



AMBER

# Hadron Physics with AMBER at CERN

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4 December 2021

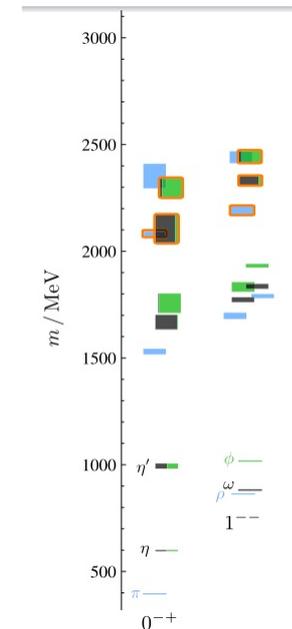
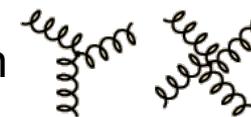
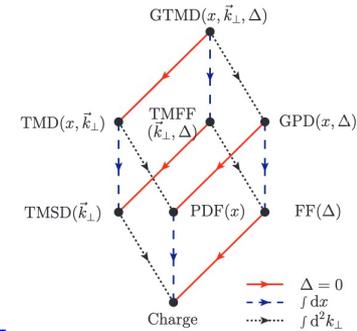
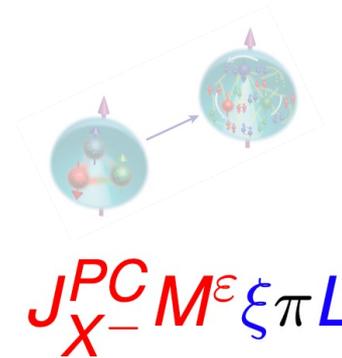


*On behalf of the AMBER Collaboration*

**Light Cone 2021**

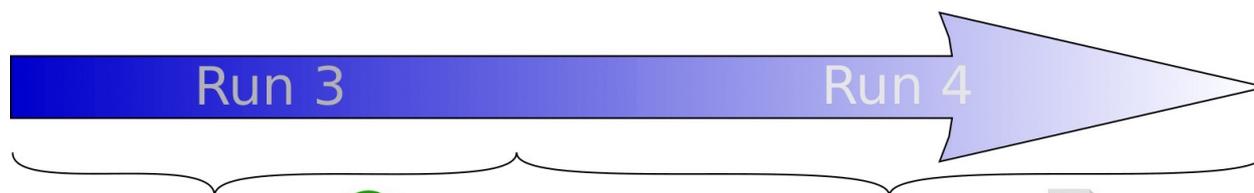
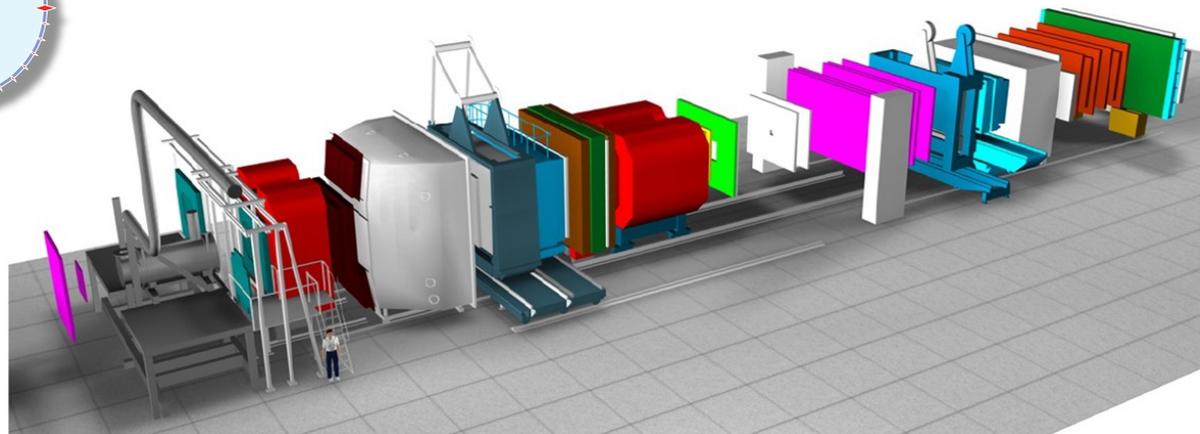
*Jeju Island, Korea*

- QCD **partons** in hadronic systems
- The **excitation** scheme of hadronic systems
- How do the **hadron masses** come about?
  - constituents: the QCD quarks and gluons
  - Small contribution of the Higgs mass of the valence quarks
  - Pion-to-proton mass ratio 1/7 vs. constituent quark expectation 2/3
- Dynamic generation of mass in continuum QCD
- Gluon self-interaction in the infra-red leads to gluon “self-mass generation”
- **E**mergence of **H**adron **M**ass is to some extent understood within continuum and lattice QCD calculations
- Prove and provide more input by measurement of
  - Quark and gluon PDFs of **pion**, **kaon** and proton
  - Hadron radii as consequence of confinement
  - Mass spectra of excited mesons



## Apparatus for Meson and Baryon Experimental Research

- Successor of *COMPASS*
- with appropriate extensions and modernisations
- at the CERN M2 beamline



Phase-1 Proposal



- Submitted 2018
- Approved by the CERN Research Board in Dec 2020

Phase-2



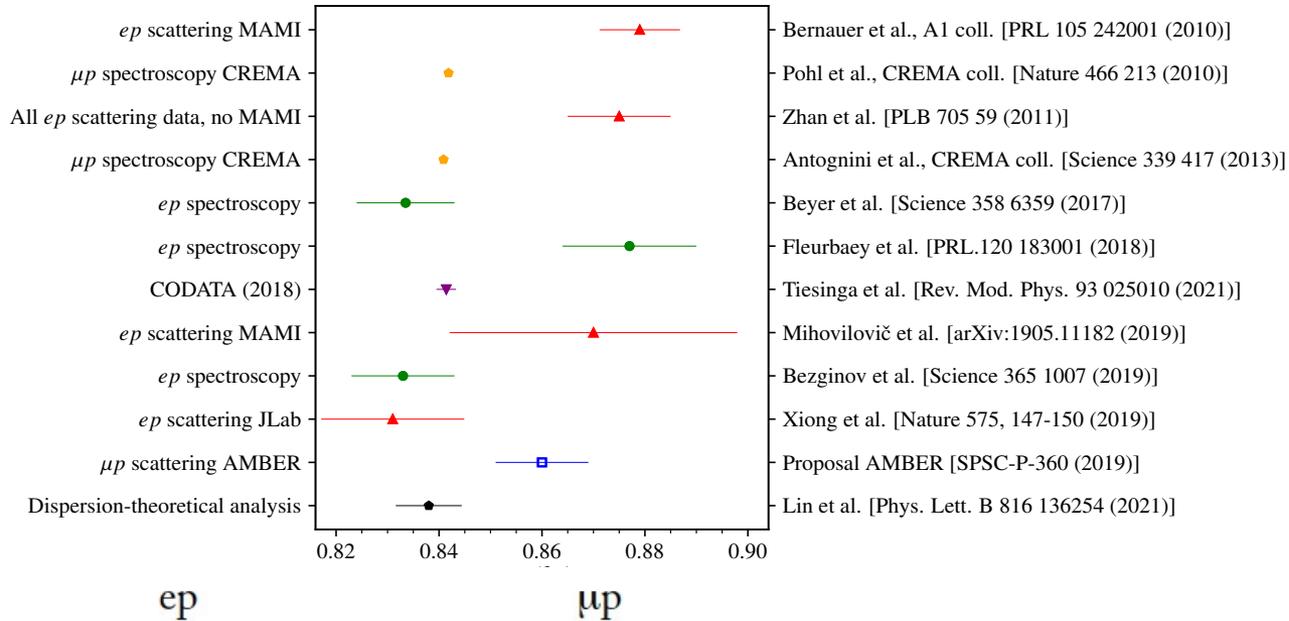
- Submission planned for 2022

Program	Physics Goals	Beam Energy [GeV]	Beam Intensity [ $s^{-1}$ ]	Trigger Rate [kHz]	Beam Type	Target	Earliest start time, duration	Hardware additions
muon-proton elastic scattering	Precision proton-radius measurement	100	$4 \cdot 10^6$	100	$\mu^\pm$	high-pressure H2	2022 1 year	active TPC, SciFi trigger, silicon veto, recoil silicon,
Hard exclusive reactions	GPD $E$	160	$2 \cdot 10^7$	10	$\mu^\pm$	$NH_3^\dagger$	2022 2 years	modified polarised target magnet
Input for Dark Matter Search	$\bar{p}$ production cross section	20-280	$5 \cdot 10^5$	25	$p$	LH2, LHe	2022 1 month	liquid helium target
$\bar{p}$ -induced spectroscopy	Heavy quark exotics	12, 20	$5 \cdot 10^7$	25	$\bar{p}$	LH2	2022 2 years	target spectrometer: tracking, calorimetry
Drell-Yan	Pion PDFs	190	$7 \cdot 10^7$	25	$\pi^\pm$	C/W	2022 1-2 years	
Drell-Yan (RF)	Kaon PDFs & Nucleon TMDs	$\sim 100$	$10^8$	25-50	$K^\pm, \bar{p}$	$NH_3^\dagger$ , C/W	2026 2-3 years	"active absorber", vertex detector
Primakoff (RF)	Kaon polarisability & pion life time	$\sim 100$	$5 \cdot 10^6$	$> 10$	$K^-$	Ni	non-exclusive 2026 1 year	
Prompt Photons (RF)	Meson gluon PDFs	$\geq 100$	$5 \cdot 10^6$	10-100	$K^\pm$ $\pi^\pm$	LH2, Ni	non-exclusive 2026 1-2 years	hodoscope
$K$ -induced Spectroscopy (RF)	High-precision strange-meson spectrum	50-100	$5 \cdot 10^6$	25	$K^-$	LH2	2026 1 year	recoil TOF, forward PID
Vector mesons (RF)	Spin Density Matrix Elements	50-100	$5 \cdot 10^6$	10-100	$K^\pm, \pi^\pm$	from H to Pb	2026 1 year	

Phase-1  
with conventional hadron and muon beams  
2022 → 2028

Phase-2  
with conventional and rf-separated beams  
2029 and beyond

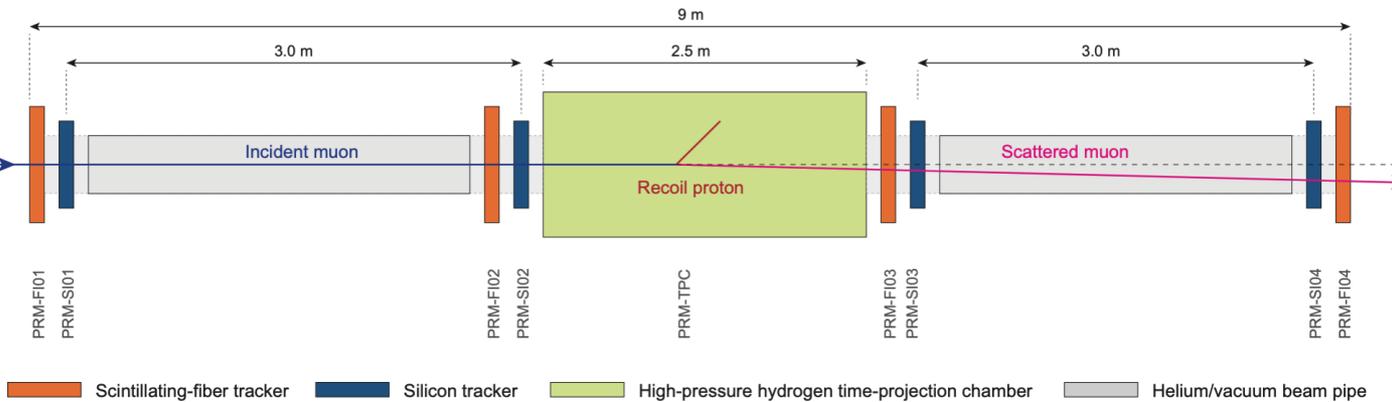
Table 2: Requirements for future programmes at the M2 beam line after 2021. Muon beams are in blue, conventional hadron beams in green, and RF-separated hadron beams in red.



