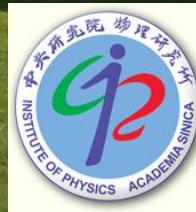


9<sup>th</sup> Workshop on Hadron physics in China and Opportunities Worldwide  
24-29 July 2017  
Nanjing University, Nanjing, China

# First transverse spin asymmetries measured in polarized Drell-Yan at COMPASS

Wen-Chen Chang 章文箴  
Institute of Physics, Academia Sinica

On behalf of COMPASS Collaboration

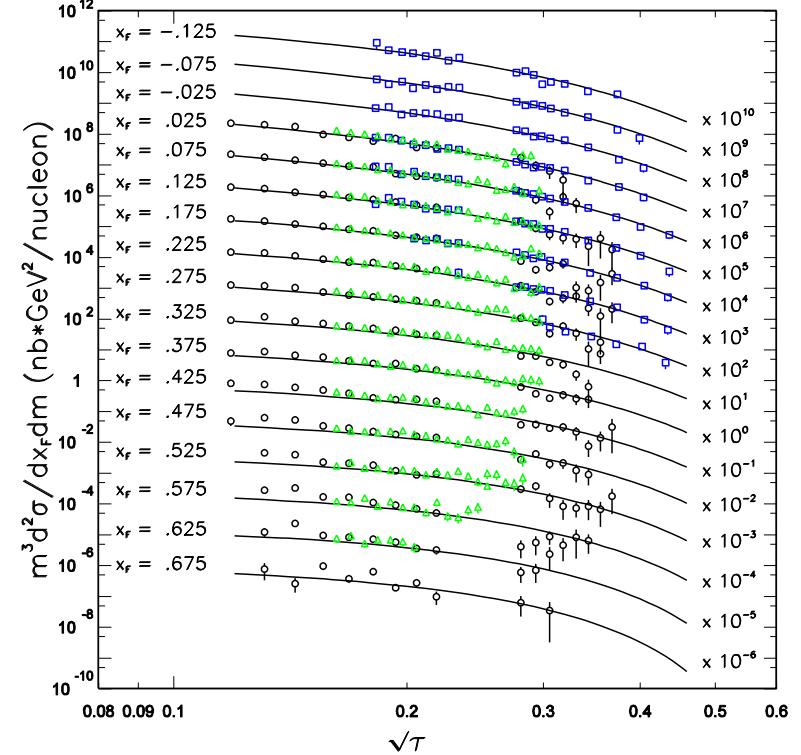
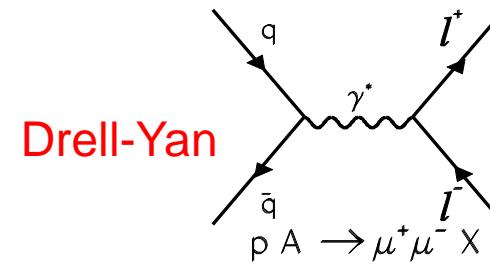
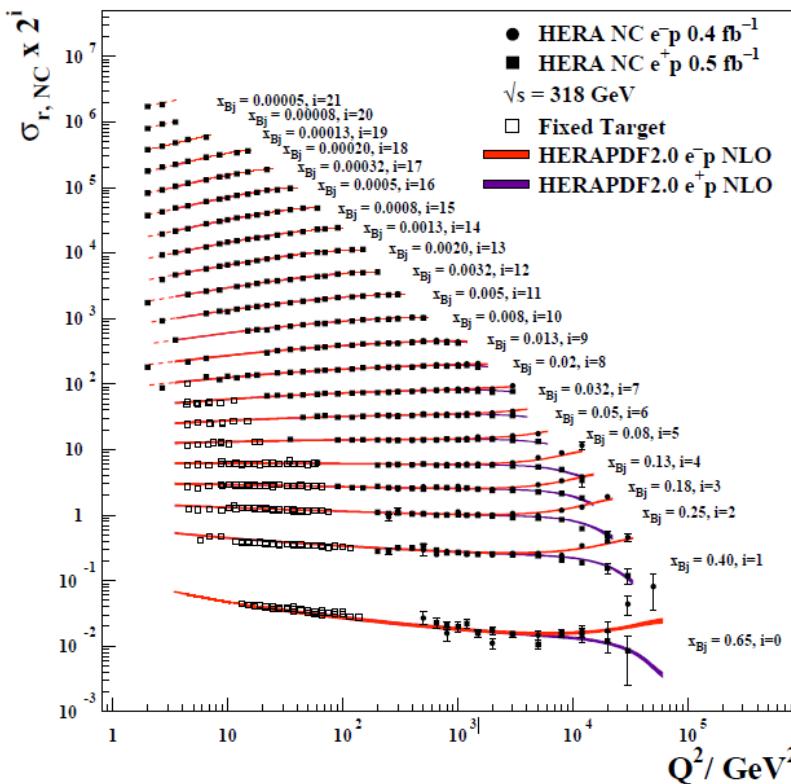
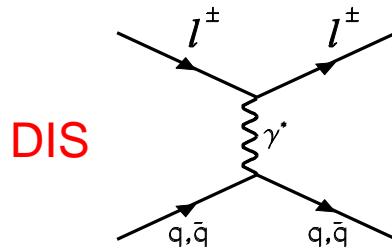




# Outline

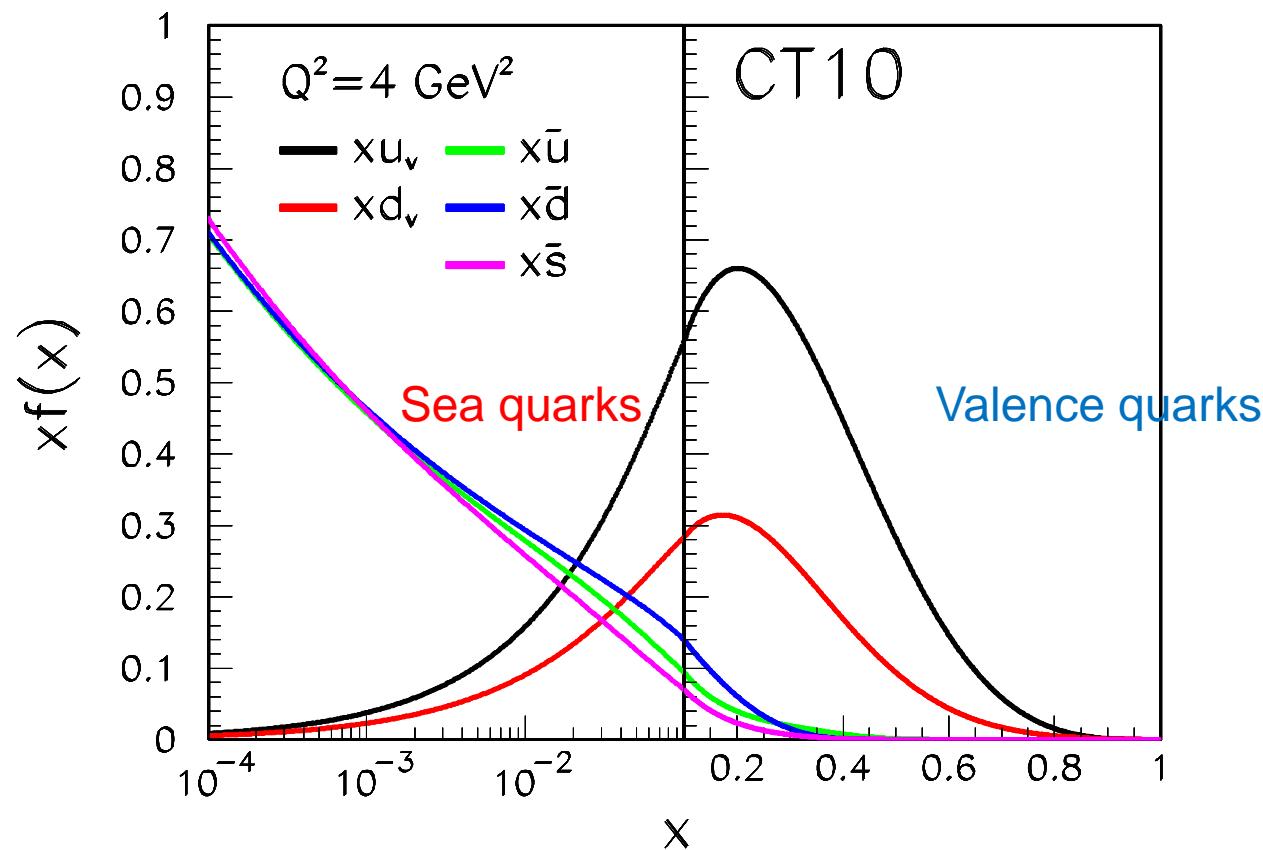
- Transverse momentum dependent distributions (TMDs) and transverse single-spin asymmetries (TSAs)
- Universality test of Sivers Functions: a predicted sign change between SIDIS and Drell-Yan processes
- First measurement of TSAs from the 2015 polarized Drell-Yan runs of COMPASS
- Summary

# Factorization of Hard Processes



$$\sigma_{proton}(x, Q^2) = f_{parton}(x, Q^2) \otimes \hat{\sigma}_{parton}(Q^2)$$

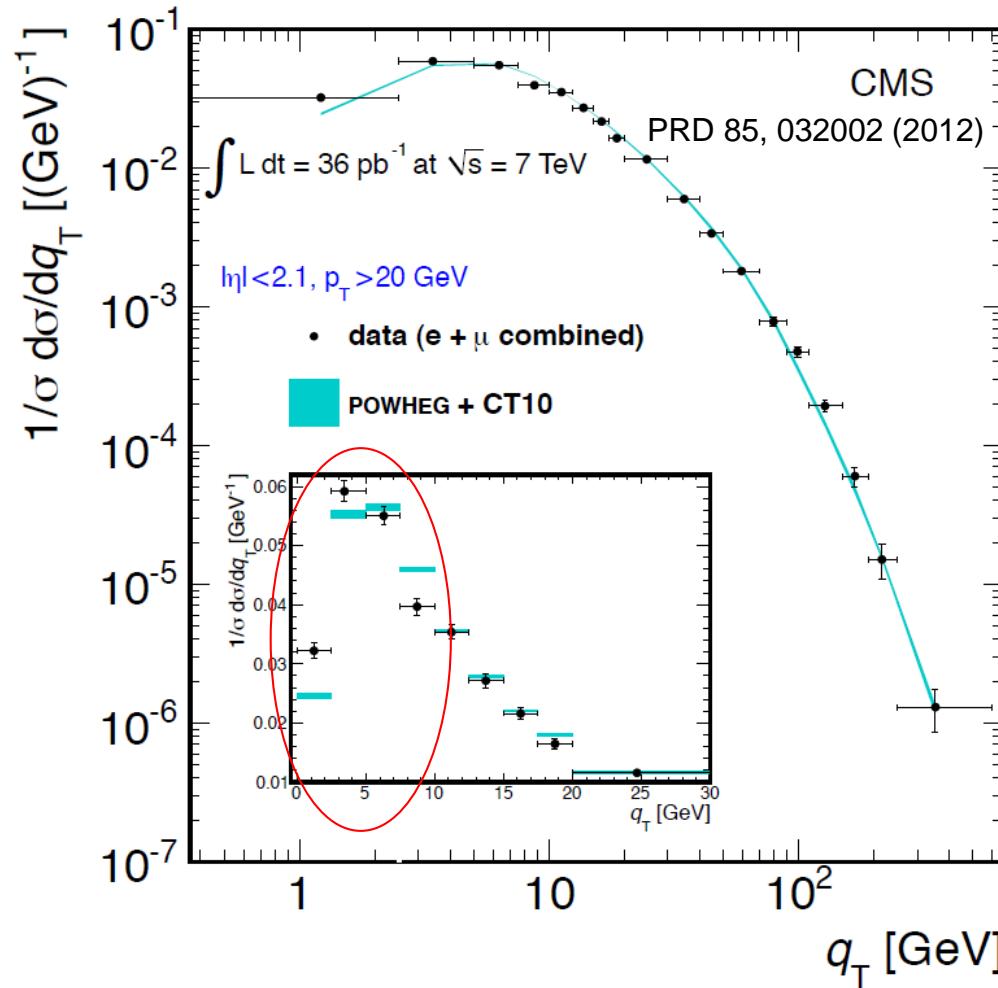
# Universality of Parton Density Functions (PDFs)



$x$ : momentum fraction of partons

# Why TMDs?

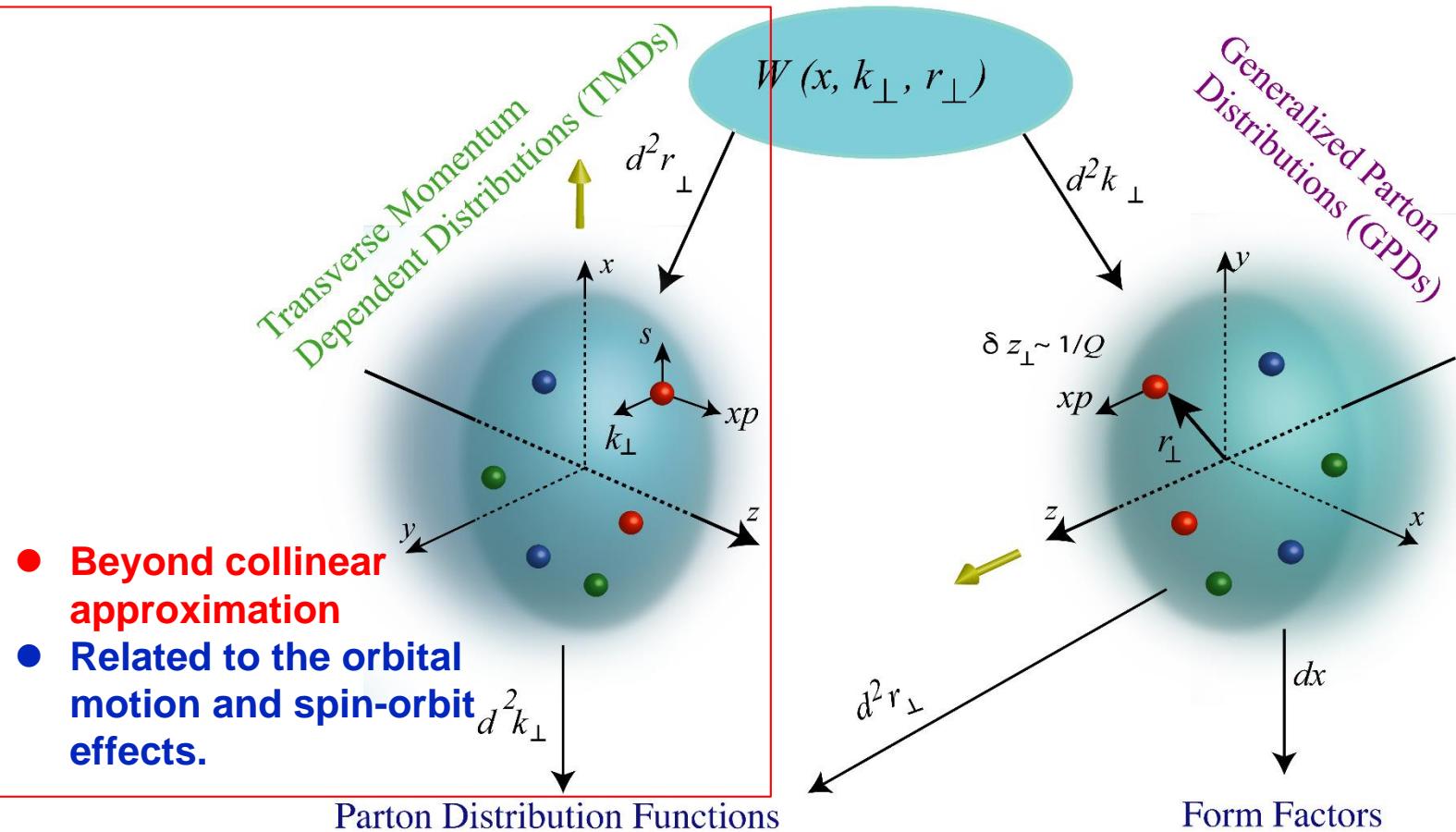
The Z-boson transverse momentum  $q_T$  spectrum in pp collisions at the LHC



- At large  $q_T$ , the NNLO pQCD describes the data better than 10%.
- For  $q_T < 10 \text{ GeV}$ , pQCD calculation fails: multi-parton QCD radiation.

