

# Measurement of the Charged-Pion Polarisability at COMPASS

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Physik-Department, TU München

*COMPASS collaboration*



EP Seminar  
May 12, 2015



Bundesministerium  
für Bildung  
und Forschung



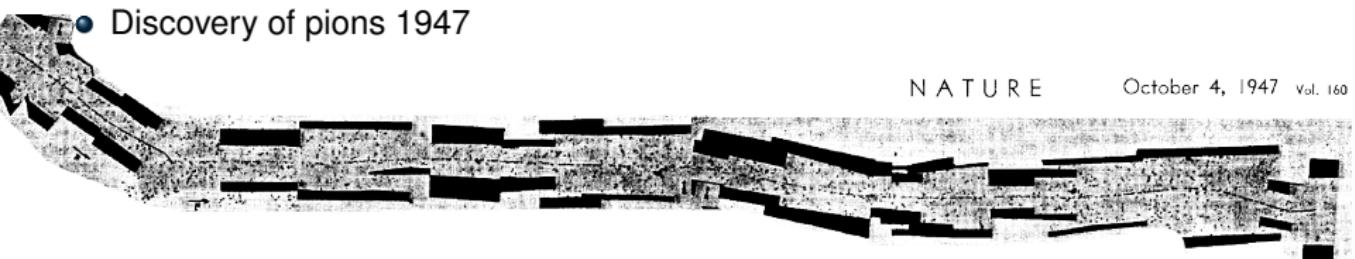
# Short story of the pion

- Yukawa 1935: hypothesis of  $\sim 100$  MeV massive exchange particle “ $\mu$ ” for the strong interaction between protons and neutrons
- Discovery of muons 1936



# Short story of the pion

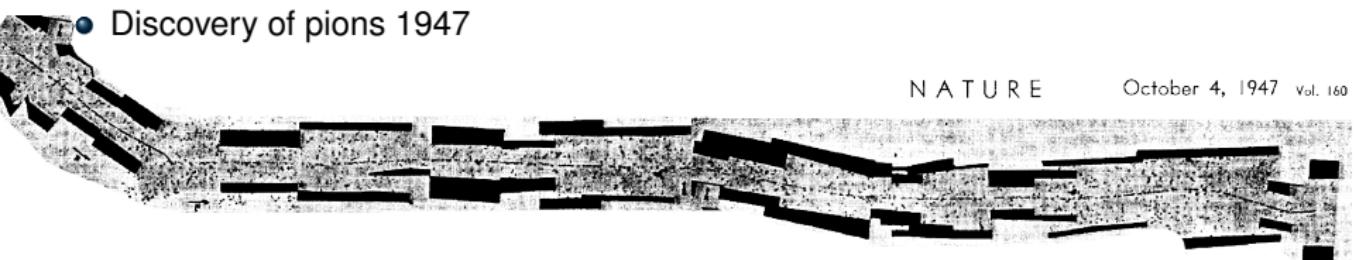
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- Discovery of pions 1947





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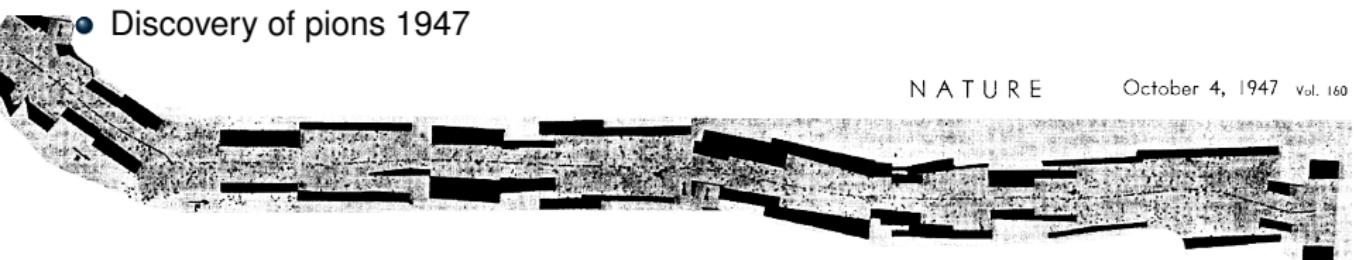


- 1958: decay  $\pi^+ \rightarrow \mu^+ \nu_\mu$  dominant, small branching  $\pi^+ \rightarrow e^+ \nu_e$   
(CERN CycloSynchrotron)  $\Rightarrow$   $V - A$  theory of weak interaction
- 1961: Spin-1 mesonic excitation of the pion ( $\rho$ -resonance)
- 1964: quark hypothesis
- 1966: pion scattering lengths
- :



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- 1964: quark hypothesis
- 1966: pion scattering lengths
- $\vdots$
- 1982: first data on the pion polarisability

## Measurement of the Charged-Pion Polarizability

C. Adolph,<sup>8</sup> R. Akhunzyanov,<sup>7</sup> M. G. Alexeev,<sup>27</sup> G. D. Alexeev,<sup>7</sup> A. Amoroso,<sup>27,29</sup> V. Andrieux,<sup>22</sup> V. Anosov,<sup>7</sup>  
 ... [213 authors]

(COMPASS Collaboration)

(Received 2 June 2014; revised manuscript received 24 December 2014; published 10 February 2015)

The COMPASS collaboration at CERN has investigated pion Compton scattering,  $\pi^-\gamma \rightarrow \pi^-\gamma$ , at center-of-mass energy below 3.5 pion masses. The process is embedded in the reaction  $\pi^-Ni \rightarrow \pi^-\gamma Ni$ , which is initiated by 190 GeV pions impinging on a nickel target. The exchange of quasireal photons is selected by isolating the sharp Coulomb peak observed at smallest momentum transfers,  $Q^2 < 0.0015 \text{ (GeV}/c)^2$ . From a sample of 63 000 events, the pion electric polarizability is determined to be  $\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3$  under the assumption  $\alpha_\pi = -\beta_\pi$ , which relates the electric and magnetic dipole polarizabilities. It is the most precise measurement of this fundamental low-energy parameter of strong

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# CERN experiment brings precision to a cornerstone of particle physics

11 Feb 2015

Geneva, 11 February 2015. In a paper published yesterday in the journal *Physical Review Letters*, the COMPASS experiment at CERN<sup>1</sup> reports a key measurement on the strong interaction. The strong interaction binds quarks into protons and neutrons, and protons and neutrons into the nuclei of all the elements from which matter is built. Inside those nuclei, particles called pions made up of a quark and an antiquark mediate the interaction. Strong interaction theory makes a precise prediction on the polarisability of

## LHC RESTART

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# Press echo in spring 2015

**CERN COURIER**

INTERNATIONAL JOURNAL OF HIGH-ENERGY PHYSICS

VOLUME 55 NUMBER 2 MARCH 2015

**News**

**QCD PHYSICS**

**COMPASS measures the pion polarizability**

The COMPASS experiment at CERN has made the first precise measurement of the polarizability of the pion – the lightest composite particle built from quarks. The result confirms the expectation from the low-energy expansion of QCD – the quantum field theory of the strong interaction between quarks – but is at variance with the previously published values, which overestimated the pion polarizability by a factor of two.

Every composite system made from charged particles can be polarized by an external electromagnetic field, which acts to separate positive and negative charges. The size of this charge separation – the induced dipole moment – is related to the external field by the polarizability. As a measure of the response of a complex system to an external force, polarizability is directly related to the system's stiffness against deformability, and hence the binding force between the constituents.

The pion, made up of a quark and an antiquark, is the lightest object bound by the strong force and has a size of about  $0.6 \times 10^{-16}$  m (0.6 fm). So to observe a measurable effect, the particle must be subjected to electric fields in the order of 100 kV across its diameter – that is, about  $10^9$  V/cm. To achieve this, the COMPASS experiment made use of the electric field around nuclei. To high-energy pions this amounts to a source of (almost) real scatter.

Such pion–photon Compton scattering, also known as the Primakoff mechanism, was explored in the early 1990s in an experiment at Serpukhov, but the small data sample led to only an impression for the polarizability of  $6.8 \pm 1.4$  (stat.)  $\pm 2.6$  (syst.)  $\times 10^{-4}$  fm $^3$ , where the systematic uncertainty was underestimated, presumably.

COMPASS has now achieved a modern Primakoff experiment, using a 190 GeV pion beam from the Super Proton Synchrotron at CERN directed at a nickel target. Importantly, COMPASS was also able to use muons, which are point-like and hence non-deformable, to calibrate the experiment. The Compton  $\pi^+ \rightarrow \pi^+$  scattering is extracted from the reaction  $\pi^- N \rightarrow \pi^+ N\bar{N}$  by selecting events from the Coulomb peak at small momentum transfer. From the analysis of a sample of 63,000 events, the collaboration obtained a value of the pion electric polarizability of  $2.08 \pm 0.41$  (stat.)  $\pm 0.73$  (syst.)  $\times 10^{-4}$  fm $^3$  – that is, about  $2 \times 10^{-4}$  of the pion's volume. This value is in good agreement with theoretical calculations in low-energy QCD, therefore solving a long-standing discrepancy between those calculations and previous experimental efforts to determine the polarizability.

Although this measurement is the first to allow a self-calibration, the accuracy is still below the estimated uncertainty of the calculations. With more data already recorded, the COMPASS collaboration expects to improve on this result by a significant factor in the near future, and thereby probe further for a benchmark of non-perturbative QCD.

**Further reading**  
 COMPASS Collaboration 2015 arXiv:1405.6377 [two-ref], to be published in Phys. Rev. Lett.

**Sommaire en français**

COMPASS mesure la polarisabilité du pion  
 L'Année internationale de la lune  
 Remise des clefs pour l'exploitation 2 du  
 Techniques de détection pour de futurs







# Press echo in spring 2015



Technische Universität München

Excellence Cluster Universe 

ING ÖFFENTLICHKEITSARBEIT SCHULPROGRAMM MIAPP C2PAP



**PRAZISIONSMESSUNG ZUR STARKEN WECHSELWIRKUNG**

Pioniern genannte Kernteilchen tragen wesentlich zur so genannten starken Wechselwirkung bei. Sie ist die Kraft, die Atomkerne zusammenhält und für die Masse der uns umgebenden Materie verantwortlich ist. Erstmals ist es Physikern nun gelungen, die Verformbarkeit von Pionen exakt zu bestimmen. Das Ergebnis, zu dem Physiker der Technischen Universität München (TUM) maßgeblich beigetragen haben, stimmt gut mit den theoretischen Vorhersagen überein und revidiert frühere Messungen, deren Ergebnisse nicht mit dem Standardmodell der Physik vereinbar waren.

CERN experiment brings precision to cornerstone of particle physics

TUM Technische Universität München

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- FORSCHUNG
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**exakte Messung der Polarisierbarkeit von Pionen stützt Standardmodell**

**Präzisionsmessung zur starken Wechselwirkung**

10.02.2015, Forschung

Das in der TUM entwickelte Detektormodul – Foto: TUM

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LHC Session 2: New frontiers in physics

# Press echo in spring 2015



Featured Research

CERN experiment brings precision to a cornerstone of particle physics

Date: February 11, 2015

Source:

CERN

The COMPASS experiment at CERN reports a key measurement on pion-nucleus interaction. The strong interaction turns protons into pions and neutrons, and protons and neutrons into nucleons. These nucleons consist of a quark and an antiquark, making up the pion. The strong interaction theory makes predictions on the shape of a pion. The pion's polarisability has baffled scientists since the 1990s, while the test measurements seem to be at odds with the theory. Now results are in close agreement with theory.

# Focus.it

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FOTO

## L'interazione forte dei quark ha meno segreti

L'esperimento COMPASS al CERN fornisce una misura chiave dell'interazione forte.



NO OFFERTO A RISETTO DA IBERI SUL PROGRAMMA MIAPP CEA  
Lo spettrometro dell'esperimento COMPASS. È lungo 60 metri e il suo interno vengono sparati raggi di particelle subatomiche ad alta intensità. | cm



J. M. Friedrich — Pion Polarizability with COMPASS

7/42

# Neue Zürcher Zeitung

Pionen-Experiment am Cern

PHYSIK UND CHEMIE

## Da schwabbeln nichts

11.2.2015, 17:08 Uhr

rtz. Wieder hat ein Experiment die theoretischen Vorhersagen des Standardmodells der Teilchenphysik bestätigt. Diesmal massen die Forschenden die Verformbarkeit sogenannter Pionen. Diese gibt Aufschluss darüber, wie stark die Bindungskraft zwischen den Elementarteilchen im Inneren von Atomkernen ist.

AVENIR  
Fondamental  
À LA UNE

Le pion se déforme moins que prévu

Par Jean-Pierre Lederre

Sur l'heure des résultats

Peter Hirsch

Sur les traces de la physique



## Press echo in spring 2015

The image is a collage of news snippets from various international media outlets, all centered around the COMPASS experiment at CERN. It includes:

- A banner for "ScienceDaily" with the headline "CERN experiment brings precision to a cornerstone of particle physics".
- A snippet from "Neue Zürcher Zeitung" with the headline "Da schwabb" (in Russian).
- A snippet from "Wydział Fizyki Uniwersytetu Warszawskiego" (Faculty of Physics, University of Warsaw) with the headline "Wydział Fizyki: pierwszy precyzyjny pomiar w CERN z udziałem fizyków warszawskich".
- A snippet from "I'NAUKA I ZHIZNY" (Science and Life) with the headline "Как COMPASS пион поляризовал".
- A snippet from "L'i" (L'esp) with the headline "19 февраля 2015 Как COMPASS пион поляризовал".
- A snippet from "Irfu" (Institut de Recherche en Physique Nucléaire et Hautes Energies) with the headline "Une expérience du CERN affine une mesure essentielle pour décrire l'interaction forte".

The collage also features several logos of scientific institutions like CERN, TUM, and IMU.



# Press echo in spring 2015

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## CERN Physicists Measure Polarizability of Pion

Feb 16, 2015 by Sci-News.com

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Physics

## Tagged as

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 Strong interaction

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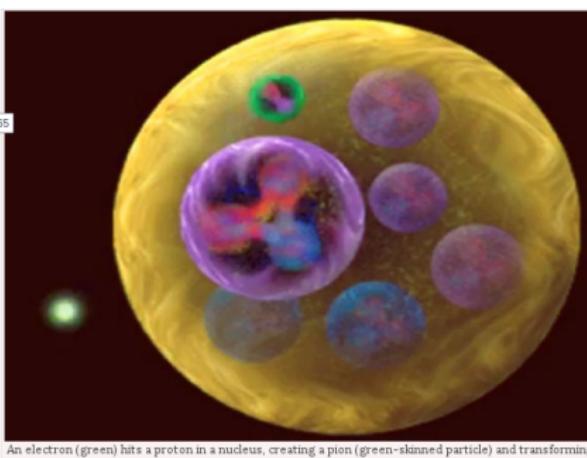


Physicists Create New Form of Ice: Square Ice



Stars May Generate Sound

Scientists from CERN's COMPASS collaboration have made the most precise measurement ever of the polarizability of pion – the fundamental low-energy parameter of strong interaction.



Everything we see in the Universe is made up of fundamental particles called

## LATEST NEWS


 New Method Precisely Measures Rotation Period of Saturn  
 Mar 28, 2015 | Astronomy

 Physicists Create New Form of ice: Square Ice  
 Mar 27, 2015 | Physics

 Colliding Galaxy Clusters Offer Clues to Dark Matter  
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 Astronomers Discover Two Extremely Old Stars in Sculptor Dwarf Galaxy  
 Mar 25, 2015 | Astronomy

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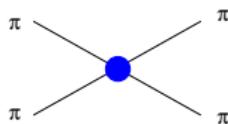
# How to understand quark-gluon dynamics?



