

# Experimental overview of transversity

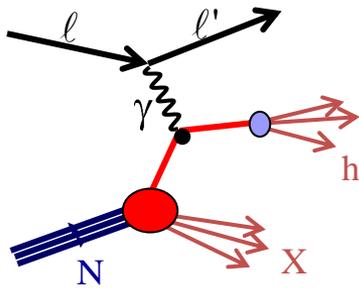
Federica Sozzi  
INFN Sezione di Trieste



**IWHSS'12**  
International Workshop on Hadron Structure and Spectroscopy  
Lisbon, 16 - 18 April 2012



# Study of transverse momentum dependent PDF



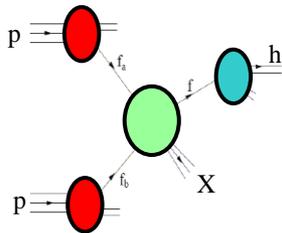
## SIDIS off polarised targets

DESY (HERMES)

CERN (COMPASS)

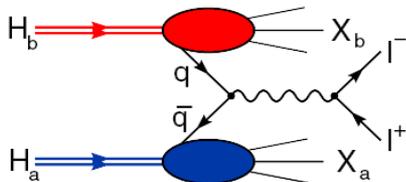
JLab

future: *eRHIC, EIC, ENC*



## hard polarised pp scattering

RHIC / BNL



## and projects for (polarised) Drell-Yan:

CERN (COMPASS), FNAL, JParc, RHIC, JINR, IHEP, GSI

# Accessing the transversity PDF

Transversity can be measured in SIDIS on a transversely polarised target via “quark polarimetry” :

$I N^{\uparrow} \rightarrow I' h X$  Collins asymmetry

$I N^{\uparrow} \rightarrow I' hh X$  Two hadron asymmetry

$I N^{\uparrow} \rightarrow I' \Lambda X$   $\Lambda$  polarization

# Accessing the transversity PDF

Transversity can be measured in SIDIS on a transversely polarised target via “quark polarimetry” :

$I N^{\uparrow} \rightarrow l' h X$     Collins asymmetry    Collins FF

$I N^{\uparrow} \rightarrow l' hh X$     Two hadron asymmetry    di-hadron FF

$I N^{\uparrow} \rightarrow l' \Lambda X$      $\Lambda$  polarization    FF of  $q^{\uparrow} \rightarrow \Lambda$

In all these processes, transversity appears together with an **unknown fragmentation function**

# Accessing the transversity PDF

Transversity can be measured in SIDIS on a transversely polarised target via “quark polarimetry” :

$I N^{\uparrow} \rightarrow I' h X$	Collins asymmetry	Collins FF
$I N^{\uparrow} \rightarrow I' hh X$	Two hadron asymmetry	di-hadron FF
$I N^{\uparrow} \rightarrow I' \Lambda X$	$\Lambda$ polarization	FF of $q^{\uparrow} \rightarrow \Lambda$

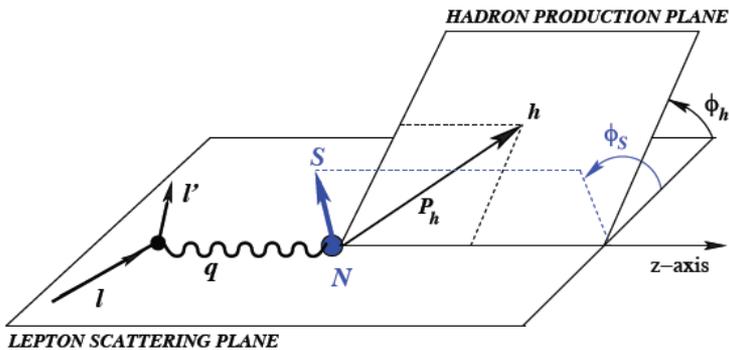
In all these processes, transversity appears together with an unknown fragmentation function

These FF can be detected in inclusive hadron production in  $e^+e^-$  annihilation.  
→ special role of electron positron collider in the extraction of transversity

# Accessing the transversity PDF: Collins mechanism

$$|N^\uparrow \rightarrow l' h X$$

amplitude of the  $\sin(\phi_h + \phi_S - \pi)$  modulation in the azimuthal distribution of the final state hadrons



$$N^\pm(\Phi_C) = N^0 \cdot (1 \pm A \sin \Phi_C)$$

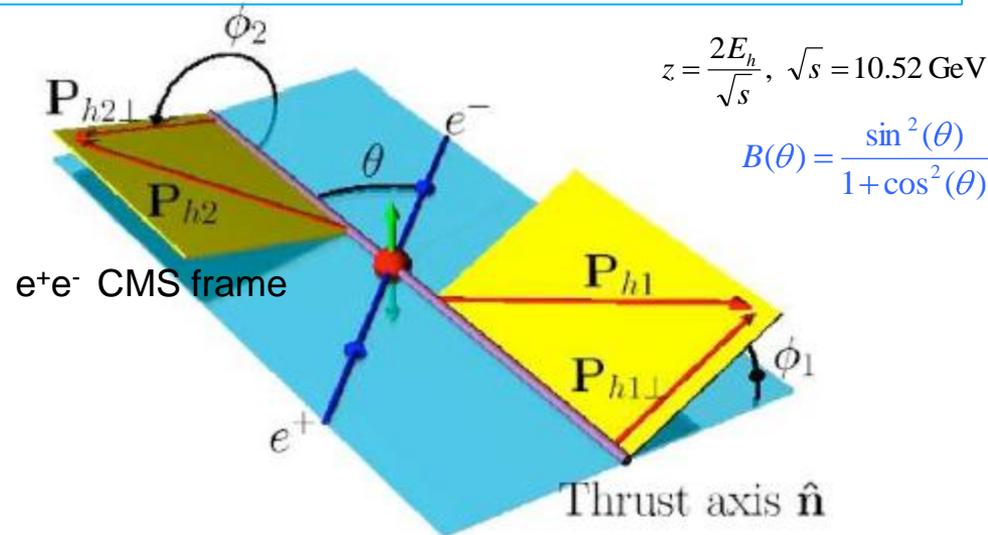
Transversity  $\times$  Collins FF

$$A_{\text{Coll}} = \frac{A}{fP_T} = \frac{\sum_q e_q^2 \Delta_T q H_1^{\perp q}}{\sum_q e_q^2 q D_1^q}$$

$$e^+e^- \rightarrow h_1 h_2 X$$

Quark spin direction unknown:  
measurement of Collins FF in one hemisphere is not possible

$\rightarrow$  Measurement of azimuthal correlations for pion pairs around the jet axis in two-jet events; amplitude of  $\cos(\phi_1 + \phi_2)$  modulation



$$z = \frac{2E_h}{\sqrt{s}}, \sqrt{s} = 10.52 \text{ GeV}$$

$$B(\theta) = \frac{\sin^2(\theta)}{1 + \cos^2(\theta)}$$

$$A \propto B(\theta) \frac{\sum_q e_q^2 H_1^{\perp q}(z_1) \cdot \bar{H}_1^{\perp q}(z_2)}{\sum_q e_q^2 D_1^q(z_1) \cdot \bar{D}_1^q(z_2)}$$

# Accessing the transversity PDF: two hadron mechanism

$$I N^\uparrow \rightarrow I' h h X$$

azimuthal asymmetry in the

$$\text{angle } \phi_{RS} = \phi_{R-L} - \phi_S$$

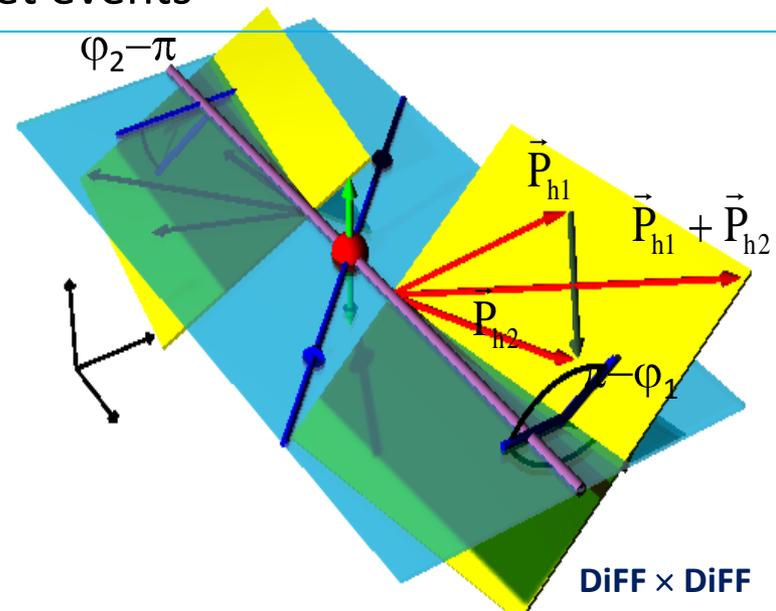
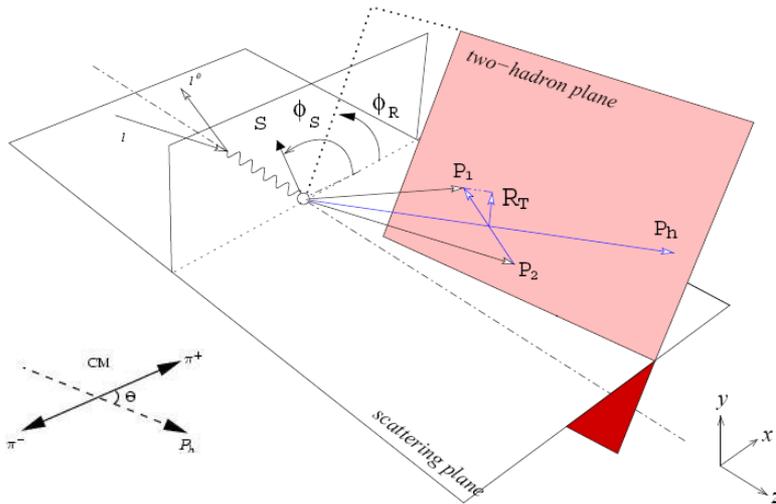
in which  $\phi_{R-L}$  is the angle of the plane defined by the two hadrons

$$e^+e^- \rightarrow (h_1 h_2)_{\text{jet1}} (h_1 h_2)_{\text{jet2}} X$$

quark spin direction unknown:

measurement of di-hadron FF in one hemisphere is not possible

→ Measurement of azimuthal correlations for di-pion pairs around the jet axis in two-jet events



$$A_{RS} = \frac{A}{fP_T} \propto \frac{\sum_q \mathbf{e}_q^2 \cdot \Delta_T q(x) \cdot H_q^{2h}(z, M_h^2)}{\sum_q \mathbf{e}_q^2 \cdot q(x) \cdot D_q^{2h}(z, M_h^2)}$$

**Transversity × DiFF**

$$A \propto B(\theta) \frac{\sum_q \mathbf{e}_q^2 H_1^{2h}(z_1, m_1) \cdot \bar{H}_1^{2h}(z_2, m_2)}{\sum_q \mathbf{e}_q^2 D_1^{2h}(z_1, m_1) \cdot \bar{D}_1^{2h}(z_2, m_2)}$$

**DiFF × DiFF**

# *Experiments*

# From the experimental point of view...

## SIDIS

Tools needed for the measurement:

- polarized targets
- large acceptance spectrometer with full particle identification : identification of scattered lepton and produced hadrons
- good coverage in azimuthal angle acceptance

For a **global interpretation of the measurements**:

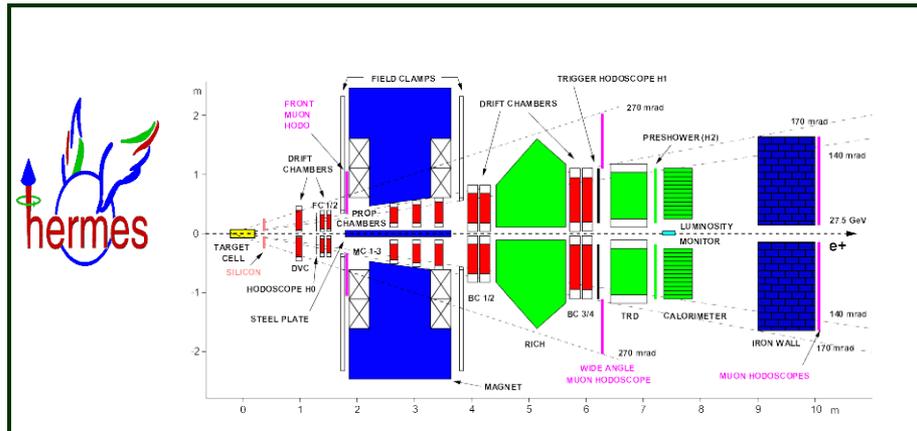
- different target materials
- cover large kinematical ranges
- measure on different hadrons

*→ complementarity between different experiments is important*

## $e^+e^-$ annihilation

- large data sample available → suitable to measure small asymmetries
- good particle ID (light quarks)
- good coverage in azimuthal angle acceptance

# The SIDIS experiments



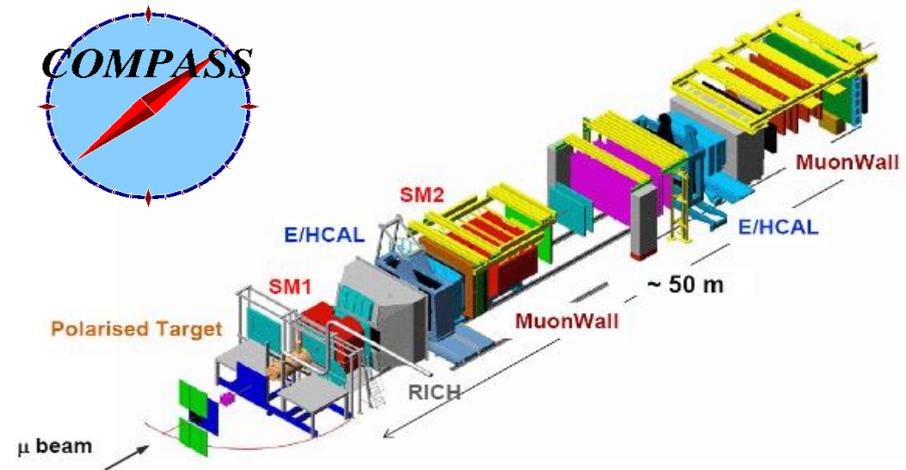
polarized (<60%)  $e^+/e^-$  beam of 27 GeV,  
both helicity states

Gaseous target, direct access to  
hydrogen/deuterium  $\rightarrow$  dilution factor  $\sim 1$

Transverse measurement:  $p$  (long.  $p, d$ )

$P_T \sim 70-85\%$

fast spin-flip of target  $\rightarrow$  same acceptance for the  
different polarization states



polarized (-80%)  $\mu^+$  of 160 GeV

Solid state target, 120 cm long

${}^6\text{LiD}$  ( $d$ )  $P_T \sim 50\%$  ;  $f \sim 0.40$  both L and T

$\text{NH}_3$  ( $p$ )  $P_T \sim 80\%$  ;  $f \sim 0.15$  both L and T

nearby cells are oppositely polarised to take data  
simultaneously on the two orientations of the  
target  $\rightarrow$  Spin reversal in order of the hours/days

