

*DVCS and HEMP  
at COMPASS experiment  
for GPD studies*

**Takahiro Iwata  
On behalf of COMPASS Collaboration**



# Outline

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- Physics motivations
- GPD, DVCS, HEMP
- COMPASS at CERN
- DVCS measurements at COMPASS
- 2016 data for exclusive photon production
- 2012-16 data Transverse extension of partons
- GPD and HEMP
- Transverse-target spin asymmetries in HEMP of  $\rho$  and  $\omega$
- SDMEs in HEMP of  $\rho$  and  $\omega$
- Exclusive  $\pi^0$  production cross section
- Summary

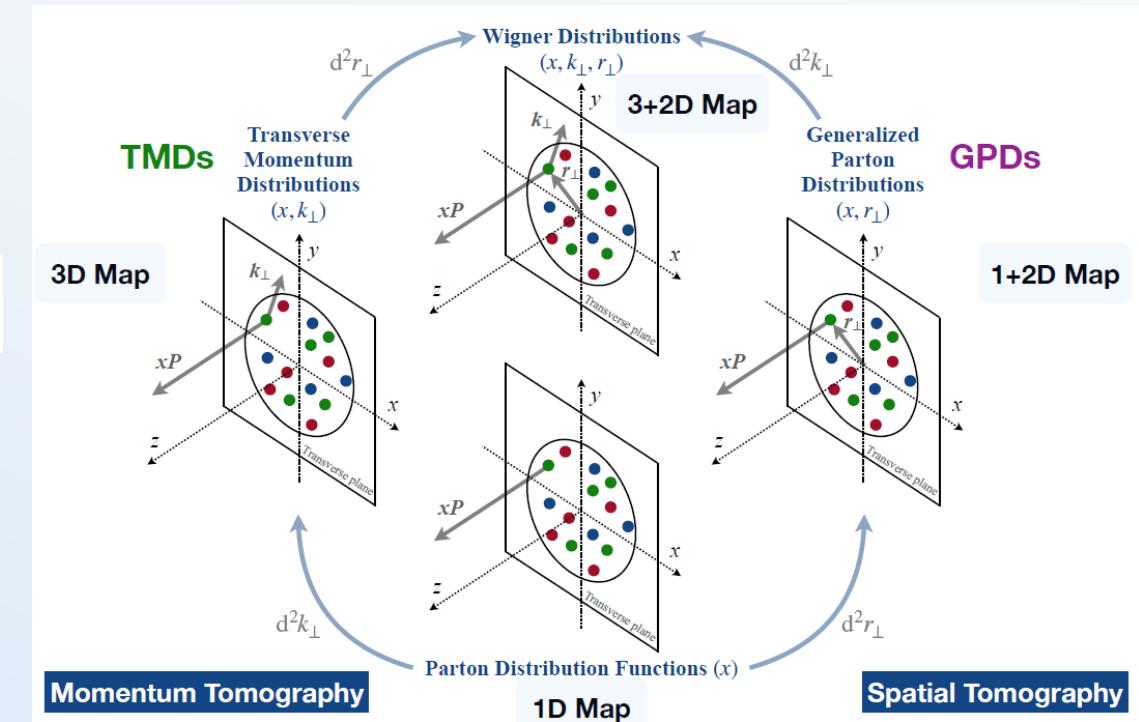
# Physics motivations

We are interested in ;

- How are hadrons made up with the partons?
- What is the origin of nucleon spin?
- How is the nucleon spin made up with parton's spin and OAMs? (Spin puzzle)

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$

- How is the nucleon spin correlated with the motion of partons?
- What is the relation between Bjorken-x and the transverse position of the partons?
- How does the spin influence the position distribution?



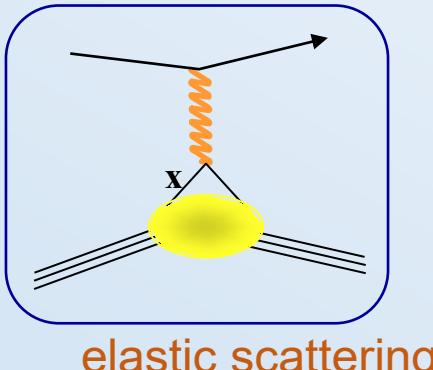
courtesy of Yu-Hsiang Lien, COMPASS (DIS2021)

One of the key concepts to solve the problems is the Generalized Parton Distributions (GPDs)

# Generalized Parton Distributions

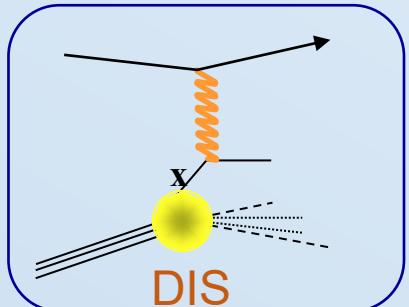
GPD is important concept merging the Form Factor (FF) and the PDF

- Form Factor probes transverse position of partons



elastic scattering

- PDF probes longitudinal parton momentum ( $x$ )



DIS

- GPD provides correlation between  $x$  and the position of the partons

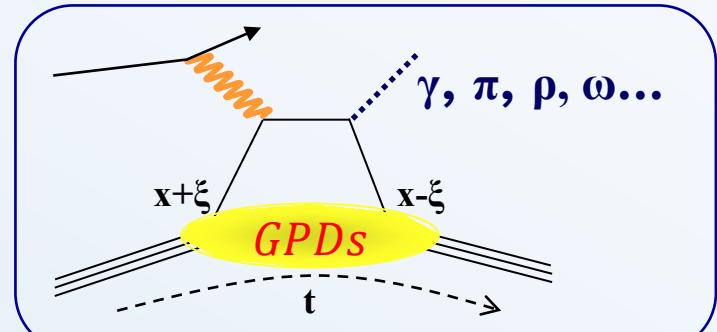
- forward limit gives PDF,

$$H(x, 0, 0) = q(x)$$

- moments of GPDs are form factors, e.g.

- impact-parameter representation:

- Ji's sum rule :



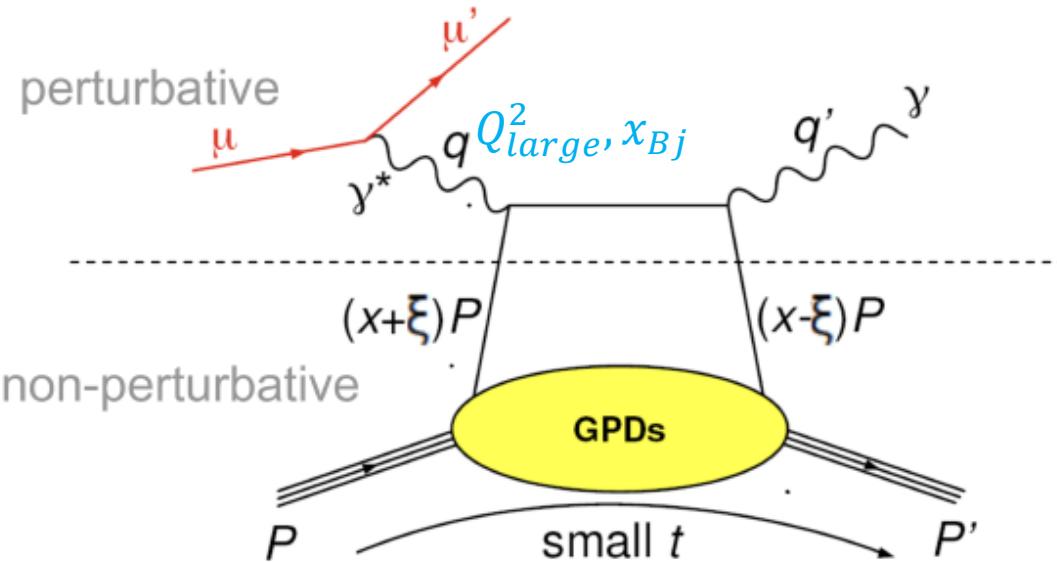
hard exclusive productions

$$\int dx H(x, \xi, t) = F_1(t)$$

$$q_f(x, b_\perp) = \frac{1}{(2\pi)^2} \int d^2 \Delta_\perp e^{-ib_\perp \cdot \Delta_\perp} H^f(x, 0, -\Delta_\perp)$$

$$J_f = \frac{1}{2} \int_{-1}^1 dx x [H^f(x, 0, t \rightarrow 0) + E^f(x, , t \rightarrow 0)]$$

# Deeply Virtual Compton Scattering (DVCS)



- ▶  $q = (p_\mu - p_{\mu'})$ : 4-momentum of virtual photon
- ▶  $Q^2 = -q^2$ : virtual photon virtuality
- ▶  $t = (p_P - p_{P'})^2$ : 4-momentum transfer to nucleon squared
- ▶  $x$ : average longitudinal momentum fraction
- ▶  $\xi$ : half of longitudinal momentum fraction transfer

DVCS: most simple reaction  
in order to study GPDs

4 (chiral-even) GPDs for each  
quark flavor in LO and leading twist

No Nucleon spin flip	With Nucleon spin flip
$H^q(x, \xi, t)$	$E^q(x, \xi, t)$
$\tilde{H}^q(x, \xi, t)$	$\tilde{E}^q(x, \xi, t)$

- **skewness**  $\xi \approx x_B / (2x_B)$  in Bjorken limit  
( $Q^2$  large &  $x_B, t$  fixed)

# Transverse imaging and Pressure distribution with GPD

In experiments, GPD is accessed through  
**Compton Form Factor** (CFF):

**CFF** convolution hard process  $\otimes$  GPD

$$\mathcal{H}(\xi, t) = \sum_f e_f^2 \int_{-1}^{+1} dx \left\{ \frac{1}{\xi - x - i\varepsilon} - \frac{1}{\xi + x - i\varepsilon} \right\} H^f(x, \xi, t)$$

$t, \xi$  fixed

with complex integration

**Imaginary part**

$$\text{Im}\mathcal{H}(\xi, t) = \sum_f e_f^2 \pi [H^f(x = +\xi, \xi, t) - H^f(x = -\xi, \xi, t)]$$

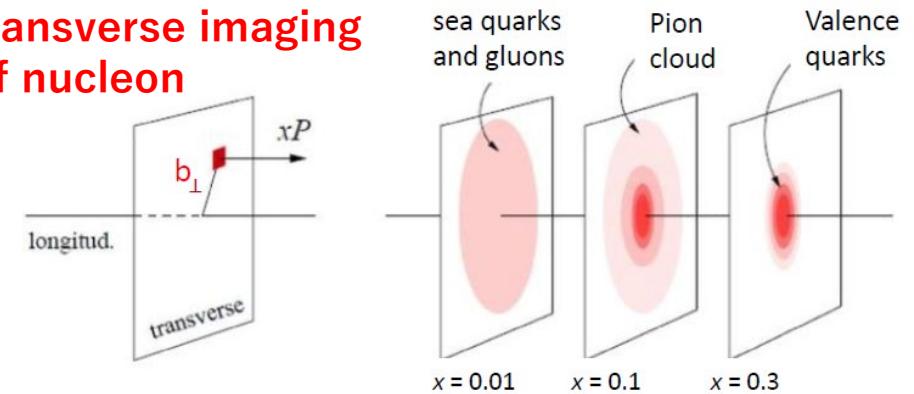
**Real part**

$$\text{Re}\mathcal{H}(\xi, t) = \sum_f e_f^2 \mathcal{P} \int_{-1}^{+1} dx \left[ \frac{1}{x - \xi} - \frac{1}{x + \xi} \right] H^f(x, \xi, t)$$

dispersion relation

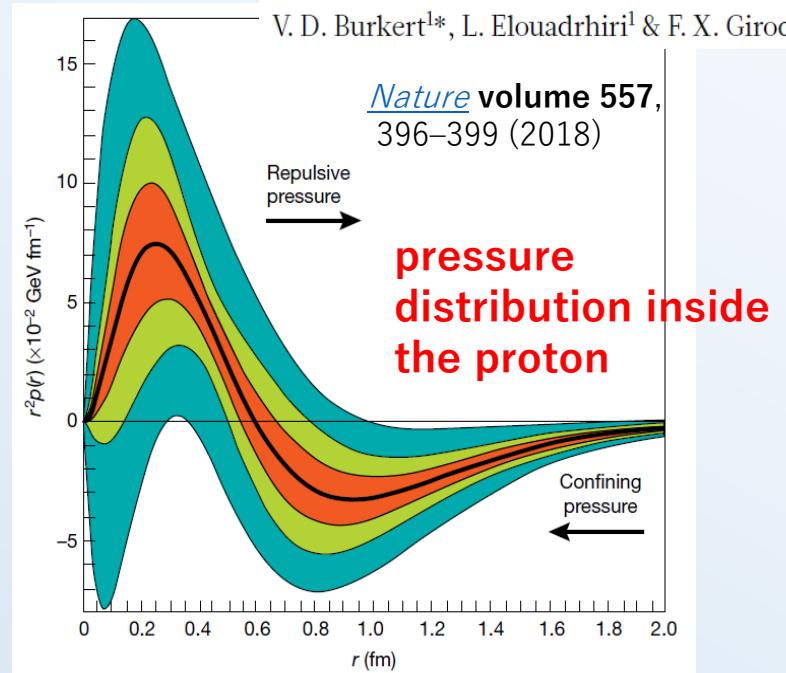
$$\text{Re}\mathcal{H}(\xi, t) = \mathcal{P} \int_{-1}^{+1} dx \left\{ \frac{1}{\xi - x} - \frac{1}{\xi + x} \right\} \text{Im}\mathcal{H}(\xi, t) + D(t)$$

