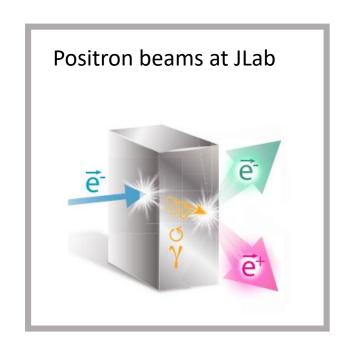
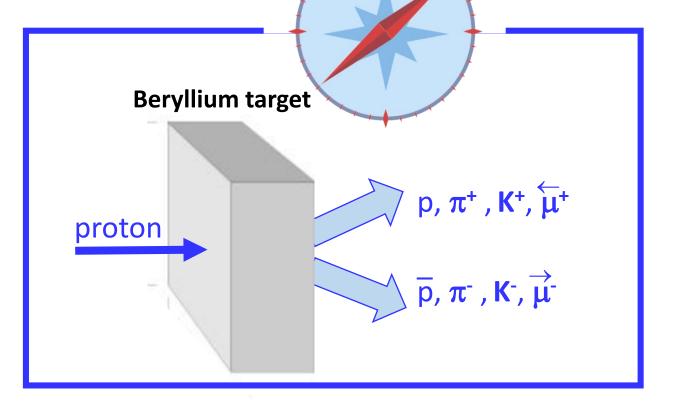
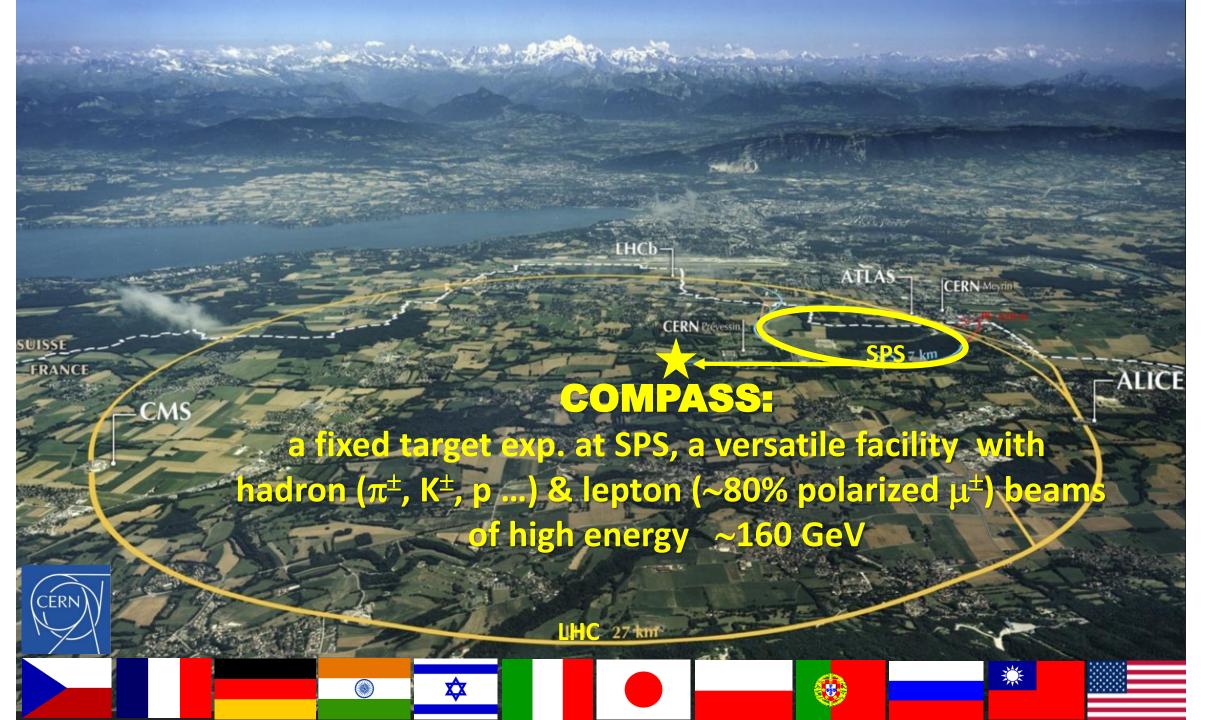
Use of positive and negative polarized muon beams to study exclusive reactions

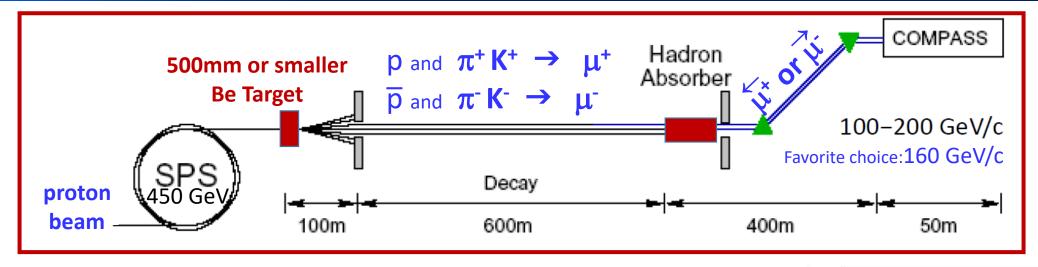
at COMPASS at CERN





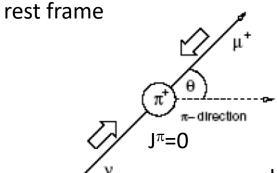


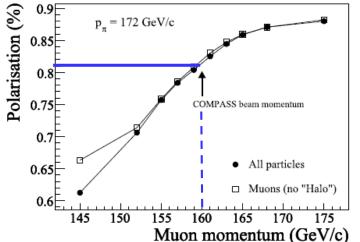
Positive and Negative Polarized Muon Beam at COMPASS

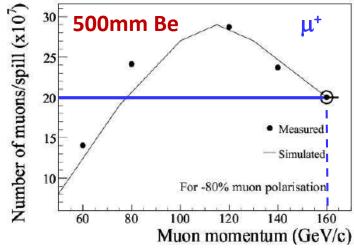


Weak decay $\pi^+ \rightarrow \mu^+ + \nu_\mu$

Parity violation and helicity conservation the muons are 100% polarized in the pion rest frame







In the lab the muon polarization of the muon depends on momenta of both meson and muon

