

# High Energy Physics at Low $Q^2$

-

## Using **COMPASS** to search for **Exotics** Structures and Dynamics

Stephan Paul

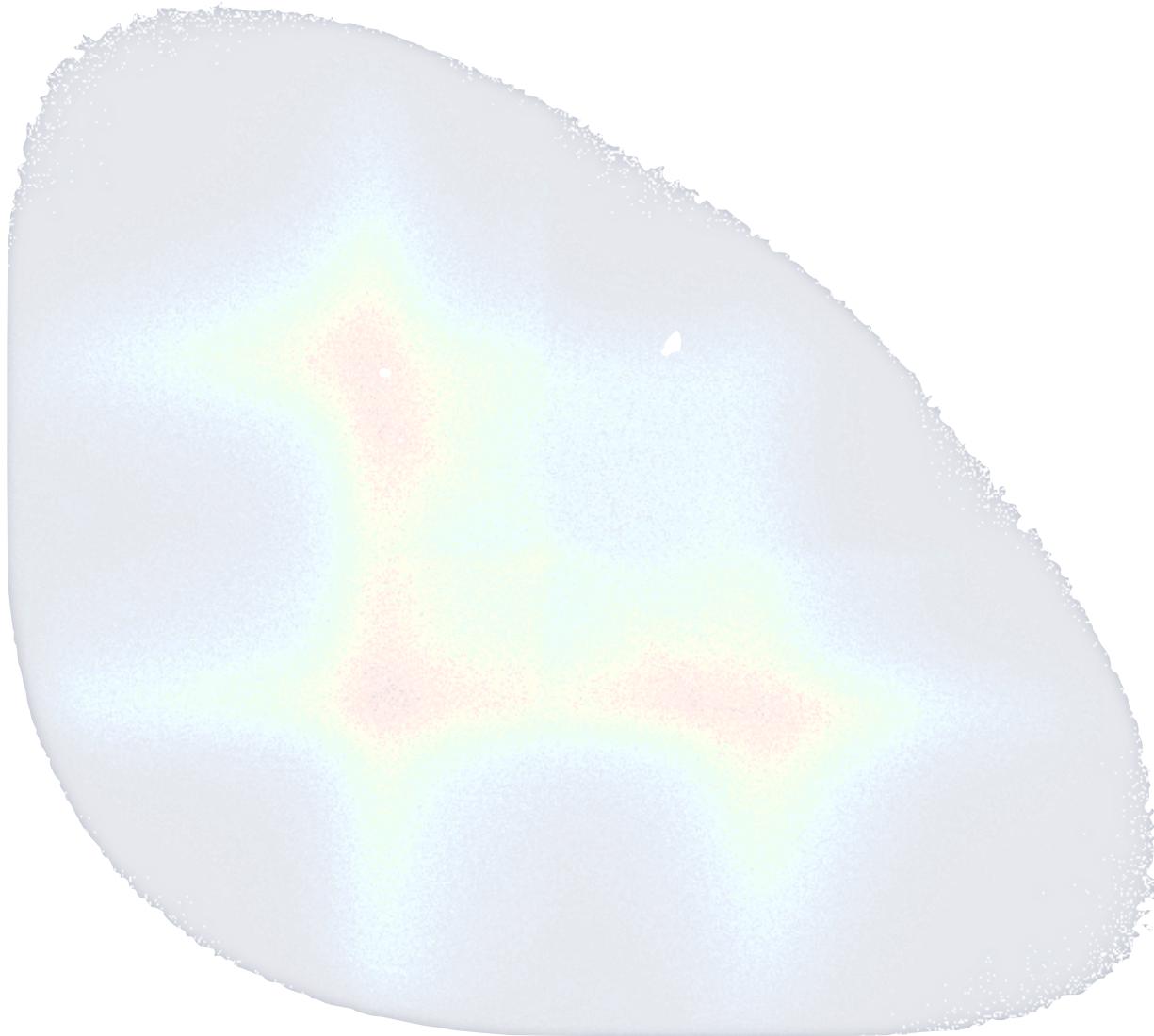
Technische Universität München



bmbf - Förderschwerpunkt  
**COMPASS**  
Großgeräte der physikalischen  
Grundlagenforschung

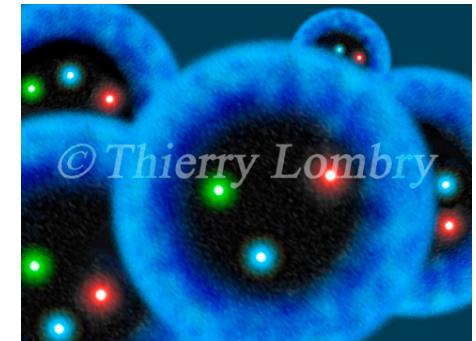


# Overview



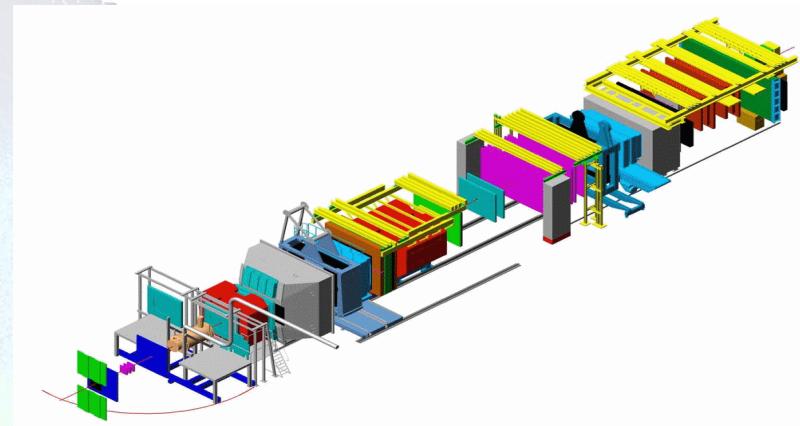
# Overview

- **Introduction**
  - Structure of matter and hadrons
  - The spectrum of mesons
  - **Exotic** structures

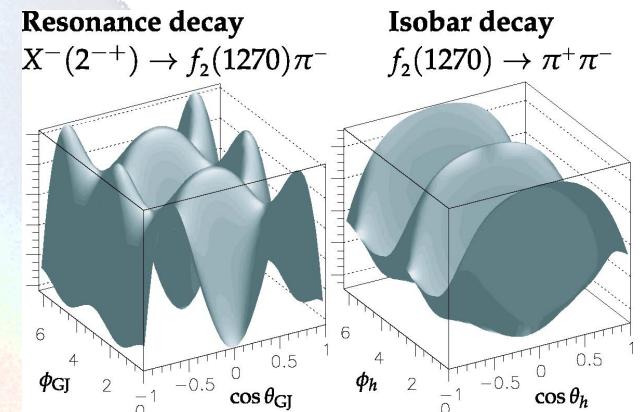


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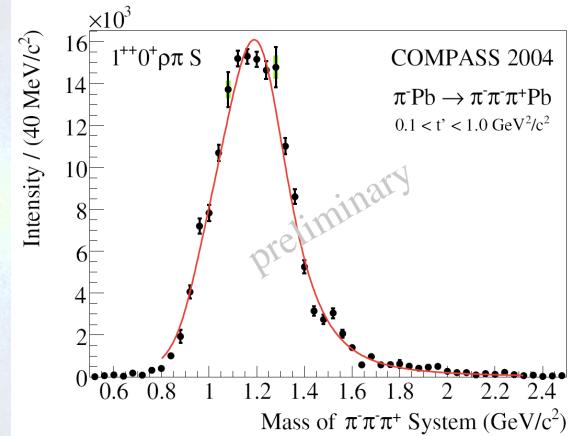
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  - Experimental methods
  - The **COMPASS** Experiment



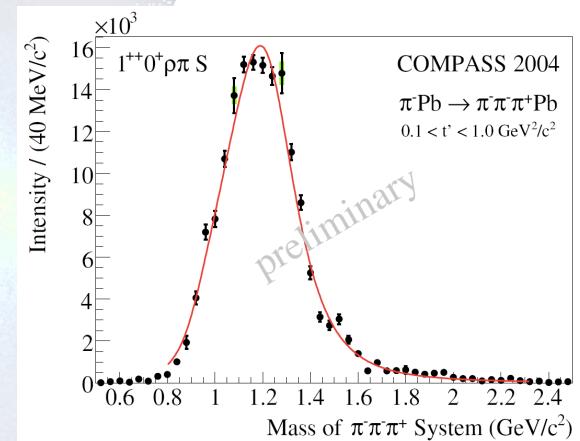
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- **Results (as by today)**
  - Search for **exotics**
  - Known mesons

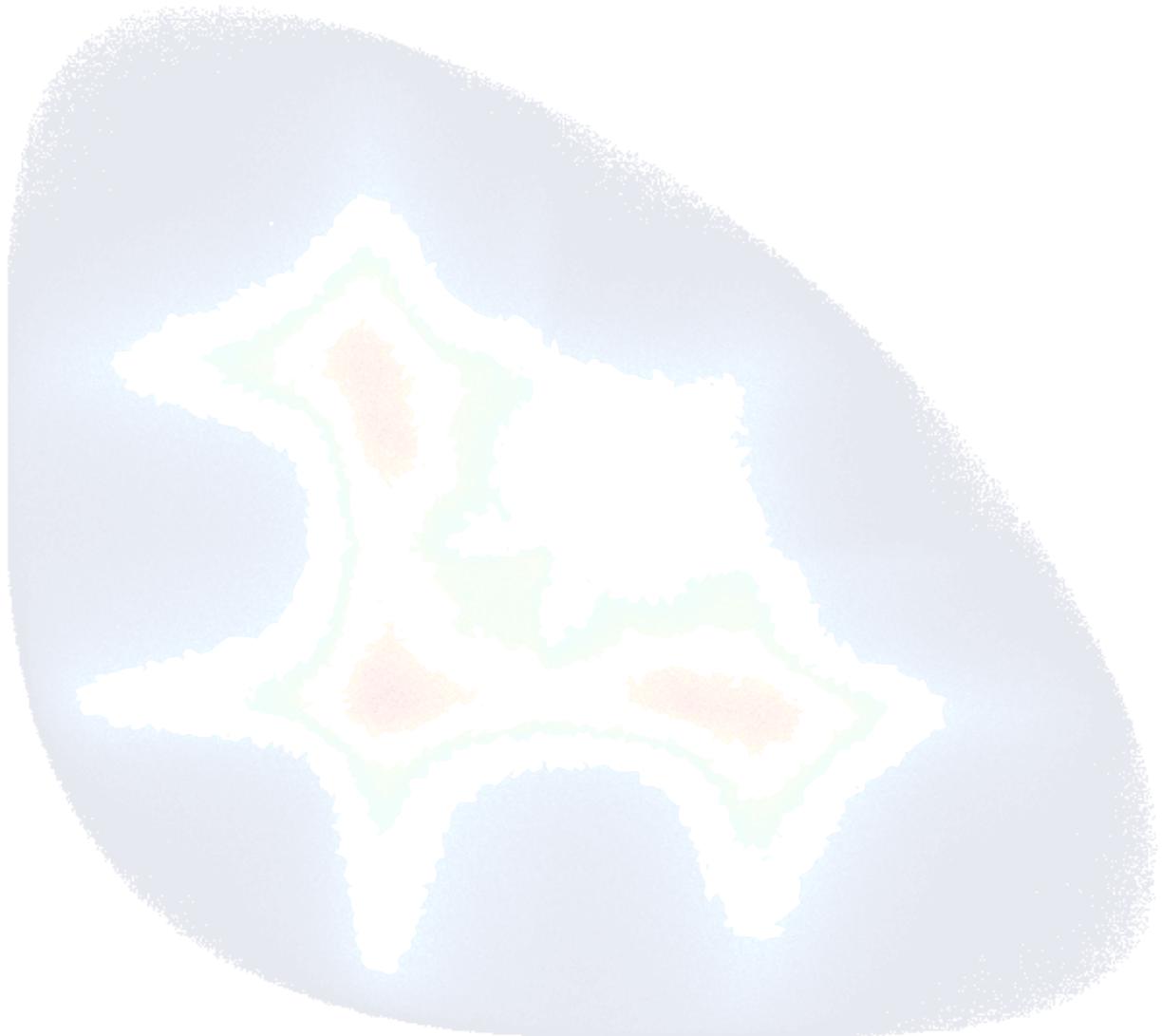


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- **Photo-induced reactions**
- **Ongoing work**
  - Mesons und Baryons

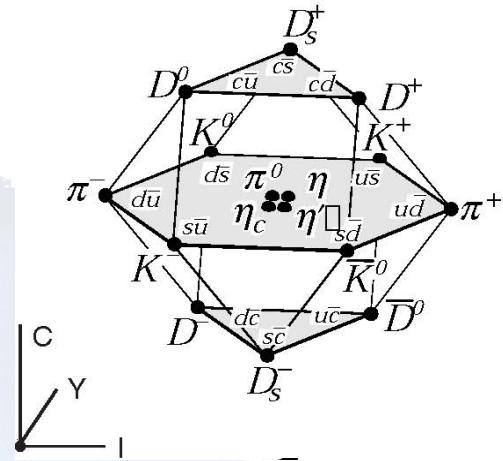
# Constituent Quark Model Mesons



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Hadrons: colour neutral system of quarks

- Baryon (qqq)
- Meson ( $q\bar{q}$ )



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Spin-Parity selection rules for bound  $q\bar{q}'$  system

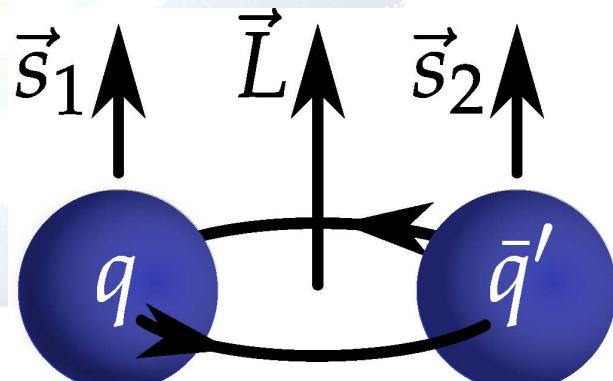
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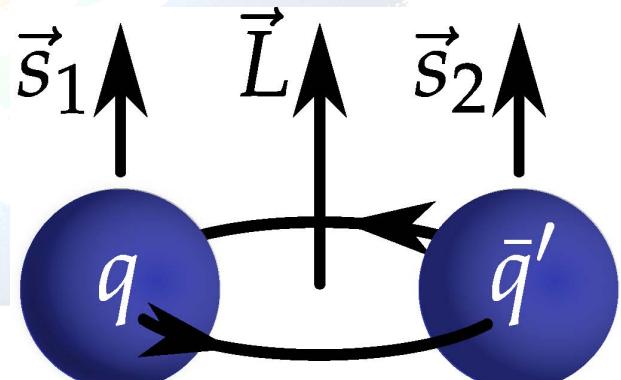
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**Meson spin:**  $\vec{J} = \vec{L} + \vec{S}$



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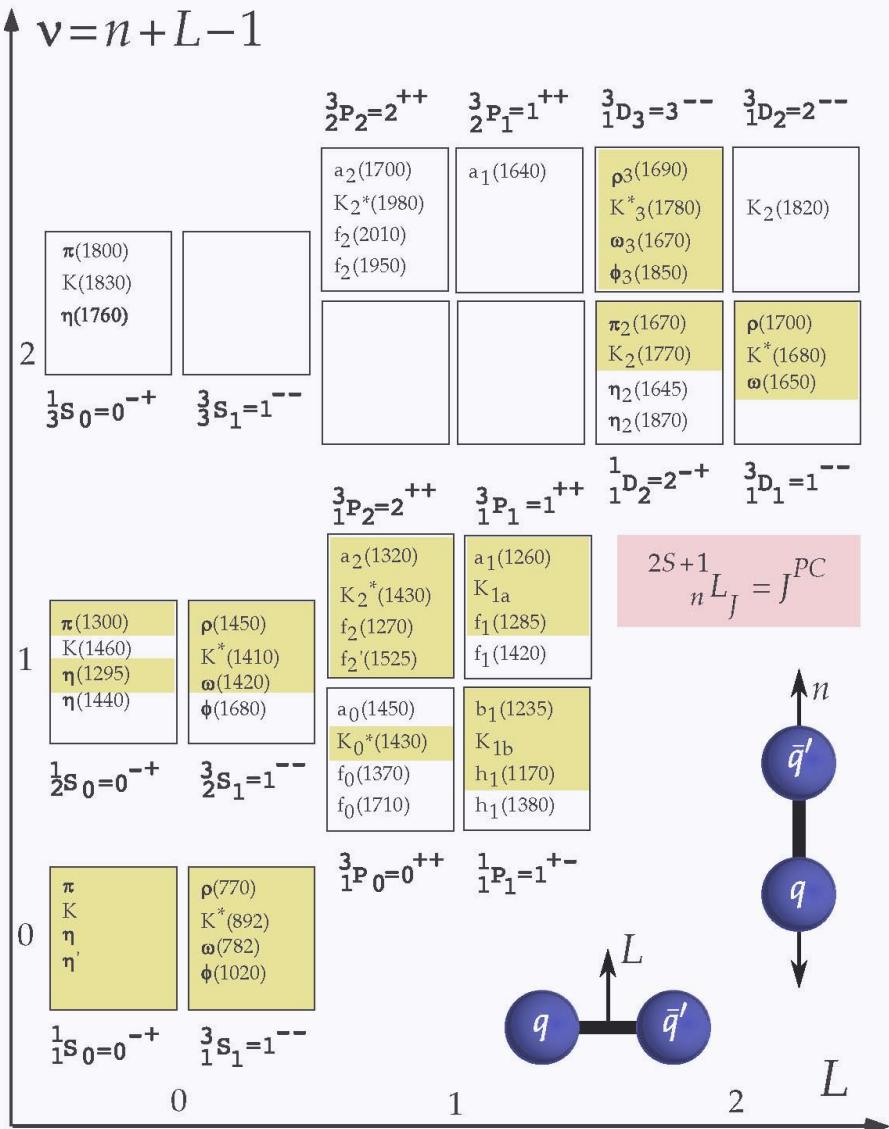
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**Meson spin:**  $\vec{J} = \vec{L} + \vec{S}$
- **Parity:**  $P = (-1)^{L+1}$
- **Charge conjugation:**  $C = (-1)^{L+S}$
- **G-parity:**  $G = C \cdot e^{i\pi I_z} = (-1)^{I+L+S}$

# Constituent Quark Model II

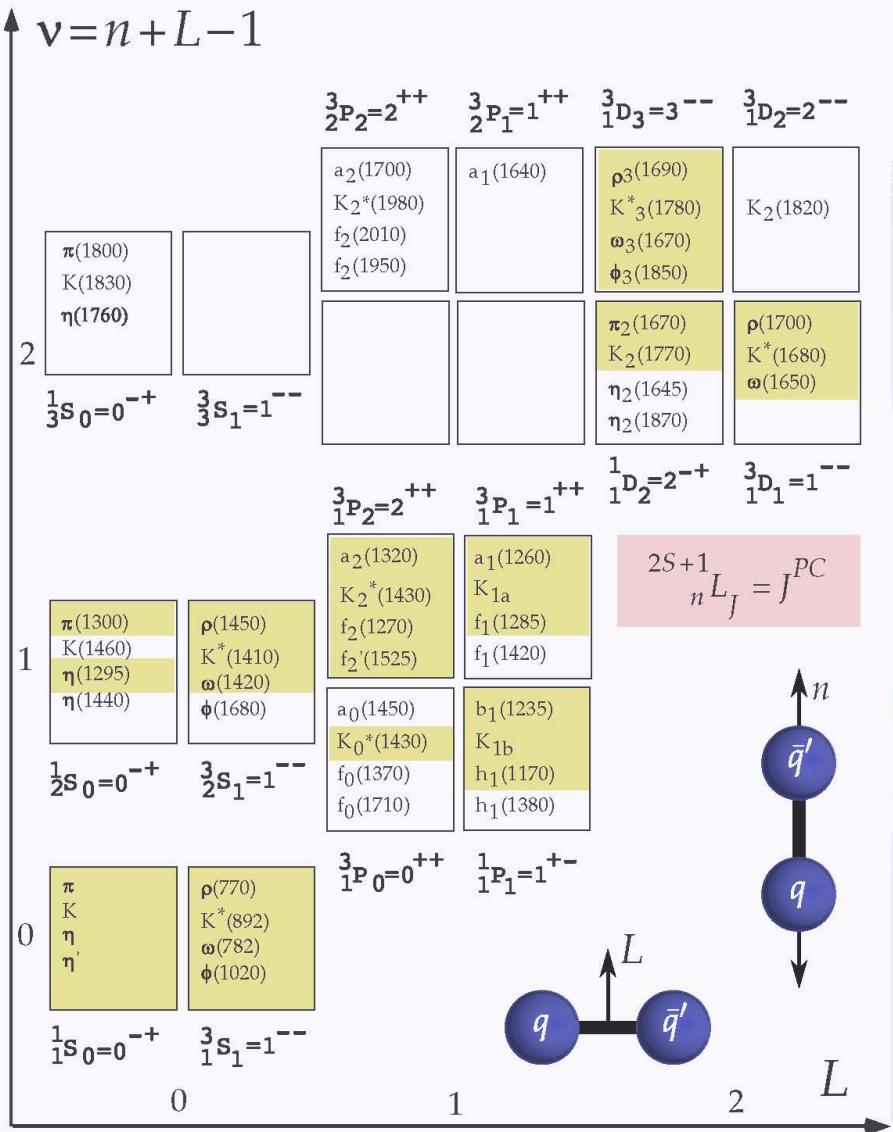
- Allowed  $J^{PC}$  combinations:
  - $L = 0 \rightarrow$  pseudo-scalar  $0^{++}$ , Vector  $1^{--}$
  - $L = 1 \rightarrow$  scalar  $0^{++}$ , axial-vector  $1^{+-}$ ,  $1^{++}$  and tensor  $2^{++}$
- Forbidden  $J^{PC}$  combinations:  $0^{--}$ ,  $0^{+-}$ ,  $1^{-+}$ ,  $2^{+-}$ ,  $3^{+-}$  .....
- Same quantum numbers mix