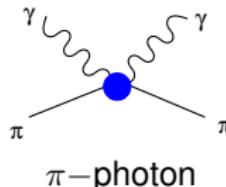
complicated system of  
interacting quarks and gluons

ChPT  
 $\xrightarrow{}$

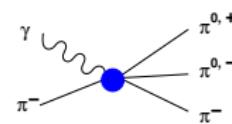
effective degrees of freedom  
at low energy: mass, charge,  
spin, effective (self-)coupling



$\pi$  only



$\pi$ -photon

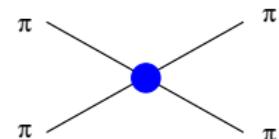


$\pi - \pi - \text{photon}$



- pion scattering lengths: 2-loop predictions

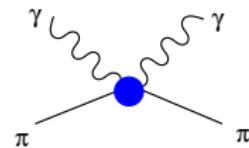
- $a_0^0 m_\pi = 0.220 \pm 0.005$  confirmed by E865 in  $K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$
- $(a_0^0 - a_0^2) m_\pi = 0.264 \pm 0.006$  confirmed by NA48 in  $0.268 \pm 0.010 \quad K^+ \rightarrow \pi^+ \pi^0 \pi^0$



- pion polarisability: electric  $\alpha_\pi$ , magnetic  $\beta_\pi$

- leading structure-dependent contribution to Compton scattering
- ChPT prediction obtained by the relation to  $\pi^+ \rightarrow e^+ \nu e \gamma$  [Gasser, Ivanov, Sainio, Nucl. Phys. B745, 2006]

[PIBETA, M. Bychkov et al., PRL 103, 051802, 2009]

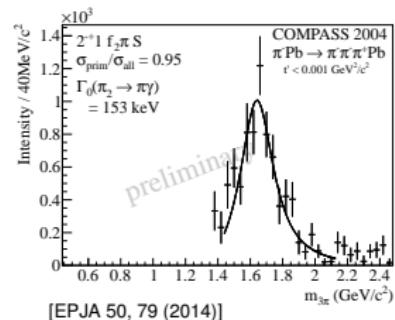
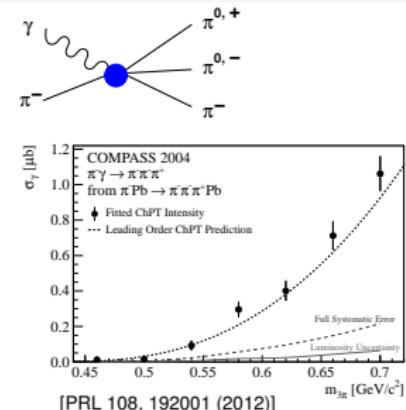
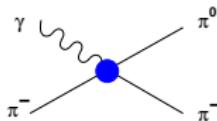


- ChPT prediction contradicts the experimental findings (prior to this analysis)



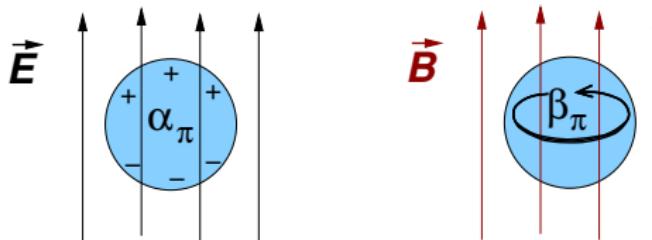
# More pion-photon reactions

- Pion scattering including a real photon
  - Leading-order prediction from ChPT pion scattering lengths + coupled photon
  - chiral loop contribution theory prediction available
- Radiative widths of meson resonances
- Chiral anomaly  $F_{3\pi}$ 
  - established on 10% level
  - further development: inclusion of the  $\rho$  resonance, theoretical work by Kubis, Hoferichter, Sakkas PRD86(2012)116009





# ChPT prediction for the pion polarisability



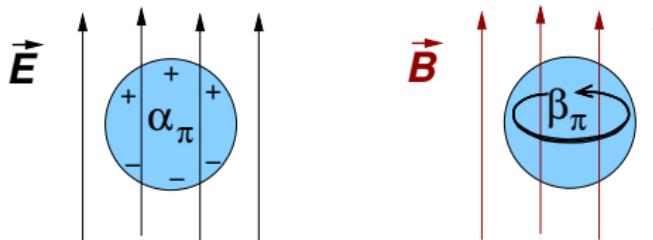
pion polarisabilities  $\alpha_\pi, \beta_\pi$  in units of  $10^{-4} \text{ fm}^3$

ChPT (2-loop) prediction:

$\alpha_\pi - \beta_\pi$	$=$	$5.7 \pm 1.0$
$\alpha_\pi + \beta_\pi$	$=$	$0.16 \pm 0.1$

experiments for  $\alpha_\pi - \beta_\pi$  lie in the range  $4 \dots 14$

( $\alpha_\pi + \beta_\pi = 0$  assumed)



pion polarisabilities  $\alpha_\pi, \beta_\pi$  in units of  $10^{-4} \text{ fm}^3$

ChPT (2-loop) prediction:

$$\begin{aligned}\alpha_\pi &= 2.93 \pm 0.5 \\ \beta_\pi &= -2.77 \pm 0.5\end{aligned}$$

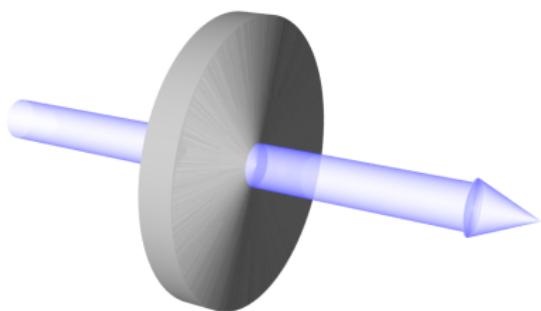
experiments for  $\alpha_\pi$  lie in the range 2 ... 7

( $\alpha_\pi + \beta_\pi = 0$  assumed)



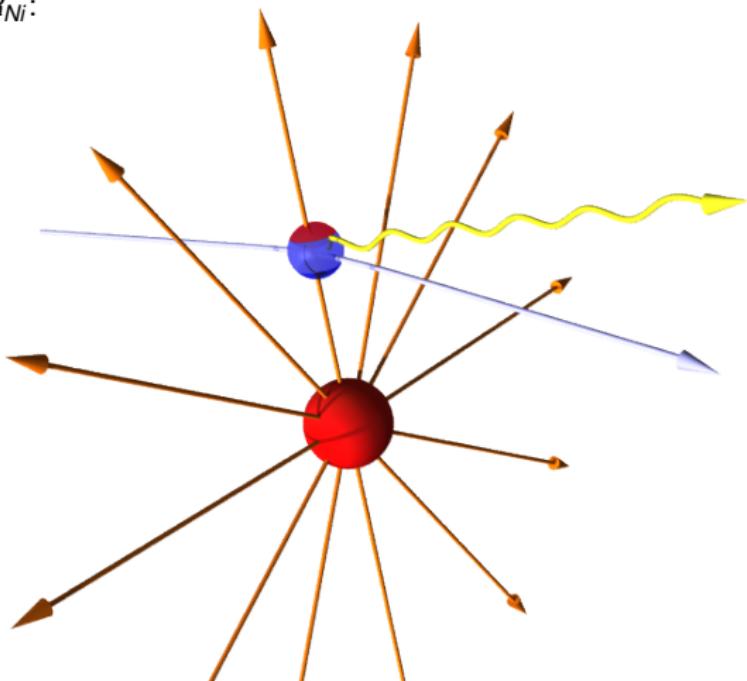
# Principle of the COMPASS measurement

- high-energetic pion beam on 4mm nickel disk
- observe scattered pions in coincidence with produced hard photons
- study of cross-section shape





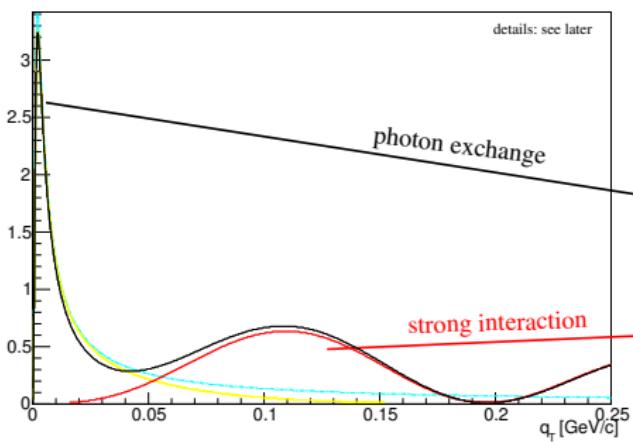
- Charged pions traverse the nuclear **electric field**
  - typical field strength at  $d = 5R_{Ni}$ :  
 $E \approx 300 \text{ kV/fm}$
- Bremsstrahlung process:
  - particles scatter off **equivalent photons**
  - tiny momentum transfer  
 $Q^2 \approx 10^{-5} \text{ GeV}^2/c^2$
  - pion/muon (quasi-)real Compton scattering
- Polarisability contribution
  - Compton cross-section typically diminished
  - equivalent charge separation  
 $\approx 10^{-5} \text{ fm} \cdot e$



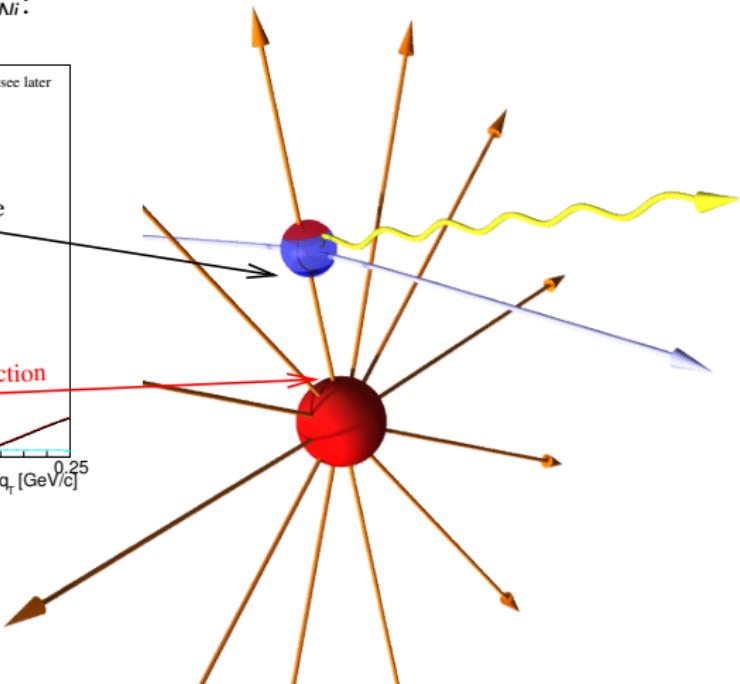


# Polarisability effect in Primakoff technique

- Charged pions traverse the nuclear **electric field**
  - typical field strength at  $d = 5R_{Ni}$ :



- equivalent charge separation  
 $\approx 10^{-5} \text{ fm} \cdot e$





# Pion Compton Scattering



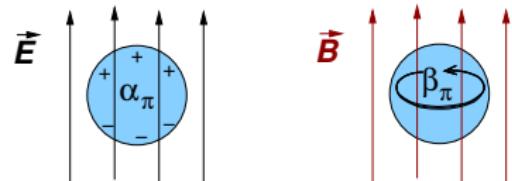
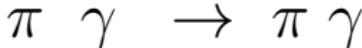
- Two kinematic variables, in CM: total energy  $\sqrt{s}$ , scattering angle  $\theta_{cm}$

$$\frac{d\sigma_{\pi\gamma}}{d\Omega_{cm}} = \frac{\alpha^2(s^2 z_+^2 + m_\pi^4 z_-^2)}{s(sz_+ + m_\pi^2 z_-)^2} - \frac{\alpha m_\pi^3 (s - m_\pi^2)^2}{4s^2(sz_+ + m_\pi^2 z_-)} \cdot \mathcal{P}$$

$$\mathcal{P} = z_-^2(\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+^2(\alpha_\pi + \beta_\pi) - \frac{(s - m_\pi^2)^2}{24s} z_-^3(\alpha_2 - \beta_2)$$

$$z_\pm = 1 \pm \cos \theta_{cm}$$

# Pion Compton Scattering



- Two kinematic variables, in CM: total energy  $\sqrt{s}$ , scattering angle  $\theta_{cm}$

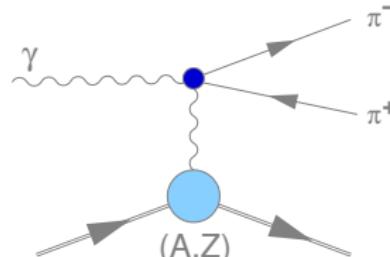
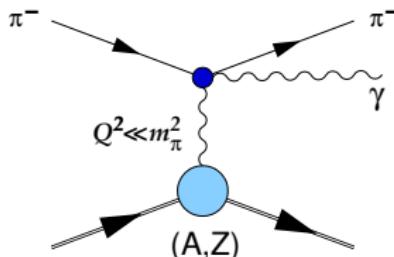
$$\frac{d\sigma_{\pi\gamma}}{d\Omega_{cm}} = \frac{\alpha^2(s^2 z_+^2 + m_\pi^4 z_-^2)}{s(s z_+ + m_\pi^2 z_-)^2} - \frac{\alpha m_\pi^3 (s - m_\pi^2)^2}{4s^2(s z_+ + m_\pi^2 z_-)} \cdot \mathcal{P}$$

$$\mathcal{P} = z_-^2(\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+^2(\alpha_\pi + \beta_\pi) - \frac{(s - m_\pi^2)^2}{24s} z_-^3(\alpha_2 - \beta_2)$$

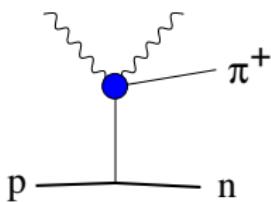
$$z_\pm = 1 \pm \cos \theta_{cm}$$



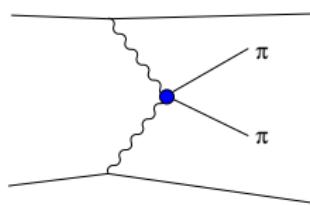
## Pion Compton scattering: embedding the process



Primakoff processes



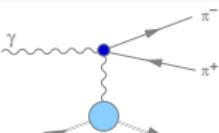
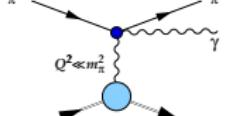
Radiative pion photoproduction



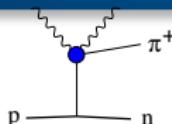
Photon-Photon fusion



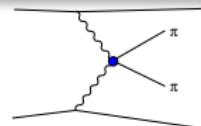
# Pion polarisability: world data before COMPASS



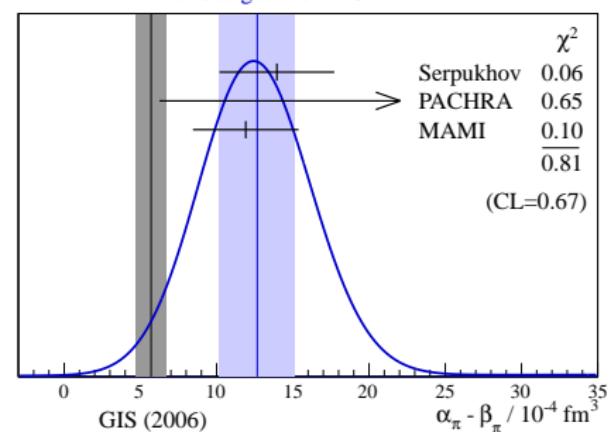
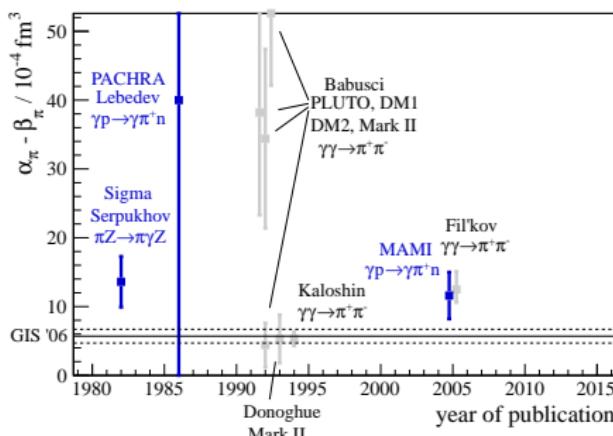
Primakoff processes



Radiative pion photoproduction



Photon-Photon fusion



GIS'06: ChPT prediction, Gasser, Ivanov, Sainio, NPB745 (2006), plots: T. Nagel, PhD

