

Measurement of the Pion Polarizability at COMPASS

Jan M. Friedrich

Physik-Department, TU München

COMPASS collaboration



Particle Physics Seminar
April 3, 2015



Bundesministerium
für Bildung
und Forschung



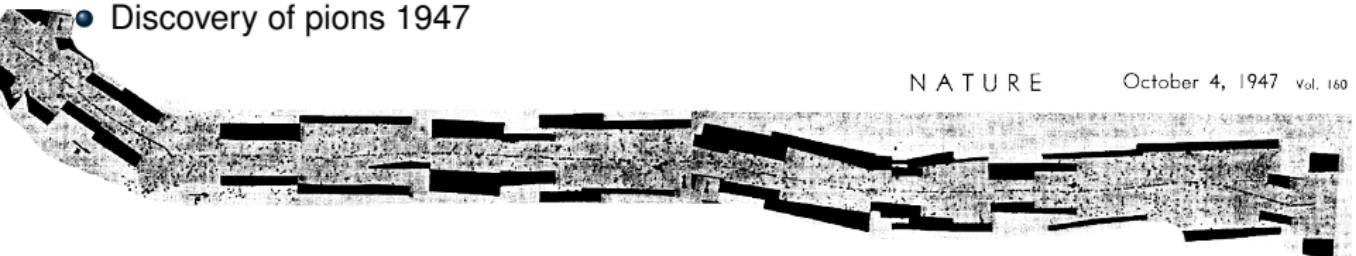
Short story of the pion

- Yukawa 1935: hypothesis of ~ 100 MeV massive exchange particle
“ μ ” for the strong interaction between protons and neutrons
- Discovery of muons 1936



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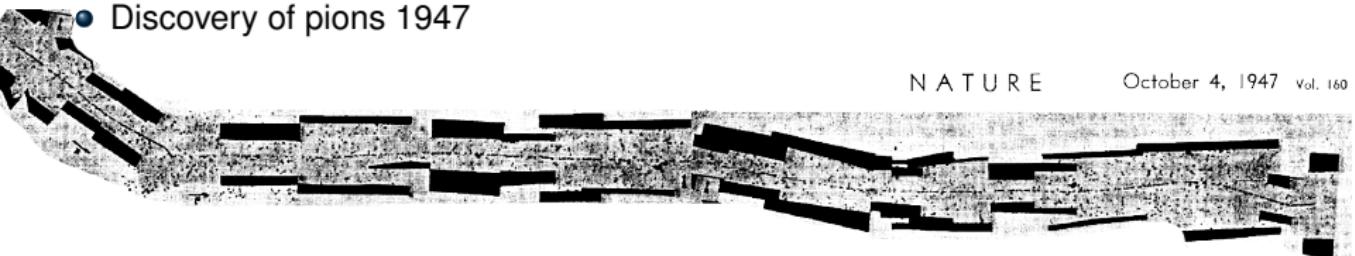
NATURE

October 4, 1947 Vol. 160



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NATURE

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- 1958: decay $\pi^+ \rightarrow \mu^+ \nu_\mu$ dominant, small branching $\pi^+ \rightarrow e^+ \nu_e$
 $\Rightarrow V - A$ theory of weak interaction
 - 1961: Spin-1 mesonic excitation of the pion (ρ -resonance at BNL)
 - 1964: quark hypothesis
 - 1966: pion scattering lengths
- ⋮



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- 1964: quark hypothesis
- 1966: pion scattering lengths
- :
- 1982: first data on the pion polarisability

Measurement of the Charged-Pion Polarizability

C. Adolph,⁸ R. Akhunzyanov,⁷ M. G. Alexeev,²⁷ G. D. Alexeev,⁷ A. Amoroso,^{27,29} V. Andrieux,²² V. Anosov,⁷
 ... [213 authors]

(COMPASS Collaboration)

(Received 2 June 2014; revised manuscript received 24 December 2014; published 10 February 2015)

The COMPASS collaboration at CERN has investigated pion Compton scattering, $\pi^-\gamma \rightarrow \pi^-\gamma$, at center-of-mass energy below 3.5 pion masses. The process is embedded in the reaction $\pi^-Ni \rightarrow \pi^-\gamma Ni$, which is initiated by 190 GeV pions impinging on a nickel target. The exchange of quasireal photons is selected by isolating the sharp Coulomb peak observed at smallest momentum transfers, $Q^2 < 0.0015 \text{ (GeV}/c)^2$. From a sample of 63 000 events, the pion electric polarizability is determined to be $\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3$ under the assumption $\alpha_\pi = -\beta_\pi$, which relates the electric and magnetic dipole polarizabilities. It is the most precise measurement of this fundamental low-energy parameter of strong

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CERN experiment brings precision to a cornerstone of particle physics

11 Feb 2015

Geneva, 11 February 2015. In a paper published yesterday in the journal *Physical Review Letters*, the COMPASS experiment at CERN¹ reports a key measurement on the strong interaction. The strong interaction binds quarks into protons and neutrons, and protons and neutrons into the nuclei of all the elements from which matter is built. Inside those nuclei, particles called pions made up of a quark and an antiquark mediate the interaction. Strong interaction theory makes a precise prediction on the polarisability of

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PRAZISIONSMESSUNG ZUR STARKEN WECHSELWIRKUNG

Pioniern genannte Kernteilchen tragen wesentlich zur so genannten starken Wechselwirkung bei. Sie ist die Kraft, die Atomkerne zusammenhält und für die Masse der uns umgebenden Materie verantwortlich ist. Erstmals ist es Physikern nun gelungen, die Verformbarkeit von Pionen exakt zu bestimmen. Das Ergebnis, zu dem Physiker der Technischen Universität München (TUM) maßgeblich beigetragen haben, stimmt gut mit den theoretischen Vorhersagen überein und revidiert frühere Messungen, deren Ergebnisse nicht mit dem Standardmodell der Physik vereinbar waren.

CERN experiment brings precision cornerstone of particle physics

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exakte Messung der Polarisierbarkeit von Pionen stützt Standardmodell

Präzisionsmessung zur starken Wechselwirkung

10.02.2015, Forschung

Das in der TUM entwickelte Detektormodul - Foto: TUM

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LHC Session 2: New frontiers in physics

Press echo in spring 2015



Featured Research

CERN experiment brings precision to a cornerstone of particle physics

Date: February 11, 2015

Source:

CERN

The COMPASS experiment at CERN reports a key measurement on the strong interaction. The strong interaction turns protons into quarks and gluons, and protons and neutrons into nucleons. Quarks, called elements from which we build, trade those nuclei, and antiquarks, called elements from which we build, trade those nuclei, and antiquarks, making up the pion. Strong interaction theory makes predictions on the strong interaction theory makes predictions on the shape of a pion. The pion's polarisability has baffled scientists since the 1990s, while the test measurements now seem to be at odds with the theory. Now result is in close agreement with theory.

Focus.it

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L'interazione forte dei quark ha meno segreti

L'esperimento COMPASS al CERN fornisce una misura chiave dell'interazione forte.



NO OFFERTO A RISETTO DA IBERI - SOTTO PROGRAMMI MIAPP CEA
Lo spettrometro dell'esperimento COMPASS. È lungo 60 metri e il suo interno vengono sparati raggi di particelle subatomiche ad alta intensità. - cms



J. M. Friedrich — Pion Polarizability with COMPASS

6/43

Nouvelles suisse Zeitung
PHYSIK UND CHEMIE
Pionen-Experiment am Cern
Da schwabbeln nichts
11.2.2015, 17:08 Uhr

rtz. Wieder hat ein Experiment die theoretischen Vorhersagen des Standardmodells der Teilchenphysik bestätigt. Diesmal massen die Forschenden die Verformbarkeit sogenannter Pionen. Diese gibt Aufschluss darüber, wie stark die Bindungskraft zwischen den Elementarteilchen im Inneren von Atomkernen ist.

Avenir Fundamental à la une

Le pion se déforme moins que prévu

C'est la confirmation d'une donnée de physique fondamentale que fournie l'expérience COMPASS menée au CERN sur une mesure relativement à l'interaction forte, la force qui lie quarks, neutrons et protons.

ScienceSeeker
Science news from science newsmakers

CERN Physicists Measure Polarizability of Pion

Scientists from CERN and the COMPASS collaboration have made the most precise measurement ever of the polarizability of the pion, a fundamental parameter of strong interaction. Everything we see in the Universe is made up of matter, consisting of three groups of three particles: quarks and leptons. Quarks are bound together in groups of three to make up the building blocks [1].

cernceaifrlu

Une expérience du CERN affine une mesure essentielle pour décrire l'interaction forte

L'expérience COMPASS du CERN, impliquant le CEA et des partenaires internationaux, rapporte une mesure de la polarisabilité du pion. Celle-ci établit les composants des noyaux atomiques (quarks et gluons) dans le myrme. Les résultats, renversant une prévision de plus faible des mesures - le pion, à l'interaction forte, devrait être plus déformé que prévu.

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The image is a collage of several news articles and snippets from different media sources, all centered around the COMPASS experiment at CERN. At the top left is a snippet from 'ScienceDaily' with the headline 'CERN experiment brings precision to a cornerstone of particle physics'. Below it is a snippet from 'Neue Zürcher Zeitung' with the headline 'Pionen-Experiment am Cern Da schwabb'. To the right is a snippet from 'Wydział Fizyki Uniwersytetu Warszawskiego' with the headline 'Polaryzowalność pionów: pierwszy precyzyjny pomiar w CERN z udziałem fizyków warszawskich'. Other snippets include a large image of zebras from 'Наука и жизнь', a snippet from 'L'i' news website, and a snippet from 'Science-Metrix' with the headline 'Wie COMPASS die Stärke der starken Wechselwirkung bestimmt'. The collage also features logos for CERN, CEA, Irfu, and TU Wien.



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Sci-News.com

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CERN Physicists Measure Polarizability of Pion

Feb 16, 2015 by Sci-News.com

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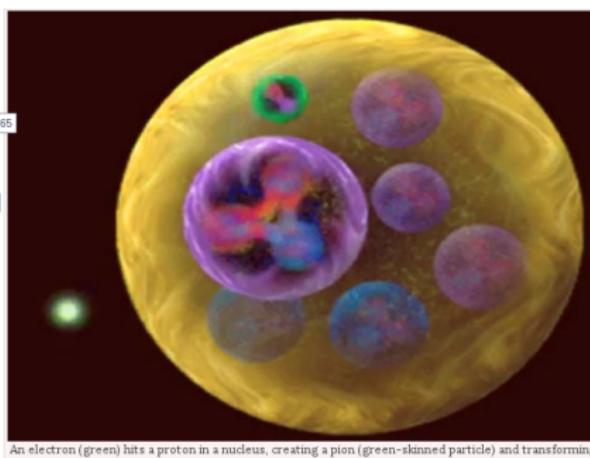


Physicists Create New Form of Ice: Square Ice



Stars May Generate Sound

Scientists from CERN's COMPASS collaboration have made the most precise measurement ever of the polarizability of pion – the fundamental low-energy parameter of strong interaction.



Everything we see in the Universe is made up of fundamental particles called

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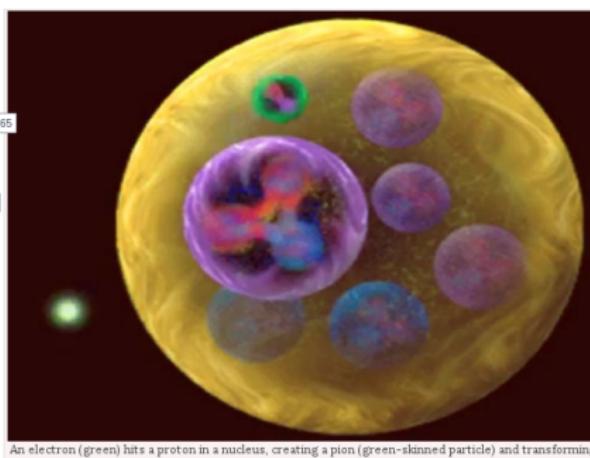


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An electron (green) hits a proton in a nucleus, creating a pion (green-skinned particle) and transforming the proton into a neutron. Image credit: Joanna Griffin / Jefferson Lab.

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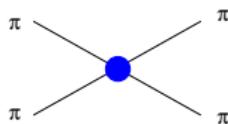
How to understand quark-gluon dynamics?



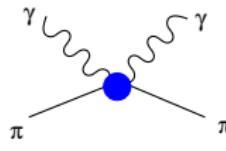
complicated system of
interacting quarks and gluons

ChPT
 $\xrightarrow{}$

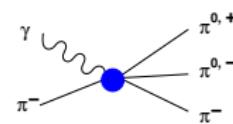
effective degrees of freedom
at low energy: mass, charge,
spin, effective (self-)coupling



π only



π -photon

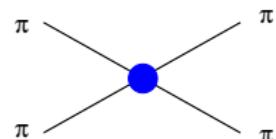


$\pi - \pi - \text{photon}$

Chiral Perturbation Theory vs. Experiment

- pion scattering lengths: 2-loop predictions

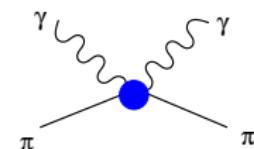
- $a_0^0 m_\pi = 0.220 \pm 0.005$ confirmed by E865 in $K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$
- $(a_0^0 - a_0^2) m_\pi = 0.264 \pm 0.006$ confirmed by NA48 in 0.268 ± 0.010 $K^+ \rightarrow \pi^+ \pi^0 \pi^0$



- pion polarisability: electric α_π , magnetic β_π

- contribution to Compton scattering
- ChPT prediction obtained by the relation to $\pi^+ \rightarrow e^+ \nu_e \gamma$ [Gasser, Ivanov, Sainio, Nucl. Phys. B745, 2006]
[PIBETA, M. Bychkov et al., PRL 103, 051802, 2009]

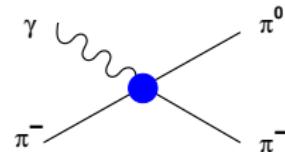
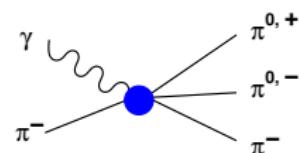
$$\begin{aligned}\alpha_\pi + \beta_\pi &= (0.2 \pm 0.1) \cdot 10^{-4} \text{fm}^3 \\ \alpha_\pi - \beta_\pi &= (5.7 \pm 1.0) \cdot 10^{-4} \text{fm}^3 \\ \alpha_\pi &= (2.9 \pm 0.5) \cdot 10^{-4} \text{fm}^3\end{aligned}$$



- ChPT prediction contradicting the experimental findings (prior to our analysis)



- Pion scattering including a real photon
 - Leading-order prediction from ChPT
 \leftrightarrow pion scattering lengths combined with photon coupling
 - **chiral loop contribution**
 theory prediction available, no measurement
- Chiral anomaly $F_{3\pi}$
 - established on 10% level
 - further development: inclusion of the ρ resonance
 theoretical work by Kubis, Hoferichter, Sakkas
 PRD86(2012)116009

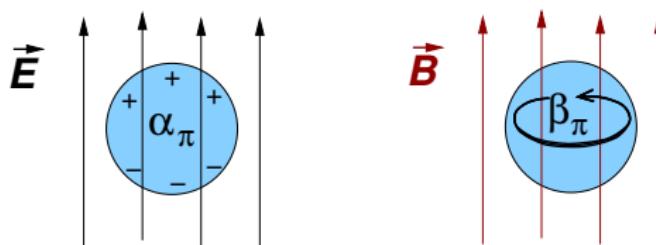




ChPT prediction for the pion polarisability

$$\pi + \gamma \rightarrow \pi + \gamma$$

Compton cross-section contains information about e.m. **polarisability**
 (as deviation from the expectation for a pointlike particle)



polarisabilities $\alpha_\pi, \beta_\pi [10^{-4} \text{ fm}^3]$

ChPT (2-loop) prediction: $\alpha_\pi - \beta_\pi = 5.7 \pm 1.0$ $\alpha_\pi + \beta_\pi = 0.16 \pm 0.1$

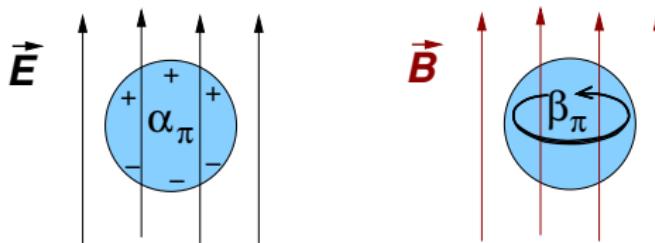
experiments: 4 — 14 ($\beta_\pi \approx -\alpha_\pi$ assumed)