# Constituent Quark Model III



C. Amsler *et al.*, Phys. Rept. 389, 61 (2004)

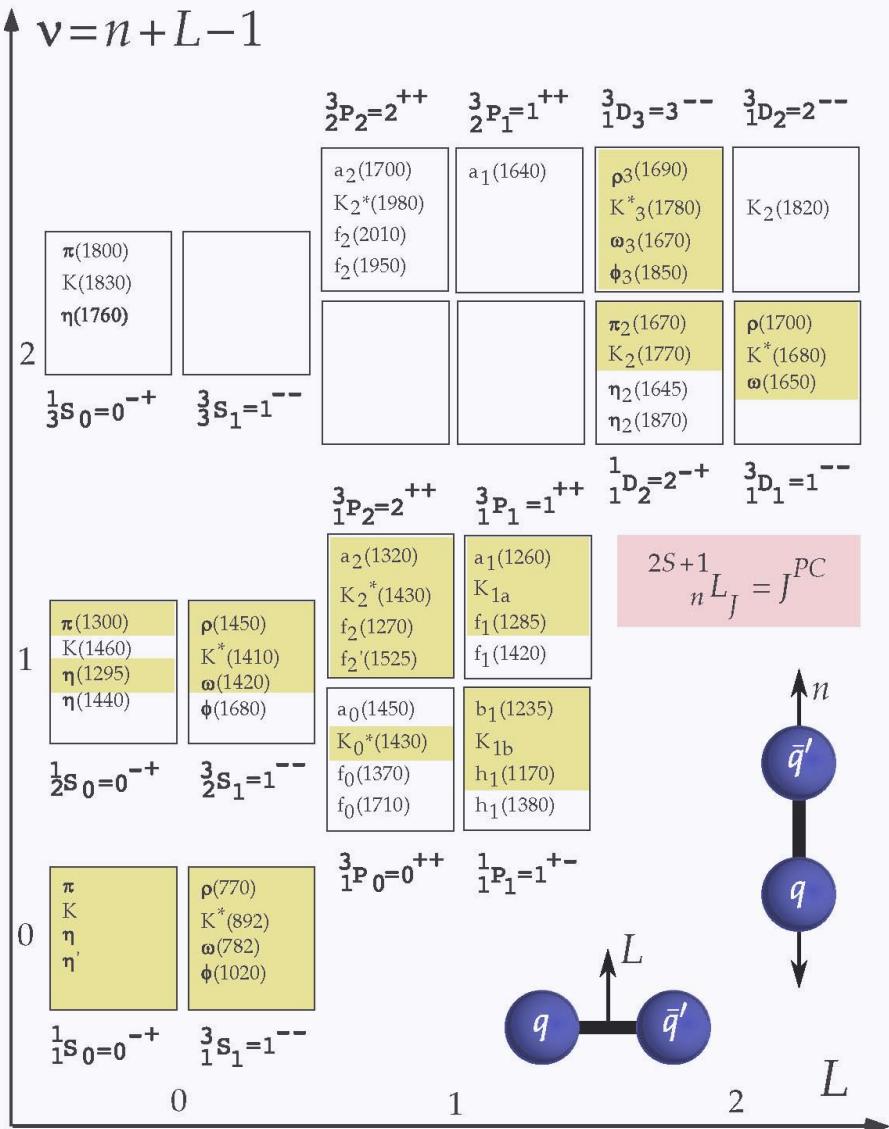
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Boundary of light mesons:

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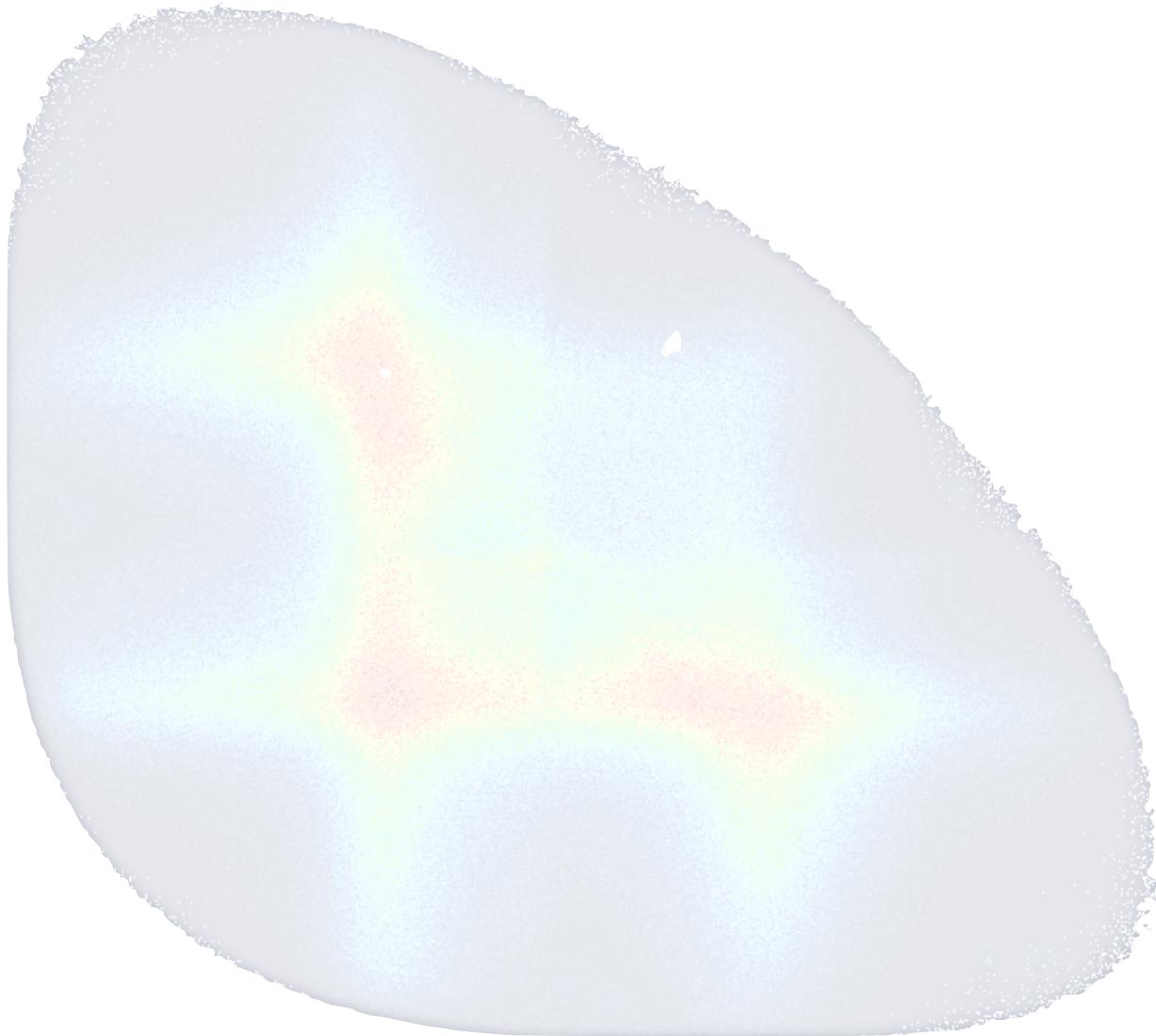


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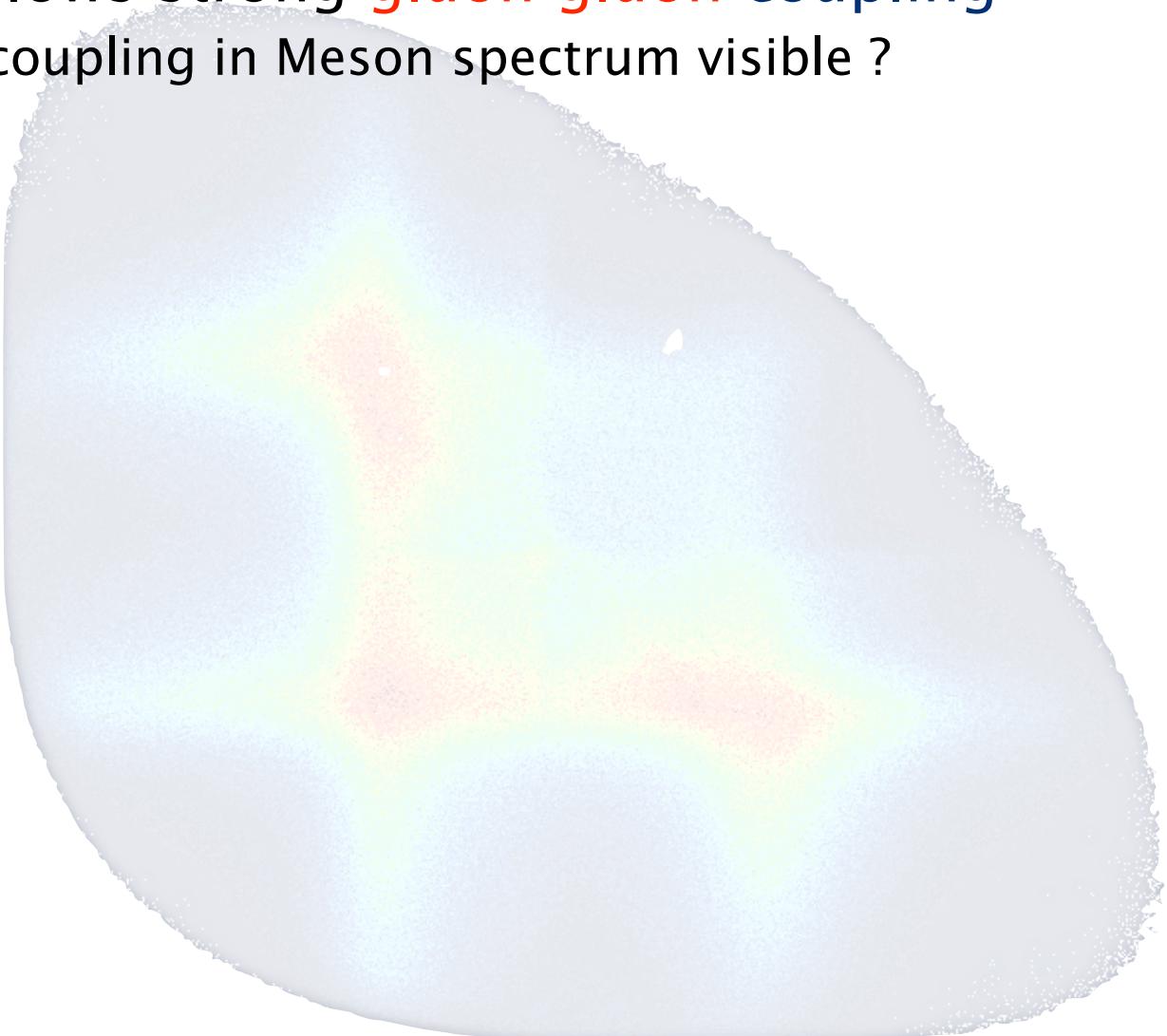
- Many **missing/disputed States** in mass region  $m \sim 2 \text{ GeV}/c^2$
- Identification heavier states **difficult**
  - Broad states
  - Large number of states

# Extension of Model



# Extension of Model

- QCD allows strong **gluon-gluon coupling**
  - Self coupling in Meson spectrum visible ?

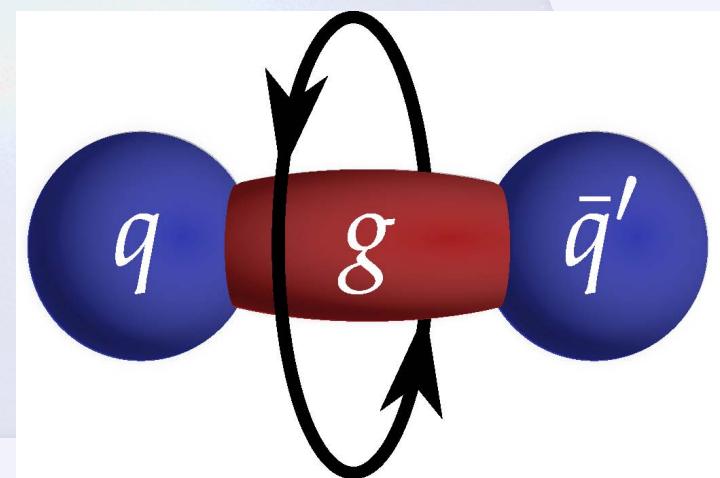


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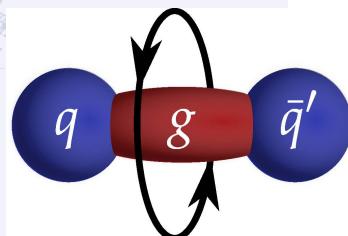
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## Hybrids

- Resonances with excitations of **gluon field**
  - Description of **gluon excitation** is model dependent
  - E.g. **flux-tube Model:**
    - „**Flux-tube**“: Gluon field between static colour charges
    - **Transversal excitation**: angular momentum of **flux-tube** couples with ( $L, S$ ) of mesons to  $J$
    - Different from  $|q\bar{q}'\rangle$  no restrictions to  $J^{PC}$
    - Lightest hybrid with  $J^{PC} = 1^{-+}$  with mass between 1.3-2.2 GeV/c<sup>2</sup> forbidden  $J^{PC}$  for  $|q\bar{q}'\rangle$



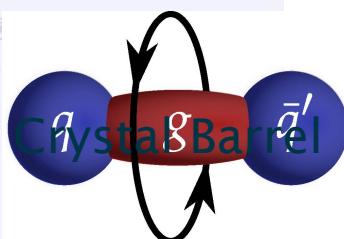
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- Experimental status:
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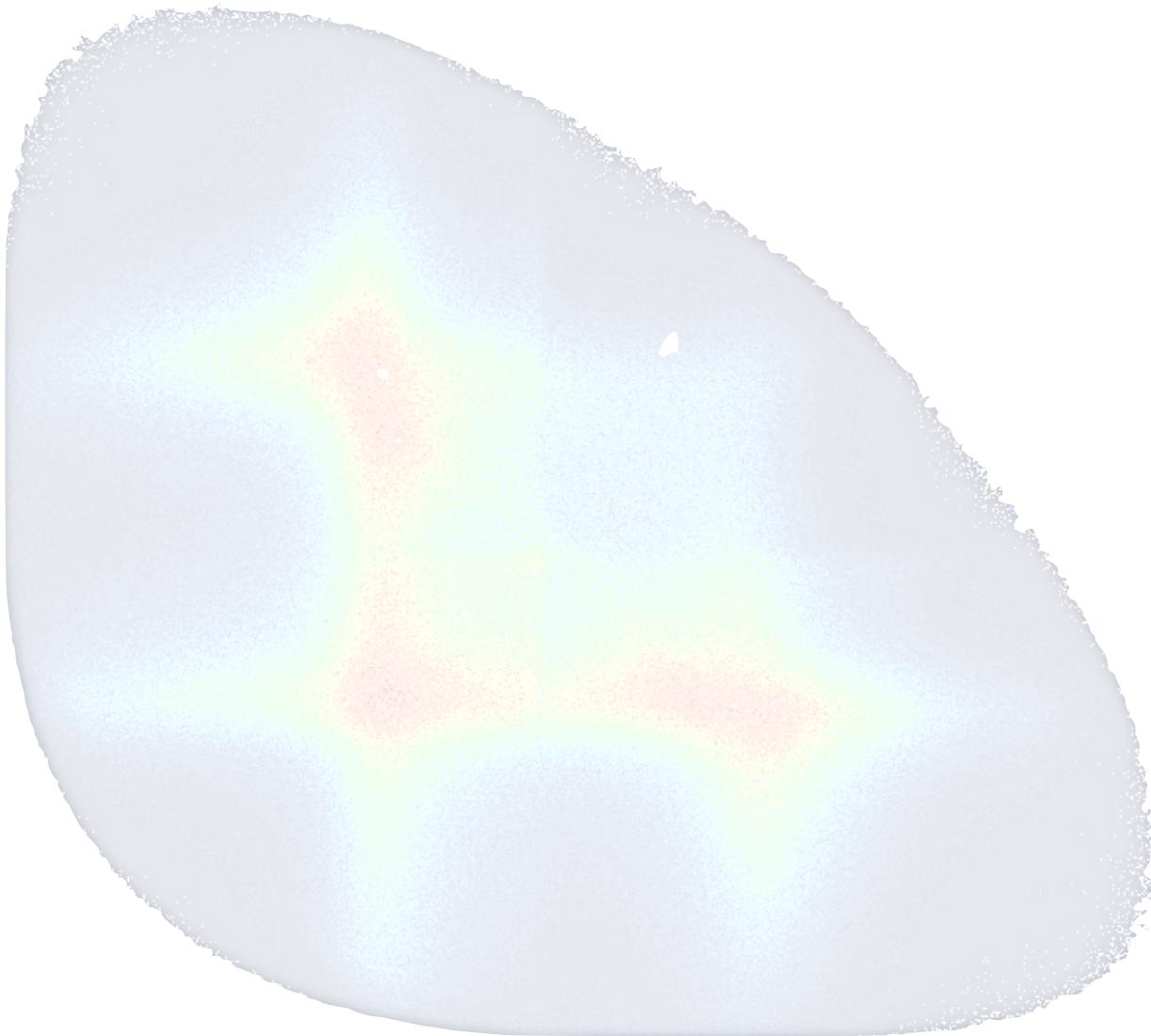


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  - Resonance structure still **disputed**

# Extension of Model II



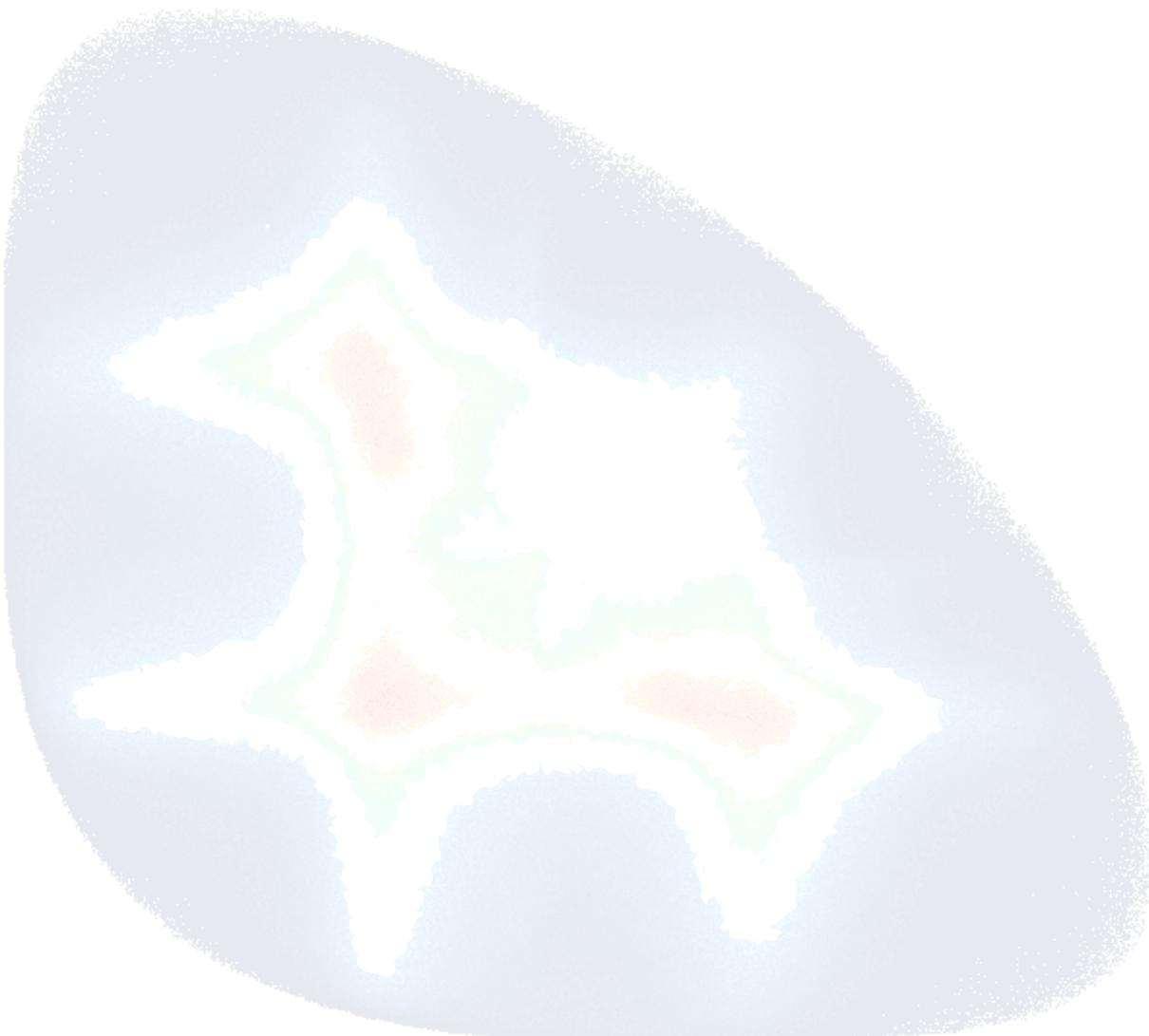
## Glueballs

- Bound system from **gluons** (without valence quarks)
  - 'Ground state' expected as  $0^{++}$
  - Strong **mixing** mit meson spectrum  $|q\bar{q}\rangle$
  - Identification via decay
    - No inherent flavour → **flavour-democratic decay** ( $KK$ ,  $\pi\pi$ )
    - Observe **characteristic final states** (e.g.  $\eta'$ )
  - **Mixing:** Interpretation only via **coupled channel analysis**