Left-handed v_{μ} and μ^{+} Right-handed $\overline{v_{\mu}}$ and μ^{-}

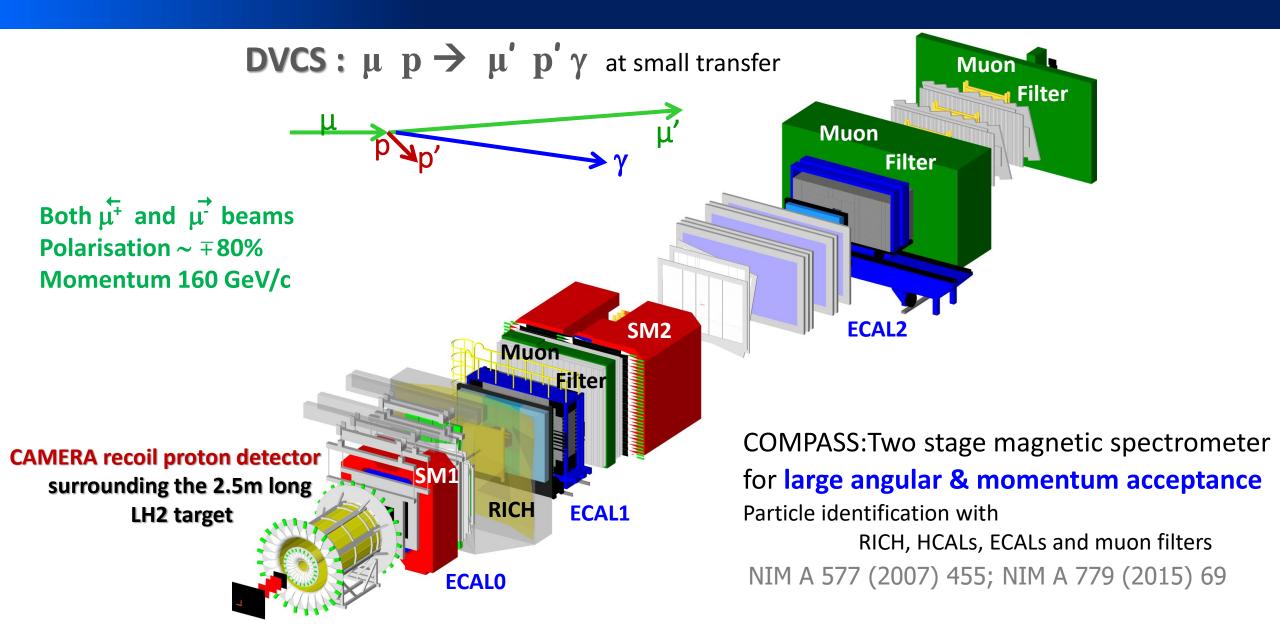
Optimisation of both polarization & muon fluxes: 160 GeV/c \sim 80% polarization 500mm Be 20 $10^7 \mu^+$ /spill but only 7.4 $10^7 \mu^-$ /spill 100mm Be to get about 7.4 $10^7 \mu^+$ /spill

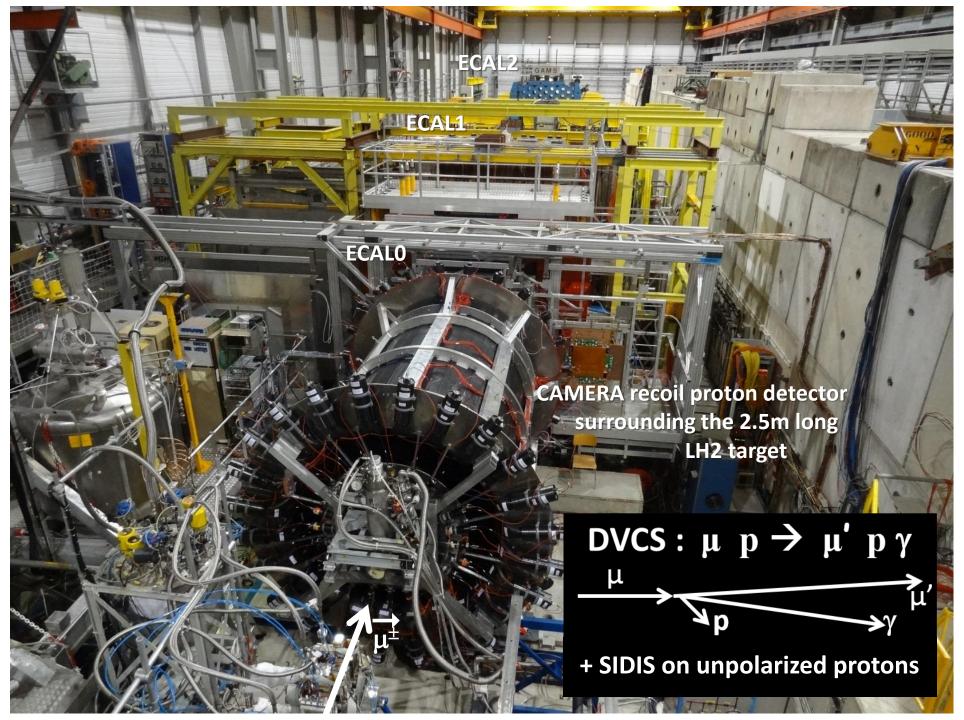
Discussed in this talk:

Advantage of positive and negative polarized muon beams for:

- 1. Deeply Virtual Compton Scattering (DVCS)
- 2. Exclusive π^0 production

Measurement of exclusive cross sections at COMPASS



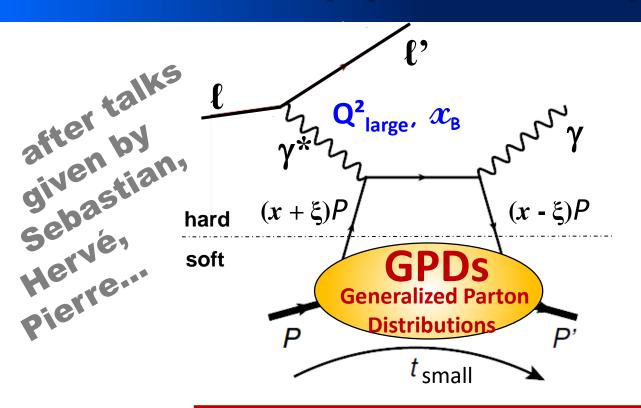


2012:

1 month pilot run

2016 -17:

