

# Measurements of transverse-momentum dependent effects in semi-inclusive DIS at COMPASS

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CHARLES UNIVERSITY  
Faculty of mathematics  
and physics

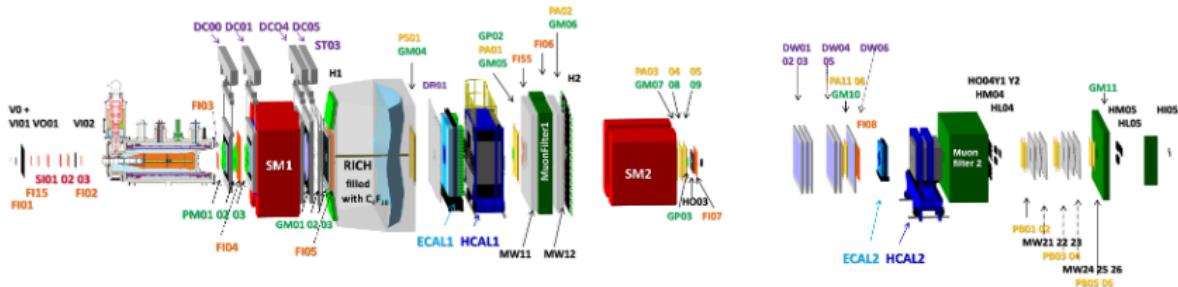


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Large research infrastructure grant CERN-CZ from Czech MEYS, and Charles university grant PRIMUS/22/SCI/017.



- Multi-purpose fixed-target setup.
  - M2 beamline of CERN's SPS North Area.
  - 24 institutes, 13 countries.
  - Nearly 200 physicists (2022).
  - Taking data 2002–2022 (20 years!)
  - Now analysis phase
  - Collaboration active, new groups joining.



2022 setup with  ${}^6\text{LiD}^\uparrow$  target.

- SIDIS with 160 GeV (200 GeV)  $\mu^+$  beam and  
2002–2011  $\vec{p}$  or  $\vec{d}$  ( $\text{NH}_3$  or  ${}^6\text{LiD}$ ) targets,  
2002–2022  $p^\uparrow$  or  $d^\uparrow$  ( $\text{NH}_3$  or  ${}^6\text{LiD}$ ) targets,  
2016–2017 unpolarised liquid  $\text{H}_2$  target.  
→ this talk.
- Hadron spectroscopy and chiral dynamics  
with hadron beams and nuclear targets  
→ New paper on strange meson spectroscopy  
[COMPASS, arXiv: 2504.09470 [hep-ex] (4/2025)].
- Drell–Yan with 190 GeV  $\pi^-$  beam and  
 $p^\uparrow$  ( $\text{NH}_3$ ) and unpolarised Al and W targets.  
→ M. Niemiec, Wed. 18:23 (poster) [Indico],  
→ Cross-section [V. Andrieux, DIS2024, Grenoble].
- Hard exclusive processes sensitive to GPDs  
with 160 GeV/c  $\mu^\pm$  beam and liquid  $\text{H}_2$  target  
→ New paper on hard exclusive  $\pi^0$  production  
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Polarised target refrigerator and MW cavity.

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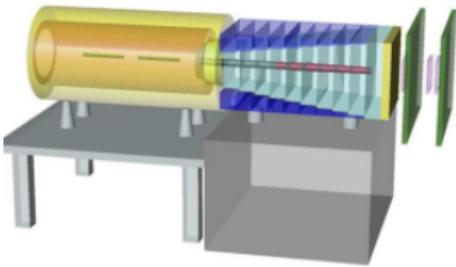
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Polarised  $\text{NH}_3^\uparrow$  target and hadron absorber.

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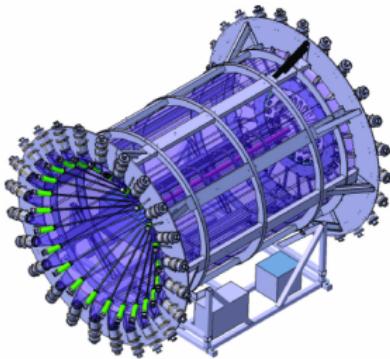
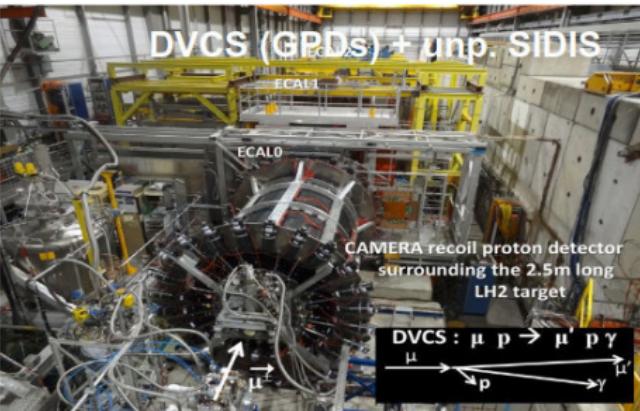
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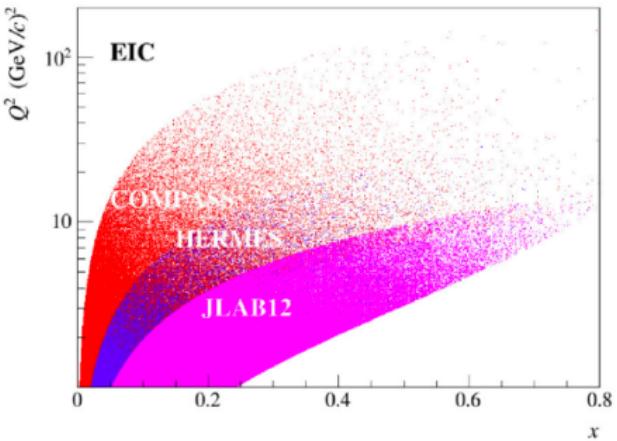
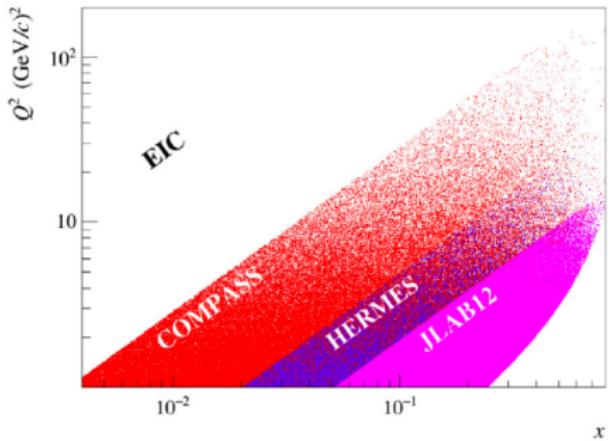
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Recoil proton detector CAMERA.

# COMPASS: Kinematic coverage for DIS



Complementarity of deep-inelastic scattering experiments  
in the coverage in standard variables  $x$  and  $Q^2$ .

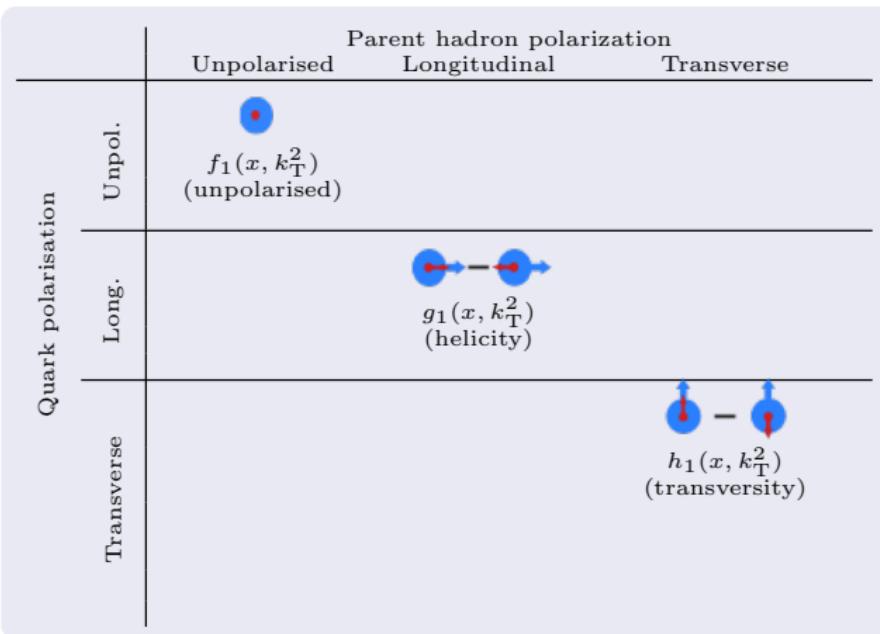
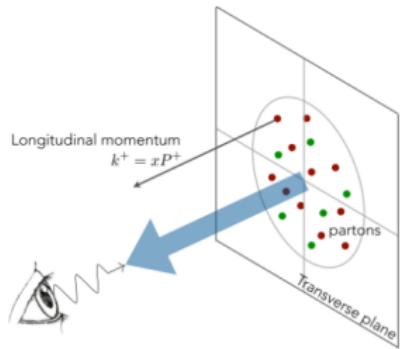
**HERMES** 1995–2007,  $\sqrt{s} \approx 7.5$  GeV with  $27.5$  GeV/c  $e^\pm$  beam and fixed gas targets.

**COMPASS** 2002–2022,  $\sqrt{s} \approx 17$  GeV with  $160$  GeV/c muon beam and fixed target.

**JLab12** 2014–present,  $\sqrt{s} \approx 5$  GeV with  $12$  GeV/c  $e^\pm$  beams and fixed targets.

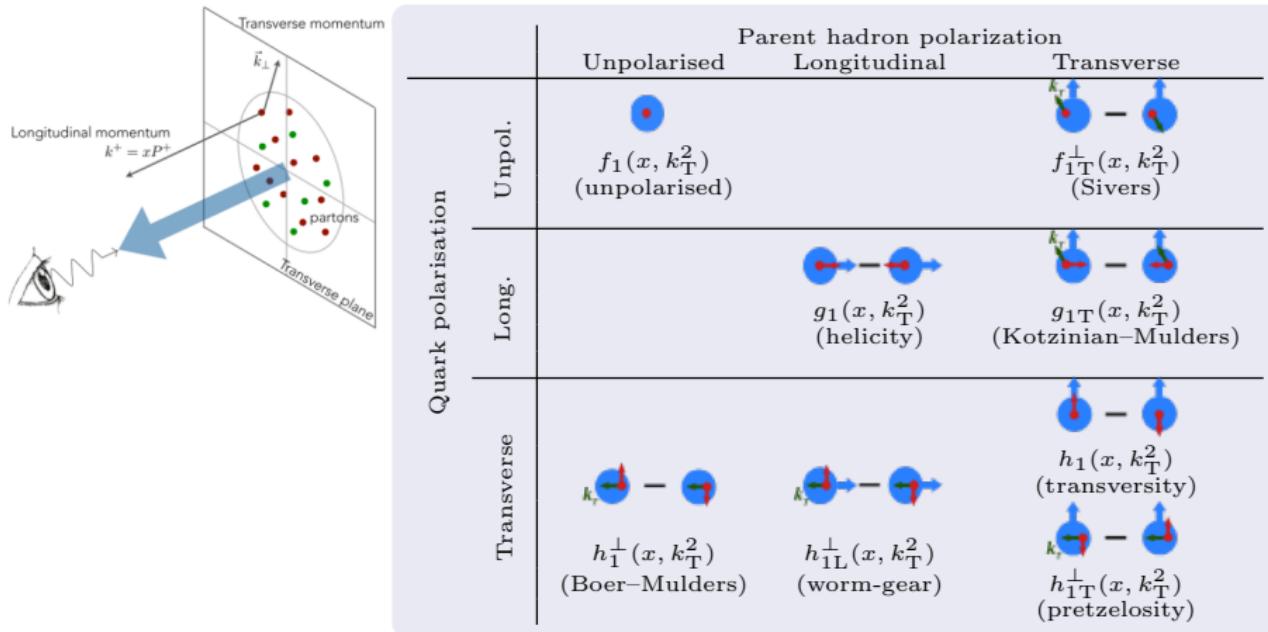
**EIC** future,  $\sqrt{s} \approx 100$  GeV with  $e^\pm$  and ion beams.

