

Resonances of the Systems $\pi^- \eta$ and $\pi^- \eta'$ in the Reaction $\pi^- p \rightarrow \pi^- \eta^{(\prime)} p_{\text{slow}}$ at COMPASS

T. Schlüter
for the COMPASS Collaboration

Department für Physik
Ludwig-Maximilians-Universität München

2013-03-21 / New Hadron Annual Workshop
“Elucidation of New Hadron with a Variety of Flavors”



bmb+f - Förderschwerpunkt
COMPASS
Großgeräte der physikalischen
Grundlagenforschung



Why study the $\eta\pi$ and $\eta'\pi$ Final States

Exotic Waves! Exotic Resonances?

- ▶ quantum numbers of a P -wave in the $\eta\pi^0$ -system are $J^{PC} = 1^{-+}$
- ▶ a quark-antiquark system cannot have these (“exotic”) quantum numbers
- ▶ therefore a P -wave resonance in $\eta\pi$ (or $\eta'\pi$) cannot be attributed to a quark-model state $u\bar{u}$, $d\bar{d}$

Exotic $\eta\pi$ state in $\bar{p}d$ annihilation at rest into $\pi^-\pi^0\eta$ $P_{\text{spectator}}$

Exotic meson with non- $q\bar{q}$ quantum numbers produced in $N\bar{N}$ annihilation

Study of the $\eta\pi$ and $\eta'\pi$ spectra and interpretation of possible exotic $J^{PC} = 1^{-+}$ mesons

PROPERTIES IN THE PARTIAL WAVE ANALYSIS OF $\pi^+p \rightarrow \eta\pi^0n$ REACTION

Study of the $\eta\pi^0$ spectrum and search for 1^{-+} exotic meson

- ▶ several experiments observed P -wave state that were interpreted as resonances ($\eta\pi$: $\pi_1(1400)$, $\eta'\pi$: $\pi_1(1600)$)
- ▶ yet, this interpretation is not firmly established

KEK's role in this Search

After GAMS claimed an exotic resonance in the $\eta\pi^0$ channel, KEK ran an experiment in order to search for this state in the charged mode $\eta\pi^-$.

Physics Letters B 314 (1993) 246–254

Study of the $\eta\pi^-$ system in the π^-p reaction at 6.3 GeV/c

H. Aoyagi^a, S. Fukui^b, T. Hasegawa^c, N. Hayashi^a, N. Horikawa^a, J. Iizuka^a, S. Inaba^d, S. Ishimoto^d, Y. Ishizaki^e, T. Iwata^a, E. Kanatani^{c,1}, H. Kawai^f, T. Kinashi^a, A. Kishi^a, K. Kobayashi^{i,2}, Y. Kobayashi^{i,3}, K. Matsuda^a, T. Matsuda^a, K. Mori^b, T. Nakagawaⁱ, S. Nakamura^a, T. Nakamura^c, T. Nakanishi^a, A. Naritaⁱ, K. Ohmi^d, C. Ohmori^e, T. Samoto^{a,4}, H. Shimizu^j, Y. Tajima^k, K. Takamatsu^d, M. Takasaki^d, T. Tsubaki^{l,5}, K. Tsuchiya^{a,3}, T. Tsuru^d, I. Yamauchi^m, Y. Yasu^d, H.Y. Yoshida^{k,6} and A. Wakai^a

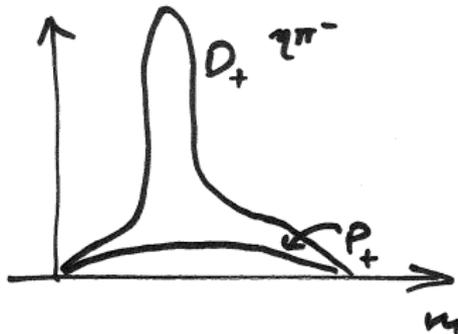
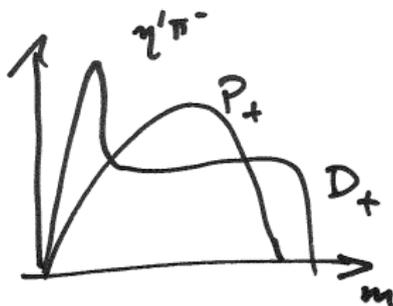
If the enhancement of the P_+ wave obtained in the present experiment can be a resonant state, it may correspond to the $J^{PC} = 1^{-+}$ object which has been observed in the GAMS experiment [2], though the mass value is lower and the width is slightly narrower than those reported by the GAMS experiment.