**transverse imaging  
of nucleon**

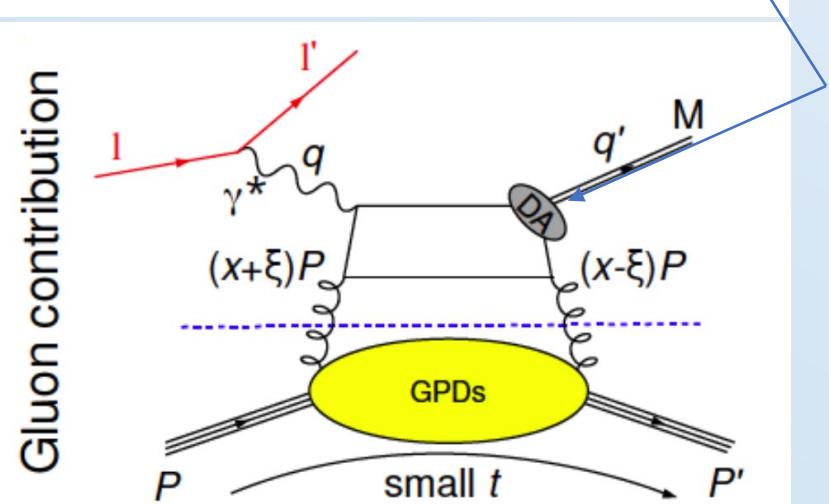
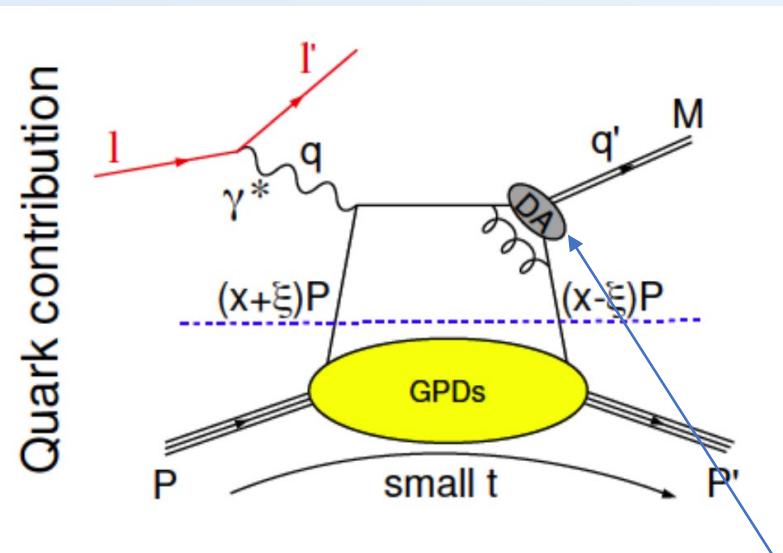


V. D. Burkert<sup>1\*</sup>, L. Elouadrhiri<sup>1</sup> & F. X. Girod<sup>1</sup>

*Nature* volume 557,  
396–399 (2018)



# Hard Exclusive Meson Production (HEMP)



- HEMP is alternatively important in GPD studies
- take account of the meson structure
- HEMP allows to give chiral-odd GPDs

$$H_T, E_T, \tilde{E}_T \text{ and } \bar{E}_T \equiv 2\tilde{H}_T + E_T$$

- Sensitive to gluon GPDs (same order in  $\alpha_s$ )  
Diehl, Vinnikov, Phys. Lett. B 609 (2005) 286
- Provide different flavor combinations for different mesons

**Distribution Amplitude:  
structure of the meson**

- We look at transverse-spin asymmetries, spin-density matrix elements for exclusive vector meson production, and cross section for exclusive  $\pi^0$  production

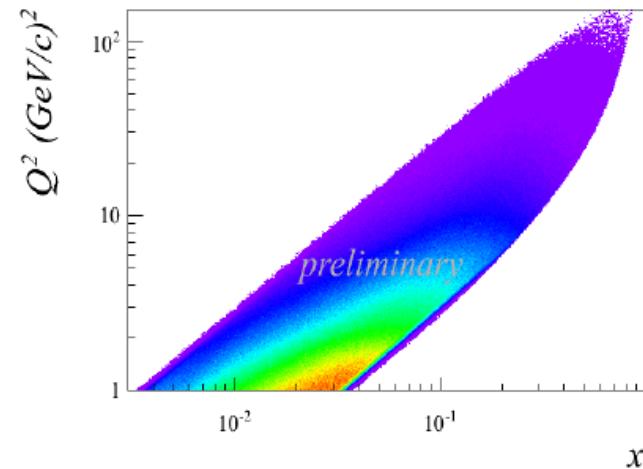
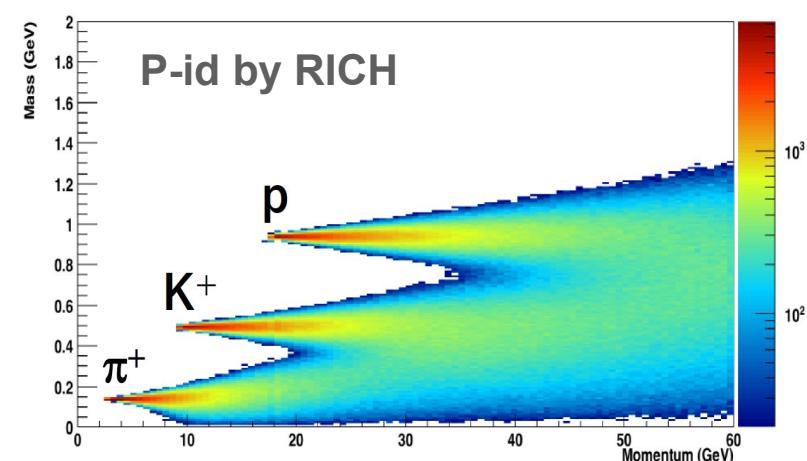
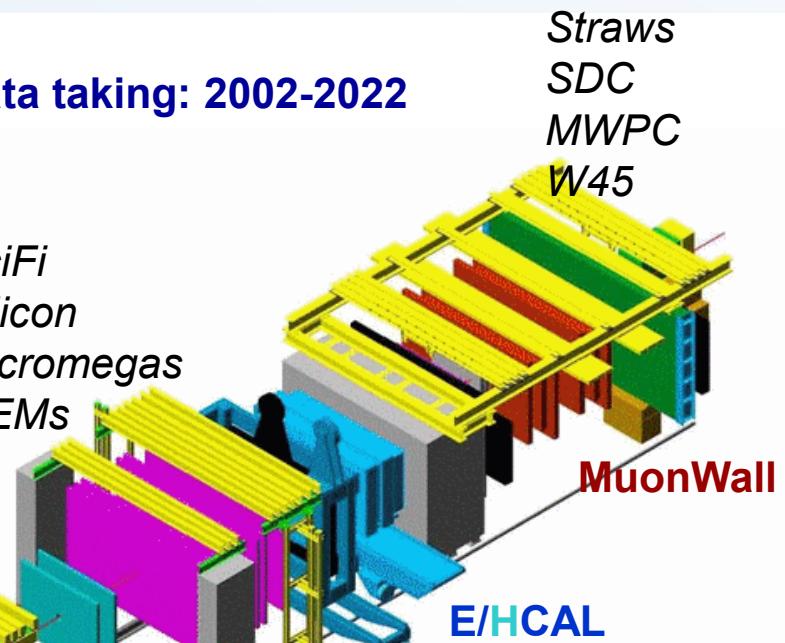
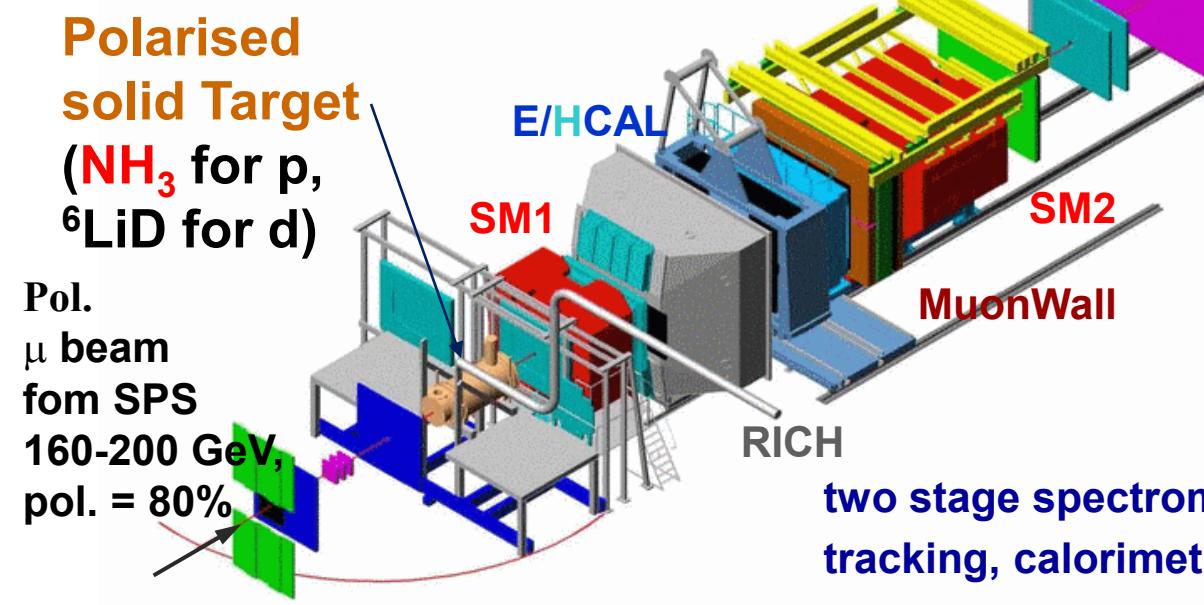
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# *COMPASS*