# Multi-dimensional Partonic Structures

## Wigner Distributions



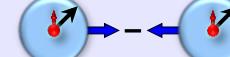
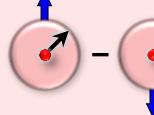
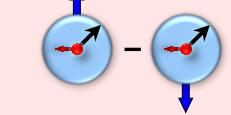
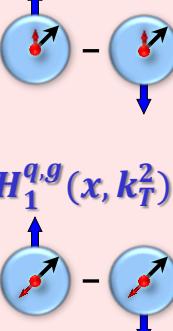


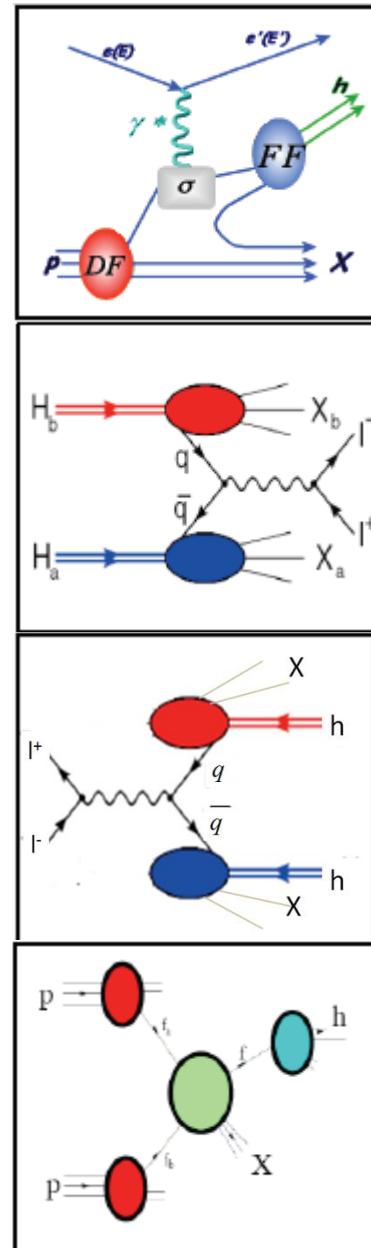
# Leading-Twist Transverse-momentum Dependent Parton Density Function (TMDs)

| Quark, Gluon |  | U   | L                                  | T   |
|--------------|--|---|------------------------------------|---|
| Nucleon      | U  | number density $f_1^{q,g}(x, k_T^2)$                            | Helicity $g_{1L}^{q,g}(x, k_T^2)$  | Boer-Mulders $h_1^{\perp q,g}(x, k_T^2)$    |
| L            | worm-gear L $h_{1L}^{\perp q,g}(x, k_T^2)$ | worm-gear T $g_{1T}^{\perp q,g}(x, k_T^2)$                      | Transversity $h_1^{q,g}(x, k_T^2)$ | Pretzelosity $h_{1T}^{\perp q,g}(x, k_T^2)$ |
| T            | Sivers $f_{1T}^{\perp q,g}(x, k_T^2)$      | Kotzinian-Mulders<br>worm-gear T $g_{1T}^{\perp q,g}(x, k_T^2)$ |                                    |   |

- spin of the nucleon
- spin of the parton
- $k_T$  of the parton

# Leading-Twist Transverse-momentum Dependent Fragmentation Function (TMDs)

|                     |                    | Quark, Gluon | U   | L   | T  |
|---------------------|--------------------|--------------|---|---|--|
|                     |                    | Nucleon      |   |   |  |
|                     |                    | U            |    |   |   |
| spin of the nucleon | spin of the parton | U            | <b>unpolarized</b><br>$D_1^{q,g}(x, k_T^2)$   |   | <b>Collins</b><br>$H_1^{\perp q,g}(x, k_T^2)$  |
|                     |                    | L            |   |    |   |
| $k_T$ of the parton |                    |              |   | $G_{1L}^{q,g}(x, k_T^2)$  | $H_{1L}^{\perp q,g}(x, k_T^2)$   |
|                     |                    | T            |  |  |  |
|                     |                    |              | $D_{1T}^{\perp q,g}(x, k_T^2)$  | $G_{1T}^{\perp q,g}(x, k_T^2)$  | $H_{1T}^{\perp q,g}(x, k_T^2)$   |



# Accessing TMDs

SIDIS:  $ep \rightarrow ehX$

$$\sigma^{ep \rightarrow ehX} = \sum_q (DF) \otimes (\sigma^{eq \rightarrow eq}) \otimes (FF)$$



Drell-Yan:  $pp \rightarrow e^+e^-X$

$$\sigma^{pp \rightarrow eeX} = \sum_q (DF) \otimes (DF) \otimes (\sigma^{qq \rightarrow ee})$$



Dihadron in  $e^+e^-$ :  $e^+e^- \rightarrow h_1 h_2 X$

$$\sigma^{ee \rightarrow hhX} = \sum_q (\sigma^{qq \rightarrow ee}) \otimes (FF) \otimes (FF)$$

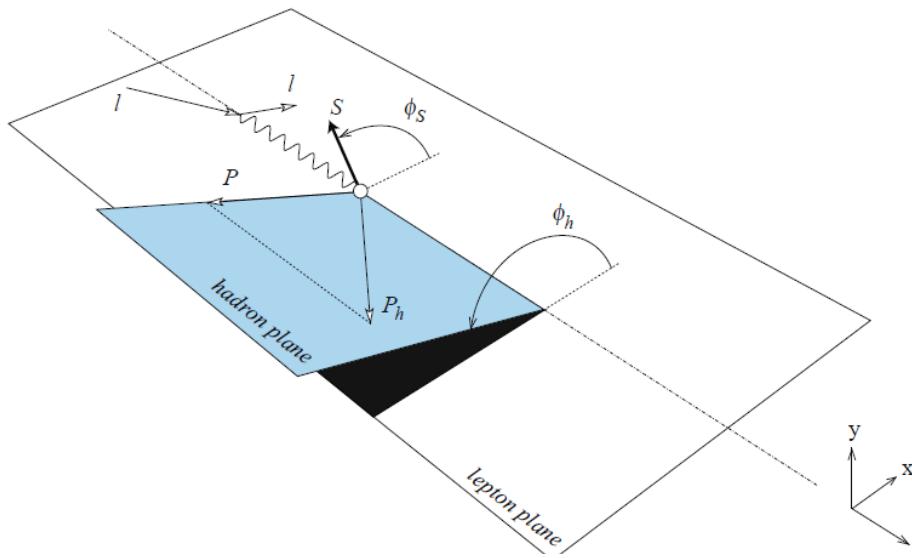


Hadron production in  $pp$ :  $pp \rightarrow hX$

$$\sigma^{pp \rightarrow hX} = \sum_q (DF) \otimes (DF) \otimes (\sigma^{qq \rightarrow qq}) \otimes (FF)$$



# SIDIS cross-sections



$F_{UU}^{\cos(2\phi)}, F_{UT}^{\sin(\phi-\phi_S)}, F_{UT}^{\sin(\phi+\phi_S)}$  :  
Structure Functions

$$\begin{aligned}
 \sigma(\phi, \phi_S) \equiv & \frac{d^6\sigma}{dx dy dz d\phi d\phi_S dP_{hT}^2} = \\
 & \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi F_{UU}^{\cos \phi} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} \right. \\
 & + \textcircled{S_L} \left[ \sqrt{2\epsilon(1+\epsilon)} \sin \phi F_{UL}^{\sin \phi} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right] + S_L \lambda_e \left[ \sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos \phi F_{LL}^{\cos \phi} \right] \\
 & + \textcircled{|S_T|} \left[ \sin(\phi - \phi_S) \left( F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \right. \\
 & + \sqrt{2\epsilon(1+\epsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \left. \right] \\
 & + \textcircled{|S_T|} \lambda_e \left[ \sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} + \sqrt{2\epsilon(1-\epsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right] \}, \quad 10
 \end{aligned}$$



# Polarization-dependent Terms: Transverse Spin Asymmetry $A_{UT}$

$$A_{UT} = \frac{F_{UT}}{F_{UU}} = \frac{1}{fS_T} \frac{N^{\uparrow} - N^{\downarrow}}{N^{\uparrow} + N^{\downarrow}}$$

$f$ : dilution factor due to non-polarizable component of the target

$S_T$ : polarization degree of transverse spin

- **Advantage:** most of the systematics due to instrumental artifacts cancel.
- **Disadvantage:** the unpolarized structure function  $F_{UU}$  has to be well known.



# SIDIS and single-polarized DY x-sections at twist-2 (LO)

$$\frac{d\sigma^{LO}}{dxdydzdp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L})$$

$$\times \left\{ \begin{array}{l} 1 + \boxed{\varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h} \\ + S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} \\ \times \left[ \begin{array}{l} A_{UT}^{\sin(\phi_h - \phi_s)} \sin(\phi_h - \phi_s) \\ + \varepsilon A_{UT}^{\sin(\phi_h + \phi_s)} \sin(\phi_h + \phi_s) \\ + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_s)} \sin(3\phi_h - \phi_s) \end{array} \right] \\ + S_T \lambda \left[ \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_s)} \cos(\phi_h - \phi_s) \right] \end{array} \right\}$$

**SIDIS**  $\frac{d\sigma^{LO}}{d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS})$

**DY**

$$\left\{ \begin{array}{l} 1 + \boxed{D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\phi_{CS}} \cos 2\phi_{CS}} \\ + S_L \sin^2 \theta_{CS} A_L^{\sin 2\phi_{CS}} \sin 2\phi_{CS} \\ \times \left[ \begin{array}{l} A_T^{\sin \phi_s} \sin \phi_s \\ + D_{[\sin^2 \theta_{CS}]} \left( A_T^{\sin(2\phi_{CS} - \phi_s)} \sin(2\phi_{CS} - \phi_s) \right. \\ \left. + A_T^{\sin(2\phi_{CS} + \phi_s)} \sin(2\phi_{CS} + \phi_s) \right) \end{array} \right] \end{array} \right\}$$

where  $D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$

$$A_{UU}^{\cos 2\phi_h} \propto h_1^{\perp q} \otimes H_{1q}^{\perp h} + \dots$$

Boer-Mulders

$$A_U^{\cos 2\phi_{CS}} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^{\perp q}$$

$$A_{UT}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

Sivers

$$A_T^{\sin \phi_s} \propto f_{1,\pi}^q \otimes f_{1T,p}^{\perp q}$$

$$A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$$

Transversity

$$A_T^{\sin(2\phi_{CS} - \phi_s)} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^q$$

$$A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

Pretzelosity

$$A_T^{\sin(2\phi_{CS} + \phi_s)} \propto h_{1,\pi}^{\perp q} \otimes h_{1T,p}^{\perp q}$$

$$A_{UL}^{\sin 2\phi_h} \propto h_{1L}^{\perp q} \otimes H_{1q}^{\perp h}$$

Worm-gear L

$$A_L^{\sin 2\phi_{CS}} \propto h_{1,\pi}^{\perp q} \otimes h_{1L,p}^{\perp q}$$

$$A_{LL} \propto g_{1L}^q \otimes D_{1q}^h, A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$$

Double polarized DY only

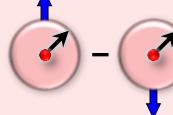
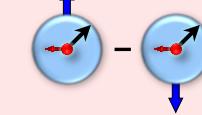
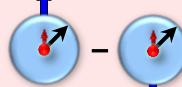
: FFs, further constrained by the e+e- process.  
5 April 2017



# Key Issues of TMDs to be Answered/Tested by Experiments

- Signals
- Factorization and universality: different processes
- Properties of QCD evolution: different energies
- Flavor dependence ( $u, d, \bar{u}, \bar{d}, s, \bar{s}, g$ ): different targets and tagged hadrons

# Leading-Twist Transverse-momentum Dependent Parton Density Function (TMDs)

|                     |  | Quark, Gluon | U   | L   | T  |
|---------------------|--|--------------|---|---|--|
|                     |  | Nucleon      |   |   |  |
|                     |  | U            |    |   |   |
| spin of the nucleon |  | U            | number density<br>$f_1^{q,g}(x, k_T^2)$   |   | <br>Boer-Mulders<br>$h_1^{\perp q,g}(x, k_T^2)$   |
|                     |  | L            |   | <br>Helicity<br>$g_{1L}^{q,g}(x, k_T^2)$                                     | <br>worm-gear L<br>$h_{1L}^{\perp q,g}(x, k_T^2)$   |
|                     |  | T            | <br>Sivers<br>$f_{1T}^{\perp q,g}(x, k_T^2)$ | <br>Kotzinian-<br>Mulders<br>worm-gear T<br>$g_{1T}^{\perp q,g}(x, k_T^2)$ | <br>Transversity<br>$h_1^{q,g}(x, k_T^2)$<br><br>Pretzelosity<br>$h_{1T}^{\perp q,g}(x, k_T^2)$ |

spin of the nucleon

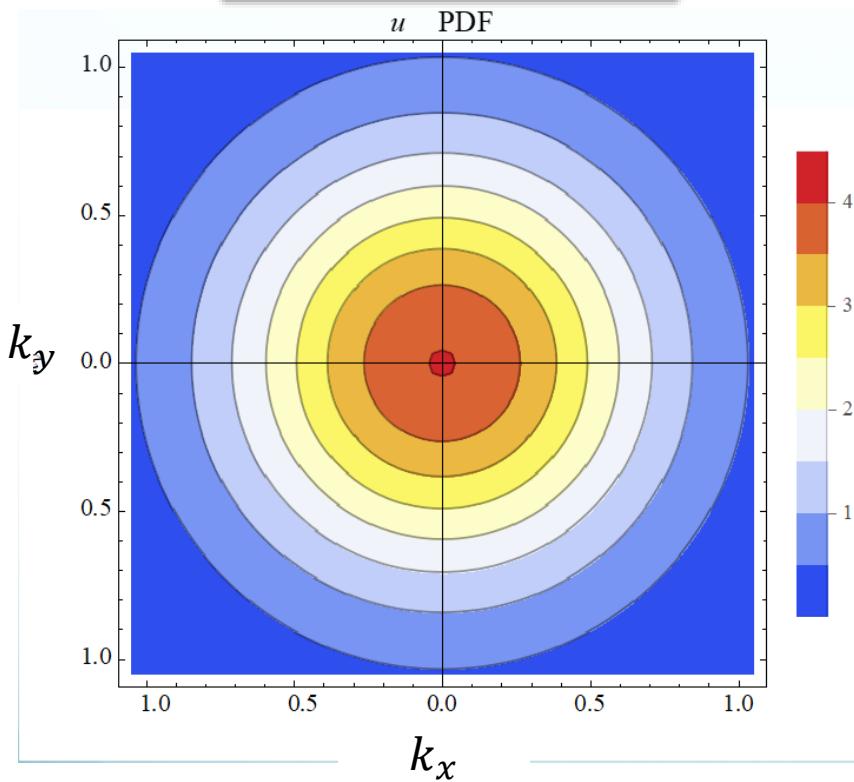
spin of the parton

$k_T$  of the parton

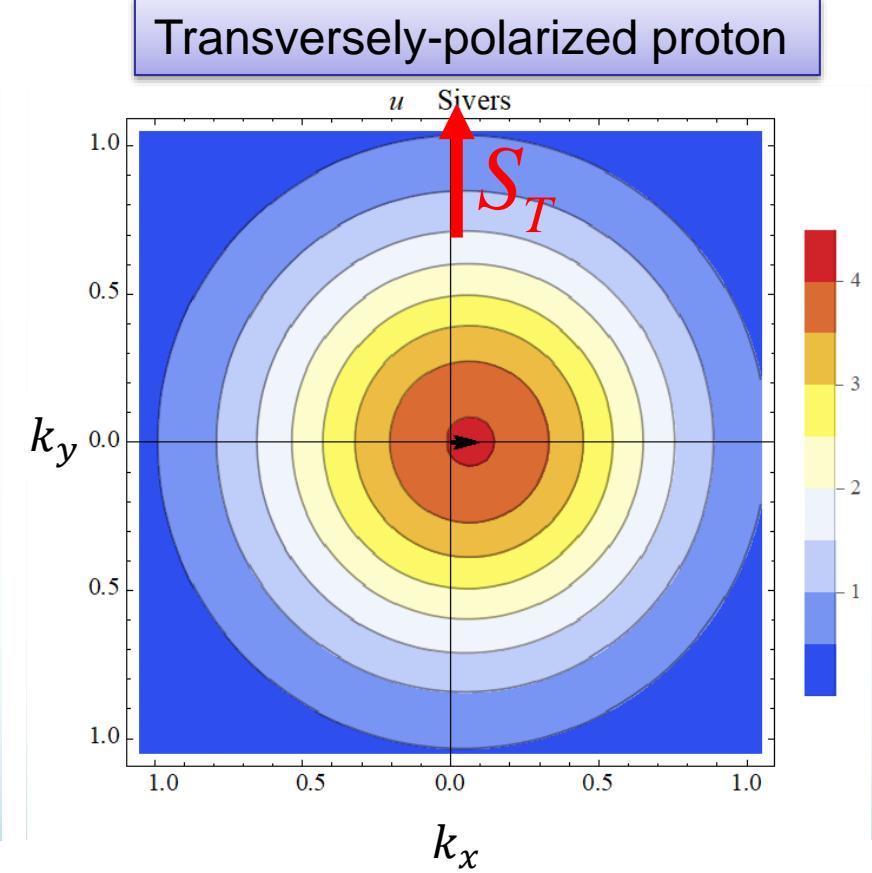
# TMD Sivers Function

$$f_{q/p\uparrow}(x, \vec{k}_T, \vec{S}_T) = f_{q/p}(x, k_T^2) - \frac{1}{M_N} f_{1T}^{\perp q}(x, k_T^2) \vec{S}_T \cdot (\hat{p}_N \times \vec{k}_T)$$

