

Single hadron multiplicities in SIDIS @ COMPASS

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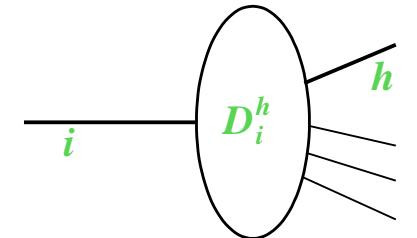
On behalf of the COMPASS collaboration

September 3, 2019



Motivation: FFs

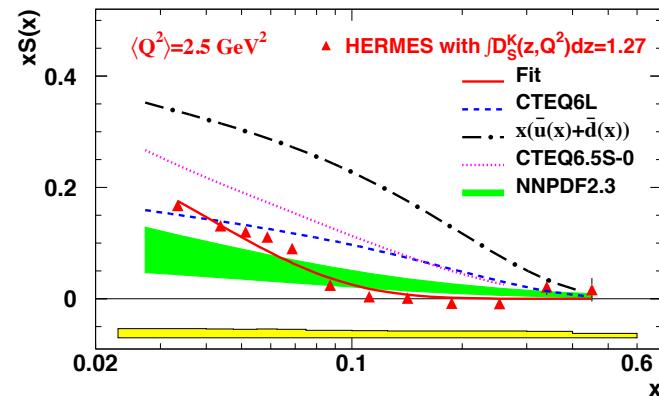
- SIDIS $lN \rightarrow lhX$ gives access to **Fragmentation Functions (FFs)**
- **Collinear** FFs $D_i^h(z, Q^2)$ describe the collinear transition of a parton i into a hadron h carrying energy fraction $z = E_h/E_i$.
 - Non-perturbative universal objects.
Factorisation: FF \otimes parton-level X-section [\otimes PDF] (*+ power suppressed...*)
 - Scale evolution: $dD_q^h(z, Q^2)/d\ln Q^2 = [P_{qq} \otimes D_q^h + P_{gq} \otimes D_g^h](z, Q^2)$
- FFs are needed in analyses with a hadron in the final state
(*when a hadron is inclusively detected in hard scattering*)
- Cleanest way to access FFs: e^+e^- annihilation. However...
 - ... only sensitive to $q + \bar{q}$, flavour separation limited.
 - In SIDIS, q/\bar{q} and flavour separation possible. However...
 - ... FFs are convoluted with PDFs.
 - $pp: pp \rightarrow hX$ at high pT : little flavour/charge separation, but with gluon at leading order
 $pp \rightarrow (\text{jet } h)X$, see PRD 92 (2015),
 - SIDIS data are crucial to understand parton fragmentation



Motivation: PDFs

$$(\Delta)\sigma^h \stackrel{\text{LO}}{\propto} \Sigma e_q (\Delta)q(x, Q^2) \int D_q^h(z, Q^2) dz \Rightarrow \text{Tagging of quark flavour}$$

- Polarised PDFs (pPDFs)
 - SIDIS data in several global QCD fits of pPDFs, *e.g.*:
 - DSSV*: PRL 113 (2014)), JAM17: PRL 119 (2017), NNPDFpol1.1: NP B887 (2014)
- PDFs: well known. . . but for Strangeness
 - LO extraction of $S(x)$ ($S = s + \bar{s}$) @ high x
from HERMES d data: PRD 89 (2014)
 - Simultaneous fit of FFs and PDFs, by JAM and DSS groups

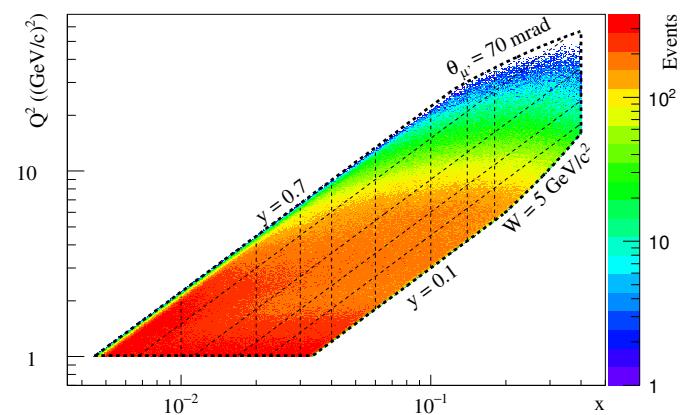


Multiplicity Measurement in SIDIS

- Multiplicity is number of hadrons *per* inclusive DIS event

$$\frac{dM^h(x, z, Q^2)}{dz} = \frac{d^3\sigma^h(x, z, Q^2)/dxdzdQ^2}{d^2\sigma^{DIS}/dxdQ^2}$$

- Measurements need to be corrected for various effects:
 - Spectrometer acceptance. . .
 - . . . taking p_T and azimuth ϕ_h into account
 - ParticleID efficiency and purity
 - Radiative effects
 - Diffractive vector meson production
 - (*Subtracted based on Handbag Model by Goloskokov and Kroll using MC generator HEPGEN*)
 - Feed-down from weak decays of charmed hadrons
 - (*Negligible in our measured z range ($z > 0.2$)*)



Multiplicity Measurement in SIDIS (*cont'd*)

- **Radiative Corrections:** Three approaches considered:

1. **TERAD**(*i.e.* **Incl.DIS**)-based + empirical correction for hard photon. . .

. . . impact on kinematics and phase-space of SIDIS

Used in earliest analyses

2. **RADGEN**-based: **Monte Carlo generation of radiative events**. . .

. . . impact on kinematics on a *per* event basis

Disagreement w/ COMPASS data ⇒ **Abandoned**

3. **DJANGOH**-based: **Monte Carlo generation of radiative events**. . .

Good agreement w/ COMPASS data ⇒ **Retained in latest analysis**

- Ongoing discussion I.Akushevich, A.Afanasev (*RADGEN*) and H.Spiesberger (*DJANGOH*): Novel Probes of the Nucleon Structure, JLab, MCEGs for future ep and eA facilities, DESY

- **Acceptance correction**

- 3D, along x, y, z

z -dependent y bin-width to stay w/in momentum range of RICH particleID

- p_T : Reasonably flat acceptance along p_T

- ϕ_h : Relying of extensive ϕ_{lab} coverage of COMPASS. . .

. . . to integrate out $\cos\phi_h$, $\cos 2\phi_h$ and $\sin\phi_h$ modulations.

COMPASS: Spectrometer

- o μ^\pm Beam (SIDIS)