ChPT prediction for the pion polarisability

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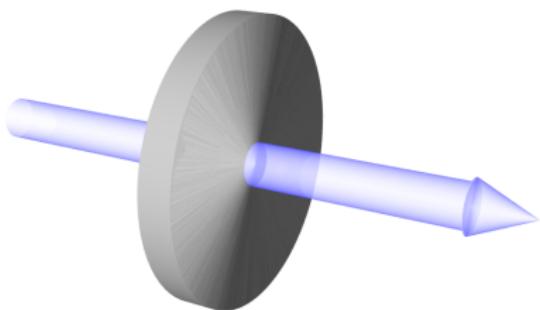
ChPT (2-loop) prediction: $\alpha_\pi = 2.93, \beta_\pi = -2.77$

experiments: 2 – 7 $(\beta_\pi \approx -\alpha_\pi \text{ assumed})$



Principle of the COMPASS measurement

- steer high-energetic pion beam on a \sim 4mm nickel disk
- observe scattered pions in coincidence with produced hard photons
- measured cross-section shape is linked to pion Compton scattering





Polarisability effect in Primakoff technique

Primakoff measurement technique

- Charged pion traversing the nuclear **electric field**

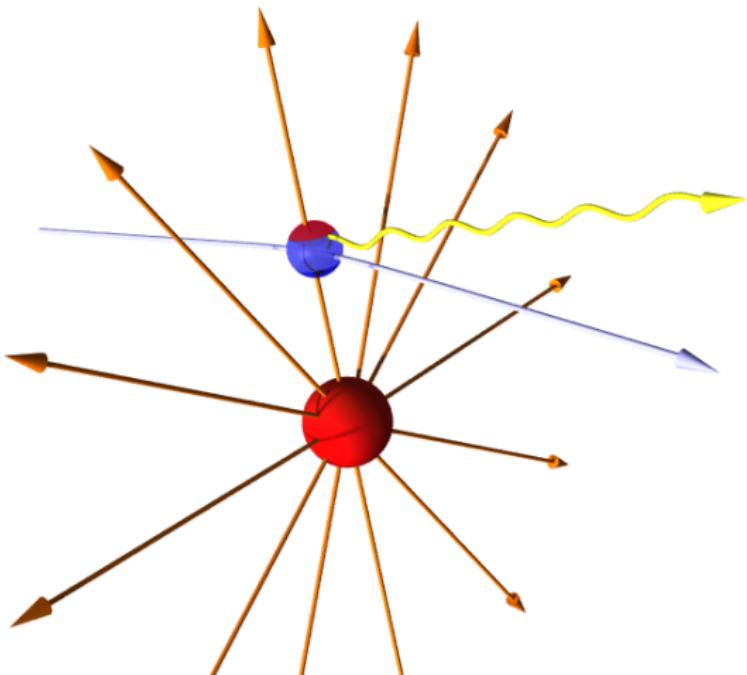
- typical field strength at $r = 5R_{Ni}$: $E \sim 300 \text{ kV/fm}$

- Bremsstrahlung emission**

- particle scatters off **equivalent photons**
- tiny momentum transfer $Q^2 \approx 10^{-5} \text{ GeV}^2/c^2$
- pion/muon (quasi-)real Compton scattering

- Polarisability contribution

- Compton cross-section typically diminished
- expected charge separation $\sim 10^{-5} \text{ fm} \cdot e$



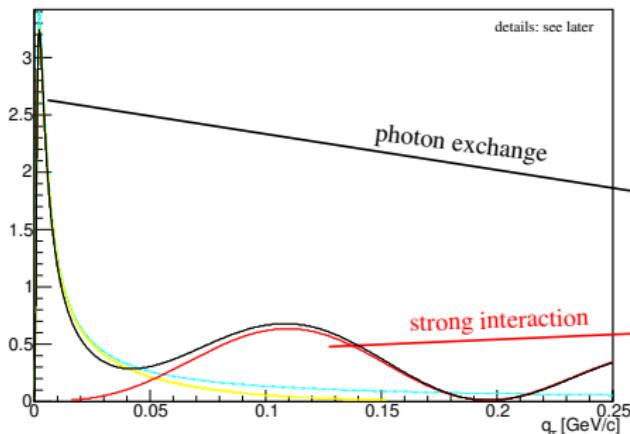


Polarisability effect in Primakoff technique

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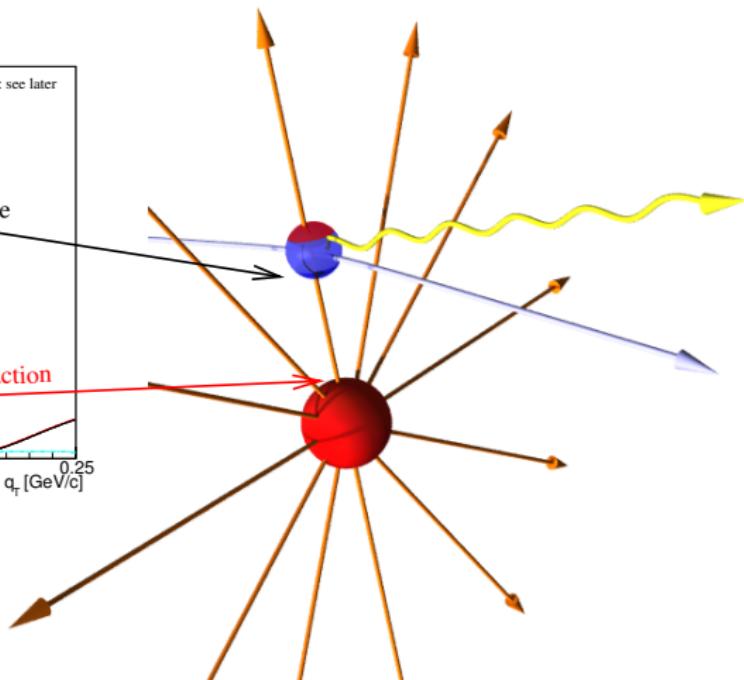
- Charged pion traversing the nuclear **electric field**

- typical field strength at

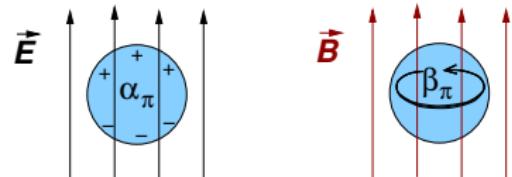
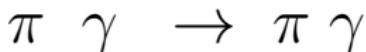


typically diminished

- expected charge separation
 $\sim 10^{-5} \text{ fm} \cdot e$



Pion Compton Scattering



- Two kinematic variables, in CM: total energy \sqrt{s} , scattering angle θ_{cm}

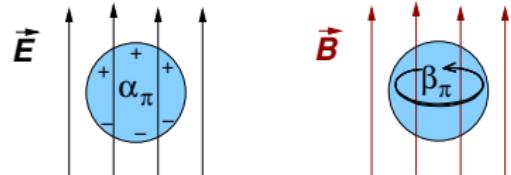
$$\frac{d\sigma_{\pi\gamma}}{d\Omega_{cm}} = \frac{\alpha^2(s^2 z_+^2 + m_\pi^4 z_-^2)}{s(sz_+ + m_\pi^2 z_-)^2} - \frac{\alpha m_\pi^3 (s - m_\pi^2)^2}{4s^2(sz_+ + m_\pi^2 z_-)} \cdot \mathcal{P}$$

$$\mathcal{P} = z_-^2(\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+^2(\alpha_\pi + \beta_\pi) - \frac{(s - m_\pi^2)^2}{24s} z_-^3(\alpha_2 - \beta_2)$$

$$z_\pm = 1 \pm \cos \theta_{cm}$$

- $\sigma_{tot}(s)$ rather insensitive to pion's low-energy structure
- Up to 20% effect on *backward* angular distributions of $d\sigma/d\Omega_{cm}$

Pion Compton Scattering



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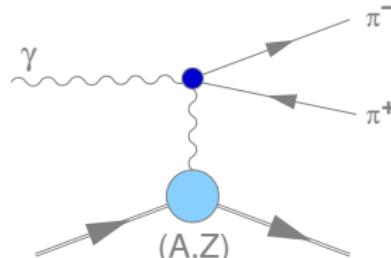
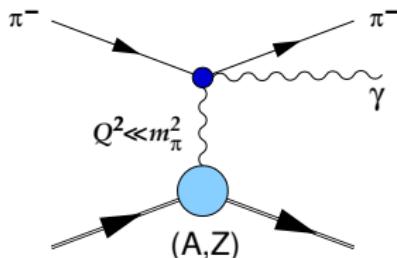
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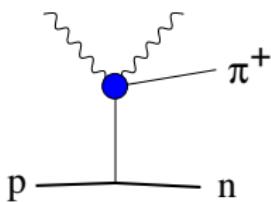
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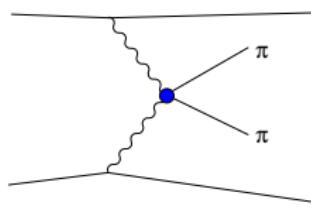
Pion Compton scattering: embedding the process



Primakoff processes



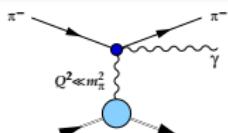
Radiative pion photoproduction



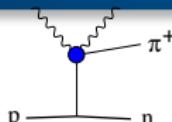
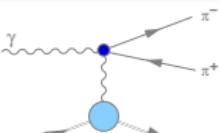
Photon-Photon fusion



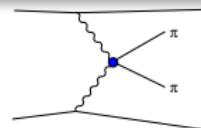
Pion polarisability: world data before COMPASS



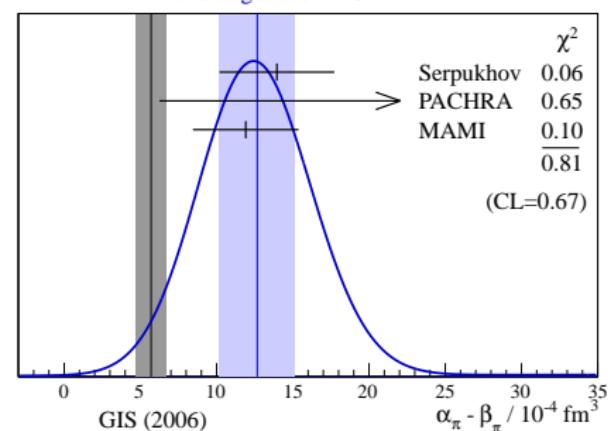
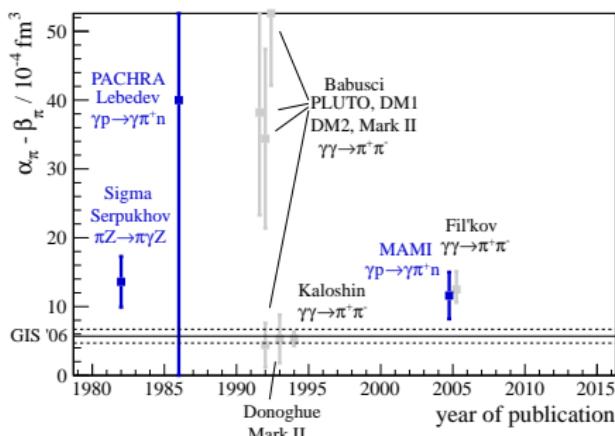
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Radiative pion photoproduction



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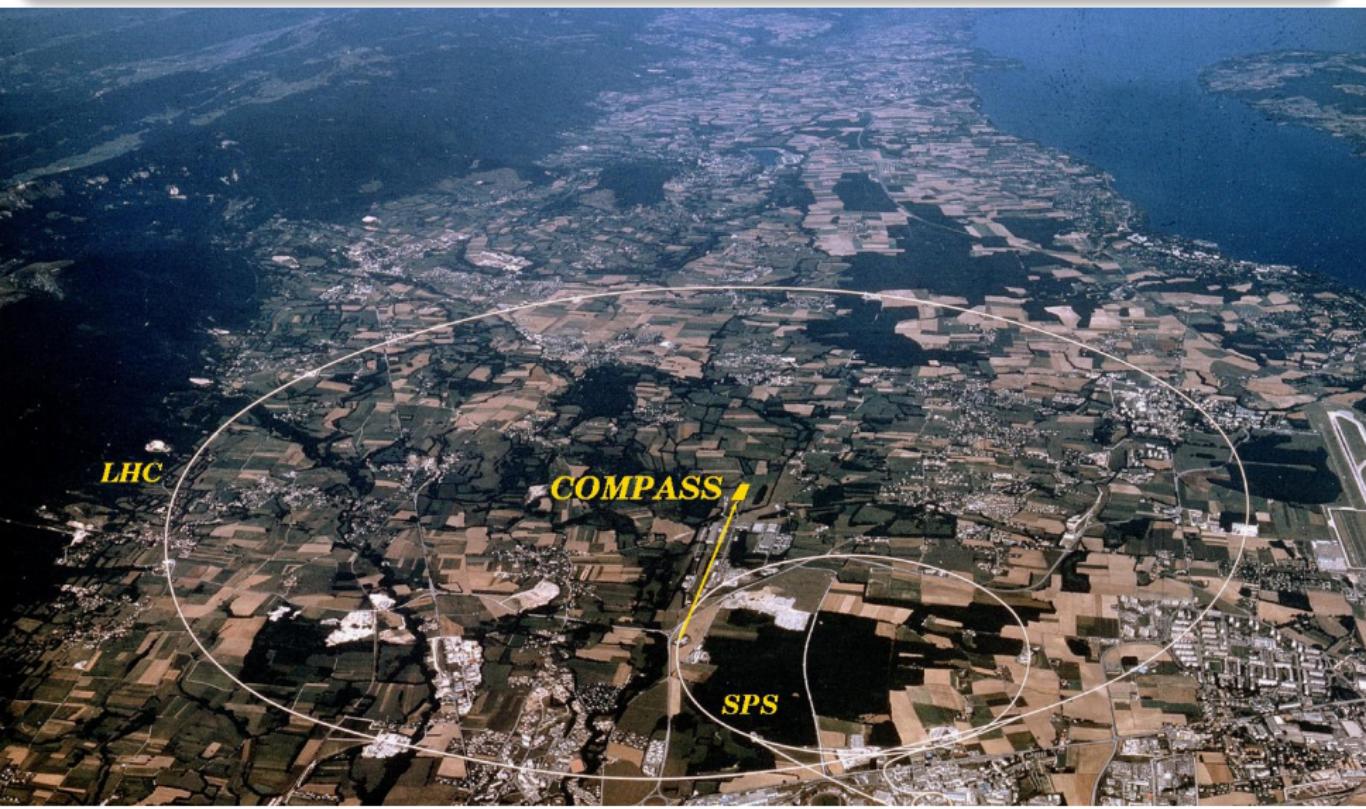


GIS'06: ChPT prediction, Gasser, Ivanov, Sainio, NPB745 (2006), plots: T. Nagel, PhD

Fil'kov analysis objected by Pasquini, Drechsel, Scherer PRC81, 029802 (2010)



COCommon Muon and Proton Apparatus for Structure and Spectroscopy

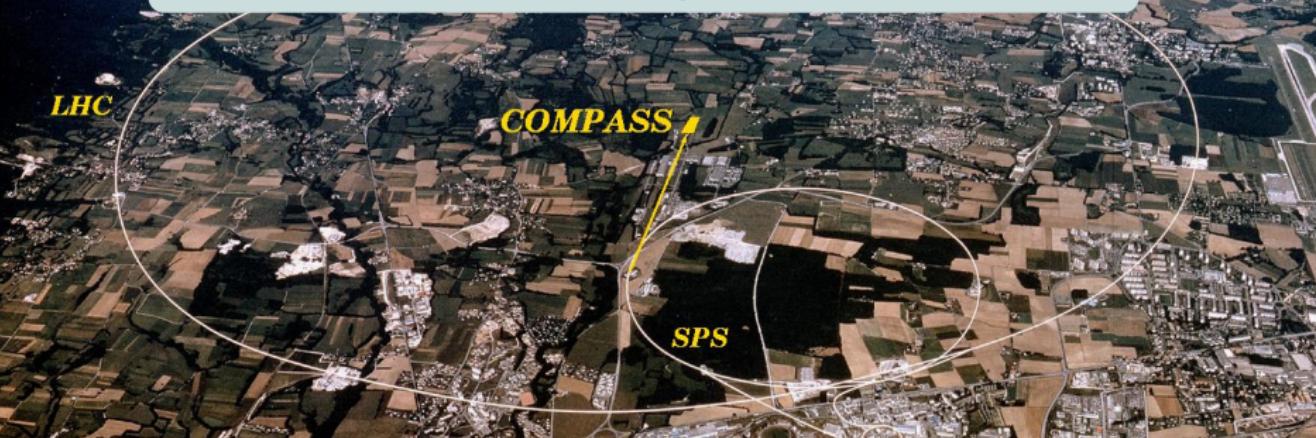




COmmon Muon and Proton Apparatus for Structure and Spectroscopy

CERN SPS: protons ~ 400 GeV (5 – 10 sec spills)