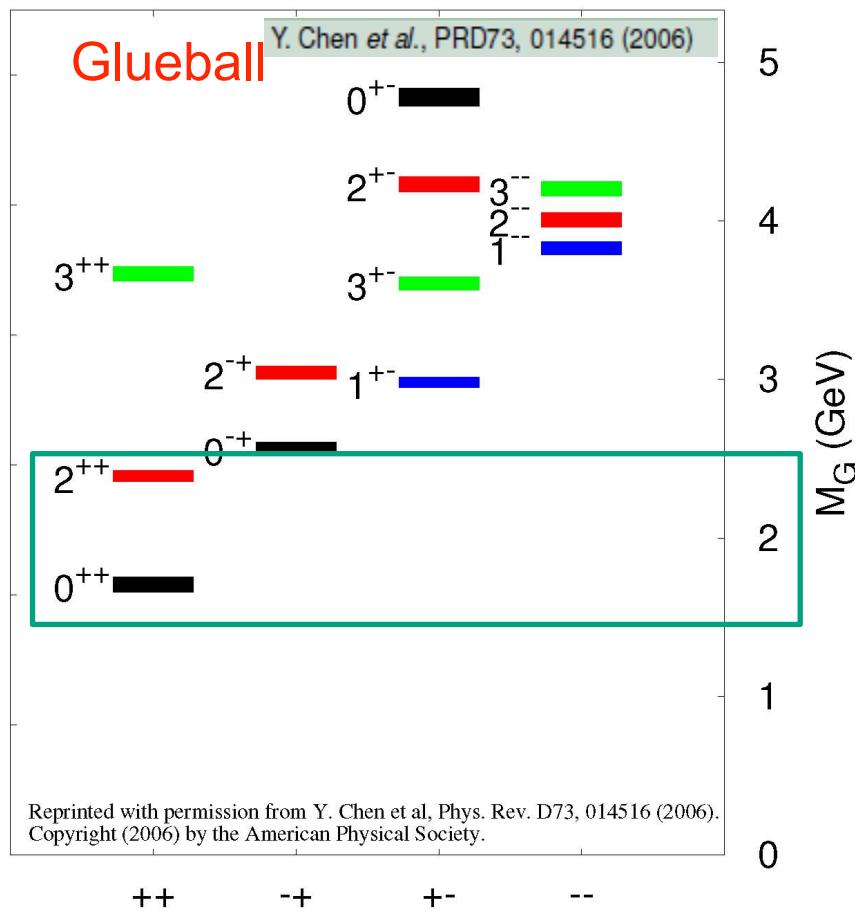
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- Experimental status:
  - $f_0(1500)$  observed in different experiments
  - Interpretation still **disputed**

# Predictions Lattice QCD



## Quenched L-QCD prediction



## Lightest glueballs:

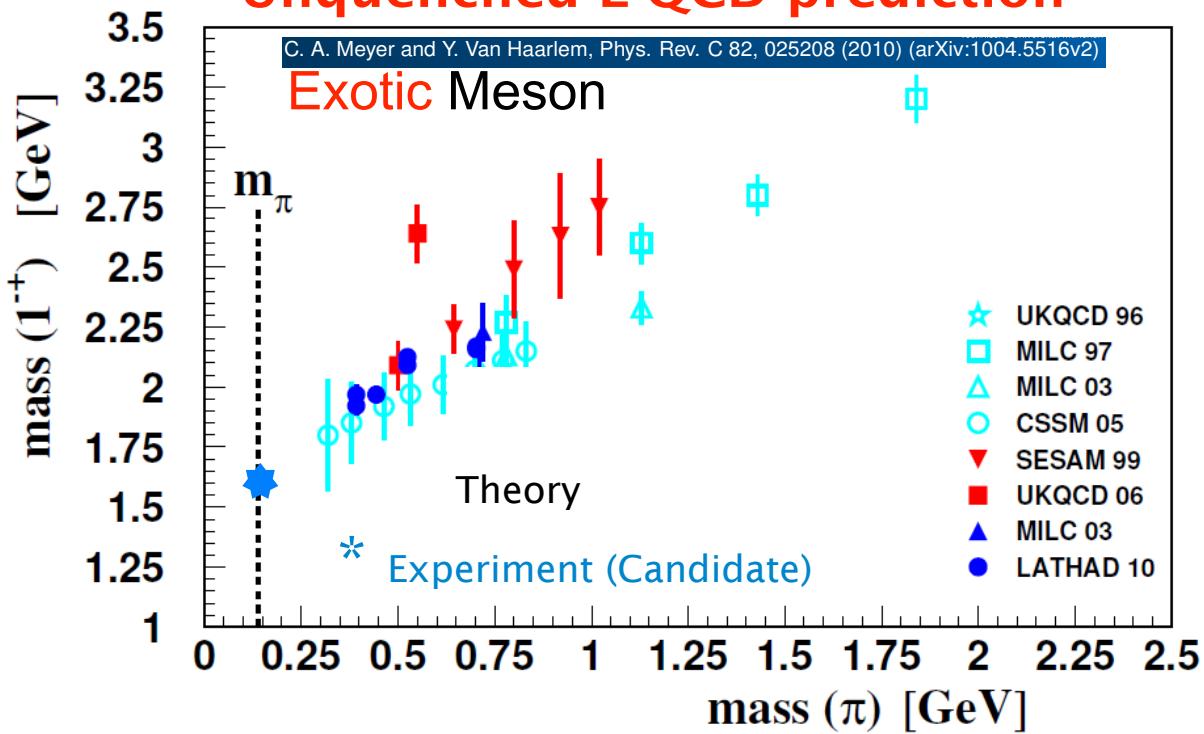
- $M \sim 1.7 \text{ GeV}/c^2$  ( $J^{PC} = 0^{++}$ )
- $M \sim 2.4 \text{ GeV}/c^2$  ( $J^{PC} = 2^{++}$ )



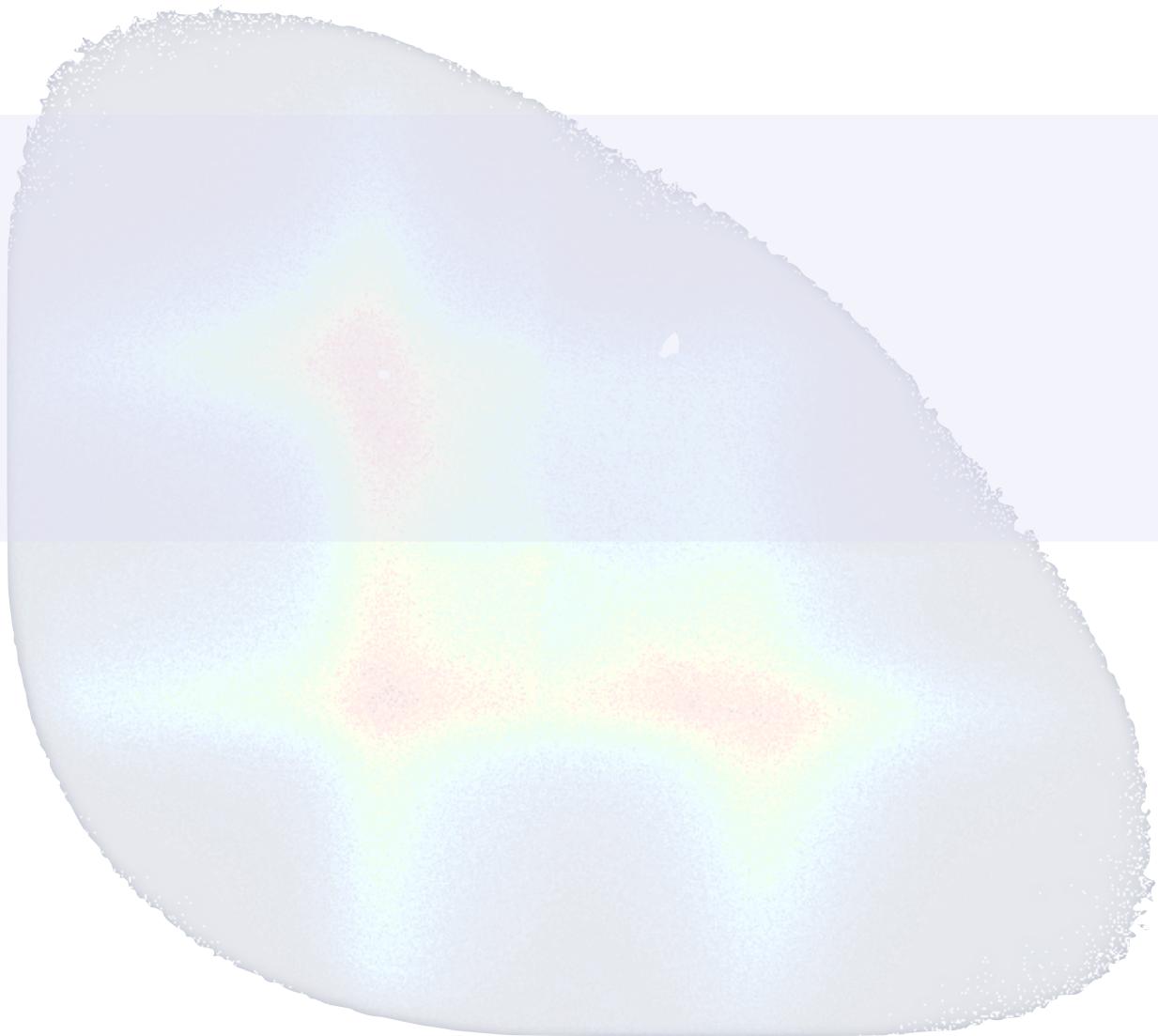
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## Unquenched L-QCD prediction

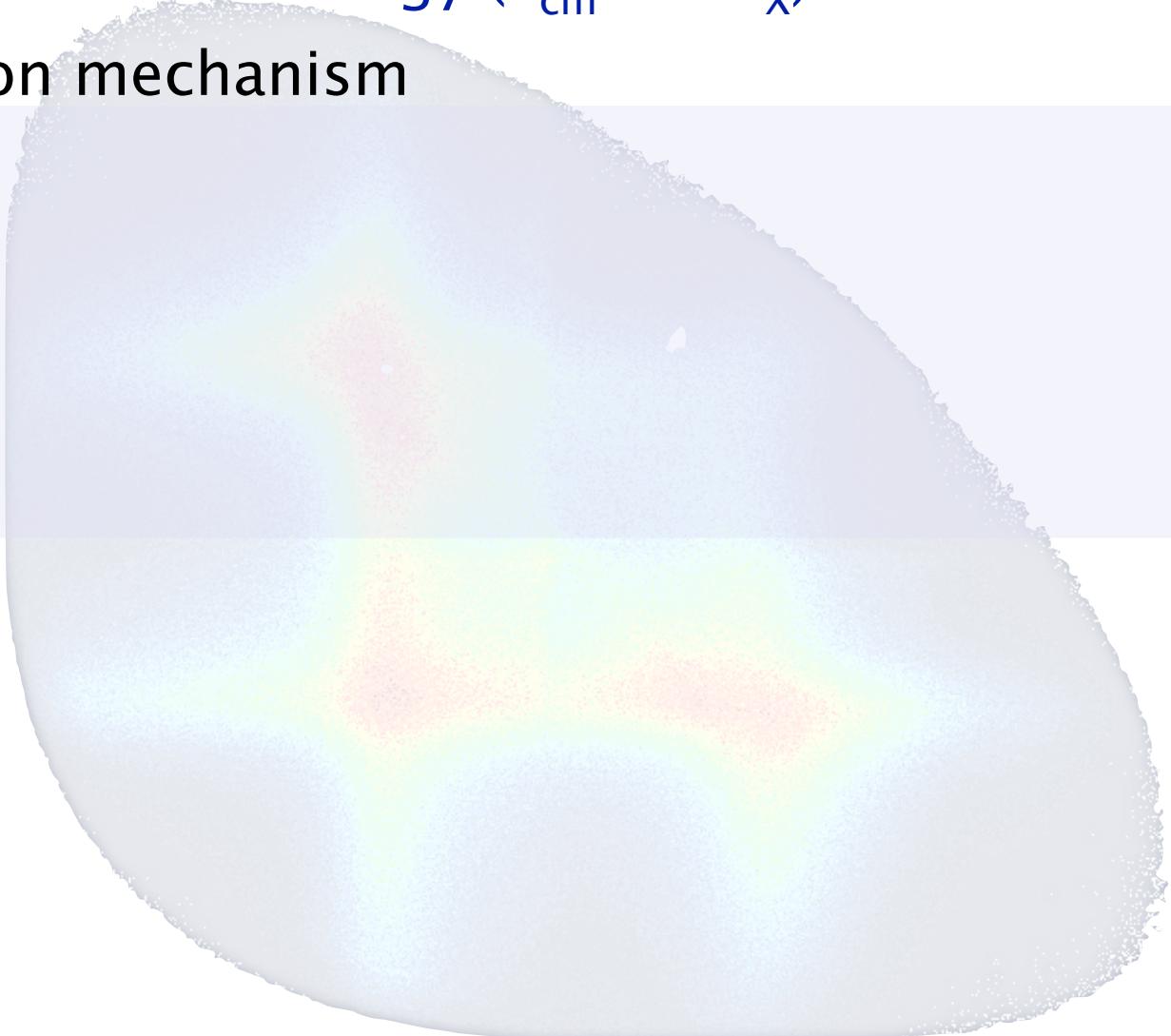


# How to Observe Exotic Mesons ?



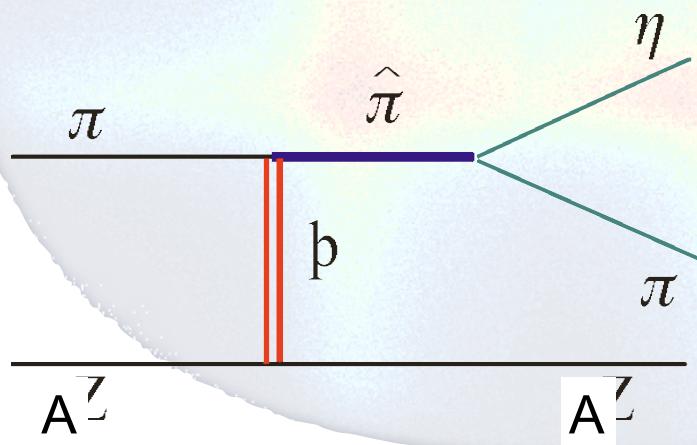
# How to Observe Exotic Mesons ?

- Centre of mass energy ( $E_{cm} > M_x$ )
- Reaction mechanism



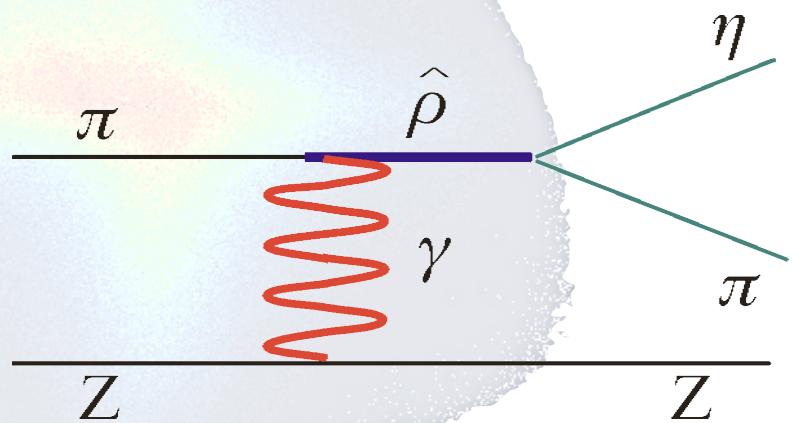
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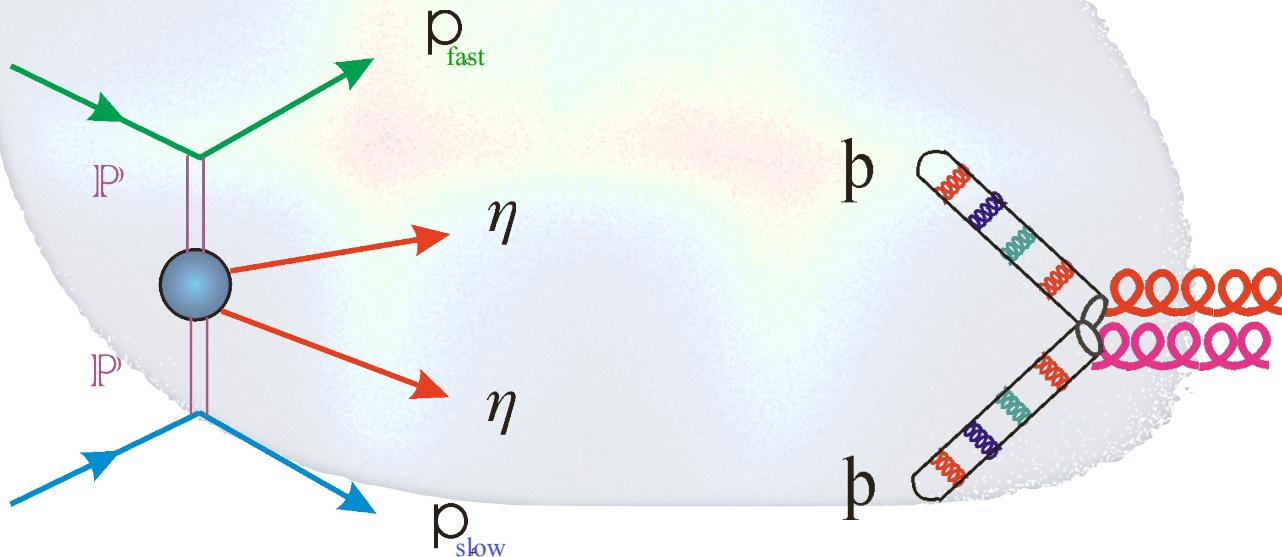


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    - Use  $\gamma - \rho - \phi$  coherence (VMD) and coupling of  $M_x$  to  $\rho, \phi$

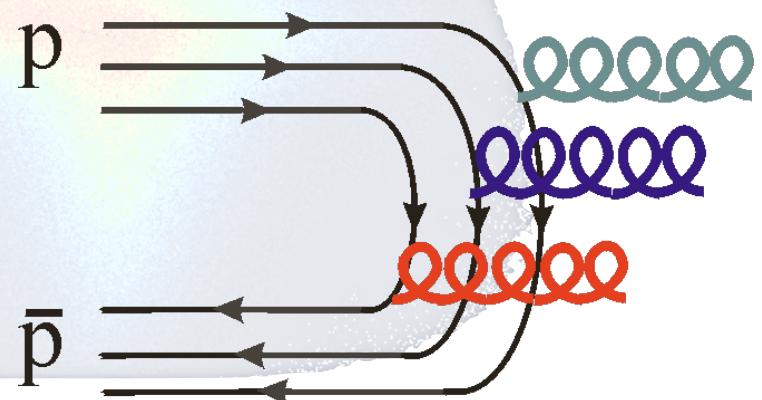


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  - **,central'** production
    - Gluon-rich exchange particles (pomeron)



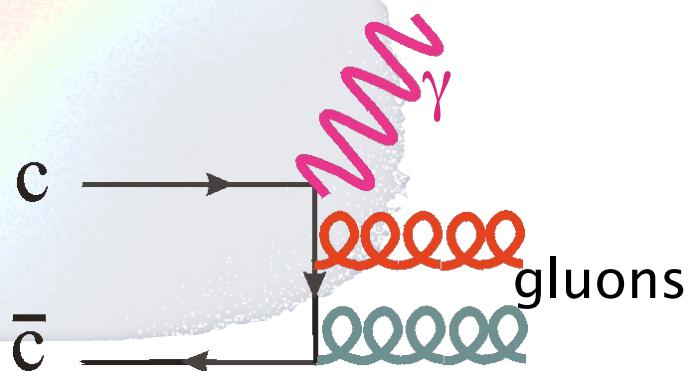
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    - Gluon-rich intermediate state in annihilation



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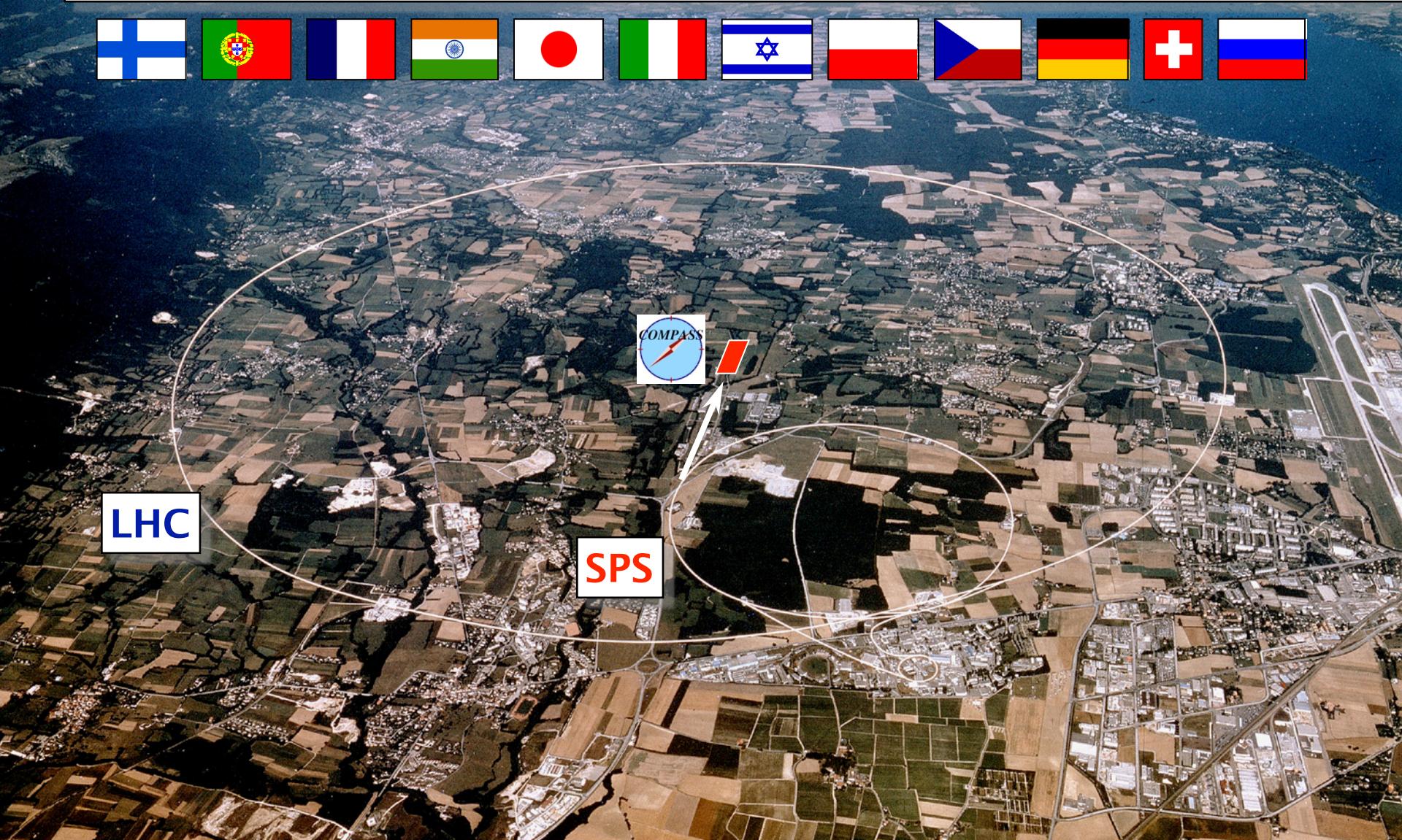
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  - **$p\bar{p}$  annihilation**
    - Gluon-rich intermediate state in annihilation
  - **Decays of heavy mesons** (e.g.  $J/\Psi$ )
    - Gluon rich final state



