

# **Study of the hadronisation process from semi-inclusive single hadron and hadron pair production at COMPASS**

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# Outline

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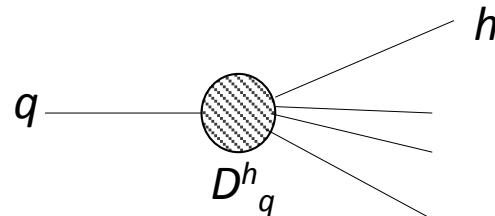


- Single-hadron fragmentation functions
- Di-hadron fragmentation functions
- Semi-inclusive DIS & Hadron multiplicities
- Results
- Summary and outlook

# Single-hadron Fragmentation Functions (FFs)



- Describe the collinear transition of a quark  $q$  into a final-state hadron  $h$  carrying momentum fraction  $z$  ( $q \rightarrow h X$ )
- $D_q^h$  gives the mean number of hadrons produced in the quark hadronization



- Relevant in every reaction where a hadron is produced in the final state
- Key role in flavor separation of polarised parton distributions
- Universal and non-perturbative quantities
- Depend on energy fraction of the photon transferred to the hadron:

$$z = \frac{E_h}{E_\gamma}$$

- Depend on  $Q^2$ , evolution described by DGLAP equations
- Energy conservation sum rule (used their determination):

$$\sum_h \int_0^1 z D_i^h(z, Q^2) dz = 1$$

# The $\Delta S$ puzzle

- Strange quark contribution to nucleon spin:

$$\Delta S = \int dx [\Delta s(x) + \Delta \bar{s}(x)]$$



## Inclusive measurement

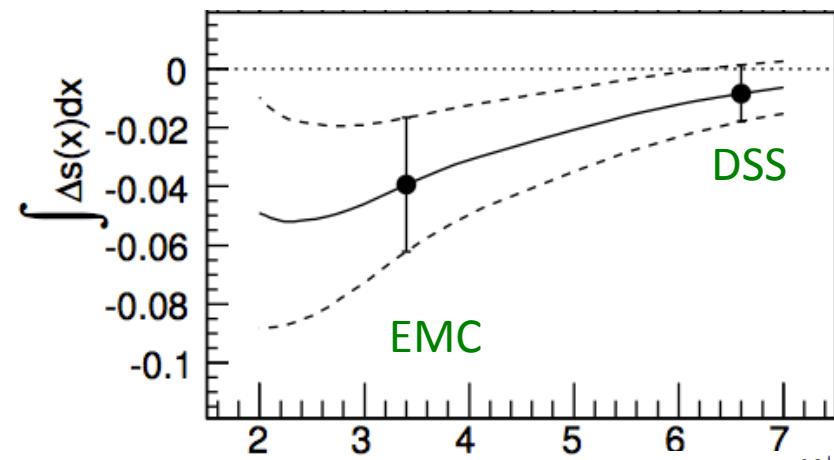
- $\Gamma_1 = g_1(x)$
- SU(3) flavor symmetry & axial charges of baryons

$$\Delta S = -0.08 \pm 0.01_{\text{stat.}} \pm 0.02_{\text{syst.}}$$

## Semi-Inclusive measurement

- Depending on fragmentation functions
- Strongly dependent on the ratio  $R_{SF}$

$$\Delta S = -0.02 \pm 0.02_{\text{stat.}} \pm 0.02_{\text{syst.}}$$



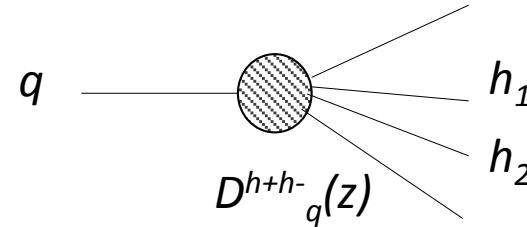
Single-hadron FFs remain a key element in  
the  $\Delta S$  puzzle

$$R_{SF} = \frac{D_{\bar{s}}^{K^+}}{D_u^{K^+}}$$

# Dihadron Fragmentation Functions (DiFFs)



- Describe the probability that a quark of given flavor ( $q_f$ ) hadronizes into a final-state hadron pair ( $q_f \rightarrow h_1^+ h_2^- X$ ):



- first introduced in the late 1970's to study the hadron structure of jets  
*Konishi, Ukawa and Veneziano, Phys. Lett. B 78, 243 (1978)*
- needed in NLO calculations in  $\alpha_s$  for two hadron production in  $e^+e^-$  annihilation  
*Phys. Lett. B 578, 139 (2004);*
- useful to investigate the in-medium effects in heavy ion collisions  
*Phys. Rett. L 99, 152301 (2007)*
- key element to access transversity distribution of the nucleon ( $h_1$ ) in SIDIS

**DiFFs are needed in several high energy processes with final state hadrons**

# Status of unpolarized FFs & DiFFs

- Experimental information available in several hard scattering reactions
- Most experimental data measured at  $e^+e^-$  colliders
  - Clean process: depends only on FFs (no dependence on PDFs)
  - Measured at fixed energy scales (far from fixed target scales)
  - Mostly sensitive to singlet combinations
  - Cannot separate Quark from Anti-Quark fragmentation
- FFs accessible in hadron-hadron collisions:
  - most sensitive to gluon FFs
  - Useful for medium modifications
- Accessible in semi-inclusive DIS using hadron yields produced in DIS events
- Several global NLO QCD analyses exist (KRE, KKP, DSS, ...)
  - Use different data sets and assumptions
  - Significantly disagree
- No global QCD analyses exist yet for unpolarized DiFFs.
- Available experimental information consists of only invariant mass spectra of hadron pairs, no information on simultaneous ( $z$ ,  $Q^2$ ,  $M_{inv}$ ) dependence
- An extraction of DiFFs done using Monte Carlo simulation of  $e^+e^-$ -annihilations  
*(by A. Courtoy, A. Bacchetta, M. Radici and A. Bianconi)*

