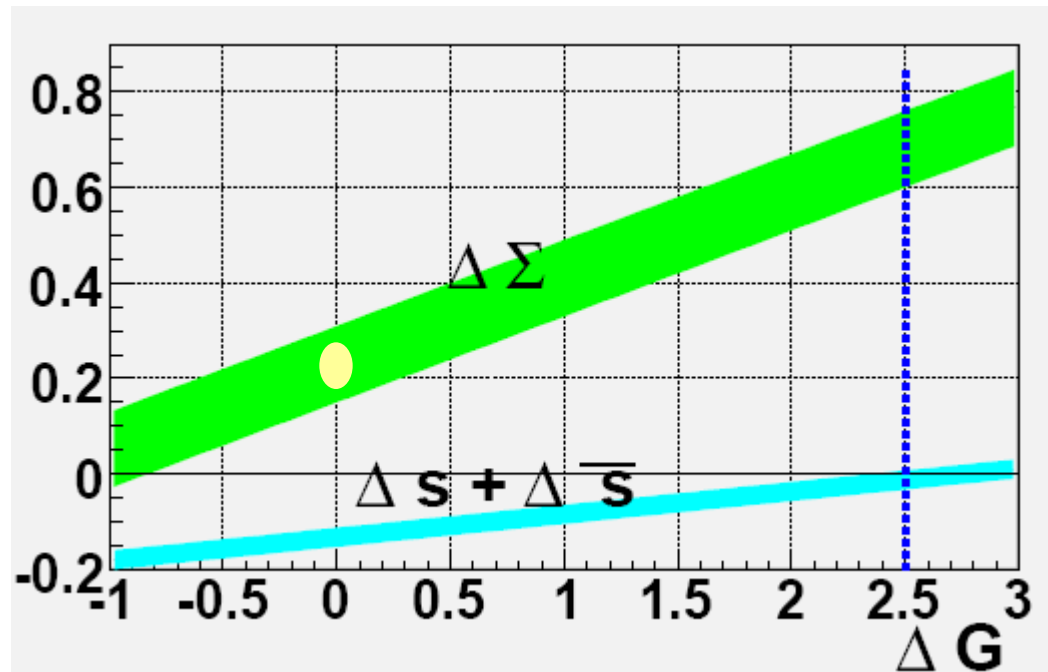


ΔG and $\Delta \Sigma$ in AB/jet scheme

$$\Delta \Sigma \leftarrow a_0 + \frac{3\alpha_s}{2\pi} \Delta G$$

α_s strong coupling constant

$$\Delta s \leftarrow \Delta s + \frac{3\alpha_s}{2\pi} \Delta G$$



Now:

$$a_0 \simeq 0.3$$

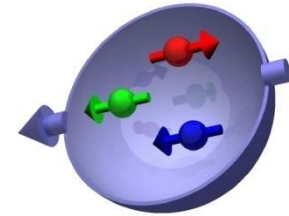
Need:

$$\Delta G \simeq 2.5$$

Spin sum rule

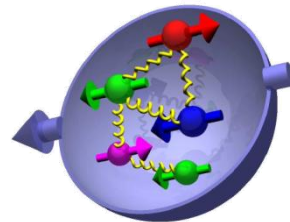
- naive QPM: only valence quarks

$$\Delta q_v$$



- QCD: sea quarks and gluons

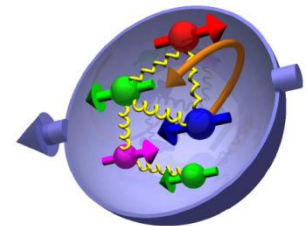
$$\Delta q_s, \Delta g$$



gluons carry 50% of momentum!

- orbital angular momentum:

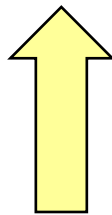
$$L_q, L_g$$



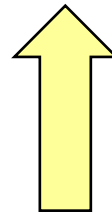
$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$

Where is the proton spin?

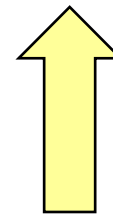
$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_z$$



small



poorly known
certainly not 6



unknown

Riddle

What is similar and what is different between the following two sets?:
The first set consists of a farmer, his pig and the truffles:



The second set consists of the theorist, the experimentalist and the big discoveries



A. De Rújula

not an experimentalist!

Answer

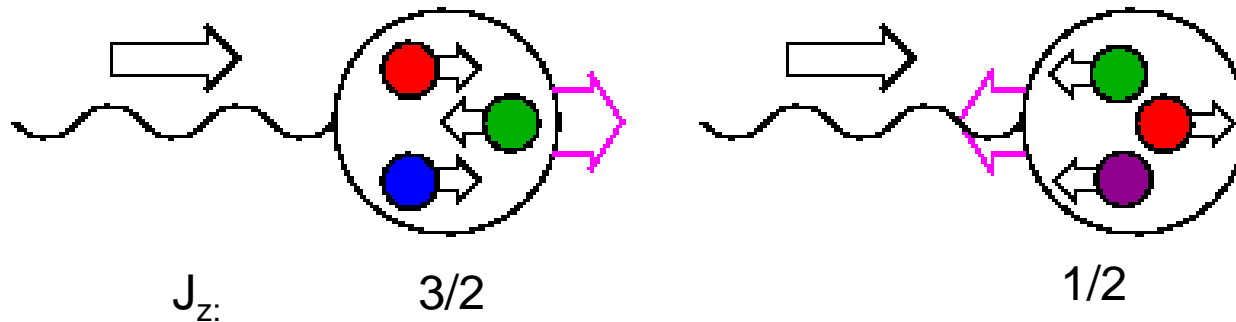
- The farmer takes his pig to the woods. The pig sniffs around looking for a truffle. When the pig gets it and is about to eat it, the farmer kicks the pig on the head with his club and steals the truffle. Those are the similarities...
- The difference is that the farmer always takes the pig to woods where there are truffles, while more often than not, the suggestions by the theorists take the experimentalists to "woods" where there are no “truffles”...
- ... often while looking for the theorists' “truffles” the experimentalists find “gold”...

<http://public.web.cern.ch/Public/Content/Chapters/AboutCERN/WhoWorksThere/ThinkersMakers/Theorists/Theorists-en.html>

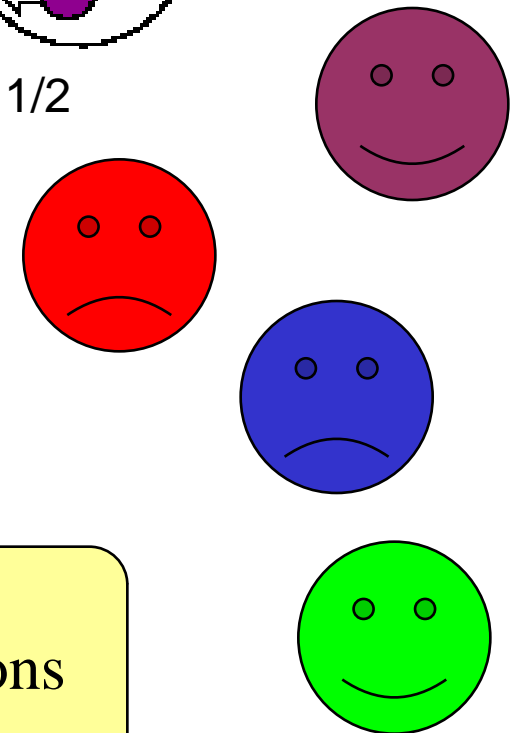
4. Principle of measurements

- Photoabsorption:

(flavours ignored)



- only quarks with opposite helicity can absorb the polarised photon via spin-flip
- # quarks in direction $\frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}}$ of nucleon



need polarised photons & nucleons

Cross Section Asymmetries

unpolarised:

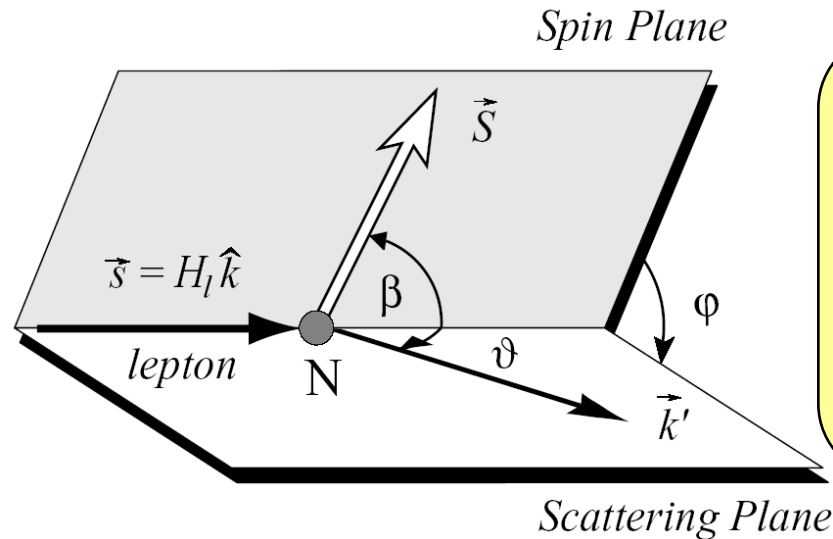
$$\frac{d^3\bar{\sigma}}{dx dy d\varphi} = \frac{4\alpha^2}{Q^2} \left\{ \frac{y}{2} F_1 + \frac{1}{2xy} \left(1 - y - \frac{y^2\gamma^2}{4} \right) F_2 \right\}$$

longitudinally polarised nucleon: $\beta=0,\pi$

$$\frac{d^3\Delta_{\parallel}\sigma}{dx dy d\varphi} = \frac{4\alpha^2}{Q^2} \left\{ \left(1 - \frac{y}{2} - \frac{y^2\gamma^2}{4} \right) g_1 - \frac{y}{2}\gamma^2 g_2 \right\}$$

transversely polarised nucleon: $\beta= \pi/2$

$$\frac{d^3\Delta_{\perp}\sigma}{dx dy d\varphi} = \frac{4\alpha^2}{Q^2} \left\{ \gamma \sqrt{1 - y - \frac{y^2\gamma^2}{4}} \left(\frac{y}{2} g_1 + g_2 \right) \right\}$$



Measure **asymmetries**:

$$A_{\parallel}(x, Q^2; E) = \frac{\Delta_{\parallel}\sigma}{\bar{\sigma}} = \frac{\sigma^{\uparrow\uparrow} - \sigma^{\downarrow\downarrow}}{\sigma^{\uparrow\uparrow} + \sigma^{\downarrow\downarrow}},$$

$$A_{\perp}(x, Q^2; E) = \frac{\Delta_{\perp}\sigma}{\bar{\sigma}} = \frac{\mathcal{H}_l}{\cos\varphi} \cdot \frac{\sigma(\varphi) - \sigma(\pi \pm \varphi)}{\sigma(\varphi) + \sigma(\pi \pm \varphi)}$$

Experimental essentials

- up to now only fixed-target pol. DIS experiments
- need polarised targets and beams
- need detection of scattered lepton, energy, direction, identification
- need to know energy and direction of incoming lepton
 - detection or given by machine
 - measurable asymmetries very small
 - need excellent control of fake asymmetries, e.g. time variations of detector efficiency

Experiment essentials

- Beams & targets:

	target	beam pol	$x_{min}(1 \text{ GeV}^2)$
• SLAC 48 GeV,	solid/gas	e, pol. source	0.01
• DESY 28 GeV,	gas internal	e, Sokolov-Ternov	0.02
• CERN 200 GeV,	solid	μ , pion decay	0.0025
(RHIC 100 – 100 GeV		pp collider)

- fake asymmetries:

- rapid variation of beam polarisation (SLAC)
- rapid variation of target polarisation (HERMES)
- simultaneous measurement of two oppositely polarised targets (CERN)
- bunch trains of different polarisation (RHIC)

Measurable asymmetries

$$A_{meas} = P_t P_b f A$$

P_b, P_t beam and target polarisations,

f target dilution factor = polarisable N/total N

note: linear in error: $f=1/2 \Rightarrow$ requires 4 times statistics

$$g_1 \simeq \frac{A_{\parallel}}{D} F_1 \simeq \frac{A_{\parallel}}{D} \frac{F_2}{2x} \quad \text{huge rise of } F_2/2x \text{ at small } x$$

D depolarisation factor, kinematics, polarisation transfer from polarised lepton to photon, $D \approx y$

Even big g_1 at small x means small asymmetries

Pol. DIS experiments

Spin Crisis



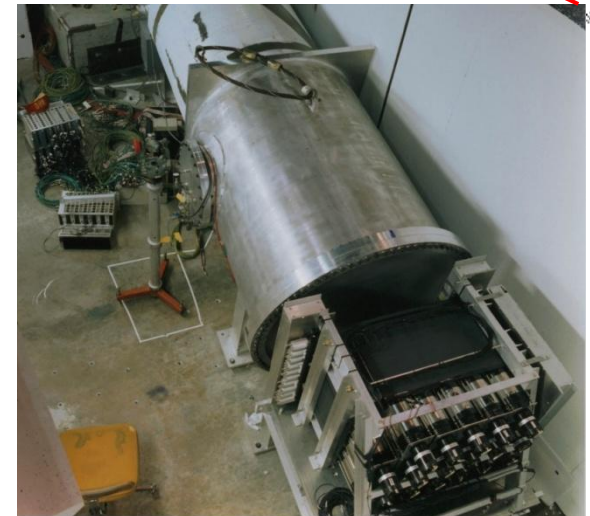
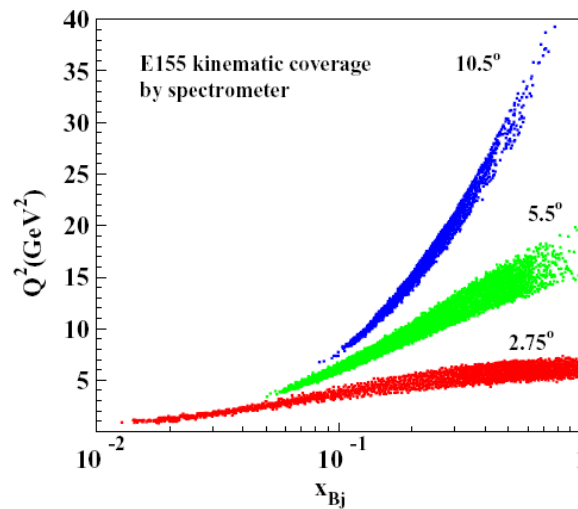
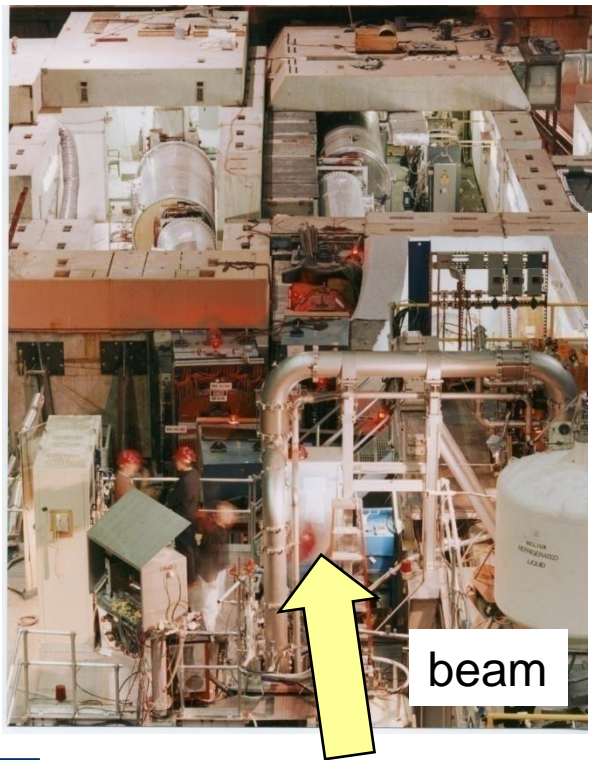
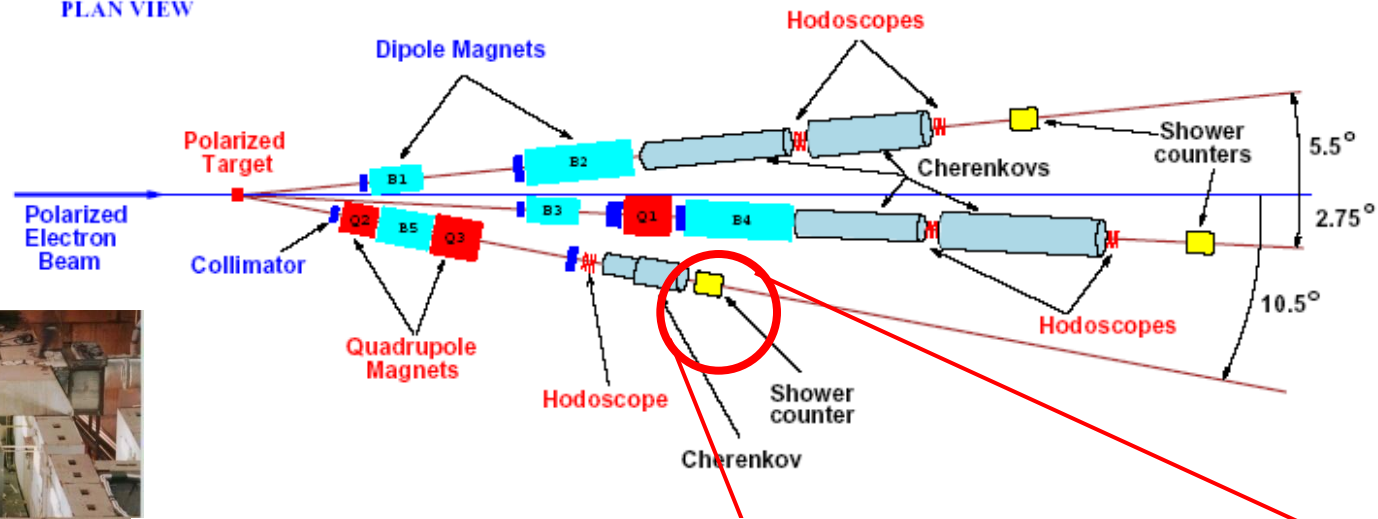
Lab	Exp	Year	Energy	Beam	P_b	target	P_t	f	result
SLAC	E80	75	10–16 GeV	e^-	0.85	H-butanol	0.50	0.13	A_1^p
SLAC	E130	80	16–23 GeV	e^-	0.81	H-butanol	0.58	0.15	A_1^p
CERN	EMC	85	200 GeV	μ^+	0.79	NH ₃	0.78	0.16	g_1^p
CERN	SMC	92	100 GeV	μ^+	0.81	D-butanol	0.40	0.19	g_1^d
SLAC	E142	92	19–26 GeV	e^-	0.39	³ He	0.35	0.12	g_1^n
CERN	SMC	93	190 GeV	μ^+	0.80	H-butanol	0.86	0.12	g_1^p, g_2^p
SLAC	E143	93	10–29 GeV	e^-	0.85	NH ₃	0.70	0.15	g_1^p
SLAC	E143	93	10–29 GeV	e^-	0.85	ND ₃	0.25	0.24	g_1^d
CERN	SMC	94/5	190 GeV	μ^+	0.80	D-butanol	0.50	0.20	g_1^d, g_2^d
SLAC	E154	95	48 GeV	e^-	0.83	³ He	0.38	0.18	g_1^n
DESY	HERMES	95	28 GeV	e^+	0.55	³ He	0.46	0.33	g_1^n
CERN	SMC	96	190 GeV	μ^+	0.80	NH ₃	0.89	0.16	g_1^p
DESY	HERMES	96/97	28 GeV	e^+	0.55	H	0.88	1.00	g_1^p
SLAC	E155	97	48 GeV	e^-	0.81	NH ₃	0.80	0.15	g_1^p
SLAC	E155	97	48 GeV	e^-	0.81	⁶ LiD	0.22	0.36	g_1^d
DESY	HERMES	98–00	28 GeV	e^\pm	0.55	D	0.85	1.00	g_1^d, b_1^d
SLAC	E155X	99	29/32 GeV	e^-	0.81	NH ₃	0.70	0.16	g_2^p
SLAC	E155X	99	29/32 GeV	e^-	0.81	⁶ LiD	0.22	0.36	g_2^d
DESY	HERMES	≥ 01	28 GeV	e^\pm	0.55	H/D	0.85	1.00	
CERN	COMPASS	≥ 01	160 GeV	μ^+	0.80	⁶ LiD	0.50	0.40	
BNL	RHIC	> 01	coll.	p		p		1.00	