# COMPASS at CERN



COmmon Muon and Proton Apparatus for Structure and Spectroscopy



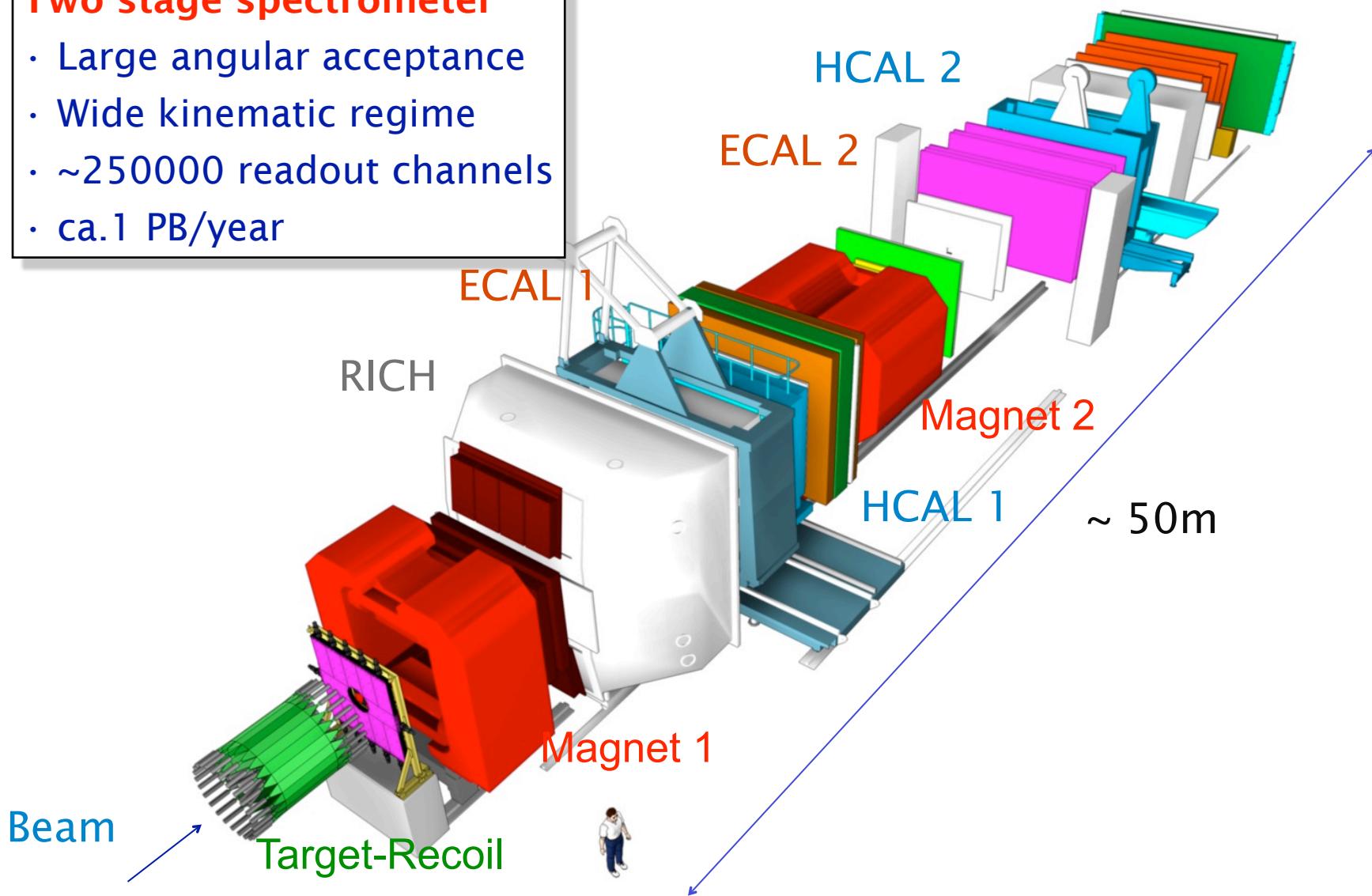
## COmmon Muon and Proton Apparatus for Structure and Spectroscopy



# Spectrometer - 2008

## Two stage spectrometer

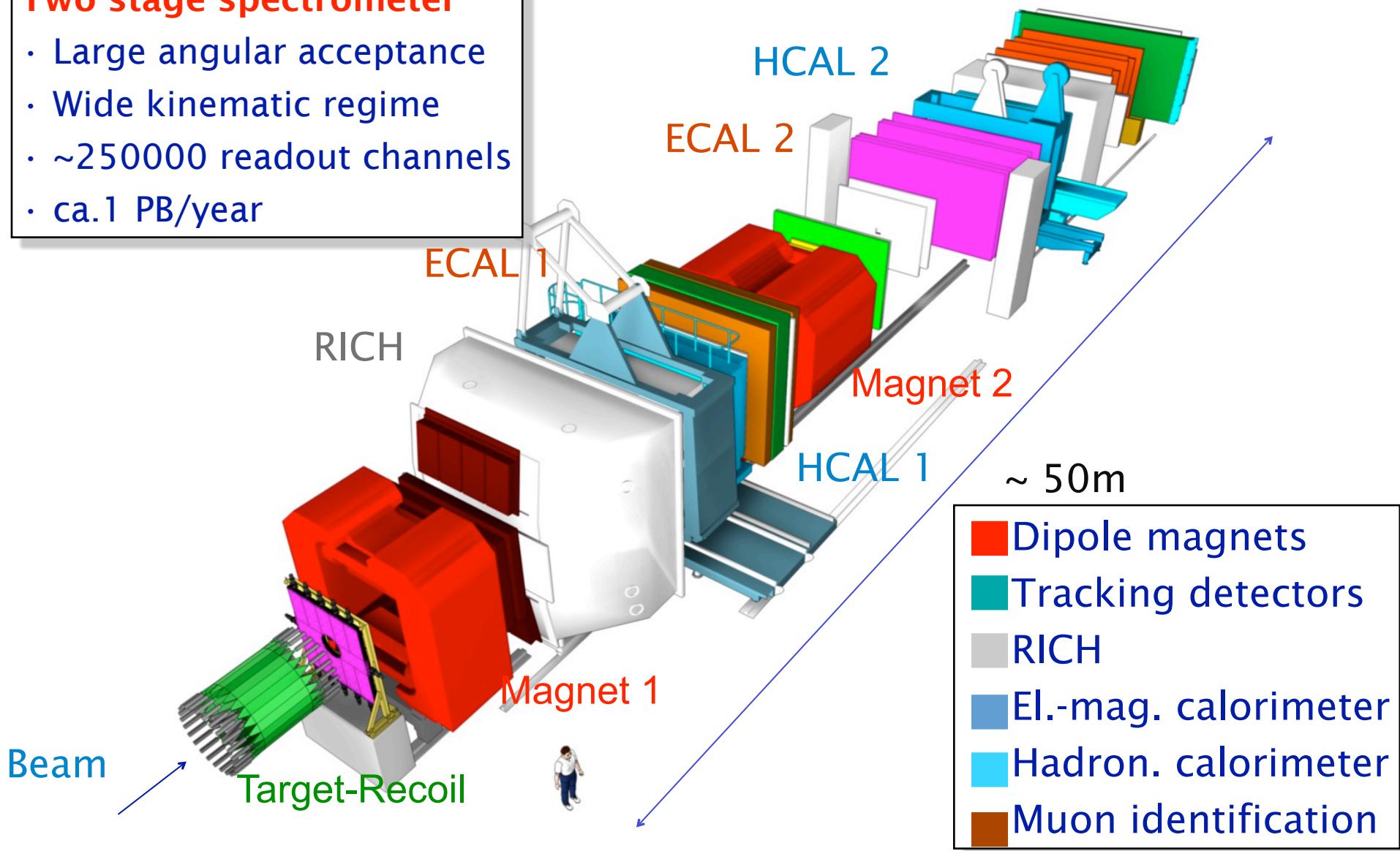
- Large angular acceptance
- Wide kinematic regime
- ~250000 readout channels
- ca.1 PB/year



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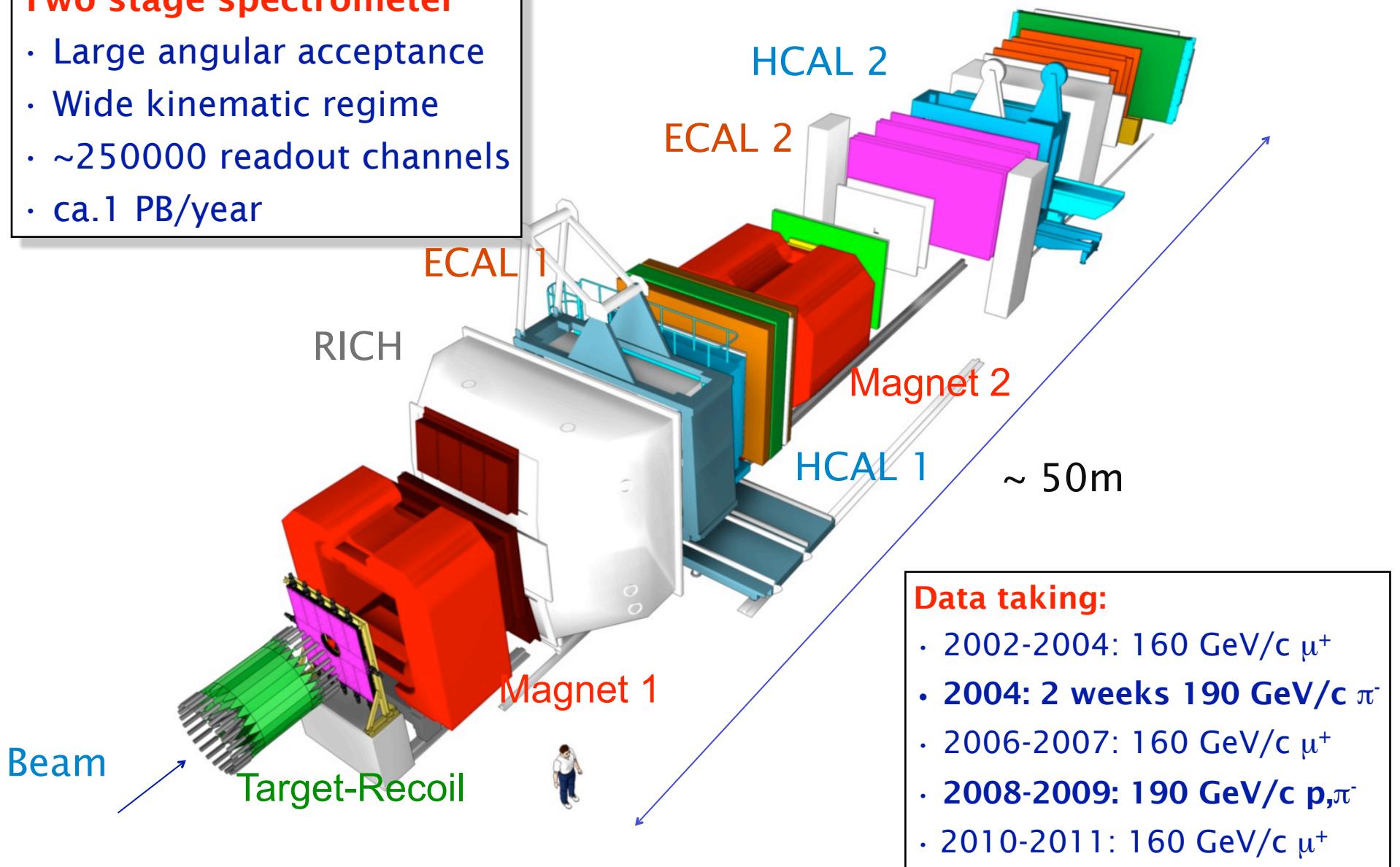
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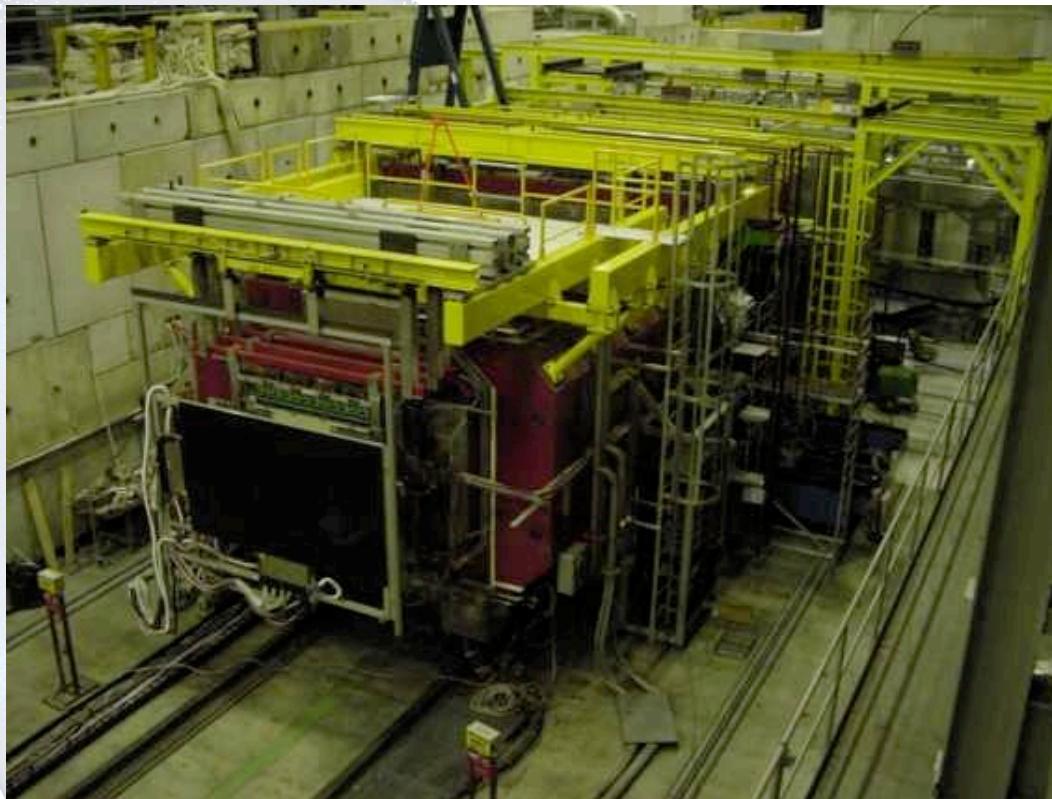
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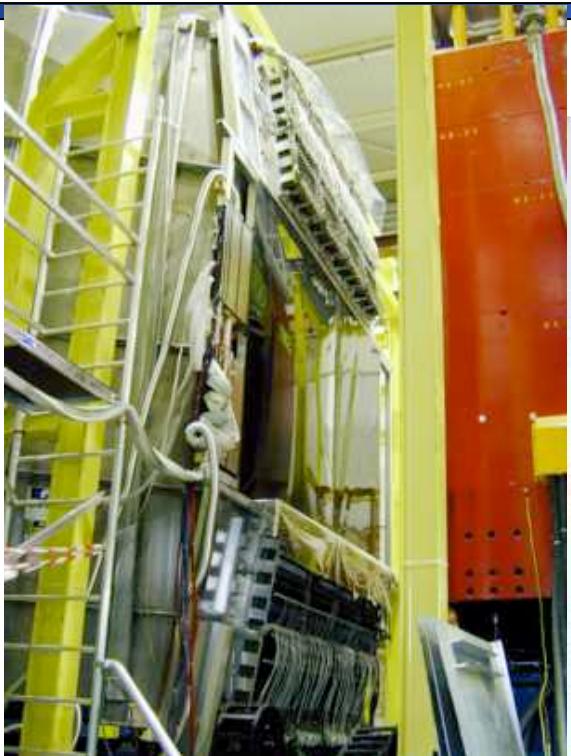
## Data taking:

- 2002-2004: 160 GeV/c  $\mu^+$
- 2004: 2 weeks 190 GeV/c  $\pi^-$
- 2006-2007: 160 GeV/c  $\mu^+$
- 2008-2009: 190 GeV/c  $p, \pi^-$
- 2010-2011: 160 GeV/c  $\mu^+$

