

# Partial-Wave Analysis of Centrally Produced Two-Pseudoscalar Final States in $pp$ Reactions at COMPASS

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for the  
COMPASS Collaboration

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**COMPASS**  
Großgeräte der physikalischen  
Grundlagenforschung





Introduction

Partial-Wave Analysis in Mass Bins

Mass-Dependent Parametrisation

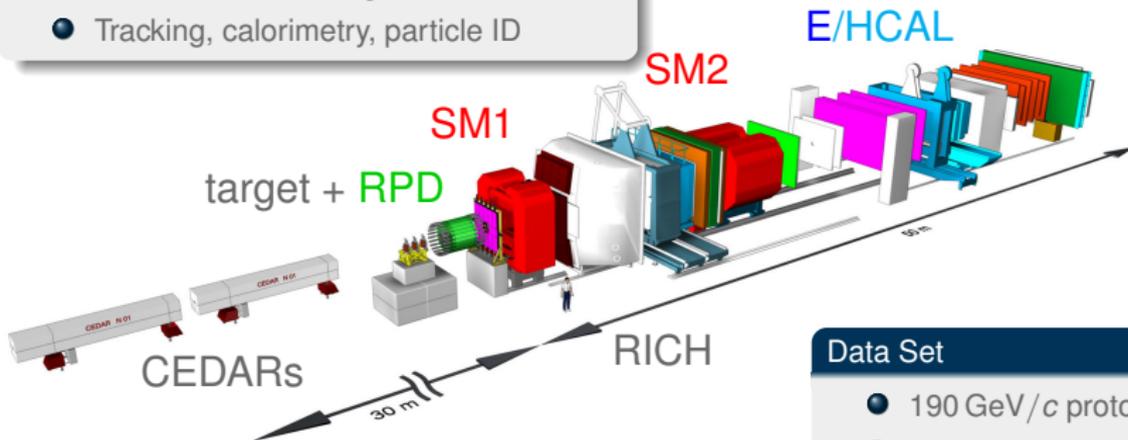
Conclusion and Outlook



# The COMPASS Experiment

## Multi-Purpose Setup

- Fixed-target experiment @ CERN SPS
- Two-stage magnetic spectrometer
- Broad kinematic range
- Tracking, calorimetry, particle ID

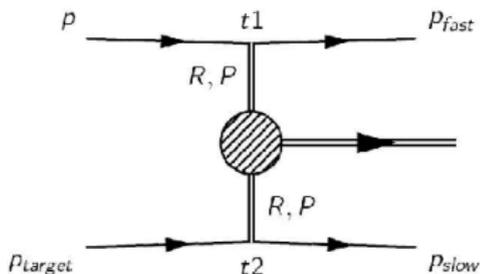


## Data Set

- 190 GeV/c proton beam
- Liquid H<sub>2</sub> target
- Trigger on recoil proton



# Central Exclusive Production

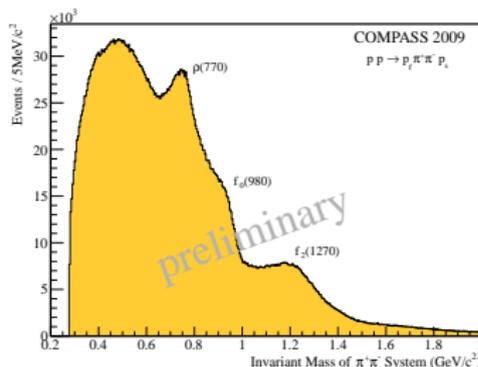
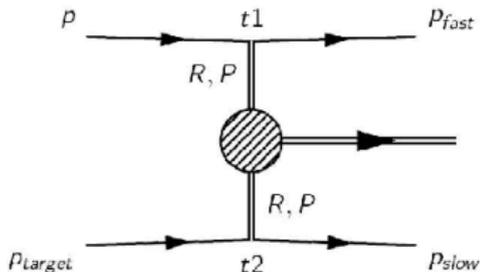


$pp \rightarrow p_{fast} X p_{slow}$

- Proton beam impinging on liquid hydrogen target
- Double-Pomeron Exchange as glue-rich environment  
 $\Rightarrow$  Production of non- $q\bar{q}$ -mesons (Glue Balls, Hybrids) at central rapidities



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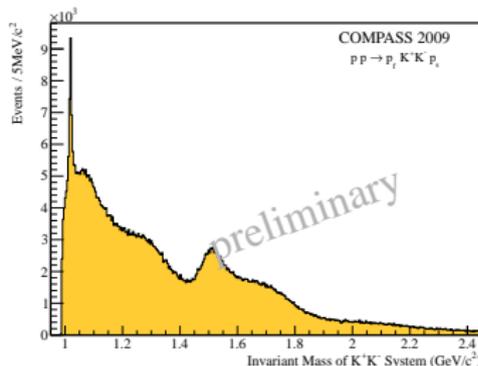
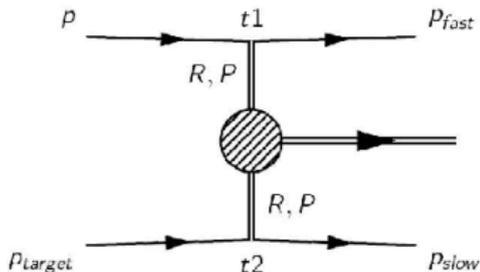


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- Decay into two-pseudoscalar final state ( $\pi^+\pi^-$ ,  $\pi^0\pi^0$ ,  $K^+K^-$ ,  $\eta\eta$ , ..)