# Status of unpolarized FFs & DiFFs

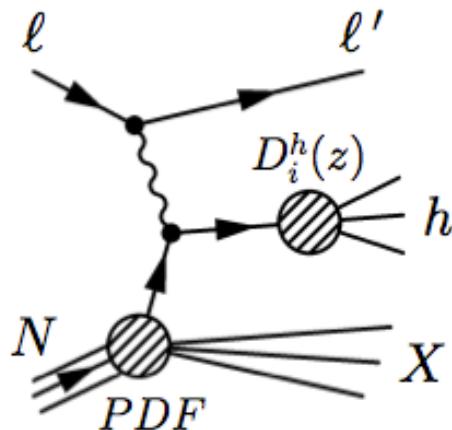
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**Poorly known  
fragmentation functions,  
especially kaon's FFs**

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 $(\text{by A. Courtoy, A. Bacchetta, M. Radici and A. Bianconi})$

**Unknown DiFFs**

# Semi-Inclusive DIS (SIDIS)



- $I\ N \rightarrow I'\ h\ X$  : at least one hadron is detected with the scattered lepton in the final state
- Allows flavor/charge separation of FFs
- Wide  $Q^2$  coverage (low to high  $Q^2$ )

Relevant observable for FF access: **Hadron Multiplicities**

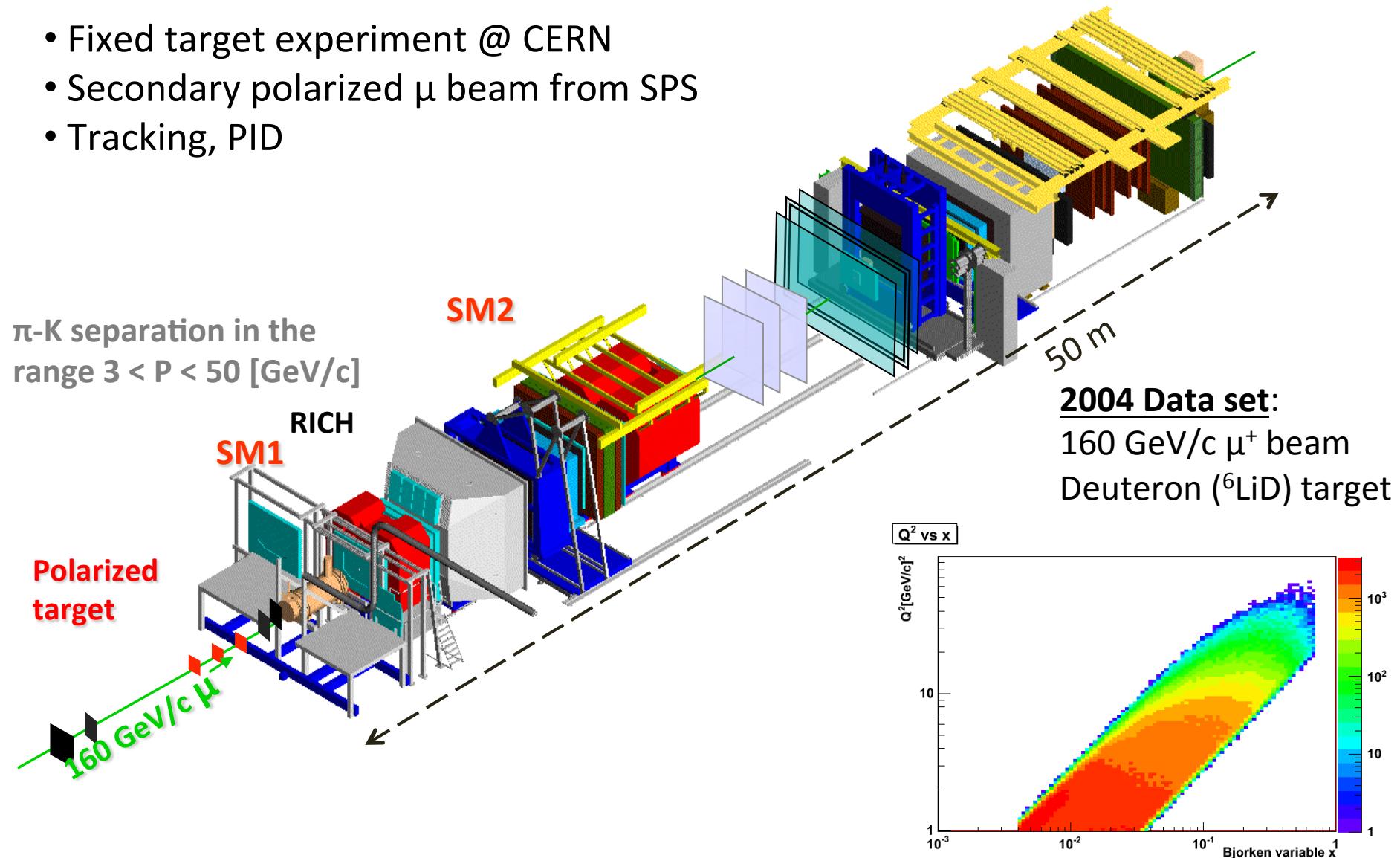
$$M^h(x, z) = \frac{d\sigma_{SIDIS}/dx dz}{\sigma_{DIS}} = \frac{\sum_q e_q^2(q(x) D_q^h(z) + \bar{q}(x) D_{\bar{q}}^h(z))}{\sum_q e_q^2(q(x) + \bar{q}(x))}$$

