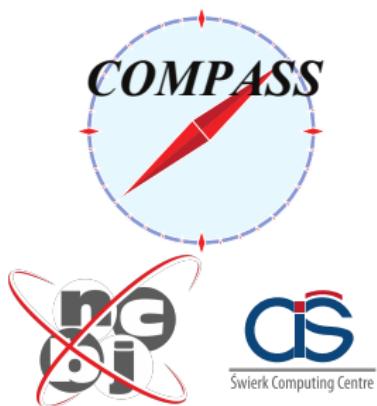


# COMPASS measurements of the longitudinal spin structure of the nucleon



Konrad Klimaszewski

National Centre for Nuclear Research  
Warsaw

On behalf of the  
COMPASS Collaboration

MENU 2013

# Outline

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Spin of the nucleon

COMPASS

Quarks

Gluons

Summary



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## Spin of the nucleon

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$

$\Delta\Sigma$  - quarks

$\Delta G$  - gluons

$L_{q,g}$  - orbital angular momentum

- $\Delta\Sigma \approx 0.3$  from direct measurement
- What about gluons?
- How different quark flavours contribute to the nucleon spin?
- How do we access  $L$ ? (cf. talk by N. D'Hose)



# Observables in $\vec{\mu}\vec{N}$ scattering

- Inclusive asymmetry
- Semi-inclusive asymmetry (LO)

$$A_{\text{meas}} = \frac{1}{fP_T P_B} \left( \frac{N^{\leftarrow} - N^{\rightarrow}}{N^{\leftarrow} + N^{\rightarrow}} \right) \approx D A_1$$

$$A_1 = \frac{g_1(x, Q^2)}{F_1(x, Q^2)} = \frac{\sum_q e_q^2 \Delta q(x, Q^2)}{\sum_q e_q^2 q(x, Q^2)}$$

$$A_1^h(x, z, Q^2) \approx \frac{\sum_q e_q^2 \Delta q(x, Q^2) D_q^h(z, Q^2)}{\sum_q e_q^2 q(x, Q^2) D_q^h(z, Q^2)}$$

$$D_q^h \neq D_{\bar{q}}^h$$

$$\Delta q = q^+ - q^-, \quad q = q^+ + q^-$$



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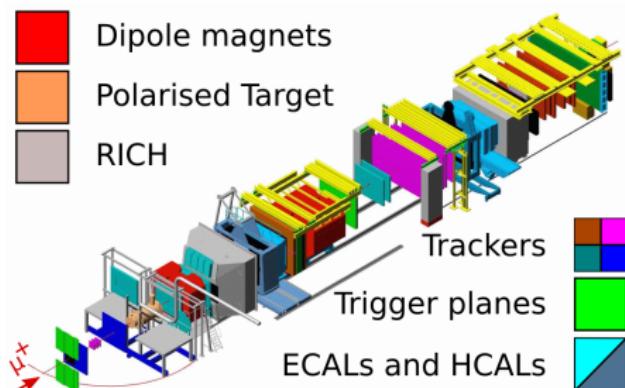
# COMPASS: Spectrometer

## Muon beam

- Beam:  $\mu^+$
- Momentum: 160 GeV (200 GeV)
- Polarisation:  $\sim 80\%$
- $2 \cdot 10^8 \mu$  per Spill of  $\sim 10\text{s}$  ( $1 \cdot 10^8$ )

## Muon data taking

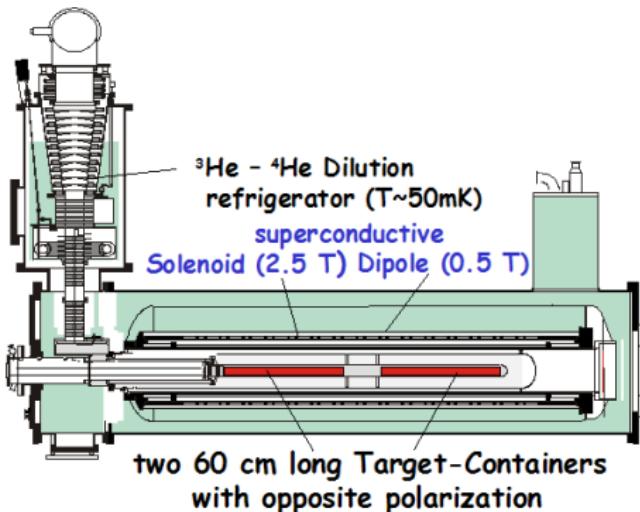
- 2002-04, 2006: deuteron, 160 GeV
  - $\sim 20\%$  in transverse mode
- 2007: proton, 160 GeV
  - $\sim 50\%$  in transverse mode
- 2010: proton, 160 GeV
  - 100% in transverse mode
- 2011: proton, 200 GeV



# COMPASS: Polarised target



- Two (three) cells, oppositely polarised
- 1.2m long
- ${}^6\text{LiD}$ :  $f \simeq 40\%$ ,  $P_T \simeq 50\%$
- $\text{NH}_3$ :  $f \simeq 16\%$ ,  $P_T \simeq 85\%$
- Acceptance:  $\sim 70$  mrad  
(>2005:  $\sim 180$  mrad)