Unpolarized proton



Transversely-polarized proton

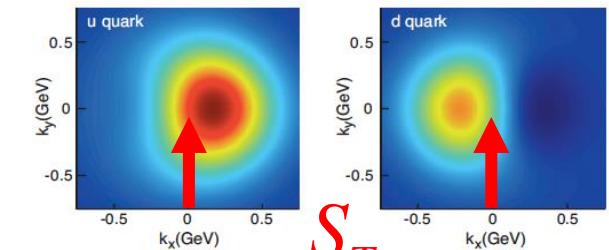
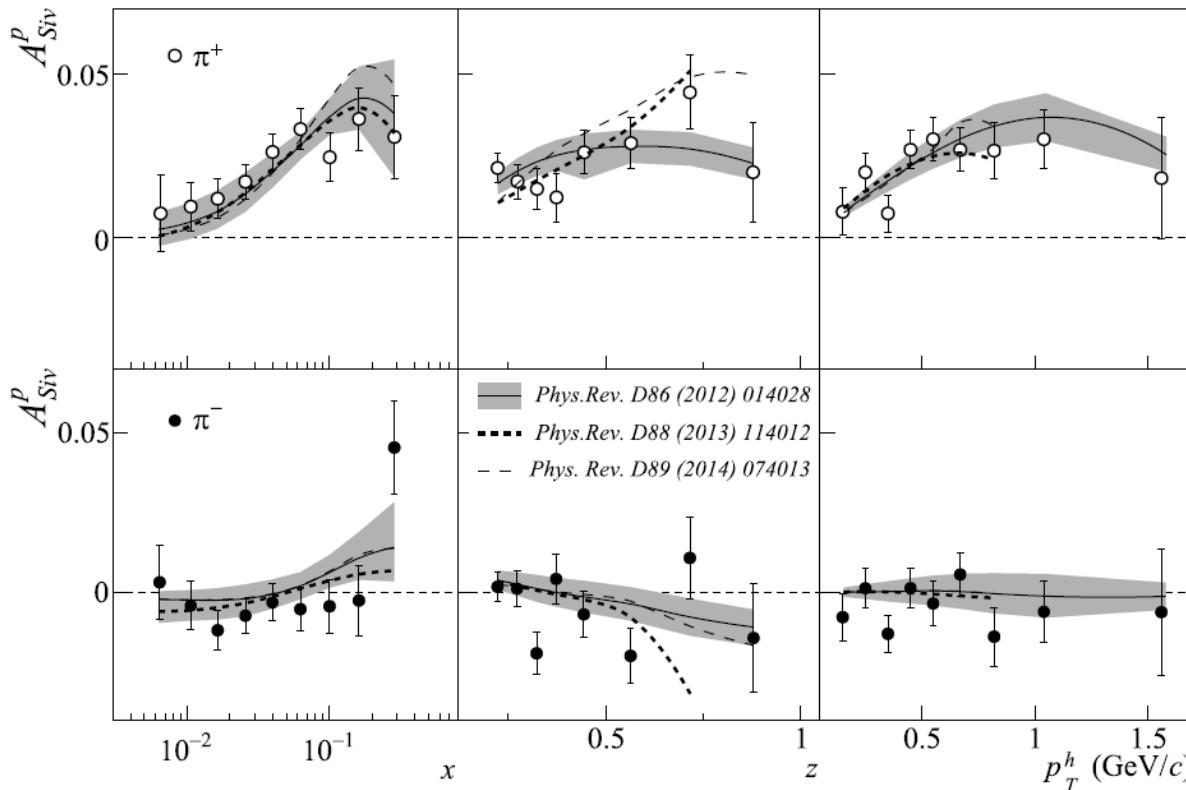


- A nonzero Sivers function is considered to be strong evidence for the presence of quark orbital angular momentum.

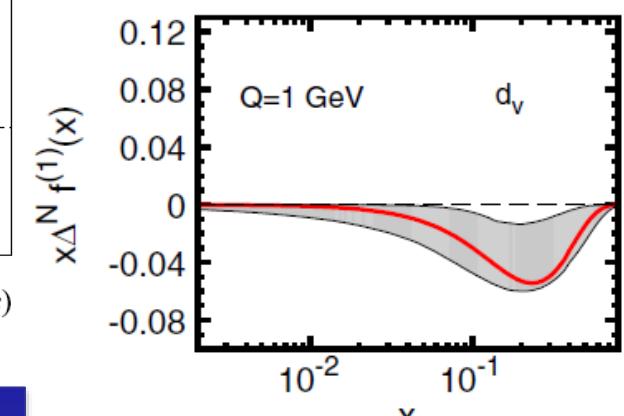
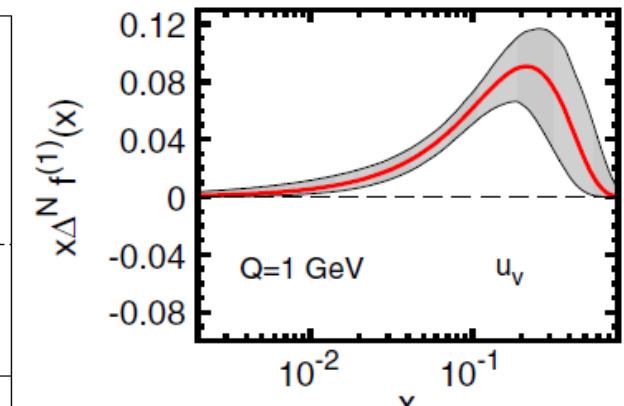
# Nonzero Sivers Asymmetries from SIDIS

T. Iwata's talk

COMPASS, PLB 744 (2015) 250



$S_T$   
Sivers Functions



Signals of Sivers functions in SIDIS.  
Flavor dependence.



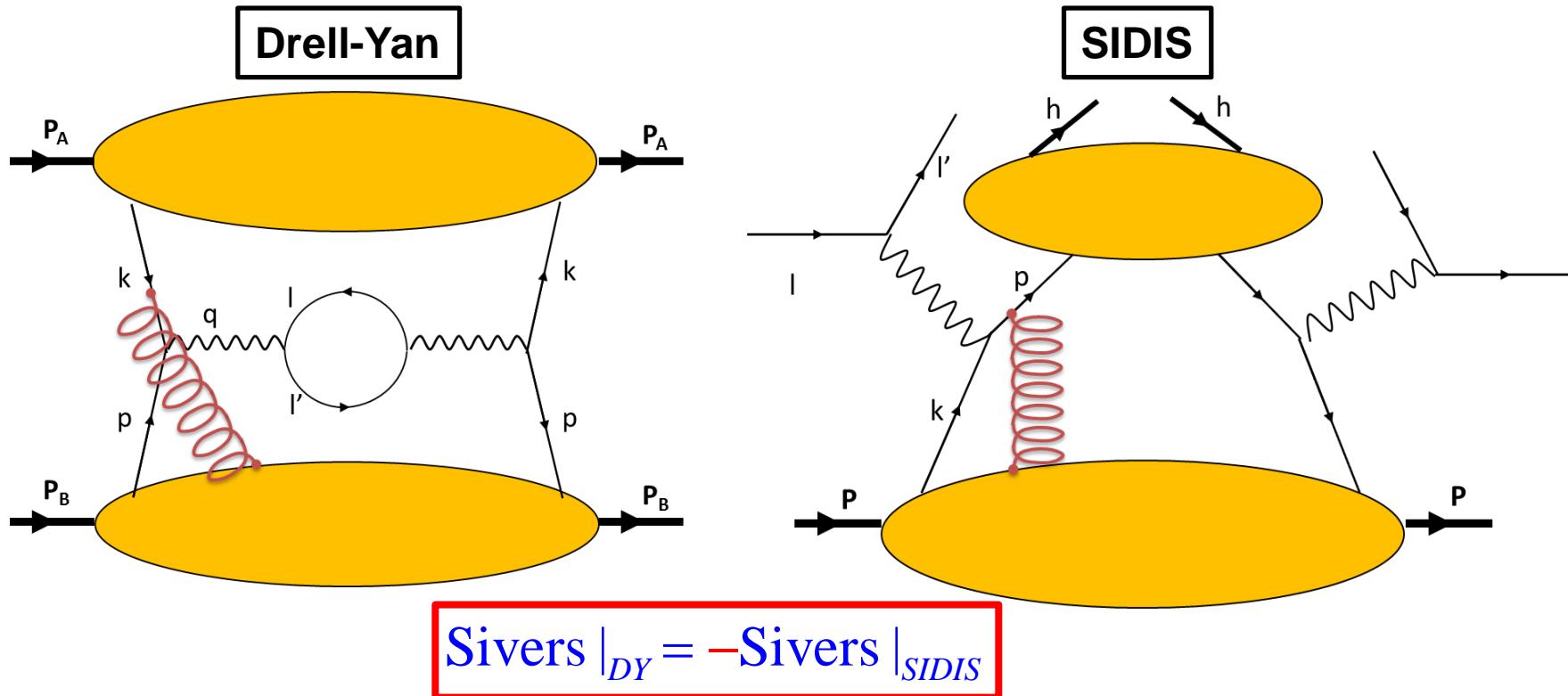
# Universality of Sivers Functions

J.C. Collins, Phys. Lett. B 536 (2002) 43

A.V. Belitsky, X. Ji, F. Yuan, Nucl. Phys. B 656 (2003) 165

D. Boer, P.J. Mulders, F. Pijlman, Nucl. Phys. B 667 (2003) 201

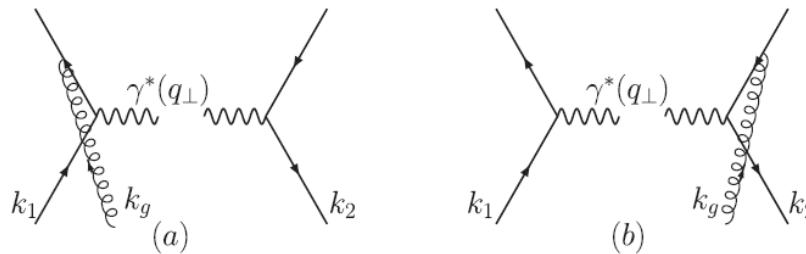
Z.B. Kang, J.W. Qiu, Phys. Rev. Lett. 103 (2009) 172001



- QCD gluon gauge link (Wilson line) in the initial state (DY) vs. final state interactions (SIDIS).
- **Fundamental predictions from TMD physics will be tested.**

# “Opposite Sign of SSA for SIDIS and DY Preserved in NLO QCD”

*Z-B Kang, B-W Xiao and F. Yuan, PRL 107, 152002 (2011)*



- Ji-Ma-Yuan factorization
- Collins-Soper-Sterman resummation

$$\frac{d\Delta\sigma(S_\perp)}{dv dO^2 d^2 a_1} = \sigma_0 \epsilon^{\alpha\beta} S_\perp^\alpha W_{\text{UT}}^\beta(Q; q_\perp), \quad (2)$$

$$W_{\text{UT}}^\alpha(Q; q_\perp) = \int \frac{d^2 b}{(2\pi)^2} e^{i\vec{q}_\perp \cdot \vec{b}} \tilde{W}_{\text{UT}}^\alpha(Q; b) + Y_{\text{UT}}^\alpha(Q; q_\perp),$$

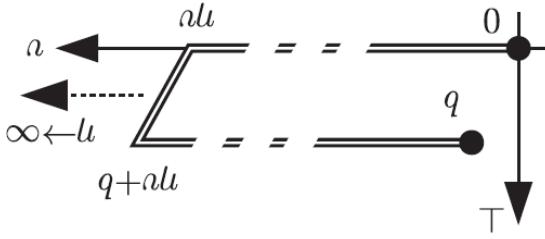
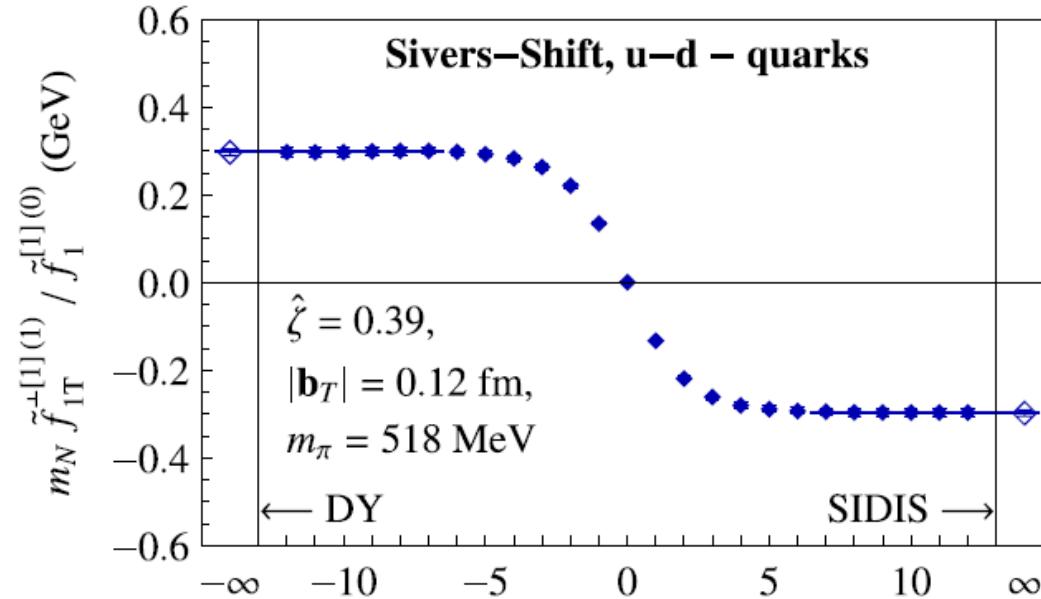
$q_\perp \square Q$

$$\begin{aligned} \tilde{W}_{\text{UT}}^\alpha(Q; b) &= e^{-S_{\text{UT}}(Q^2, b)} \tilde{W}_{\text{UT}}^\alpha(C_1/b, b) \\ &= (-ib_\perp^\alpha/2) e^{-S_{\text{UT}}(Q^2, b)} \Sigma_{i,j} \\ &\times \Delta C_{qi}^T \otimes f_{i/A}^{(3)}(z'_1, z''_1) C_{\bar{q}j} \otimes f_{j/B}(z'_2), \end{aligned} \quad (9)$$

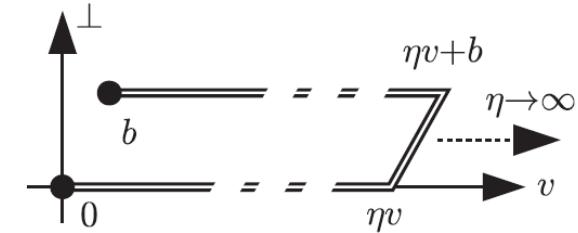
$$\Delta C_q^T \Big|_{DY} = -\Delta C_q^T \Big|_{SIDIS}$$

# Sivers Function with Lattice QCD

*B. U. Musch et al., PRD 85, 094510 (2012)*



$\eta|v|$  (lattice units)



As the vertical gauge link ( $\eta v$ ) goes from  $\infty$  (**SIDIS**) to  $-\infty$  (**Drell-Yan**), the sign of Sivers function reverses.