running

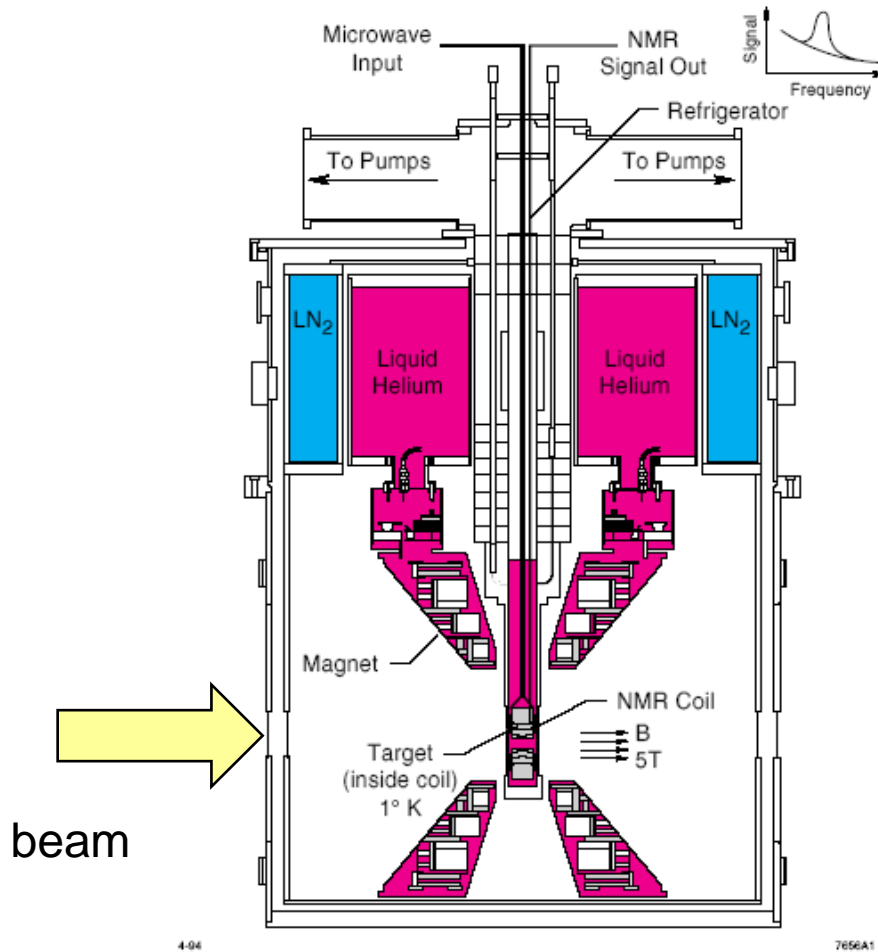


SLAC E155 Spectrometer

PLAN VIEW



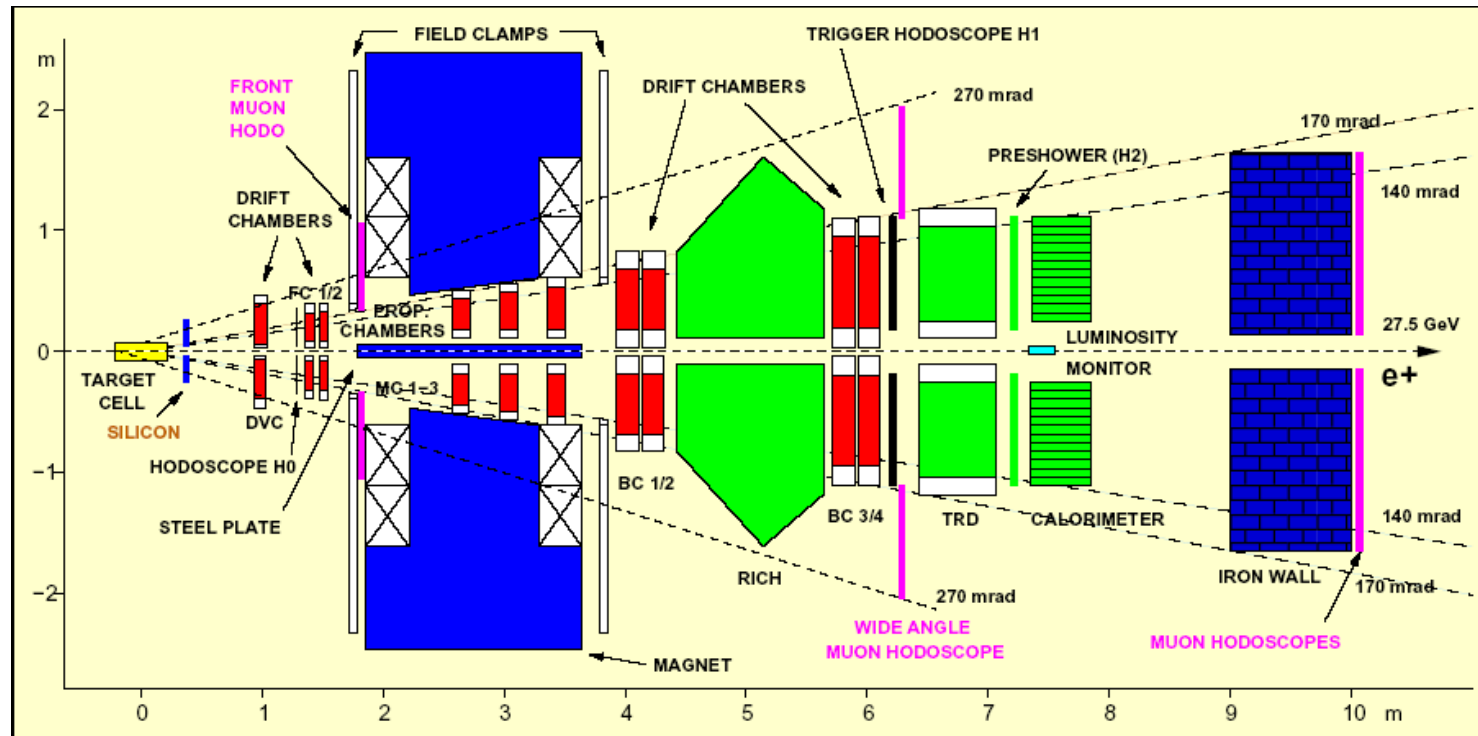
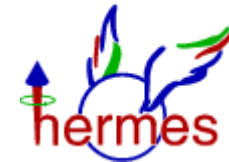
E155 Target