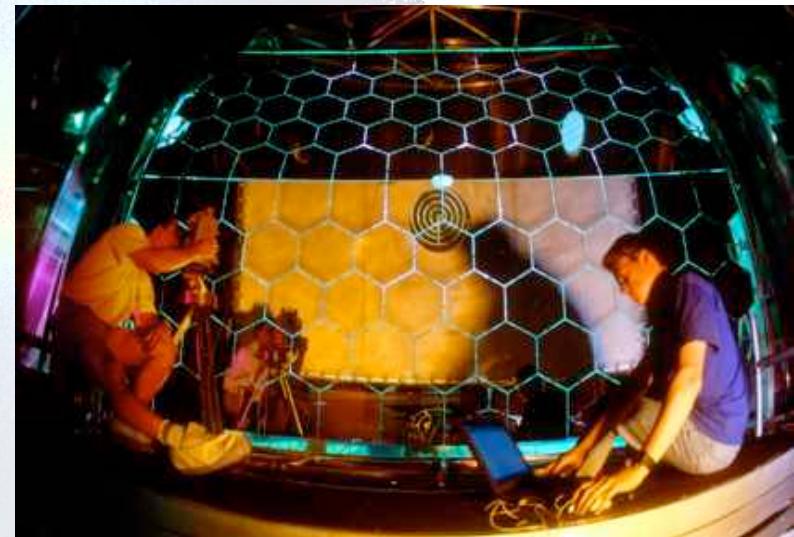
# Impressions



# Impressions



RICH

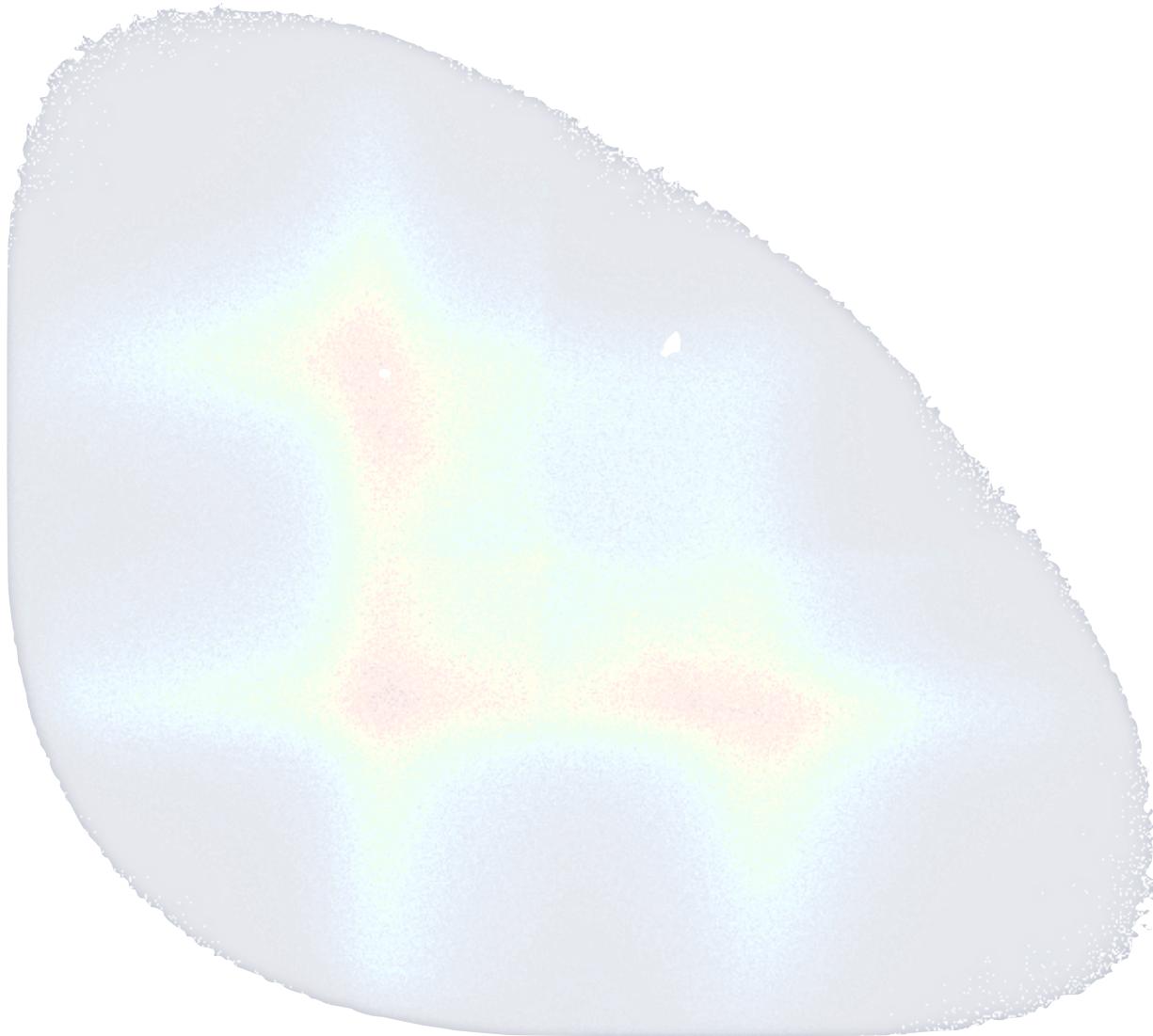


# Impressions

## Heavy Equipment



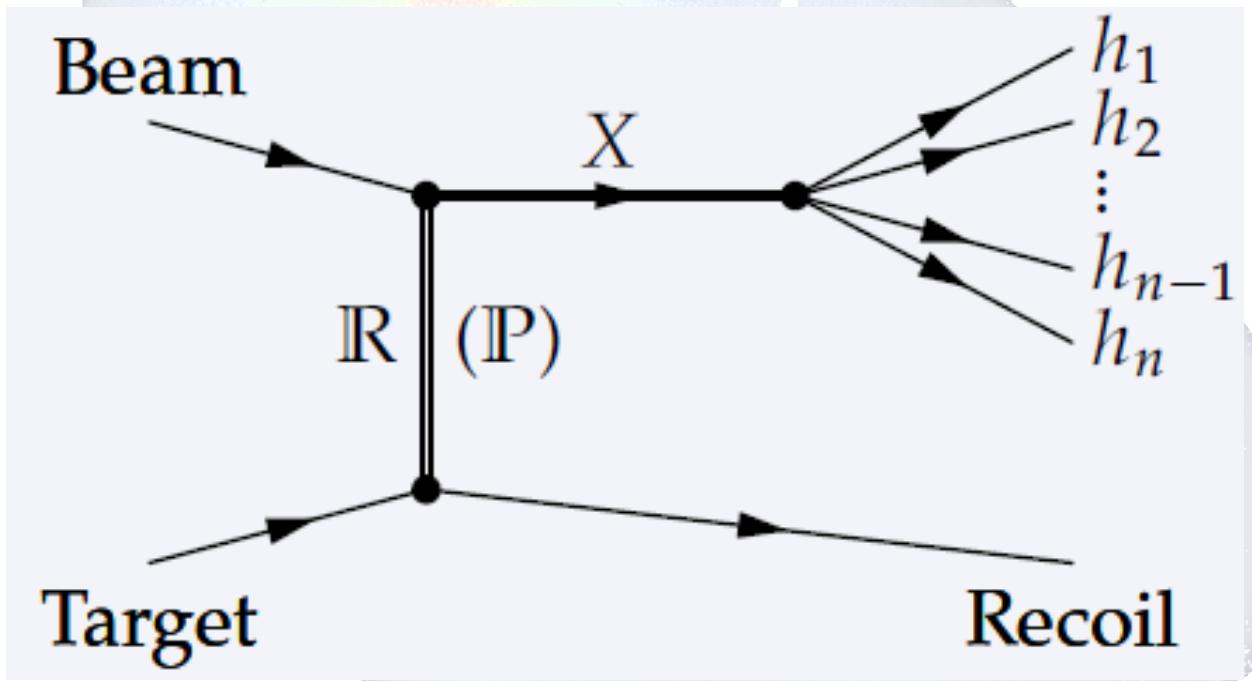
# Analysis - Diffractive Production



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Beam particle gets excited to state  $X$  – total cross section ist  $\mathcal{O}(\text{mb})$

- State  $X$  decays in  $n$ -Hadrons
- Target takes up recoil, stays intact



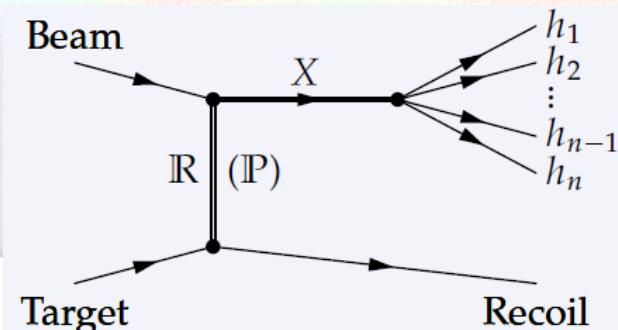
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What can I say about **X** ?

- Angular momentum production via
  - Spin flip of target (not with pure Pomeron-exchange)
  - Orbital angular momentum (pomeron-projectile) in reaction
  - Projection of **orbital angular momentum** to X with  $m=0$
  - ,Pomeron'  $0^{++}$  exchange: **no Quantum Numbers are exchanged**
  - 4-momentum transfer  $t$  determines mass spectrum

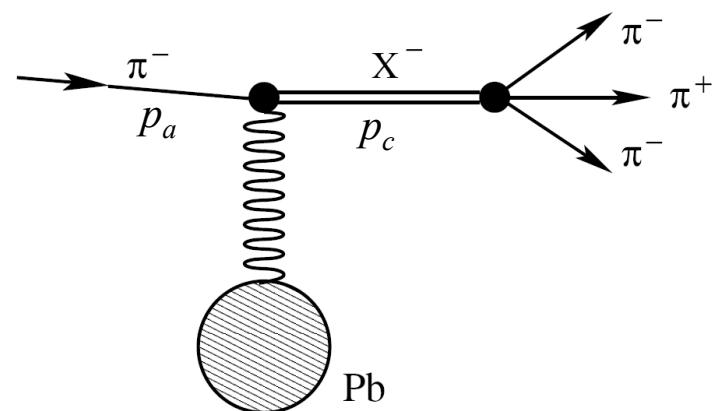


# Diffractive Reactions at COMPASS

**Example:**  $\pi^- + \text{Pb} \rightarrow \pi^-\pi^-\pi^+ + \text{Pb}$

- 4 $\pi$  vertex in Pb target
- Exclusivity  $\Rightarrow$  target stays intact
- Momentum transfer

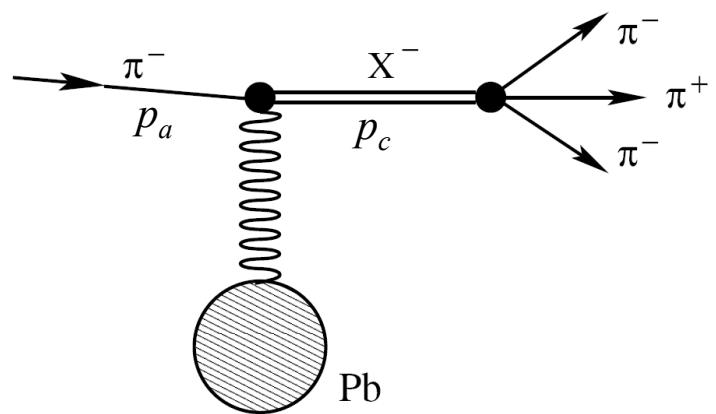
$$-t \equiv Q^2 = -(p_a - p_c)^2$$



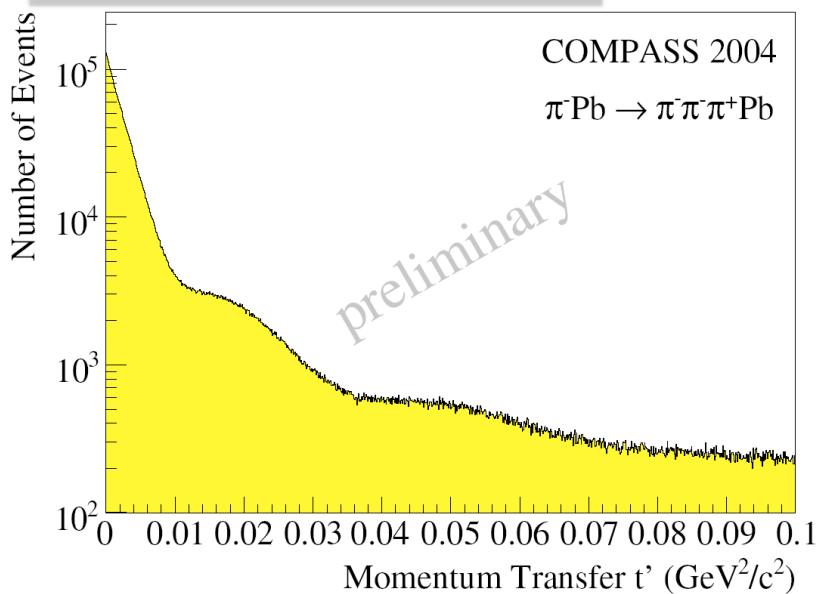
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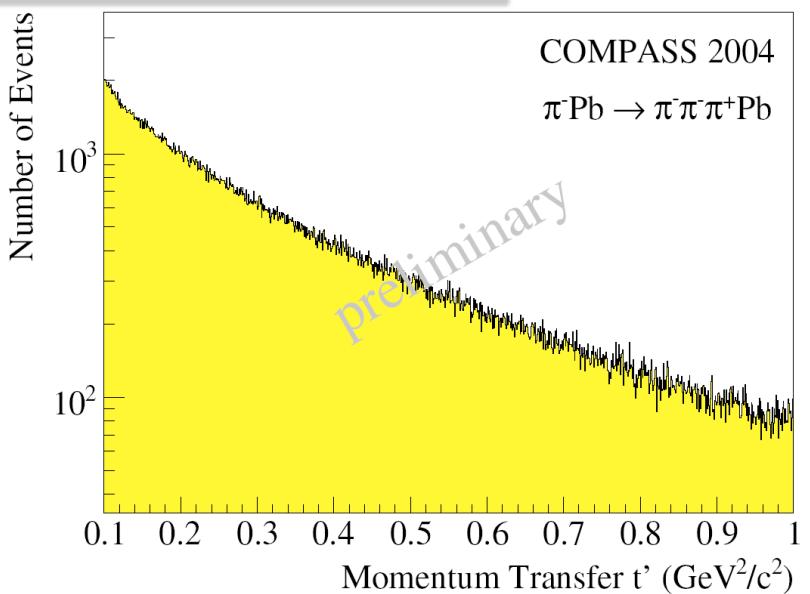
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Diffraction on Pb nuclei



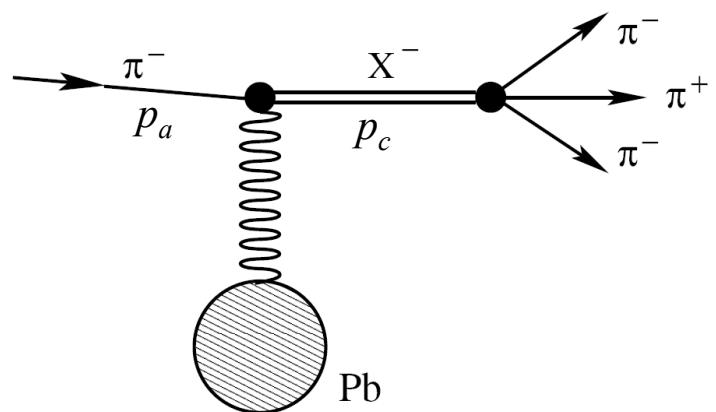
Diffraction on nucleons



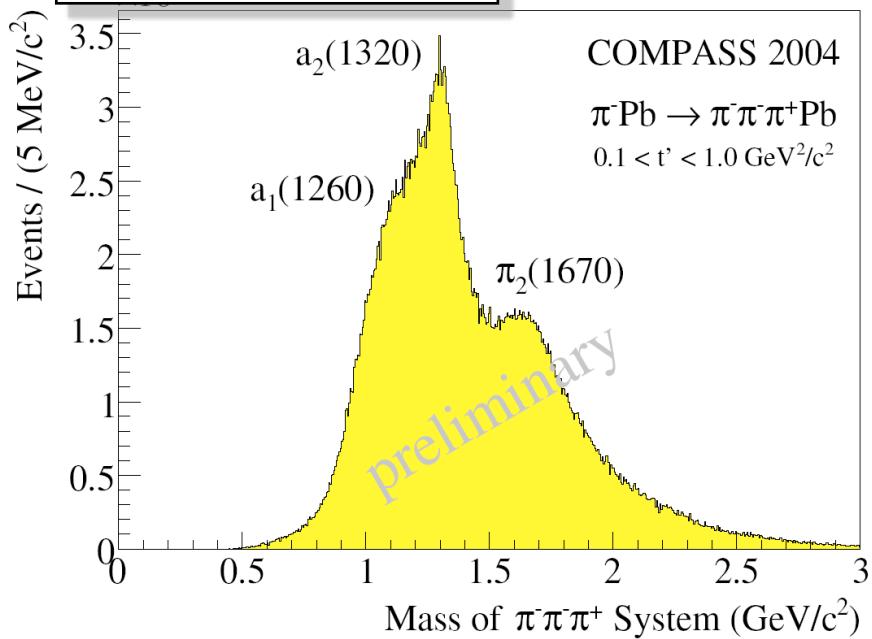
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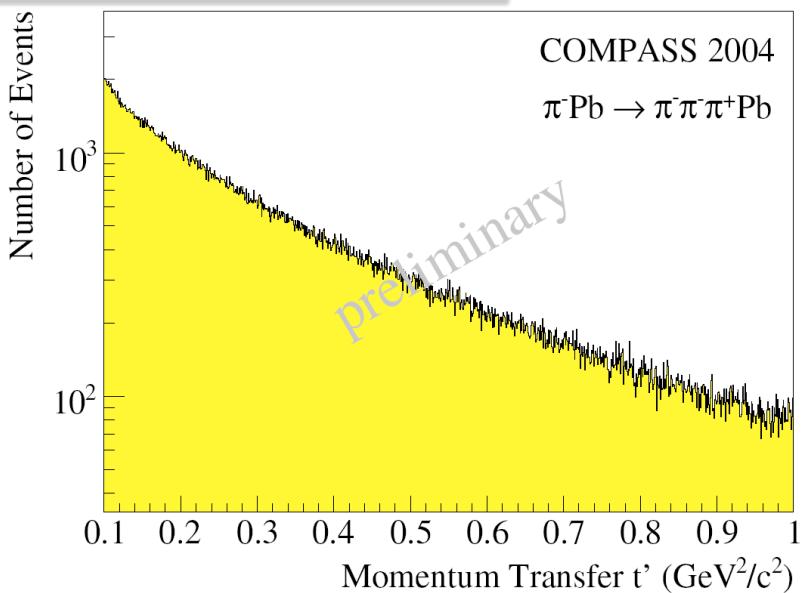
$$-t \equiv Q^2 = -(p_a - p_c)^2$$



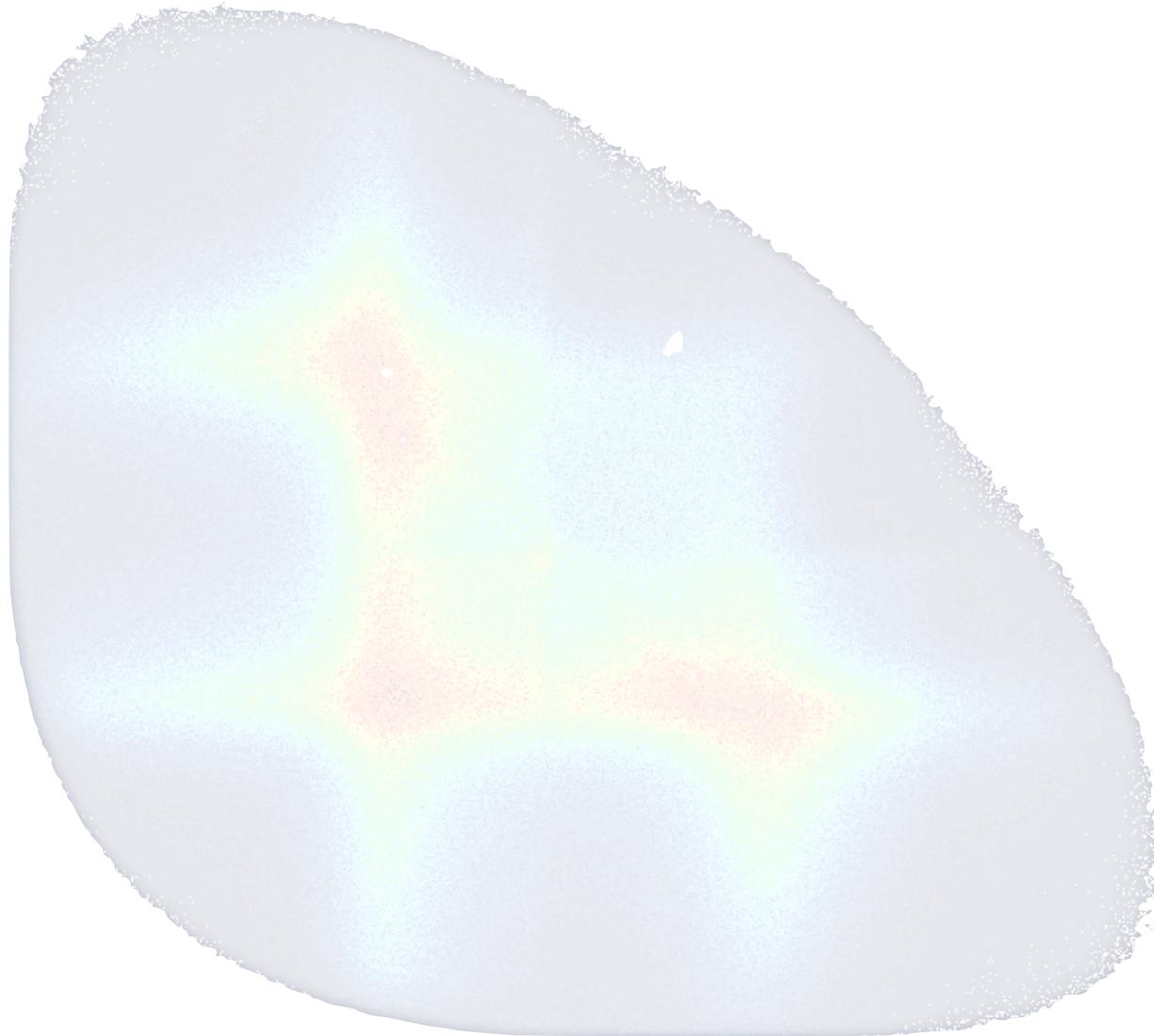
3 $\pi$  invariant mass



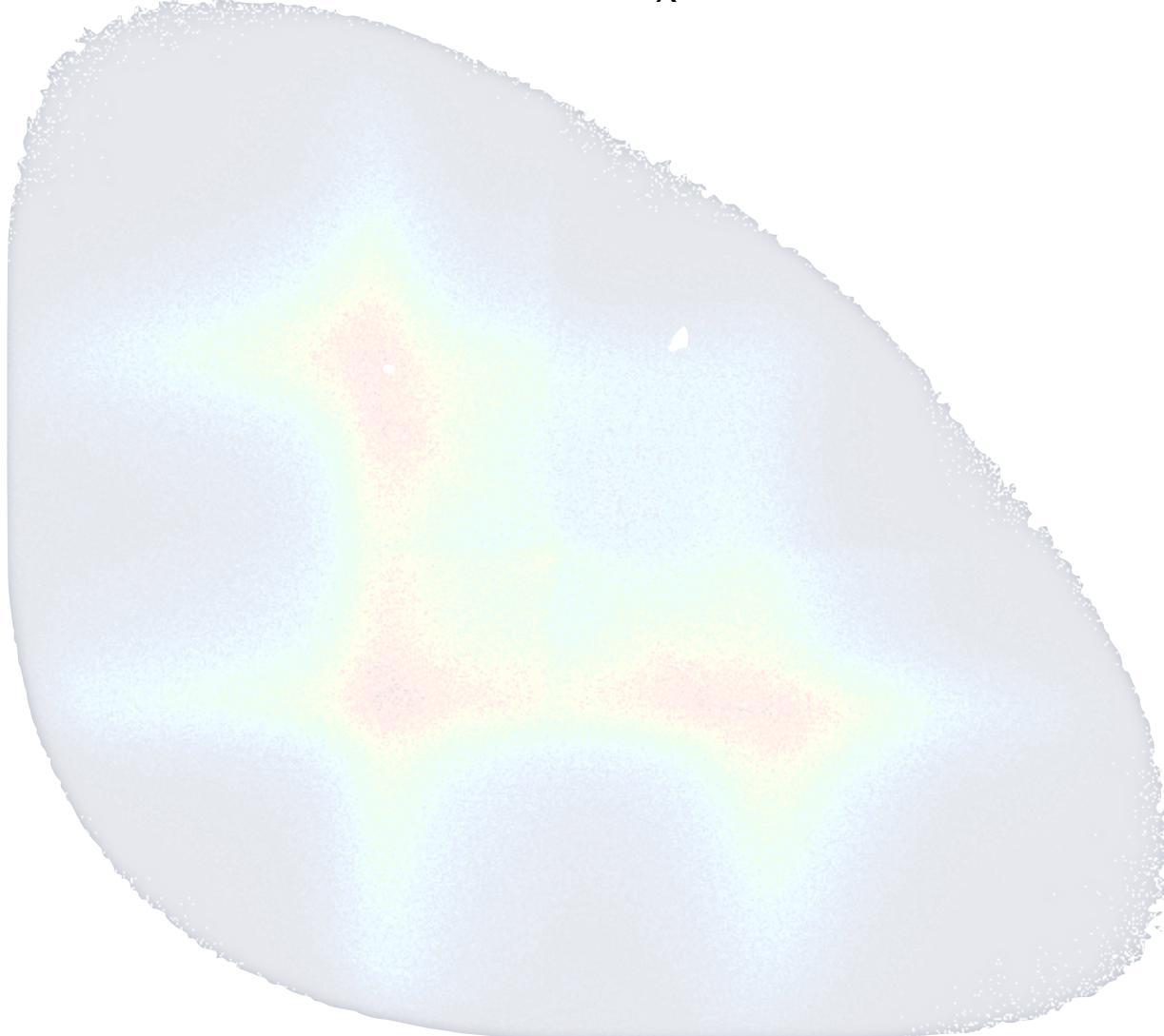
Diffraction on nucleons



# Analysis Inelastic Final State II



- Consider 3-body decay for fixed  $m_x$ :