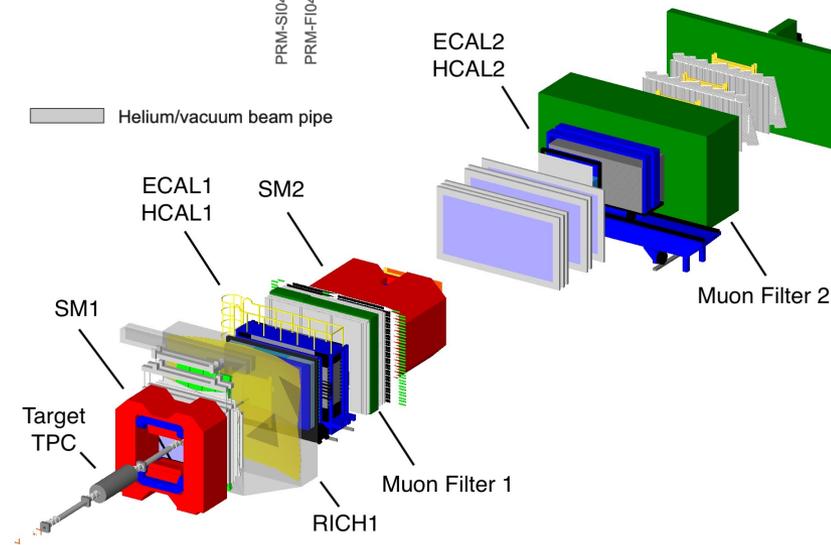
	$ep$	$\mu p$
Spectroscopy	<p>New measurements with</p> <ul style="list-style-type: none"> <li>lower systematics</li> <li>new transitions</li> </ul>	
Scattering	<p>New measurements with</p> <ul style="list-style-type: none"> <li>lower systematics</li> <li>reaching lower <math>Q^2</math></li> </ul> <p>ProRAD, ULQ2, ISR @ MESA, PRad</p>	<p>No data yet.</p> <p>MUSE at PSI coming soon</p>

- $\mu p$  scattering:
- Different systematic uncertainties
  - small radiative corrections

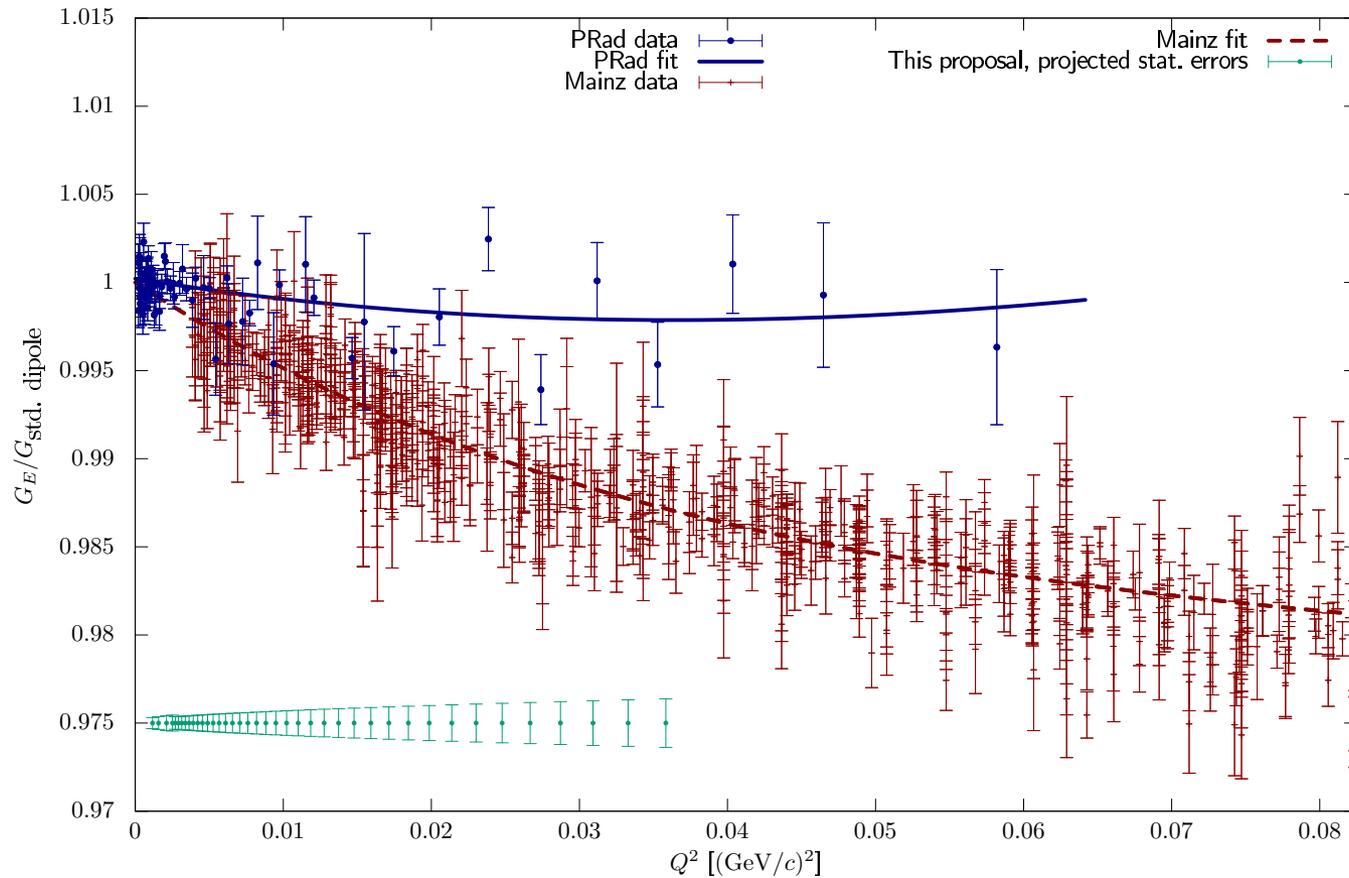
# Muon-proton scattering at high energy



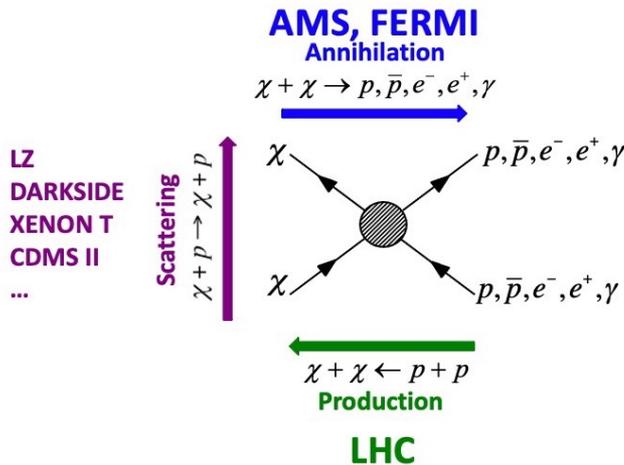
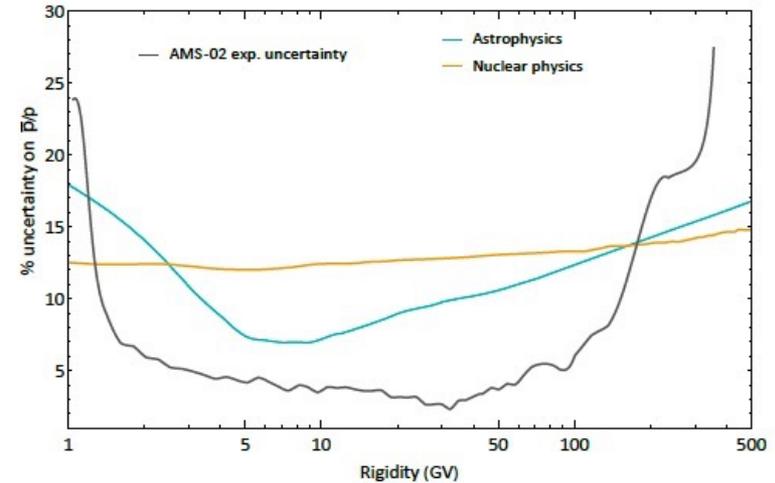
- 100 GeV muon beam
- Active-target TPC with high-pressure H<sub>2</sub>
- goal: 70 million elastic scattering events in the  $10^{-3} < Q^2 < 4 \cdot 10^{-2} \text{ GeV}^2$  range
- Precision on the proton radius  $\sim 0.01 \text{ fm}$
- Pilot run with smaller TPC in 2021



# Precision on the proton form factor measurement with 100 GeV muons



- New AMS(2) data – the antiparticle flux is well known now (few % prec.) (<http://dx.doi.org/10.1103/PhysRevLett.117.091103>)
- Two types of processes contribute – SM interactions (proton on the inter-stellar matter with the production for example of antiprotons) and contribution from dark particle – antiparticle annihilation;
- In order to detect a possible excess in the antiparticles flux a good knowledge of inclusive cross sections of p-He interaction with antiparticles in the final state is a must, currently the typical precision is of 30-50%.



AMBER proton beam: from a few tens of GeV/c up to 250 GeV/c, in the pseudo-rapidity range  $2.4 < \eta < 5.6$ . Goal is to measure the doubly differential (momentum and pseudo-rapidity) antiproton production cross section from p+H and p+He at different proton momenta (50, 100, 190, 250 GeV/c).