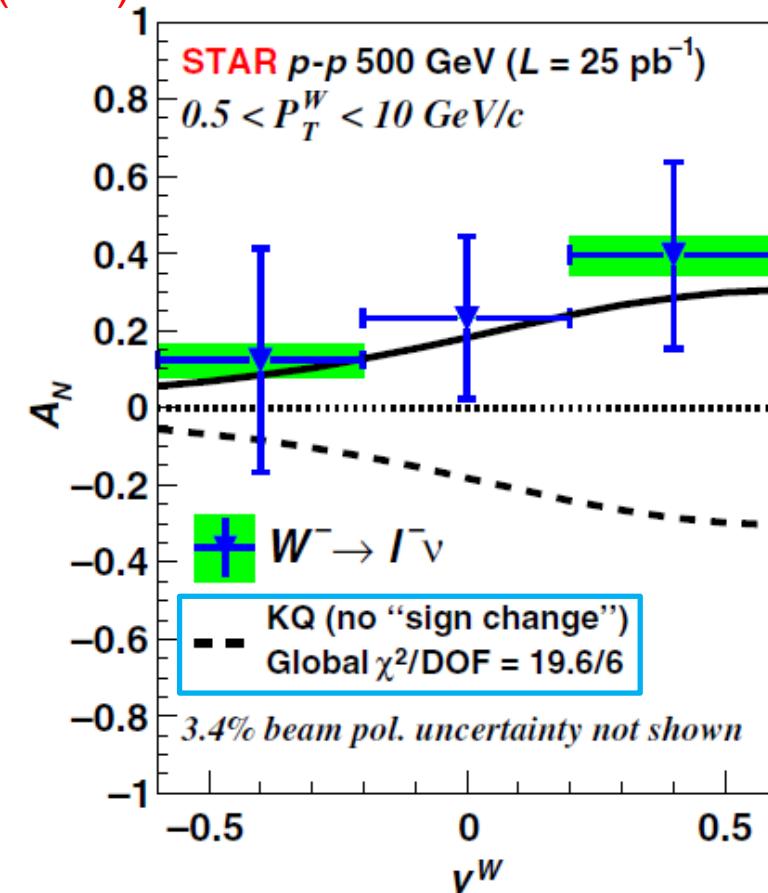
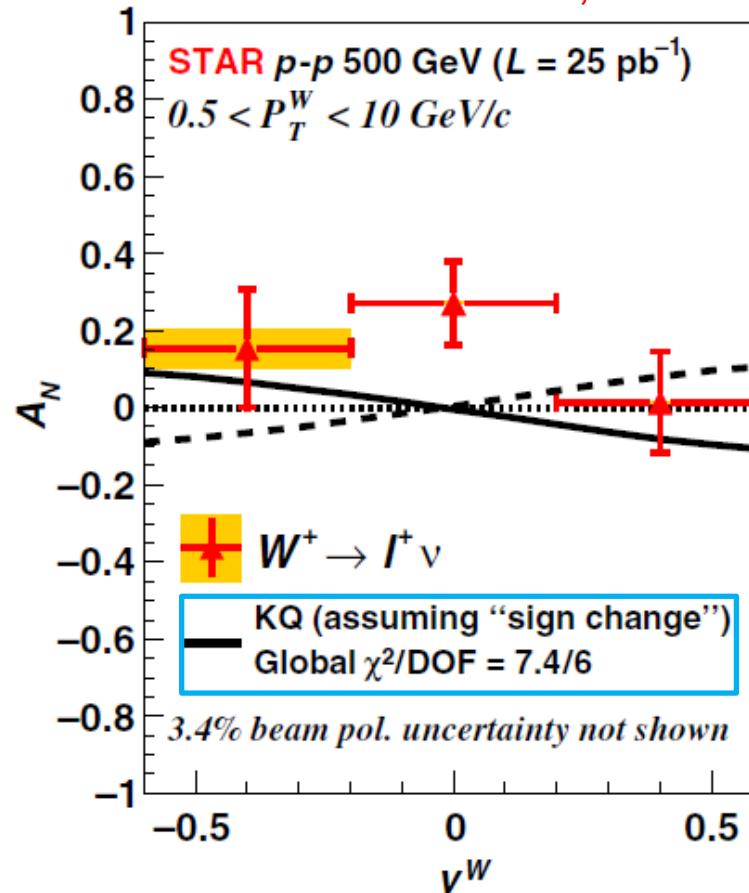
# 2015 U.S. Long Range Plan

The cover of the 2015 U.S. Long Range Plan for Nuclear Science. It features a large aerial photograph of a coastal town and highway. A yellow banner across the middle contains the text "REACHING FOR THE HORIZON". Below the banner is a smaller yellow box containing the text "The Site of the Wright Brothers' First Airplane Flight". Below this are four small photographs showing people working in laboratory or experimental settings. At the bottom, the title "The 2015 LONG RANGE PLAN for NUCLEAR SCIENCE" is written in large blue serif font. Below the title are two circular logos: one for the University of Michigan and one for the National Science Foundation (NSF).

A nonzero Slvers function is considered to be strong evidence for the presence of quark orbital angular momentum. Indeed, it has been measured to be nonzero in the HERMES and JLab experiments. Figure 2.5 shows the unique potential of the JLab 12-GeV program to map the Slvers function for the up quark. The Slvers function has a quite intriguing property predicted by QCD. When measured in SIDIS, it will have one sign, yet when measured in a collision with a proton or pion beam, it should have the opposite sign. This sign change is due to the nature of QCD color interactions and provides an important test of our understanding. It is imperative that the quark Slvers functions that will be measured in SIDIS are also accurately measured with hadron beams, such as the proton beams available at RHIC or Fermilab and the pion beams used by the COMPASS-II experiment at CERN.

# Transverse SSA of W in polarized pp collisions at RHIC

STAR, PRL 116 (2016) 132301



$$A_N = \frac{1}{\langle P \rangle} \frac{\sqrt{N_{\uparrow}(\phi)N_{\downarrow}(\phi + \pi)} - \sqrt{N_{\uparrow}(\phi + \pi)N_{\downarrow}(\phi)}}{\sqrt{N_{\uparrow}(\phi)N_{\downarrow}(\phi + \pi)} + \sqrt{N_{\uparrow}(\phi + \pi)N_{\downarrow}(\phi)}},$$

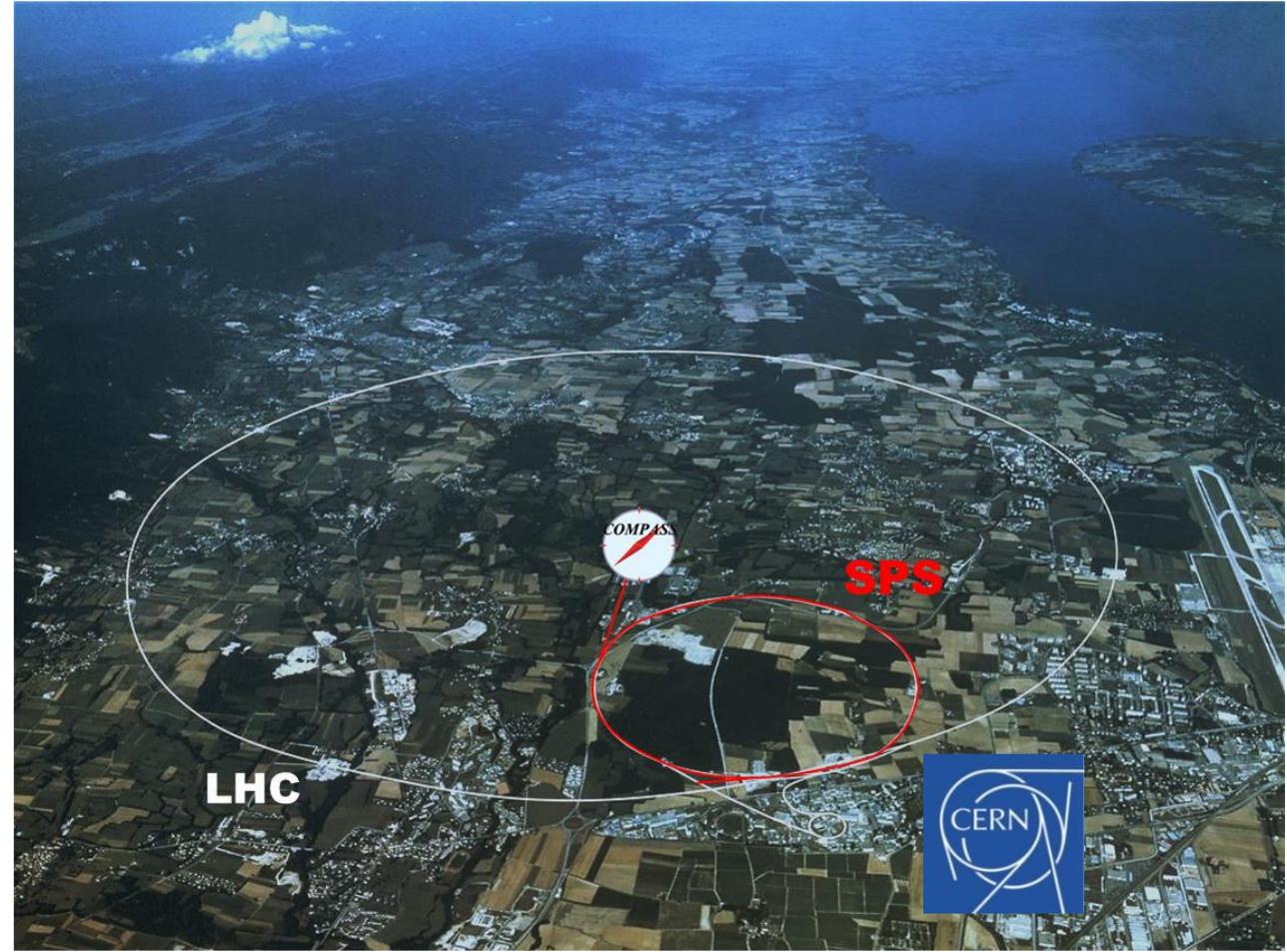


# COMPASS Collaboration

(Common Muon and Proton Apparatus for Structure and Spectroscopy)

M.G. Perdekamp's talk

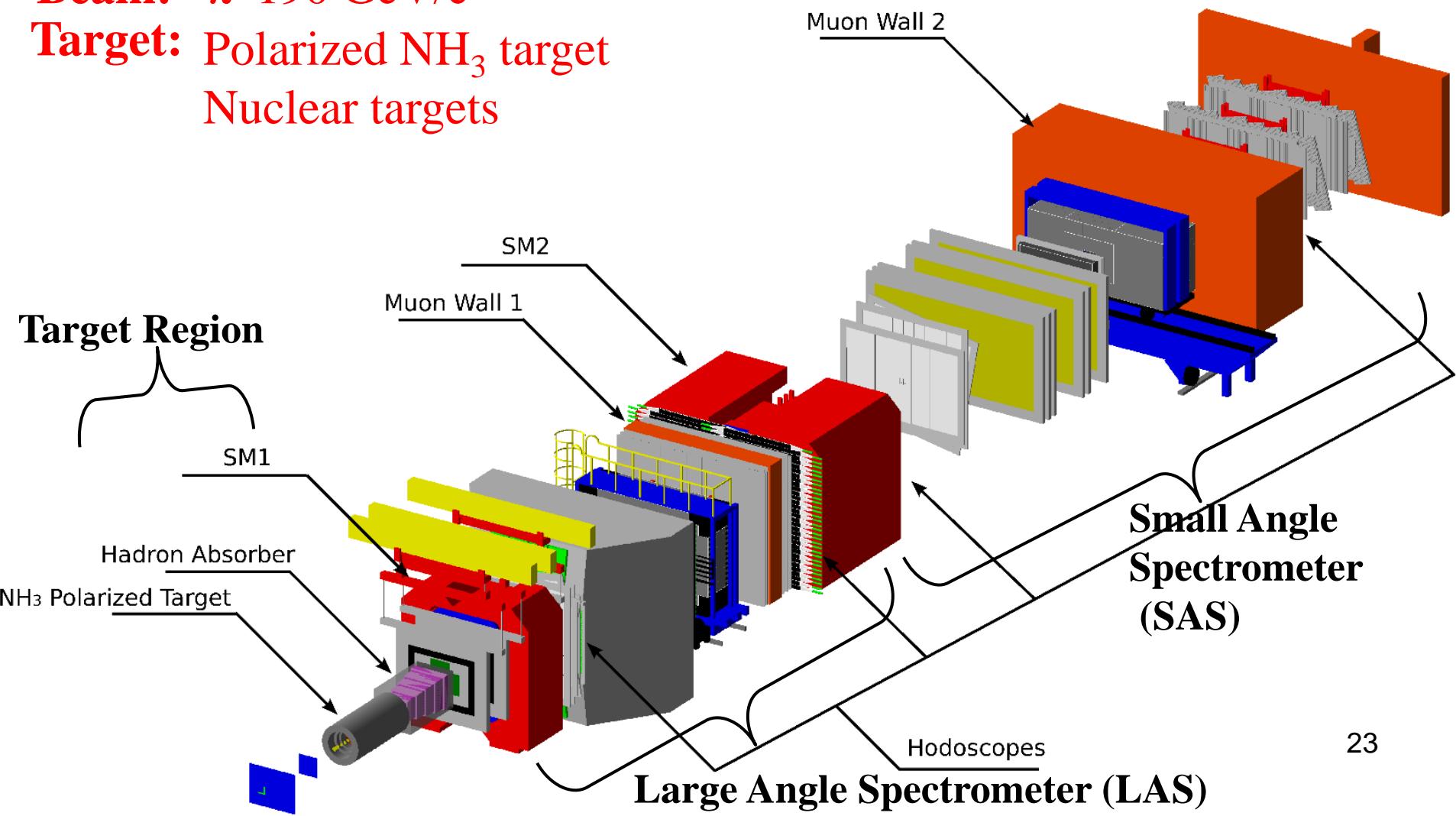
- 24 institutions from 13 countries – nearly 250 physicists
- Fixed-target experiment at SPS north area
- Physics programs:
  - Nucleon spin and partonic structures
  - Hadron spectroscopy



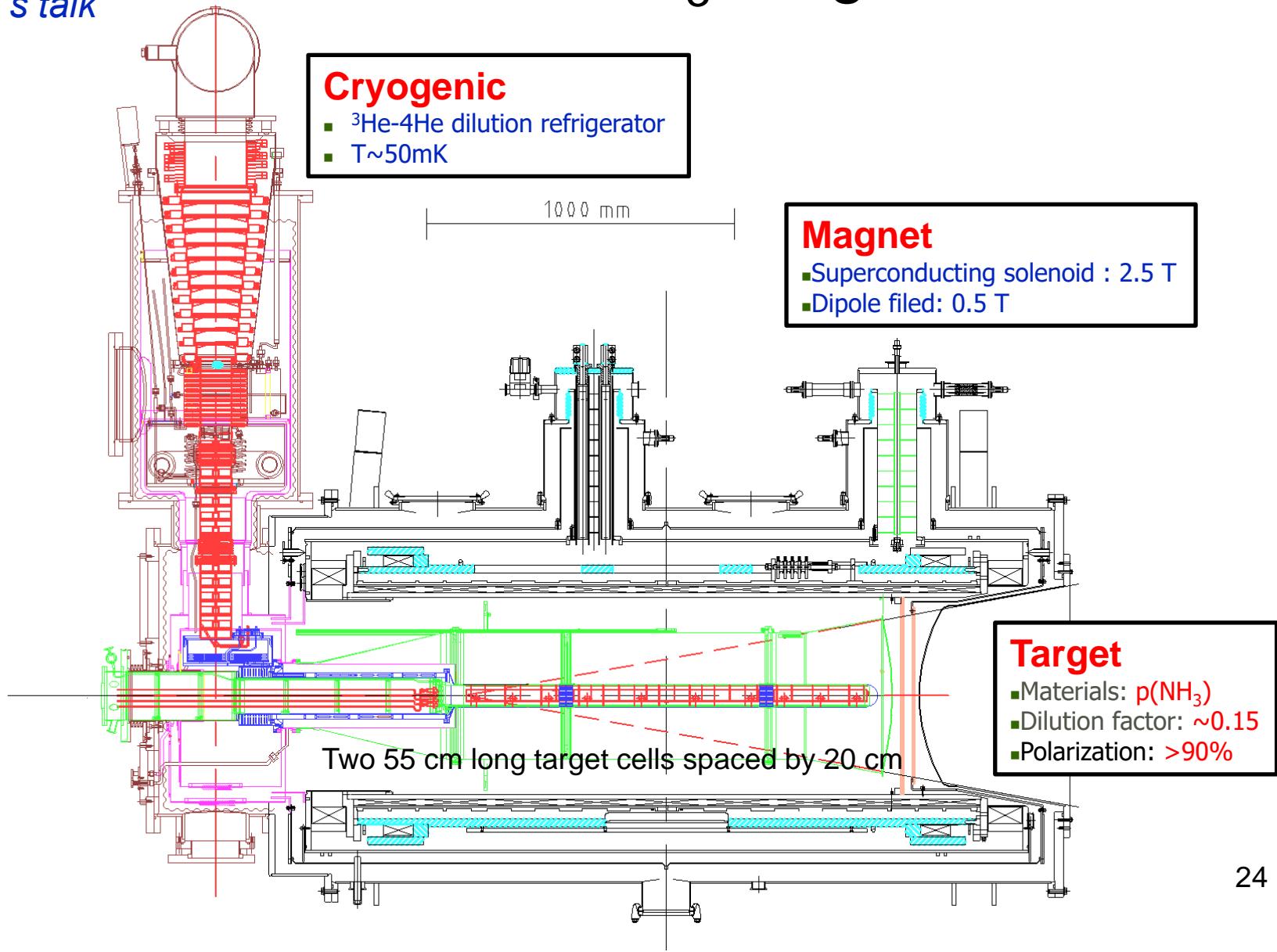
# COMPASS Setup (Drell-Yan Runs)

