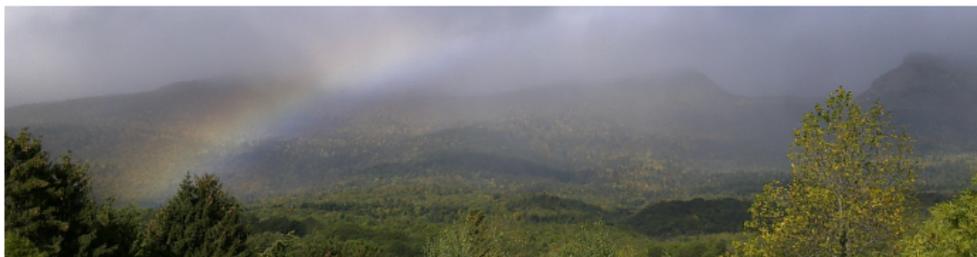


# (Light-meson) exotic resonances by COMPASS

Jan M. Friedrich

Physik-Department, TU München

*COMPASS collaboration*

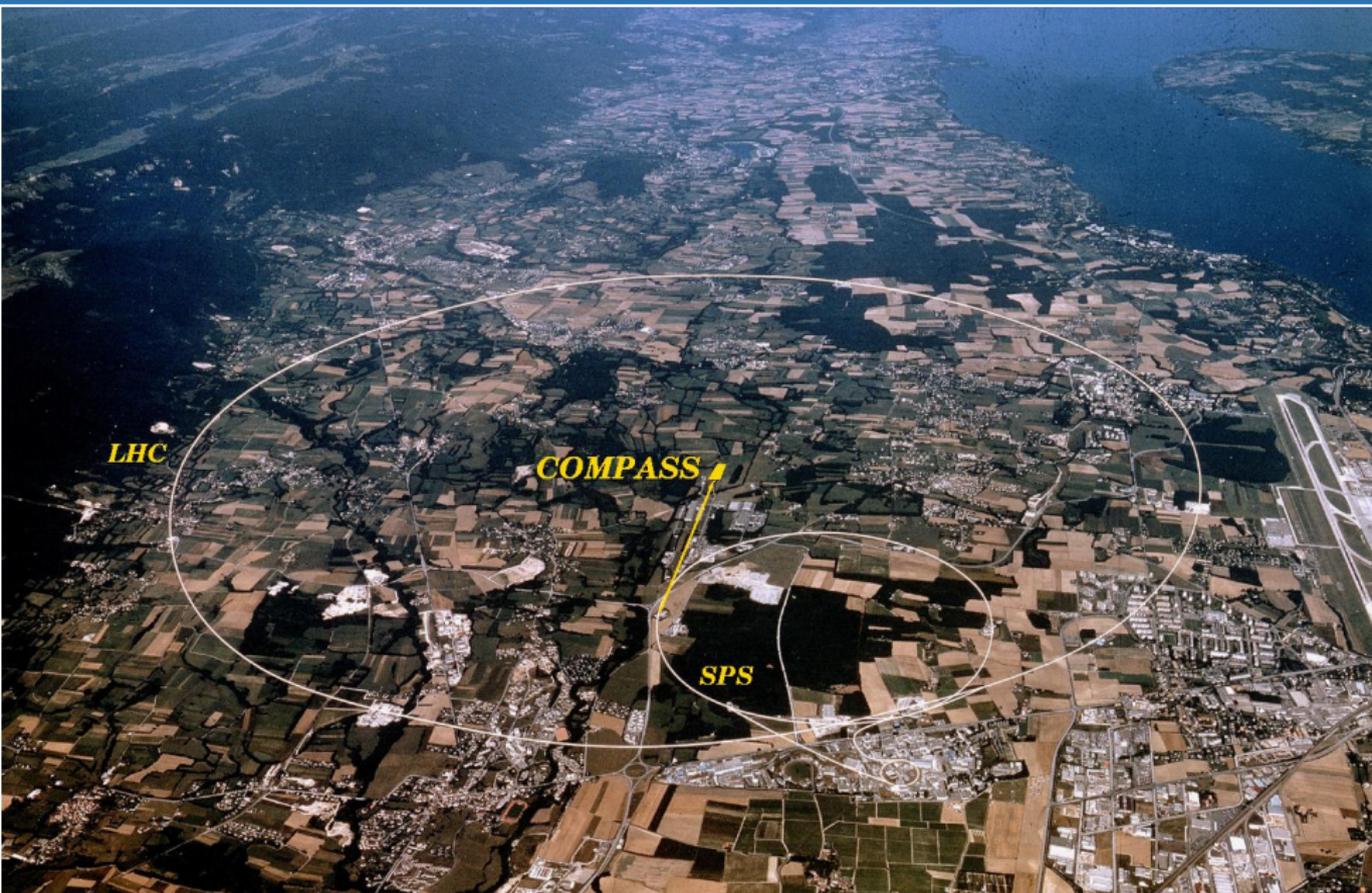


Resonance Workshop, Bergamo  
October 12, 2017



# The COMPASS experiment

Common Muon Proton Apparatus for Structure and Spectroscopy



LHC

COMPASS

SPS

# The COMPASS experiment

Common Muon Proton Apparatus for Structure and Spectroscopy

CERN SPS: protons  $\sim 450$  GeV (5 – 10 sec spills)

- tertiary muons:  $4 \cdot 10^7 / \text{s}$   
2002-04, 2006-07, 2010-11, 2016: nucleon spin structure
- secondary  $\pi, K, (\bar{p})$ : up to  $2 \cdot 10^7 / \text{s}$  (typ.  $5 \cdot 10^6 / \text{s}$ )  
Nov. 2004, 2008-09, 2012, 2015:  
hadron spectroscopy, Primakoff, Drell-Yan

LHC

COMPASS

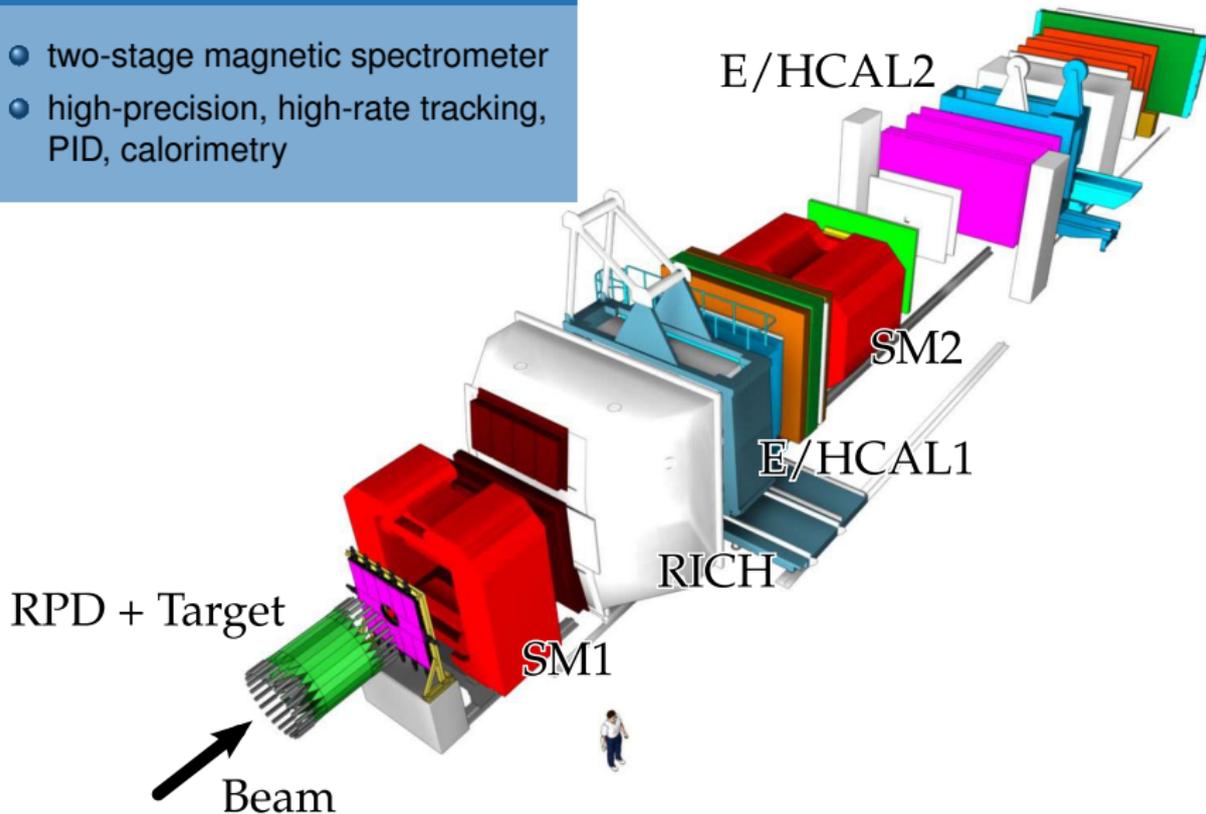
SPS

# The COMPASS experiment

Common Muon Proton Apparatus for Structure and Spectroscopy

## Fixed-target experiment

- two-stage magnetic spectrometer
- high-precision, high-rate tracking, PID, calorimetry

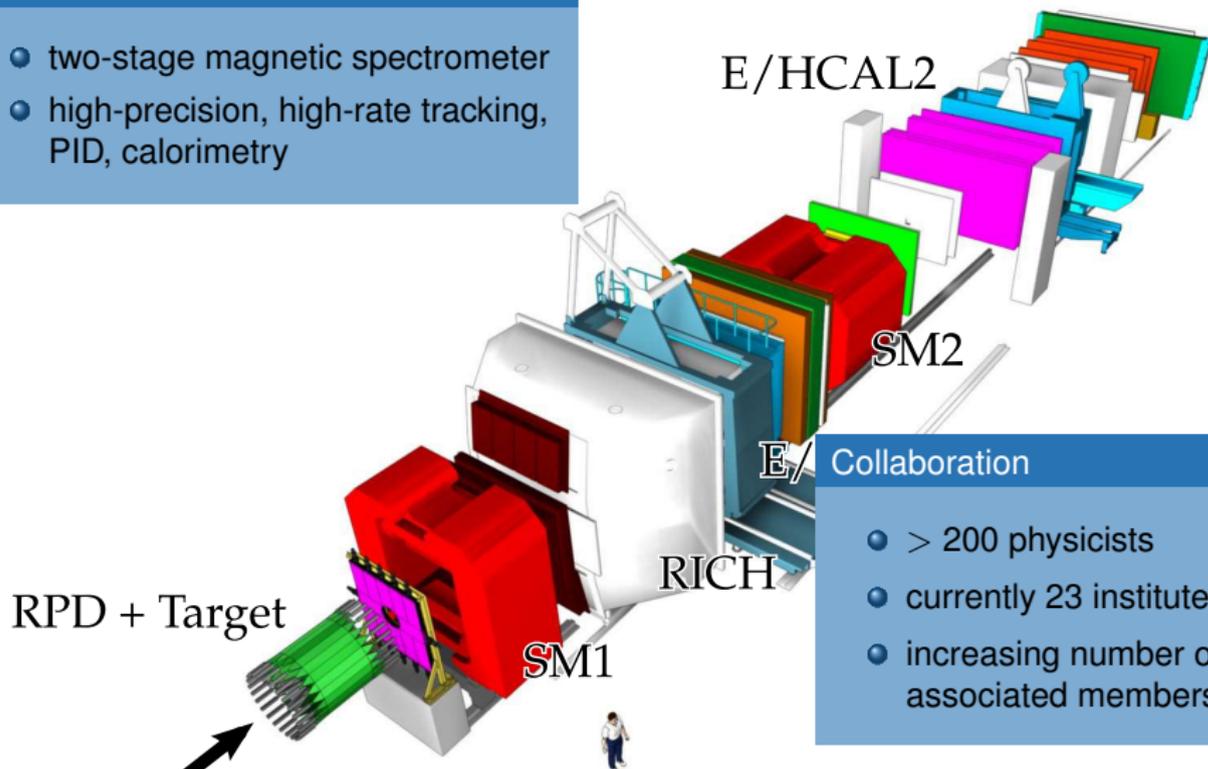


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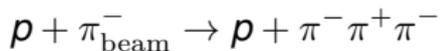


- ### Collaboration
- > 200 physicists
  - currently 23 institutes
  - increasing number of associated members



# Diffractive $3\pi$ production

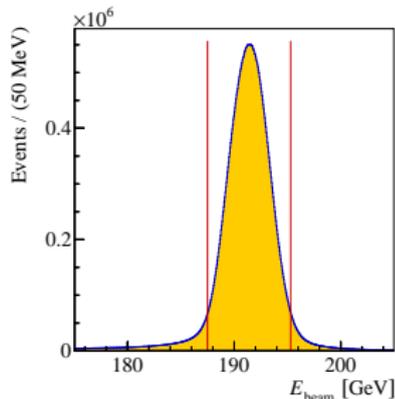
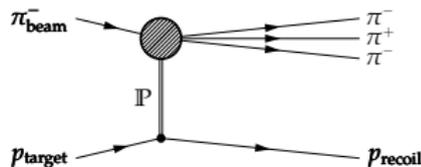
- COMPASS: World's currently largest data set for the diffractive process



taken in 2008

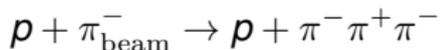
( $\sim 46 \cdot 10^6$  exclusive Events)

- Exclusive measurement



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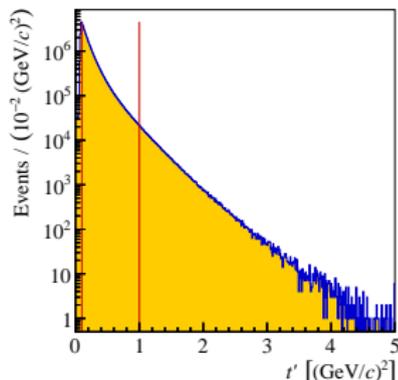
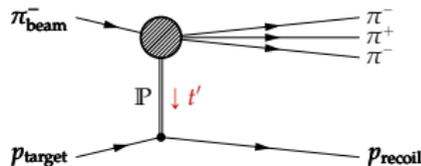
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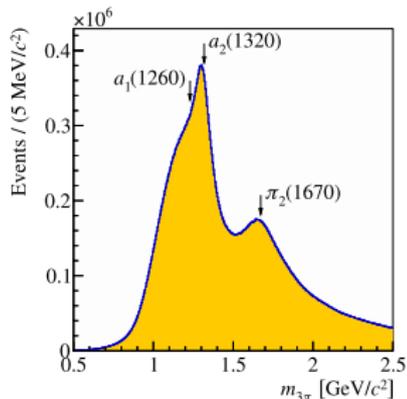
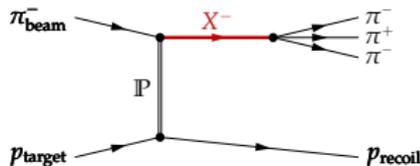
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$$p + \pi_{\text{beam}}^- \rightarrow p + \pi^- \pi^+ \pi^-$$

taken in 2008

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- Rich structure in  $\pi^- \pi^+ \pi^-$  mass spectrum: Intermediary states  $X^-$



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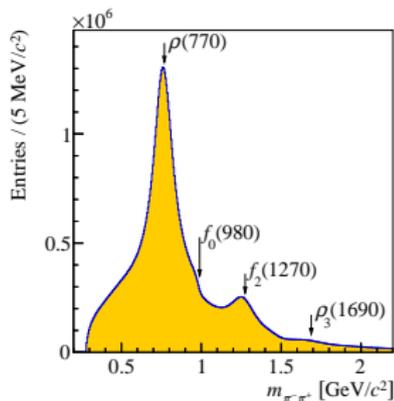
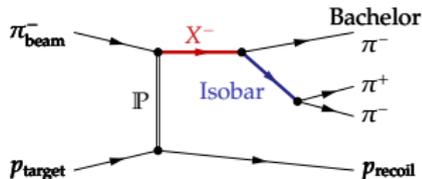
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- Squared four-momentum transfer  $t'$  by Pomeron  $\mathbb{P}$
- Rich structure in  $\pi^- \pi^+ \pi^-$  mass spectrum: Intermediary states  $X^-$
- Also structure in  $\pi^+ \pi^-$  subsystem: Intermediary states  $\xi$  (Isobar)



# Wanted: really good fits



- (1) all details of the three-body phase-space shall be matched, including momentum transfer dependence
- (2) Breit-Wigner resonances + smoother non-resonant contributions

# The isobar model

- Intermediate states appear as dynamic amplitudes  $\Delta(m)$ :  
Complex-valued functions of invariant mass  $m$

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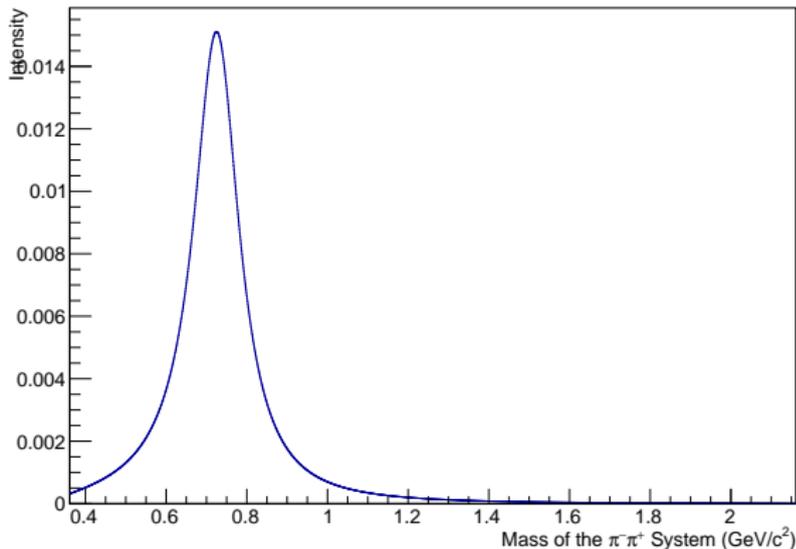
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# The isobar model

- Inter
- Com
- Simp
- Anal
- the c
- Dyna

Dynamic isobar amplitude:  $\rho(770)$ ,  $J^{PC} = 1^{--}$



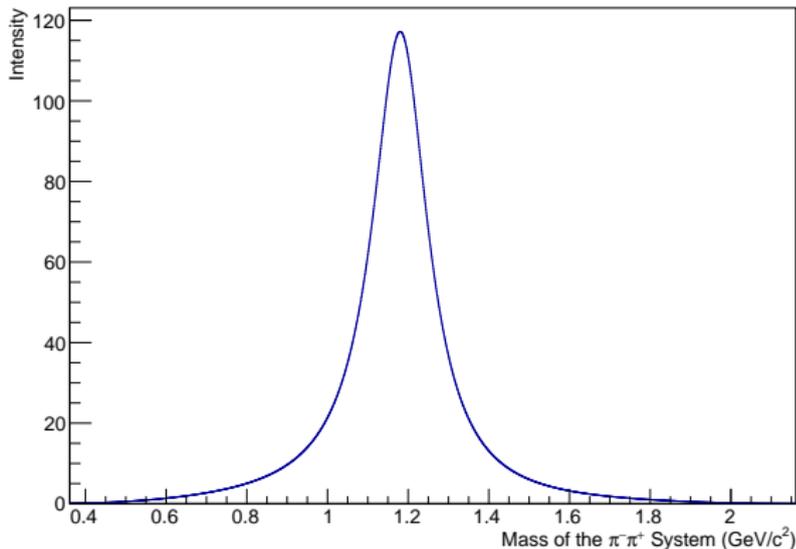
width  $\Gamma_0$ :

erred form

# The isobar model

- Inter
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- Anal
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- Dyna