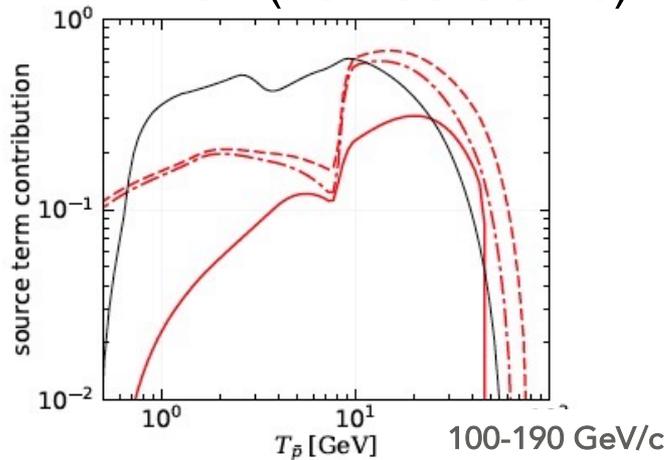
# Antiproton production cross section **AMBER**

The impact of the proposed p + p measurements on constraining the production of cosmic anti-protons versus their kinetic energy. Each curve represents the fraction of anti-proton production phase space as constrained by AMBER cross section measurements in p-p, p-He and He-p channels, compared to NA61 (p-p) and LHC-b (p-He) measurements

p-H channel, in three different energy ranges

**AMBER**

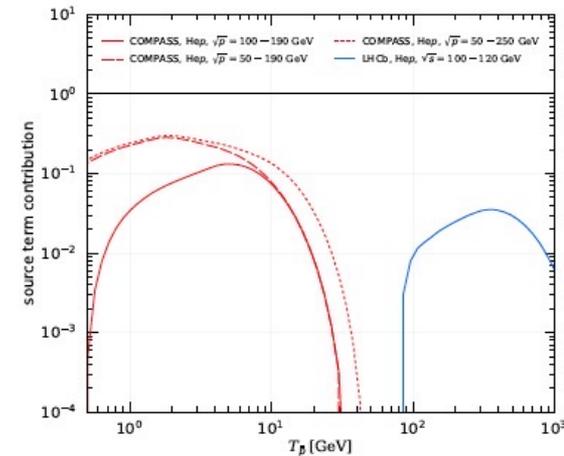
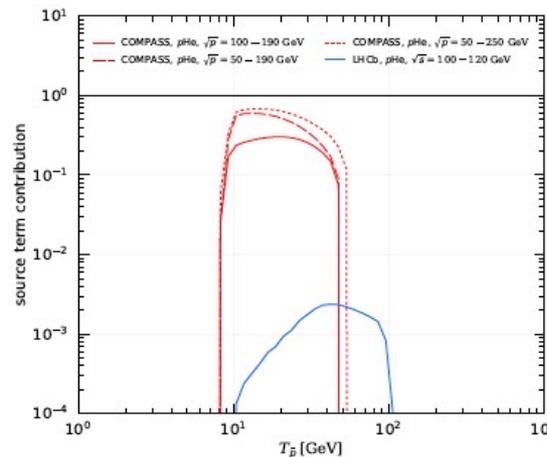
NA61 (20-158 GeV/c)



50-190 GeV/c

50 - 250 GeV/c

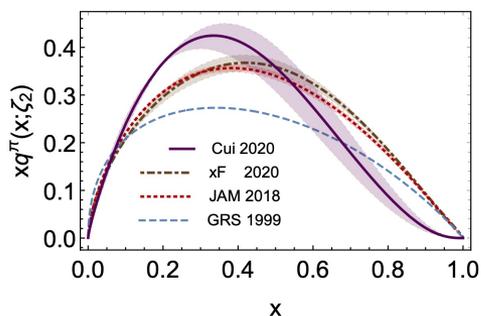
p-He and He-p channels **AMBER**  
**LHCb**



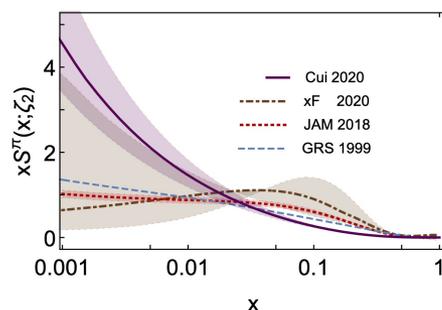
# Pion-induced Drell-Yan

## Status of knowledge of the pion structure

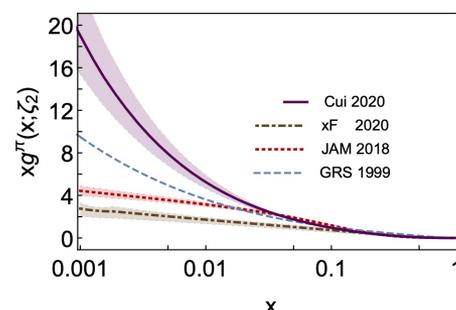
*valence quarks*



*sea quarks*

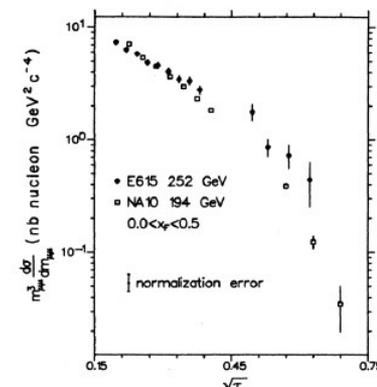


*gluons*



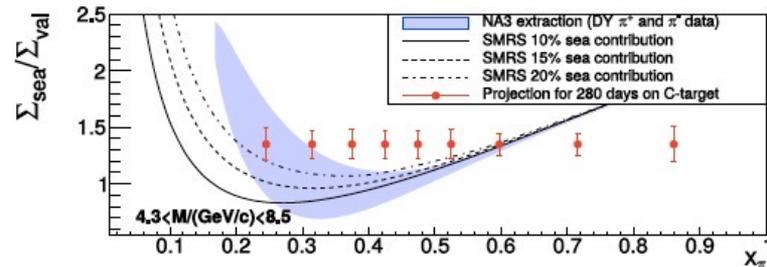
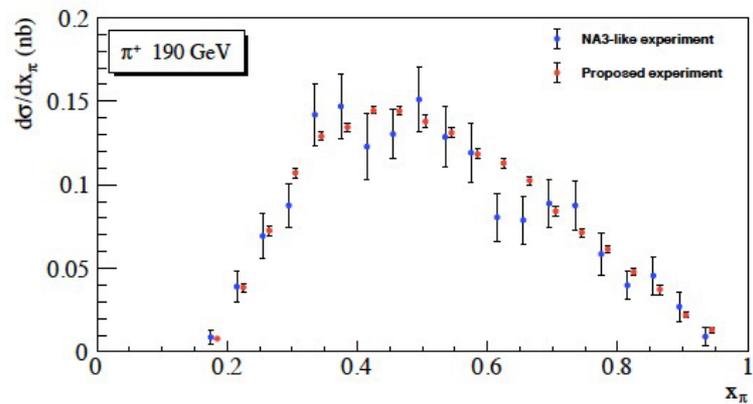
plots from: Chang & Roberts, arXiv:2106.08451v1

From: E615, PRD 1989



### Pion structure status:

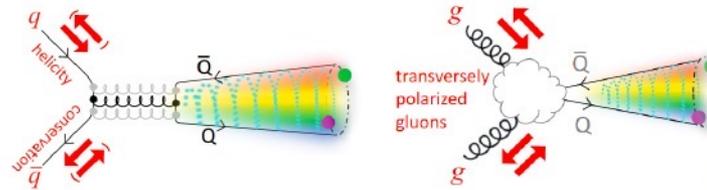
- Scarce data, poor knowledge of valence, sea and glue basically unknown
- Mostly heavy nuclear targets: large nuclear effects
- For some experiments, no information on absolute cross sections
- Two experiments (E615, NA3) have measured so far with both pion beam signs, but only one (NA3) has used its data to separate sea-valence quark contributions
- Discrepancy between different experiments (i.e. NA10, E615)
- Old data, no way to reanalyse them using modern approaches



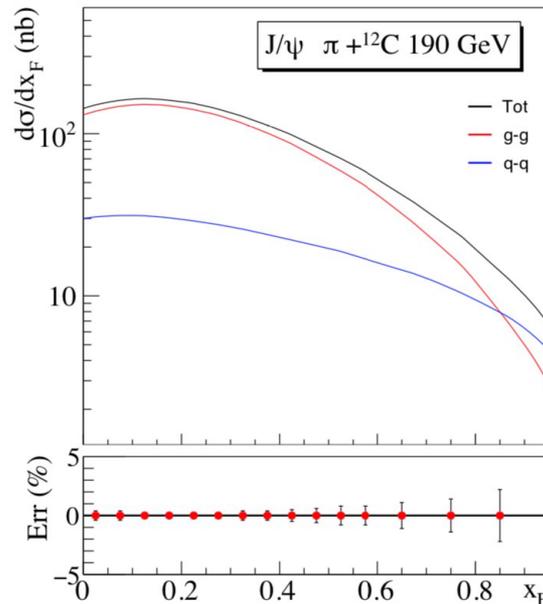
- Pion structure in pion induced DY
- Expected accuracy as compared to NA3

Experiment	Target type	Beam energy (GeV)	Beam type	Beam intensity (part/sec)	DY mass (GeV/c <sup>2</sup> )	DY events
E615	20 cm W	252	$\pi^+$	$17.6 \times 10^7$	4.05 – 8.55	5000
			$\pi^-$	$18.6 \times 10^7$		30000
NA3	30 cm H <sub>2</sub>	200	$\pi^+$	$2.0 \times 10^7$	4.1 – 8.5	40
			$\pi^-$	$3.0 \times 10^7$		121
	6 cm Pt	200	$\pi^+$	$2.0 \times 10^7$	4.2 – 8.5	1767
			$\pi^-$	$3.0 \times 10^7$		4961
NA10	120 cm D <sub>2</sub>	286	$\pi^-$	$65 \times 10^7$	4.2 – 8.5	7800
		140				4.35 – 8.5
	12 cm W	286	$\pi^-$	$65 \times 10^7$	4.2 – 8.5	49600
		194				4.07 – 8.5
		140			4.35 – 8.5	29300
COMPASS 2015	110 cm NH <sub>3</sub>	190	$\pi^-$	$7.0 \times 10^7$	4.3 – 8.5	35000
COMPASS 2018						52000
This exp	75 cm C	190	$\pi^+$	$1.7 \times 10^7$	4.3 – 8.5	21700
			$\pi^-$			31000
	12 cm W	190	$\pi^+$	$6.8 \times 10^7$	4.3 – 8.5	67000
			$\pi^-$			91100
		190	$\pi^+$	$0.4 \times 10^7$	4.3 – 8.5	8300
			$\pi^-$			11700
		190	$\pi^-$	$1.6 \times 10^7$	4.3 – 8.5	24100
					4.0 – 8.5	32100

Isoscalar target + Both positive and negative beams + High statistics

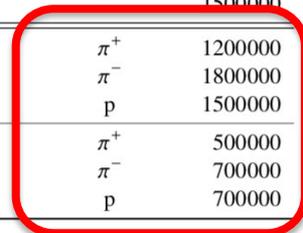


Cheung and Vogt, priv. comm.



Improved CEM, CT10 + GRS99  
global fit for proton/pion

Experiment	Target type	Beam energy (GeV)	Beam type	$J/\psi$ events
NA3 [76]	Pt	150	$\pi^-$	601000
		280	$\pi^-$	511000
		200	$\pi^+$ $\pi^-$	131000 105000
E789 [129, 130]	Cu	800	p	200000
	Au			110000
	Be			45000
E866 [131]	Be	800	p	3000000
	Fe			
	Cu			
NA50 [132]	Be	450	p	124700
	Al			100700
	Cu			130600
	Ag			132100
	W			78100
NA51 [133]	p	450	p	301000
	d			312000
HERA-B [134]	C	920	p	152000
COMPASS 2015	110 cm NH <sub>3</sub>	190	$\pi^-$	1000000
COMPASS 2018				1500000
This exp	75 cm C	190	$\pi^+$	1200000
			$\pi^-$	1800000
			p	1500000
This exp	12 cm W	190	$\pi^+$	500000
			$\pi^-$	700000
			p	700000

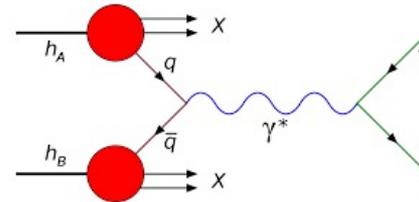


- simultaneously collected with DY data, with large counting rates

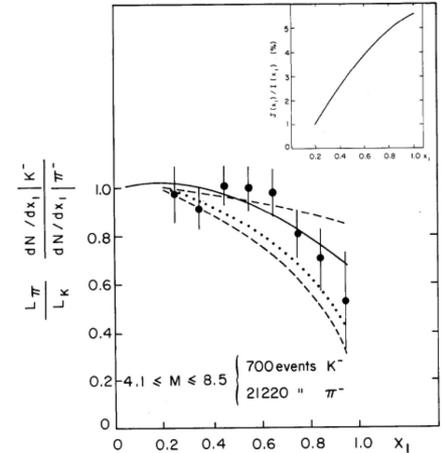
Physics objectives:

- Study of the  $J/\psi$  (charmonia) production mechanisms ( $gg$ -fusion vs  $q\bar{q}$ -annihilation), comparison of **CEM** and **NRQCD**
- Probe gluon and quark PDFs of pion
- arXiv:2103.11660v1
- $\Psi(2S)$  signal study, free of feed-down effect from  $X_{c1}$   $X_{c2}$

# Farer future: Kaon structure via the Drell-Yan process

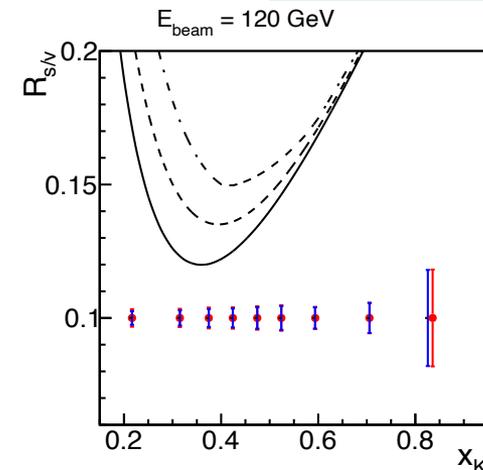
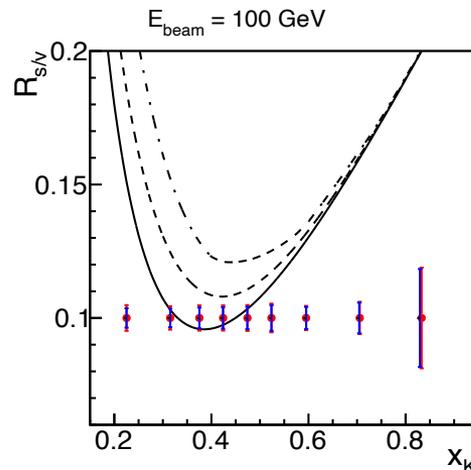
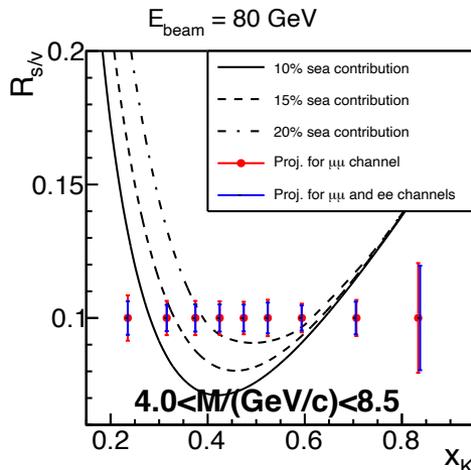


NA3: PLB 93 (1980) 354

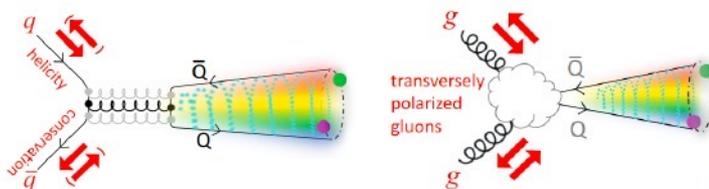


- Available data
  - Only 700 events from NA3
  - The kaon valence distributions are practically unknown
  - There is no data on kaon sea and gluon content
- Prospects for AMBER measurements
  - Kaon valence PDF: can be addressed with negative kaon beam
  - Kaon sea PDF: combine the two beam charges

$$R_{S/v} = \frac{\sigma(K^+)}{\sigma(K^+) + \sigma(K^-)}$$



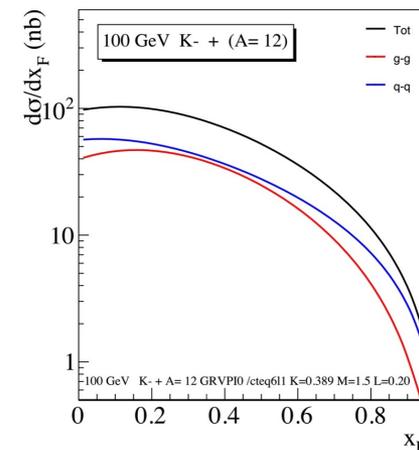
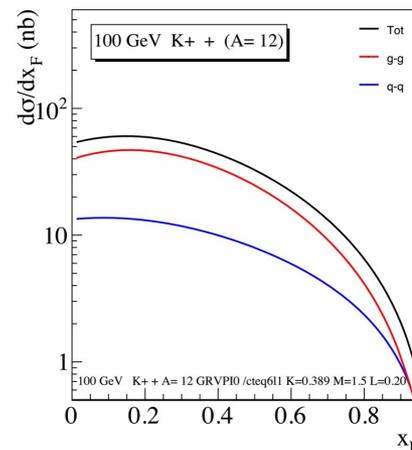
Status as  
of Lol



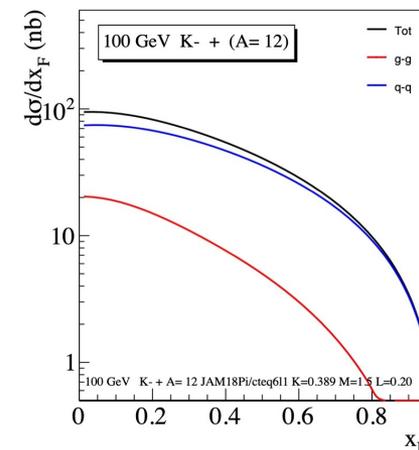
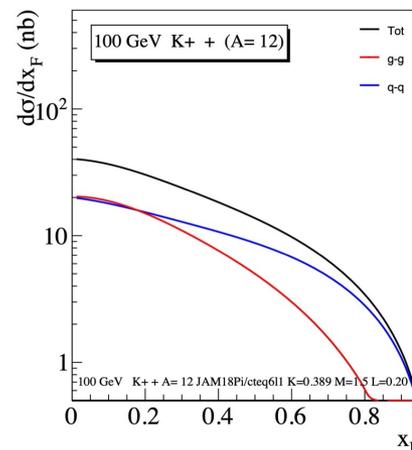
- The difference between the two kaon charges is sensitive to isolate the **valence quark contribution**
- Possibility to access the **gluon structure** of the kaon
- Opportunity to study the  $J/\psi$  **production mechanism** ( $gg$  vs.  $q\bar{q}$ )
- For 80 GeV beam energy, we aim at 300k events for each kaon charge

strong dependence on the kaon PDF parametrisation

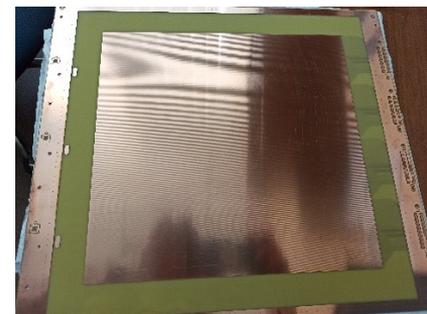
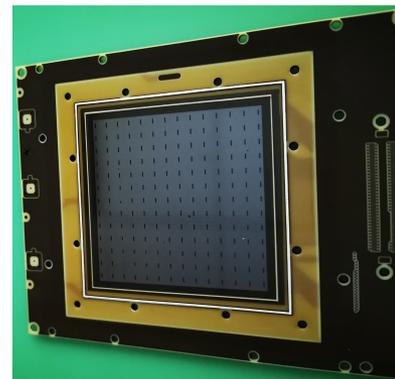
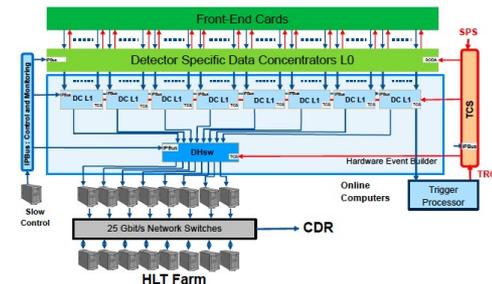
PDF: from GRV (pion)



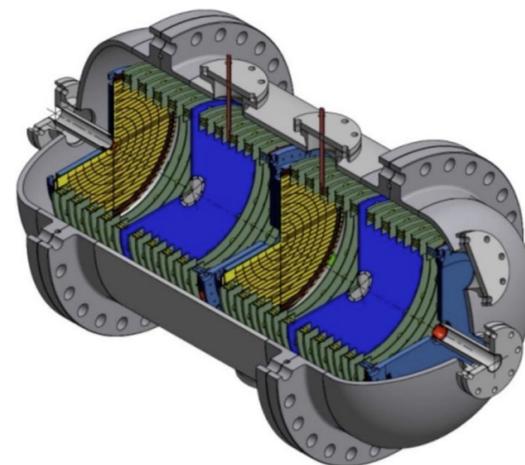
PDF: from JAM (pion)



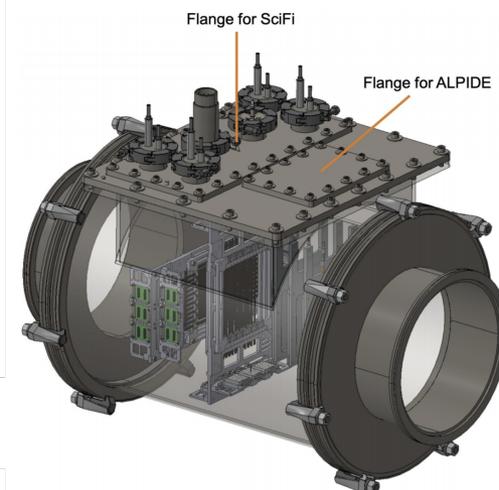
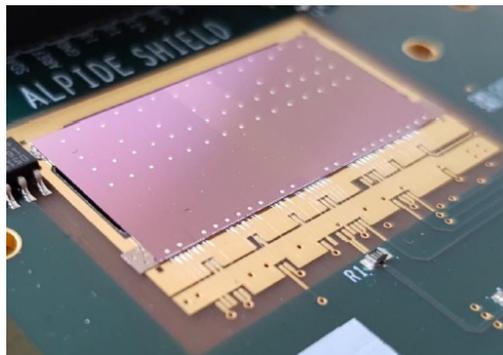
- New triggerless DAQ system, new front-end electronics and trigger logic compatible with triggerless readout
- New large-size PixelGEM detectors
- New large-area micro-pattern gaseous detectors (MPGD)
- High-rate-capable CEDARs detectors (beam line)
- A new RICH-0 detector to extend significantly phase space coverage (lower momenta)



- High-pressure hydrogen filled active TPC (PRM)
- Combined scintillating fibres / silicon tracking system (4 stations) (PRM)
- Triggerless electromagnetic calorimeter electronics (PRM)
- High rate capable silicon-based vertex detector (DY)
- New high-purity and high efficiency di-muon trigger (DY)



ECAL2 DAQ Hardware – Carrier Board III



# Collaboration founding

- currently 189 full members (PhD and above) from 12 countries and ~40 institutions, growing up
- (proto-)Collaboration Board meetings since (April 2019) August 2020
- Since Feb 2021: Memorandum of Understanding writing group
- May 2021: First Collaboration Meeting