**Beam:**  $\pi^-$  190 GeV/c

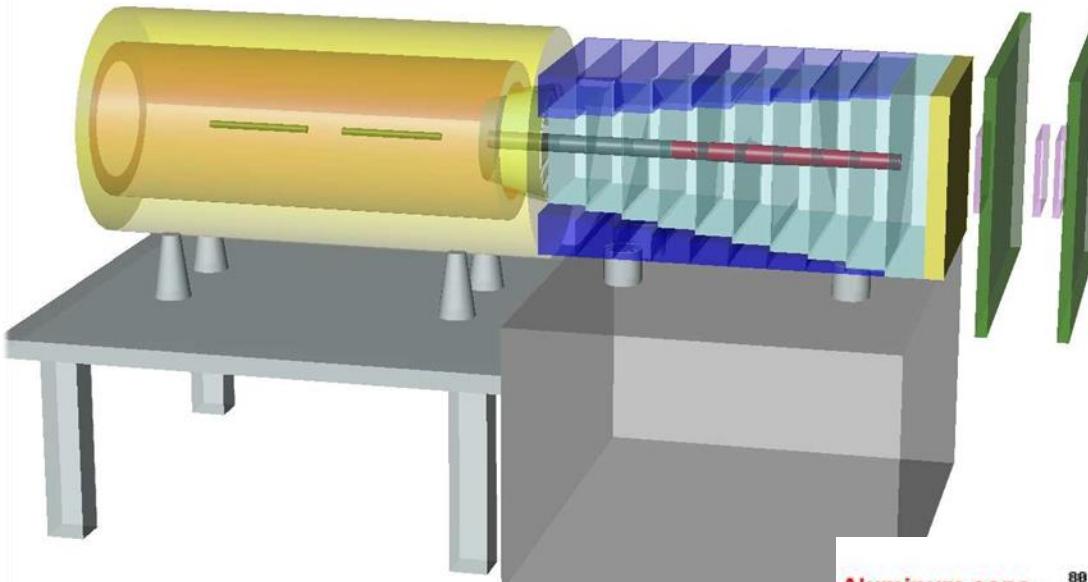
**Target:** Polarized  $\text{NH}_3$  target  
Nuclear targets



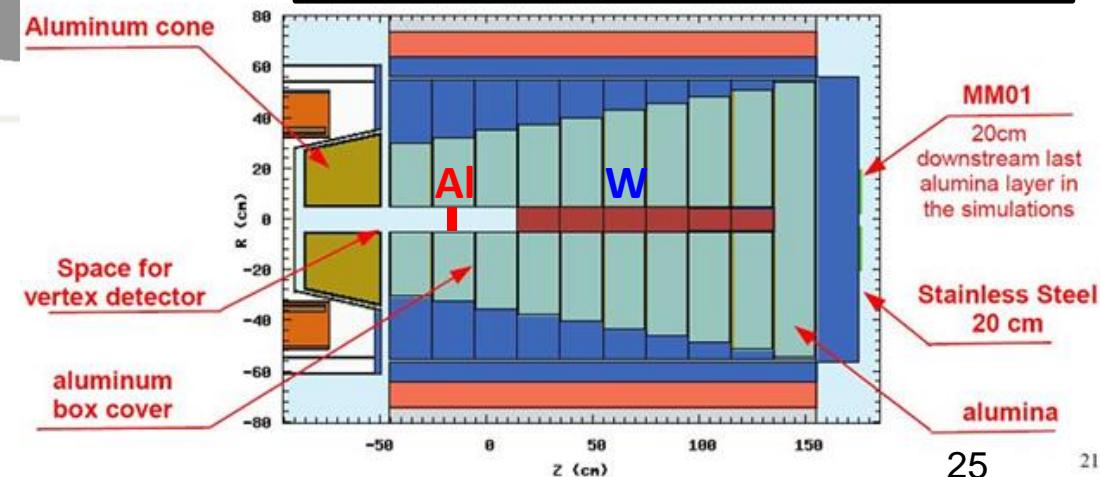
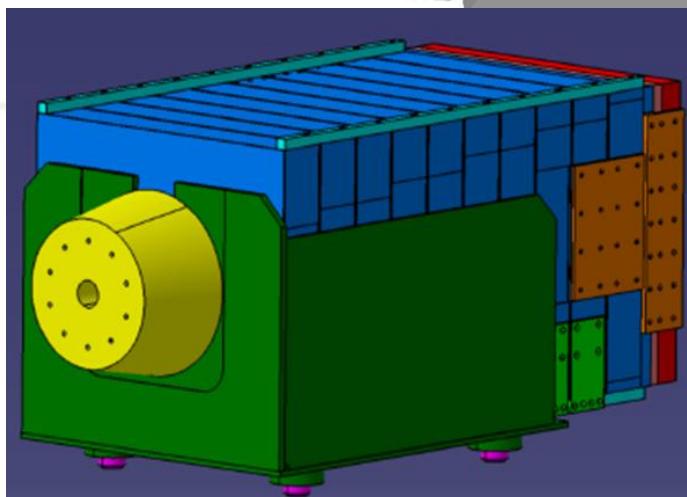
# Polarized NH<sub>3</sub> Target



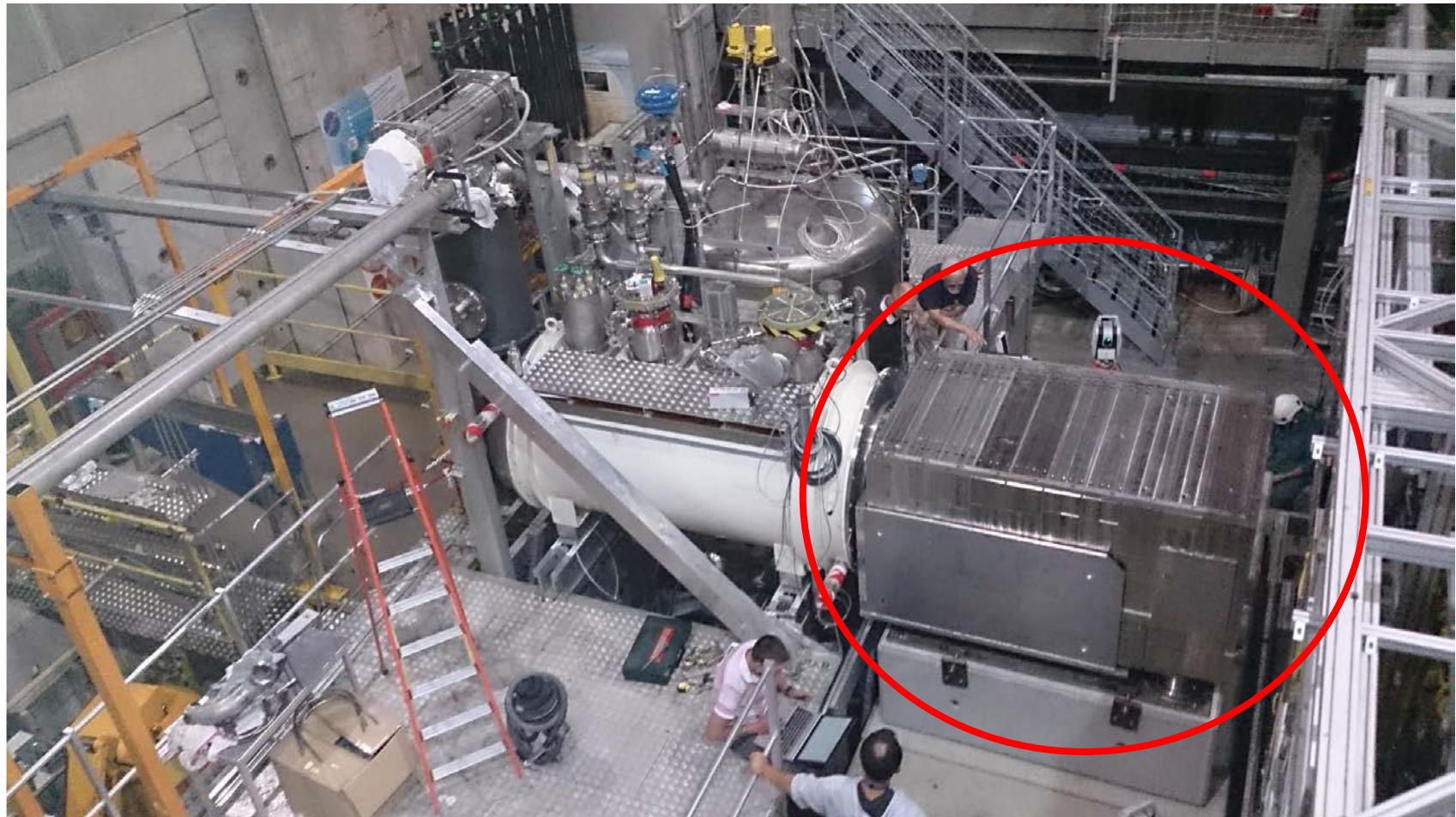
# Hadron Absorber & Nuclear Targets



- Absorber: 236 cm long, made of  $\text{Al}_2\text{O}_3$ .
- Radiation lengths (multiple scattering for  $\mu$ ):  $x/X_0 = 33.53$
- Hadronic interaction lengths (stopping power for  $\pi$ ):  $x/\lambda_{\text{int}} = 7.25$
- 7 cm Al target
- 120 cm W beam dump



# Hadron Absorber & Nuclear Targets

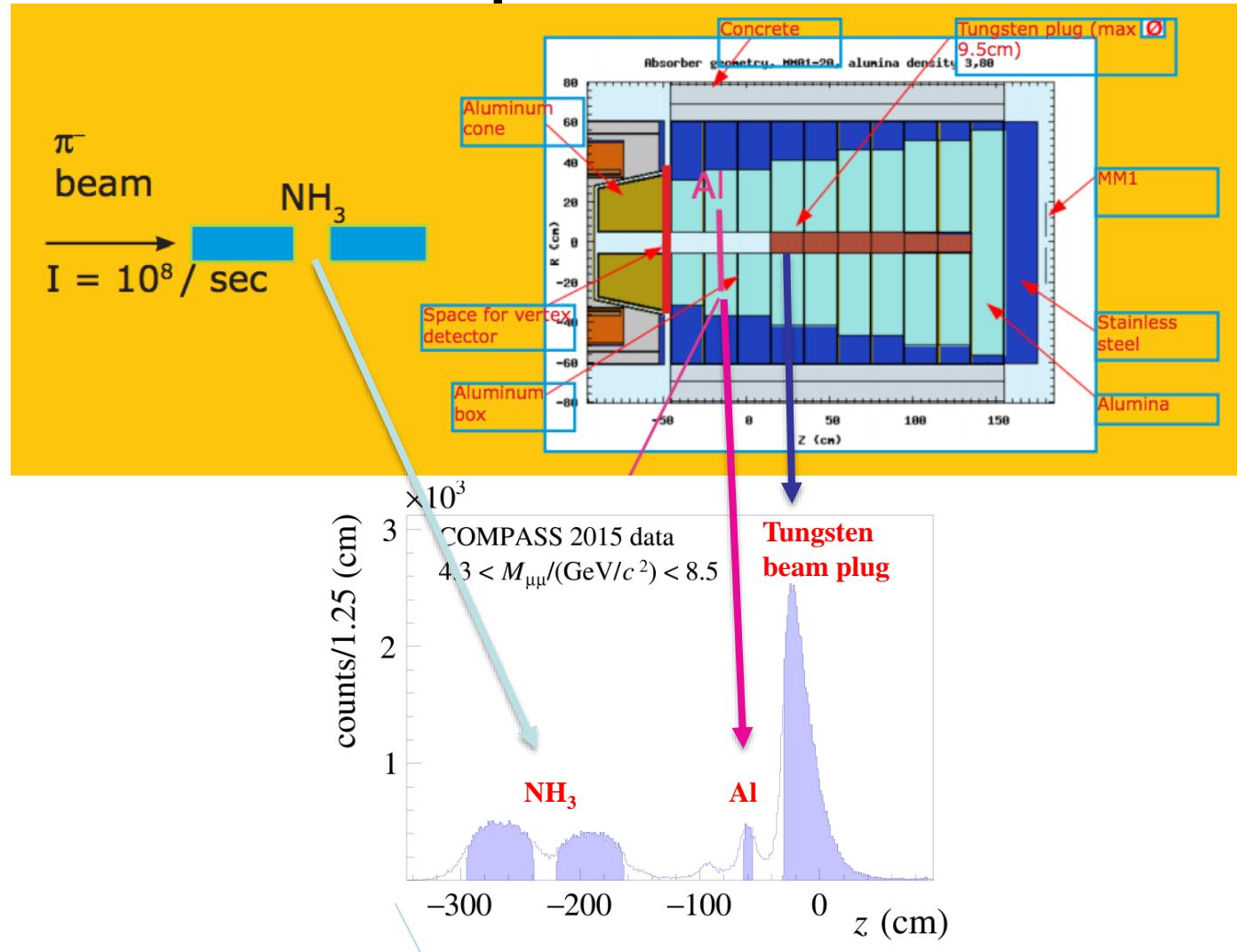




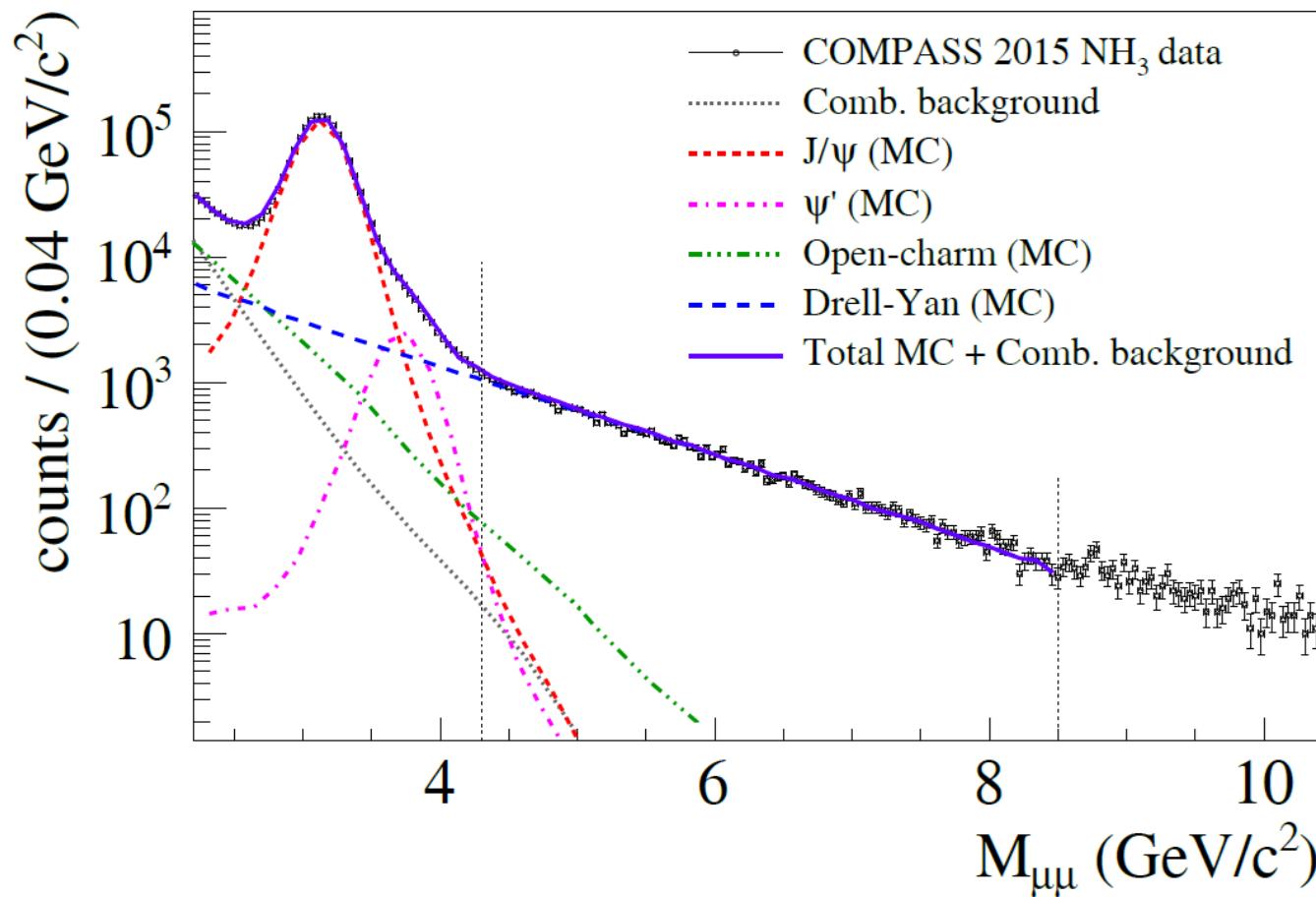
# COMPASS-II Transversely Polarized Drell-Yan Program

- Schedules:
  - 2014 Oct – Dec: commission Drell-Yan runs
  - 2015: first year of transversely polarized Drell-Yan runs with 190 GeV  $\pi^-$  beam