cryogenic target
 ${}^6\text{LiD}$, NH_3

1K evaporator fridge
5 T magnetic field

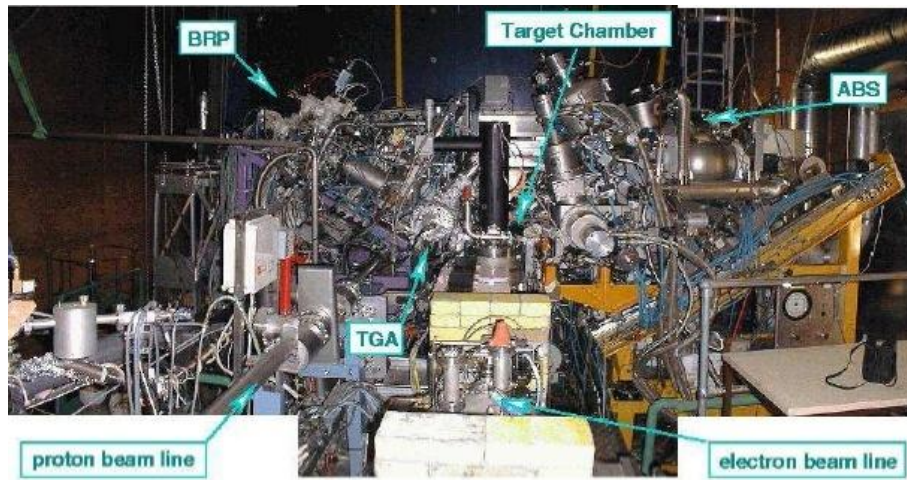
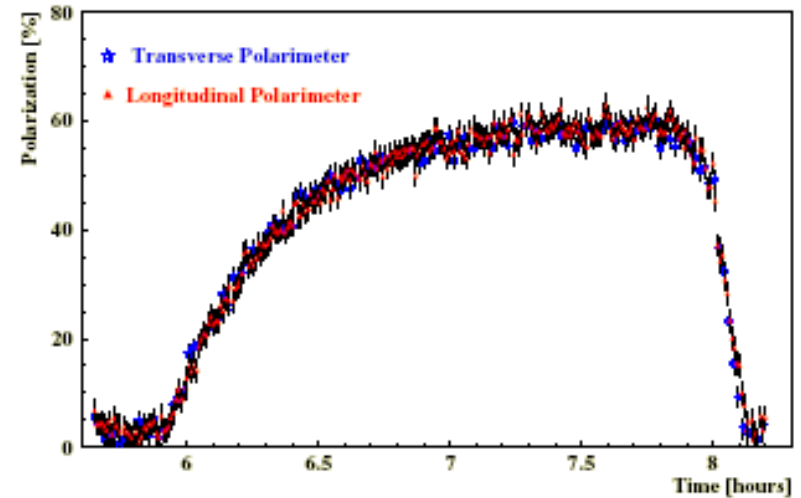
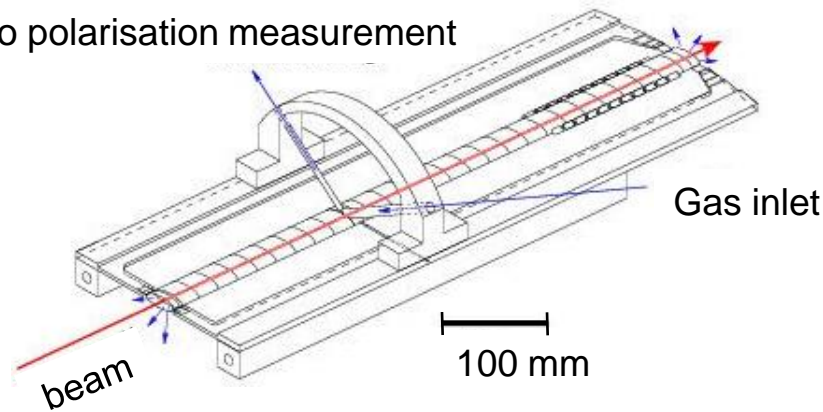
HERMES