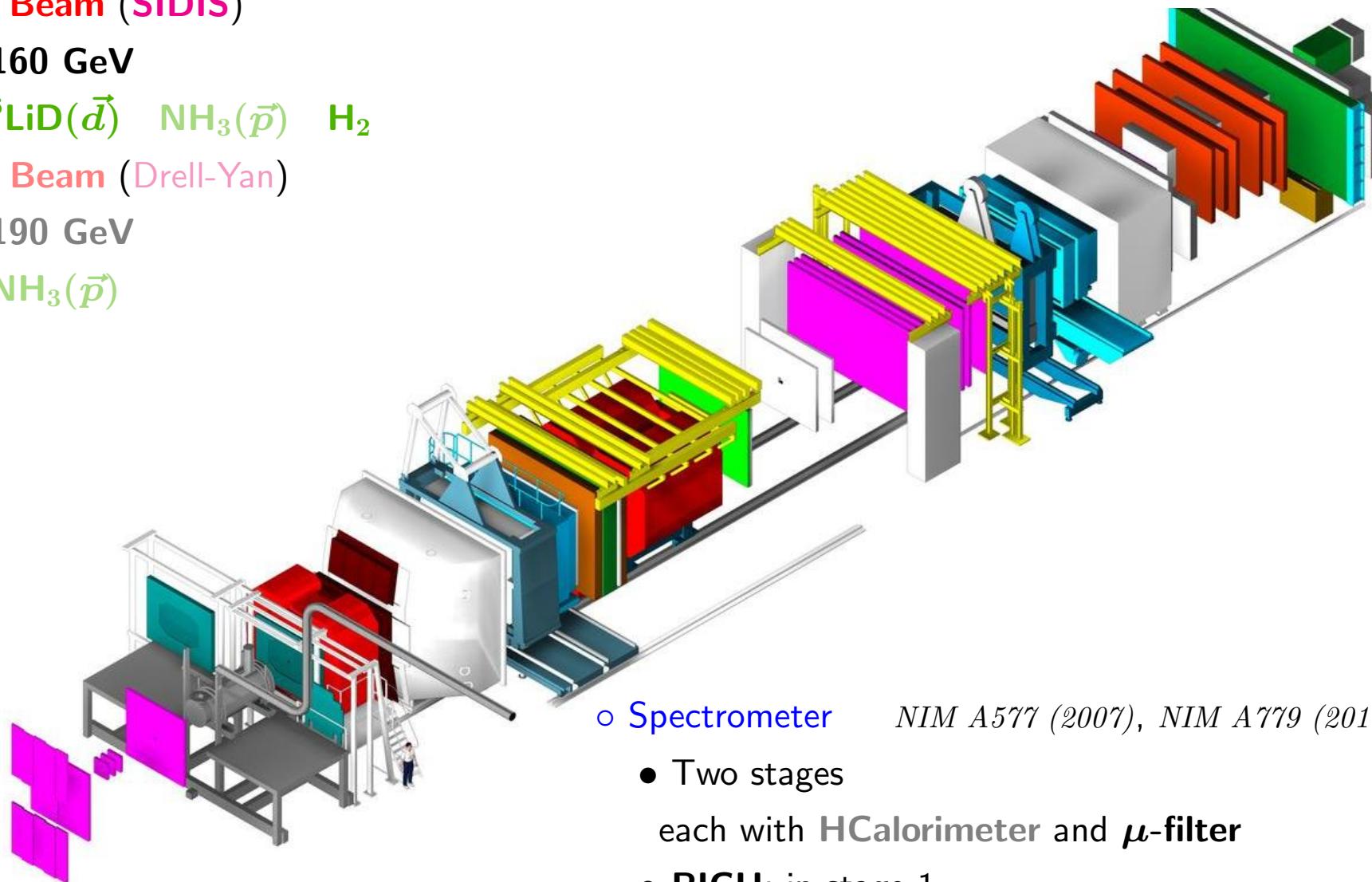
- 160 GeV

- ${}^6\text{LiD}(\vec{d})$ $\text{NH}_3(\vec{p})$ H_2

- o π^- Beam (Drell-Yan)

- 190 GeV

- $\text{NH}_3(\vec{p})$



- o Spectrometer *NIM A577 (2007), NIM A779 (2015)*

- Two stages
each with **HCalorimeter** and **μ -filter**
 - **RICH**: in stage 1
 - **ECalorimeters(0,1,2)**

Multiplicity of π^\pm on isoscalar target (${}^6\text{LiD}$)

- PLB764 (2017) 1
- 3D binning: $x \times y \times z$

- LO QCD Fit,

using Hirai, Kumano software with:

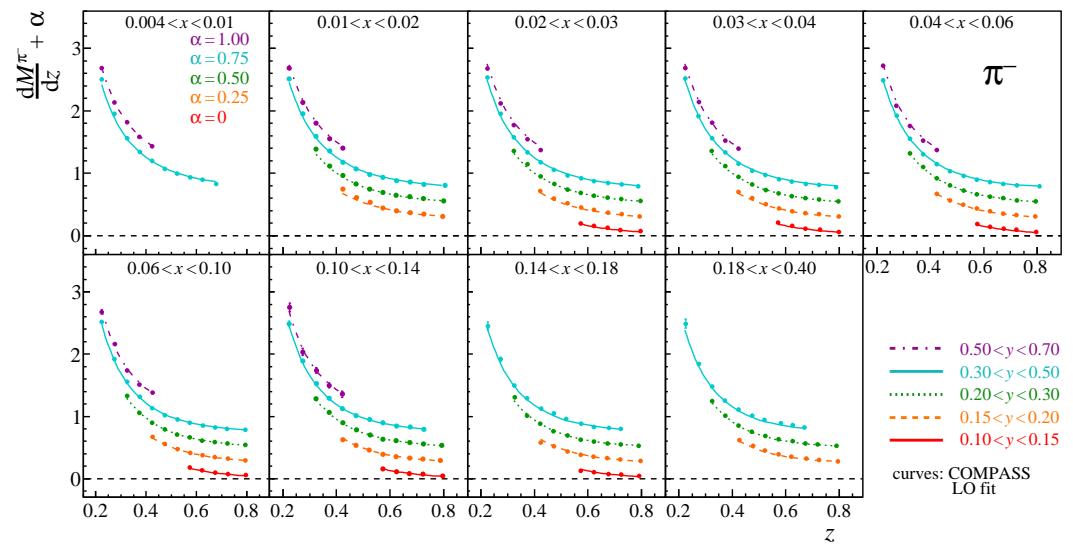
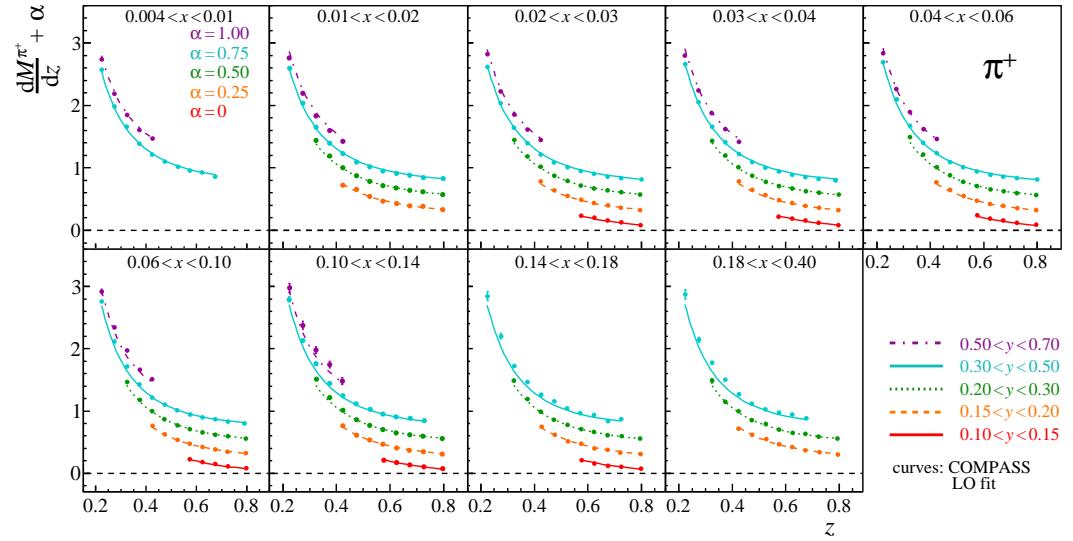
$$D_{fav}^\pi = D_u^{\pi^+} = D_{\bar{d}}^{\pi^+} \text{ and } c.c.$$

$$D_g^\pi \quad (\text{in } Q^2 \text{ evolution only})$$

Simplification:

$$D_{unf}^\pi = D_q^{\pi^\pm}, \forall \text{ non-valence } q$$

- Also unidentified h^\pm



Multiplicity of K^\pm on isoscalar target (${}^6\text{LiD}$)

- PLB767 (2017) 133

- LO QCD Fit

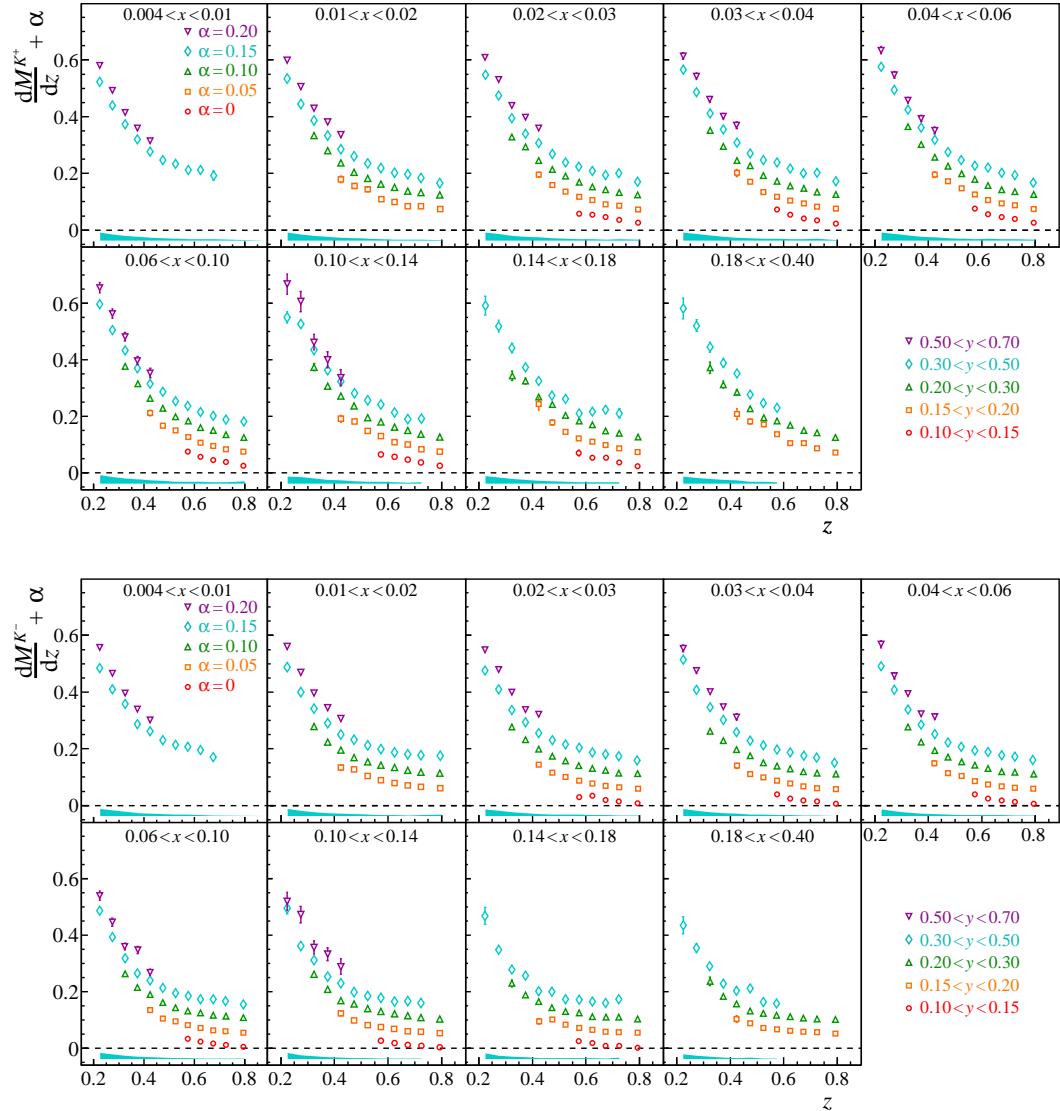
$$D_{fav}^K = D_u^{K+} \text{ and } c.c.$$

