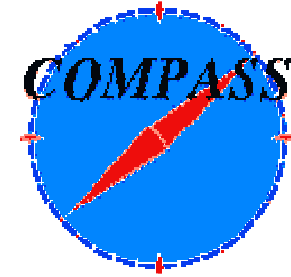


# Precyzyjny pomiar polaryzowalności pionu



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Konwersatorium IFD im. Jerzego Pniewskiego  
Warszawa, 13 kwietnia 2015

## Electromagnetic polarisabilities of the pion

- Magnitude of polarisability of a composite system by an external electromagnetic field characterises the „rigidity” of the system
- $\pi$  meson, quark-antiquark system, lightest object bound by the strong force  
its rigidity reflects the strength of the binding force
- Theory of strong interactions (ChPT) predicts the pion electric and magnetic polarisabilities with (present) uncertainties of  $\approx 18\%$
- Expected ‘deformation’ is about  $2 \times 10^{-4}$  of the pion volume, tiny effect  
➔ good control of experimental systematics needed
- To produce such deformation the electric field of  $10^{18}$  V/cm needed
- No trustworthy measurements of pion polarisabilities prior to COMPASS  
➔ no entry in „Review of Particle Physics” yet

## Chiral perturbation theory in a nut-shell

- Chiral symmetry – symmetry of Lagrangian under which left- and right-handed Dirac fields (QCD quarks) transform independently
  - in QCD with mass-less quarks the chiral symmetry is *spontaneously* broken by a quark condensate  $\langle \bar{q}_R^a q_L^b \rangle$  formed through nonperturbative action of QCD gluons, with mass-less pion identified as the Goldstone boson
  - due to non-vanishing and differing quark masses, in the real world the chiral symmetry is *explicitly* broken, and pions are not massless, they are pseudo-Goldstone bosons
- Chiral perturbative theory (ChPT) is low-energy expansion of QCD with the same symmetries as ‘mother’ theory, and hadrons as effective degrees of freedom
- Unknown coupling constants in ChPT Lagrangian are determined by fits to experimental data or derived from the underlying theory (QCD)
- ChPT provides a consistent description of low-energy hadronic physics:  
light-meson masses, decays, effective couplings, pion scattering lengths  $a_0$  and  $a_2$   
proton and neutron electric and magnetic polarisabilities etc,

## COMPASS result makes 'an event' at CERN

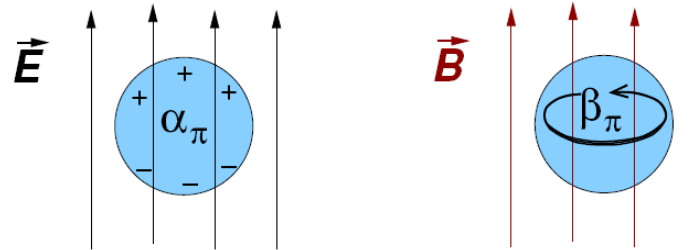
- on February 11, 2015 in Physical Review Letters published COMPASS article  
„Measurement of Charged-Pion Polarizability”

- the same day the result announced at the CERN press release

*some citations from the press release*

- ” CERN experiment brings precision to a cornerstone of particle physic ”
  - ” [...] a key measurements on the strong interaction”
  - ” This result is admirably complementary to the studies of fundamental interactions performed at the LHC and a testimony to the diversity and strength of CERN’s research program”, *Rolf Heuer, Director General*
- the first page in News of March 2015 issue of the CERN Courier

# Pion polarisabilities – definitions and access



differential cross section for  $\pi \gamma \rightarrow \pi \gamma$  modified compared to poin-like pion

CMS kinematic variables:

$s$  - total energy squared

$\theta_{cm}$  - scattering angle

$$\frac{d\sigma_{\pi\gamma}}{d\Omega_{cm}} = \frac{\alpha^2 (s^2 z_+^2 + m_\pi^4 z_-^2)}{s (s z_+ + m_\pi^2 z_-)^2} - \frac{\alpha m_\pi^3 (s - m_\pi^2)^2}{4s^2 (s z_+ + m_\pi^2 z_-)} \cdot \mathcal{P}$$

$$\mathcal{P} = z_-^2 (\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+^2 (\alpha_\pi + \beta_\pi) - \frac{(s - m_\pi^2)^2}{24s} z_-^3 (\alpha_2 - \beta_2)$$

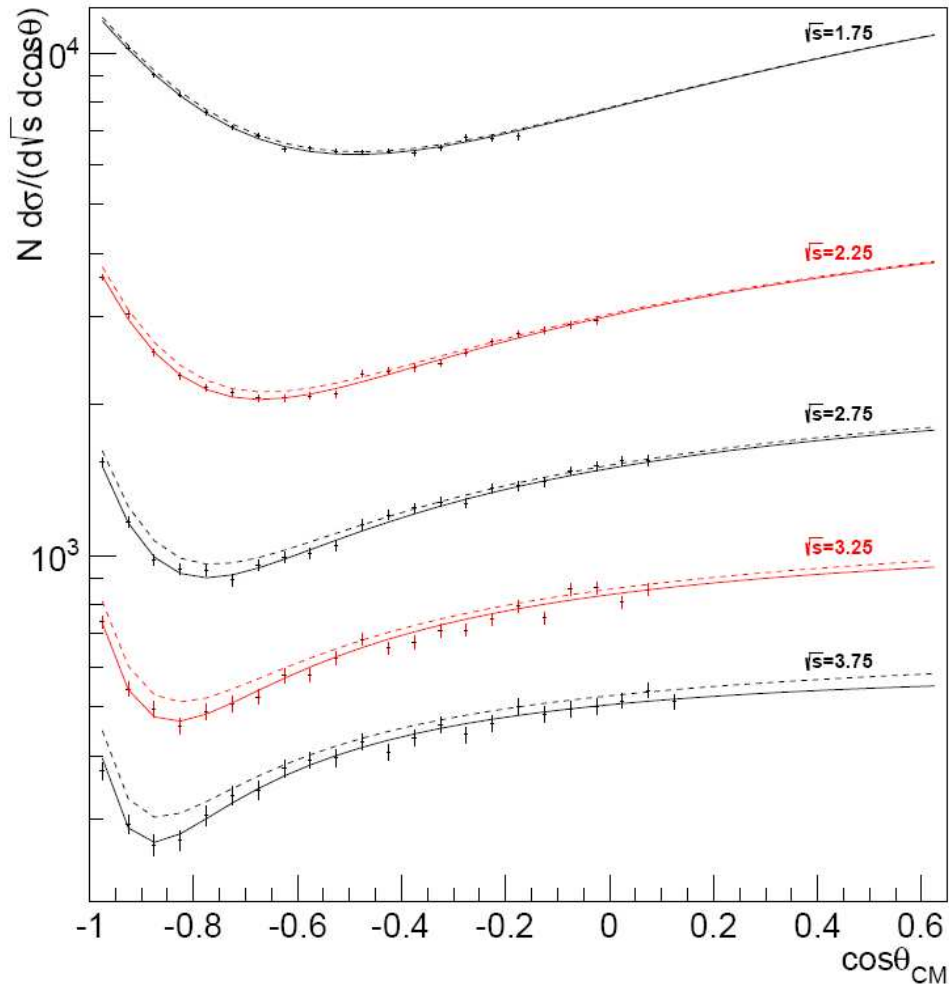
$$z_\pm = 1 \pm \cos \theta_{cm} \quad \alpha = 1/137 \text{ fine structure constant}$$

2-loop ChPT prediction:

$$\alpha_\pi - \beta_\pi = (5.7 \pm 1.0) 10^{-4} \text{ fm}^3 \quad \alpha_\pi + \beta_\pi = (0.2 \pm 0.1) 10^{-4} \text{ fm}^3$$

# Effect of the pion polarisabilities on measured cross section

$$\pi \gamma \rightarrow \pi \gamma$$



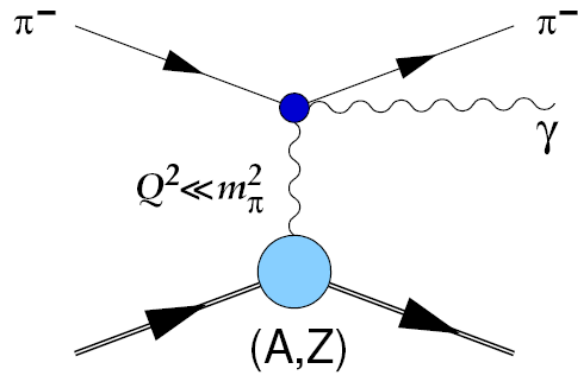
- point-like pion
- ChPT 2-loop prediction
- + simulation assuming statistics collected in 2012

[s in units of  $m_\pi^2$ ]

- ❖  $\sigma_{\text{tot}}(s)$  weak sensitivity to pion's structure
- ❖ up to 20% effect on backward  $\theta_{\text{CM}}$  scattering angles

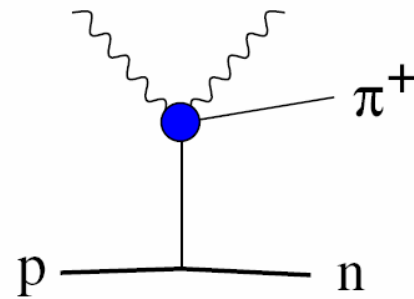
Ways to access  $\pi \gamma \rightarrow \pi \gamma$  scattering

(A)