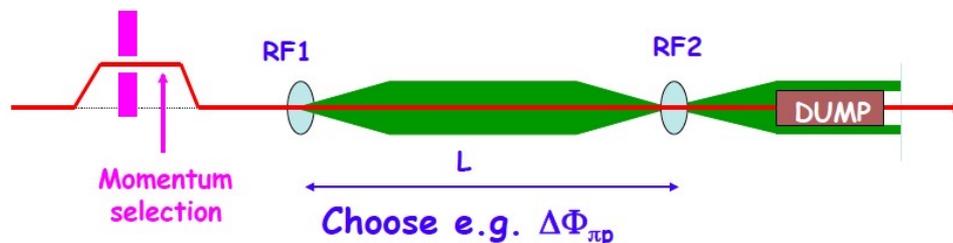
- Second Collaboration Meeting September 2021
- Initial annual budget (for 2022) ~400kCHF
- Submission of Phase-2 Proposal planned for beginning of 2022
- Theory workshop series “Emergence of Hadron Mass”

## Perceiving the Emergence of Hadron Mass through **AMBER@CERN**

27 April to 30 April 2021  
CERN, Geneva - Switzerland



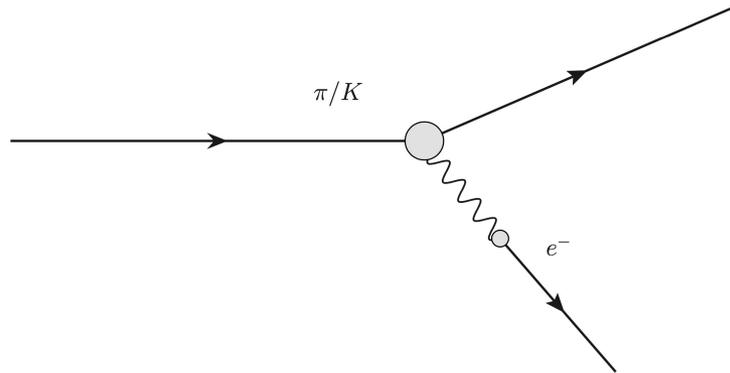
- Sixth 3-day workshop in September 27-29
- Focus on physics cases for rf-separated hadron beams
- Followed by a 1-day workshop of the CERN accelerator group
- Large physics cases: Kaon-induced meson spectroscopy and Drell-Yan processes



Particle species separation  
by radio-frequency modulation

$$\Delta\Phi = 2\pi (L f / c) (\beta_1^{-1} - \beta_2^{-1}) \text{ with } \beta_1^{-1} - \beta_2^{-1} = (m_1^2 - m_2^2) / 2p^2$$

# A physics case with rf-separated kaon beam: kaon radius



$$K^- e^-_{target} \rightarrow K^- e^-$$

S. R. Amendolia, et al. , Phys. Lett. B **178**, 435 (1986)

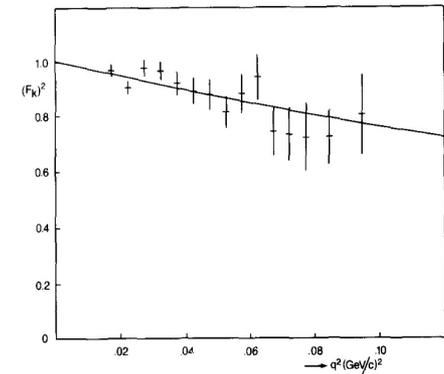


Fig. 3. The measured kaon form factor squared. The line corresponds to the pole fit with  $\langle r^2 \rangle = 0.34 \text{ fm}^2$ .

Beam	$E_b$ [GeV]	$Q_{max}^2$ [GeV <sup>2</sup> ]	$E'_{b,min}$ [GeV]	Relative charge-radius effect on c.s. at $Q_{max}^2$
$\pi$	190	0.176	17.3	~40%
$K$	190	0.086	105.7	~20%
	80	0.066	59.9	~15%
	50	0.037	41.3	~8%

- For **kaons**, a significant increase of the form factor knowledge in the range  $0.001 < Q^2 < 0.07$  appears in reach with AMBER using an **80 GeV rf-separated kaon beam**

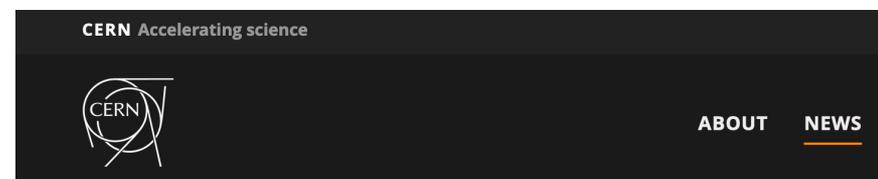
# Possible timelines for AMBER and ongoing/planned other experiments to study EHM



- NA66/AMBER is a new collaboration at CERN dedicated to hadron research at the M2 beamline
- Broad physics program from hadron radii to parton distributions in Drell-Yan processes
- Collaboration formation is ongoing - approach us if interested!

<https://amber.web.cern.ch>

<https://home.cern/news/news/physics/meet-amber>



*Voir en [français](#)*

## Meet AMBER

The next-generation successor of the COMPASS experiment will measure fundamental properties of the proton and its relatives

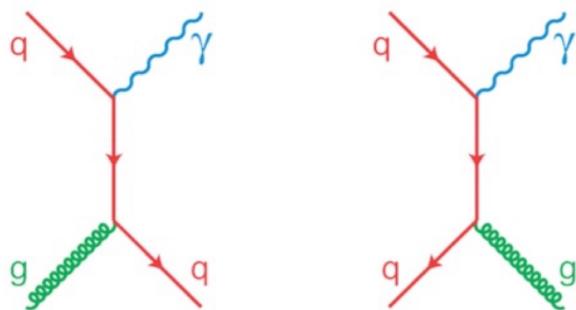
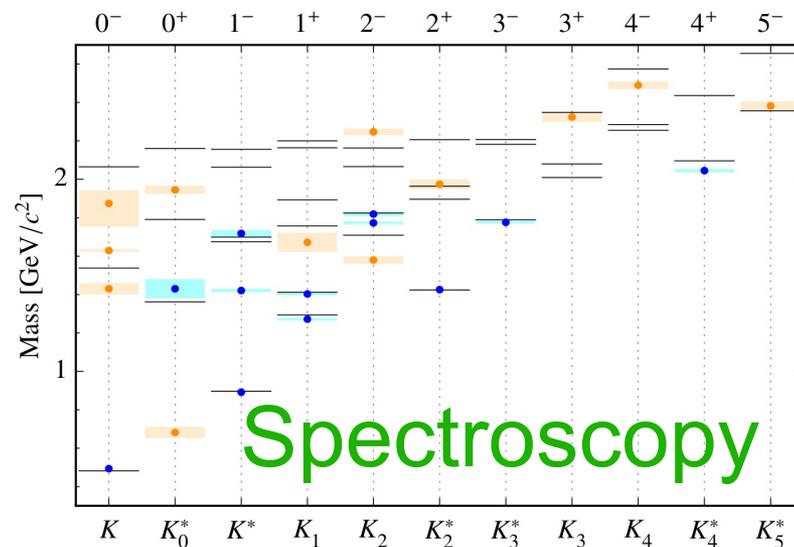
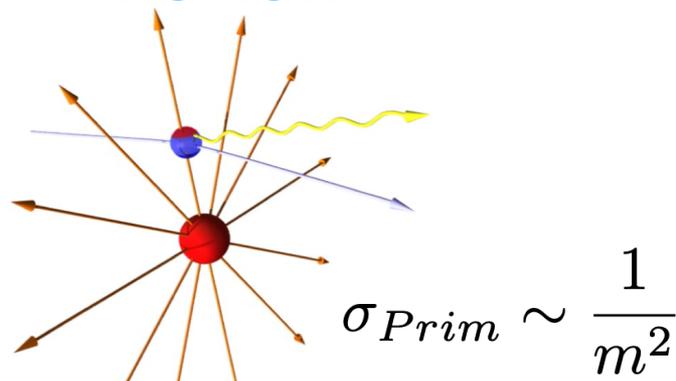
8 MARCH, 2021 | By [Ana Lopes](#)



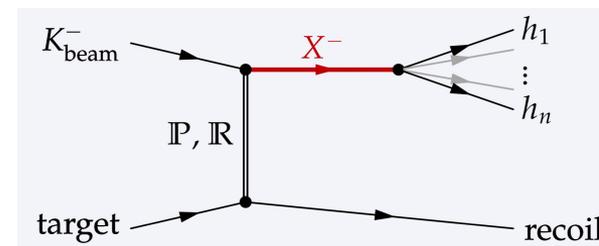


# Backup

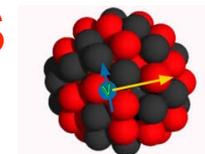
## Primakoff



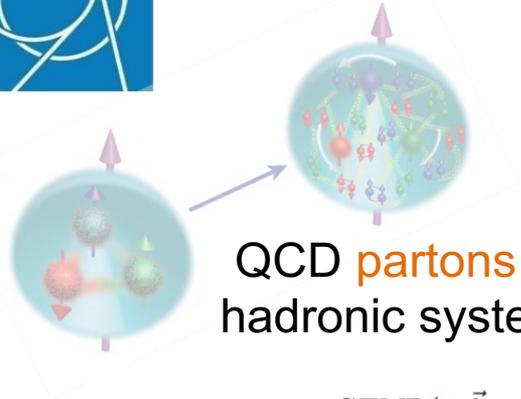
## Prompt photons



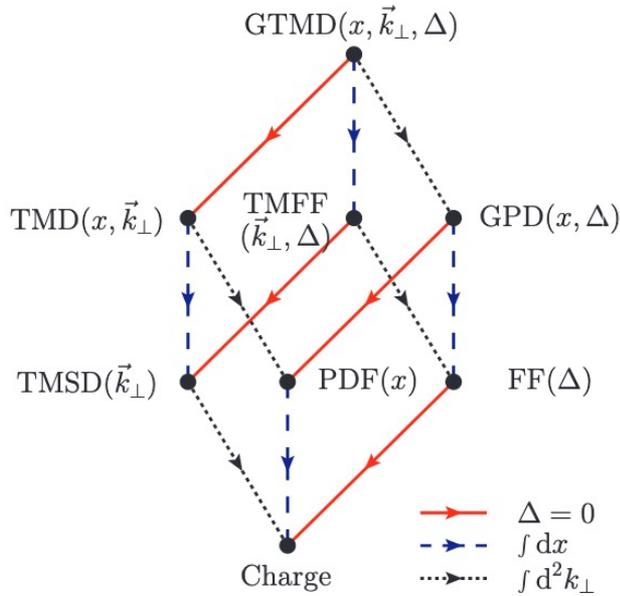
## Vector mesons



# Open Questions in Hadron Physics



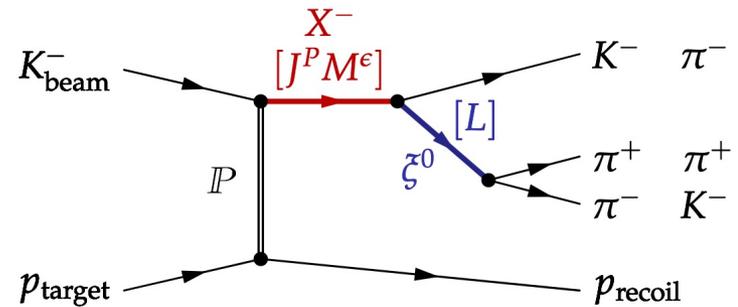
QCD **partons** in hadronic systems



The complete picture:  
Wigner distributions

[from: Lorcé, Pasquini, Vanderhaeghen, JHEP05 (2011)]

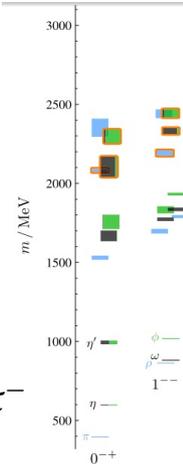
The **excitation** scheme of hadronic systems



$$J^P C \quad X^- M^E \xi \pi L$$

Measurable quantities: (iso)spin-parity, masses, couplings and decay widths

[from: Grube, EHM workshop (2020)]



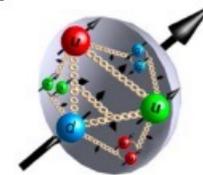
# A fundamental question: how do the **hadron masses** come about?