$$D_{str}^K = D_{\bar{s}}^{K+} \text{ and } c.c.$$

$$D_g^K$$

$$D_{unf}^K = D_q^{K^\pm}, \forall \text{ non-valence } q$$

unstable \Rightarrow not displayed



Comparison w/ Other SIDIS Measurements

- **EMC:** h^\pm ZPC52 (1991), **HERMES:** π^\pm, K^\pm PRD87 (2013), **JLab E00-108:** π^\pm : PRC85 (2012)
- Sum/Ratio of **integrals** (*over measured z range*) **averaged over y** / **integrated over Q^2**

$$\mathcal{M} = \int \frac{dM}{dz} dz \quad (\mathcal{D} = \int D dz)$$

LO pQCD + **simplifying assumptions** yield simple expressions and **provide guidance**

*(Shown is the **isoscalar target case**)*

$$\circ \mathcal{M}^\pi^+ + \mathcal{M}^\pi^- \stackrel{\text{LO}}{=} \mathcal{D}_{fav}^\pi + \mathcal{D}_{unf}^\pi - \frac{2S}{5Q + 2S} (\mathcal{D}_{fav}^\pi - \mathcal{D}_{unf}^\pi) \simeq \mathcal{D}_{\mathbf{fav}}^\pi + \mathcal{D}_{\mathbf{unf}}^\pi$$

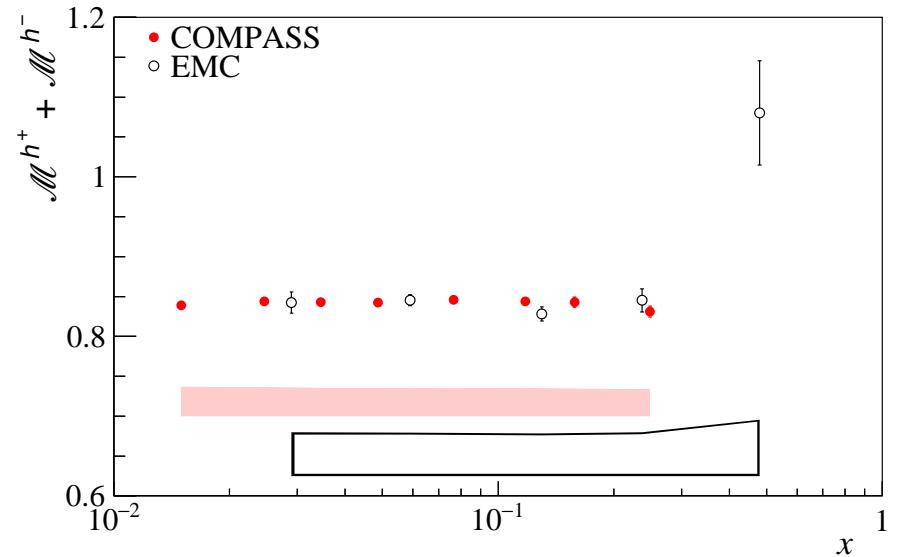
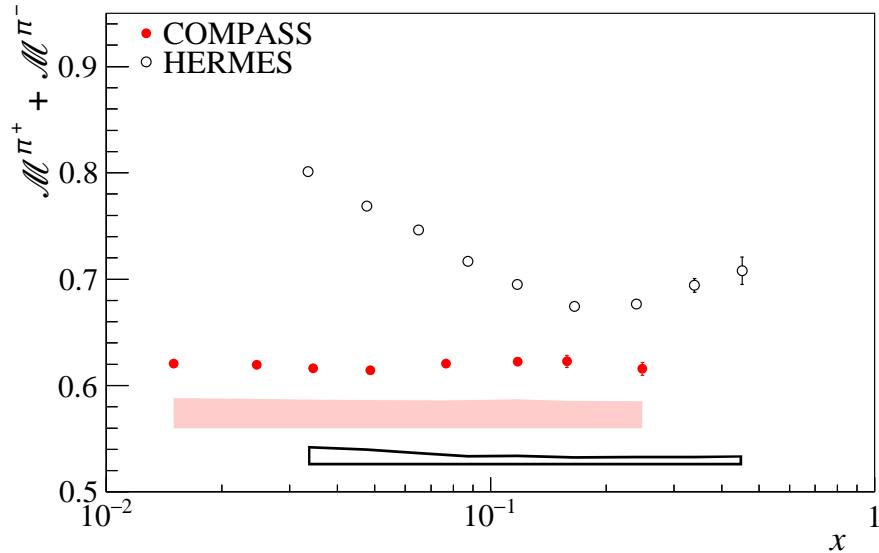
$$Q = u + \bar{u} + d + \bar{d}, S = s + \bar{s}$$

\Rightarrow depends on x only weakly via $\mathcal{D}(Q^2)$ evolution and x/Q^2 correlation at fixed target.

$$\circ 5(\mathcal{M}^{K^+} + \mathcal{M}^{K^-}) \stackrel{\text{LO}}{\simeq} 4\mathcal{D}_{fav}^K + 6\mathcal{D}_{unf}^K + S/Q \mathcal{D}_S^K$$

Comparison w/ Other SIDIS Measurements: π Multiplicity Sum

- COMPASS data averaged over y

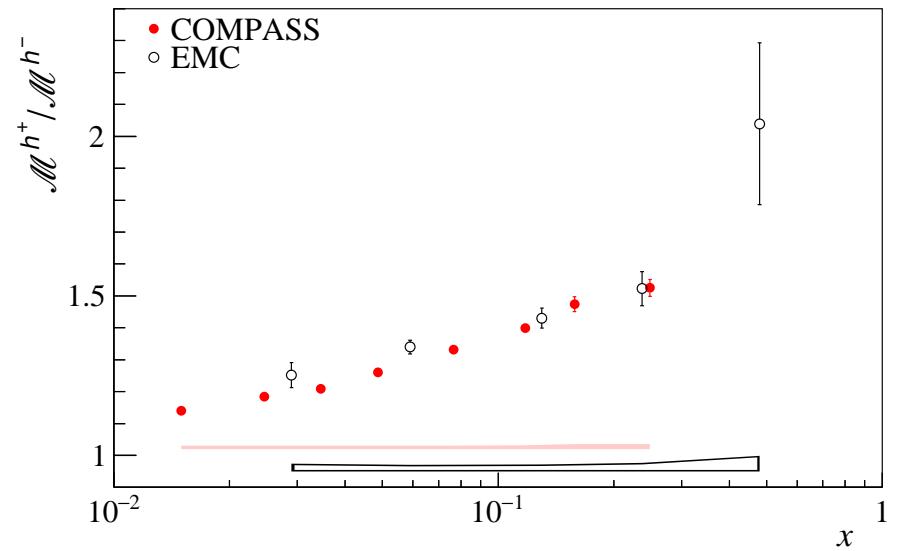
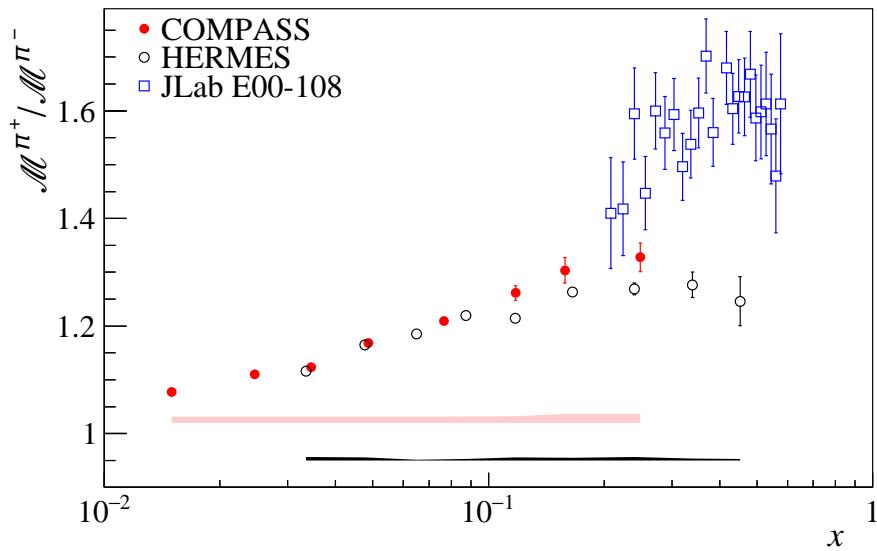