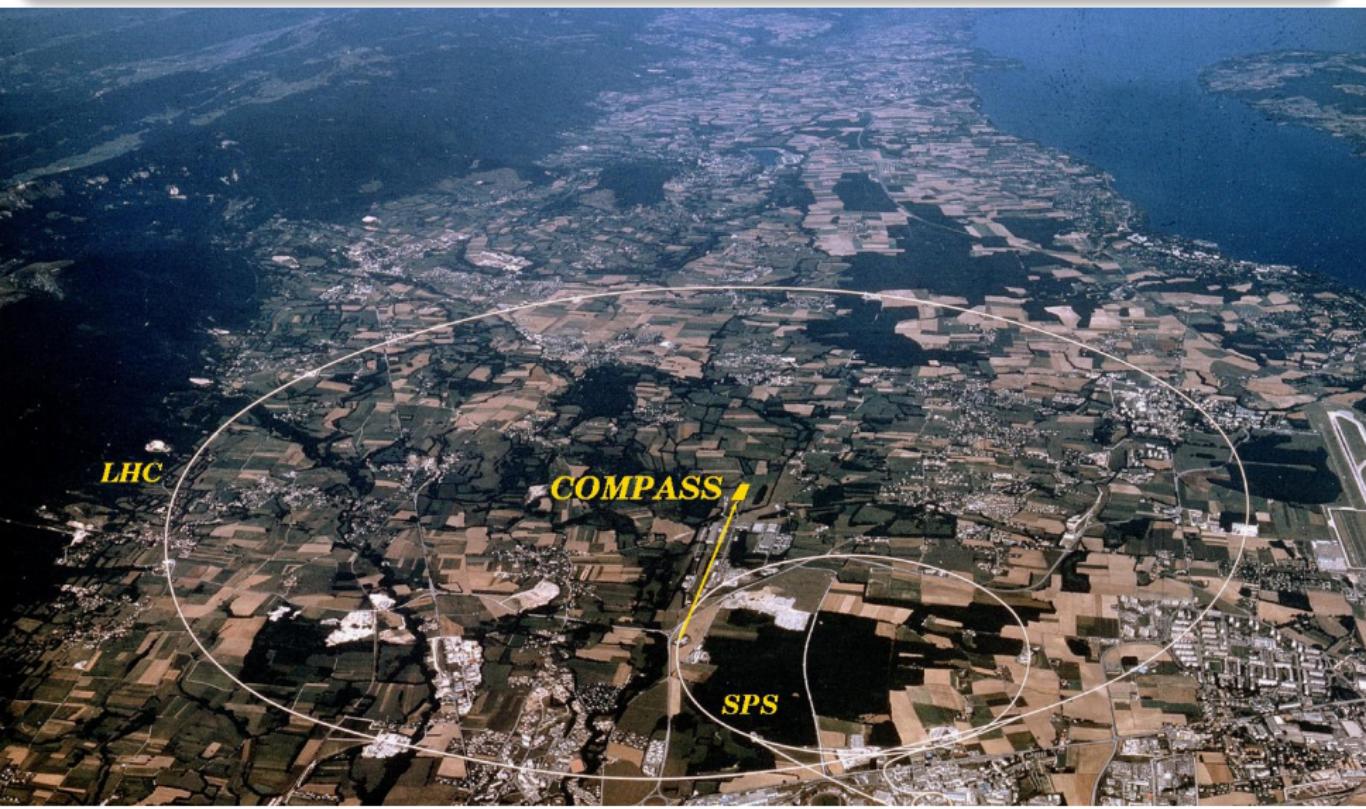
Fil'kov analysis objected by Pasquini, Drechsel, Scherer PRC81, 029802 (2010)



# COCommon Muon and Proton Apparatus for Structure and Spectroscopy



Technische Universität München

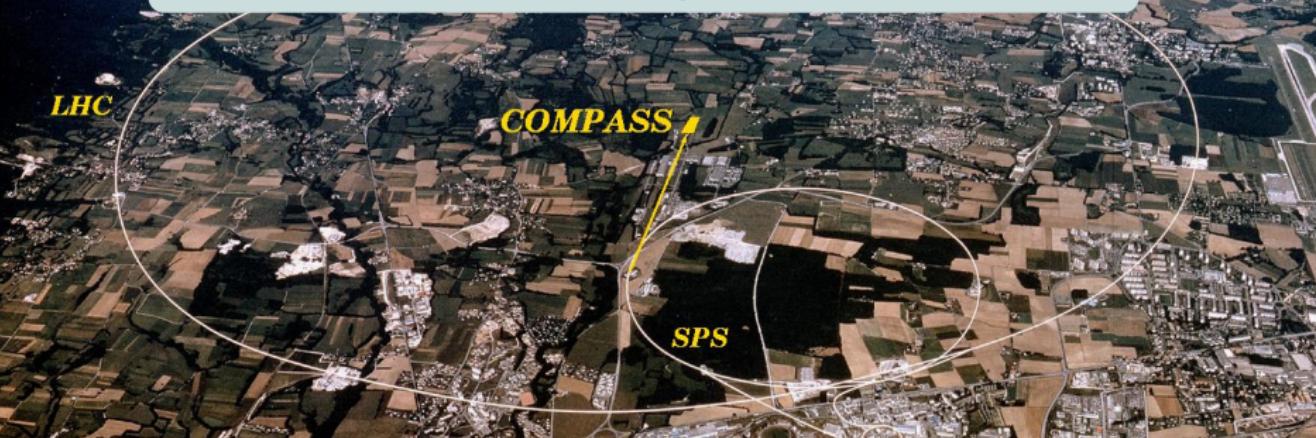




# COCommon Muon and Proton Apparatus for Structure and Spectroscopy

CERN SPS: protons  $\sim 400$  GeV (5 – 10 sec spills)

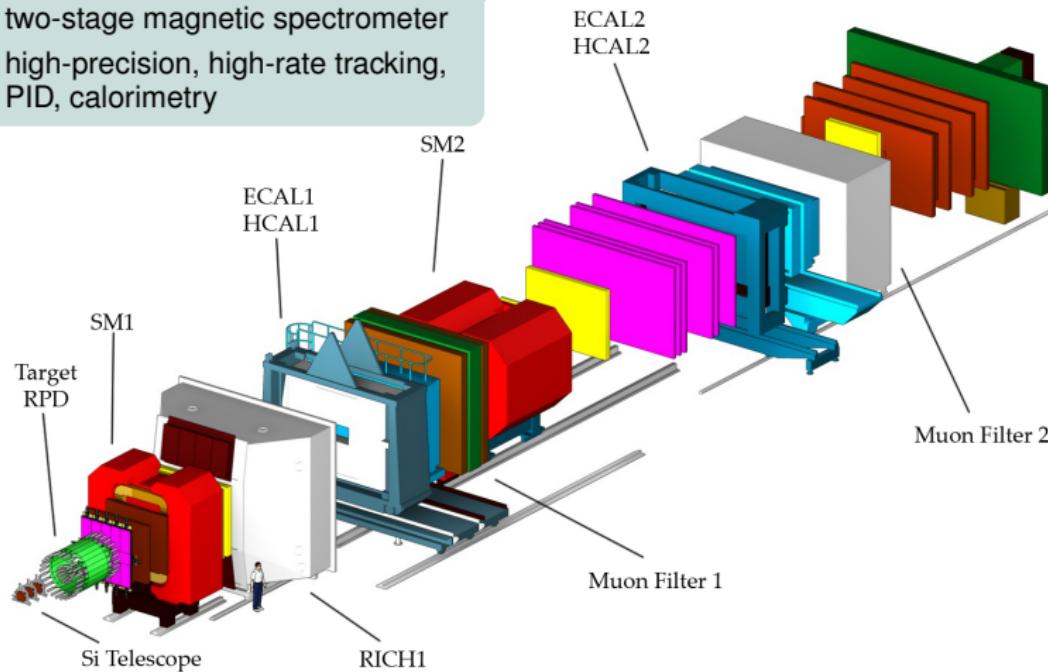
- secondary  $\pi, K, (\bar{p})$ : up to  $2 \cdot 10^7$ /s (typ.  $5 \cdot 10^6$ /s)  
Nov. 2004, 2008-09, 2012:  
hadron spec. & Primakoff reactions
- tertiary muons:  $4 \cdot 10^7$  / s  
2002-04, 2006-07, 2010-11: spin structure of the nucleon



## Experimental Setup

## Fixed-target experiment

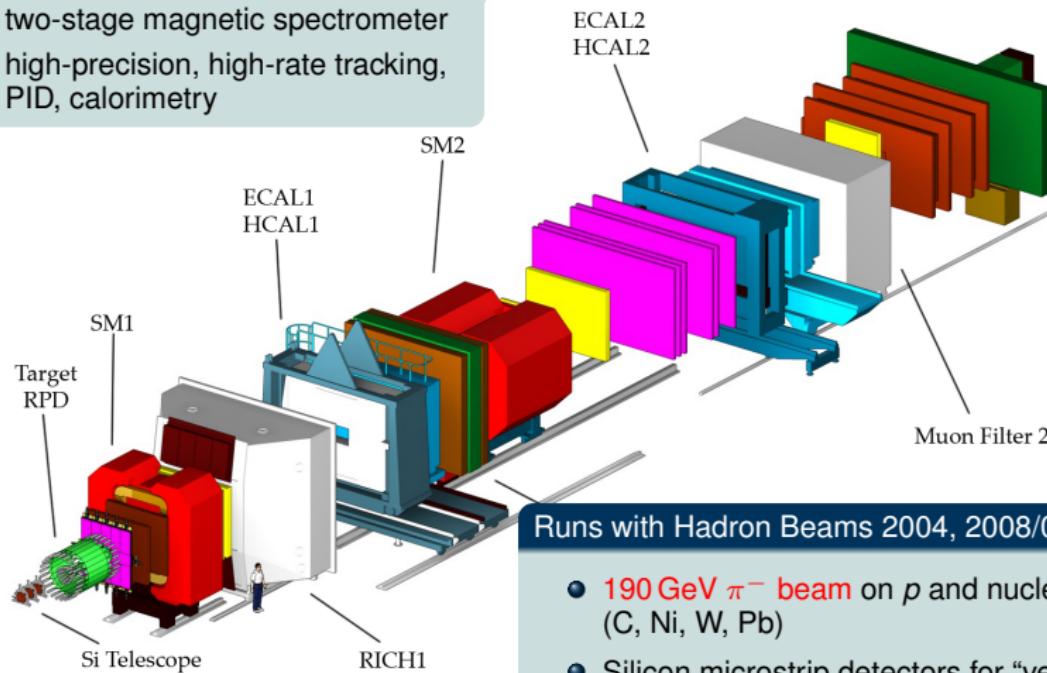
- two-stage magnetic spectrometer
- high-precision, high-rate tracking, PID, calorimetry



## Experimental Setup

## Fixed-target experiment

- two-stage magnetic spectrometer
- high-precision, high-rate tracking, PID, calorimetry

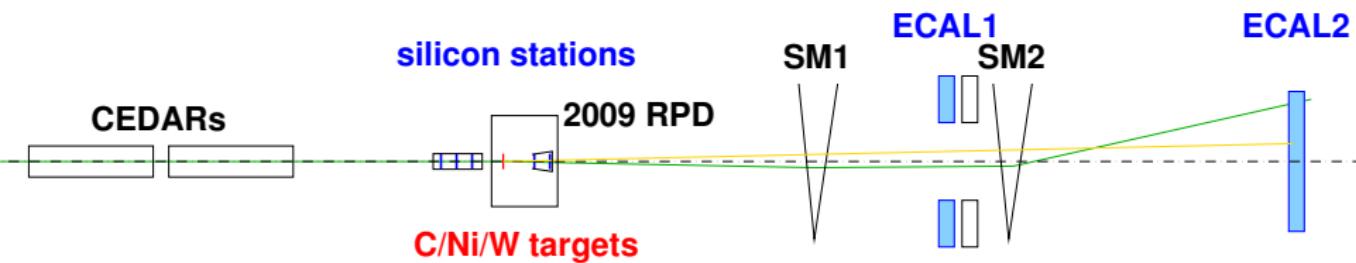


Runs with Hadron Beams 2004, 2008/09, 2012

- **190 GeV  $\pi^-$  beam** on  $p$  and nuclear targets (C, Ni, W, Pb)
- Silicon microstrip detectors for “vertexing”
- recoil and (digital) ECAL triggers



# Principle of the measurement



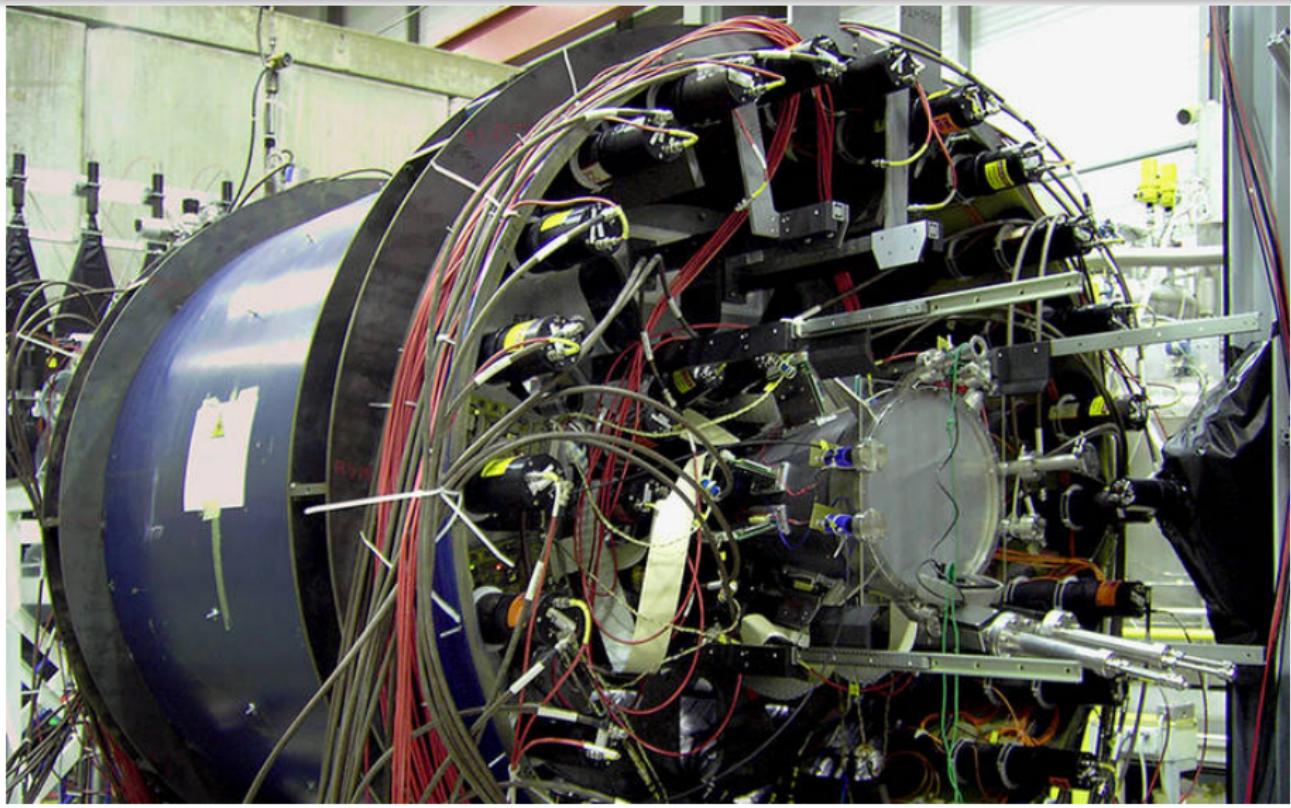


## Silicon detector module





# Silicon cryostat in the recoil detector




  
**Extraction of the pion polarisability**

- Identify exclusive reactions



at smallest momentum transfer  $< 0.001 \text{ GeV}^2/c^2$

- Assuming  $\alpha_\pi + \beta_\pi = 0$ , from the cross-section

$$R = \frac{\sigma(x_\gamma)}{\sigma_{\alpha_\pi=0}(x_\gamma)} = \frac{N_{\text{meas}}(x_\gamma)}{N_{\text{sim}}(x_\gamma)} = 1 - \frac{3}{2} \cdot \frac{m_\pi^3}{\alpha} \cdot \frac{x_\gamma^2}{1-x_\gamma} \alpha_\pi$$

is derived, depending on  $x_\gamma = E_{\gamma(\text{lab})}/E_{\text{Beam}}$ .  
Measuring  $R$  the polarisability  $\alpha_\pi$  can be concluded.

