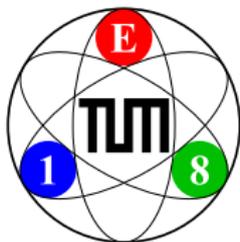


Measuring Excitation Spectra in $K\pi\pi$ Final States with AMBER Phase-2

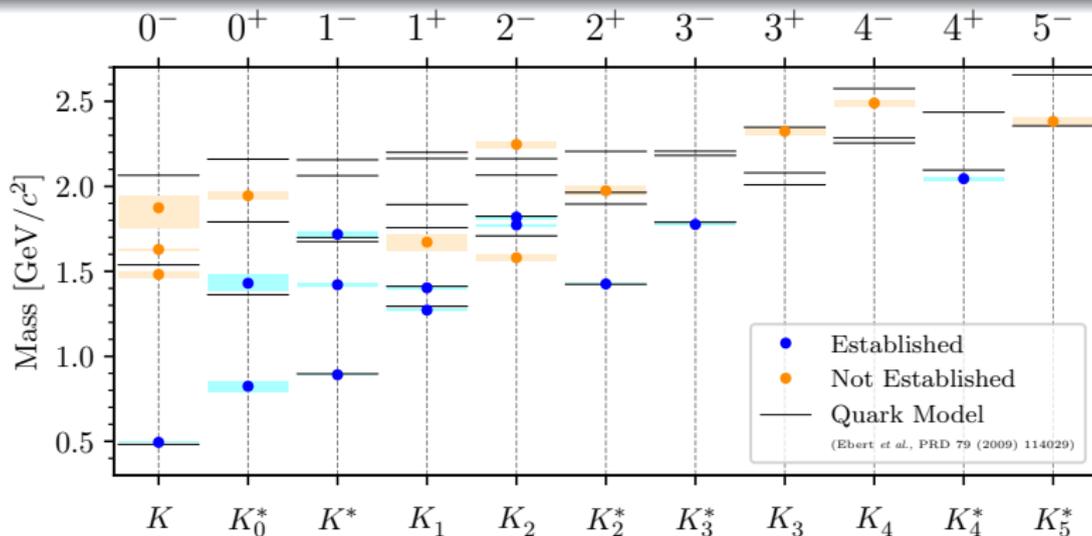
Boris Grube

Institute for Hadronic Structure and Fundamental Symmetries
Technische Universität München
Garching, Germany

Perceiving the Emergence of Hadron Mass
through AMBER@CERN
CERN, 27. Apr 2021



Why Kaon Spectroscopy?



[Courtesy S. Wallner, TUM]

PDG 2020: 25 kaon states below 3.1 GeV/c²

- Only 13 kaon states well established, 12 need confirmation
- Many predicted quark-model states still missing
- Some hints for supernumerous states ⇒ non- $q\bar{q}$ states?

Why Kaon Spectroscopy?

Little progress in the past

- Many kaon states need confirmation
- Many PDG entries more than 30 years old
- Since 1990: 4 kaon states added to PDG (1 to summary table)

Kaon spectrum crucial to understand light-meson spectrum

- Identify supernumerous states by completing $SU(3)_{\text{flavor}}$ multiplets
 - E.g. $J^P = 0^+$ nonet with $a_0(980)$, $K_0^*(700)$ [or κ], $f_0(500)$ [or σ], and $f_0(980)$ is hypothesized to be tetra-quark multiplet
 - $K_0^*(700)$ still listed as “needs confirmation” by PDG

Kaon spectrum required as input in other fields

- E.g. search for CP violation in multi-body decays of heavy mesons such as $B^\pm \rightarrow D^0 K^\pm$ with $D^0 \rightarrow K_S^0 \pi^+ \pi^-$
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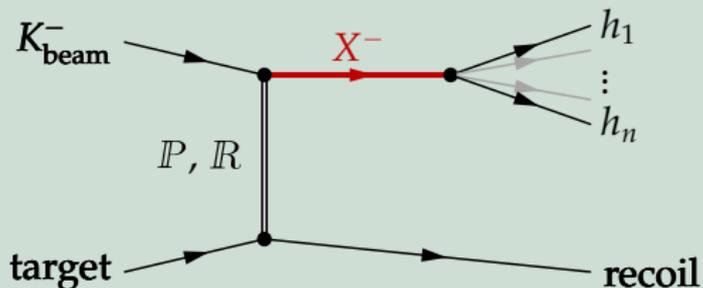
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Main production process: diffractive dissociation



- 190 GeV/c kaon beam on stationary proton or nuclear target
- Process has large cross section
- Triggering on target recoil ensures elastic scattering at target vertex
- Decays into various hadronic n -body final states measurable
- n -body final state strongly boosted
⇒ measured by forward spectrometer

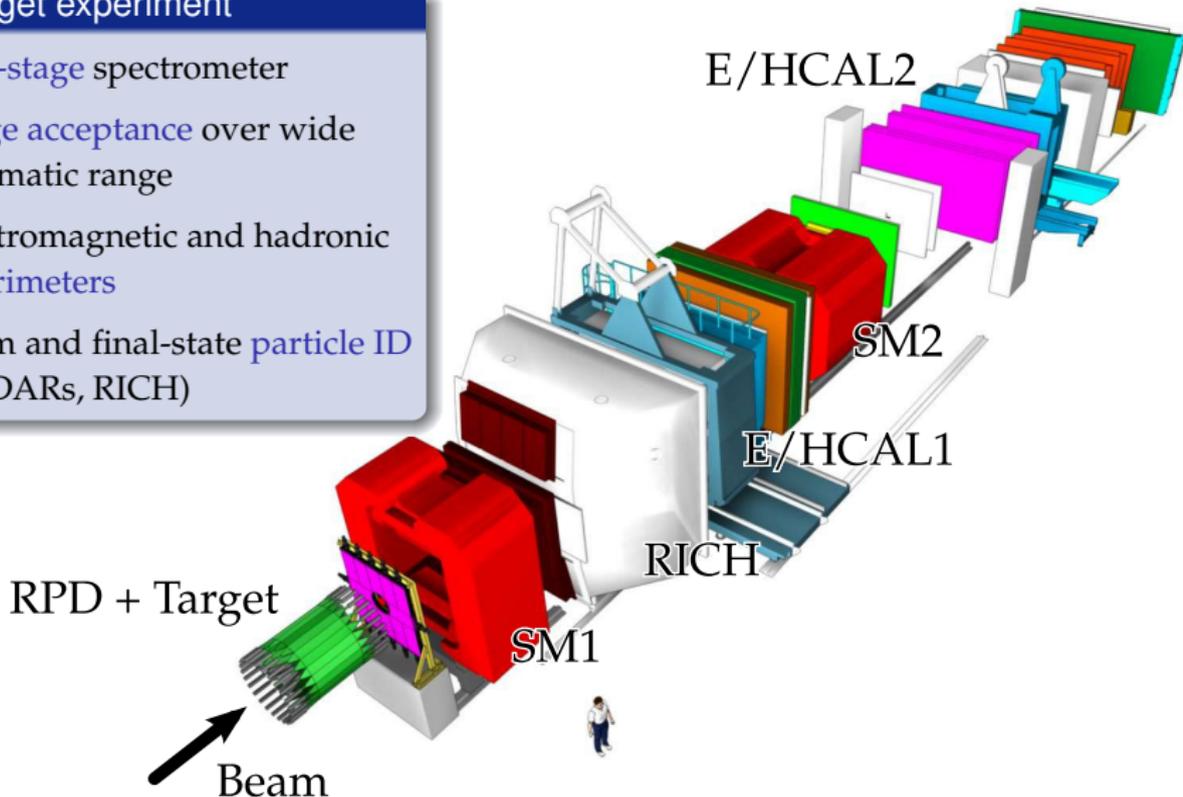
The COMPASS Experiment at the CERN SPS

Experimental Setup

C. Adolph, NIMA 779 (2015) 69

Fixed-target experiment

- Two-stage spectrometer
- Large acceptance over wide kinematic range
- Electromagnetic and hadronic calorimeters
- Beam and final-state particle ID (CEDARs, RICH)