# Transverse-momentum-dependent PDFs



3 collinear parton distribution functions (PDFs).

# Transverse-momentum-dependent PDFs



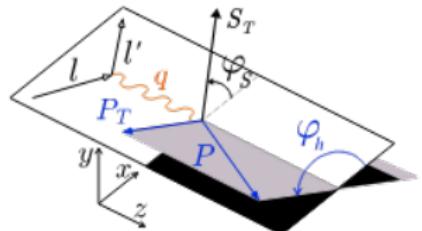
8 leading twist transverse momentum dependent (TMD) PDFs.

# Semi-inclusive DIS

Cross-section for

- transversely polarised target ( $\mathbf{S}_T$ ) and
- longitudinally polarised beam ( $\lambda \approx 0.8$  at COMPASS):

$$\frac{d\sigma_{\text{SIDIS}}}{dx dy dz d\phi_S d\phi_h dP_{\text{LT}}^2} = \frac{\alpha^2}{xyQ^2} \left( 1 + \frac{\gamma^2}{2x} \right) \times \left\{ \begin{array}{l} \text{[Transversely polarised target]} \\ \text{[Longitudinally polarised beam]} \end{array} \right. \begin{aligned} & \left. \begin{aligned} & \left\{ \frac{2-2y+y^2}{2} F_{\text{UU,T}} + (1-y) F_{\text{UU,L}} + (2-y)\sqrt{1-y} \cos \phi_h F_{\text{UU}}^{\cos \phi_h} \right. \right. \\ & + (1-y) \cos(2\phi_h) F_{\text{UU}}^{\cos 2\phi_h} + \lambda y \sqrt{1-y} \sin \phi_h F_{\text{LU}}^{\sin \phi_h} \\ & + |\mathbf{S}_T| \left[ \sin(\phi_h - \phi_S) \left( \frac{2-2y+y^2}{2} F_{\text{UT,T}}^{\sin(\phi_h-\phi_S)} + (1-y) F_{\text{UT,L}}^{\sin(\phi_h-\phi_S)} \right) \right. \\ & \left. \left. + (1-y) \left( \sin(\phi_h + \phi_S) F_{\text{UT}}^{\sin(\phi_h+\phi_S)} + \sin(3\phi_h - \phi_S) F_{\text{UT}}^{\sin(3\phi_h-\phi_S)} \right) \right] \right\} \\ & + \lambda |\mathbf{S}_T| \left[ \frac{2y-y^2}{2} \cos(\phi_h - \phi_S) F_{\text{LT}}^{\cos(\phi_h-\phi_S)} + y \sqrt{1-y} \cos \phi_S F_{\text{LT}}^{\cos \phi_S} \right. \\ & \left. \left. + y \sqrt{1-y} \cos(2\phi_h - \phi_S) F_{\text{LT}}^{\cos(2\phi_h-\phi_S)} \right] \right\}, \end{aligned} \right.$$



Gamma–nucleon system.

Transversely polarised target

Longitudinally polarised beam

TMD factorisation ( $P_T/z \ll Q$ ):

$$F = \mathcal{C}[wfD] = x \sum_q e_q^2 \int d^2 k_T d^2 P_\perp \delta^{(2)}(z k_T + P_\perp - P_T) w(k_T, P_\perp) f^q(x, k_T, Q^2) D^{q \rightarrow h}(z, P_\perp, Q^2)$$

# Semi-inclusive DIS

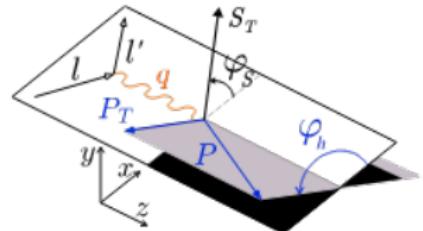
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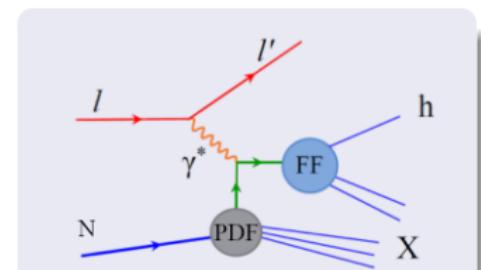
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Transversely polarised target

Longitudinally polarised beam

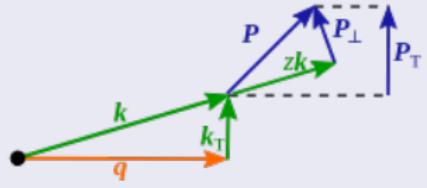


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# Structure functions in TMD factorisation

Unpolarised-target part up to order  $1/Q$ , and denoting ‘...’ terms vanishing in Wandzura–Wilczek-type approximation:

$$F_{\text{UU,T}} = \mathcal{C} [f_1 D_1],$$

$$F_{\text{UU,L}} = 0,$$

$$F_{\text{UU}}^{\cos \phi_h} = \frac{2M}{Q} \mathcal{C} \left[ - \underbrace{\frac{\hat{h} \cdot \mathbf{k}_T}{M} f_1 D_1}_{\text{Cahn effect}} - \underbrace{\frac{(\hat{h} \cdot \mathbf{P}_\perp) k_T^2}{M^2 M_h} h_1^\perp H_1^\perp}_{\text{Boer–Mulders effect}} + \dots \right]$$

$$F_{\text{UU}}^{\cos 2\phi_h} = \mathcal{C} \left[ - \underbrace{\frac{2(\hat{h} \cdot \mathbf{k}_T)(\hat{h} \cdot \mathbf{P}_\perp) - \mathbf{k}_T \cdot \mathbf{P}_\perp}{MM_h} h_1^\perp H_1^\perp}_{\text{Boer–Mulders effect}} \right]$$

$$F_{\text{LU}}^{\sin \phi_h} = \frac{2M}{Q} \mathcal{C} [\dots]$$

Transversely-polarised target part at leading twist:

Collins effect:  $F_{\text{UT}}^{\sin(\phi_h + \phi_S)} = \mathcal{C} \left[ - \frac{\hat{h} \cdot \mathbf{k}_T}{M_h} h_1 H_1^\perp \right]$

Sivers effect:  $F_{\text{UT}}^{\sin(\phi_h - \phi_S)} = \mathcal{C} \left[ - \frac{\hat{h} \cdot \mathbf{P}_\perp}{M} f_{1\text{T}}^\perp D_1 \right]$

and many more...

- $\hat{h} = \mathbf{P}_T / P_T$ ,

- $f_1(x, k_T^2, Q^2)$



unpolarised TMD PDF,

- $h_1^\perp(x, k_T^2, Q^2)$



Boer–Mulders function,

- $D_1(z, P_\perp^2, Q^2)$   
unpolarised TMD FF,

- $H_1^\perp(z, P_\perp^2, Q^2)$   
Collins FF.

- $h_1(x, k_T^2, Q^2)$

transversity,

- $f_{1\text{T}}^\perp(x, k_T^2, Q^2)$

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- $\hat{\mathbf{h}} = \mathbf{P}_{\text{T}}/P_{\text{T}}$ ,

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unpolarised TMD PDF,

- $h_1^{\perp}(x, k_{\text{T}}^2, Q^2)$



Boer–Mulders function,

- $D_1(z, P_{\perp}^2, Q^2)$

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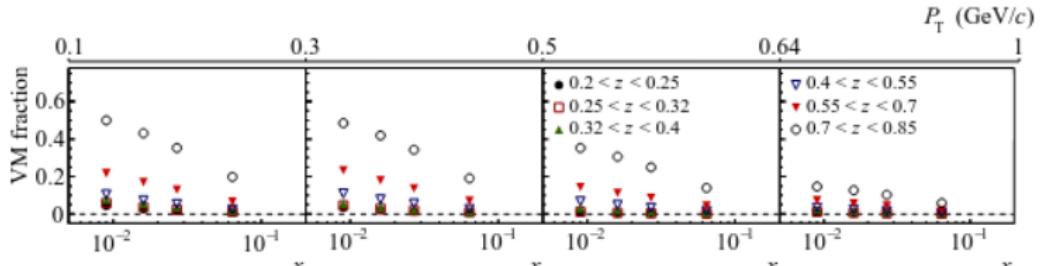
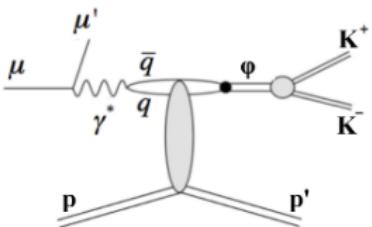
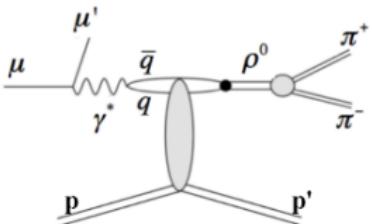


Sivers function.

# Background from diffractive vector mesons (DVMs)

- Significant contributors:  $\rho \rightarrow \pi^+ \pi^-$  and  $\phi \rightarrow K^+ K^-$
- Strong  $x$ -,  $z$ - and  $P_T$ -dependence.
- Up to 50% of observed  $h^\pm$  at low  $x$ , low  $P_T$  and high  $z$   
 $\rightarrow$  Important for multiplicities, cross sections.
- Strong azimuthal modulations for decay products  
 $\rightarrow$  Important for (unpolarised) asymmetries too!
- Current COMPASS recipe (new H target results):
- Visible decays (both  $h$  reconstructed,  $\approx 85\%$ ):  
 $\rightarrow$  can be rejected in event selection.
- Non-visible decays (only one reconstructed,  $\approx 15\%$ ):  
 $\rightarrow$  can be simulated and subtracted by HEPGEN MC

[A. Sandacz, P. Sznajder, arXiv:1207.0333]

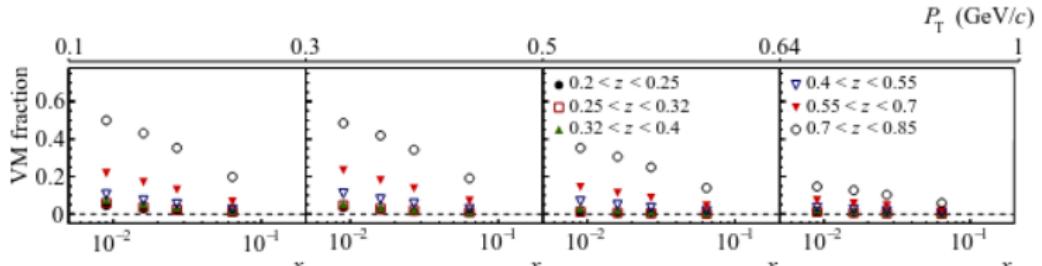
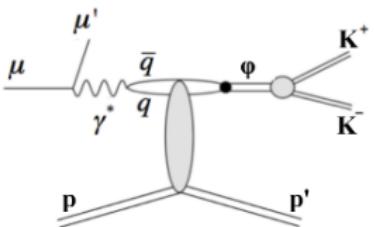
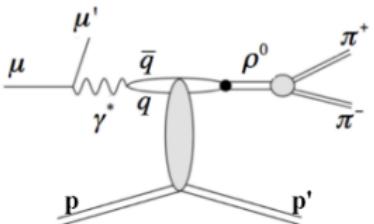


