

***EXPERIMENTAL  
STUDY  
WITH  
LEPTON  
SCATTERING***

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*Yamagata University*

***"Latest results and future programs on the nucleon structure  
- Toward an understanding of the nucleon spin -"  
Meeting of the Japan Physical Society, March 27-30, 2014, Hiratsuka, Japan***

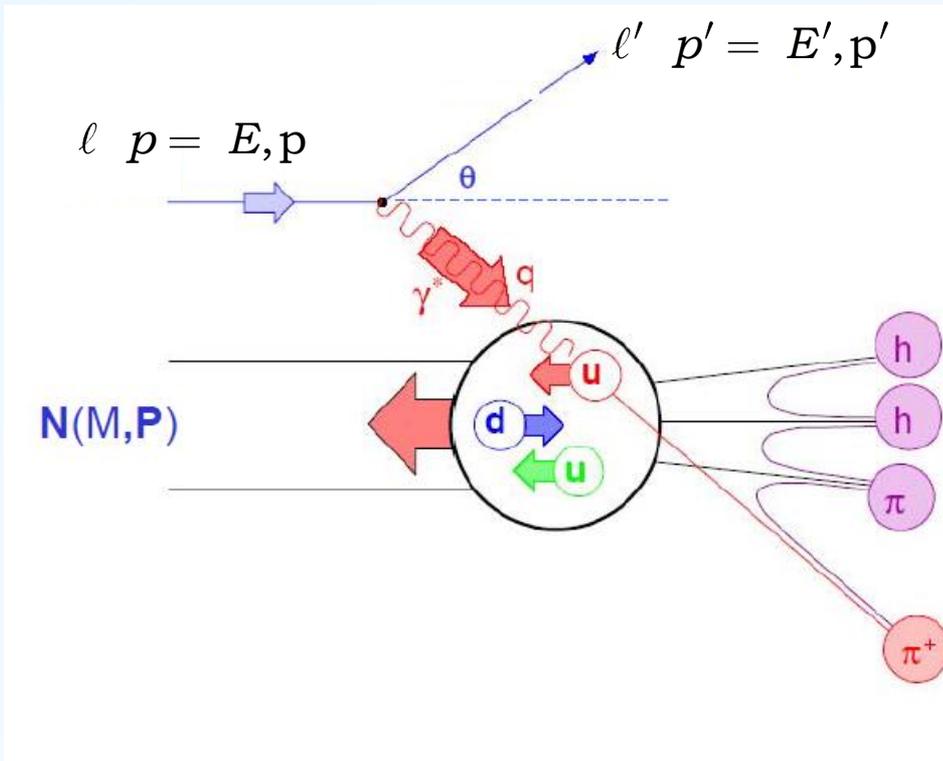
# OUTLINE

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- **Introduction**
  - *DIS, SIDIS & PDF*
  - *The Major Experiments*
- **Longitudinal Spin Structure**
  - *Polarized Structure Functions*
  - *Helicity Distributions*
  - *Gluon polarization Studies*
- **Transverse Spin Effects**
  - *Collins & Sivers Asymmetry*
  - *Asymmetry related to BM-PDF*
- **GPD Studies**
  - *GPD studies by HERMES & Jlab*
  - *Further studies on GPD*
- **Conclusion**

# DIS

## Lepton scattering off nucleon



$$Q^2 = -(p - p')^2$$

$$\nu = E - E' \quad \leftarrow \text{Energy of the photon}$$

$$\text{Lab. } x = Q^2 / 2M\nu$$

$$y = \nu / E$$

momentum fraction of the struck quark in Bjorken limit

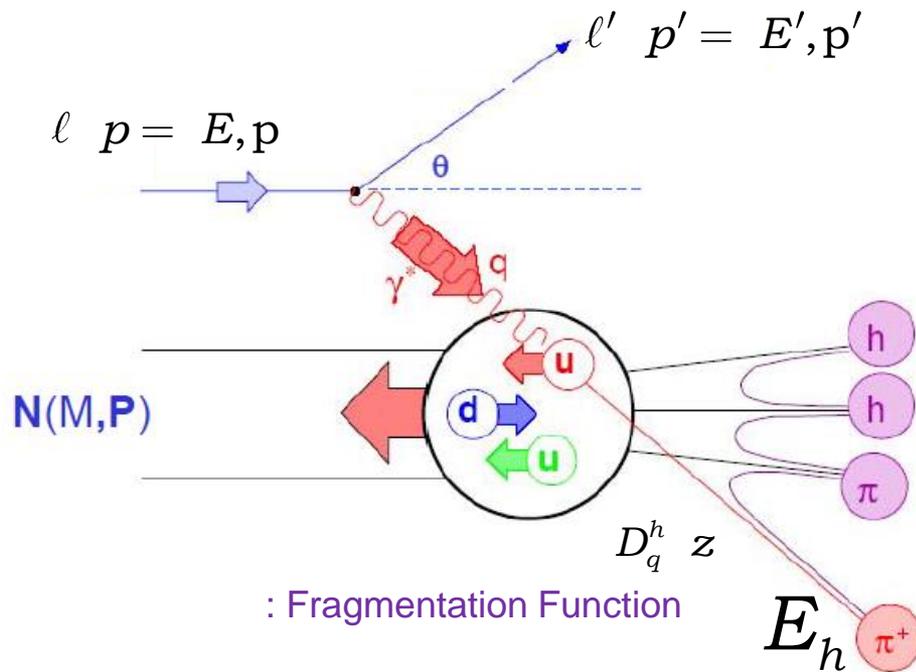
$$Q^2 \rightarrow \infty$$

$$\nu \rightarrow \infty$$

**Inclusive DIS:** only the scattered leptons are measured

# DIS and SI-DIS

## Lepton scattering off nucleon



$$Q^2 = -(p - p')^2$$

$$\nu = E - E' \quad \leftarrow \text{Energy of the photon}$$

$$\text{Lab.} \quad x = Q^2 / 2M\nu$$

$$y = \nu / E$$

$$z = E_h / \nu$$

momentum fraction of the struck quark in Bjorken limit

$$Q^2 \rightarrow \infty$$

$$\nu \rightarrow \infty$$

**Inclusive DIS:** only the scattered leptons are measured

**Semi-Inclusive DIS:** at least one final state hadrons are measured as well as the scattered leptons

# PDFs at LO

in collinear case, neglecting  $k_T$

## Nucleon

unpol.

long. pol.

trans. pol.

unpol.

long. pol.

trans. pol.

$$q(= f_1)$$

**number density**



$$\Delta q(= g_{1L})$$

**helicity**



$$\Delta_T q(= h_1)$$

**transversity**



Only three functions to describe the nucleon structure

Quark

# TMD PDFs

taking account of  $k_T$ , additional 5 TMD PDFs are necessary for a full description of unclean structure at LO

(Transverse Momentum Dependent PDFs)

## Nucleon

unpol.

long. pol.

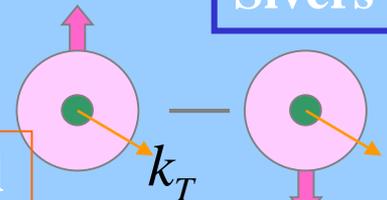
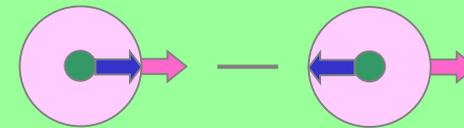
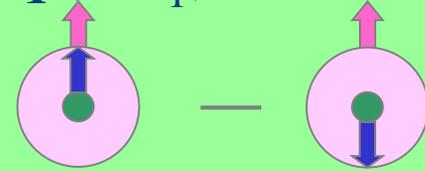
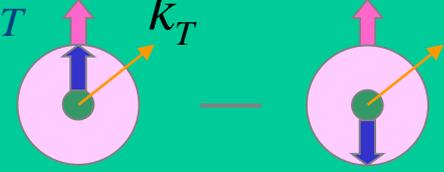
trans. pol.

unpol.

long. pol.

trans. pol.

Quark

	unpol.	long. pol.	trans. pol.
unpol.	$q(= f_1)$ <b>number density</b> 		$f_{1T}^\perp$ <b>Sivers</b> 
long. pol.		$\Delta q(= g_{1L})$ <b>helicity</b> 	$g_{1T}$ <b>worm-gear-1</b> 
trans. pol.	$h_1^\perp$ <b>Boer-Mulders</b> 	<p>survive after integration over <math>k_T</math></p>	$\Delta_T q(= h_1)$ <b>transversity</b> 
		$h_{1L}^\perp$ <b>worm-gear-2</b> 	$h_{1T}^\perp$ <b>pretzelosity</b> 

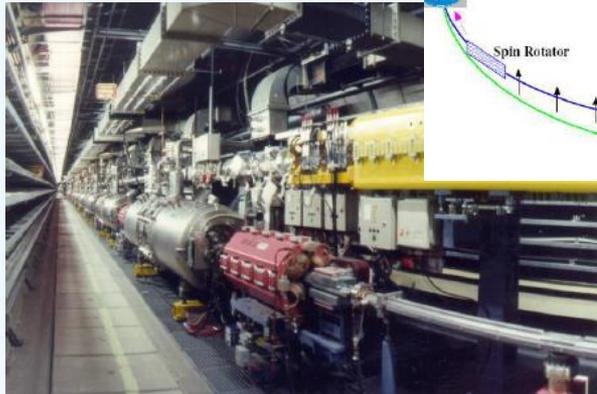
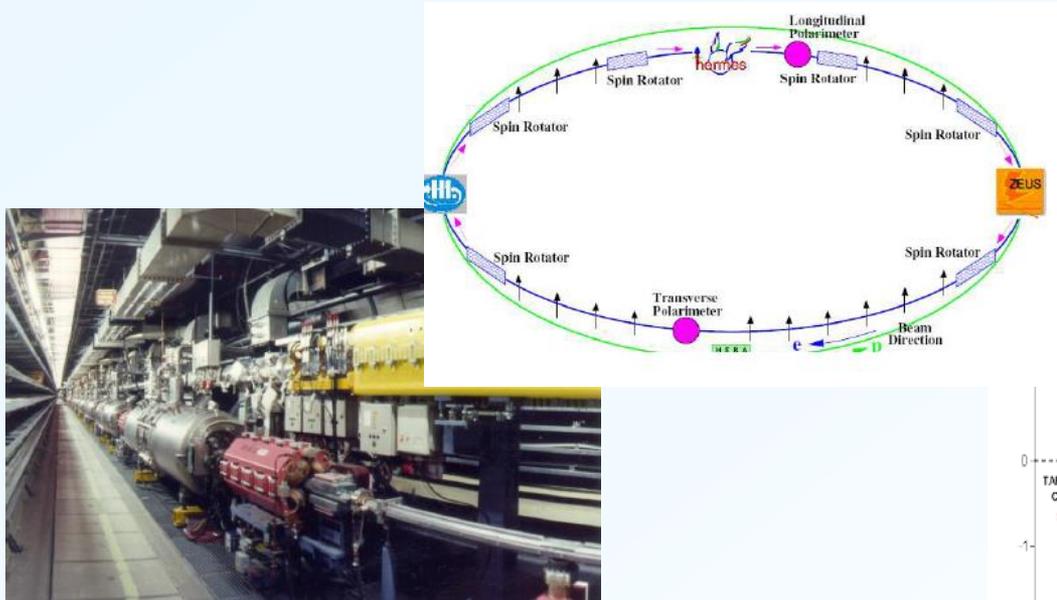
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# *The Major Experiments*