- **Disadvantage:** Dependence on unpolarised PDFs:
  - Up, down unpolarized PDFs well known
  - Strange PDF  $s(x)$  poorly known => More information from hadron multiplicities
- Useful to study the hadronisation process in nuclear medium (using different targets)

# The COMPASS Experiment

Common Muon and Proton Apparatus for Structure and Spectroscopy

- Fixed target experiment @ CERN
- Secondary polarized  $\mu$  beam from SPS
- Tracking, PID





# Multiplicity definition and method of extraction

Definition: averaged number of hadrons produced per DIS event.

Method of extraction: In a given kinematic bin  $i$

1. Experimental hadron multiplicity:

$$M_{\text{raw}}(i) = N^h(i) / N^{\text{DIS}}(i)$$

2. Acceptance estimation using Monte Carlo simulation, acceptance defined as

$$a_i = M_{\text{rec}}(i_R) / M_{\text{gen}}(i_G)$$

3. Final multiplicities:

$$M_{\text{cor}}(i) = M_{\text{raw}}(i) / a_i$$

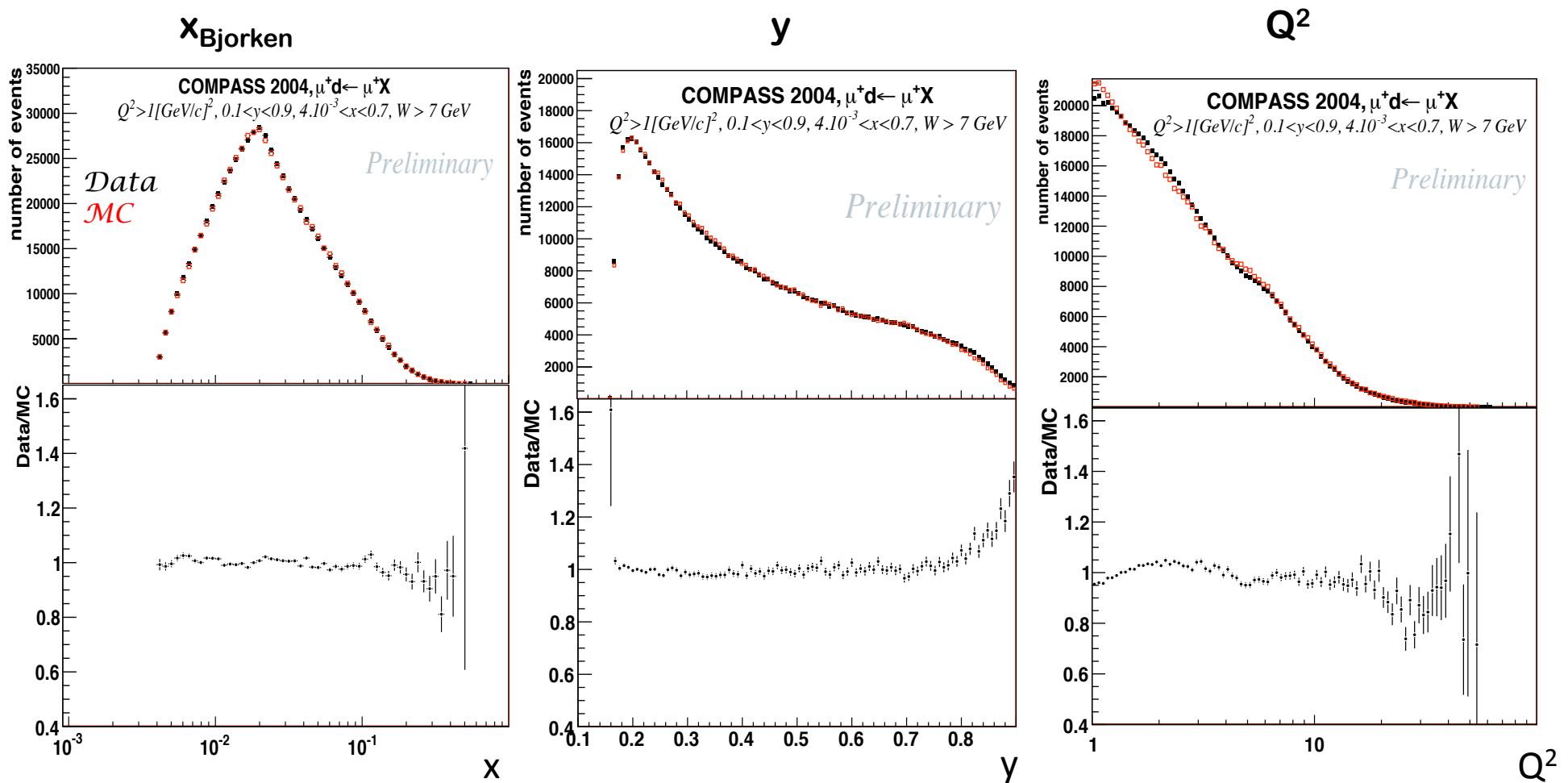
Kinematic domain

$Q^2 > 1 \text{ (GeV/c)}^2$ ,  $0.1 < y < 0.9$ ,  $W > 7 \text{ (GeV)}$ ,  $0.003 < x < 0.7$