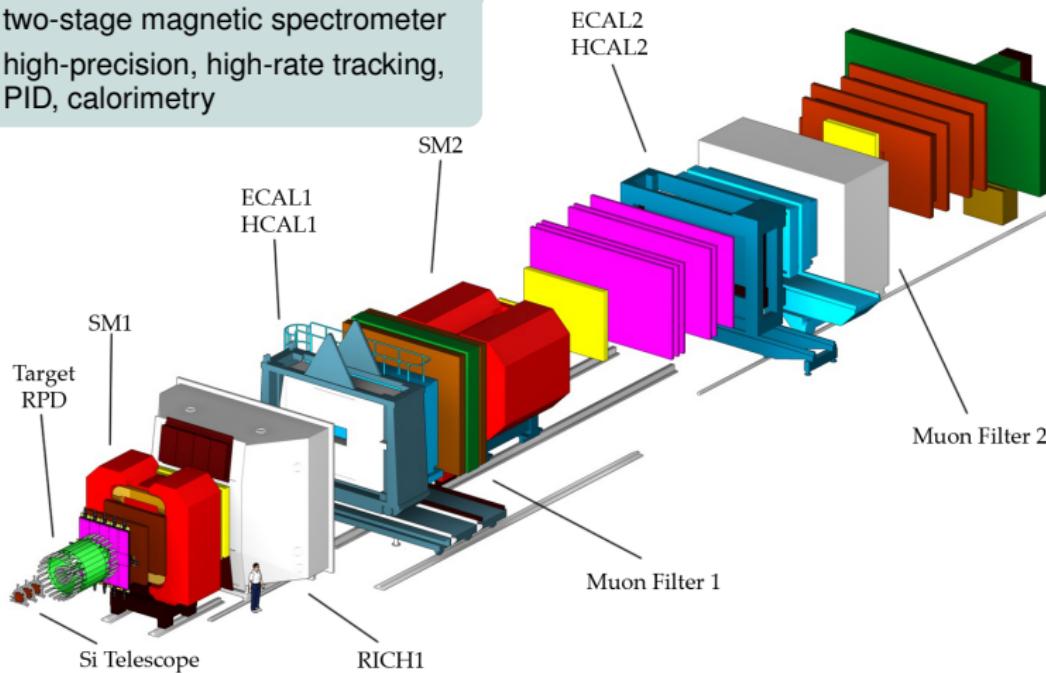
- secondary $\pi, K, (\bar{p})$: up to $2 \cdot 10^7$ /s (typ. $5 \cdot 10^6$ /s)
Nov. 2004, 2008-09, 2012:
hadron spec. & Primakoff reactions
- tertiary muons: $4 \cdot 10^7$ / s
2002-04, 2006-07, 2010-11: spin structure of the nucleon



Experimental Setup

Fixed-target experiment

- two-stage magnetic spectrometer
- high-precision, high-rate tracking, PID, calorimetry

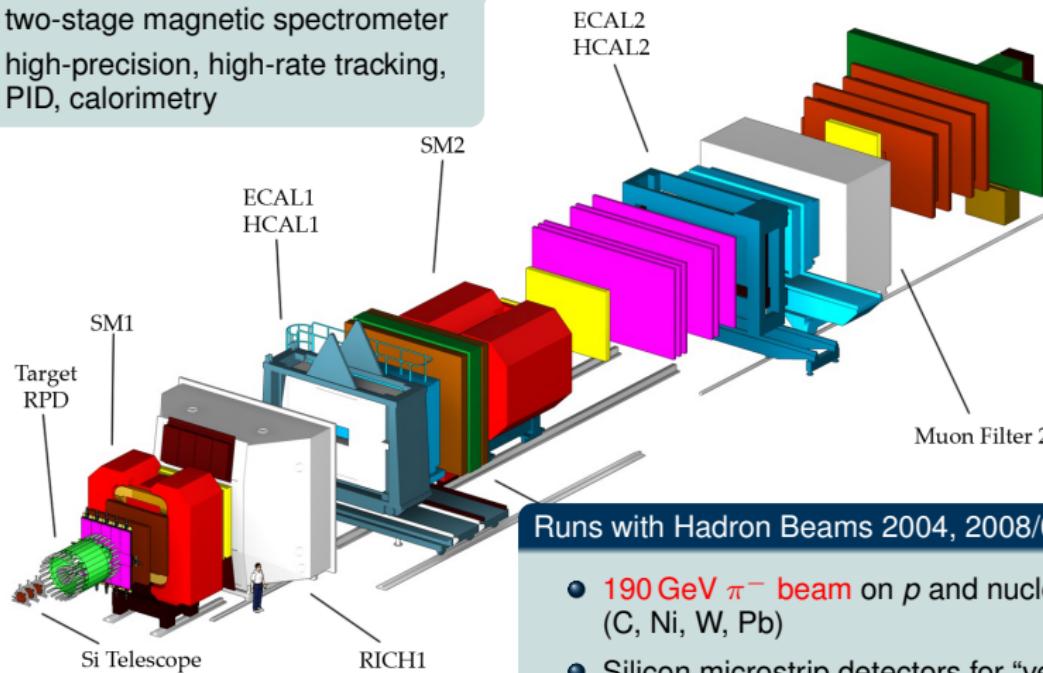




Experimental Setup

Fixed-target experiment

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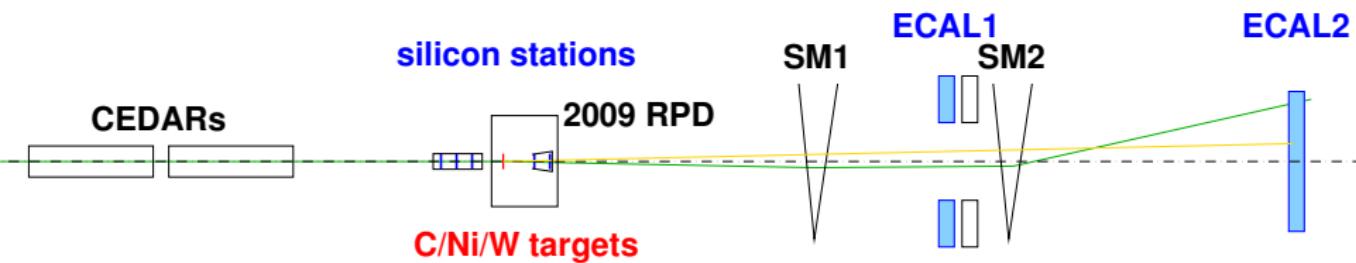


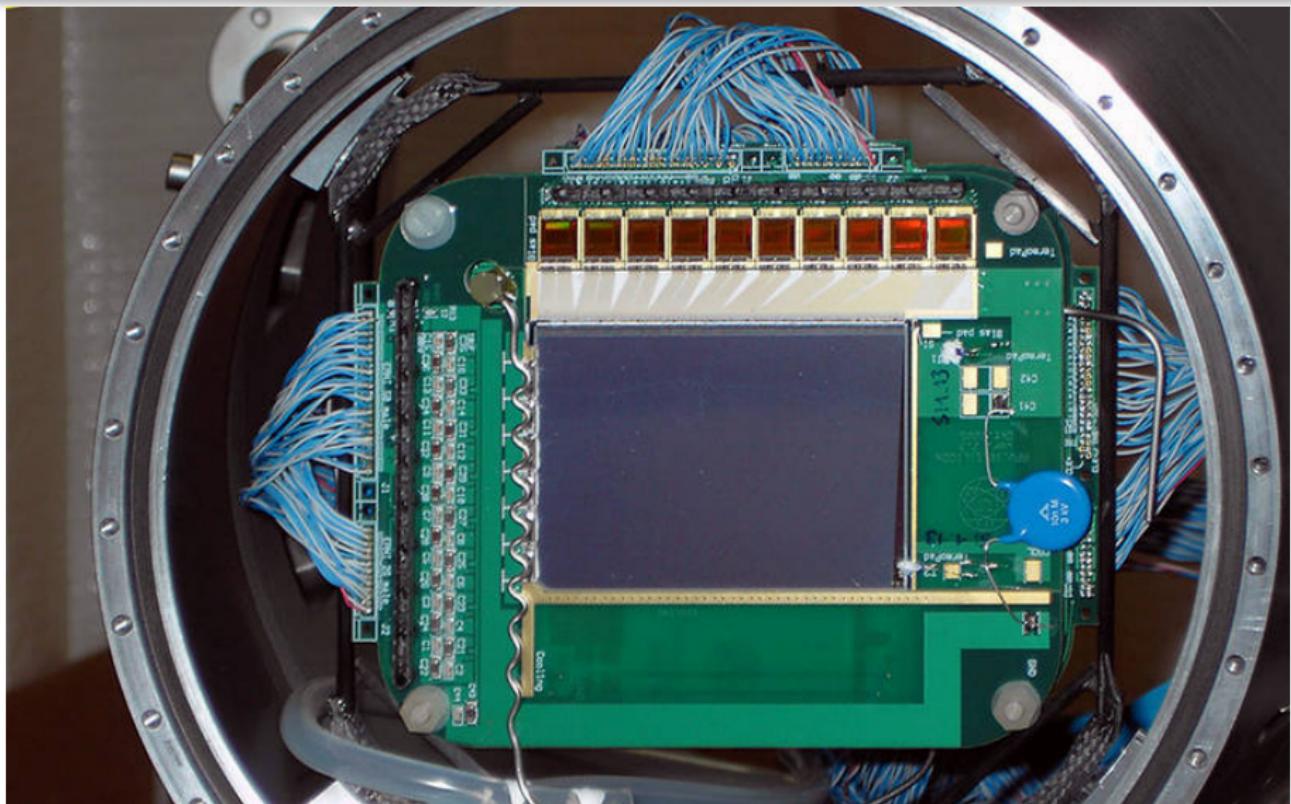
Runs with Hadron Beams 2004, 2008/09, 2012

- **190 GeV π^- beam** on p and nuclear targets (C, Ni, W, Pb)
- Silicon microstrip detectors for “vertexing”
- recoil and (digital) ECAL triggers



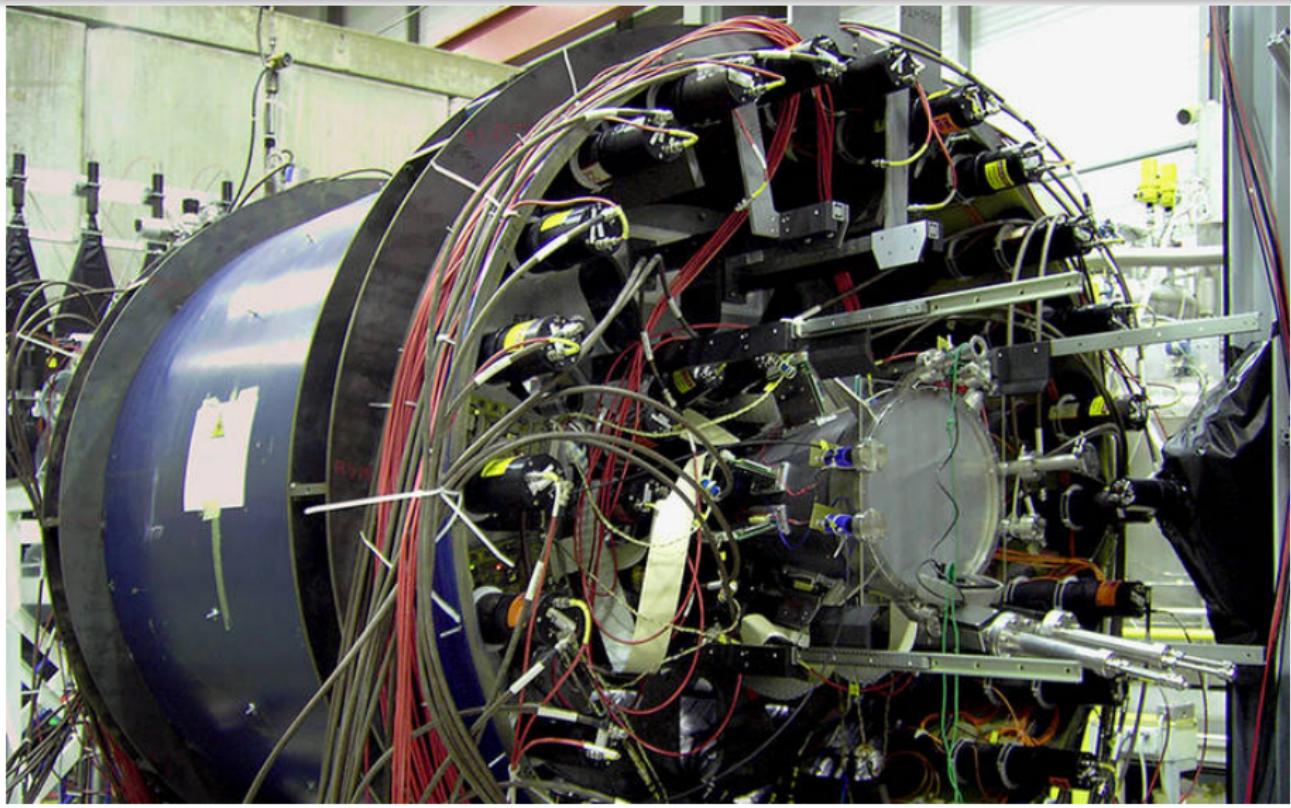
Principle of the measurement



Silicon detector module, two-sided $\sigma_{x,y} \sim 5\mu\text{m}$ 



Silicon cryostat in the recoil detector





Extraction of the pion polarisability

- Identify exclusive reactions



at smallest momentum transfer $< 0.001 \text{ GeV}^2/c^2$

- Assuming $\alpha_\pi + \beta_\pi = 0$, from the cross-section

$$R = \frac{\sigma(x_\gamma)}{\sigma_{\alpha_\pi=0}(x_\gamma)} = \frac{N_{\text{meas}}(x_\gamma)}{N_{\text{sim}}(x_\gamma)} = 1 - \frac{3}{2} \cdot \frac{m_\pi^3}{\alpha} \cdot \frac{x_\gamma^2}{1-x_\gamma} \alpha_\pi$$

is derived, depending on $x_\gamma = E_{\gamma(\text{lab})}/E_{\text{Beam}}$.
Measuring R the polarisability α_π can be concluded.

- Control systematics by



and





Extraction of the pion polarisability

- Identify **exclusive reactions**



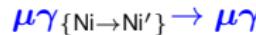
at smallest momentum transfer $< 0.001 \text{ GeV}^2/c^2$

- Assuming $\alpha_\pi + \beta_\pi = 0$, from the cross-section

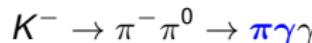
$$R = \frac{\sigma(x_\gamma)}{\sigma_{\alpha_\pi=0}(x_\gamma)} = \frac{N_{\text{meas}}(x_\gamma)}{N_{\text{sim}}(x_\gamma)} = 1 - \frac{3}{2} \cdot \frac{m_\pi^3}{\alpha} \cdot \frac{x_\gamma^2}{1-x_\gamma} \alpha_\pi$$

is derived, depending on $x_\gamma = E_{\gamma(\text{lab})}/E_{\text{Beam}}$.
Measuring R the polarisability α_π can be concluded.