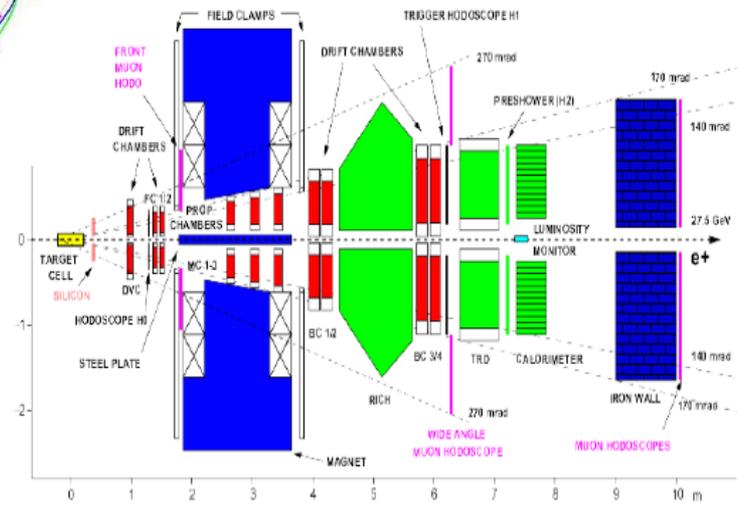
# HERMES



## DIS & SI-DIS experiment



**Detector:**  
 $\Delta p/p \sim 2\%$ ,  $\Delta\theta < 1$  mrad  
 hadron ID ( $\pi$ ,  $K$ ,  $p$ )



Pol.  $e^-$  &  $e^+$

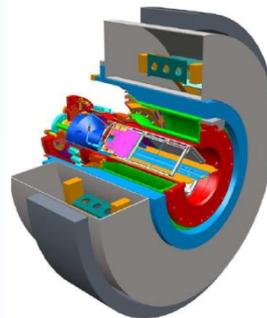
in **HERA** at 27 GeV

Gaseous internal target

Longit. Polar. 85% H, D, He

Transv. Polar H

Unpol H, D, Ne, Kr



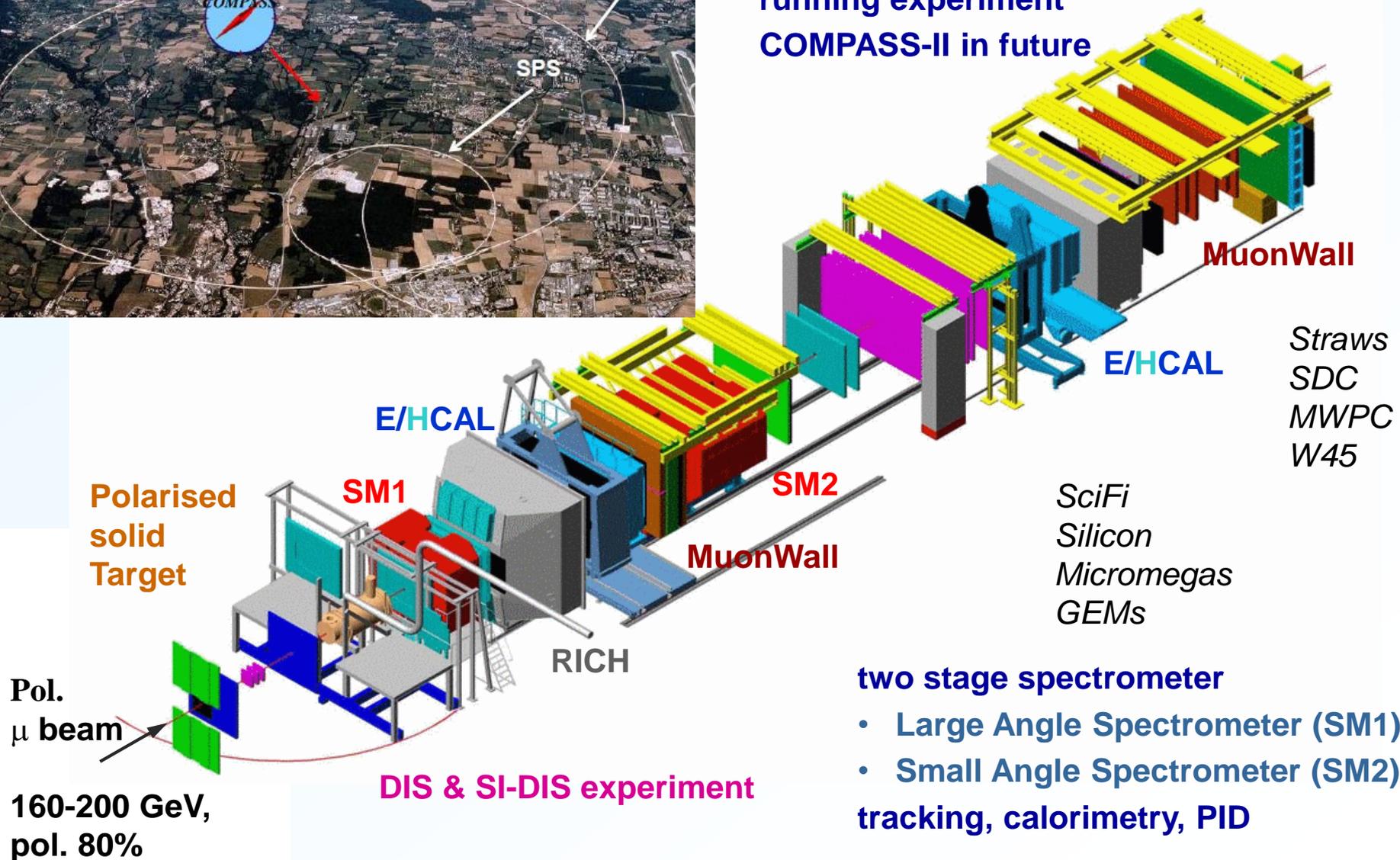
Recoil  
 Proton  
 Detector  
 for DVCS  
 measurements

**data taking: 1996-2007**  
**shutdown : 2007**  
**data analysis on going**

# COMPASS at CERN



data taking: 2002-  
running experiment  
COMPASS-II in future



**two stage spectrometer**

- Large Angle Spectrometer (SM1)
  - Small Angle Spectrometer (SM2)
- tracking, calorimetry, PID**

# JLab Experiments

6 GeV polarized  
electron beam  
Pol=85%, 180 $\mu$ A

several types  
of polarized  
targets  
→ various  
polarization  
experiments



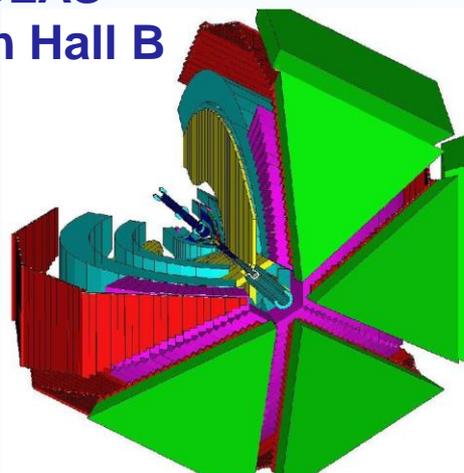
to be upgraded  
up to 12 GeV  
by 2014

Hall C



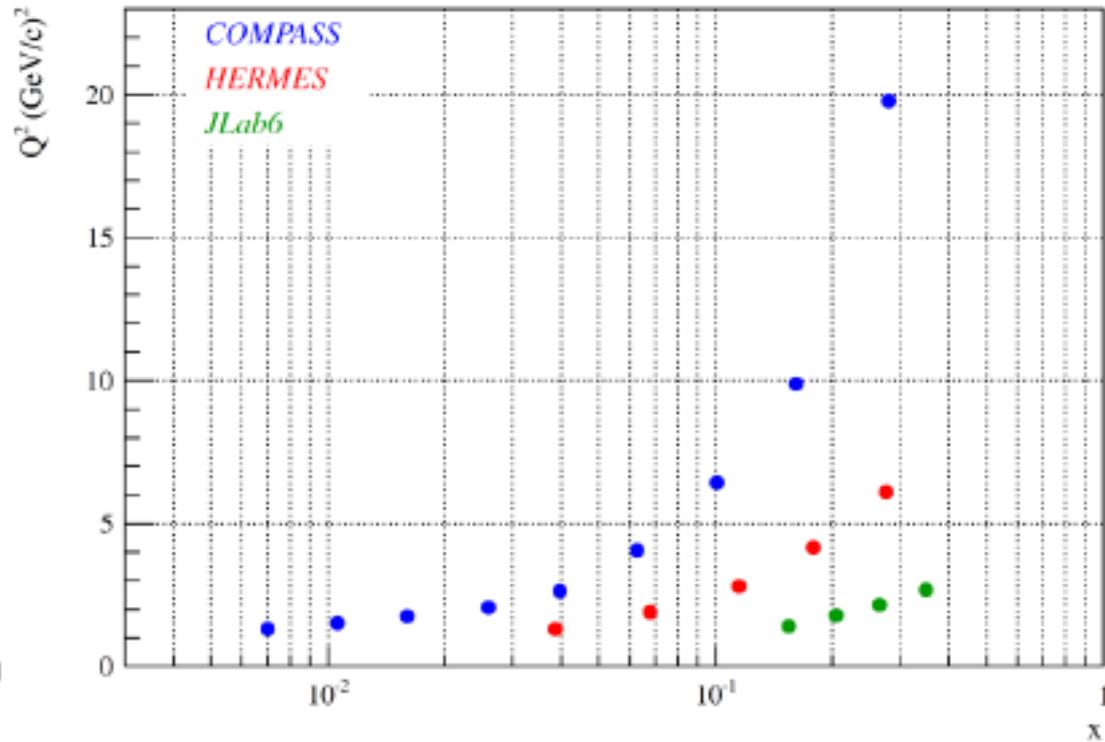
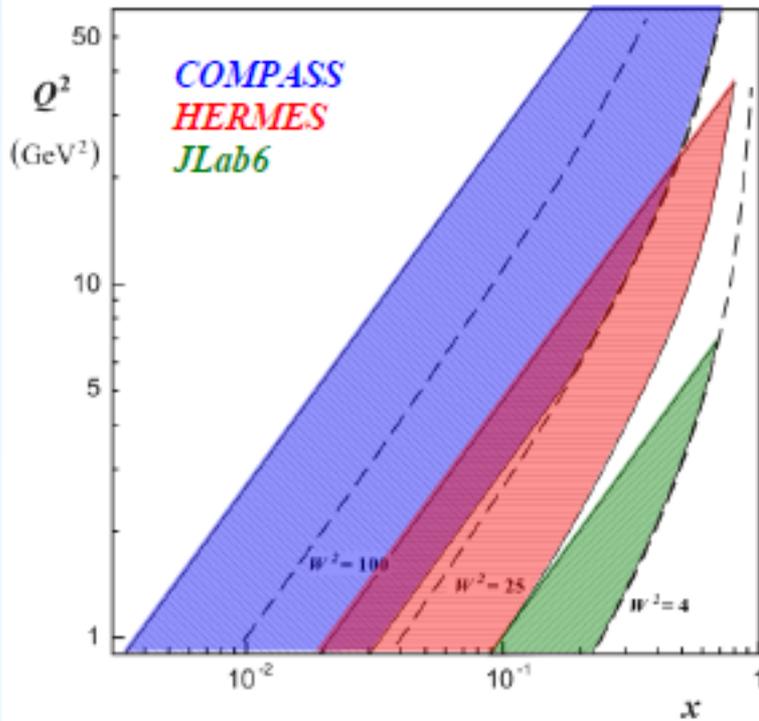
Hall A

CLAS  
in Hall B



E07-003

# Kinematical Coverage



These experiments are complementary

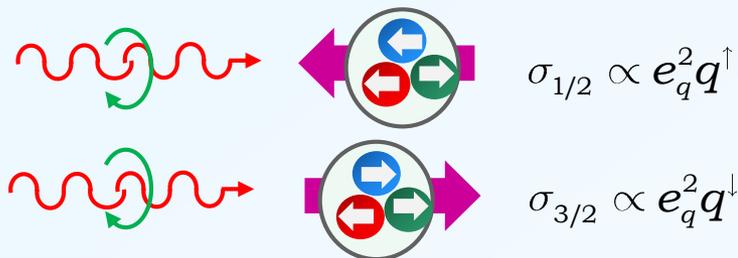
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# *Longitudinal Spin Structure*

# $g_1$ from Polarized Inclusive DIS

- Photon nucleon asymmetry

$$A_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}} \approx \frac{g_1(x)}{F_1(x)}$$



- Structure functions with PDF

$$F_1(x) = \frac{1}{2} \sum_q e_q^2 [q(x) + \bar{q}(x)]$$

$$g_1(x) = \frac{1}{2} \sum_q e_q^2 [\Delta q(x) + \Delta \bar{q}(x)]$$

**Polarized Structure Function**

with

$$q(x) = q^\uparrow(x) + q^\downarrow(x)$$

$$\Delta q(x) = q^\uparrow(x) - q^\downarrow(x)$$

- First moment of  $g_1$

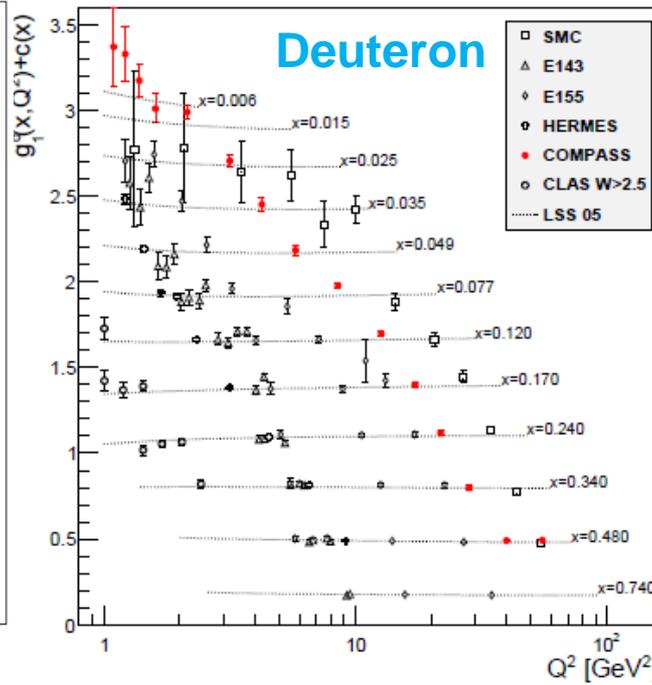
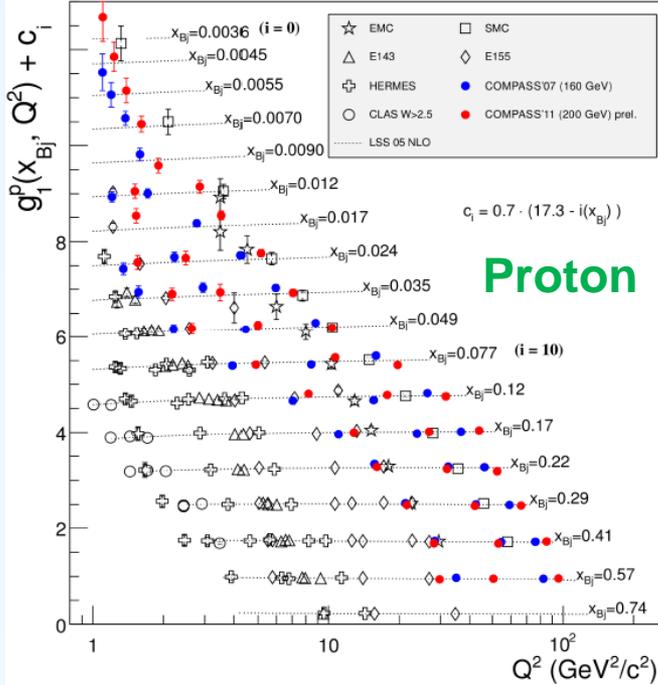
$$\Gamma_1 = \int_0^1 g_1(x) dx = \frac{1}{2} \sum_q e_q^2 \underbrace{\int_0^1 dx [\Delta q(x) + \Delta \bar{q}(x)]}_{\Delta q} \quad \text{with } \Delta q \equiv \int_0^1 dx \Delta q(x)$$