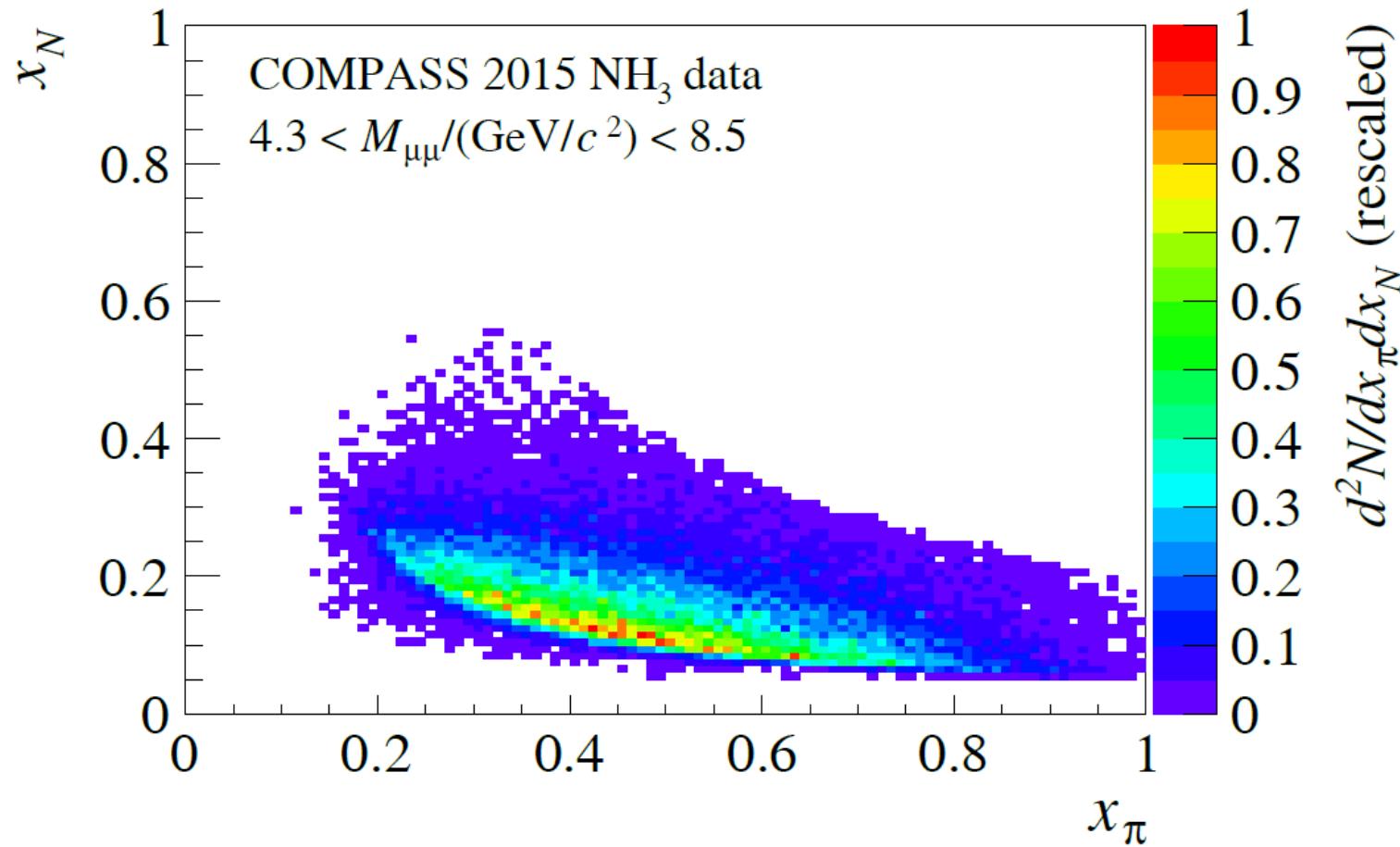
# Dimuon Vertex Distributions (2015 Trans.-pol. Drell-Yan Runs)



# Dimuon Invariant-mass Distributions (2015 Trans.-pol. Drell-Yan Runs)



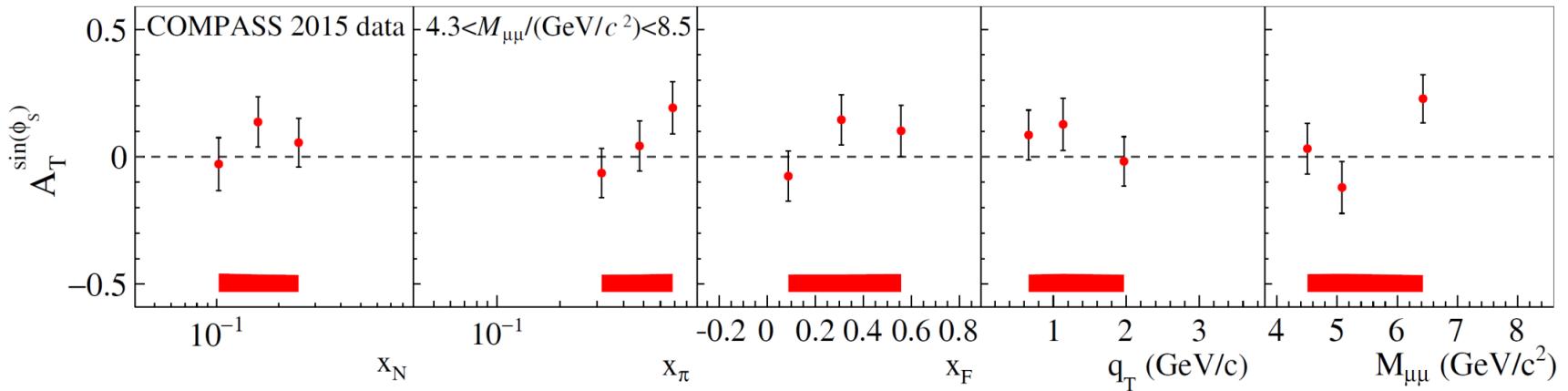
# Kinematic Acceptance (2015 Trans.-pol. Drell-Yan Runs)



# Transverse Spin Asymmetries in Trans.-pol. Drell-Yan: Sivers

$$\begin{aligned}
 & \frac{d\sigma^{LO}}{d^4 q d\Omega} \\
 &= \frac{\alpha_{em}^2}{F q^2} \hat{\sigma}_U^{LO} \left\{ \left( 1 + D_{[\sin^2 \theta]}^{LO} A_U^{\cos 2\phi} \cos 2\phi \right) \right. \\
 &+ \left| \vec{S}_T \right| \left[ A_T^{\sin \phi_s} \sin \phi_s \right.
 \end{aligned}$$

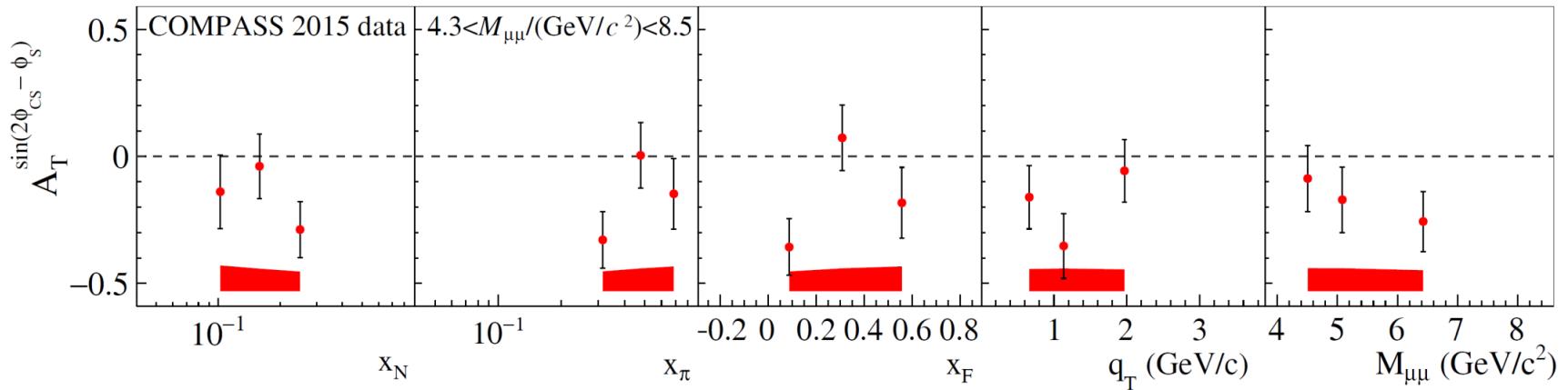
$$A_T^{\sin \phi_s} \propto \text{Density } f_1|_\pi \otimes \text{Sivers } f_{1T}^\perp|_p$$



# Transverse Spin Asymmetries in Trans.-pol. Drell-Yan: Transversity

$$\begin{aligned}
 & \frac{d\sigma^{LO}}{d^4 q d\Omega} \\
 &= \frac{\alpha_{em}^2}{F q^2} \hat{\sigma}_U^{LO} \left\{ \left( 1 + D_{[\sin^2 \theta]}^{LO} A_U^{\cos 2\phi} \cos 2\phi \right) \right. \\
 &+ \left| \vec{S}_T \right| \left[ A_T^{\sin \phi_s} \sin \phi_s \right.
 \end{aligned}$$

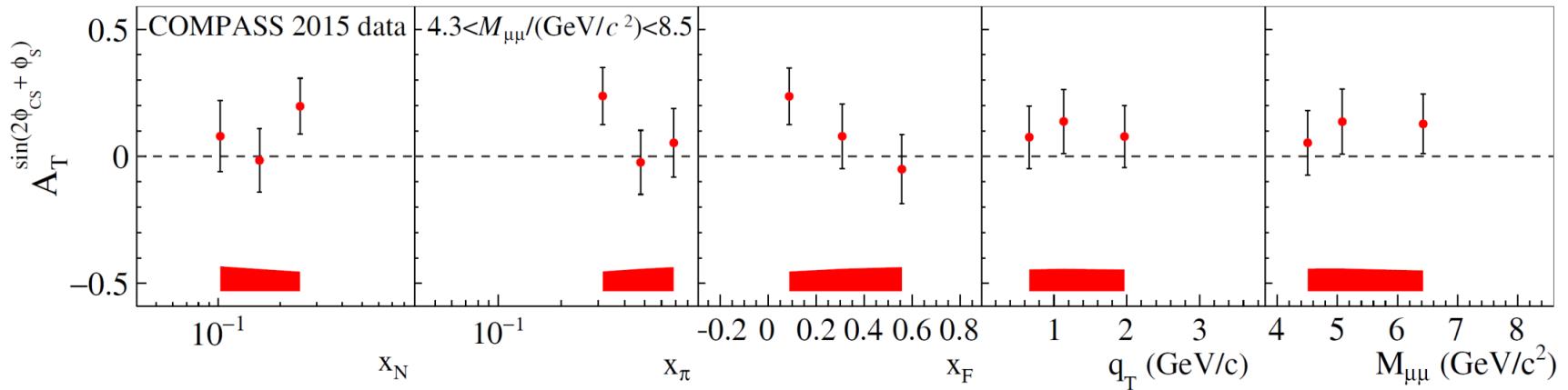
$$A_T^{\sin(2\phi - \phi_s)} \propto \text{BM } h_1^\perp |_\pi \otimes \text{Transversity } h_1 |_p$$



# Transverse Spin Asymmetries in Trans.-pol. Drell-Yan: Pretzelosity

$$\begin{aligned}
 & \frac{d\sigma^{LO}}{d^4 q d\Omega} \\
 &= \frac{\alpha_{em}^2}{F q^2} \hat{\sigma}_U^{LO} \left\{ \left( 1 + D_{[\sin^2 \theta]}^{LO} A_U^{\cos 2\phi} \cos 2\phi \right) \right. \\
 &+ \left| \vec{S}_T \right| \left[ A_T^{\sin \phi_s} \sin \phi_s \right.
 \end{aligned}$$

$$A_T^{\sin(2\phi + \phi_s)} \propto \text{BM } h_1^\perp |_\pi \otimes \text{Pretzelosity } h_{1T}^\perp |_p$$





# SIDIS and single-polarized DY x-sections at twist-2 (LO)

$$\frac{d\sigma^{LO}}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L})$$

$$\times \left\{ \begin{array}{l} 1 + \boxed{\varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h} \\ + S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} \\ + S_T \left[ \begin{array}{l} A_{UT}^{\sin(\phi_h - \phi_s)} \sin(\phi_h - \phi_s) \\ + \varepsilon A_{UT}^{\sin(\phi_h + \phi_s)} \sin(\phi_h + \phi_s) \\ + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_s)} \sin(3\phi_h - \phi_s) \end{array} \right] \\ + S_T \lambda \left[ \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_s)} \cos(\phi_h - \phi_s) \right] \end{array} \right\}$$

**SIDIS**  $\frac{d\sigma^{LO}}{d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS})$

**DY**

$$\left\{ \begin{array}{l} 1 + \boxed{D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\phi_{CS}} \cos 2\phi_{CS}} \\ + S_L \sin^2 \theta_{CS} A_L^{\sin 2\phi_{CS}} \sin 2\phi_{CS} \\ + S_T \left[ \begin{array}{l} A_T^{\sin \phi_s} \sin \phi_s \\ + D_{[\sin^2 \theta_{CS}]} \left( A_T^{\sin(2\phi_{CS} - \phi_s)} \sin(2\phi_{CS} - \phi_s) \right. \\ \left. + A_T^{\sin(2\phi_{CS} + \phi_s)} \sin(2\phi_{CS} + \phi_s) \right) \end{array} \right] \end{array} \right\}$$

where  $D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$

$A_{UU}^{\cos 2\phi_h} \propto h_1^{\perp q} \otimes H_{1q}^{\perp h} + \dots$

Boer-Mulders

$A_U^{\cos 2\phi_{CS}} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^{\perp q}$

$A_{UT}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$

Sivers

$A_T^{\sin \phi_s} \propto f_{1,\pi}^q \otimes f_{1T,p}^{\perp q}$

$A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$

Transversity

$A_T^{\sin(2\phi_{CS} - \phi_s)} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^q$

$A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$

Pretzelosity

$A_T^{\sin(2\phi_{CS} + \phi_s)} \propto h_{1,\pi}^{\perp q} \otimes h_{1T,p}^{\perp q}$

$A_{UL}^{\sin 2\phi_h} \propto h_{1L}^{\perp q} \otimes H_{1q}^{\perp h}$

Worm-gear L

$A_L^{\sin 2\phi_{CS}} \propto h_{1,\pi}^{\perp q} \otimes h_{1L,p}^{\perp q}$

$A_{LL} \propto g_{1L}^q \otimes D_{1q}^h, A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$

Double polarized DY only

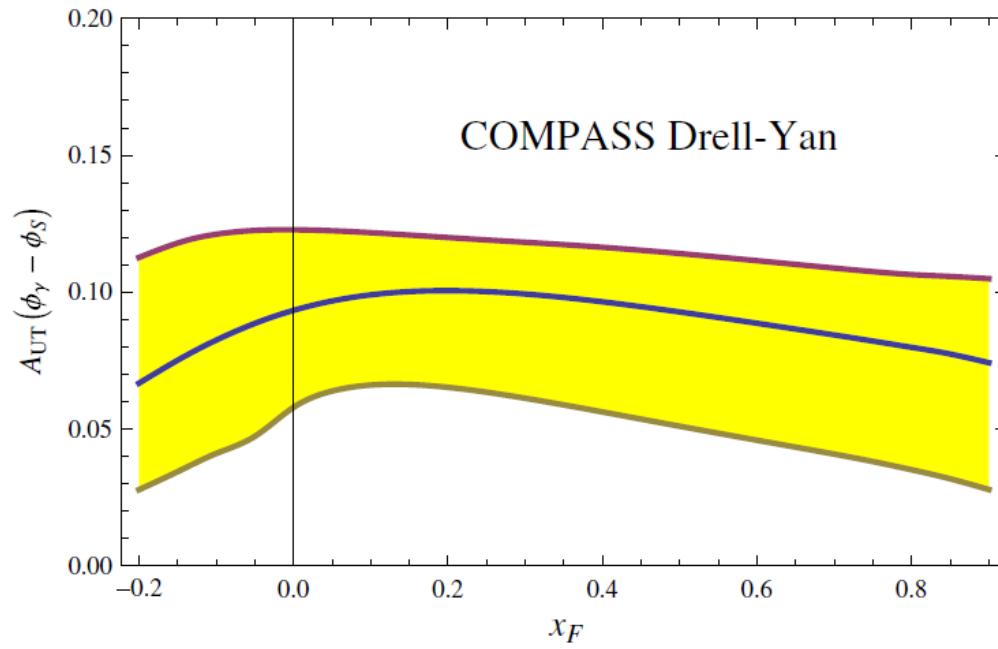


5 April 2017

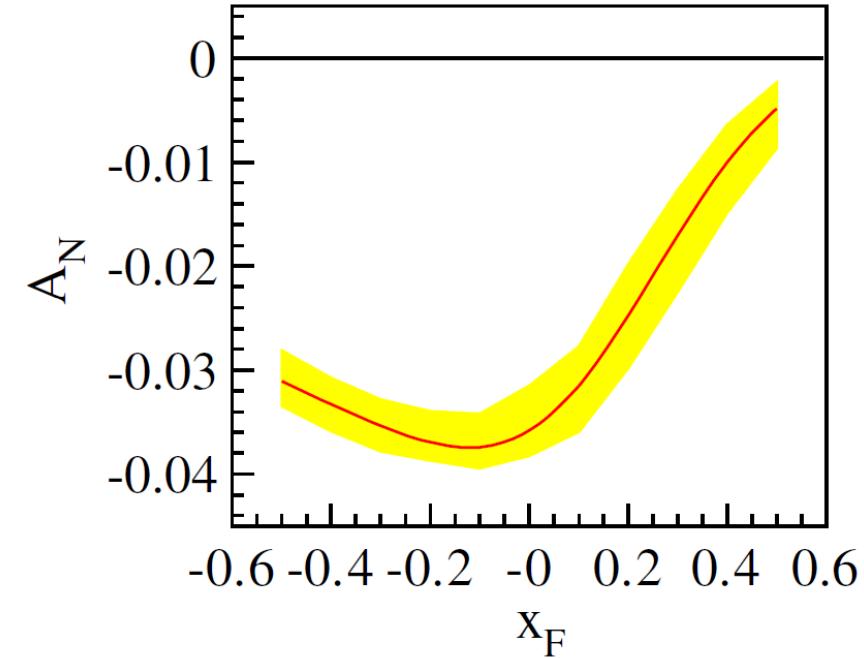
: FFs, further constrained by the e+e- process.