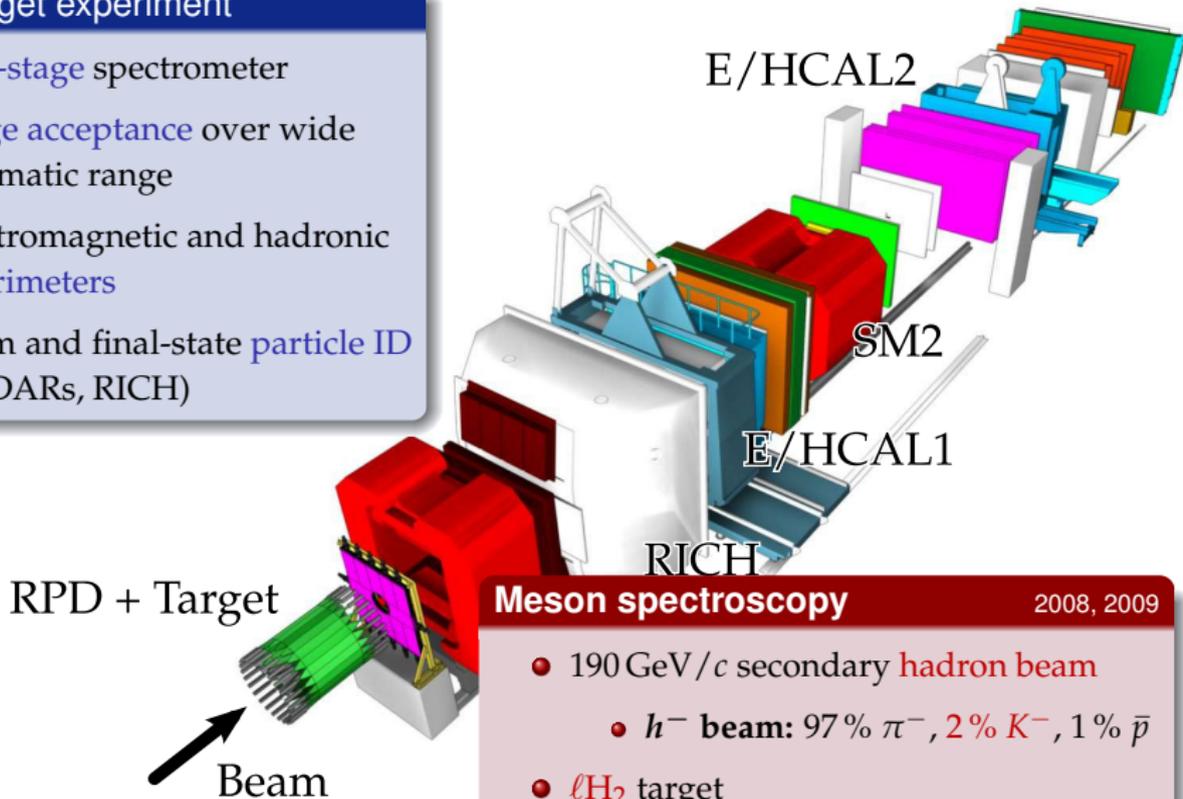
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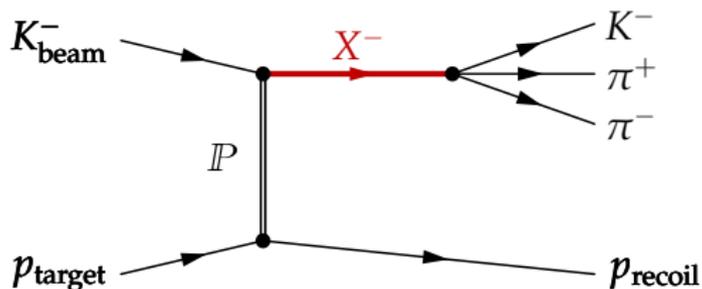
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Diffractive Production of $K^- \pi^- \pi^+$

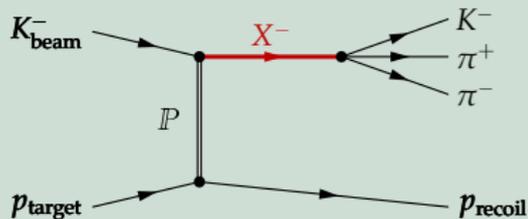


The “golden” channel for kaon spectroscopy

- All kaon states (except $J^P = 0^+$) can appear as intermediate states X^-
- Highly excited states prefer to decay into multi-body final states
- Allows us to study several decay modes in one analysis, e.g.
 - $X^- \rightarrow \rho(770) K^-, f_2(1270) K^-, \dots$
 - $X^- \rightarrow K^*(892) \pi^-, K_2^*(1430) \pi^-, \dots$
- Strange partner process to $\pi^- + p \rightarrow \pi^- \pi^- \pi^+ + p$
 - Studied in great detail at COMPASS

Diffractive Production of $K^- \pi^- \pi^+$ at COMPASS

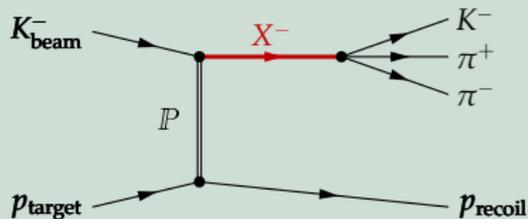
190 GeV/c K^- beam on p target



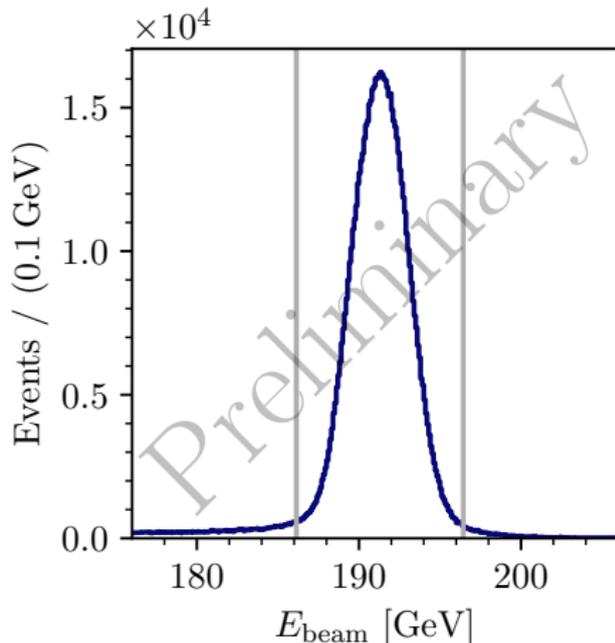
- Beam contains 2.4% K^-
- 720 000 exclusive events
- $0.1 < t' < 1.0$ (GeV/c)²
- Potential resonance signals
 - Need partial-wave analysis (PWA) to disentangle
- Largest data sample so far
 - $\approx 3.5\times$ larger than WA03 sample

Diffractive Production of $K^- \pi^- \pi^+$ at COMPASS

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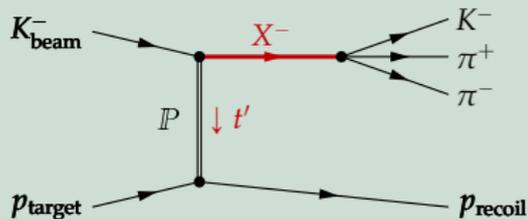


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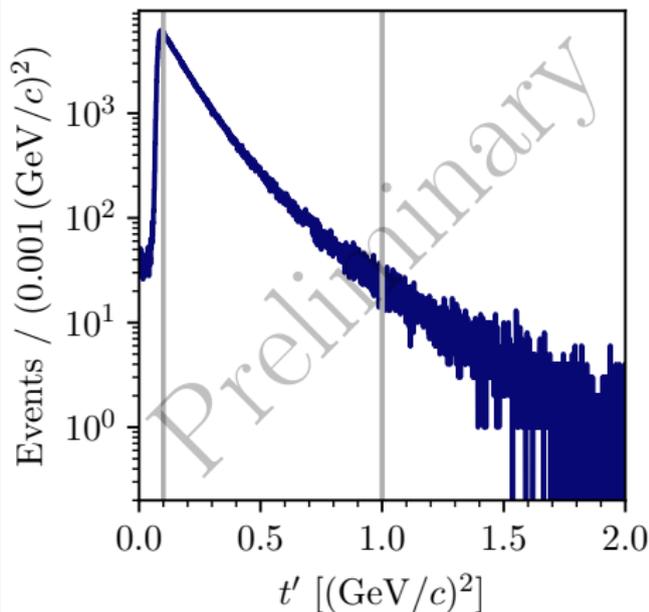