neutron-beta decay  
& hyperon decay constants,  
 $Q^2$  dependence by pQCD

$$\Delta\Sigma = \Delta u + \Delta d + \Delta s$$

**Quark Spin Contribution**

# World Data of $g_1$



$$\Delta\Sigma$$

$$= \Delta u + \Delta d + \Delta s$$

$$= 0.30 \pm 0.01 \pm 0.02$$

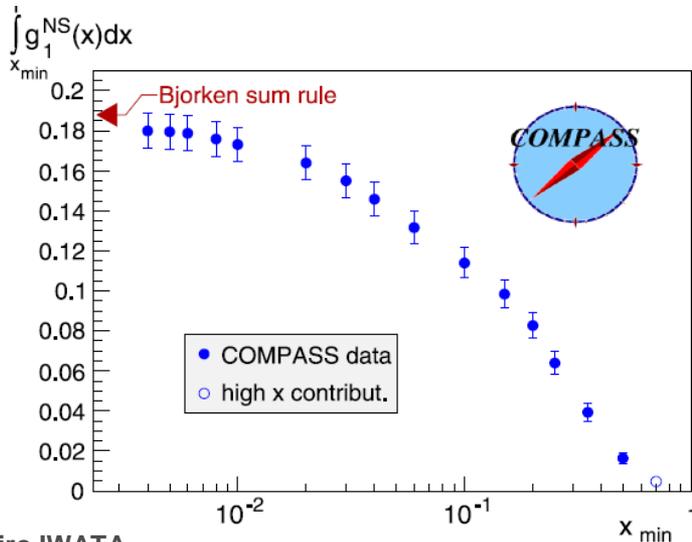
@  $Q^2 = 3 \text{ GeV} / c^2$

$$\Delta s + \Delta \bar{s}$$

$$= -0.08 \pm 0.01 \pm 0.02$$

$Q^2 \rightarrow \infty$

by COMPASS fit for all  $g_1$   
arXiv:hep-ex/0609038



**Bjorken sum rule**  
(QCD exact) well satisfied

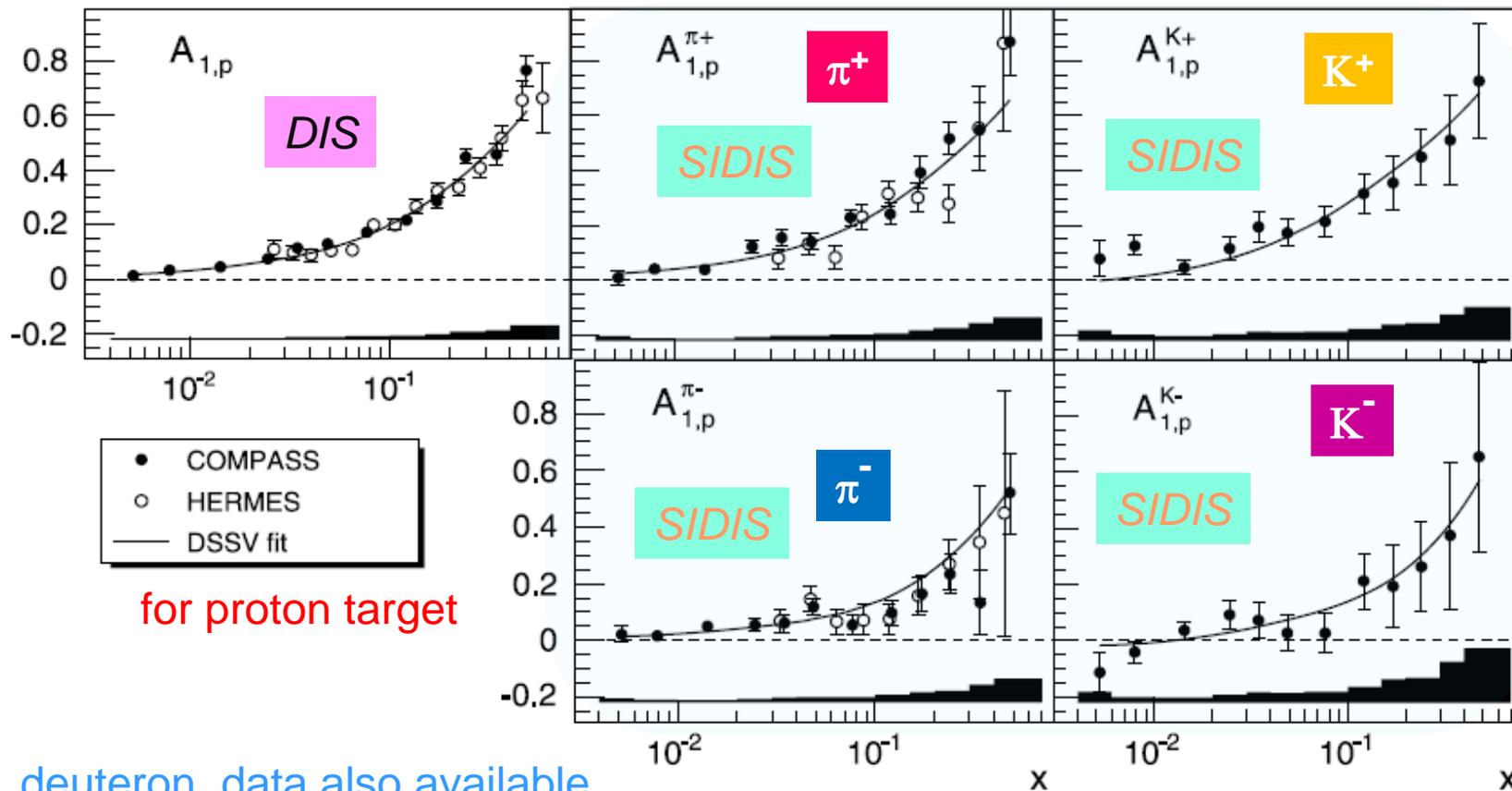
$$\Gamma_1^{NS} Q^2 \equiv \Gamma_1^p Q^2 - \Gamma_1^n Q^2$$

$$= \frac{1}{6} \left| \frac{g_V}{g_A} \right| C_1^{NS} Q^2$$

*QCD works well !*

COMPASS; Phys.Lett. B  
690(2010) 466-472

# Semi-Inclusive DIS Asymmetry



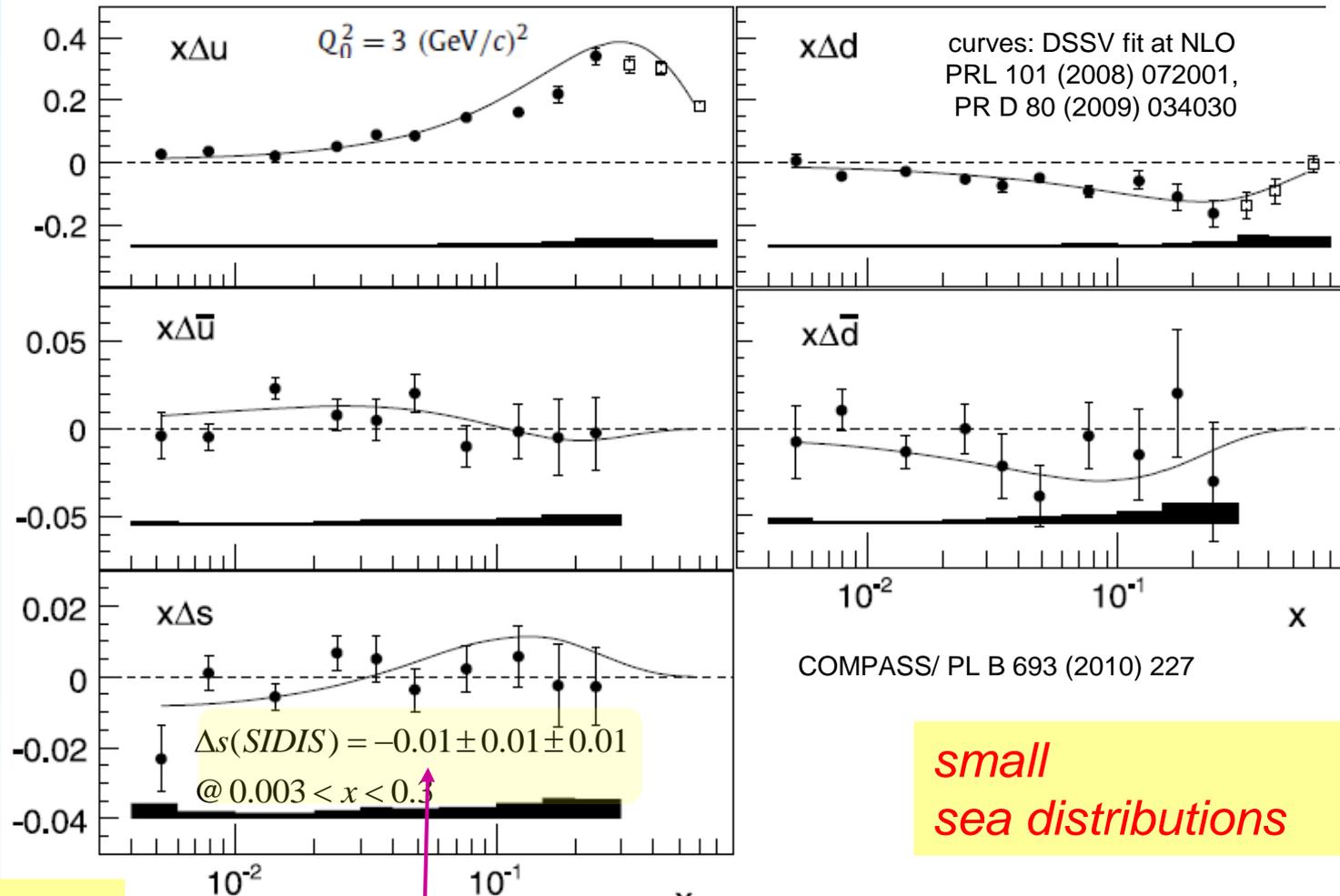
→ flavor decomposition

COMPASS Collaboration / *Physics Letters B* 693 (2010) 227–235

HERMES Collaboration, A. Airapetian, et al., *Phys. Rev. D* 71 (2005) 012003.

HERMES Collaboration, A. Airapetian, et al., *Phys. Rev. D* 75 (2007) 012007.

# Flavor Decomposition by COMPASS



COMPASS/ PL B 693 (2010) 227

*small sea distributions*

*strange sea not polarized*

$$2\Delta s(\text{Incl.}) = -0.08 \pm 0.02 \pm 0.02$$

arXiv:hep-ex/0609038

choice of FF ?

from DIS and SI-DIS for proton and deuteron

LO analysis

DSS fragmentation functions  
(Phys. Rev. D75 (2007) 114010)

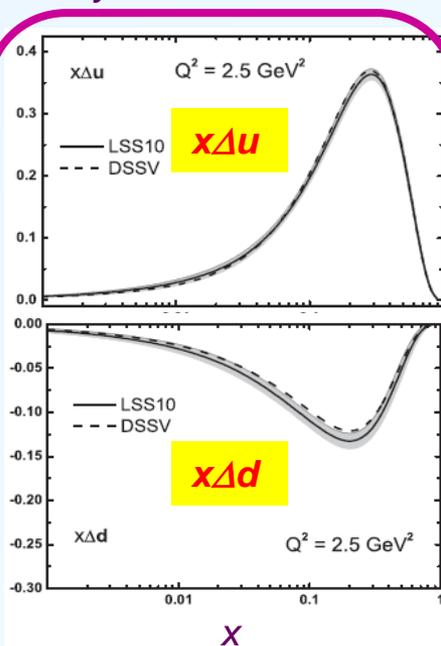
# Helicity Distributions from Global Analysis

PHYSICAL REVIEW D 82, 114018 (2010)

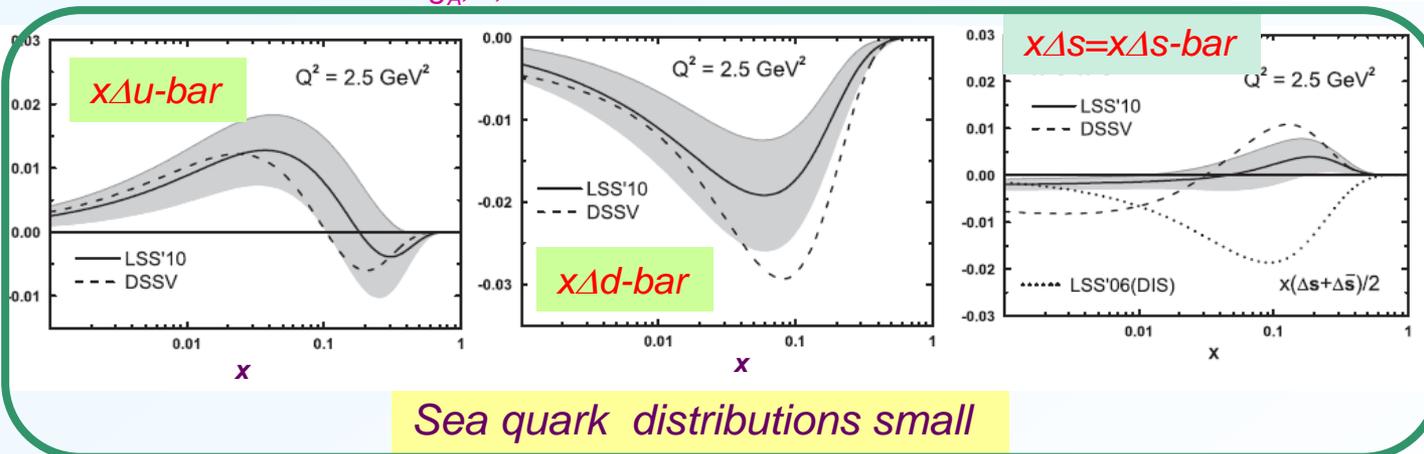
NLO QCD Analysis with DIS and SI-DIS data only,  
with  $g_A$ ,  $F, D$  constraints

$\overline{\text{MS}}$  scheme.