[COMPASS, Nucl.Phys.B 956 (2020) 115039]

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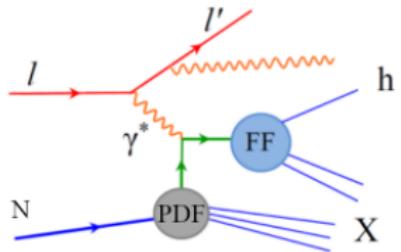
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TMD interpretation defined at tree level  
 → QED radiative effects need to be accounted for:

- radiation of photons along the  $\ell$ ,  $\ell'$  and  $\gamma^*$ ,  
 → changes in  $x$ ,  $Q^2$ , tail from elastic scattering,  
 → orientation of  $\gamma$ -nucleon system distorted.
- Our approach before 2024:
  - Only ‘inclusive corrections’,
  - based on TERAD (semi-analytical)

[A.A. Akhundov *et al.*, Fortschr. Phys. 44 (1996) 373]

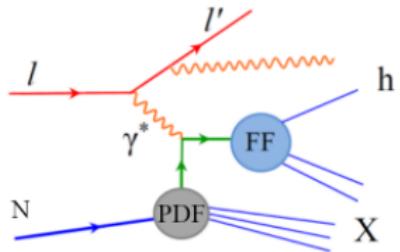
- New approach:
  - Based on DJANGOH Monte Carlo  
 [K. Charchula, G.A. Schuler, H. Spiesberger, Comput. Phys. Commun. 81 (1994) 381–402]
  - Takes into account:  
 → hadron phase space,  
 →  $z$ -,  $P_T$ - and  $\phi_h$ -dependences.



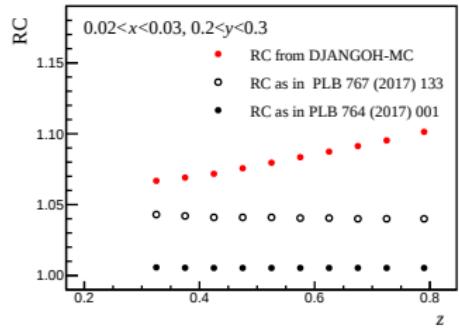
Example of a real photon emission.

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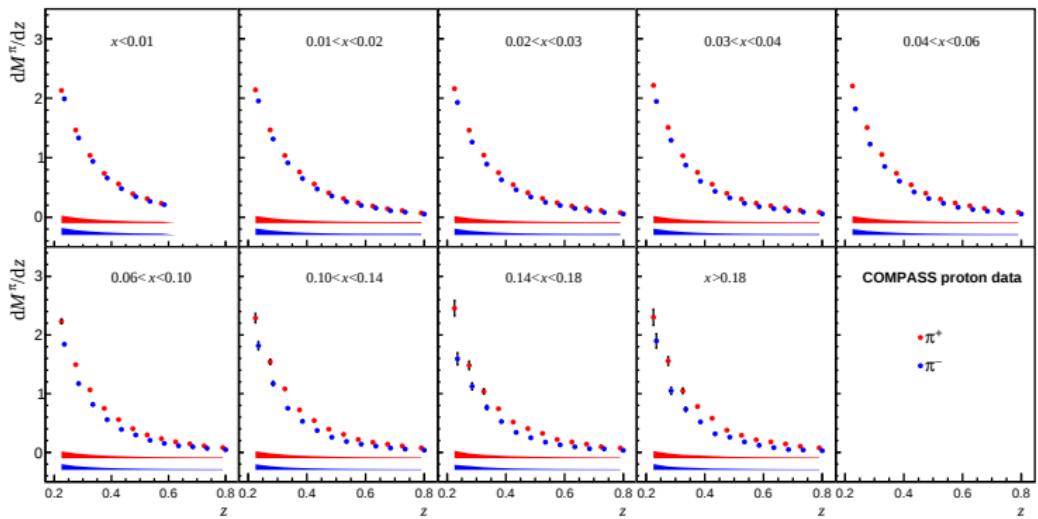
Comparison of the old and new RC for  $\pi^+$  multiplicity in a bin in  $x$  and  $y$ ,  
 where  $RC = \frac{M_{rad, OFF}^h}{M_{rad, ON}^h}$ .

# Collinear hadron multiplicities

- Sensitive to fragmentation functions  $D_1^{q \rightarrow h}(z, y)$ , including  $q/\bar{q}$  and flavour separation.

$$\frac{dM^h(x, y, z)}{dz} = \frac{F_{UU}(x, y, z)}{F_2(x, y)} \propto \sum_q e_q^2 f_1^q(x, Q^2) D_1^{q \rightarrow h}(z, Q^2)$$

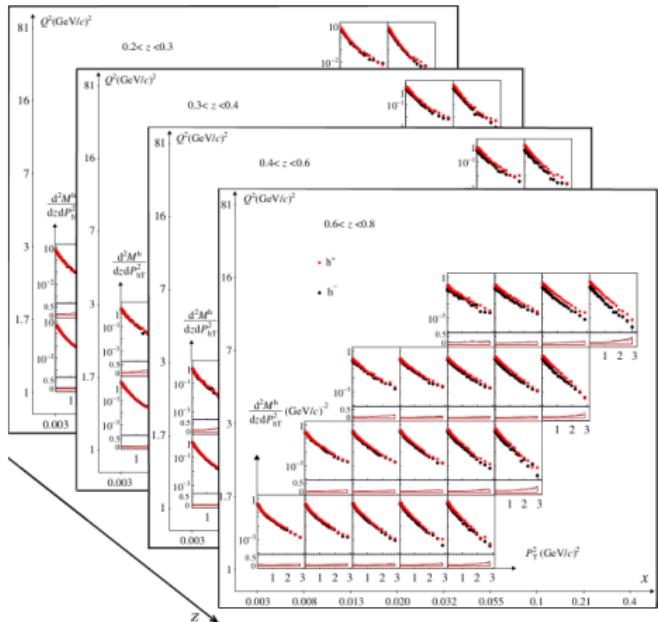
- Corrected for acceptance, diffractive VMs and for radiative effects.
- Previous results on isoscalar target:  
 $h^\pm, \pi^\pm$  [COMPASS, Phys. Lett. B 764 (2017) 001],  $K^\pm$  [COMPASS, Phys. Lett. B 767 (2017) 133].
- New results on H<sub>2</sub> target [COMPASS, Phys. Rev. D 112 (2025) 1, 012002]



Example: Multiplicity of charged pions in bins of  $x$  and  $z$ .

# Transverse-momentum-dependent distributions

## $P_T$ -dependent multiplicities on isoscalar target

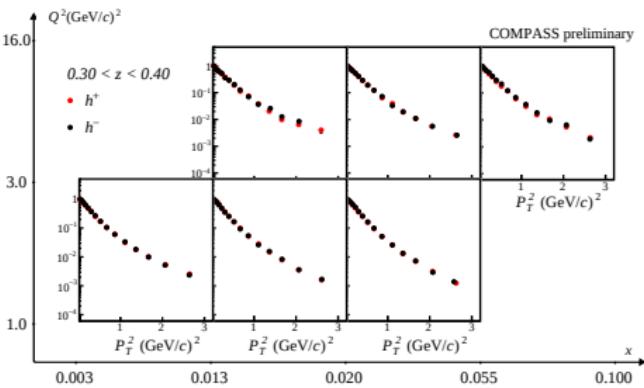
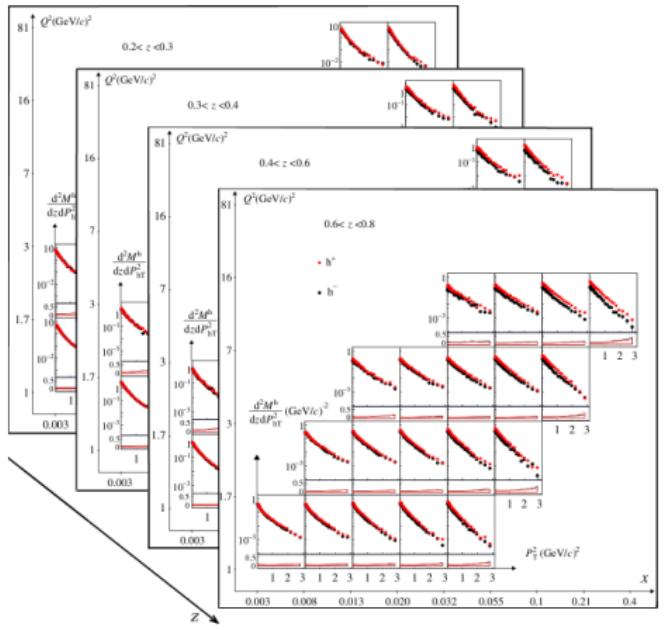


- Results in bins of  $x, Q^2, z, P_T^2$
- DVM contamination subtracted.
- Radiative corrections based on RADGEN.
- [COMPASS, Phys. Rev. D97 (2018)]

# Transverse-momentum-dependent distributions

$P_T$ -dependent multiplicities on isoscalar target

$P_T$ -dependent distributions on H<sub>2</sub> target  
(2016 data)



Preliminary results, DVM contamination subtracted, no RC [A. Moretti, Proc. of ICNFP 2020].

- Results in bins of  $x, Q^2, z, P_T^2$
- DVM contamination subtracted.
- Radiative corrections based on RADGEN.
- [COMPASS, Phys. Rev. D97 (2018)]

Ongoing work:

- Expanding kinematic domain.
- New radiative corrections using DJANGOH. [V. Benešová, IWHSS–CPHI 2024, 30.9.–4.10. 2024, Yerevan, Armenia]

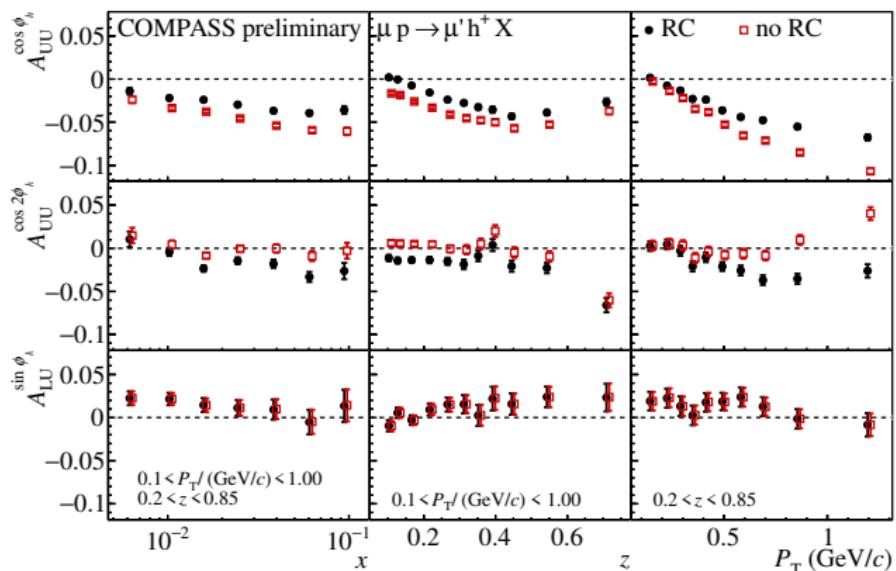
# Unpolarised and beam-spin asymmetries

Results from isoscalar target (2004 data, no RC, no DVM corr.): [COMPASS, Nucl.Phys.B 886 (2014)]