# COMPASS at CERN



data taking: 2002-2022



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# *DVCS*

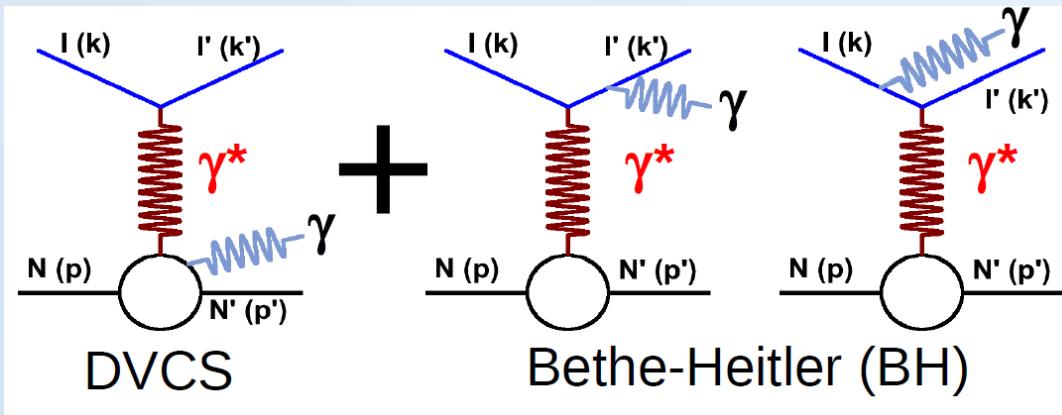
# DVCS measurements @ COMPASS



- study exclusive photon production for DVCS

$$\mu + p \rightarrow \mu' + p' + \gamma$$

- Bethe-Heitler(BH) process also gives the same final state

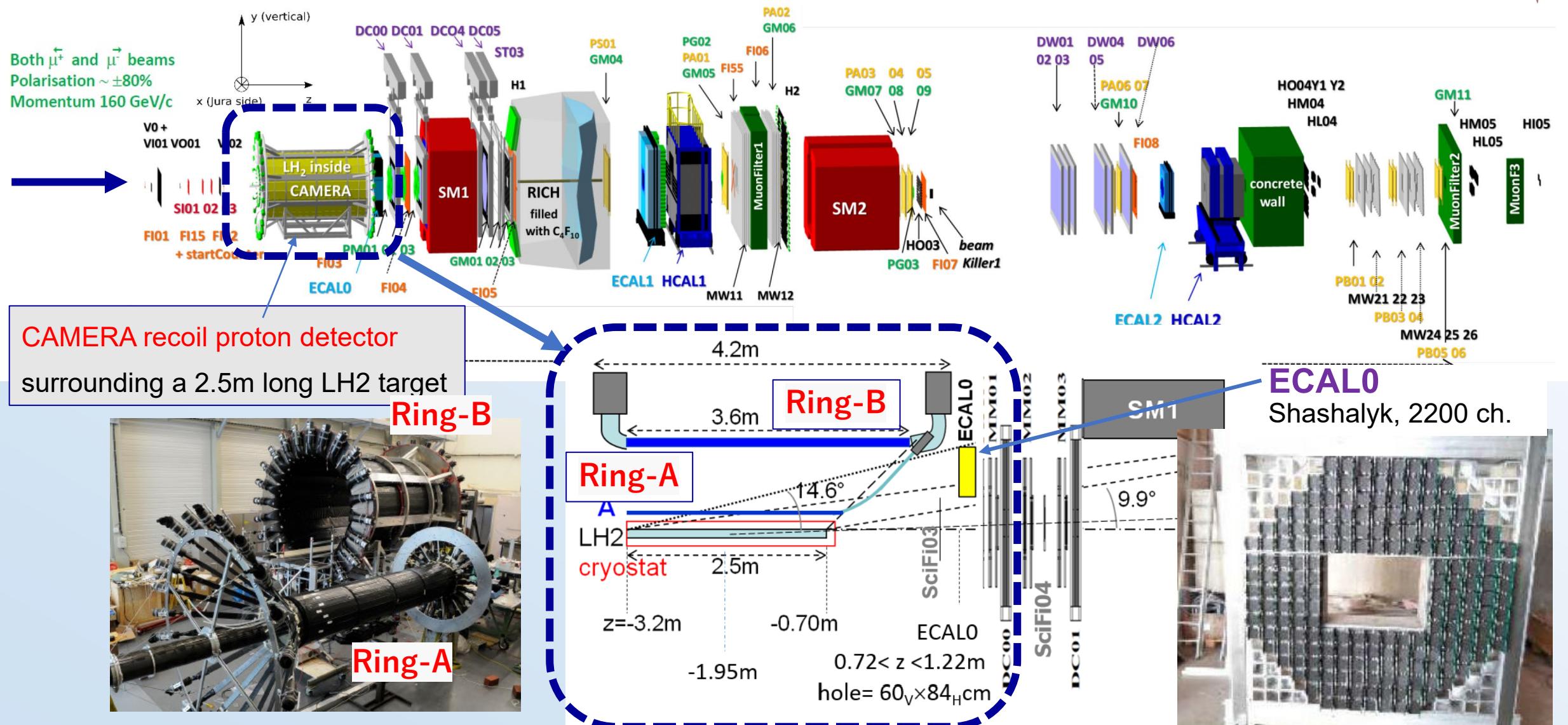


$$\sigma(\mu p \rightarrow \mu' p' \gamma) = \sigma_{DVCS} + \sigma_{BH} + \sigma_{Int.}$$

Dedicated data taking for DVCS (and HEMP)

- 2012 pilot run for 4 weeks
  - Analysis finished and published
- Long runs in 2016/17
  - 2x6 months
  - 2016+2017 statistics: 9x 2012
  - Analysis on going → preliminary results
- 2016 data will be presented in this talk

# Dedicated Setup for DVCS & HEMP @ COMPASS



# Access to CFFs @ COMPASS



opposite charge and spin states for  $\mu$ -beam

160GeV     $\mu^{+\leftarrow}$     &     $\mu^{-\rightarrow}$

$$d\sigma = d\sigma_{UU}^{\text{BH}} + (d\sigma_{UU}^{\text{DVCS}} + P_\mu d\sigma_{LU}^{\text{DVCS}}) + e_\mu (d\sigma_{UU}^{\mathcal{I}} + P_\mu d\sigma_{LU}^{\mathcal{I}})$$

## [1] beam charge & spin sum

$$\mathcal{S}_{CS,U} = d\sigma^{\leftarrow} + d\sigma^{\rightarrow} = 2 \left( d\sigma_{UU}^{\text{BH}} + d\sigma_{UU}^{\text{DVCS}} - |P_\mu| d\sigma_{LU}^{\mathcal{I}} \right)$$

easier, to be done first

$$c_0^{\text{DVCS}} \propto (\text{Im } \mathcal{H})^2$$

$$s_1^{\mathcal{I}} \propto \text{Im} (F_1 \mathcal{H})$$

in the COMPASS kinematics

small  $x_B$  and  $|t|$ , for proton target ( $F_1 > F_2$ )

## [2] beam charge & spin difference

$$\mathcal{D}_{CS,U} = d\sigma^{\leftarrow} - d\sigma^{\rightarrow} = 2 (-|P_\mu| d\sigma_{LU}^{\text{DVCS}} + |e_\mu| d\sigma_{LU}^{\mathcal{I}})$$

BH cancels

challenging, but promising

$$c_0^{\mathcal{I}}, c_1^{\mathcal{I}} \propto \text{Re} (F_1 \mathcal{H})$$

$$s_k^i = \sin(k\phi_{\gamma\gamma^*})$$

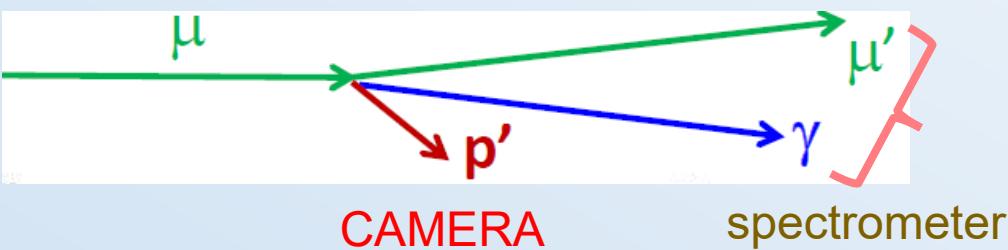
$$c_k^i = \cos(k\phi_{\gamma\gamma^*})$$

$i$ : DVCS/BH/I

# 2016 data Exclusive photon production



information given by the spectrometer  
and also CAMERA



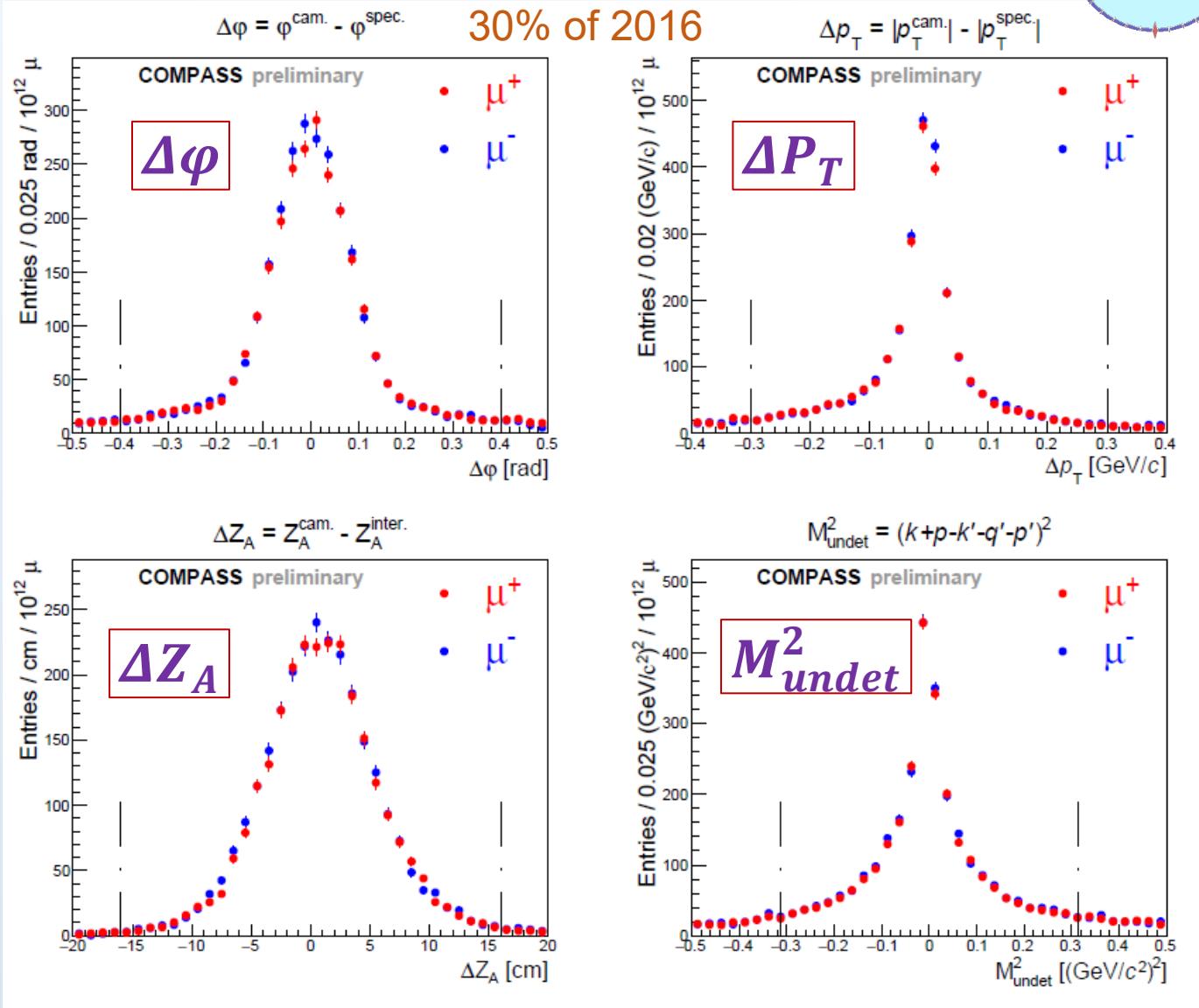
$$\Delta\varphi = \varphi^{CAM} - \varphi^{SPEC}$$

$$\Delta P_T = P_T^{CAM} - P_T^{SPEC}$$

$$\Delta Z_A = Z_A^{CAM} - Z_A^{Inter.}$$

$$M_{undet}^2 = (k + p - k' - q' - p')^2$$

exclusive events surely selected

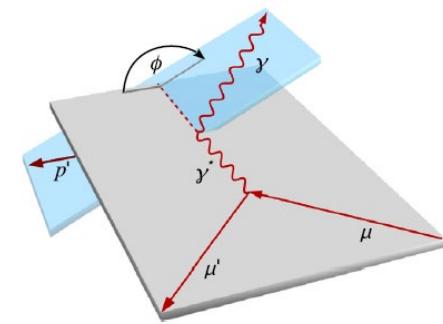


# 2016 data Charge Spin sum ; $\phi$ distribution

$$\Sigma = d\sigma(\mu^+) + d\sigma(\mu^-)$$

30% of 2016 data analyzed

$v$ : virtual photon energy



$$\phi = \phi_{\gamma^*\gamma}$$

high  $v$

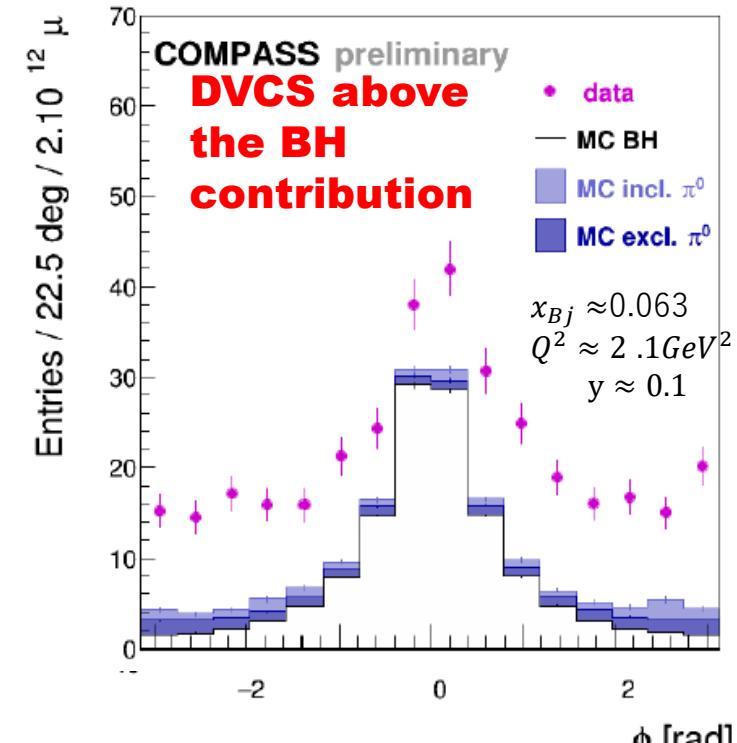
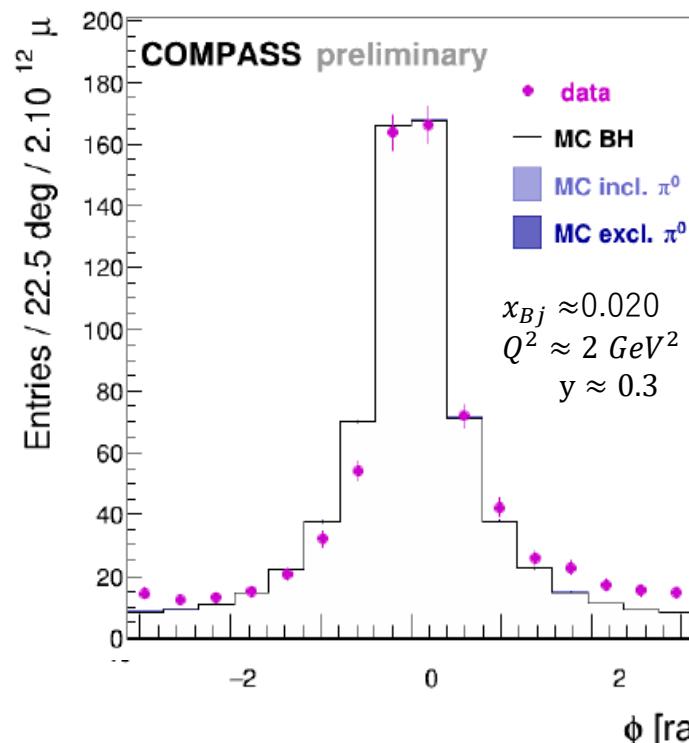
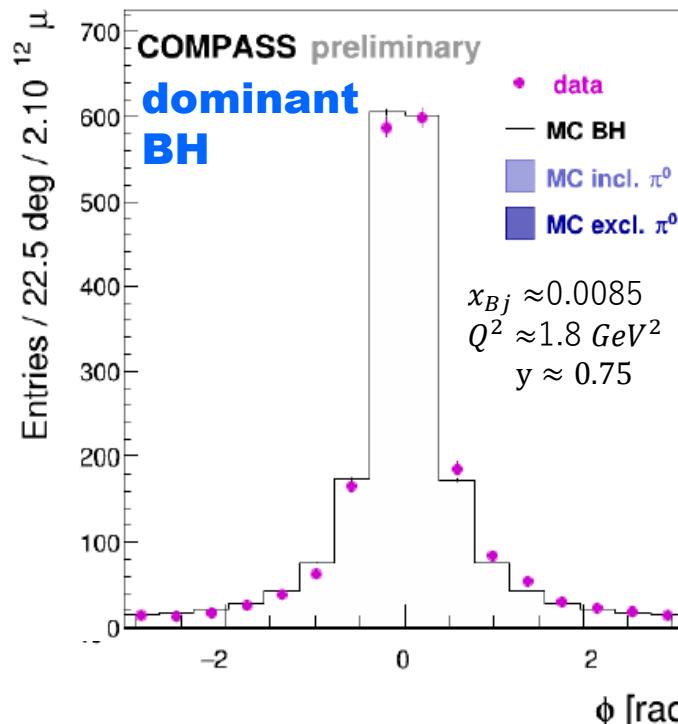
middle  $v$