HERMES

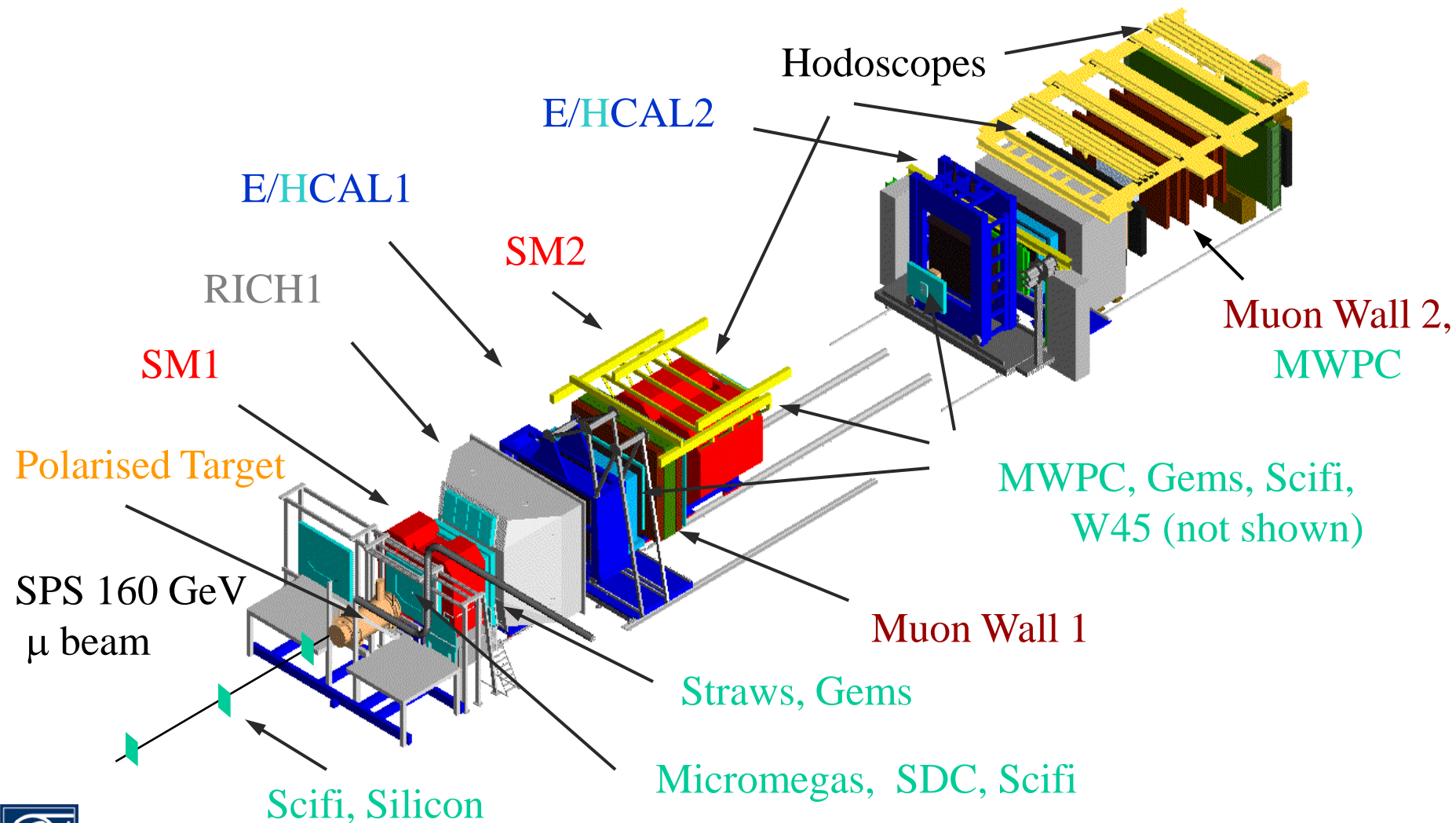
Target cell

Gas to polarisation measurement

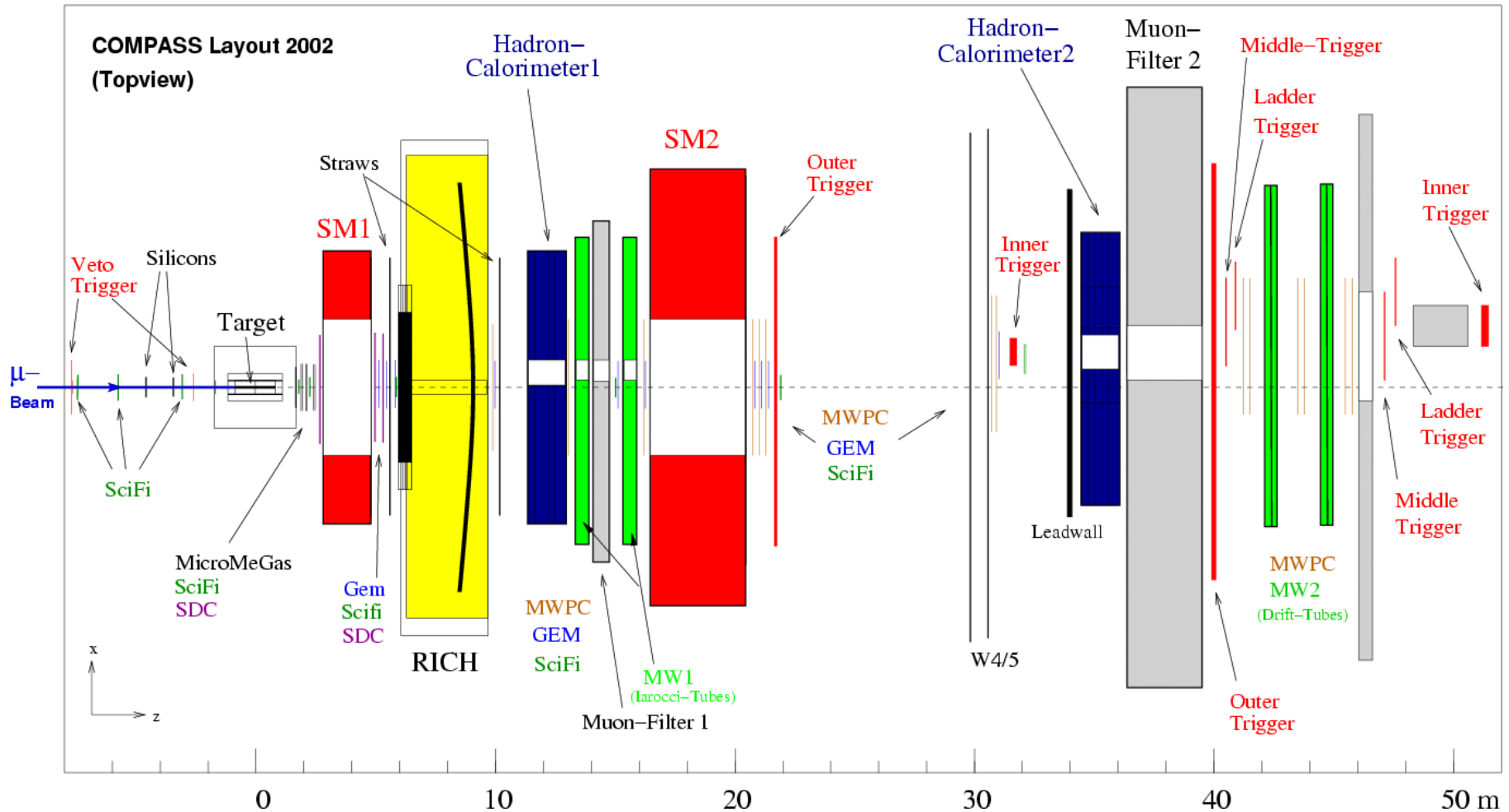


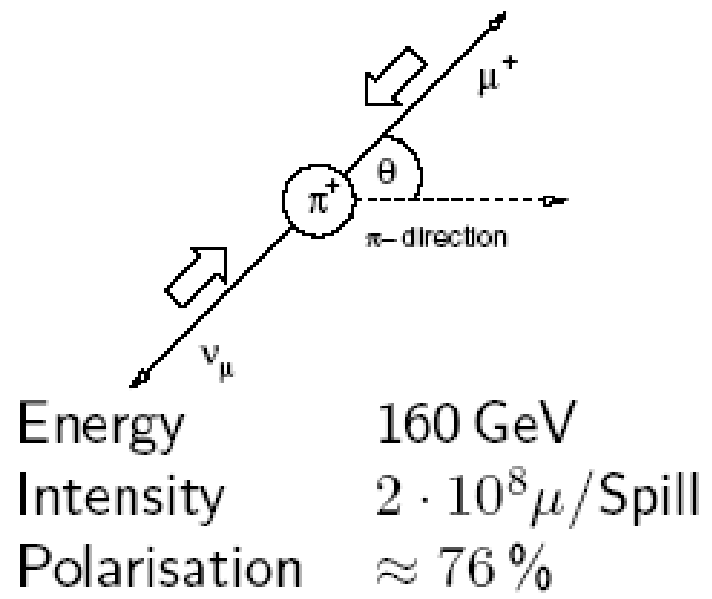
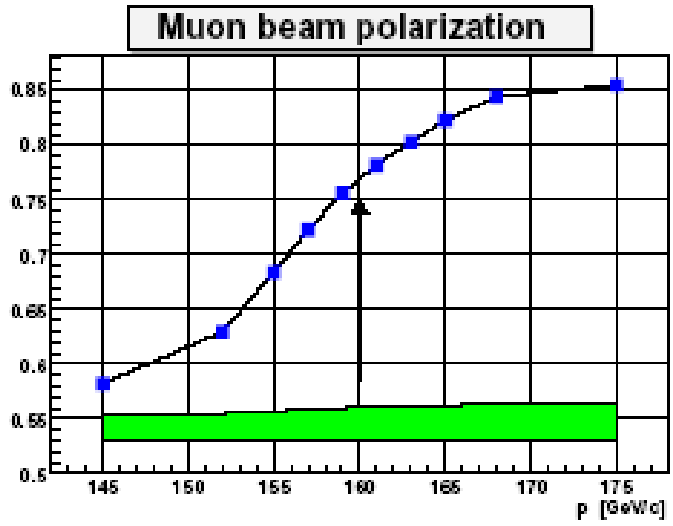
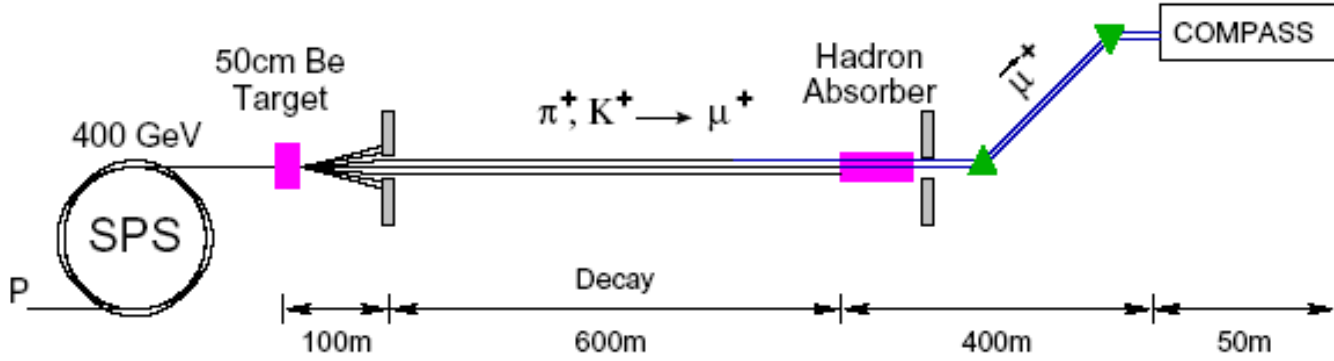
beam polarisation
built-up by
Sokolov-Ternov
effect