- ⇒ Discrepancy w/ HERMES, beyond systematics uncertainty
- ⇒ COMPASS (*averaged over y*) and EMC agree w/ LO pQCD prediction

Caveat: ◦ **One of two available HERMES data sets**, *viz.* $x \times z$ as opposed to $Q^2 \times z$
◦ Q^2 differs among the experiments

π^+/π^- Multiplicity Ratio

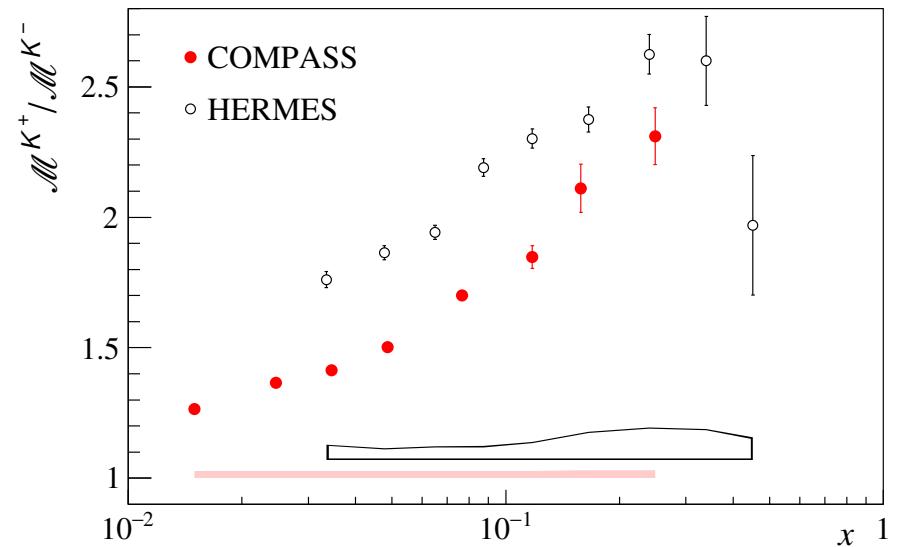
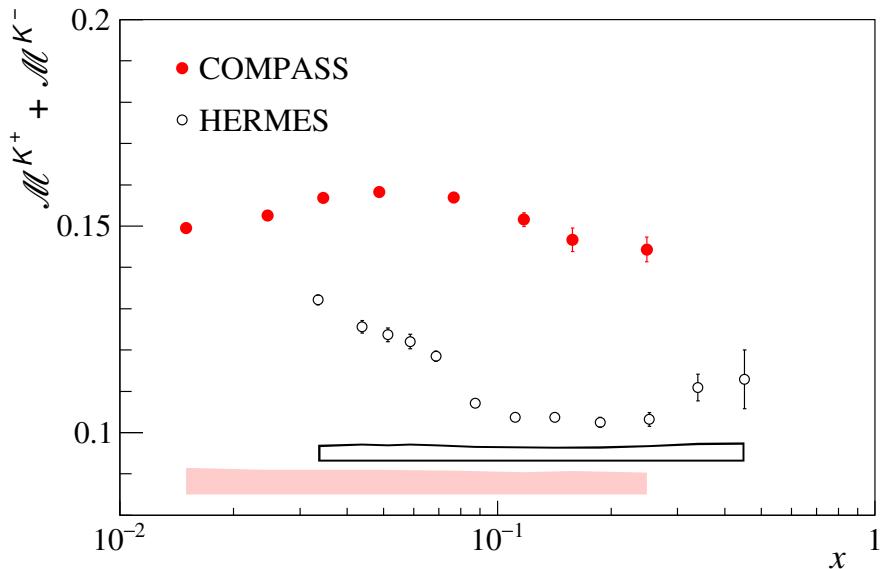
- The ratio π^+/π^- is interesting because of cancellation of many systematic errors.



- ⇒ Agreement with HERMES, w/in uncertainty
- ⇒ HERMES vs. JLab discrepancy at high x likely due to different W range
and possible higher twist contribution

K Multiplicity Sum and Ratio

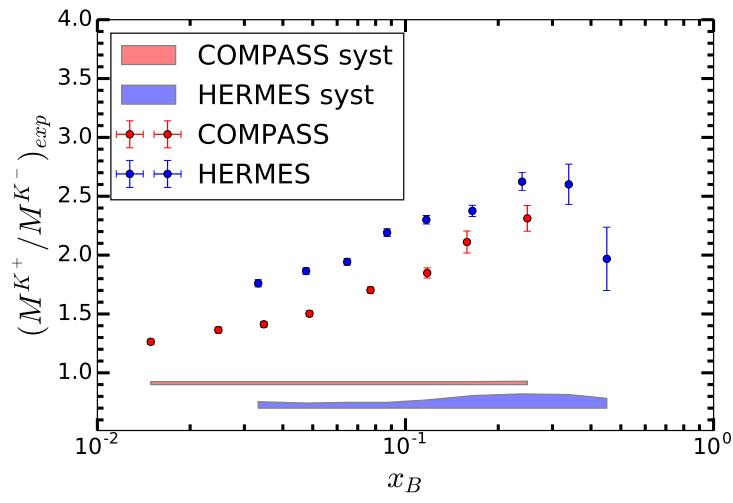
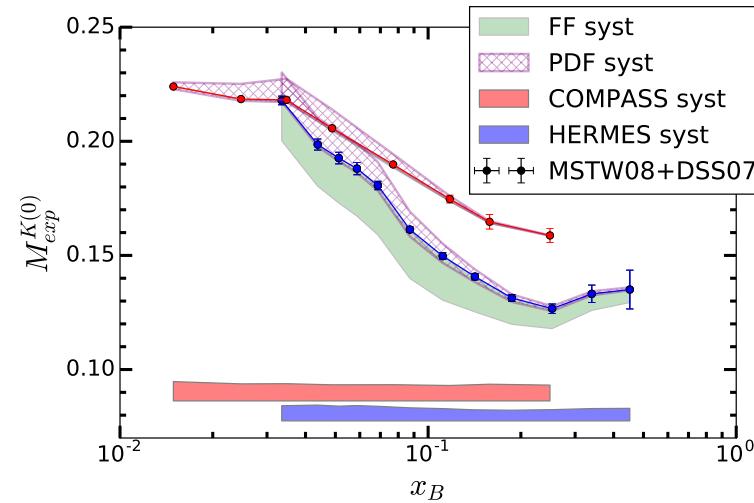
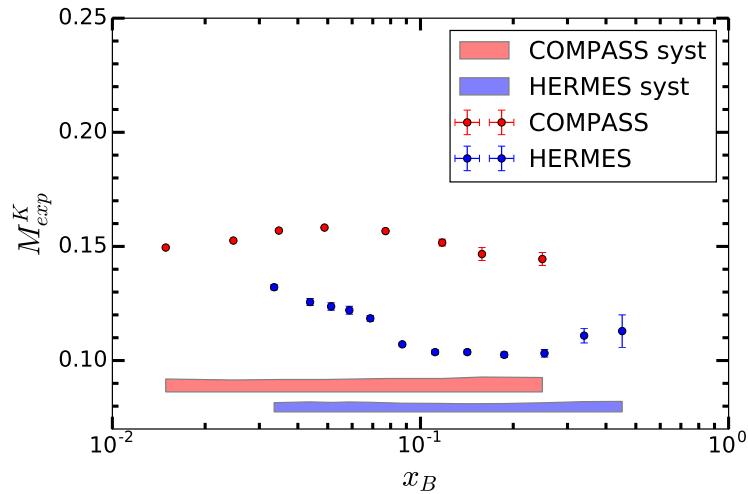
- Comparison w/ HERMES $x \times z$ data set



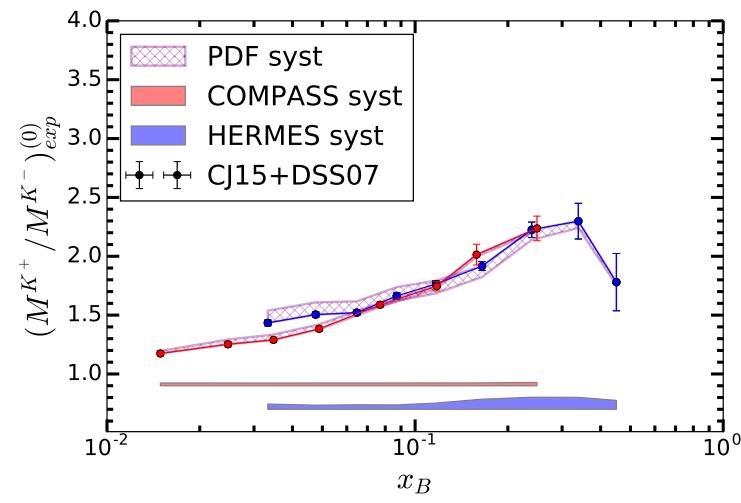
⇒ Significant differences between COMPASS and HERMES