low  $v$

$80 < v [\text{GeV}] < 144$

$32 < v [\text{GeV}] < 80$

$10 < v [\text{GeV}] < 32$



# 2016 data DVCS cross section



DVCS cross section evaluated from  $10 < \nu < 32$  GeV data

$$d\sigma^I \propto (s_1^I \sin \phi_{\gamma^*\gamma} + s_2^I \sin 2\phi_{\gamma^*\gamma})$$

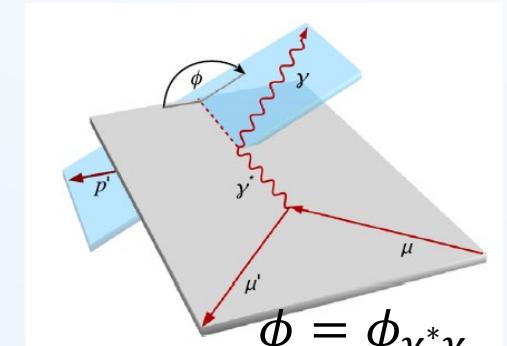
$$\mathcal{S}_{CS,U} \equiv d\sigma^{\leftarrow} + d\sigma^{\rightarrow} = 2(d\sigma^{BH} + d\sigma_{unpol}^{DVCS} - |P_\mu| d\sigma^I)$$

calculable  
(well known)

$$d\sigma_{unpol}^{DVCS}$$

$$\propto (c_0^{DVCS} + c_1^{DVCS} \cos \phi_{\gamma^*\gamma} + c_2^{DVCS} \cos 2\phi_{\gamma^*\gamma})$$

cancellation



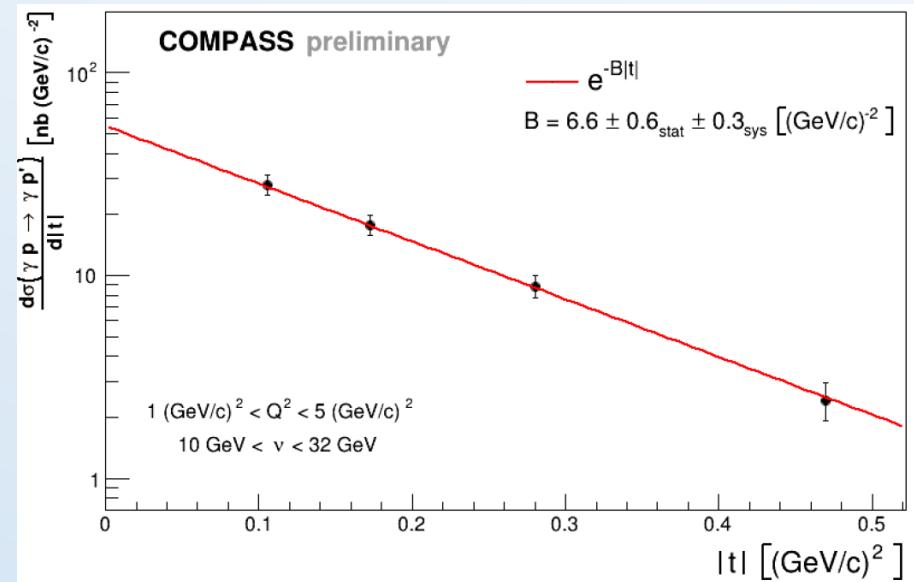
- subtract BH contribution and integrating over  $\phi$

$$\frac{d^3\sigma_T^{\mu p}}{dQ^2 d\nu dt} = \int_{-\pi}^{\pi} d\phi_{\gamma^*\gamma} (d\sigma - d\sigma^{BH}) \propto c_0^{DVCS}$$

- cross section for virtual photon

$$\frac{d\sigma^{\gamma^* p}}{d|t|} = \frac{1}{\Gamma(Q^2, \nu, E_\mu)} \frac{d^3\sigma_T^{\mu p}}{dQ^2 d\nu dt}$$

flux



# 2012-16 data Transverse extension of partons



$$c_0^{DVCS} \approx (\text{Im } \mathcal{H})^2$$

in COMPASS with  $x_{Bj} = 0.06$

Impact-parameter representation

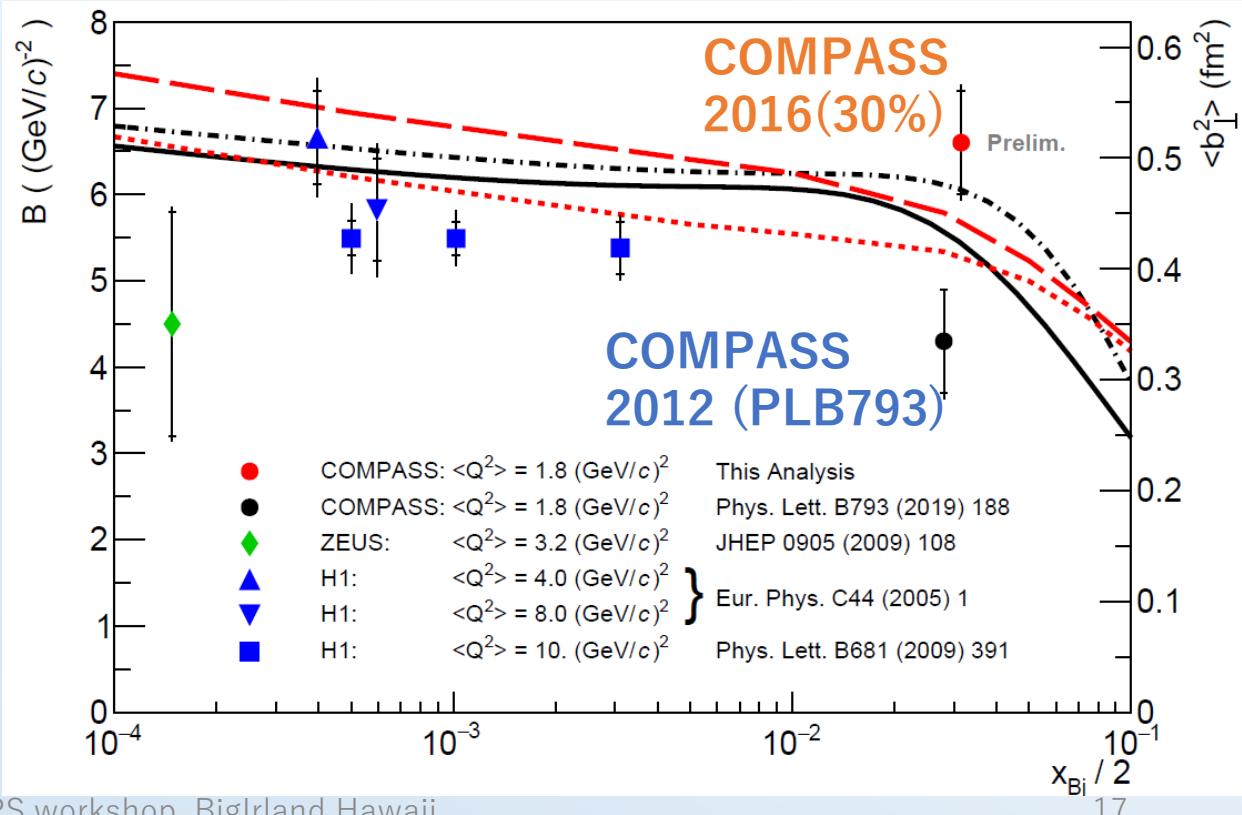
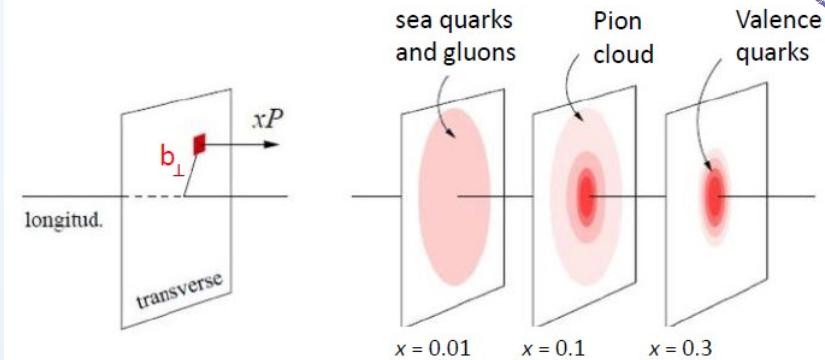
[Burkardt, Int. J. Mod. Phys. A18 (2003) 173]

$$q(x, b_\perp) = \int \frac{d^2 \Delta_\perp}{(2\pi)^2} e^{-ib_\perp \cdot \Delta_\perp} H(x, 0, -\Delta_\perp^2)$$

The DVCS cross section allows to probe the transverse extension of partons

$$\frac{d\sigma^{DVCS}}{dt} \propto e^{-B|t|} = e^{-\frac{1}{2}\langle b_\perp^2 \rangle |t|}$$

$$\langle b_\perp^2 \rangle = \frac{\int d^2 b_\perp b_\perp^2 q(x, b_\perp)}{\int d^2 b_\perp q(x, b_\perp)} = -4 \frac{\partial}{\partial t} \ln H(x, 0, t) \Big|_{t=0}$$