$0.2 < z < 0.85$

$N(\text{DIS})$	$N(\pi^+)$	$N(\pi^-)$	$N(K^+)$	$N(K^-)$
$5.3 \cdot 10^6$	$10^6$	$9.5 \cdot 10^5$	$\sim 2 \cdot 10^5$	$\sim 1.3 \cdot 10^5$

# Monte Carlo description of COMPASS data for DIS variables

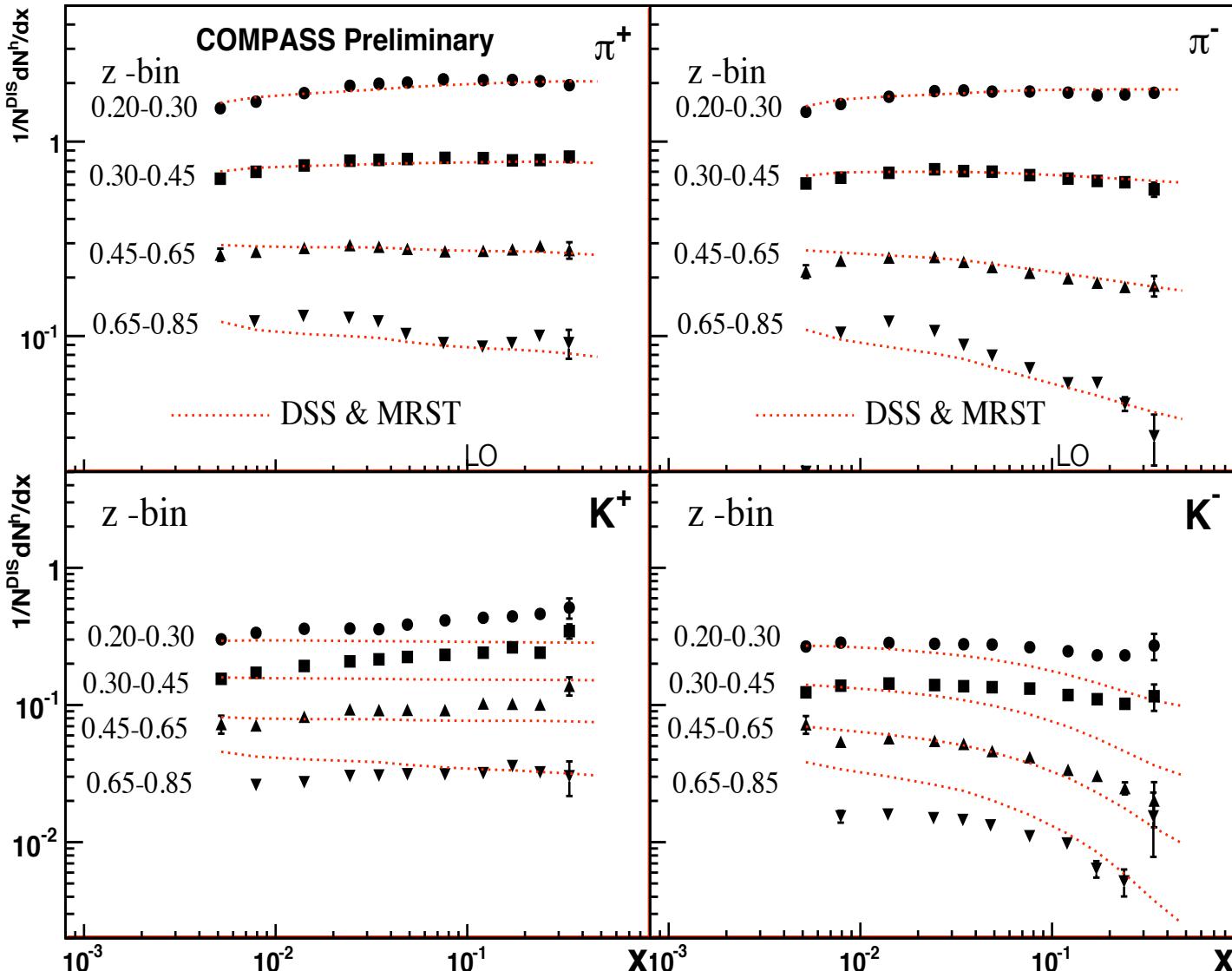


Good description of data by Monte Carlo for inclusive variables

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## Results on single hadron multiplicities