Pion


- $M_\pi \sim 140\text{MeV}$
- Spin 0
- 2 light valence quarks

Kaon

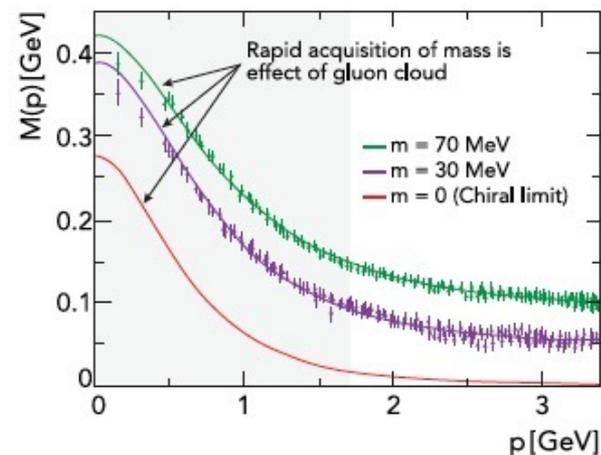
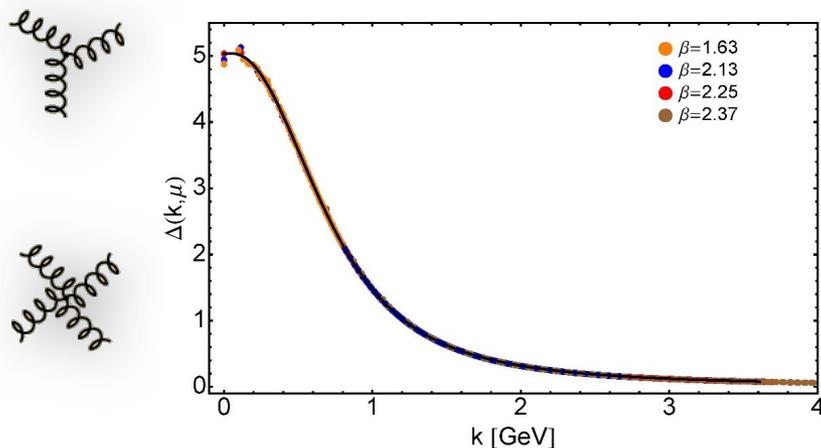

- $M_K \sim 490\text{MeV}$
- Spin 0
- 1 light and 1 "heavy" valence quarks

Proton


- $M_p \sim 940\text{MeV}$
- Spin 1/2
- 3 light valence quarks

- As composite systems, hadrons are to be understood in terms of their constituents: the QCD quarks and gluons
- The Higgs mass of the valence quarks contributes only little to the physical hadron masses
- Pion-to-proton mass ratio 1/7 much different from the constituent-quark inspired value of 2/3

- Dynamic generation of mass in continuum QCD
- Gluon self-interaction in the infra-red leads to gluon “self-mass generation”

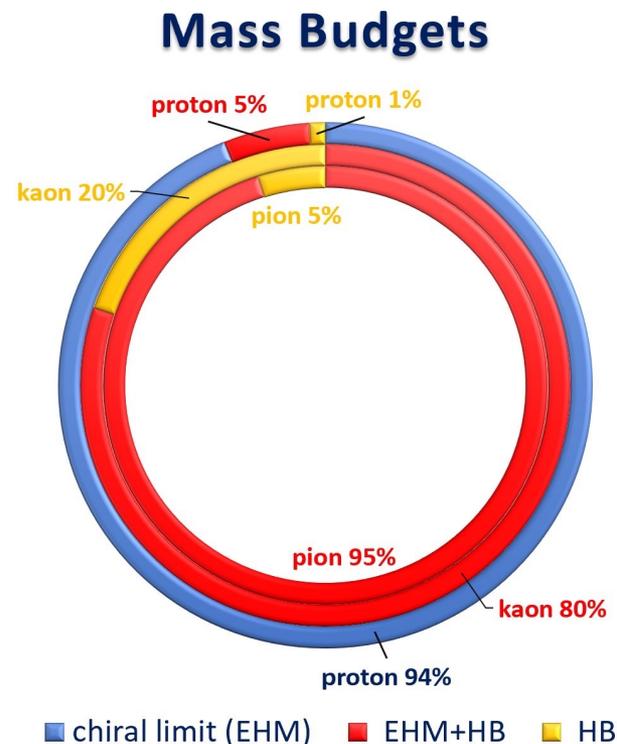


- Emergence of Hadron Mass is to some extent understood within continuum and lattice QCD calculations
- Prove and provide more input by measurement of
  - Quark and gluon PDFs of pion, kaon and proton
  - Hadron radii as consequence of confinement
  - Mass spectra of excited mesons

# EHM for proton, pion and kaon

- The mass composition of the proton is structurally different from that of pions and kaons
- Pions and kaons are the Nambu-Goldstone bosons of the (approximate and spontaneously broken) chiral symmetry of strong interaction
- In the chiral limit
  - the mass of the proton remains basically unchanged
  - pions and kaons are massless

Thus for a full understanding the partonic structure of hadrons, the meson PDFs must be known on a similar level as those of the nucleon



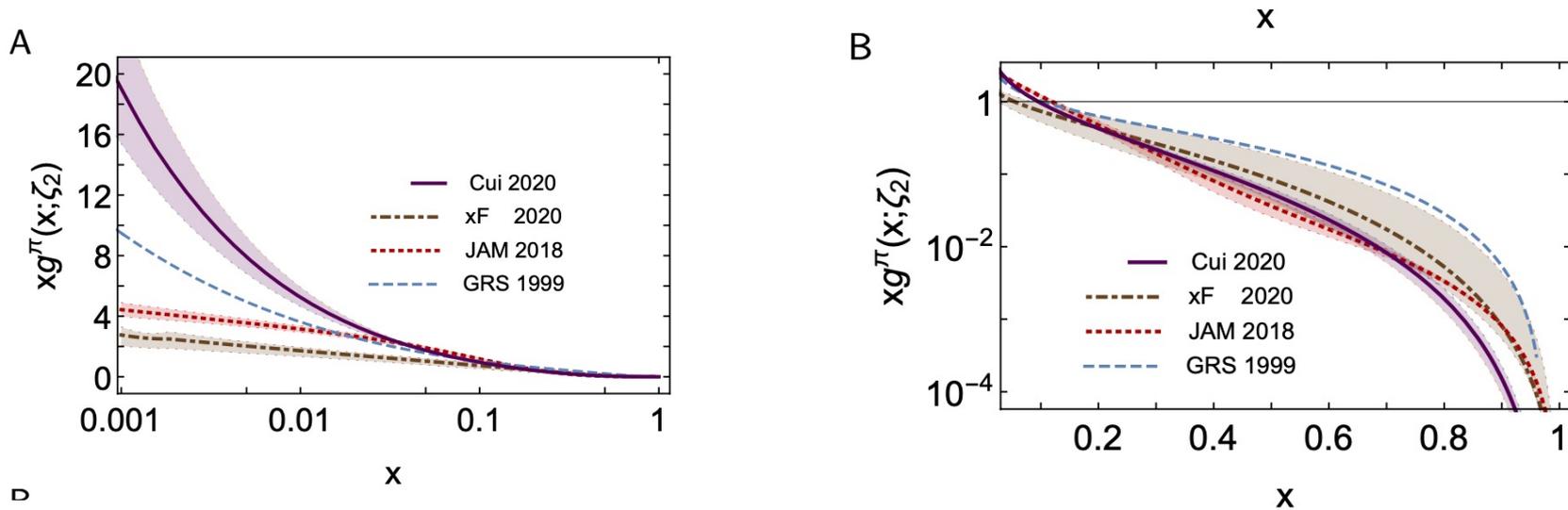
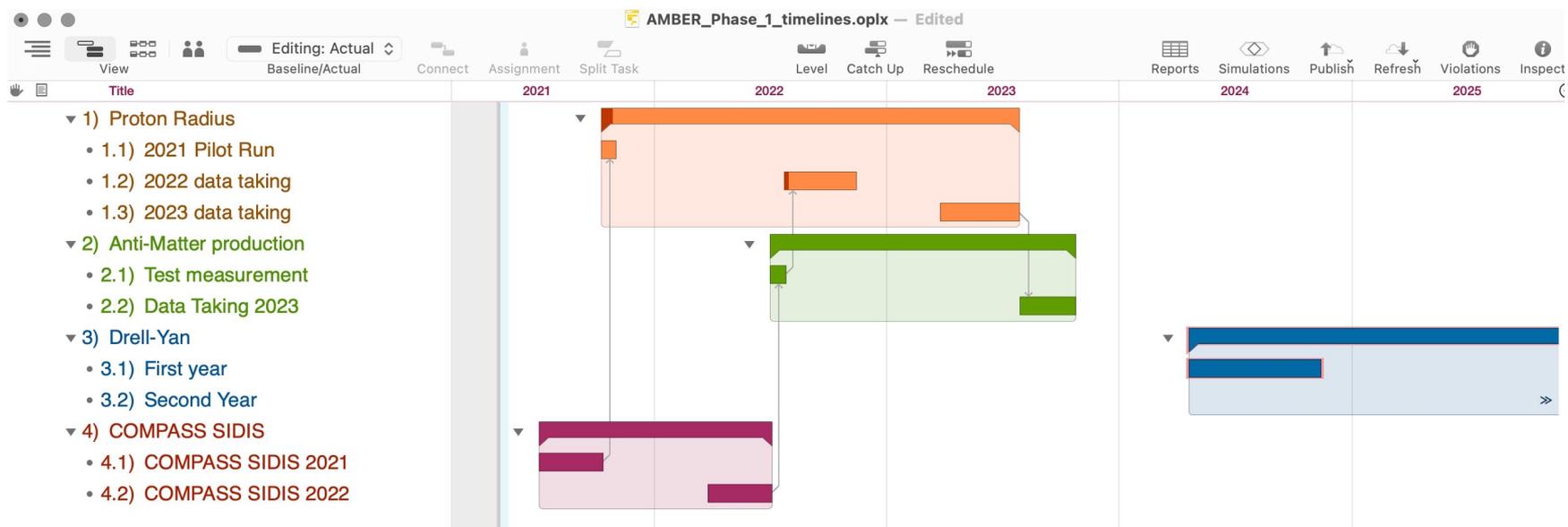
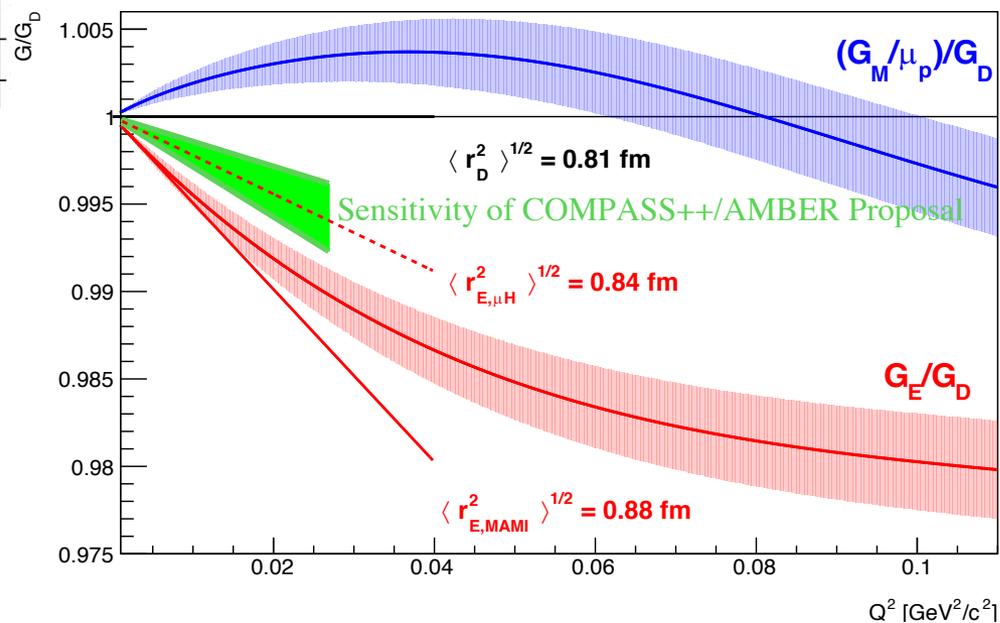
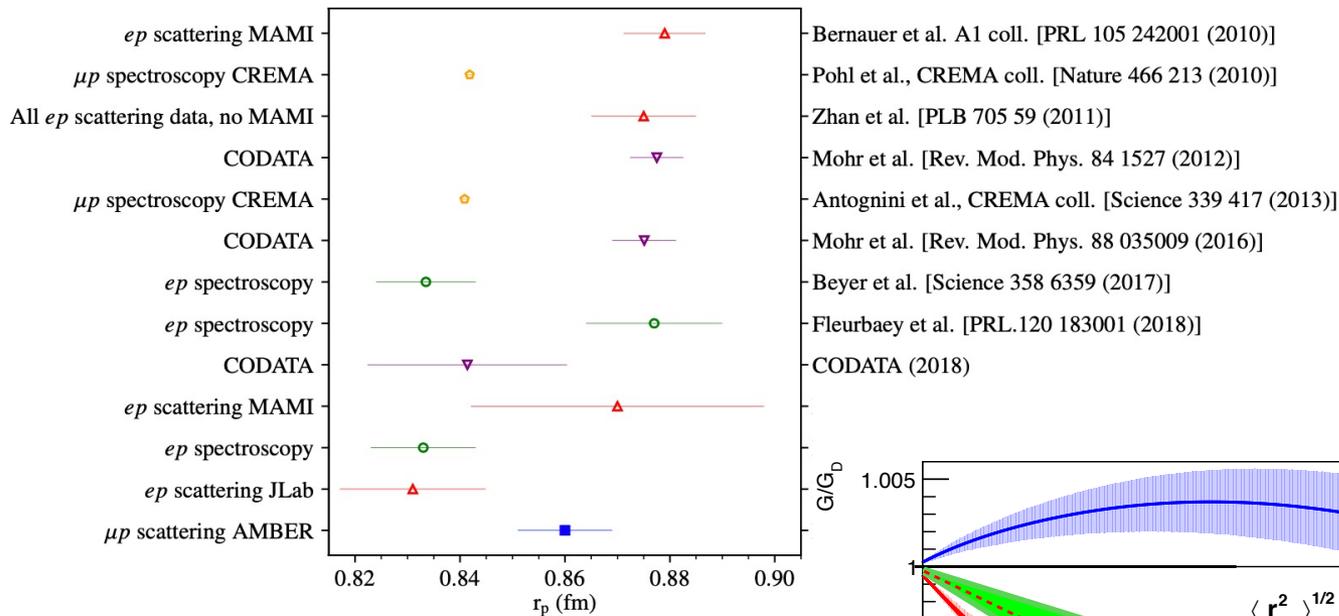
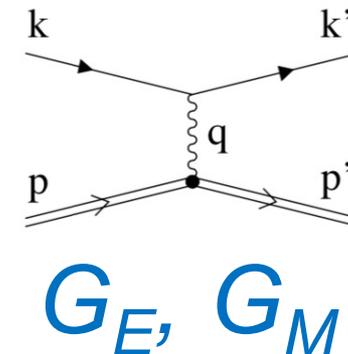