# The SIDIS experiments

## JLab E06-010

e- beam at  $\sim 6$  GeV/c

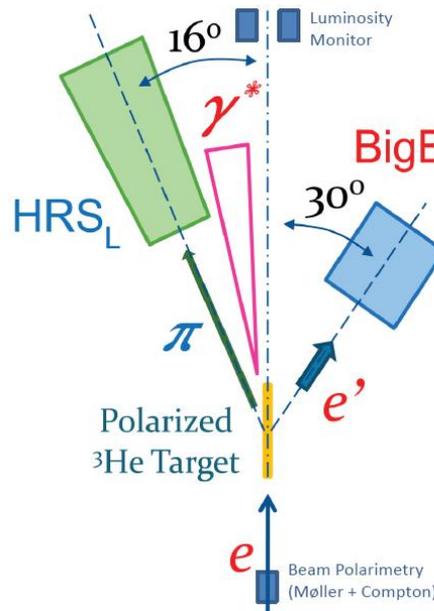
40cm  $^3\text{He}$  gas target

transversely polarised,

different orientations possible

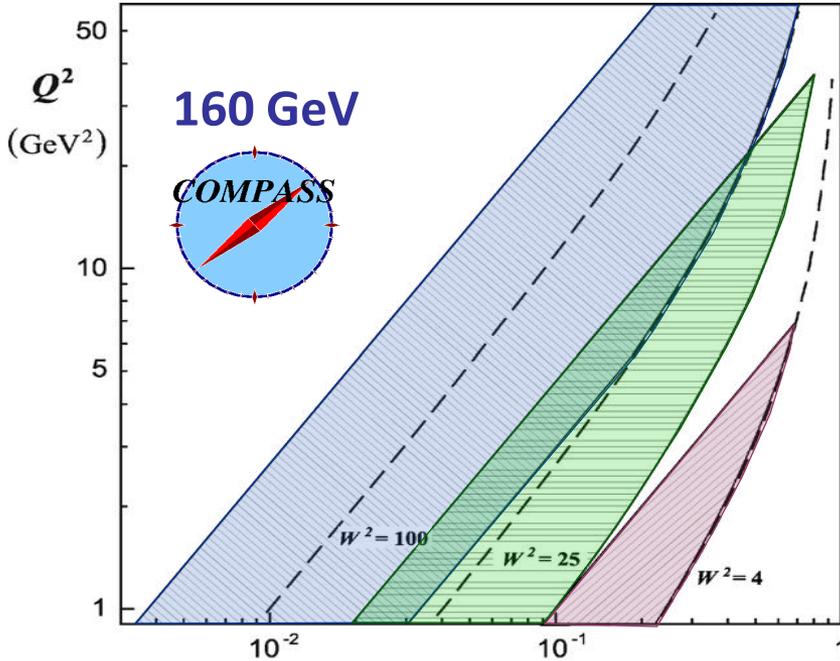
$P_T \sim 55\%$  (n)  $f \sim 0.1-0.3$

Spin flip every 20 minutes



# Phase space of different experiments

Strong dependence of  $x$ ,  $Q^2$  and  $W$ , depending on the lepton beam energy.



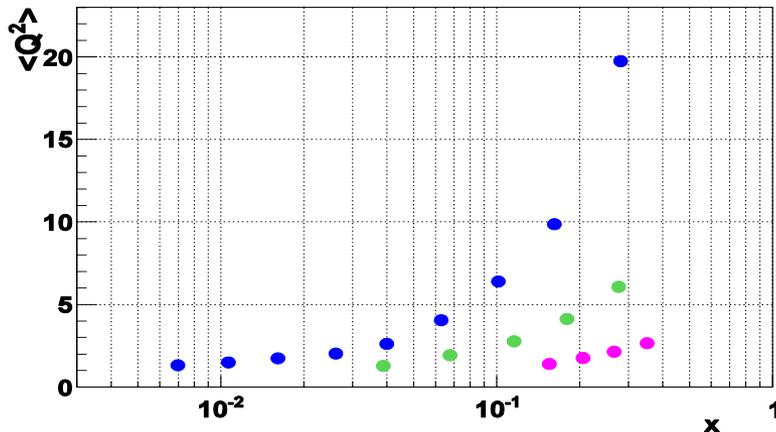
27.5 GeV

$0.004 < x < 0.3$ ,  $25 < W^2 < 200 \text{ GeV}^2$

$0.023 < x < 0.4$ ,  $10 < W^2 < 50$

$0.14 < x < 0.48$ ,  $4 < W^2 < 10$

JLab 6 GeV



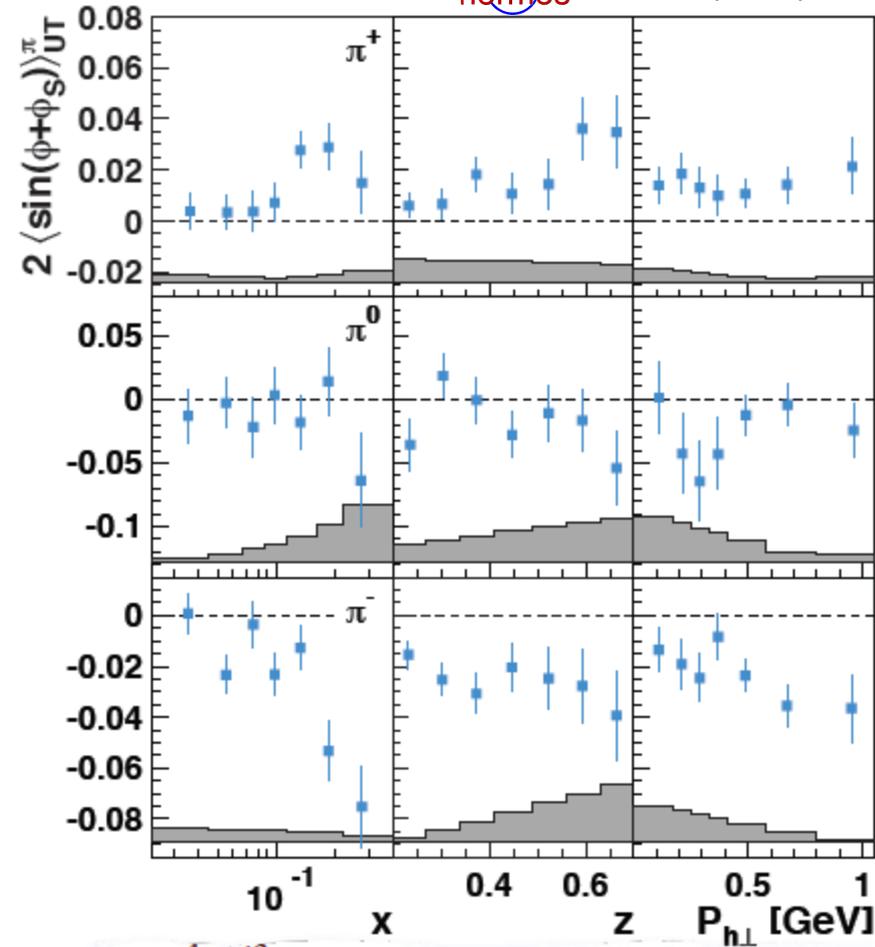
Phase space determined also by cuts

- $Q^2 > 1 (\text{GeV}/c)^2$
- $y$  ( $0.1 < y < 0.9/0.95$ )
- low  $W$  to avoid resonance regions
- cut on **momenta** imposed by PID
- **relative energy  $z$**  of each hadron:
  - lower cut to avoid fragmentation region, usually  $z > 0.1-0.2$  (*depending on  $W$* )
  - higher cut ( $z < 0.7, 0.85$ )

# *Results*

# Collins asymmetries, results on proton

hermes PLB 693 (2010) 11



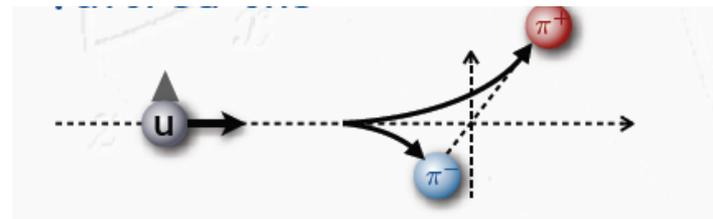
2005: First evidence that transversity PDF and Collins FF are different from zero

- Increase signal with  $x$ , valence region
- Increase also with  $z$  (agreement with Belle)
- clear signal for  $\pi^+$  and  $\pi^-$   $x > 0.1$

$$A_{\text{Coll}}^{p, \pi^+} \sim e_u^2 h_1^u H_1^{\perp, \text{fav}} + e_d^2 h_1^d H_1^{\perp, \text{unf}}$$

$$A_{\text{Coll}}^{p, \pi^-} \sim e_u^2 h_1^u H_1^{\perp, \text{unf}} + e_d^2 h_1^d H_1^{\perp, \text{fav}}$$

$$\rightarrow H_1^{\text{unf}} \sim -H_1^{\text{fav}}$$

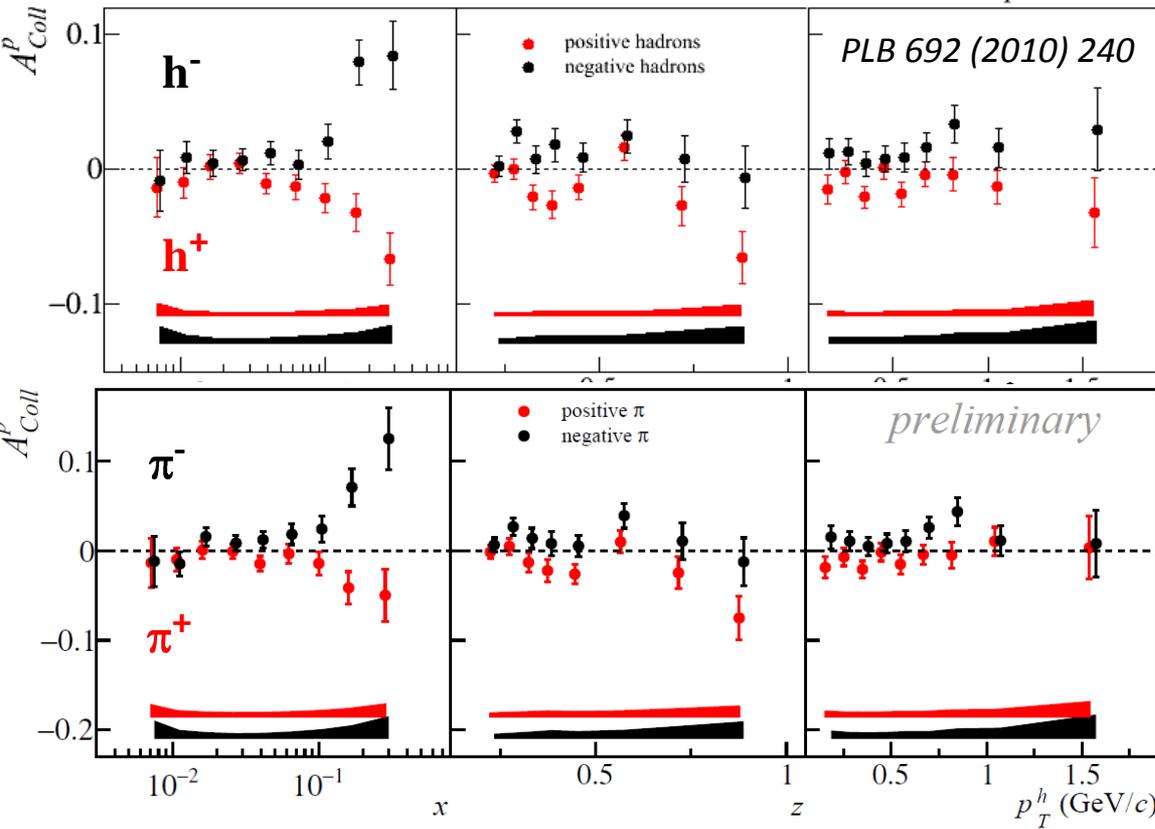


As predicted in recursive fragmentation model with quark spin [X.Artru, arXiv:1001.1061]

# Collins asymmetries, results on proton



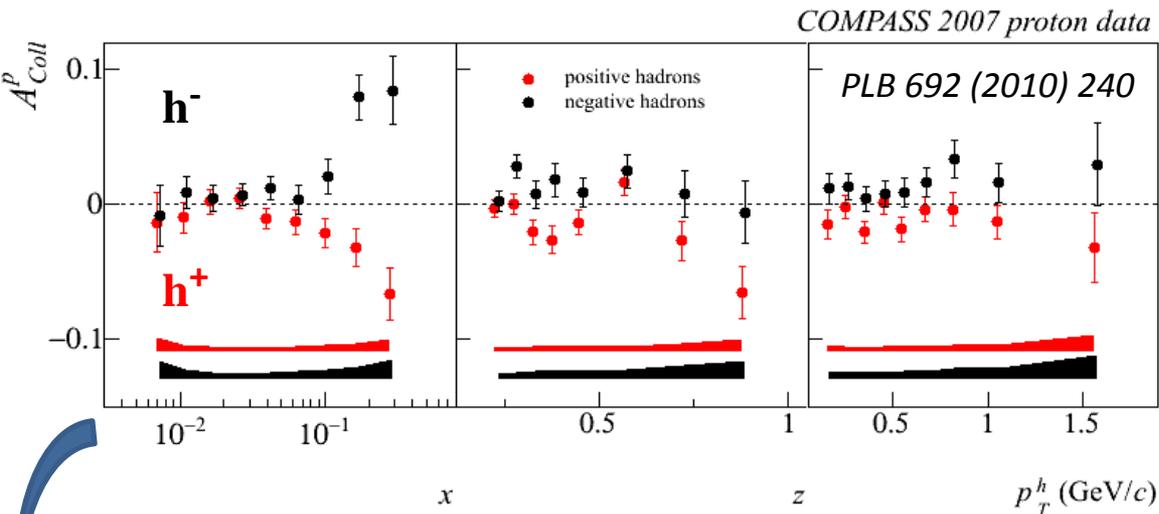
COMPASS 2007 proton data



COMPASS results from 2007 proton run

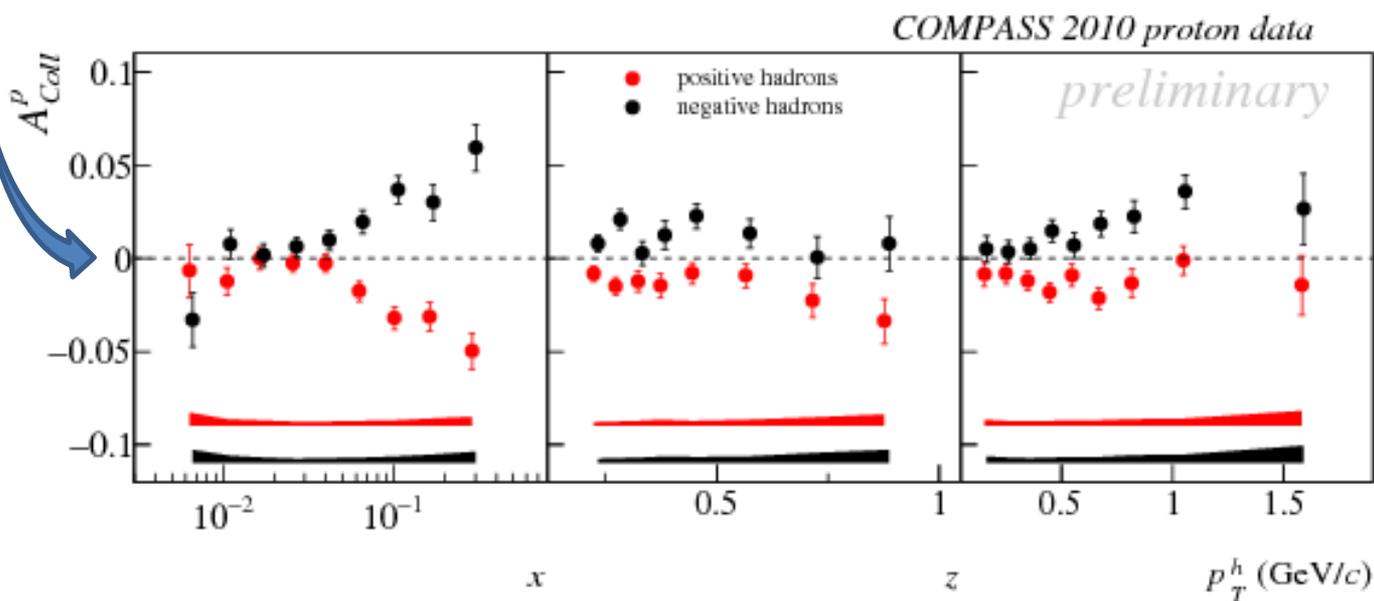
- at small  $x$ , region not covered by HERMES asymmetries compatible with zero
- Strong signal in the valence region of opposite sign for  $\pi^+$  and  $\pi^-$  - agreement with HERMES