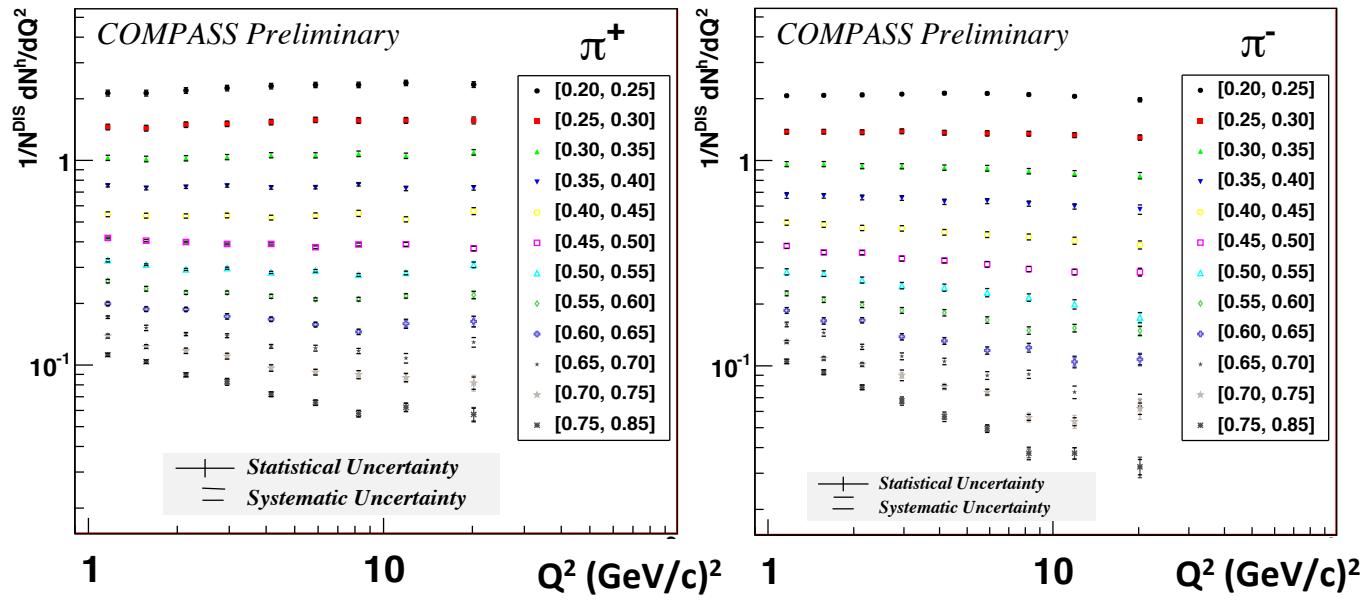
# Results: 2D (x,z) multiplicities



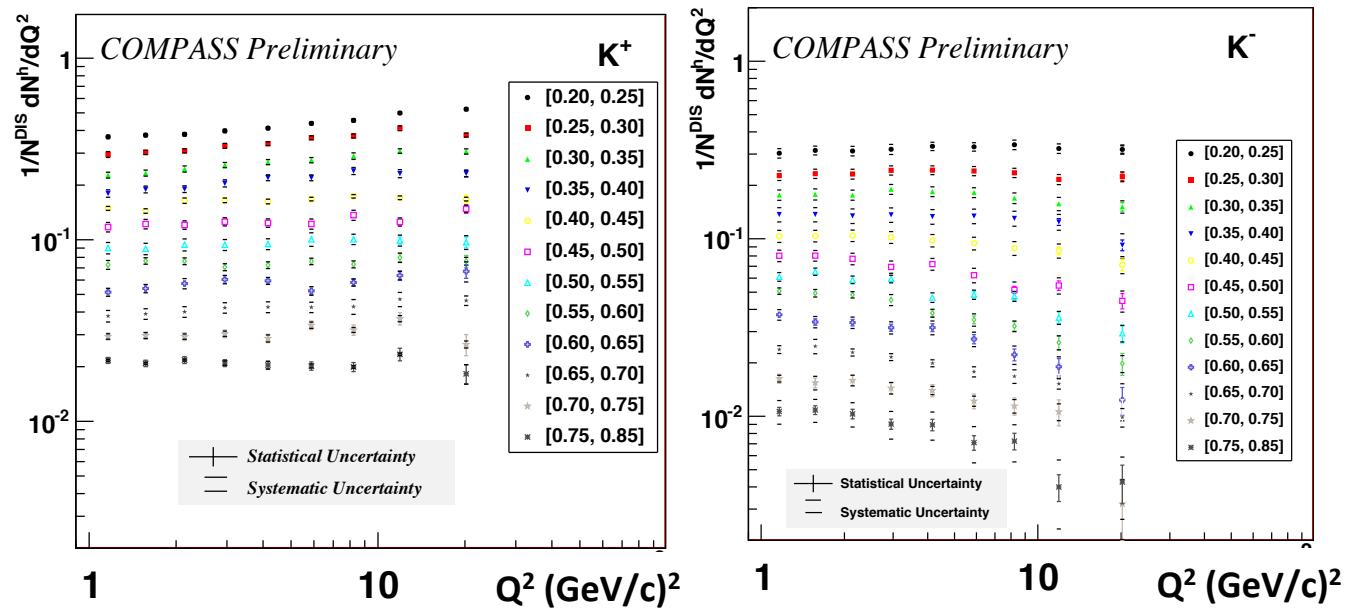
syst. Uncertainties due to: MC:  $\sim 1\%$  (2%) for  $\pi$  ( $K$ ) for  $x < 0.15$   
 Particle identification < 8% (5%) for  $\pi$  ( $K$ )

- $\pi^\pm$ : poor agreement up to  $z < 0.65$
- $K^\pm$ : Significant disagreement in all z bins
  - Unknown  $s(x)$  ?
  - Missing higher orders ?
  - COMPASS data favors different FFs than DSS  
*Cf. presentation by A. Sidorov*
- $K^0$  under investigation