Spin of the nucleon

COMPASS

Quarks

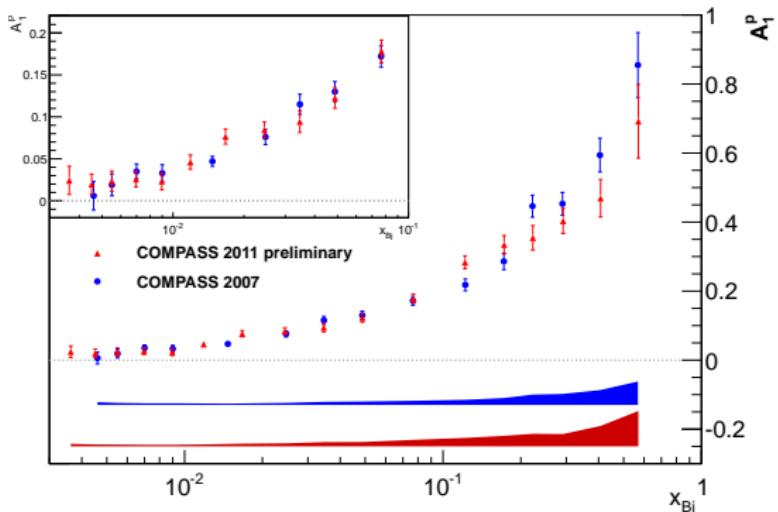
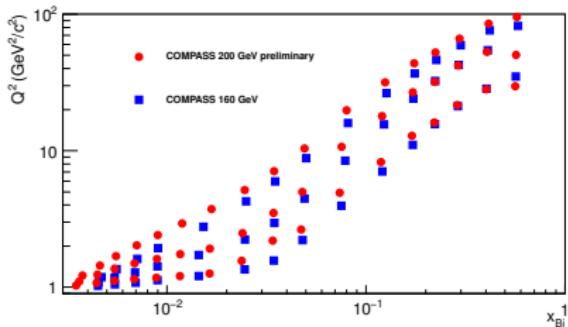
Gluons

Summary



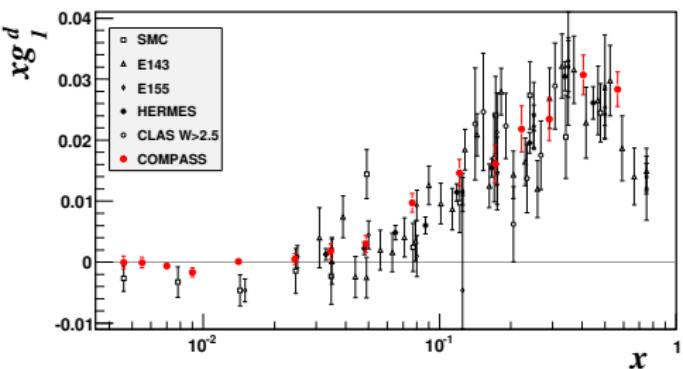
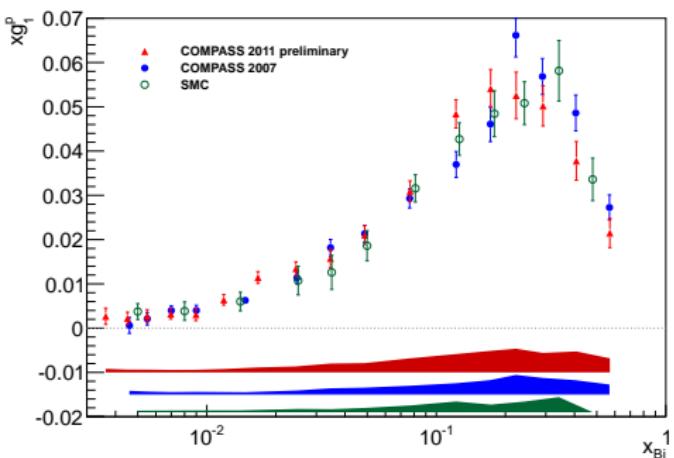
# $A_1^p$ - new results at 200 GeV

- Extend measured range to lower  $x$
- Provide balance to deuteron data
  - Increase precision of Bjorken sum rule test
  - Better constrain strange quark polarisation  $\Delta s$