2 x 6 month data taking



The GPDs depend on the following variables:

x: average quark longitudinal ξ : transferred momentum fraction

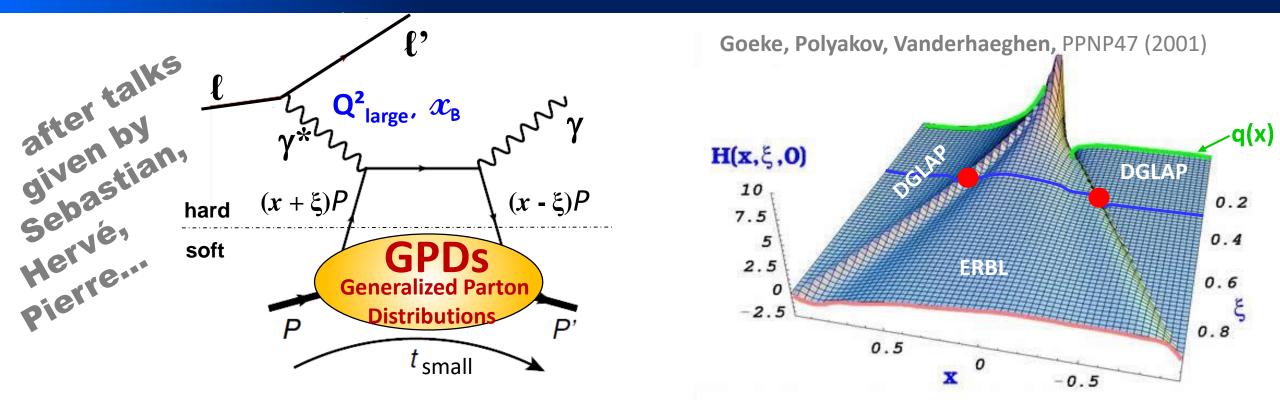
t: proton momentum transfer squared related to b_{\perp} via Fourier transform Q^2 : virtuality of the virtual photon

D. Mueller *et al*, Fortsch. Phys. 42 (1994) **X.D. Ji**, PRL 78 (1997), PRD 55 (1997) **A. V. Radyushkin**, PLB 385 (1996), PRD 56 (1997)

DVCS: $\ell p \rightarrow \ell' p' \gamma$ the golden channel because it interferes with the Bethe-Heitler process also meson production $\ell p \rightarrow \ell' p' \pi^0$, ρ , ω or ϕ or J/ψ ...

The variables measured in the experiment:

$$E_{\ell}$$
, Q^2 , $x_B \sim 2\xi$ /(1+ ξ),
t (or $\theta_{\gamma*\gamma}$) and ϕ ($\ell\ell'$ plane/ $\gamma\gamma*$ plane)



The amplitude DVCS at LT & LO in α_s (GPD H): Real part Imaginary part

$$\mathcal{H} = \int_{t, \, \xi \, \text{fixed}}^{+1} dx \, \frac{H(x, \xi, t)}{x - \xi + i \, \epsilon} = \mathcal{P} \int_{-1}^{+1} dx \, \frac{H(x, \xi, t)}{x - \xi} \, - i \, \pi \, H(x = \pm \, \xi, \, \xi, \, t)$$

In an experiment we measure Compton Form Factor ${\mathcal H}$

M. Burkardt, PRD66(2002)

M. Polyakov, P. Schweitzer, Int.J.Mod.Phys. A33 (2018)

0.01

0.005

 $r^2p(r)$ in GeV fm⁻¹

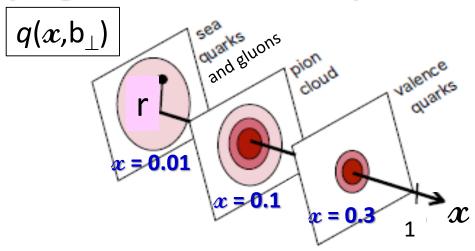
 $\mathrm{d}r\,r^2p(r)=0$

In χQSM-

r in fm

confining pion cloud

Mapping in the transverse plane



Pressure Distribution

FT of H(x, ξ =0,t)

-0.005

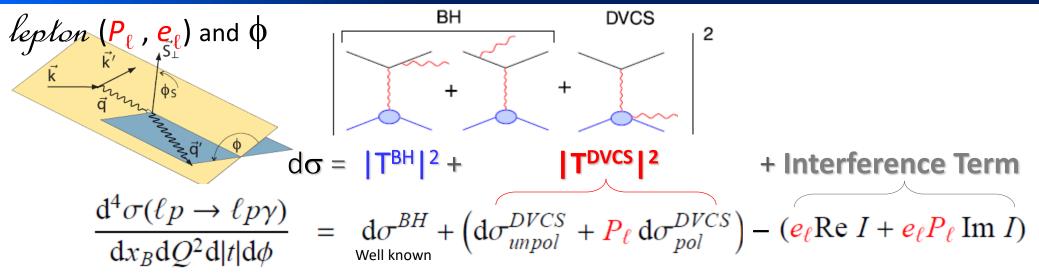
quark core repulsive 0 0.5

The amplitude DVCS at LT & LO in α_{S} (GPD f H): Real part Imaginary part

$$\mathcal{H} = \int_{t, \, \xi \, \text{fixed}}^{+1} dx \, \frac{\mathbf{H}(x, \xi, t)}{x - \xi + i \, \epsilon} = \mathcal{P} \int_{-1}^{+1} dx \, \frac{\mathbf{H}(x, \xi, t)}{x - \xi} \, - i \, \pi \, \mathbf{H}(x = \pm \, \xi, \, \xi, \, t)$$

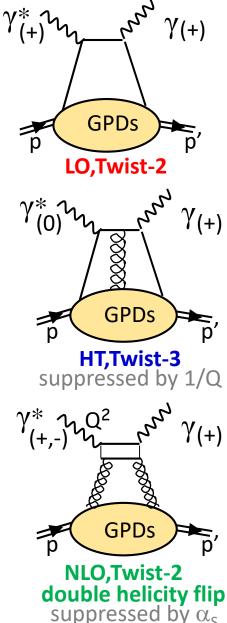
In an experiment we measure Compton Form Factor ${\cal H}$

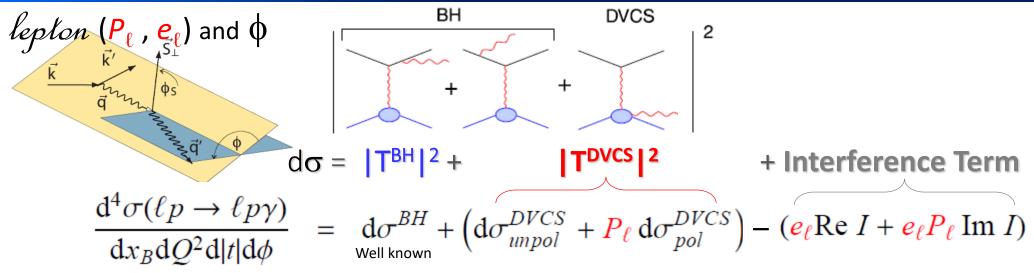
$$\operatorname{Re}\mathcal{H}(\xi,t) = \pi^{-1} \int_0^1 dx \, \frac{2x \, \operatorname{Im}\mathcal{H}(x,t)}{x^2 - \xi^2} + \Delta(t)$$



With unpolarized target:

Belitsky, Müller, Kirner, NPB629 (2002)





With unpolarized target:

$$d\sigma^{BH} \propto c_0^{BH} + c_1^{BH} \cos \phi + c_2^{BH} \cos 2\phi$$

$$d\sigma^{\leftarrow} - d\sigma^{\rightarrow}$$

With electrons and positrons

$$d\sigma^{+}-d\sigma^{-}$$

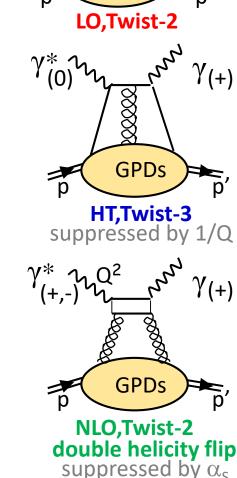
$$I \propto c_0^I + c_1^I \cos \phi + c_2^I \cos 2\phi + c_3^I \cos 3\phi$$

 $\propto c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi$

Belitsky, Müller, Kirner, NPB629 (2002)

Im
$$I \propto s_1^I \sin \phi + s_2^I \sin 2\phi$$

 $\propto s_1^{DVCS} \sin \phi$



GPDs

 γ (+)

With both μ^{+} and μ^{-} beams we can build:

• beam charge-spin sum

$$\Sigma \equiv d\sigma \stackrel{+}{\leftarrow} + d\sigma \stackrel{-}{\rightarrow}$$

2 difference

$$\Delta \equiv d\sigma \stackrel{+}{\leftarrow} - d\sigma \stackrel{-}{\rightarrow}$$

$$d\sigma^{BH} \propto c_0^{BH} + c_1^{BH} \cos \phi + c_2^{BH} \cos 2\phi$$

$$d\sigma_{unpol}^{DVCS} \propto c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi$$

$$d\sigma_{pol}^{DVCS} \propto s_1^{DVCS} \sin \phi$$

$$Re I \propto c_0^I + c_1^I \cos \phi + c_2^I \cos 2\phi + c_3^I \cos 3\phi$$

$$Im I \propto s_1^I \sin \phi + s_2^I \sin 2\phi$$

$$\sum \equiv d\sigma^{+} + d\sigma^{-} \rightarrow s_{1}^{I} \propto Im \mathcal{F}$$
and $c_{0}^{\text{DVCS}} \propto (Im\mathcal{H})^{2}$

$$\Delta \equiv d\sigma \stackrel{+}{\leftarrow} - d\sigma \stackrel{-}{\rightarrow} \rightarrow c_1^I \propto Re \ \mathcal{F}$$

$$\mathbf{F} = \mathbf{F}_1 \mathbf{H} + \xi (\mathbf{F}_1 + \mathbf{F}_2) \mathbf{H} - t/4m^2 \mathbf{F}_2 \mathbf{E}$$
for proton
$$\mathbf{F}_1 \mathbf{H}$$
at small \mathbf{x}_B
COMPASS domain

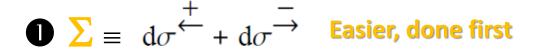
COMPASS 2016 data Selection of exclusive single photon production

Comparison between the observables given by the spectro or by CAMERA

DVCS: μ p \rightarrow μ' p γ

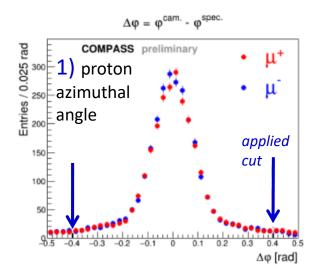
- 1) $\Delta \varphi = \varphi^{\text{cam}} \varphi^{\text{spec}}$
- 2) $\Delta p_T = p_T^{cam} p_T^{spec}$
- 3) $\Delta z_A = z_A^{cam} z_A^{Z_B and vertex}$
- 4) $M^2_{X=0} = (p_{\mu_{in}} + p_{p_{in}} p_{\mu_{out}} p_{p_{out}} p_{\gamma})^2$

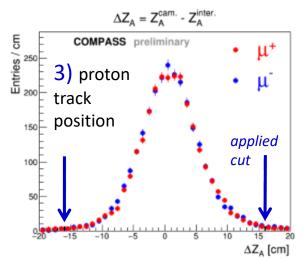
Good agreement between $\vec{\mu}$ and $\vec{\mu}$ yields Important achievement for:

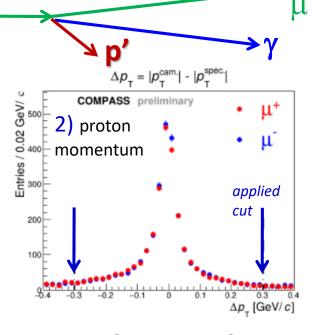


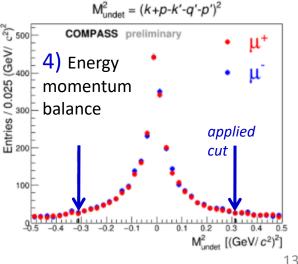
$$2 \Delta \equiv d\sigma^{+} - d\sigma^{-}$$
 Challenging, but promising