# Collins asymmetries, results on proton



COMPASS results from 2007 proton run

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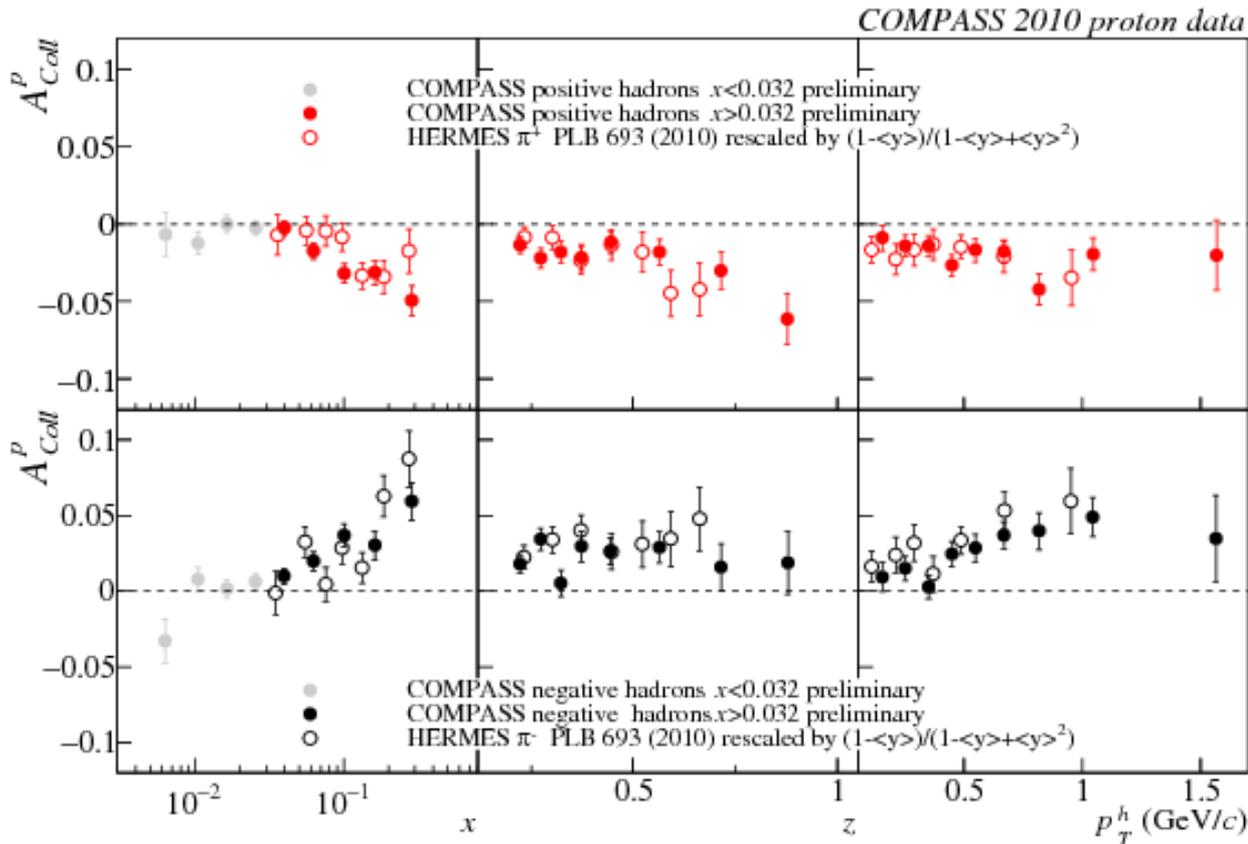


Recent result from the 2010 run, independent measurement:

confirm the 2007 results with higher precision (factor  $\sim 2$ )

# Collins asymmetries, results on proton

- Comparison between HERMES and COMPASS, taking into account the different conventions (sign,  $D_{nn}$ )
- and limiting COMPASS range to the  $x > 0.032$  region, overlap with HERMES

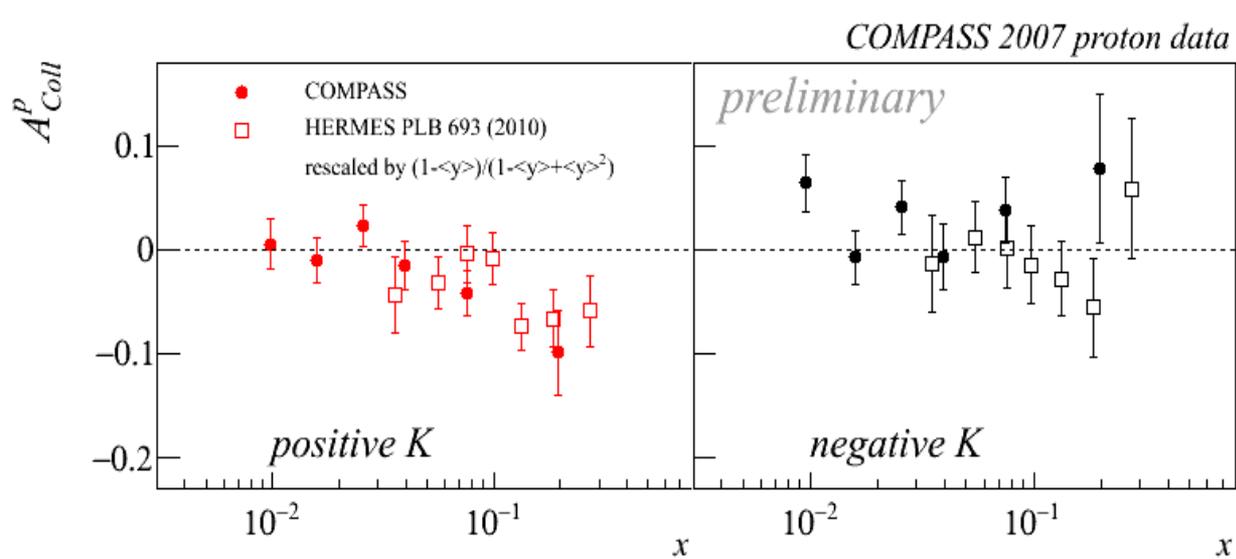


Good agreement :

- Non trivial result:  
 $Q^2$  COMPASS larger  
of HERMES's of a factor  
2-3 in the last  $x$  bins  
 $\rightarrow$  weak  $Q^2$  dependence  
of the Collins effect



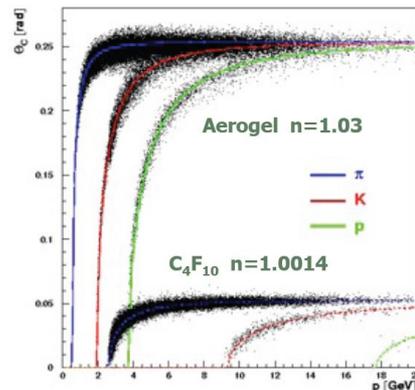
# Collins kaon asymmetries, results on proton



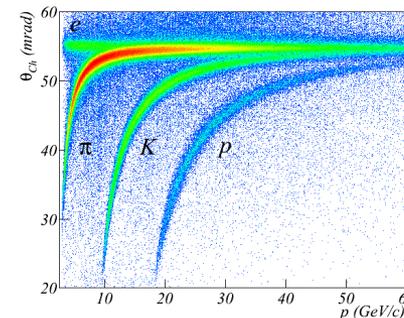
Results in agreement

- $K^-$  consistent with zero
- $K^+$  are similar to  $\pi^+$ , expected from u-dominance;
- $K^+$  signal slightly larger than  $\pi^+$ : role of sea quarks?

More precise K results from 2010 COMPASS data soon available



RICH PID K:  
2-15 GeV

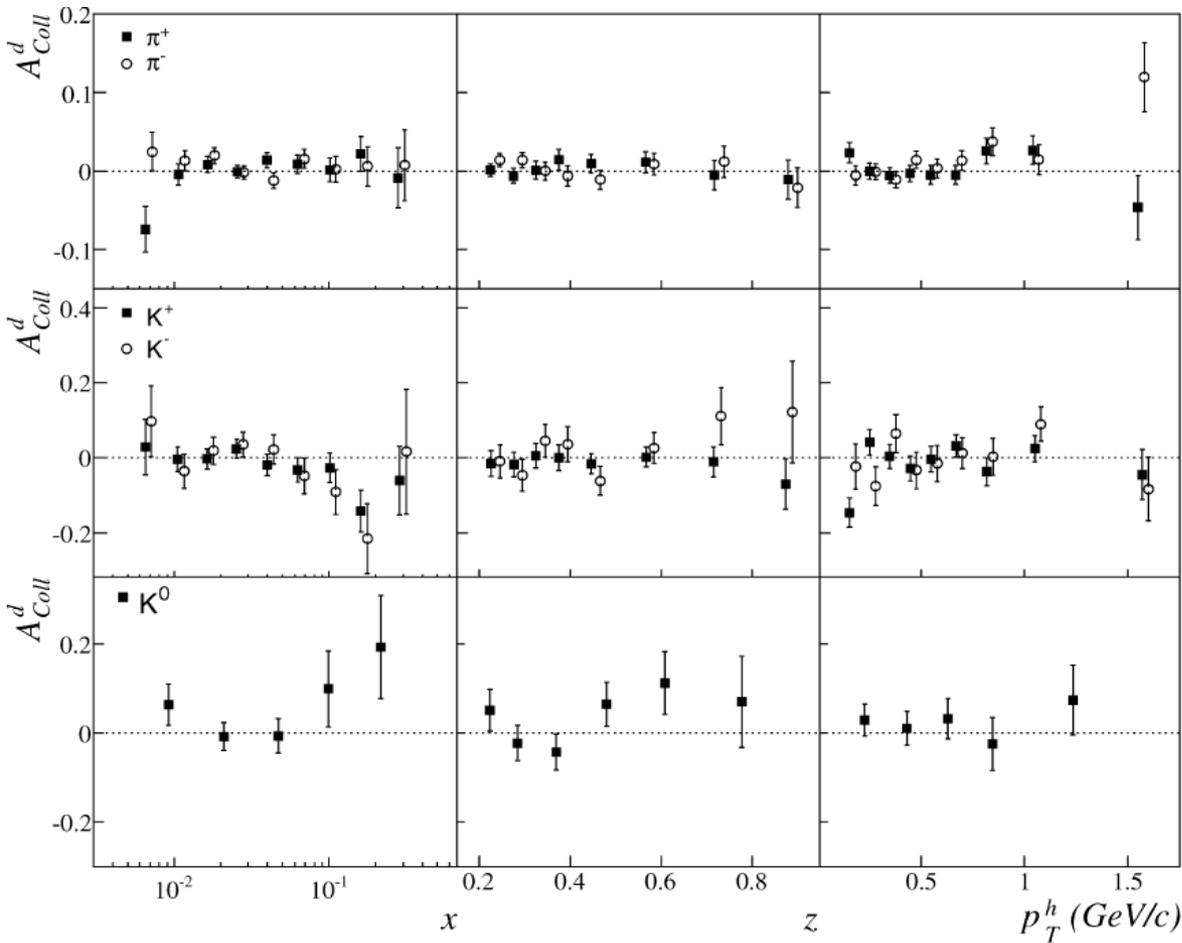


RICH PID K:  
9-50 GeV

# Collins asymmetries, results on deuterium



PLB 673(2009)127-135



$$A_d^{\pi^+} = - \frac{(h_1 T_u + h_1 T_d) \otimes (4H_{fav} + H_{unf})}{(u + d) \otimes (4D_{fav} + D_{unf})}$$

$$A_d^{\pi^-} = - \frac{(h_1 T_u + h_1 T_d) \otimes (H_{fav} + 4H_{unf})}{(u + d) \otimes (D_{fav} + 4D_{unf})}$$

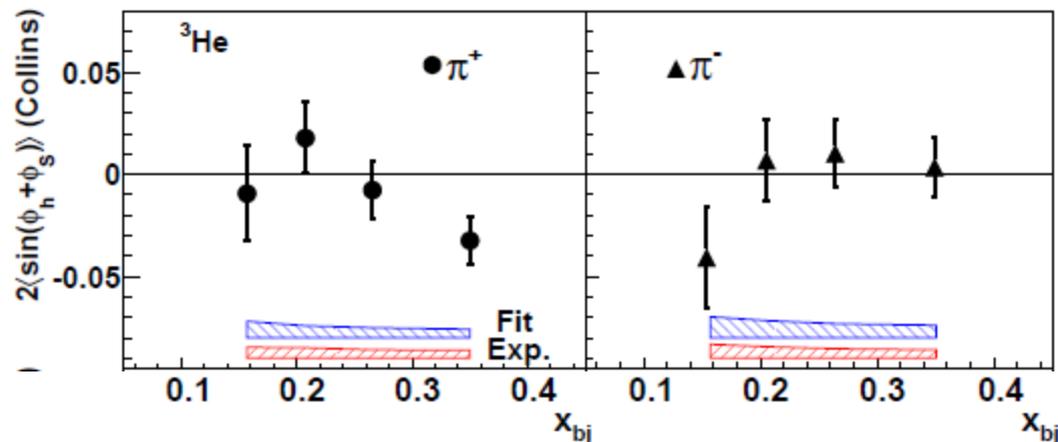
Some small effect expected even if  $H_{unf}^1 \sim -H_{fav}^1$   
 $\rightarrow$  cancellation between  $\Delta_T u(x)$  and  $\Delta_T d(x)$