Dynamic isobar amplitude:  $f_2(1270)$ ,  $J^{PC} = 2^{++}$



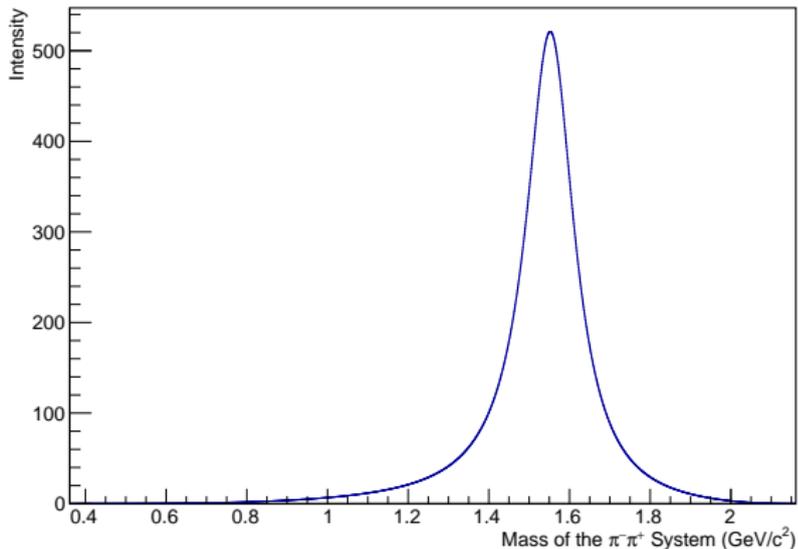
width  $\Gamma_0$ :

ferred form

# The isobar model

- Inter
- Com
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Dynamic isobar amplitude:  $\rho_3(1690)$ ,  $J^{PC} = 3^{--}$



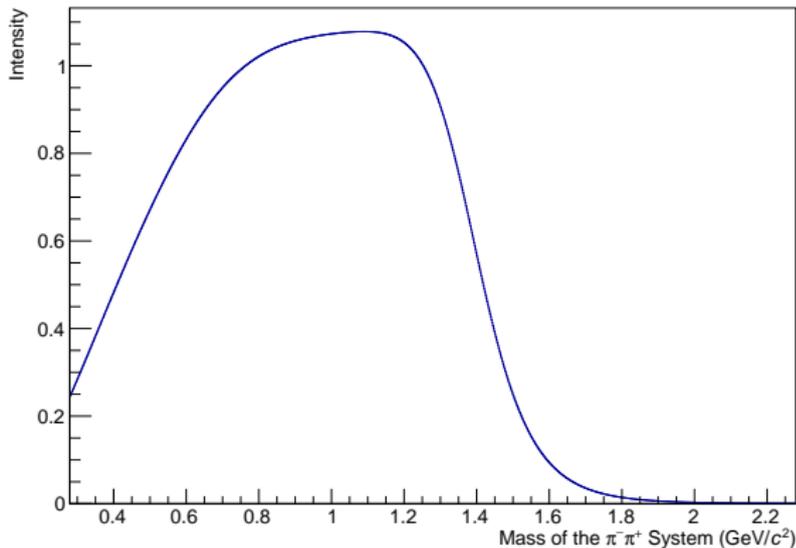
width  $\Gamma_0$ :

ferred form

# The isobar model

- Inter
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Dynamic isobar amplitude:  $[\pi\pi]_S$  wave,  $J^{PC} = 0^{++}$



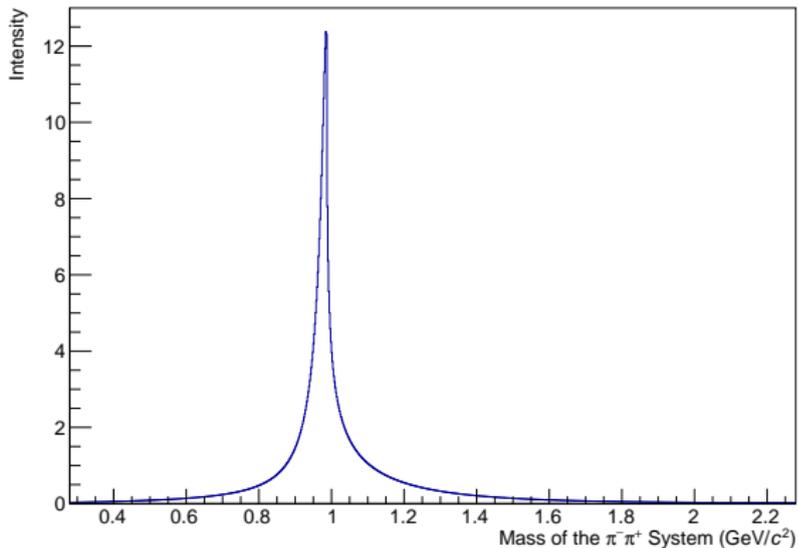
width  $\Gamma_0$ :

ferred form

# The isobar model

- Inter
- Com
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- Dyna

Dynamic isobar amplitude:  $f_0(980)$ ,  $J^{PC} = 0^{++}$



width  $\Gamma_0$ :

ferred form

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- Free parameters in dynamic isobar amplitudes computationally unfeasible

# Freed isobars: powerful test of the assumptions

Step-like isobar amplitudes

- Total intensity in each single  $(m_{3\pi}, t')$ -bin

$$\mathcal{I}(\vec{\tau}) = \left| \sum_i^{\text{waves}} \mathcal{T}_i [\psi_i(\vec{\tau}) \Delta_i(m_{\pi^-\pi^+}) + \text{Bose Symm.}] \right|^2$$

as function of phase-space variables  $\vec{\tau}$

Fit parameters: Production amplitudes  $\mathcal{T}_i$

Fixed: Angular distributions  $\psi(\vec{\tau})$ , dynamic isobar amplitudes  $\Delta_i(m_{\pi^-\pi^+})$

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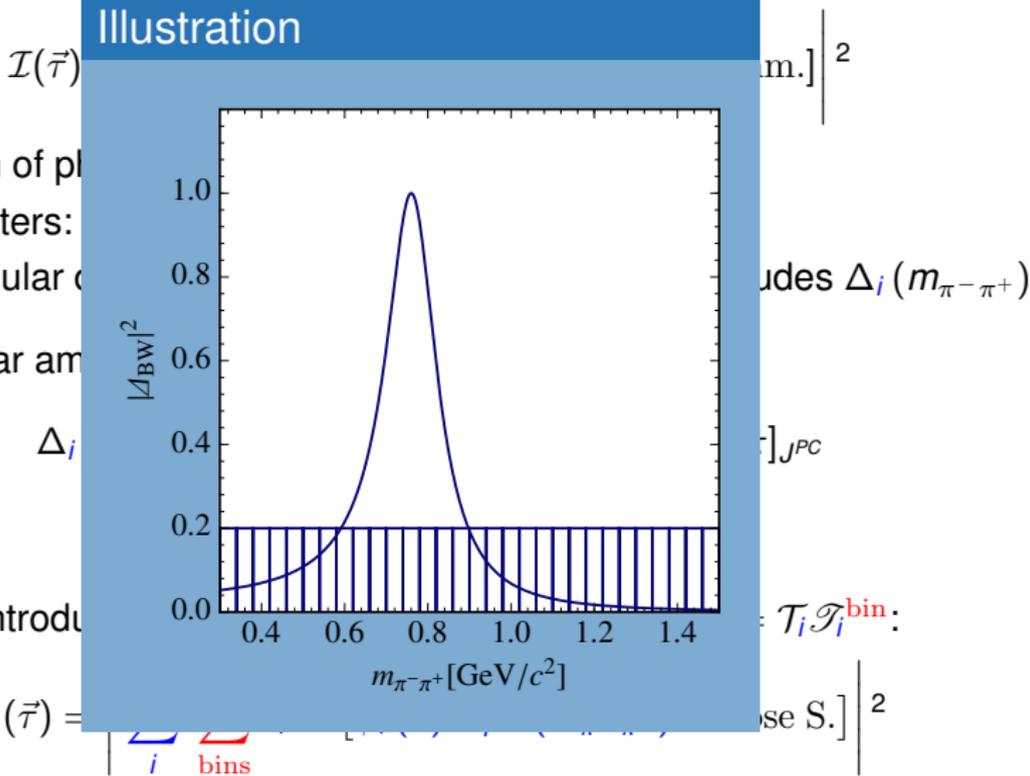
- Each bin introduces an independent Partial Wave  $\mathcal{T}_i^{\text{bin}} = \mathcal{T}_i \mathcal{F}_i^{\text{bin}}$ :

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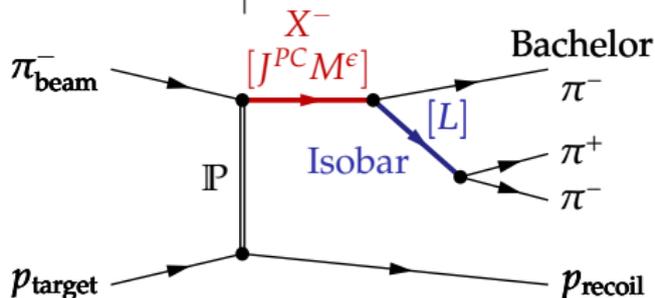


# Partial-Wave Analysis

$$\mathcal{I}(\vec{\tau}) = \left| \sum T_i \psi_i(\vec{\tau}) \Delta_i(m_{\pi^-\pi^+}) \right|^2$$

Waves specified by:

$$J^{PC} M^{\epsilon} \xi \pi L$$

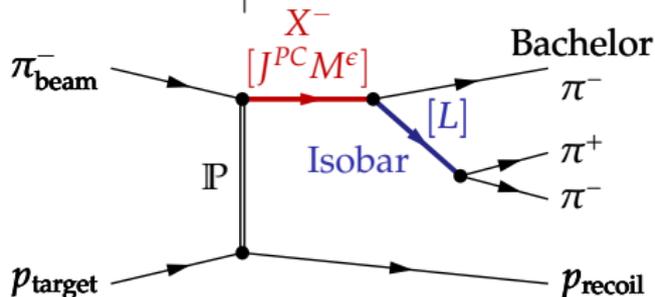


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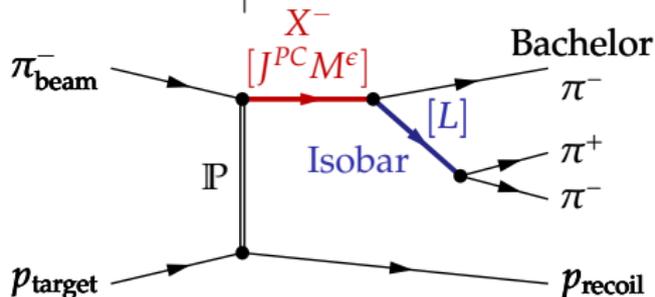
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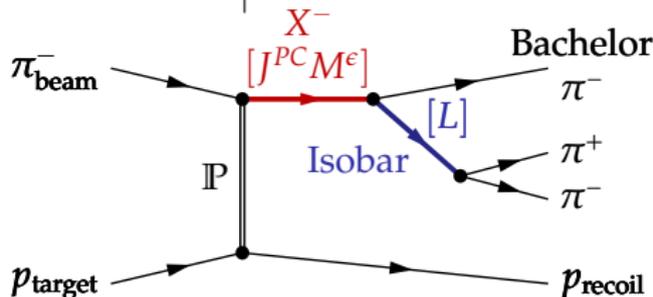
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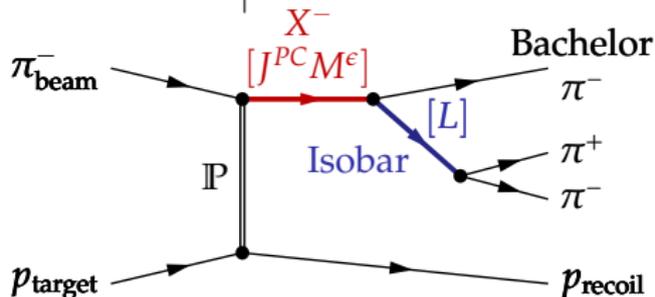
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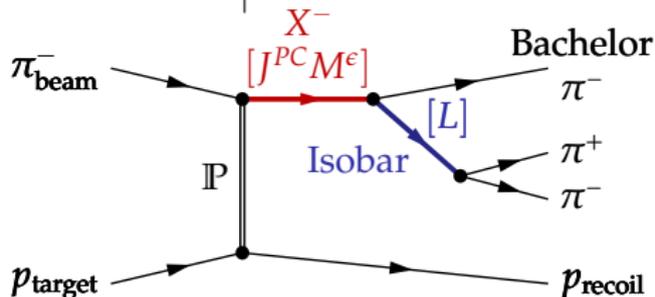
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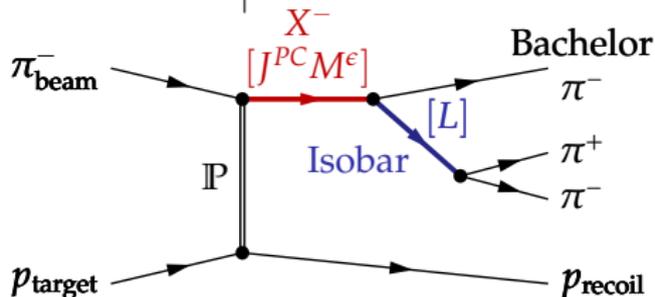
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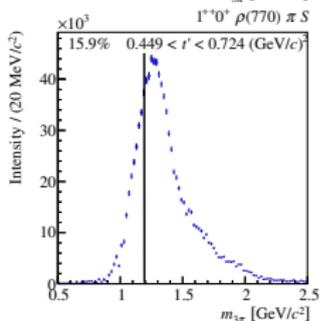
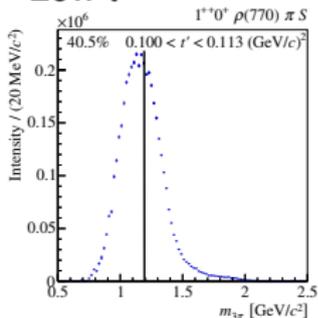
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**88 waves needed** to describe the data (“hand-selected”) interference terms  $\rightarrow$  get (relative) **phases**

# Step 1: Partial-Wave Analysis

Selected Waves (1 of 88) in two of the 11 independent  $t'$  bins

Low  $t'$

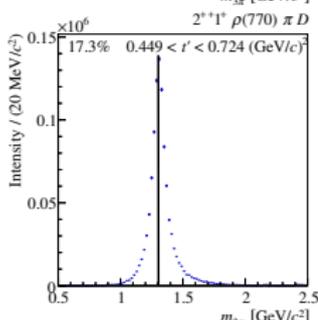
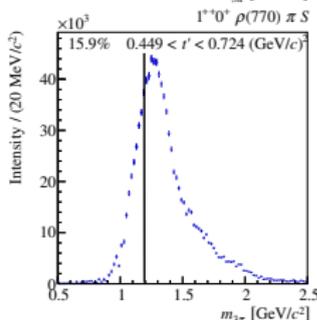
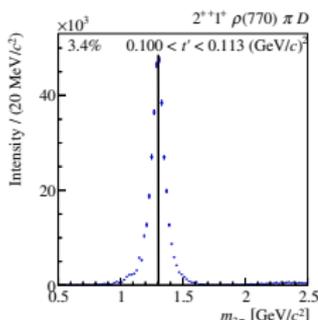
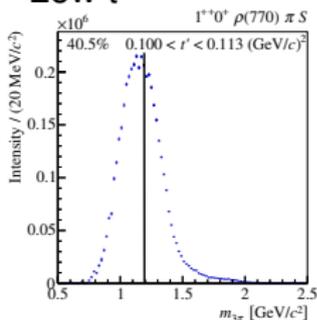


High  $t'$

# Step 1: Partial-Wave Analysis

Selected Waves (2 of 88) in two of the 11 independent  $t'$  bins

Low  $t'$

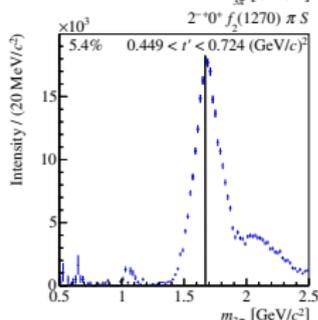
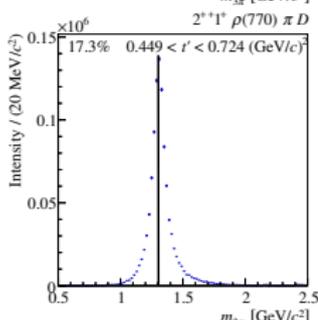
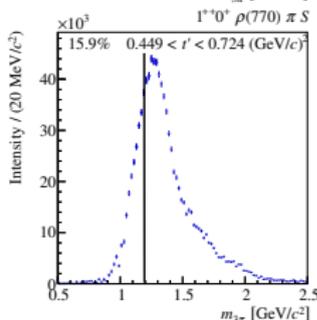
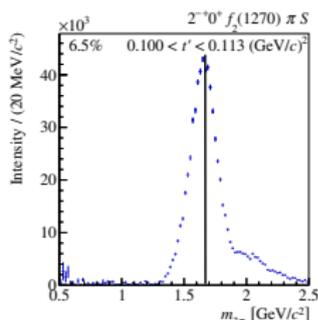
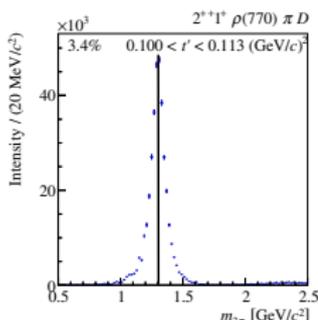
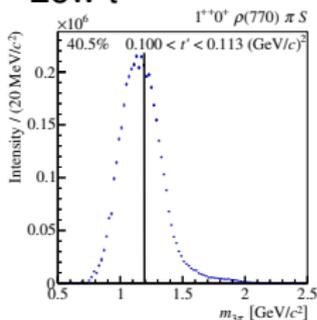