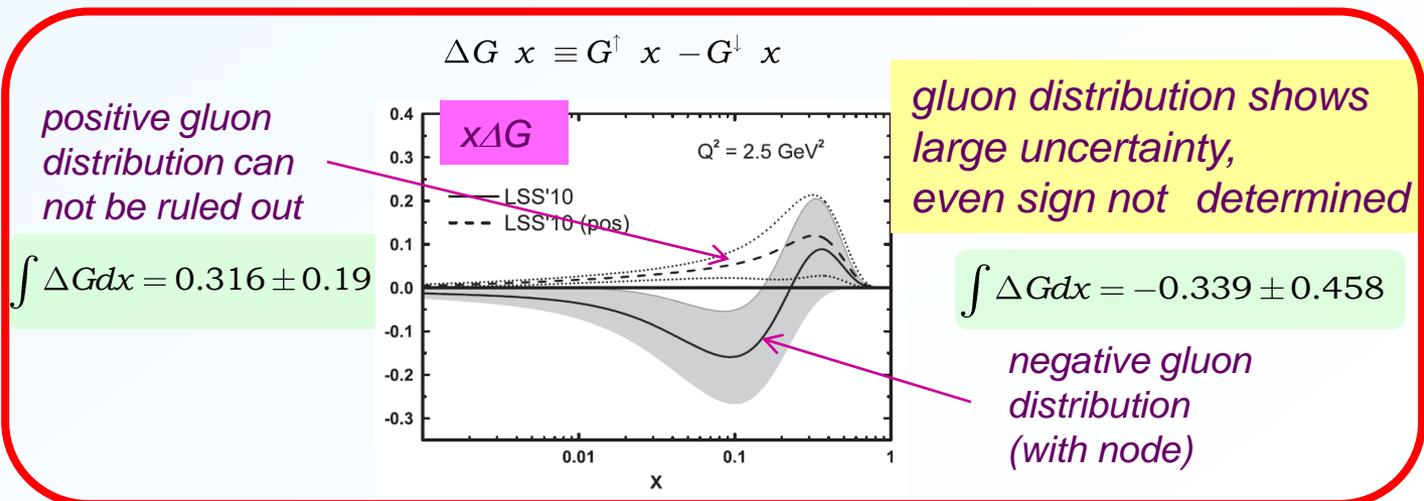
by LSS



$\Delta u$  and  $\Delta d$  well determined



Sea quark distributions small



positive gluon distribution can not be ruled out

$$\int \Delta G dx = 0.316 \pm 0.19$$

gluon distribution shows large uncertainty, even sign not determined

$$\int \Delta G dx = -0.339 \pm 0.458$$

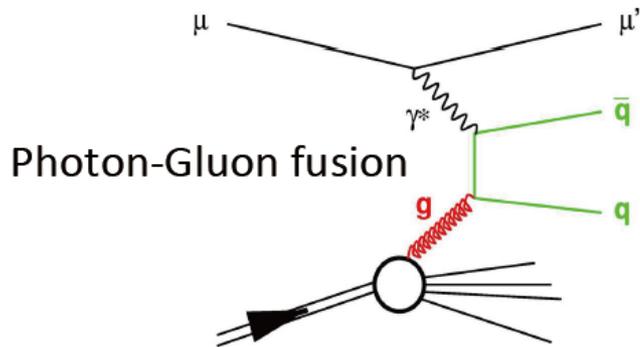
negative gluon distribution (with node)

$Q^2=4\text{GeV}^2$

Fit	$\Delta \bar{s}$	$\Delta G$	$\Delta \Sigma$
LSS10 (pos $x\Delta G$ )	$-0.063 \pm 0.004$	$0.316 \pm 0.190$	$0.207 \pm 0.034$
LSS10 (node $x\Delta G$ )	$-0.055 \pm 0.006$	$-0.339 \pm 0.458$	$0.254 \pm 0.042$

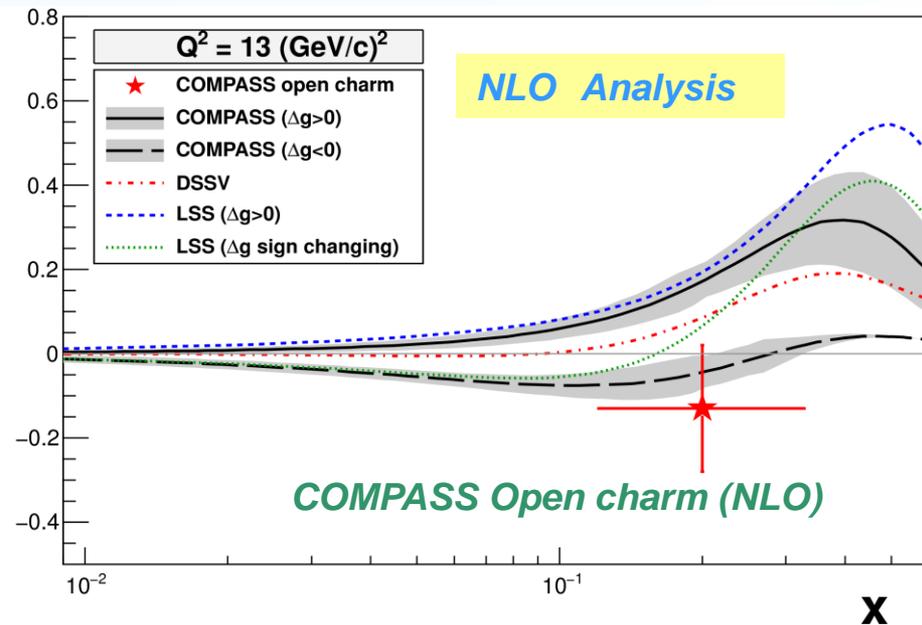
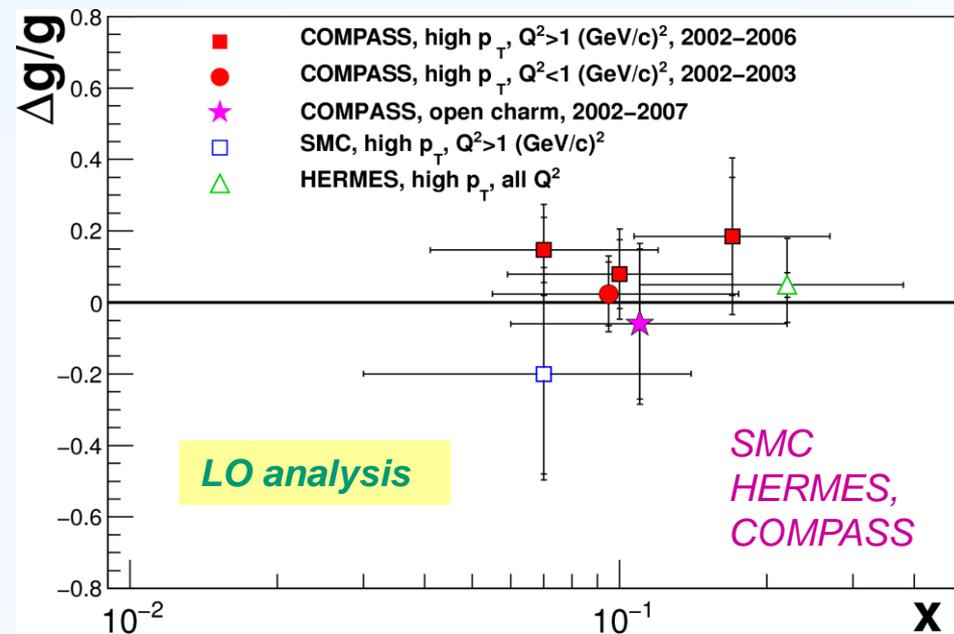
# Direct Measurement of Gluon Polarization

## Double Spin Asymmetry for Photon-Gluon fusion



The process is identified by  
*high Pt hadron pair events*  
 (COMPASS, SMC)  
*high Pt single hadron events*  
 (HERMES)  
*open charm events*  
 (COMPASS)

*compatible with zero-polarization in this range.*



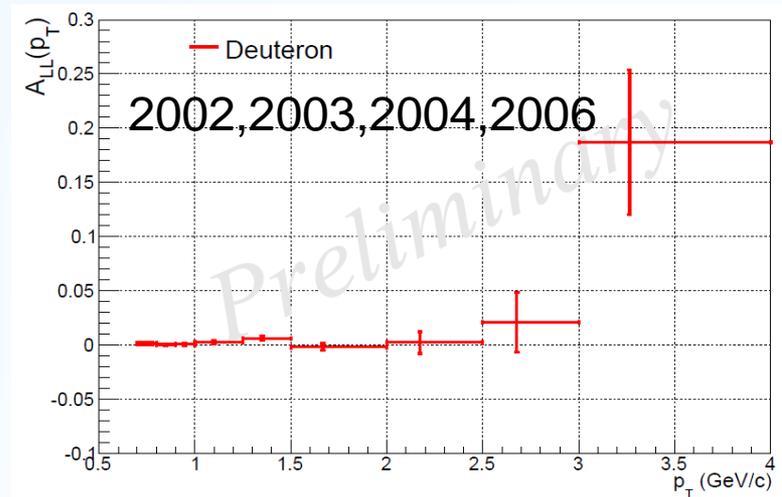
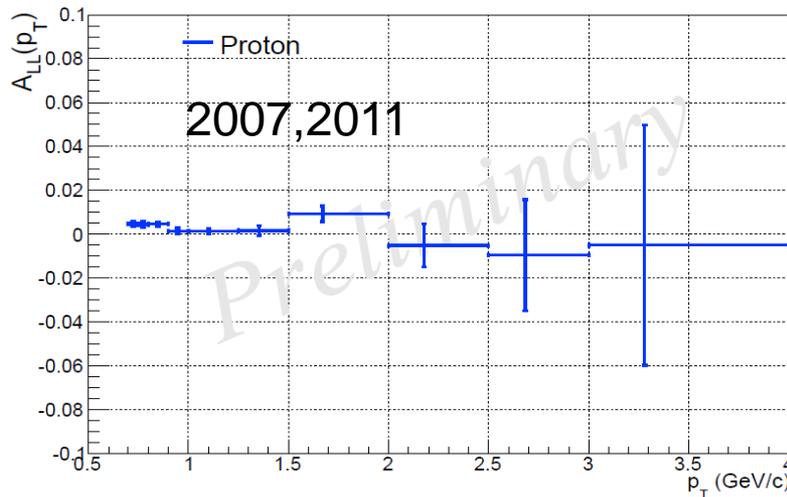
# $A_{LL}$ for Inclusive Single High $P_T$ Hadron



Low  $Q^2$  (photo production)  
based on the pQCD framework  
allowing a NLO extraction of  $\Delta G$

**VERY NEW!**

- $0.1 < y < 0.9$
- $Q^2 < 1 \text{ GeV}^2$
- $P_T > 0.7 \text{ GeV}/c$
- $z < 0.8$



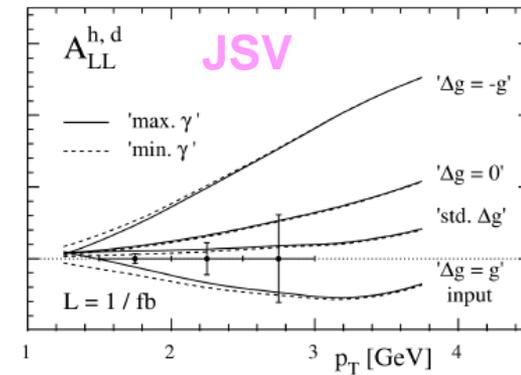
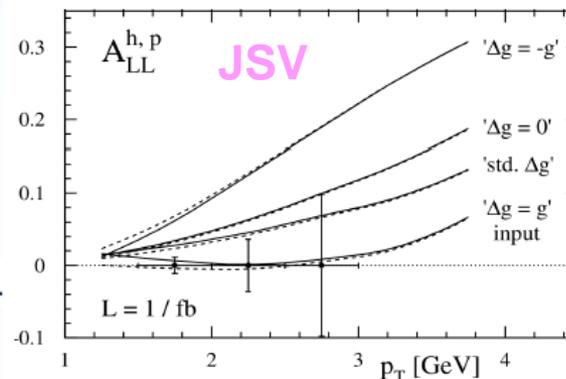
theoretical framework based on

Jäger, B. and Stratmann, M. and Vogelsang, W.,

Eur.Phys.J. **C44**, 533 (2005), hep-ph/0505157.

C. Hendlmeier, A. Schafer, and M. Stratmann,

Eur.Phys.J. **C55**, 597 (2008), arXiv:0803.1940.



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# *Transverse Spin Effects*

# Angular Modulation in SIDIS & PDFs

SIDIS for transv. pol. target gives angular modulation:

$$d\sigma_{SIDIS} \propto \left[ 1 + \underbrace{a_1 \cdot \sin \phi_C}_{\text{Collins}} + \underbrace{a_2 \cdot \sin \phi_S}_{\text{Sivers}} + \dots \right]$$

$$A_{\text{Coll}} \approx \frac{\sum_q e_q^2 \cdot \Delta_T q \cdot \Delta_T^0 D_q^h}{\sum_q e_q^2 \cdot q \cdot D_q^h}$$

Transversity (points to  $\Delta_T q$ )  
Collins F.F. (points to  $\Delta_T^0 D_q^h$ )

$$A_{\text{Siv}} \approx \frac{\sum_q e_q^2 \cdot f_{1T,q}^\perp \cdot D_q^h}{\sum_q e_q^2 \cdot q \cdot D_q^h}$$

Sivers PDF (points to  $f_{1T,q}^\perp$ )

**Collins angle:** Azim. angle of a hadron wrt struck quark spin

$$\Phi_C = \phi_h - \phi_{S'} \quad (= \phi_h + \phi_S - \pi)$$

**Sivers angle:** Azim. angle of a hadron wrt nucleon spin

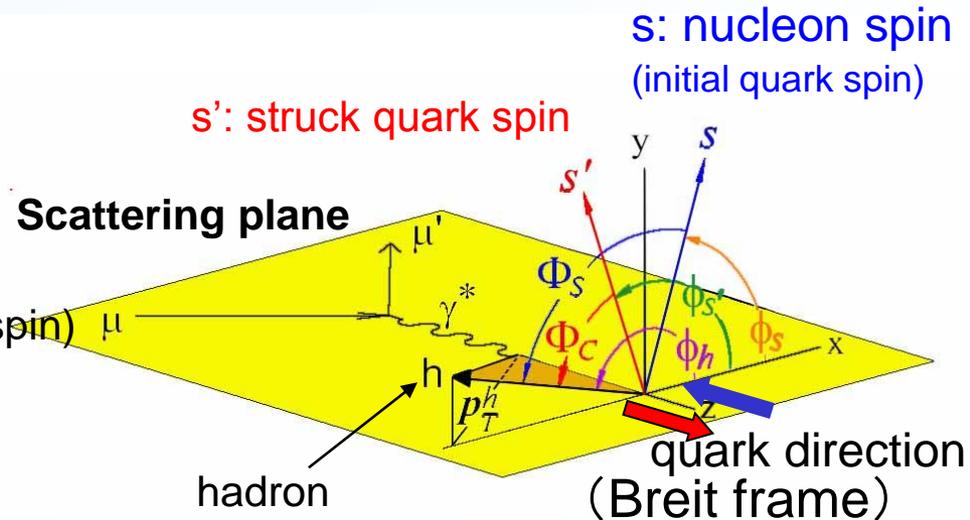
$$\Phi_S = \phi_h - \phi_S$$

$\phi_S$  = azim. angle of nucleon spin (initial quark spin)