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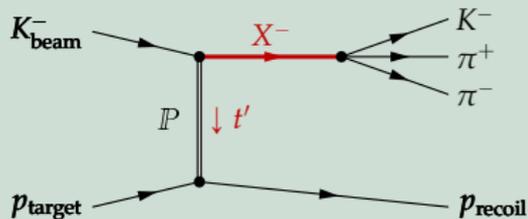


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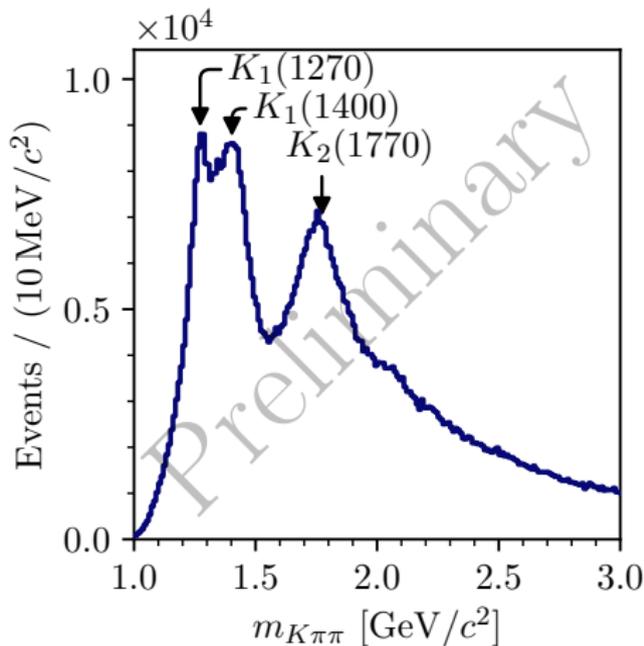


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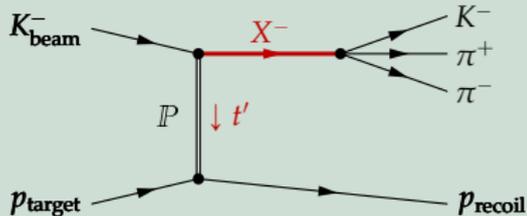


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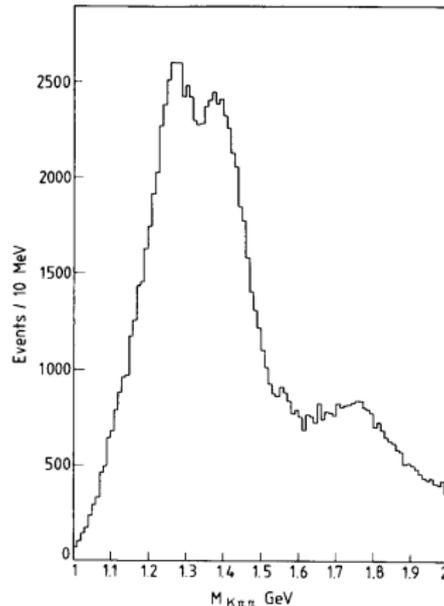


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WA03 (CERN):

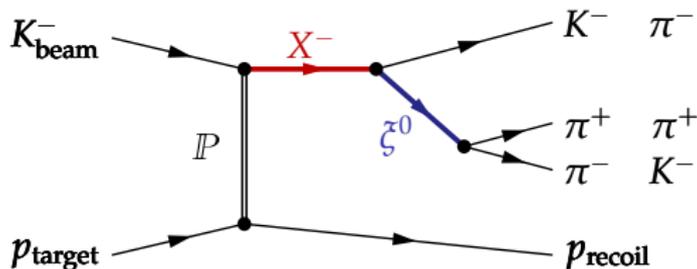
200 000 events

$0 < t' < 0.7$ (GeV/c)²



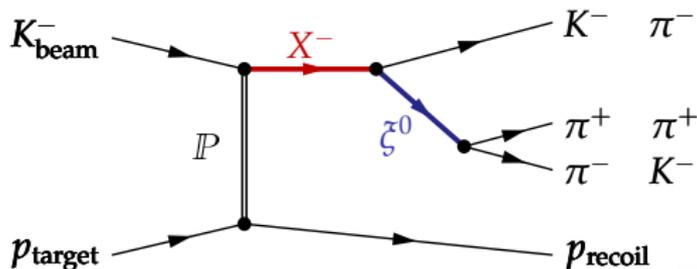
ACCMOR, NPB 187 (1981) 1

Partial-Wave Analysis of $K^- \pi^- \pi^+$: Isobar Model



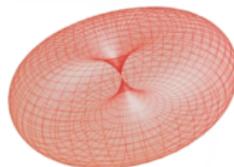
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- *Analogy: multipole radiation in classical electrodynamics*
- Determine J^P of intermediate resonances X^- and ζ^0 from measured angular distribution of final-state particles

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Dipole
($L = 1$)



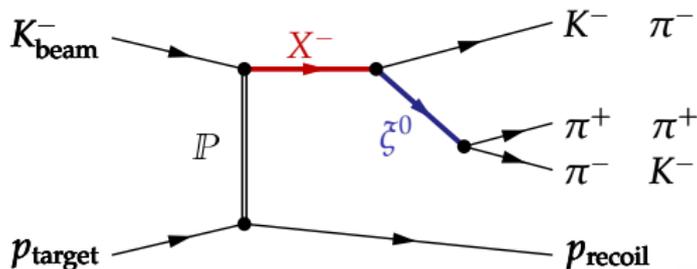
Quadrupole
($L = 2$)



Octupole
($L = 3$)

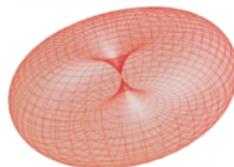


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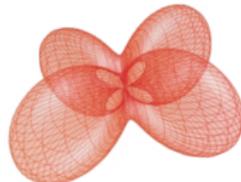


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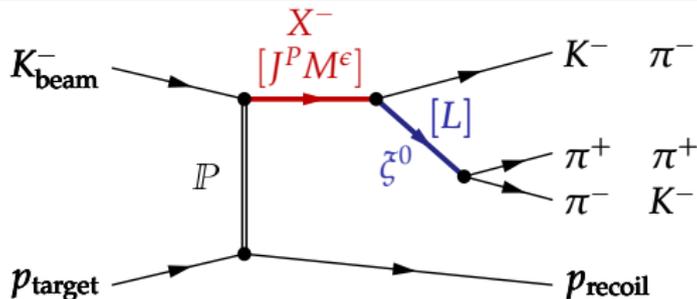
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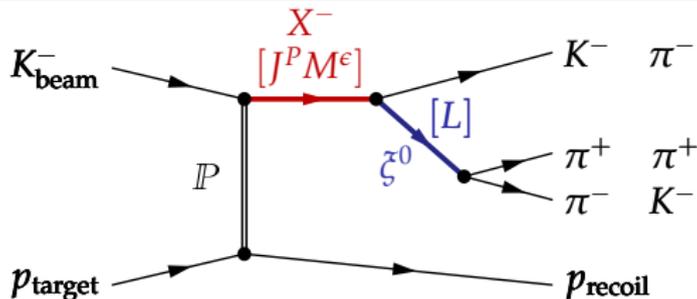
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For $m_{K\pi\pi} = \text{const}$, $K\pi\pi$ kinematic distribution is completely defined by:

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- Orbital angular momentum L between ζ^0 and bachelor π/K
- Isobar resonance $\zeta^0 \Rightarrow$ model for $m_{\pi^- \pi^+} / m_{K^- \pi^+}$ dependence of amplitude
 - E.g. Breit-Wigner amplitudes for $\rho(770) \rightarrow \pi^- \pi^+$ and $K^*(892) \rightarrow K^- \pi^+$
- *Partial wave*: represents specific 5-dimensional kinematic distribution