- Shape of $\mathcal{M}_{K^+} + \mathcal{M}_{K^-}$
- Mean value of $\mathcal{M}_{K^+} + \mathcal{M}_{K^-}$, while at high x it's, approx., a combination of \mathcal{D}_q
(Note: COMPASS on top, contrary to π case)
- Ratio, whereas there's agreement for pions
- Guerrero and Accardi PRD97 (2018): discrepancy suppressed by Hadron Mass Corrections

J. V. Guerrero and A. Accardi, PRD97 (2018) 114012



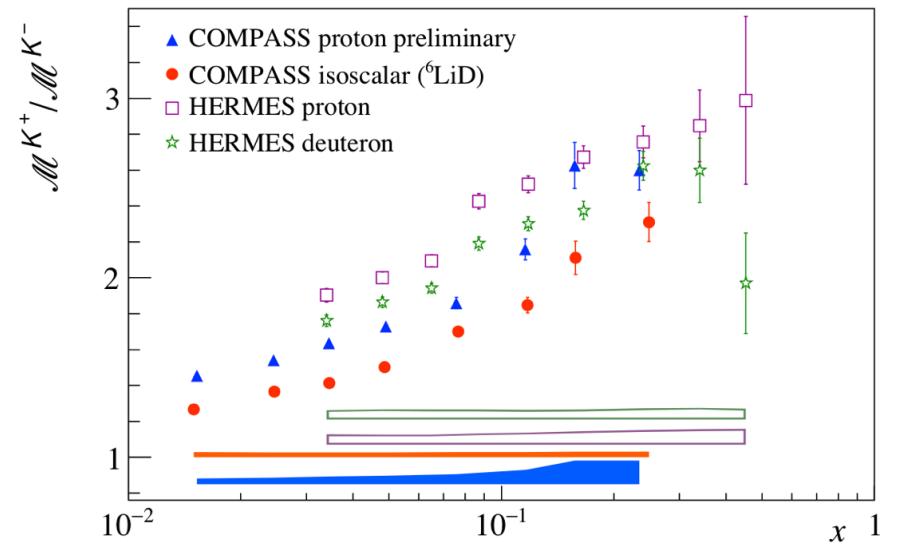
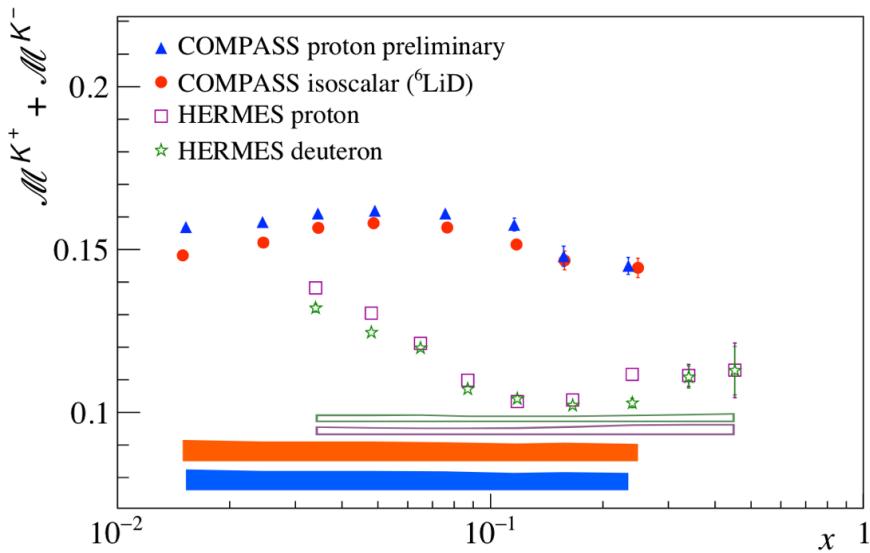
Experimental data



Massless parton multiplicities
(@ common energy)

K from p target (preliminary)

- Result from 2016 run *More to come from the 2017 run*
- **RC by Event Generator DJANGOH by H. Spiesberger**
 ⇒ Expecting better control on RC ⇒ associated systematics reduced
- Comparison w/ **HERMES $p \times z$ data set**



- ⇒ **Confirmation of COMPASS *vs.* HERMES discrepancy**
- p sitting $\sim 5\%(\text{sum})/10\%(\text{ratio})$ above d as expected (*different PDFs involved*)

Experimental Status of FFs: Global QCD Fits

- Global fits exploit universality by **combining** data sets from **several processes**:
 - **DEHSS** = De Florian, Sassot, Stratmann *et al.*: PRD91 (2015), PRD95 (2017): e^+e^- , pp and **SIDIS**.
 - **NNPDF**: Bertone *et al.*: EPJC78 (2018): e^+e^- , $pp(\bar{p})$.
 - **HKKS** = Hirai, Kawamura, Kumano, Saito PTEP (2016): e^+e^- .
 - **LSS** = Leader, Sidorov, Stamenov PRD93 (2016): **SIDIS**.
 - **AKK** = Albino, Kniehl, Kramer NPB803 (2008): e^+e^- , $pp(\bar{p})$.
- Exploit SIDIS full potential *via* combined fit of FFs, PDFs and/or pPDFs
 - **JAM17** Ethier, Sato, Melnitchouk: PRL119 (2017) (e^+e^- , **SIDIS = COMPASS only**)
 - Borsa, Sassot, Stratmann: PRD96 (2017)
Help clarify PDFs of strange sea, COMPASS/HERMES disagreement

K^-/K^+ Multiplicity Ratio at high z

- PLB786 (2018) 390
- Ratio?
 - Ratio cancels out many of the systematics
⇒ Can explore otherwise experimentally difficult SIDIS high z
- Ratio of Kaons, as opposed to pions?
 - Diffractively produced vector meson decays . . .
 - . . . dominate at **high z** in pion case ($\rho^0 \rightarrow \pi^+ \pi^-$)
 - . . . stay w/in $0.3 < z < 0.7$ in kaon case ($\phi \rightarrow K^+ K^-$)
because break-up momentum is small.
- Domain of validity of pQCD + independent fragmentation in SIDIS?
What SIDIS data to consider in global fit?

K^-/K^+ at high z : Predictions

- At LO in pQCD, on a **p target**:

- $$\frac{dM^{K^-}}{dM^{K^+}} \stackrel{\text{LO}}{=} \frac{4\bar{u}D_{fav} + (4u + \bar{d} + d + \bar{s})D_{unf} + sD_{str}}{4uD_{fav} + (4\bar{u} + d + \bar{d} + s)D_{unf} + \bar{s}D_{str}}$$

Neglecting D_{unf} (*since high z*), and trivial simplifications:

$$\frac{dM^{K^-}}{dM^{K^+}} \stackrel{\text{LO}}{\approx} \frac{4\bar{u}D_{fav} + sD_{str}}{4uD_{fav} + \bar{s}D_{str}} > \frac{\bar{u}}{u}$$

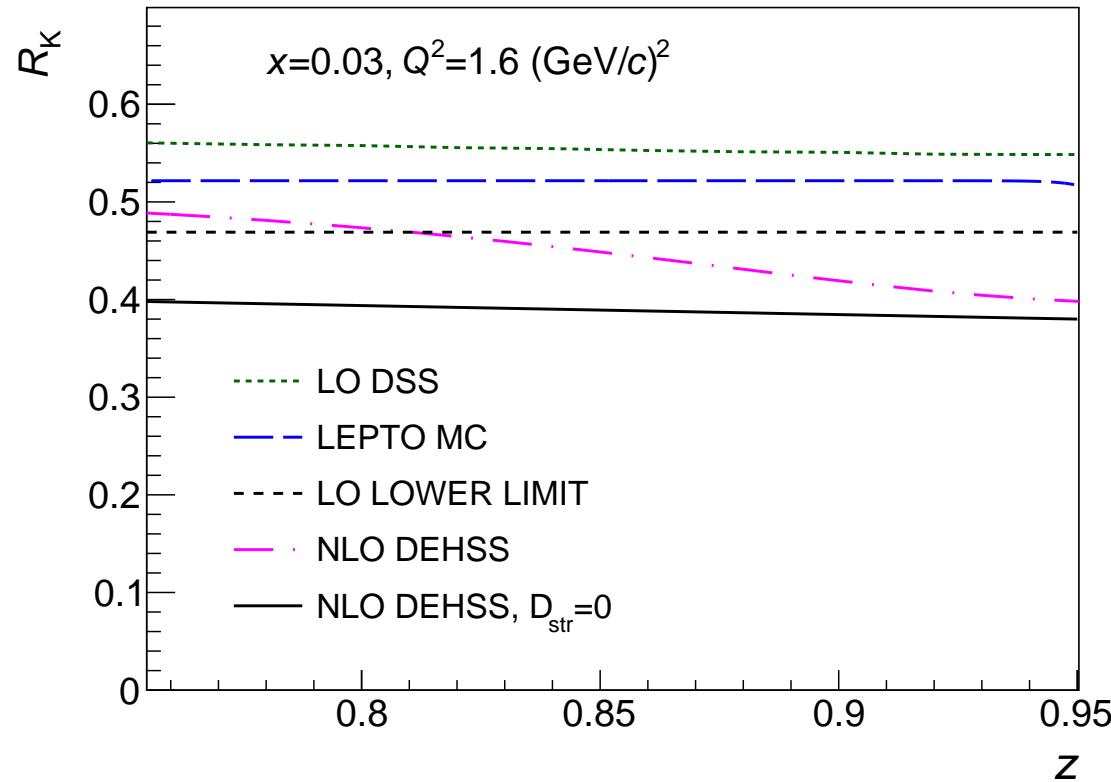
- On a **d target**:

$$R_K = \frac{dM^{K^-}}{dM^{K^+}} > \frac{\bar{u} + \bar{d}}{u + d}$$

- At NLO,

- Reasonably safe lower bound obtained by setting $D_{str} = 0$, working around dispersion among PDF and FF sets.