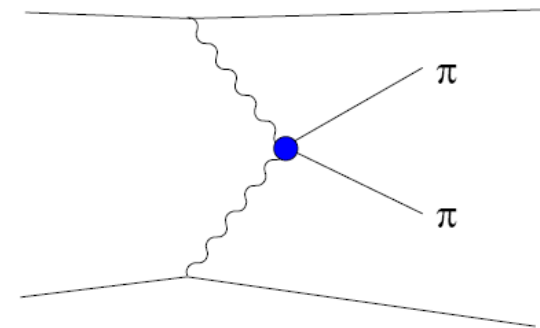
Primakoff process

(B)



radiative pion photoproduction

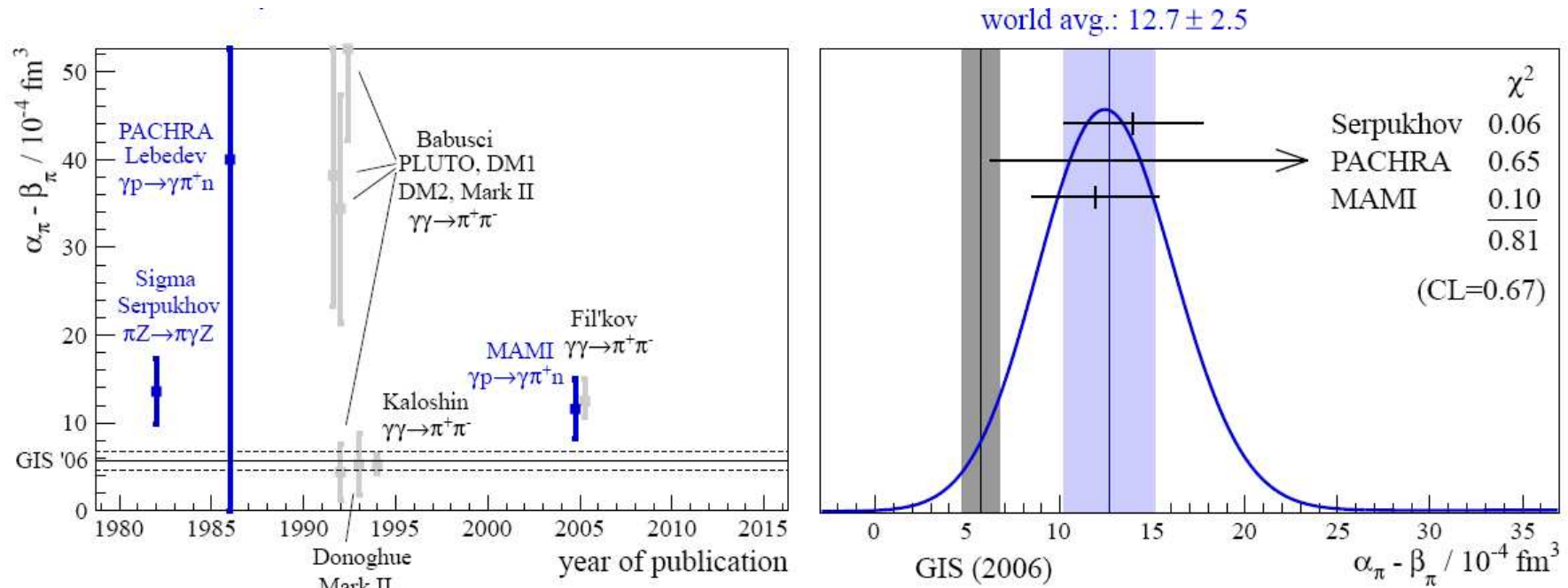
(C)



photon-photon fusion

$$Q^2 = - (p_{\pi}^{\mu} + p_{\gamma}^{\mu} - p_{\text{beam}}^{\mu})^2$$

# Pion polararisability – world data before COMPASS



GIS'06: ChPT prediction, Gasser, Ivanov, Sainio, NPB745 (2006)

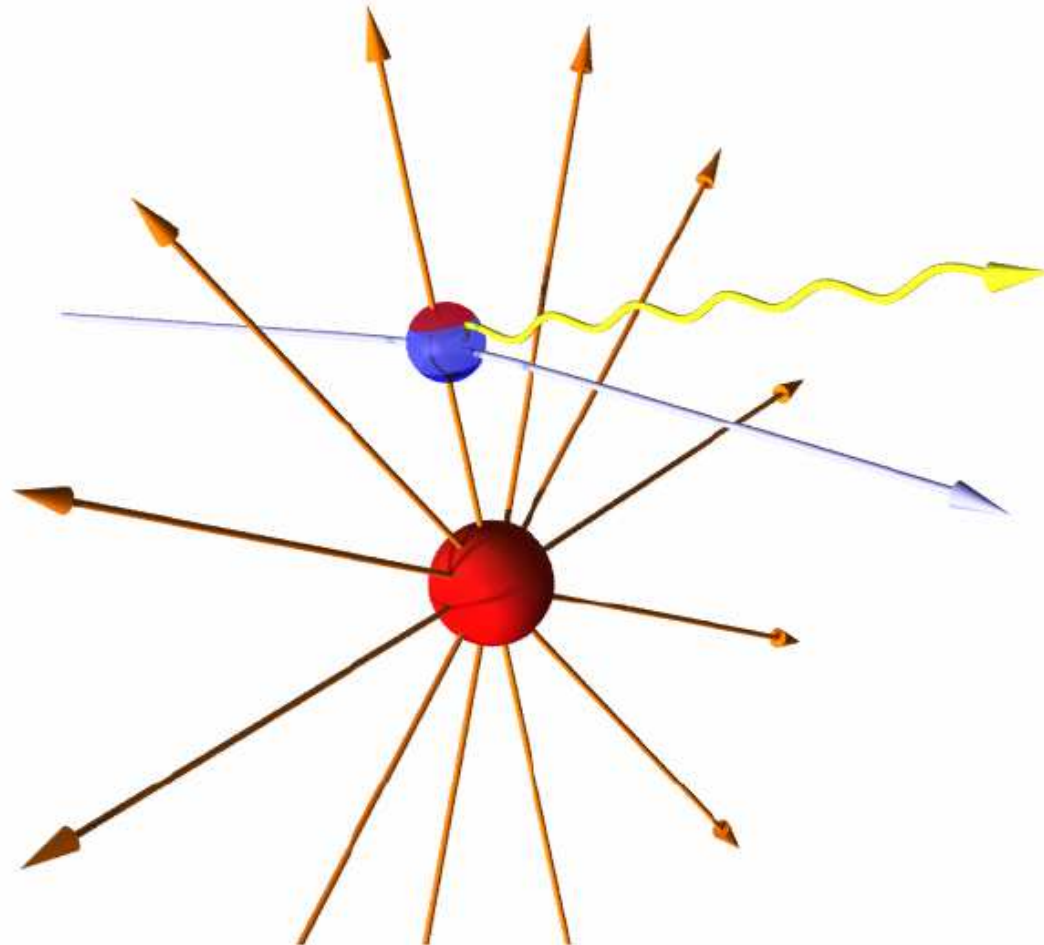
plots from Thiemo Nagel, PhD thesis, TUM 2012

Fil'kov analysis objected by Pasquini, Drechsel, Scherer, PR C81 (2010) 029802

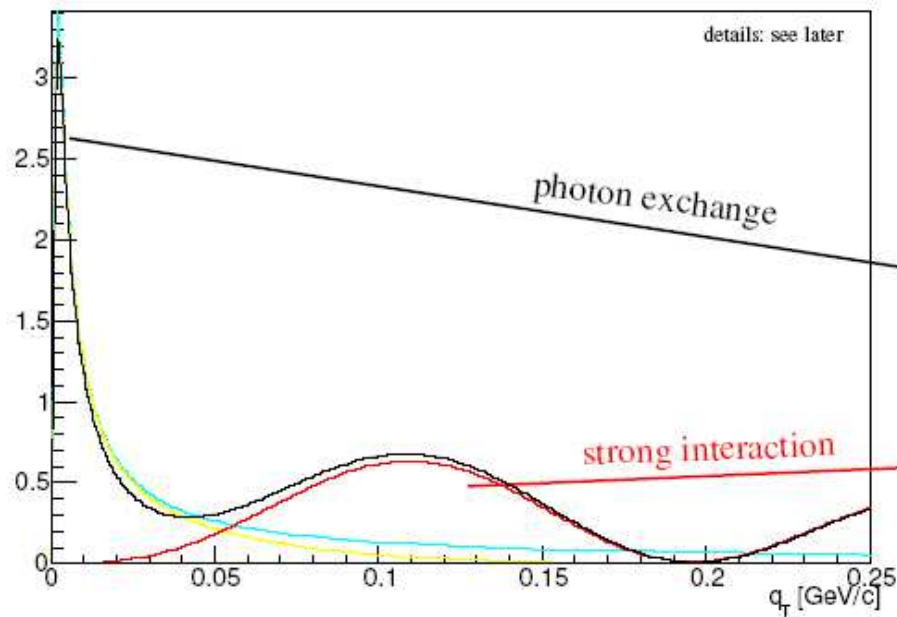


## Pion polarisability via Primakoff Compton scattering

- Charged pion traversing the nuclear **electric** field
  - typical field strength at  $r = 5R_{Ni}$ :  $E \sim 300 \text{ kV/fm}$
- Bremsstrahlung emission
  - particle scatters off **equivalent photons**
  - tiny momentum transfer  $Q^2 \approx 10^{-5} \text{ GeV}^2/c^2$
  - pion/muon (quasi-)real Compton scattering
- Polarisability contribution
  - Compton cross-section typically diminished
  - expected charge separation  $\sim 10^{-5} \text{ fm} \cdot e$