- Control systematics by



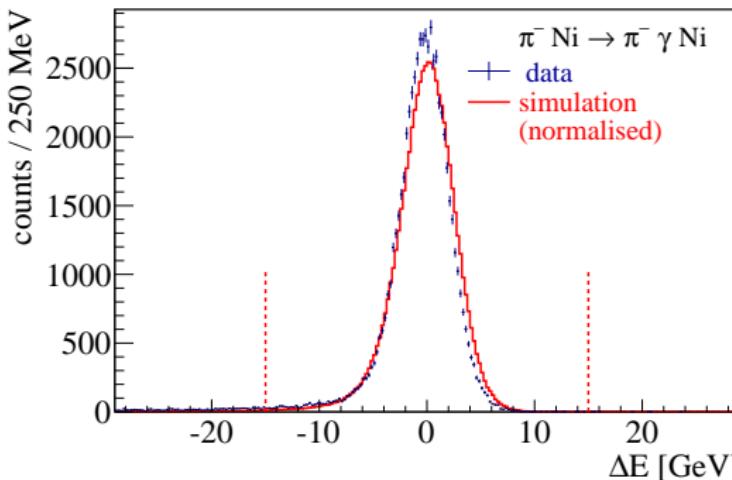
and





Identifying the $\pi\gamma \rightarrow \pi\gamma$ reaction

Phys. Rev. Lett. 114, 062002 (2015)

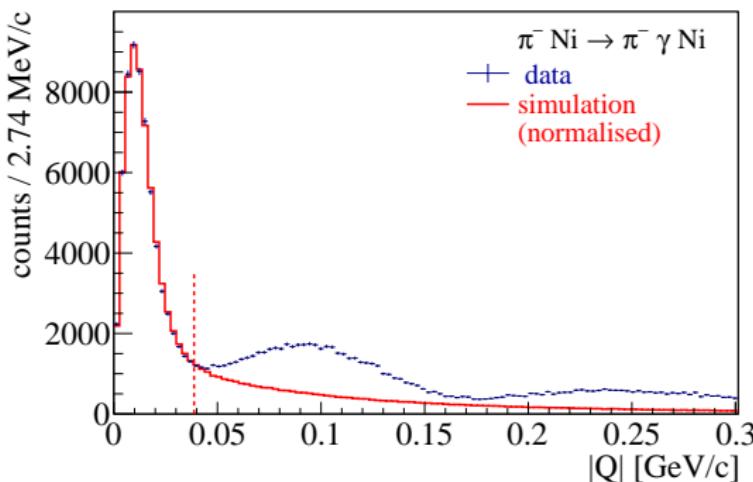


- Energy balance $\Delta E = E_\pi + E_\gamma - E_{\text{Beam}}$
- Exclusivity peak $\sigma \approx 2.6 \text{ GeV}$ (1.4%)
- ~ 63.000 exclusive events ($x_\gamma > 0.4$) (Serpukhov ~ 7000 for $x_\gamma > 0.5$)



Primakoff peak

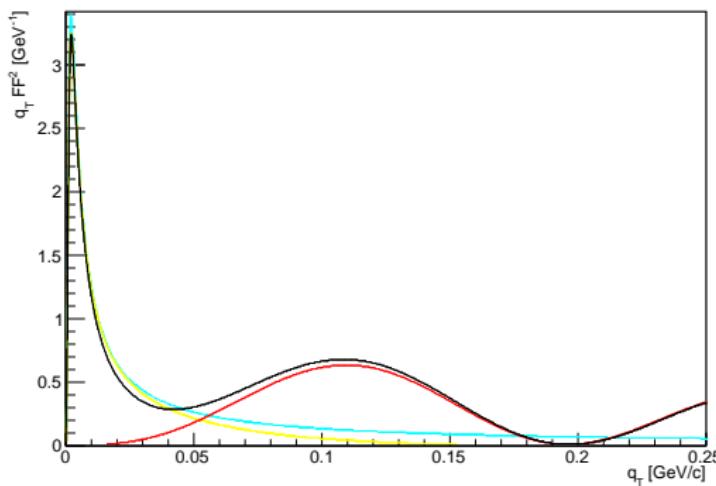
Phys. Rev. Lett. 114, 062002 (2015)



- $\Delta Q_T \approx 12 \text{ MeV}/c$ ($190 \text{ GeV}/c$ beam \rightarrow requires few- μrad angular resolution)
- first diffractive minimum on Ni nucleus at $Q \approx 190 \text{ MeV}/c$
- data a little more narrow than simulation \rightarrow negative interference?



Photon density squared form factor

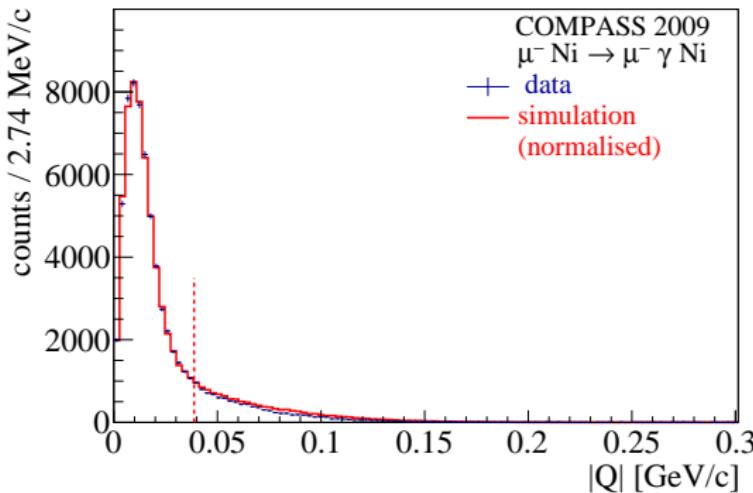


- calculation following G. Fäldt (Phys. Rev. C79, 014607)
- eikonal approximation: pions traverse Coulomb and strong-interaction potentials



Primakoff peak: muon data

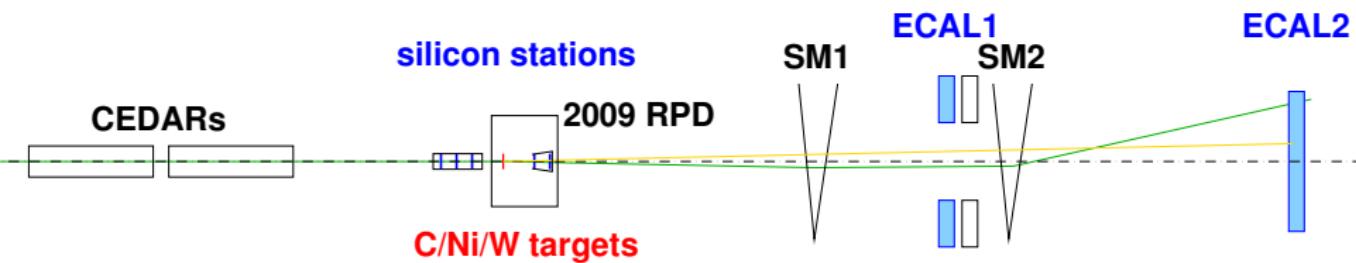
Phys. Rev. Lett. 114, 062002 (2015)



- **muon control measurement:** pure electromagnetic interaction



Principle of the measurement





ECAL2: 3000 cells of different types





ECAL2: quest for precision

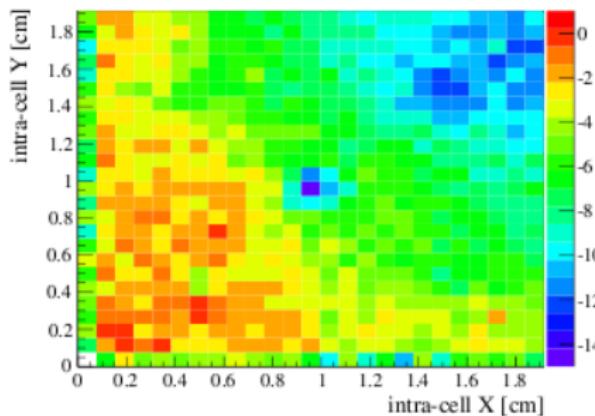


Figure 3.5: Profile of energy deviations shown for 1/4 of a shashlik block and for muon data photons within the range $133 \text{ GeV} < E_\gamma < 152 \text{ GeV}$.

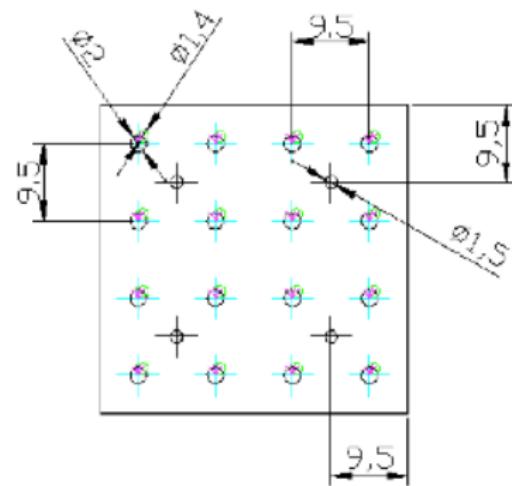
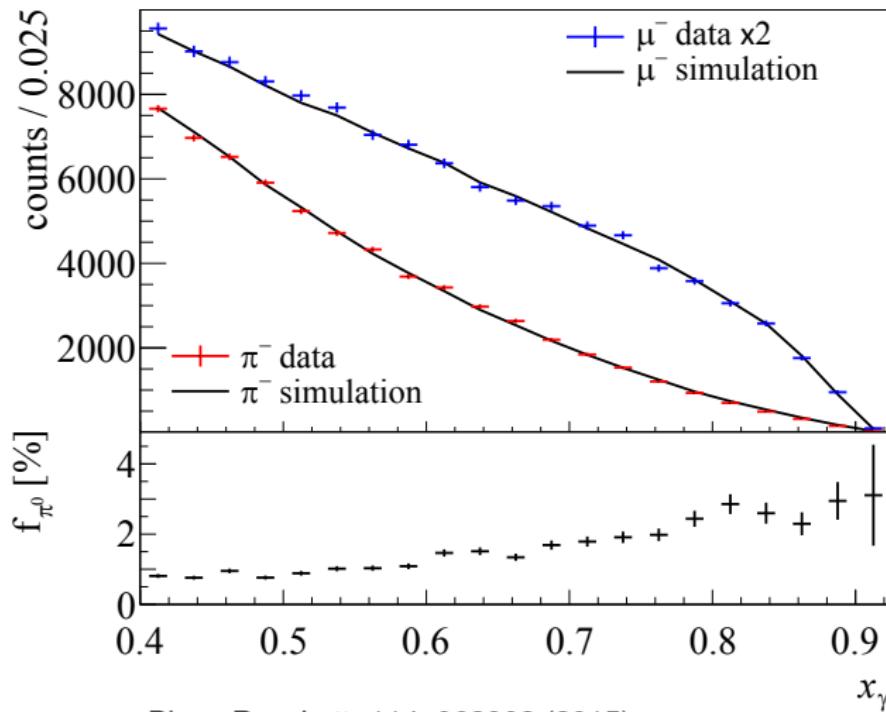


Figure 3.6: Technical drawing of a full shashlik cell to be compared with the figure to the left.

from: Th. Nagel, PhD thesis TUM 2012



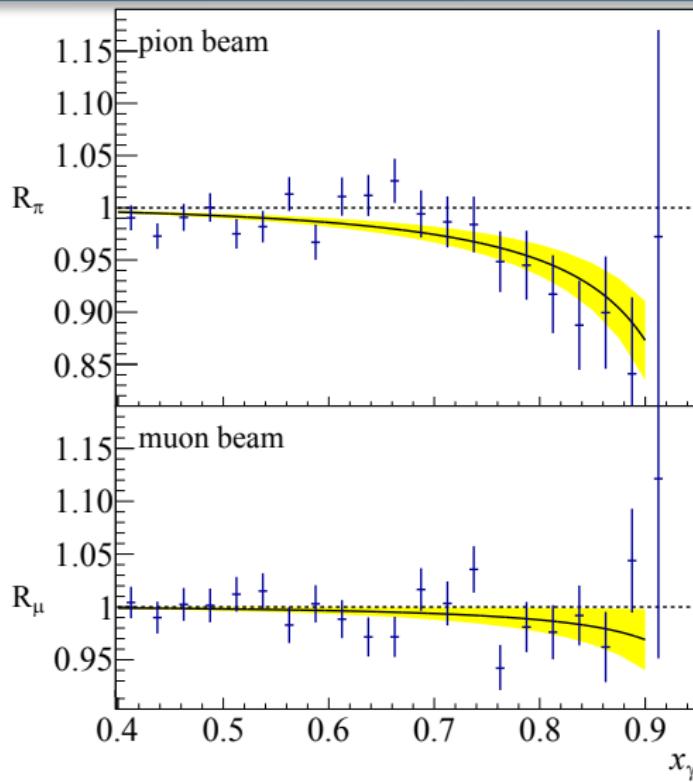
Photon energy spectra for muon and pion beam



Phys. Rev. Lett. 114, 062002 (2015)



Pion polarisability: COMPASS result



$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}}) \times 10^{-4} \text{ fm}^3$$

(assuming $\alpha_\pi = -\beta_\pi$)

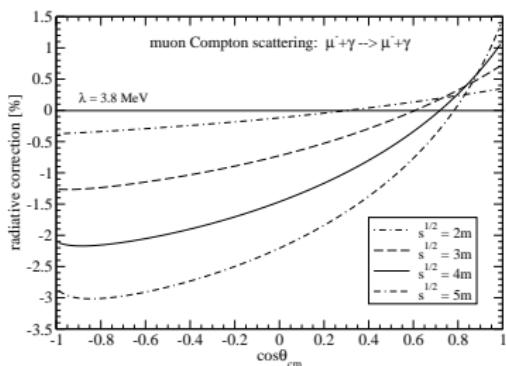
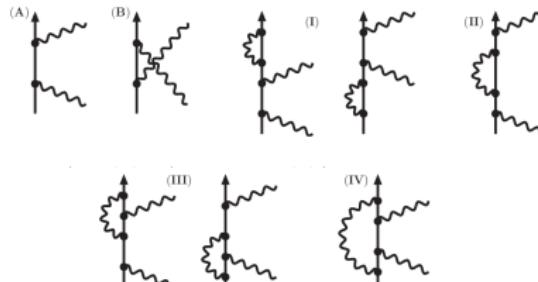
“false polarisability” from muon data:

$$(0.5 \pm 0.5_{\text{stat}}) \times 10^{-4} \text{ fm}^3$$

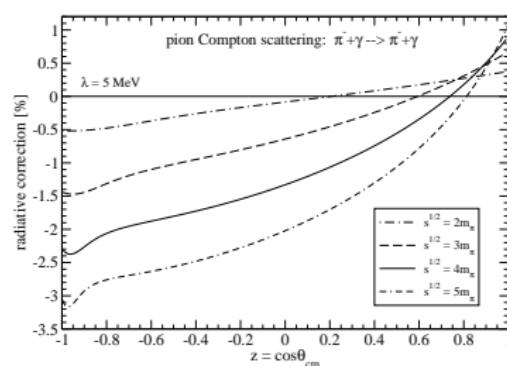
Phys. Rev. Lett. 114, 062002 (2015)



Radiative corrections (Compton scattering part)



Nucl.Phys. A837 (2010)



Eur.Phys.J. A39 (2009) 71



source of systematic uncertainty	estimated magnitude CL = 68 % [10 ⁻⁴ fm ³]
tracking	0.5
radiative corrections	0.3
background subtraction in Q	0.4
pion electron scattering	0.2
quadratic sum	0.7



source of systematic uncertainty	estimated magnitude CL = 68 % [10 ⁻⁴ fm ³]
tracking	0.5
radiative corrections	0.3
background subtraction in Q	0.4
pion electron scattering	0.2
quadratic sum	0.7

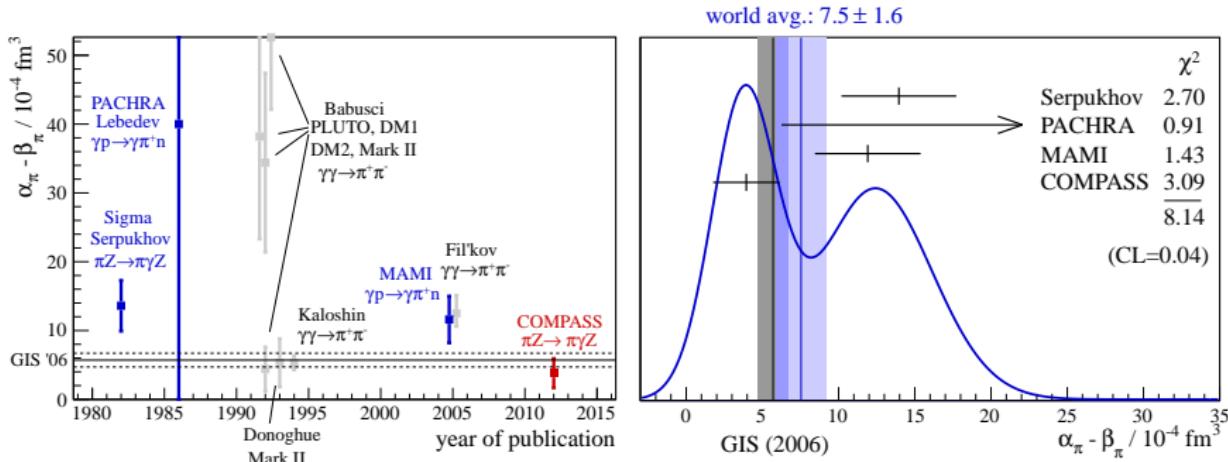
COMPASS result for the pion polarisability:

$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3$$

with $\alpha_\pi = -\beta_\pi$ assumed



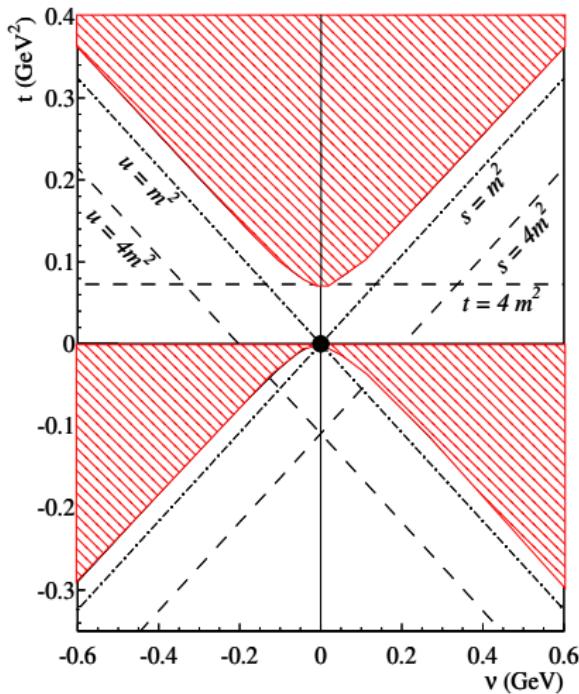
Pion polarisability: world data including COMPASS