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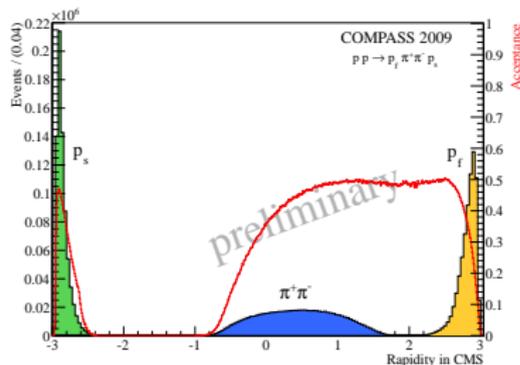
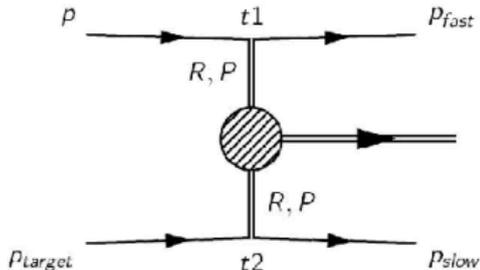


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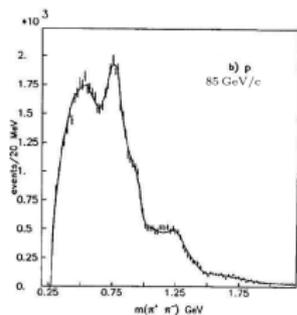


$$pp \rightarrow p_{\text{fast}} X p_{\text{slow}}$$

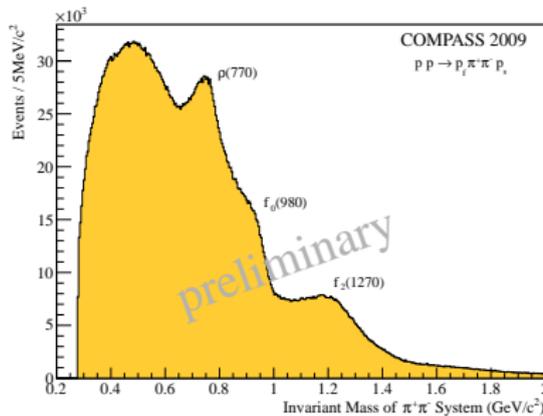
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- Decay into two-pseudoscalar final state ( $\pi^+\pi^-$ ,  $\pi^0\pi^0$ ,  $K^+K^-$ ,  $\eta\eta$ , ..)
- Rapidity gap between  $p_s$  and the central system  $X$  introduced by the principal trigger



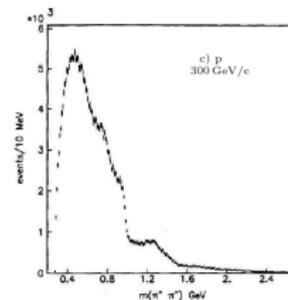
T.A. Armstrong et al. [Z. Phys. C51 (1991)]



$$\sqrt{s} = 12.7 \text{ GeV}/c^2$$



$$\sqrt{s} = 18.9 \text{ GeV}/c^2$$



$$\sqrt{s} = 23.7 \text{ GeV}/c^2$$

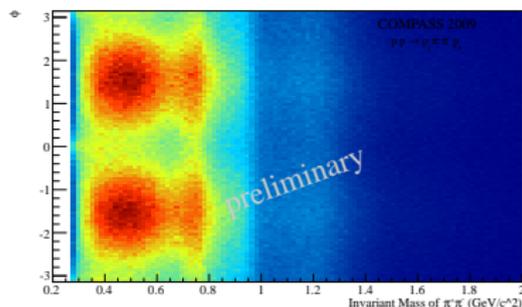
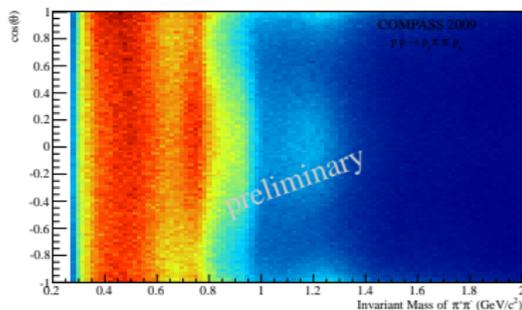
- Production of  $\rho(770)$  disappears rapidly with increasing  $\sqrt{s}$
- Low-mass enhancement and  $f_0(980)$  remain practically unchanged  
→ characteristic for  $s$ -independent Pomeron-Pomeron scattering
- Kinematic selection cannot single out pure DPE sample