K^-/K^+ at high z : Predictions

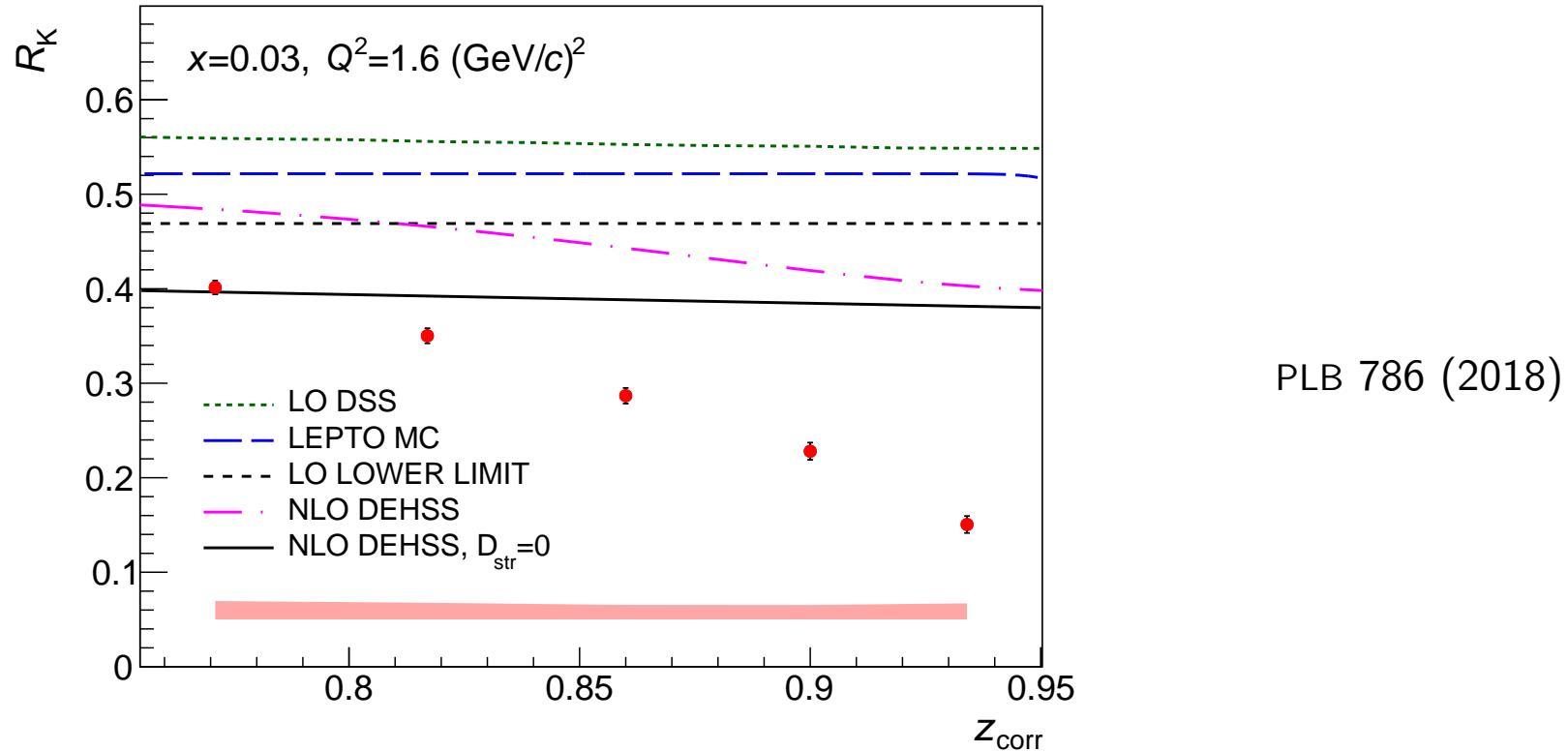


- Model calculations (*in addition to lower limits*)

LO DSS07, NLO DEHSS

LEPTO, w/ $H_{q/N}^K(x, z, Q^2)$ fragmentation ansatz

K^-/K^+ at high z : COMPASS Results vs. Predictions



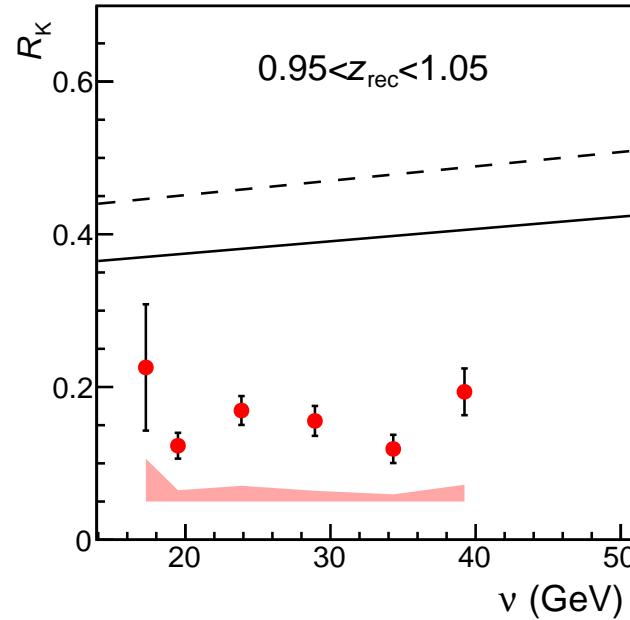
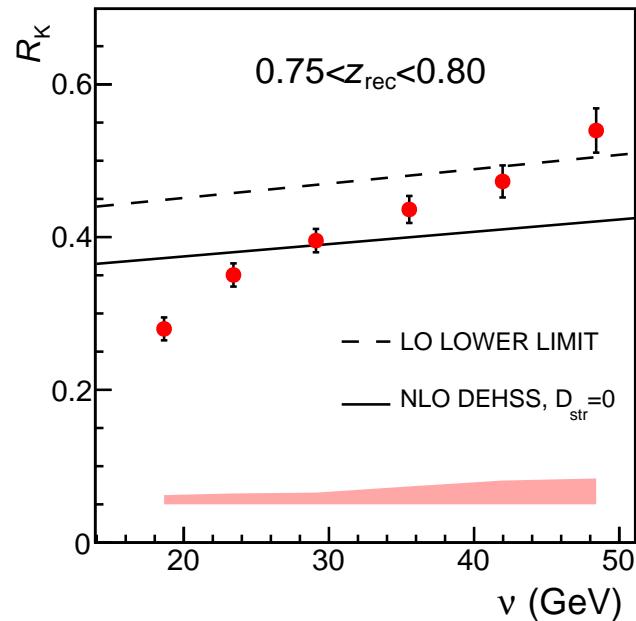
⇒ Clear disagreement w/ models. Violation of LO and NLO limits

(Safe result: all effects, here unaccounted for, in theory, tend to further increase disagreement.)