High  $t'$

# Step 1: Partial-Wave Analysis

Selected Waves (3 of 88) in two of the 11 independent  $t'$  bins

Low  $t'$

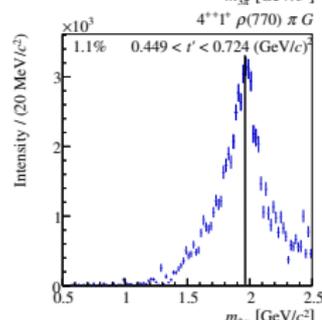
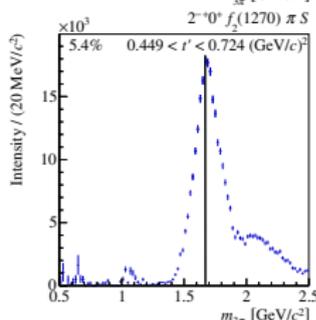
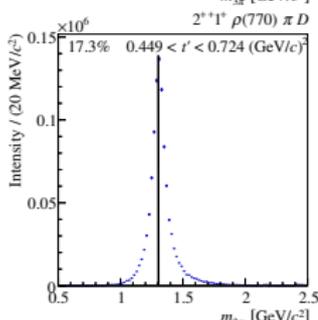
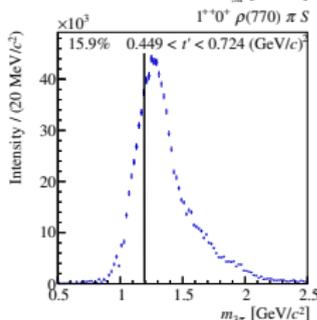
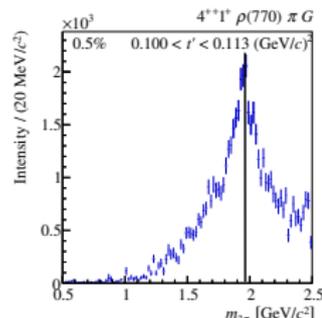
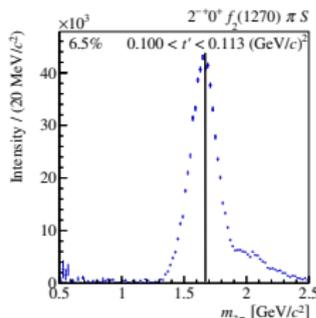
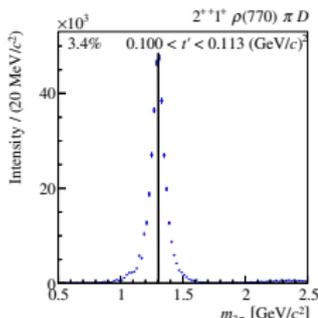
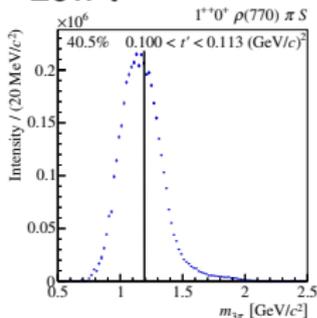


High  $t'$

# Step 1: Partial-Wave Analysis

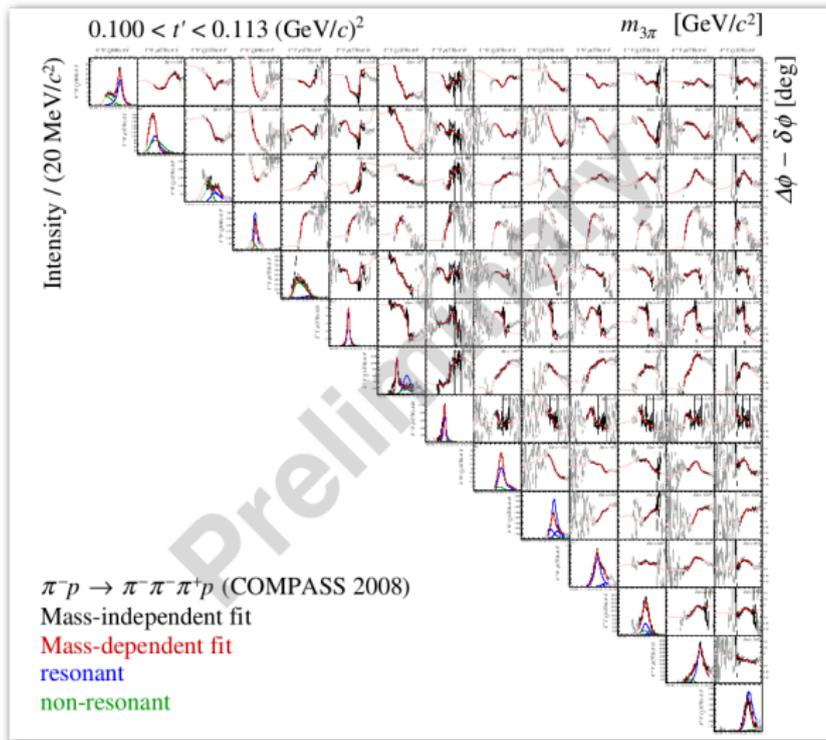
Selected Waves ( 4 of 88) in two of the 11 independent  $t'$  bins

Low  $t'$

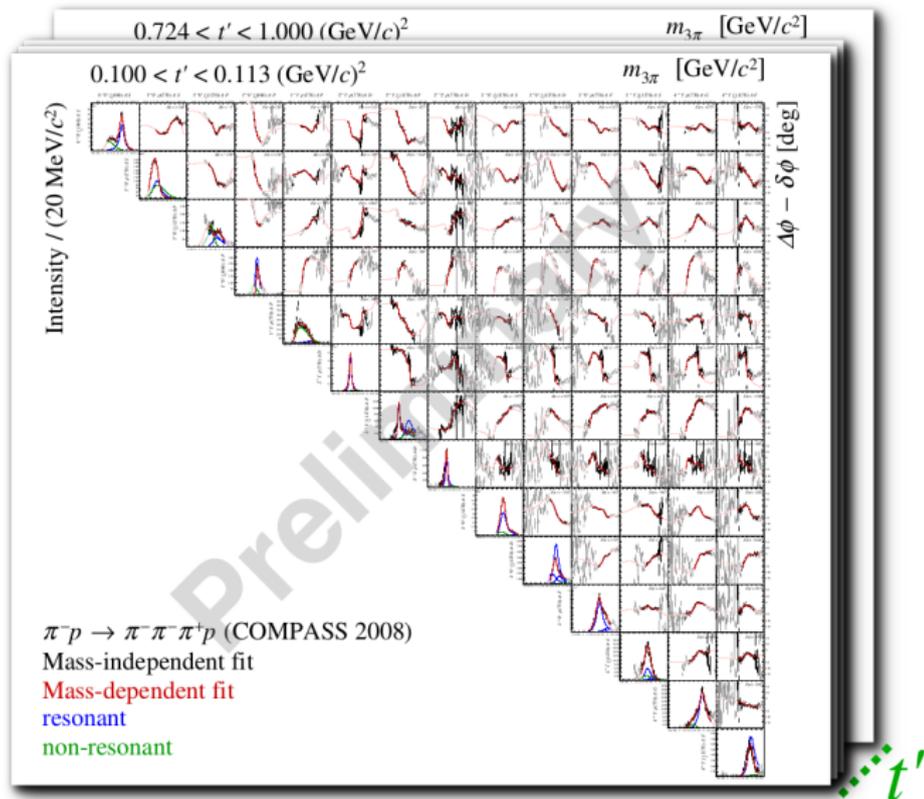


High  $t'$

# Step 2: Resonance model fit



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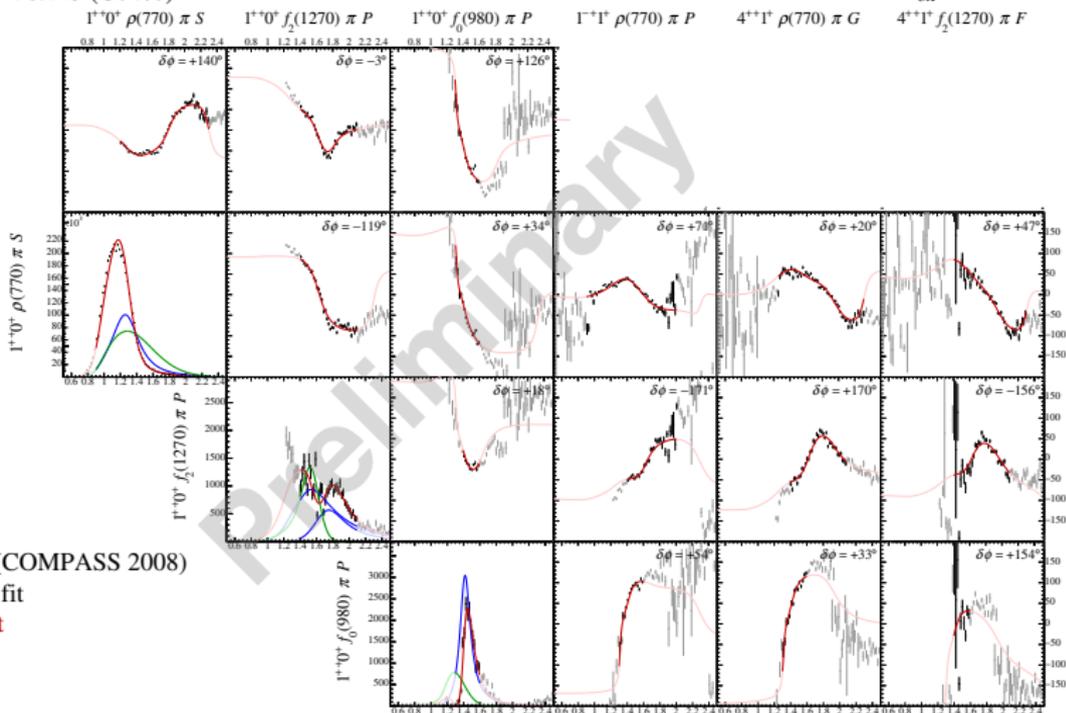


# Towards the first exotic signal: $J^{PC} = 1^{++}$ sector

$0.100 < t' < 0.113 \text{ (GeV}/c^2\text{)}$

$m_{3\pi} \text{ [GeV}/c^2\text{]}$

Intensity / (20 MeV/c<sup>2</sup>)  
 $0^{+0+} f_0(980) \pi S$



$\pi^- p \rightarrow \pi^- \pi^- \pi^+ p$  (COMPASS 2008)

Mass-independent fit

Mass-dependent fit

resonant

non-resonant

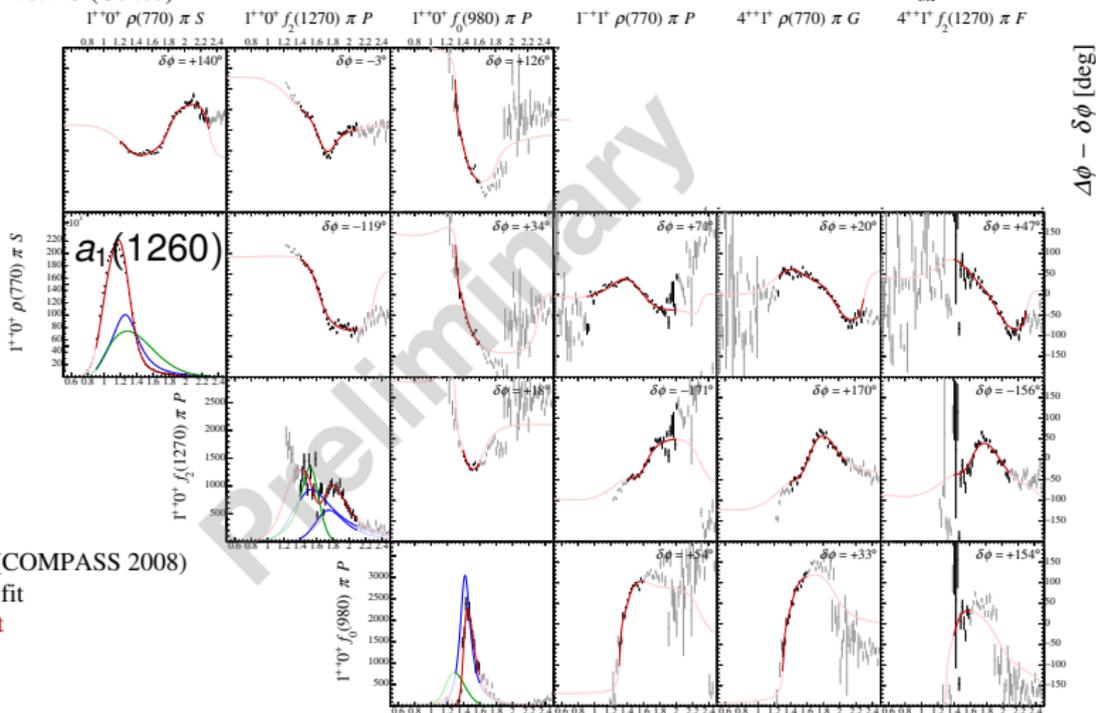
$\Delta\phi - \delta\phi \text{ [deg]}$

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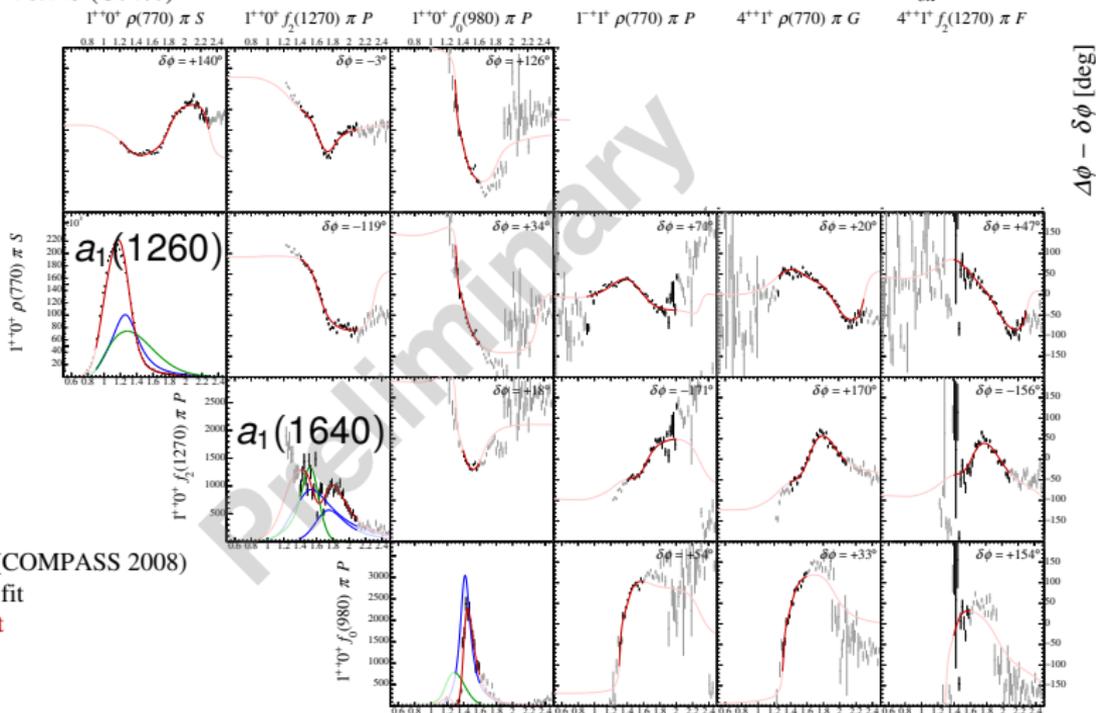
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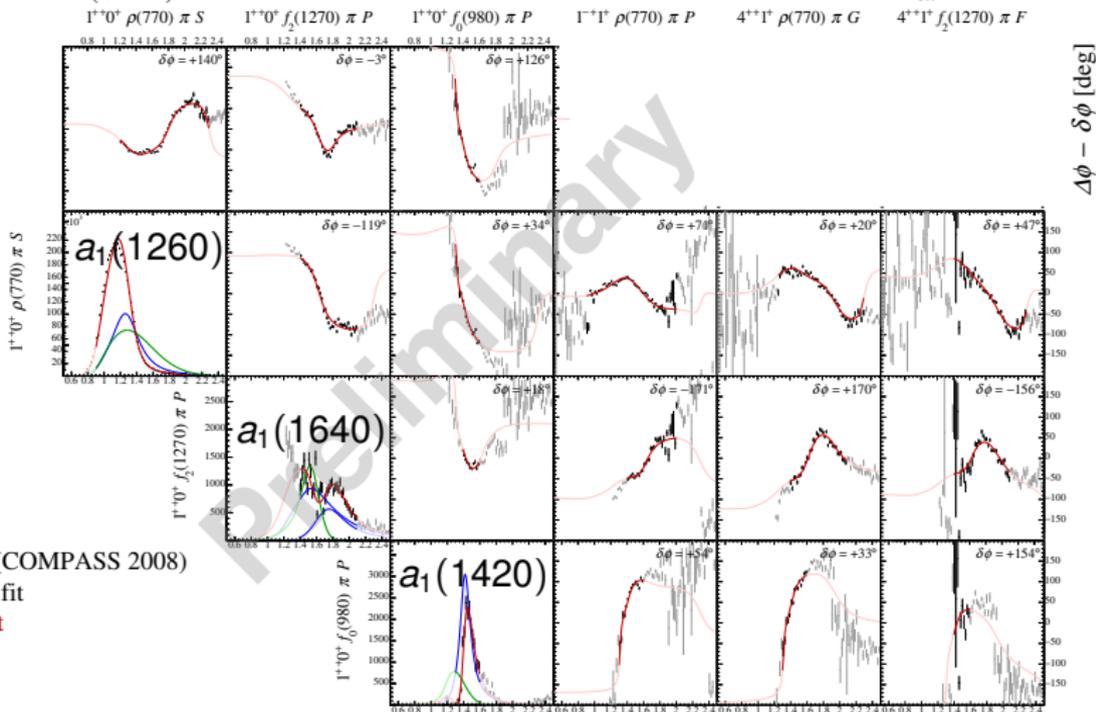


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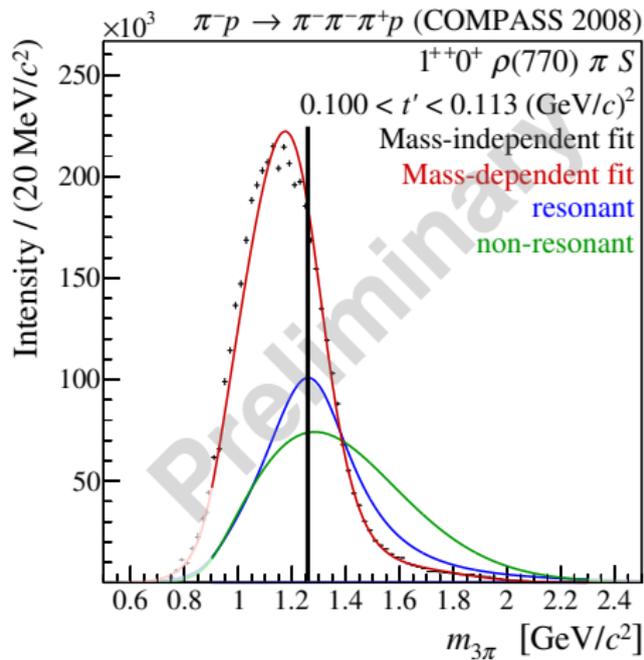
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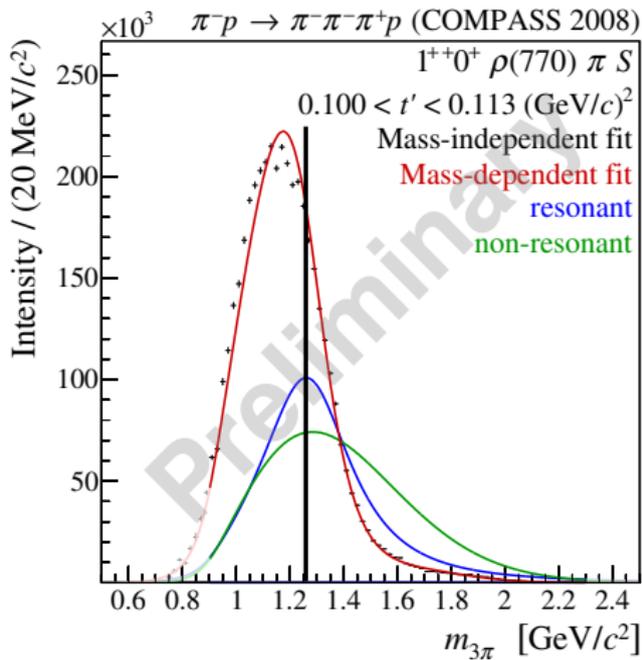
resonant

non-resonant

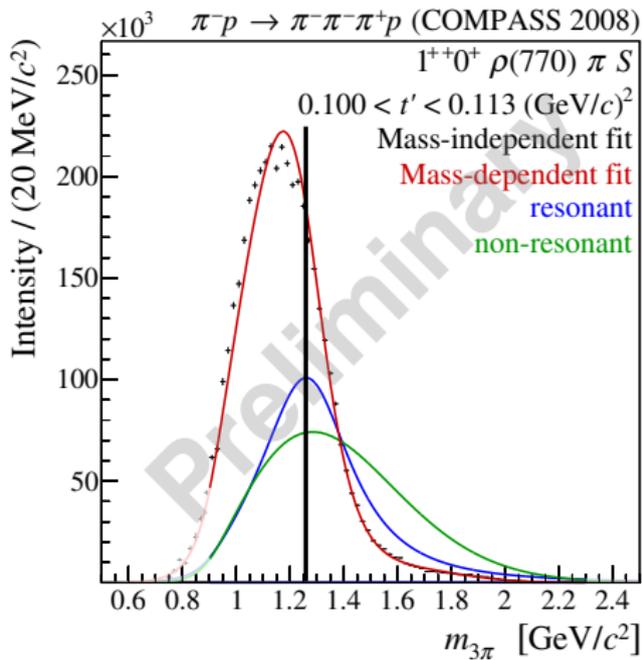
- resonance parameters do not depend on production mechanism