FIG. 4. Glue distribution,  $xg^\pi(x, \zeta_2 = 2 \text{ GeV})$ : solid purple curve, prediction from Ref. [43]. Panel A highlights low- $x$  and Panel B, large- $x$ . The band surrounding this curve expresses a conservative estimate of uncertainty in the prediction, obtained by varying  $\zeta_H$  by  $\pm 10\%$ . Comparisons are selected fits to data: dashed blue curve, [32]; dotted red curve and associated band, [33]; dot-dashed brown curve and band, [34].

## Possible timeline Phase-1

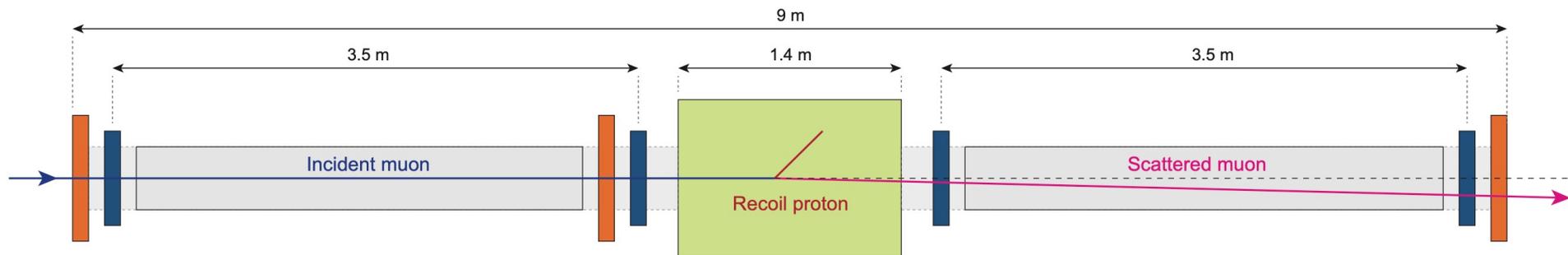




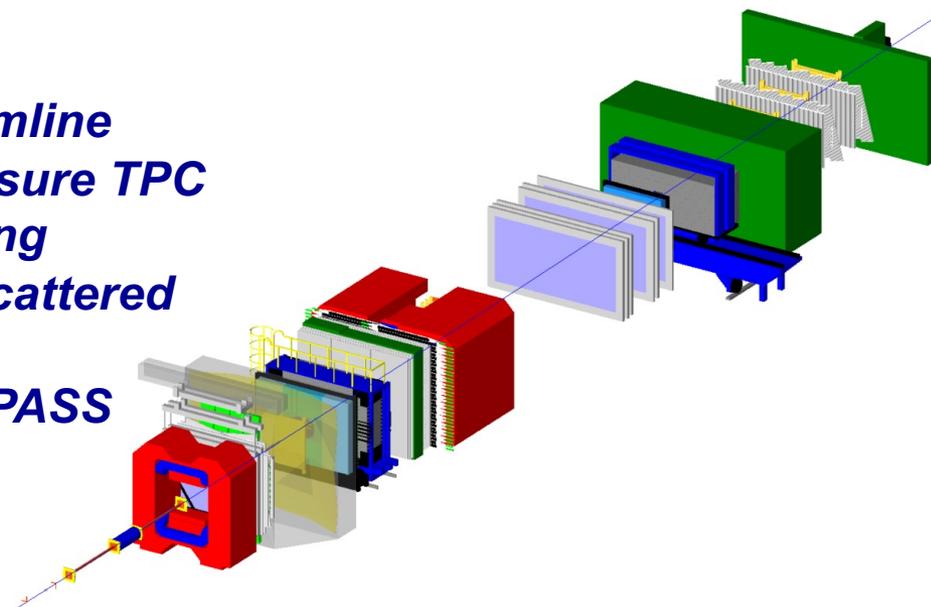
## Proposal for Measurements at the M2 beam line of the CERN SPS

– Phase-1 –

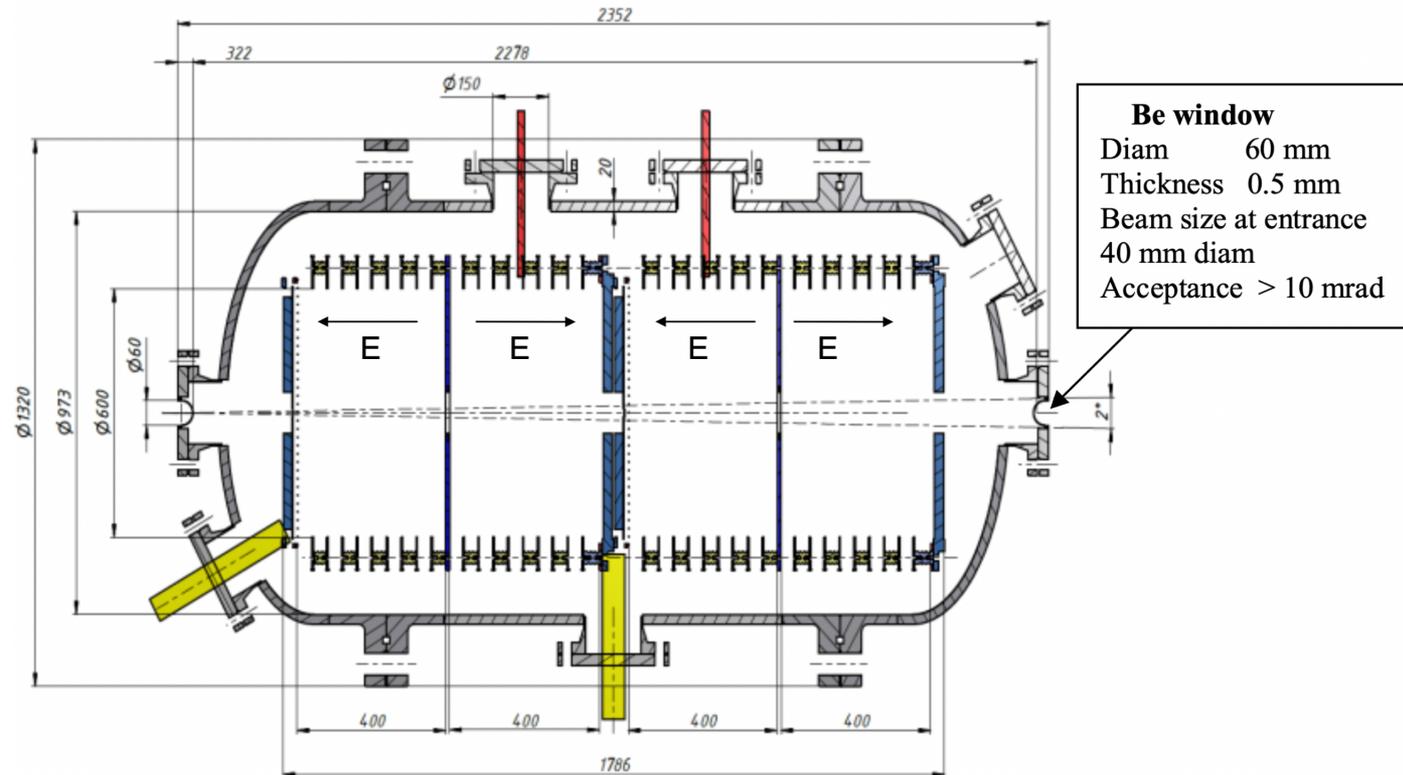
COMPASS++<sup>\*</sup>/AMBER<sup>†</sup>



- **100 GeV muons of the CERN M2 beamline**
- **Protons in an active-target high-pressure TPC**
- **Silicon detectors for precision tracking**
- **200 $\mu$ m SciFi stations for trigger on scattered muons**
- **inner tracking and ECAL of the COMPASS spectrometer**



# Active target: high-pressure TPC **AMBER**



- up to 20 bar pressure
- 600mm diameter of active volume
- reconstruction of recoil energy 0.5-20 MeV ( $10^{-3} \dots 4 \times 10^{-2} \text{ GeV}^2$ )

# Schedule for Proton-Charge Radius Measurement

- Planning for the upcoming three years**

*Preliminary feedback SPSC's April meeting:*



- Schedule for the setup, preparation and pilot run with the following main data taking and concluding systematic studies.