Necessity to use the same μ^+ and μ^- flux



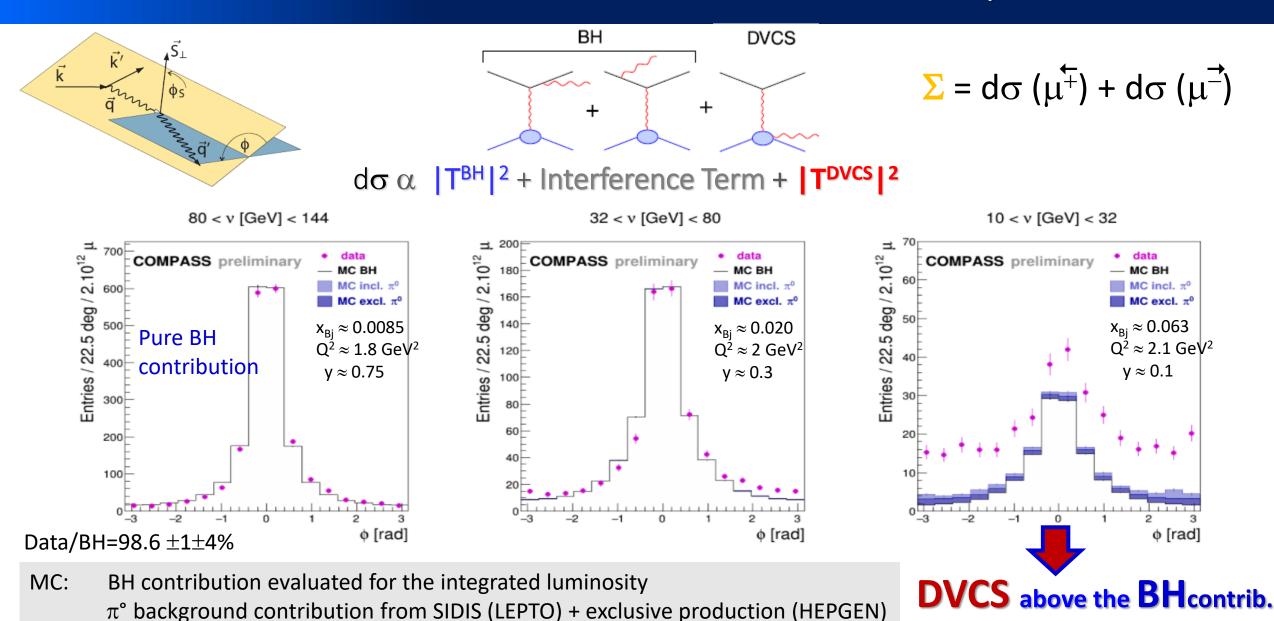






COMPASS 2016 data

DVCS+BH cross section at Eµ=160 GeV



COMPASS 2016

DVCS cross section for $10 < \upsilon < 32$ GeV

At COMPASS using polarized positive and negative muon beams:

$$\sum_{A} \equiv d\sigma \xrightarrow{+} + d\sigma \xrightarrow{-} = 2[d\sigma^{BH} + d\sigma^{DVCS}_{unpol} + \operatorname{Im} I]$$

$$= 2[d\sigma^{BH} + (c_0^{DVCS}) + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi + s_1^{I} \sin \phi + s_2^{I} \sin 2\phi]$$

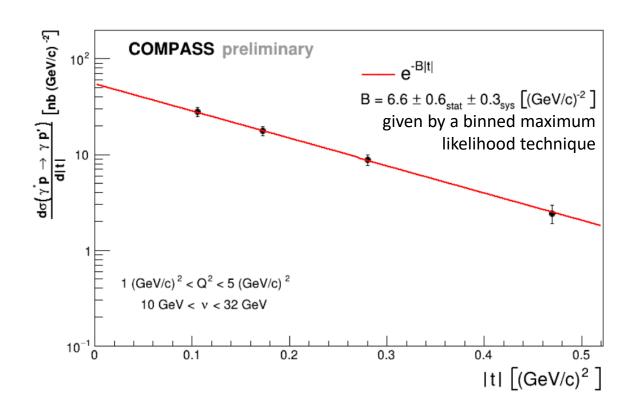
calculable can be subtracted

All the other terms are cancelled in the integration over ϕ

$$\frac{\mathrm{d}^3 \sigma_{\mathrm{T}}^{\mu p}}{\mathrm{d} Q^2 \mathrm{d} \nu dt} = \int_{-\pi}^{\pi} \mathrm{d}\phi \, \left(\mathrm{d}\sigma - \mathrm{d}\sigma^{BH}\right) \propto c_0^{DVCS}$$

$$\frac{\mathrm{d}\sigma^{\gamma^* p}}{\mathrm{d}t} = \frac{1}{\Gamma(Q^2, \nu, E_\mu)} \frac{\mathrm{d}^3 \sigma_{\mathrm{T}}^{\mu p}}{\mathrm{d}Q^2 \mathrm{d}\nu dt}$$

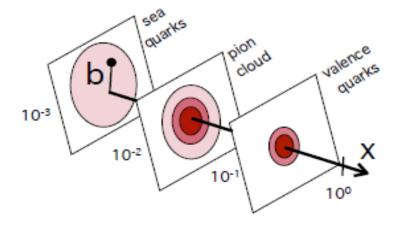
Flux for transverse virtual photons



COMPASS 12-16 Transverse extention of partons in the sea quark range

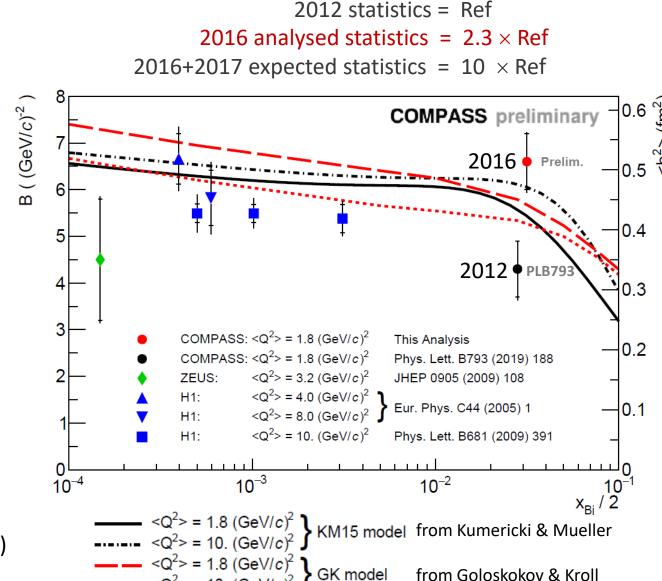
$$d\sigma^{DVCS}/dt = e^{-B|t|} = c_0^{DVCS} \propto (Im\mathcal{H})^2$$

$$\left\langle b_{\perp}^{2}(x)\right\rangle pprox 2B\left(\xi\right)$$



 3σ difference between 2012 and 2016 data

- > more advanced analysis with 2016 data
- $\succ \pi^0$ contamination with different thresholds
- \triangleright binning with 3 variables (t,Q²,v) or 4 variables (t, ϕ ,Q²,v)



Possible next steps for DVCS

- ✓ DVCS and the sum $\sum = d\sigma^{+} + d\sigma^{-}$
 - $\rightarrow c_0 \sim (\text{Im}\mathcal{H})^2$ final conclusion using all the data sets 2012, 2016, 2017
 - $\rightarrow s_1 \sim \text{Im}\mathcal{H}$

constrain on $Im\mathcal{H}$ and Transverse extension of partons

- ✓ DVCS and the difference $\triangle = d\sigma^{+} d\sigma^{-}$
 - $ightharpoonup c_1$ and constrain on $m Re \mathcal{H}$ (>0 as H1 or <0 as HERMES) for D-term and pressure distribution