Corrections for diffractive vector mesons: [COMPASS, Nucl.Phys.B 956 (2020)]

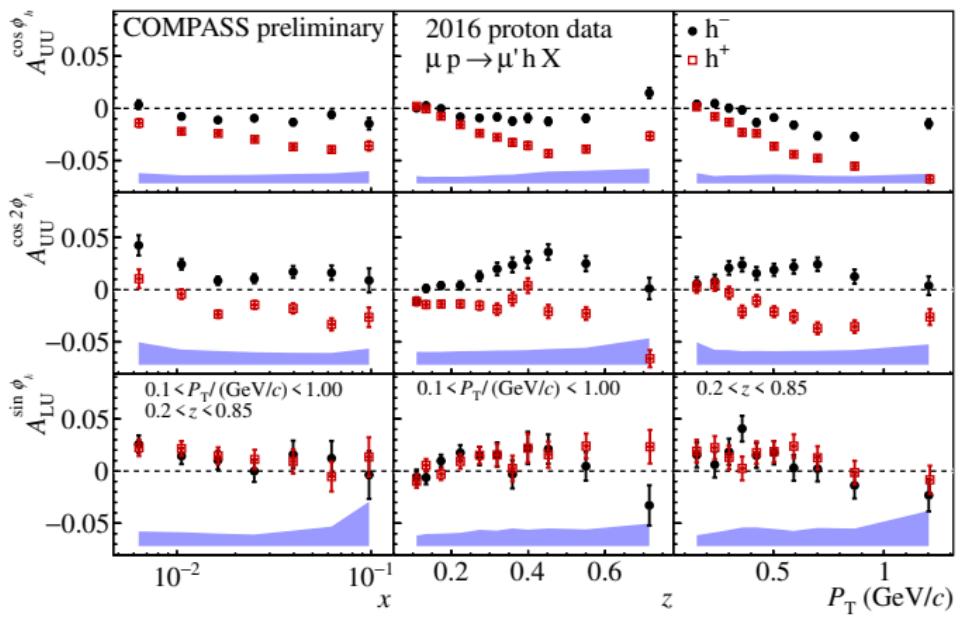
New preliminary results on H<sub>2</sub> target (2016 data): [V. Benešová, PoS DIS2024 (2025), 223]

- Both DVM and RC based on DJANGOH ( $\rightarrow$  new, important!).
- 1D and multi-D results in preparation for publication.



The impact of DJANGOH radiative corrections on  $h^+$ .

# Unpolarised and beam-spin asymmetries

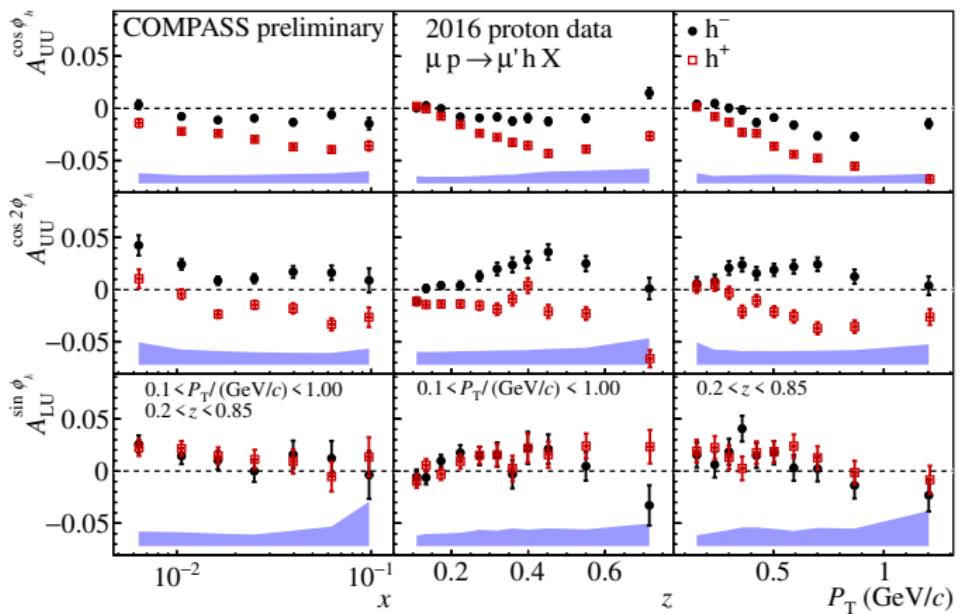


[V. Benešová, PoS DIS2024 (2025), 223]

Unpolarised-target part up to order  $1/Q$  and in Wandzura–Wilczek-type approximation:

$$A_{\text{UU}}^{f(\phi_h)} = \frac{F_{\text{xx}}^{f(\phi_h)}}{F_{\text{UU,T}}} = \frac{F_{\text{xx}}^{f(\phi_h)}}{c [f_1 D_1]} \quad F_{\text{UU}}^{\cos \phi_h} = \frac{2M}{Q} c \left[ - \underbrace{\frac{\hat{h} \cdot \mathbf{k}_T}{M} f_1 D_1}_{\text{Cahn effect}} - \underbrace{\frac{(\hat{h} \cdot \mathbf{P}_\perp) k_T^2}{M^2 M_h} h_1^\perp H_1^\perp}_{\text{Boer–Mulders effect}} + \dots \right]$$

# Unpolarised and beam-spin asymmetries



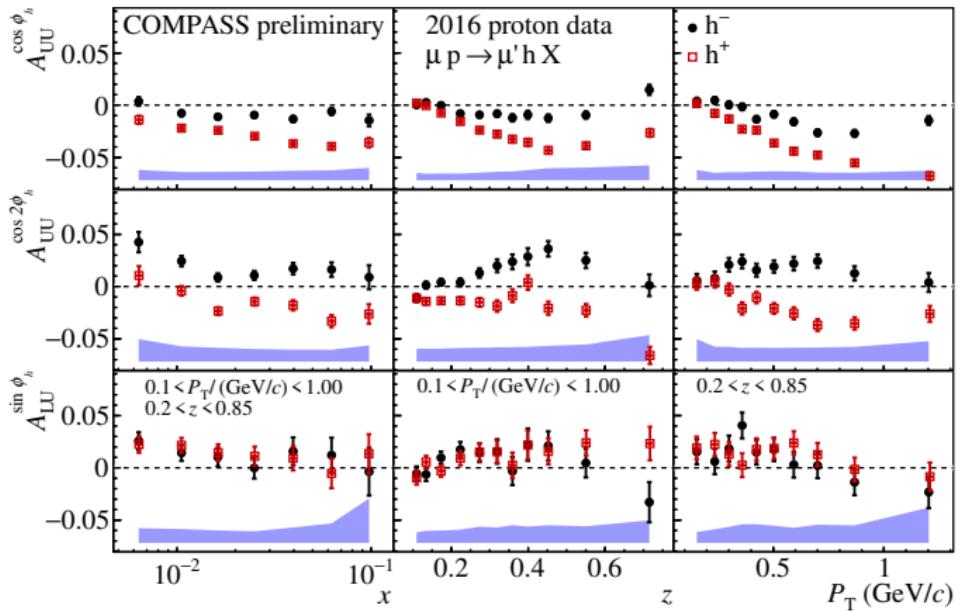
[V. Benešová, PoS DIS2024 (2025), 223]

Unpolarised-target part up to order  $1/Q$  and in Wandzura–Wilczek-type approximation:

$$A_{xx}^{f(\phi_h)} = \frac{F_{xx}^{f(\phi_h)}}{F_{UU,T}} = \frac{F_{xx}^{f(\phi_h)}}{C [f_1 D_1]}$$

$$F_{UU}^{\cos 2\phi_h} = C \left[ - \underbrace{\frac{2(\hat{h} \cdot \mathbf{k}_T)(\hat{h} \cdot \mathbf{P}_{\perp}) - \mathbf{k}_T \cdot \mathbf{P}_{\perp} h_1^{\perp} H_1^{\perp}}{M M_h}}_{\text{Boer–Mulders effect}} \right]$$

# Unpolarised and beam-spin asymmetries

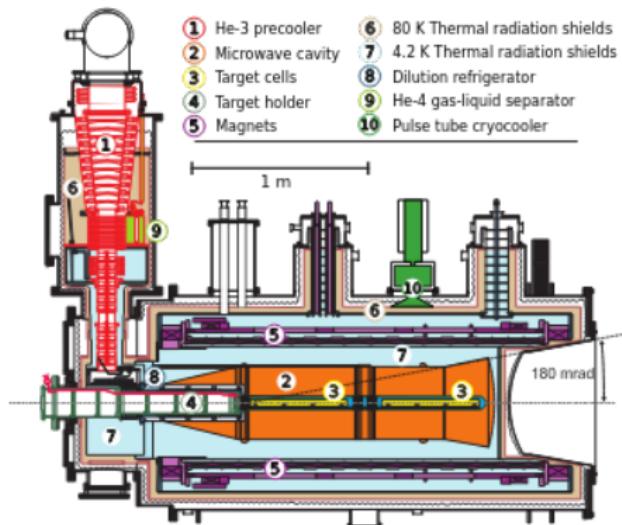


[V. Benešová, PoS DIS2024 (2025), 223]

Unpolarised-target part up to order  $1/Q$  and in Wandzura–Wilczek-type approximation:

$$A_{UU}^{f(\phi_h)} = \frac{F_{UU,T}^{f(\phi_h)}}{F_{UU,T}} = \frac{F_{UU,T}^{f(\phi_h)}}{C [f_1 D_1]} \quad F_{LU}^{\sin \phi_h} = \frac{2M}{Q} C \left[ \text{pure twist-3 qqq terms} \right]$$

# Transverse-spin asymmetries



Polarised target system (2015).

- Large-acceptance superconducting magnet.
- Dilution refrigerator to reach below 100 mK.
- Dynamic nuclear polarisation with microwaves.
- NMR for polarisation measurement.



## Measurement method

- 2 (3) target cells,
- alternating polarisation
- → azimuthal acceptance is cancelled.

## DVM and radiative effects

- not sensitive to polarisation,
- DVMs: small effect,
- RC taken into account in the dilution factor (TERAD-based).

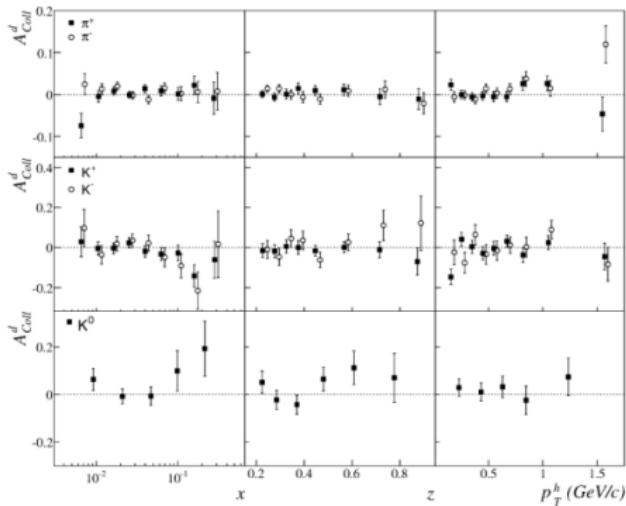
# Transverse-spin asymmetries: First measurements

1st COMPASS measurement of transverse spin asymmetries:

- $d^\uparrow$  in  ${}^6\text{LiD}$  target, data taking 2002–2004.
- Both Collins and Sivers asymmetries compatible with zero (unlike HERMES on  $p^\uparrow$ ).