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# *HE vector meson $P$*

# Transverse-target spin asymmetries for HEMP of $\rho$ and $\omega$

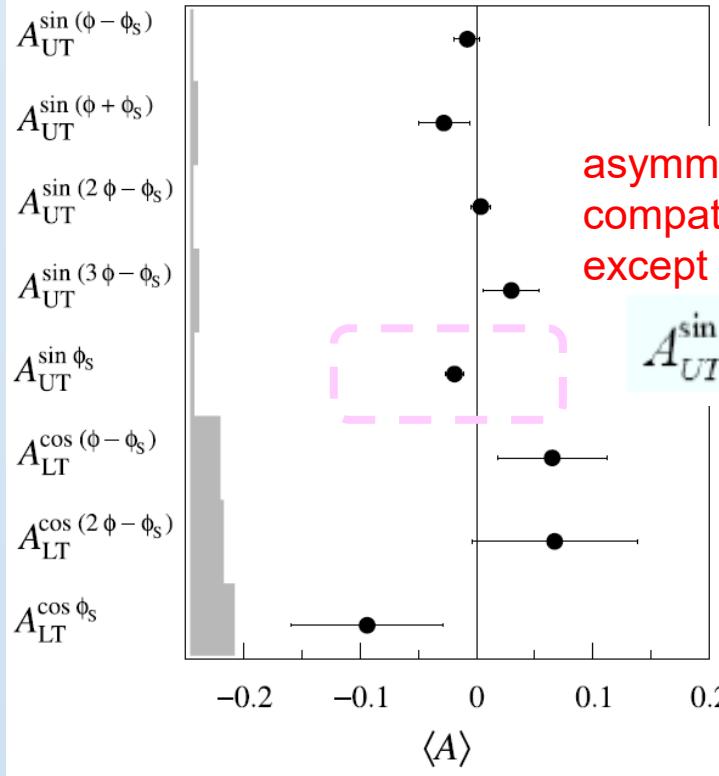


$$\mu^+ p^\uparrow \rightarrow \mu^- p^- \rho^0/\omega$$

160 GeV/c  $\mu^+$  with  $P_\mu \approx -80\%$

data collected with the standard setup with the polarized target

$$\rho^0 \rightarrow \pi^+ \pi^-$$

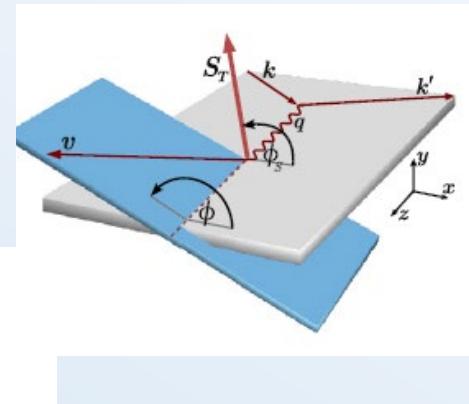


asymmetries small,  
compatible with 0,  
except

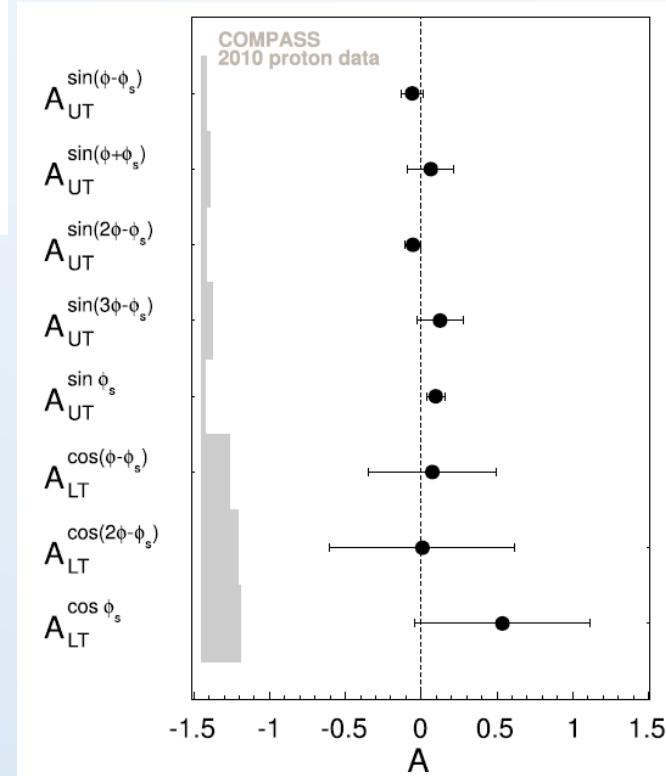
$$A_{UT}^{\sin \phi_s} = -0.019 \pm 0.008 \pm 0.003$$

indication of GPD  
 $H_T$  contribution

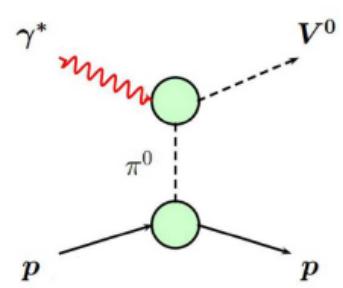
reasonable  
agreement with  
GPD-GK model



$$\omega \rightarrow \pi^+ \pi^- \pi^0$$



promising  
agreement with  
GPD-GK model  
with pion pole



EPJ A50 (2014) 146

COMPASS NPB 865 (2012) 1, PLB731 (2014) 19

2007&10 data for NH3 target

COMPASS NPB915 (2017)

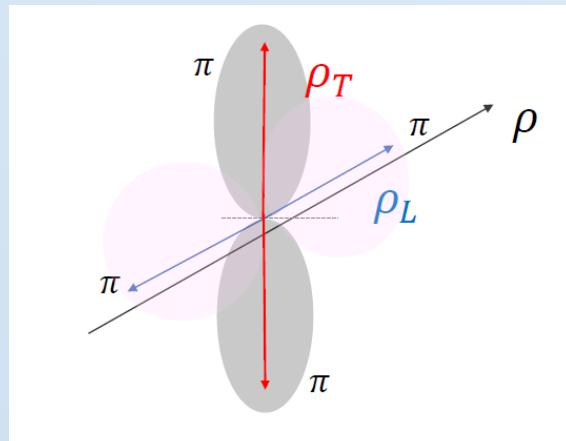
2010 data for NH3 target

# Spin density matrix elements for HEMP of $\rho$ and $\omega$



$$\mu^\pm p \rightarrow \mu^- p^- \rho^0/\omega \quad 160 \text{ GeV/c } \mu^\pm \text{ with } P_\mu \approx \mp 80\%$$

- Spin density matrix elements (**SDMEs**) describe how the spin components of the virtual photon are transferred to the created vector meson
- provide test of s-channel helicity conservation (SCHC)
- Further constraints on GPD parameterization
- Sensitive to chiral-odd GPDs  $H_T$  and  $\tilde{E}_T$



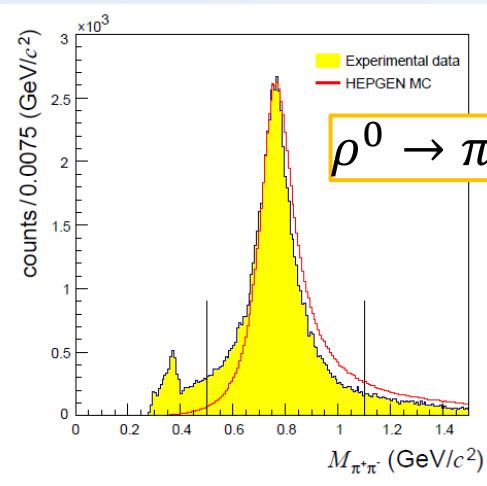
spin state of the vector meson is given by the decay angular distribution

$$d\sigma \propto \mathcal{W}(\mathfrak{R}, \Phi, \phi, \cos\theta)$$

a set of the SDMEs

23 SDMEs in total:  
15 unpolarized and 8 polarized

# Spin density matrix elements for HEMP of $\rho$



data collected with the dedicated setup with the H<sub>2</sub> target

**COMPASS 2012 data**

misidentified KK  
peak < 0.4 GeV

interference between  
resonant and  
non-resonant  $\pi\pi$  seen  
(B.G.3%)

If SCHC( $\lambda_\gamma = \lambda_V$ ) holds:

measurements

[1] $r_{1-1}^1 + \text{Im}(r_{1-1}^2) = 0$	$0.000 \pm 0.005 \pm 0.003$
[2] $\text{Re}(r_{10}^5) + \text{Im}(r_{10}^6) = 0$	$0.011 \pm 0.002 \pm 0.002$
[3] $\text{Im}(r_{10}^7) - \text{Re}(r_{10}^8) = 0$	$0.009 \pm 0.014 \pm 0.028$

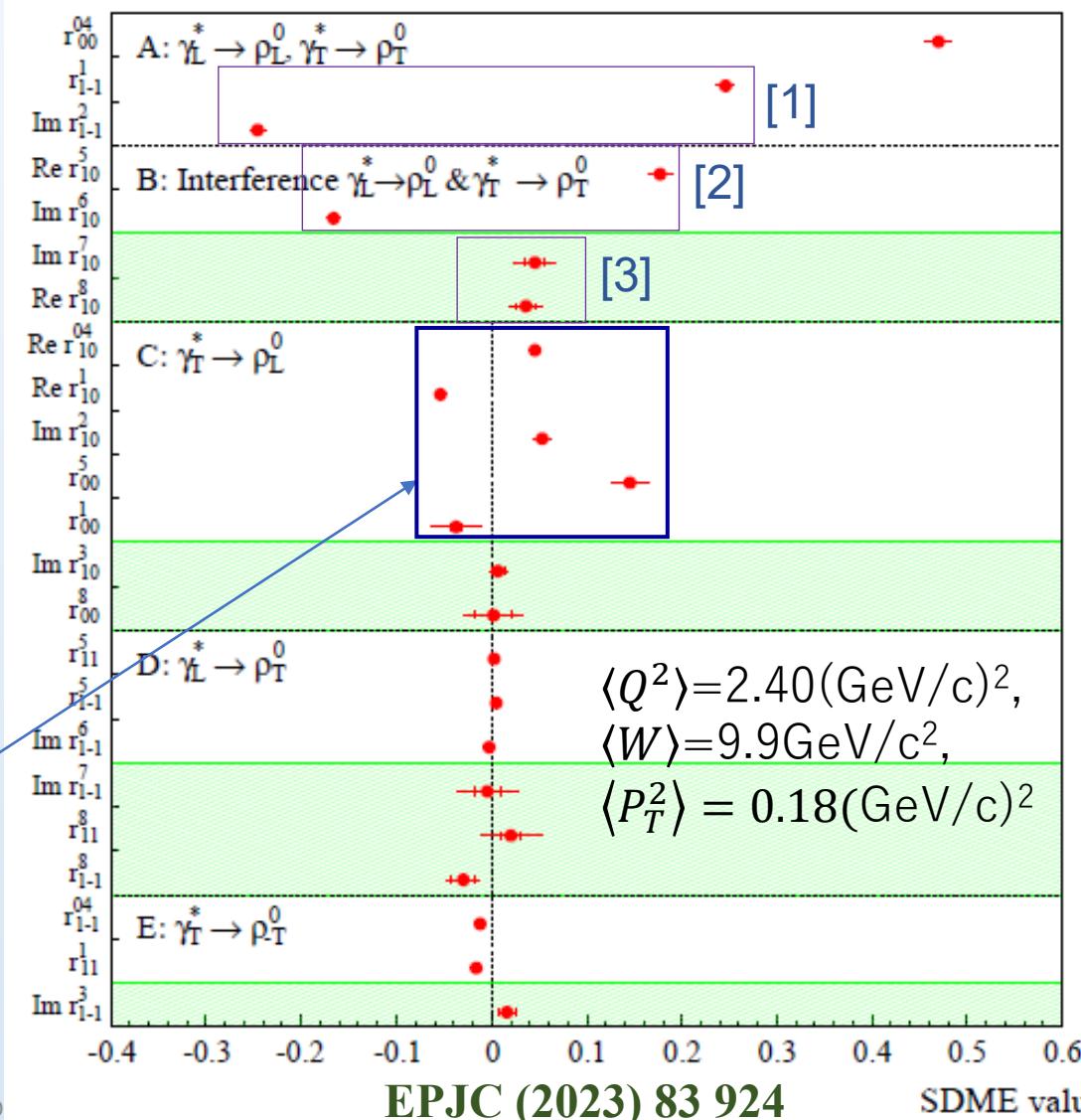
All other elements should be 0

Clear deviation of SCHC

possible Interpretation with chiral-odd GPDs:

$$H_T \text{ and } \bar{E}_T \equiv 2\tilde{H}_T + E_T$$

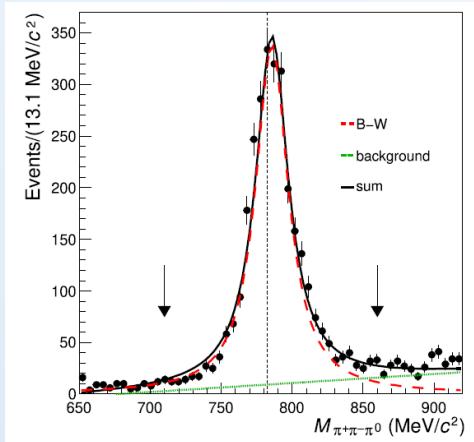
Goloskokov, Kroll, EPJC 74 (2014) 2725



# Spin density matrix elements for HEMP of $\omega$



$$\omega \rightarrow \pi^+ \pi^- \pi^0 \\ (Br \approx 89\%)$$



If SCHC( $\lambda_\gamma = \lambda_V$ ) holds:

measurements

[1] $r_{1-1}^1 + \text{Im}(r_{1-1}^2) = 0$	$-0.010 \pm 0.032 \pm 0.047$
[2] $\text{Re}(r_{10}^5) + \text{Im}(r_{10}^6) = 0$	$0.014 \pm 0.011 \pm 0.013$
[3] $\text{Im}(r_{10}^7) - \text{Re}(r_{10}^8) = 0$	$0.088 \pm 0.110 \pm 0.196$