*"The AMBER proton radius experiment (core program) will likely run in 2022, keeping again in mind that at this point it is not at all clear how much NA operations will be delayed."*

Phase	Year	Task	Time (days)	Particle	p (GeV)	Rate ( $\mu/s$ )	Comment
Ia	2021	Preparation	100	$\mu^+/\mu^-$	160	$10^5 - 10^7$	Parasitic testing of single components
Ib	2021	Pilot run	20	$\mu^+/\mu^-$	100	$2 \cdot 10^6$	CEDAR location, down-scaled setup
IIa	2022	Data taking	43	$\mu^+/\mu^-$	100	$2 \cdot 10^6$	$Q^2: 1.0 \cdot 10^{-3} - 8 \cdot 10^{-3} \text{ GeV}^2/c^2$
IIb	2022	Data taking	107	$\mu^+/\mu^-$	100	$2 \cdot 10^6$	$Q^2: 2.5 \cdot 10^{-3} - 4 \cdot 10^{-2} \text{ GeV}^2/c^2$
IIIa	2023	Empty target	50	$\mu^+$	100	$2 \cdot 10^6$	Empty TPC
IIIb	2023	Energy dep.	25	$\mu^+/\mu^-$	60	$2 \cdot 10^6$	Multiple scat. and scat. angle
IIIc	2023	Energy dep.	25	$\mu^+/\mu^-$	150	$2 \cdot 10^6$	Multiple scat. and scat. angle

# Proposed $Q^2$ -Range Measurement

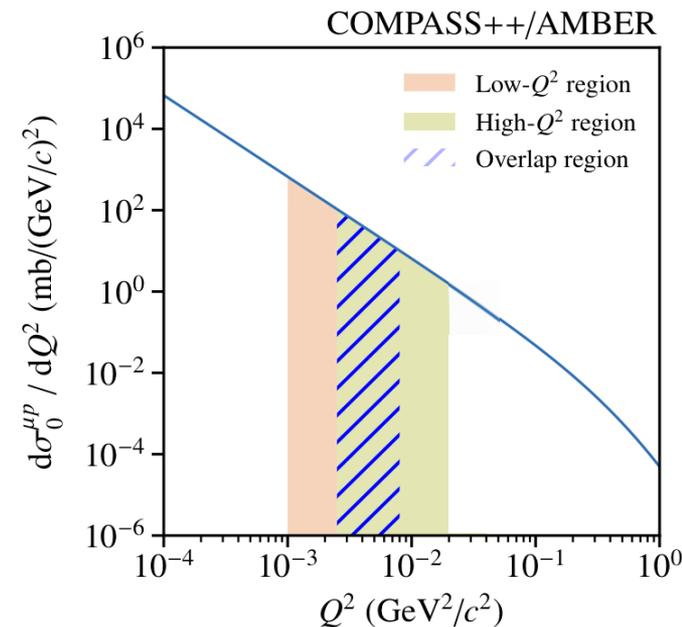
## Measurement of elastic $\mu$ -p-scattering

Active-target pressurised hydrogen TPC combined with tracking and *COMPASS* spectrometer.

- Direct measurement of recoil-proton energy:  
 $0.001 \leq Q^2 / (\text{GeV}^2/c^2) \leq 0.02$
- Conservative scenario:  
 → Low- $Q^2$ :  $0.001 \leq Q^2 / (\text{GeV}^2/c^2) \leq 0.0025$   
 → High- $Q^2$ :  $0.0025 \leq Q^2 / (\text{GeV}^2/c^2) \leq 0.02$
- Data taking of 150 days - Phase II:  
 → 43 days - low- $Q^2$  at 4 bar  
 → 107 days - high- $Q^2$  at 20 bar

- Data set with  $33 \cdot 10^6$  events:  
 → stat. prec. on  $\langle r^2 \rangle$ : 1.6 %  
 → fixed  $\langle r^6 \rangle$  term: 0.7 %  
 (values from simulation)

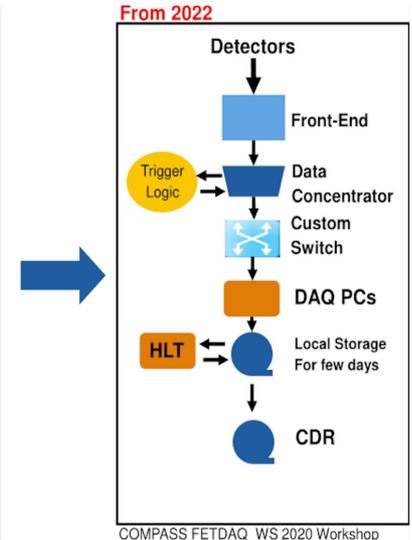
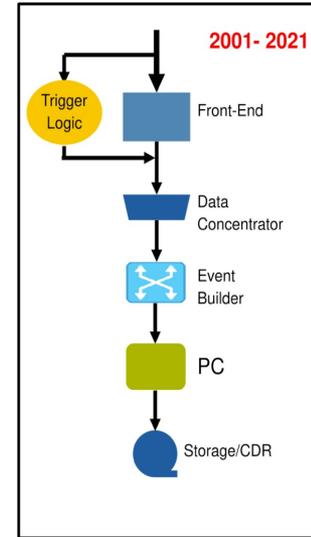
Stat. Prec.	fixed $\langle r^6 \rangle$	$Q^2$ ( $\text{GeV}^2/c^2$ )	Statistics	Pressure	Comment
0.9 %	0.5 %	0.0010 - 0.04	70 mio.	20 bar	150 days
1.2 %	0.6 %	0.0025 - 0.04	37 mio.	20 bar	150 days
1.6 %	0.7 %	0.0010 - 0.04	6 + 27 mio.	4 + 20 bar	43 + 107 days
1.4 %	0.7 %	0.0010 - 0.04	12 + 27 mio.	4 + 20 bar	86 + 107 days



## New DAQ development

A concept applying continuous DAQ based on the following principals:

- Trigger-less front-end electronics
- Front-end data can be forwarded to trigger processors
- Hardware event builder stores data until trigger decision
- Status and Plans:
  - Adaption of DAQ firmware and software (within 2020)
  - Increase of data rate capability (2/10 GB/s 2022/2023)
  - Development of digital trigger (iFTDC card since 2019)



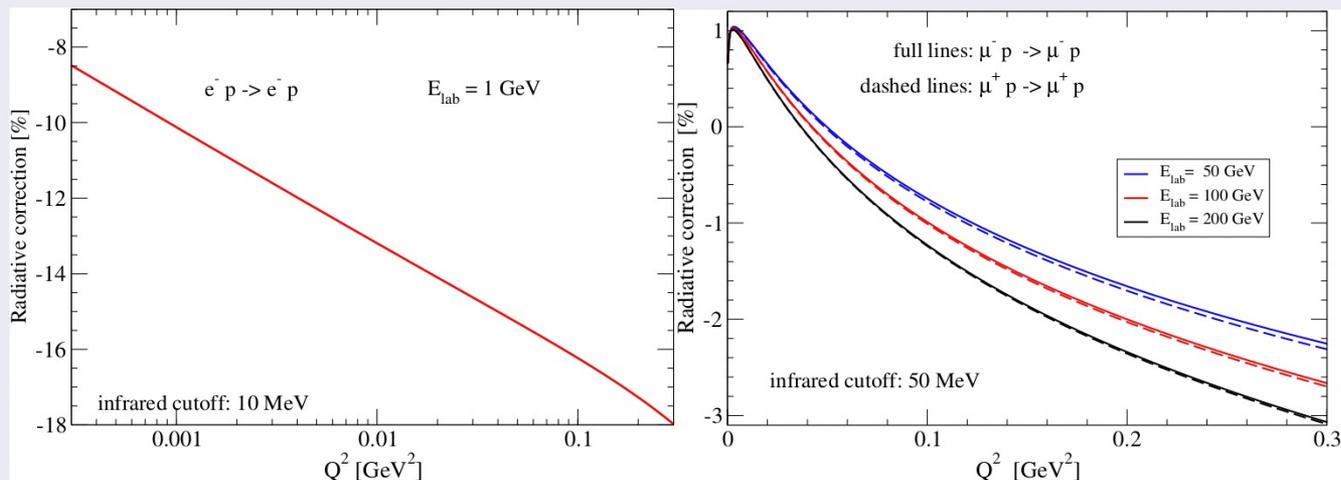
COMPASS FETDAQ\_WS 2020 Workshop

		Spill										
		Slice 1 100µs					Slice 2 100µs					
Very slow Detectors (TPC, ...)		Image 1 50µs		Image 2 50µs			Image 1 50µs		Image 2 50µs			
		Image 1 500ns		...	Image 200 500ns			Image 1 500ns		...	Image 200 500ns	
Slow Detectors (DCs, W45, ...)		Image 1 100ns	Image 2 100ns	Image 3 100ns	Image 4 100ns	Image 5 100ns	...	Image 996 100ns	Image 997 100ns	Image 998 100ns	Image 999 100ns	Image 1000 100ns
		Image 1 500ns	Image 2 500ns	Image 3 500ns	Image 4 500ns	Image 5 500ns	...	Image 996 500ns	Image 997 500ns	Image 998 500ns	Image 999 500ns	Image 1000 500ns



- Bremsstrahlung accompanies the elastic process
- for low-energy photons roughly  $1/E_\gamma$  ('infrared divergence')
- angular spectrum: peaking in the relativistic case, opening angle  $1/\gamma$  [Lorentz factor]
- 100 GeV beam:  $E_\gamma$  **between 50 MeV and 5 GeV** emission probability at  $\theta_\mu = 0.3 \text{ mrad}$  ( $Q^2 = 0.001$ ):  $5 \times 10^{-4}$
- Bremsstrahlung events in  $Q^2 = 0.001 \dots 0.04 \text{ GeV}^2/c^2$  **about 38000**

## QED radiative corrections



- for soft bremsstrahlung photon energies ( $E_\gamma/E_{\text{beam}} \sim 0.01$ ), QED radiative corrections amount to  $\sim 15\text{-}20\%$  for electrons, and to  $\sim 1.5\%$  for muons
- important contribution to the uncertainty of elastic scattering intensities: *change* of this correction over the kinematic range of interest
- check: impact of exponentiation procedure (strictly valid only for vanishing photon energies):  $e^-$ : 2 – 4%,  $\mu^-$ : 0.1%
- integrating the radiative tail out to large fraction of beam energy: shifts the correction to smaller values, but only *increases* the uncertainty