# Structure functions $g_1^p$ and $g_1^d$ at low $x$

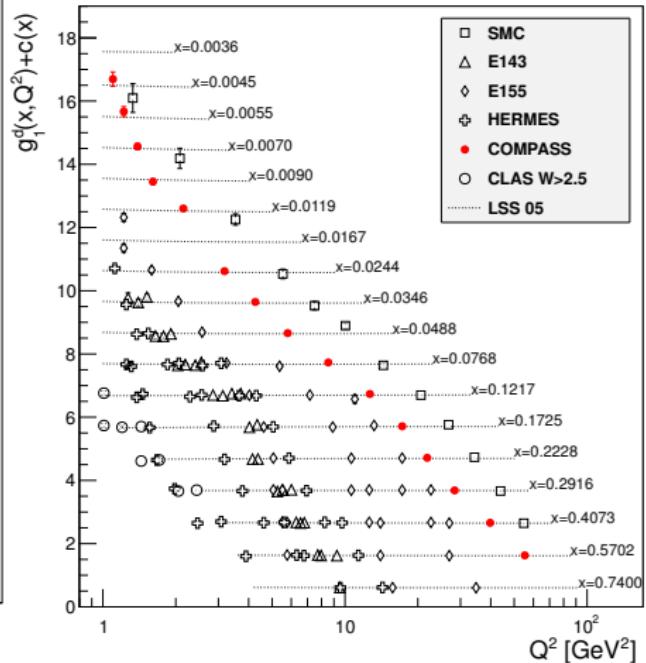
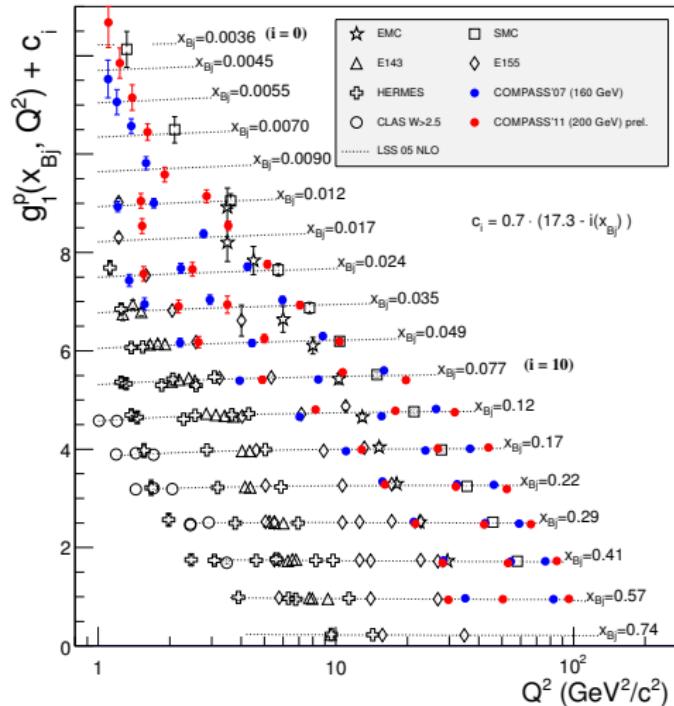


- SMC parametrisation of  $F_2$   
SMC PRD 55 (1998) 112001

- $R = \frac{\sigma^L}{\sigma^T}$   
COMPASS PLB 647 (2007) 330



# World data on $g_1$ structure function



# Bjorken sum rule



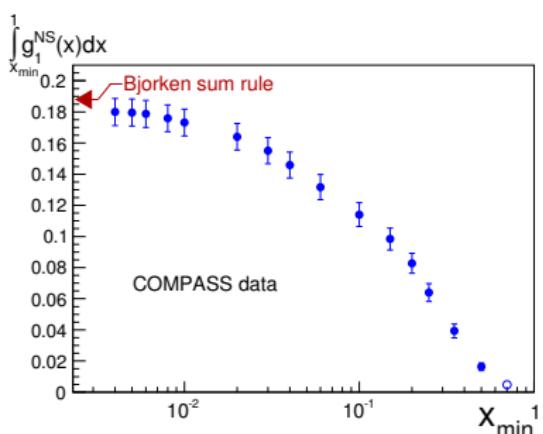
$$\Gamma_1^p - \Gamma_1^n = \frac{1}{6} \left| \frac{g_A}{g_V} \right| C_1^{NS}$$

$$\Gamma_1^{NS} \cong \int_{0.004}^{0.7} g_1^{NS}(x) dx$$

$$g_1^{NS} = g_1^p - g_1^n = 2g_1^p - \frac{g_1^d}{1 - \frac{3}{2}\omega_D}$$

$$\Gamma_1^{NS} = 0.175 \pm 0.009 \pm 0.015$$

$$x\epsilon(0.004, 0.7)$$



- $\omega_D = 0.05 \pm 0.1$
- $g_{A,V}$  - measured in weak  $\beta$  decays
- $C_1^{NS}$  - calculable in pQCD



## Bjorken sum rule

$$\Gamma_1^p - \Gamma_1^n = \frac{1}{6} \left| \frac{g_A}{g_V} \right| C_1^{NS}$$

$$\Gamma_1^{NS} \cong \int_{0.004}^{0.7} g_1^{NS}(x) dx$$

Projected precision (2011)