## Two-Body Partial-Wave Analysis in Mass Bins

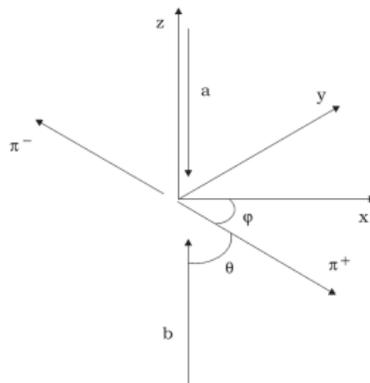


# Partial-Wave Analysis



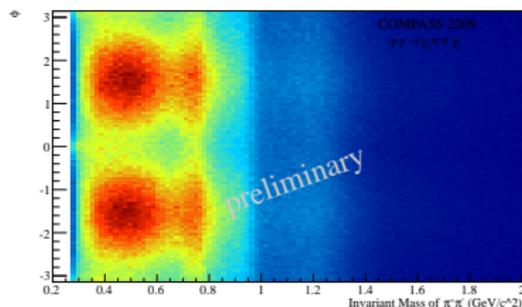
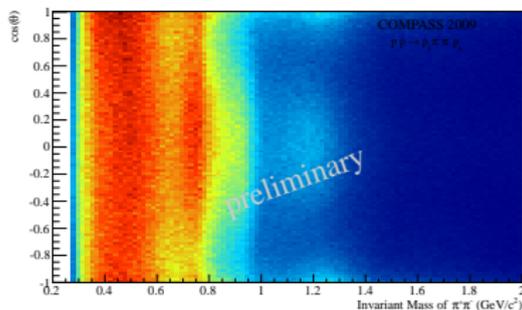
$$X \rightarrow \pi^+ \pi^-$$

- **Assumption:** collision of two space-like exchange particles ( $\mathbb{P}, \mathbb{R}$ )
- Decay fully described by  $M(\pi^+ \pi^-)$ ,  $\cos(\theta)$  and  $\phi$



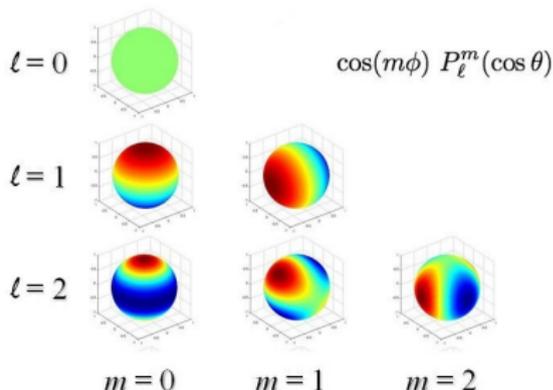


# Partial-Wave Analysis



$$X \rightarrow \pi^+ \pi^-$$

- **Assumption:** collision of two space-like exchange particles ( $\mathbb{P}, \mathbb{R}$ )
- Decay fully described by  $M(\pi^+ \pi^-)$ ,  $\cos(\theta)$  and  $\phi$
- Fit complex production amplitudes in mass bins to match spin contributions and interference pattern





Expand intensity  $I(\theta, \phi)$  in terms of partial-waves for narrow mass bins:

$$I(\theta, \phi) = \sum_{\varepsilon} \left| \sum_{\ell m} T_{\varepsilon \ell m} Y_m^{\varepsilon \ell}(\theta, \phi) \right|^2$$

- Complex transition amplitudes  $T_{\varepsilon \ell m}$ , no assumption on mass-dependence
- Spectroscopic notation:  $\ell_m^{\varepsilon}$
- Significant contributions only from  $\ell = S, P, D, m \leq 1$

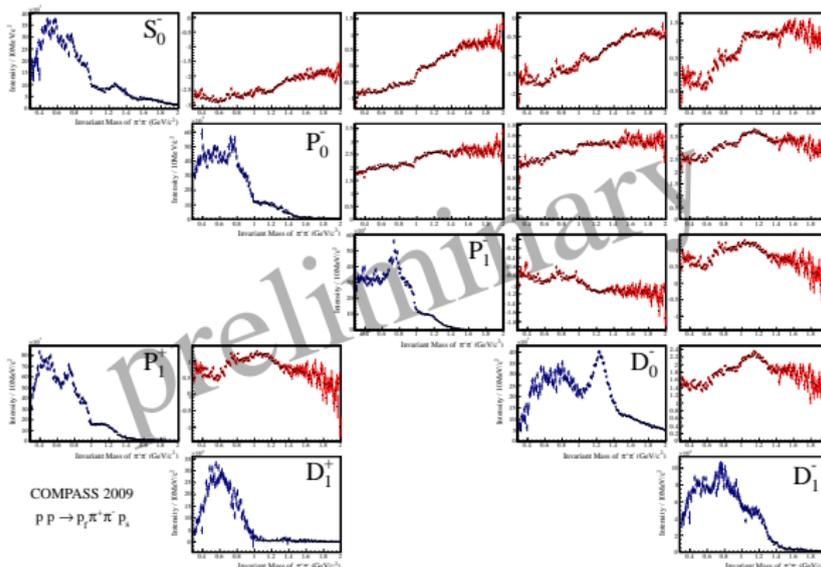
⇒ **Maximum Likelihood Fit in Mass Bins**

$$\ln L = \sum_{i=1}^N \ln I(\theta_i, \phi_i) - \int d\Omega I(\theta, \phi) \eta(\theta, \phi)$$