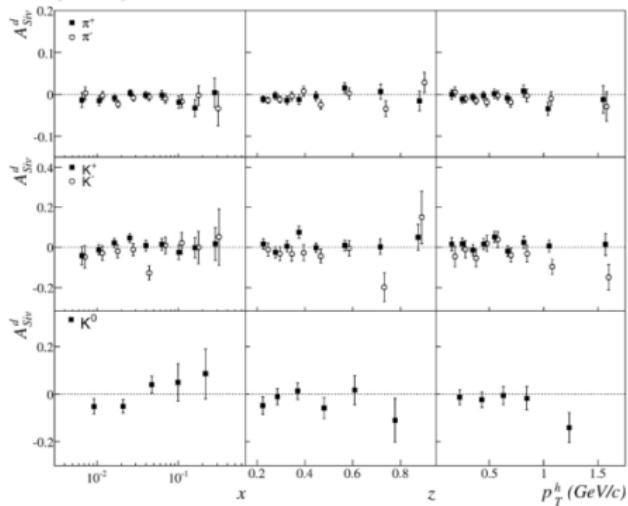
Collins asymmetry

$$A_{\text{UT}}^{\sin(\phi_h + \phi_S)} = \frac{F_{\text{UT}}^{\sin(\phi_h + \phi_S)}}{F_{\text{UU}}} = \frac{c \left[ -\frac{\hat{h} \cdot \mathbf{k}_{\text{T}}}{M_h} h_1 H_1^\perp \right]}{c [f_1 D_1]}$$



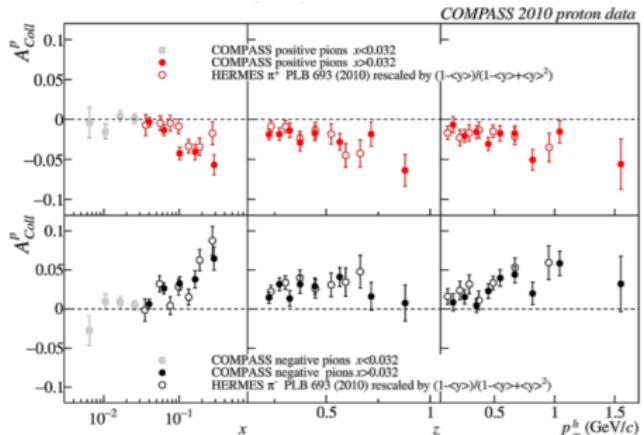
Sivers asymmetry

$$A_{\text{UT}}^{\sin(\phi_h - \phi_S)} = \frac{F_{\text{UT}}^{\sin(\phi_h - \phi_S)}}{F_{\text{UU}}} = \frac{c \left[ -\frac{\hat{h} \cdot \mathbf{P}_1}{M} f_{1\text{T}}^\perp D_1 \right]}{c [f_1 D_1]}$$



[COMPASS, Phys. Lett. B 673 (2009) 127]

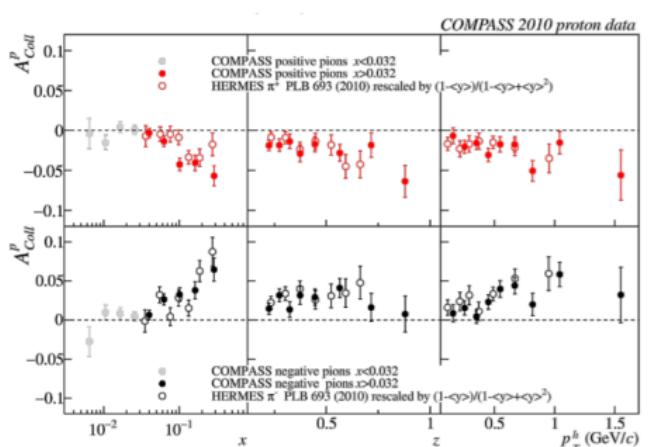
# Transverse-spin asymmetries: Transversity and Collins effect



[COMPASS, Phys. Lett. B 774 (2015) 250]

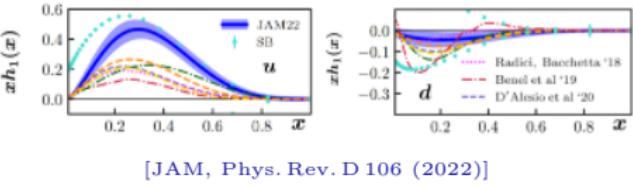
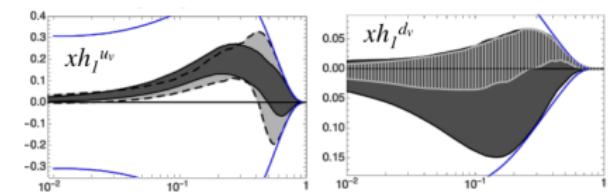
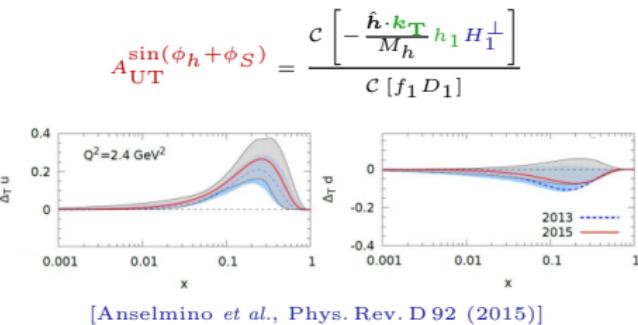
- $p^\uparrow$  in  $\text{NH}_3$  target, data taking 2007–2010.
- Collins asymmetries non-zero.
- Compatible with HERMES.
- Number of global extractions,
- d-quark not well constrained.
- Deuteron is necessary,  
only COMPASS measured on  $d^\uparrow$ .

# Transverse-spin asymmetries: Transversity and Collins effect

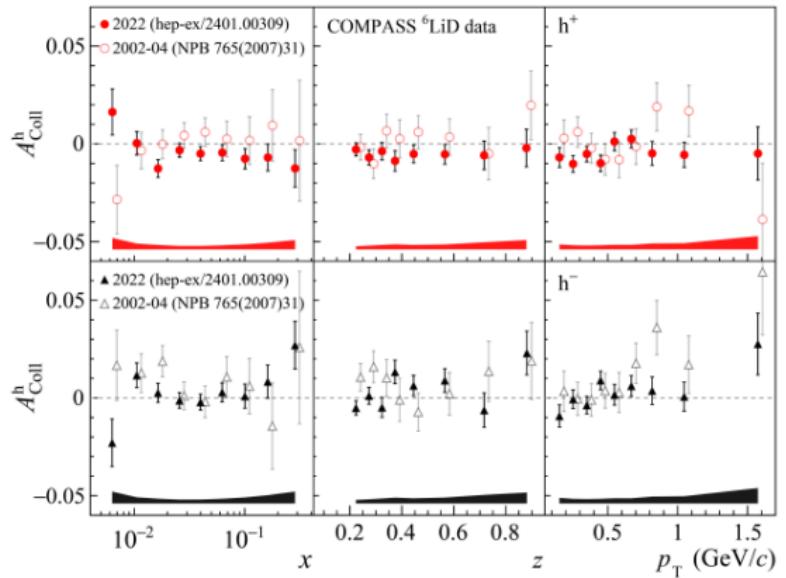


[COMPASS, Phys. Lett. B 774 (2015) 250]

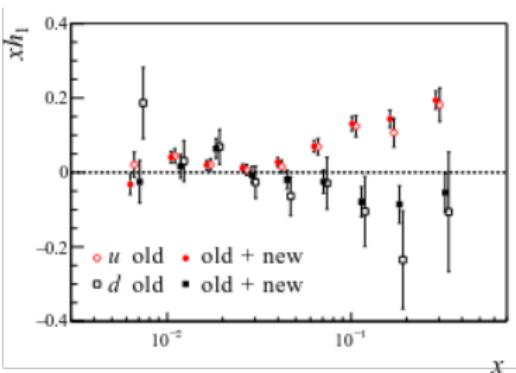
- $p^\uparrow$  in NH<sub>3</sub> target, data taking 2007–2010.
- Collins asymmetries non-zero.
- Compatible with HERMES.
- Number of global extractions,
- d-quark not well constrained.
- Deuteron is necessary,  
only COMPASS measured on d<sup>↑</sup>.



# Transverse-spin asymmetries: New Collins on deuteron



$$A_{\text{UT}}^{\sin(\phi_h + \phi_S)} = \frac{c \left[ -\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} h_1 H_1^\perp \right]}{c [f_1 D_1]}$$



Point-by-point extraction to show  
the expected impact.

Looking forward to global fits!

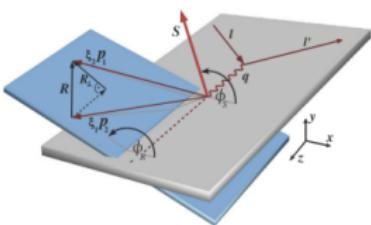
See the new paper [COMPASS, Phys. Rev. Lett. 133 (2024) 10, 101903]

# Transverse-spin asymmetries: Dihadrons

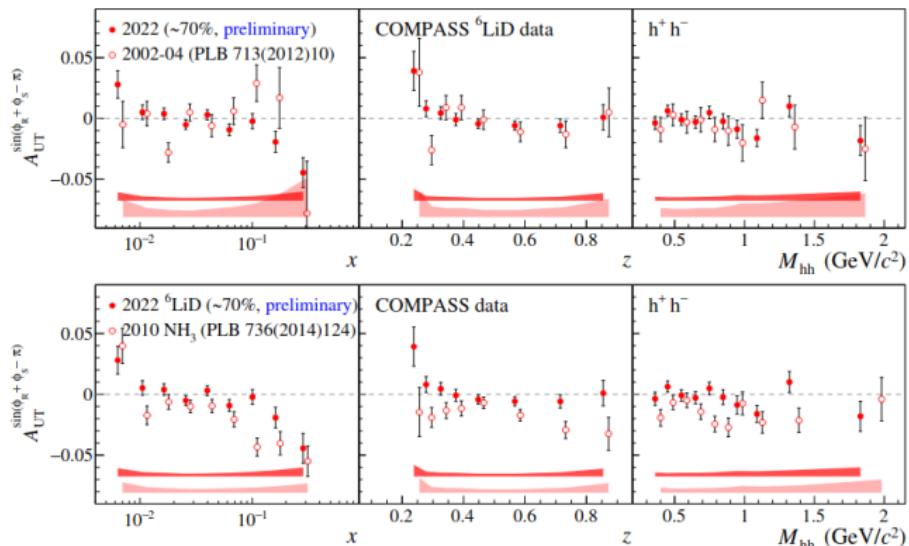
Collinear way to access transversity (no TMD factorisation) [M. Radici *et al.*, Phys. Rev. D 65 (2002)]

$$\frac{d^7\sigma}{d\cos\theta dM_{hh} d\phi_R dz dx dy d\phi_S} = \frac{\alpha^2}{2\pi Q^2 y} \left( (1-y + \frac{y^2}{2}) \sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_{hh}^2, \cos\theta) + \right. \\ \text{transversity PDF} \quad \text{dihadron FF} \\ \left. S_\perp(1-y) \sum_q e_q^2 \frac{|\mathbf{p}_1 - \mathbf{p}_2|}{2M_{hh}} \sin\theta \sin\phi_{RS} h_1^q(x) H_{1,q}^\triangleleft(z, M_{hh}^2, \cos\theta) \right)$$

COMPASS proton results are available [COMPASS, Phys. Lett. B 736 (2014)]



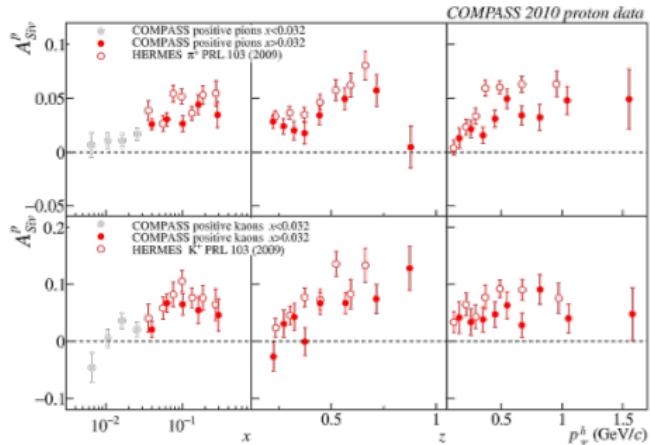
Definition of the angles in the gamma–nucleon system.