$$g_1^{NS} = g_1^p - g_1^n = 2g_1^p - \frac{g_1^d}{1 - \frac{3}{2}\omega_D}$$

$$\Gamma_1^{NS} = \pm 0.006 \pm 0.011$$

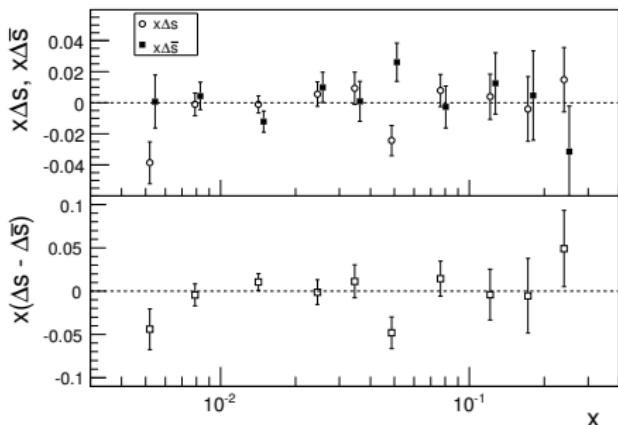
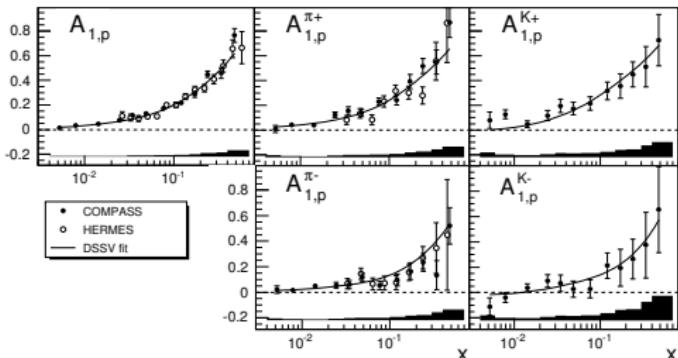
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- $\omega_D = 0.05 \pm 0.1$
- $g_{A,V}$  - measured in weak  $\beta$  decays
- $C_1^{NS}$  - calculable in pQCD



# Semi-inclusive asymmetries

- Data collected on both  $p$  and  $d$  targets
- Measured:  
 $A_1^d, A_{1d}^{\pi^\pm}, A_{1d}^{K^\pm}, A_1^p, A_{1p}^{\pi^\pm}, A_{1p}^{K^\pm}$
- Determined:  
 $\Delta u, \Delta \bar{u}, \Delta d, \Delta \bar{d}, \Delta s \equiv \Delta \bar{s}$
- LO approximation

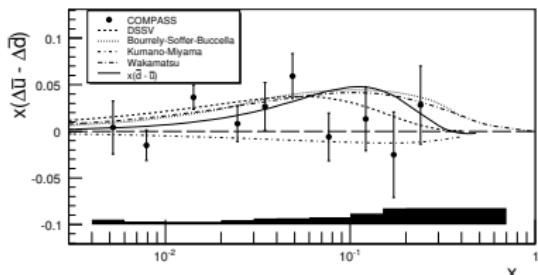
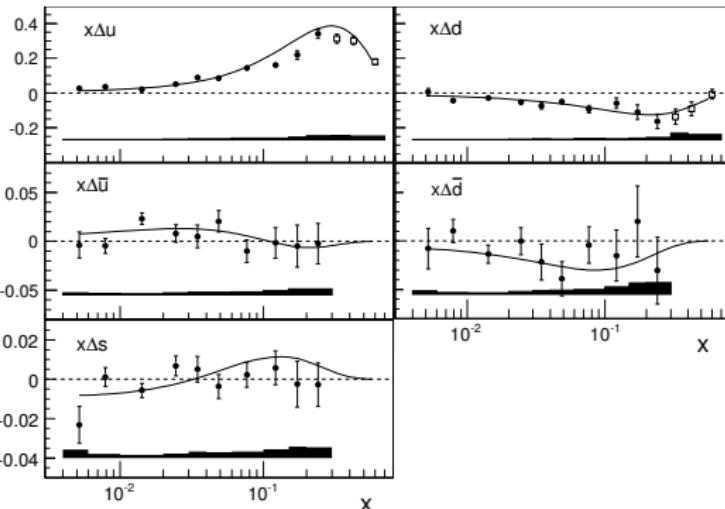


- LO DSS fragmentation functions
- LO unpolarised MRST pdf

COMPASS, Phys. Lett. B 680 (2009) 217  
DSSV, Phys. Rev. D 80 (2009) 034030



# Flavour separation



- NLO parametrisation of DSSV describes the data well
- The sea is not unsymmetric
- Thus the data disfavour models predicting  $\Delta\bar{u} - \Delta\bar{d} \gg \bar{d} - \bar{u}$

$$\int_{0.004}^{0.3} [\Delta\bar{u}(x, Q^2) - \Delta\bar{d}(x, Q^2)] dx = 0.06 \pm 0.04 \pm 0.02 @ Q^2 = 3 \text{ GeV}^2$$