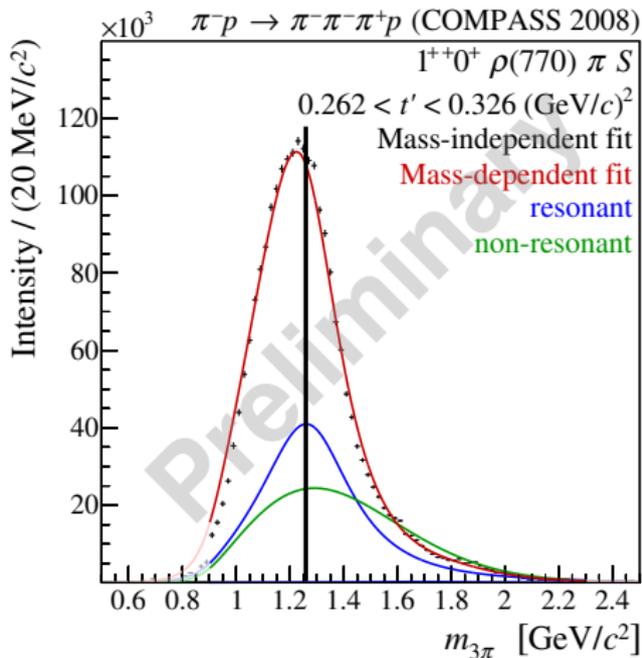
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- couplings and non-resonant parts may vary with  $t'$



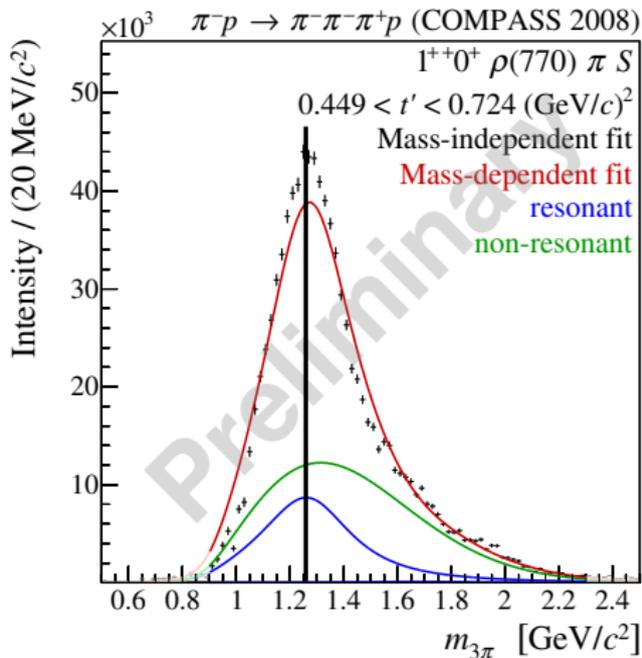
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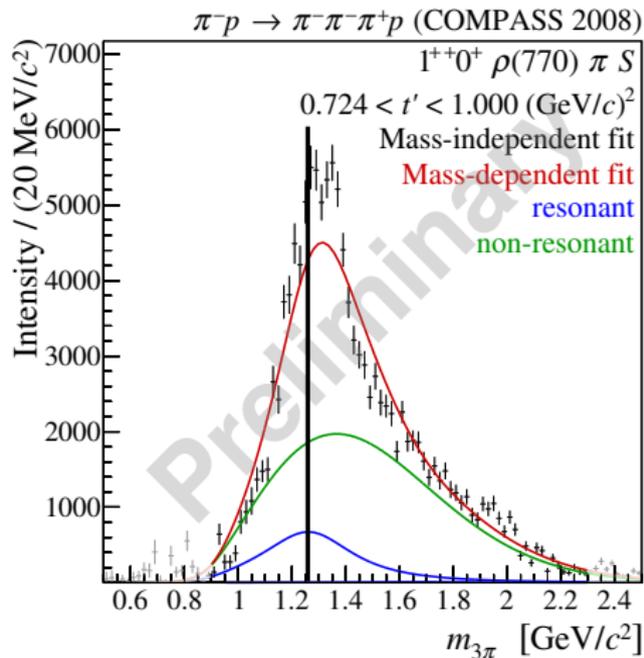
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# $a_1(1260)$

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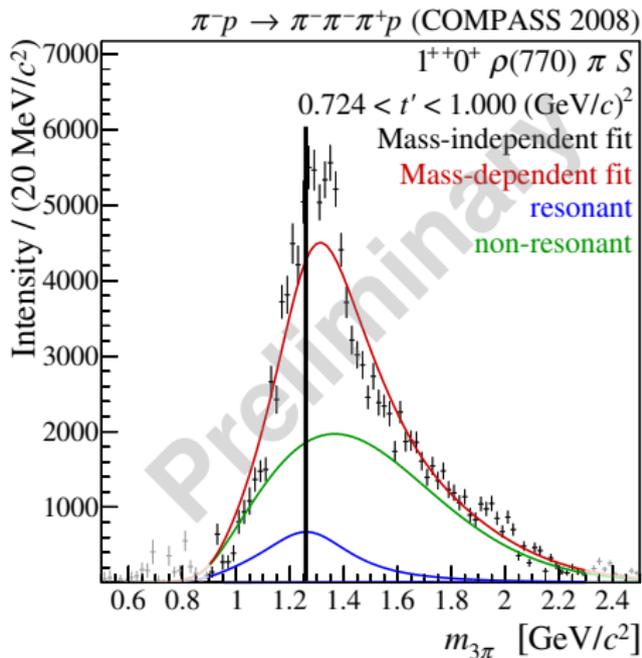
- $a_1(1260)$  reproduced:

$$m^{fit} = 1298^{+13}_{-22} \text{ MeV}/c^2$$

$$m^{PDG} = 1230 \pm 40 \text{ MeV}/c^2$$

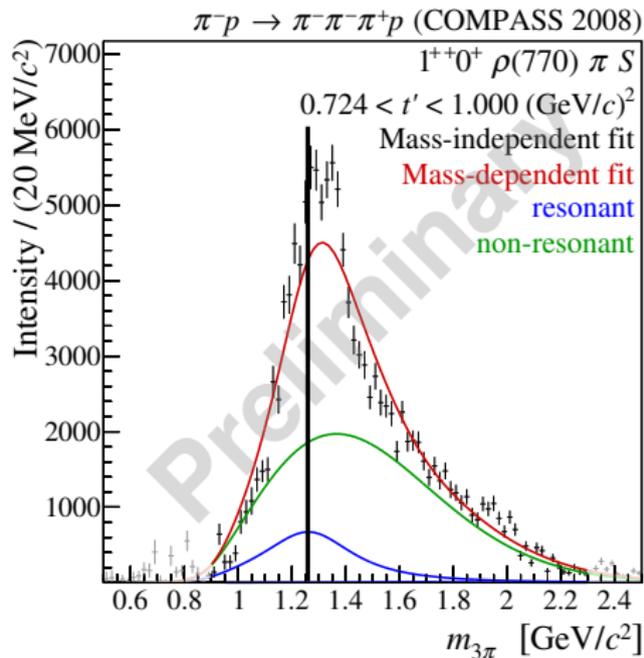
$$\Gamma^{fit} = 403^{+0}_{-100} \text{ MeV}/c^2$$

$$\Gamma^{PDG} = 250 - 600 \text{ MeV}/c^2$$



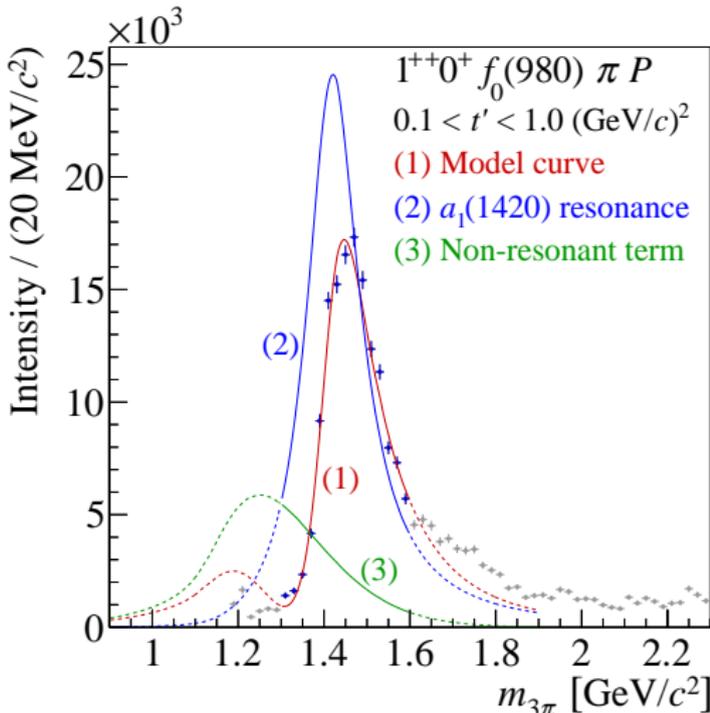
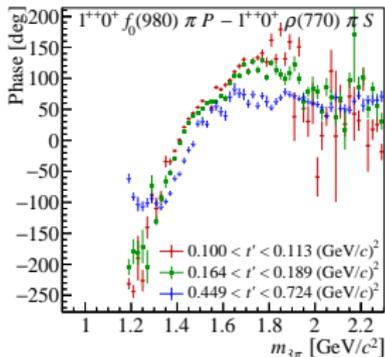
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- weak signal for  $a_1(1640)$



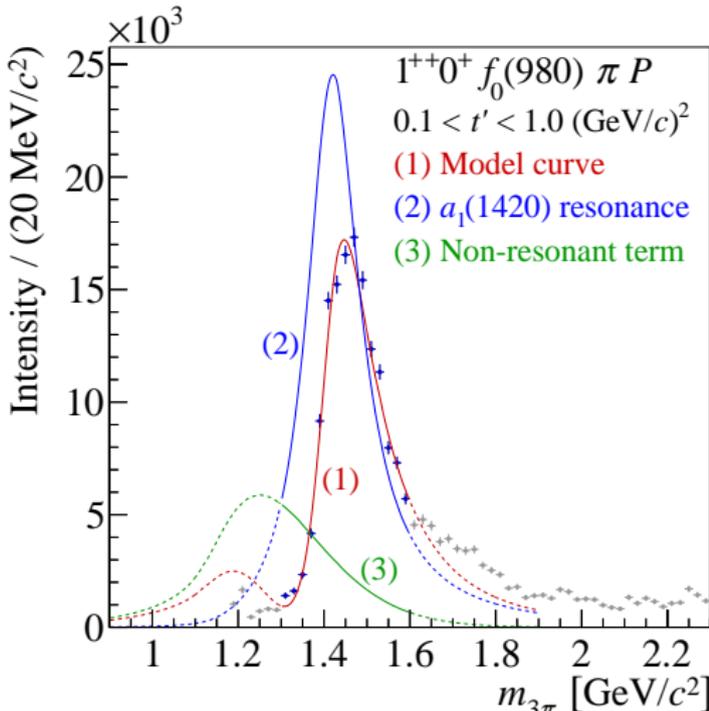
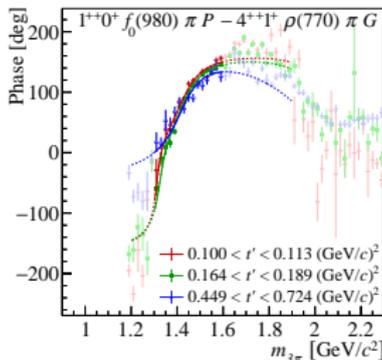
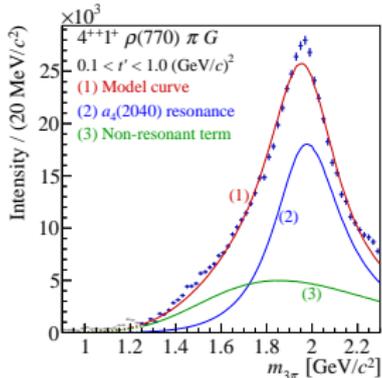
# $a_1(1420)$

a new - quite exotic - signal



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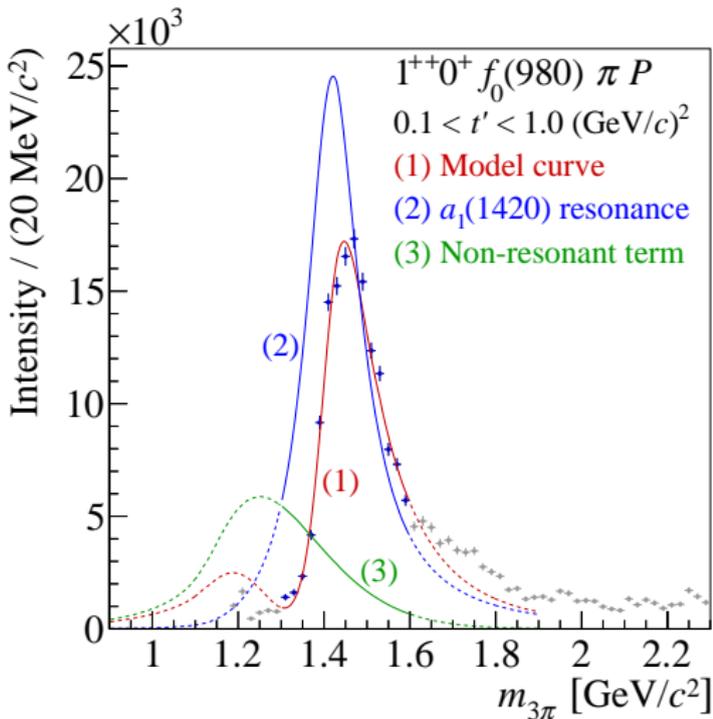
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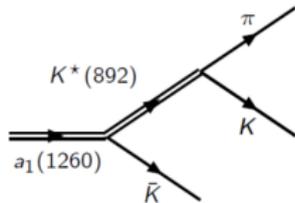
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- new signal:  $a_1(1420)$
- decay into  $f_0(980)\pi$

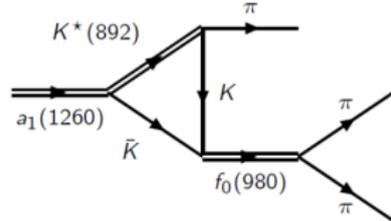


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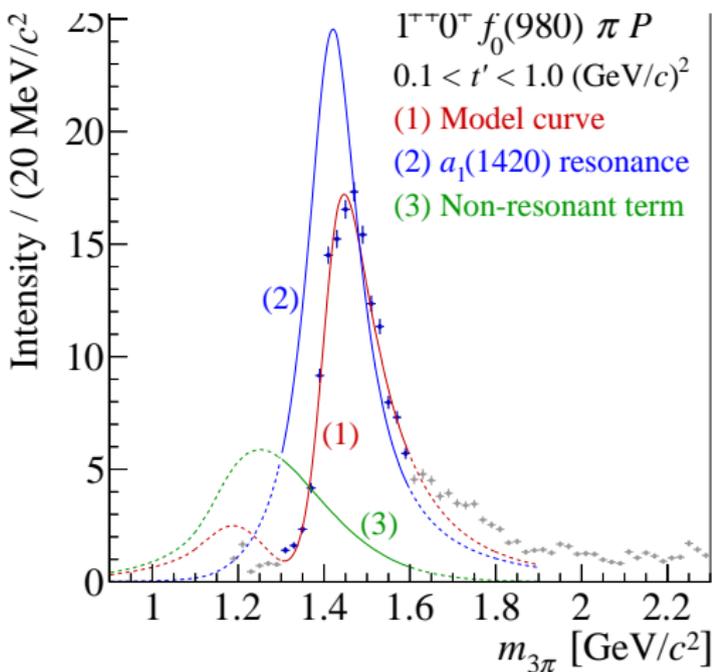
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→

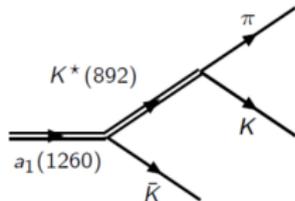


- new signal:  $a_1(1420)$
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- possible explanations:
  - ▶ triangle diagram *Mikhasenko, Ketzer, Sarantsev* PRD91 (2015) 094015
  - ▶ two-channel unitarized Deck amplitude *Basdevant, Berger* PRL114 (2015) 192001

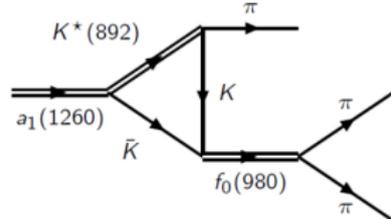


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→



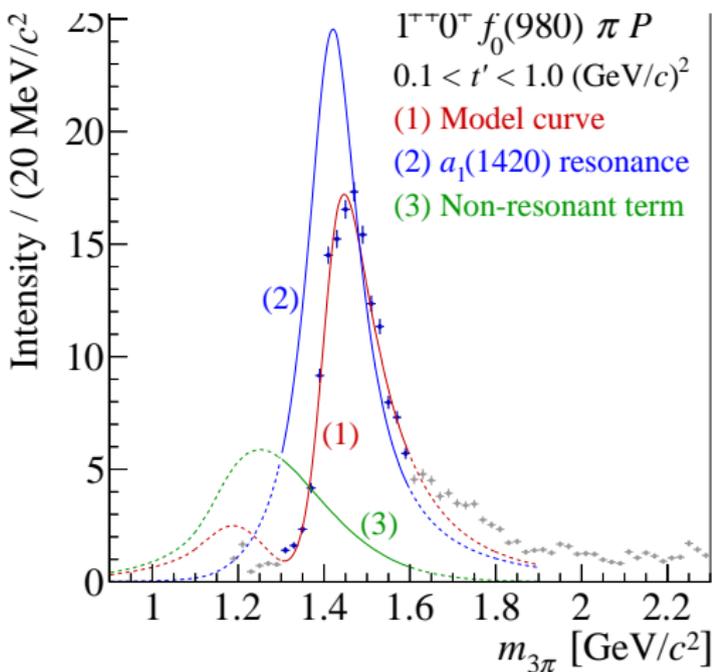
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- Mass:

$$m_{a_1(1420)} = 1411.8^{+1.0}_{-4.4} \text{ MeV}/c^2$$

Width:

$$\Gamma_{a_1(1420)} = 158^{+8}_{-8} \text{ MeV}/c^2$$



- the analysis so far:
  - ▶ Wave set: 88 waves
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- Replace 7 fixed-isobar waves