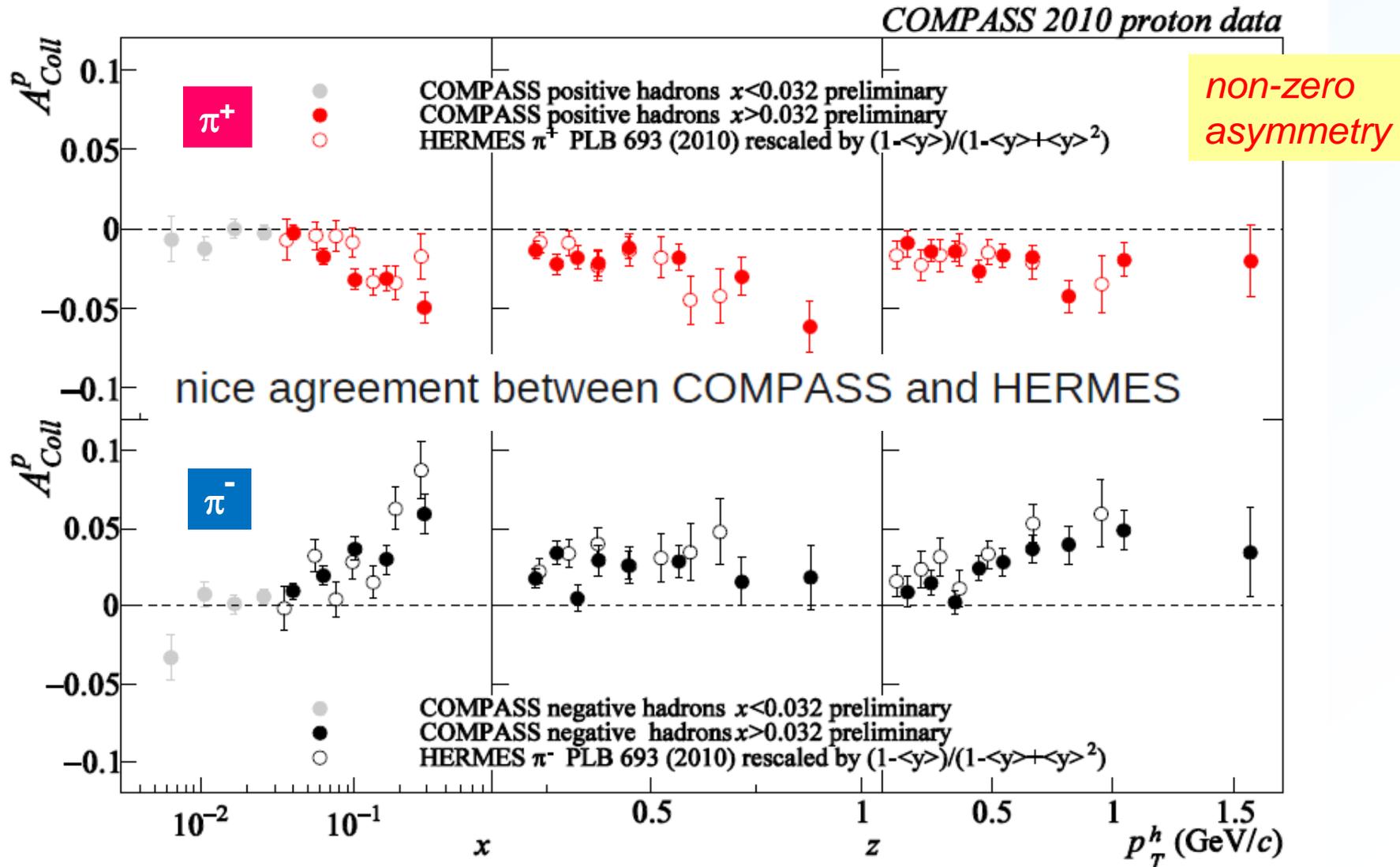
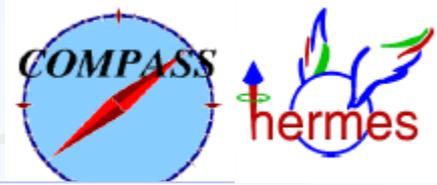
$\phi_{S'}$  = azim. angle of struck quark spin

$\phi_S = \pi - \phi_{S'}$  (due to helicity conservation)

$\phi_h$  = azim. angle of leading hadron

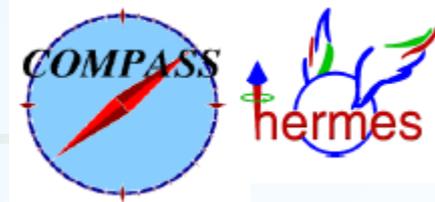


# Collins Asymmetry



Deuteron data also available from COMPASS

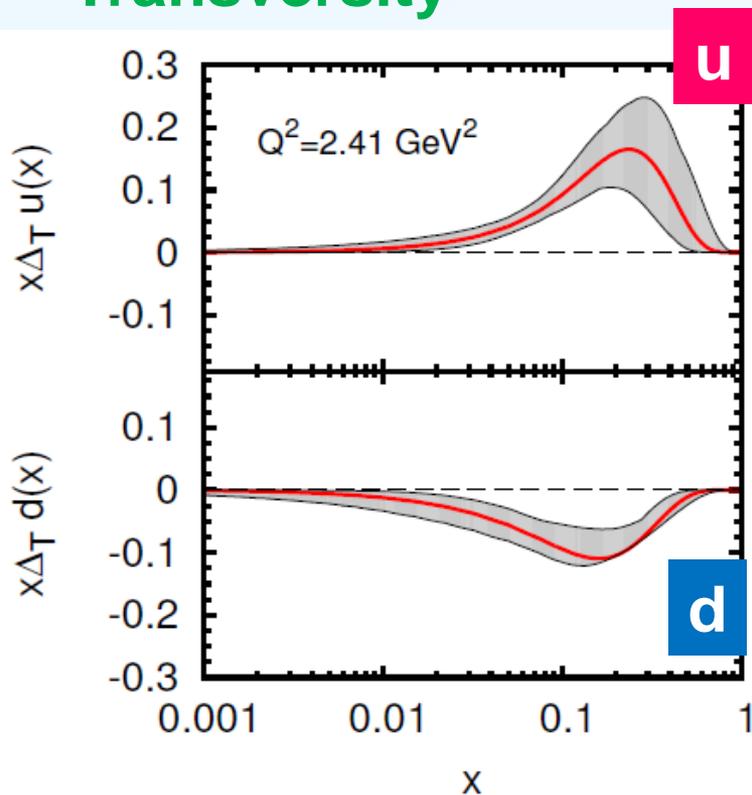
# Transversity Global Analysis



M. Anselmino et al., PRD87 (2013) 094019

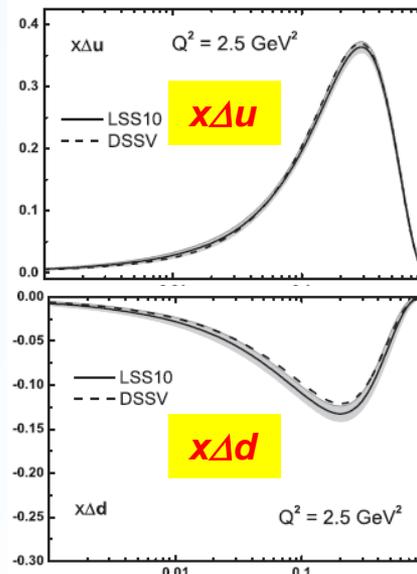
- fit to  $A_{\text{coll}}^{p,d}$  from COMPASS,  $A_{\text{Coll}}^p$  from HERMES and BELLE data ( $e^+e^- \rightarrow h_1 h_2 X$ )

## Transversity

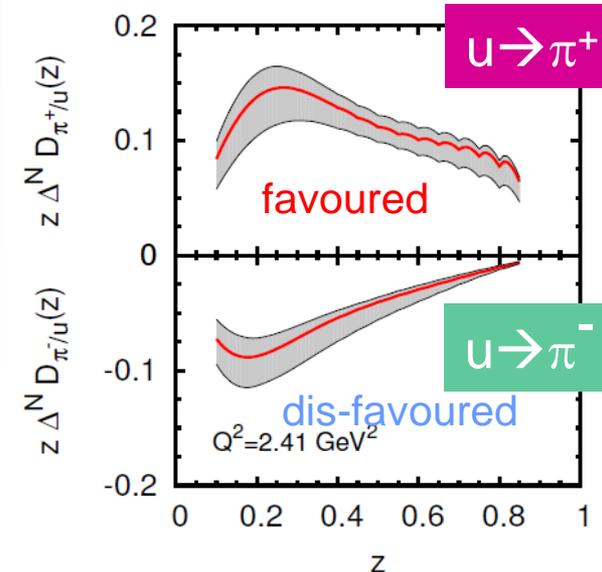


*Opposite signs*  
*Similar shapes to Helicity PDF*  
*But intensities slightly smaller*

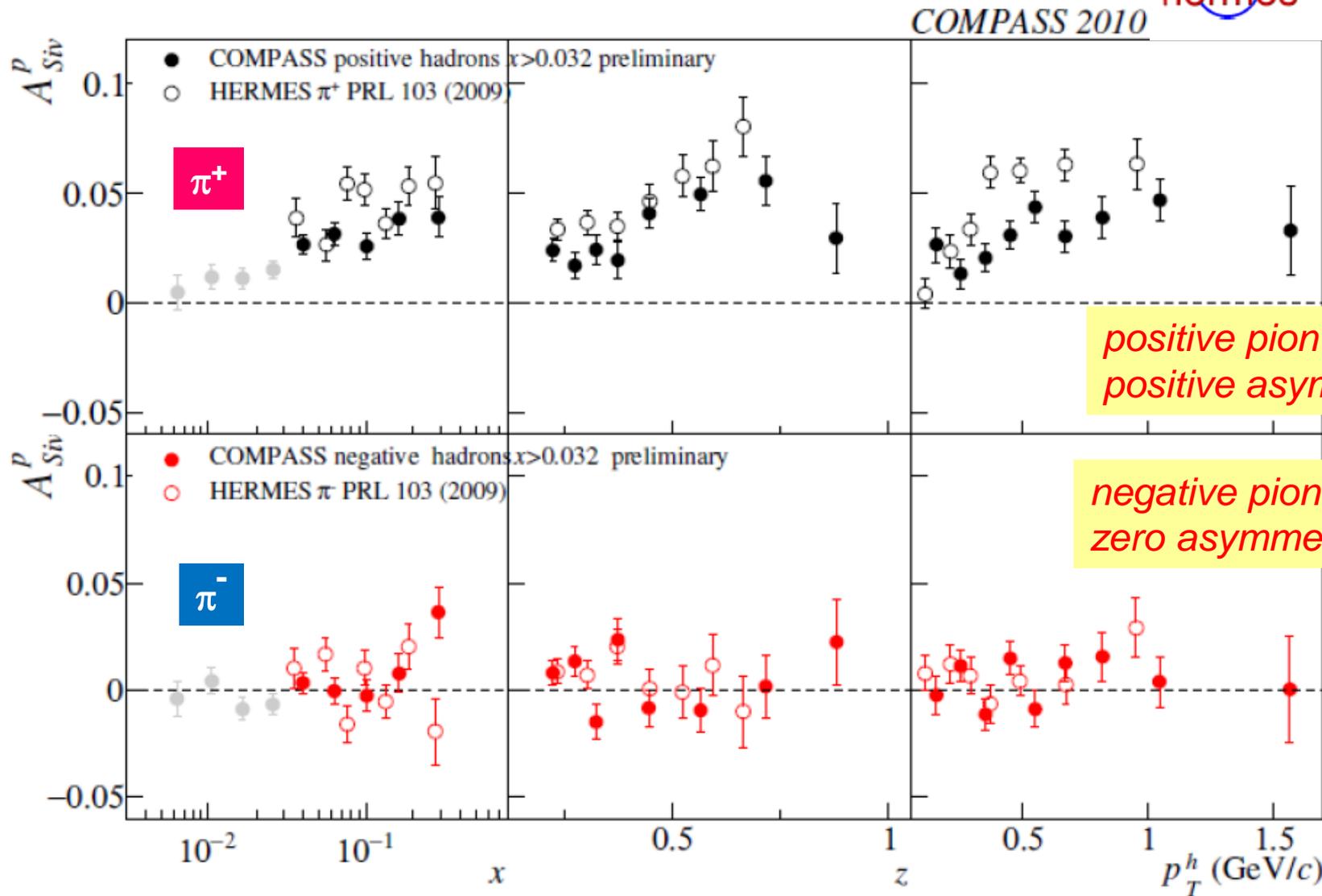
## Helicity PDF



## Collins F.F.



# Sivers Asymmetry



*Deuteron data also available from COMPASS*

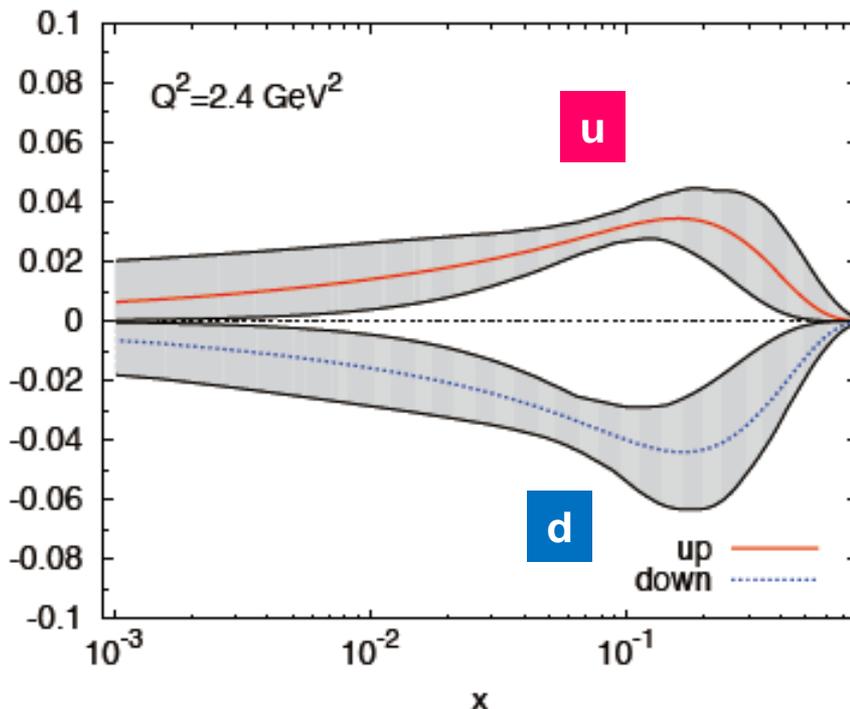
# Sivers PDF Global Analysis

M. Anselmino, QNP2012

fit to  $A_{\text{Siv.}}^{p,d}$  from COMPASS,  
 $A_{\text{Siv.}}^p$  from HERMES