- Control systematics by



and




  
**Extraction of the pion polarisability**

- Identify **exclusive reactions**



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- Assuming  $\alpha_\pi + \beta_\pi = 0$ , from the cross-section

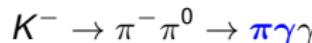
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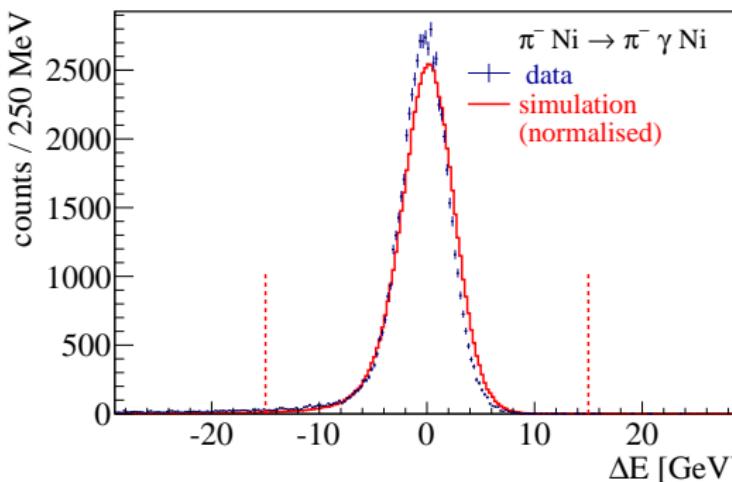
and





# Identifying the $\pi\gamma \rightarrow \pi\gamma$ reaction

Phys. Rev. Lett. 114, 062002 (2015)

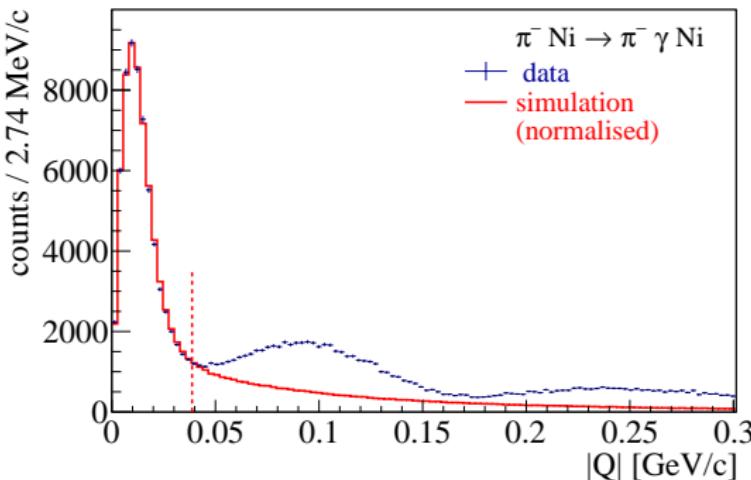


- Energy balance  $\Delta E = E_\pi + E_\gamma - E_{\text{Beam}}$
- Exclusivity peak  $\sigma \approx 2.6 \text{ GeV}$  (1.4%)
- $\sim 63.000$  exclusive events ( $x_\gamma > 0.4$ ) (Serpukhov  $\sim 7000$  for  $x_\gamma > 0.5$ )



# Primakoff peak

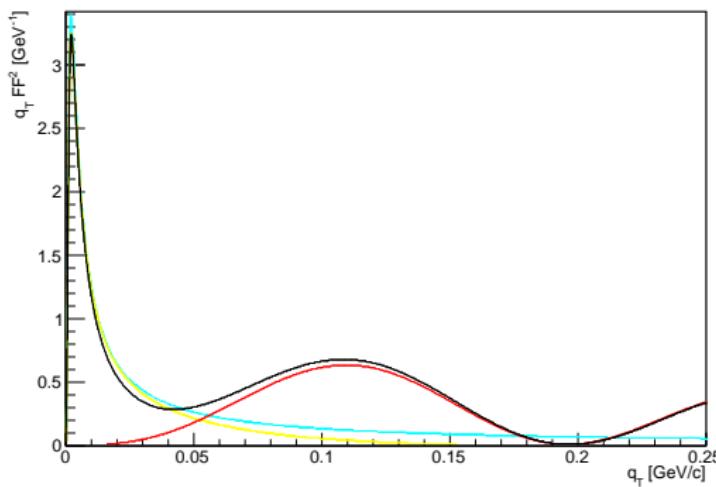
Phys. Rev. Lett. 114, 062002 (2015)



- $\Delta Q_T \approx 12 \text{ MeV}/c$  ( $190 \text{ GeV}/c$  beam  $\rightarrow$  requires few- $\mu\text{rad}$  angular resolution)
- first diffractive minimum on Ni nucleus at  $Q \approx 190 \text{ MeV}/c$
- data a little more narrow than simulation  $\rightarrow$  negative interference?



Photon density squared form factor

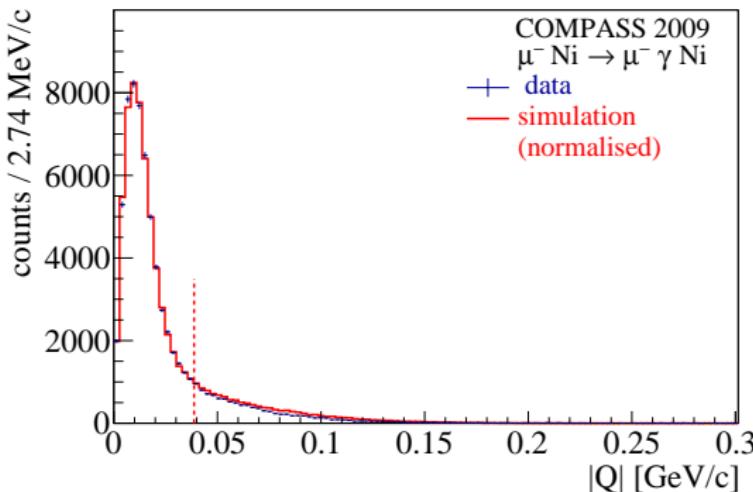


- calculation following G. Fäldt (Phys. Rev. C79, 014607)
- eikonal approximation: pions traverse Coulomb and strong-interaction potentials



## Primakoff peak: muon data

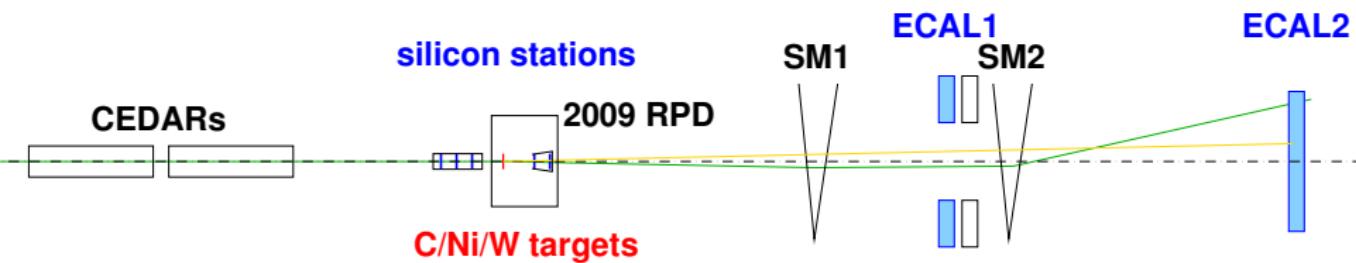
Phys. Rev. Lett. 114, 062002 (2015)



- **muon control measurement:** pure electromagnetic interaction
- e.m. nuclear effects well understood



# Principle of the measurement





## ECAL2: 3000 cells of different types





# ECAL2: the quest for precision

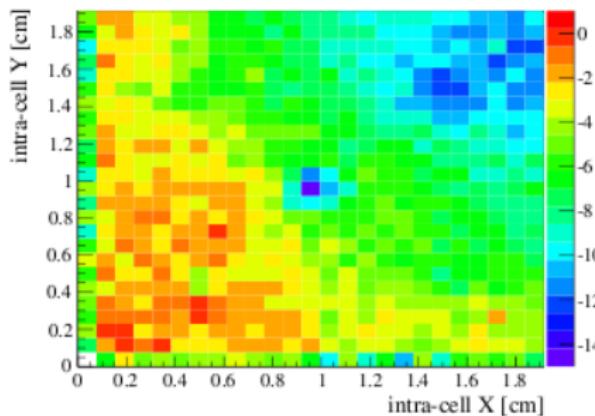


Figure 3.5: Profile of energy deviations shown for 1/4 of a shashlik block and for muon data photons within the range  $133 \text{ GeV} < E_\gamma < 152 \text{ GeV}$ .

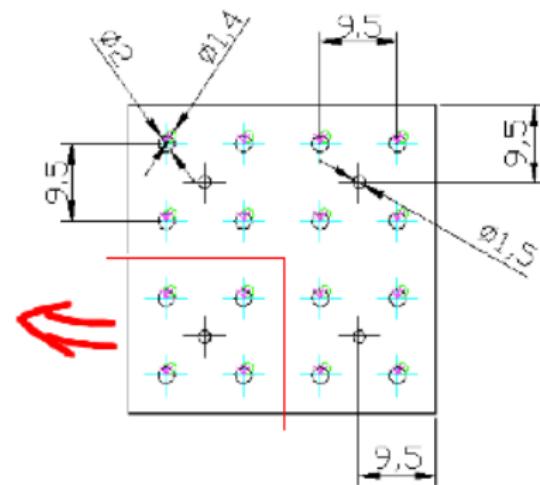
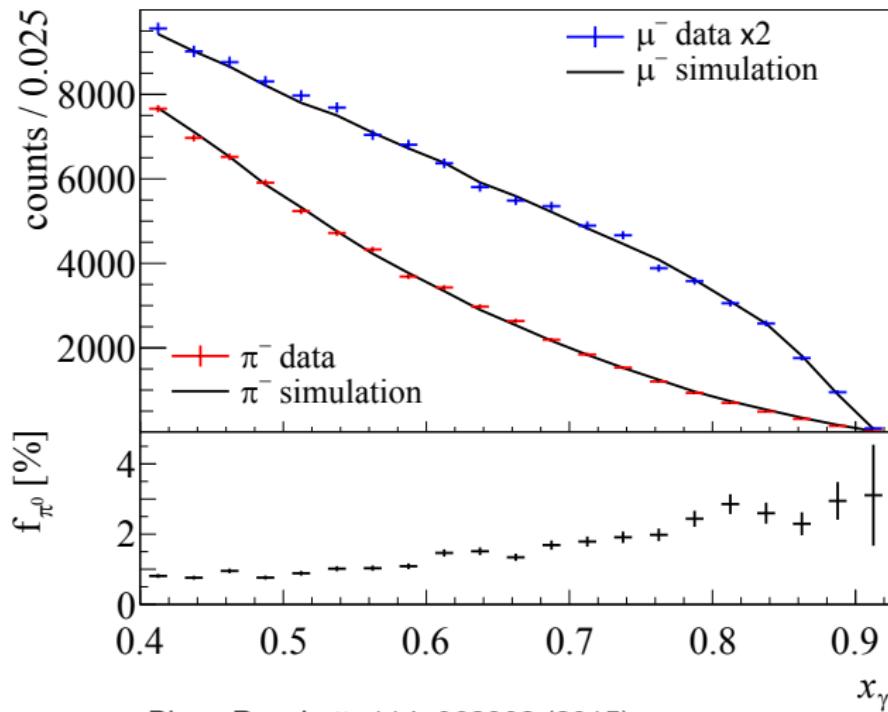


Figure 3.6: Technical drawing of a full shashlik cell to be compared with the figure to the left.

from: Th. Nagel, PhD thesis TUM 2012



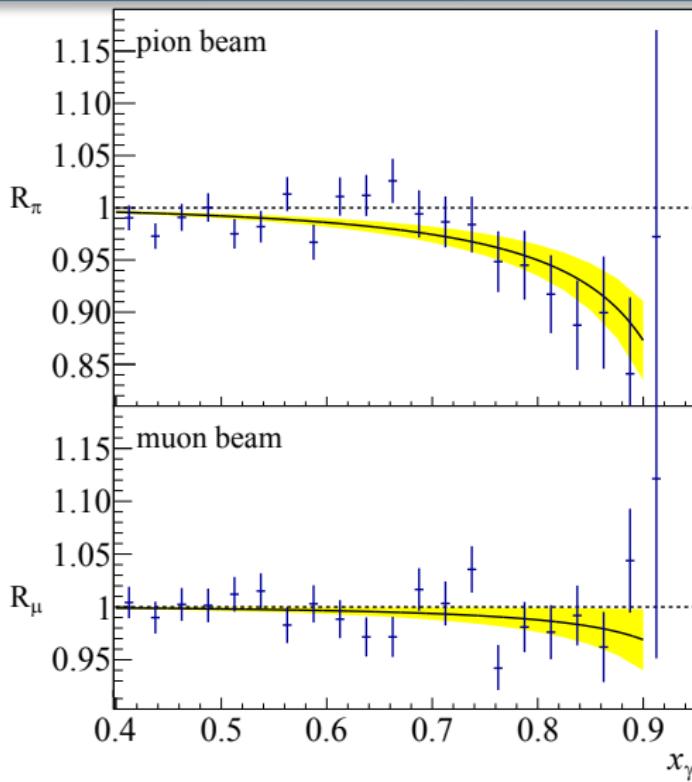
## Photon energy spectra for muon and pion beam



Phys. Rev. Lett. 114, 062002 (2015)



# Pion polarisability: COMPASS result



$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}}) \times 10^{-4} \text{ fm}^3$$

(assuming  $\alpha_\pi = -\beta_\pi$ )

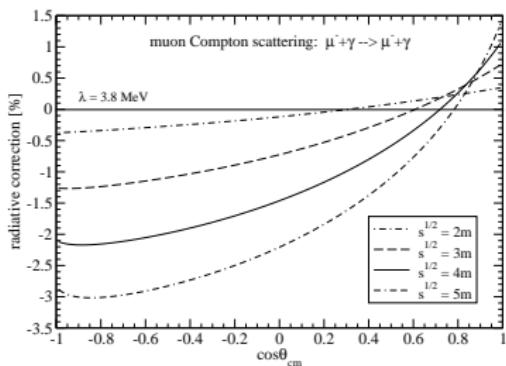
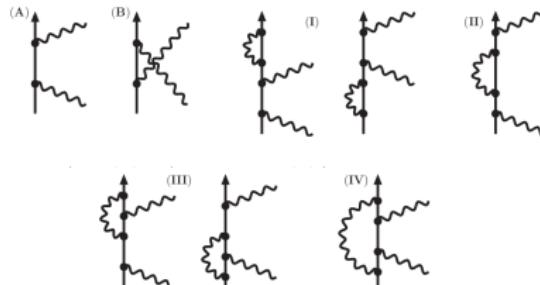
“false polarisability” from muon data:

$$(0.5 \pm 0.5_{\text{stat}}) \times 10^{-4} \text{ fm}^3$$

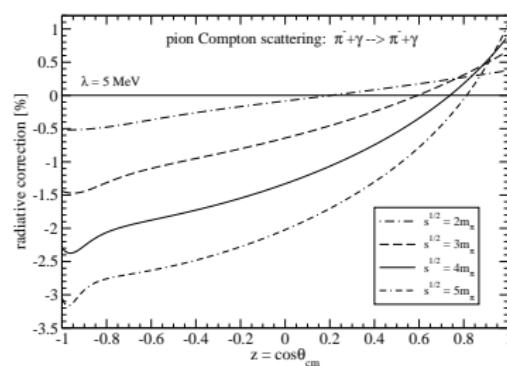
Phys. Rev. Lett. 114, 062002 (2015)



# Radiative corrections (Compton scattering part)



Nucl.Phys. A837 (2010)



Eur.Phys.J. A39 (2009) 71



source of systematic uncertainty	estimated magnitude CL = 68 % [10 <sup>-4</sup> fm <sup>3</sup> ]
tracking	0.5
radiative corrections	0.3
background subtraction in $Q$	0.4
pion electron scattering	0.2
quadratic sum	0.7



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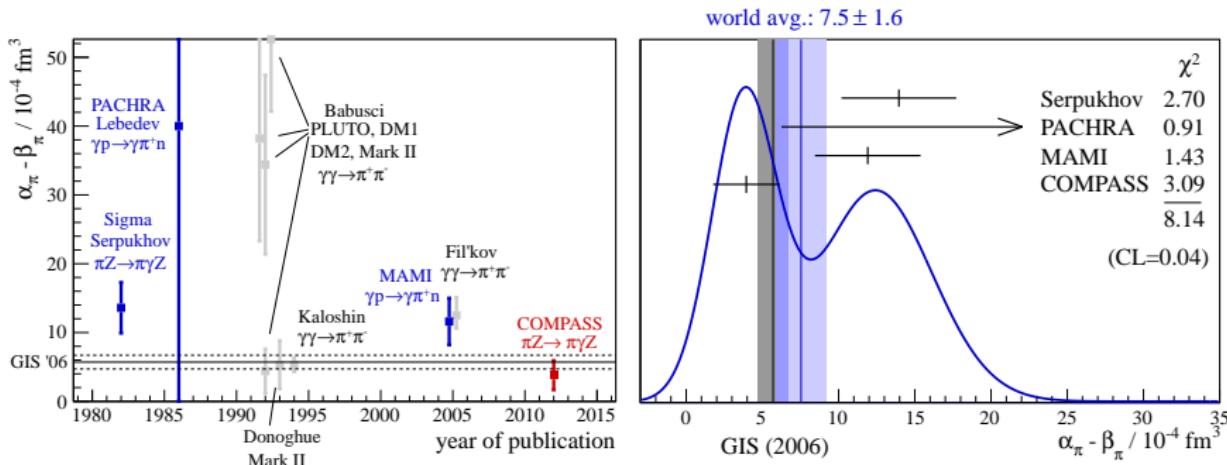
COMPASS result for the pion polarisability:

$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3$$

with  $\alpha_\pi = -\beta_\pi$  assumed



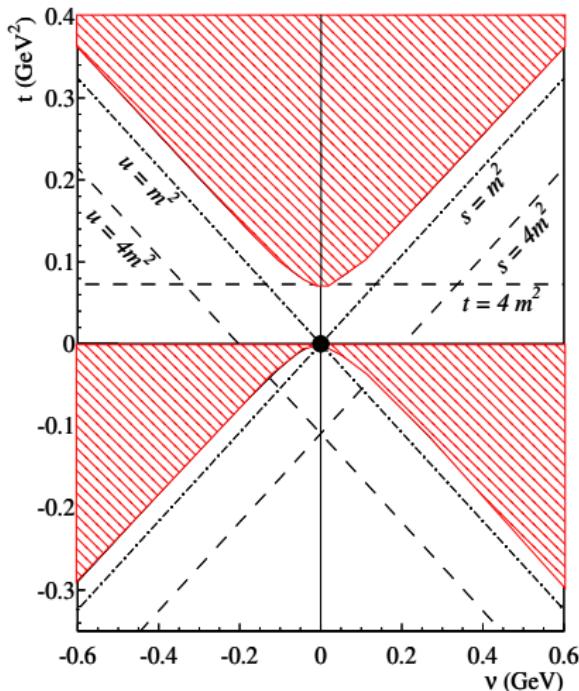
# Pion polarisability: world data including COMPASS