- The new COMPASS result is in significant tension with the earlier measurements of the pion polarisability
- The expectation from ChPT is confirmed within the uncertainties



About crossing



- ▶ red hatched:
physical regions
 $\gamma + \gamma \rightarrow \pi + \pi$
 $\gamma + \pi \rightarrow \gamma + \pi$
- ▶ two-pion thresholds
at $s = 4m_\pi^2$, $u = 4m_\pi^2$,
 $t = 4m_\pi^2$
- ▶ DR integration paths
 $t = 0$ (forward),
 $\theta = 180^\circ$ (backward)
 $u = m_\pi^2$, $s = m_\pi^2$, ...

from: D. Drechsel, talk at IWHSS 2011 Paris



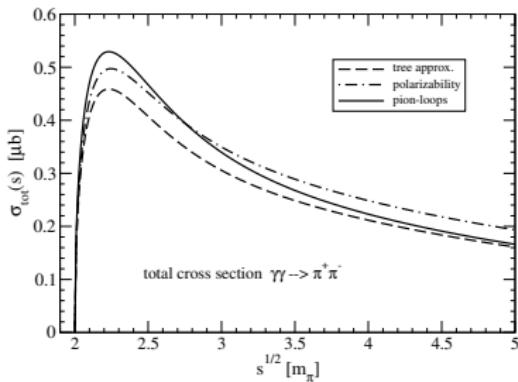
Photon-photon fusion process $\gamma\gamma \rightarrow \pi^+\pi^-$

- Planned measurements at ALICE and JLab

$$\sigma_{tot}(s) = \frac{2\pi\alpha^2}{\hat{s}^3 m_\pi^2} \left\{ [4 + \hat{s} + \hat{s}|\mathcal{C}(\hat{s})|^2] \sqrt{\hat{s}(\hat{s}-4)} \right.$$

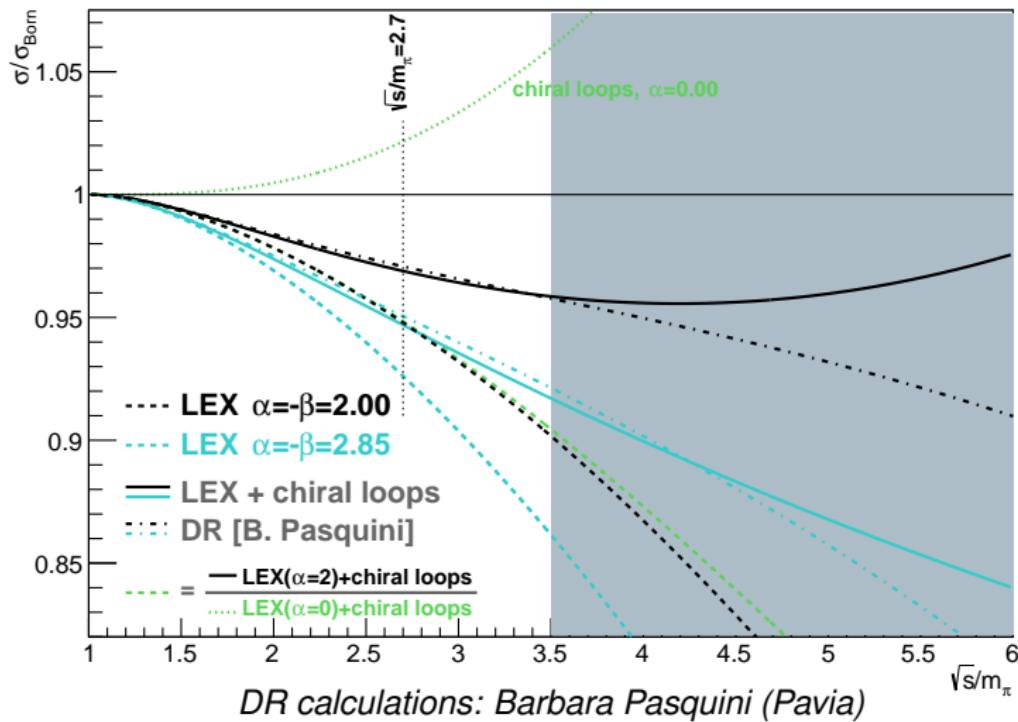
$$\left. + 8[2 - \hat{s} + \hat{s} \operatorname{Re} \mathcal{C}(\hat{s})] \ln \frac{\sqrt{\hat{s}} + \sqrt{\hat{s}-4}}{2} \right\},$$

$$\mathcal{C}(\hat{s}) = -\beta_\pi \frac{m_\pi^3}{2\alpha} \hat{s} - \frac{m_\pi^2}{(4\pi f_\pi)^2} \left\{ \frac{\hat{s}}{2} + 2 \left[\ln \frac{\sqrt{\hat{s}} + \sqrt{\hat{s}-4}}{2} - \frac{i\pi}{2} \right]^2 \right\}$$



courtesy Norbert Kaiser (TUM)

Polarisability and Loop Contributions $z=1.0$





Pion polarisability on the lattice

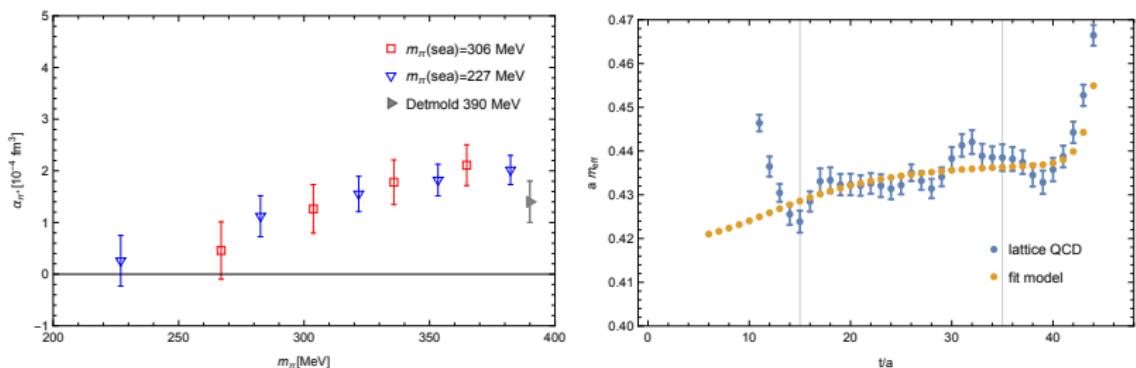
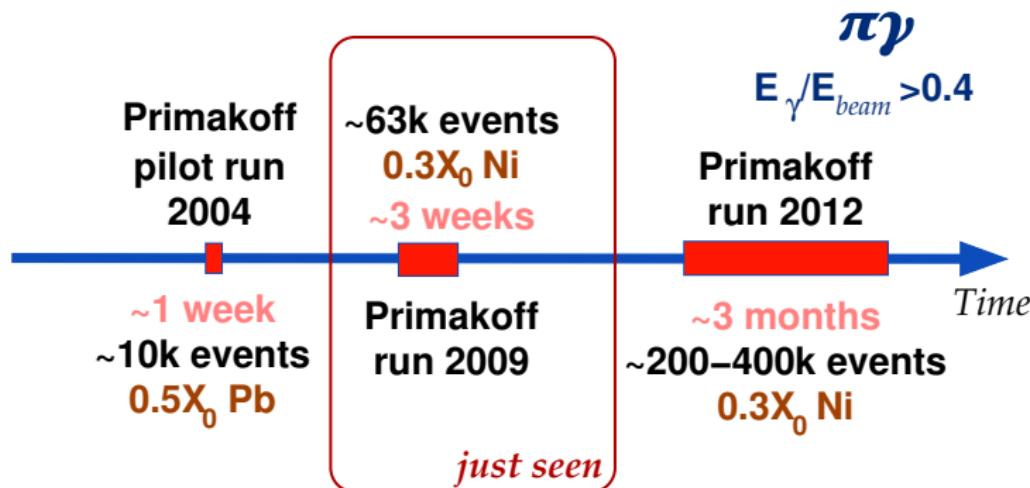


FIGURE 3. Left: electric polarizability for the charged pions as a function of the valence quark mass. The data for $m_\pi = 390 \text{ MeV}$ is taken from [5]. Right: effective mass for a charged pion correlator together with the scalar particle correlator determined from the fit. The fitting range is indicated by the vertical bars.

Alexandru *et al.*, Pion electric polarizability from lattice QCD, arXiv:1501.06516



Pion polarisability measurements at COMPASS



 Summary and Outlook

- Measurement of the **pion polarisability** at COMPASS

- Via the Primakoff reaction, COMPASS has determined

$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3 \quad \text{assuming } \alpha_\pi + \beta_\pi = 0$$

- Most precise experimental determination
- Systematic control: $\mu\gamma \rightarrow \mu\gamma$, $K^- \rightarrow \pi^-\pi^0$

- Chiral dynamics** in $\pi^-\gamma \rightarrow \pi^-\pi^0$ and $\pi\gamma \rightarrow \pi\pi\pi$ reactions

- Charged-channel $\pi\gamma \rightarrow \pi^-\pi^-\pi^+$ tree-level ChPT prediction confirmed
- Neutral-channel $\pi\gamma \rightarrow \pi^-\pi^0\pi^0$ analysis ongoing
- Resonance properties, radiative couplings

- High-statistics run 2012

- separate determination of α_π and β_π
- s -dependent quadrupole polarisabilities
- First measurement of the kaon polarisability



Thanks for your attention!





Access to $\pi + \gamma$ reactions via the **Primakoff effect**:

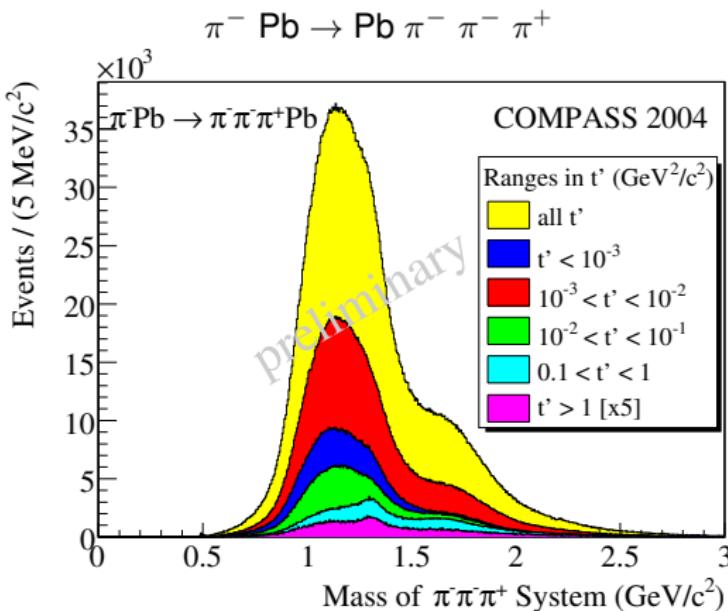
At smallest momentum transfers to the nucleus, high-energetic particles scatter predominantly off the **electromagnetic field quanta** ($\sim Z^2$)

$$\pi^- + \gamma \rightarrow \left\{ \begin{array}{l} \pi^- + \gamma \\ \pi^- + \pi^0 / \eta \\ \pi^- + \pi^0 + \pi^0 \\ \pi^- + \pi^- + \pi^+ \\ \pi^- + \pi^- + \pi^+ + \pi^- + \pi^+ \\ \pi^- + \dots \end{array} \right.$$

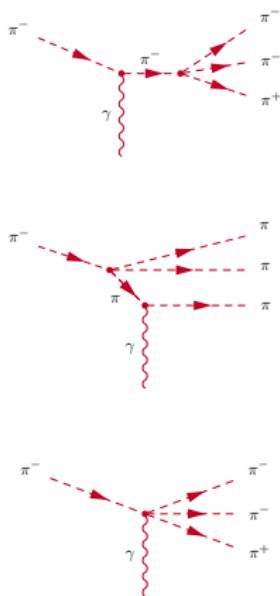
analogously: Kaon-induced reactions $K^- + \gamma \rightarrow \dots$



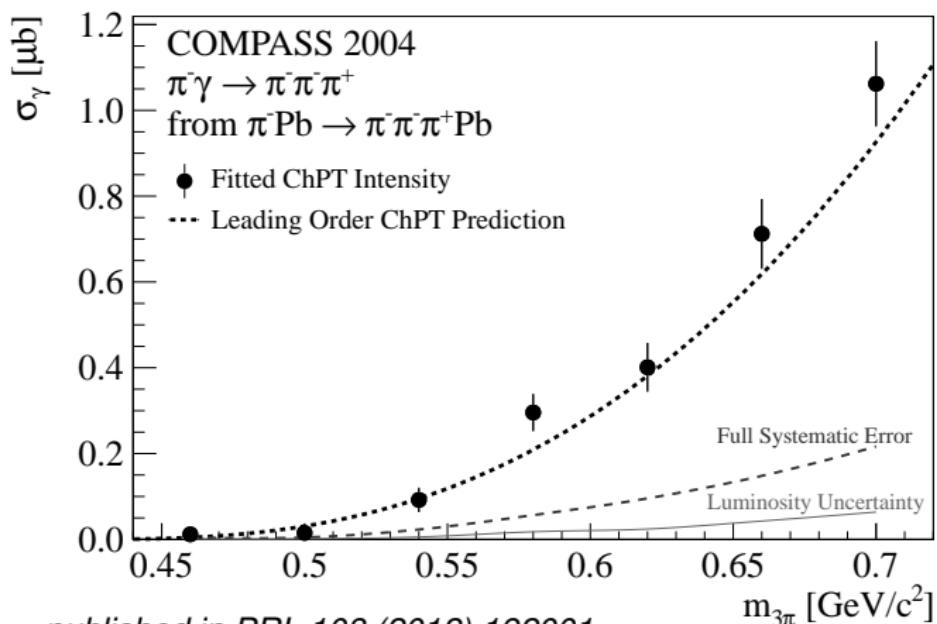
2004 Primakoff results



- "Low t' ": $10^{-3} (\text{GeV}/c)^2 < t' < 10^{-2} (\text{GeV}/c)^2$ $\sim 2\,000\,000$ events
- "Primakoff region": $t' < 10^{-3} (\text{GeV}/c)^2$ $\sim 1\,000\,000$ events



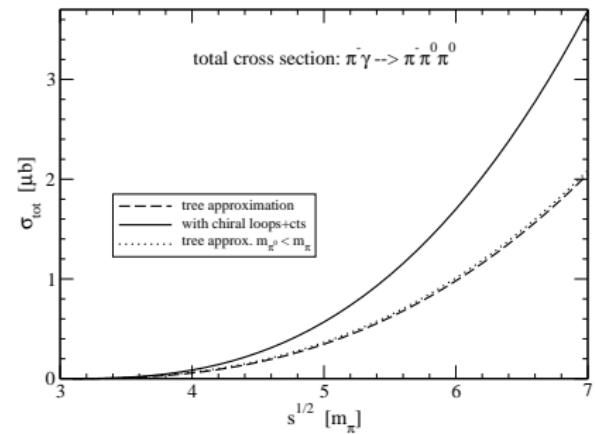
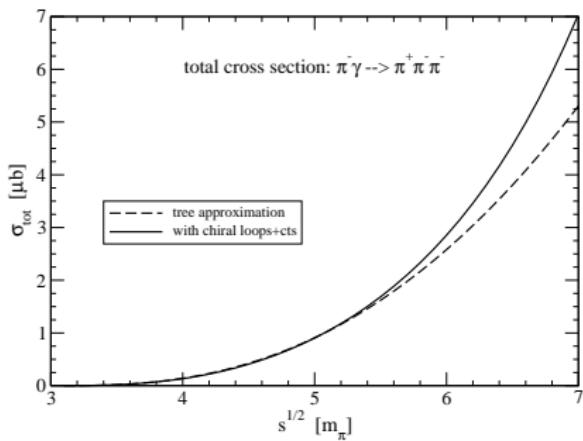
Measured absolute cross-section of $\pi^- \gamma \rightarrow \pi^- \pi^- \pi^+$



published in PRL 108 (2012) 192001

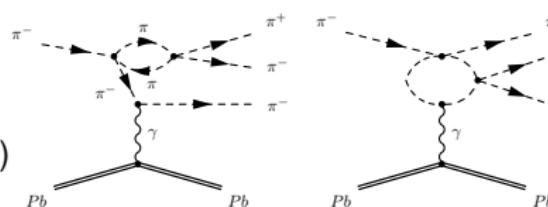


Higher-order effects

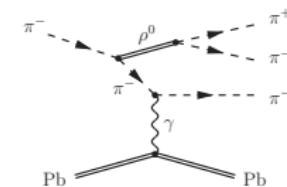


Chiral loops, e.g.