# Polarisation of strange sea

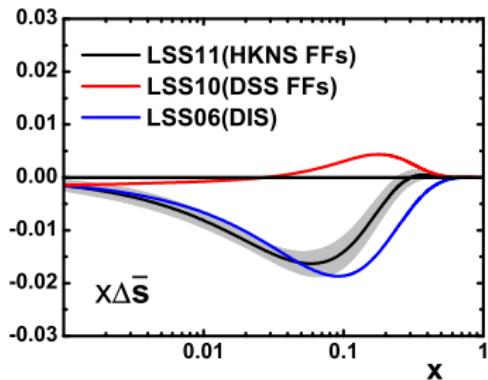
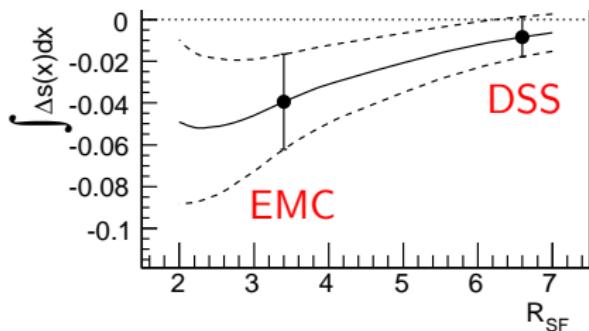
- Inclusive measurements:

$$2\Delta S = \int_0^1 (\Delta s(x) + \Delta \bar{s}(x)) dx = -0.09 \pm 0.01 \pm 0.02$$

- Semi-inclusive measurements compatible with zero

- $\Delta S$  obtained in semi-inclusive analysis strongly depends on the fragmentation functions

- Most critical:  $R_{SF} = \frac{\int D_{\bar{s}}^{K^+}(z) dz}{\int D_u^{K^+}(z) dz}$





# Fragmentation Functions

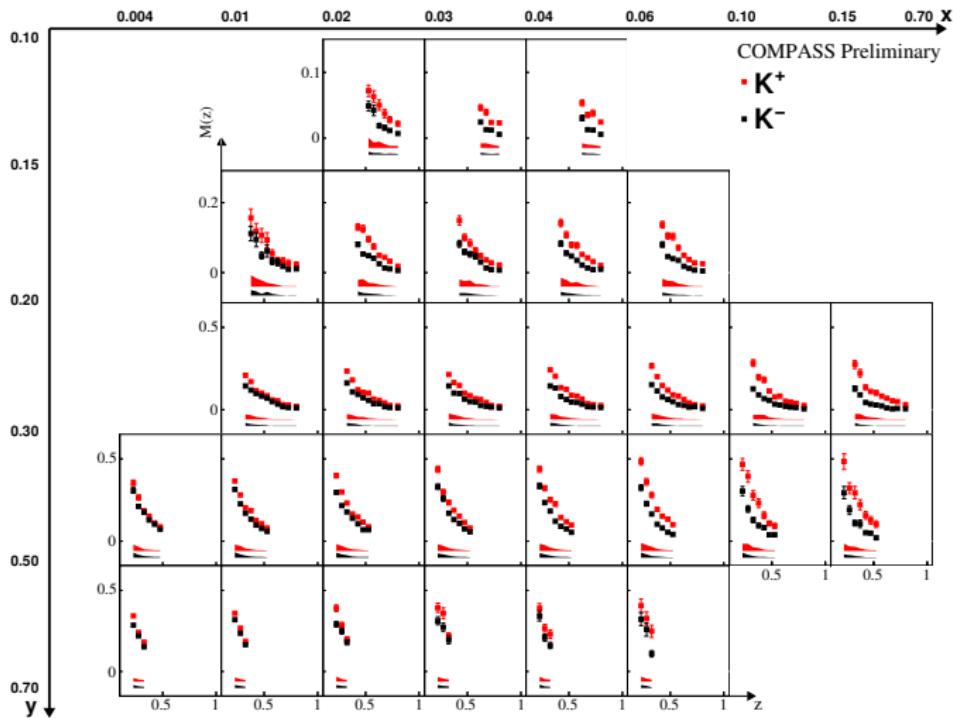
Current knowledge of FFs based on

- High precision data from  $e^+e^-$  colliders
  - Fixed energy scales (far from fixed target experiments)
  - No separation of  $q$  and  $\bar{q}$
- Data from hadron colliders (RHIC)
  - Most sensitive to gluon FFs
- Data from semi-inclusive DIS (new results from HERMES)
  - Sensitive to parton flavour and hadron charge

COMPASS contributes with measurement of charged hadron multiplicities with  $K$  and  $\pi$  identification

$$M^h(x, z) = \frac{d\sigma^h/dxdz}{d\sigma^{DIS}/dxdz} = \frac{\sum_q e_q^2 [q(x)D_q^h(z) + \bar{q}(x)D_{\bar{q}}^h(z)]}{\sum_q e_q^2 [q(x) + \bar{q}(x)]}$$

## Charged hadron multiplicities (identified kaons)





Spin of the nucleon

COMPASS

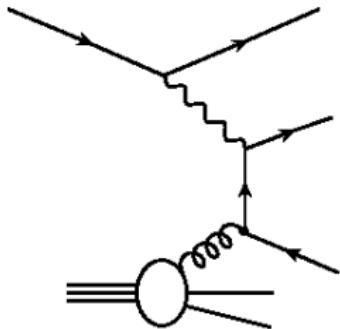
Quarks

Gluons

Summary



# Access to gluons



**PGF**

**Photon Gluon  
Fusion**

- **Open Charm**

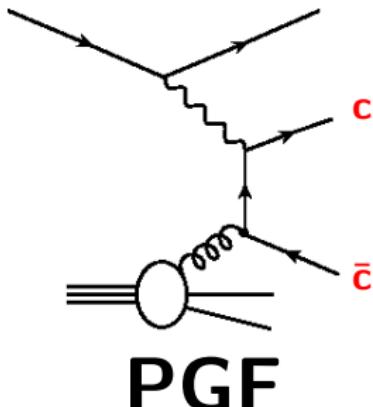
- Search for  $D^0$  meson in the final state
- No charm in the nucleon in COMPASS kinematics
- Charm is produced only via PGF (LO)
- Perturbative region ensured by charm mass
- Weakly depends on MC simulations
- Low statistics