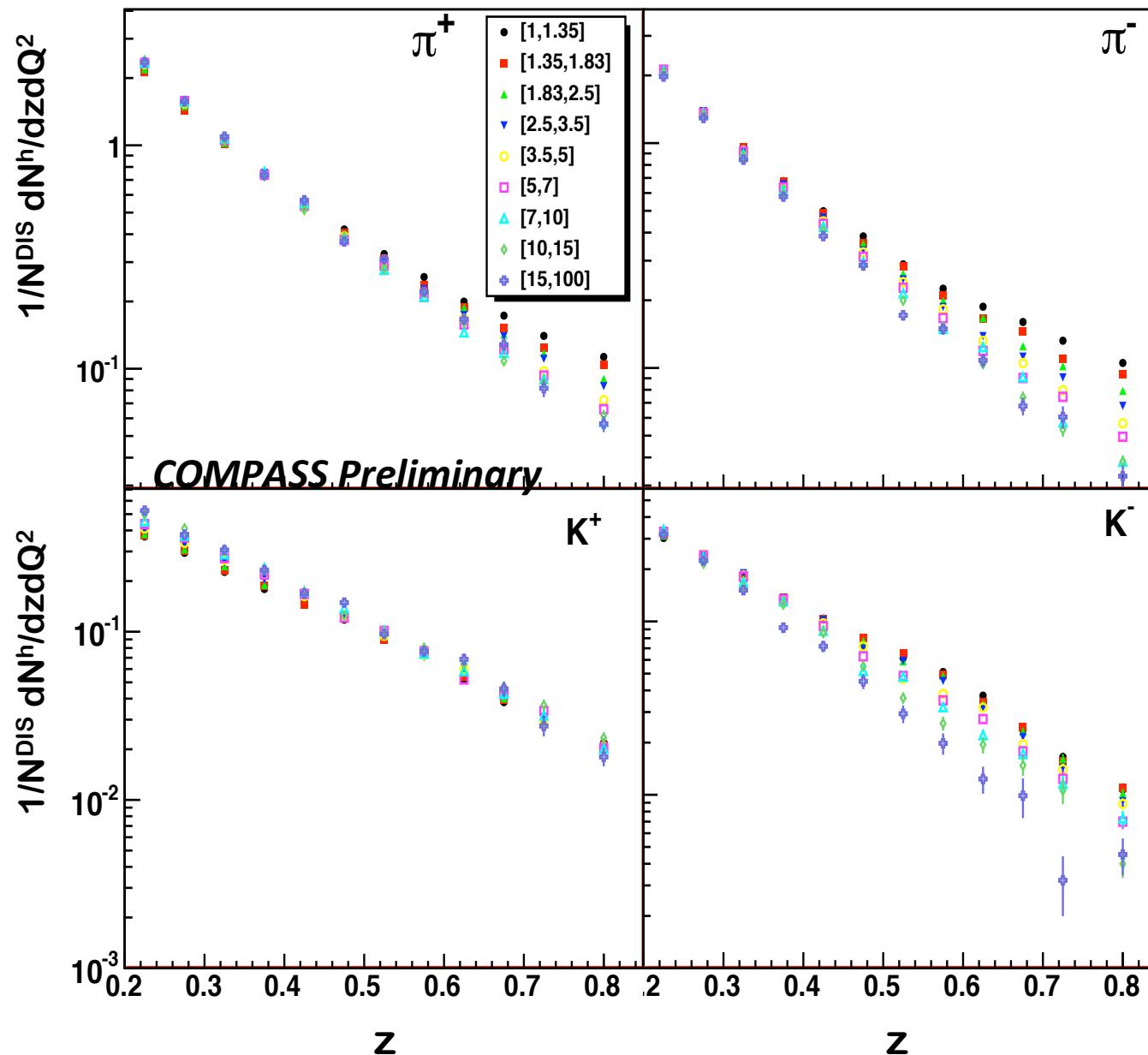
# Results: 2D ( $Q^2, z$ ) Multiplicities for $\pi^\pm$



- Strongest  $Q^2$  dependence for  $h^-$
- In fair agreement with LO predictions