- The new COMPASS result is in significant tension with the earlier measurements of the pion polarisability
- The expectation from ChPT is confirmed within the uncertainties



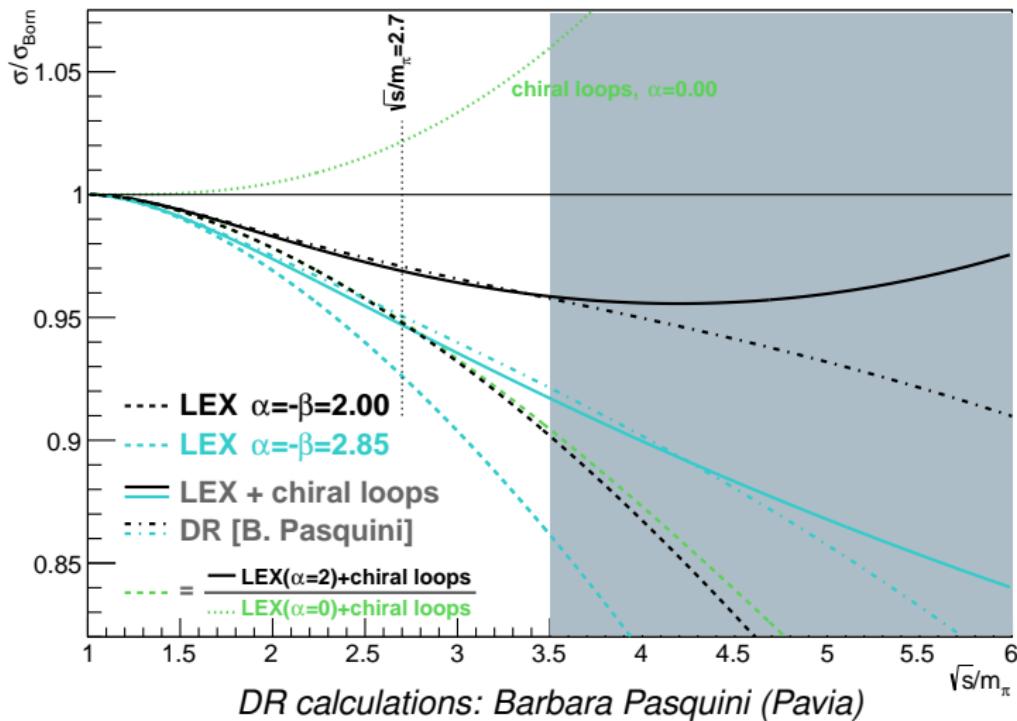
# About crossing



- ▶ red hatched:  
physical regions  
 $\gamma + \gamma \rightarrow \pi + \pi$   
 $\gamma + \pi \rightarrow \gamma + \pi$
- ▶ two-pion thresholds  
at  $s = 4m_\pi^2$ ,  $u = 4m_\pi^2$ ,  
 $t = 4m_\pi^2$
- ▶ DR integration paths  
 $t = 0$  (forward),  
 $\theta = 180^\circ$  (backward)  
 $u = m_\pi^2$ ,  $s = m_\pi^2$ , ...

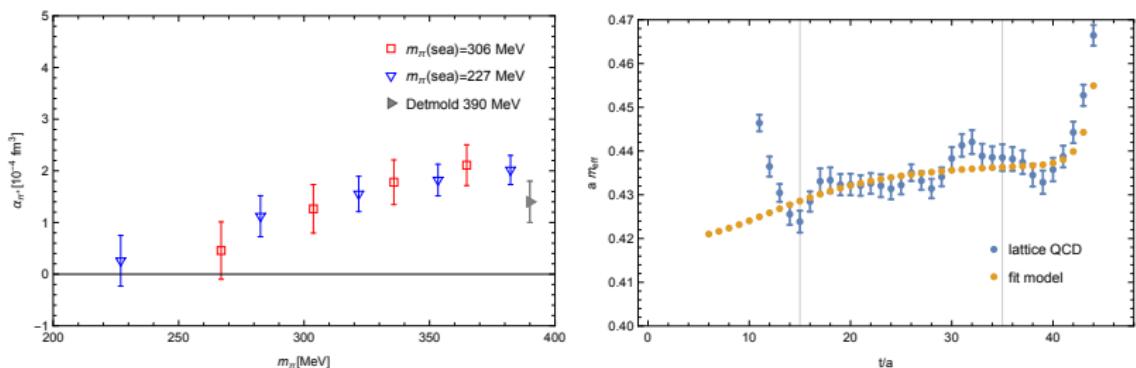
from: D. Drechsel, talk at IWHSS 2011 Paris

## Polarisability and Loop Contributions $z=1.0$





# Pion polarisability on the lattice

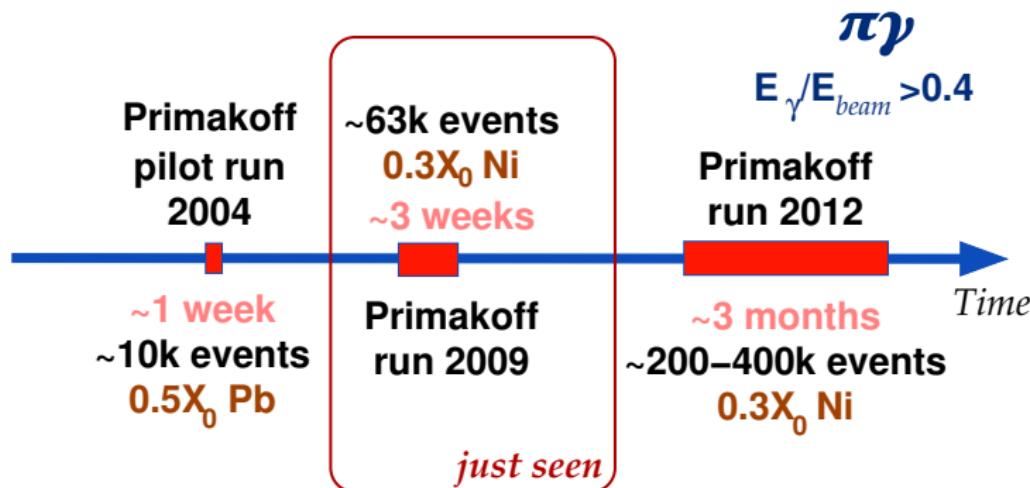


**FIGURE 3.** Left: electric polarizability for the charged pions as a function of the valence quark mass. The data for  $m_\pi = 390 \text{ MeV}$  is taken from [5]. Right: effective mass for a charged pion correlator together with the scalar particle correlator determined from the fit. The fitting range is indicated by the vertical bars.

Alexandru *et al.*, Pion electric polarizability from lattice QCD, arXiv:1501.06516



## Pion polarisability measurements at COMPASS



 Summary and Outlook

- Measurement of the **pion polarisability** at COMPASS

- Via the Primakoff reaction, COMPASS has determined

$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3 \quad \text{assuming } \alpha_\pi + \beta_\pi = 0$$

- most direct access to the  $\pi\gamma \rightarrow \pi\gamma$  process
  - Most precise experimental determination
  - Systematic control:  $\mu\gamma \rightarrow \mu\gamma$ ,  $K^- \rightarrow \pi^-\pi^0$

- (not shown today:) COMPASS measures other aspects of chiral dynamics in  $\pi^-\gamma \rightarrow \pi^-\pi^0$  and  $\pi\gamma \rightarrow \pi\pi\pi$  reactions

- High-statistics run 2012

- separate determination of  $\alpha_\pi$  and  $\beta_\pi$
  - $s$ -dependent quadrupole polarisabilities
  - First measurement of the kaon polarisability



*Thank you for your attention!*



# Backup

Access to  $\pi + \gamma$  reactions via the **Primakoff effect**:

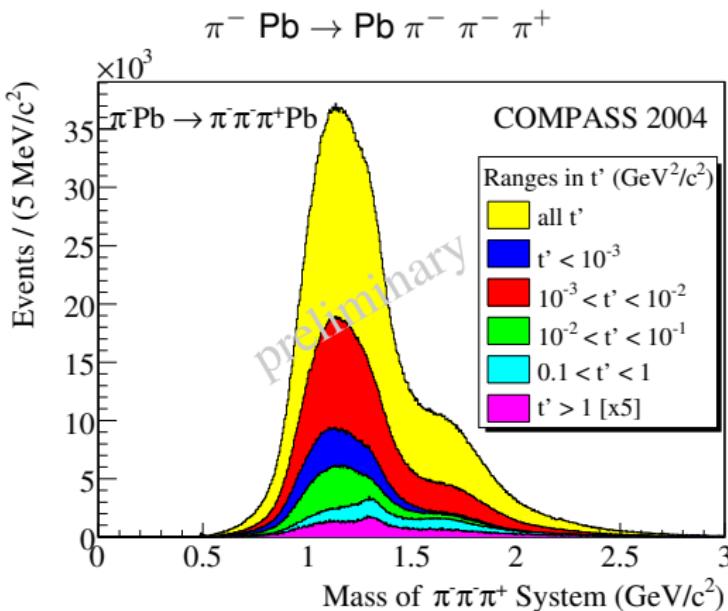
*At smallest momentum transfers* to the nucleus, high-energetic particles scatter predominantly off the **electromagnetic field quanta** ( $\sim Z^2$ )

$$\pi^- + \gamma \rightarrow \left\{ \begin{array}{l} \pi^- + \gamma \\ \pi^- + \pi^0 / \eta \\ \pi^- + \pi^0 + \pi^0 \\ \pi^- + \pi^- + \pi^+ \\ \pi^- + \pi^- + \pi^+ + \pi^- + \pi^+ \\ \pi^- + \dots \end{array} \right.$$

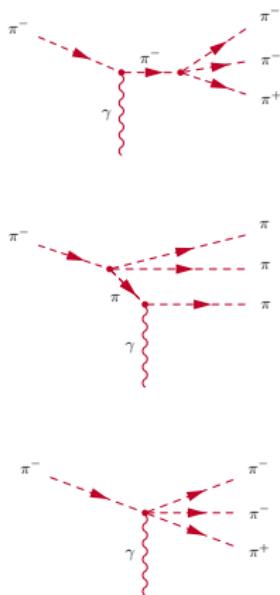
*analogously: Kaon-induced reactions  $K^- + \gamma \rightarrow \dots$*



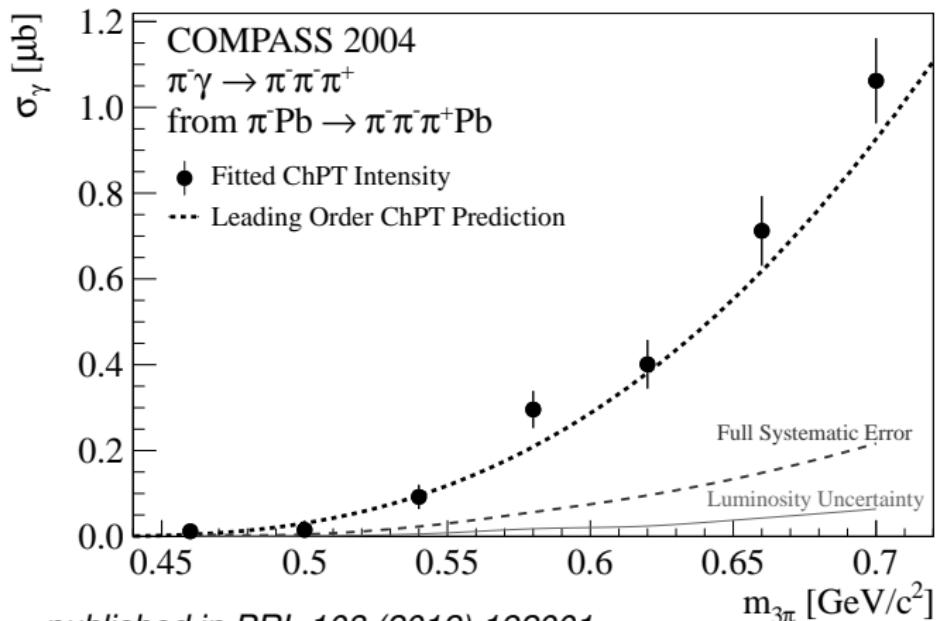
# 2004 Primakoff results



- "Low  $t'$ ":  $10^{-3} (\text{GeV}/c)^2 < t' < 10^{-2} (\text{GeV}/c)^2$   $\sim 2\,000\,000$  events
- "Primakoff region":  $t' < 10^{-3} (\text{GeV}/c)^2$   $\sim 1\,000\,000$  events



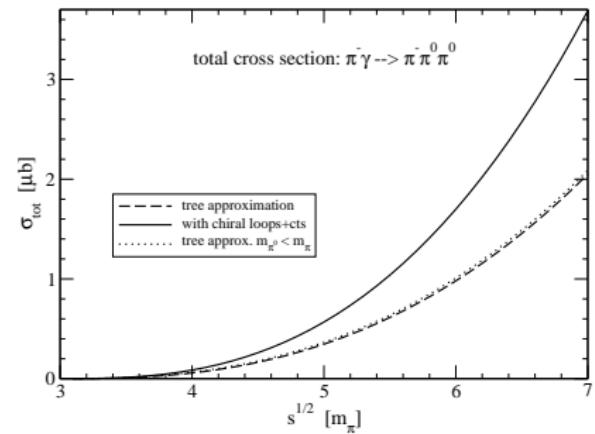
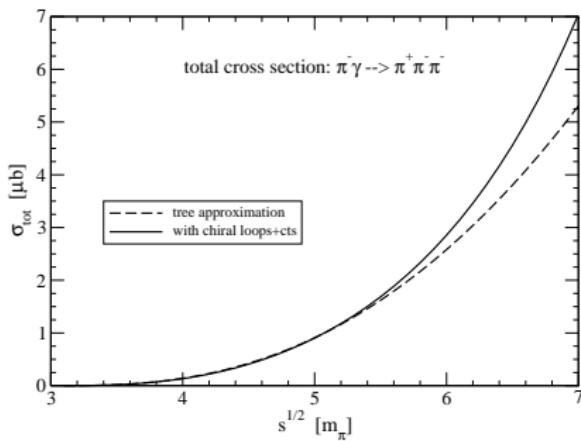
Measured absolute cross-section of  $\pi^- \gamma \rightarrow \pi^- \pi^- \pi^+$



published in PRL 108 (2012) 192001

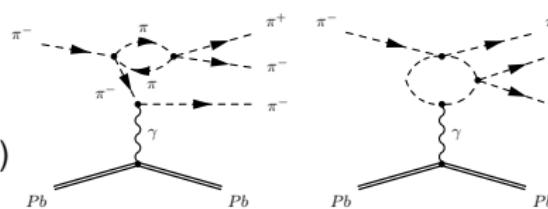


# Higher-order effects

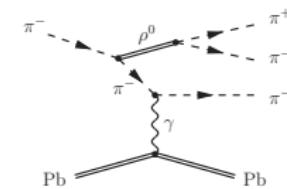


Chiral loops, e.g.