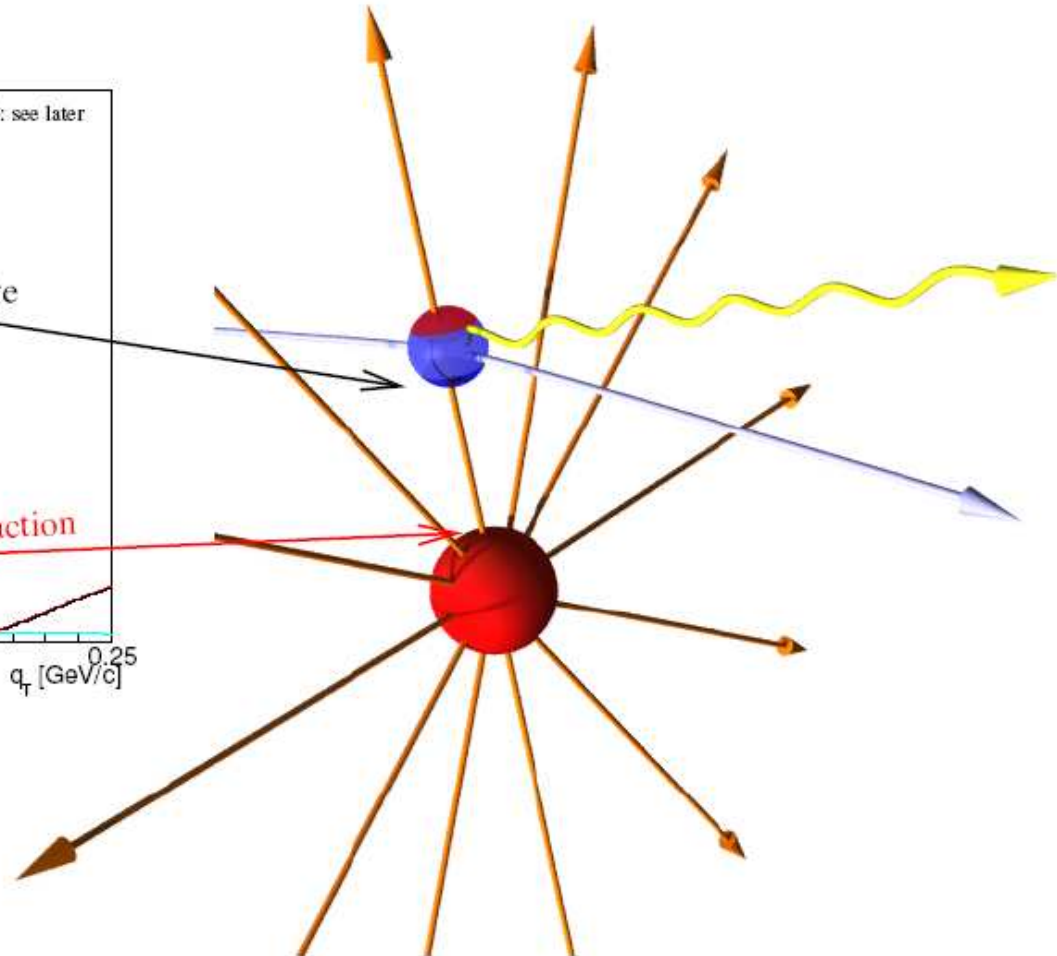


# Interplay of electromagnetic and strong interactions

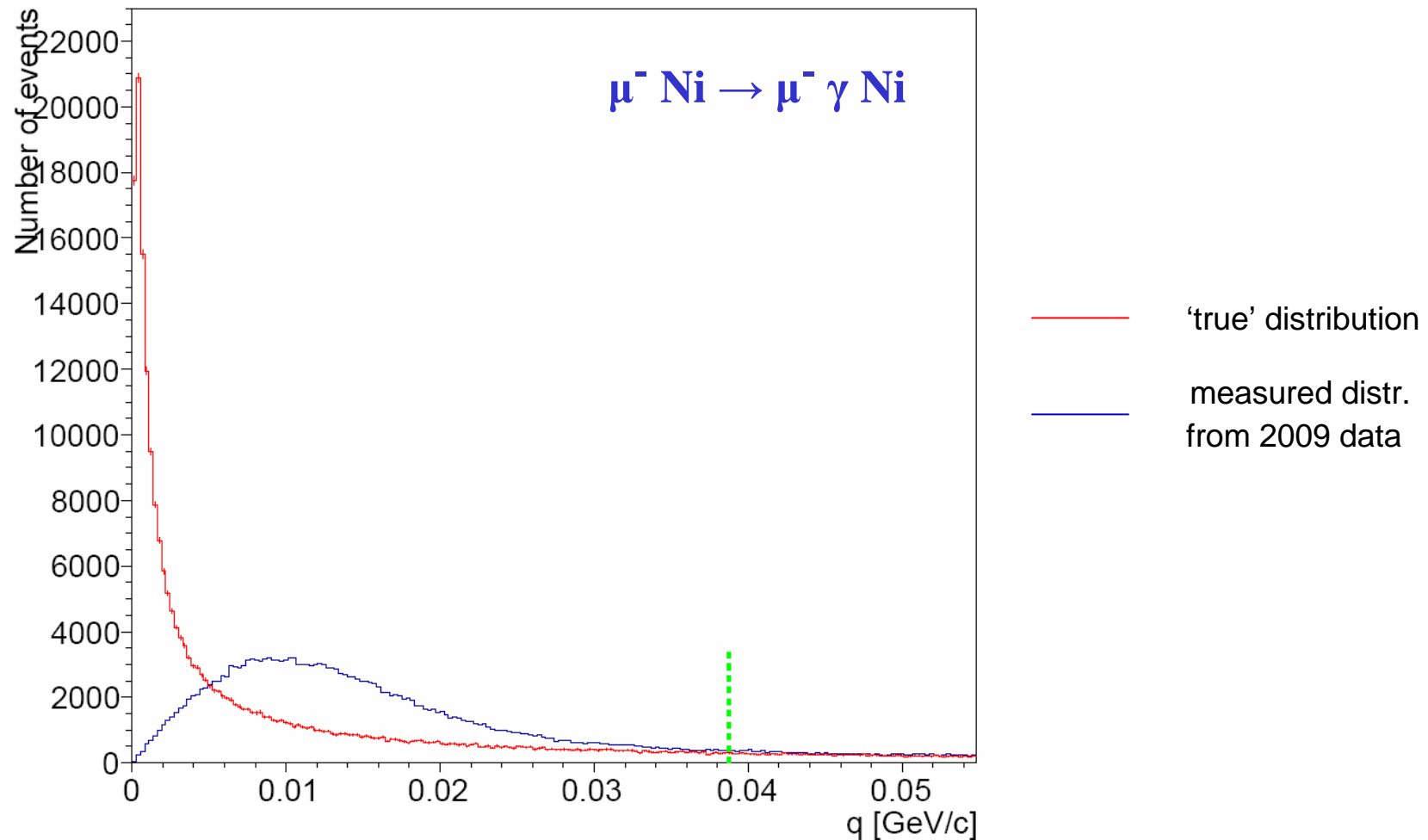


$$q_T = |(\vec{p}_\pi + \vec{p}_\gamma - \vec{p}_{beam})_T|$$

G. Fäldt, Phys.Rev. C79, 014607



Pure Primakoff sample from  $\mu^- \text{Ni} \rightarrow \mu^- \gamma \text{Ni}$



$$q = | \vec{p}_\pi + \vec{p}_\gamma - \vec{p}_{beam} |$$

achieved resolution **12 MeV/c** (10 times larger than the true peak structure)

# $\pi$ -nucleus cross-section connection to $\pi\gamma$ cross section

equivalent-photon approximation approach

$\pi (A,Z) \rightarrow X (A,Z)$

$\pi \gamma \rightarrow X$

$$\frac{d\sigma_{(A,Z)}^{\text{EPA}}}{dsdQ^2d\Phi_n} = \frac{Z^2\alpha}{\pi(s - m_\pi^2)} F^2(Q^2) \frac{Q^2 - Q_{\text{min}}^2}{Q^4} \frac{d\sigma_{\pi\gamma \rightarrow X}}{d\Phi_n}$$

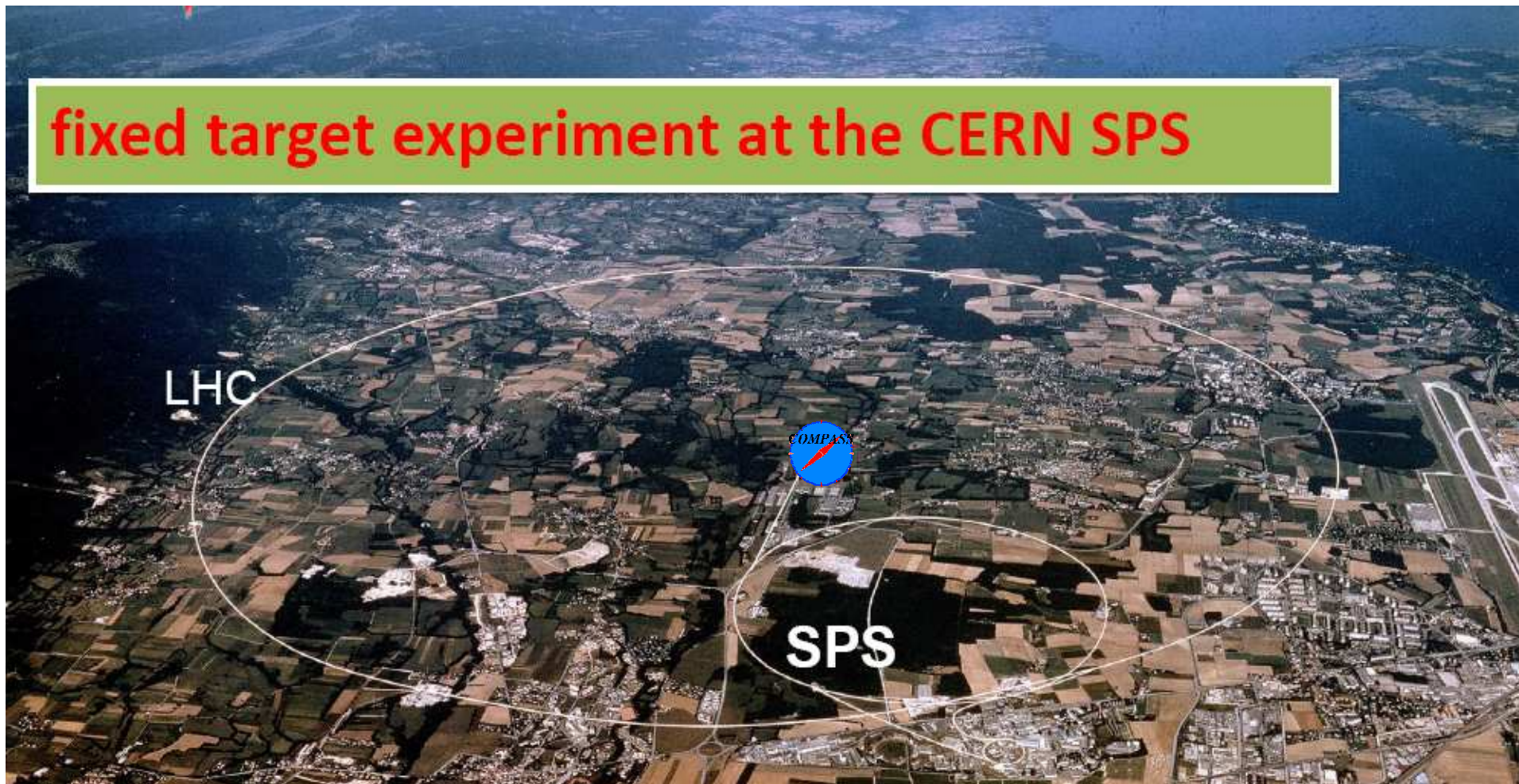
nucleus electromagnetic form factor

phase-space element of final state X



# COmmon Muon Proton Apparatus for Structure and Spectroscopy

**fixed target experiment at the CERN SPS**



~ 220 physicists from 24 institutions



- Located at CERN North Area M2 beam line
  - Possible beams:  $\mu^+$ ,  $\mu^-$ ,  $\pi^+$ ,  $\pi^-$ , K, p → Several physics programs