*handle on  $\Delta_T d(x)$*

# Collins asymmetries, results on neutron

Another handle on  $\Delta_T d(x)$  is provided by measurement on neutron

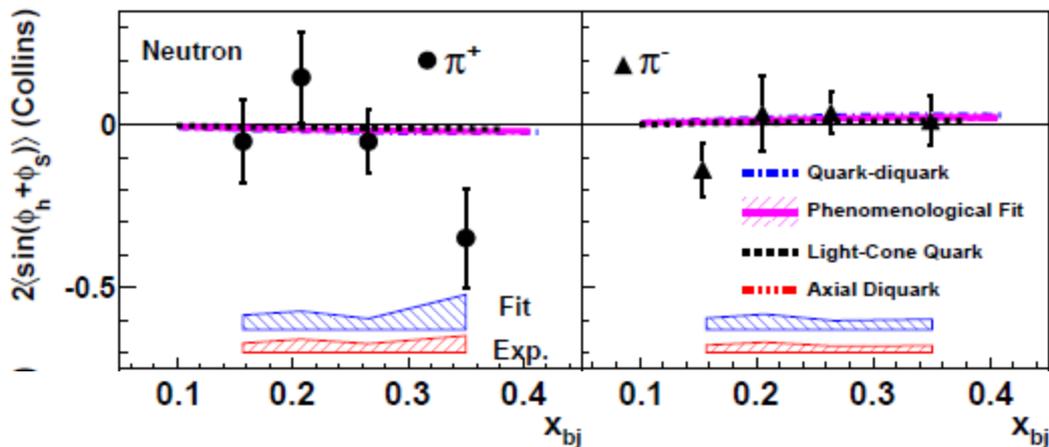
JLAB E06-010 Collaboration *PRL 107:072003,2011*



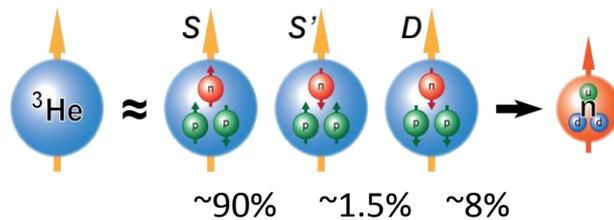
Consistent with zero except  $\pi^+$  at  $x \sim 0.34$

Agreement with expectation from models and fit

Limited statistical precision



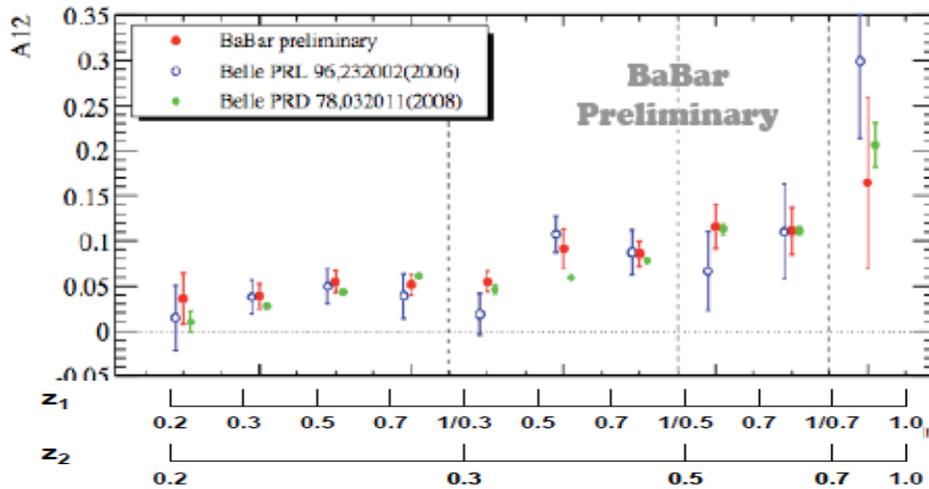
$$A_{^3\text{He}}^{C/S} = P_n \cdot (1 - f_p) \cdot A_n^{C/S} + P_p f_p \cdot A_p^{C/S}$$



1<sup>st</sup> order 2p have spins anti-aligned  $\rightarrow$  spin carried by the neutron

# Collins effect in $e^+e^-$ annihilation

2005: Belle measured sizeable asymmetries : Independent proof that Collins FF are different from zero



Belle: 547 fb<sup>-1</sup> data set, small statistical uncertainties;  
Measured asymmetries rising with  $z$ .

Preliminary results from BaBar, 45 fb<sup>-1</sup>

Asymmetries in good agreement

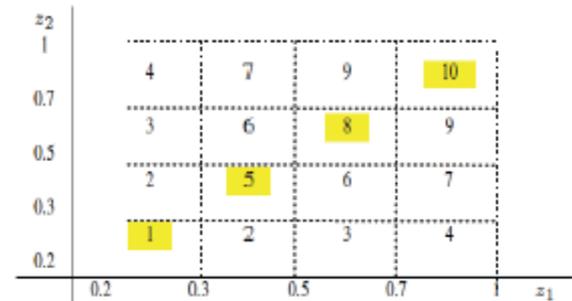
BaBar preliminary:  
 $\mathcal{L} \approx 45 \text{ fb}^{-1}$

Belle Off-peak:  
 $\mathcal{L} \approx 29 \text{ fb}^{-1}$

Belle full statistics  
(supersede previous results)  
 $\mathcal{L} \approx 547 \text{ fb}^{-1}$



I. Garzia, Transversity2011



# Collins asymmetries: summary

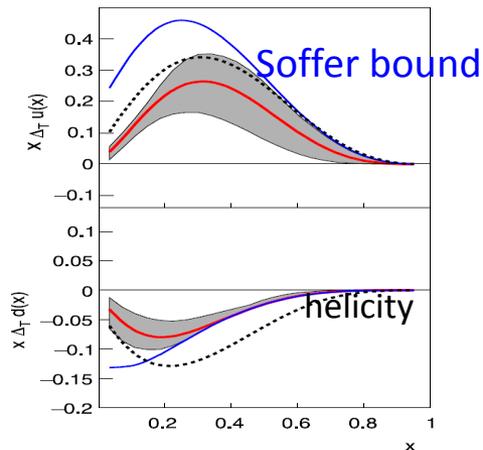
From 2005 onward, many new results for the Collins asymmetries at SIDIS experiments and  $e^+e^-$  colliders :

high statistical precision

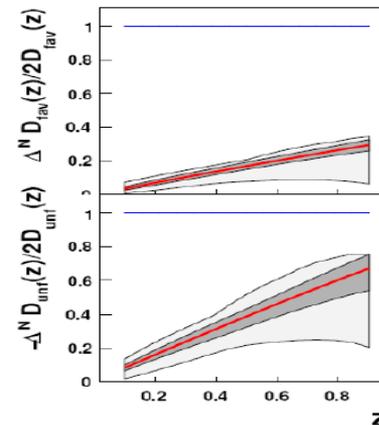
and

covering large kinematical range

→ they can be used in a global fits to extract transversity PDF and Collins FF with improved precision



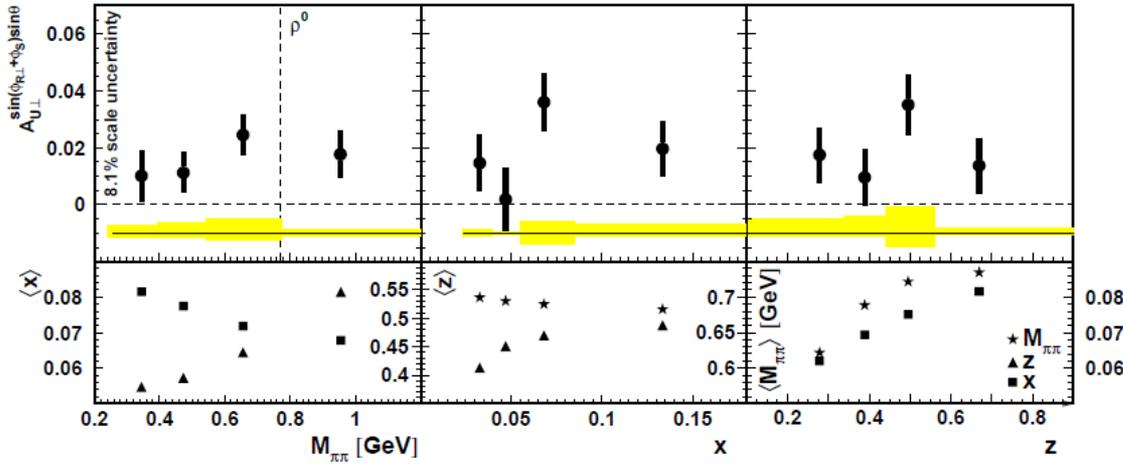
**M. Anselmino et al.,**  
Nucl.Phys.Proc.Suppl.  
191 (2009) 98



# Two hadron asymmetries, proton



JHEP 0806 (2008) 017



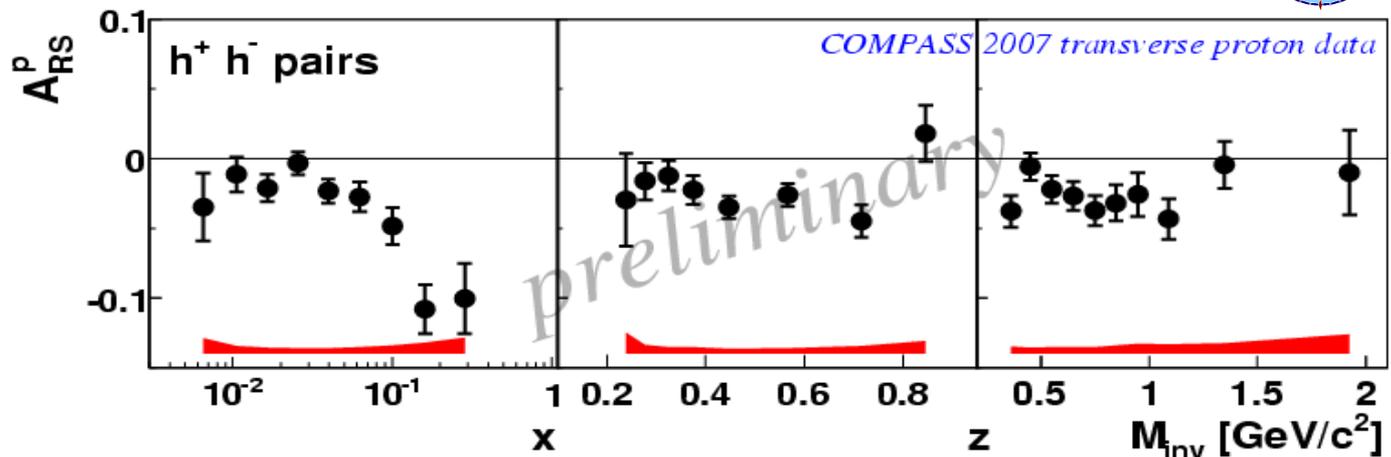
First evidence for a interference FF different from zero

Invariant mass dependence ruled out Jaffe model of a change sign to  $\rho$  mass

Submitted to PLB 

At small  $x$ , region not covered by HERMES asymmetries compatible with zero

large signal in the valence region

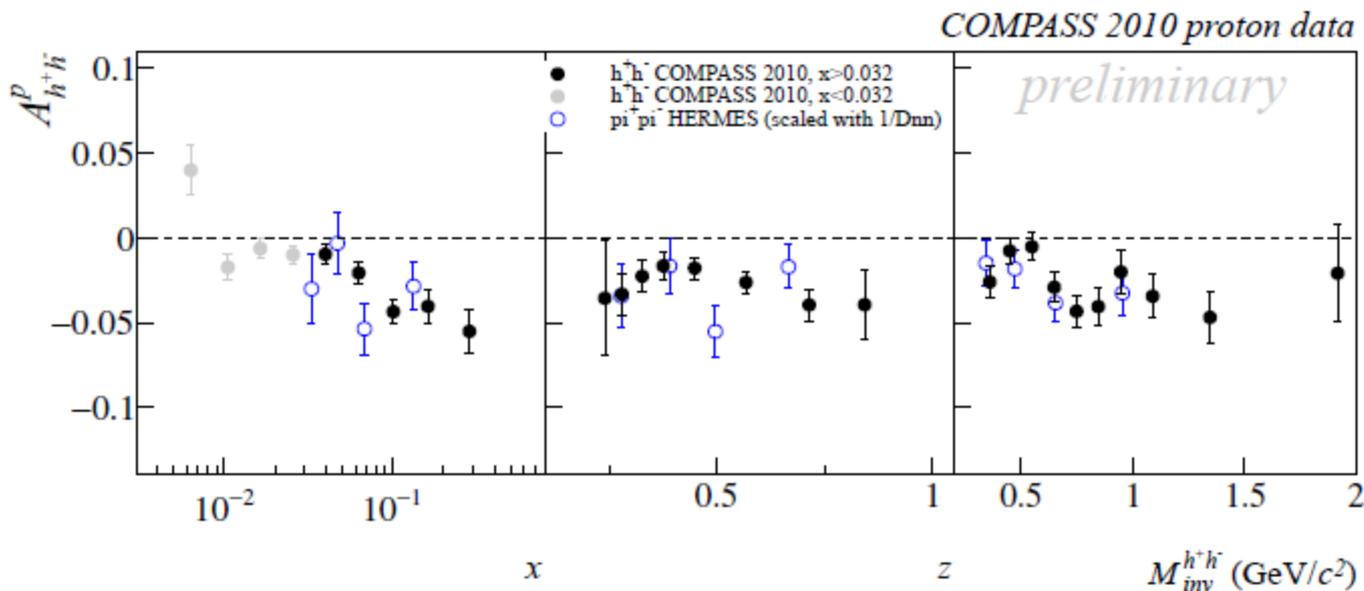


# Two hadron asymmetries, proton

Results from 2010 run COMPASS available, here compared with HERMES

- Comparison between HERMES and COMPASS taking into account the different conventions (sign,  $D_{nn}$ )
- and limiting COMPASS range to the  $x > 0.032$  region, overlap with HERMES