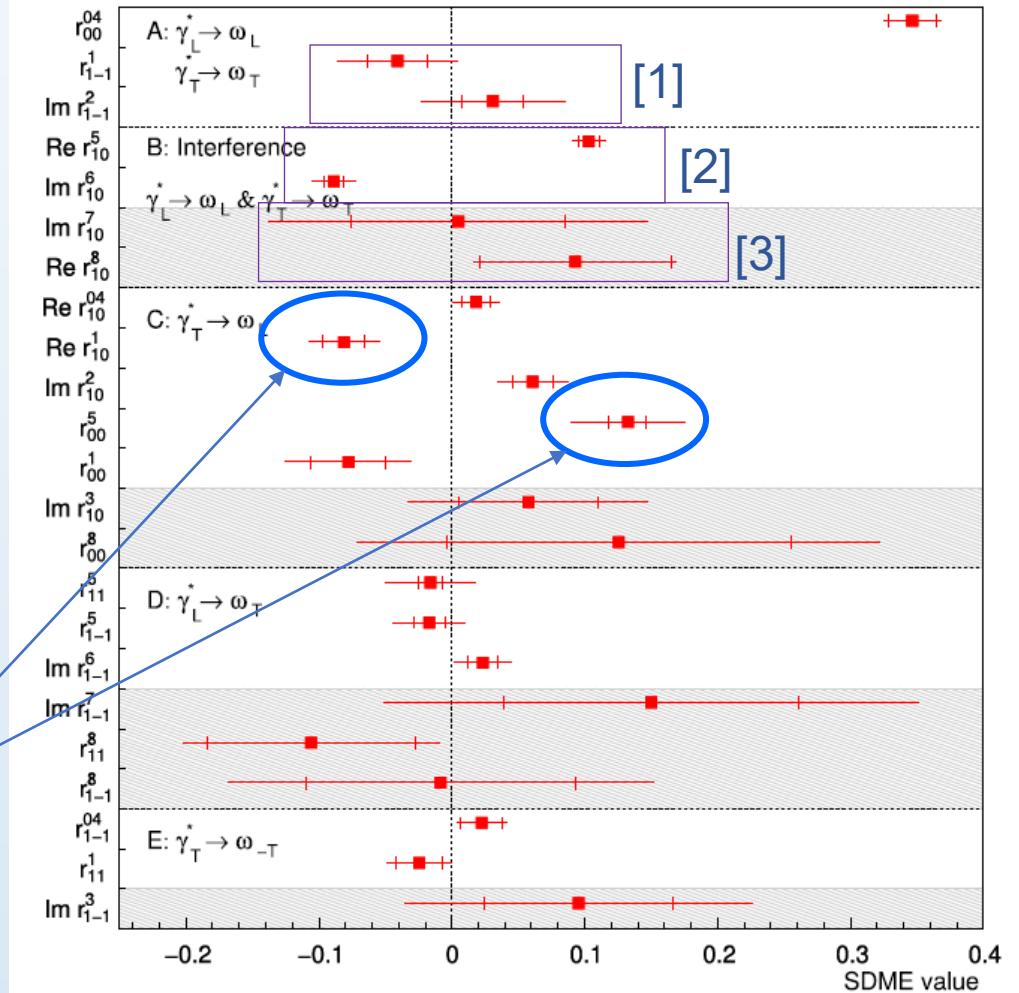
All other elements should be 0

Clear violation of SCHC  
for  $\text{Re}r_{10}^{04}$  and  $r_{00}^5$

related to the chiral-odd GPDs

$H_T$  and  $\bar{E}_T \equiv 2\tilde{H}_T + E_T$  in the GPD GK model

COMPASS 2012 data



COMPASS EPJC (2021) 81126

# Spin density matrix elements for HEMP of $\omega$



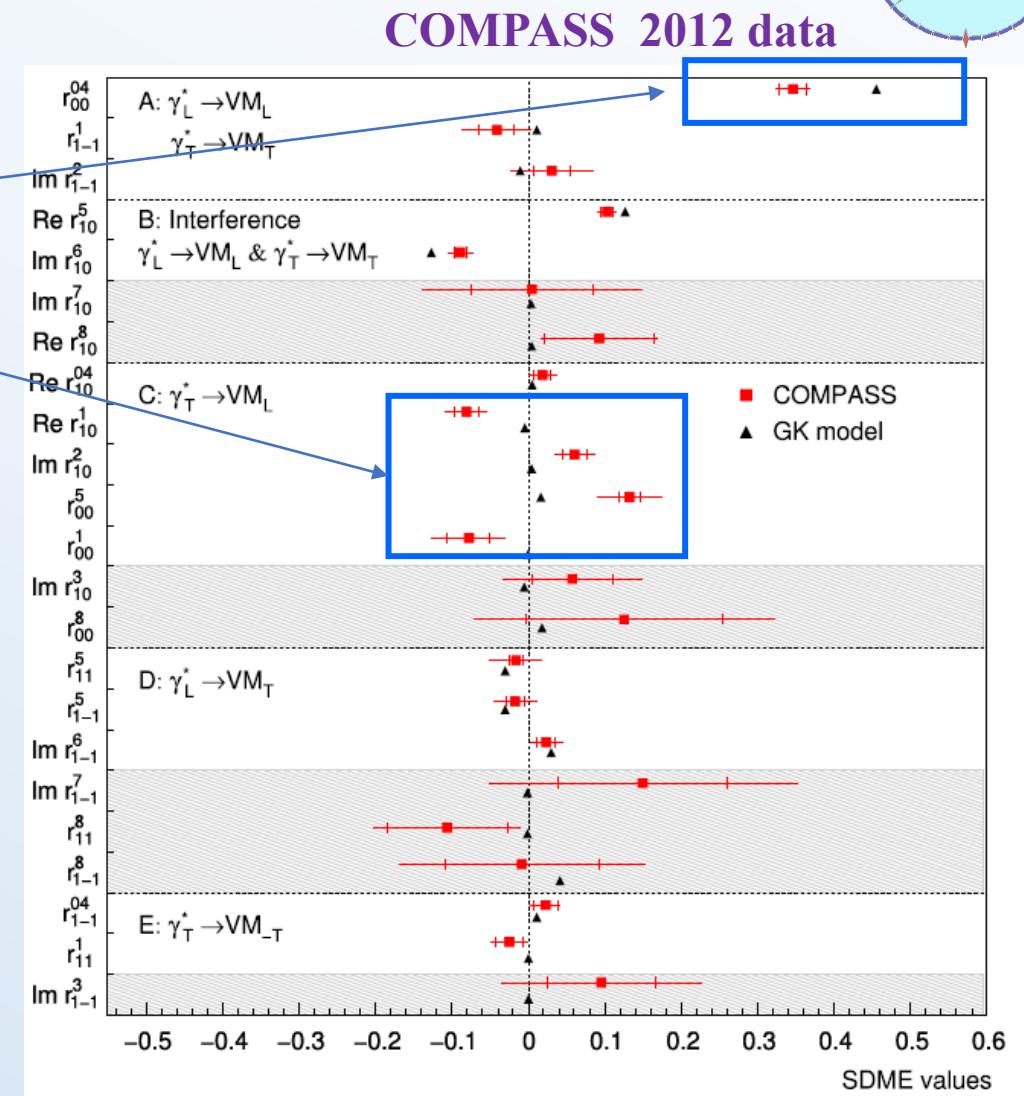
$\omega$  data in comparison with the GPD model

- $r_{00}^{04}$  is significantly different from the model
- Clear deviation for  $\gamma_T^* \rightarrow \omega_L$  elements

GPD GK model

[Eur. Phys. J. C **74**, 2725 (2014), Eur. Phys. J. A **50**, 146 (2014)]

- chiral-odd GPDs included
- pion-pole exchange included
- tuned to HERMES results on SDMEs and spin asymmetries for  $\rho$  and  $\omega$  production



**COMPASS EPJC (2021) 81126**

# $\rho$ and $\omega$ comparison ; Parity exchange property



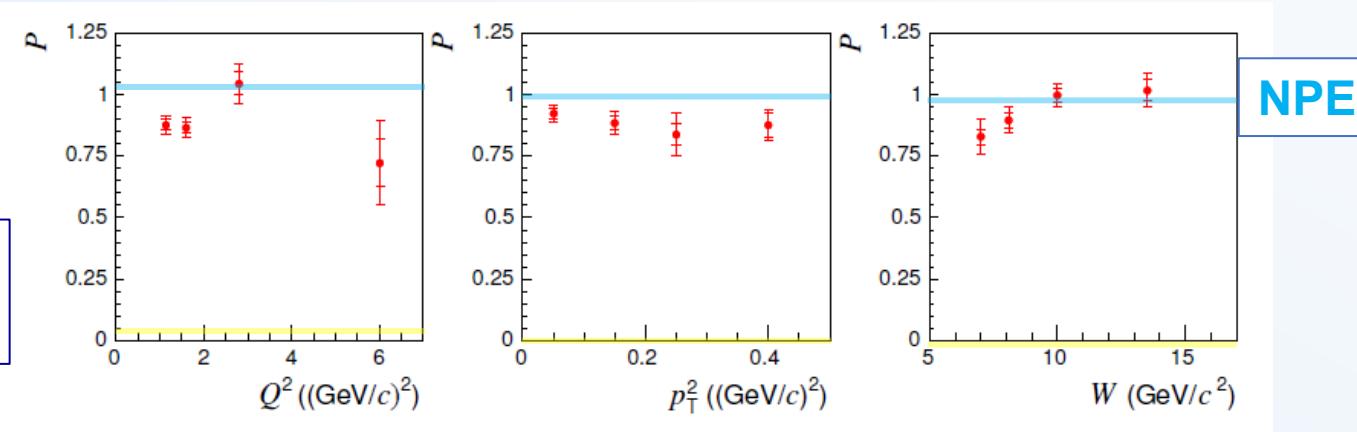
## Parity exchange property

NPE/UPE asymmetry for  $\gamma_T^* \rightarrow V_L$

$$P \equiv \frac{d\sigma_T^{NPE} - d\sigma_T^{UPE}}{d\sigma_T^{NPE} + d\sigma_T^{UPE}} \approx \frac{2r_{1-1}^1}{1 - r_{00}^{04} - r_{1-1}^{04}}$$

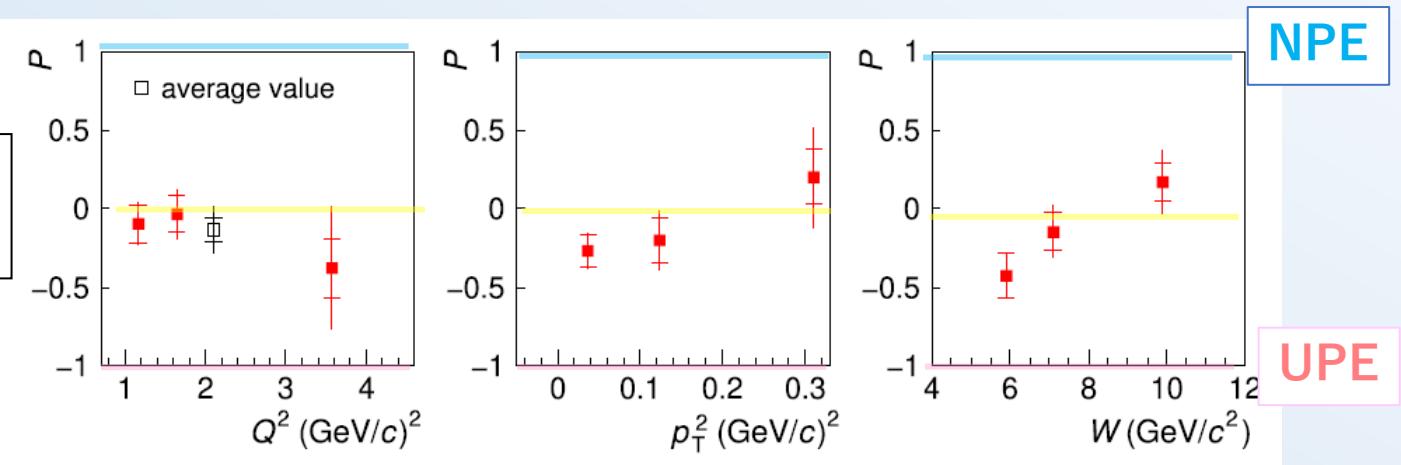
- $\rho$  production

- NPE dominant
- Sensitive to GPDs  $E, H$



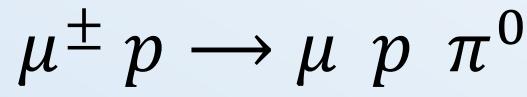
- $\omega$  production

- NPE~UPE on average
- Sensitive also to GPDs  $\tilde{E}, \tilde{H}$  and pion pole



*HE  $\pi^0 P$*

# Exclusive $\pi^0$ production cross section



160 GeV/c  $\mu^\pm$  with  $P_\mu \approx \mp 80\%$

$$\frac{d^2\sigma_{\gamma^* p}}{dt d\phi} = \frac{1}{2\pi} \left[ \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \epsilon \cos(2\phi) \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) \frac{d\sigma_{LT}}{dt} \right]$$

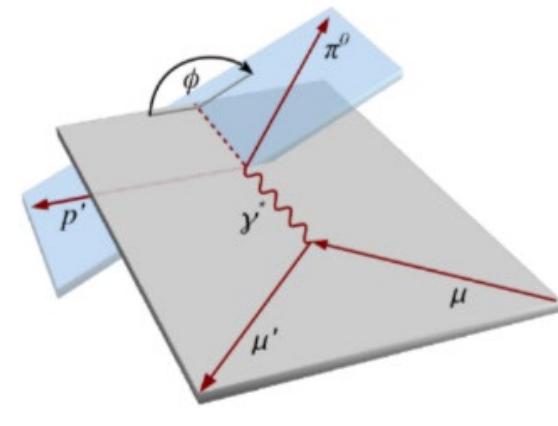
$\frac{d\sigma_T}{dt} \sim |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2$   
 $\frac{d\sigma_L}{dt} \sim |\langle \tilde{H} \rangle|^2 - \frac{t'}{4m^2} |\langle \tilde{E} \rangle|^2$   
 $\frac{d\sigma_{TT}}{dt} \sim \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2$   
 $\frac{d\sigma_{LT}}{dt} \propto \frac{\sqrt{-t'}}{2m} \operatorname{Re} [\langle H_T \rangle^* \langle \tilde{E} \rangle]$