- ▶ results non-conclusive
- ▶ since then the situation has only improved slightly

Why is the interpretation difficult?

At a production experiment such as COMPASS (GAMS, KEK, VES, BNL E852)

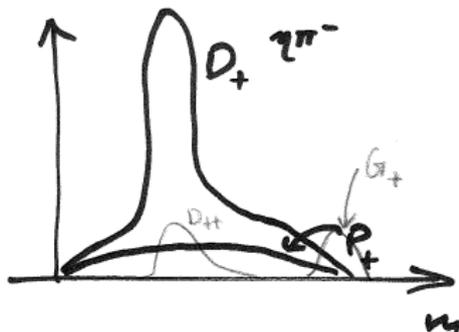
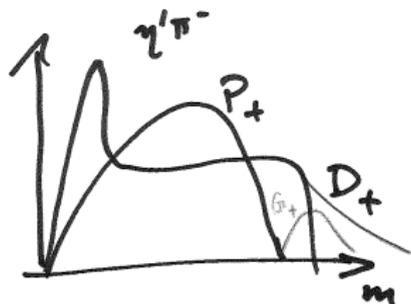
- ▶ the only significant wave overlapping the exotic P wave is the D wave ($J^{PC} = 2^{++}$, contains the well-known $a_2(1320)$)
- ▶ the structure of the D wave is not understood
- ▶ but the interpretation of the P wave requires understanding the D wave, because we only measure relative phases between waves



Input from COMPASS

How does COMPASS enhance the picture?

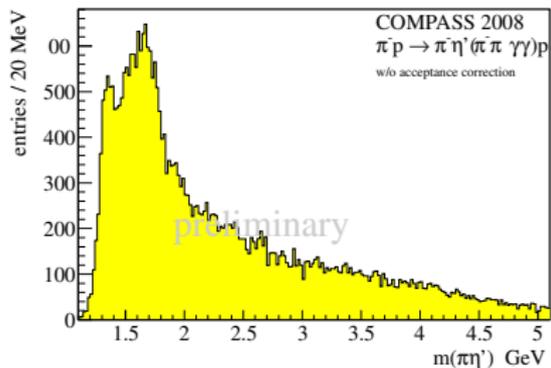
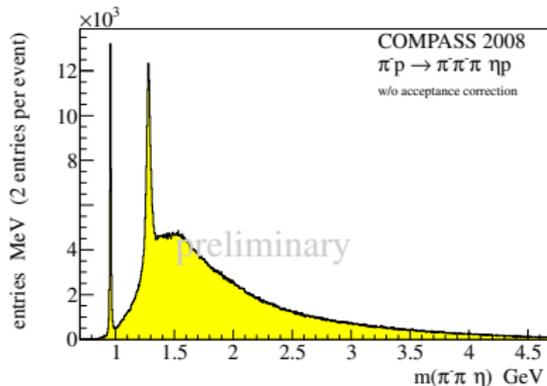
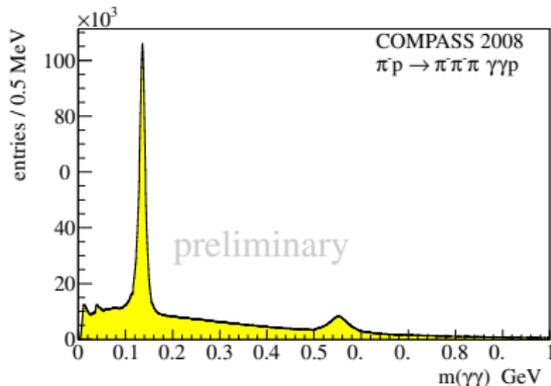
- ▶ higher invariant masses
- ▶ higher statistics
- ▶ additional waves: D_{++} (spin 2, $M = 2$), G_+ (spin 4, $M = 1$), F_+ (spin 3, but not yet ready for public consumption)
- ▶ knowledge transfer $\eta\pi \leftrightarrow \eta'\pi$



Data Selection for $\pi^- p \rightarrow \eta^{(\prime)} \pi^- p$

Selected exclusive final state: slow recoil proton, three tracks ($- - +$), two photons.