*Sivers PDF*  
*( $k_T^2$  integrated)*

$x \Delta^N f_q^{(1)}(x, Q)$



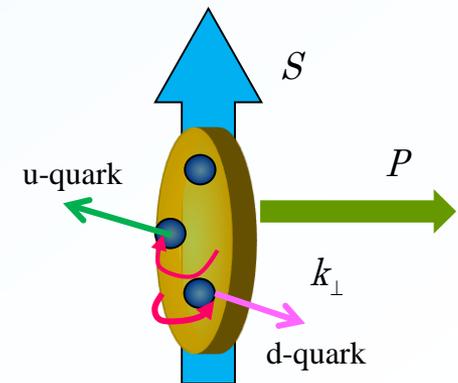
$$\Delta^N f_q^{(1)}(x, Q)$$

$$= \int d^2 \mathbf{k}_\perp \frac{k_\perp}{4M_p} \Delta^N \hat{f}_{q/p^\uparrow}(x, k_\perp; Q)$$

$$= -f_{1T}^{\perp(1)q}(x, Q)$$

Sivers: distribution of unpol. quarks in  $\perp$  pol. proton

$$f_{q/p^\uparrow}(x, \mathbf{k}_\perp) = f_1^q(x, k_\perp^2) - f_{1T}^{\perp q}(x, k_\perp^2) \frac{(\hat{\mathbf{P}} \times \mathbf{k}_\perp) \cdot \mathbf{S}}{M}$$



*u-quark and d-quark  
 give opposite  $k_T$   
 w.r.t. the proton spin*

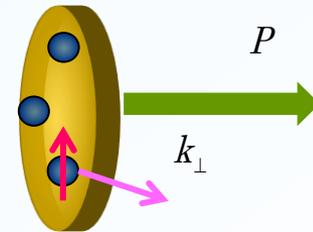
# Asymmetry related to Boer-Mulders PDF

**Boer-Mulders PDF** : transverse spin & transverse momentum of the quark  
 ← access through SIDIS on un-polarized nucleon

$$\frac{d\sigma}{p_T^h dp_T^h dx dy dz d\phi_h} =$$

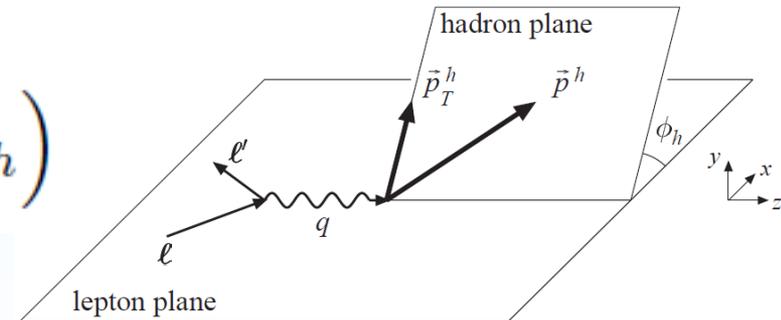
**BM x Collins FF** +  
 Cahn effect (kinematical effect from  $k_T$ )

$$A_{\cos\phi_h}^{UU} = \frac{1}{Q} \text{Cahn} + \frac{1}{Q} \text{BM}$$



$$h_1^q(x, k_\perp^2) > 0$$

$$\sigma_0 \left( 1 + \epsilon_1 A_{\cos\phi_h}^{UU} \cos\phi_h + \epsilon_2 A_{\cos 2\phi_h}^{UU} \cos 2\phi_h + \lambda \epsilon_3 A_{\sin\phi_h}^{LU} \sin\phi_h \right)$$



in the  $\gamma^* N$  system

**BM x Collins FF**  
 + twist4 Cahn effect

$$A_{\cos 2\phi_h}^{UU} = \text{BM} + \frac{1}{Q^2} \text{Cahn}$$

# COS $\phi$ Asymmetry from HERMES



for proton & deuteron targets

$\pi^+/\pi^-$  difference  
 → may be due to BM effects  
 (Cahn expected to be flavor blind)

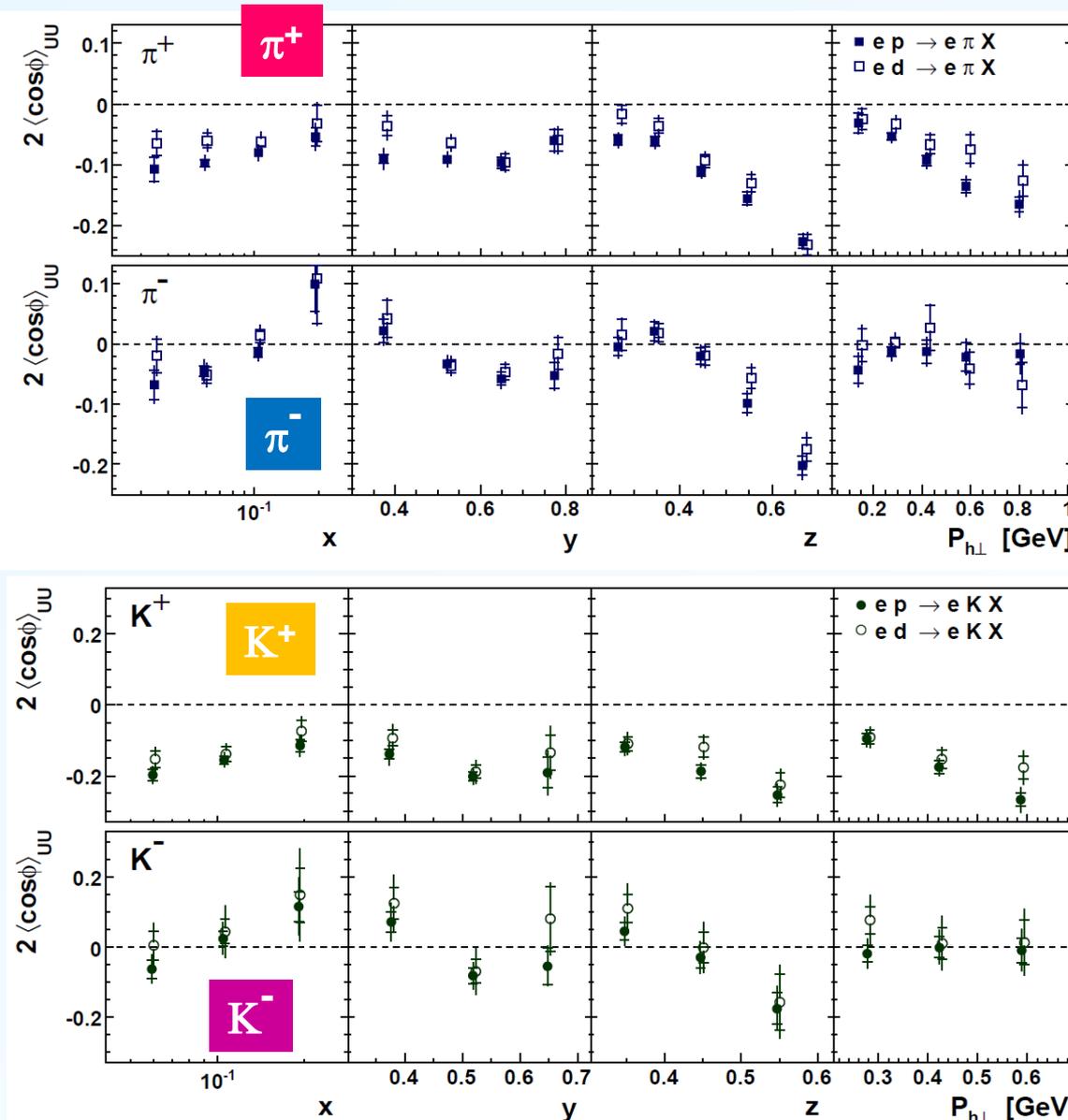
$$A_{UU}^{\cos\phi_h} \propto$$

$$\frac{M}{Q} \left\{ -h_1^{\perp q} \otimes H_{1q}^{\perp} - f_1^q \otimes D_{1q}^h \right\}$$

BM Cahn

$K^+$  : larger than  $\pi^+$   
 $K^-$  : compatible with 0

Phys. Rev. D 87,  
 012010 (2013)

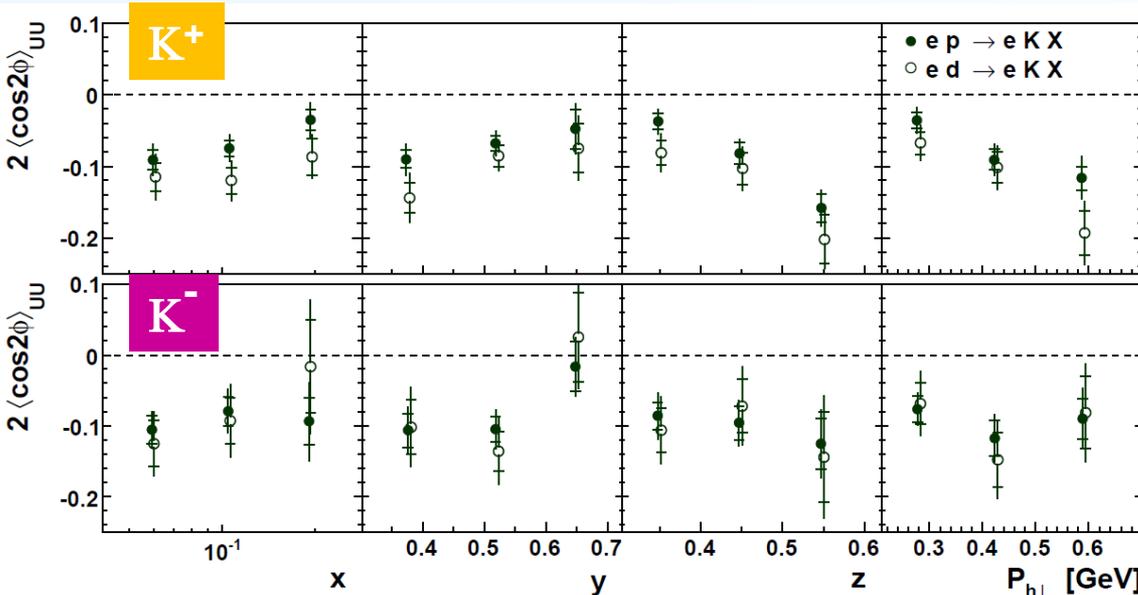
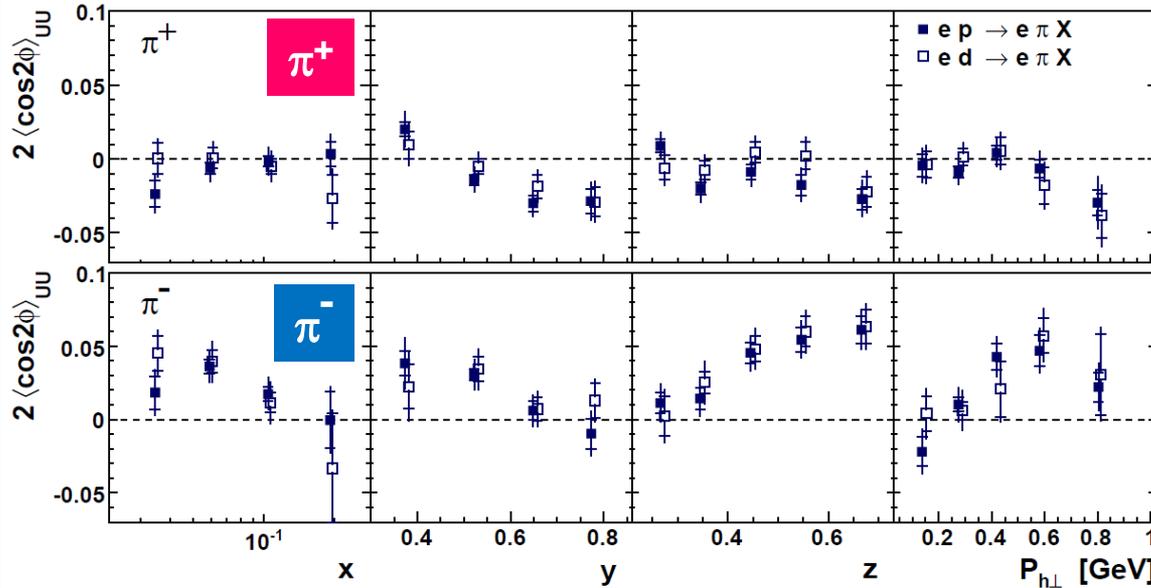