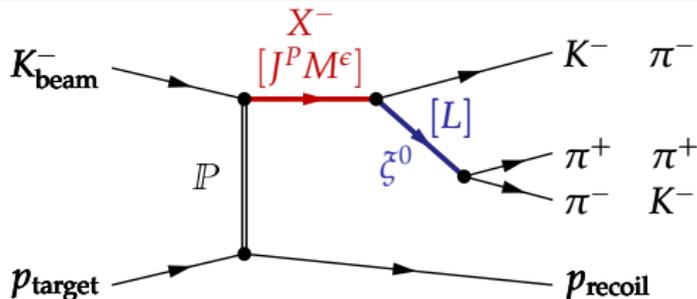
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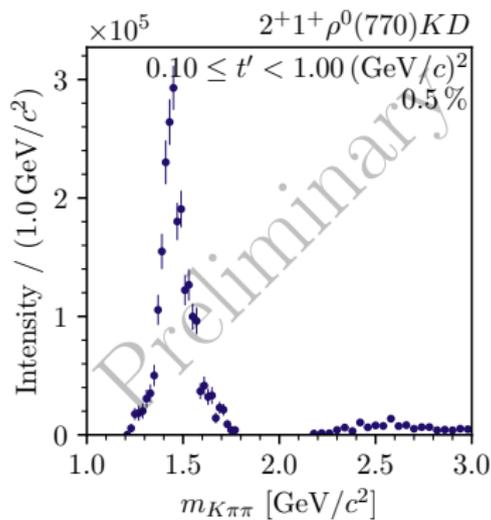
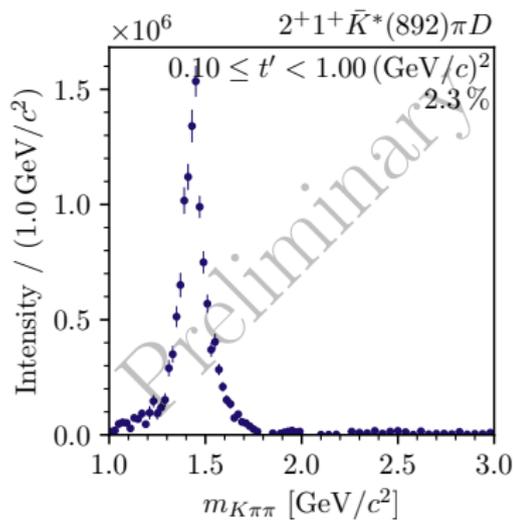


PWA model

- Sum of partial-wave amplitudes
- Wave set:
 - Spin $J \leq 7$
 - Orbital angular momentum $L \leq 7$
 - Positive naturality of the exchange particle
 - 12 isobar resonances:
 - $[K\pi]_S^{K\pi}, [K\pi]_S^{K\eta}, K^*(892), K_2^*(1430), K^*(1680), K_3^*(1780)$
 - $[\pi\pi]_S, f_0(980), f_0(1500), \rho(770), f_2(1270), \rho_3(1690)$

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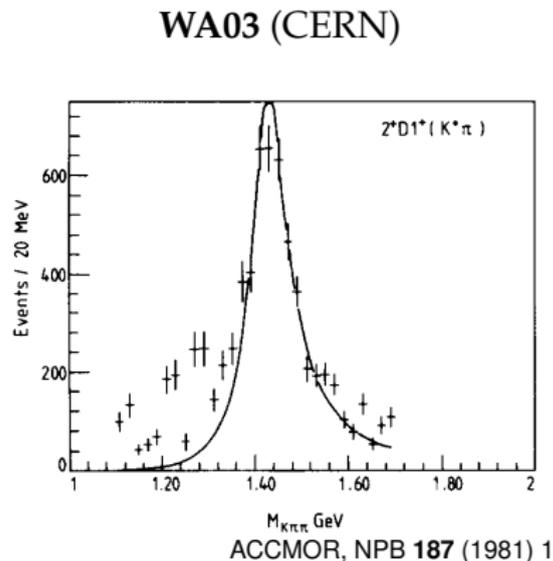
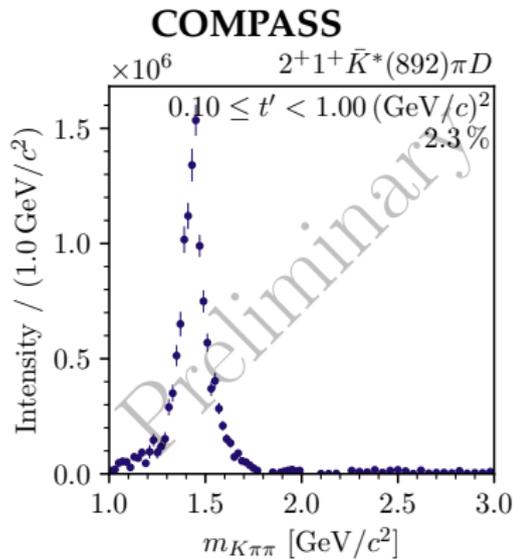
Example: $J^P = 2^+$ Waves



- Clear signals for $K_2^*(1430) \rightarrow K^*(892) \pi$ and $\rho(770) K$
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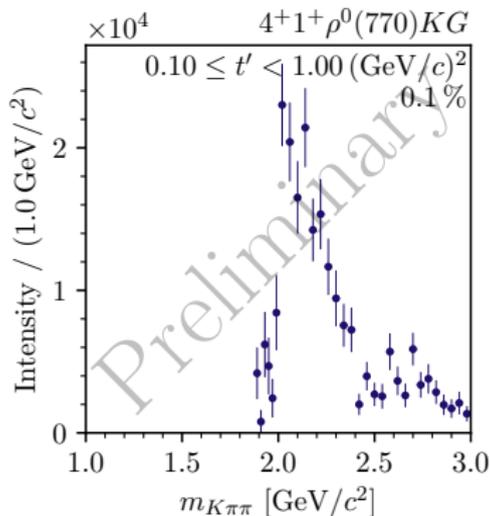
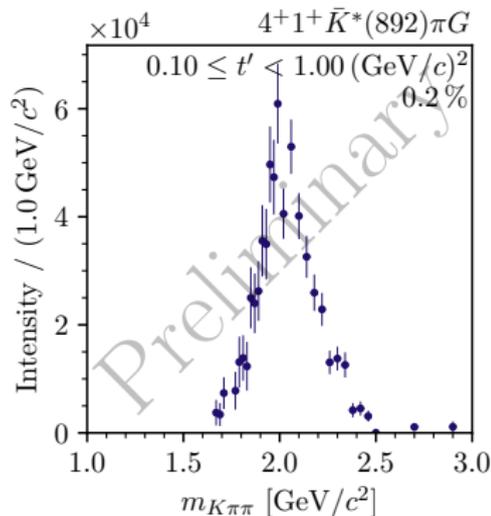
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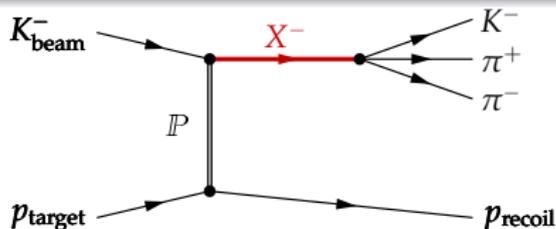
Example: $J^P = 4^+$ Waves



- Small waves: order of **per-mille of total intensity**
- Signals for $K_4^*(2045) \rightarrow K^*(892) \pi$ and $\rho(770) K$

Partial-Wave Analysis of $K^- \pi^- \pi^+$ at COMPASS

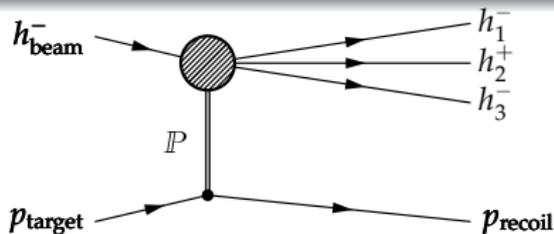
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 - Issue: limited momentum range for π^- and K^- ID