The COMPASS Spectrometer



Spectrometer





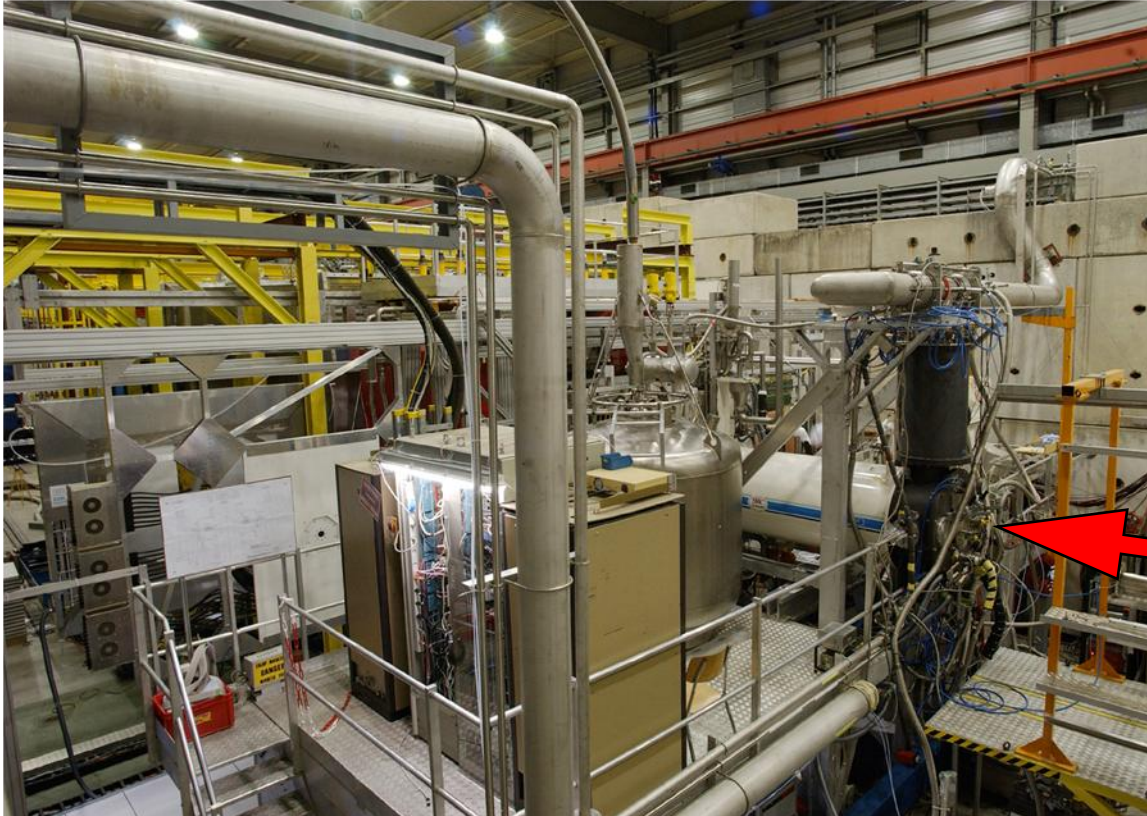


COMPASS Spectrometer



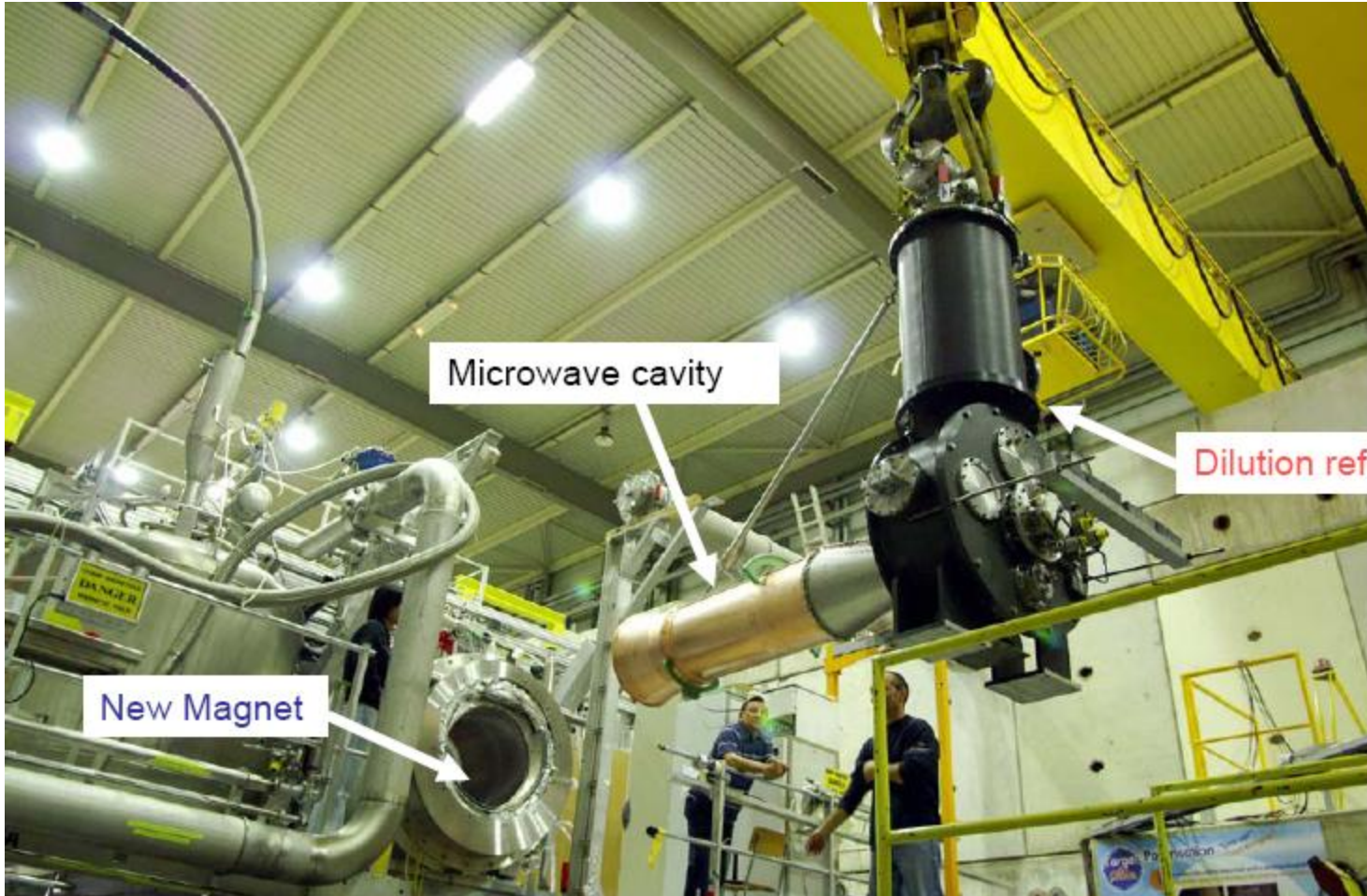


Polarised target



- ${}^6\text{LiD}/\text{NH}_3$
- 50/90% polarisation
- 50/16% dilution fact.
- 2.5 T
- 50 mK