# Analysis Inelastic Final State II

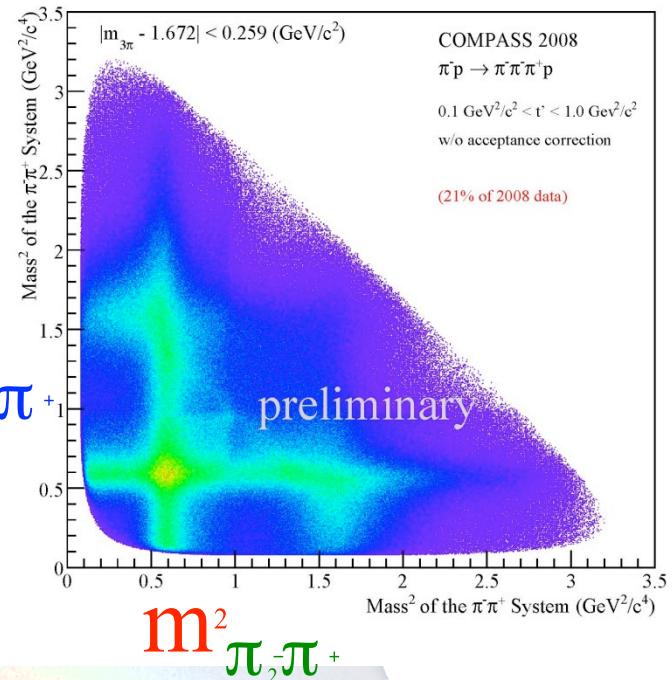
- Consider 3-body decay for fixed  $m_X$ :

$$X^- \rightarrow \pi_1^- \pi_2^- \pi^+$$

$\pi_1^- \pi_2^-$  are not distinguishable  
built  $m_{\pi_1^- \pi^+}$  and  $m_{\pi_2^- \pi^+}$

- Enhancements are sign for decay into isobars

Dalitzplot



# Analysis Inelastic Final State II

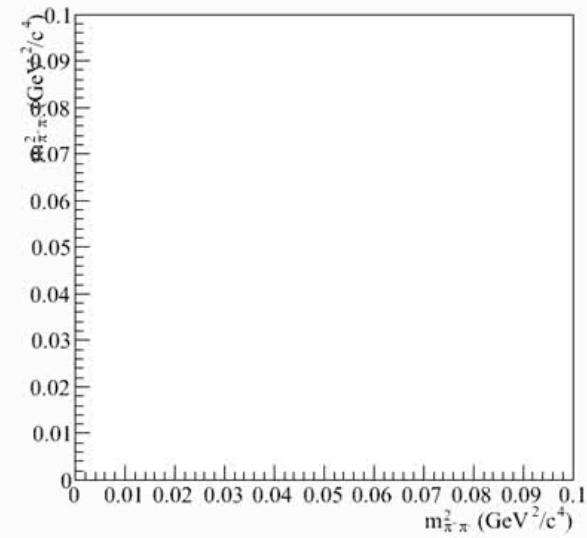
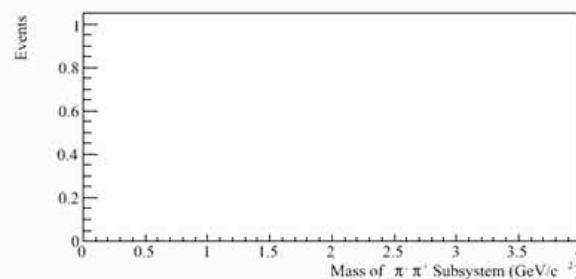
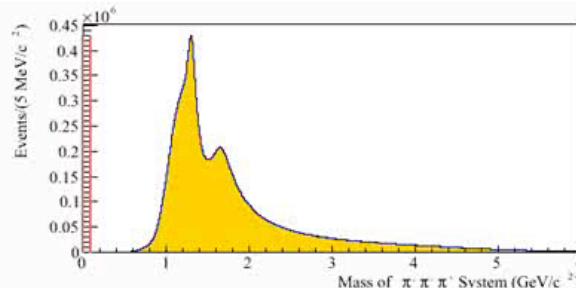
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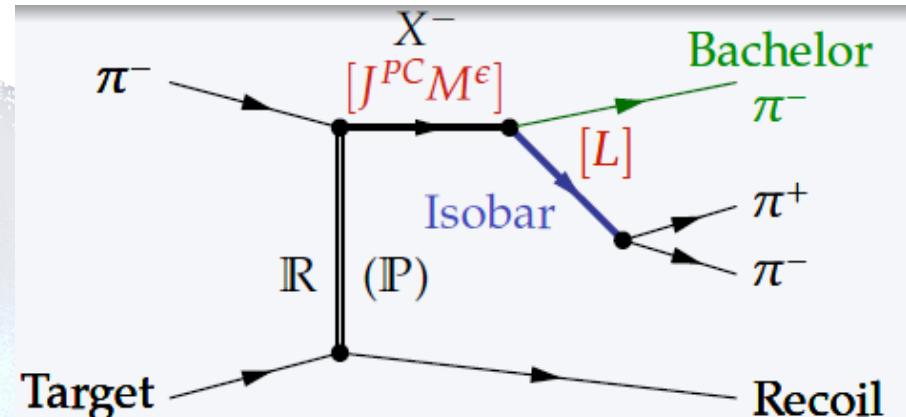
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→ full information about all partial waves in decay



$J^{PC} M^\epsilon [\text{isobar}] L$

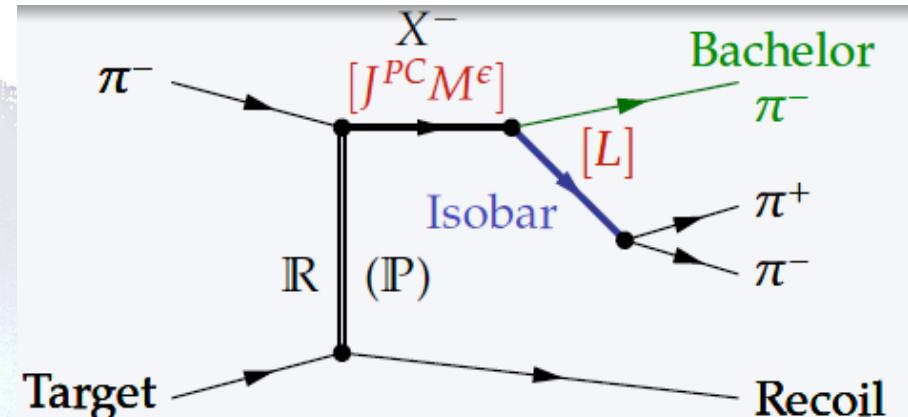
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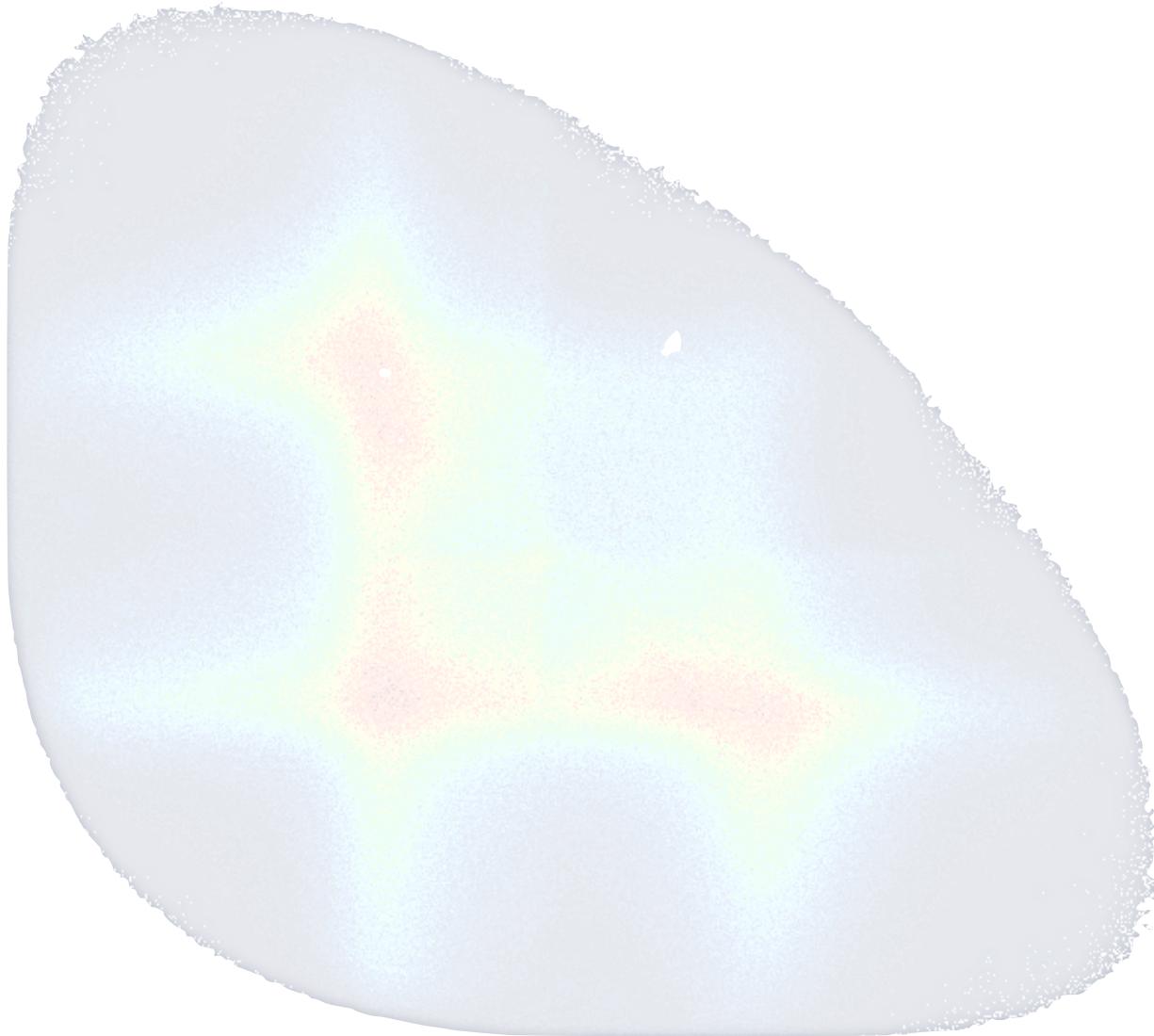
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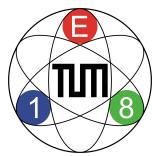


$J^{PC} M^\epsilon [\text{isobar}] L$

- Proceed in 2-step process
  - Analyze fixed mass bin: obtain production amplitudes  $T_i$   
→ spin density Matrix
  - Combine  $T_i$  of all mass bins: obtain resonance parameters of individual  $J^{PC}$

# Wave Set for the Fit

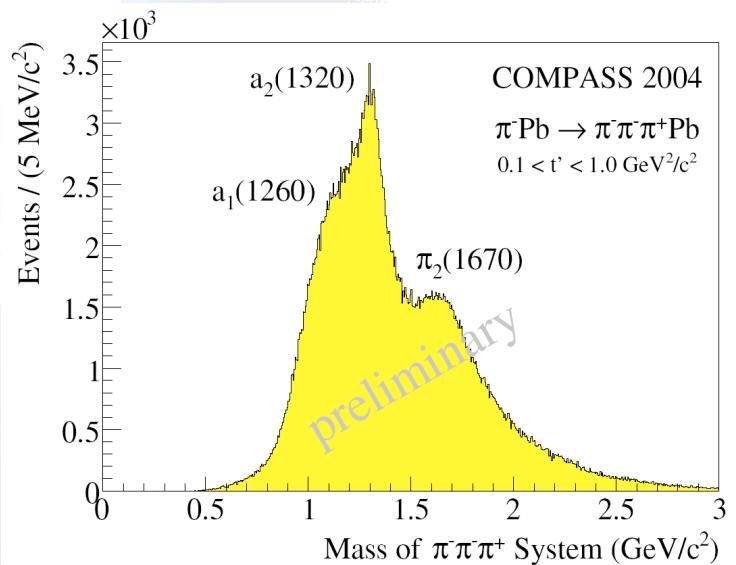
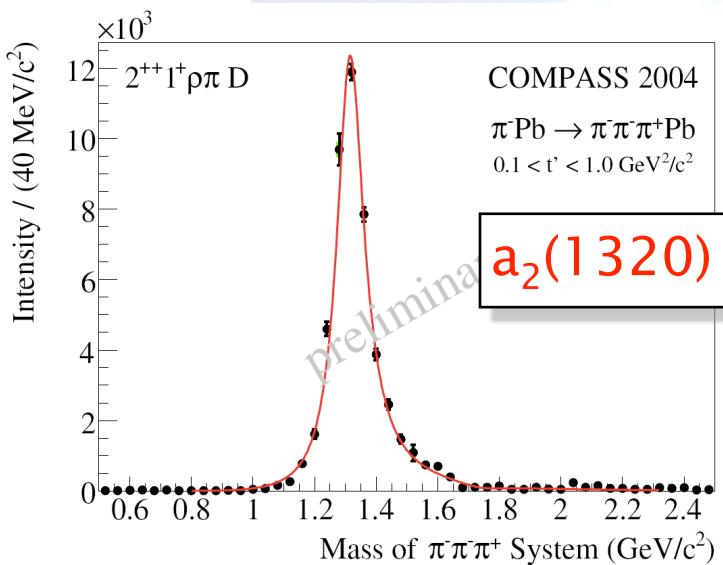
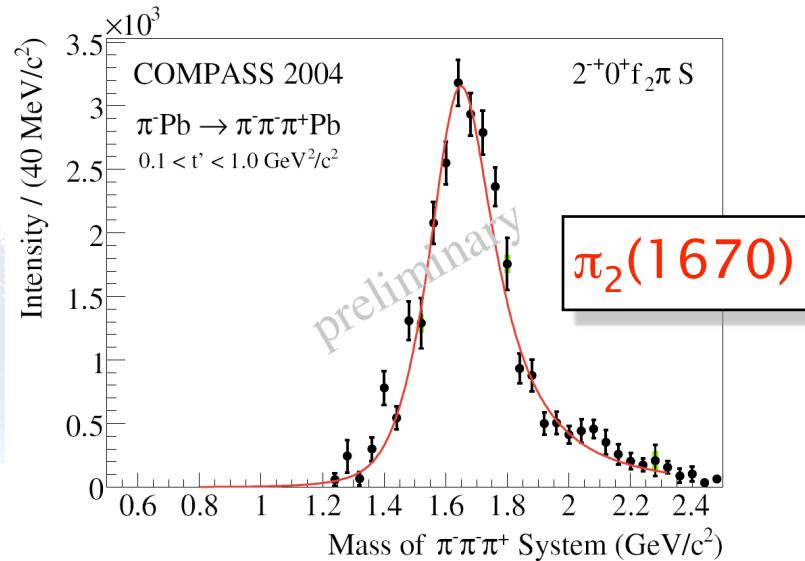
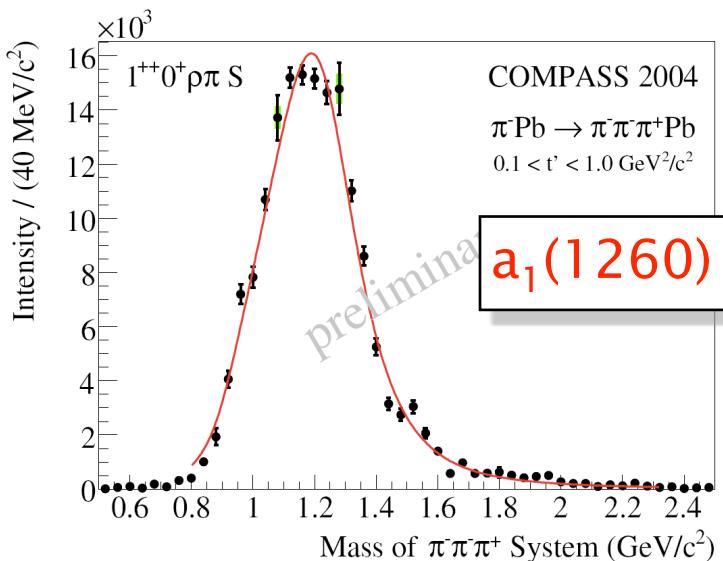




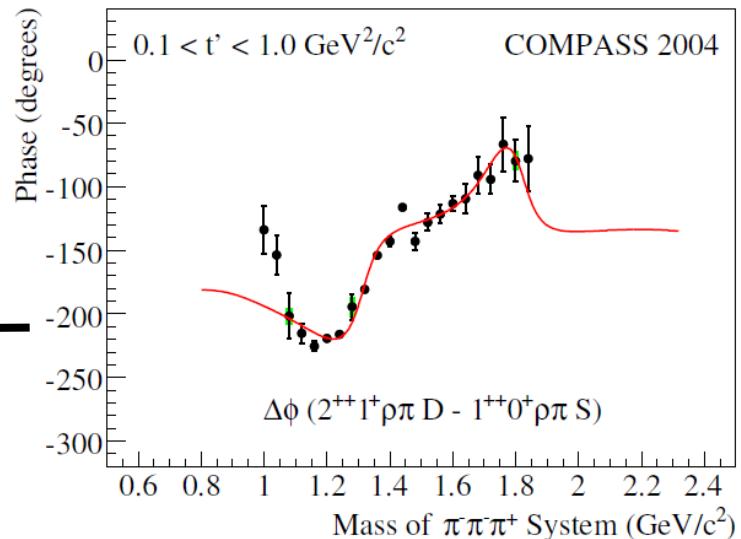
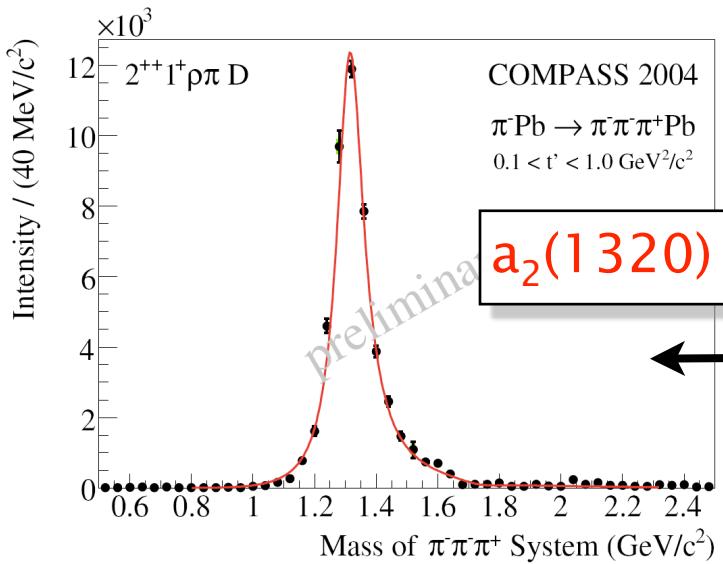
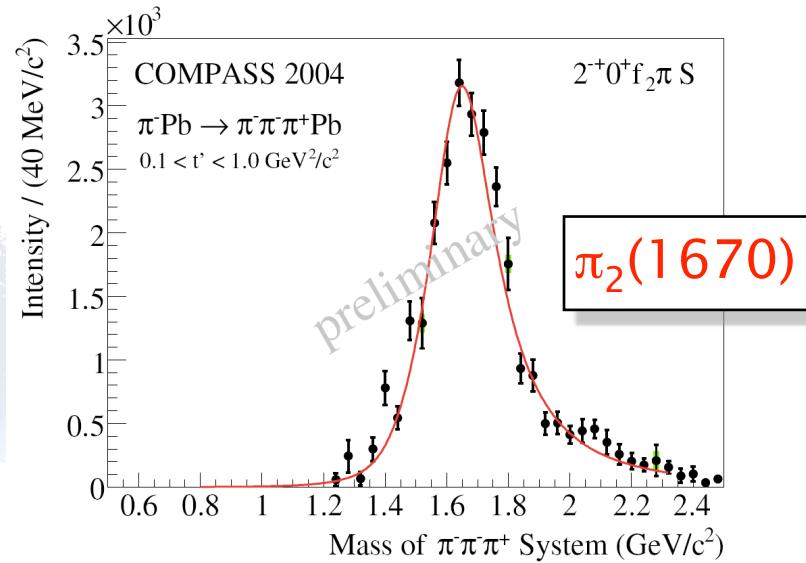
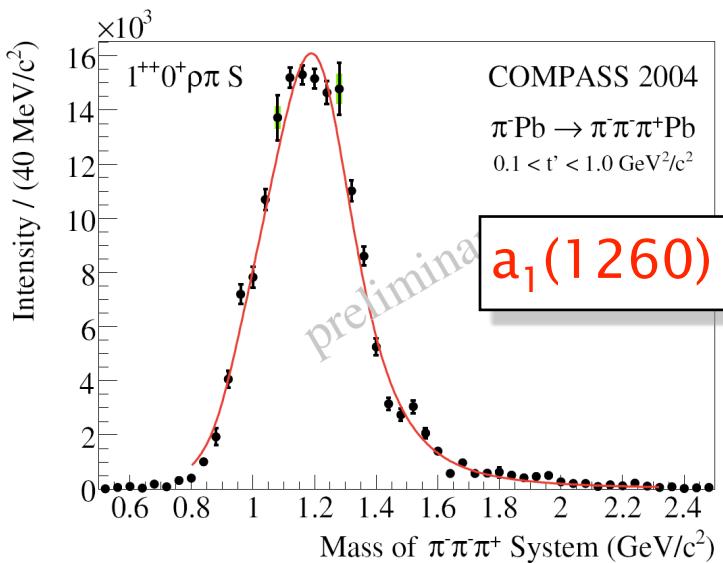
# Wave Set for the Fit