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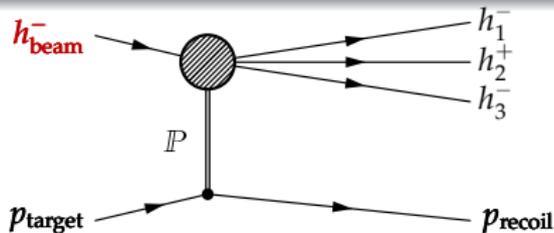
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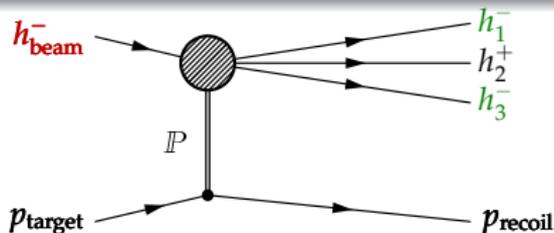
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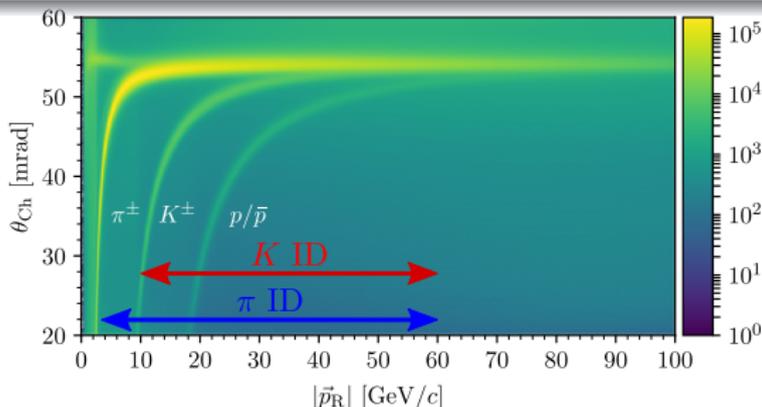
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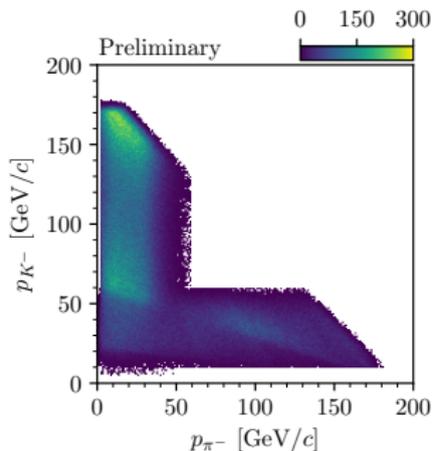


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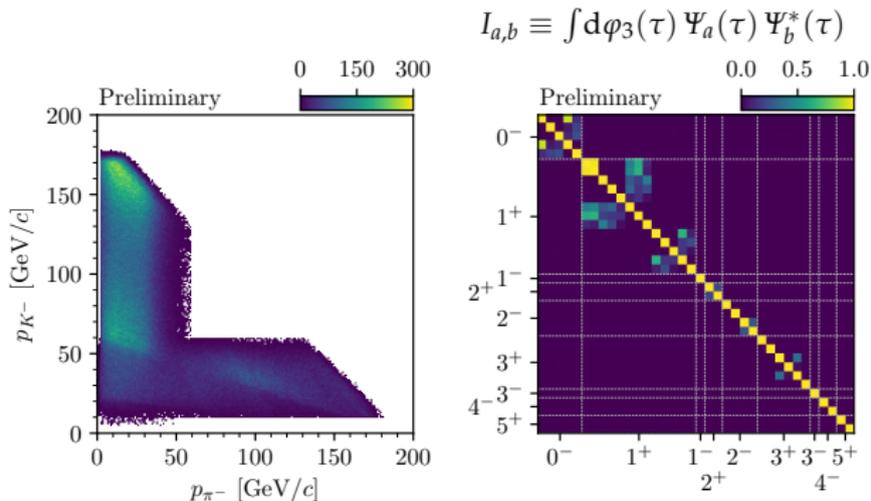
Challenge: non-uniform Acceptance due to RICH Particle ID



- Kinematic region with **vanishing acceptance** \Rightarrow not recoverable
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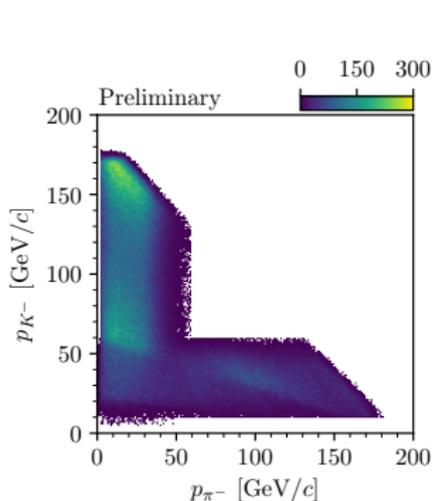
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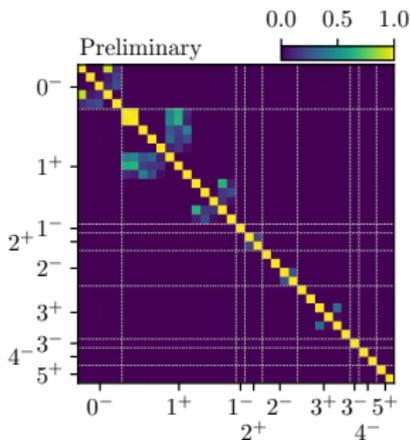
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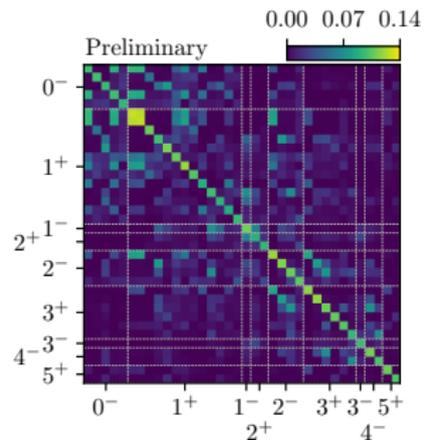
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$$I_{a,b} \equiv \int d\varphi_3(\tau) \Psi_a(\tau) \Psi_b^*(\tau)$$



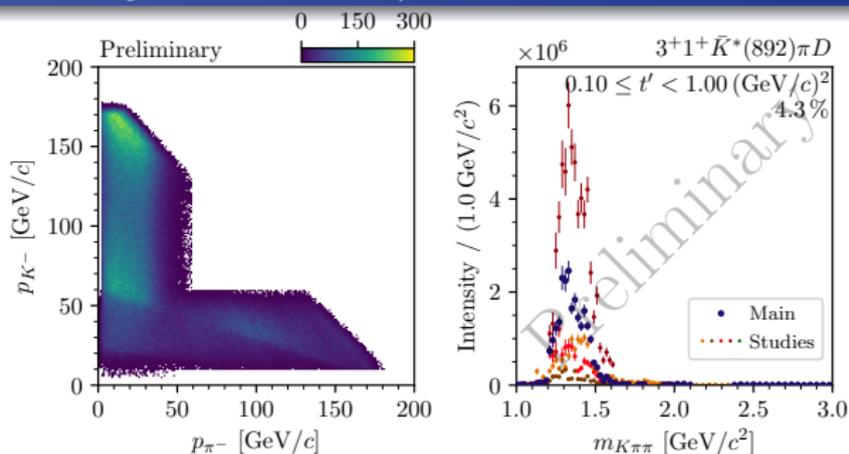
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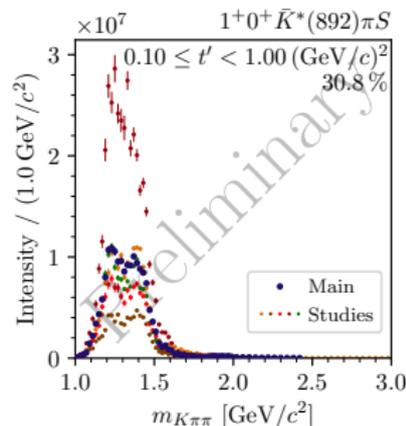
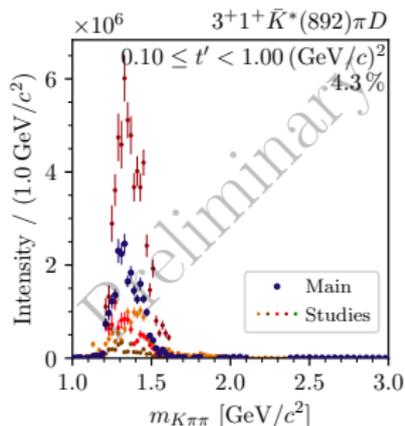
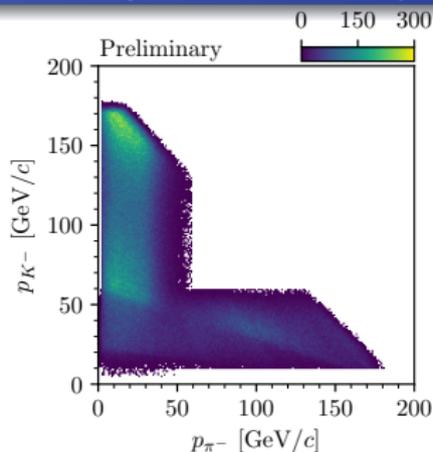