- **High  $p_T$  hadrons**

- Search for hadrons with high transverse momenta in the final state
- Large statistics
- Perturbative region:  $Q^2 > 1 \text{ GeV}^2$  or  $p_T$
- Background processes
- MC simulations essential



# Access to gluons



Photon Gluon  
Fusion

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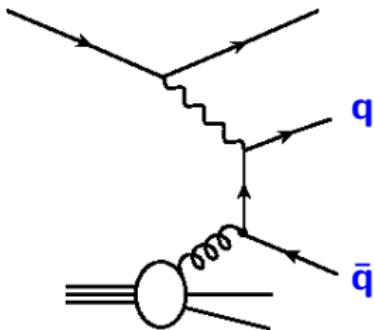
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# $\Delta G$ : High- $p_T$ pairs ( $Q^2 > 1 \text{ GeV}^2$ ) PLB 718 (2013) 922

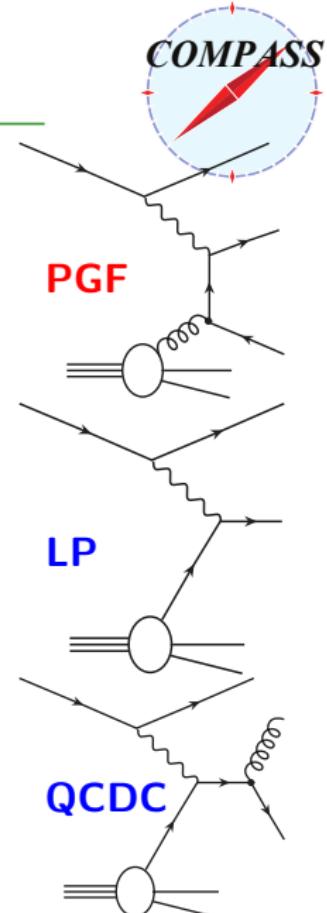
$$A_{LL}^{2h}(x_{Bj}) = \frac{\Delta\sigma}{\sigma} \approx \frac{\Delta G}{G} a_{LL}^{PGF} R_{PGF} + A_1^{LO}(x_C) a_{LL}^C R_C + A_1^{LO}(x_{Bj}) D R_{LP}$$

- $R_n$  - process fraction (MC+NN)
- $a_{LL}^n$  - partonic asymmetry (pQCD)
- $A_1^{LO} = \frac{\sum_i e_i^2 \Delta q_i}{\sum_i e_i^2 q_i}$

$$\frac{\Delta G}{G} = 0.125 \pm 0.060(\text{stat}) \pm 0.063(\text{syst})$$

$$x_G = 0.09^{+0.08}_{-0.04} @ \mu^2 \approx 3(\text{GeV}/c)^2$$

| bin          | 1                        | 2                        | 3                        |
|--------------|--------------------------|--------------------------|--------------------------|
| $\Delta G/G$ | $0.15 \pm 0.09 \pm 0.09$ | $0.08 \pm 0.10 \pm 0.08$ | $0.19 \pm 0.17 \pm 0.14$ |
| $x_G$        | $0.07^{+0.05}_{-0.03}$   | $0.10^{+0.07}_{-0.04}$   | $0.17^{+0.10}_{-0.06}$   |



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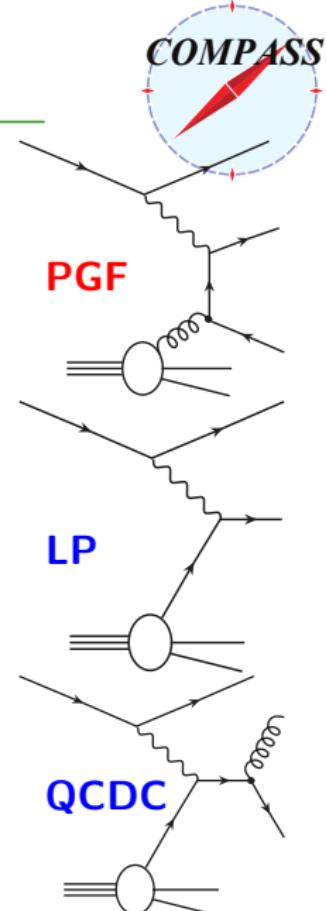
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# $\Delta G$ : Open charm LO