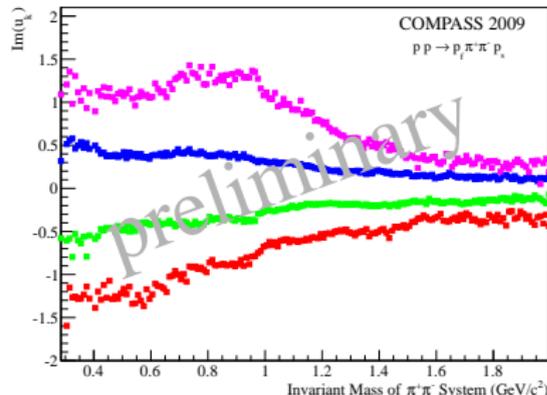
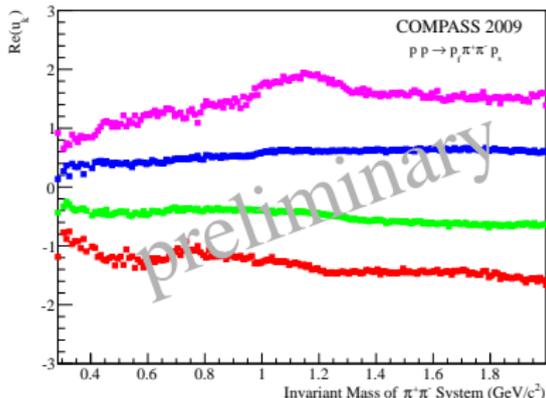
- the **normalisation integral** is evaluated by a phase-space Monte Carlo sample



# Ambiguities in the $\pi^+\pi^-$ System



- 8 mathematically ambiguous solutions result in the same angular distribution
- Analytical computation via method of [Barrelet Zeros](#)



- Real (left) and imaginary (right) part of polynomial roots
- Well separated, imaginary parts do not cross the real axis

⇒ Solutions can be uniquely identified and linked from mass bin to mass bin



# Ambiguities in the $\pi\pi$ Systems

## $\pi^+\pi^-$ System

- 8 different solutions can be calculated analytically
- Differentiation requires additional input (e.g. behaviour at threshold, physics content)

## $\pi^0\pi^0$ System

- Identical particles, only even waves allowed
- Reduces number of ambiguities to 2

## Combination of $\pi\pi$ Systems

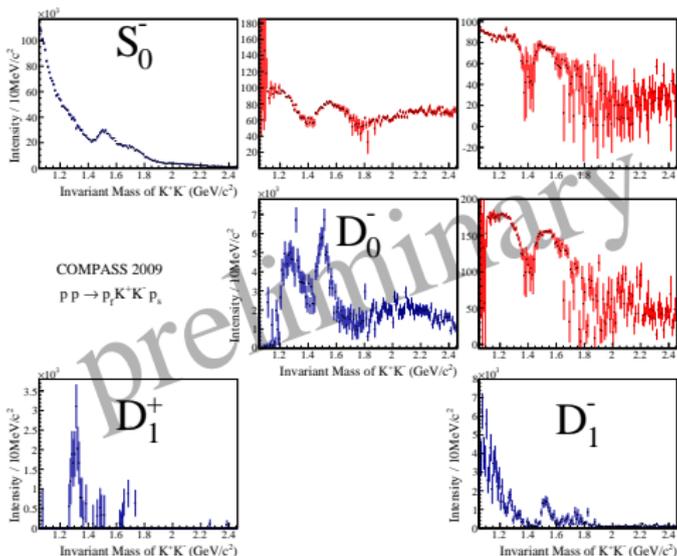
- Consistent picture of the reaction, measured with different parts of experimental setup
- Interpretation with mass dependent parametrisation under way!



## Mass-Dependent Parametrisation of $K^+K^-$ -System



# Fit to the $K^+K^-$ System



- Similar partial-wave analysis of  $K^+K^-$ -system
- Odd waves do not play a significant role above the  $\phi(1020)$ -mass  
 $\Rightarrow$  Reduction of ambiguities



## $S_0$ -Wave

- Relativistic Breit-Wigner parametrisation:  $f_0(1370)$ ,  $f_0(1500)$ ,  $f_0(1710)$

## $D_0$ -Wave

- Relativistic Breit-Wigner parametrisation:  $f_2(1270)$ ,  $f_2'(1525)$

## Non-Resonant Contribution

- Phase space factor  $q^\ell \cdot \sqrt{\frac{q}{m^2}}$  with breakup momentum  $q$
- Exponential background  $\exp(-\alpha q - \beta q^2)$  with fit parameters  $\alpha$ ,  $\beta$