- Programs with **muon beam**

- Programs with **hadron beams**

COMPASS (2002 – 2011)

- Spin structure, gluon polarization
- Flavour decomposition
- Transversity
- Transverse Momentum-dependent PDFs

- Pion polarisability
- Diffractive and Central production
- Light meson spectroscopy
- Baryon spectroscopy

p, d polarised target (L & T)

small LH<sub>2</sub> or nuclear targets

COMPASS - II (2012 – 2017)

- DVCS and HEMP
- Unpolarized SIDIS and TMDs

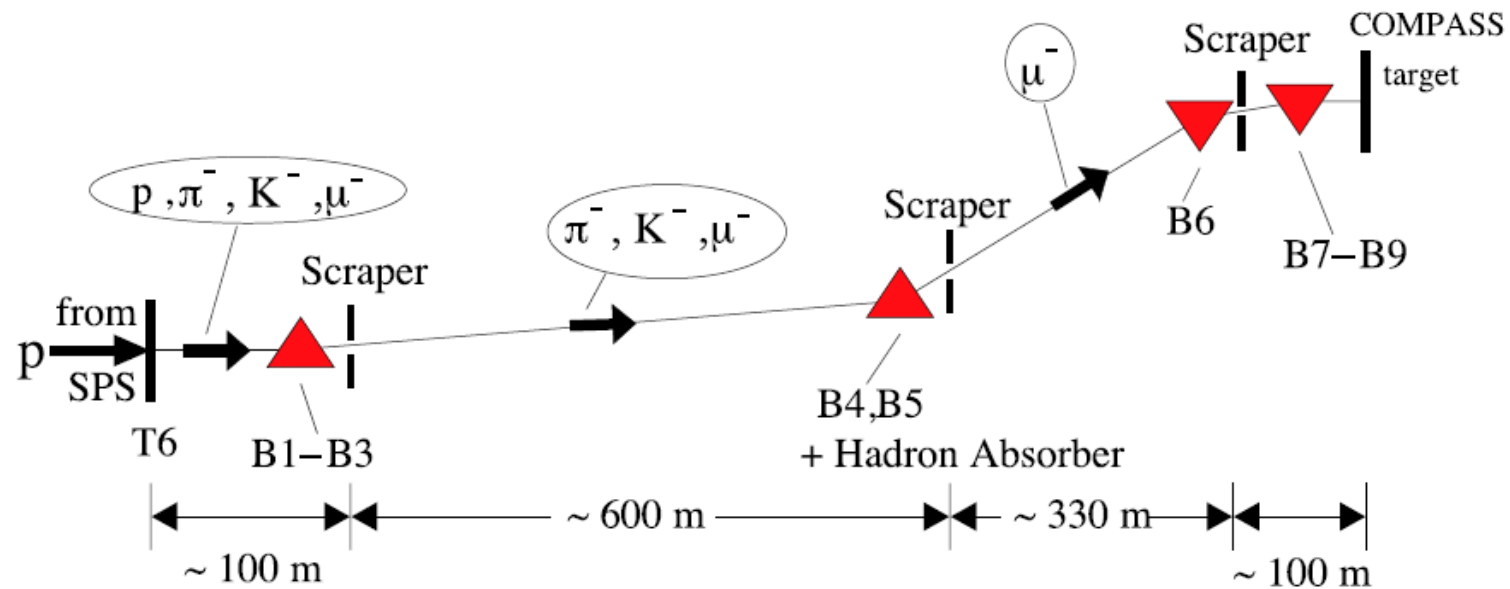
- Pion and Kaon polarisabilities
- Drell-Yan process

long LH<sub>2</sub> target

nuclear targets or polarised p target (T)

**Reconfigurable target region - versatile experimental setup!**

## M2 beam line schematics for 'muon' configuration

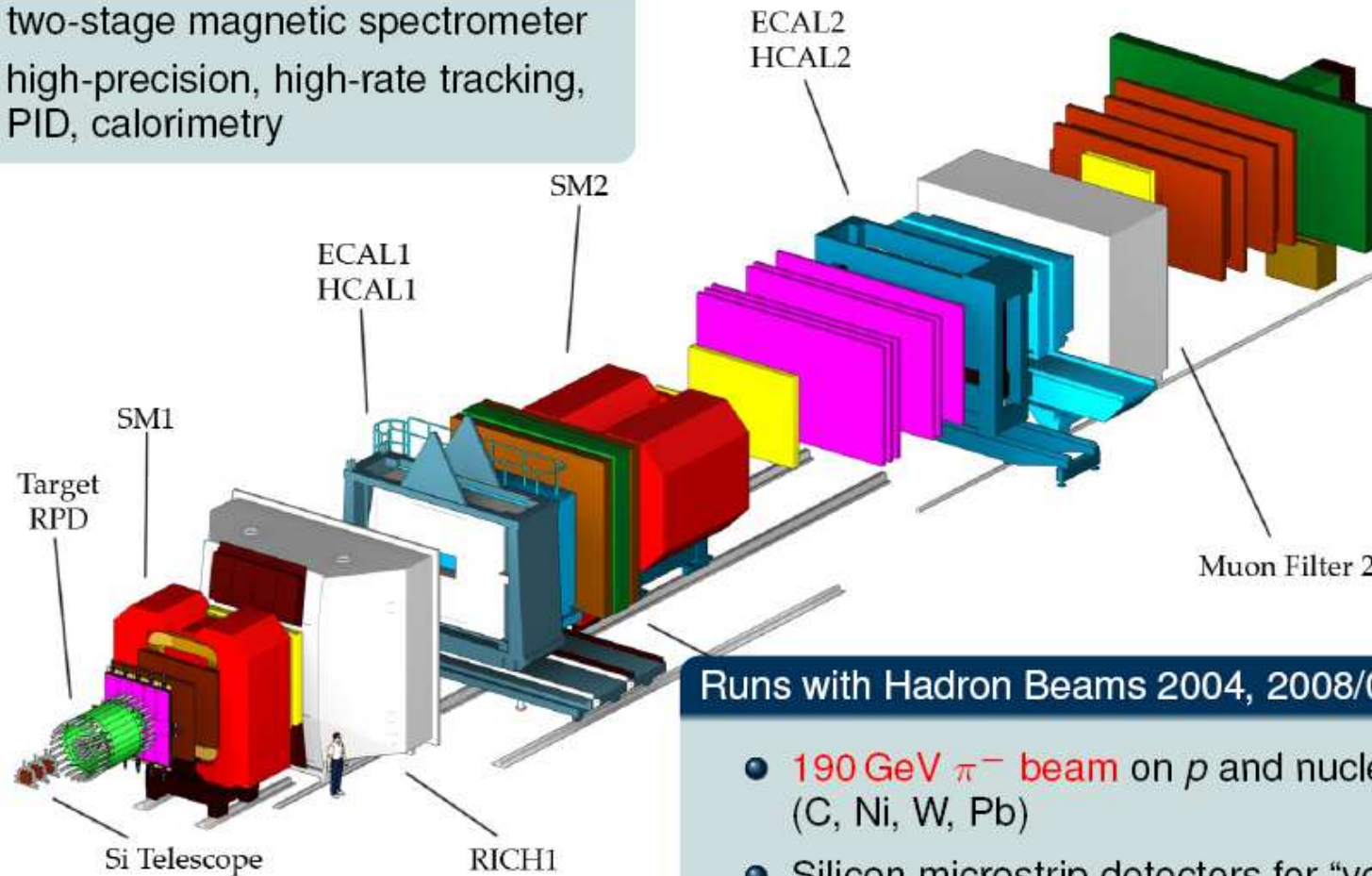


9.9 m long Be absorber (at B4): **in** for muon beam, **out** for hadron beam

# COMPASS experimental setup

## Fixed-target experiment

- two-stage magnetic spectrometer
- high-precision, high-rate tracking, PID, calorimetry