mH and ReH using global fits of the world data

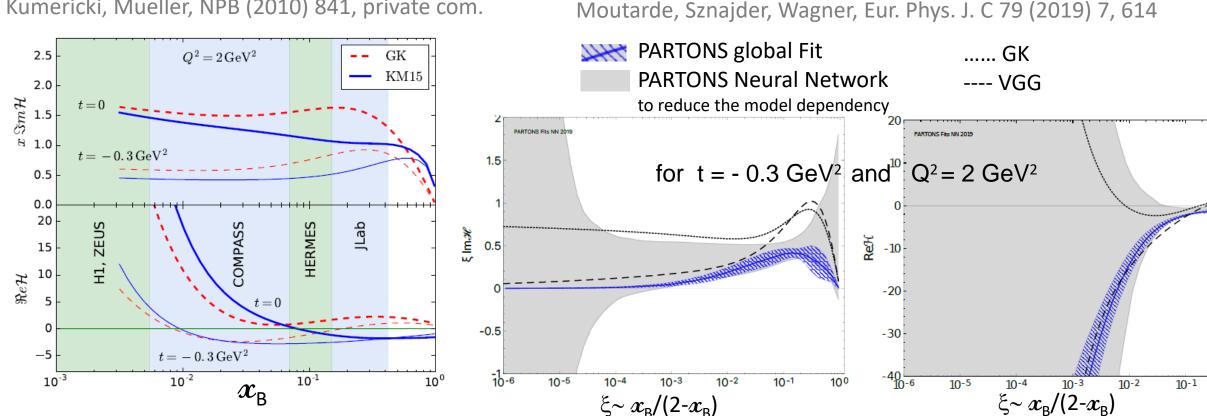
Global Fits using PARTONS framework

Compared to GK and VGG Models

Global Fit KM15

Compared to GK Model GK

Kumericki, Mueller, NPB (2010) 841, private com.



Reminder with BCA: ReH < 0 at HERMES

> 0 at H1 (but not used in PARTONS?)

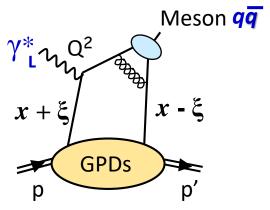
ReH is still poorly known (importance of DVCS with μ^{\pm} at COMPASS, e^{\pm} at JLab or TCS at JLab and EIC)

GPDs and Hard Exclusive Meson Production

Factorisation proven only for σ_L

The meson wave function
Is an additional non-perturbative term

Quark contribution



For Pseudo-Scalar Meson, as π^0

chiral-even GPDs: helicity of parton unchanged

$$\widetilde{\mathbf{H}}^q(x,\,\xi,\,\mathsf{t})$$
 $\widetilde{\mathbf{E}}^q(x,\,\xi,\,\mathsf{t})$

+ chiral-odd or transversity GPDs: helicity of parton changed

$$\mathbf{H}_{\mathbf{T}}^{q}(x, \xi, t)$$
 (as the transversity TMD)

related to the transverse spin structure and to the tensor charge

$$\mathbf{E}_{\mathbf{T}}^{q} = \mathbf{2} \ \mathbf{H}_{\mathbf{T}}^{q} + \mathbf{E}_{\mathbf{T}}^{q}$$
 (as the Boer-Mulders TMD)

related to the distortion of the polarized quark distribution in the transverse plane for an unpolarized nucleon

 σ_T is asymptotically suppressed by $1/Q^2$ but large contribution observed GK model: k_T of q and \overline{q} and Sudakov suppression factor are considered Chiral-odd GPDs with a twist-3 meson wave function

GPDs and Hard Exclusive π^0 Production

$$\frac{\mathrm{d}^4 \sigma_{\mu \mathrm{p}}^{\leftrightarrows}}{\mathrm{d} Q^2 \mathrm{d} \nu \mathrm{d} |t| \mathrm{d} \phi} = \Gamma(Q^2, \nu, E_{\mu}) \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\leftrightarrows}}{\mathrm{d} |t| \mathrm{d} \phi}$$

$$\frac{\mathrm{d}^{4}\sigma_{\mu p}^{\leftrightarrows}}{\mathrm{d}Q^{2}\mathrm{d}\nu\mathrm{d}|t|\mathrm{d}\phi} = \Gamma(Q^{2}, \nu, E_{\mu}) \frac{\mathrm{d}^{2}\sigma_{\gamma^{*}p}^{\leftrightarrows}}{\mathrm{d}|t|\mathrm{d}\phi} \qquad \frac{\mathrm{d}^{2}\sigma_{\gamma^{*}p}^{\leftrightarrows}}{\mathrm{d}|t|\mathrm{d}\phi} = \frac{1}{2\pi} \left[\frac{\mathrm{d}\sigma_{T}}{\mathrm{d}t} + \epsilon \frac{\mathrm{d}\sigma_{L}}{\mathrm{d}t} + \epsilon \cos\left(2\phi\right) \frac{\mathrm{d}\sigma_{TT}}{\mathrm{d}t} + \epsilon \frac{\mathrm{d}\sigma_{LT}}{\mathrm{d}t} + \epsilon \cos\left(2\phi\right) \frac{\mathrm{d}\sigma_{TT}}{\mathrm{d}t} + \epsilon \cos\left(2\phi\right) \frac{\mathrm{d}\sigma_{TT}}$$

With both $\stackrel{\leftarrow}{\mu}$ and $\stackrel{\rightarrow}{\mu}$ beams we can build:

• the beam charge-spin sum, or spin-independent cross section

$$\sum \equiv \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} = \frac{1}{2} \left(\frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\leftarrow}}{\mathrm{d}t \mathrm{d}\phi} + \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}t \mathrm{d}\phi} \right)$$

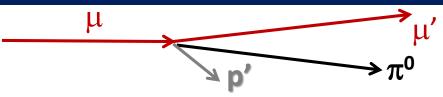
2 the difference

$$\Delta \equiv \left(\frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\leftarrow}}{\mathrm{d} t \mathrm{d} \phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d} t \mathrm{d} \phi}\right)$$

$$\begin{split} &\sum \equiv \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} = \frac{1}{2} \Big(\frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\leftarrow}}{\mathrm{d}t \mathrm{d}\phi} + \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}t \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} = \frac{1}{2} \Big(\frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\leftarrow}}{\mathrm{d}t \mathrm{d}\phi} + \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}t \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}t \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}t \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}t \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}t \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}t \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}t \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}t \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}t \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}}{\mathrm{d}^2 \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} - \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big) \\ &= \mathbf{d}^2 \frac{\mathrm{d}^2 \sigma_{\gamma^* \mathrm{p}}^{\rightarrow}}{\mathrm{d}^2 \mathrm{d}\phi} \Big$$

Exclusive π^0 production on unpolarized proton

Comparison between the observables given by the spectro or by CAMERA



$$\mu p \rightarrow \mu' p \pi^0$$

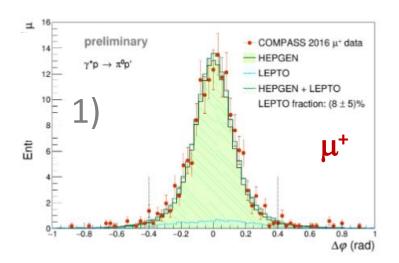
- 1) $\Delta \varphi = \varphi^{\mathrm{cam}} \varphi^{\mathrm{spec}}$
- 2) $\Delta p_T = p_T^{cam} p_T^{spec}$