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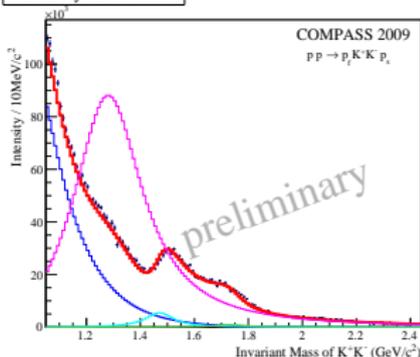
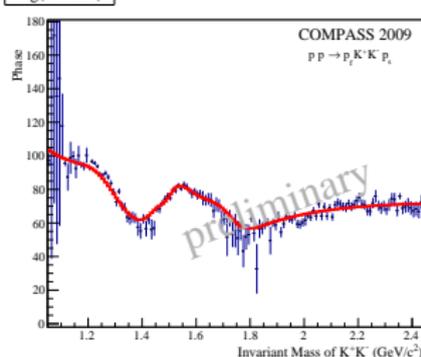
**In total: 27 parameters**  
(to fit 438 points)



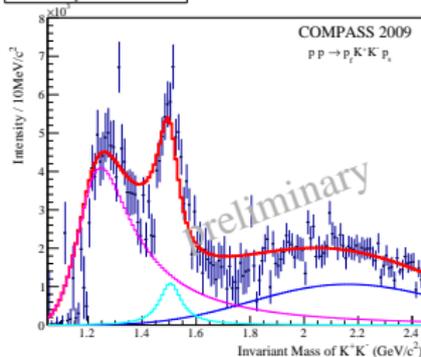
# Intensities and Phase



Intensity of S0 wave

 $\arg(S0 / D0)$ 

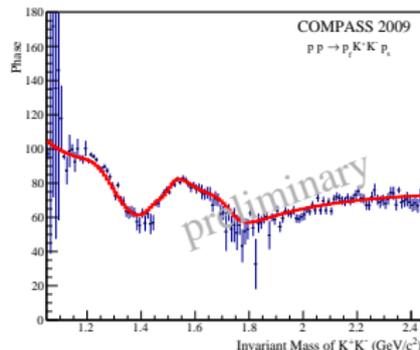
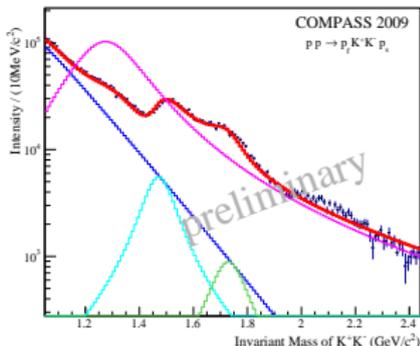
Intensity of D0 wave



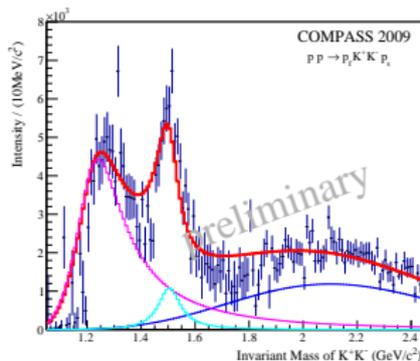
- BW contributions
- non-resonant contribution
- coherent sum



# Intensities and Phase



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## Summary

- Order-of-magnitude **larger sample** than previous experiments (for charged channels)
- **Acceptance corrected PWA** with unprecedented precision
- Simplistic **mass-dependent parametrisation** can describe the  $K^+ K^-$  fit
- Breit-Wigner parameters mostly consistent with **PDG values**



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## Outlook

- **Unitary models** ( $K$ -matrix, ..)
- **Combined fit** of all available channels ( $\pi^+\pi^-$ ,  $K^+K^-$ ,  $K_S K_S$ ,  $\pi^0\pi^0$ ,  $\eta\eta$ , ...)
- Extract **resonance parameters** in the scalar sector
- Information about the **composition** of supernumerous resonances



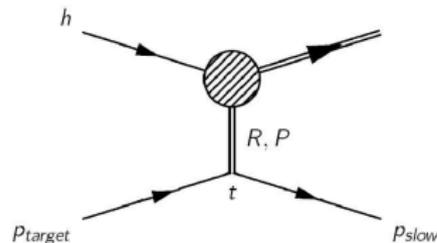
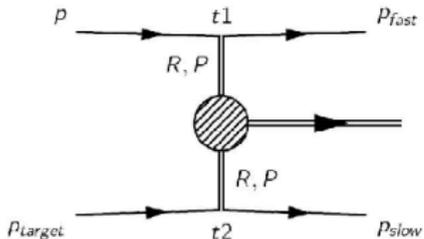
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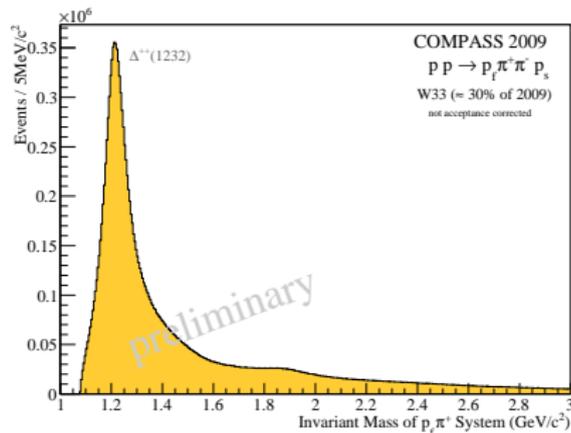
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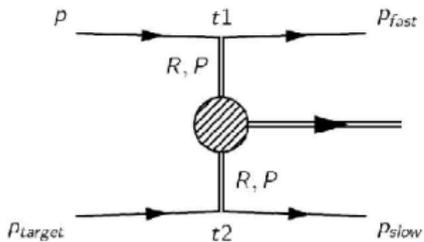
Thank you for your attention!