# Results: 2D ( $Q^2, z$ ) Multiplicities for $\pi$ and $K$

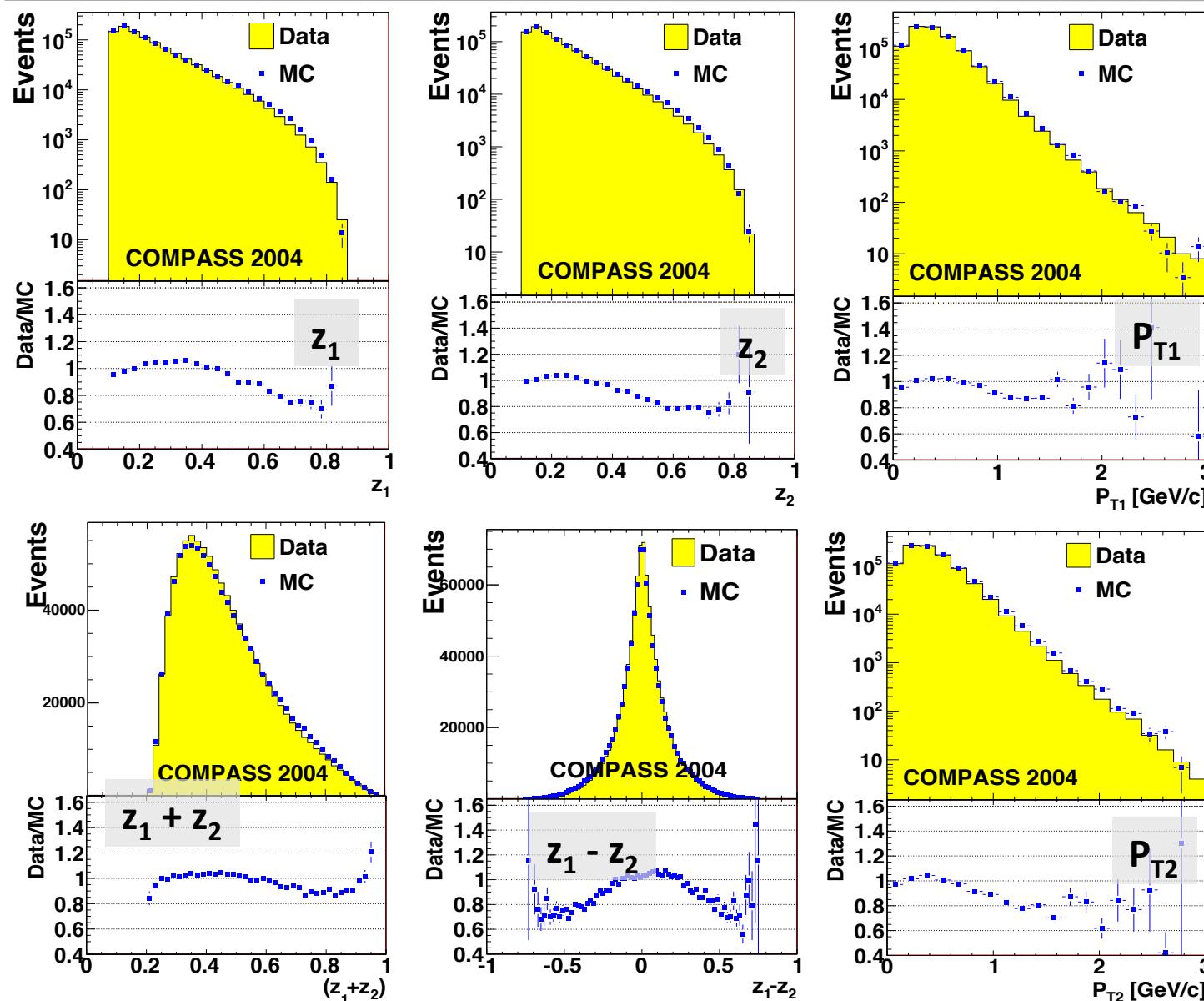


- Distributions needed for global QCD analysis of single FFs
- Strongest  $Q^2$  dependence for negative hadrons at high  $z$  and  $Q^2$

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## Results on hadron pair multiplicities

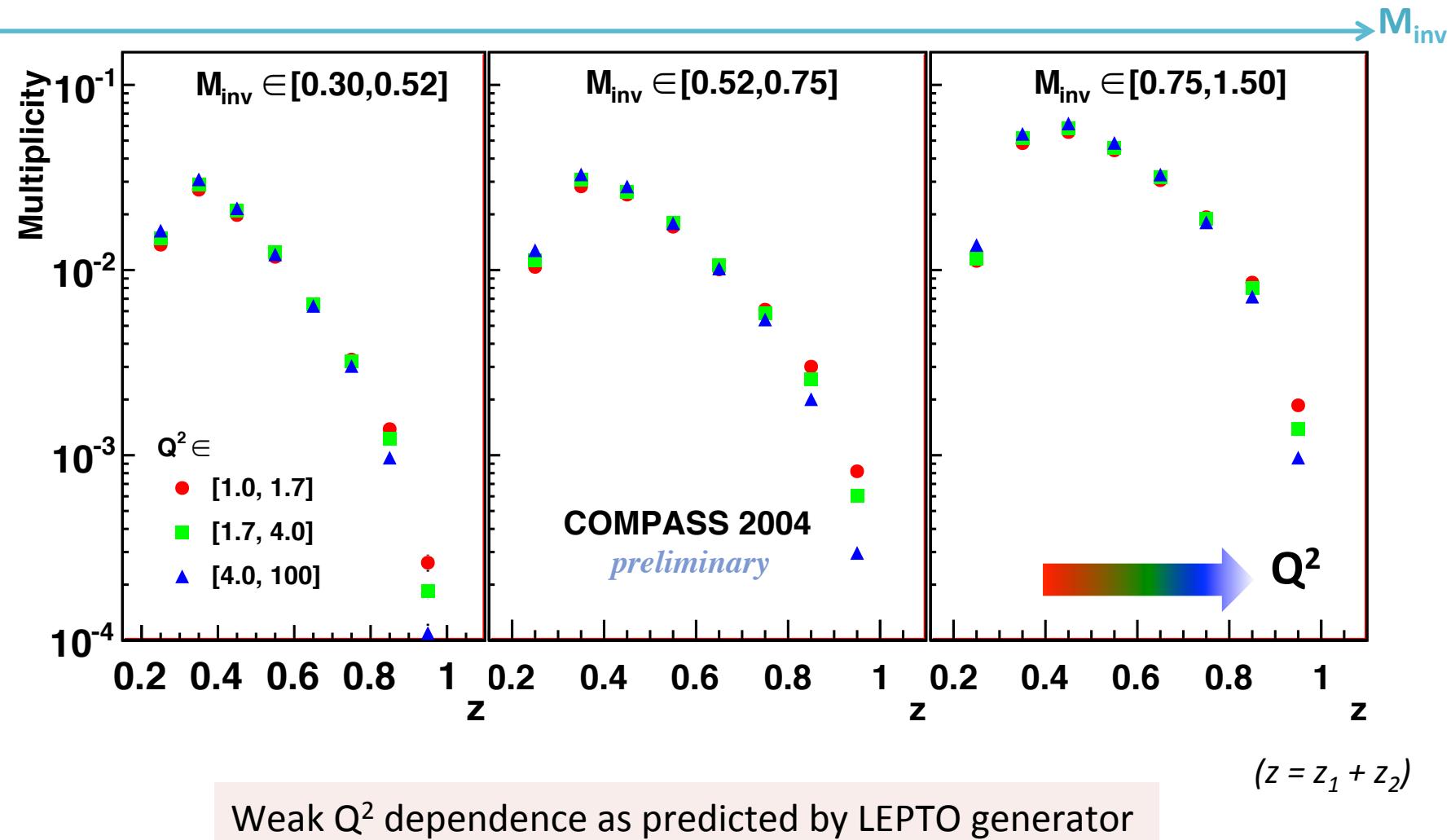
# Monte Carlo description of COMPASS data (I)