Leakage effects in PWA

- **Unphysical enhancement** of intensity at low $m_{K\pi\pi}$ in some waves; depends strongly on RICH cut and PWA model
 - Induced by **loss of orthogonality** of decay amplitudes
 - Only **subset of waves** affected
- Extraction of **resonances** from unaffected waves still possible
 - *Work in progress*: simultaneous **resonance-model fit** of 10 selected waves described by 8 resonances

Partial-Wave Analysis of $K^- \pi^- \pi^+$ at COMPASS

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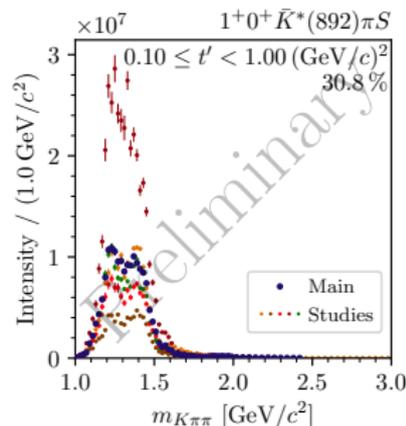
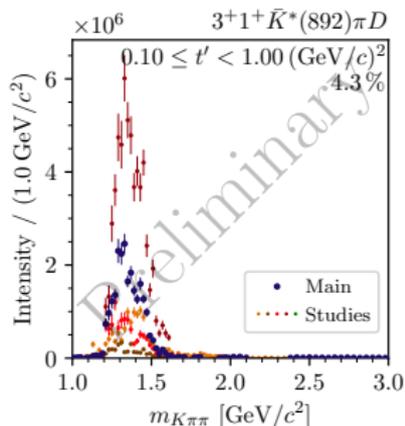
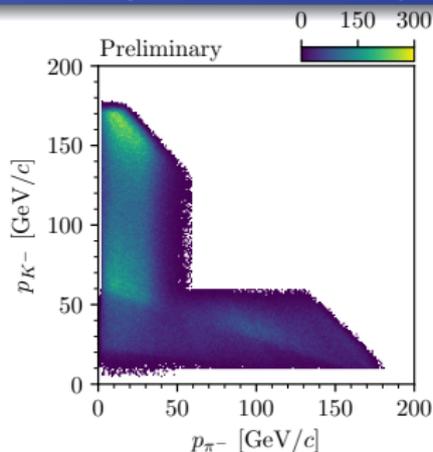


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 - *Work in progress*: simultaneous **resonance-model fit** of 10 selected waves described by 8 resonances

Partial-Wave Analysis of $K^- \pi^- \pi^+$ at COMPASS

Challenge: non-uniform Acceptance due to RICH Particle ID



Leakage effects in PWA

- **Unphysical enhancement** of intensity at low $m_{K\pi\pi}$ in some waves; depends strongly on RICH cut and PWA model
 - Induced by **loss of orthogonality** of decay amplitudes
 - Only **subset of waves** affected
- Extraction of **resonances** from unaffected waves still possible
 - *Work in progress*: simultaneous **resonance-model fit** of 10 selected waves described by 8 resonances

High-Precision Kaon Spectroscopy at AMBER

Goal: $10\times$ world data

- Using **diffraction** of high-energy **kaon beam** (as COMPASS)
- Corresponds to $> 10^7 K^- \pi^- \pi^+$ events
- Also gives **access to other channels** with smaller branching fraction and/or acceptance, e.g.
 - $K^- \pi^0 \pi^0, K_S^0 \pi^- \pi^0 \Rightarrow$ important cross-checks for $K^- \pi^- \pi^+$
 - 2-body channels: $K_S^0 \pi^-, K^- \pi^0, K^- \eta^{(\prime)}, K^- \omega, \dots$
 - 3-body channels: $K \eta^{(\prime)} \pi, K \omega \pi, K K K, \dots$
 - 4-body channels: $K 3\pi, \dots$

- **Main limiting factor: only 2.4% K^- fraction in beam**
 - Intensity of K^- component: 10^5 s^{-1} for approximately 10 s every 45 s
- **Need to increase intensity of kaon component by factor > 10**
- **Solution: RF-separated beam**

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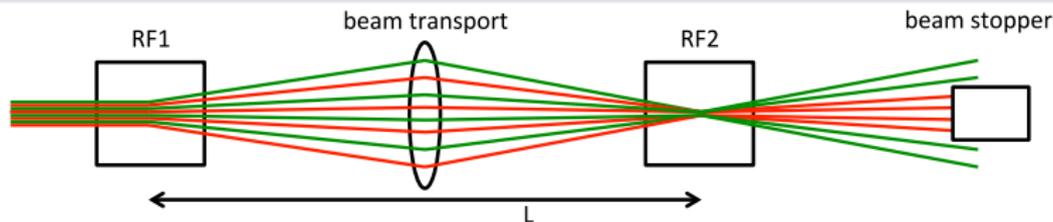
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RF-separated Kaon Beam at SPS M2 Beam Line

Panofsky-Schnell Method

P. Bernard *et al.*, CERN-1968-029

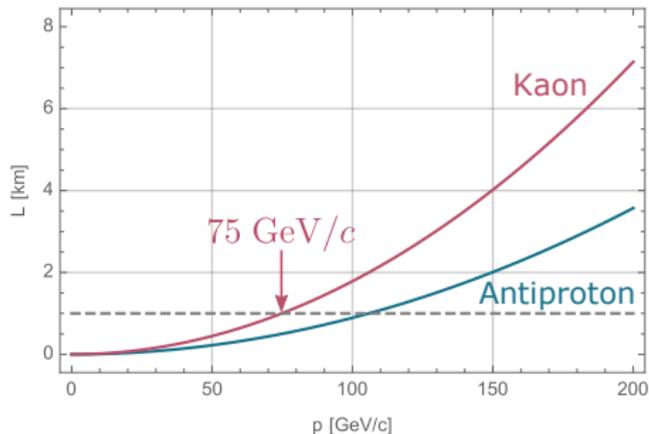
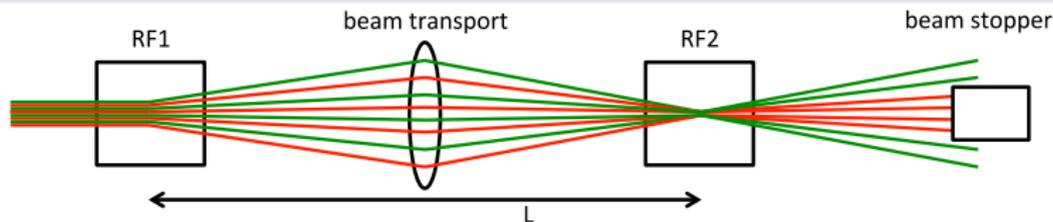


- Beam momentum limited by length of beam line
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- More detailed studies needed to determine beam parameters more precisely
- Requires major investment

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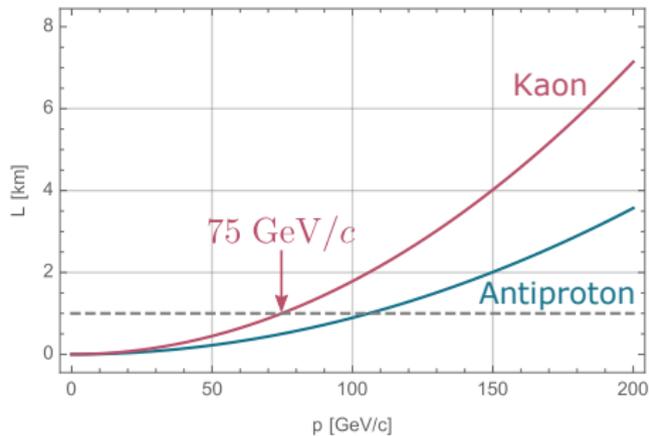
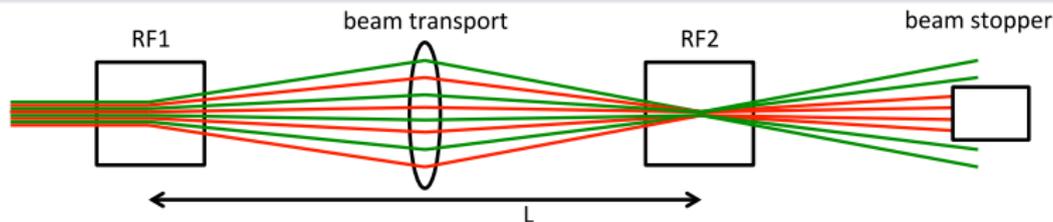
CERN-PBC-REPORT-2018-002

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Requirements for AMBER Setup