## Kinematic Selection

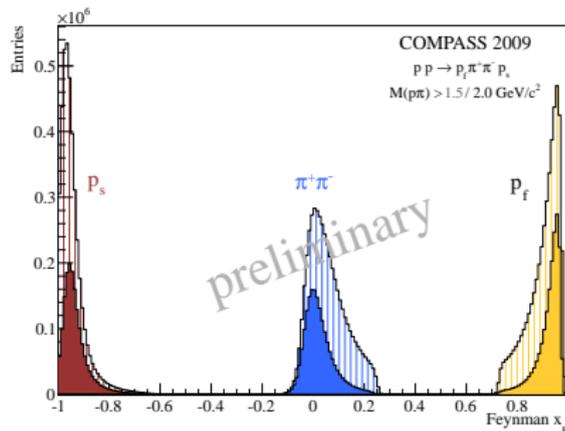
- $M(p\pi) > 1.5 \text{ GeV}/c^2$

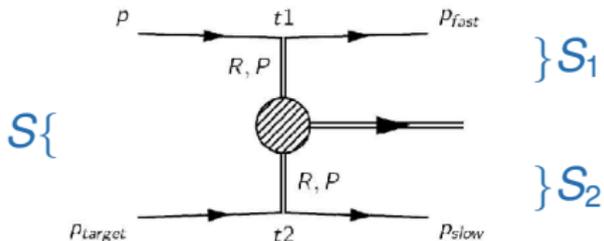




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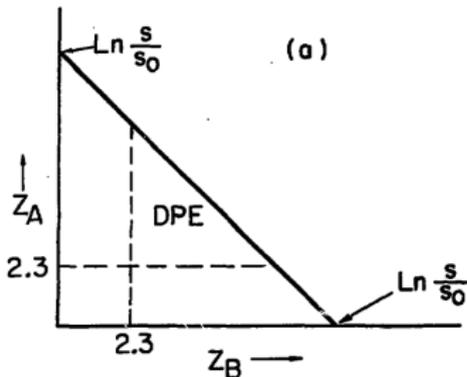
- $x_F(p_f) > .9$





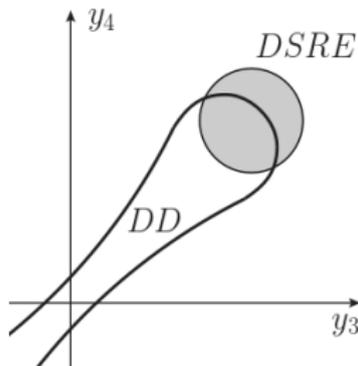
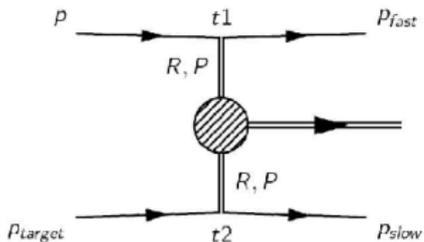
## Kinematic Selection

- $Z_{A,B} > 2.3$



- $Z_A = \ln \frac{s}{s_1}$
- $Z_B = \ln \frac{s}{s_2}$

D.M. Chew, [Nucl. Phys. B 82 (1974)]

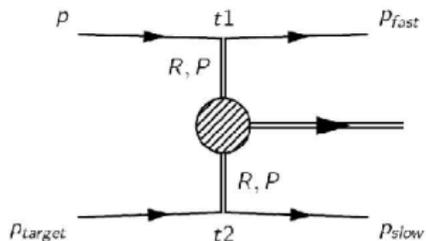


## Kinematic Selection

- $|y(\pi)| < 1$

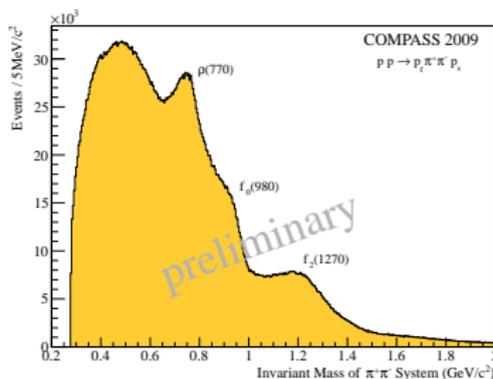
- DD: double diffraction (= central production)
- DSRE: diffractive single resonance excitation

P. Lebiedowicz and A. Szczurek, [Phys. Rev. D 81 (2010)]



## Kinematic Selection

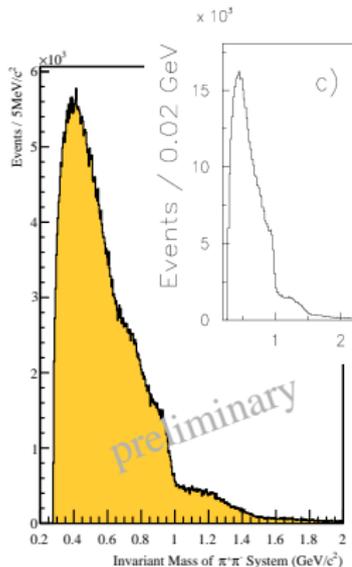
- $M(p\pi) > 1.5 \text{ GeV}/c^2$
- $x_F(p_f) > .9$
- $Z_{A,B} > 2.3$
- $|y(\pi)| < 1$
- ...