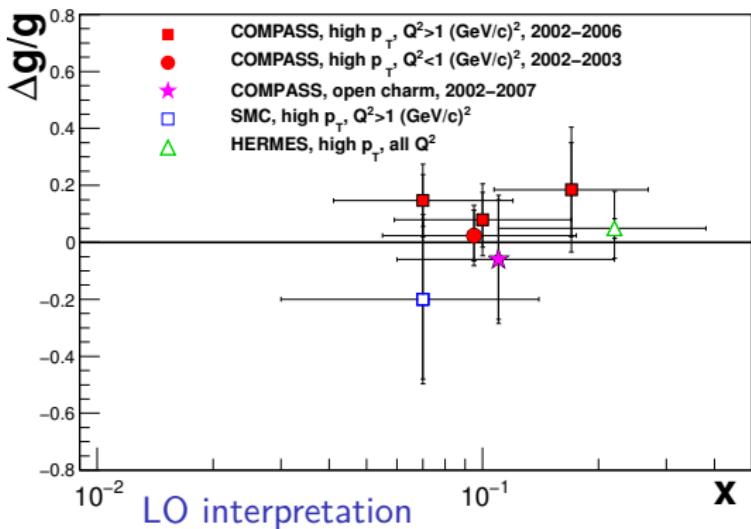
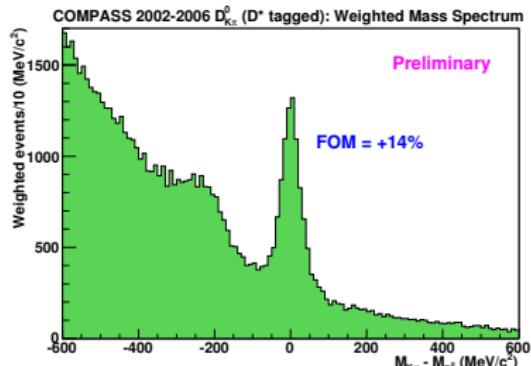
PRD 87 (2013) 052018



$$A_{meas} = P_B P_T f a_{LL} \frac{\sigma_{PGF}}{\sigma_{PGF} + \sigma_{BG}} \frac{\Delta g}{g} + A_{BG}$$

Open charm selection

E.g.  $D^* \rightarrow D^0\pi \rightarrow K\pi\pi$



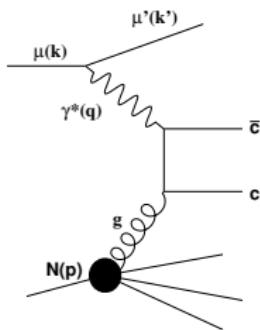
$$\Delta G/G = -0.08 \pm 0.21 \pm 0.11$$

$$x_g = 0.11^{+0.11}_{-0.05}; \quad \mu^2 = 13 \text{ GeV}^2$$

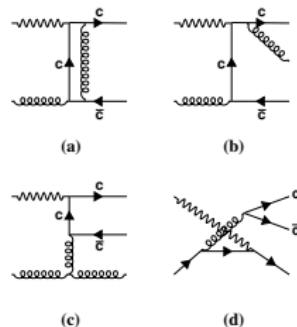
# $\Delta G$ : Open charm NLO



LO



NLO examples



- AROMA with parton shower used for simulation of phase space for NLO
- NLO calculations by I. Bojak and M. Stratmann, [PL B433 \(1998\) 411](#); [NP B 540 \(1999\) 345](#)
- $a_{LL}^{NLO}$  calculated event-by-event
- NLO background corrected for ( $A_{corr}$ )

$$A^{\gamma N} = \frac{a_{LL}}{D} \frac{\Delta g}{g} + A_{corr}$$

# $\Delta G$ : Open charm NLO

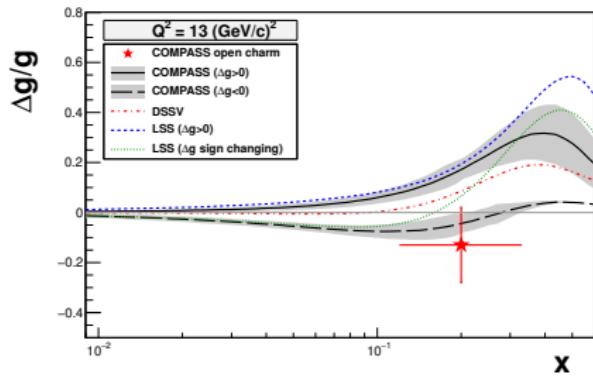
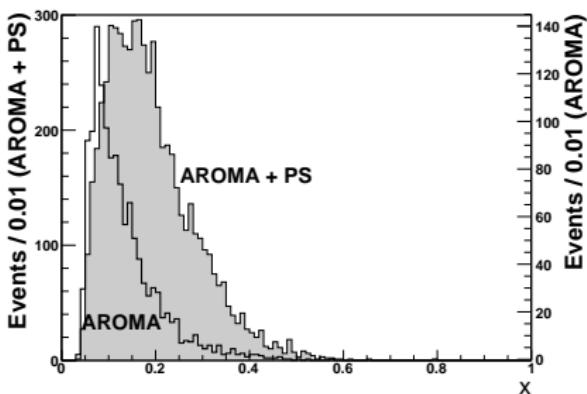
PRD 87 (2013) 052018