μ



Microwave cavity

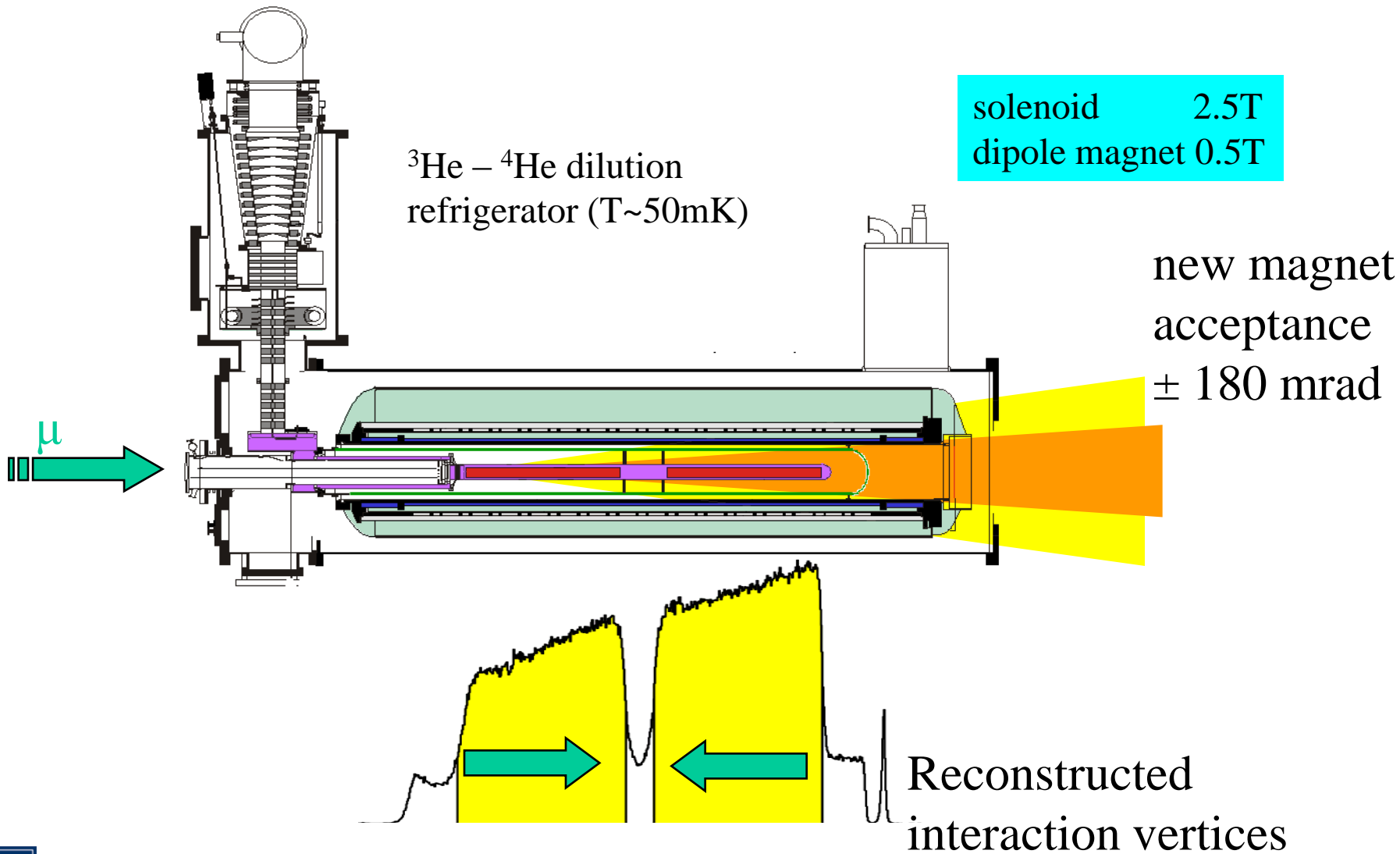
Dilution refrigerator

New Magnet

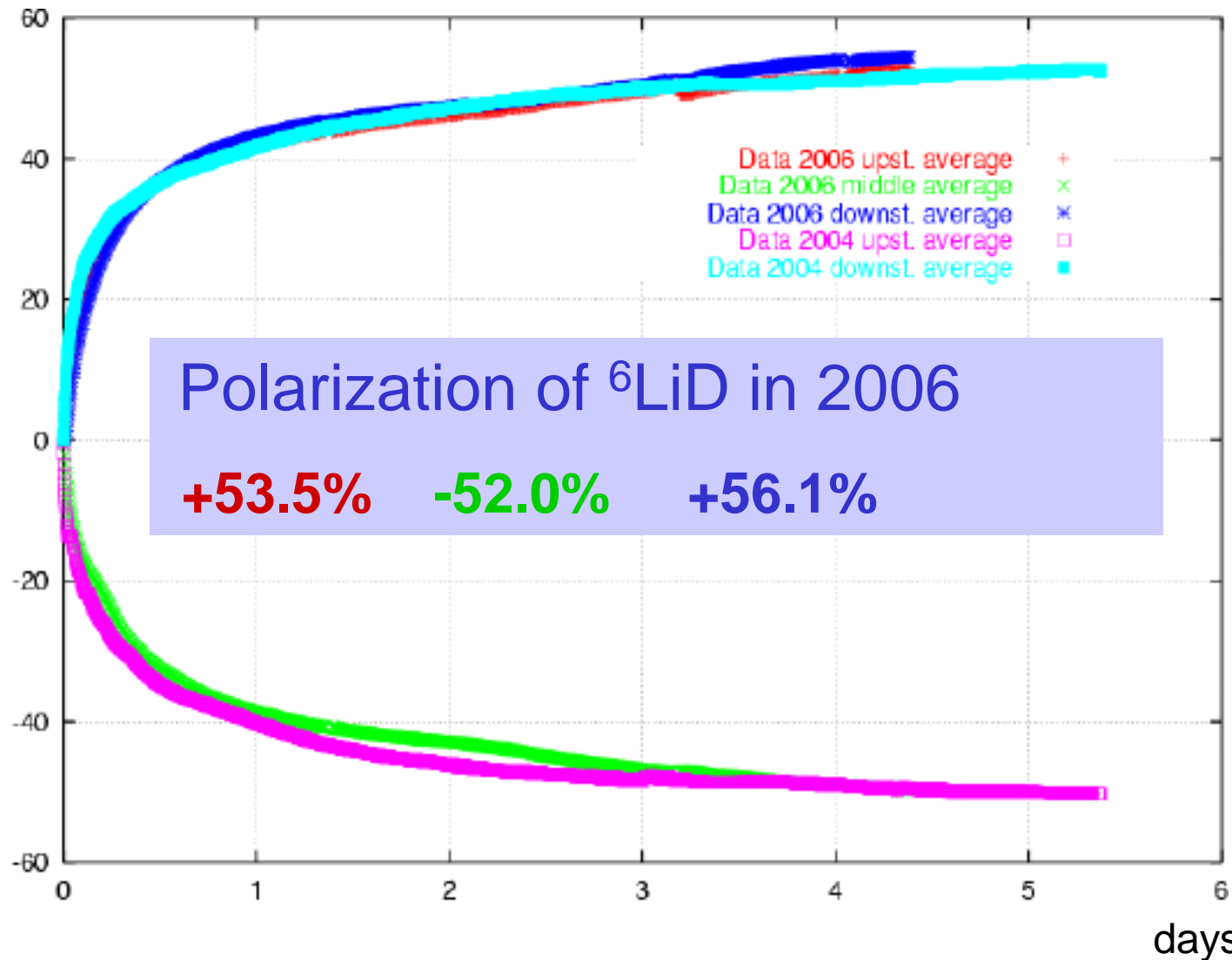




Target system

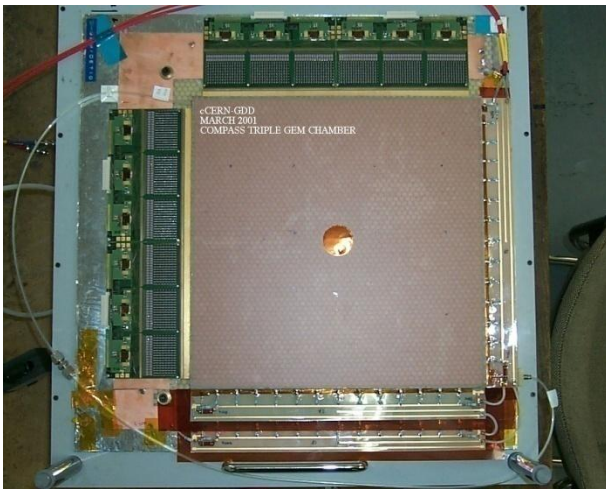


Polarized target performances

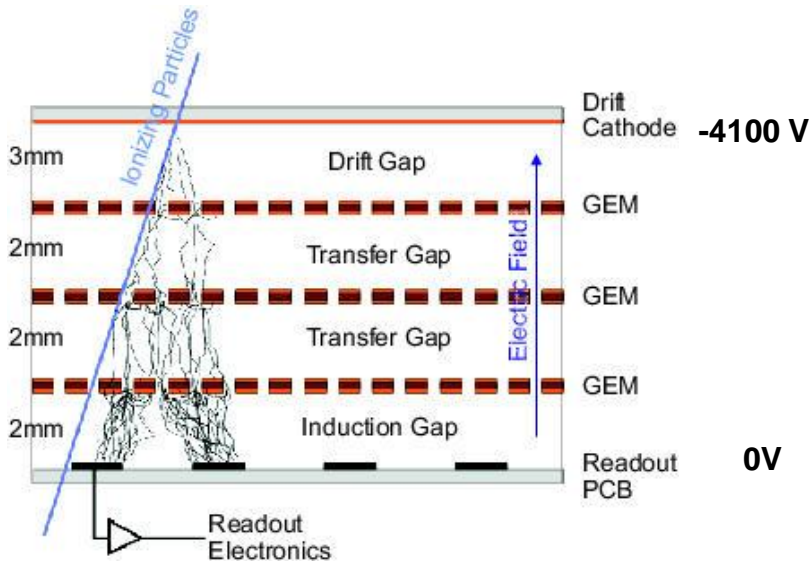




Gems



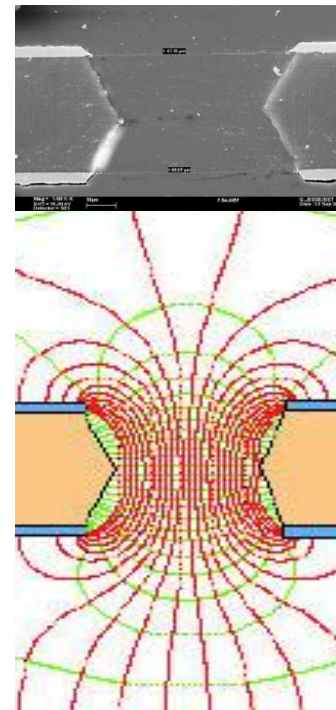
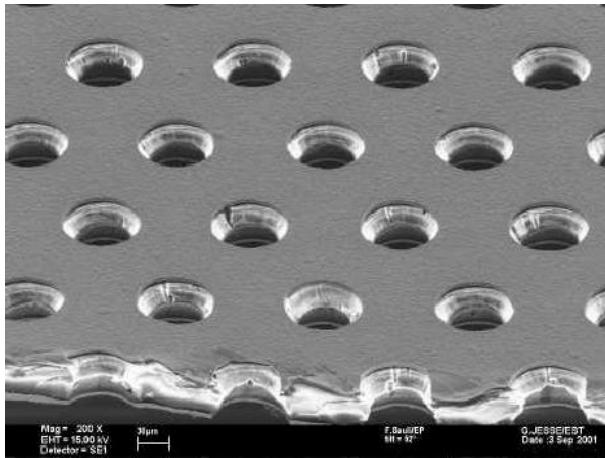
- 20 triple Gems detectors
- in 10 stations
- 40 coordinates
- size 30x30 cm²
- 12 ns time resolution
- 50 μm space resolution
- efficiency $\sim 97\%$
- Ar/CO₂ 70/30 %