$J^{PC} M^\epsilon$	$L$	Isobar $\pi$	Cut [GeV]	$J^{PC} M^\epsilon$	$L$	Isobar $\pi$	Cut [GeV]
$0^{-+0^+}$	$S$	$f_0\pi$	1.40	$2^{++1^+}$	$P$	$f_2\pi$	1.50
$0^{-+0^+}$	$S$	$(\pi\pi)_s\pi$	-	$2^{++1^+}$	$D$	$\rho\pi$	-
$0^{-+0^+}$	$P$	$\rho\pi$	-	$3^{++0^+}$	$S$	$\rho_3\pi$	1.50
$1^{-+1^+}$	$P$	$\rho\pi$	-	$3^{++0^+}$	$P$	$f_2\pi$	1.20
$1^{++0^+}$	$S$	$\rho\pi$	-	$3^{++0^+}$	$D$	$\rho\pi$	1.50
$1^{++0^+}$	$P$	$f_2\pi$	1.20	$3^{++1^+}$	$S$	$\rho_3\pi$	1.50
$1^{++0^+}$	$P$	$(\pi\pi)_s\pi$	0.84	$3^{++1^+}$	$P$	$f_2\pi$	1.20
$1^{++0^+}$	$D$	$\rho\pi$	1.30	$3^{++1^+}$	$D$	$\rho\pi$	1.50
$1^{++1^+}$	$S$	$\rho\pi$	-	$4^{-+0^+}$	$F$	$\rho\pi$	1.20
$1^{++1^+}$	$P$	$f_2\pi$	1.40	$4^{-+1^+}$	$F$	$\rho\pi$	1.20
$1^{++1^+}$	$P$	$(\pi\pi)_s\pi$	1.40	$4^{++1^+}$	$F$	$f_2\pi$	1.60
$1^{++1^+}$	$D$	$\rho\pi$	1.40	$4^{++1^+}$	$G$	$\rho\pi$	1.64
$2^{-+0^+}$	$S$	$f_2\pi$	1.20	$1^{-+0^-}$	$P$	$\rho\pi$	-
$2^{-+0^+}$	$P$	$\rho\pi$	0.80	$1^{-+1^-}$	$P$	$\rho\pi$	-
$2^{-+0^+}$	$D$	$f_2\pi$	1.50	$1^{++1^-}$	$S$	$\rho\pi$	-
$2^{-+0^+}$	$D$	$(\pi\pi)_s\pi$	0.80	$2^{-+1^-}$	$S$	$f_2\pi$	1.20
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$2^{-+1^+}$	$D$	$f_2\pi$	1.50				
$2^{-+1^+}$	$D$	$(\pi\pi)_s\pi$	1.20				
$2^{-+1^+}$	$F$	$\rho\pi$	1.20				
FLAT							

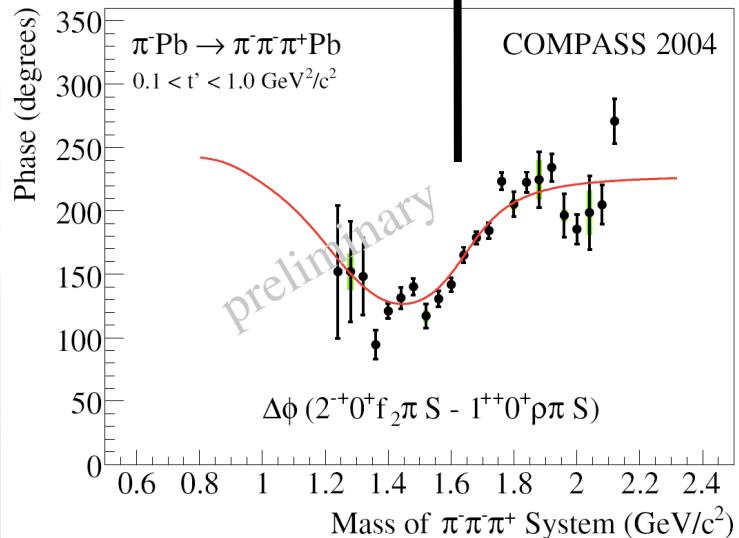
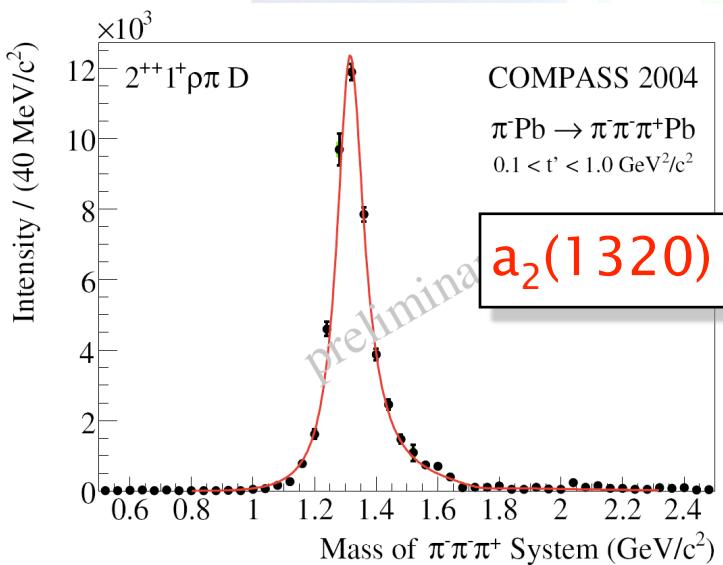
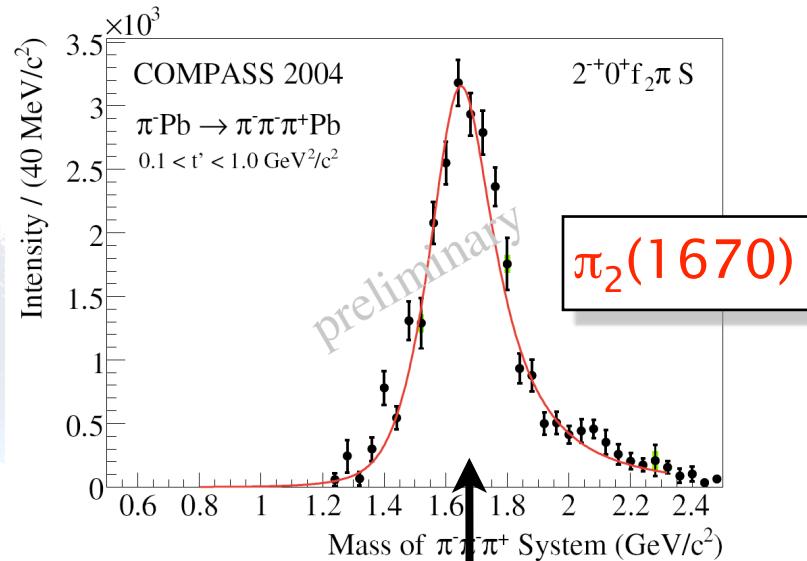
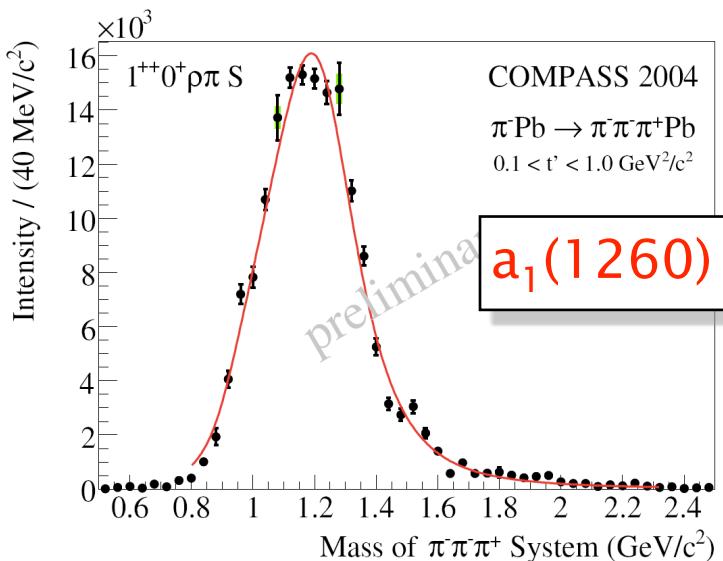
# Most Prominent Partial Waves

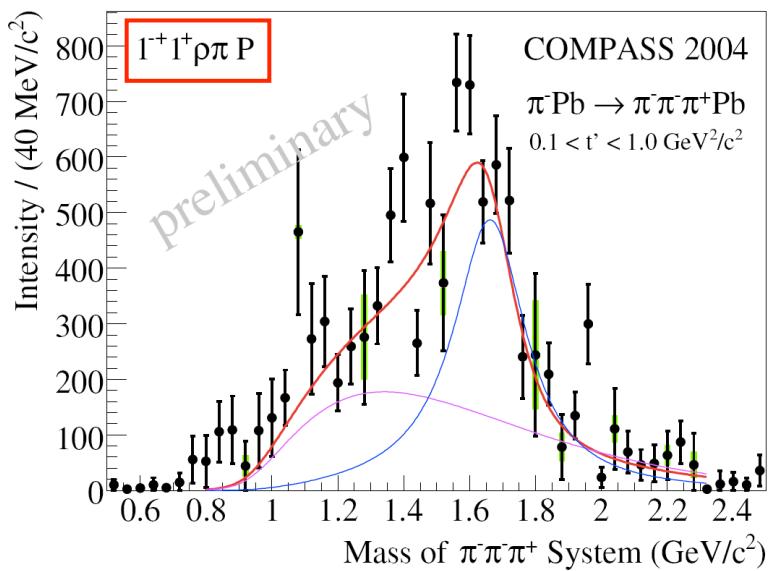


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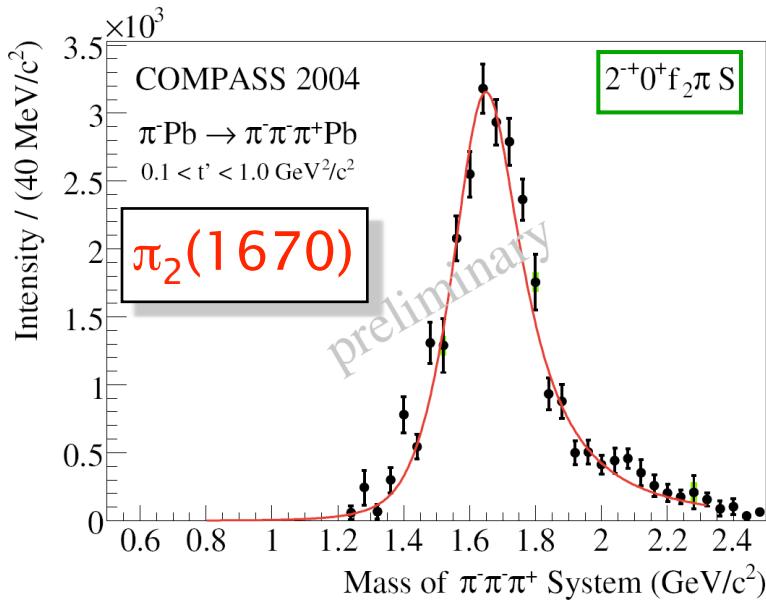
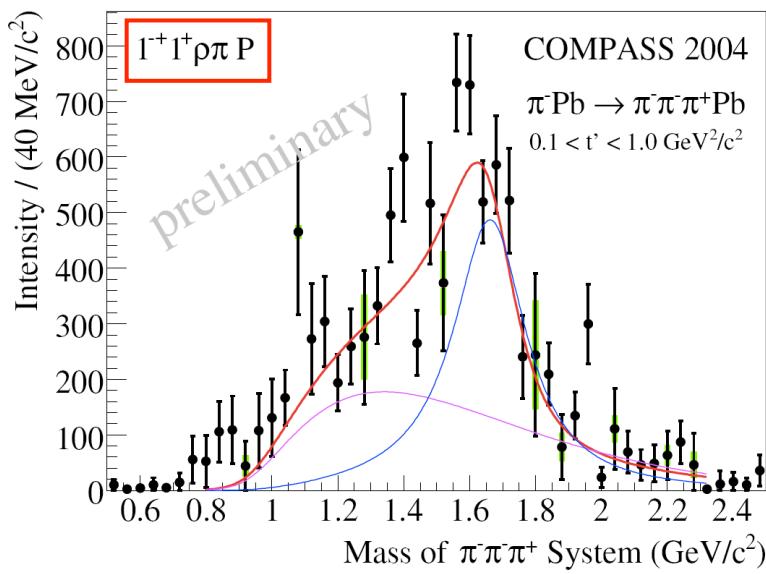


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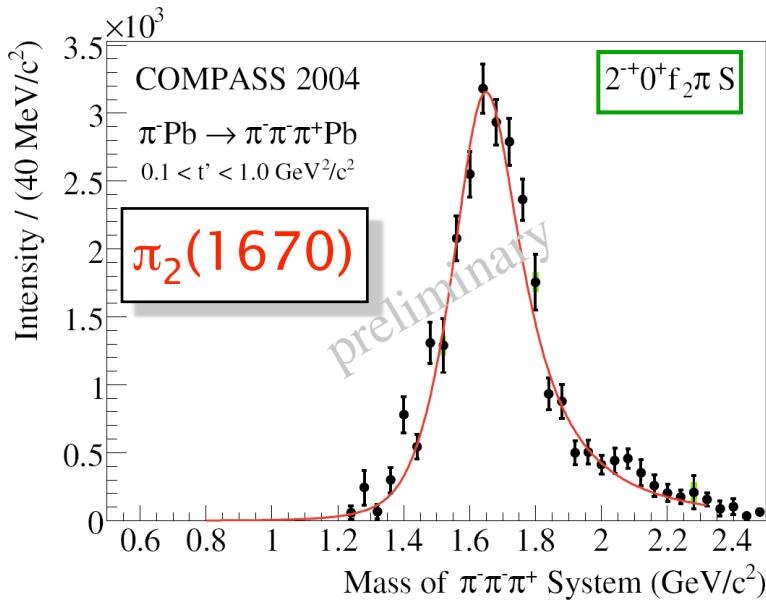
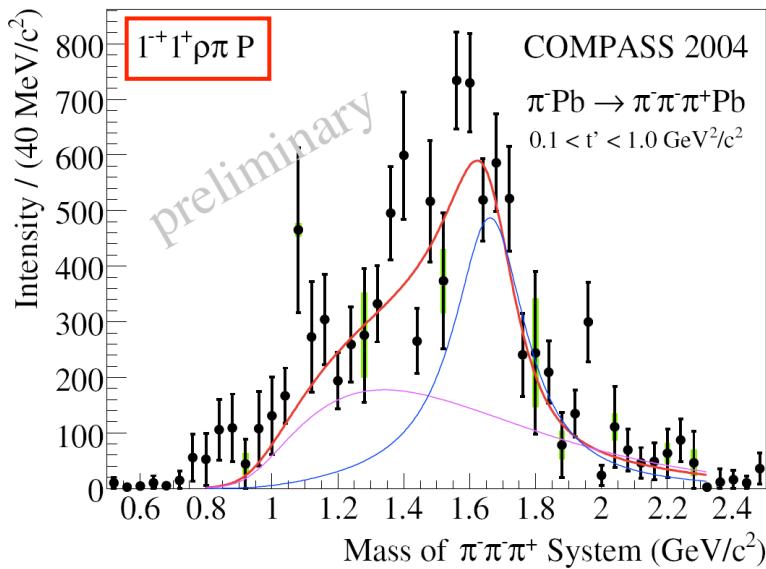




[PRL 104 241803 \(2010\)](#)



PRL 104 241803 (2010)



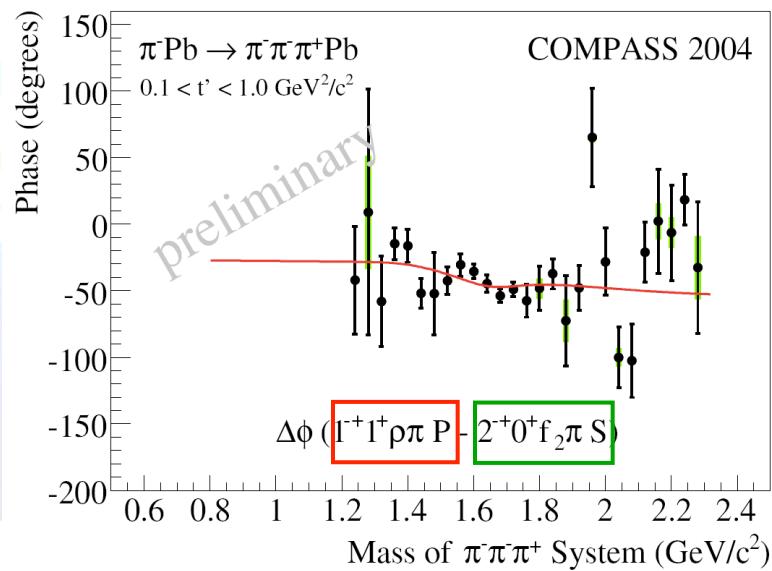
- BW parameter for  $\pi_1(1600)$

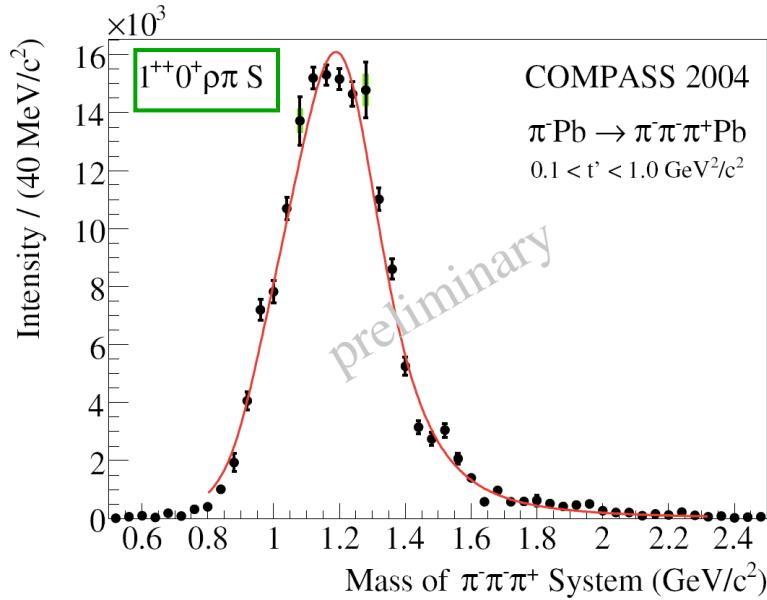
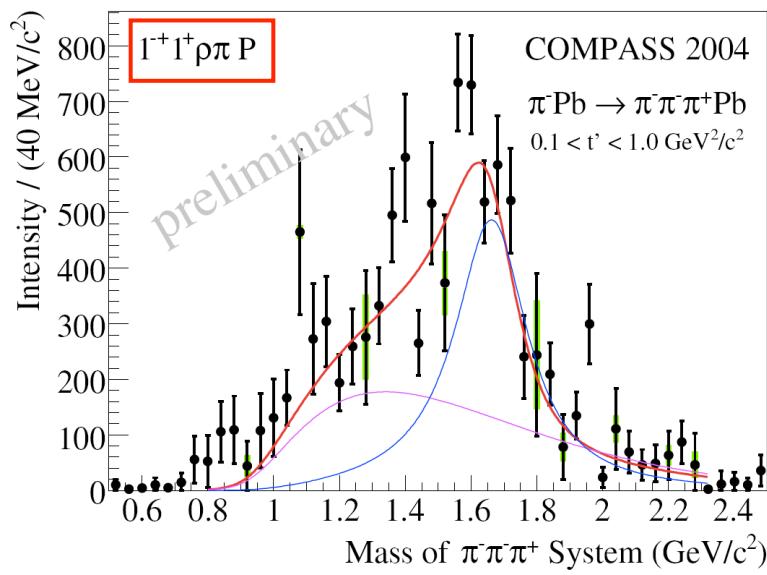
$$M = (1.660 \pm 0.010 {}^{+0.000}_{-0.064}) \text{ GeV}/c^2$$

$$\Gamma = (0.269 \pm 0.021 {}^{+0.042}_{-0.064}) \text{ GeV}/c^2$$

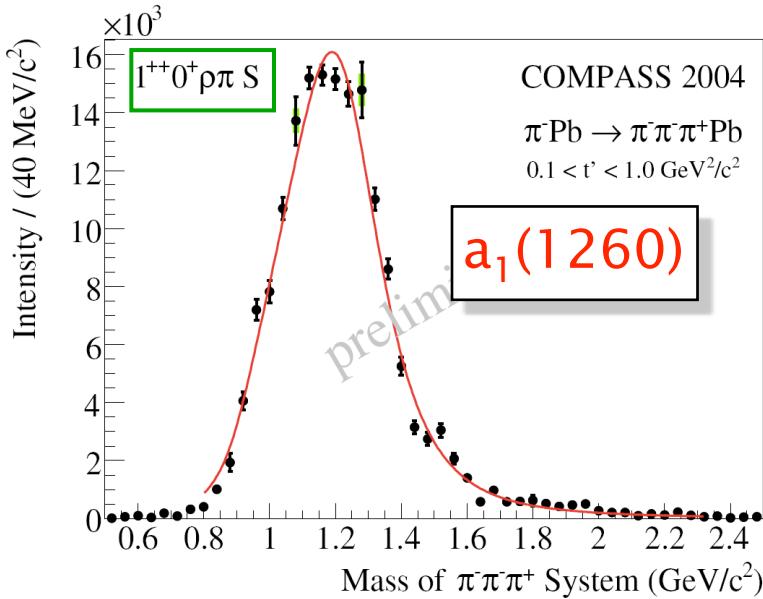
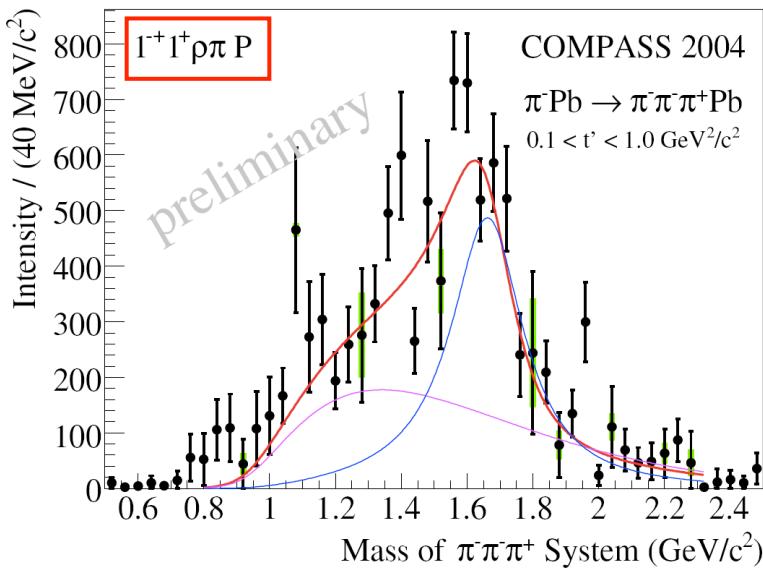
- Negligible ‘miss-ID’