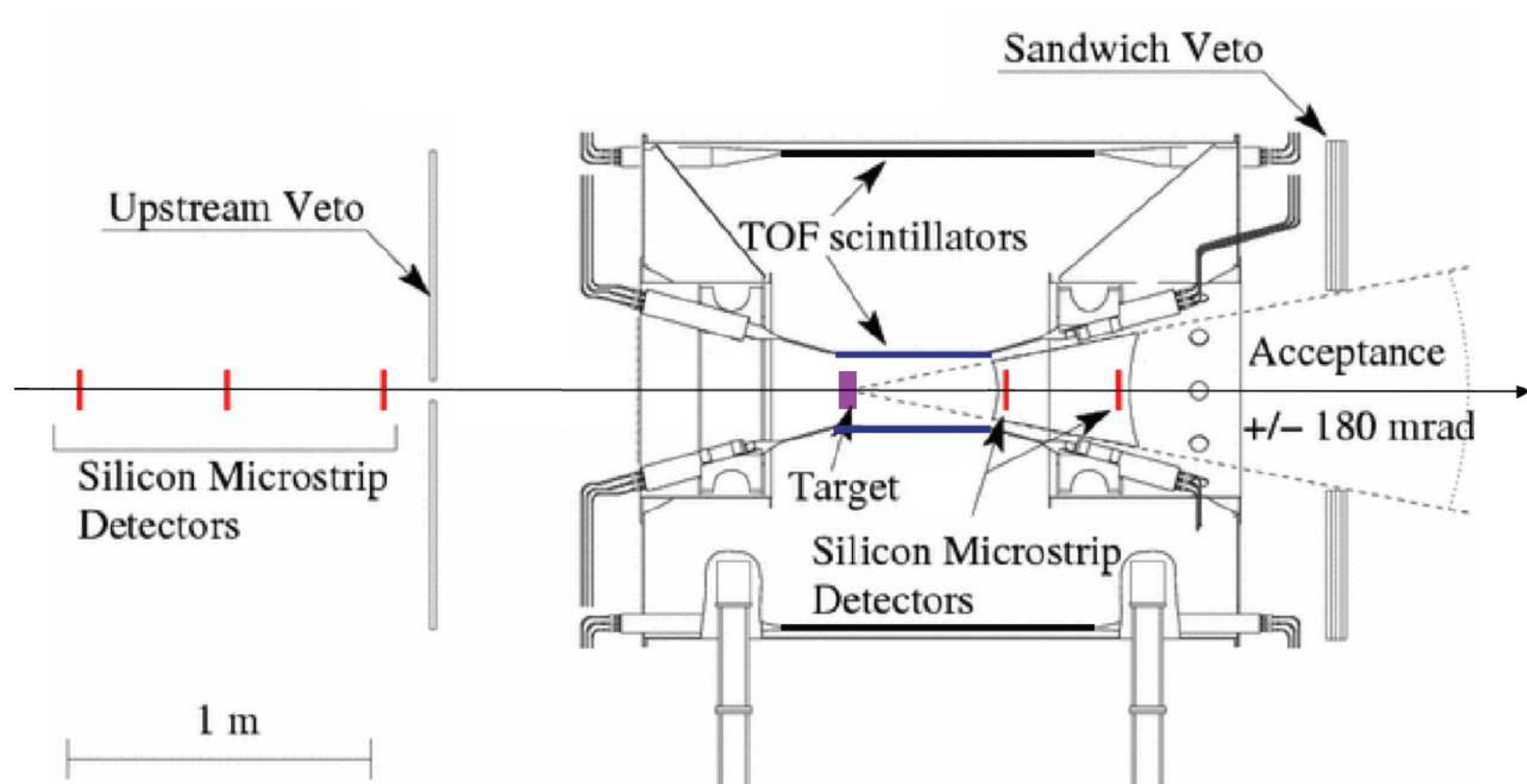


## Runs with Hadron Beams 2004, 2008/09, 2012

- **190 GeV  $\pi^-$  beam** on  $p$  and nuclear targets (C, Ni, W, Pb)
- Silicon microstrip detectors for “vertexing”
- recoil and (digital) ECAL triggers



## Target region

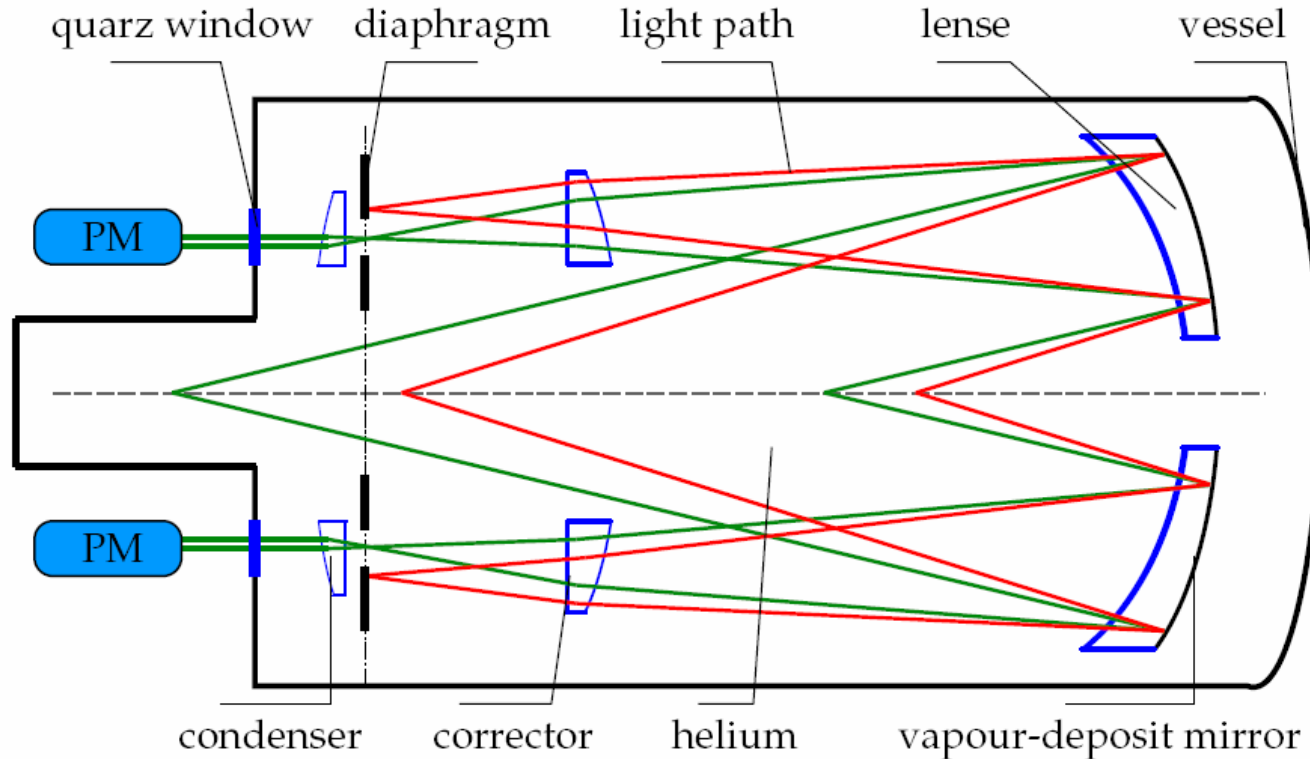


Main target: disc 4.2 mm long and 5 cm  $\varnothing$  of **Ni** (fraction of spin-0 isotopes 99%)

5 cryogenic silicon micro-strip detector stations, with spacial resolution of **4 – 11  $\mu\text{m}$**   
excellent for vertexing and precise determination of momentum transfer to the nucleus

CEDAR – to select beam pions (96.8%)

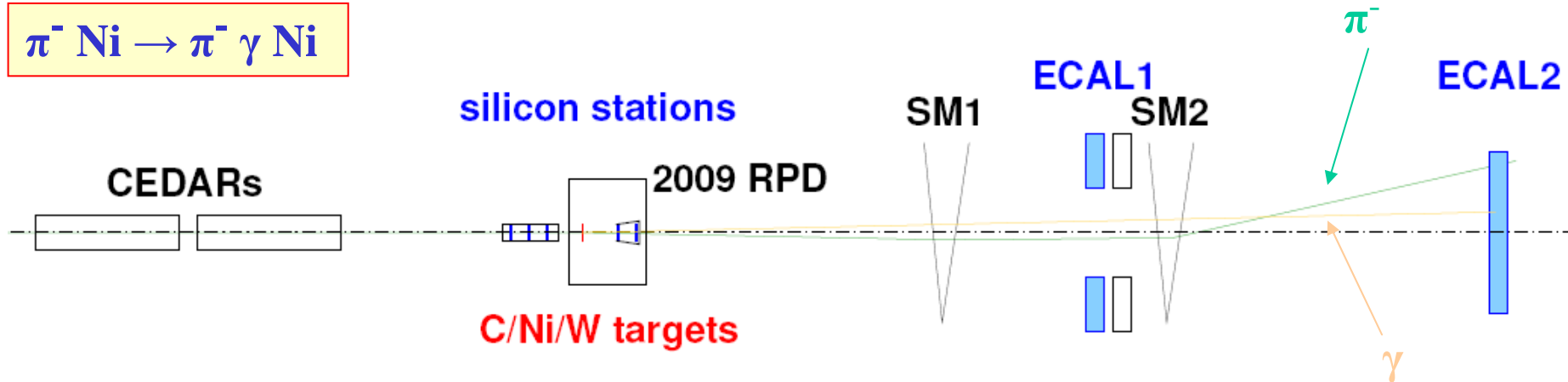
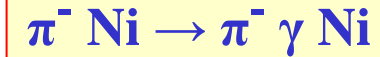
ChErenkov Differential counter with Achromatic Ring focus



Two CEDAR detectors located about 30 m upstream of the target

In 2009 Primakoff data taking both CEDARs set on kaons  
to attain the highest kaon suppression

## Principle of measurement and event selection



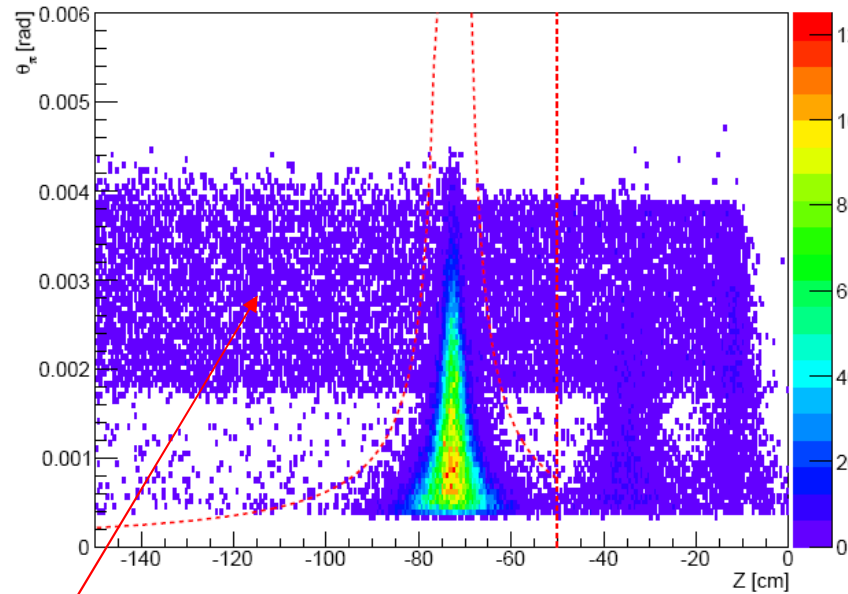
- Two dedicated Primakoff triggers:** incoming beam particle AND energy deposit either  $> 60$  or  $> 40$  GeV in central part of ECAL2
- Topology** of event: just one outgoing negatively charged track  
 + common vertex of beam and charged tracks within the target  
 + just one ECAL2 energy cluster  $> 2$  GeV not attributed to charged track
- Outgoing pion with  $p_T > 40$  MeV/c**  
 to avoid region dominated by multiple scattering of pion in the target
- Exclusivity** selection: energy balance must be  $|\Delta E| < 15$  GeV  

$$\Delta E = E_\pi + E_\gamma - E_{\text{beam}}$$
- Selection of photon exchange** (Primakoff process):  $Q^2 < 0.0015$  (GeV/c)<sup>2</sup>
- Invariant mass  $m_{\pi\gamma} < 3.5m_\pi \approx 0.49$  GeV/c<sup>2</sup>**  
 to suppress background from  $\rho^-(770)$  production with decay into  $\pi^- \pi^0$