$\frac{d\sigma}{dt d\phi} \sim A + B \cos(2\phi) + C \cos(\phi)$

$\langle GPD \rangle$ : denotes convolution of GPD and DA of the meson

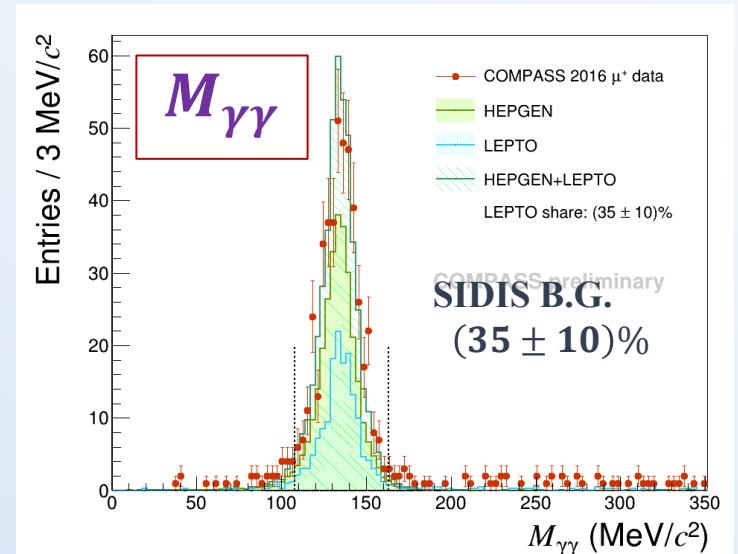
$t' = t - t_{min}$ , where  $|t_{min}|$  is minimum value of  $|t|$

$L, T$  indices indicate polarization of virtual photon. Double index –interference



COMPASS  
 $\langle x_B \rangle = 0.10$   
 $\epsilon$  close to 1

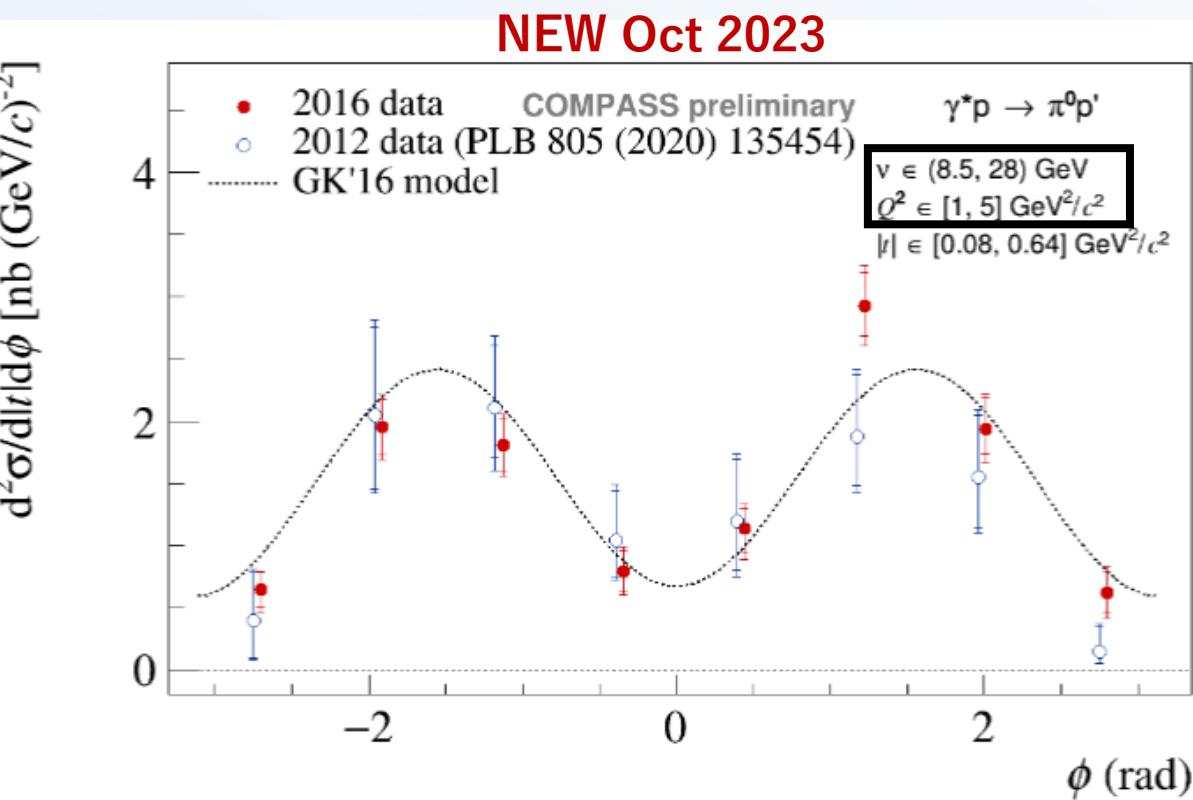
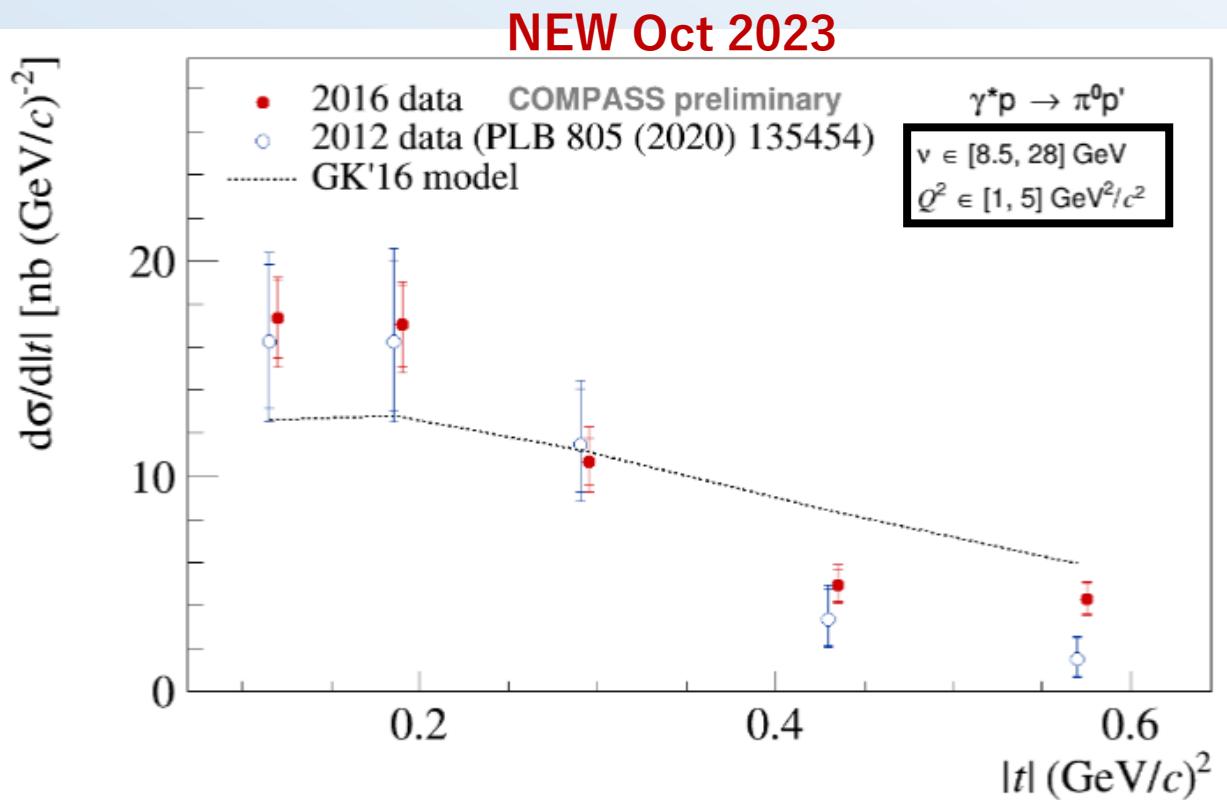
2016 data collected with the dedicated setup with the H2 target



# Exclusive $\pi^0$ production cross section



$\mu^\pm p \rightarrow \mu^- p \pi^0$  160 GeV/c  $\mu^\pm$  with  $P_\mu \approx \mp 80\%$



Models: **GK** Kroll Goloskokov EPJC47 (2011)

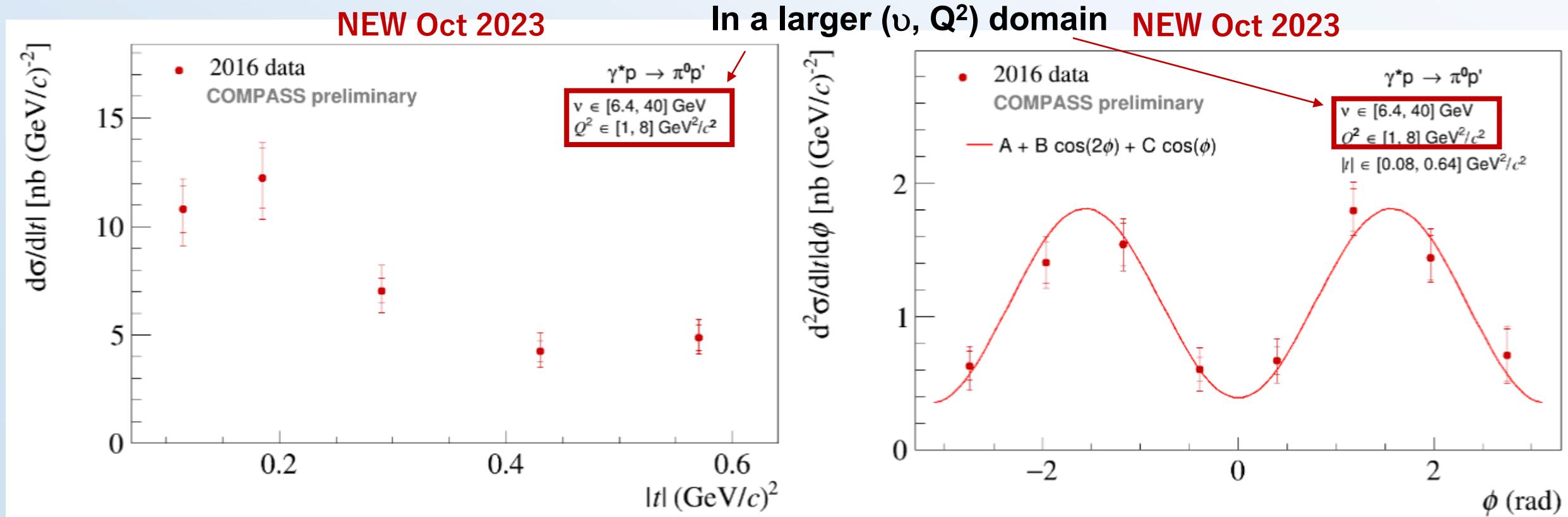
Also **GGL**: Golstein Gonzalez Liuti PRD91 (2015)

# Exclusive $\pi^0$ production cross section



ECAL0 (2016/17) to enlarge the kinematic domain

2016 data in larger  $v$  and  $Q^2$  domain



# Exclusive $\pi^0$ production cross section



$$\mu^\pm p \rightarrow \mu^- p \pi^0$$

160 GeV/c  $\mu^\pm$  with  $P_\mu \approx \mp 80\%$

$$\frac{d^2\sigma_{\gamma^* p}}{dt d\phi} = \frac{1}{2\pi} \left[ \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \epsilon \cos(2\phi) \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) \frac{d\sigma_{LT}}{dt} \right]$$

$$\frac{d\sigma_T}{dt} \sim |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2$$

$$\frac{d\sigma_L}{dt} \sim |\langle \tilde{H} \rangle|^2 - \frac{t'}{4m^2} |\langle \tilde{E} \rangle|^2$$

$$\frac{d\sigma_{TT}}{dt} \sim \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2$$

$$\frac{d\sigma_{LT}}{dt} \propto \frac{\sqrt{-t'}}{2m} \operatorname{Re} [\langle H_T \rangle^* \langle \tilde{E} \rangle]$$

@COMPASS  $\langle x_B \rangle = 0.13$

$v \in [6.4, 40] \text{ GeV}$

$Q^2 \in [1, 8] \text{ GeV}^2/c^2$

$|t| \in [0.08, 0.64] \text{ GeV}^2/c^2$

from the fit

$$\left\langle \frac{\sigma_T}{|t|} + \epsilon \frac{\sigma_L}{|t|} \right\rangle = (6.9 \pm 0.3_{\text{stat}} \pm 0.8_{\text{syst}}) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\left\langle \frac{\sigma_{TT}}{|t|} \right\rangle = (-4.5 \pm 0.5_{\text{stat}} \pm 0.2_{\text{syst}}) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\left\langle \frac{\sigma_{LT}}{|t|} \right\rangle = (0.06 \pm 0.2_{\text{stat}} \pm 0.1_{\text{syst}}) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

negative  
→ role of  $\bar{E}_T$

rather small

We will determine the evolution with  $v$  and  $Q^2$

The 2017 data set will still increase the statistics (by a factor 3)

(GPD): denotes convolution of GPD and DA of the meson

$t' = t - t_{min}$ , where  $|t_{min}|$  is minimum value of  $|t|$

$L, T$  indices indicate polarization of virtual photon. Double index –interference