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Some data set

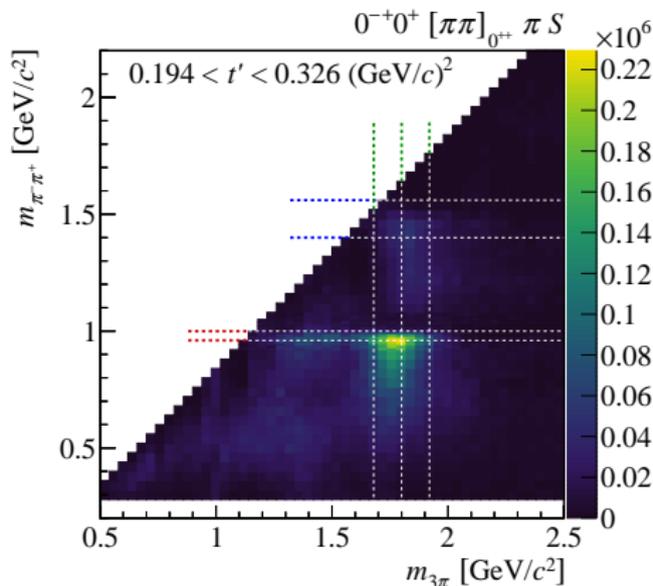
## Matching isobar quantum numbers

- T  
f  
$$\left. \begin{array}{l} 0^{-+}0^{+} [\pi\pi]_S \pi S \\ 0^{-+}0^{+} f_0(980) \pi S \\ 0^{-+}0^{+} f_0(1500) \pi S \end{array} \right\} 0^{-+}0^{+} [\pi\pi]_{0^{++}} \pi S$$
- F  
$$\left. \begin{array}{l} 1^{++}0^{+} [\pi\pi]_S \pi P \\ 1^{++}0^{+} f_0(980) \pi P \end{array} \right\} 1^{++}0^{+} [\pi\pi]_{0^{++}} \pi P$$
- F  
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# Towards another exotic: freed-isobar wave set

Already published

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- Replace 7 fixed-isobar waves
- Published in Phys. Rev. **D95** no. 3, (2017) 032004
- Promising results



# Freed-isobar wave set

Extended wave set

*credit: Fabian Krinner (PhD work, cf. HADRON2017 talk), Dima Ryabchikov*

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## Freed isobar wave set

$$\begin{array}{lll} 0^{-+}0^{+}[\pi\pi]_{0^{++}}\pi S & 2^{-+}0^{+}[\pi\pi]_{0^{++}}\pi D & 1^{++}1^{+}[\pi\pi]_{1^{--}}\pi S \\ 0^{-+}0^{+}[\pi\pi]_{1^{--}}\pi P & 2^{-+}0^{+}[\pi\pi]_{1^{--}}\pi P & 2^{-+}1^{+}[\pi\pi]_{1^{--}}\pi P \\ 1^{++}0^{+}[\pi\pi]_{0^{++}}\pi P & 2^{-+}0^{+}[\pi\pi]_{1^{--}}\pi F & 2^{++}1^{+}[\pi\pi]_{1^{--}}\pi D \\ 1^{++}0^{+}[\pi\pi]_{1^{--}}\pi S & 2^{-+}0^{+}[\pi\pi]_{2^{++}}\pi S & \end{array}$$

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- 40 MeV bin width in  $m_{3\pi}$  from 0.5 to 2.5 GeV
- 50 bins in  $m_{3\pi}$ , four bins in  $t'$ :  $4 \times 50 = 200$  independent bins

# Zero mode in the spin-exotic wave

What is a “zero mode”?

- Freed-isobar analysis: much more freedom than fixed-isobar analysis  
→ introduces continuous mathematical ambiguities in the model

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→ introduces continuous mathematical ambiguities in the model
- “Zero mode”: dynamic isobar amplitudes  $\Omega(m_{\pi^-\pi^+})$   
that do **not** contribute to the **total**  $3\pi$ -amplitude
- Spin-exotic wave:

$$\psi(\vec{\tau}) \Omega(m_{\pi^-\pi^+}) + \text{Bose S.} = 0$$

at **every point**  $\vec{\tau}$  in phase space

# Zero mode in the spin-exotic wave

## Mathematical origin

- Process:  $X^- \rightarrow \xi \pi_3^- \rightarrow \pi_1^- \pi_2^+ \pi_3^-$ .
- Partial-wave amplitude

$$\psi(\vec{\tau}) \Omega(m_{12}) + \text{Bose S.} = 0 \quad (1)$$

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$$|\psi(\vec{\tau}) \Delta^{\text{phys}}(m_\xi) + \text{B. S.}|^2 = |\psi(\vec{\tau}) [\Delta^{\text{phys}}(m_\xi) + C \Omega(m_\xi)] + \text{B. S.}|^2$$

for any complex-valued zero-mode coefficient  $C$

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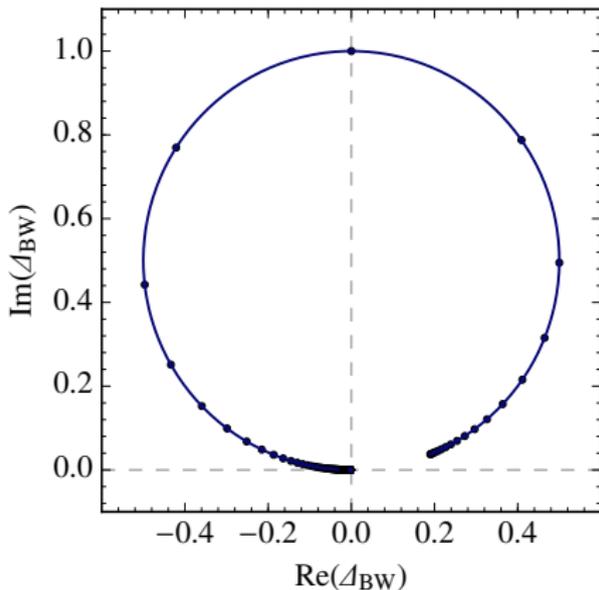
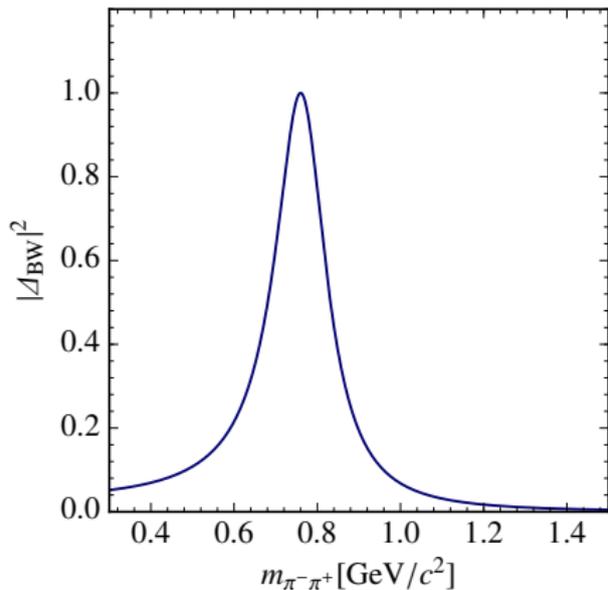
- $\mathcal{C}$ : complex-valued ambiguity in the model

# Zero mode in the spin-exotic wave

Effects on dynamic isobar amplitudes

$$\Delta_{\text{BW}}(m_{\pi^-\pi^+}) + \mathcal{C}\Omega(m_{\pi^-\pi^+})$$

$$\mathcal{C} = 0.00 + 0.00i$$



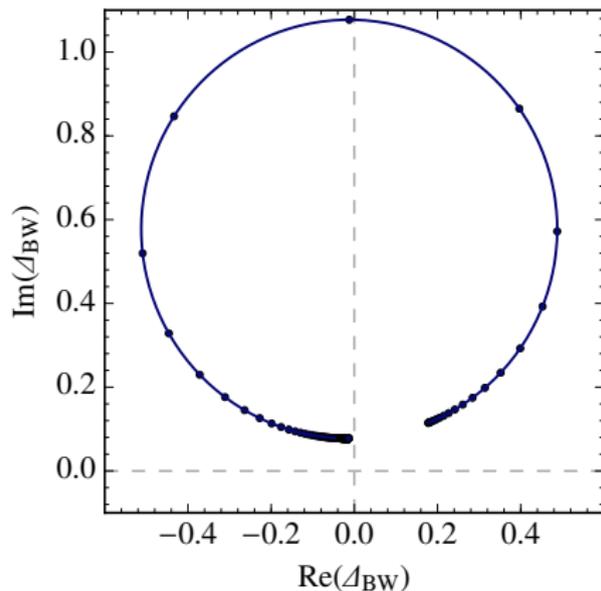
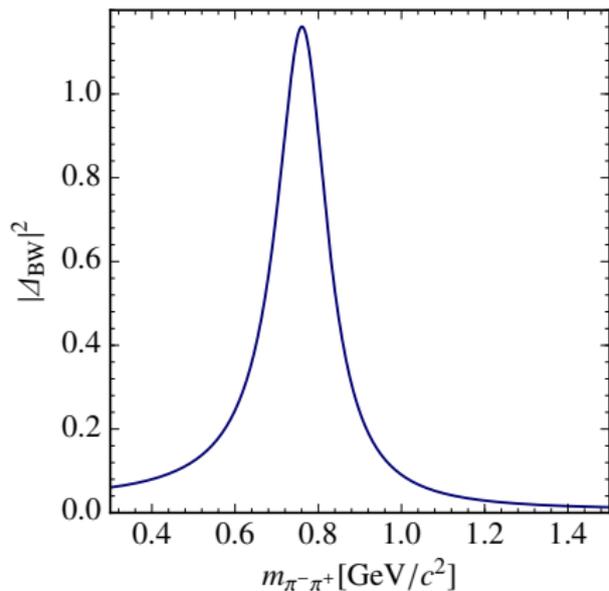
All describe the same  $3\pi$ -intensity

# Zero mode in the spin-exotic wave

Effects on dynamic isobar amplitudes

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$$\mathcal{C} = -0.01 + 0.08i$$



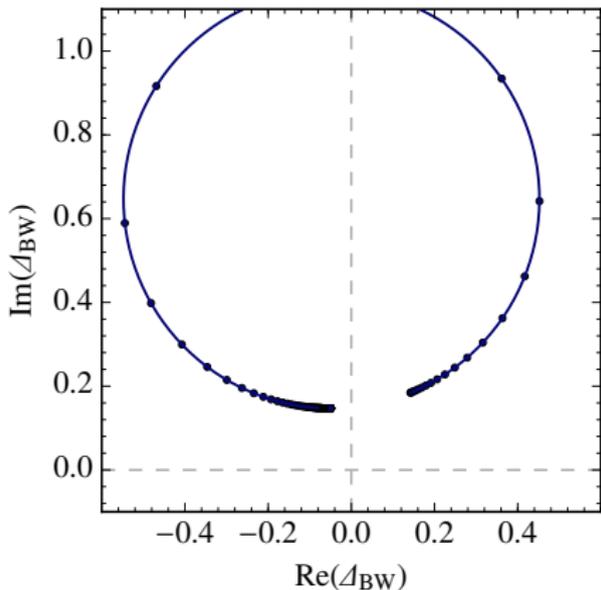
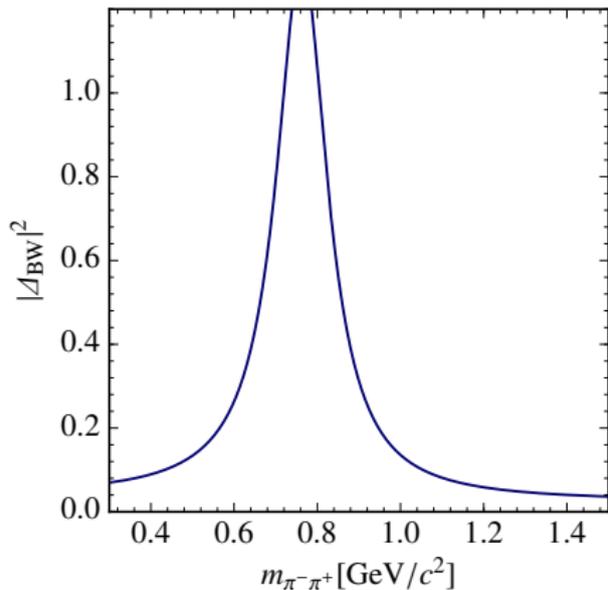
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# Zero mode in the spin-exotic wave

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$$\Delta_{\text{BW}}(m_{\pi^-\pi^+}) + \mathcal{C}\Omega(m_{\pi^-\pi^+})$$

$$\mathcal{C} = -0.05 + 0.15i$$



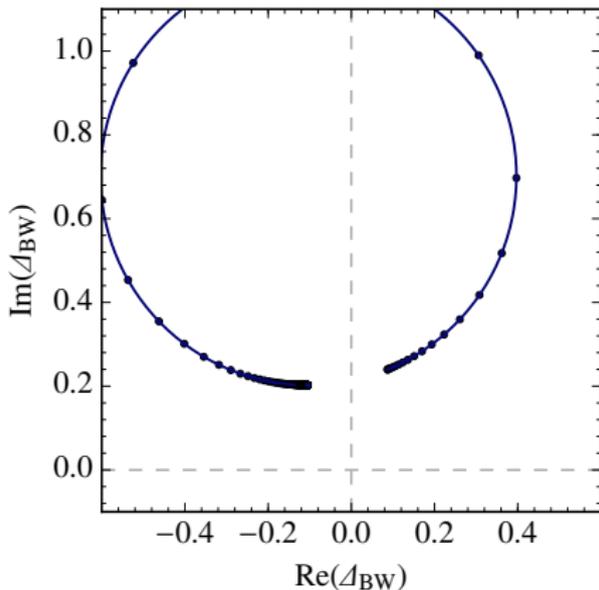
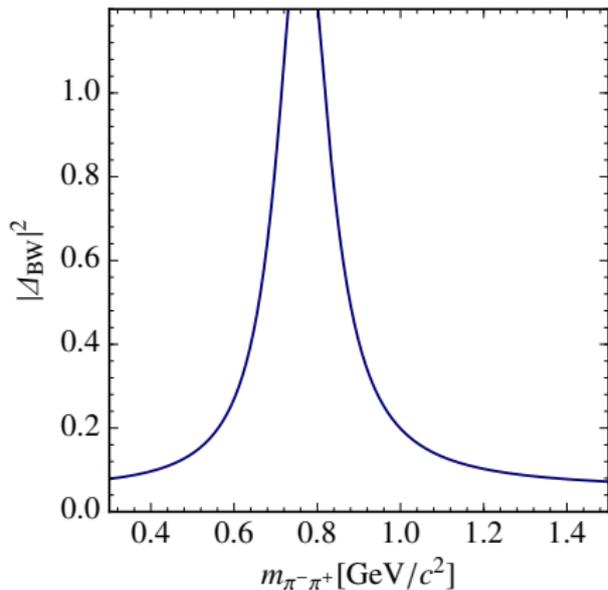
All describe the same  $3\pi$ -intensity

# Zero mode in the spin-exotic wave

Effects on dynamic isobar amplitudes

$$\Delta_{\text{BW}}(m_{\pi^-\pi^+}) + \mathcal{C}\Omega(m_{\pi^-\pi^+})$$

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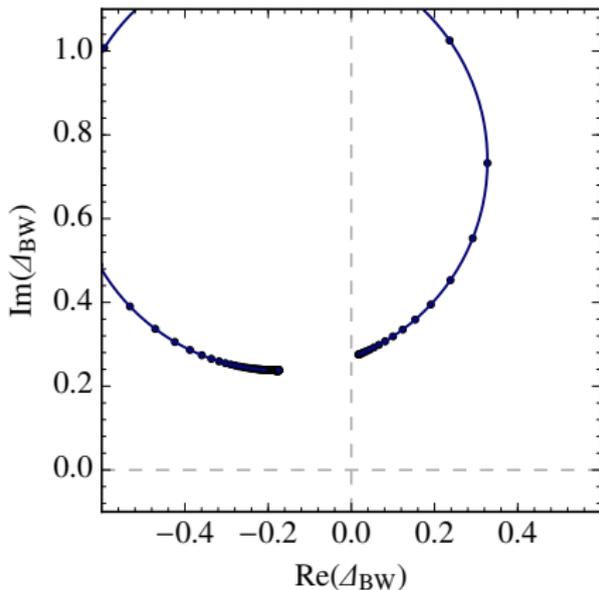
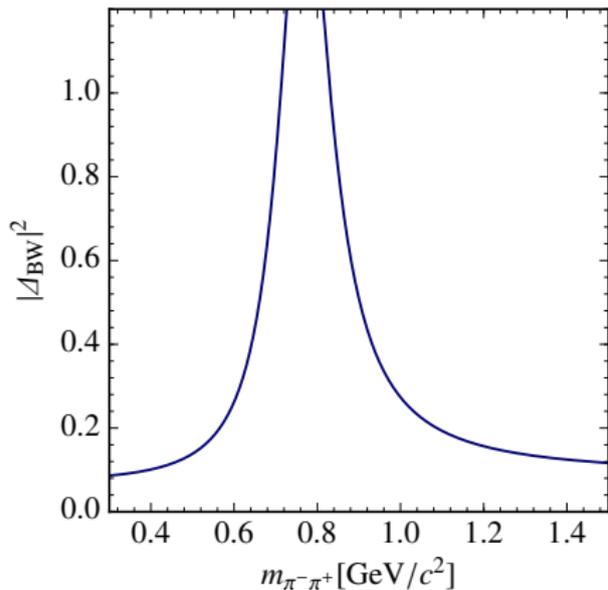
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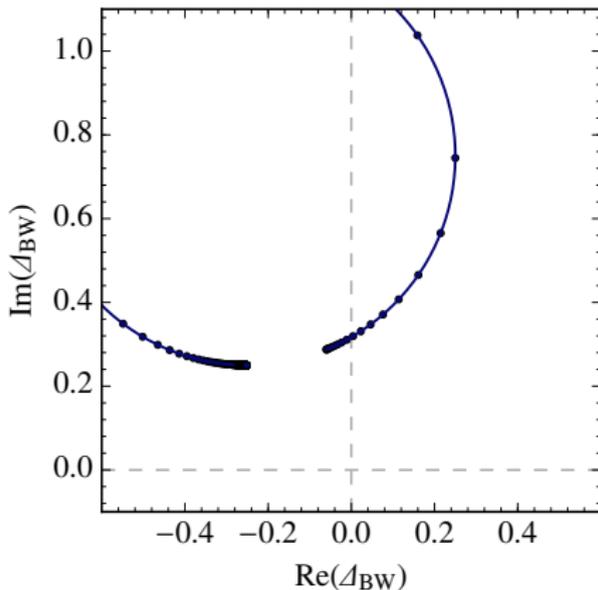
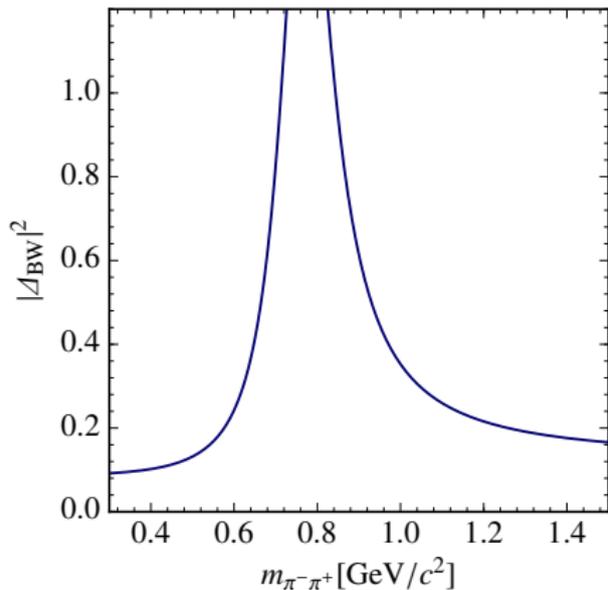
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# Zero mode in the spin-exotic wave