New deuteron results [A. Asatryan, PoS DIS2024 (2025), 236]

# Transverse-spin asymmetries: Sivers effect

$$A_{\text{UT}}^{\sin(\phi_h - \phi_S)} = \frac{c \left[ -\frac{\hat{h} \cdot \mathbf{P}_\perp}{M} f_{1\text{T}}^\perp D_1 \right]}{c [f_1 D_1]}$$

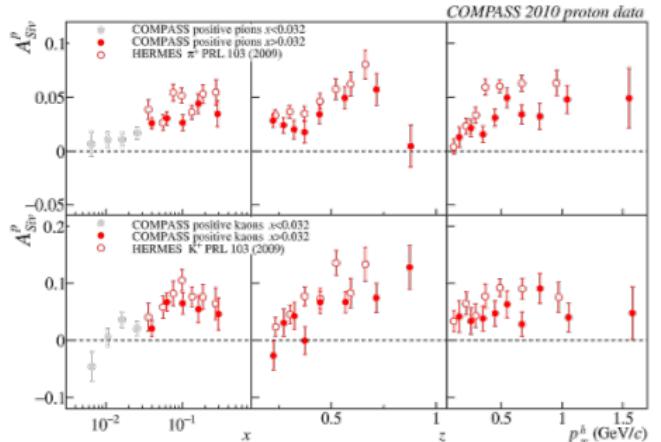


[COMPASS, Phys. Lett. B 774 (2015) 250]

- $\mathbf{p}^\dagger$  in NH<sub>3</sub> target, data taking 2007–2010.
- Nonzero, smaller than HERMES.
- Number of global extractions.
- Again, unique role of COMPASS in providing deuteron data.

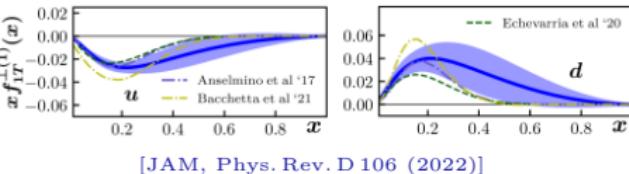
# Transverse-spin asymmetries: Sivers effect

$$A_{\text{UT}}^{\sin(\phi_h - \phi_S)} = \frac{c \left[ -\frac{\hat{h} \cdot P_\perp}{M} f_{1T}^\perp D_1 \right]}{c [f_1 D_1]}$$

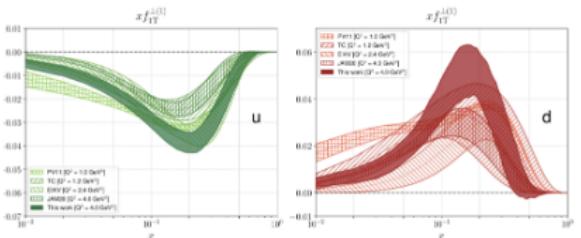


[COMPASS, Phys. Lett. B 774 (2015) 250]

- $p_T^\uparrow$  in NH<sub>3</sub> target, data taking 2007–2010.
- Nonzero, smaller than HERMES.
- Number of global extractions.
- Again, unique role of COMPASS in providing deuteron data.

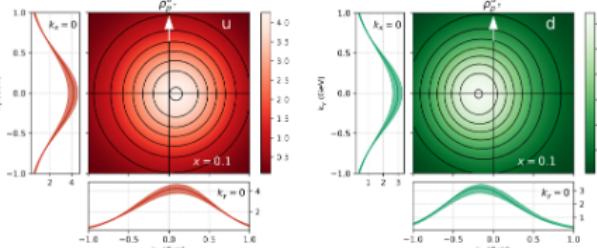


[JAM, Phys. Rev. D 106 (2022)]



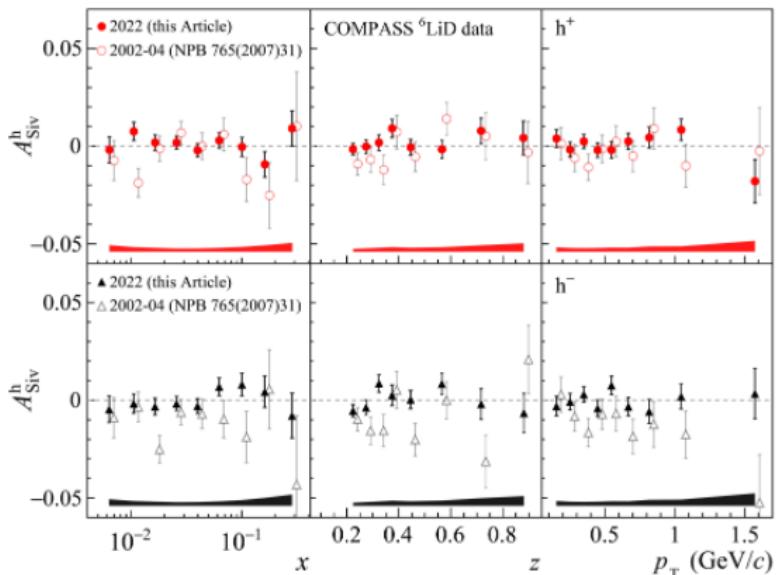
Distortion in the transverse plane of the TMD quark distribution in a  $p_T^\uparrow$

$$\Phi_{q/p_T^\uparrow}^{[\gamma^+]}(x, k_x, k_y) = f_1^q(x, k_T^2) - \frac{k_x}{M} f_{1T}^{1\perp q}(x, k_T^2) \quad [Q^2 = 4 \text{ GeV}^2]$$



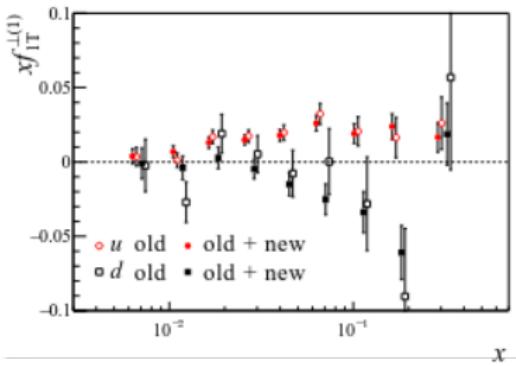
[A. Bacchetta et al., Phys. Lett. B 827 (2022)]

# Transverse-spin asymmetries: New Sivers on deuteron



Sivers asymmetries on  $d^\dagger$ : old and new (2022) data.

$$A_{\text{UT}} \sin(\phi_h - \phi_S) = \frac{c \left[ -\frac{\hbar \cdot P_\perp}{M} f_{1T}^\perp D_1 \right]}{c [f_1 D_1]}$$

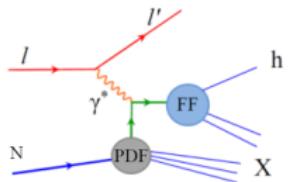


Point-by-point extraction to show  
the expected impact.

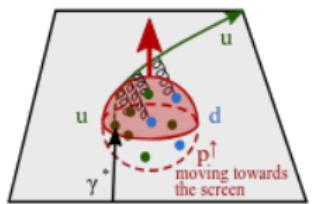
Looking forward to global fits!

See the new paper [COMPASS, Phys. Rev. Lett. 133 (2024) 10, 101903]

# Transverse-spin asymmetries: Universality of TMDs



Pion production in DIS off  $p^\uparrow$



Sivers effect in SIDIS

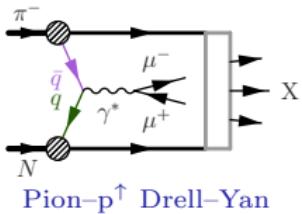
[M. Burkardt, Nucl. Phys. A735 (2004)].

A change of sign predicted for Sivers and Boer–Mulders TMD PDFs due to gauge link structure:

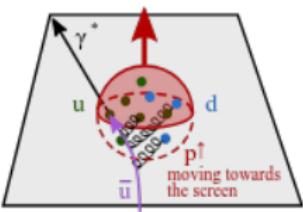
$$f_{1T}^{\perp q}|_{\text{SIDIS}} = -f_{1T}^{\perp q}|_{\text{DY}}$$

$$h_1^{\perp q}|_{\text{SIDIS}} = -h_1^{\perp q}|_{\text{DY}}$$

[J. Collins, Phys.Lett. B536 (2002) 43]

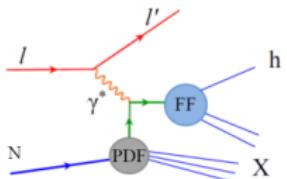


Pion- $p^\uparrow$  Drell-Yan

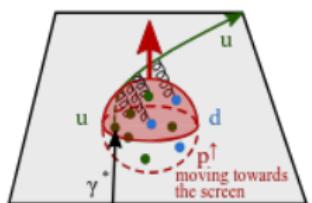


Sivers effect in Drell-Yan drawn in the same manner.

# Transverse-spin asymmetries: Universality of TMDs



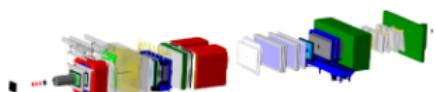
Pion production in DIS off  $p^\uparrow$



Sivers effect in SIDIS

[M. Burkardt, Nucl. Phys. A735 (2004)].

COMPASS 2007 + 2010 data



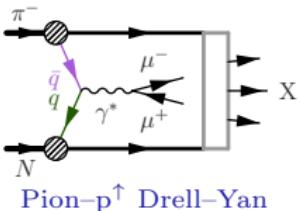
Very close  $Q^2$  range to COMPASS Drell-Yan, the same apparatus.

A change of sign predicted for Sivers and Boer–Mulders TMD PDFs due to gauge link structure:

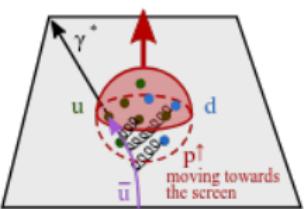
$$f_{1T}^{\perp q}|_{\text{SIDIS}} = -f_{1T}^{\perp q}|_{\text{DY}}$$

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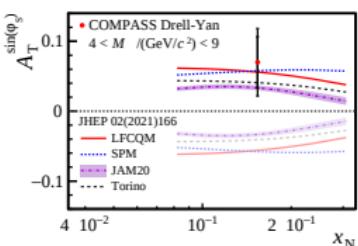


Pion- $p^\uparrow$  Drell-Yan



Sivers effect in Drell-Yan drawn in the same manner.

COMPASS 2015 + 2018 data



Data favour the change.  
[COMPASS, Phys. Rev. Lett. 133 (2024) 7, 071902]

Weighted asymmetry approach:  
M. Niemiec, Wed. 18:23 (poster)  
[Indico].