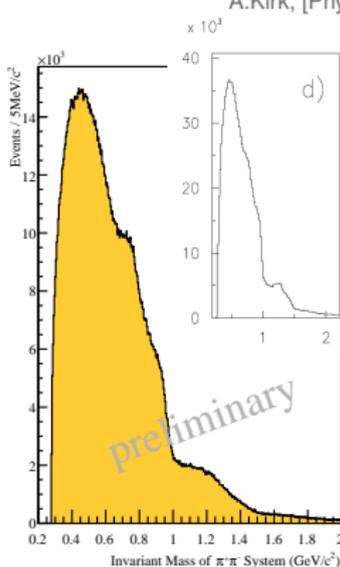
Large overlap of the cuts, weak dependence of the results  
(CEP sample by all definitions, but not pure DPE!)



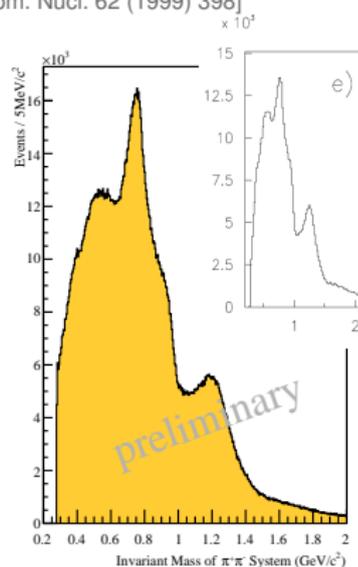
A.Kirk, [Phys. Atom. Nucl. 62 (1999) 398]



$$dP_T \leq 0.2 \text{ GeV}/c$$



$$0.2 \leq dP_T < 0.5 \text{ GeV}/c$$



$$dP_T \geq 0.5 \text{ GeV}/c$$

- $dP_T = |\vec{p}_{T_1} - \vec{p}_{T_2}|$  in  $pp$  centre-of-mass
- Only scalar signals remain for small  $dPt$



Maximise likelihood function

$$\ln L = \sum_{i=1}^N \ln I(\theta_i, \phi_i) - \int d\Omega I(\theta, \phi) \eta(\theta, \phi)$$

- by choosing  $T_{\varepsilon\ell m}$  such that the intensity fits the observed  $N$  events
- the **normalisation integral** is evaluated by a phase-space Monte Carlo sample
- with the **acceptance**  $\eta(\theta, \phi)$



- Through variable transformation  $u = \tan(\theta/2)$ , angular distribution for this wave set can be written as a function of  $|G(u)|^2$  with  

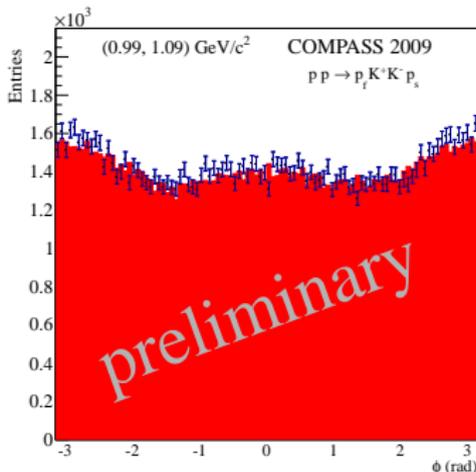
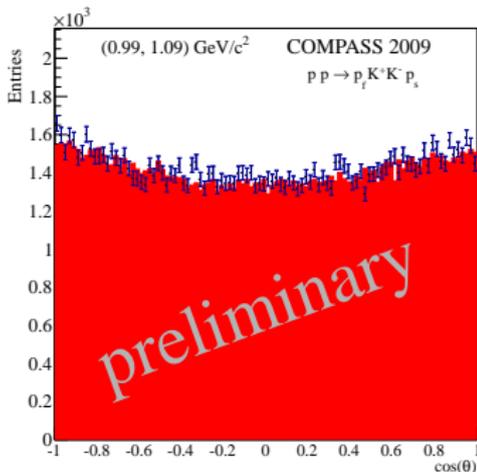
$$G(u) = a_4 u^4 - a_3 u^3 + a_2 u^2 - a_1 u + a_0$$
 where coefficients  $a_i$  are functions of amplitudes
- or with in terms of 4 complex roots  $u_i$  ('Barrelet zeros')  

$$G(u) = a_4 (u - u_1)(u - u_2)(u - u_3)(u - u_4)$$
- *Laguerre's method* to find polynomial roots numerically
- Complex conjugation of one/more of these roots result in the same measured angular distribution  
 → **8 different ambiguous solutions** (same likelihood per definition!)