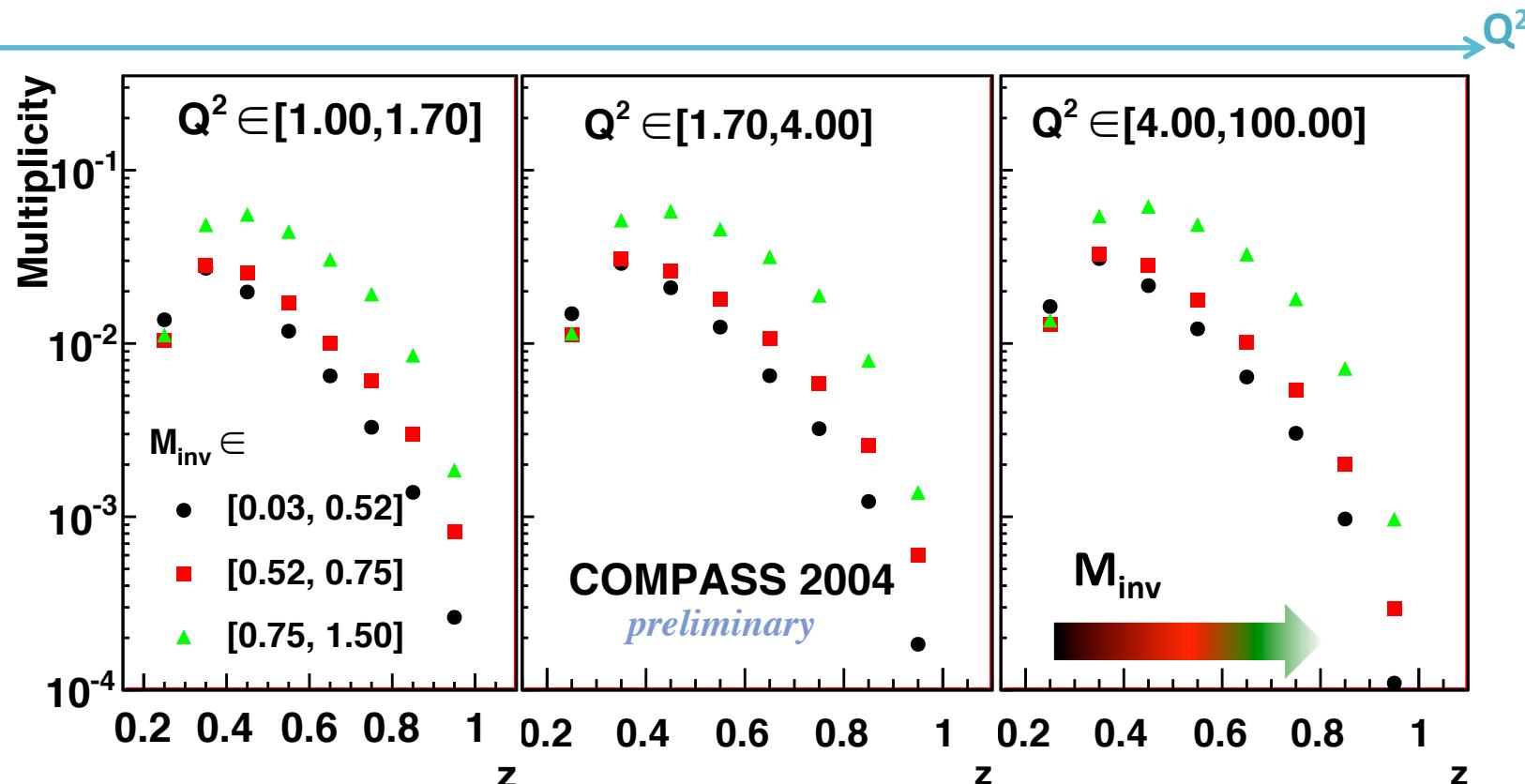
Reasonable description of COMPASS data by MC simulation

## New: 2004 Hadron pair multiplicities versus $(z, Q^2, M_{inv})$

- Goal: measurement of  $D_q^{h+, h-}(z, M_{inv}, Q^2)$
- Key ingredient to access transversity function



# New: 2004 Hadron pair multiplicities versus $(z, Q^2, M_{\text{inv}})$



- Non negligible dependence upon  $M_{\text{inv}}$  and  $z (= z_1 + z_2)$
- $(z, M_{\text{inv}})$  dependence in agreement with LEPTO prediction

First determination of hadron pair multiplicities from SIDIS

# Summary



- $\pi/K$  charged multiplicities versus  $(x,z)$  and  $(Q^2,z)$  from  $\mu$ -d DIS measured at COMPASS
- $\pi$ : poor agreement with LO predictions,  $K$ : significant disagreement
- Resulting multiplicities can significantly contribute to global QCD analyses for FFs
- Useful for the determination of strange quark distribution  $s(x)$
- First measurement of unidentified hadron pair multiplicities aiming to determine Dihadron fragmentation functions

## Outlook

- Single hadron multiplicities from  $\mu$ -p DIS
- Measurement of Identified hadron pair multiplicities
- Determination of  $s(x)$