- COMPASS entered analysis phase, but still very active.
- Plenty of results to come!
- Recent results in semi-inclusive DIS:
  - Multiplicities of  $h^\pm, \pi^\pm, K^\pm$  on  $H_2$  with new RC [COMPASS, Phys. Rev. D 112 (2025) 1, 012002]
  - Sivers and Collins asymmetries on  $d^\dagger$  [COMPASS, Phys. Rev. Lett. 133 (2024) 10, 101903],
- Ongoing work in semi-inclusive DIS:
  - Unpolarised asymmetries on  $H_2$  with new RC [V. Benešová, PoS DIS2024 (2025), 223]
  - $P_T$ -dependent distributions on  $H_2$  with new RC.
  - Transversity-induced dihadron asymmetry [A. Asatryan, PoS DIS2024 (2025), 236]
  - Other transverse spin asymmetries on  $d^\dagger$ .
  - Multi-dimensional analyses of  $d^\dagger$  data...
- Other selected highlights:
  - Strange meson spectroscopy [COMPASS, arXiv: 2504.09470 [hep-ex] (4/2025)].
  - Drell–Yan weighted asymmetries [M. Niemiec, Wed. 18:23 (poster)].
  - Drell–Yan multi-D cross-section [V. Andrieux, DIS2024, Grenoble, France, 4/2024].
  - Hard exclusive  $\pi^0$  muoproduction [COMPASS, arXiv: 2412.19923 [hep-ex] (12/2024)]

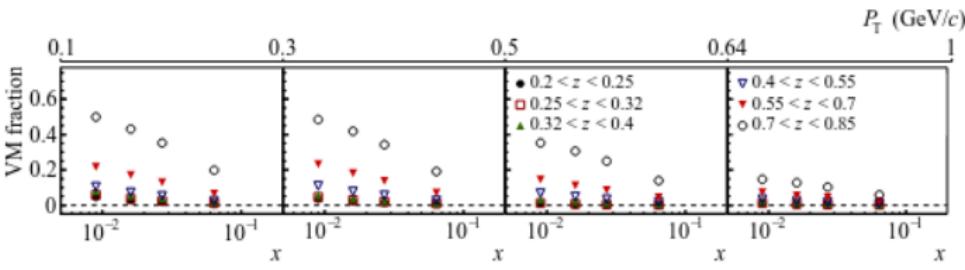
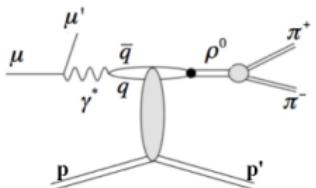
Thank you for your attention!

# Conclusion

- COMPASS entered analysis phase, but still very active.
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- Recent results in semi-inclusive DIS:
  - Multiplicities of  $h^\pm, \pi^\pm, K^\pm$  on  $H_2$  with new RC [COMPASS, Phys. Rev. D 112 (2025) 1, 012002]
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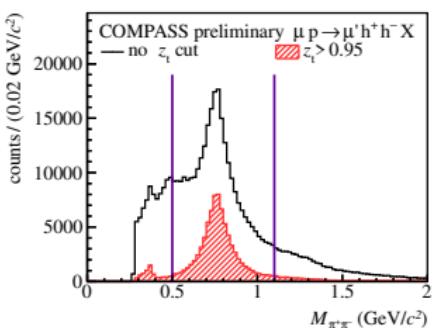
Significant contributors:  $\rho \rightarrow \pi^+\pi^-$  and  $\phi \rightarrow K^+K^-$



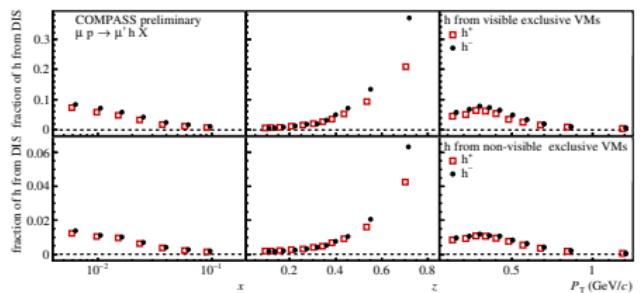
[COMPASS, Nucl.Phys.B 956 (2020) 115039]

- Strong  $x$ -,  $z$ - and  $P_T$ -dependence.
- Up to 50% of observed  $h^\pm$  at low  $x$ , low  $P_T$  and high  $z$   
→ Important for multiplicities, cross sections.
- Strong azimuthal modulations for decay products  
→ Important for (unpolarised) asymmetries too!
- Visible decays (both  $h$  reconstructed):  
→ can be rejected in event selection.
- Non-visible decays (only one reconstructed):  
→ can be simulated and subtracted by HEPGEN MC

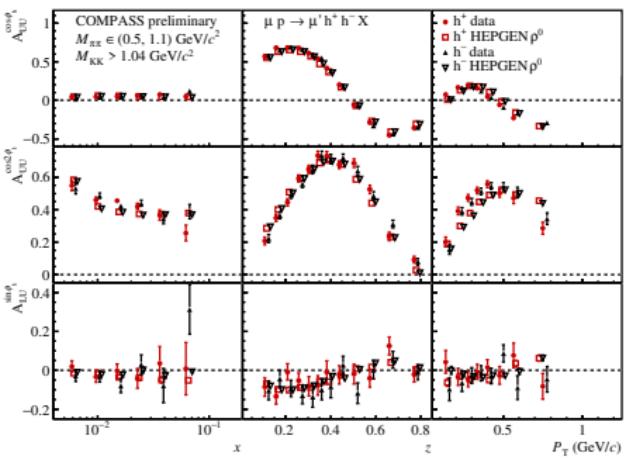
[A. Sandacz, P. Sznajder, arXiv:1207.0333]



# Backup: Background from diffractive vector mesons



Visible and non-visible contamination in bins of 1D asymmetries.

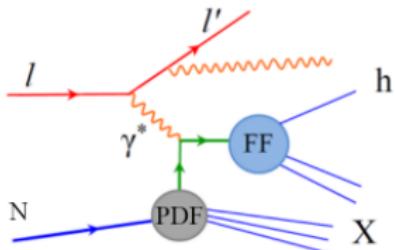


Modulations can be reasonably reproduced by HEPGEN MC.

[V. Benešová, PoS DIS2024 (2025), 223]

TMD interpretation defined at tree level  
→ QED radiative effects need to be accounted for:

- radiation of photons along the  $\ell$ ,  $\ell'$  and  $\gamma^*$ ,  
→ changes in  $x$ ,  $Q^2$ , tail from elastic scattering,  
→ orientation of  $\gamma$ -nucleon system distorted.
  - Our approach before 2024:
    - Only ‘inclusive corrections’,
    - based on TERAD
- [A.A. Akhundov *et al.*, Fortschr. Phys. 44 (1996) 373]



Example of a real photon emission.

New approach based on DJANGOH (DJANGO6) MC:

- [K. Charchula, G.A. Schuler, H. Spiesberger,  
Comput. Phys. Commun. 81 (1994) 381–402]
- Updated recently  
[E.C. Aschenauer *et al.*, Phys. Rev. D88 (2013) 114025]
- Hadron phase space,  $z$ -,  $P_T$ - and  $\phi_h$ -dependences  
taken into account

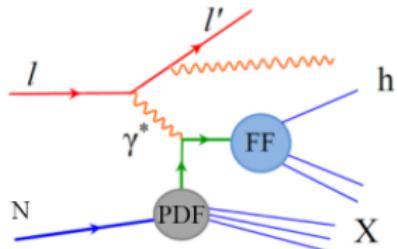
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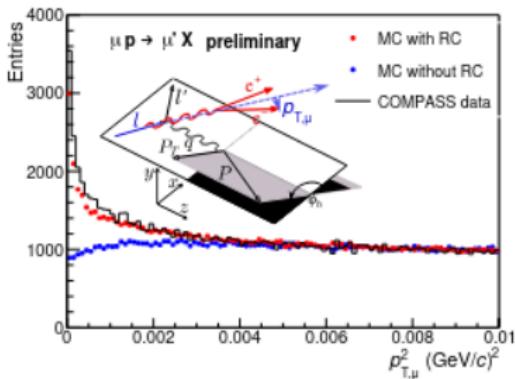
[A.A. Akhundov *et al.*, Fortschr. Phys. 44 (1996) 373]

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     taken into account



Example of a real photon emission.



Example: DJANGOH reproduces  $e^\pm$  from radiative  $\gamma$  in COMPASS data.

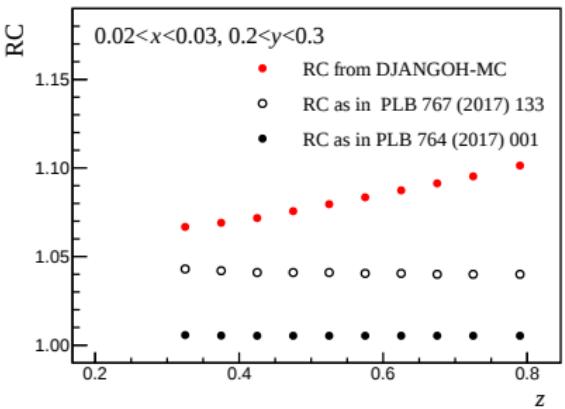
# Backup: Collinear hadron multiplicities

- The multiplicities are corrected for acceptance, diffractive VMs and for radiative effects.

$$\frac{dM^h(x, y, z)}{dz} = \frac{dM_{\text{raw}}^h(x, y, z)}{dz} \frac{C_{\text{VM}}(x, y, z) \text{RC}(x, y, z)}{a(x, y, z)} = \frac{F_{\text{UU}}(x, y, z)}{F_2(x, y)}$$

$$\text{RC} = \frac{M_{\text{rad.OFF}}^h}{M_{\text{rad.ON}}^h} = \frac{N_{h,\text{rad.OFF}}^{\text{DIS}}}{N_{\text{events,rad.OFF}}^{\text{DIS}}} \Big/ \frac{N_{h,\text{rad.ON}}^{\text{DIS}}}{N_{\text{events,rad.ON}}^{\text{DIS}}}$$

- Sensitive to fragmentation functions  $D_q^h(z, Q^2)$ , including  $q/\bar{q}$  and flavour separation.
- Previous results – TERAD corrections:
  - No explicit  $z$ -dependence.
  - [Phys. Lett. B 764 (2017) 001] ( $h^\pm, \pi^\pm$ ).
  - [Phys. Lett. B 767 (2017) 133] ( $K^\pm$ ),
- New RC from DJANGOH:
  - Rise in  $z$  (DIS events shifted to higher  $y$  by radiative effects have fewer high- $z$  hadrons).
  - New paper: [COMPASS, Phys. Rev. D 112 (2025) 1, 012002]
- Diference up to 15% in certain bins.
- Publication of the new corrections for the old d results is foreseen.



Example: comparison of the old and new RC for  $\pi^+$  in a given bin in  $x$  and  $y$ .

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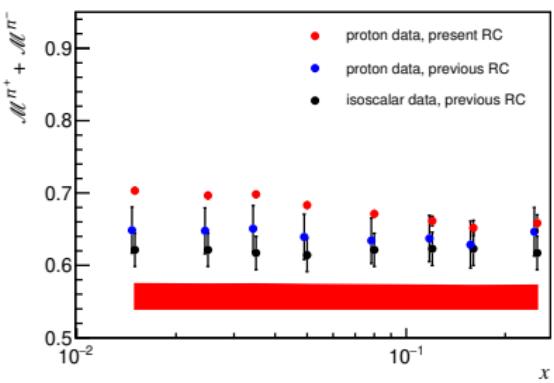
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Comparison of COMPASS pion multiplicities.