This selection makes the  $M_{inv}$  dependence more visible



Good agreement

Broader range  
for COMPASS data  
in invariant mass

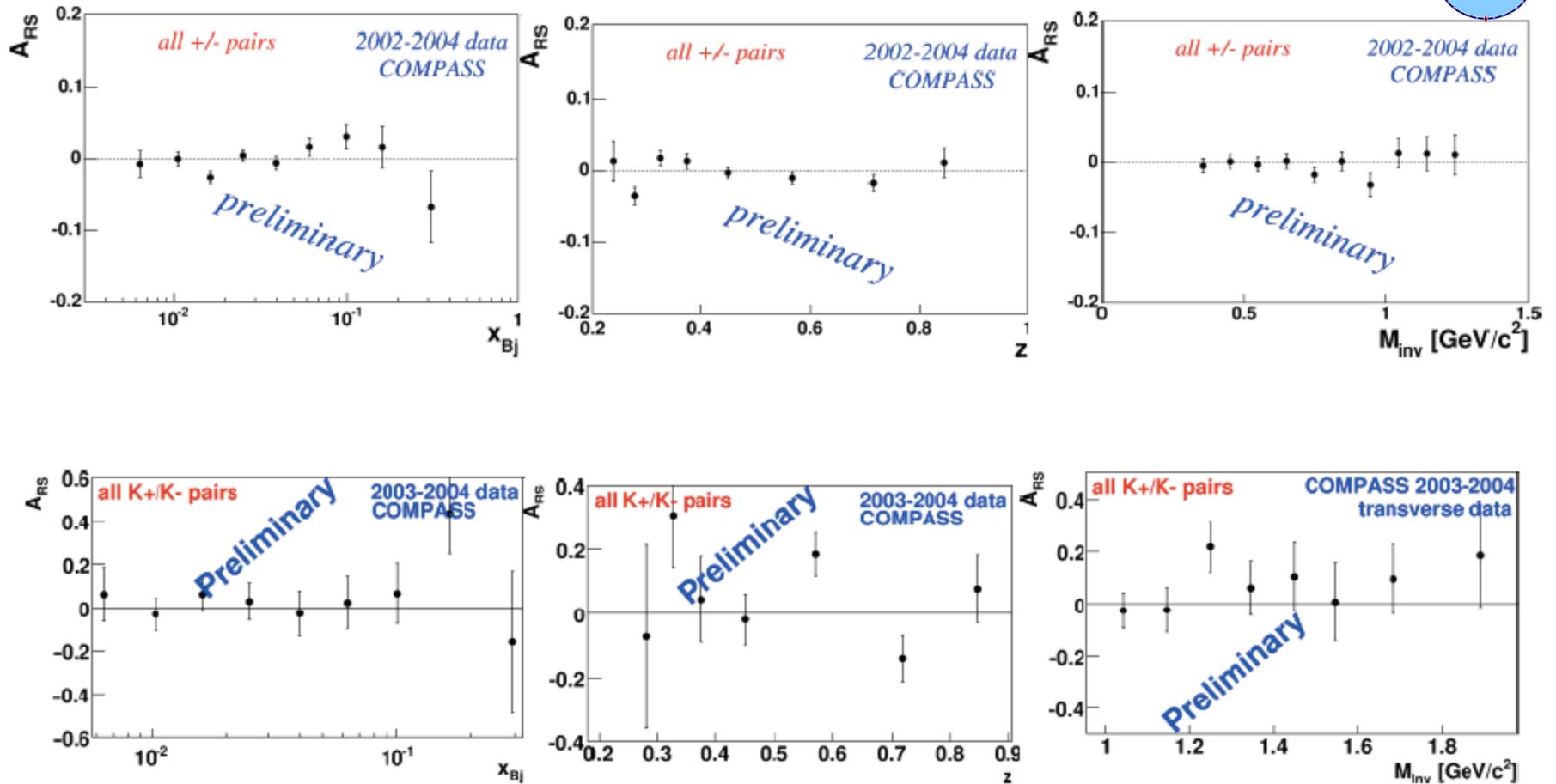


# Two hadron asymmetries, deuterium

Compass measured also very small asymmetries on deuterium



Submitted to PLB



Also other hadron combination  $\pi^+\pi^-$   $K^+\pi^-$   $\pi^+K^-$  compatible with zero

# Two hadron asymmetries in $e^+e^-$ annihilation

PRL107:072004(2011)

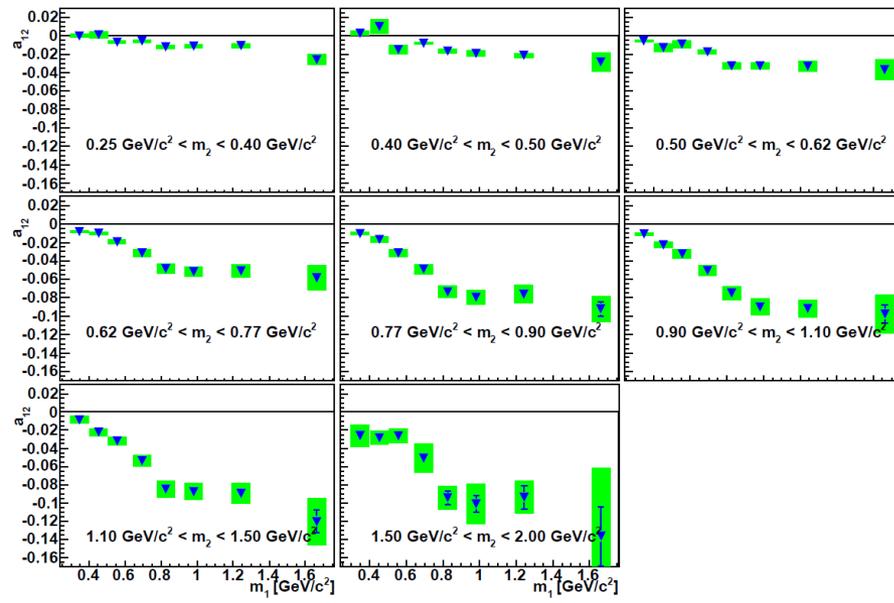
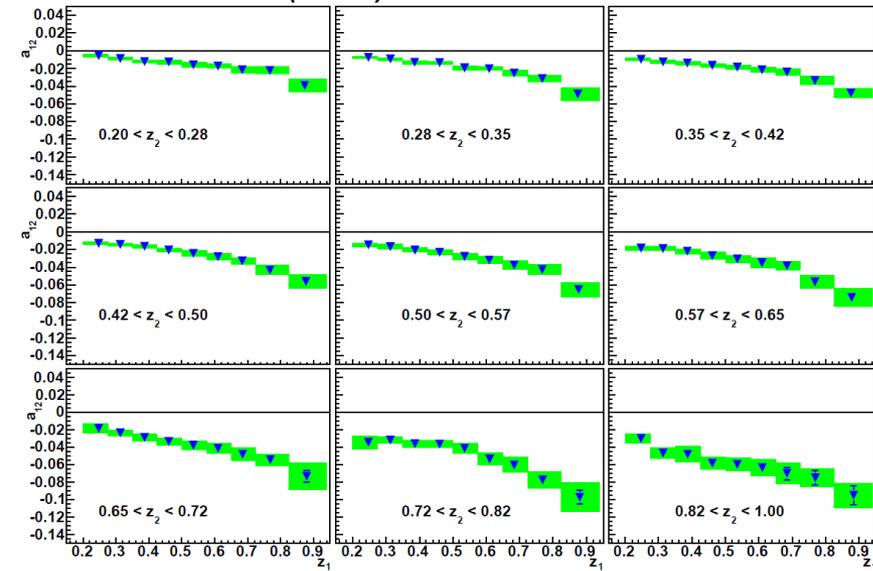
$672\text{fb}^{-1}$



Large asymmetries  
increasing with  $z$

and

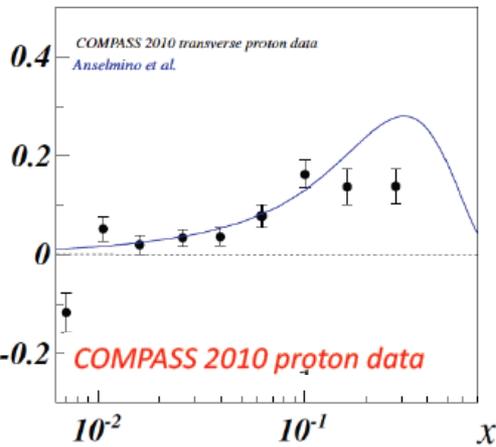
with invariant mass



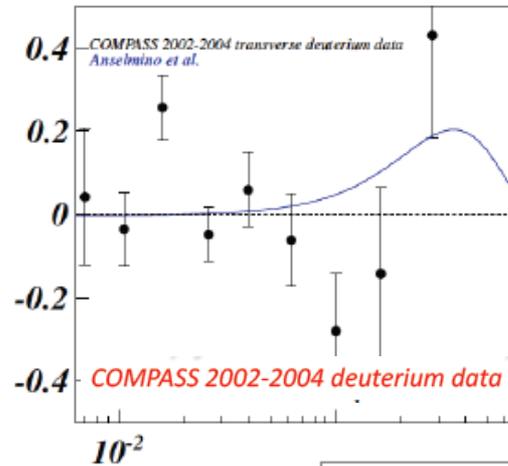
# Extracting u and d transversity from COMPASS data

Extract information on DiFF from Belle data as in “*Bacchetta, Courtoy, Radici, PRL 107:012001,2011*”; u and d transversity PDF can be extracted using COMPASS deuterium and 2010 proton data

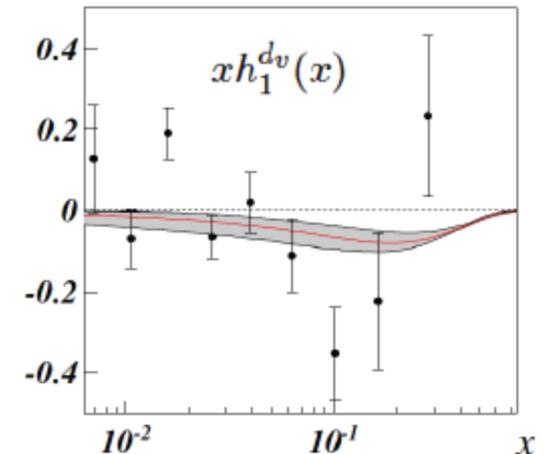
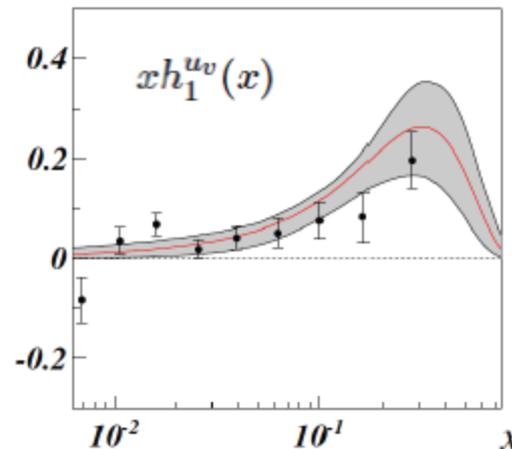
$$xh_1^{uv}(x) - \frac{1}{4}xh_1^{dv}(x)$$



$$xh_1^{uv}(x) + xh_1^{dv}(x)$$



C.Elia PhD thesis,  
Trieste  
December 2011



# Conclusions

- Big progress in few years in the field of transversity
- Several precise measurements that provide information on transversity and spin dependent FF are available:
  - SIDIS results, from experiments complementary on phase space and targets;
  - results from  $e^+e^-$  collider

First extraction of transversity for valence quarks ;  
still, more data are useful to study its properties

More data to come, available in near future:

- COMPASS 2010 data: pions and kaons, study of asymmetries kinematical behavior
- Babar: Collins FF full statistics
- Belle Collins and DiFF with identifications , and unpolarized FF

Further results :

JLab 12 GeV/c (plan to measure Diff also) and on a longer time scale: ep collider

backup

$$D_{1,q}(z, M_{\pi\pi}, \cos\theta) \simeq D_{1,q}(z, M_{\pi\pi}) + D_{1,q}^{sp}(z, M_{\pi\pi}) \cos\theta + D_{1,q}^{pp}(z, M_{\pi\pi}) \frac{1}{4}(3 \cos^2\theta - 1) \quad (3)$$

and

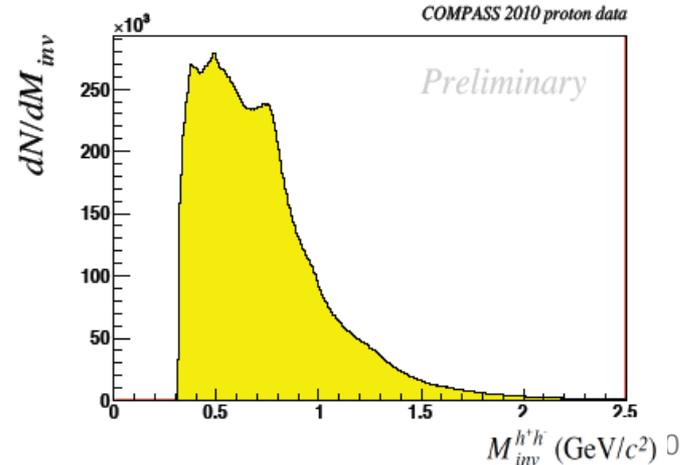
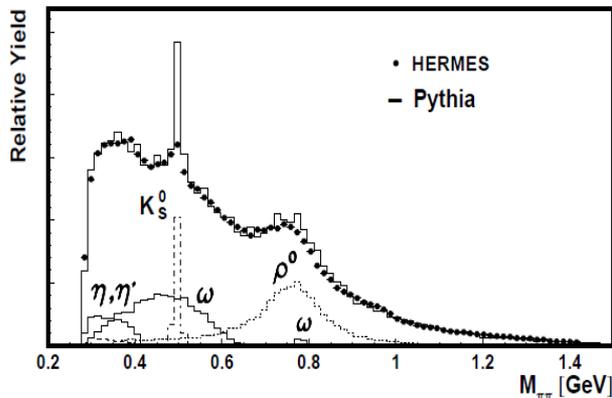
$$H_{1,q}^{\triangleleft}(z, M_{\pi\pi}, \cos\theta) \simeq H_{1,q}^{\triangleleft,sp}(z, M_{\pi\pi}) + H_{1,q}^{\triangleleft,pp}(z, M_{\pi\pi}) \cos\theta, \quad (4)$$

In compass,  $\cos\theta \sim 0$ , sensitive to  $H_{sp}$ ;  
 Extract  $A \sin(\phi) \cdot \sin(\theta)$

In HERMES

$$A_{U\perp}(\phi_{R\perp} + \phi_S, \theta') = \sin(\phi_{R\perp} + \phi_S) \frac{a \sin\theta'}{1 + b \frac{1}{4}(3 \cos^2\theta' - 1)};$$

$a \equiv A_{U\perp}^{\sin(\phi_{R\perp} + \phi_S) \sin\theta}$  is a free parameter of the fit