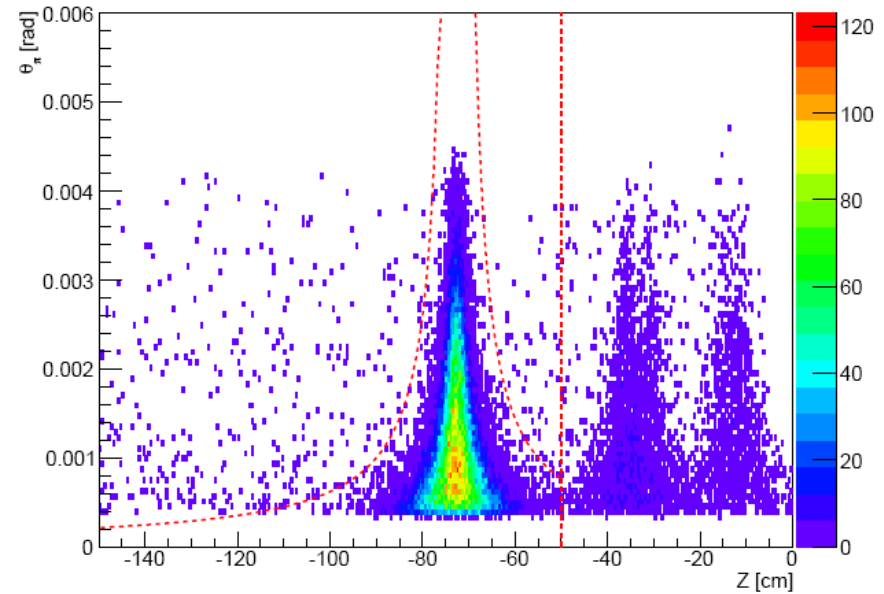
## Vertex resolution and suppression of beam kaons (2.4%)

here and in the following slides all 'Primakoff selections' applied  
except those those shown in a given plot

no PID of beam



kaons suppressed using CEDAR info.



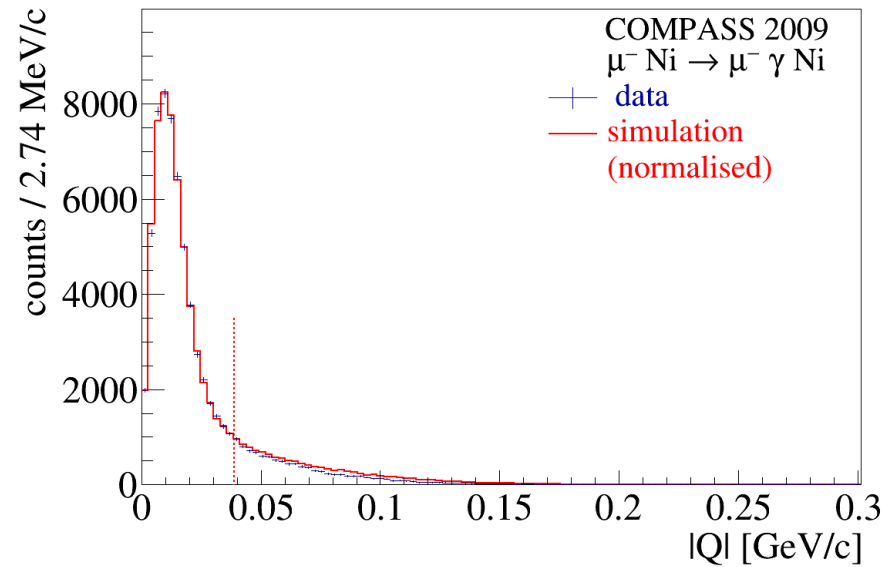
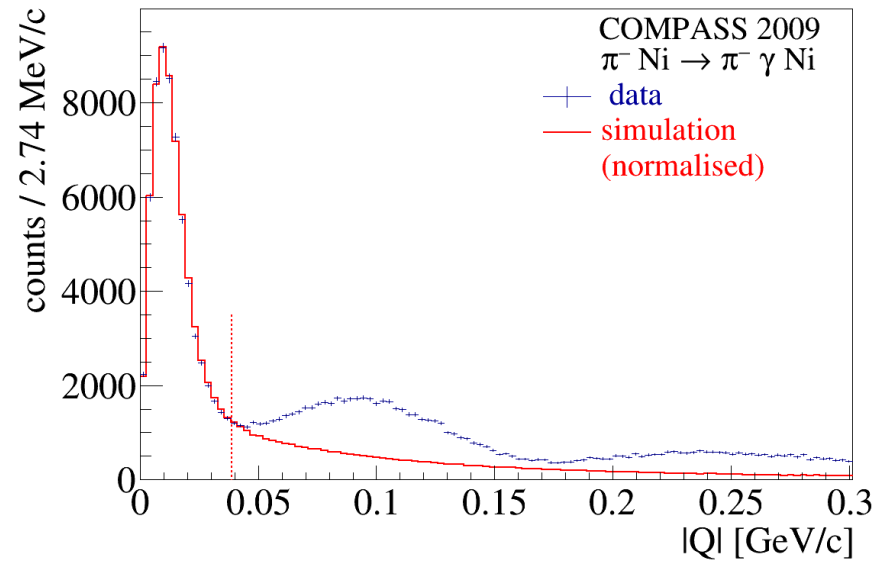
decays of beam kaons:  $K^- \rightarrow \pi^- \pi^0 \rightarrow \pi^- \gamma \gamma$

pion scattering angle vs. longitudinal position of the vertex



$\theta_\pi$ -dependent cut on  $z$  to isolate interactions on Ni target (denoted by red lines)

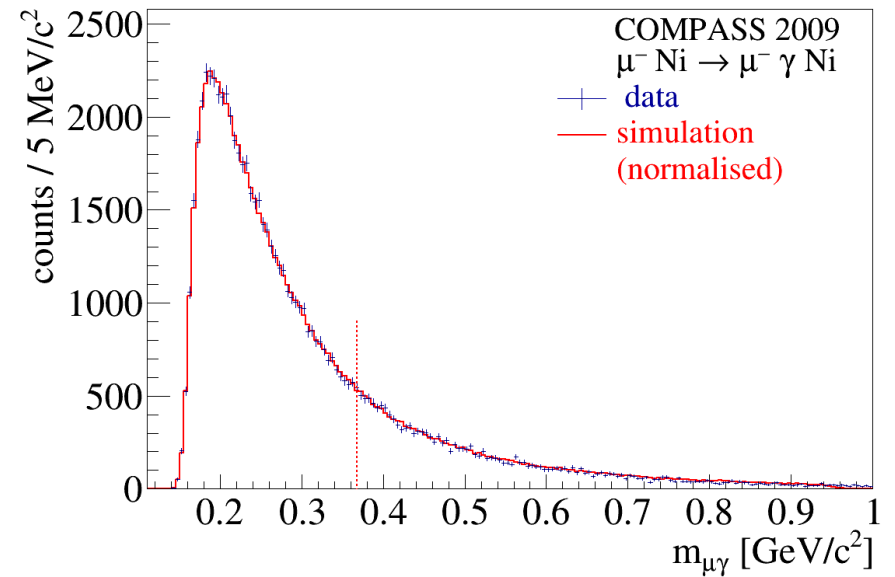
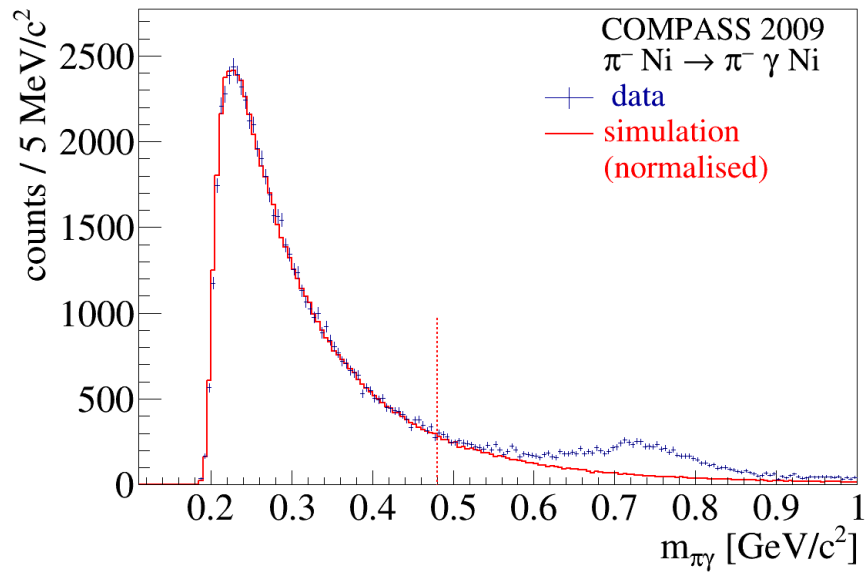
# Identifying $\pi\gamma\rightarrow\pi\gamma$ (or $\mu\gamma\rightarrow\mu\gamma$ ) reaction; selection of photon exchange