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$$\Delta_{\text{BW}}(m_{\pi^-\pi^+}) + \mathcal{C}\Omega(m_{\pi^-\pi^+})$$

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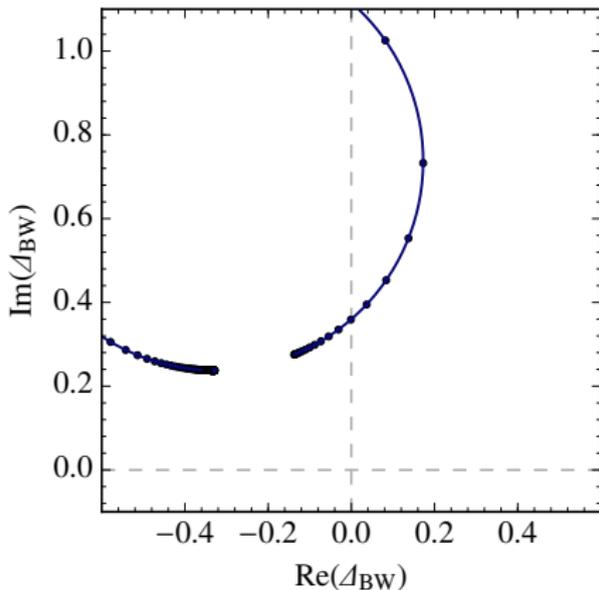
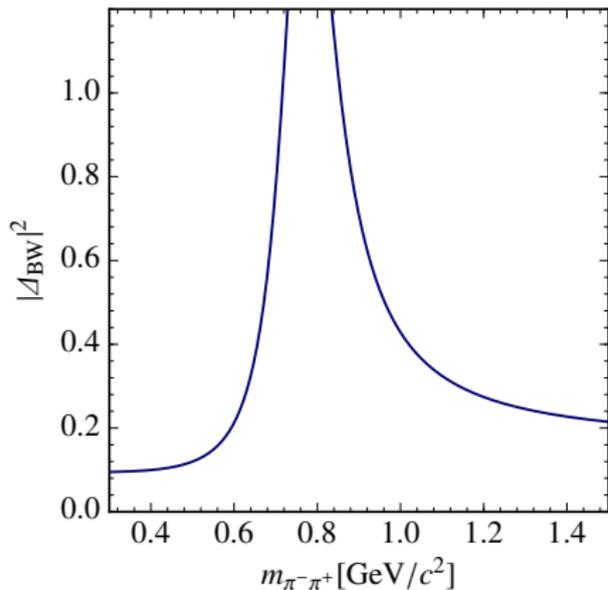
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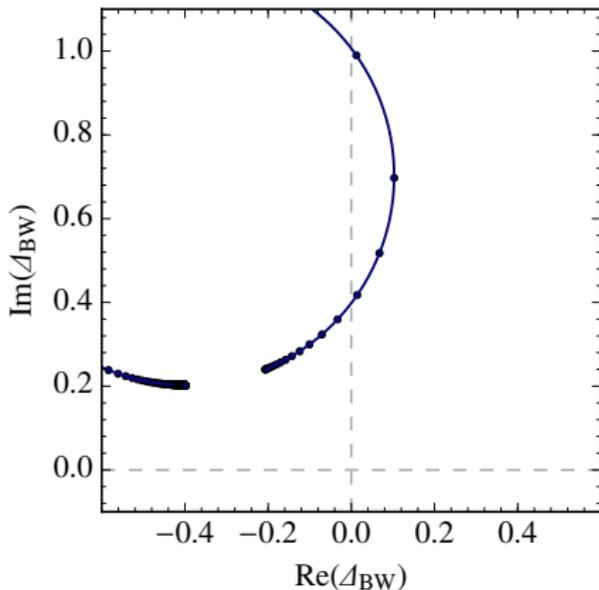
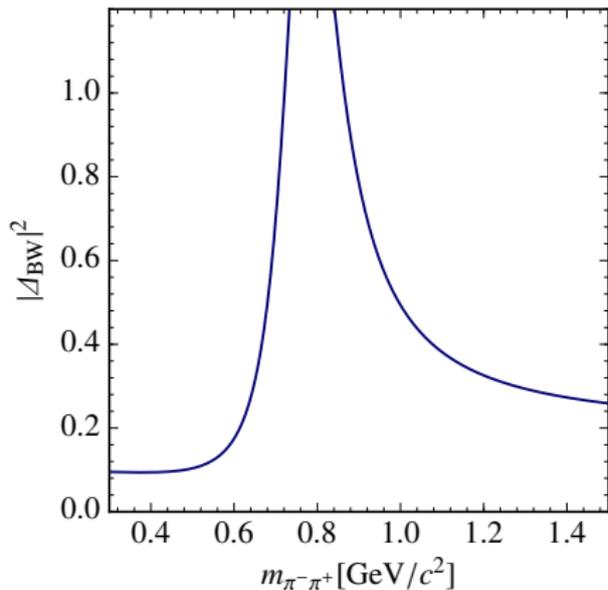
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Effects on dynamic isobar amplitudes

$$\Delta_{\text{BW}}(m_{\pi^-\pi^+}) + \mathcal{C}\Omega(m_{\pi^-\pi^+})$$

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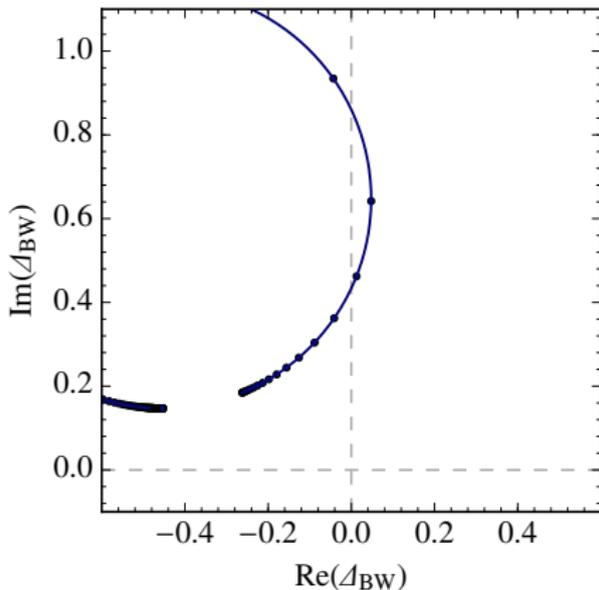
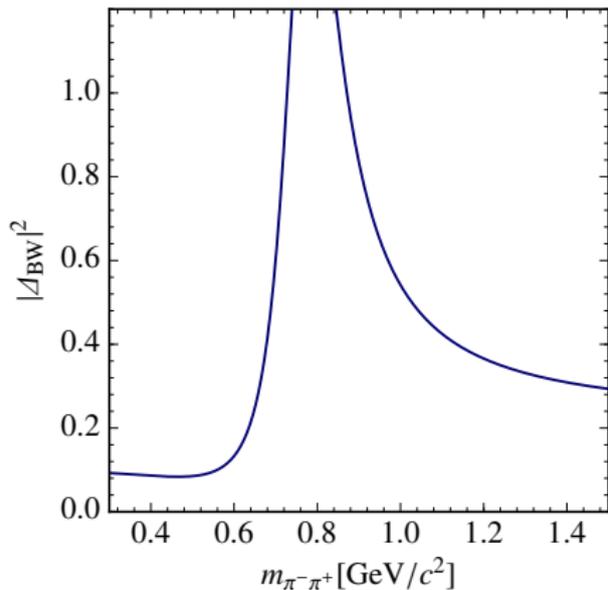
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$$\Delta_{\text{BW}}(m_{\pi^-\pi^+}) + \mathcal{C}\Omega(m_{\pi^-\pi^+})$$

$$\mathcal{C} = -0.45 + 0.15i$$



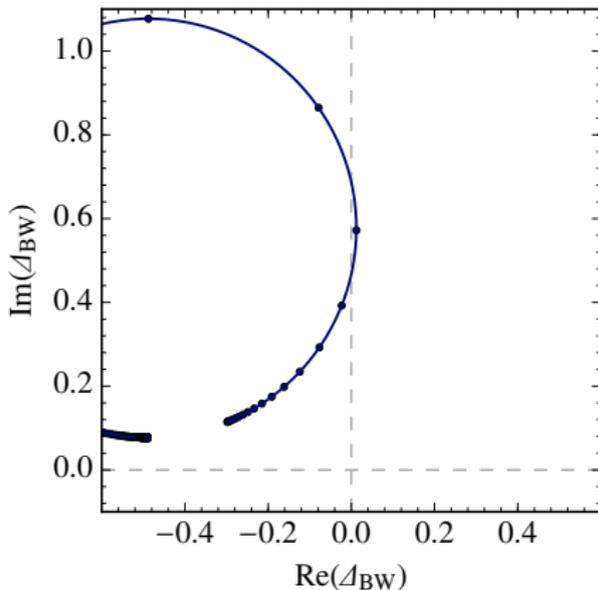
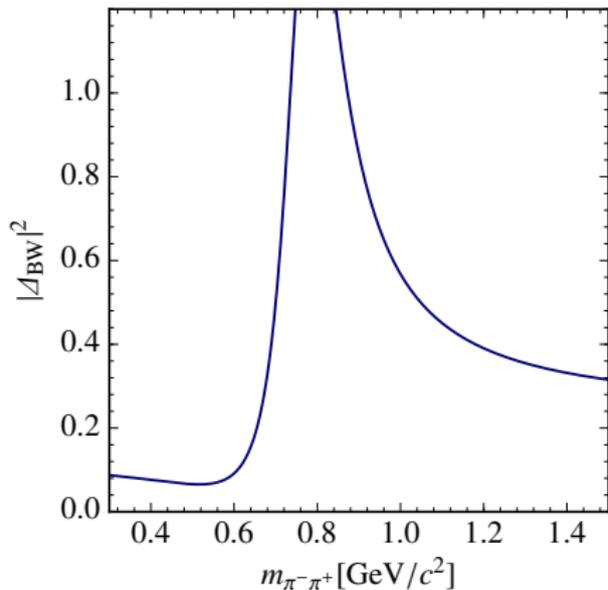
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$$\Delta_{\text{BW}}(m_{\pi^-\pi^+}) + \mathcal{C}\Omega(m_{\pi^-\pi^+})$$

$$\mathcal{C} = -0.49 + 0.08i$$



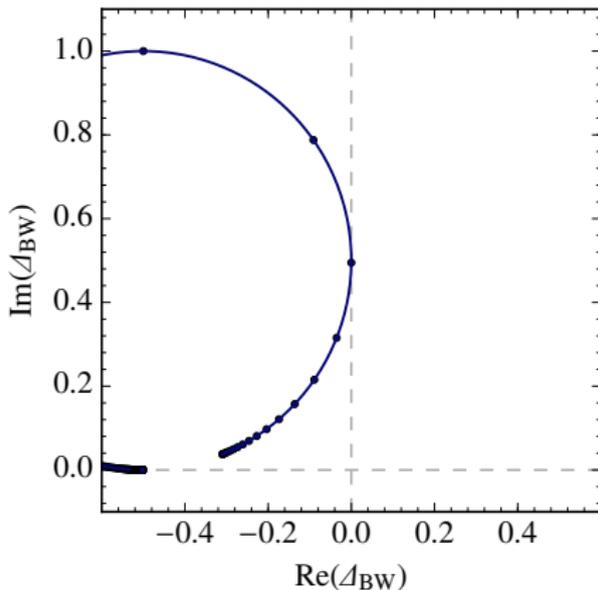
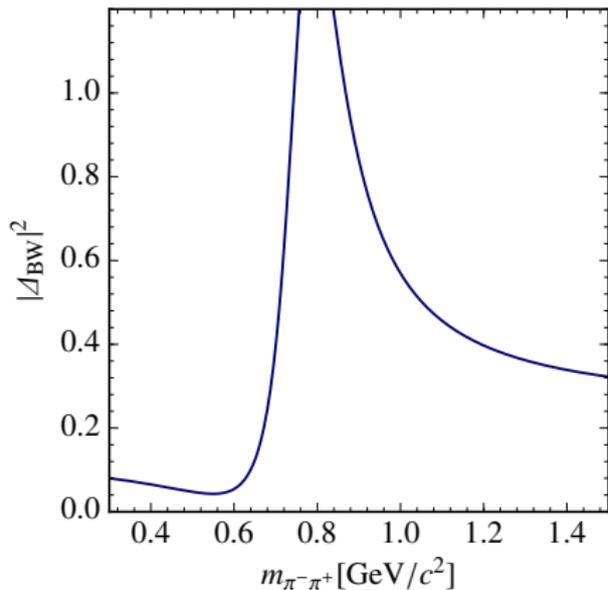
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$$\Delta_{\text{BW}}(m_{\pi^-\pi^+}) + \mathcal{C}\Omega(m_{\pi^-\pi^+})$$

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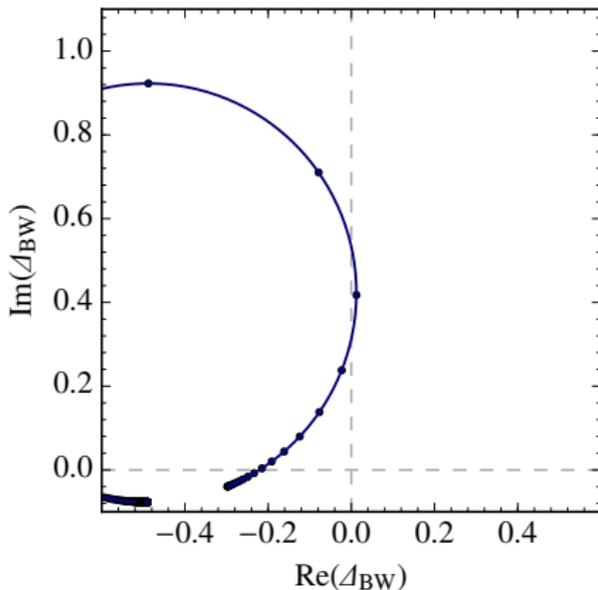
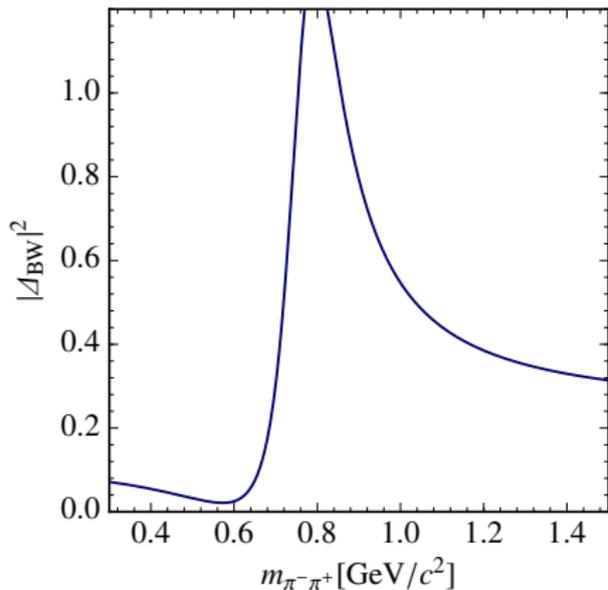
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$$\Delta_{\text{BW}}(m_{\pi^-\pi^+}) + \mathcal{C}\Omega(m_{\pi^-\pi^+})$$