(N. Kaiser,
NPA848 (2010) 198)

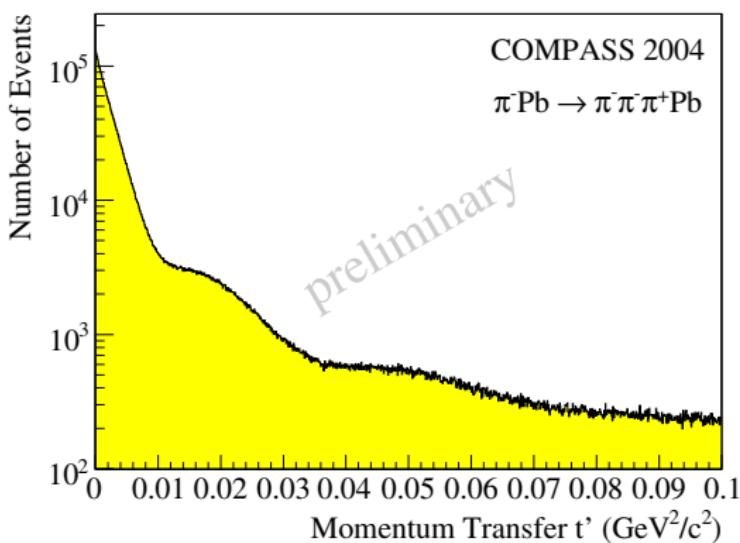


not (yet)
included:





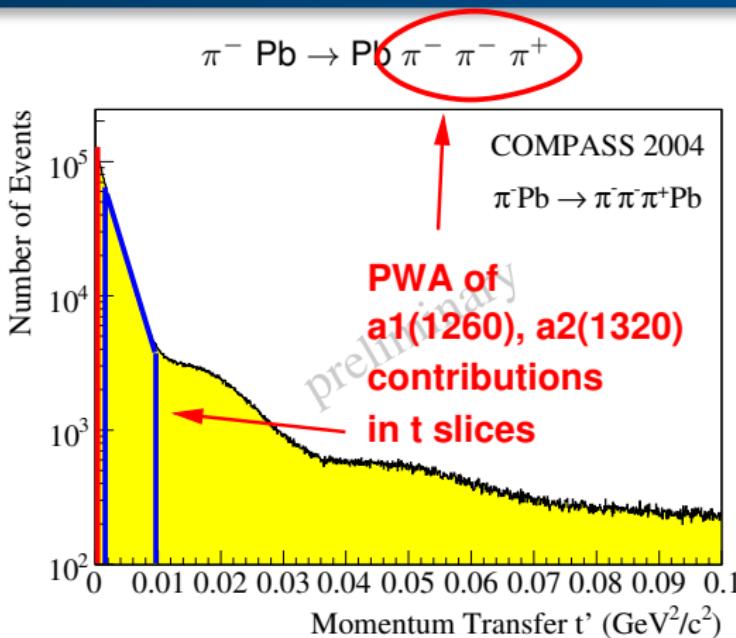
2004 Primakoff results

$$\pi^- \text{ Pb} \rightarrow \text{Pb} \pi^- \pi^- \pi^+$$


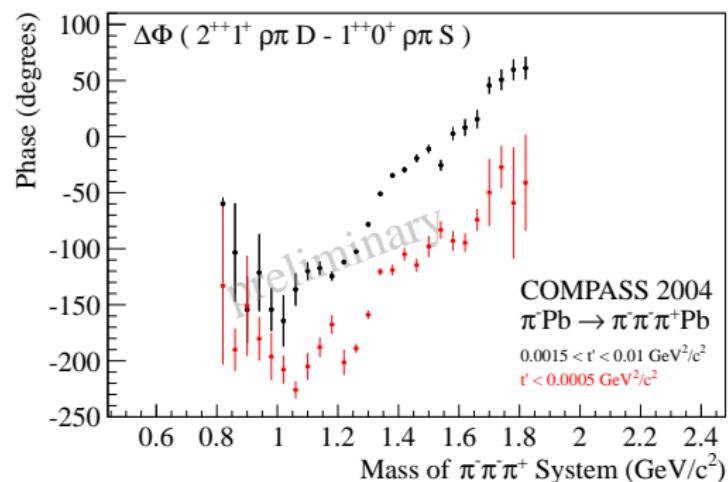
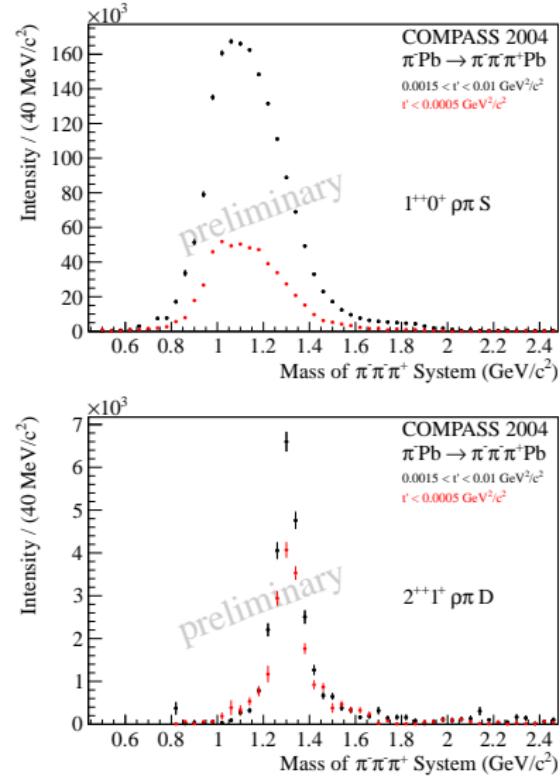
- "Low t' ": $10^{-3} (\text{GeV}/\text{c})^2 < t' < 10^{-2} (\text{GeV}/\text{c})^2$ $\sim 2\,000\,000$ events
- "Primakoff region": $t' < 10^{-3} (\text{GeV}/\text{c})^2$ $\sim 1\,000\,000$ events

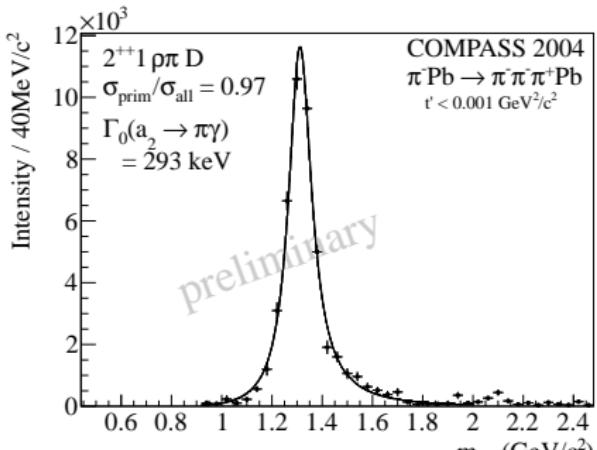


2004 Primakoff results

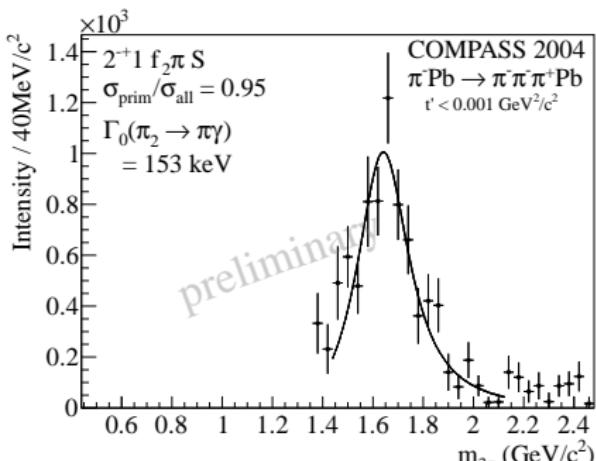


- "Low t' ": $10^{-3} (\text{GeV}/\text{c})^2 < t' < 10^{-2} (\text{GeV}/\text{c})^2$ $\sim 2\,000\,000$ events
- "Primakoff region": $t' < 10^{-3} (\text{GeV}/\text{c})^2$ $\sim 1\,000\,000$ events



Radiative Coupling of $a_2(1320)$ and $\pi_2(1670)$ 

$\Gamma_0(a_2(1320) \rightarrow \pi\gamma)$ M2



$\Gamma_0(\pi_2(1670) \rightarrow \pi\gamma)$ E2

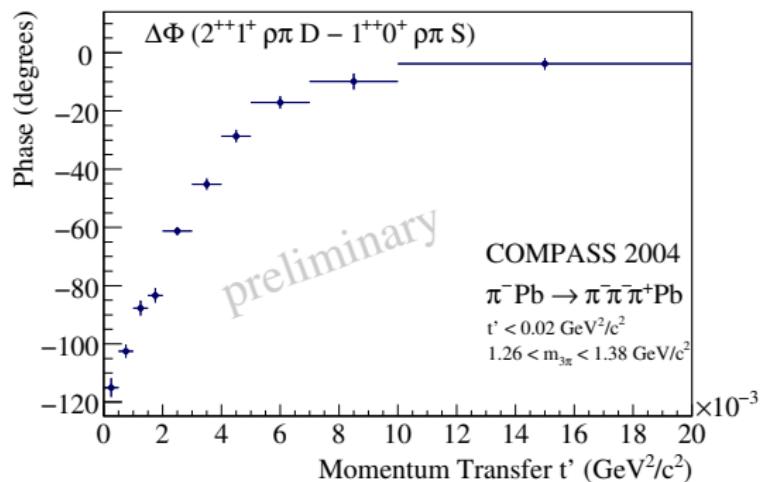
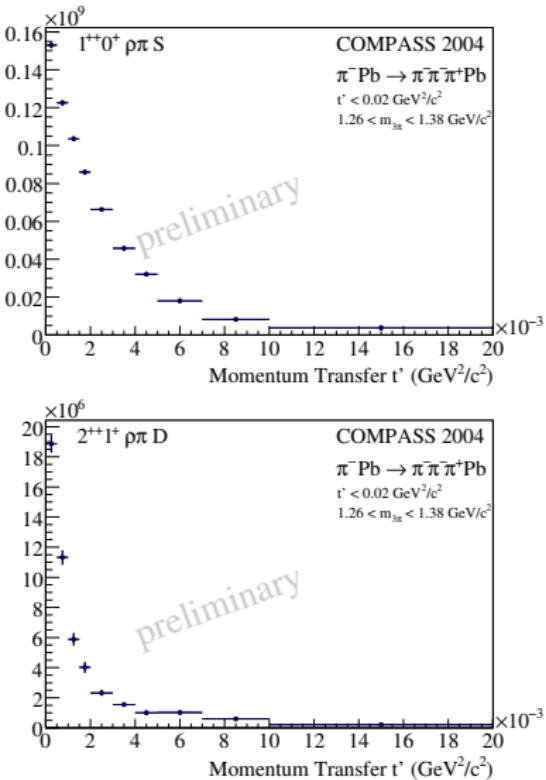
\Leftrightarrow meson w.f.'s: $\Gamma_{i \rightarrow f} \propto | \langle \Psi_f | e^{-i\vec{q} \cdot \vec{r}} \hat{\epsilon} \cdot \vec{p} | \Psi_i \rangle |^2$, VMD

- normalization via beam kaon decays
- large Coulomb correction

published in EPJ A50 (2014) 79



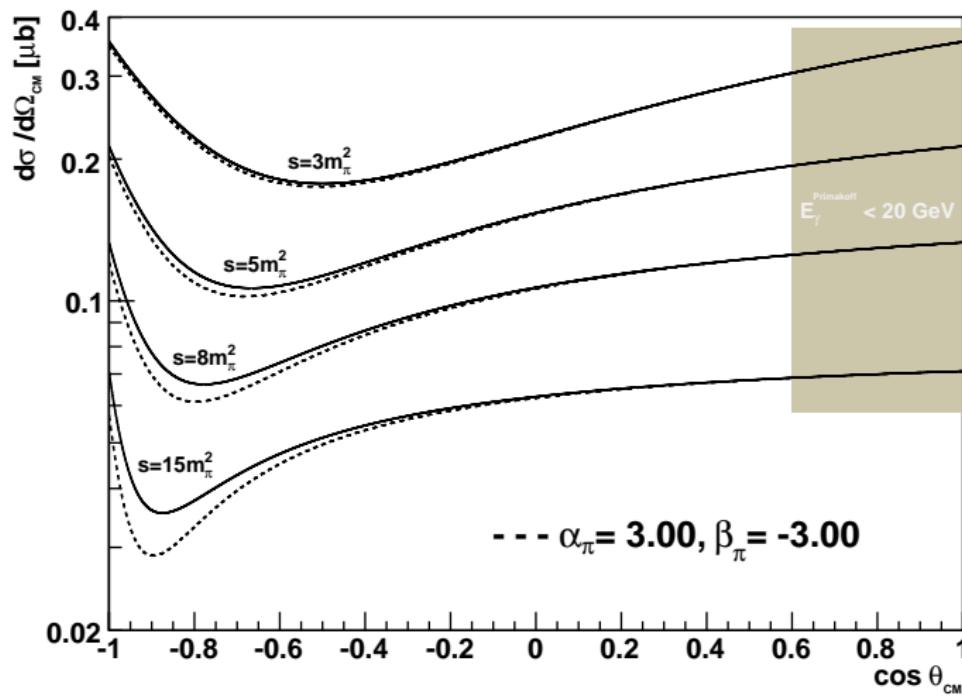
Phase $a_2 - a_1$ in detail: t' dependence



- transition of $\pi\gamma$ to $\pi IP \rightarrow a_2$ production
- work in progress
- interference can be used to map details of resonances and production mechanisms



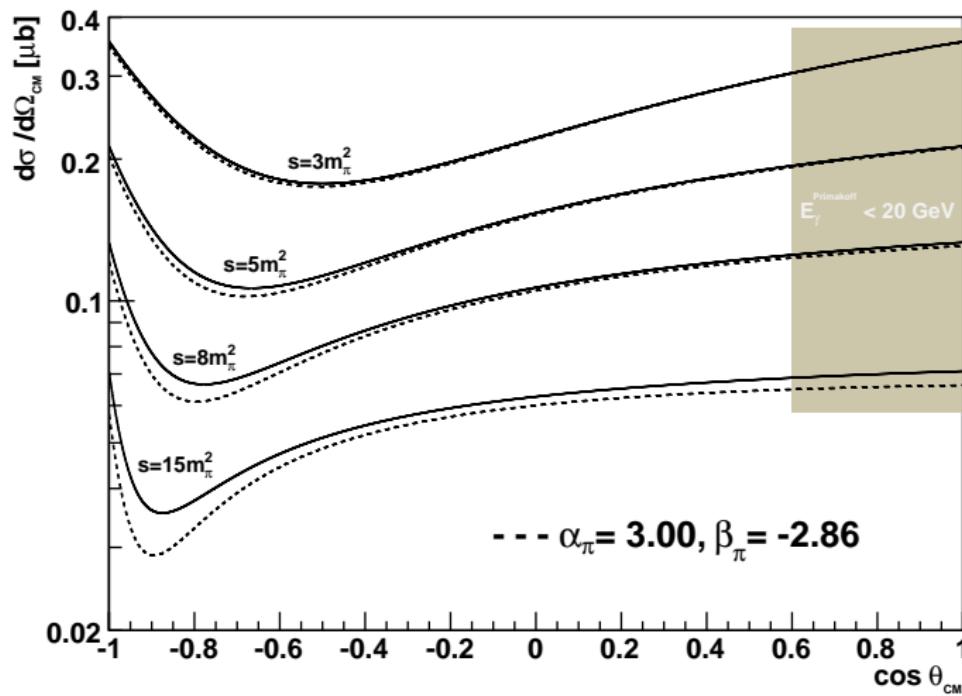
loop effects not shown





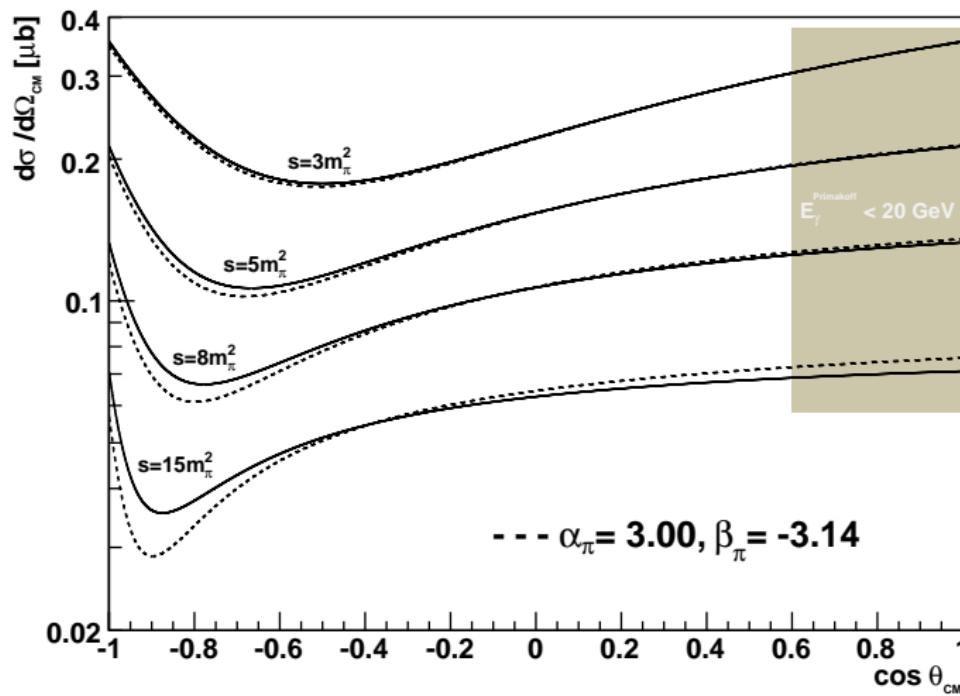
Polarisability effect (NLO ChPT values)

loop effects not shown



Polarisability effect (wrong sign $\alpha_\pi + \beta_\pi$)