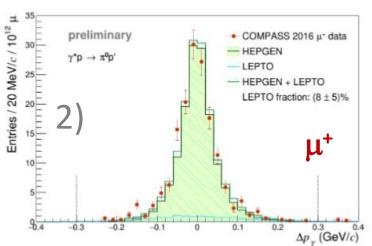
Good description of the data with MC including

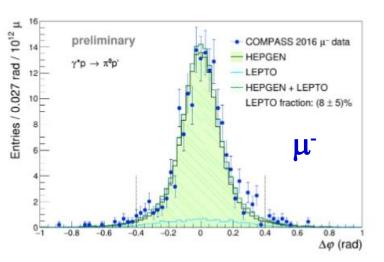
Exclusive π^0 production (HEPGEN)

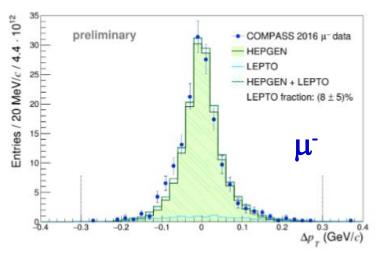
+ Semi-inclusive π^0 production (LEPTO)

Good agreement between $\vec{\mu}^{+}$ and $\vec{\mu}^{-}$ yields









COMPASS 2012 - 16 spin-independent cross section for exclusive π^0

 $\mu^{\pm} p \rightarrow \mu^{\pm} \pi^{0} p$ μ^{\pm} beams with opposite polarization

$$\frac{1}{2} \left(\frac{d^2 \sigma^+}{dt d\phi_{\pi}} + \frac{d^2 \sigma^-}{dt d\phi_{\pi}} \right) = \frac{1}{2\pi} \left[\left(\epsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} \right) + \epsilon \cos 2\phi_{\pi} \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon (1+\epsilon)} \cos \phi_{\pi} \frac{d\sigma_{LT}}{dt} \right]$$

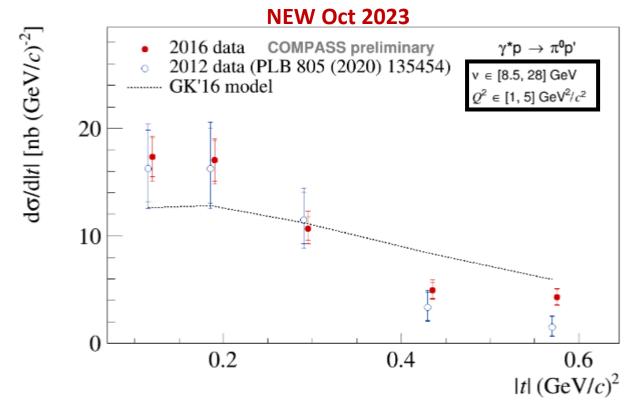
COMPASS $\langle x_B \rangle = 0.10$ ϵ close to 1

$$\frac{d\sigma_L}{dt} \propto \left| \left\langle \tilde{H} \right\rangle \right|^2 - \frac{t'}{4m^2} \left| \left\langle \tilde{E} \right\rangle \right|^2$$

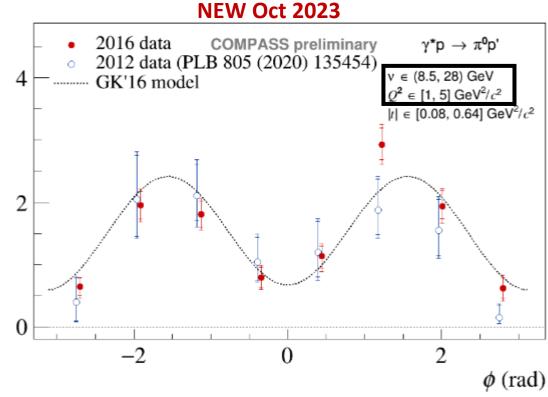
$$\frac{d\sigma_T}{dt} \propto \left| \langle H_T \rangle \right|^2 - \frac{t'}{8m^2} \left| \langle \bar{E}_T \rangle \right|^2$$

$$\frac{\sigma_{TT}}{dt} \propto \frac{t'}{16m^2} \left| \langle \bar{E}_T \rangle \right|^2$$

$$\frac{\sigma_{LT}}{dt} \propto \frac{\sqrt{-t'}}{2m} \operatorname{Re}\left[\langle H_T \rangle^* \langle \tilde{E} \rangle\right]$$







Models: **GK** Kroll Goloskokov EPJC47 (2011)

Also **GGL**: Golstein Gonzalez Liuti PRD91 (2015)

COMPASS 2016

spin-independent cross section for exclusive π^0

 $\mu^{\pm} p \rightarrow \mu^{\pm} \pi^{0} p$ μ^{\pm} beams with opposite polarization

$$\frac{1}{dt}\left(\frac{d^2\sigma^+}{dtd\phi_\pi} + \frac{d^2\sigma^-}{dtd\phi_\pi}\right) = \frac{1}{2\pi}\left[\left(\epsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt}\right) + \epsilon\cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)}\cos\phi_\pi \frac{d\sigma_{LT}}{dt}\right]$$

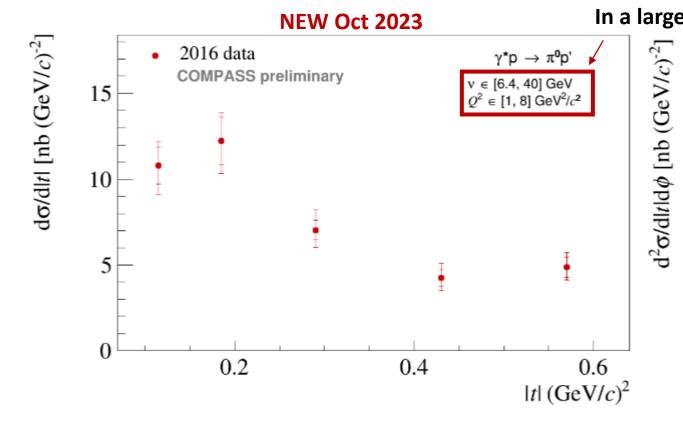
COMPASS $\langle x_B \rangle = 0.13$ ϵ close to 1