Step-by-step for the $\eta' \pi^-$ final state:

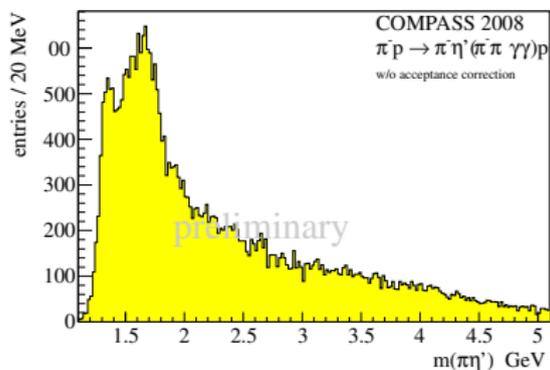


We obtain:

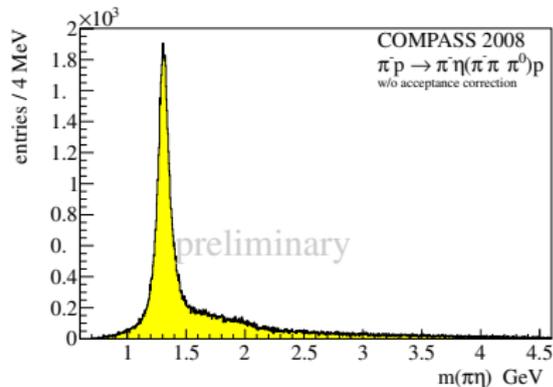
- ▶ 18 000 events with $m(\eta' \pi) < 2$ GeV, 35 000 total
- ▶ inv. masses well above 2 GeV

The Data

Invariant mass of $\pi^- \eta'$



Invariant mass of $\pi^- \eta$

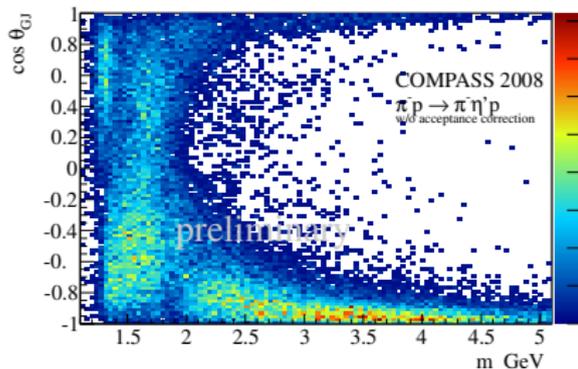


- ▶ $\pi^- \eta$ spectrum dominated by $a_2(1320)$
- ▶ in $\pi^- \eta'$, the a_2 appears as bump close to threshold
- ▶ a broad structure around 1700 MeV dominates the $\pi^- \eta'$ spectrum (P wave)

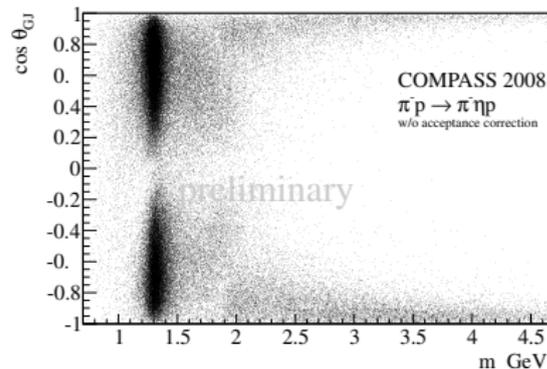
The Data

Now in Several Dimensions!

$m(\pi^- \eta')$ vs. $\cos \theta_{\text{GJ}}(\eta')$

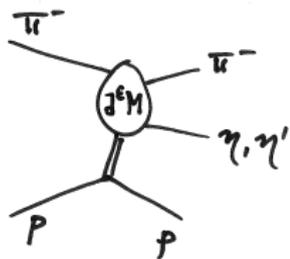


$m(\pi^- \eta)$ vs. $\cos \theta_{\text{GJ}}(\eta)$



- ▶ horizontal: inv. mass (as before), vertical: $\cos \theta_{\eta(\prime)}$ in Gottfried-Jackson frame (that is: $\eta\pi$ rest frame, angles are such that $\cos \theta = 1$ means “ η along beam”)
- ▶ $a_2(1320)$ clearly visible, hints of $a_4(2040)$
- ▶ P -waves visible (asymmetry!)
- ▶ for high masses the data are concentrated on the edges