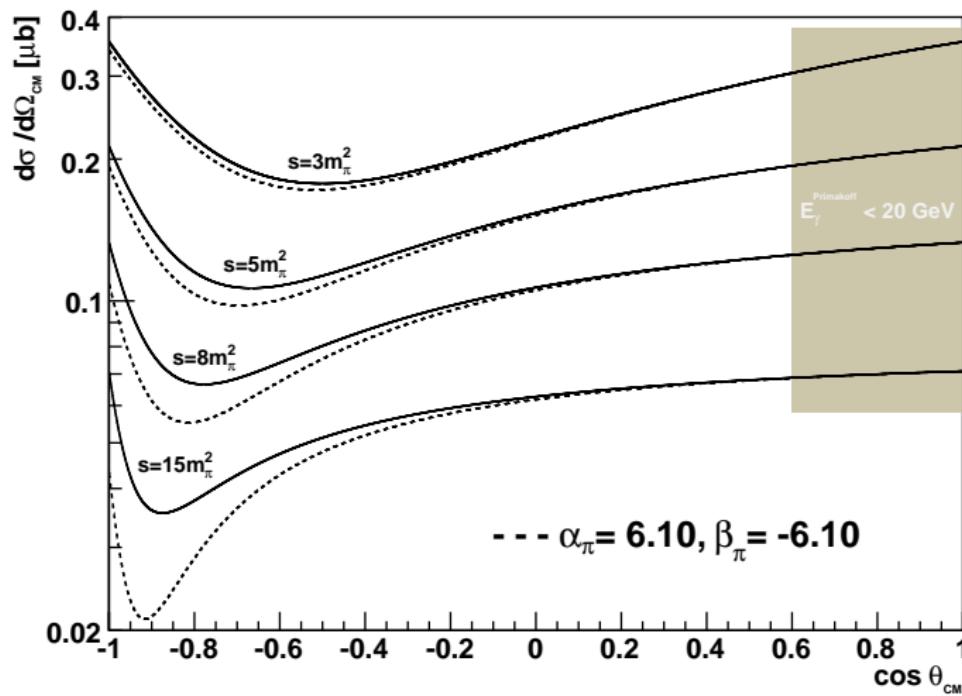
loop effects not shown





Polarisability effect (Serpukhov values)

loop effects not shown





- Radiative π^+ production on the proton:



Mainz (2005) measurement: $\alpha_\pi - \beta_\pi = 11.6 \pm 1.5 \pm 3.0 \pm 0.5$

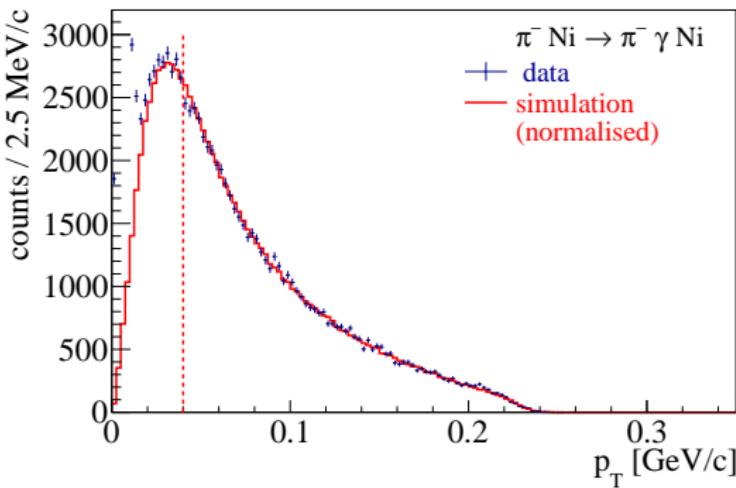
“ ± 0.5 ”: model error *only within the used ansatz,*
full systematics not under control

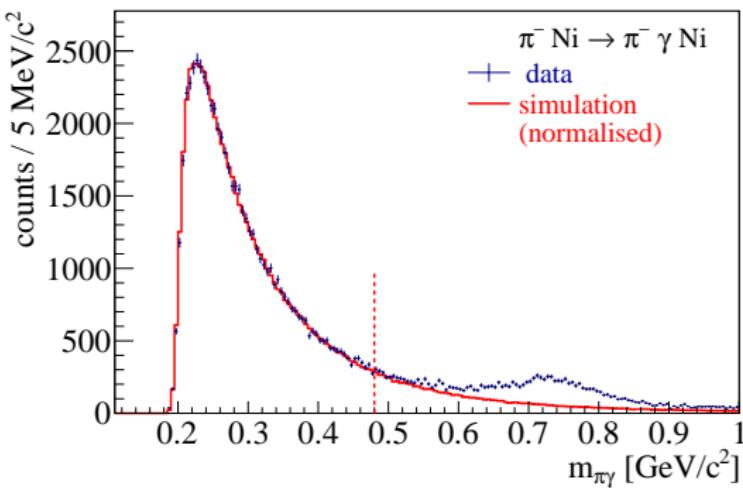
- Primakoff Compton reaction:



tiny extrapolation $\gamma^* \rightarrow \gamma \mathcal{O}(10^{-3} m_\pi^2)$
fully under theoretical control

[N. Kaiser, J.F., Nucl. Phys. A 812 (2008) 186]

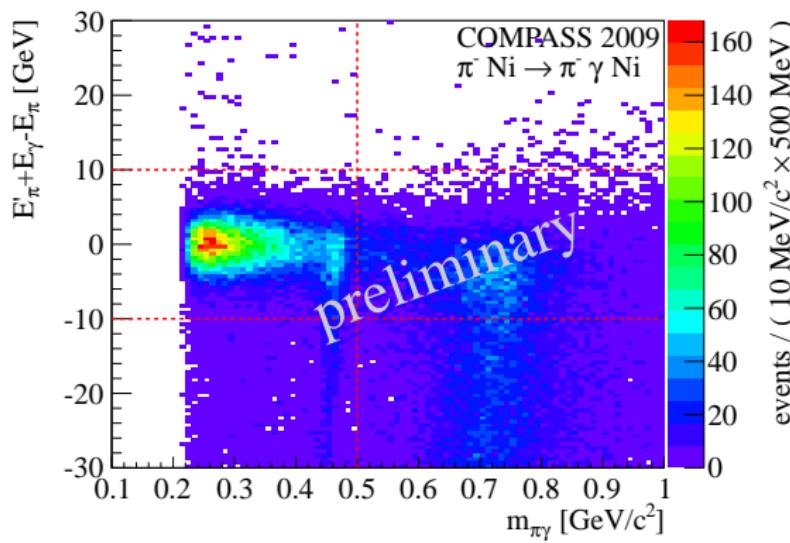


 CM energy in $\pi\gamma \rightarrow \pi\gamma$ 

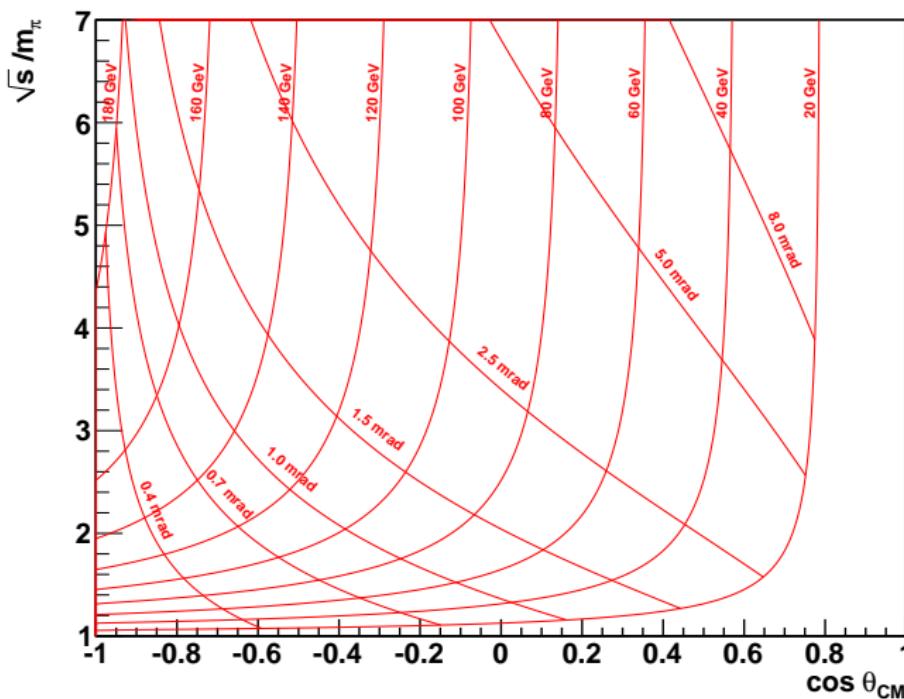
- ρ contribution from $\pi\gamma \rightarrow \pi\pi^0$



Exclusivity vs. \sqrt{s}

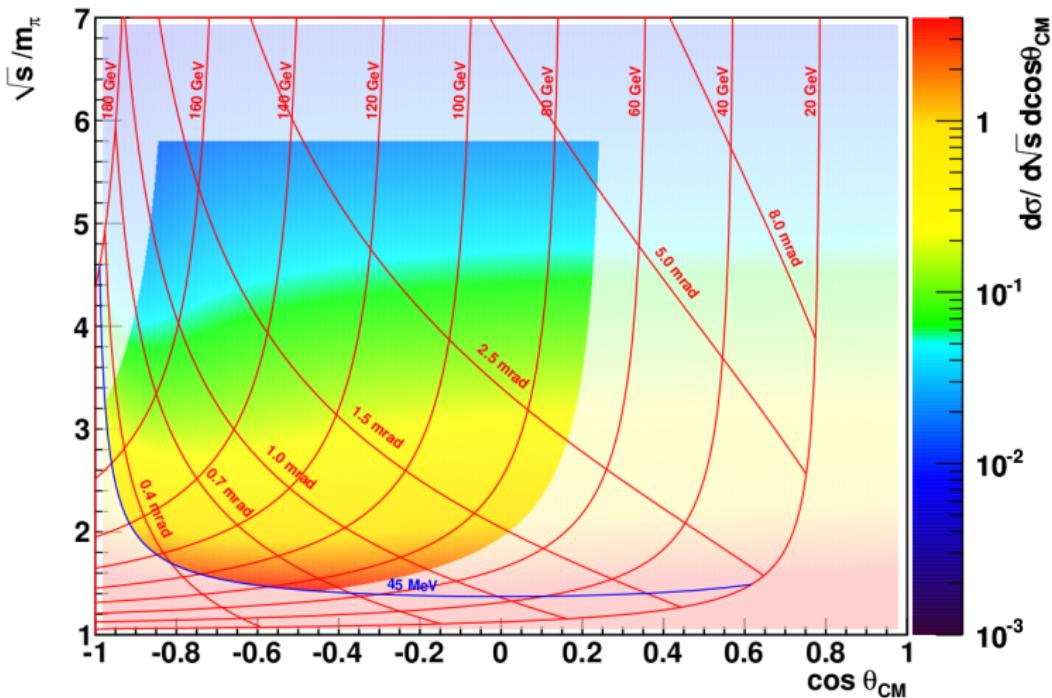


- ρ contribution from $\pi\gamma \rightarrow \pi\pi^0$

for $\pi\gamma \rightarrow \pi\gamma$ 



Cross section



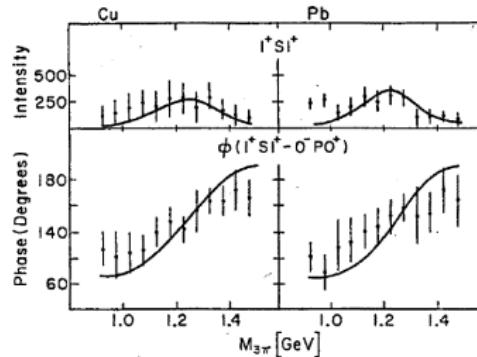
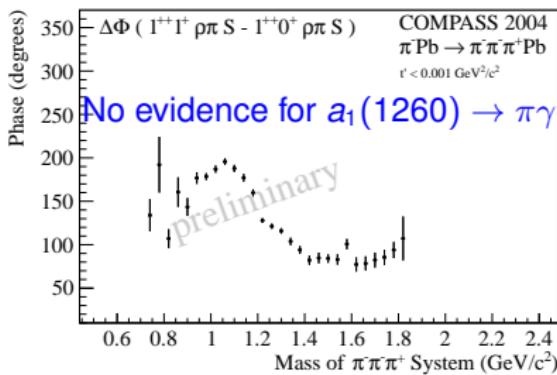
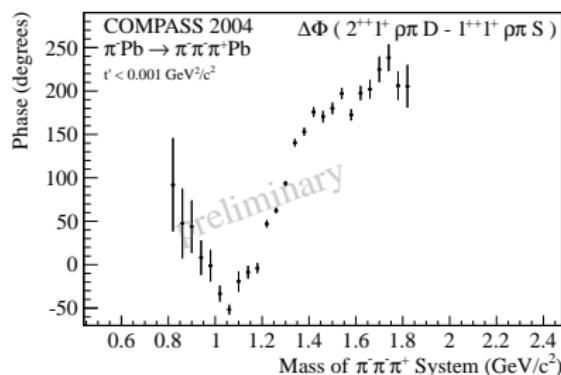
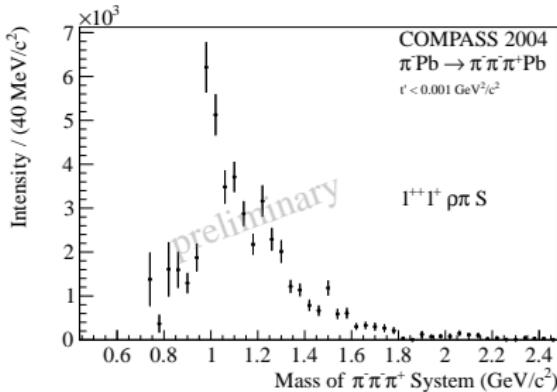
 $\gamma\gamma \rightarrow \pi\pi$ and the pion polarisability

M.R. Pennington in the 2nd DAΦNE Physics Handbook,
“What we learn by measuring $\gamma\gamma \rightarrow \pi\pi$ at DAΦNE”:

All this means that the only way to measure the pion polarisabilities is in the Compton scattering process near threshold and not in $\gamma\gamma \rightarrow \pi\pi$. Though the low energy $\gamma\gamma \rightarrow \pi\pi$ scattering is seemingly close to the Compton threshold (...) and so the *extrapolation* not very far, the dominance of the pion pole (...) means that the energy scale for this continuation is m_π . Thus the polarisabilities cannot be determined accurately from $\gamma\gamma$ experiments in a model-independent way and must be measured in the Compton scattering region.