- Significant impact on  $x_g$
- NLO QCD result of COMPASS influences  $\Delta g(x) > 0$  fit  
 $\Delta G = 0.36 \pm 0.07 \Rightarrow \Delta G = 0.24 \pm 0.09$

$$\Delta G/G = -0.13 \pm 0.15 \pm 0.15$$

$$x_g = 0.20^{+0.13}_{-0.08}; \quad \mu^2 \approx 13 \text{ GeV}^2$$

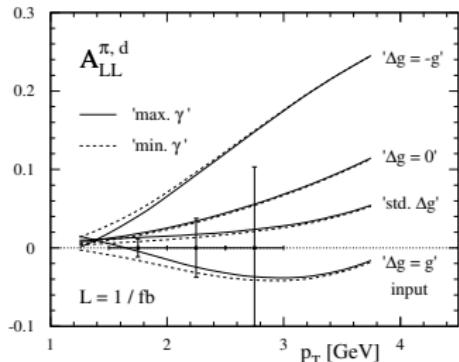
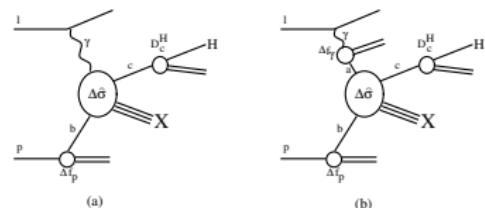


- In addition asymmetries binned along  $p_T$  are provided (also in  $(p_T, E)$  bins)

# $\Delta G$ : High- $p_T$ hadron photoproduction



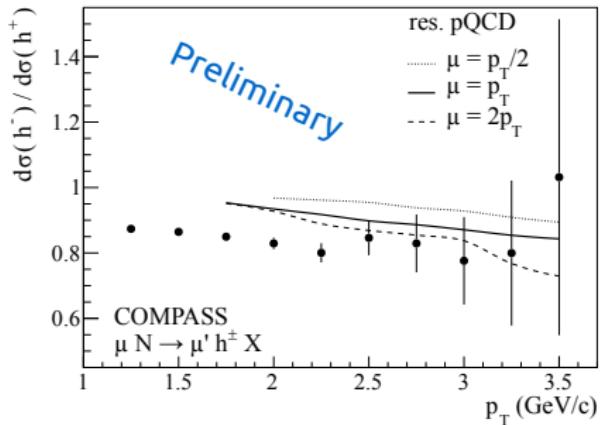
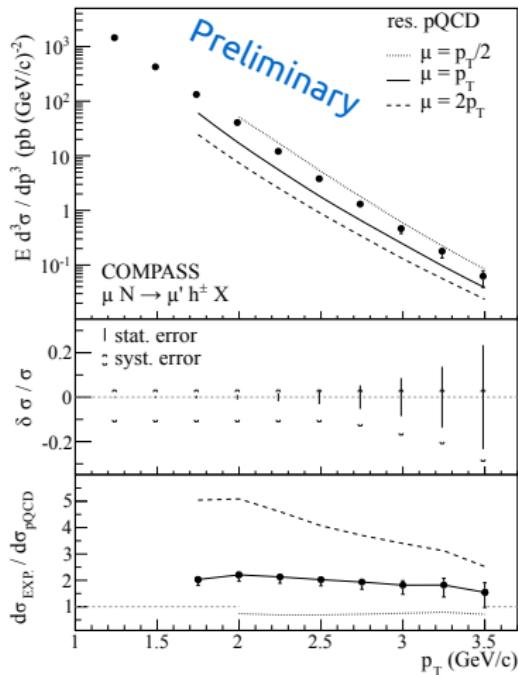
- Measured cross-section: COMPASS hep-ex/1207.2022  
 $Q^2 < 0.1 \text{ GeV}^2$ ,  $-0.1 < \eta_{CMS} < 2.4$ ,  $p_T < 3.6 \text{ GeV}$
- NLO pQCD photoproduction of inclusive hadrons  
B. Jäger, M. Stratmann and W. Vogelsang, EPJ C44 (2005) 533
- Projections ( $1 \text{ fb}^{-1}$ ) compared to GRSV options
- Goal: constrain the  $\Delta g$  by the QCD calculations of the single high- $p_T$  hadron asymmetries.



Total COMPASS integrated luminosity:  $\sim 4 \text{ fb}^{-1}$



# $\Delta G$ : Hadron photoproduction x-section vs $p_T$



New calculation w/ "threshold resummation"

de Florian, Pfeuffer, Schäfer, Vogelsang arXiv:1305.6468 [hep-ph]



## Summary

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- New proton (2011) data extend measurements of  $g_1^P$  to low  $x$  and will permit a more accurate extraction of polarised pdf
- Extraction of FF ratios from hadron multiplicities on the way
  - Will help to solve the “ $\Delta s$  puzzle”
- Gluon polarisation,  $\Delta g$  updated in LO and (new) NLO suggest a small  $\Delta G$  at the measured  $x$  with all world measurements compatible
- COMPASS II with interesting scientific program awaits restart of SPS (cf. talk by **N. D'Hose**)