# Predicted Sivers Asymmetries in COMPASS with QCD Evolution

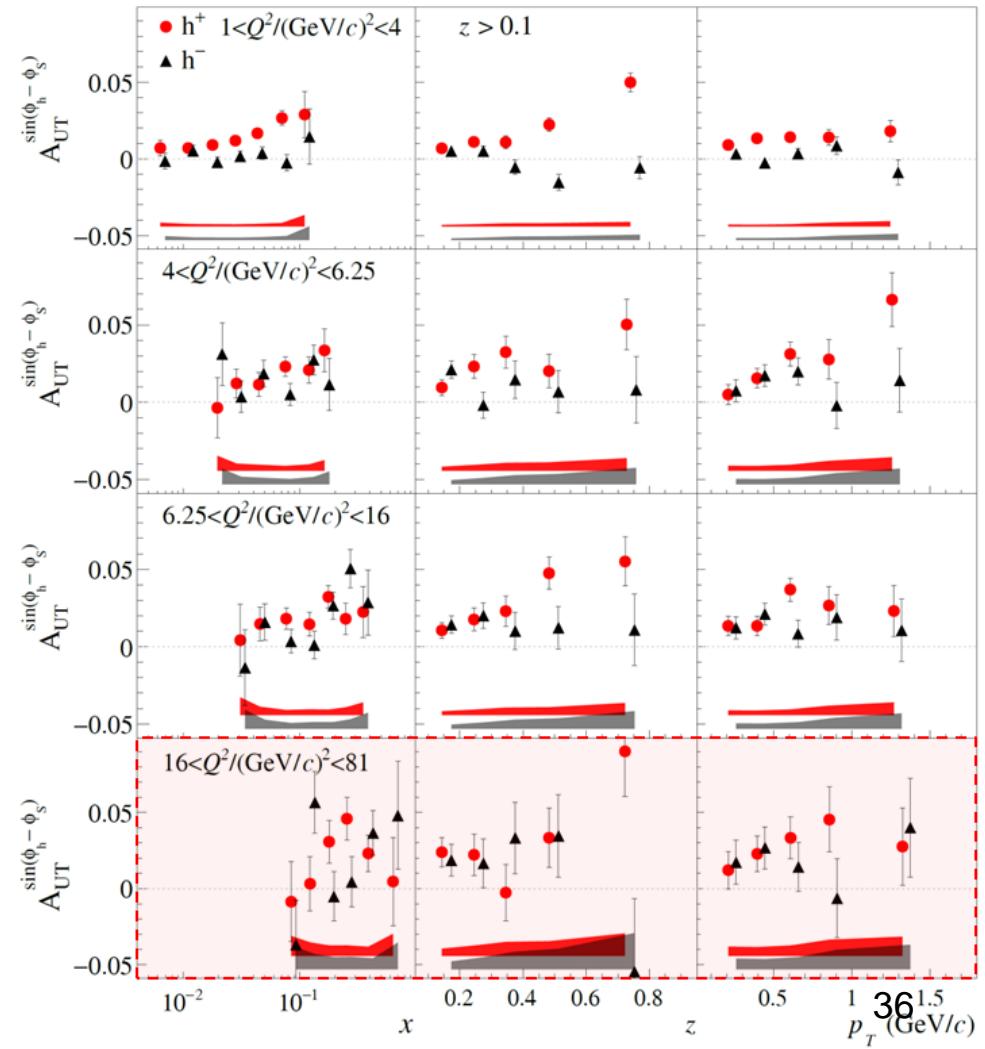
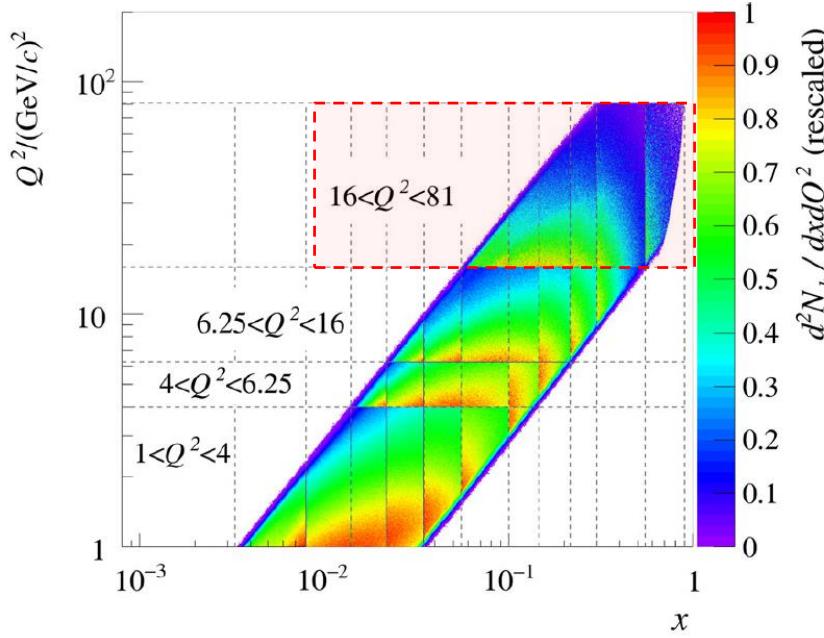


Sun and Yuan,  
PRD 88, 114012 (2013)



Echevarria, Idilbi, Kang and Vitev,  
PRD 89, 074013 (2014)

# Sivers Asymmetries ( $x, z, p_T^h, Q^2$ )



Sivers asymmetry extracted in SIDIS at the hard scales of the Drell–Yan process at COMPASS

COMPASS, PLB 770 (2017) 138



# SIDIS and DY TSAs at COMPASS

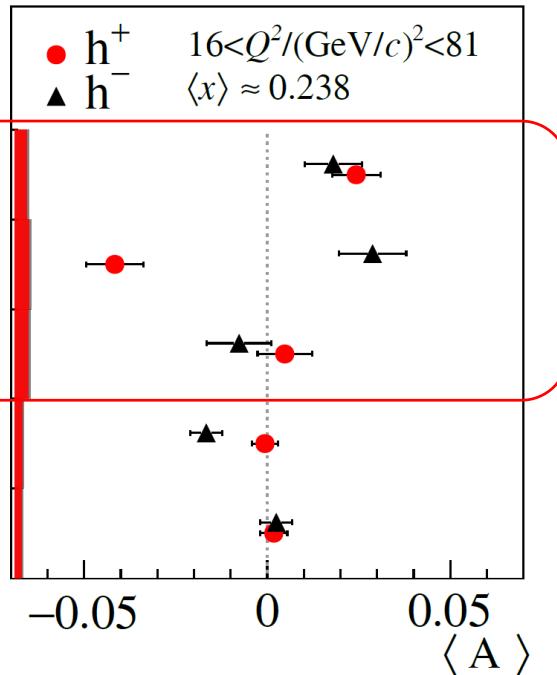
$$\frac{d\sigma}{dxdydzdp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots \right.$$

$$+ S_T \left[ \begin{array}{l} A_{UT}^{\sin(\phi_h - \phi_S)} \sin(\phi_h - \phi_S) \\ + \varepsilon A_{UT}^{\sin(\phi_h + \phi_S)} \sin(\phi_h + \phi_S) \\ + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)} \sin(3\phi_h - \phi_S) \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_S} \sin\phi_S \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h - \phi_S)} \sin(2\phi_h - \phi_S) \end{array} \right] \right\}$$

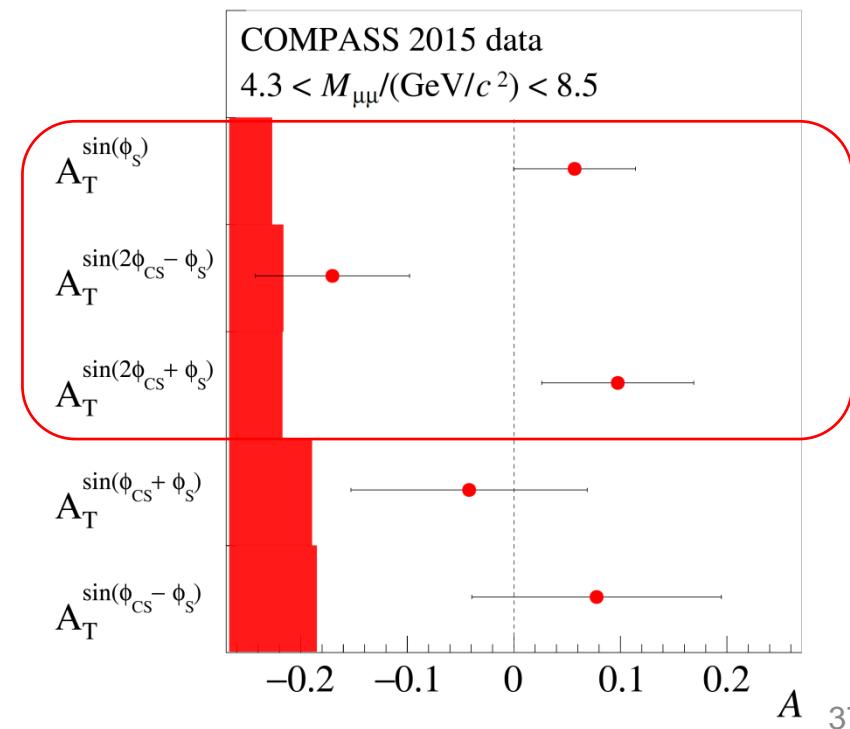
$$\frac{d\sigma^{LO}}{d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS}) \left\{ 1 + \dots \right.$$

$$+ S_T \left[ \begin{array}{l} A_T^{\sin\varphi_S} \sin\varphi_S \\ + D_{[\sin^2 \theta_{CS}]} \left( A_T^{\sin(2\phi_{CS} - \phi_S)} \sin(2\phi_{CS} - \phi_S) \right. \\ \left. + A_T^{\sin(2\phi_{CS} + \phi_S)} \sin(2\phi_{CS} + \phi_S) \right) \\ + D_{[\sin 2\theta_{CS}]} \left( A_T^{\sin(\phi_{CS} - \phi_S)} \sin(\phi_{CS} - \phi_S) \right. \\ \left. + A_T^{\sin(\phi_{CS} + \phi_S)} \sin(\phi_{CS} + \phi_S) \right) \end{array} \right] \right\}$$

COMPASS, PLB 770 (2017) 138



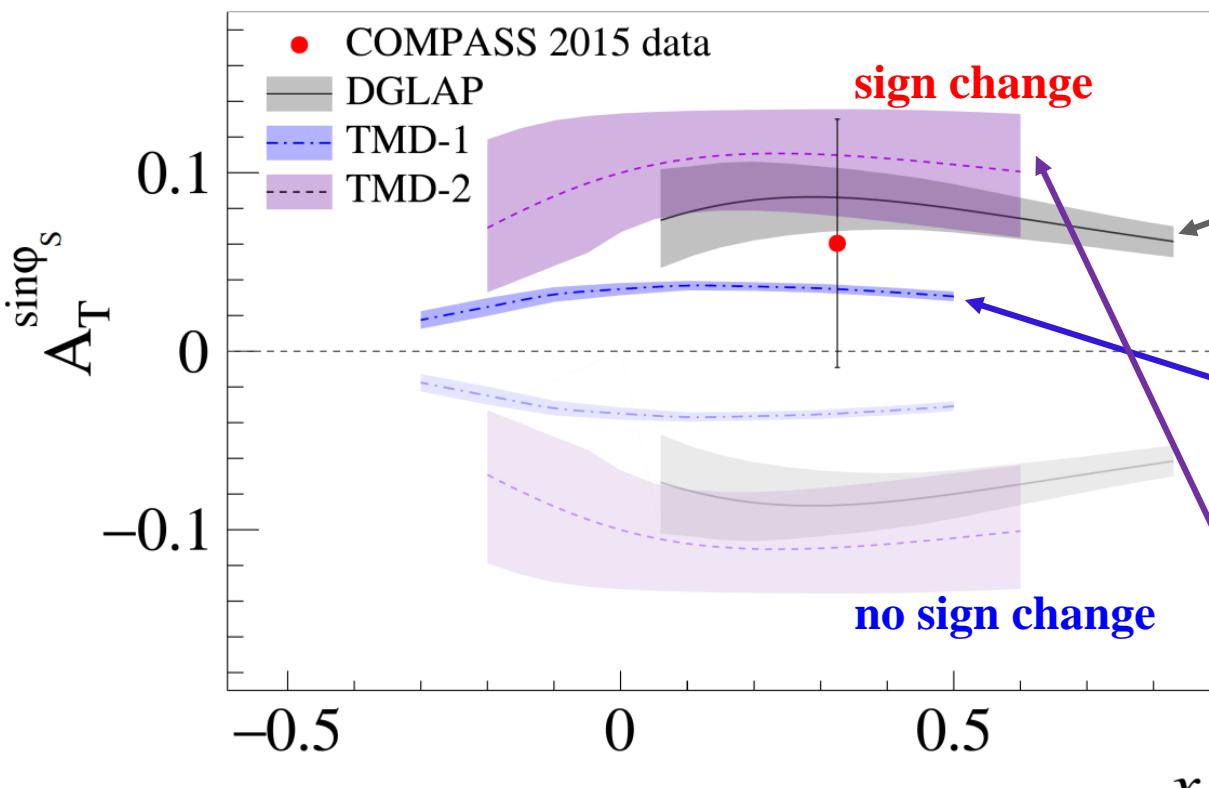
COMPASS, arXiv:1704.00488





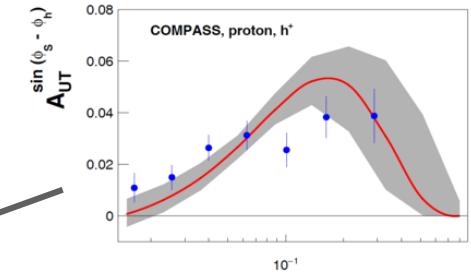
# Sivers Asymmetry in Drell-Yan: Hint of Sign Change!

DGLAP (2016)  
M. Anselmino et al., arXiv:1612.06413

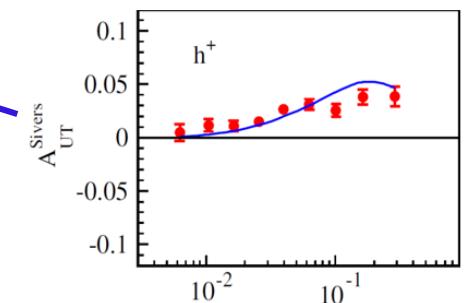


$$A_T^{\sin\phi_s} = 0.060 \pm 0.057(\text{stat.}) \pm 0.040(\text{sys.})$$

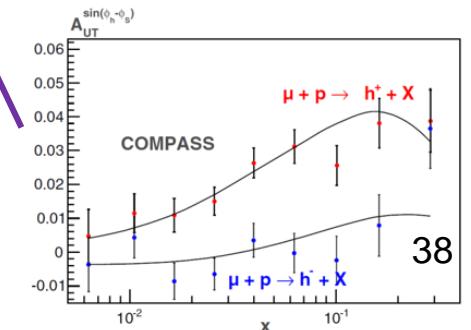
arXiv:1704.00488, to appear in PRL.



TMD-1 (2014)  
M. G. Echevarria et al. PRD89,074013



TMD-2 (2013)  
P. Sun, F. Yuan, PRD88, 114012





# COMPASS-II Programs

- **2014-2018:**
  - Commissioning of polarized Drell-Yan experiment started in mid-October 2014.
  - 2015: Polarized Drell-Yan program.
  - 2016-2017: DVCS program.
  - 2018: Polarized Drell-Yan program (improved statistics errors of Sivers asymmetries are expected).
- **2020-2024 (under planning) :**
  - Polarized  ${}^6\text{Li}$  target: flavor separation of TMD SSAs.
  - Long  $\text{LH}_2$  and nuclei targets: un-polarized pion-induced DY.



# Summary

- In 2015 COMPASS has successfully collected first ever transversely polarized Drell-Yan data:
  - Sivers asymmetry is found to be above zero at about 1 sigma.
  - 1st measurement of the DY Sivers asymmetry is consistent with the predicted change of sign for the Sivers function.
- Other TMDs like transversity and pretzelosity as well as pion BMs are also accessed by TSAs of Drell-Yan process.
- A second year of polarized DY data-taking will take place in 2018. Hopefully it will provide more stringent quantitative test of Sivers universality.