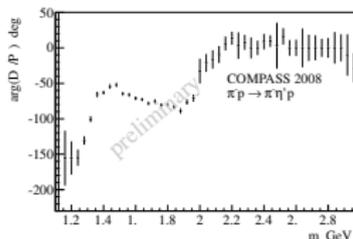
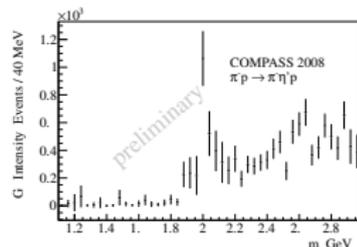
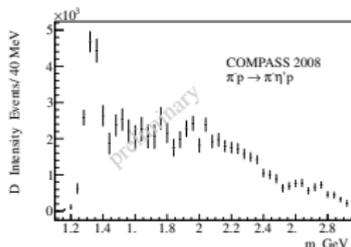
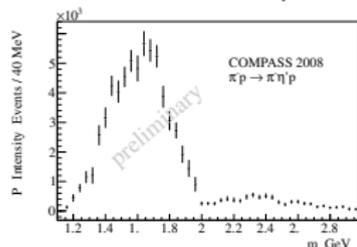
Partial-wave Analysis in Mass Bins



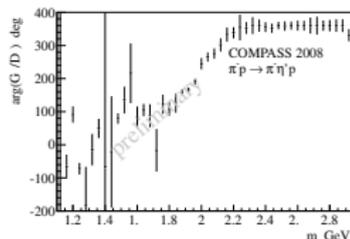
Procedure:

- ▶ divide data into mass bins (40 MeV)
- ▶ fit of each bin to an acceptance-corrected partial-wave model defined in the reflectivity basis

Results for $\pi^- \eta'$:



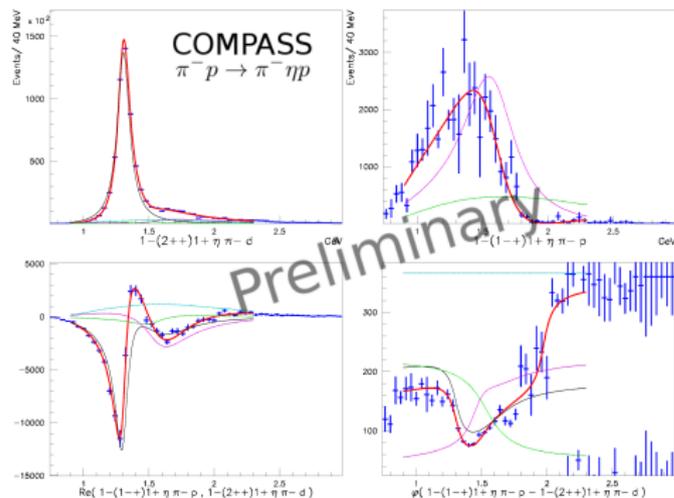
First row:
Intensity of P_+ , D_+ , G_+
Second row:
Relative phases of
 $D_+ - P_+$, $G_+ - D_+$



Modelling Physics

“Mass-dependent PWA” of $\pi^- \eta$

Fit of a model to the data, e.g. $\pi^- \eta$



Colors: binned fit, model fit, others:
components

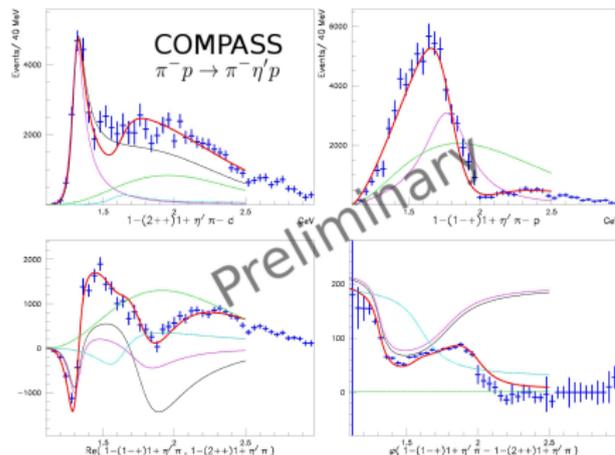
Model:

- ▶ depicted: D_+ , P_+ waves
- ▶ two BWs in D_+
(dynamical BW for $a_2(1320)$)
- ▶ one BW in P_+
- ▶ coherent exponential BG
with phase-space factors
in both waves

Modelling Physics

“Mass-dependent PWA” of $\pi^- \eta'$

For comparison D_+ , P_+ in $\pi^- \eta'$



- ▶ D_+ wave: as before, but second BW mass fixed at $m = 1600$ MeV
- ▶ P_+ wave: one Breit-Wigner, exponential BG as before
- ▶ fits the data but very much non-BW in P_+ -wave description

Colors: **binned fit**, **model fit**, others: components

Improvement desirable!

Similarity of $\pi^- \eta$, $\pi^- \eta'$

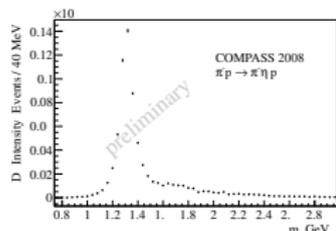
An interesting result is the similarity between the two final states, which can be observed by applying the following recipe:

- ▶ multiply the amplitudes obtained in the $\pi^- \eta$ fit results by the following factor (q = mass-dependent breakup momentum):

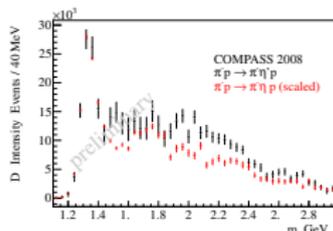
$$\left(\frac{q_{\pi \eta'}}{q_{\pi \eta}} \right)^{J+1/2} \times \text{Amplitude}(\text{Spin } J)$$

- ▶ overlay the scaled $\pi^- \eta$ data on the $\pi^- \eta'$ data taking into account the branching fractions of the η' , η decays

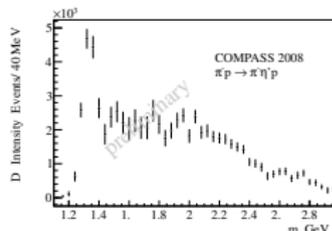
Example with D_+ wave:



D_+ wave in $\pi^- \eta$



Scaled Overlay



D_+ wave in $\pi^- \eta'$

η - η' Mixing

In the quark model, there are two isospin-zero states in the fundamental octet of the light quarks u , d , s :

- ▶ the $SU(3)_{\text{flavor}}$ singlet η_1 and the octet η_8
- ▶ these mix to form the physical states $\eta(548)$, $\eta'(958)$

Alternatively, but easier to understand, one can introduce the flavor basis,

- ▶ $\eta_q = \frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d})$ and $\eta_s = s\bar{s}$
- ▶ the physical states are then again obtained via mixing:

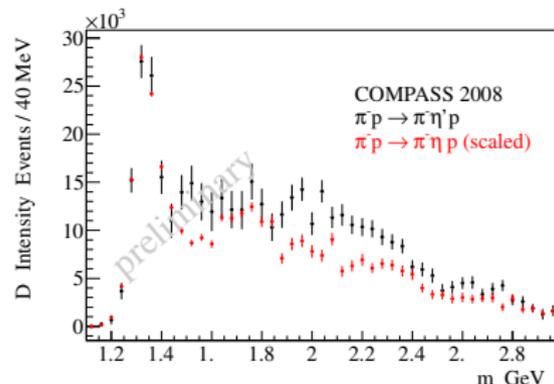
$$\begin{aligned}\eta &= \eta_q \cos \phi - \eta_s \sin \phi \\ \eta' &= \eta_s \sin \phi + \eta_q \cos \phi\end{aligned}$$

- ▶ for every reaction that can be drawn in terms of quark lines, the relative η and η' cross-sections should be determined by ϕ : the η' couples preferentially to $s\bar{s}$, the η to $n\bar{n}$.