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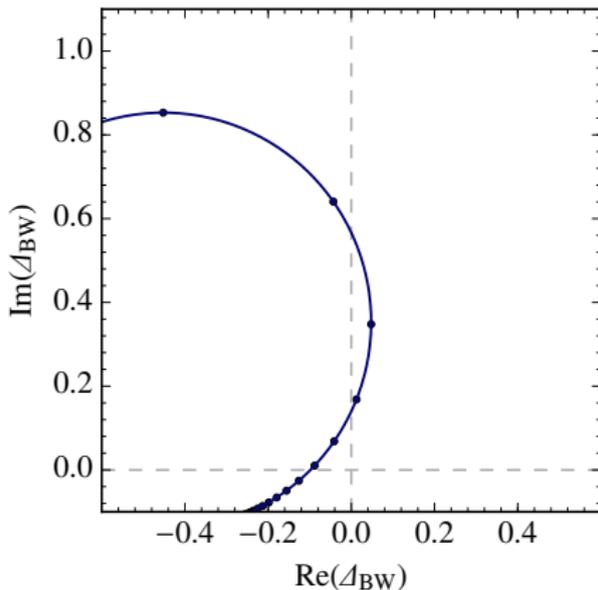
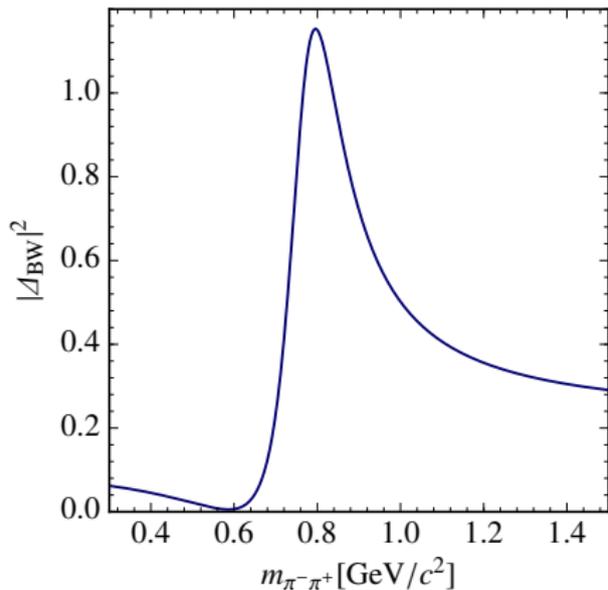
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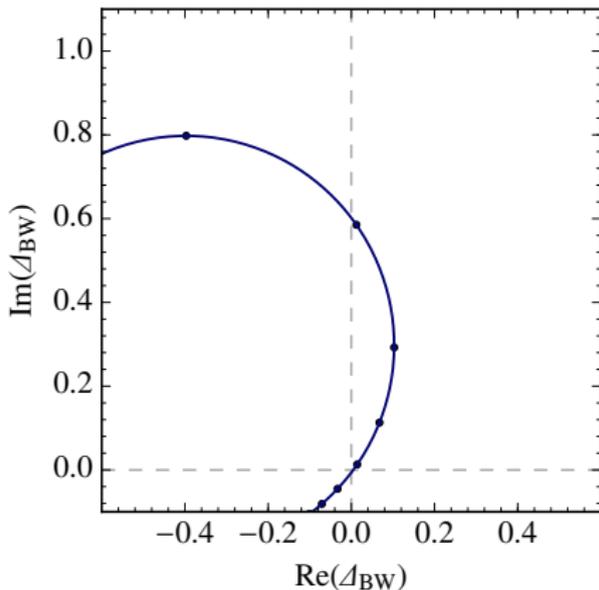
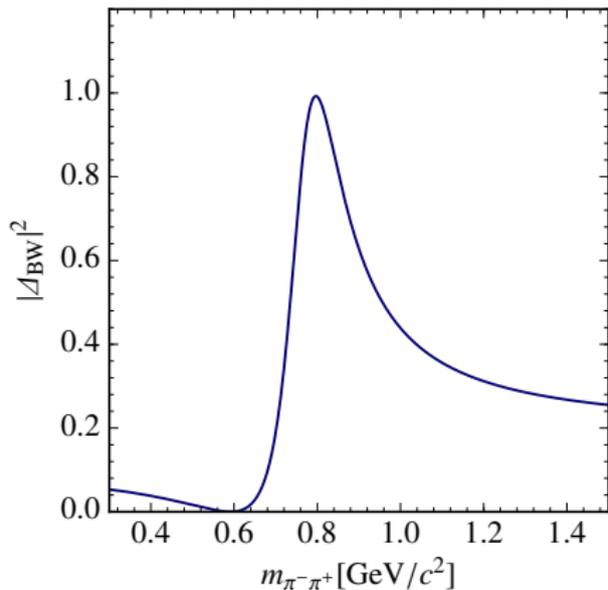
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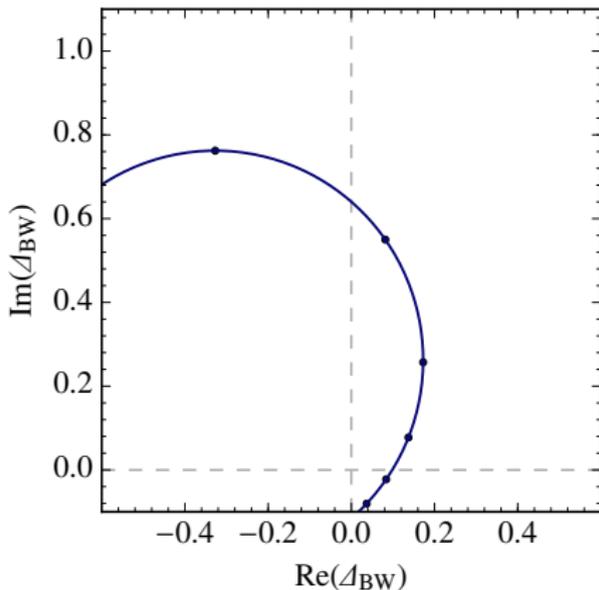
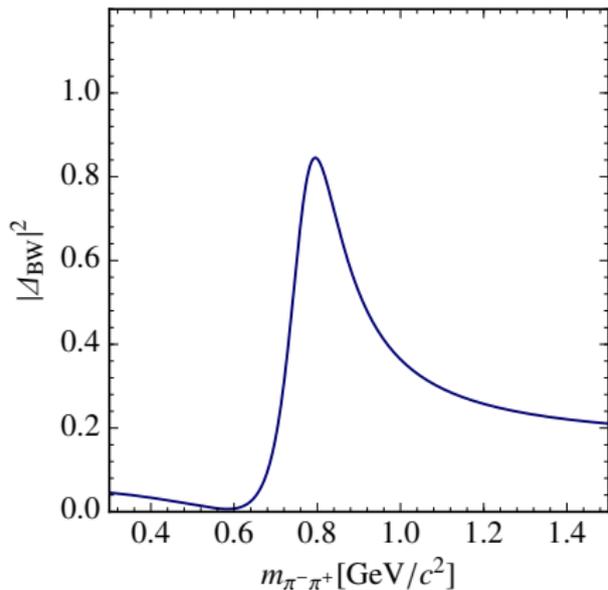
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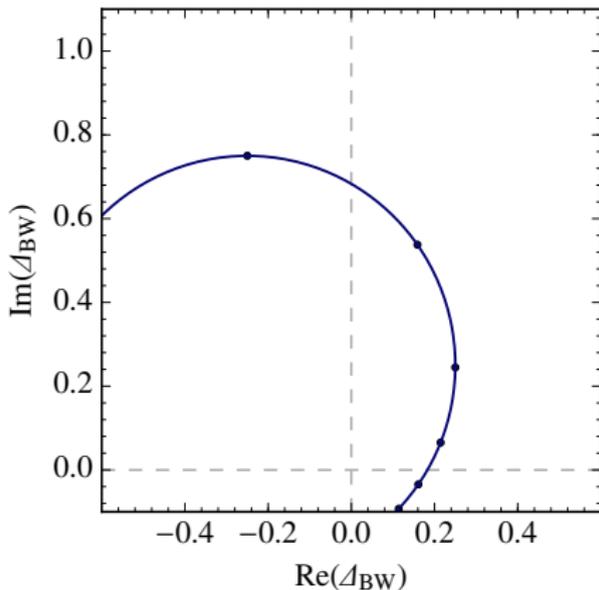
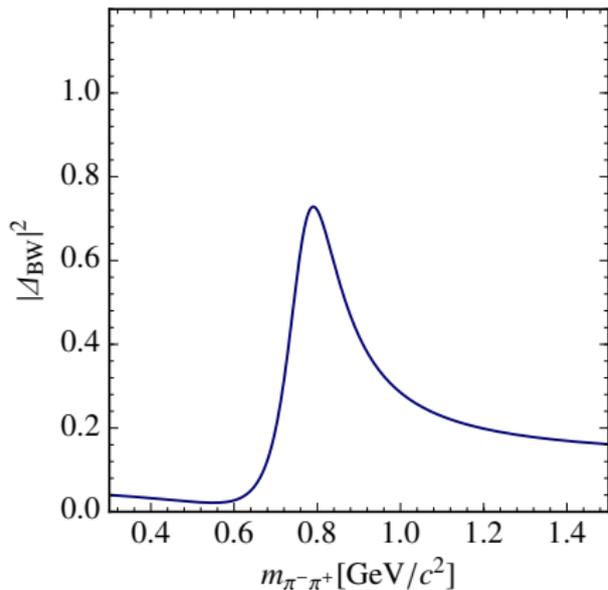
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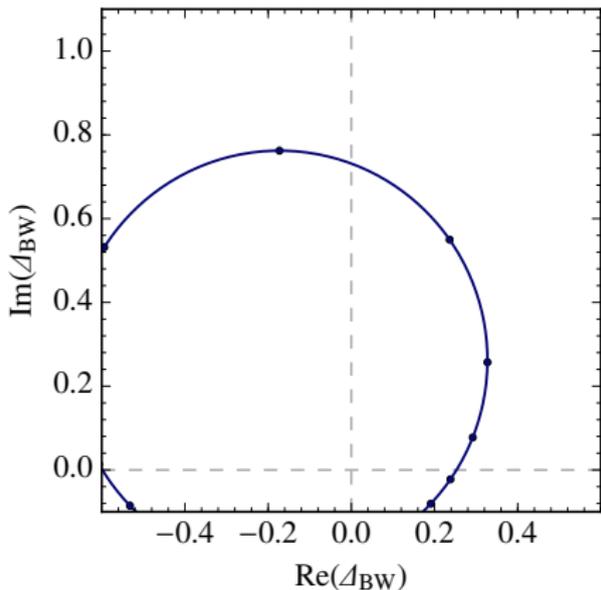
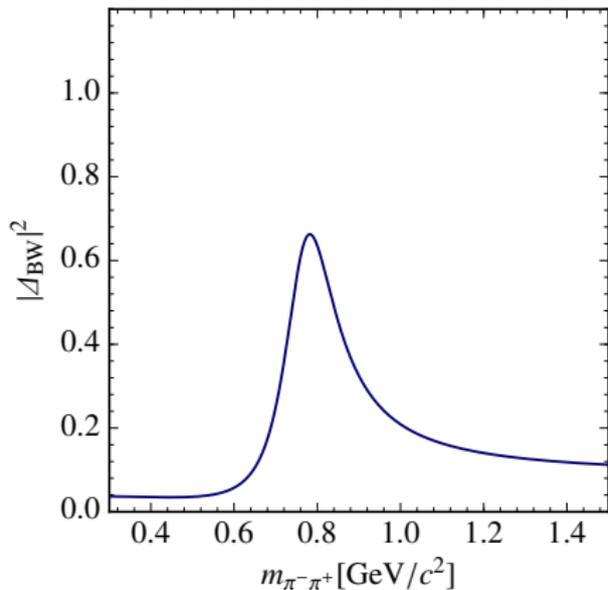
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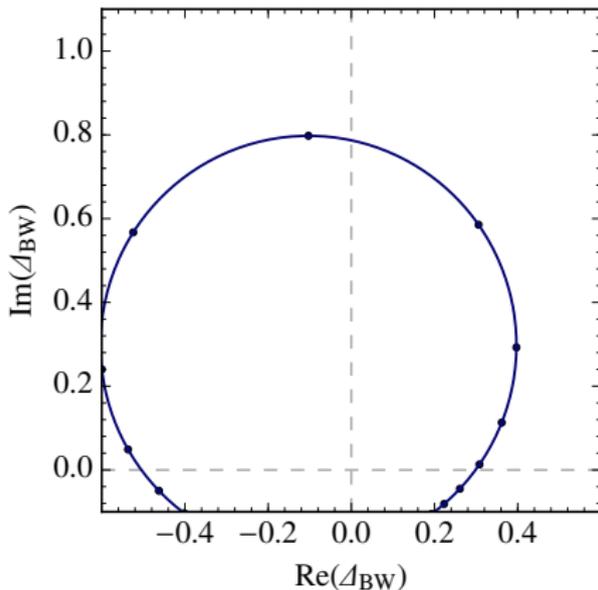
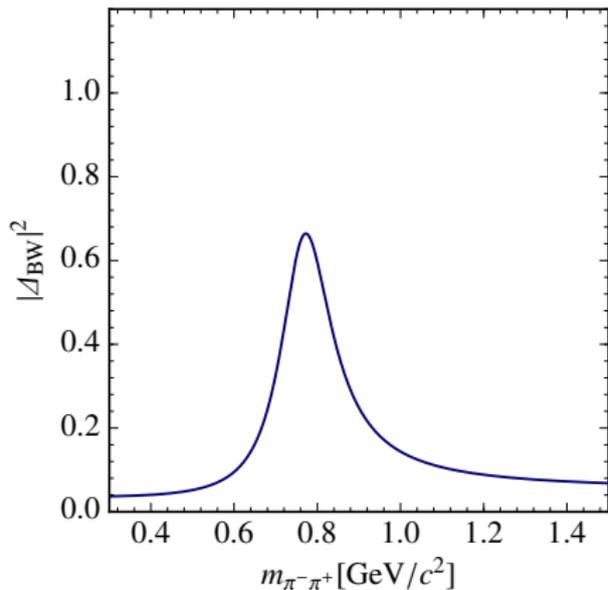
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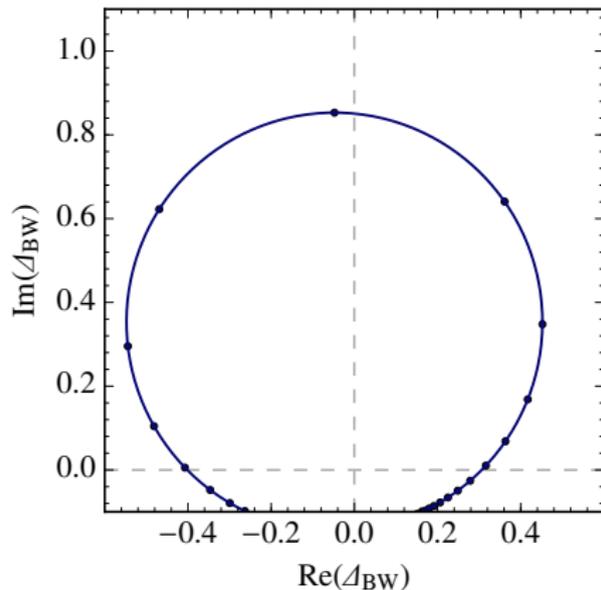
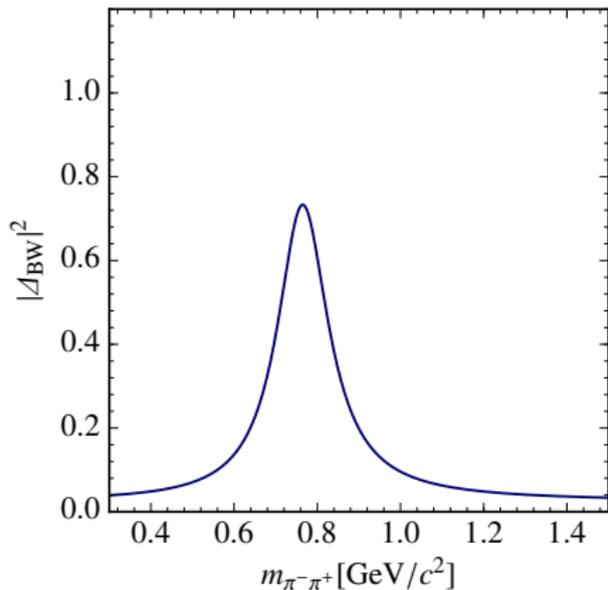
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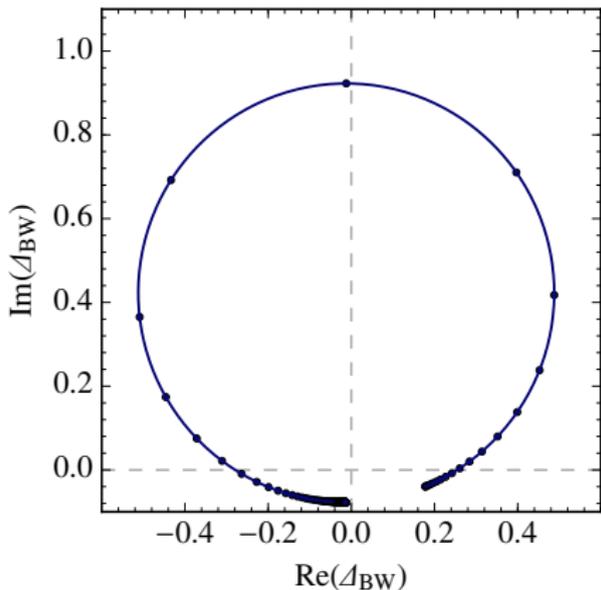
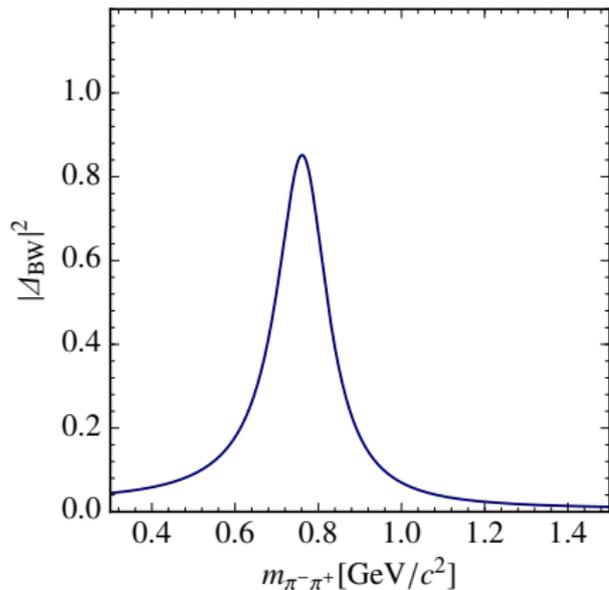
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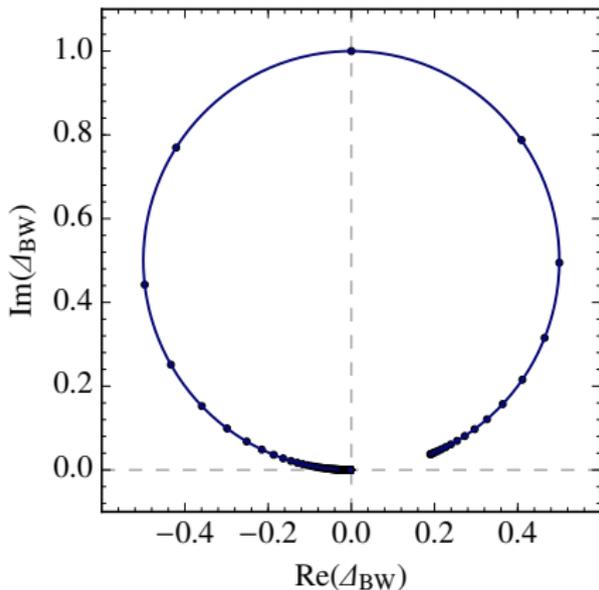
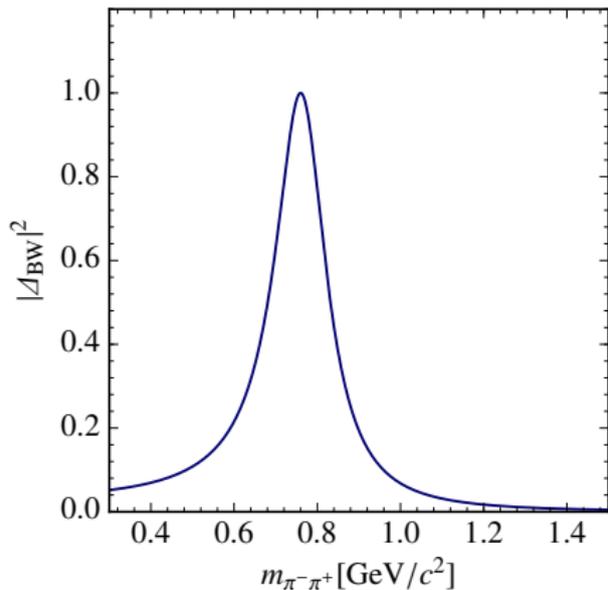
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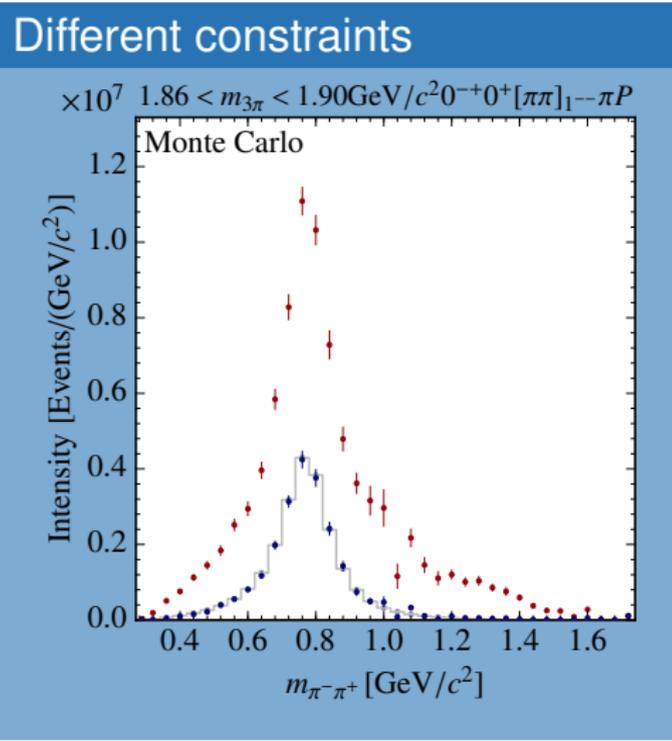
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 $n_{\text{bins}} - 1$  complex-valued d.o.f. remain free.