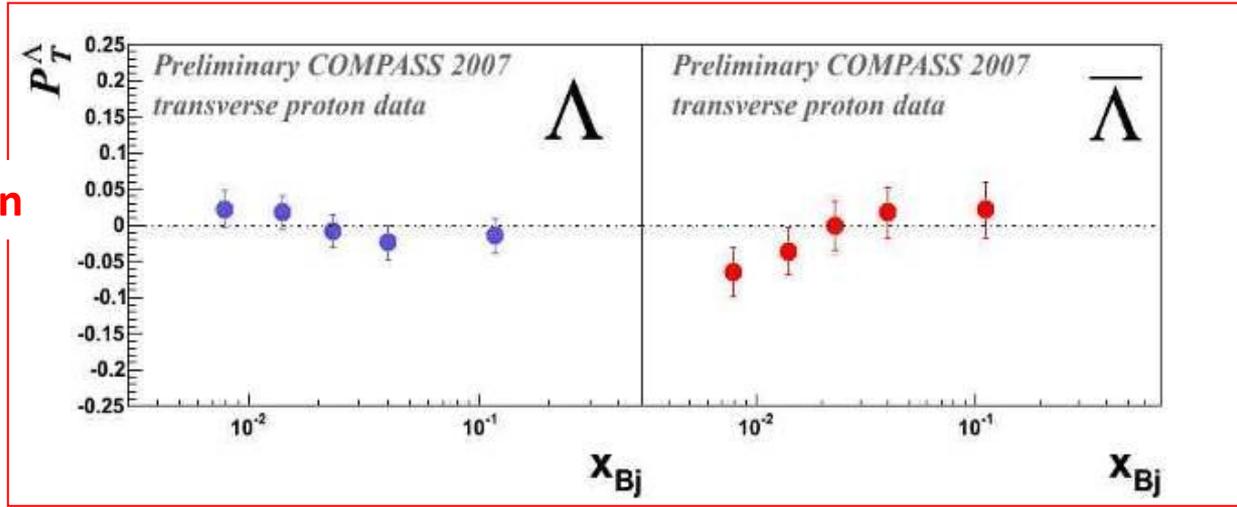
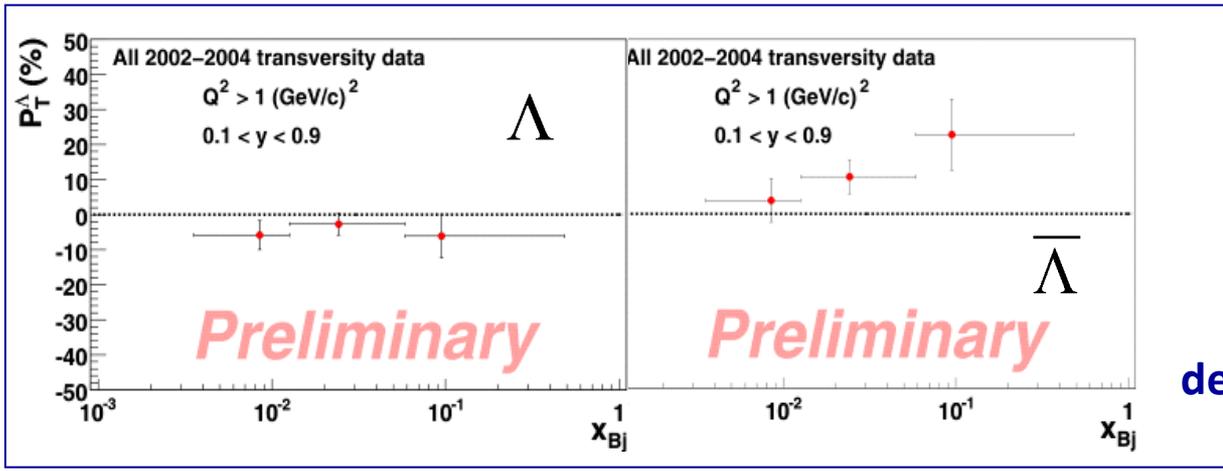
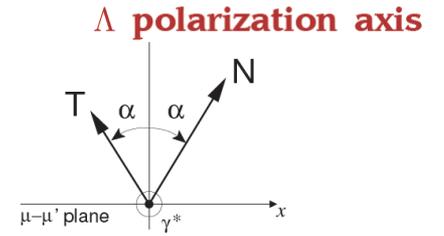


# $\Lambda$ polarisation

$$\mu N^\uparrow \rightarrow \mu' \Lambda X$$

$$\mu N^\uparrow \rightarrow \mu' \bar{\Lambda} X$$

$$P_{T,exp}^\Lambda = f P_N D(y) \frac{\sum_q e_q^2 \Delta_T q(x) \Delta_T D_{\Lambda/q}(z)}{\sum_q e_q^2 q(x) D_{\Lambda/q}(z)}$$

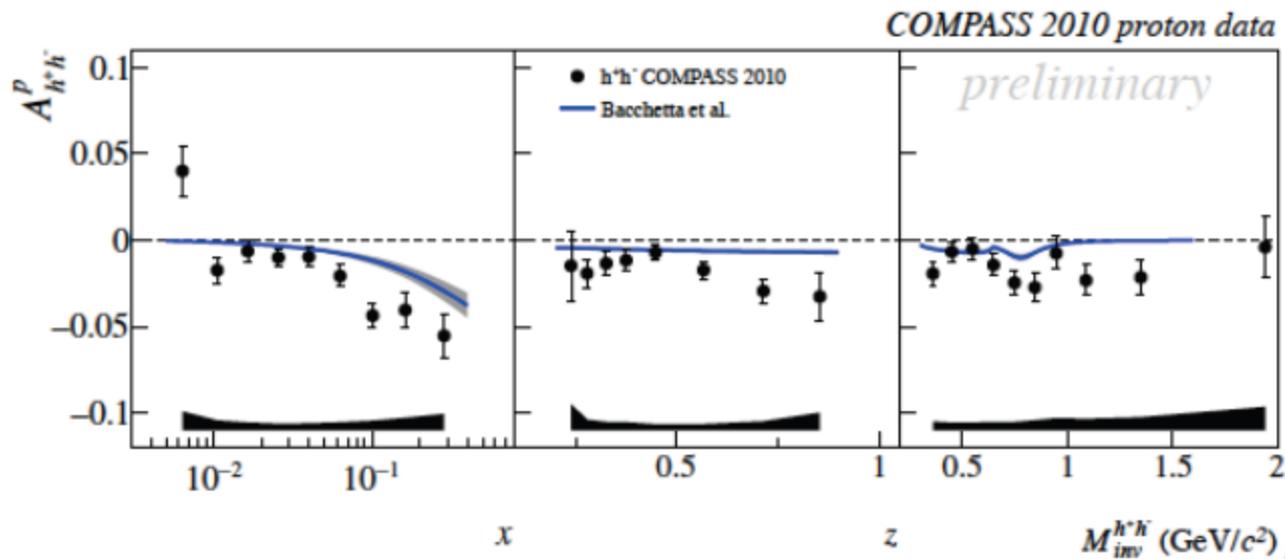


proton

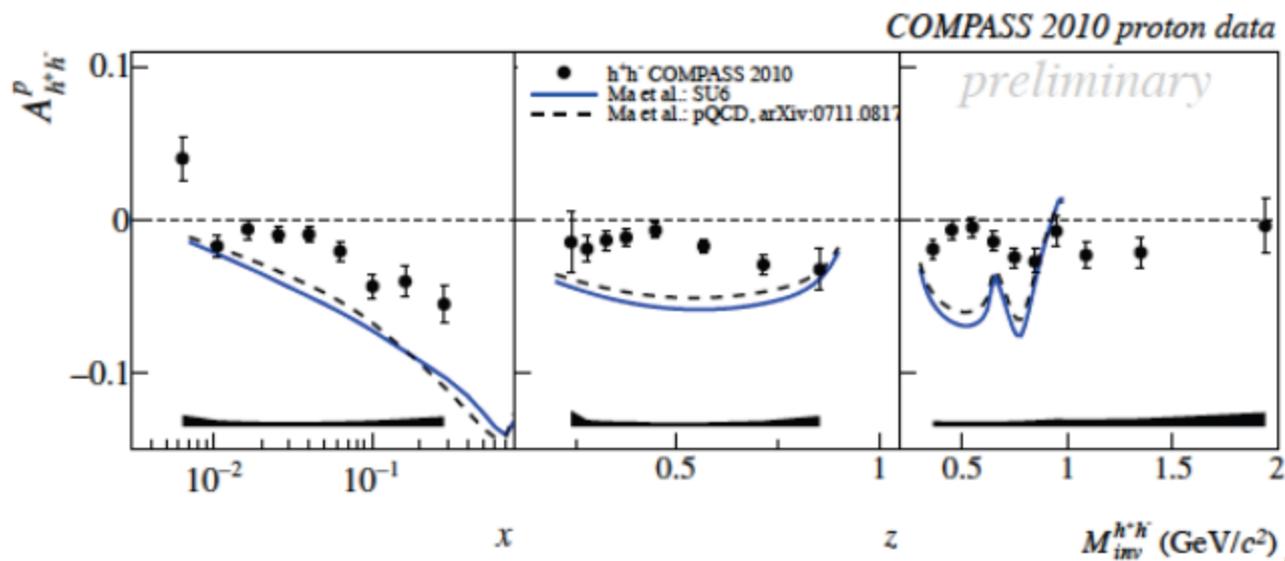
compatible with zero

more statistics is needed

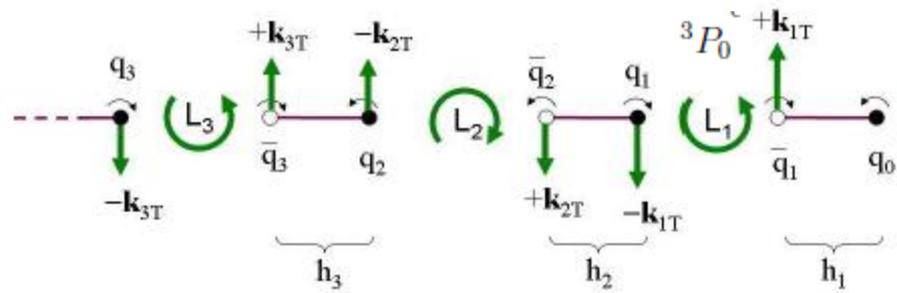
# 2010 proton data : comparison with model predictions



Bacchetta & Radici



Ma et al.

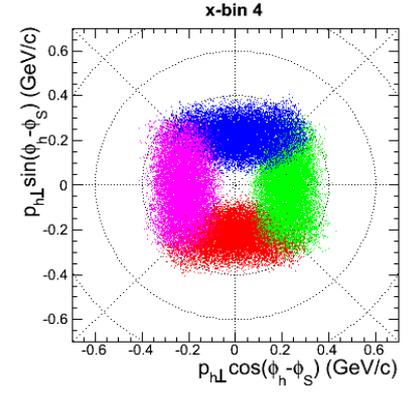
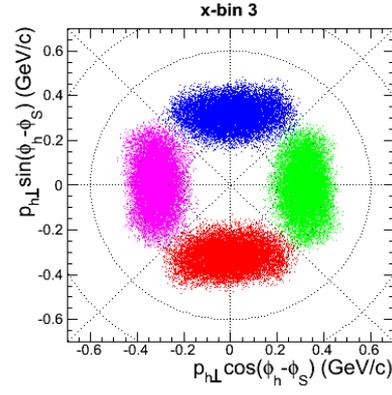
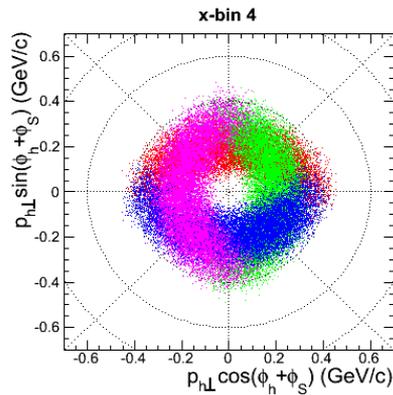
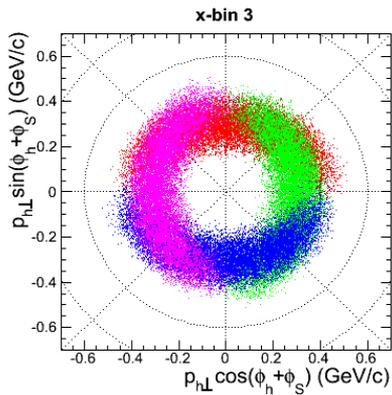
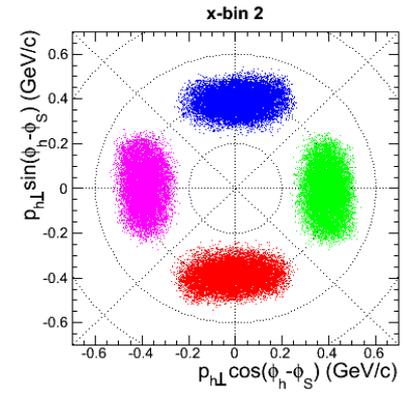
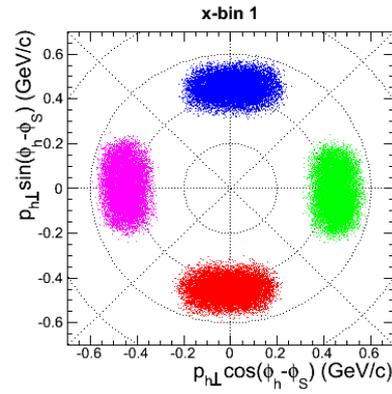
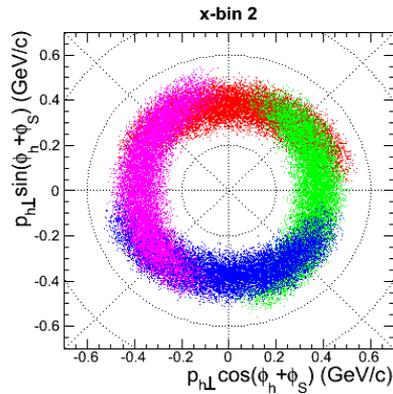
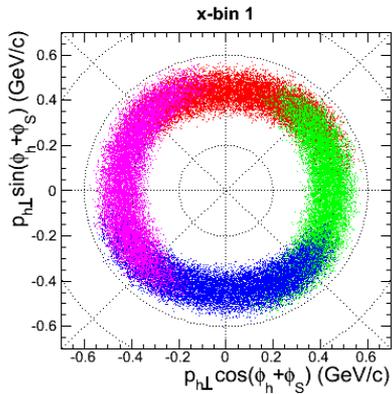


# Angular Coverage

color coded for each target spin direction: up, down, left and right.