# Summary and outlook

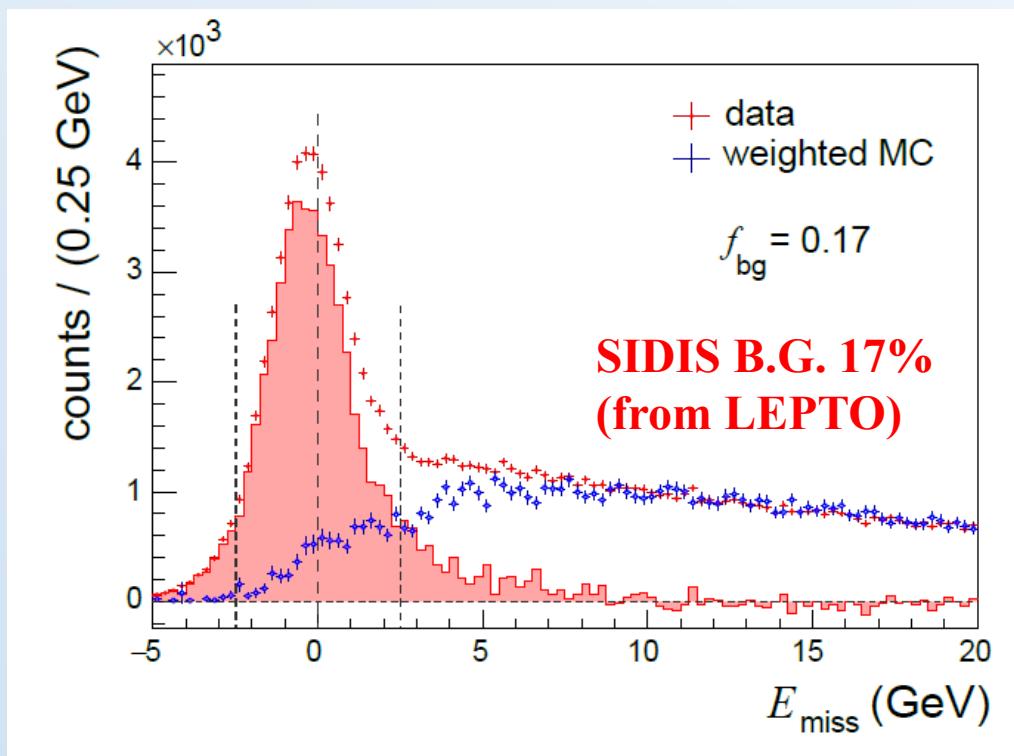
- GPD is one of the key concepts to solve the problems of the nucleon structure
- COMPASS measurements related to the GPD have been reported.
- The new data for DVCS have been presented(30% of 2016).
- Results of  $\rho$  and  $\omega$  production have been given:  
Transverse-target spin asymmetries and SDMEs
- The new data for the cross section for  $\pi^0$  exclusive production have been shown  
(full of 2016)
- These results are useful to give constraints to GPDs
- More data are being analyzed ( in particular 2017 data)
- HEMP for  $\phi$  ( $\sigma$  and SDMEs); work in progress on 2016 data
- HEMP for  $J/\psi$  ; feasibility study on going

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# **Backup Slides**

# Background for excl.- $\rho$ production

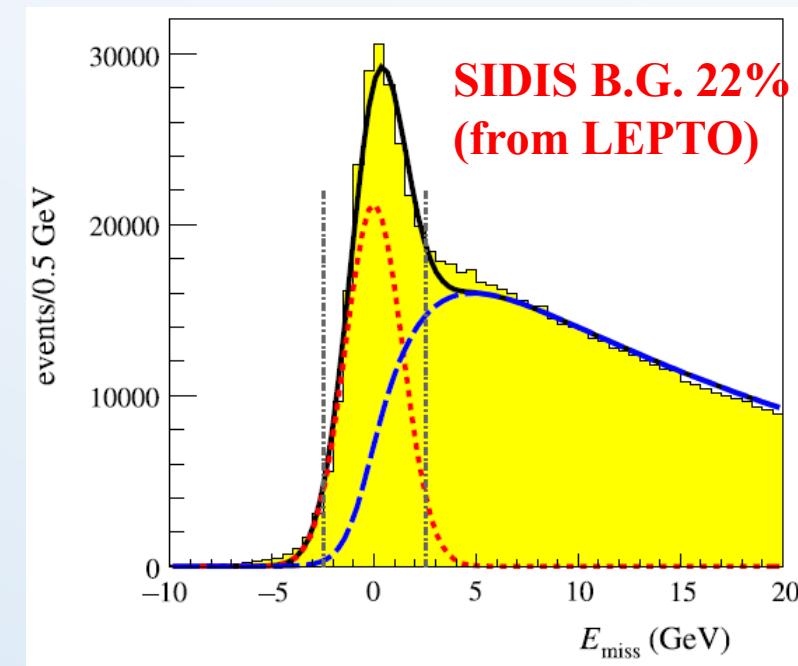
SDME



COMPASS arXiv:2210.16932v1 acc. EPJC

angular distribution corrected by SIDIS MC

Target spin asymmetry

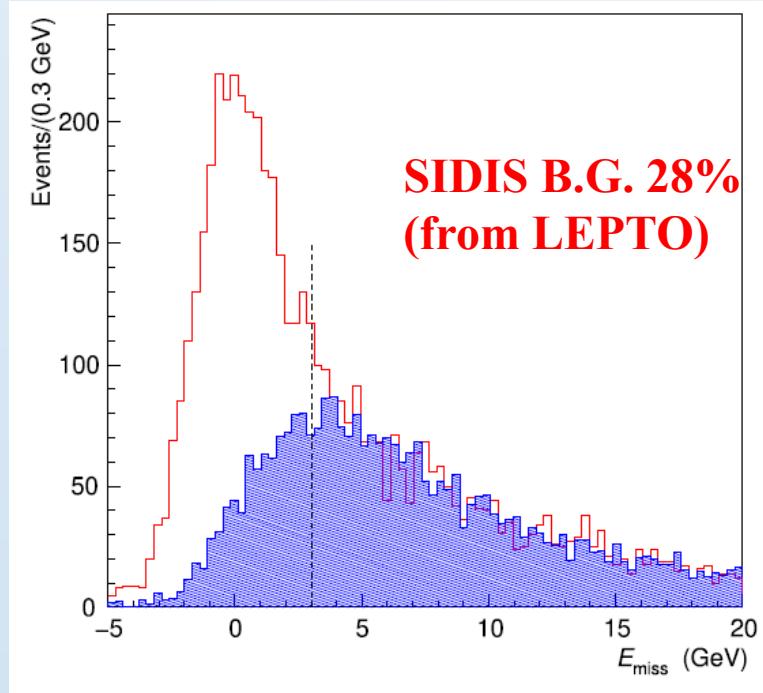


COMPASS PLB731 (2014) 19

angular distribution corrected by SIDIS MC

# Background for excl.- $\omega$ production

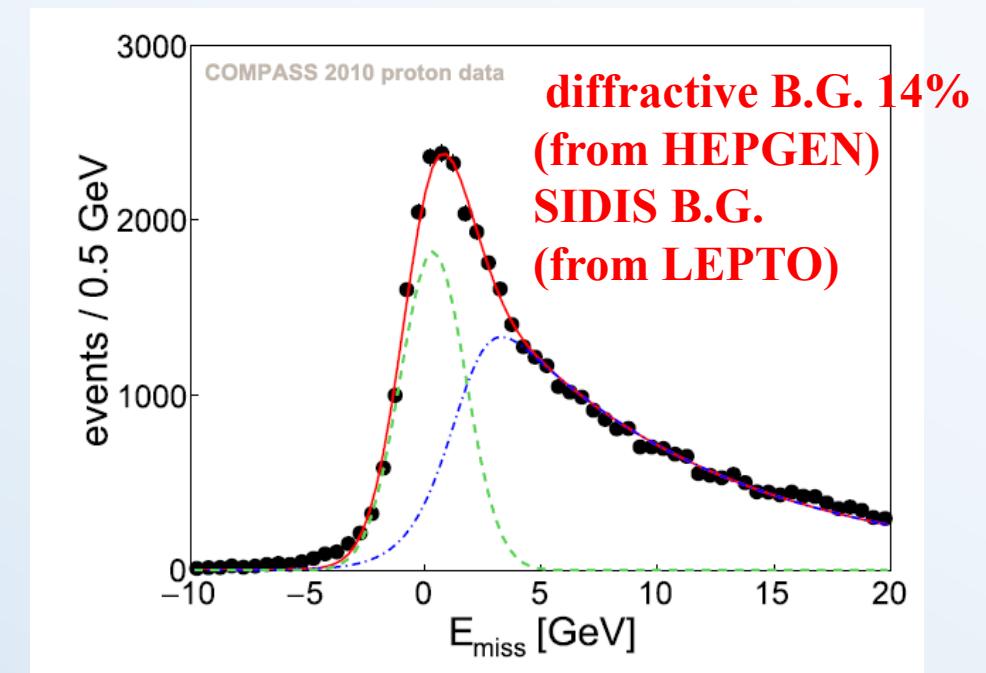
SDME



COMPASS EPJC (2021) 81126

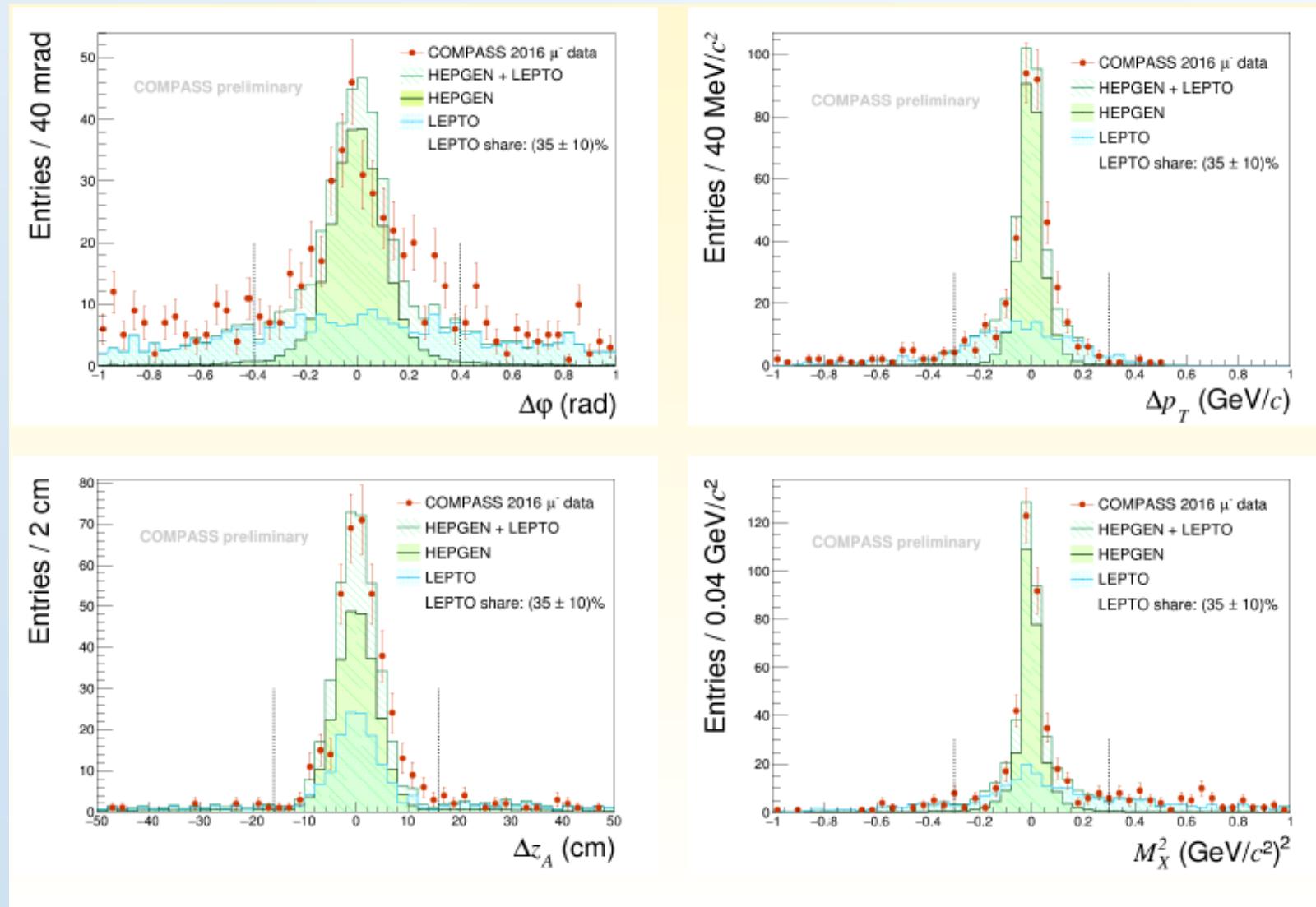
angular distribution corrected by MC

Target spin asymmetry



angular distribution corrected by MC

# Background for excl.- $\pi^0$ production



exclusive  $\pi^0$   
(from HEPGEN++)  
SIDIS B.G.  
(from LEPTO)

B.G.  $(35 \pm 10)\%$

# Summary table for GPDs

		Quark Polarization		
		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$H$		$2\tilde{H}_T + \bar{E}_T = \bar{E}_T$
	L		$\tilde{H}$	$\tilde{\bar{E}}_T$
	T	$E$	$\tilde{E}$	$H_T, \tilde{H}_T$

- 4 chiral-even, 4 chiral-odd (subscript  $T$ ).
- 2 T-odd ( $E, \bar{E}_T$ ).