(N. Kaiser,  
NPA848 (2010) 198)

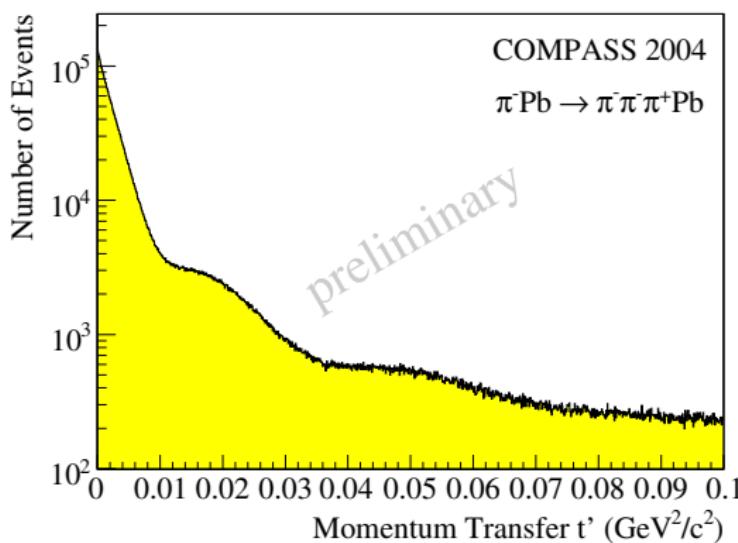


not (yet)  
included:





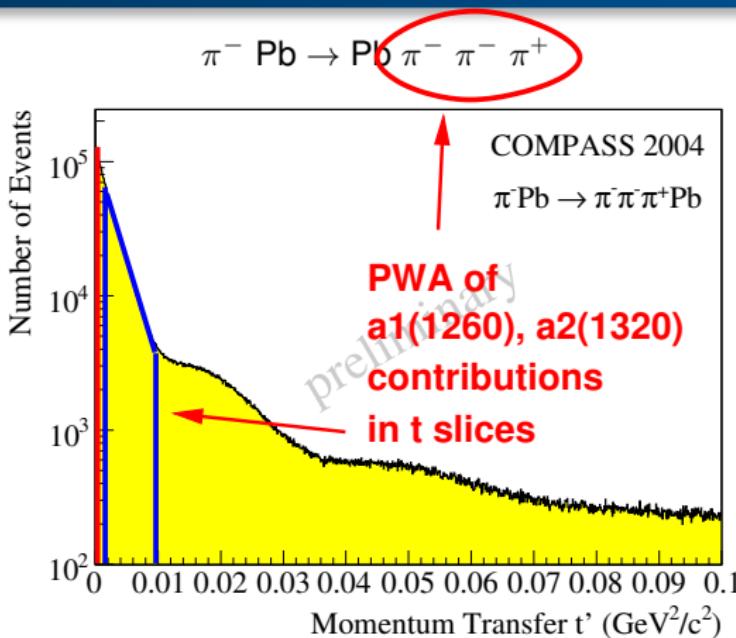
# 2004 Primakoff results

$$\pi^- \text{ Pb} \rightarrow \text{Pb} \pi^- \pi^- \pi^+$$


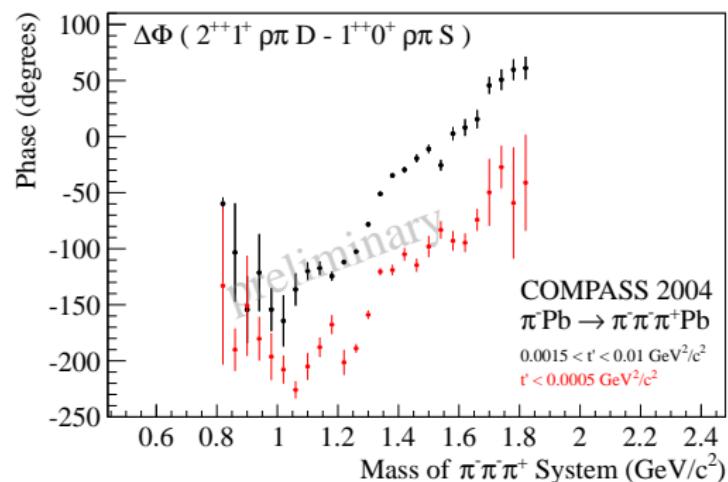
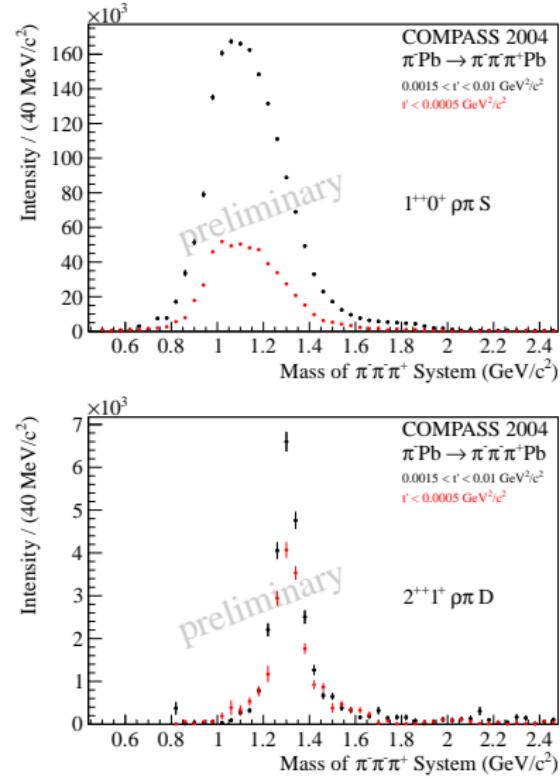
- "Low  $t'$ ":  $10^{-3} (\text{GeV}/\text{c})^2 < t' < 10^{-2} (\text{GeV}/\text{c})^2$   $\sim 2\,000\,000$  events
- "Primakoff region":  $t' < 10^{-3} (\text{GeV}/\text{c})^2$   $\sim 1\,000\,000$  events

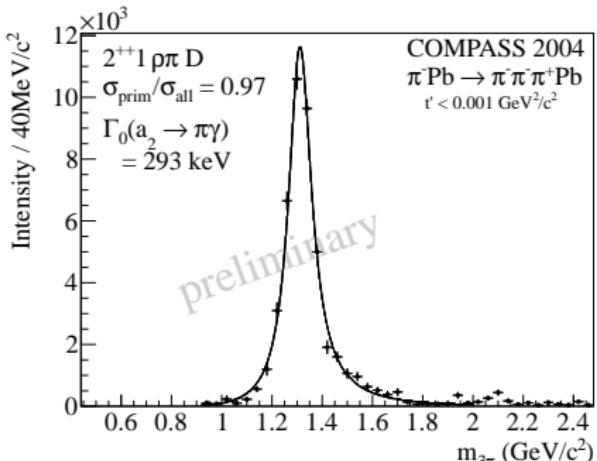


# 2004 Primakoff results

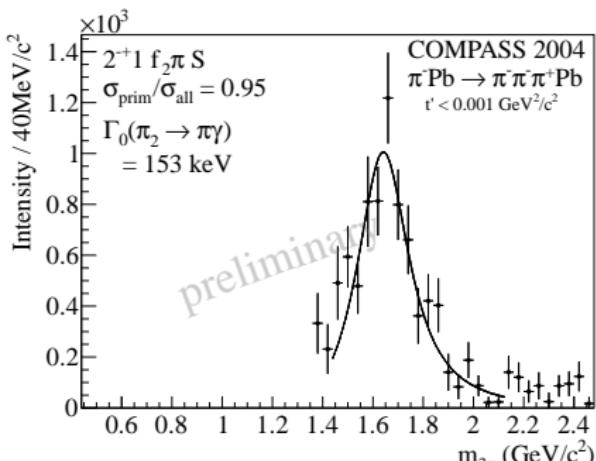


- "Low  $t'$ ":  $10^{-3} (\text{GeV}/\text{c})^2 < t' < 10^{-2} (\text{GeV}/\text{c})^2$   $\sim 2\,000\,000$  events
- "Primakoff region":  $t' < 10^{-3} (\text{GeV}/\text{c})^2$   $\sim 1\,000\,000$  events



Radiative Coupling of  $a_2(1320)$  and  $\pi_2(1670)$ 

$\Gamma_0(a_2(1320) \rightarrow \pi\gamma)$  M2



$\Gamma_0(\pi_2(1670) \rightarrow \pi\gamma)$  E2

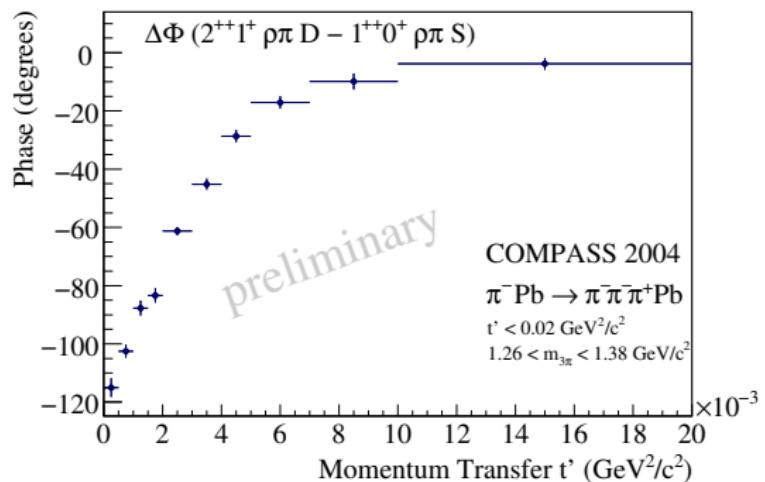
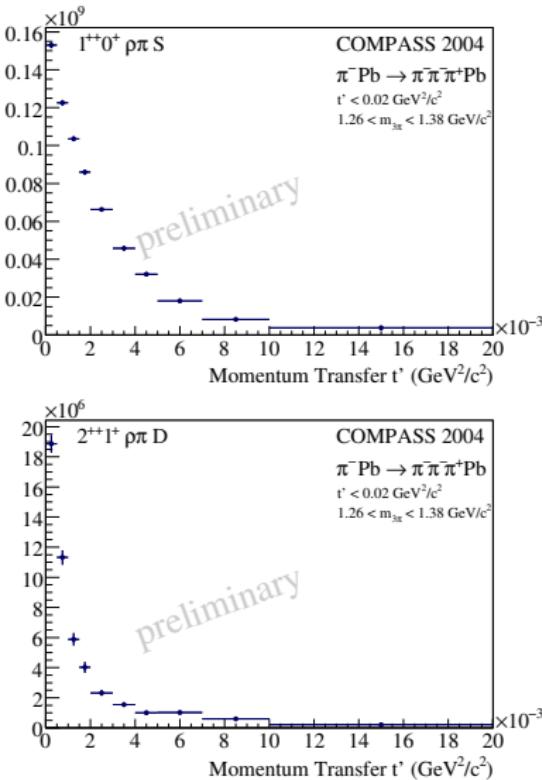
$\Leftrightarrow$  meson w.f.'s:  $\Gamma_{i \rightarrow f} \propto | \langle \Psi_f | e^{-i\vec{q} \cdot \vec{r}} \hat{\epsilon} \cdot \vec{p} | \Psi_i \rangle |^2$ , VMD

- normalization via beam kaon decays
- large Coulomb correction

published in EPJ A50 (2014) 79



# Phase $a_2 - a_1$ in detail: $t'$ dependence



- transition of  $\pi\gamma$  to  $\pi IP \rightarrow a_2$  production
- work in progress
- interference can be used to map details of resonances and production mechanisms



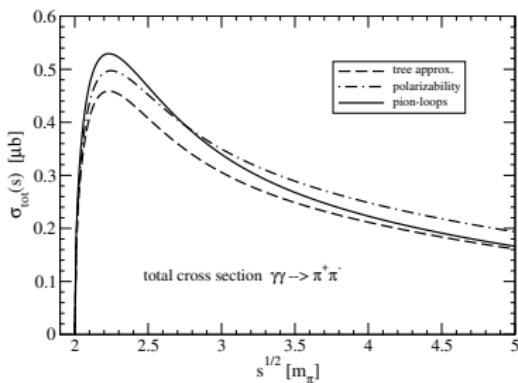
# Photon-photon fusion process $\gamma\gamma \rightarrow \pi^+ \pi^-$

- Planned measurements at ALICE and JLab

$$\sigma_{tot}(s) = \frac{2\pi\alpha^2}{\hat{s}^3 m_\pi^2} \left\{ [4 + \hat{s} + \hat{s}|\mathcal{C}(\hat{s})|^2] \sqrt{\hat{s}(\hat{s} - 4)} \right.$$

$$\left. + 8[2 - \hat{s} + \hat{s} \operatorname{Re} \mathcal{C}(\hat{s})] \ln \frac{\sqrt{\hat{s}} + \sqrt{\hat{s} - 4}}{2} \right\},$$

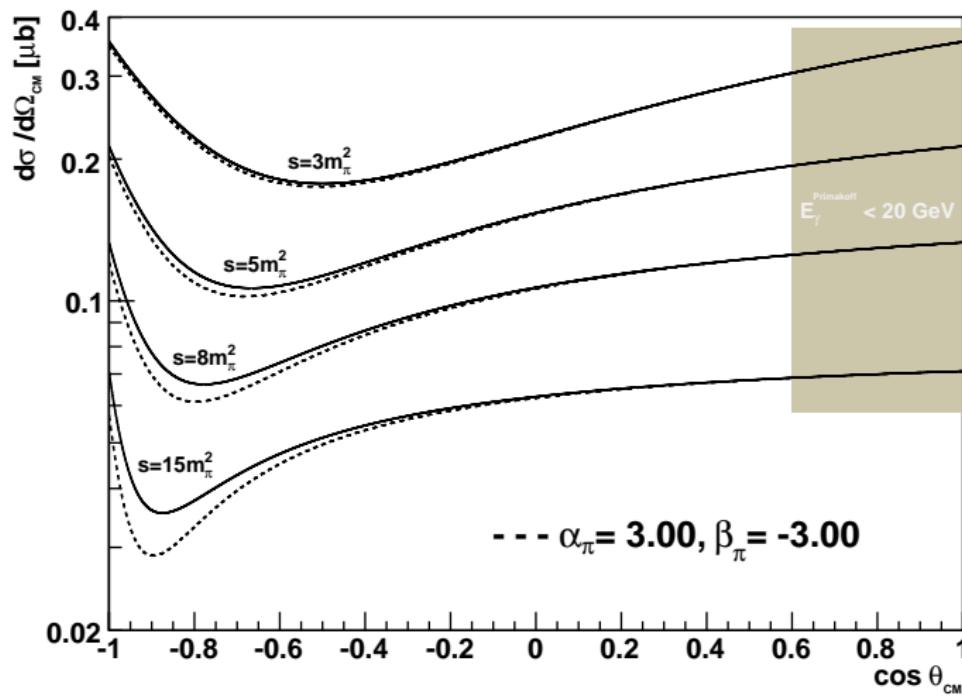
$$\mathcal{C}(\hat{s}) = -\beta_\pi \frac{m_\pi^3}{2\alpha} \hat{s} - \frac{m_\pi^2}{(4\pi f_\pi)^2} \left\{ \frac{\hat{s}}{2} + 2 \left[ \ln \frac{\sqrt{\hat{s}} + \sqrt{\hat{s} - 4}}{2} - \frac{i\pi}{2} \right]^2 \right\}$$



courtesy Norbert Kaiser (TUM)



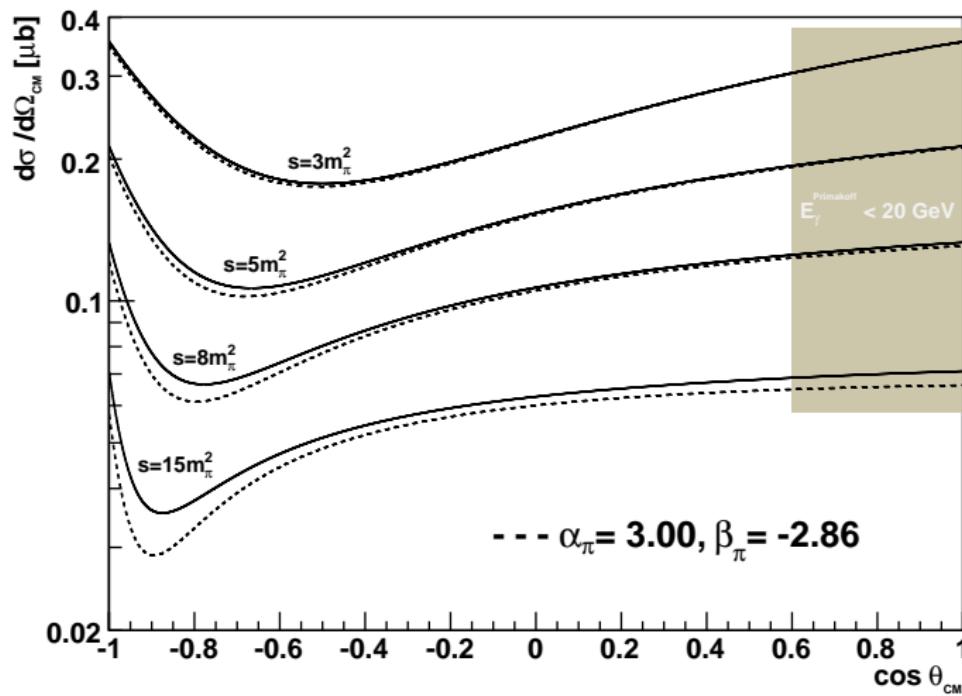
loop effects not shown





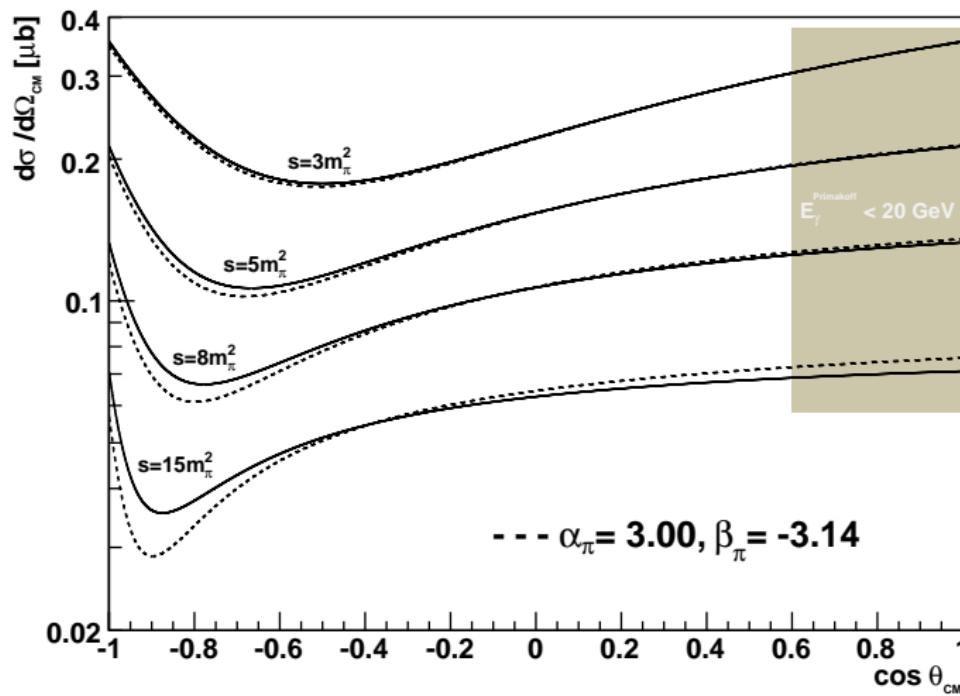
## Polarisability effect (NLO ChPT values)

loop effects not shown



Polarisability effect (wrong sign  $\alpha_\pi + \beta_\pi$ )