- Upgrade beam PID; adjust for lower beam momentum
 - Improve rate capability and thermal stability of CEDARs
 - Improve measurement of beam trajectories at CEDAR position
⇒ silicon beam momentum stations?
- High-resolution silicon beam telescope and vertex detector
- Improve detection of target recoil particle
- Extend kinematic coverage of final-state PID
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 - Access e.g. to $K^- K^- K^+$ final state
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- COMPASS has already acquired the **so far largest data sample for $K^- + p \rightarrow K^- \pi^+ \pi^- + p$** (720 000 events)

AMBER

- **Goal:** collect 10× world data using high-intensity **RF-separated kaon beam**
- **High physics potential:**
 - All states (except $J^P = 0^+$) directly accessible
 - $J^P = 0^+$ may be studied **in subsystems**
 - All major decay modes accessible
 - AMBER could **rewrite PDG for kaon states above $1.5 \text{ GeV}/c^2$**
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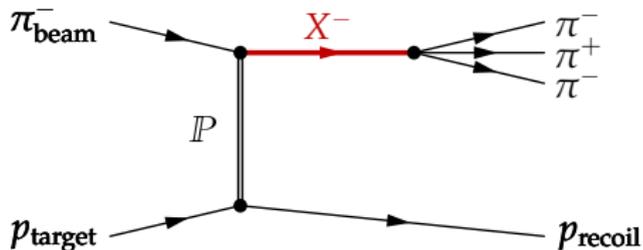
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4 Backup slides

Why do we need more data?

Example: $\pi^- + p \rightarrow \pi^- \pi^- \pi^+ + p_{\text{recoil}}$

COMPASS, PRD 95 (2017) 032004

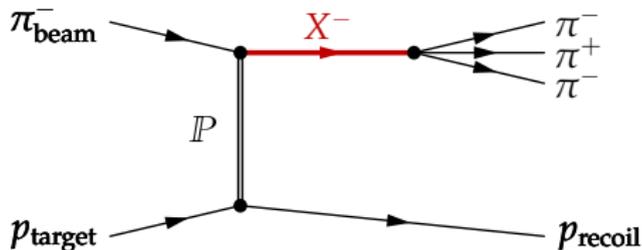


- $46 \times 10^6 \pi^- \pi^- \pi^+$ events \Rightarrow approx. $10 \times$ previous experiments

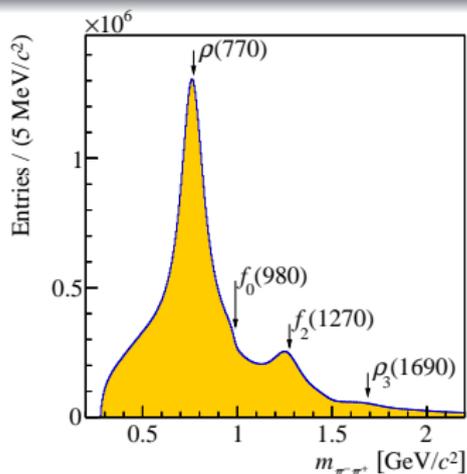
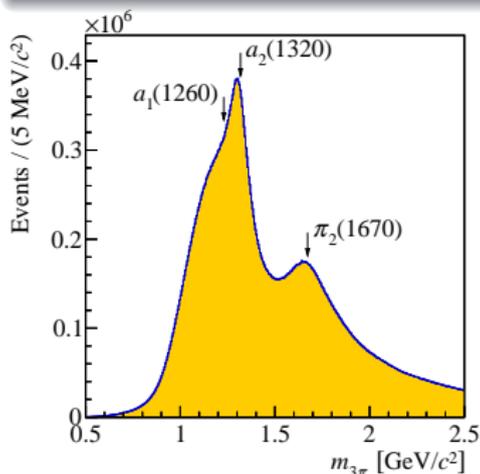
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COMPASS, PRD 95 (2017) 032004



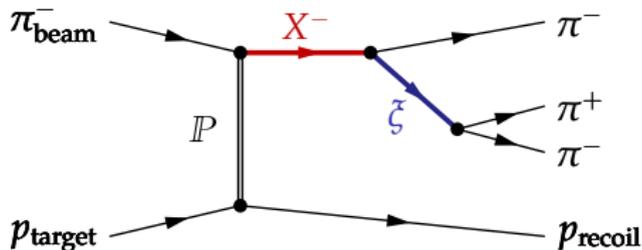
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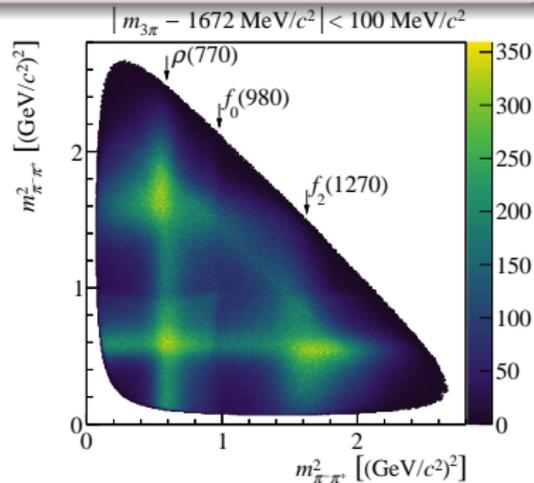
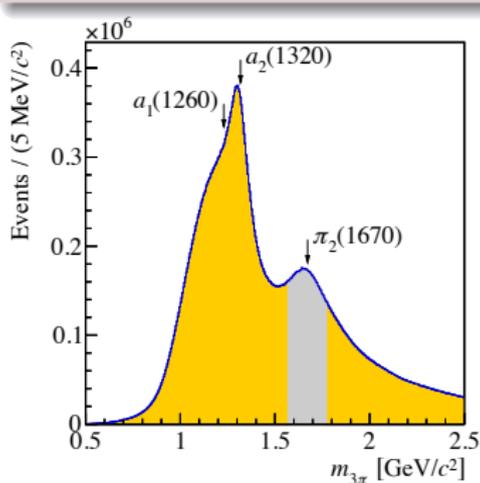
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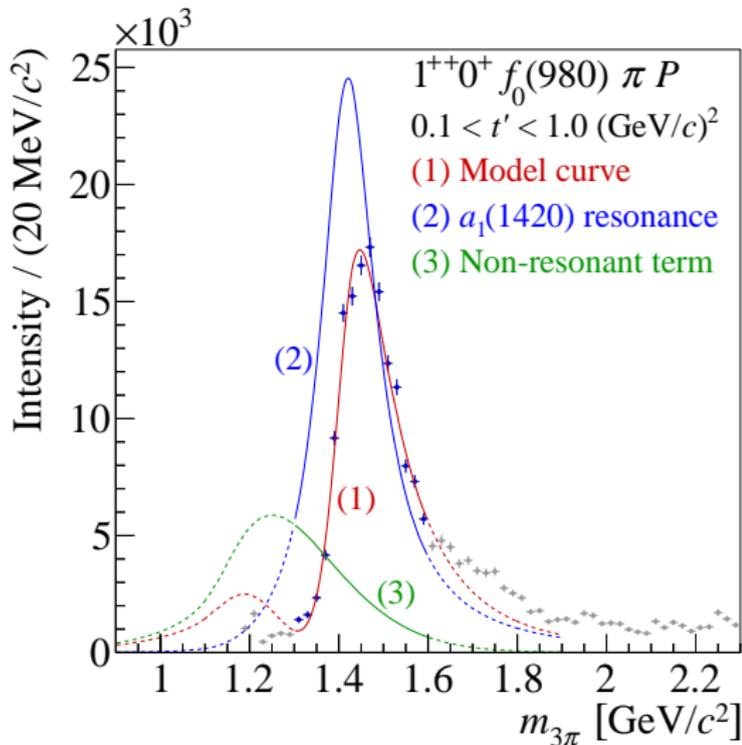


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Improved sensitivity for small signals

- E.g. surprising find: **resonance-like $a_1(1420)$ signal** in peculiar decay mode
- Only **0.3 % of total intensity**