Collins:  $\phi_h + \phi_S$

Sivers and Worm-Gear:  $\phi_h - \phi_S$

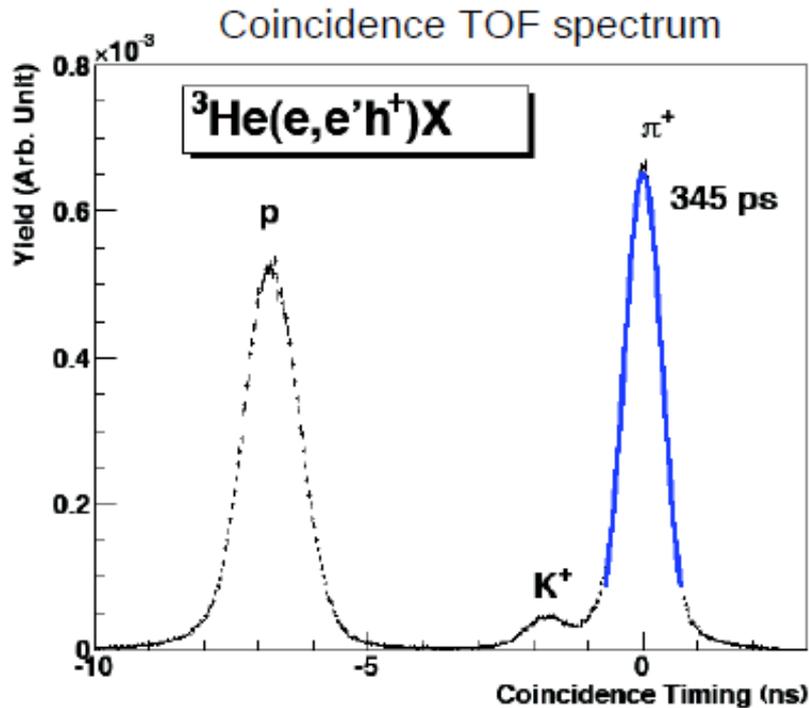


Target spin orientations: **up-down** and **left-right**  
(increases angular coverage)

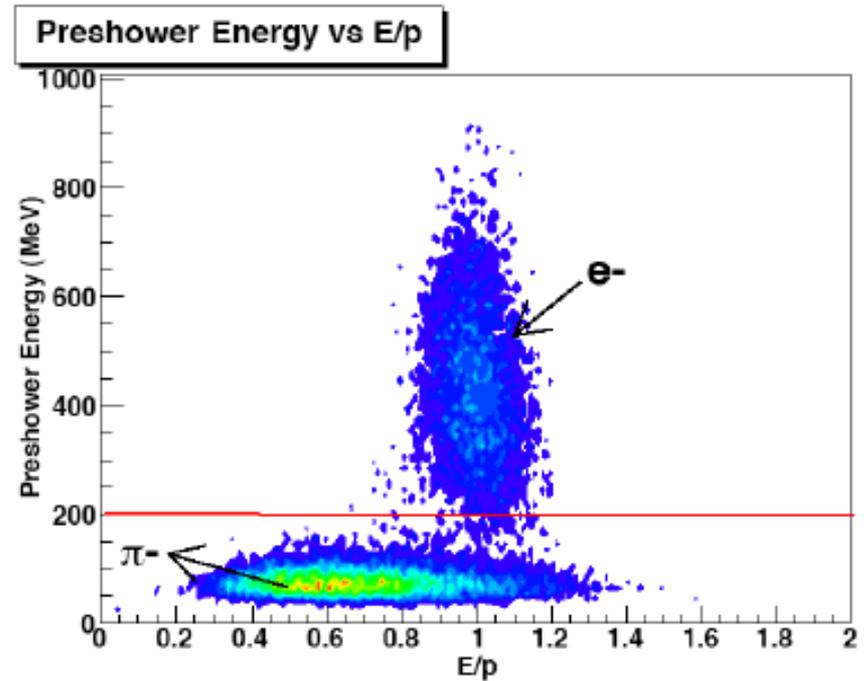


# Particle Identification

## Hadron Identification from HRS



## Electron Identification from BigBite



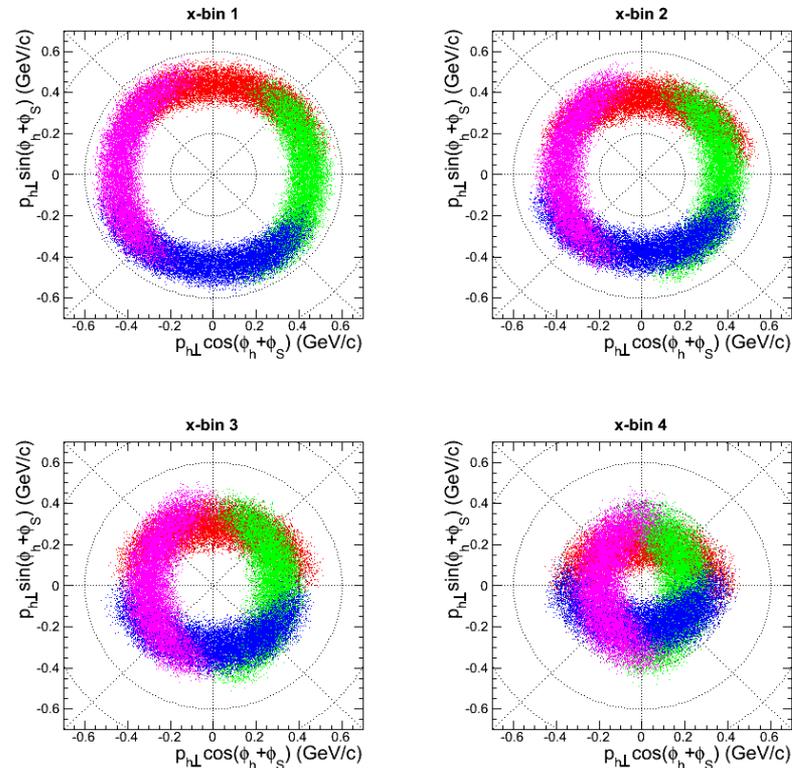
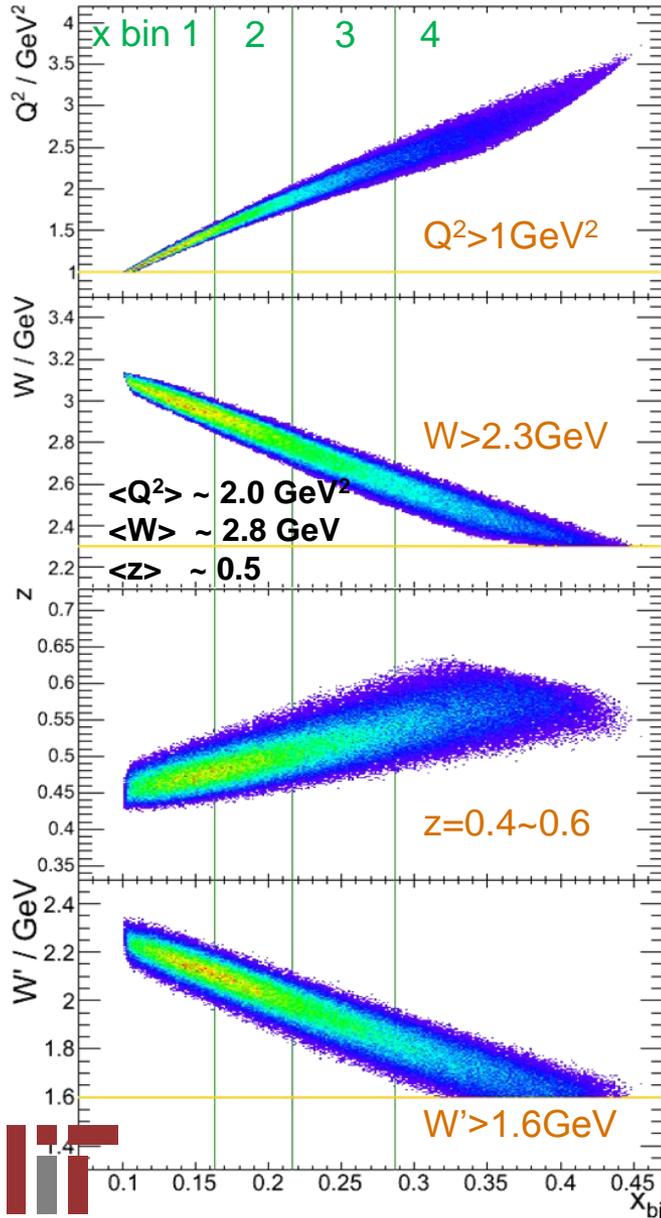
- Kaon and proton data can be separated by coincidence/TOF and the RICH detector: both provide  $K/\pi \sim 4\sigma$  separation
- Combined pion rejection 99.9%

# Kinematic Coverage

## Angular Coverage

color coded for each target spin direction: up, down, left and right.

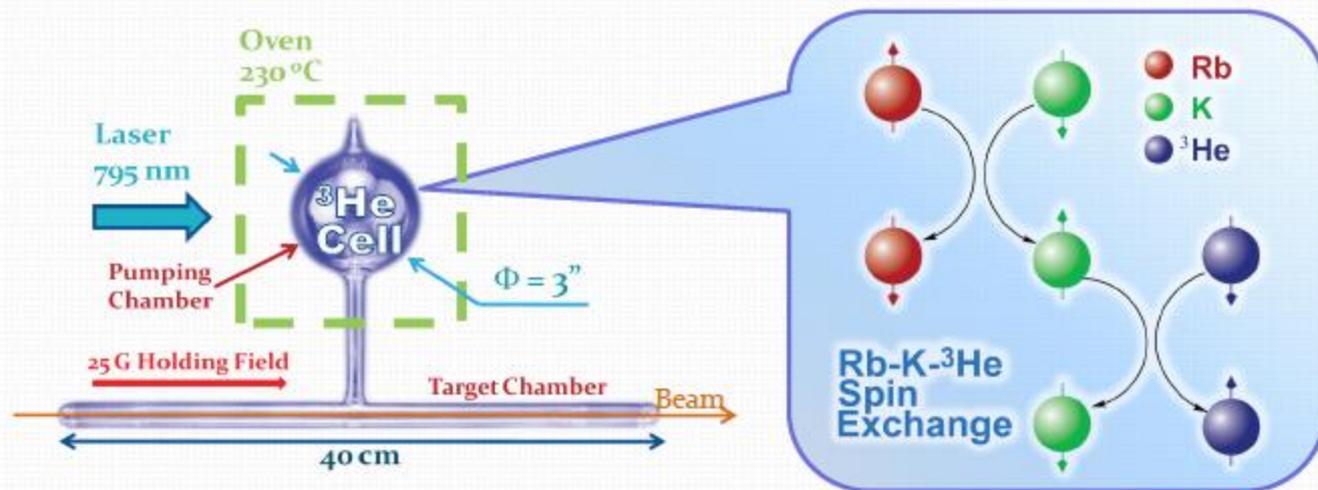
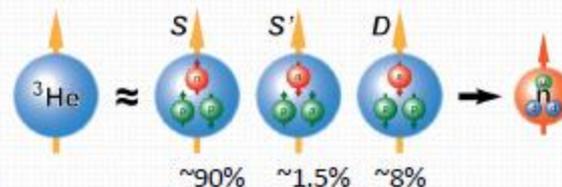
Collins:  $\phi_h + \phi_S$



Target spin orientations: **up-down** and **left-right** (increases angular coverage)

# Polarized $^3\text{He}$ Target

- Effectively a polarized neutron target
- Improved figure of merit
  - Rb+K hybrid mixture cell
  - Narrow bandwidth lasers
- Compact size: No cryogenic support needed



Jefferson Lab

# Correction for N<sub>2</sub> Dilution

$$A_{raw} = f \cdot P_{^3\text{He}} \cdot A_{^3\text{He}}$$

$$f = \frac{N_{^3\text{He}} \sigma_{^3\text{He}}}{N_{^3\text{He}} \sigma_{^3\text{He}} + N_{\text{N}_2} \sigma_{\text{N}_2}}$$

Cross section ratios determined through reference cell N<sub>2</sub> and <sup>3</sup>He data.

$x$	$f_{\text{N}_2}^{\pi^+}$	$f_{\text{N}_2}^{\pi^-}$
0.137	0.911 ± 0.011	0.925 ± 0.009
0.189	0.908 ± 0.011	0.905 ± 0.011
0.249	0.909 ± 0.010	0.898 ± 0.012
0.336	0.915 ± 0.009	0.916 ± 0.010

# From $^3\text{He}$ to Neutron

$$g_1^{^3\text{He}} = P_n g_1^n + 2P_p g_1^p$$

$$P_n = 0.86_{-0.02}^{+0.036} \quad \text{and} \quad P_p = -0.028_{-0.004}^{+0.009}$$

$$A_{^3\text{He}}^{C/S} = P_n \cdot (1 - f_p) \cdot A_n^{C/S} + \underline{P_p f_p \cdot A_p^{C/S}}$$

very small ( $< 0.003$ )

$$f_p = \frac{2\sigma_p}{\sigma_{^3\text{He}}}$$

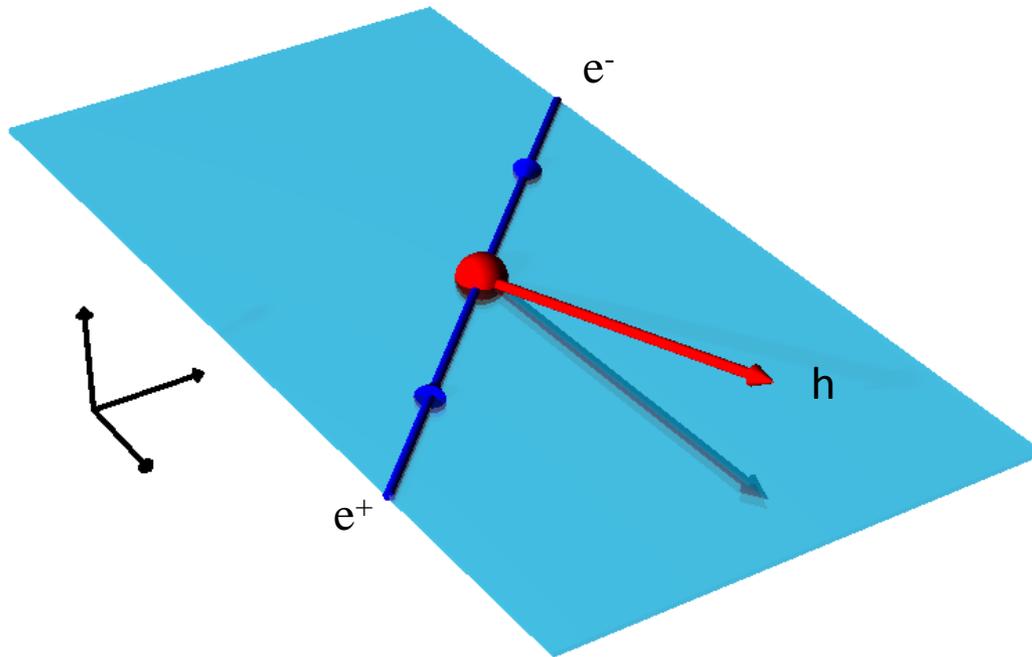
Cross section ratios determined through reference cell  $\text{H}_2$  and  $^3\text{He}$  data  $\rightarrow$  MEASURED

$x$	$1 - f_p^{\pi^+}$	$1 - f_p^{\pi^-}$
0.156	$0.212 \pm 0.032$ (0.027)	$0.348 \pm 0.032$ (0.022)
0.206	$0.144 \pm 0.031$ (0.029)	$0.205 \pm 0.037$ (0.027)
0.265	$0.171 \pm 0.029$ (0.028)	$0.287 \pm 0.036$ (0.024)
0.349	$0.107 \pm 0.026$ (0.030)	$0.220 \pm 0.032$ (0.026)

# Fragmentation functions in $e^+e^-$ annihilation

$$z = \frac{2E_h}{\sqrt{s}}, \quad \sqrt{s} = 10.52 \text{ GeV}$$

- Process:  $e^+ e^- \rightarrow hX$
- At leading order sum of unpolarized fragmentation functions from quark and anti-quark side