# BACKUP SLIDES



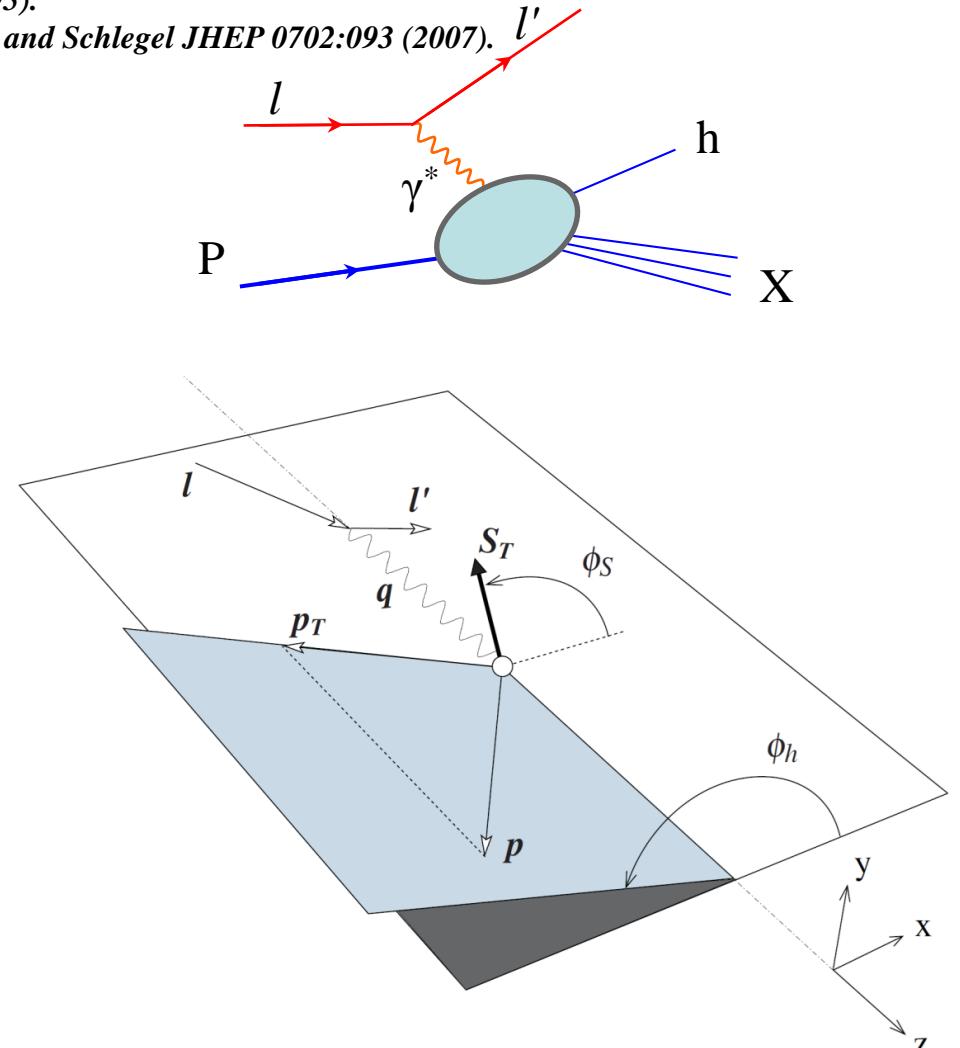
# SIDIS x-section

A.Kotzinian, Nucl. Phys. B441, 234 (1995).

Bacchetta, Diehl, Goeke, Metz, Mulders and Schlegel JHEP 0702:093 (2007).

$$\frac{d\sigma}{dxdydzdp_T^2d\phi_hd\phi_s} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L})$$

$$\left. \begin{aligned} & 1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ & + \lambda \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin\phi_h} \sin\phi_h \\ & + S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h \right] \\ & + S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\phi_h} \cos\phi_h \right] \\ & \times \left[ \begin{aligned} & A_{UT}^{\sin(\phi_h-\phi_s)} \sin(\phi_h - \phi_s) \\ & + \varepsilon A_{UT}^{\sin(\phi_h+\phi_s)} \sin(\phi_h + \phi_s) \\ & + \varepsilon A_{UT}^{\sin(3\phi_h-\phi_s)} \sin(3\phi_h - \phi_s) \\ & + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_s} \sin\phi_s \\ & + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h-\phi_s)} \sin(2\phi_h - \phi_s) \end{aligned} \right] \\ & + S_T \left[ \begin{aligned} & \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h-\phi_s)} \cos(\phi_h - \phi_s) \\ & + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\phi_s} \cos\phi_s \\ & + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h-\phi_s)} \cos(2\phi_h - \phi_s) \end{aligned} \right] \end{aligned} \right]$$



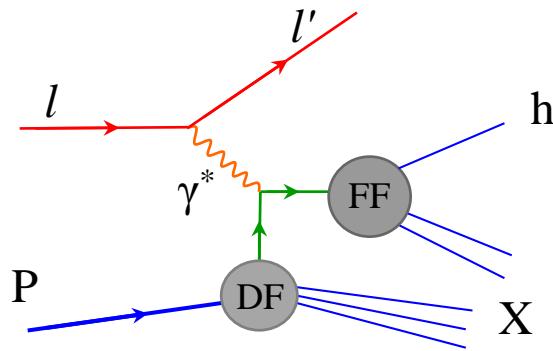
$$A_{U(L),T}^{w(\phi_h, \phi_s)} = \frac{F_{U(L),T}^{w(\phi_h, \phi_s)}}{F_{UU,T} + \varepsilon F_{UU,L}}; \quad \varepsilon = \frac{1-y - \frac{1}{4}\gamma^2 y^2}{1-y + \frac{1}{2}y^2 + \frac{1}{4}\gamma^2 y^2}, \quad \gamma = \frac{2Mx}{Q}$$



# SIDIS x-section and TMDs at twist-2

$$\frac{d\sigma}{dxdydzdp_T^2d\phi_h d\phi_s} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L})$$

$$\left\{ \begin{array}{l} 1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ + \lambda \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin\phi_h} \sin\phi_h \\ + S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h \right] \\ + S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\phi_h} \cos\phi_h \right] \\ \times \left\{ \begin{array}{l} + S_T \left[ A_{UT}^{\sin(\phi_h - \phi_s)} \sin(\phi_h - \phi_s) \right. \\ + \varepsilon A_{UT}^{\sin(\phi_h + \phi_s)} \sin(\phi_h + \phi_s) \\ + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_s)} \sin(3\phi_h - \phi_s) \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_s} \sin\phi_s \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h - \phi_s)} \sin(2\phi_h - \phi_s) \\ + S_T \lambda \left[ \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_s)} \cos(\phi_h - \phi_s) \right. \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\phi_s} \cos\phi_s \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h - \phi_s)} \cos(2\phi_h - \phi_s) \end{array} \right] \end{array} \right\}$$



| Quark<br>Nucleon | U  | L  | T  |
|------------------|--|--|--|
| U                | $f_1^q(x, \mathbf{k}_T^2)$<br>number density   |  | $h_1^{q\perp}(x, \mathbf{k}_T^2)$<br>Boer-Mulders    |
| L                |  | $g_1^q(x, \mathbf{k}_T^2)$<br>helicity                                   | $h_{1L}^{q\perp}(x, \mathbf{k}_T^2)$<br>worm-gear L  |
| T                | $f_{1T}^{q\perp}(x, \mathbf{k}_T^2)$<br>Sivers | $g_{1T}^{q\perp}(x, \mathbf{k}_T^2)$<br>Kotzinian-Mulders<br>worm-gear T | $h_{1T}^{q\perp}(x, \mathbf{k}_T^2)$<br>pretzelosity |

+ two FFs:  $D_{1q}^h(z, P_\perp^2)$  and  $H_{1q}^{\perp h}(z, P_\perp^2)$



# SIDIS x-section: transverse spin dependent part

$$\frac{d\sigma}{dxdydzdp_T^2d\phi_hd\phi_s} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots \right.$$

$$+ S_T \left[ \begin{array}{l} A_{UT}^{\sin(\phi_h-\phi_s)} \sin(\phi_h - \phi_s) \\ + \varepsilon A_{UT}^{\sin(\phi_h+\phi_s)} \sin(\phi_h + \phi_s) \\ + \varepsilon A_{UT}^{\sin(3\phi_h-\phi_s)} \sin(3\phi_h - \phi_s) \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_s} \sin\phi_s \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h-\phi_s)} \sin(2\phi_h - \phi_s) \end{array} \right] \\ + S_T \lambda \left[ \begin{array}{l} \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h-\phi_s)} \cos(\phi_h - \phi_s) \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\phi_s} \cos\phi_s \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h-\phi_s)} \cos(2\phi_h - \phi_s) \end{array} \right]$$

$$A_{UT}^{\sin(\phi_h-\phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

$$A_{UT}^{\sin(\phi_h+\phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin(3\phi_h-\phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin(\phi_s)} \stackrel{WW}{\propto} Q^{-1} (h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots)$$

$$A_{UT}^{\sin(2\phi_h-\phi_s)} \stackrel{WW}{\propto} Q^{-1} (h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots)$$

$$A_{LT}^{\cos(\phi_h-\phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$$

$$A_{LT}^{\cos(\phi_s)} \stackrel{WW}{\propto} Q^{-1} (g_{1T}^q \otimes D_{1q}^h + \dots)$$

$$A_{LT}^{\cos(2\phi_h-\phi_s)} \stackrel{WW}{\propto} Q^{-1} (g_{1T}^q \otimes D_{1q}^h + \dots)$$

Eight transverse-spin-dependent azimuthal asymmetries (TSA) appear in SIDIS x-section

- Four “twist-2” TSAs  
(Sivers, Collins, pretzelosity, Kotzinian-Mulders)
- Four “higher-twist”

Twist-2

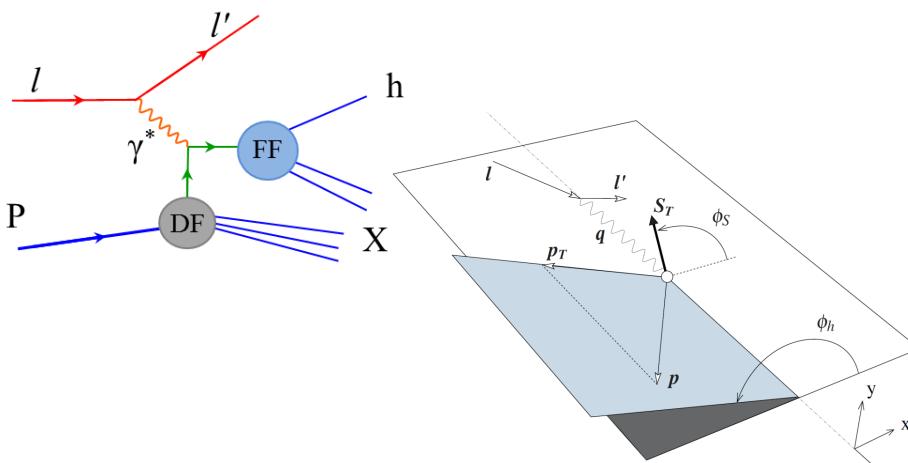
Twist-3



# SIDIS and single-polarized DY x-sections

$$\frac{d\sigma}{dxdydzdp_T^2d\phi_h d\phi_s} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots \right\}$$

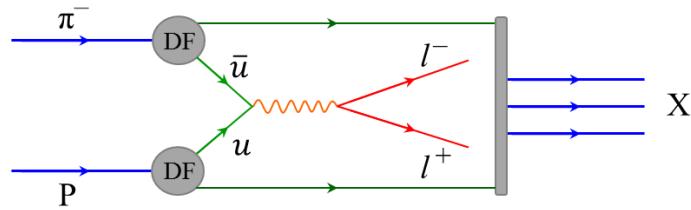
$$+ S_T \left[ \begin{array}{l} A_{UT}^{\sin(\phi_h - \phi_s)} \sin(\phi_h - \phi_s) \\ + \varepsilon A_{UT}^{\sin(\phi_h + \phi_s)} \sin(\phi_h + \phi_s) \\ + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_s)} \sin(3\phi_h - \phi_s) \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_s} \sin\phi_s \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h - \phi_s)} \sin(2\phi_h - \phi_s) \end{array} \right] \\ + S_T \lambda \left[ \begin{array}{l} \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_s)} \cos(\phi_h - \phi_s) \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\phi_s} \cos\phi_s \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h - \phi_s)} \cos(2\phi_h - \phi_s) \end{array} \right]$$



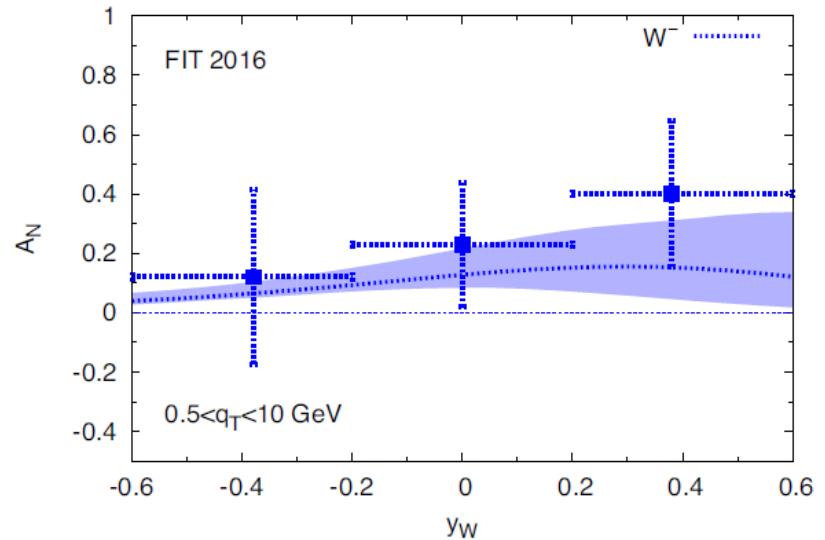
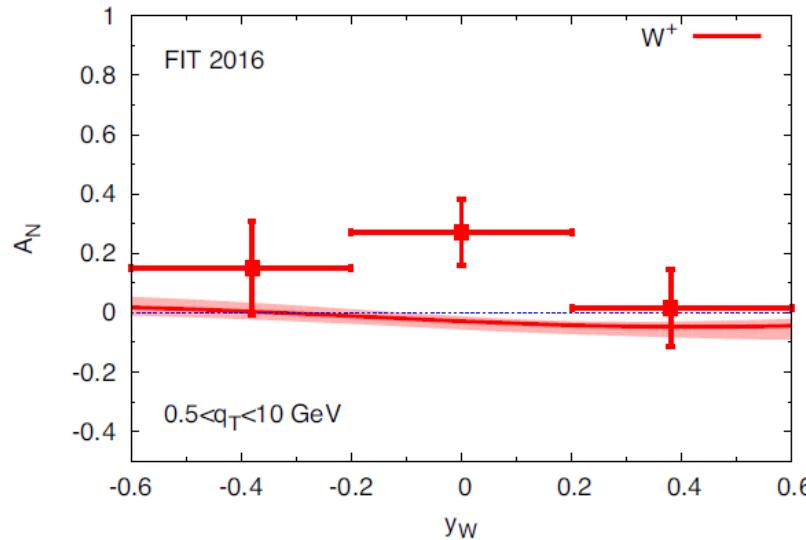
**SIDIS**  $\frac{d\sigma}{d\Omega} \propto (F_U^1 + F_U^2)$

**DY**

$$\times \left\{ \begin{array}{l} 1 + A_U^1 \cos^2 \theta_{CS} \\ + \sin 2\theta_{CS} A_U^{\cos\varphi_{CS}} \cos\varphi_{CS} + \sin^2 \theta_{CS} A_U^{\cos 2\varphi_{CS}} \cos 2\varphi_{CS} \\ + S_L \left[ \sin 2\theta_{CS} A_L^{\sin\varphi_{CS}} \sin\varphi_{CS} + \sin^2 \theta_{CS} A_L^{\sin 2\varphi_{CS}} \sin 2\varphi_{CS} \right] \\ \times \left[ \begin{array}{l} \left( A_T^{\sin\varphi_s} + \cos^2 \theta_{CS} \tilde{A}_T^{\sin\varphi_s} \right) \sin\varphi_s \\ + \sin^2 \theta_{CS} \left( A_T^{\sin(2\varphi_{CS} - \varphi_s)} \sin(2\varphi_{CS} - \varphi_s) \right. \\ \left. + A_T^{\sin(2\varphi_{CS} + \varphi_s)} \sin(2\varphi_{CS} + \varphi_s) \right) \\ + \sin 2\theta_{CS} \left( A_T^{\sin(\varphi_{CS} - \varphi_s)} \sin(\varphi_{CS} - \varphi_s) \right. \\ \left. + A_T^{\sin(\varphi_{CS} + \varphi_s)} \sin(\varphi_{CS} + \varphi_s) \right) \end{array} \right] \end{array} \right\}$$



# Predicted Sivers asymmetry $A_N$ , assuming a sign change of the SIDIS Sivers functions



Anselmino et al., , JHEP04 (2017) 046 [arXiv:1612.06413]

Signals of Sivers functions in  $W$  production.  
Hints of (non)universality.