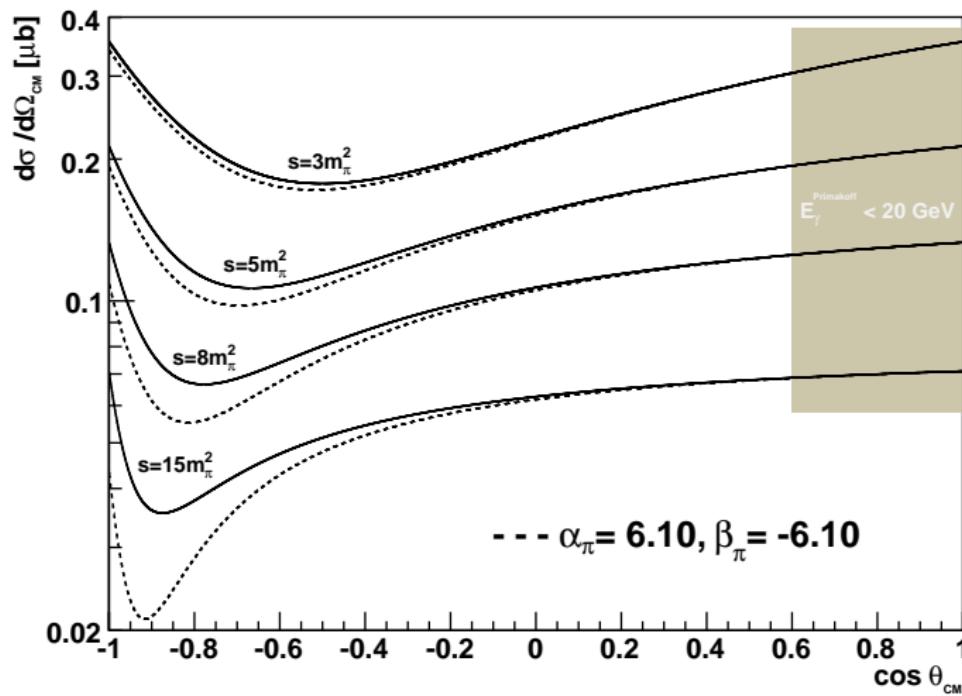
loop effects not shown





## Polarisability effect (Serpukhov values)

loop effects not shown





- Radiative  $\pi^+$  production on the proton:



Mainz (2005) measurement:  $\alpha_\pi - \beta_\pi = 11.6 \pm 1.5 \pm 3.0 \pm 0.5$

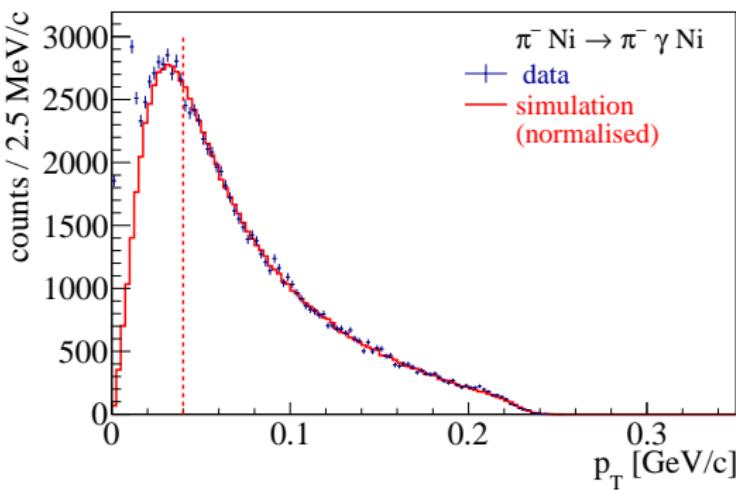
“ $\pm 0.5$ ”: model error *only within the used ansatz,*  
*full systematics not under control*

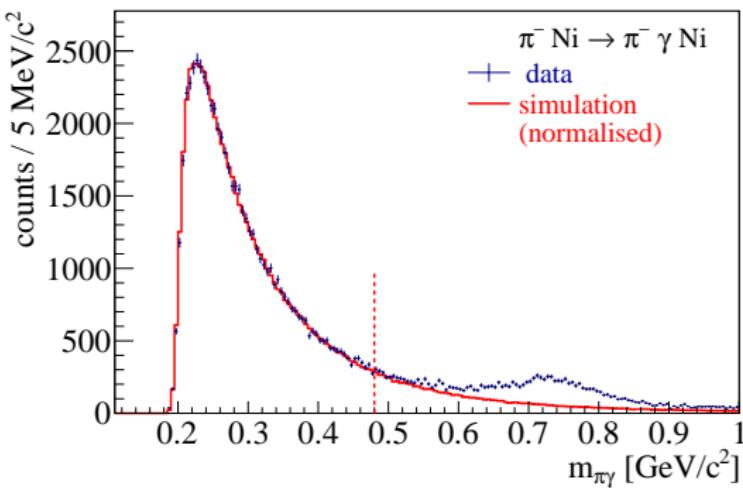
- Primakoff Compton reaction:



tiny extrapolation  $\gamma^* \rightarrow \gamma \mathcal{O}(10^{-3} m_\pi^2)$   
*fully under theoretical control*

[N. Kaiser, J.F., Nucl. Phys. A 812 (2008) 186]

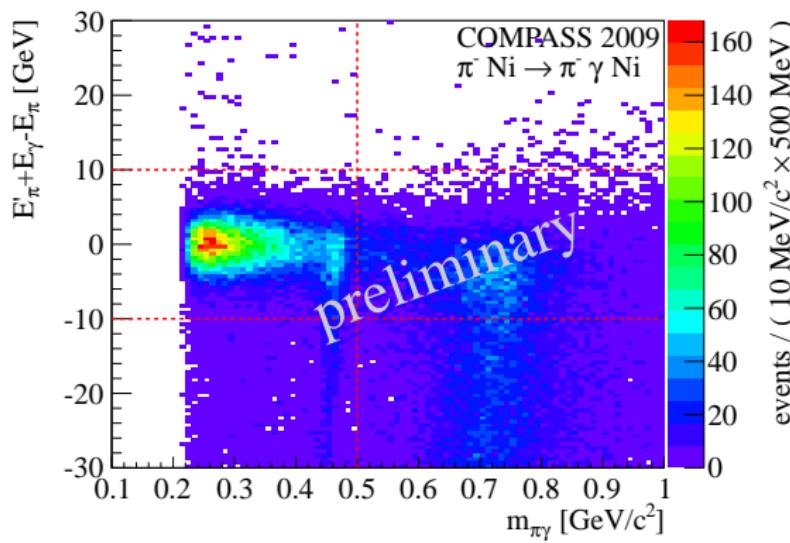


 CM energy in  $\pi\gamma \rightarrow \pi\gamma$ 


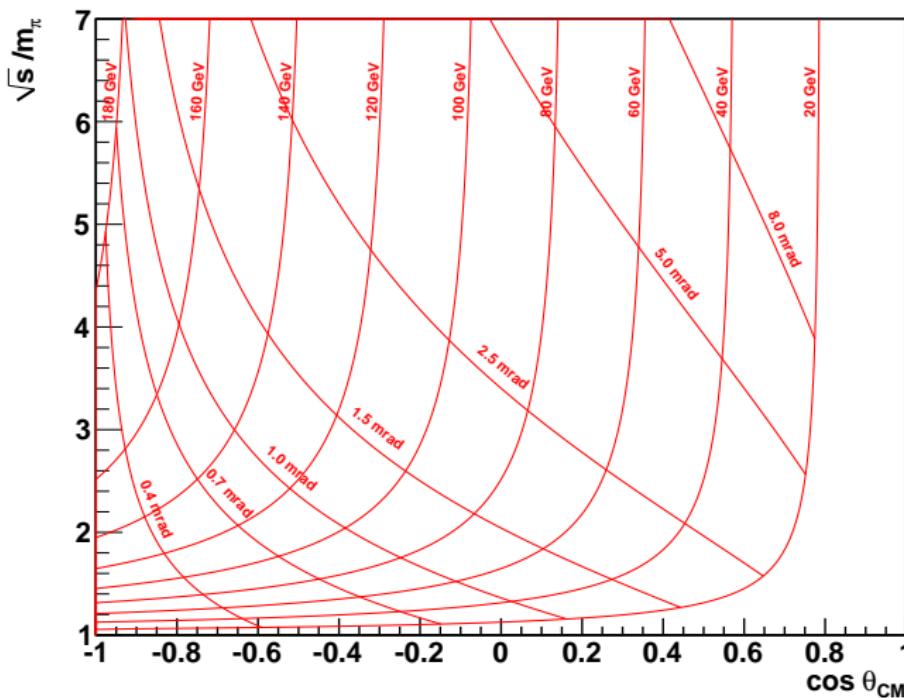
- $\rho$  contribution from  $\pi\gamma \rightarrow \pi\pi^0$



# Exclusivity vs. $\sqrt{s}$

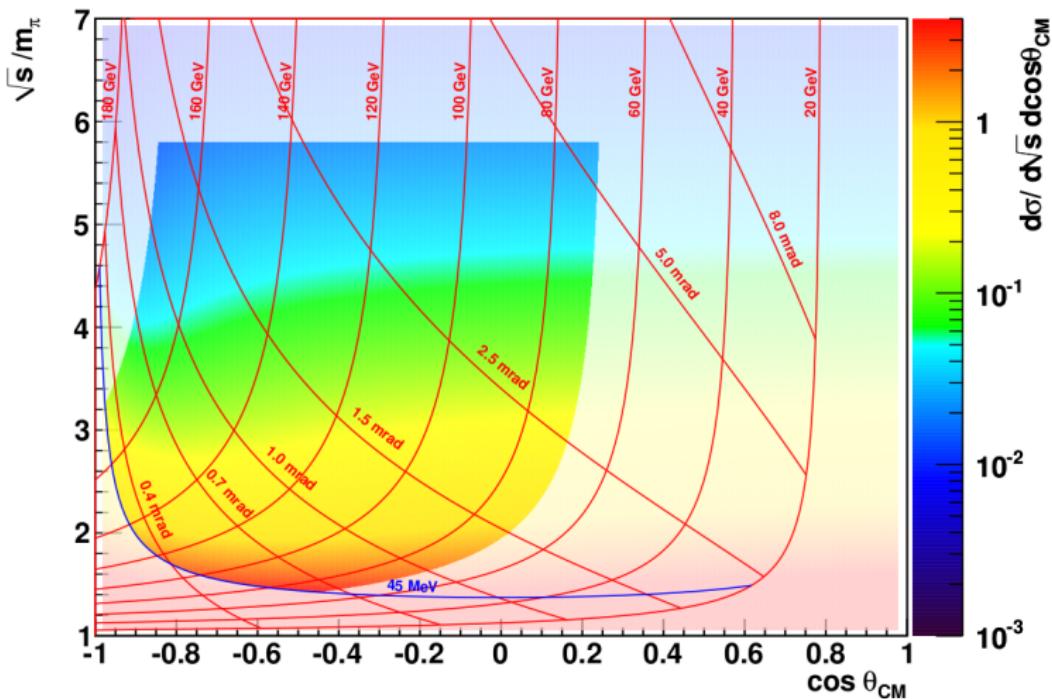


- $\rho$  contribution from  $\pi\gamma \rightarrow \pi\pi^0$

for  $\pi\gamma \rightarrow \pi\gamma$ 



## Cross section



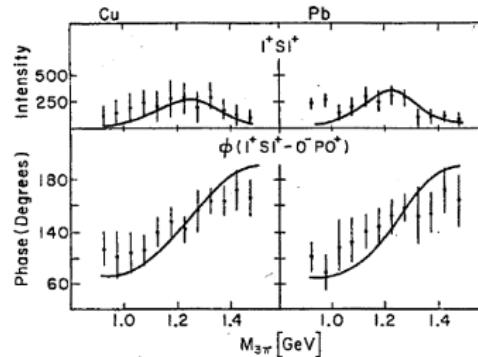
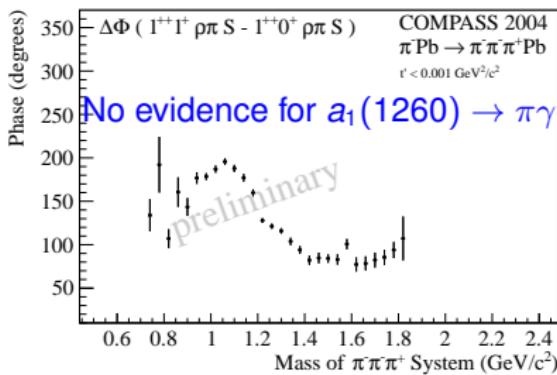
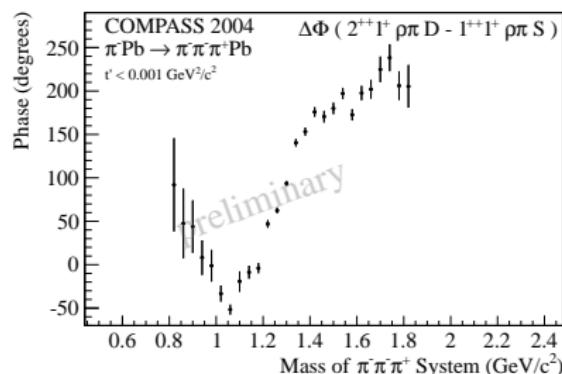
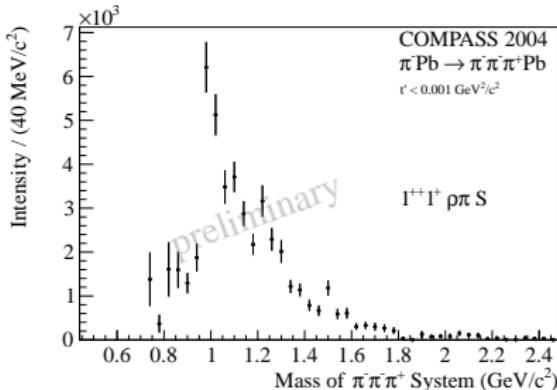
  $\gamma\gamma \rightarrow \pi\pi$  and the pion polarisability

M.R. Pennington in the 2<sup>nd</sup> DAΦNE Physics Handbook,  
“What we learn by measuring  $\gamma\gamma \rightarrow \pi\pi$  at DAΦNE”:

All this means that the only way to measure the pion polarisabilities is in the Compton scattering process near threshold and not in  $\gamma\gamma \rightarrow \pi\pi$ . Though the low energy  $\gamma\gamma \rightarrow \pi\pi$  scattering is seemingly close to the Compton threshold (...) and so the *extrapolation* not very far, the dominance of the pion pole (...) means that the energy scale for this continuation is  $m_\pi$ . Thus the polarisabilities cannot be determined accurately from  $\gamma\gamma$  experiments in a model-independent way and must be measured in the Compton scattering region.