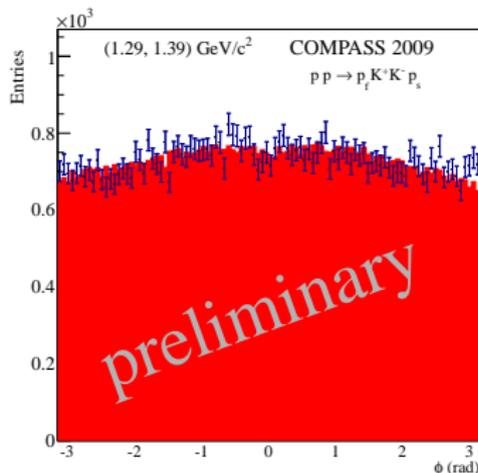
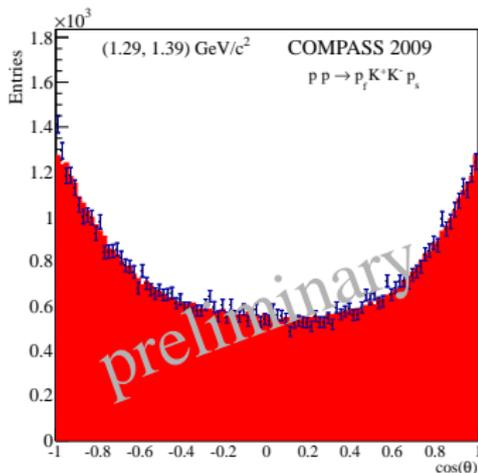
Techniques of amplitude analysis for two-pseudoscalar systems  
 S.U. Chung, [Phys. Rev. D 56 (1997), 7299]



# Evaluation of Fit with Weighted MC



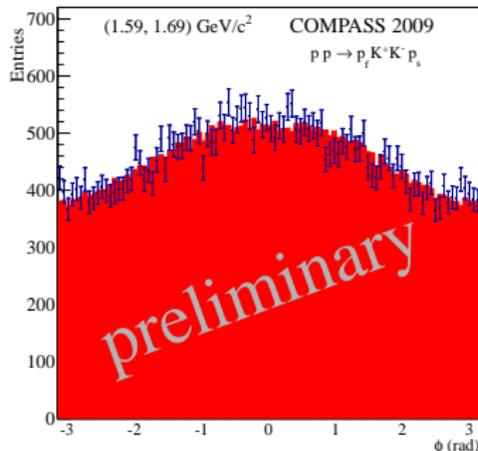
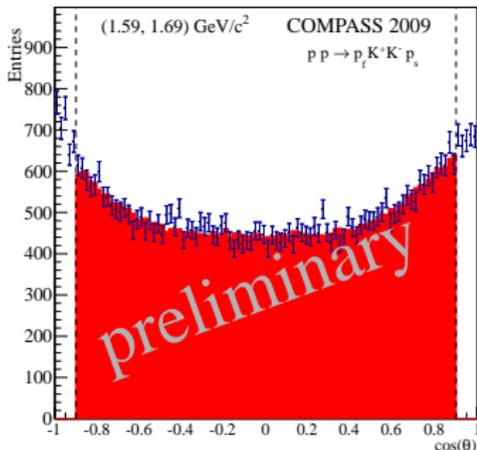
- Blue: data, red: weighted MC



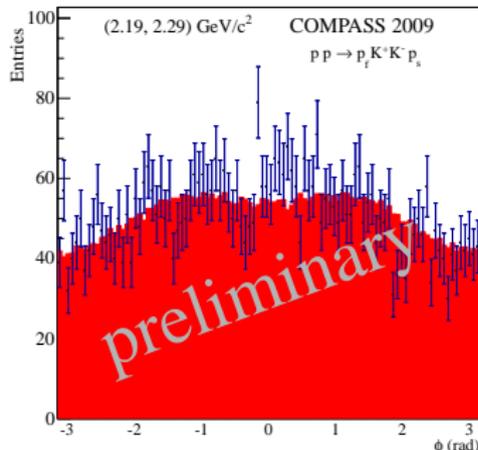
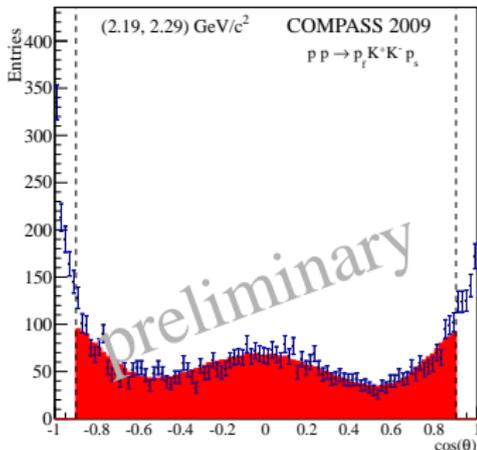
- Blue: data, red: weighted MC



# Evaluation of Fit with Weighted MC



- Blue: data, red: weighted MC



- Blue: data, red: weighted MC
- Peaking distribution for  $|\cos(\theta)| > 0.9$  for masses above  $2 \text{ GeV}/c^2$  cannot be described by fit (limited wave set)
- Signature of diffractive dissociation background