# COS 2φ Asymmetry from HERMES



for proton & deuteron targets

$\pi^+$ : zero or negative  
 $\pi^-$ : positive, large signal  
 $\rightarrow$  non-zero BM



$$A_{UU}^{\cos 2\phi_h} \propto$$

$$-h_1^{\perp q} \otimes H_{1q}^{\perp} + \left(\frac{M}{Q}\right)^2 f_1^q \otimes D_{1q}^h$$

BM

Cahn

$K^+/K^-$ : larger than  $\pi^+/\pi^-$

Phys. Rev. D 87,  
012010 (2013)

# Asymmetry on deuteron from COMPASS



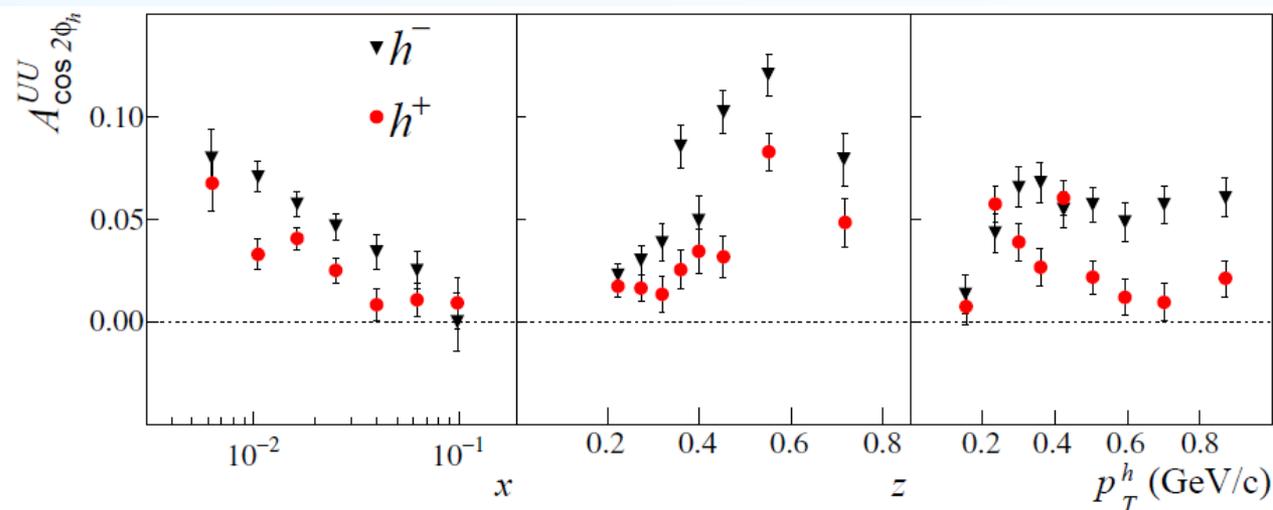
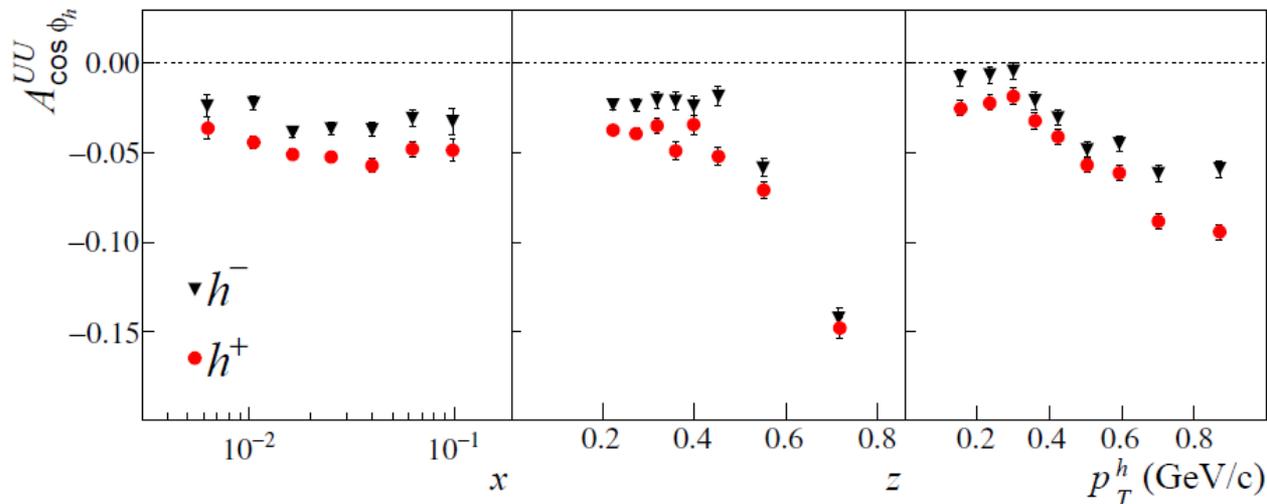
COMPASS 2004  ${}^6\text{LiD}$

CERN-PH-EP-2014-009

*negative for  $h^+/h^-$   
strong  $z$  dependence*

*similar trends to  
HERMES data  
in overlapping region*

*positive for  $h^+/h^-$   
strong dependence  
on kinematical variables*



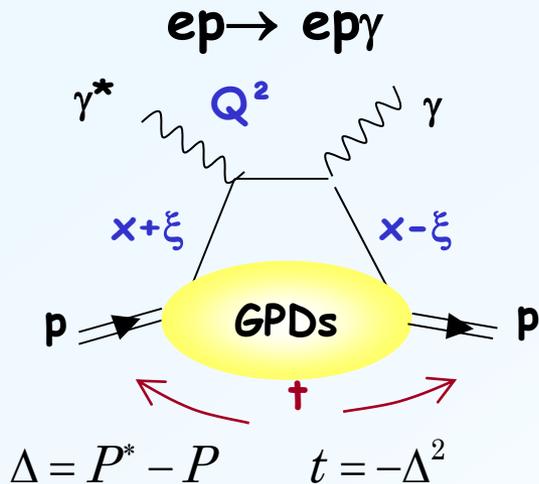
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# *GPD Studies*

# GPD & DVCS

Generalized Parton Distribution (GPD) → a key concept for nucleon structure access through Deeply Virtual Compton Scattering (DVCS)

→ In experiments, hard exclusive photon production should be studied



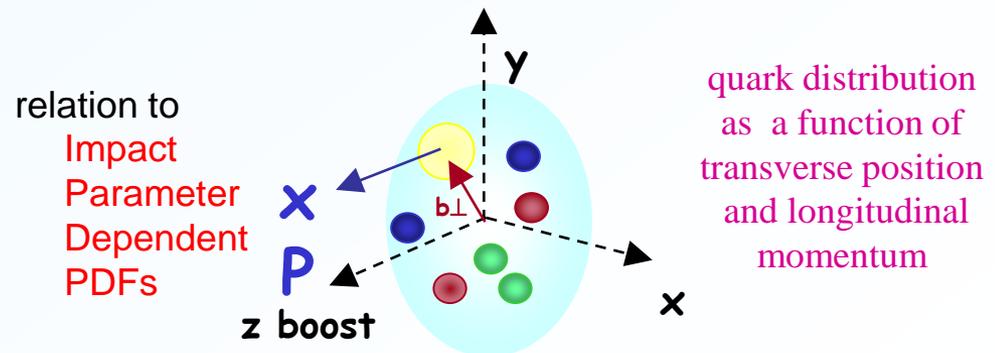
**GPDs: (in twist-2 level)**

Vector	$H^q(x, \xi, t)$
Tensor	$E^q(x, \xi, t)$
Axial vector	$\tilde{H}^q(x, \xi, t)$
Pseudo scalar	$\tilde{E}^q(x, \xi, t)$

give total angular momentum of quarks

$$\lim_{t \rightarrow \infty, \xi \rightarrow 0} \frac{1}{2} \int_{-1}^1 x \left[ H^q(x, \xi, t) + E^q(x, \xi, t) \right] dx = J^q$$

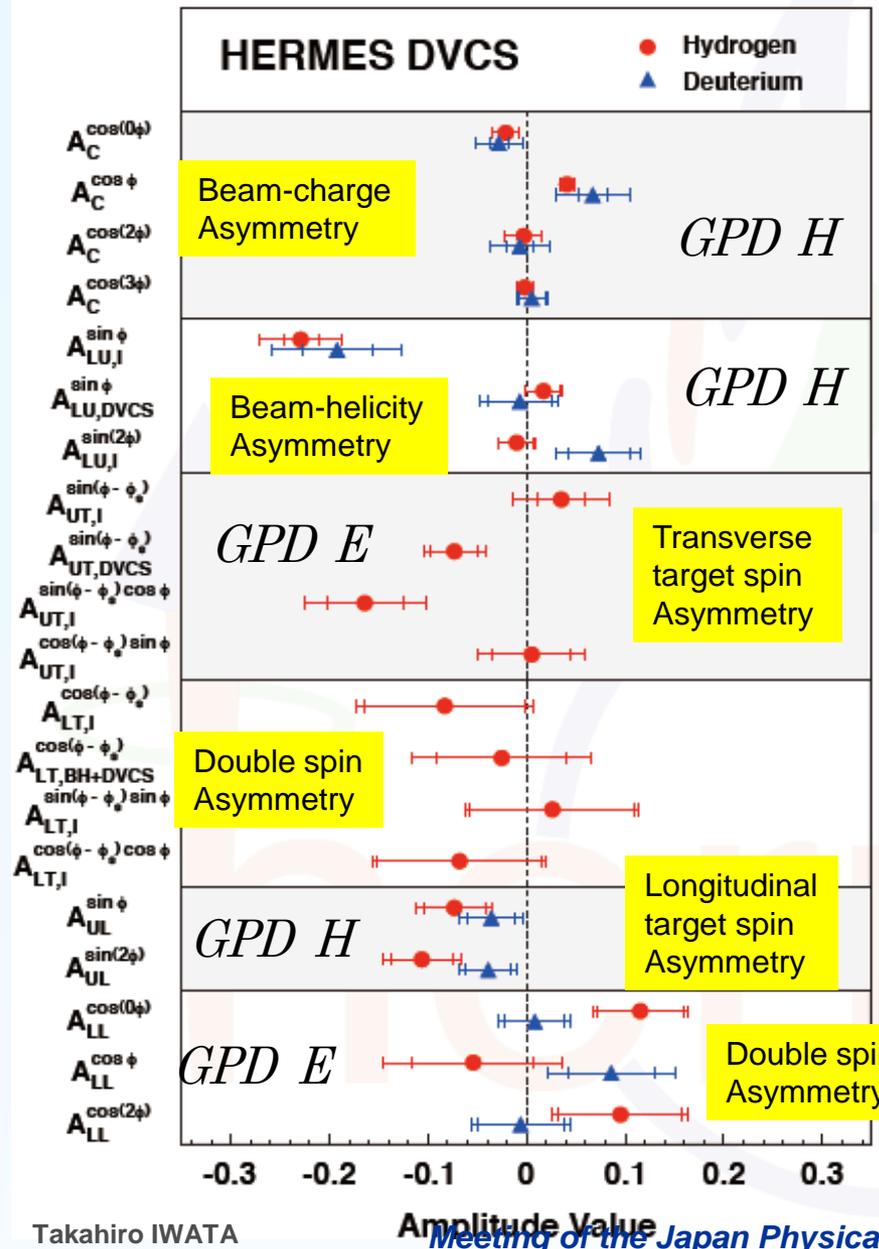
[10] X. Ji: J. Phys. G 24 (1998) 1181.



BURKARDT M., *Phys. Rev. D*, 66 (2002) 114005.  
 BURKARDT M., *Int. J. Mod. Phys. A*, 18 (2003) 173.

→ 3D picture

# DVCS Data Accumulated by HERMES

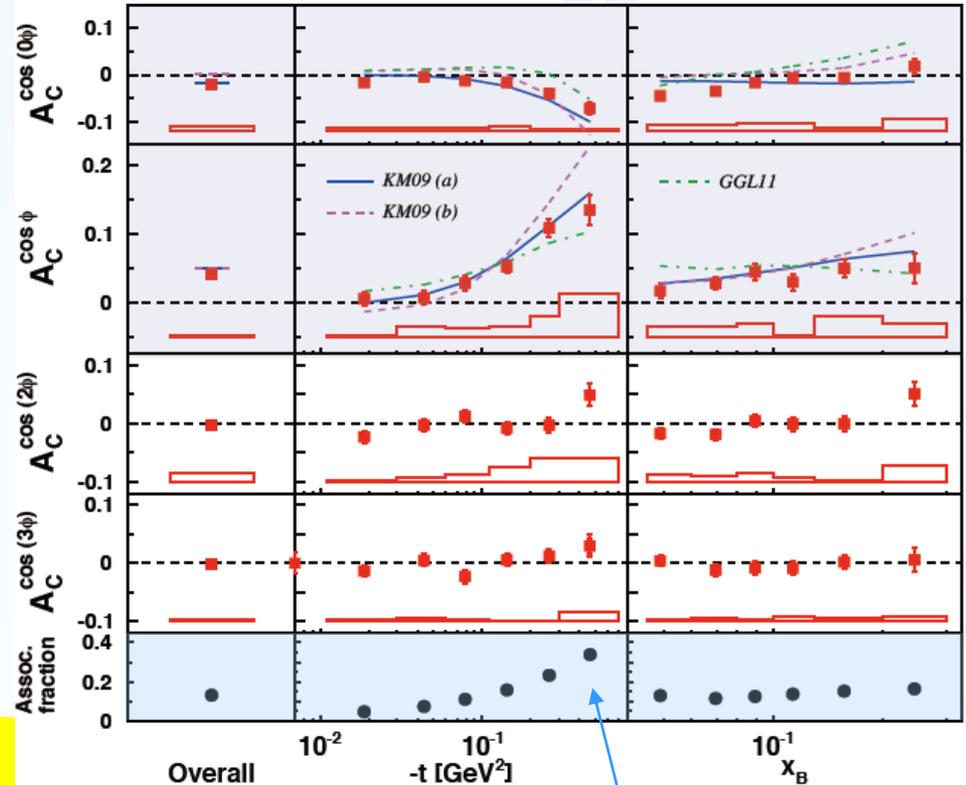


Pioneering work by HERMES

Hard Exclusive Photon Production identified with missing mass technique

Beam-charge Asymmetry

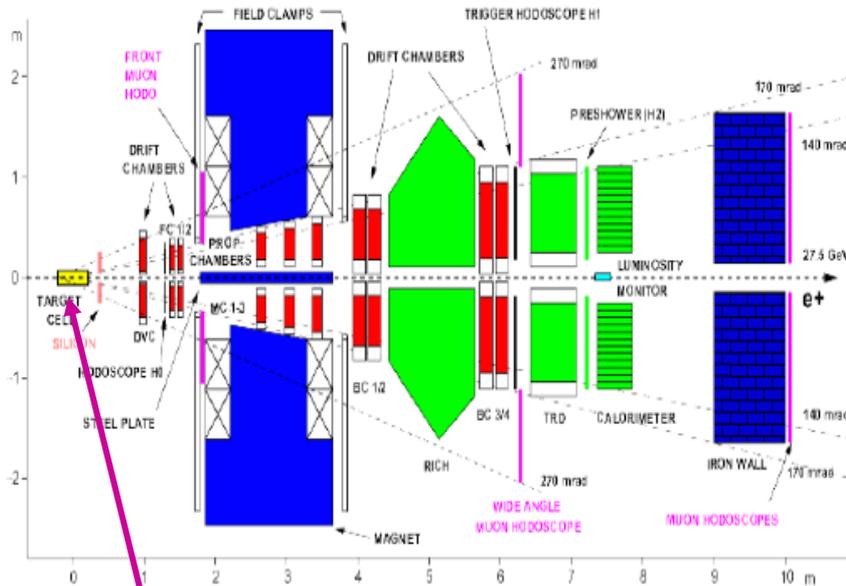
[Airapetian et al., JHEP 07 (2012) 032]