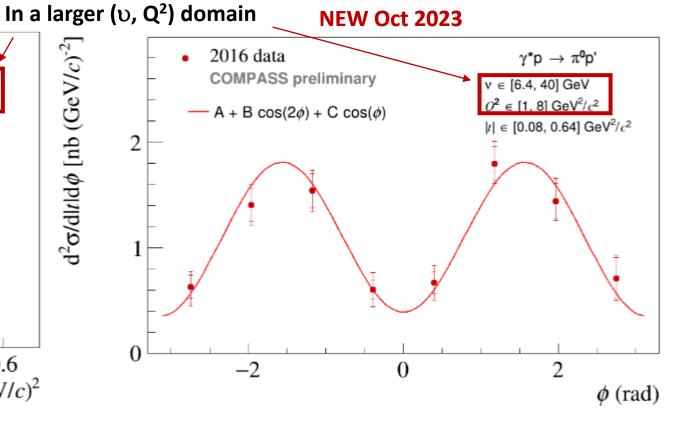
$$\frac{d\sigma_L}{dt} \propto \left| \langle \tilde{H} \rangle \right|^2 - \frac{t'}{4m^2} \left| \langle \tilde{E} \rangle \right|^2$$

$$\frac{d\sigma_T}{dt} \propto \left| \langle H_T \rangle \right|^2 - \frac{t'}{8m^2} \left| \langle \bar{E}_T \rangle \right|^2$$

$$\frac{\sigma_{TT}}{dt} \propto \frac{t'}{16m^2} \left| \langle \bar{E}_T \rangle \right|^2$$

$$\frac{\sigma_{LT}}{dt} \propto \frac{\sqrt{-t'}}{2m} \operatorname{Re}\left[\langle H_T \rangle^* \langle \tilde{E} \rangle\right]$$





COMPASS 2016

spin-independent cross section for exclusive π^0

opposite polarization

$$\mu^{\pm} \mathbf{p} \rightarrow \mu^{\pm} \pi^{0} \mathbf{p}$$

$$\mu^{\pm} \text{ beams with opposite polarization}$$

$$\frac{1}{2} \left(\frac{d^{2}\sigma^{+}}{dt d\phi_{\pi}} + \frac{d^{2}\sigma^{-}}{dt d\phi_{\pi}} \right) = \frac{1}{2\pi} \left[\left(\epsilon \frac{d\sigma_{L}}{dt} + \frac{d\sigma_{T}}{dt} \right) + \epsilon \cos 2\phi_{\pi} \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_{\pi} \frac{d\sigma_{LT}}{dt} \right]$$

$$\frac{d\sigma_L}{dt} \propto \left| \langle \tilde{H} \rangle \right|^2 - \frac{t'}{4m^2} \left| \langle \tilde{E} \rangle \right|^2 \qquad \frac{d\sigma_T}{dt} \propto \left| \langle H_T \rangle \right|^2 - \frac{t'}{8m^2} \left| \langle \bar{E}_T \rangle \right|^2 \qquad \frac{\sigma_{TT}}{dt} \propto \frac{t'}{16m^2} \left| \langle \bar{E}_T \rangle \right|^2 \qquad \frac{\sigma_{LT}}{dt} \propto \frac{\sqrt{-t'}}{2m} \operatorname{Re} \left[\langle H_T \rangle^* \langle \tilde{E} \rangle \right]$$

$$\frac{d\sigma_T}{dt} \propto \left| \langle H_T \rangle \right|^2 - \frac{t'}{8m^2} \left| \langle \bar{E}_T \rangle \right|^2$$

$$\frac{\sigma_{TT}}{dt} \propto \frac{t'}{16m^2} \left| \langle \bar{E}_T \rangle \right|^2$$

$$\frac{\sigma_{LT}}{dt} \propto \frac{\sqrt{-t'}}{2m} \operatorname{Re} \left[\langle H_T \rangle^* \langle \tilde{E} \rangle \right]$$

$$v \in [6.4, 40] \text{ GeV}^2$$

COMPASS

ε close to 1

NEW Oct 2023

 $|t| \in [0.08, 0.64] \text{ GeV}^2/c^2$

$$\left\langle \frac{\sigma_{\mathrm{T}}}{|t|} + \epsilon \frac{\sigma_{\mathrm{L}}}{|t|} \right\rangle = (6.9 \pm 0.3_{\mathrm{stat}} \pm 0.8_{\mathrm{syst}}) \frac{\mathrm{nb}}{(\mathrm{GeV}/c)^2}$$

$$\left\langle \frac{\sigma_{\rm TT}}{|t|} \right\rangle = (-4.5 \pm 0.5_{\rm stat} \pm 0.2_{\rm syst}) \frac{\rm nb}{({\rm GeV}/c)^2}$$

$$\left\langle \frac{\sigma_{\rm LT}}{|t|} \right\rangle = (0.06 \pm 0.2_{\rm stat} \pm 0.1_{\rm syst}) \frac{\rm nb}{({\rm GeV}/c)^2}$$

 σ_{TT} is negative and large comparatively to $\sigma_{T} + \varepsilon \sigma_{I}$ \rightarrow impact of \overline{E}_{T}

 σ_{IT} rather small

We will present soon the evolution in 3 bins in varphi and 4 bins in Q^2

The 2017 data set will still increase the statistics

Lessons on experiments with data collected with ℓ + and ℓ - beams

For ex:
$$\sigma^{\pm} = (\varepsilon \sigma_{L} + \sigma_{T}) + a \cos 2\phi \sigma_{TT} + b \cos \phi \sigma_{LT} + c \sin \phi \sigma_{LT}$$

With polarized electron beams we change continously from one to the other polarization to build directly only 1 observable: $\frac{1}{1}$ asymmetry = $\frac{1}{1}$ (N+ + N-) gives the $\frac{1}{1}$ directly only 1 observable electron beams we change continously from one to the other polarization to build directly only 1 observable:

Richness but complexity dealing with runs with ℓ + and ℓ - beams \rightarrow we build $\underline{4}$ correlated observables or $\underline{4}$ cross sections:

- σ^+ σ^- Constant, $\cos \phi$, $\cos 2 \phi$ and $\sin \phi$ terms σ^- Constant, $\cos \phi$, $\cos 2 \phi$ and $\sin \phi$ terms $\sigma^+ + \sigma^-$ Constant, $\cos \phi$, $\cos 2 \phi$ terms
- $\sigma^+ \sigma^- \rightarrow \sin \phi \text{ term}$
- ✓ Necessity of accurate acceptance and efficiency determination
- ✓ Requirement of detector stability for ℓ + and ℓ runs not taken at the same time
- ✓ Background depending on the lepton flux (recommendation to use the same lepton flux)
- ✓ Relative positions of background (mainly electrons) and signal are not located at the same place in the detectors with ℓ + and ℓ beams → precise MC description
- ✓ Radiative corrections of opposite sign for ℓ+ and ℓ- for the 2 photon exchange (see Andrei Afanasev....)

mH and ReH using global fits of the world data