Primakoff production of $a_1(1260)$ vs. E272 result



M. Zielinski et al, Phys. Rev. Lett 52 (1984) 1195

- Mass-independent PWA (narrow mass bins):

$$\sigma_{\text{indep}}(\tau, m, t') = \sum_{\epsilon=\pm 1} \sum_{r=1}^{N_r} \left| \sum_i T_{ir}^\epsilon f_i^\epsilon(t') \psi_i^\epsilon(\tau, m) \right|^2 \sqrt{\int |f_i^\epsilon(t')|^2 dt'} \sqrt{\int |\psi_i^\epsilon(\tau', m)|^2 d\tau'}^2$$

- Production strength assumed constant in single bins
- Decay amplitudes $\psi_i^\epsilon(\tau, m)$, with t' dependence $f_i^\epsilon(t')$
- Production amplitudes T_{ir}^ϵ → Extended log-likelihood fit
- Acceptance corrections included

- Spin-density matrix: $\rho_{ij}^\epsilon = \sum_r T_{ir}^\epsilon T_{jr}^{\epsilon*}$

→ Physical parameters:

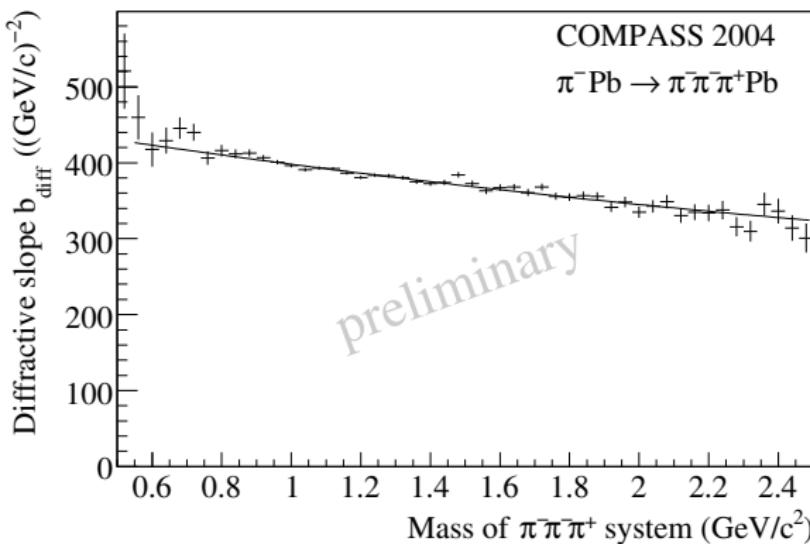
$$\text{Intens}_i^\epsilon = \rho_{ii}^\epsilon,$$

relative phase Φ_{ij}^ϵ

$$\text{Coh}_{i,j}^\epsilon = \sqrt{(\text{Re } \rho_{ij}^\epsilon)^2 + (\text{Im } \rho_{ij}^\epsilon)^2} / \sqrt{\rho_{ii}^\epsilon \rho_{jj}^\epsilon}$$

- Mass-dependent χ^2 -fit (not presented here):

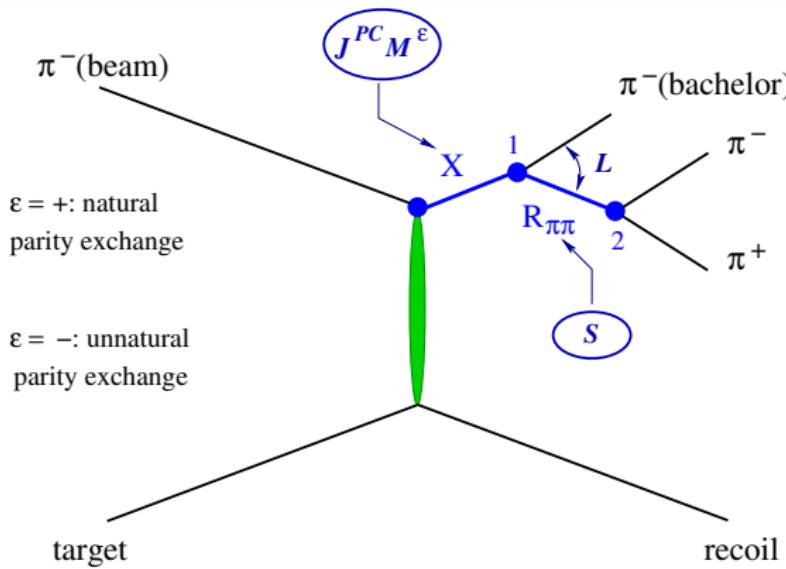
- X parameterized by Breit-Wigner (BW) functions
- Background can be added





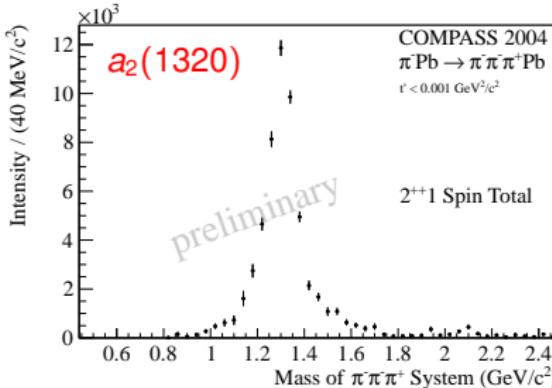
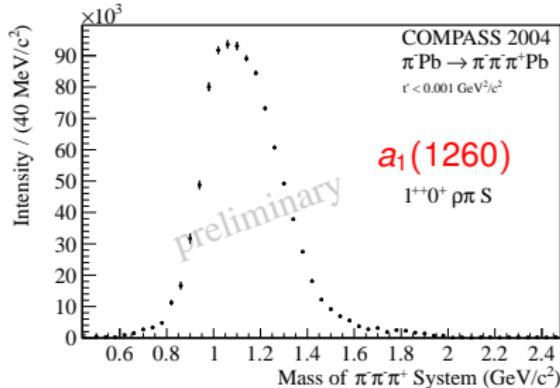
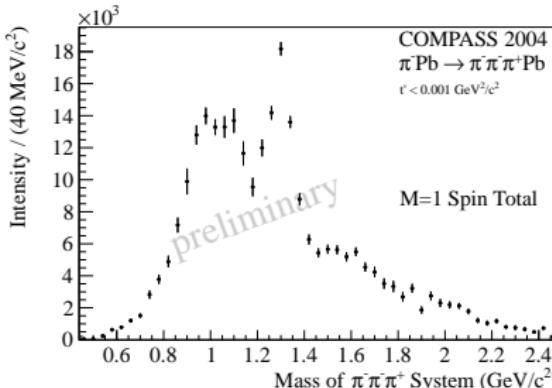
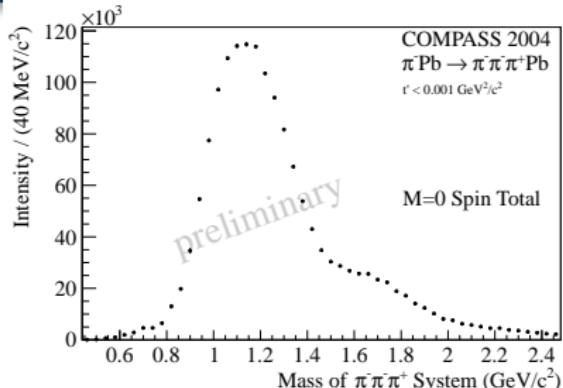
Partial Wave Analysis Formalism

Isobar Model



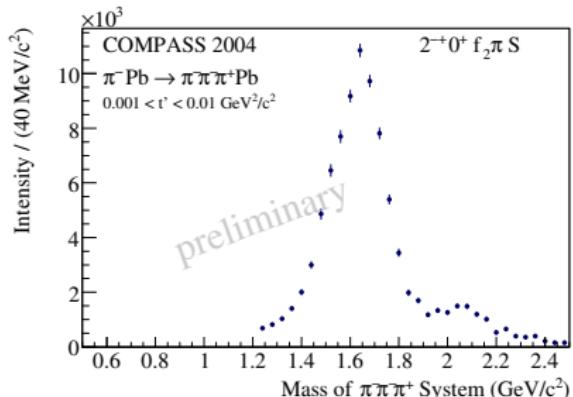
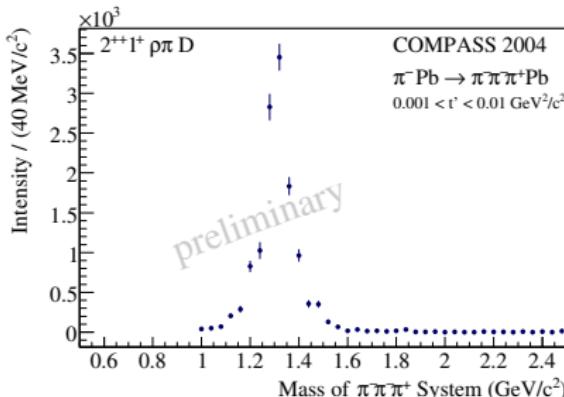
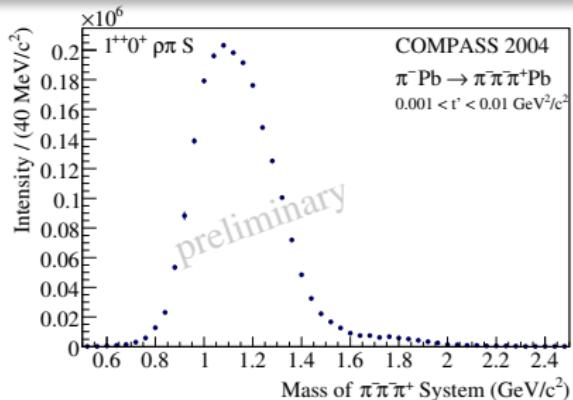
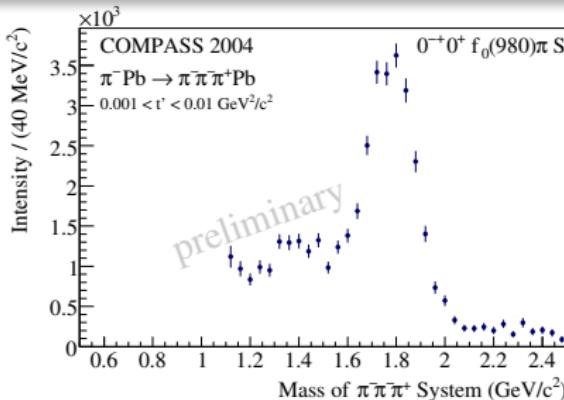
- Isobar model:
Intermediate 2-particle decays
- Partial wave in reflectivity basis:
 $J^{PC} M^\epsilon$ [isobar] L

- Mass-independent PWA (40 MeV/ c^2 mass bins): 38 waves
Fit of angular dependence of partial waves, interferences
- Mass-dependent χ^2 -fit (Not presented here)



PWA of data with low t'

Intensity of selected waves: $0^{-+} 0^+ f_0(980)\pi S$, $1^{++} 0^+ \rho\pi S$, $2^{++} 1^+ \rho\pi D$, $2^{-+} 0^+ f_2(1270)\pi S$





Spin Totals for $t' < 10^{-3} (\text{GeV}/c)^2$

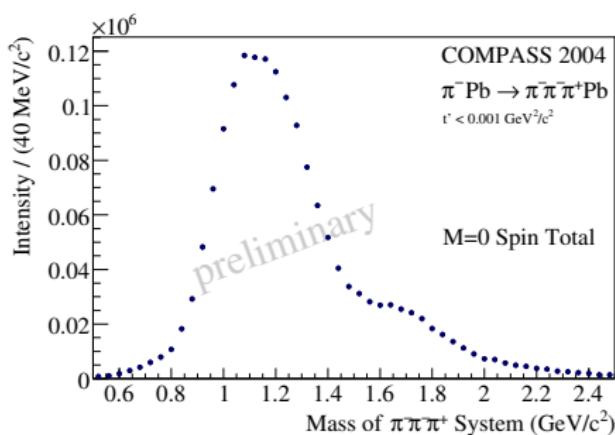
"Spin Totals": Sum of all contributions for given M (i.e. z-projection of J)

t' -dependent amplitudes:

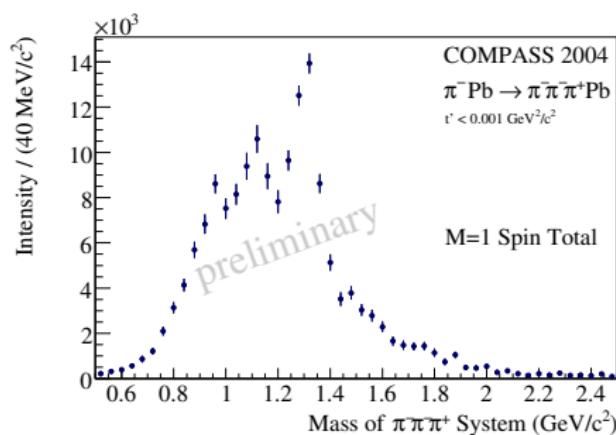
Primakoff production: **M=1**: $\sigma(t') \propto e^{-b_{\text{Prim}} t'} \rightarrow$ arises at $t' \approx 0$ (resolved shape!)

Diffractive production: **M=0**: $\sigma(t') \propto e^{-b_{\text{diff}}(m) t'}$

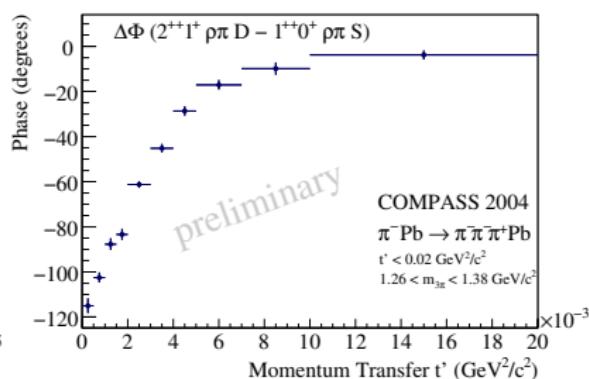
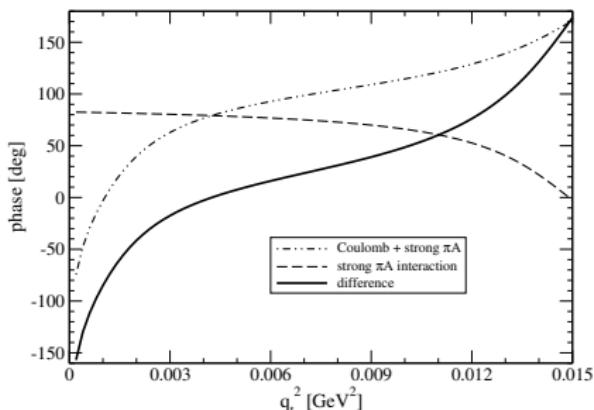
M=1: $\sigma(t') \propto t' e^{-b_{\text{diff}}(m) t'} \rightarrow$ vanishes for $t' \approx 0$



M=0



M=1



Glauber modell

G. Fäldt and U. Tengblad, Phys. Rev. C79, 014607 (2009)

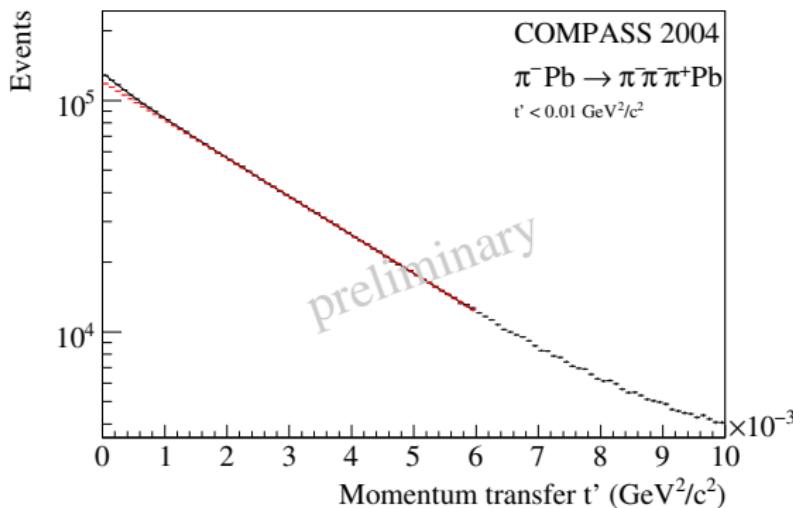
Plot: N. Kaiser (TU München)

- ⇒ indicates confirmation of interference Coulomb-interaction - strong interaction
- ⇒ detailed studies of the nature of resonances



Primakoff contribution at $t' < 10^{-3} (\text{GeV}/c)^2$

Primakoff: $\sigma(t') \propto e^{-b_{\text{Prim}} t'}$, $b_{\text{Prim}} \approx 2000 (\text{GeV}/c)^{-2}$ (mainly resolution)
 Diffractive: $\sigma(t') \propto e^{-b_{\text{diff}} t'}$, $b_{\text{diff}} \approx 400 (\text{GeV}/c)^{-2}$ for lead target



(Mass) spectrum of this Primakoff contribution?

⇒ Statistical subtraction of diffractive background (for bins of $m_{3\pi}$)