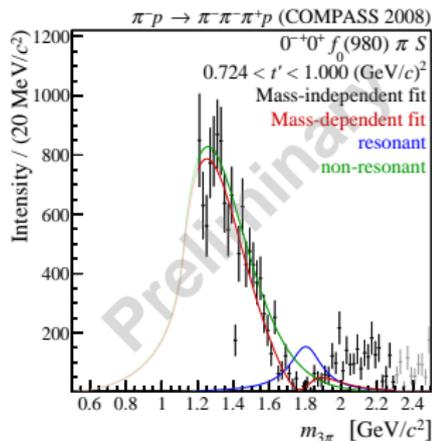
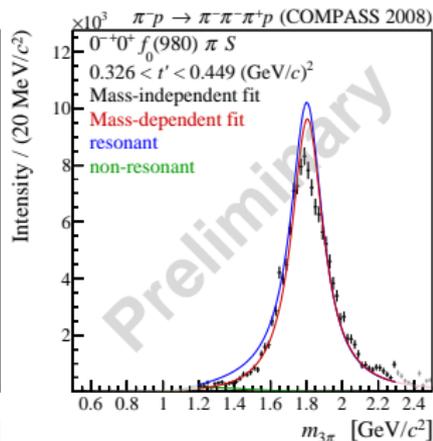
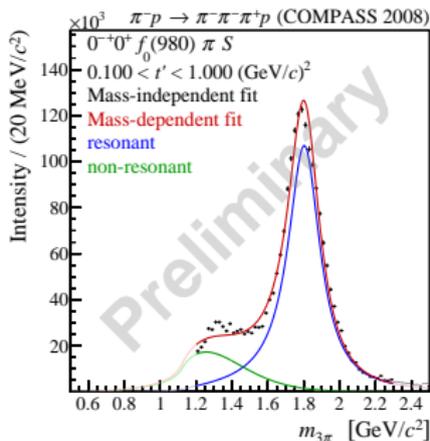
COMPASS, PRL **115** (2015) 082001

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PWA in narrow bins of four-momentum transfer squared t'

- Resolve t' dependence of partial-wave amplitudes
- Improved separation between resonant and nonresonant components in resonance-model fits
- First extraction of t' spectra of resonances from such an analysis
⇒ can study production mechanism(s)

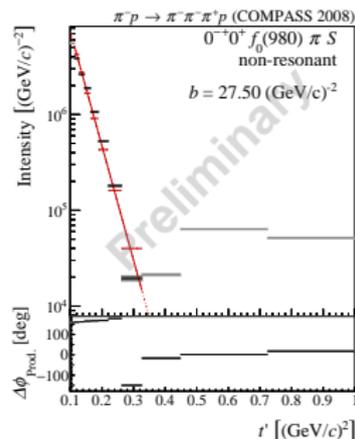
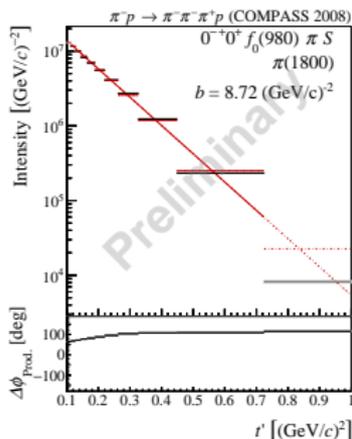
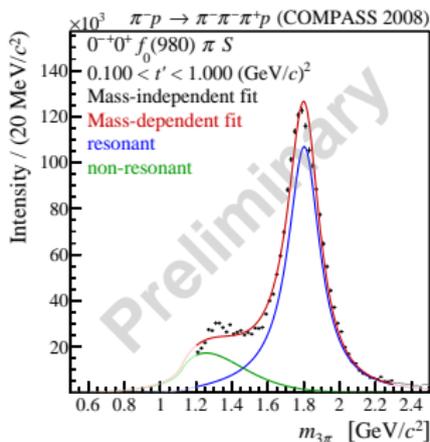


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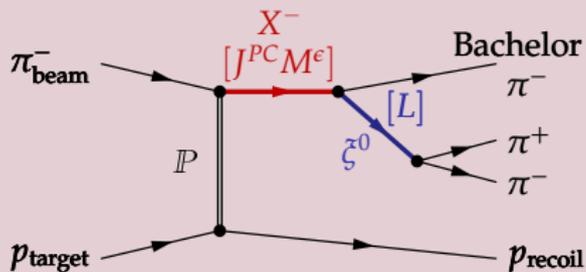


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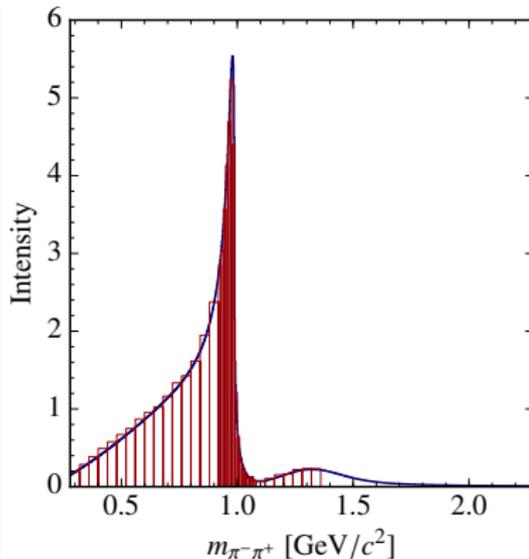
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Novel analysis technique: “freed-isobar” PWA

Krinner *et al.*, PRD **97** (2018) 114008



- Conventional PWA requires complete **knowledge of isobar amplitude**
- *Novel approach*: replace fixed parametrization by step functions
 - **Isobar amplitude determined from data** \Rightarrow reduced model dependence
 - E.g. amplitude of $\pi^- \pi^+$ subsystem with $J^{PC} = 0^{++}$
 $\Rightarrow f_0(500)$ (?), $f_0(980)$, $f_0(1500)$

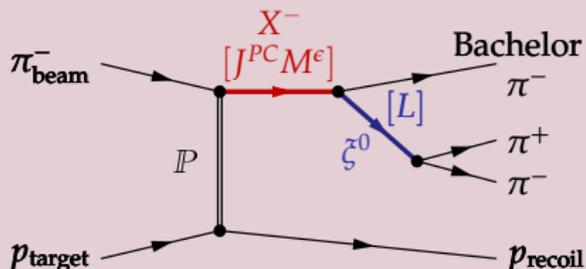


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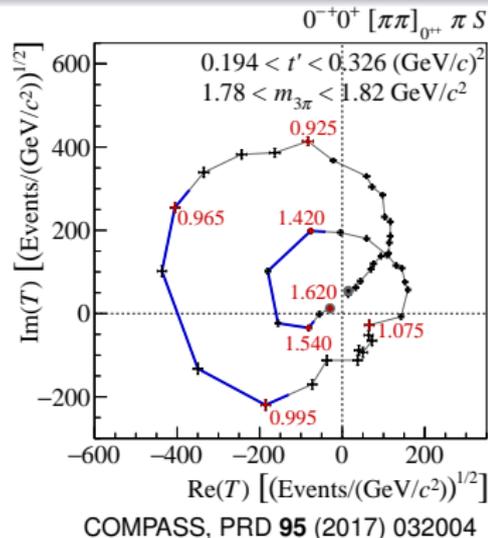
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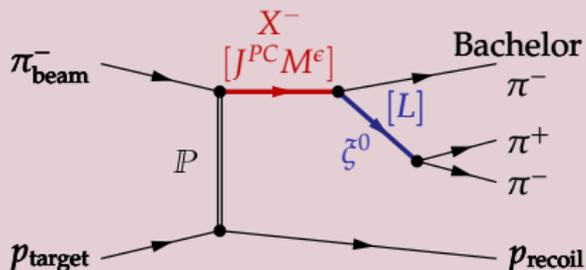


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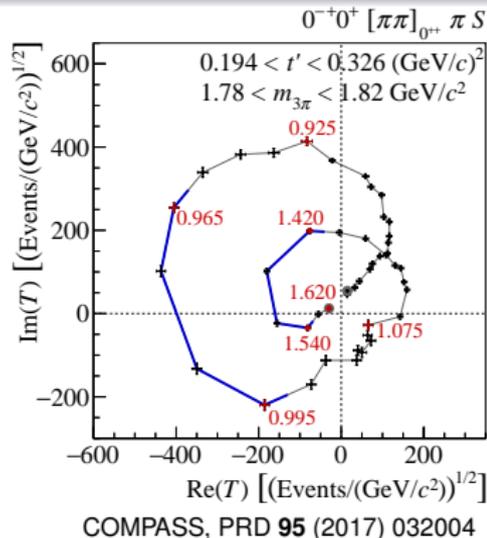
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- Would allow to **study $K^- \pi^+$ subsystem** with $J^P = 0^+$ in $K^- \pi^- \pi^+$
- Requires huge data samples