$$Q^2 < 0.0015 \text{ (GeV/c)}^2$$

$$Q^2 = - (p_{\pi}^{\mu} + p_{\gamma}^{\mu} - p_{\text{beam}}^{\mu})^2$$

## Mass of the final $\pi\gamma$ (or $\mu\gamma$ ) system

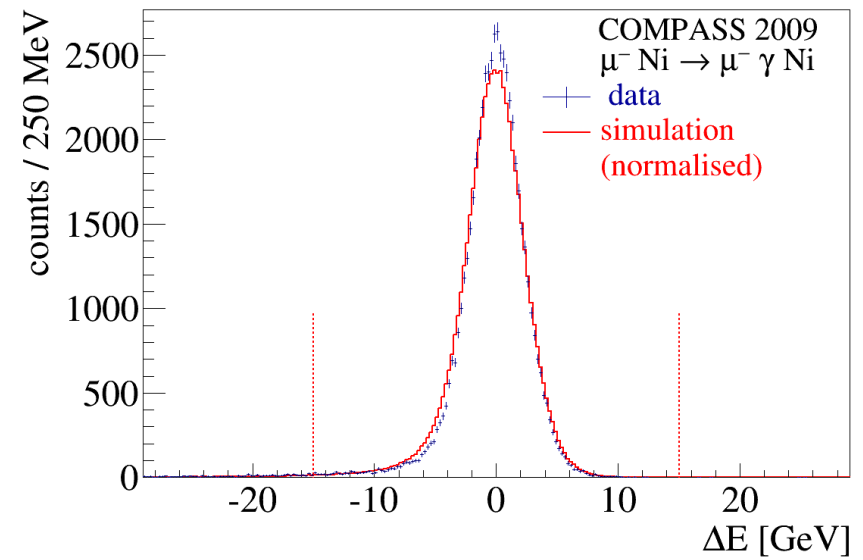
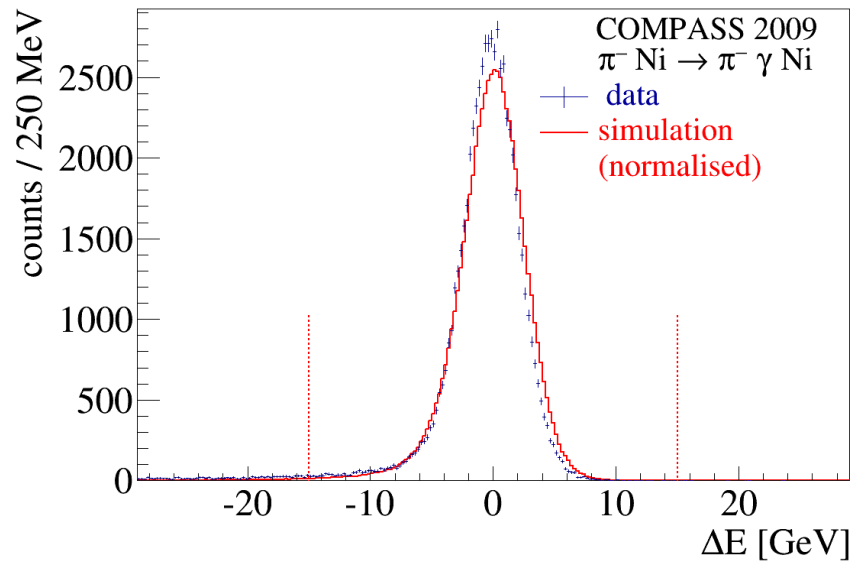


$$\underline{m_{\pi\gamma} < 3.5m_{\pi} \approx 0.49 \text{ GeV}/c^2}$$

to suppress background from  $\rho^-(770)$  production

with decay into  $\pi^- \pi^0 \rightarrow \pi^- \gamma \gamma$

# Identifying $\pi\gamma\rightarrow\pi\gamma$ (or $\mu\gamma\rightarrow\mu\gamma$ ) reaction; exclusivity selection



$$|\Delta E| < 15 \text{ GeV}$$

$$\Delta E = E_{\pi} + E_{\gamma} - E_{\text{beam}}$$

$\sigma \approx 3 \text{ GeV}$ , mainly from ECAL2

for selected range  $Q^2 < 0.0015 \text{ (GeV}/c)^2$

kinetic energy of Ni recoil  $< 8 \text{ keV}$ , neglected for  $\Delta E$

## Extraction of the pion polarisability

- Assuming  $\alpha_\pi = -\beta_\pi$ , from the cross section for  $\pi \gamma^*_{\{Ni\}} \rightarrow \pi \gamma$

$$R_\pi = \left( \frac{d\sigma_{\pi\gamma}}{dx_\gamma} \right) / \left( \frac{d\sigma_{\pi\gamma}^0}{dx_\gamma} \right) = 1 - \frac{3 m_\pi^3}{2 \alpha} \frac{x_\gamma^2}{1 - x_\gamma} \alpha_\pi \quad x_\gamma = E_\gamma / E_{\text{beam}}$$

measured cross section

simulated cross section expected for  $\alpha_\pi = 0$

fit to  $R_\pi(x_\gamma) \rightarrow \alpha_\pi$

- Control systematics by

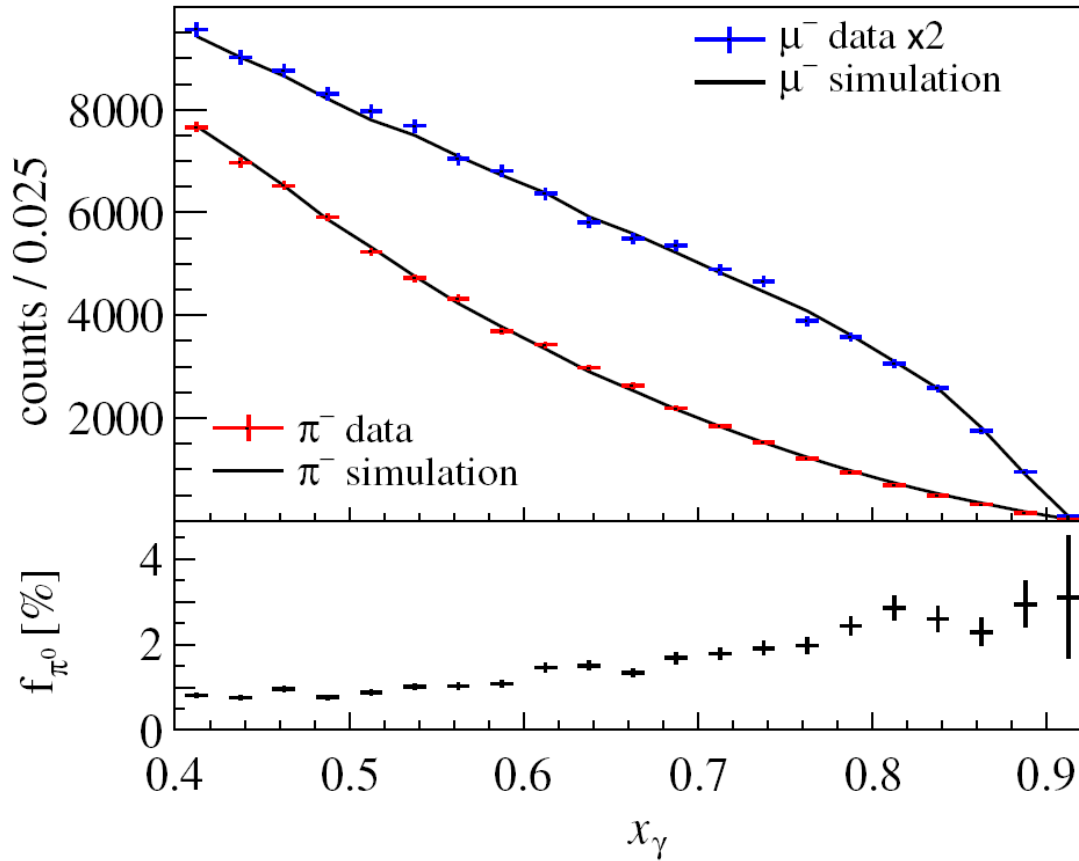
- $\mu \gamma^*_{\{Ni\}} \rightarrow \mu \gamma$

and

- $K^- \rightarrow \pi^- \pi^0 \rightarrow \pi^- \gamma \gamma$



# Photon energy spectra for pion and muon beams



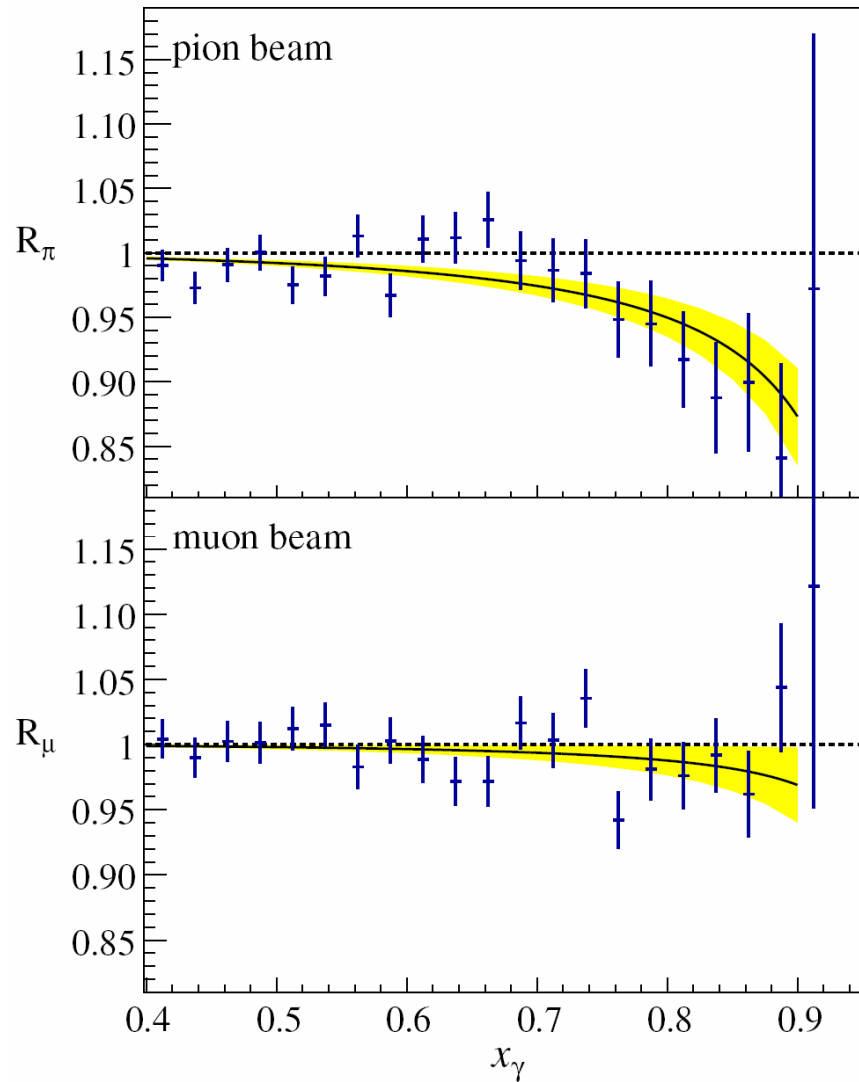
$\approx$  63 000 Primakoff events ( $x_\gamma > 0.4$ )  
 (Serpukhov  $\approx$  7 000 for  $x_\gamma > 0.5$ )

$$x_\gamma = E_\gamma / E_{\text{beam}}$$

fraction  $f_{\pi^0}$  of  $\pi^0$  background from  $\pi^- \text{Ni} \rightarrow \pi^- \pi^0 X \rightarrow \pi^- \gamma \cancel{\gamma} X$   
 subtracted from the pion data

estimated from decays of beam kaons  $K^- \rightarrow \pi^- \pi^0 \begin{cases} \rightarrow \pi^- \gamma \gamma \\ \rightarrow \pi^- \gamma \cancel{\gamma} \end{cases}$