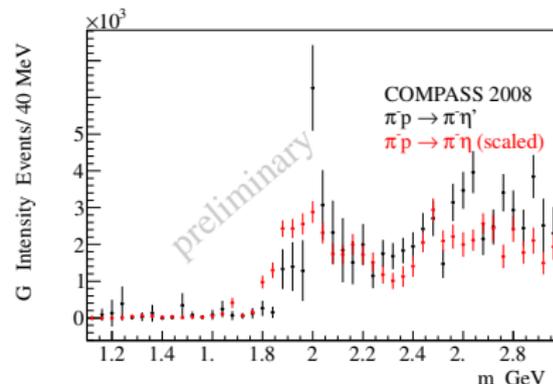
NB: This is just the simplest model for η - η' mixing. Glueball, different decay constants, ...

Overlay of Even Waves

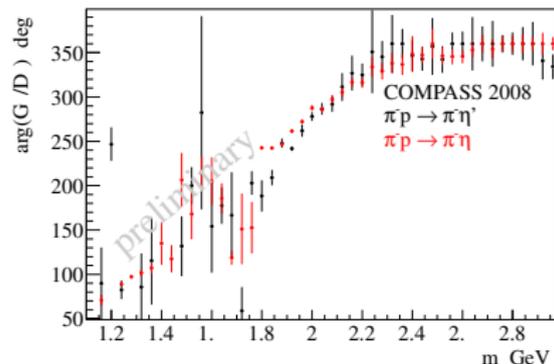
D_+ wave



G_+ wave



Phase difference ($G_+ - D_+$)



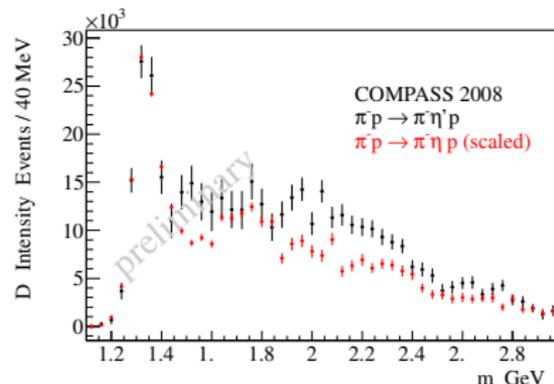
Very similar in $\pi^- \eta$, $\pi^- \eta'$.

Reasonable for $n\bar{n}$ resonances (η - η' mixing). But it's unlikely that all of this is resonant.

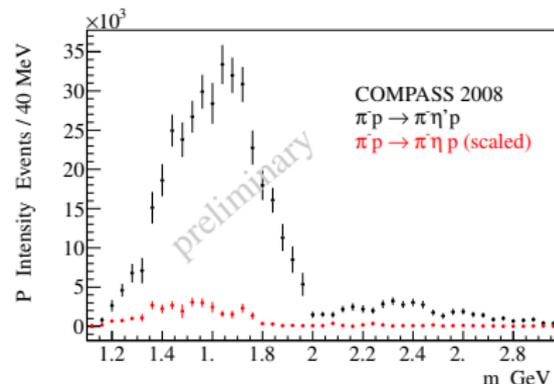
(Absolute scale may have large systematics.)

Overlays of D_+ , P_+ Waves

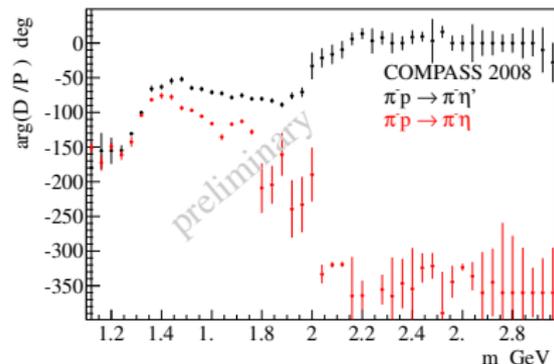
D_+ wave



P_+ wave



Phase difference ($D_+ - P_+$)



P_+ wave behaves entirely differently. There are theoretical arguments for a suppression of the P -wave in initial states involving valence glue (hybrid meson?).

Summary

COMPASS has performed partial-wave analyses of the $\pi^- \eta$ and $\pi^- \eta'$ channels

- ▶ a resonance-only interpretation appears difficult

Most striking results:

- ▶ Similarity between the even partial waves
- ▶ Dissimilarity for odd (“exotic”) waves

Publication forthcoming. It also contains

- ▶ resonance parameters of known resonances (a_2, a_4)
- ▶ measurement of branchign fraction (input for η - η' mixing angle determination)
- ▶ the spin-3 wave and its scaling behavior

Thanks!