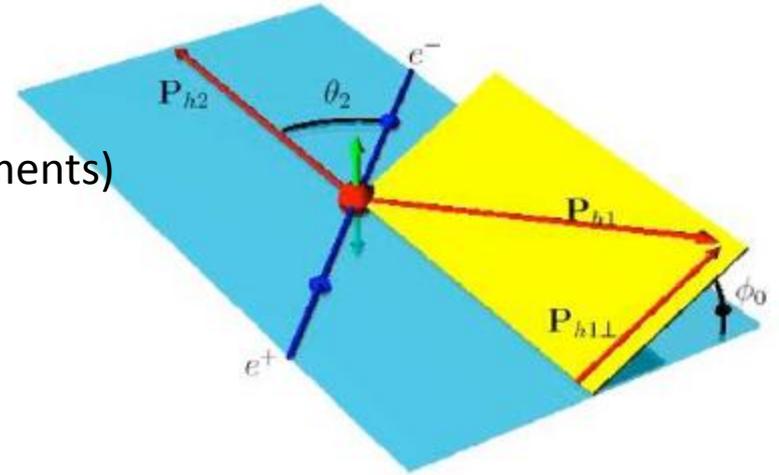
$$\text{LO } F^h(z, s) = \frac{\sum_q e_q^2 [D_q^h(z) + D_{\bar{q}}^h(z)]}{\sum_q e_q^2}$$

$$\text{NLO } F^h(z, s) = \sum_i \int_z^1 \frac{dz'}{z'} C_i(s; z' \alpha_s) D_q^h(z)$$

Other method, does not require the reconstruction of the thrust axis  
(Useful for the systematic control of the measurements)

$q\bar{q}$  is not accessible experimentally  $\rightarrow$   
approximated by the thrust axis in 1<sup>st</sup> method:

$$T = \max \frac{\sum_h |P_h \cdot \hat{n}|}{\sum_h |P_h|},$$

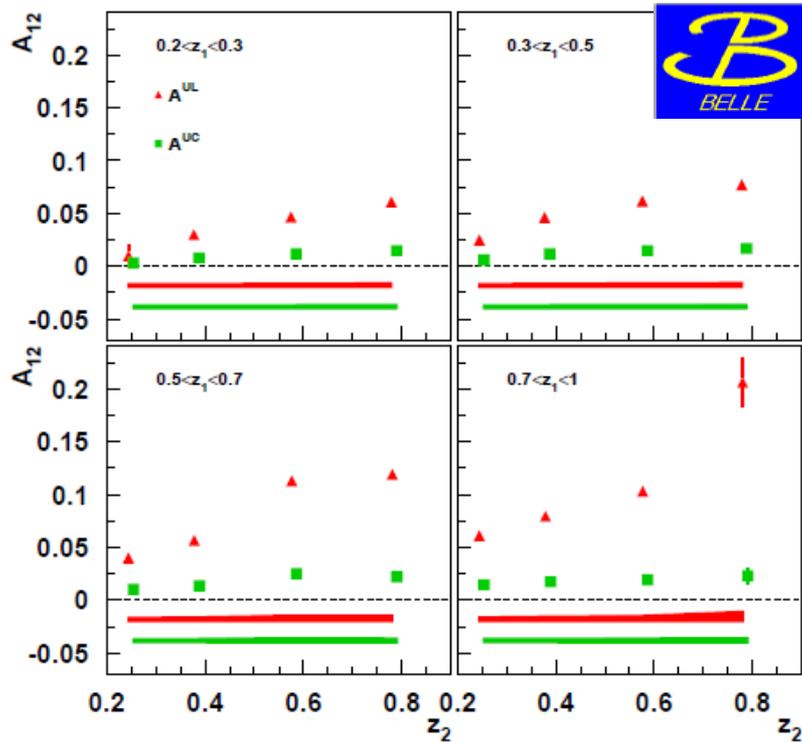


$$A_{12}^{UL} = \left\langle \frac{\sin^2 \theta}{1 + \cos^2 \theta} \right\rangle \frac{\pi \langle k_{tC}^2 \rangle}{4M^2} \left[ \frac{H_1^{fav} \bar{H}_2^{fav} + H_1^{dis} \bar{H}_2^{dis}}{D_1^{fav} \bar{D}_2^{fav} + D_1^{dis} \bar{D}_2^{dis}} - \frac{H_1^{fav} \bar{H}_2^{dis} + H_1^{dis} \bar{H}_2^{fav}}{D_1^{fav} \bar{D}_2^{dis} + D_1^{dis} \bar{D}_2^{fav}} \right]$$

$$A_{12}^{UC} = \left\langle \frac{\sin^2 \theta}{1 + \cos^2 \theta} \right\rangle \frac{\pi \langle k_{tC}^2 \rangle}{4M^2} \left[ \frac{H_1^{fav} \bar{H}_2^{fav} + H_1^{dis} \bar{H}_2^{dis}}{D_1^{fav} \bar{D}_2^{fav} + D_1^{dis} \bar{D}_2^{dis}} - \frac{(H_1^{fav} + H_1^{dis})(\bar{H}_2^{fav} + \bar{H}_2^{dis})}{(D_1^{fav} + D_1^{dis})(\bar{D}_2^{fav} + \bar{D}_2^{dis})} \right]$$

# Collins effect in $e^+e^-$ annihilation

PR D78:032011,2008

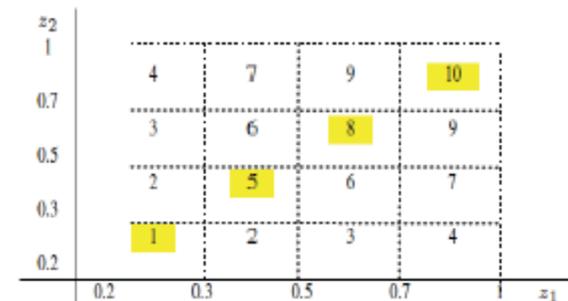


547 fb-1 data set, small statistical uncertainties;  
Measured asymmetries rising with  $z$ ,

Extraction of double ratios  
unlike sign **over like sign**  $A^{UL}$  and  
unlike **over charged/neutral pairs**  $A^{UC}$   
→ gives different combinations of  
favored and unfavored FF

The data do not allow to extract  
the fav and unfav Collins FFs  
→ Only from global fit

$$A_{12}^{UL} = \left\langle \frac{\sin^2 \theta}{1 + \cos^2 \theta} \right\rangle \frac{\pi \langle k_{tC}^2 \rangle}{4M^2} \left[ \frac{H_1^{fav} \overline{H}_2^{fav} + H_1^{dis} \overline{H}_2^{dis}}{D_1^{fav} \overline{D}_2^{fav} + D_1^{dis} \overline{D}_2^{dis}} - \frac{H_1^{fav} \overline{H}_2^{dis} + H_1^{dis} \overline{H}_2^{fav}}{D_1^{fav} \overline{D}_2^{dis} + D_1^{dis} \overline{D}_2^{fav}} \right]$$



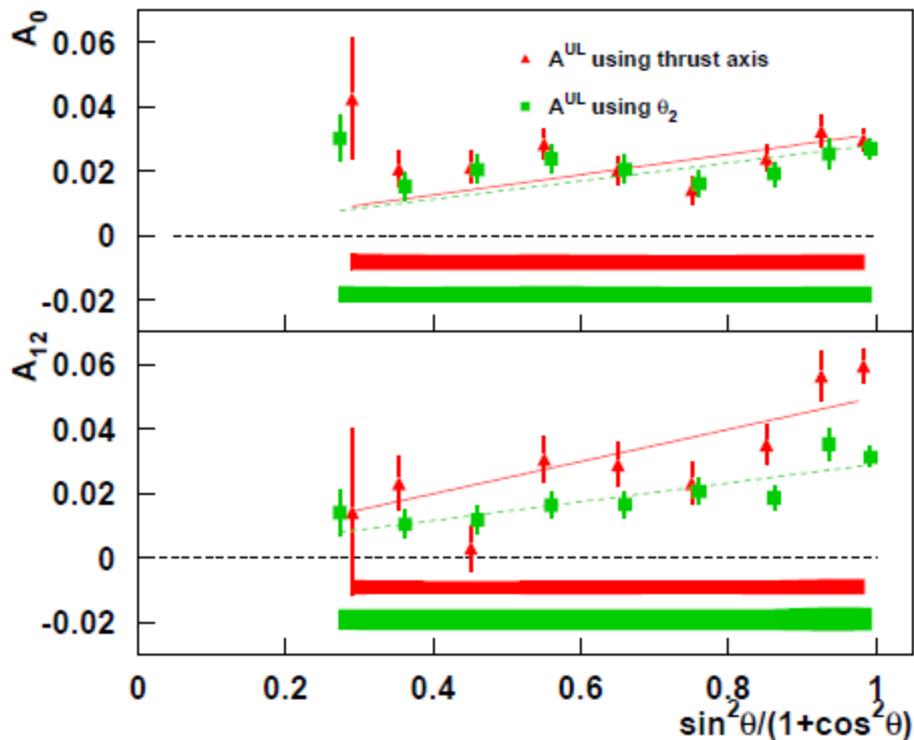
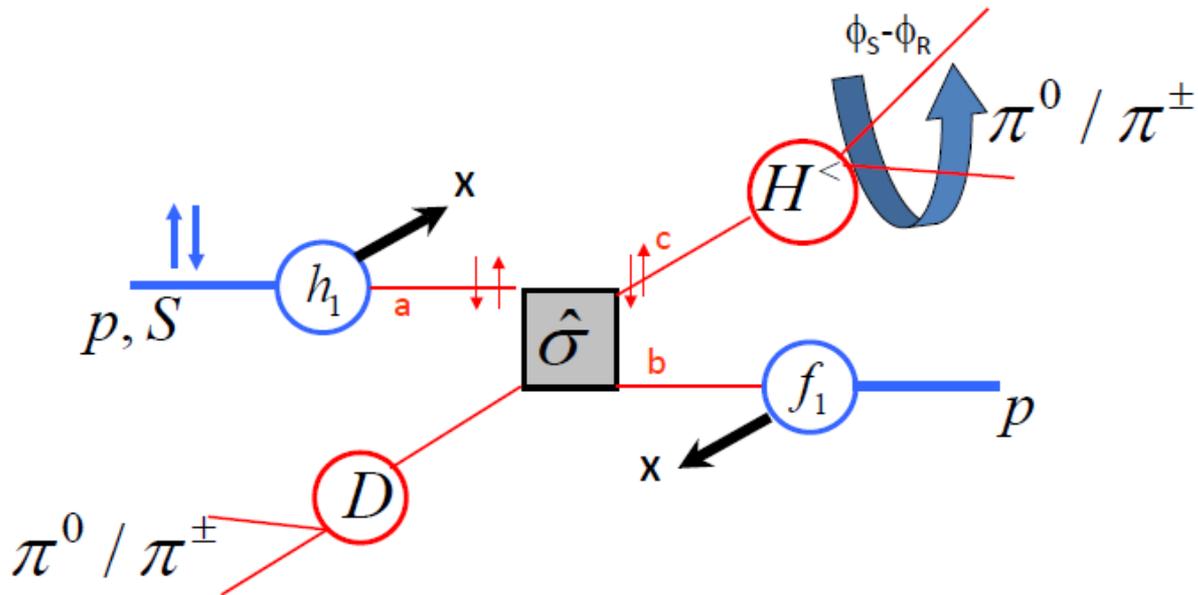


FIG. 19: Light quark (uds)  $A_0^{UL}$  (top) and  $A_{12}^{UL}$  (bottom) asymmetry parameters as a function of  $\sin^2 \theta / (1 + \cos^2 \theta)$ , for  $\theta_2$  (squares) and for  $\hat{n}_z$  (triangles). Linear fits are also displayed as dashed and continuous lines, respectively. The systematic error for  $\theta_2$  case is represented by the lower, that for  $\hat{n}_z$  by the upper error band.

Transverse quark spins leads to a  $\sin^2/1+\cos^2$  dependence of the asymmetries

More linear behavior in the  $A_{12}$  asym, explained by the fact that the thrust axis describes the original quark direction better than the second hadron polar angle (additional transv mom relative to the quark axis)

# Interference Fragmentation Function in p-p



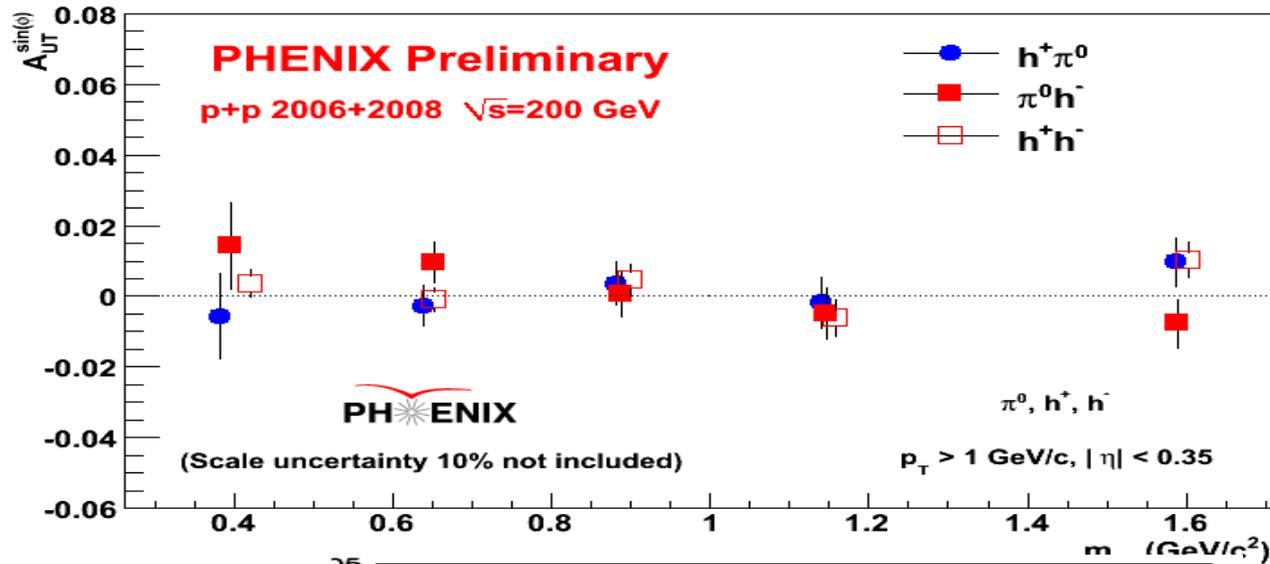
$$\frac{\sigma^\uparrow - \sigma^\downarrow}{\sigma^\uparrow + \sigma^\downarrow}(\phi_S - \phi_R) = A_{UT} \sin(\phi_S - \phi_R) \quad A_{UT} \propto h_1 \otimes H_1^<$$

- $\phi_S$ : Angle between polarisation vector and event plane
- $\phi_R$ : Angle between two hadron plane and event plane

$$A_{UT}^{\sin\phi}$$

# vs Invariant Mass of the Pair

First measurement of IFF in pp



These DIFF are being measured at Belle

Results and Projections  
 From run 12+13