# Primakoff production of $a_1(1260)$ vs. E272 result



M. Zielinski et al, Phys. Rev. Lett 52 (1984) 1195

- Mass-independent PWA (narrow mass bins):

$$\sigma_{\text{indep}}(\tau, m, t') = \sum_{\epsilon=\pm 1} \sum_{r=1}^{N_r} \left| \sum_i T_{ir}^\epsilon f_i^\epsilon(t') \psi_i^\epsilon(\tau, m) \right|^2 \sqrt{\int |f_i^\epsilon(t')|^2 dt'} \sqrt{\int |\psi_i^\epsilon(\tau', m)|^2 d\tau'}^2$$

- Production strength assumed constant in single bins
- Decay amplitudes  $\psi_i^\epsilon(\tau, m)$ , with  $t'$  dependence  $f_i^\epsilon(t')$
- Production amplitudes  $T_{ir}^\epsilon$  → Extended log-likelihood fit
- Acceptance corrections included
- Spin-density matrix:  $\rho_{ij}^\epsilon = \sum_r T_{ir}^\epsilon T_{jr}^{\epsilon*}$

→ Physical parameters:

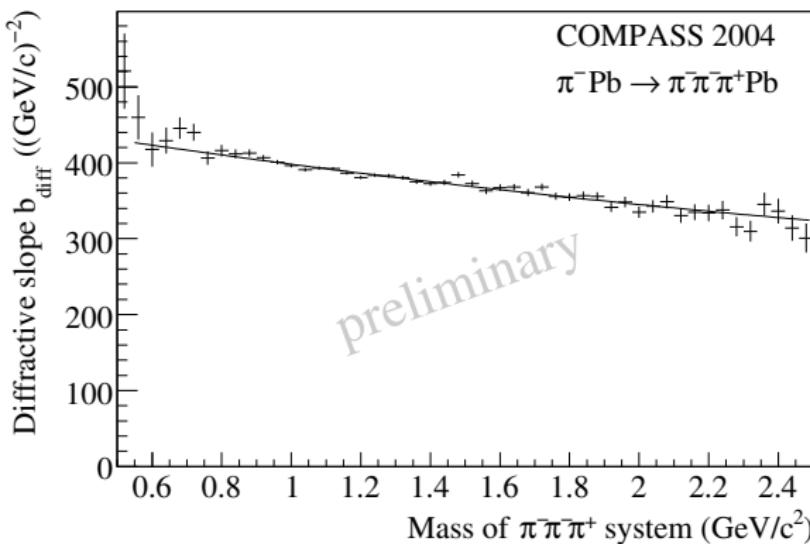
$$\text{Intens}_i^\epsilon = \rho_{ii}^\epsilon,$$

relative phase  $\Phi_{ij}^\epsilon$

$$\text{Coh}_{i,j}^\epsilon = \sqrt{(\text{Re } \rho_{ij}^\epsilon)^2 + (\text{Im } \rho_{ij}^\epsilon)^2} / \sqrt{\rho_{ii}^\epsilon \rho_{jj}^\epsilon}$$

- Mass-dependent  $\chi^2$ -fit (not presented here):

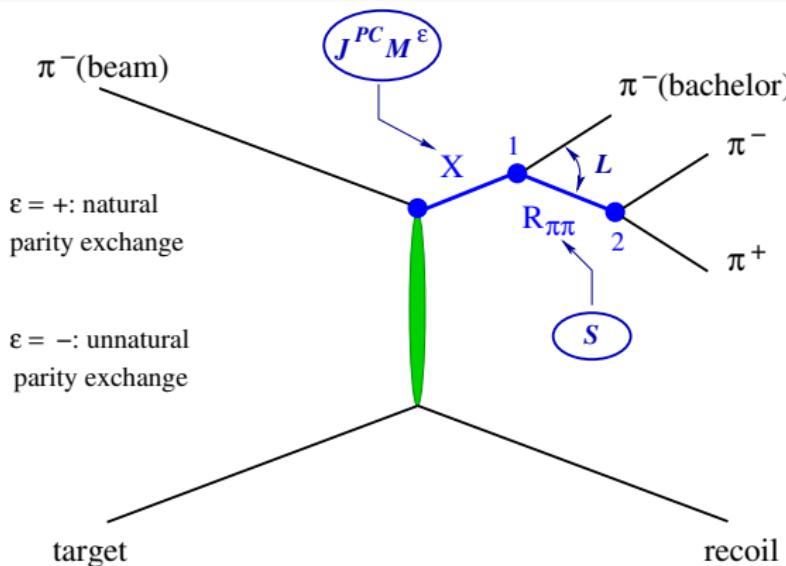
- $X$  parameterized by Breit-Wigner (BW) functions
- Background can be added





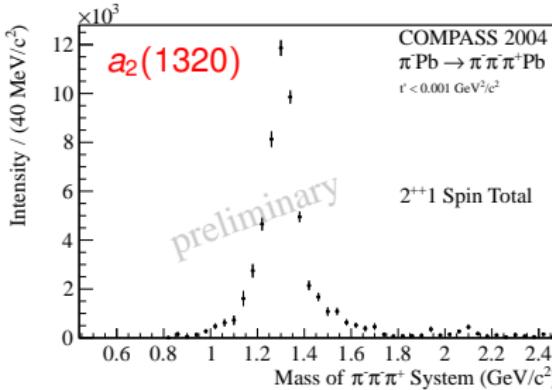
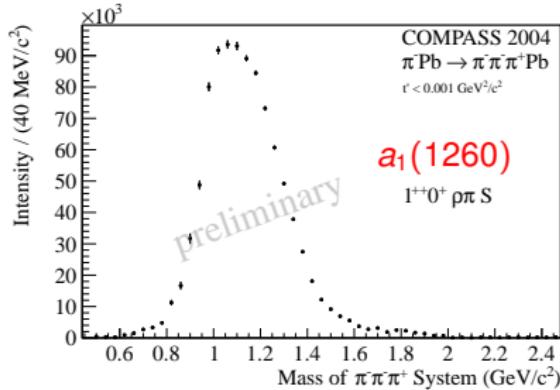
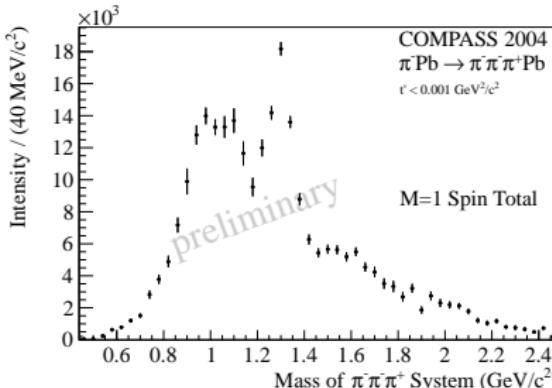
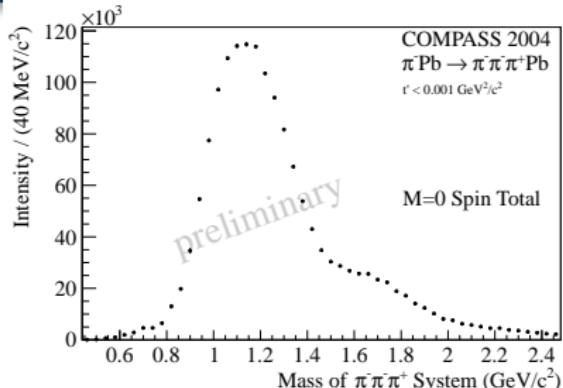
# Partial Wave Analysis Formalism

## Isobar Model



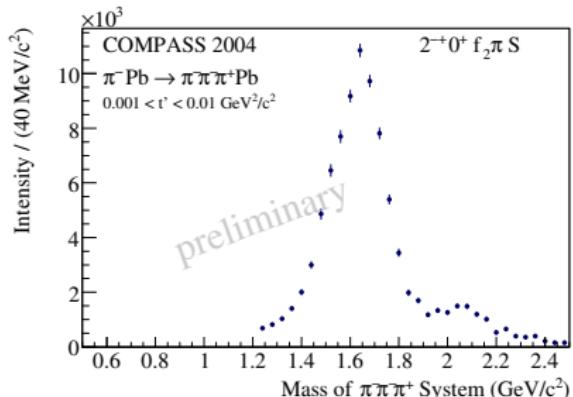
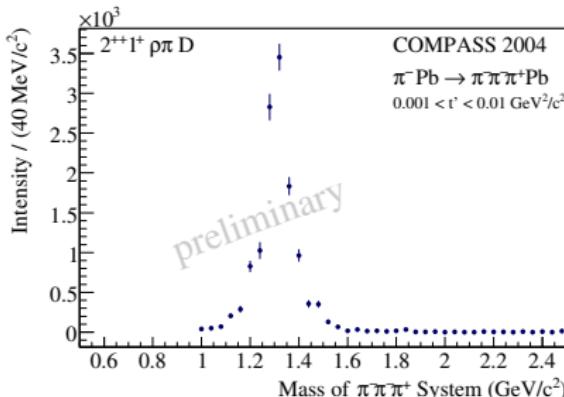
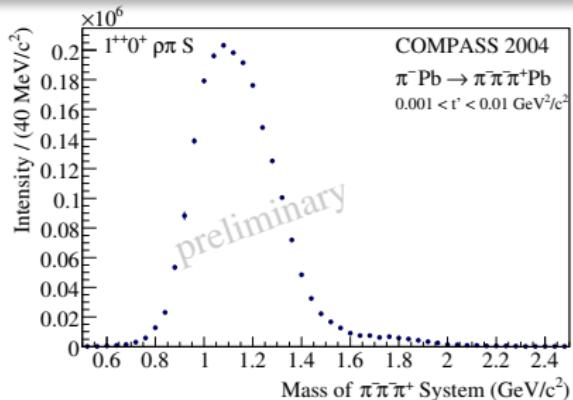
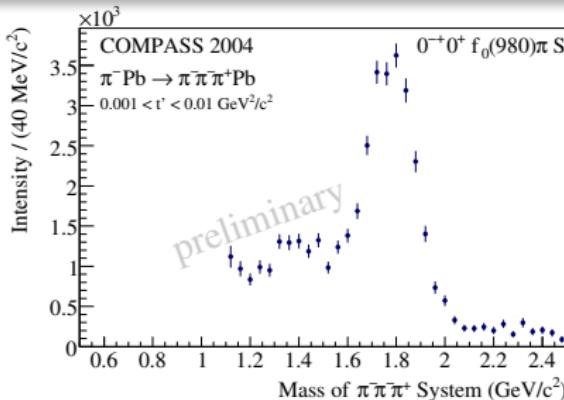
- Isobar model:  
Intermediate 2-particle decays
- Partial wave in reflectivity basis:  
 $J^{PC} M^\epsilon$  [isobar]  $L$

- Mass-independent PWA (40 MeV/ $c^2$  mass bins): 38 waves  
Fit of angular dependence of partial waves, interferences
- Mass-dependent  $\chi^2$ -fit (Not presented here)



# PWA of data with low $t'$

Intensity of selected waves:  $0^{-+} 0^+ f_0(980)\pi S$ ,  $1^{++} 0^+ \rho\pi S$ ,  $2^{++} 1^+ \rho\pi D$ ,  $2^{-+} 0^+ f_2(1270)\pi S$





# Spin Totals for $t' < 10^{-3} (\text{GeV}/c)^2$

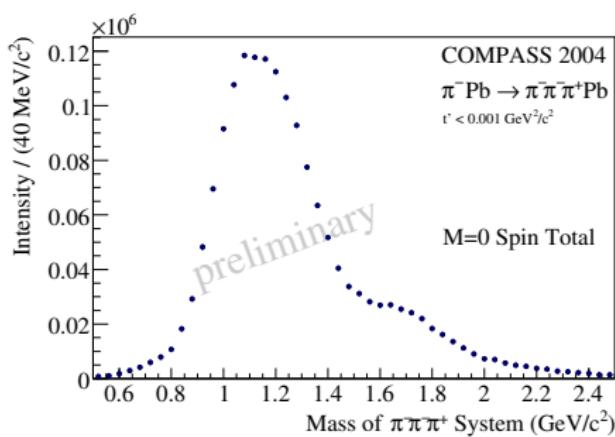
"Spin Totals": Sum of all contributions for given M (i.e. z-projection of J)

$t'$ -dependent amplitudes:

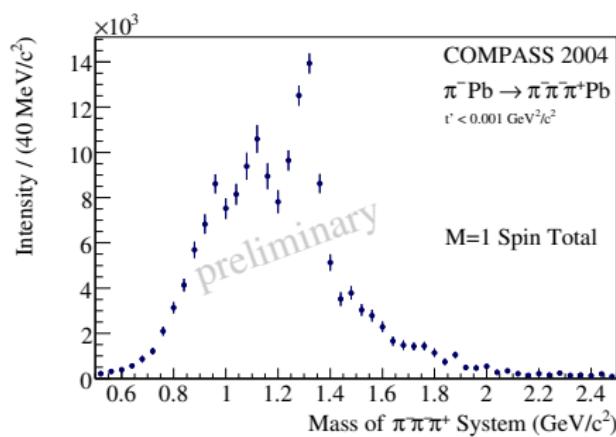
Primakoff production: **M=1**:  $\sigma(t') \propto e^{-b_{\text{Prim}} t'} \rightarrow$  arises at  $t' \approx 0$  (resolved shape!)

Diffractive production: **M=0**:  $\sigma(t') \propto e^{-b_{\text{diff}}(m) t'}$

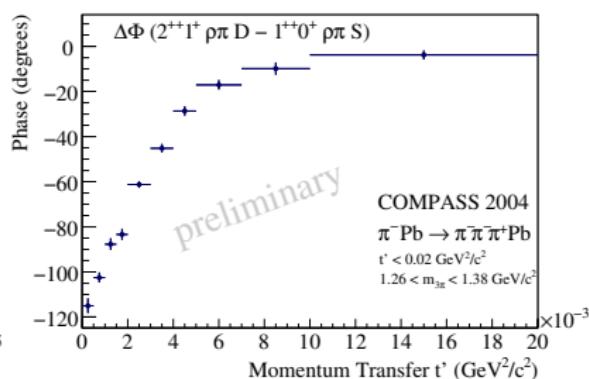
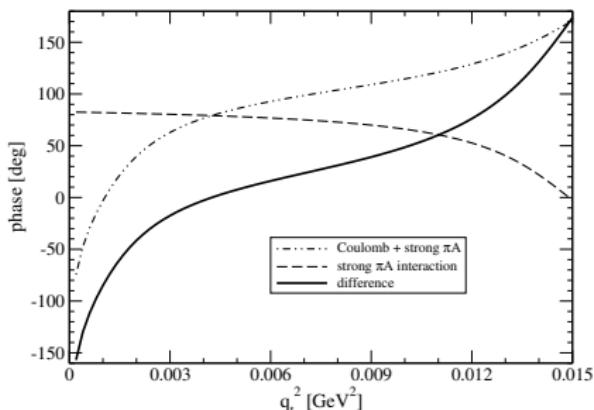
**M=1**:  $\sigma(t') \propto t' e^{-b_{\text{diff}}(m) t'} \rightarrow$  vanishes for  $t' \approx 0$



**M=0**



**M=1**



## Glauber modell

G. Fäldt and U. Tengblad, Phys. Rev. C79, 014607 (2009)

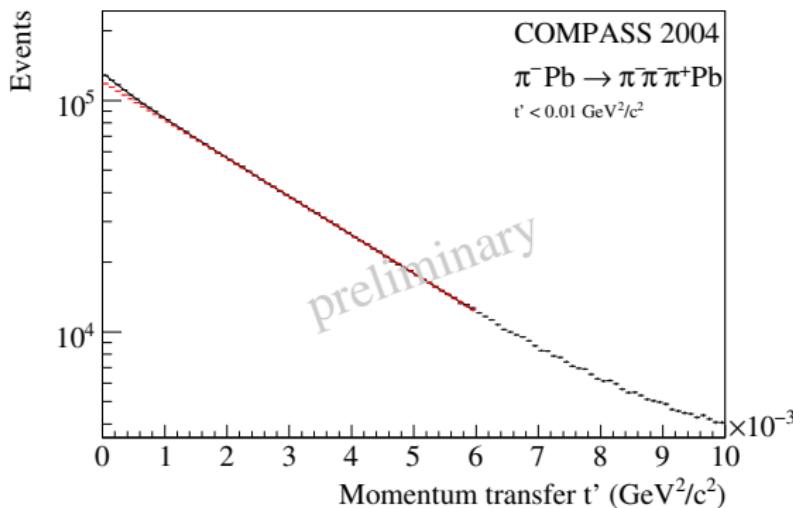
Plot: N. Kaiser (TU München)

- ⇒ indicates confirmation of interference Coulomb-interaction - strong interaction
- ⇒ detailed studies of the nature of resonances



# Primakoff contribution at $t' < 10^{-3} (\text{GeV}/c)^2$

Primakoff:  $\sigma(t') \propto e^{-b_{\text{Prim}} t'}$ ,  $b_{\text{Prim}} \approx 2000 (\text{GeV}/c)^{-2}$  (mainly resolution)  
 Diffractive:  $\sigma(t') \propto e^{-b_{\text{diff}} t'}$ ,  $b_{\text{diff}} \approx 400 (\text{GeV}/c)^{-2}$  for lead target



(Mass) spectrum of this Primakoff contribution?

⇒ Statistical subtraction of diffractive background (for bins of  $m_{3\pi}$ )