- (Note: Similar result @ higher x , w/ $R_K(x < 0.05)/R_K(x > 0.05)$ flat)

K^-/K^+ at high z : COMPASS Results vs. photon energy ν

- R_K in 5 bins of z (2 shown)
compared to LO and NLO lower limits



PLB 786 (2018)

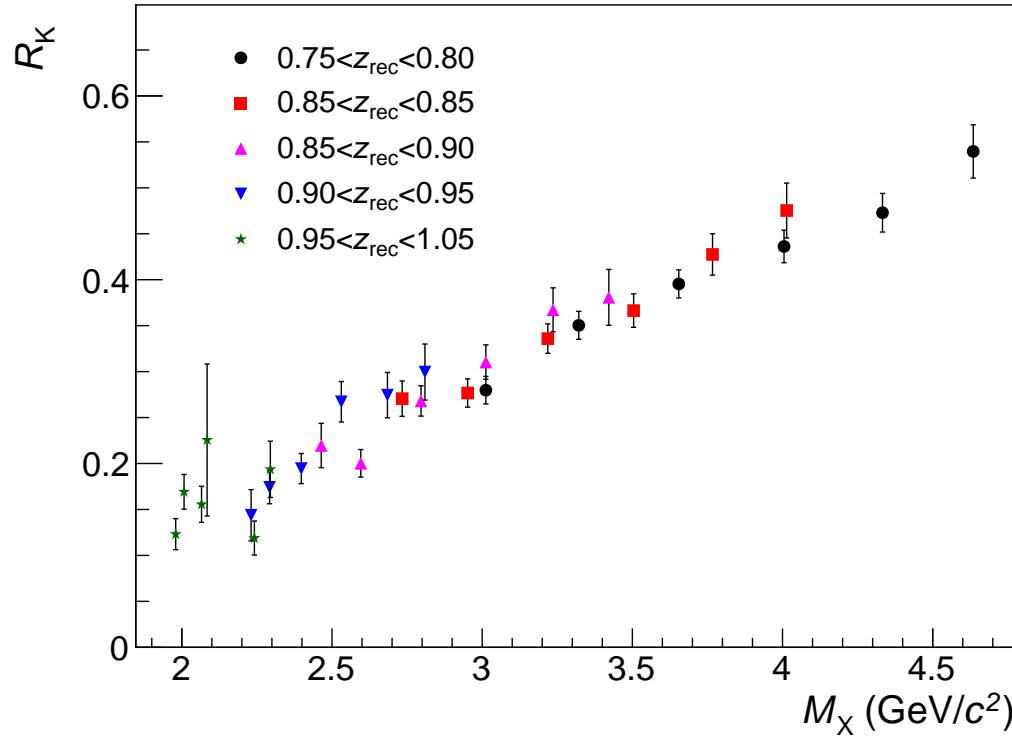
- Strong **dependence upon ν** (*beyond expected from $x(\nu)$*)

Not foreseen w/in independent fragmentation in pQCD

⇒ Low ν high z : **Applicability of independent fragmentation pQCD questionable**

K^-/K^+ at high z : COMPASS Results vs. Missing Mass

- Missing Mass M_X : $M_X^2 \approx 2M\nu(1 - z)$

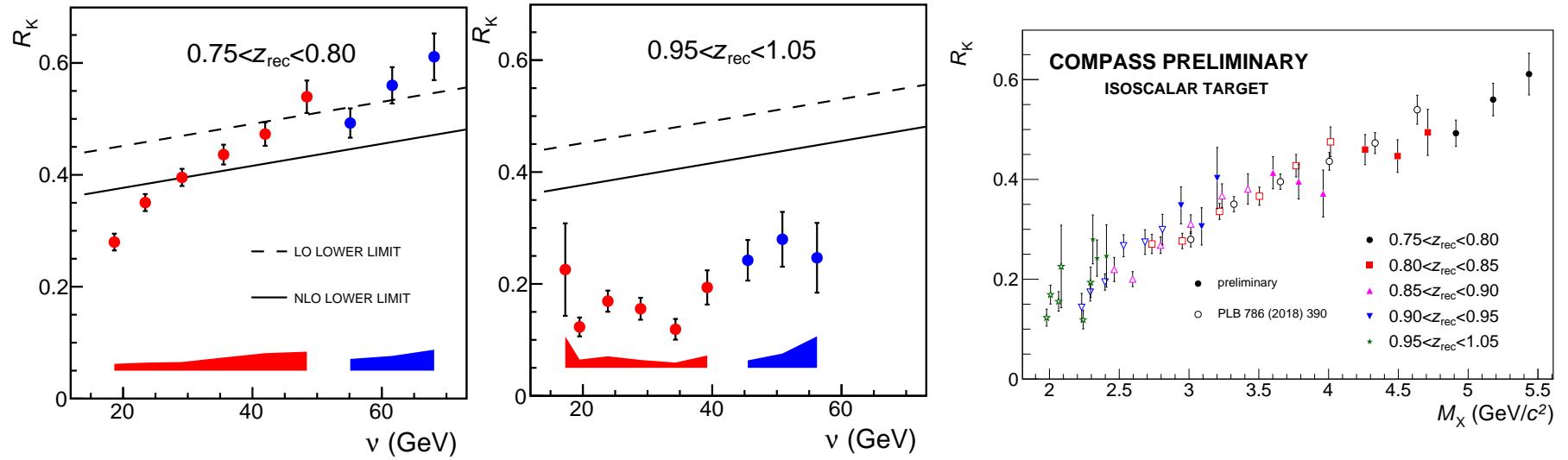


PLB 786 (2018)

- M_X nicely expresses both z and ν dependences
- ⇒ Low ν high z : Independent fragmentation is what becomes invalid
Fragmentation becomes sensitive to phase space for hadronisation of target remnants

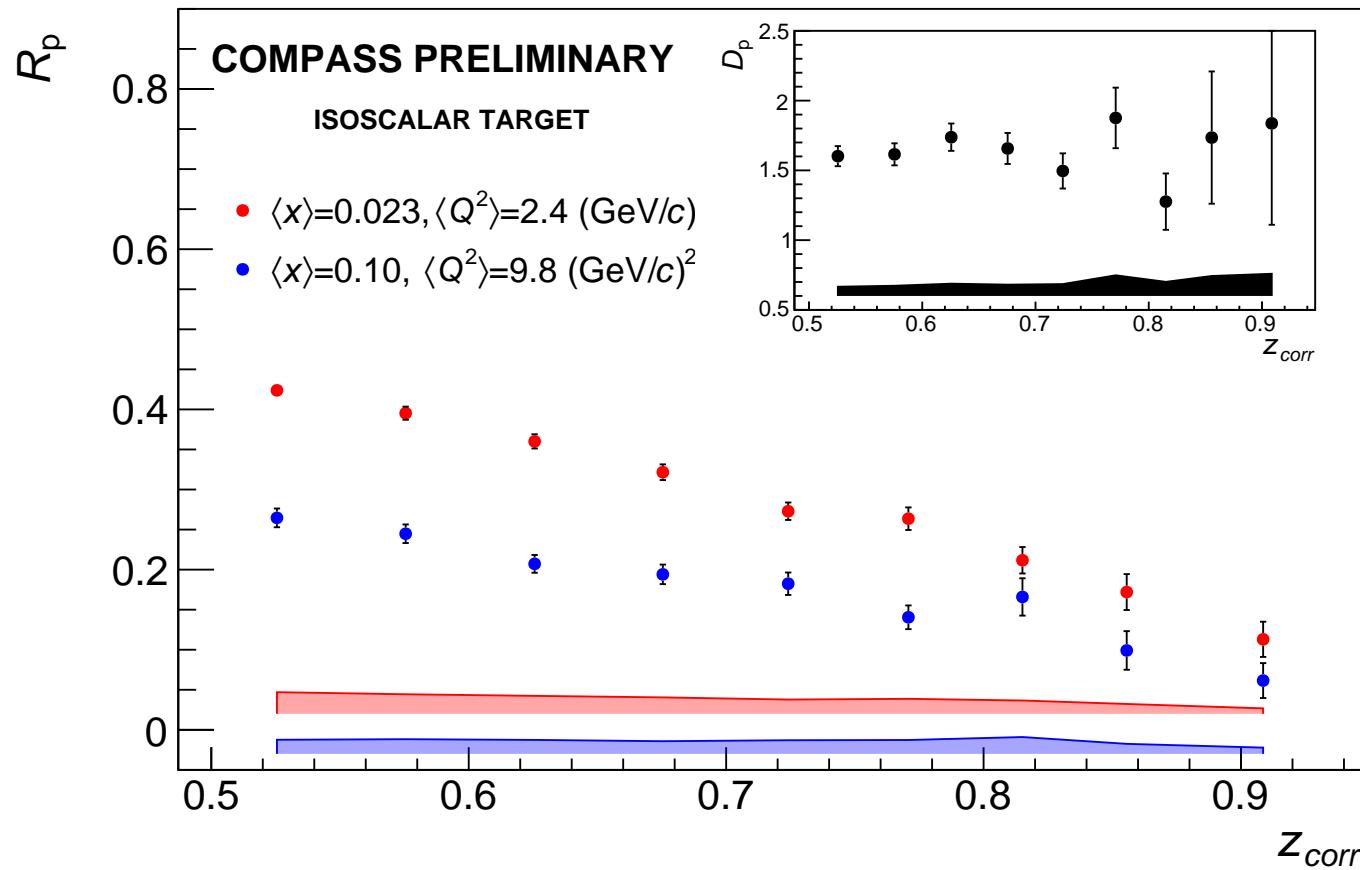
K^-/K^+ at high z : Extended ν range (Preliminary)

- RICH pID range extended: $[12,40] \rightarrow [12,55]$ GeV/ c
(thanks to, in part, Machine Learning techniques)



⇒ Extended range nicely completes the picture
w/ signs of saturation of R_K and restoration of independent fragmentation