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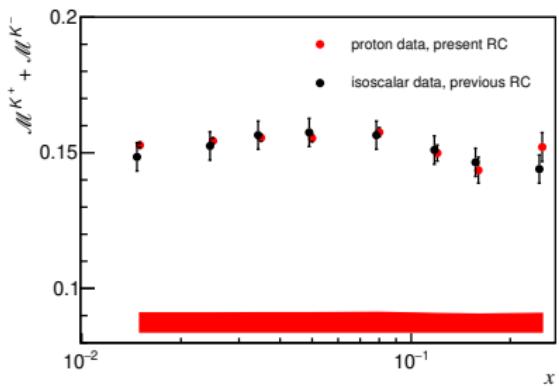
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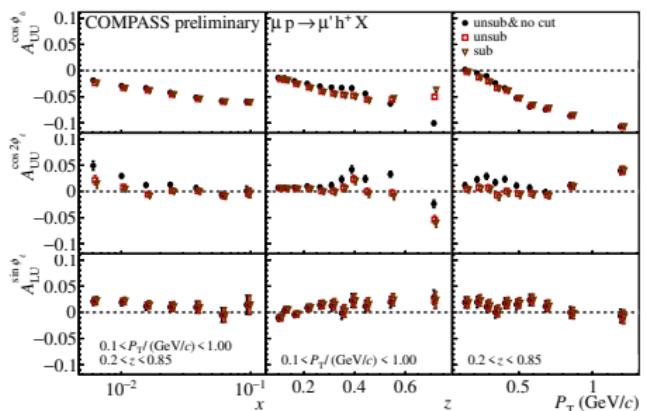
Comparison of COMPASS kaon multiplicities.

# Backup: Unpolarised and beam-spin asymmetries

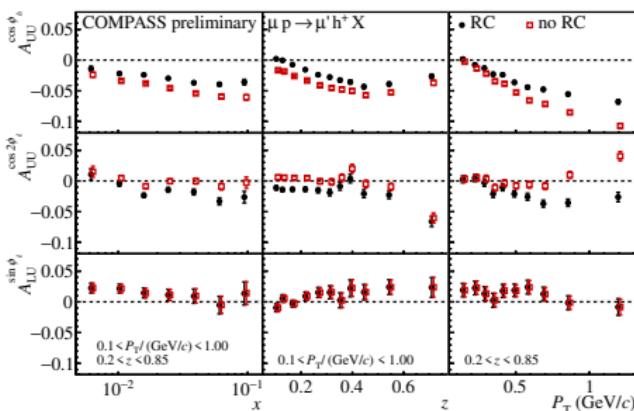
Results from **isoscalar target** (2004 data): [COMPASS, Nucl.Phys.B 886 (2014)]

Corrections for diffractive vector mesons: [COMPASS, Nucl.Phys.B 956 (2020)]

New preliminary results on H<sub>2</sub> target (2016 data): [V. Benešová, PoS DIS2024 (2025), 223]

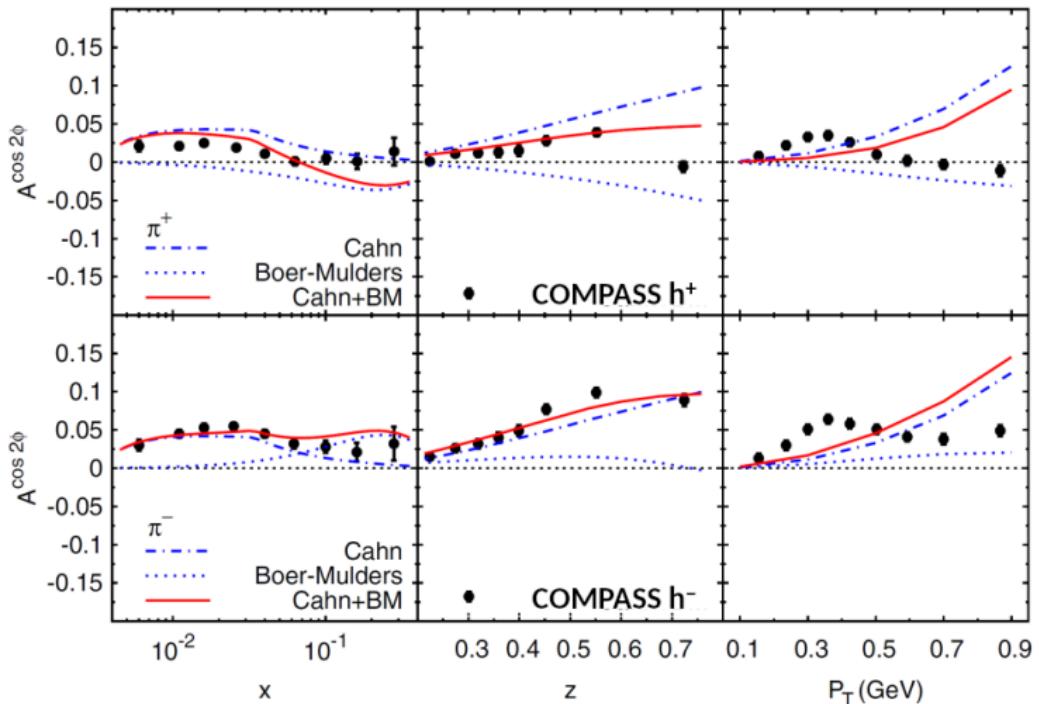


Impact of DVM rejection and subtraction.



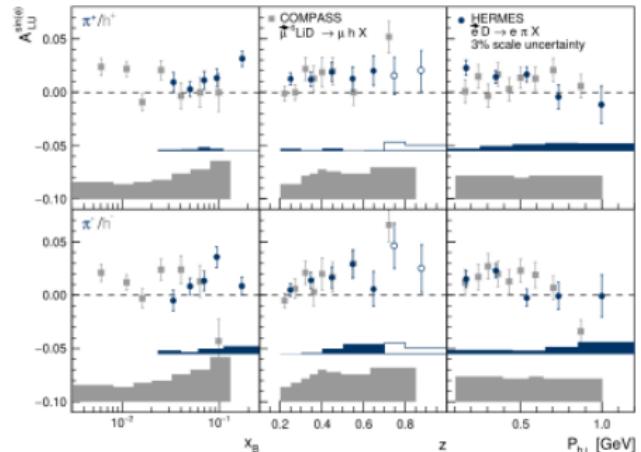
Impact of DJANGOH radiative corrections.

Ongoing work, 1D and multi-D results in preparation for publication.  
Feasibility studies for  $\pi^0$  reconstruction and  $\pi^\pm/K^\pm$  identification with RICH.

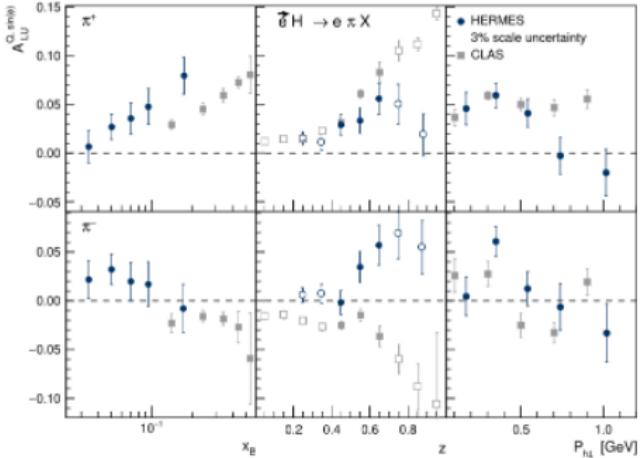


COMPASS  $A_{UU}^{\cos 2\phi h}$  for  $h^\pm$  on isoscalar target (no RC, no DVM corr.)  
 [COMPASS, Nucl.Phys.B886 (2014) 1046–1077],  
 fitted [V. Barone *et al.*, Phys.Rev.D91 (2015) 074019].

# Backup: Unpolarised and beam-spin asymmetries



Beam-spin asymmetry at HERMES and COMPASS.



Beam-spin asymmetry at HERMES and CLAS.

[HERMES, Phys.Lett.B 797 (2019) 134886]

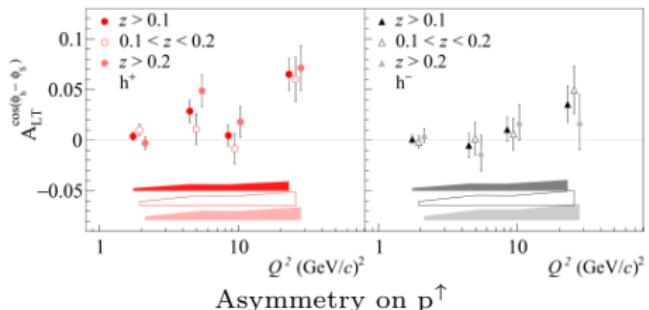
# Backup: What else with 2022 data?

## Other transverse spin asymmetries

$$\frac{d\sigma_{\text{SIDIS}}}{dx dy dz d\phi_b d\phi_h d\mathbf{P}_{hT}^2} = \frac{\alpha^2}{xyQ^2} \left( 1 + \frac{\gamma^2}{2x} \right) \\ \times \left[ \frac{2 - 2y + y^2}{2} F_{UU,T} + (1-y) F_{UU,L} + (2-y)\sqrt{1-y} \cos \phi_h F_{UU}^{\cos \phi_h} \right. \\ + (1-y) \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda y \sqrt{1-y} \sin \phi_h F_{UU}^{\sin \phi_h} \\ + |\mathcal{S}_T| \left[ \sin(\phi_h - \phi_S) \left( \frac{2 - 2y + y^2}{2} F_{UT,T}^{\sin(\phi_h - \phi_S)} + (1-y) F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\ \left. + (1-y) \left( \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \right) \right] \\ \left. + \lambda |\mathcal{S}_T| \left[ \frac{2y - y^2}{2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + y\sqrt{1-y} \cos \phi_S F_{LT}^{\cos \phi_S} \right. \right. \\ \left. \left. + y\sqrt{1-y} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right],$$

Transversely polarized target  
longitudinally polarized beam

## E.g. Kotzinian–Mulders asymmetry:

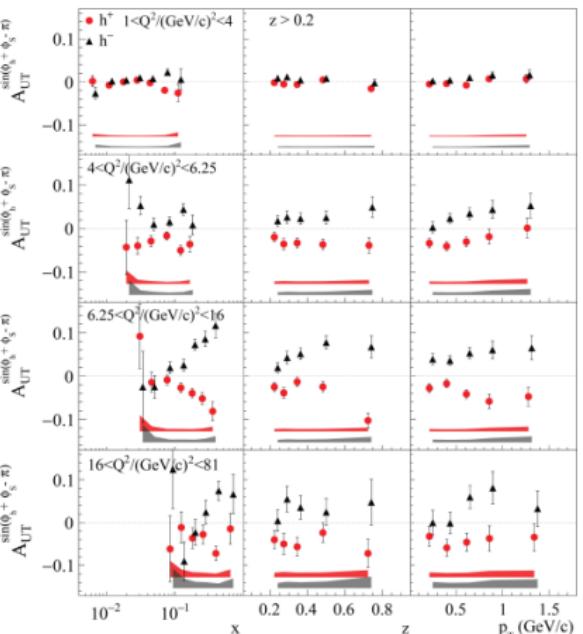


[COMPASS, Phys. Lett. B 770 (2017) 138]

$$A_{LT}^{\sin(\phi_h - \phi_S)} = \frac{c \left[ \frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M} g_{1T} D_1 \right]}{c [f_1 D_1]}$$

## Multi-dimensional studies

E.g.  $Q^2$  dependence of Collins asymmetry:



[COMPASS, Phys. Lett. B 770 (2017) 138]

Unpolarised measurements,  $J/\psi$  production...