Gems

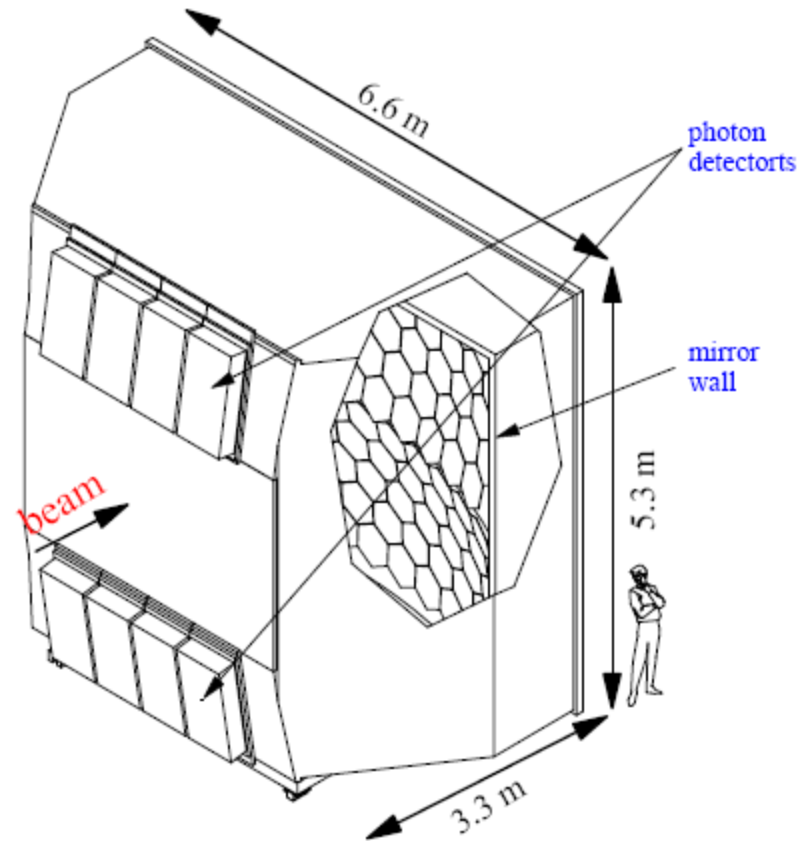
Gem foil





RICH

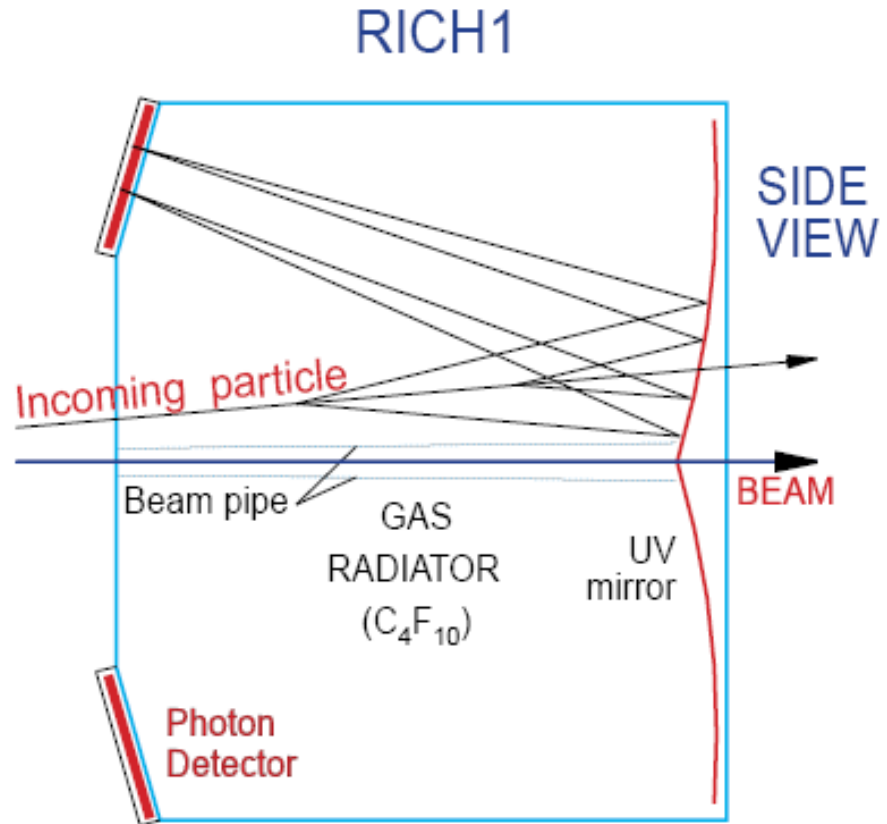
- 80 m³ (3 m C₄F₁₀ radiator)
- 116 VUV mirrors
- 5.3 m² VUV detectors
 - MWPC CsI photo-sensitive cathodes
 - 8x8 mm² pads
- 84k analog r/o channels
- 2006 inner quarter with maPMTs





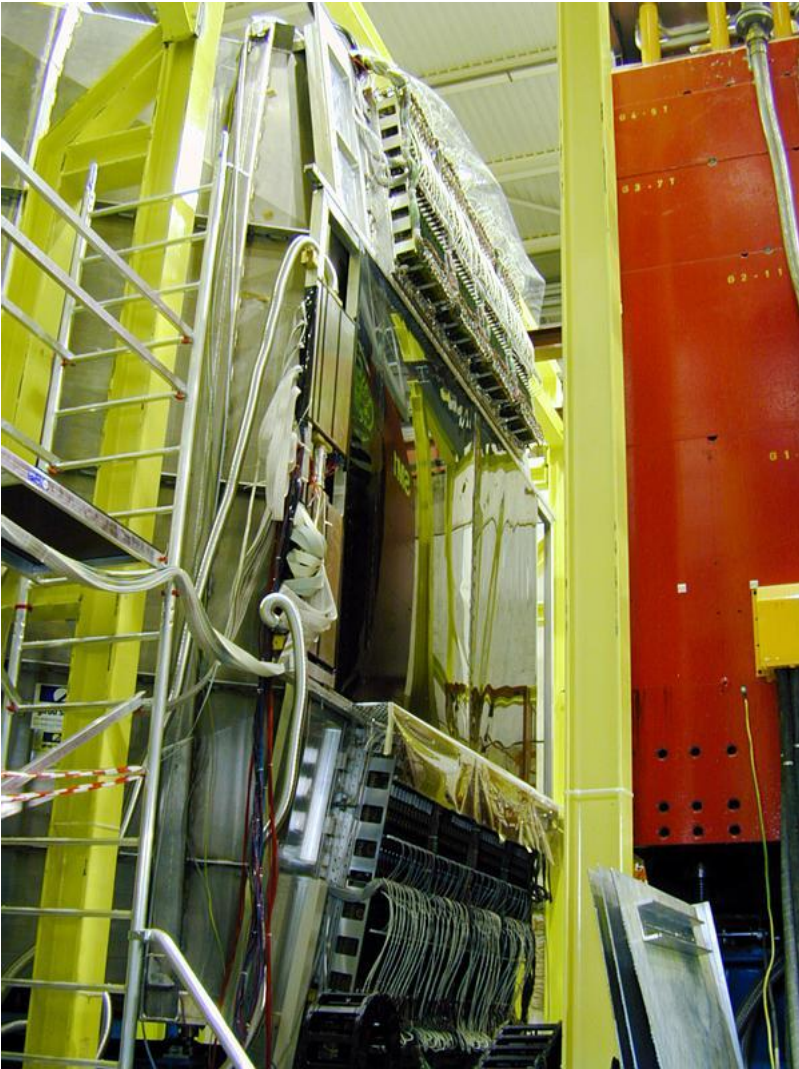
RICH

1. π/K separation up to $\sim 60 \text{ GeV}/c$
2. Large angular acceptance:
 $\pm 250 \text{ mrad (H)}, \pm 200 \text{ mrad (V)}$
3. Minimize materials





RICH



Lecture 2

- Experimental status
 - Q^2 evolution, scaling violations, DGLAP
 - status of g_1 and QCD analyses
 - interplay: g_2
 - semi-inclusive data
 - ΔG from hadron pairs