## Pion polarisability – COMPASS result



$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) 10^{-4} \text{ fm}^3$$

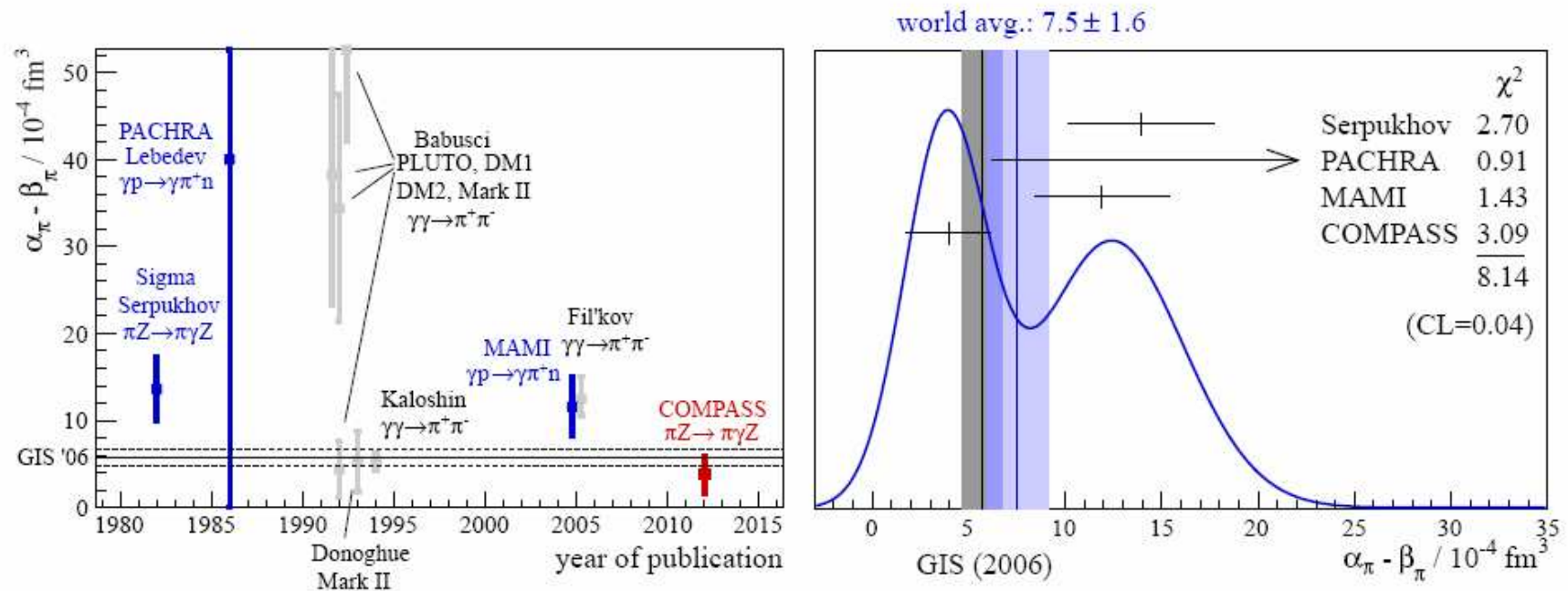
2-loop ChPT prediction  $\alpha_\pi = 2.93 \times 10^{-4} \text{ fm}^3$   
⇒ expectation from ChPT confirmed  
within the uncertainties

control measurements of ‘false polarisability’  
with muon beam

$$\alpha_\mu = (0.5 \pm 0.5_{\text{stat}}) 10^{-4} \text{ fm}^3$$

⇒ no significant systematic bias

# Pion polarisability – world data including COMPASS



- The new COMPASS result is in significant tension with the earlier measurements of the pion polarisability
- The expectation from ChPT is confirmed within the uncertainties

## Conclusions and outlook

- measurement of the **pion polarisability** via the Primakoff reaction (2009 data)

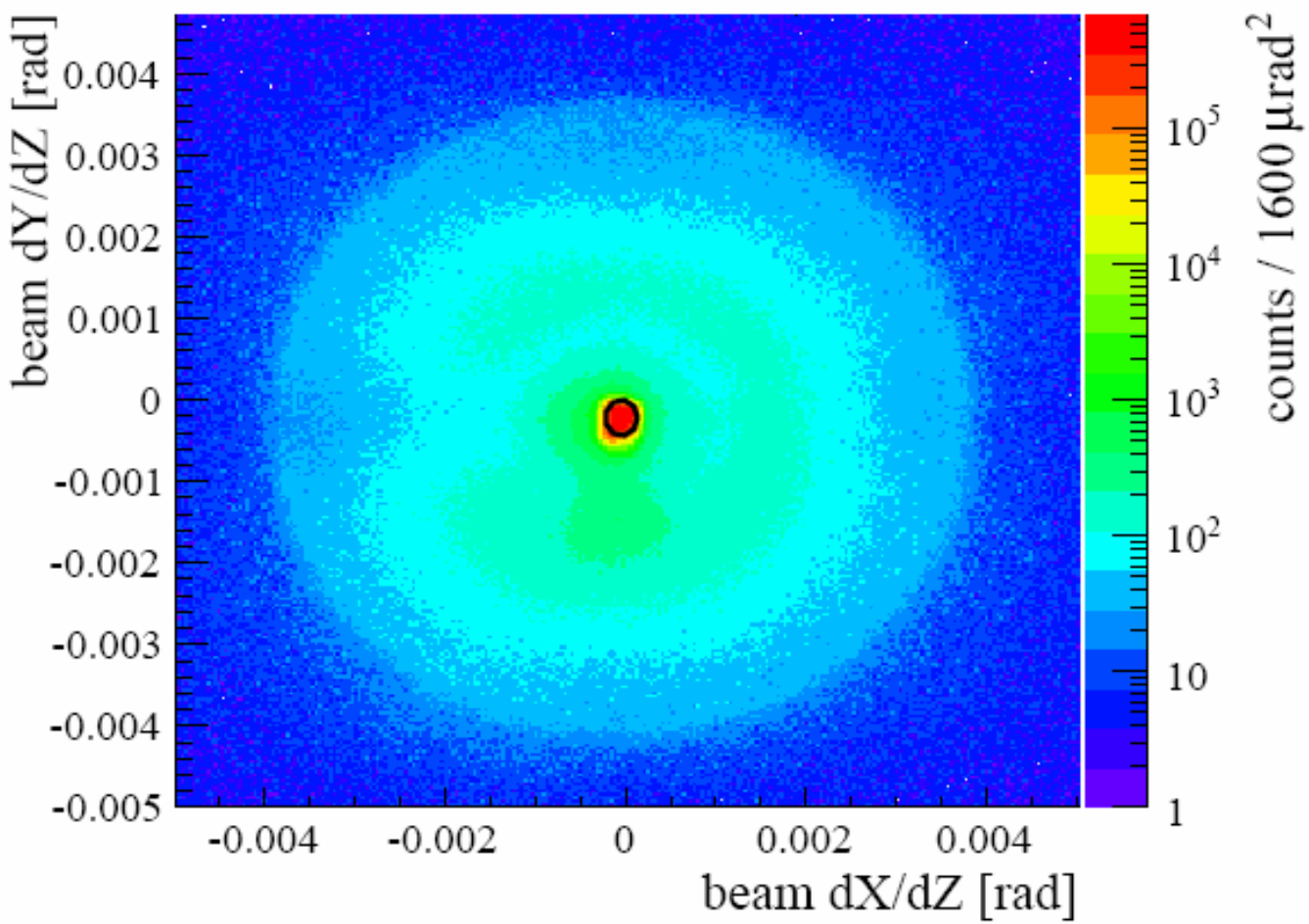
$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) 10^{-4} \text{ fm}^3$$

with assumption  $\alpha_\pi = -\beta_\pi$

- new precise experimental determination
  - control of systematics:  $\mu \gamma \rightarrow \mu \gamma$
  - the expectation for ChPT confirmed within the uncertainties
  - the COMPASS results is in tension with the earlier measurements
- 
- high statistics run 2012 (COMPASS-II) ( $\approx 4$  times larger than in 2009)
    - separate determination of  $\alpha_\pi$  and  $\beta_\pi$
    - measurement of quadrupole polarisabilities of  $\alpha_2$  and  $\beta_2$
    - s-dependence of polarisabilities
    - first measurement of the kaon polarisability

Backup

Divergence of the hadron beam



beam divergence cut indicated in black

## Systematic uncertainties

TABLE I. Estimated systematic uncertainties at 68% confidence level.

Source of uncertainty	Estimated magnitude [ $10^{-4}$ fm <sup>3</sup> ]
Determination of tracking detector efficiency	0.5
Treatment of radiative corrections	0.3
Subtraction of $\pi^0$ background	0.2
Strong interaction background	0.2
Pion-electron elastic scattering	0.2
Contribution of muons in the beam	0.05
Quadratic sum	0.7

# Other Primakoff processes

$$\pi^- + \gamma \rightarrow \begin{cases} \pi^- + \gamma \\ \pi^- + \pi^0 / \eta \\ \pi^- + \pi^0 + \pi^0 \\ \pi^- + \pi^- + \pi^+ \quad \leftarrow \text{published} \\ \pi^- + \pi^- + \pi^+ + \pi^- + \pi^+ \\ \pi^- + \dots \end{cases}$$

analogously: *Kaon-induced reactions*  $K^- + \gamma \rightarrow \dots$

Measured absolute cross-section of  $\pi^- \gamma \rightarrow \pi^- \pi^- \pi^+$