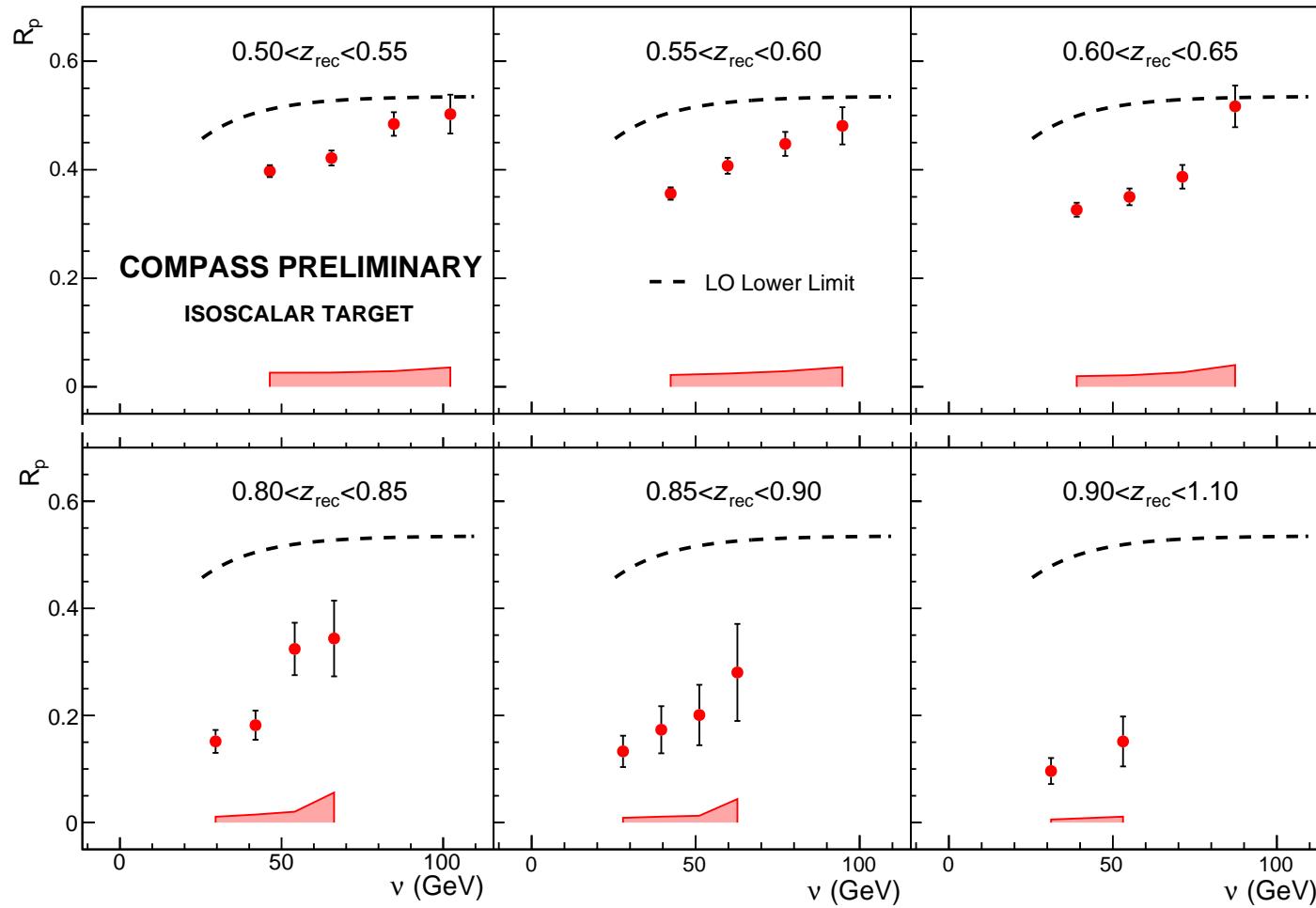
p^-/p^+ at high z (Preliminary)



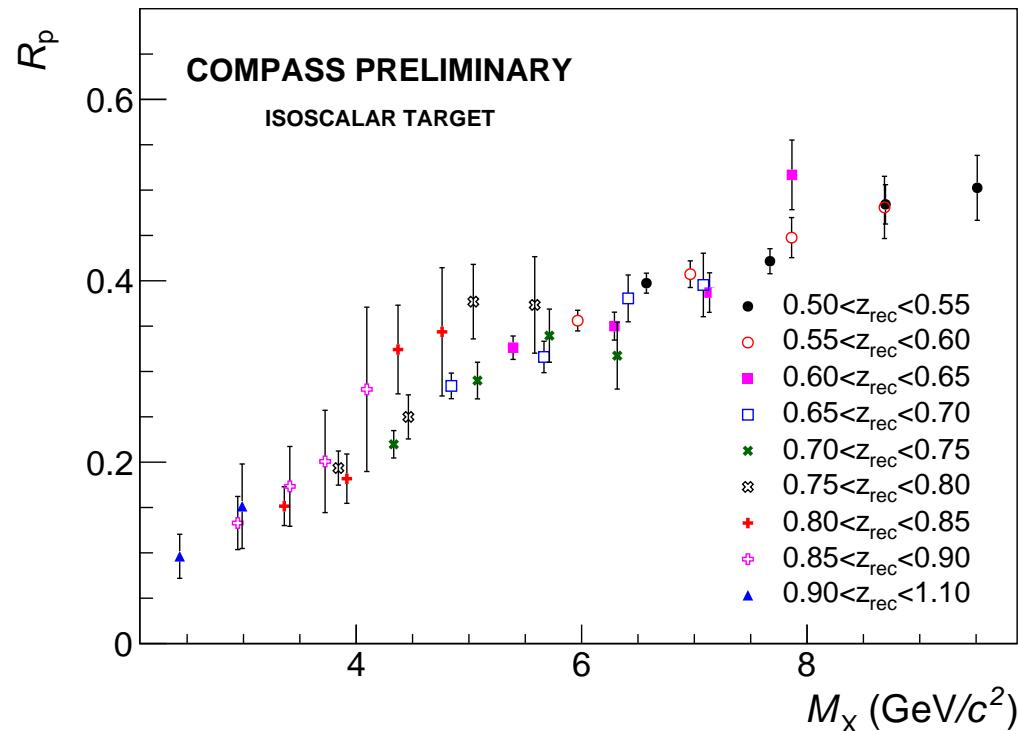
⇒ Well below LO pQCD limits, *viz.*: 0.51 and 0.28
(Note: Q^2 reaches $\sim 10 \text{ GeV}^2$)

p^-/p^+ at high z vs. ν (Preliminary)

- R_p in 9 bins of z (6 shown)
- Compared to LO limit



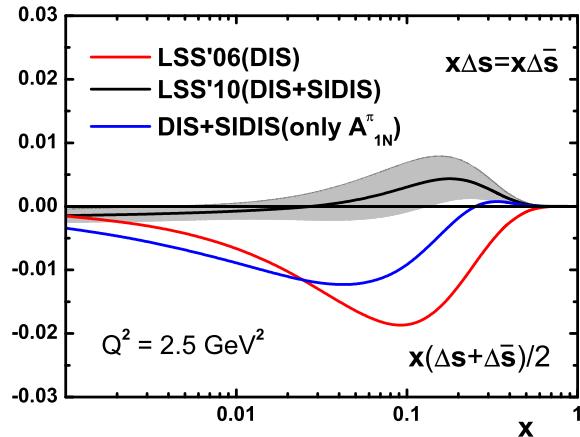
p^-/p^+ at high z vs. Missing Mass



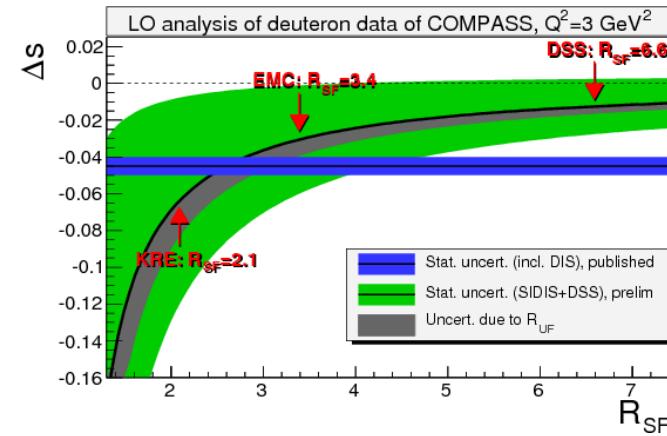
- As for K , M_X nicely expresses both z and ν dependences
- Hint that scaling variable is $(M_X - Thr)/M_h$

h^-/h^+ : Conclusions

- In COMPASS, we're sitting in a corner region of the phase space. . .
 - . . . but at lower energy, larger region is affected
- ⇒ This gives interesting insights:
- Possible explanation for HERMES/COMPASS K discrepancy supplementing (*w/ some overlap?*) HMC alla Accardi/Guerrero.
 - @ low ν positive contribution from Δu may mistaken for ΔS
⇒ biasing the extraction of ΔS from polarised DIS+SIDIS



LSS, PRD 84 (2011)



Δs dependence upon $R_{SF} = \mathcal{D}_s/\mathcal{D}_u$

- K and p account for 20-25% of all hadrons.
⇒ Analyses based on unidentified hadrons, *e.g.* TMD, may be biased

Outlook

- The region of applicability of pQCD in SIDIS should be revisited
- COMPASS: More results from 2016-17 runs: on proton target, $\sim .5 \text{ fb}^{-1}$

Spares