# Zero mode in the spin-exotic wave

Resolving the ambiguity

- Zero-mode cont
- Fitted solution p
- Find matching C
- In the case of th
  - ▶ use  $\rho(770)$  l
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- Final results: we
- **Note:** this fixes  $n_{\text{bins}} - 1$  c



l solution

# Zero mode in the spin-exotic wave

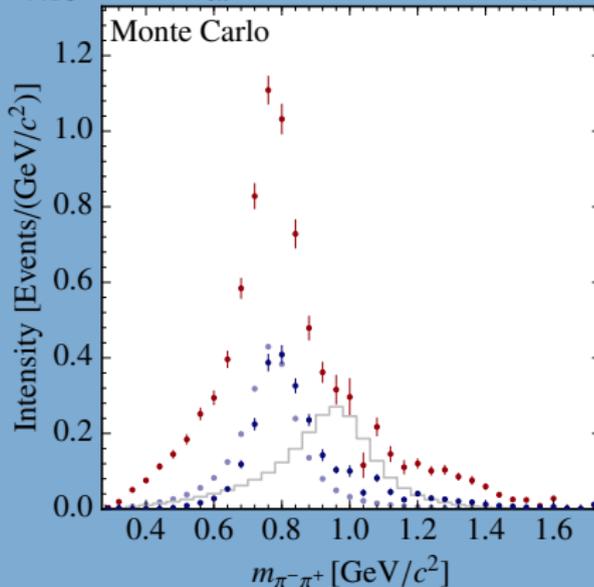
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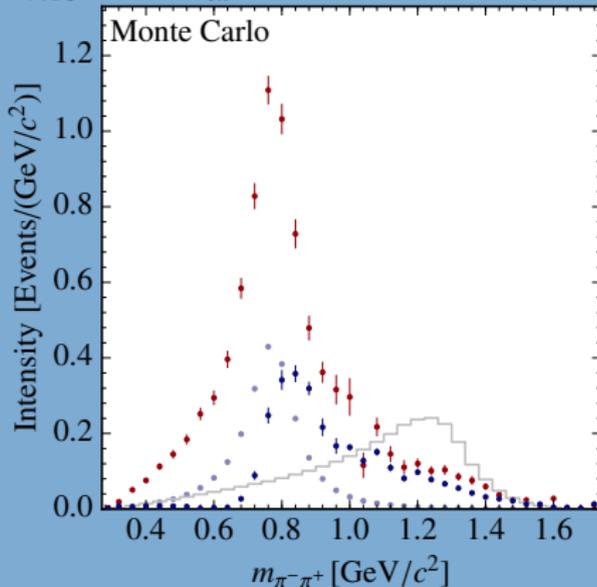
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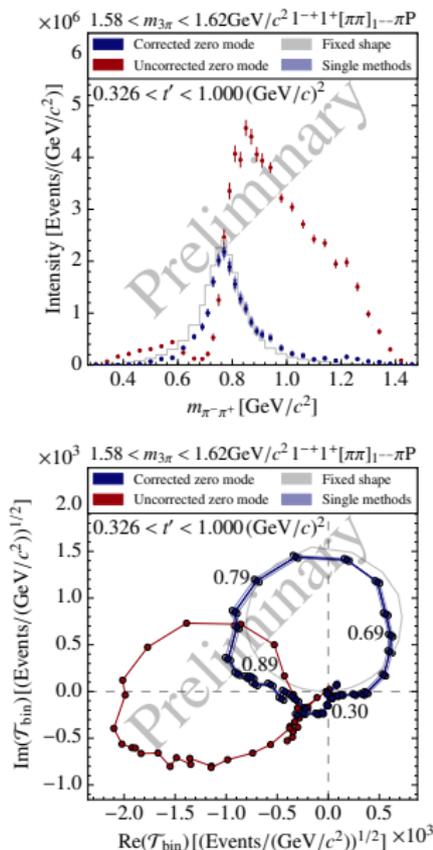
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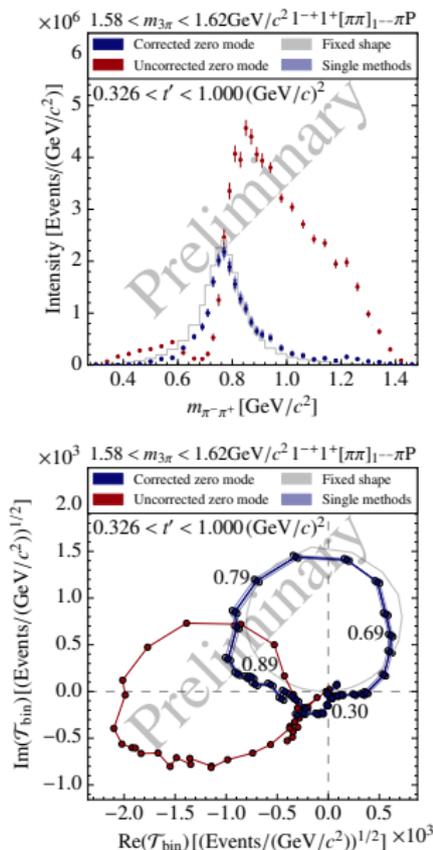
# The spin-exotic wave

- Example: One bin in  $(m_{3\pi}, t')$ 
  - ▶  $1.58 < m_{3\pi} < 1.62 \text{ GeV}/c^2$
  - ▶  $0.326 < t' < 1.000 \text{ (GeV}/c^2)^2$



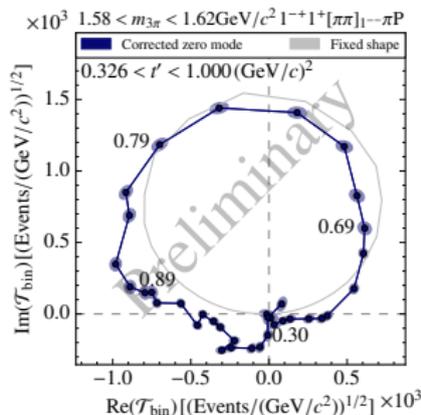
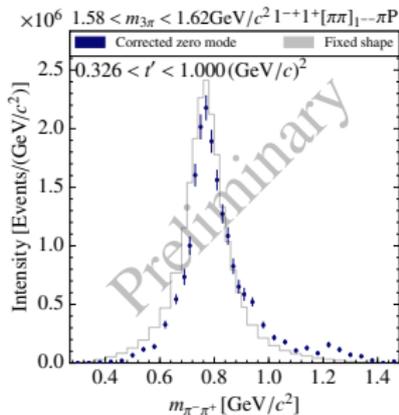
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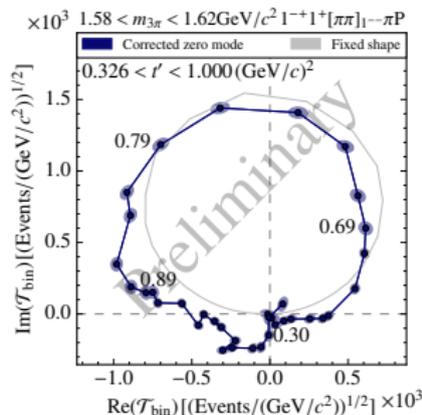
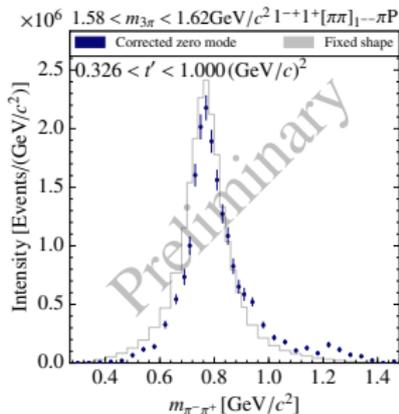
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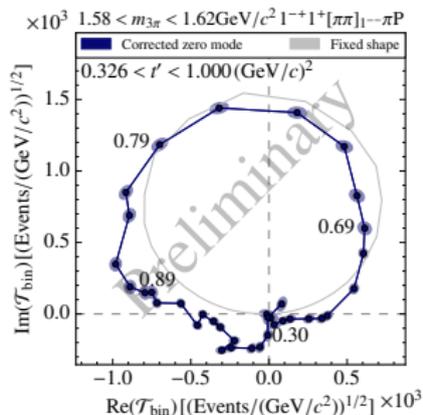
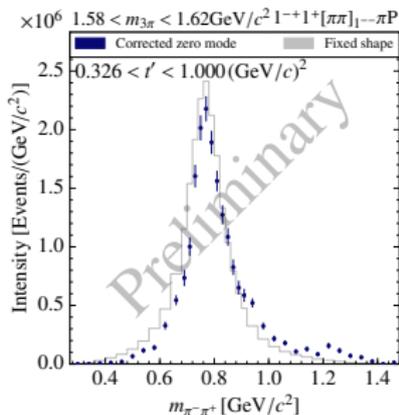
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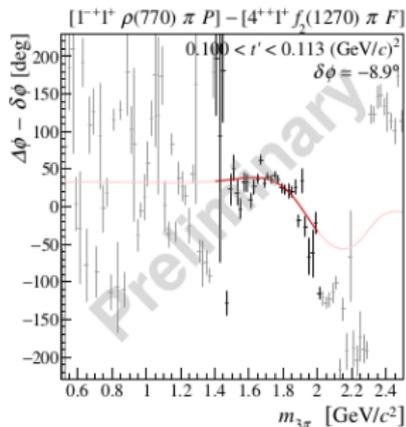
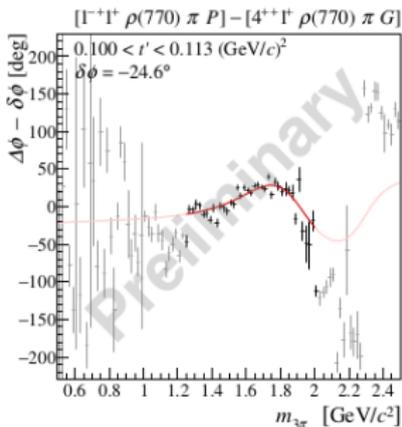
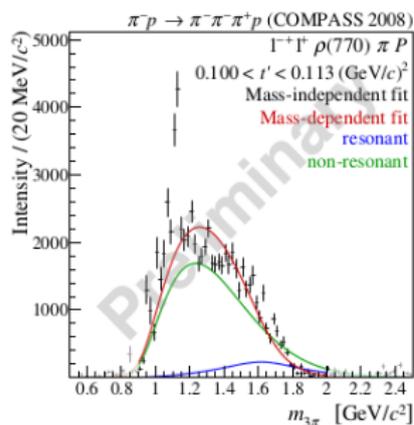


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- Zero-mode ambiguity resolved with  $\rho(770)$  used as constraint
- Dynamic isobar amplitude dominated by  $\rho(770)$
- Still significant deviations from a pure Breit-Wigner shape

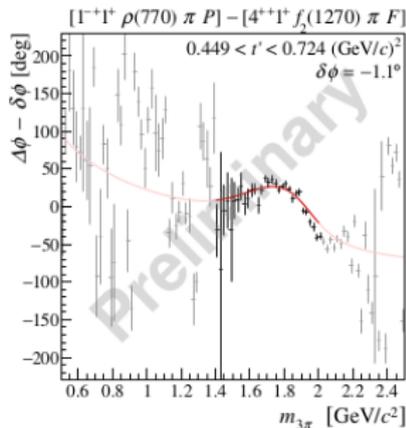
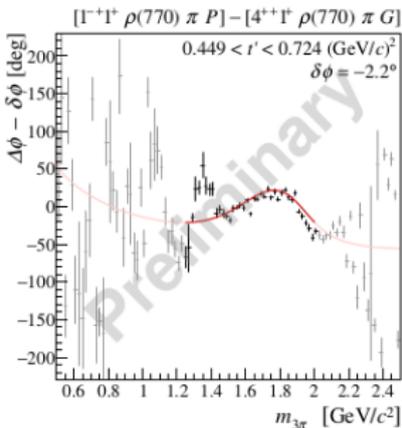
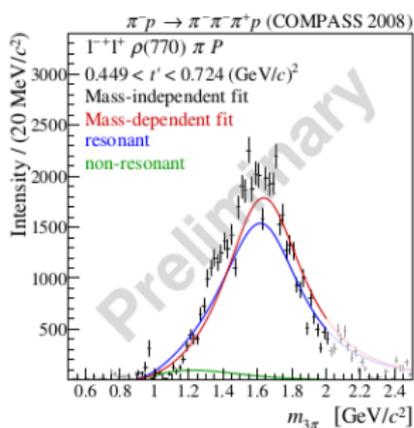


# The $1^{-+}1^{+}\rho(770)\pi P$ wave



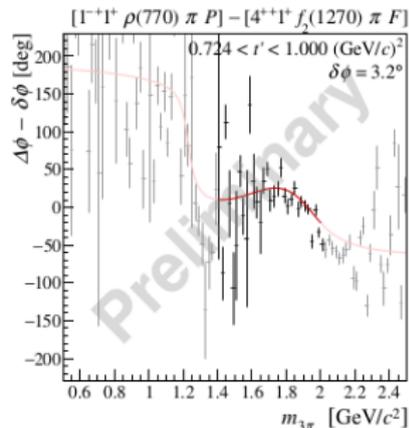
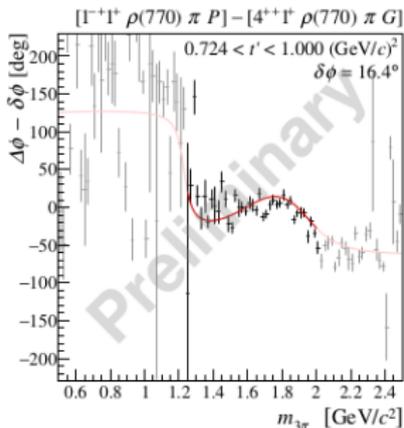
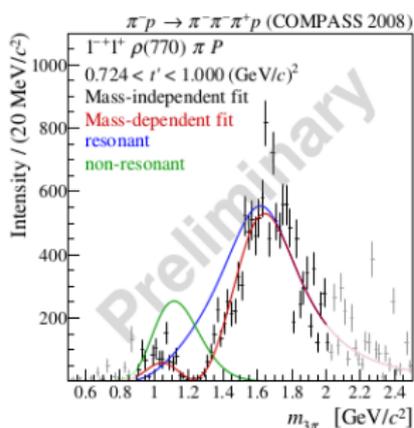
at low  $t'$  very weak resonant component

# The $1^{-+}1^{+}\rho(770)\pi P$ wave



at higher  $t'$  resonant component dominant

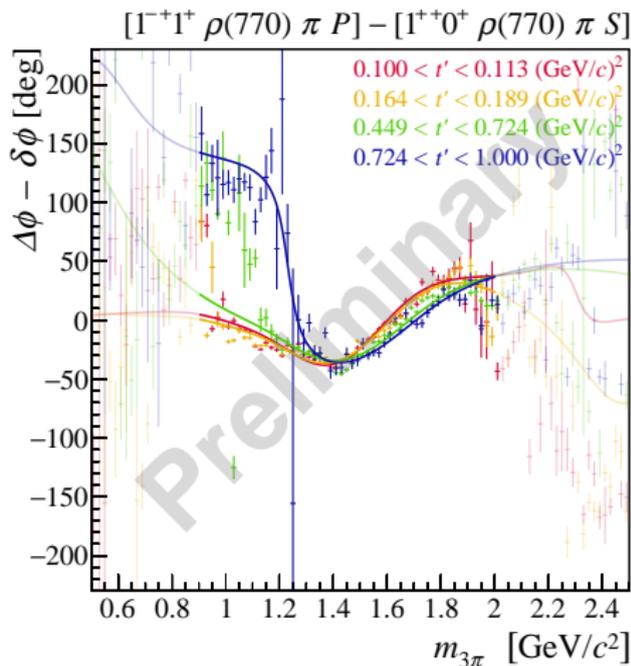
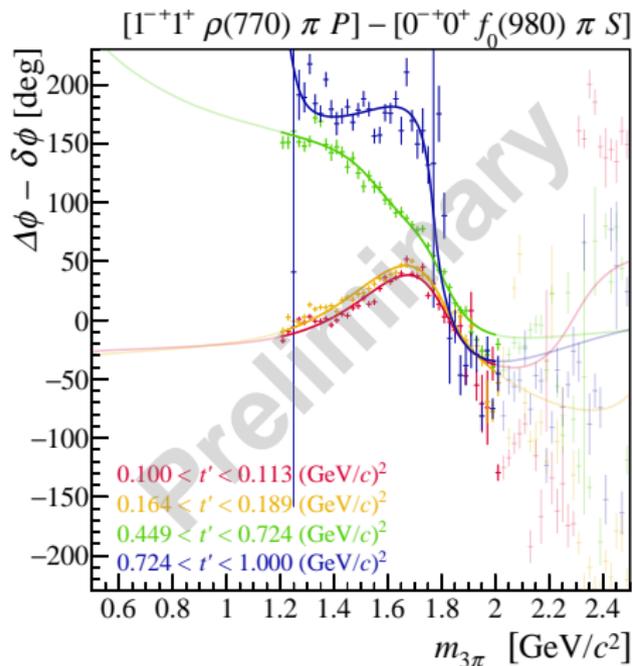
# The $1^{-+}1^{+}\rho(770)\pi P$ wave



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# The $1^{-+}1^{+}\rho(770)\pi P$ wave

Phase motion



resonance with mass  $\sim 1600 \text{ MeV}/c^2$  very broad  $\Gamma \sim 600 \text{ MeV}/c^2$

## COMPASS on exotic mesons:

- 46 million events for  $\pi^- p \rightarrow p \pi^- \pi^+ \pi^-$  analyzed
- partial-wave decomposition with 88 waves
- two exotic signals analyzed:
  - ▶  $a_1(1420)$  *supernumerous*
    - ★ matches a Breit-Wigner description with  $\Gamma = 158 \text{ MeV}/c^2$
    - ★ position at  $K^* \bar{K}$  threshold  $\rightarrow$  rescattering interpretation
    - ★ and/or Deck interference
  - ▶  $\pi_1(1600)$  *spin-exotic*
    - ★ at small  $t'$  dominant background
    - ★ slow phase motion
    - ★ much broader than previous analyses

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- lower statistics for incoming  $K^-$  beams  
 $\rightarrow$  dedicated future option: dedicated RF-separated beam

*Thank you for your attention!*