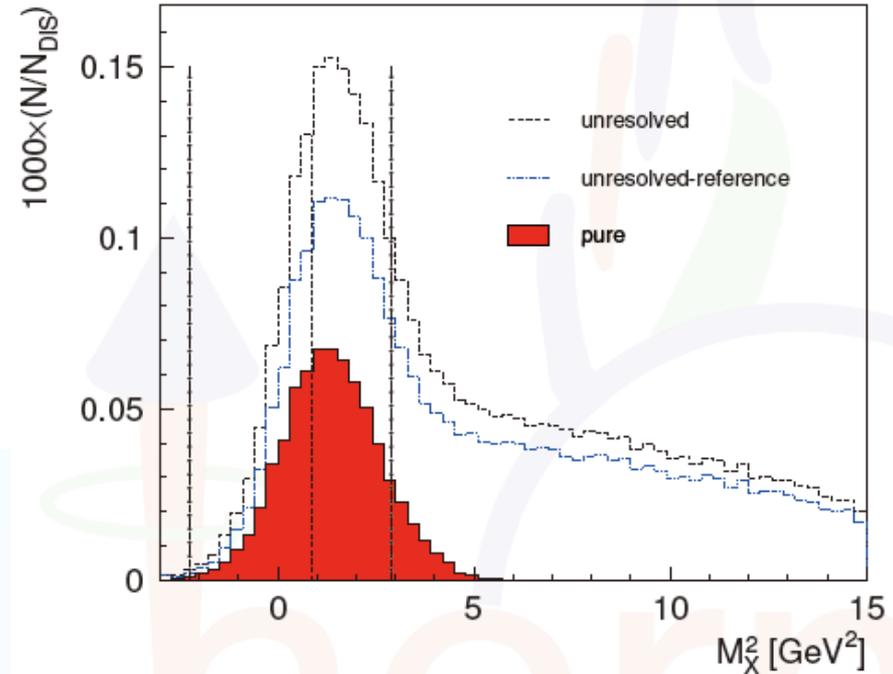
Resonant fraction :  $e p \rightarrow e \Delta^+ \gamma$

Courtesy: G.Shnell, DVCS 2014

# The Recoil Detector at HERMES



kinematic fitting



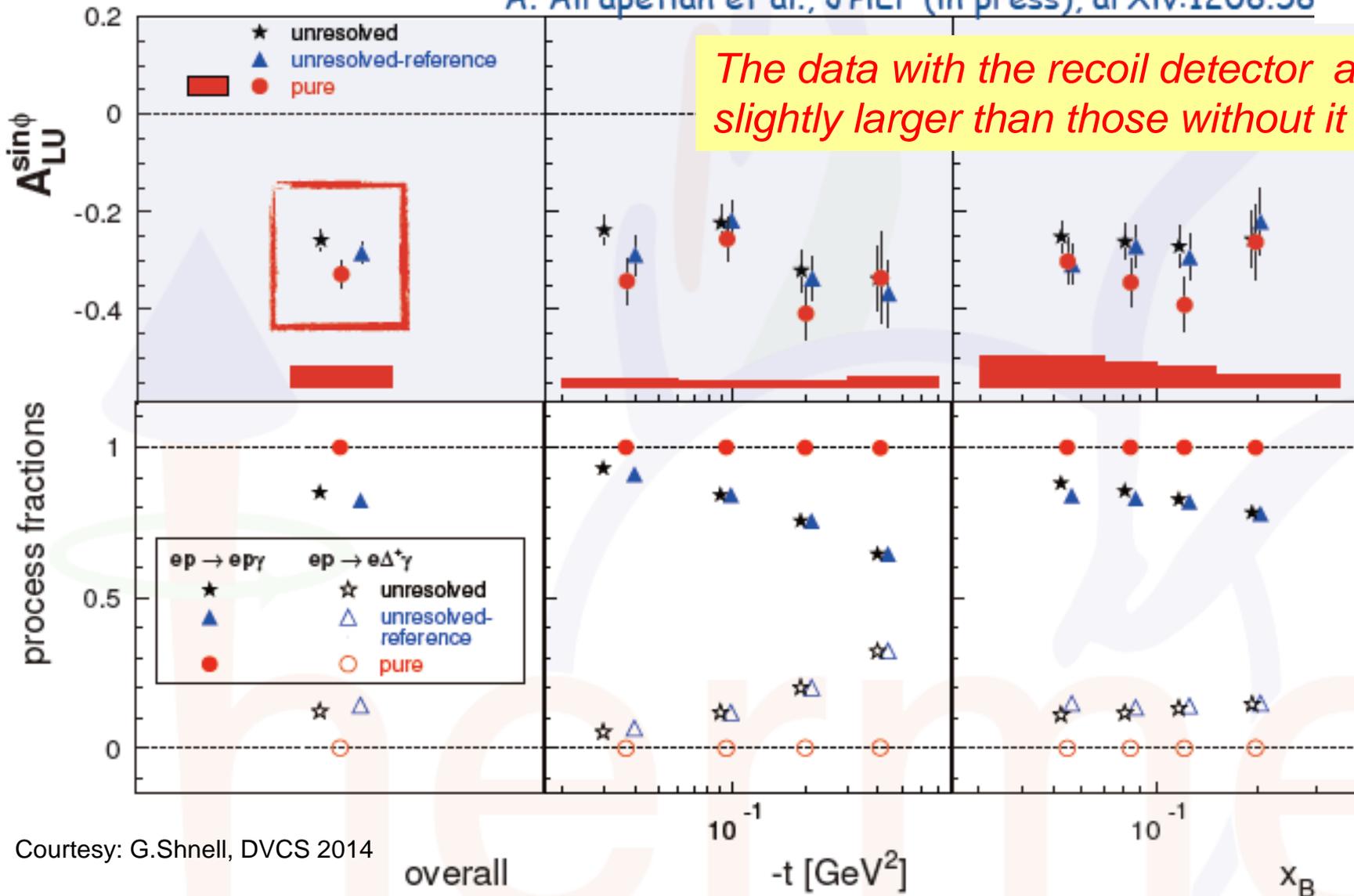
Courtesy: G.Shnell, DVCS 2014

- \* Selection of pure BH/DVCS( $ep \rightarrow ep\gamma$ ) with high efficiency
- \* Allows to suppress background to a negligible level ( $<0.2\%$ )

# Data with Recoil Detector at HERMES



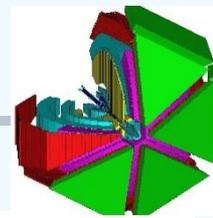
A. Airapetian et al., JHEP (in press), arXiv:1206.56



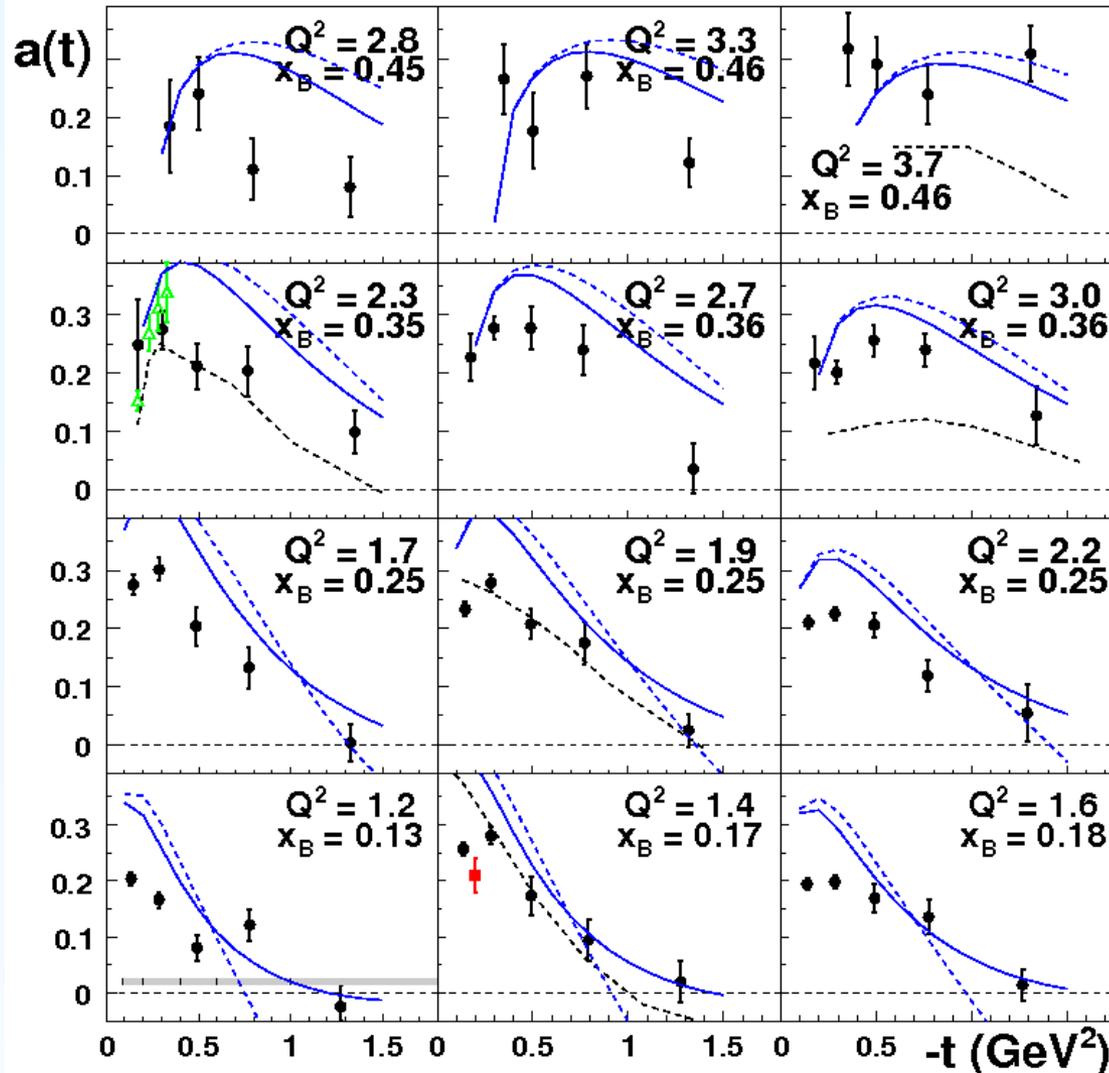
*The data with the recoil detector are slightly larger than those without it*

Courtesy: G.Shnell, DVCS 2014

# GPD Studies in JLab



## Beam-Spin asymmetries by CLAS



*Jlab experiments are playing an important role to study GPD*

*Precise data in valence region*

**Hall A:**

high accuracy,  
limited kinematics,

**Hall B:**

wide kinematic range,  
limited accuracy

$E_e = 5.766$  GeV

F.-X. Girod et al., Phys. Rev. Lett. 100, 162002 (2008).

Meeting of the Japan Physical Society, March 27-30, 2014, Hiratsuka, Japan

# Further Studies on GPD

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## Dedicated GPD programs at Jlab-12 GeV

- **Hall A: E12-06-114** fixed  $x$ , several  $Q^2$ , several beam energies,  $t$ -dependence,  $\text{Im } H$ ,  $\text{Re } H$
- **Hall B: E12-06-119** large kinematic coverage with CLAS  
beam energy at 11 GeV, high statistics, BSA, TSA
- **Hall B: E12-11-003** CLAS with new recoil neutron detector,  
BSA, flavour separation of GPD-H

## GPD program in COMPASS-II

polarized  $\mu^+$  &  $\mu^-$ , hydrogen target

new recoil proton detector, new 2.5m hydrogen target, new ECAL0

Beam Charge Spin Sum, Beam Charge Spin Difference

simultaneously HEMP, SIDIS on proton (FF, TMDs)

data taking: 2016, 17 (after the run for pol. DY)

# Conclusions

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- Significant progress in the study with lepton scattering was achieved
- $\Delta u$  and  $\Delta d$  are well determined
- Polarized sea distributions are small
- Gluon polarization is compatible with 0 in the measured range
- Transversity and Sivers PDF have been extracted
- The asymmetry on un-polarized nucleon gives a hint of BM PDF
- Wealth of GPD data were accumulated by HERMES and Jlab-experiments
- Exciting GPD programs at COMPASS-II and JLab-12GeV are planned