[PRL 104, 241803 \(2010\)](#)





[PRL 104 241803 \(2010\)](#)



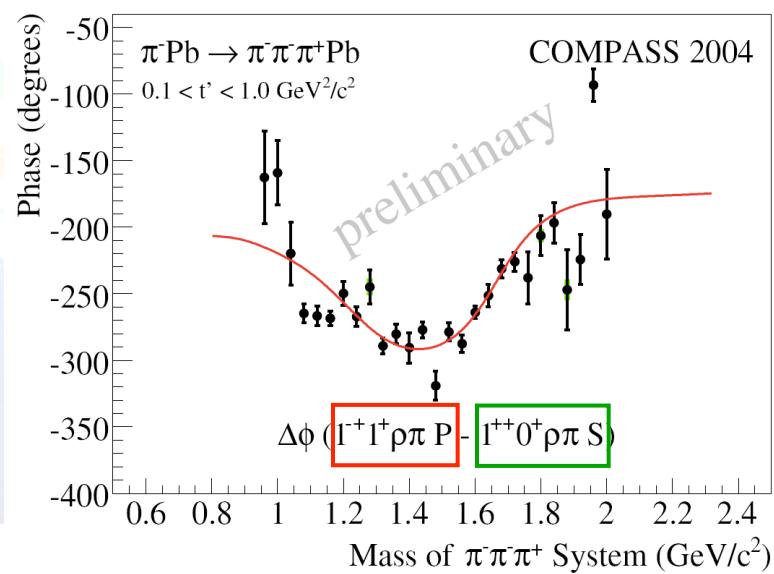
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PRL 104, 241803 (2010)





# Nuclear Effect - $\pi^-\pi^-\pi^+$

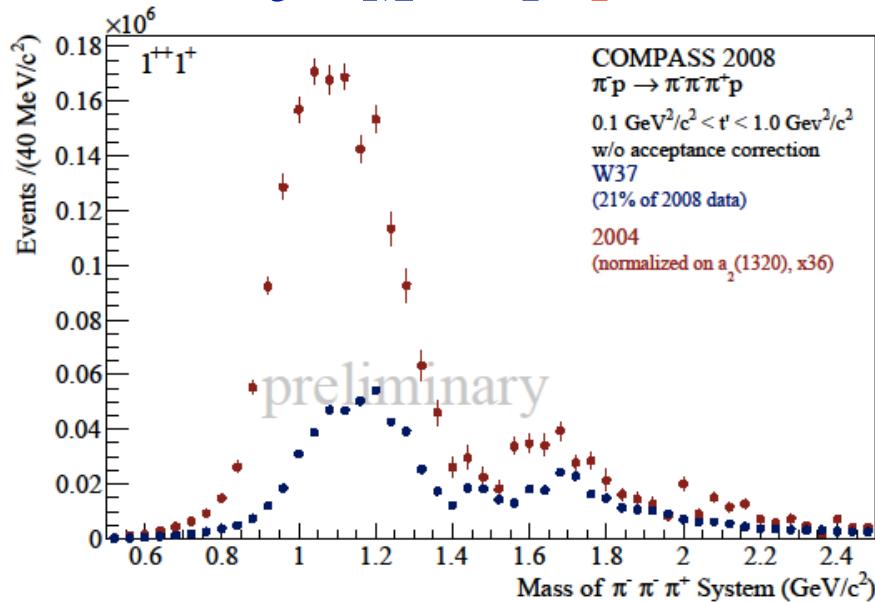


- Compare intensities of  $a_1(1260)$  and  $\pi_2(1670)$  from **Pb** and **H<sub>2</sub>** targets
- Normalise to intensity of  $a_2(1320)$  ( $J^{PC}M^\epsilon = 2^{++}1^+$ )
- Pb target: enhancement of spin projection M=1  
suppression of spin projection M=0
- Total intensity (both spin projections) roughly the same

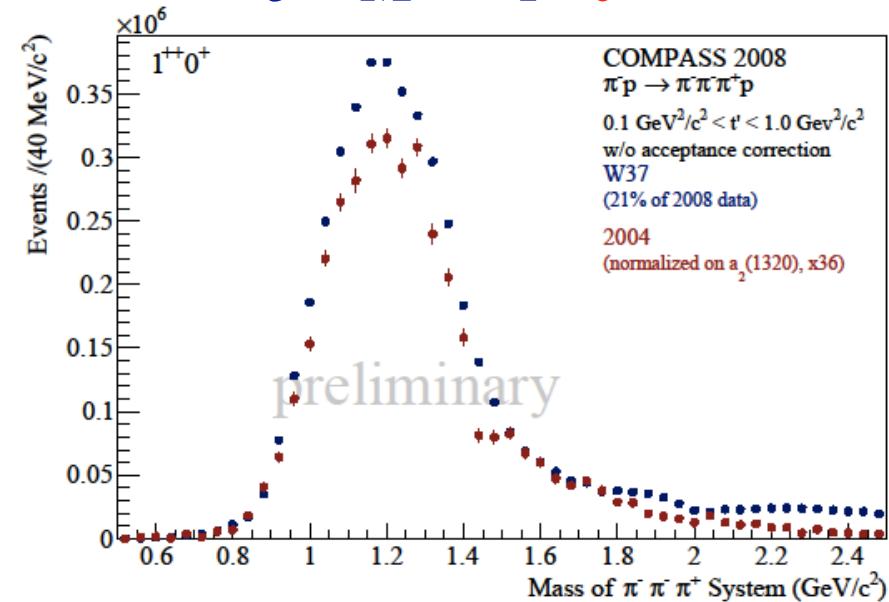
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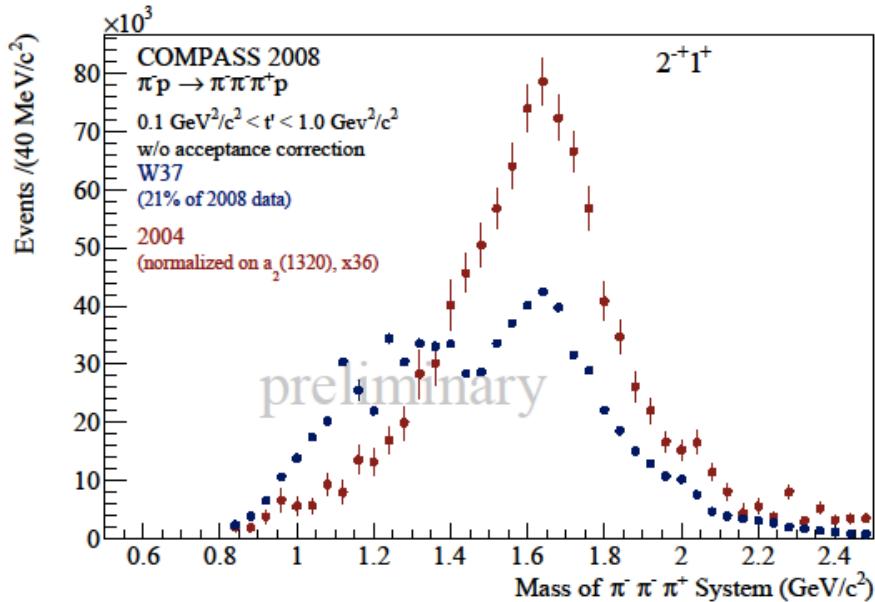
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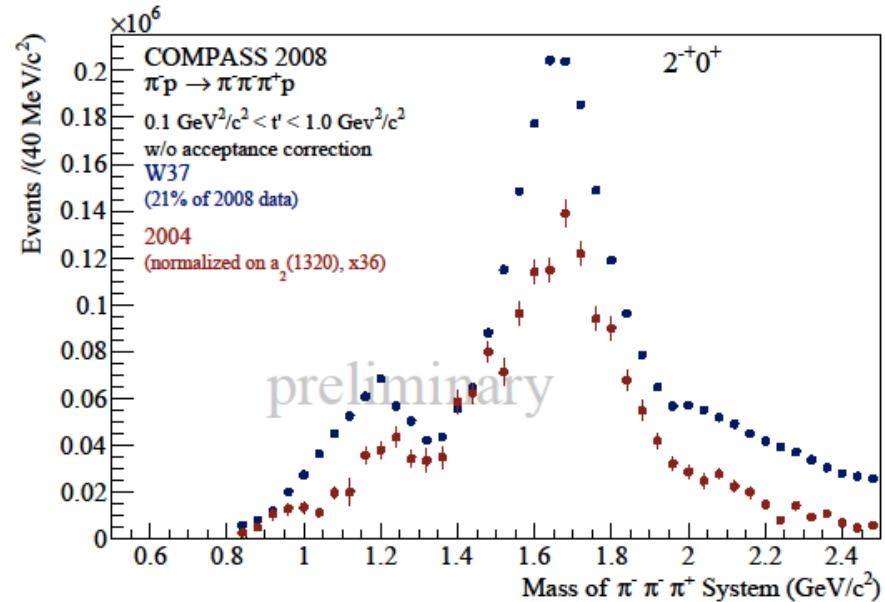
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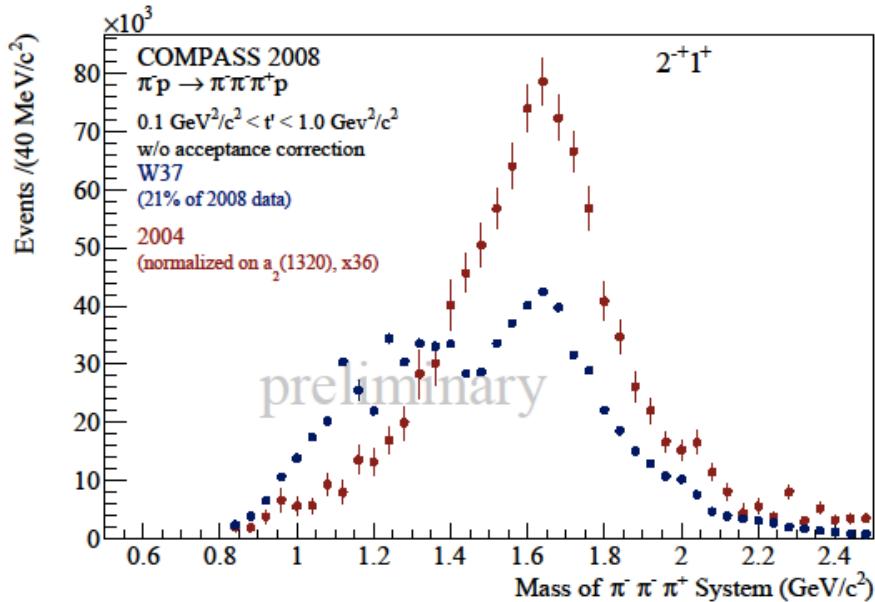
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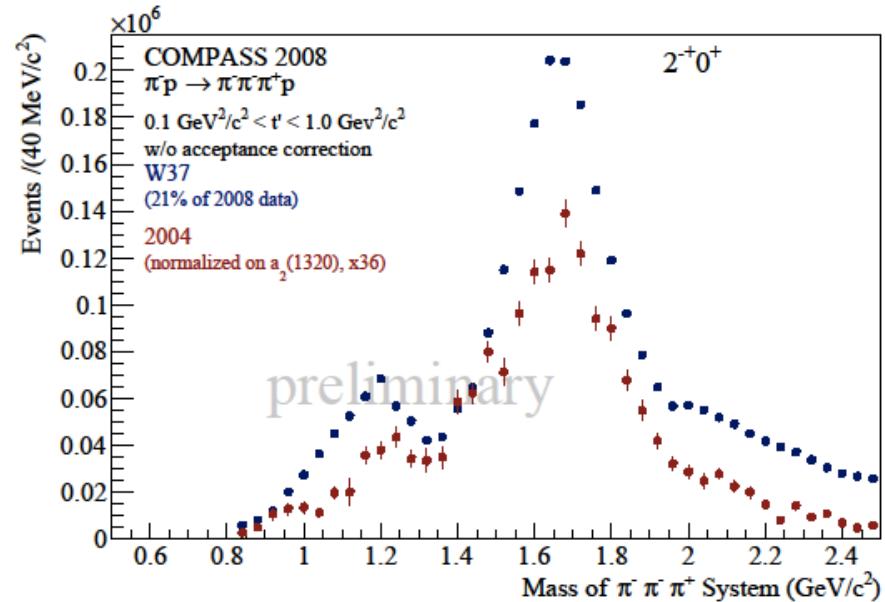
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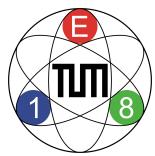
$$\left[ \frac{\text{Intensity}(M=1)}{\text{Intensity}(M=0)} \right]_{Pb} > \left[ \frac{\text{Intensity}(M=1)}{\text{Intensity}(M=0)} \right]_{H_2}$$

$$J^{PC} M^\varepsilon = 2^{-+} 1^+$$



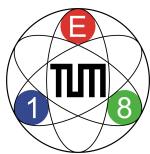
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# Data with Proton Beam





# Data with Proton Beam



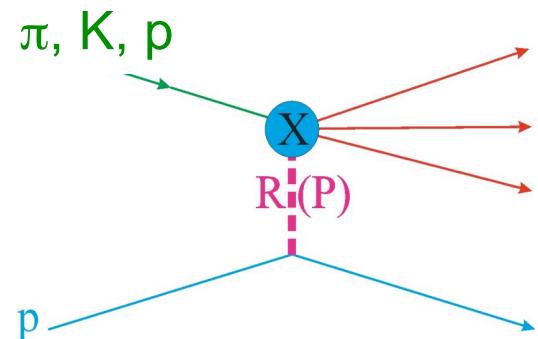
- Beam: 190 GeV/c, 71.5% p, 25.5%  $\pi$ , 3.0% K
- CEDARs tagging protons
- Trigger: Recoil proton
- ~10% of total 2008/2009 statistics

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- Baryon spectroscopy:

$$pp \rightarrow p_f \pi^+ \pi^- p_s$$

$$pp \rightarrow p_f K^+ K^- p_s$$

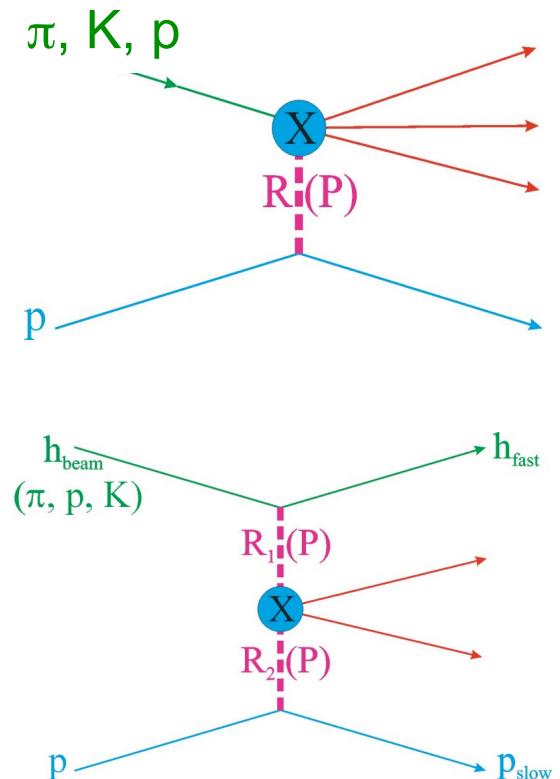


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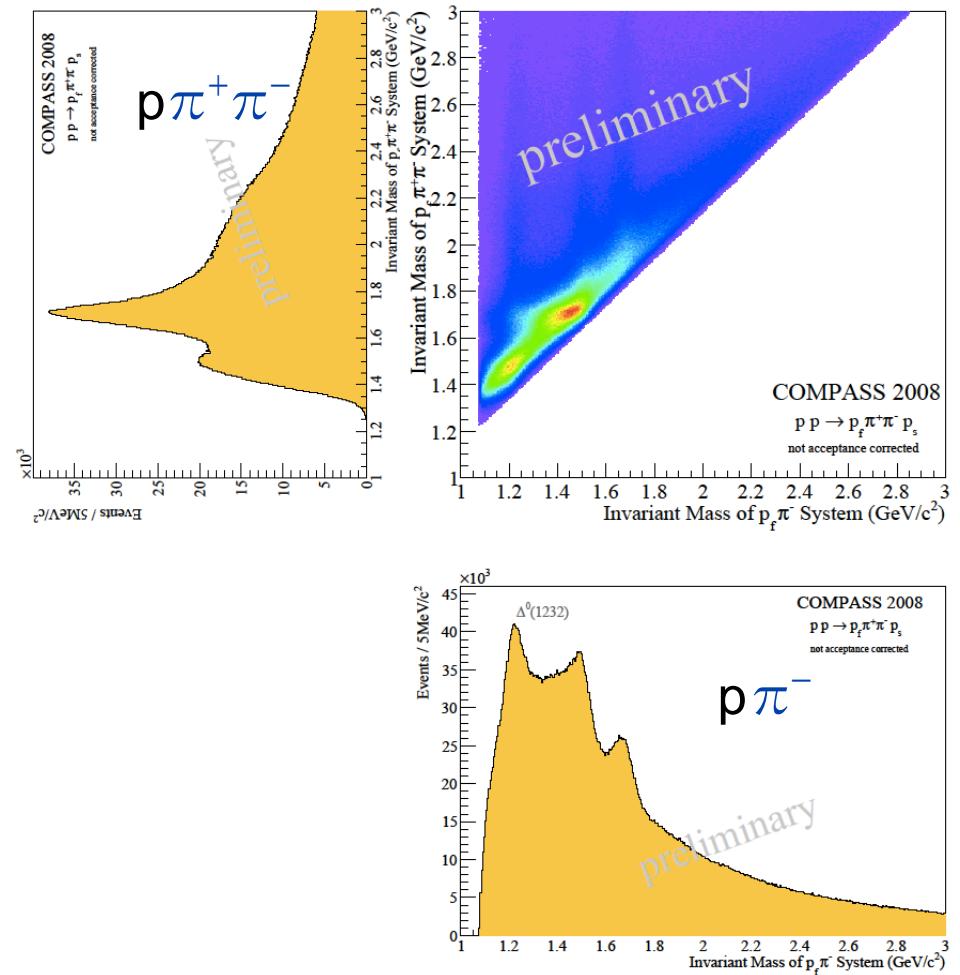


- Central Production

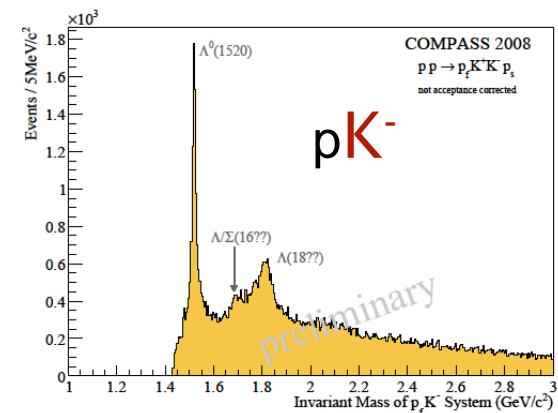
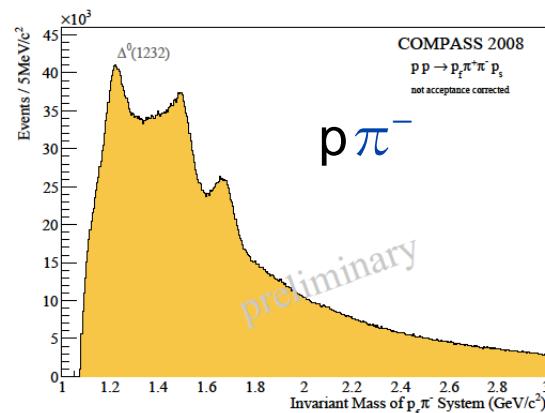
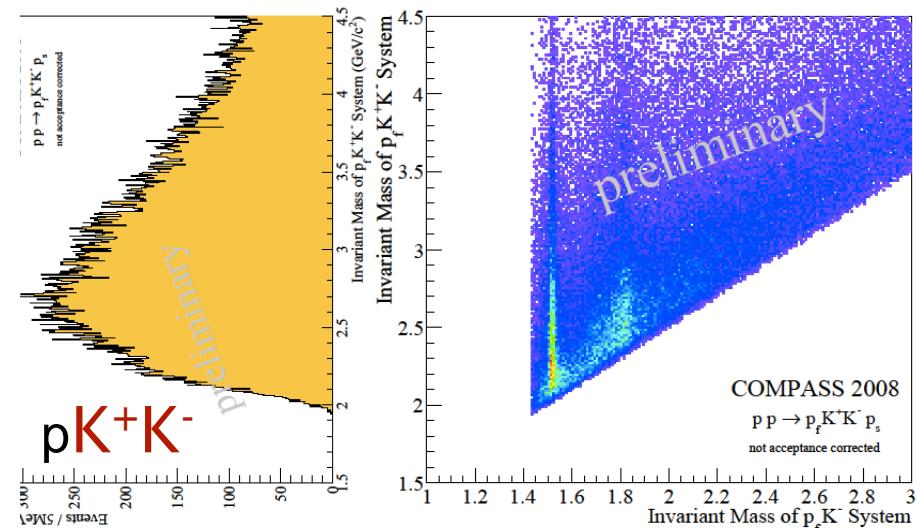
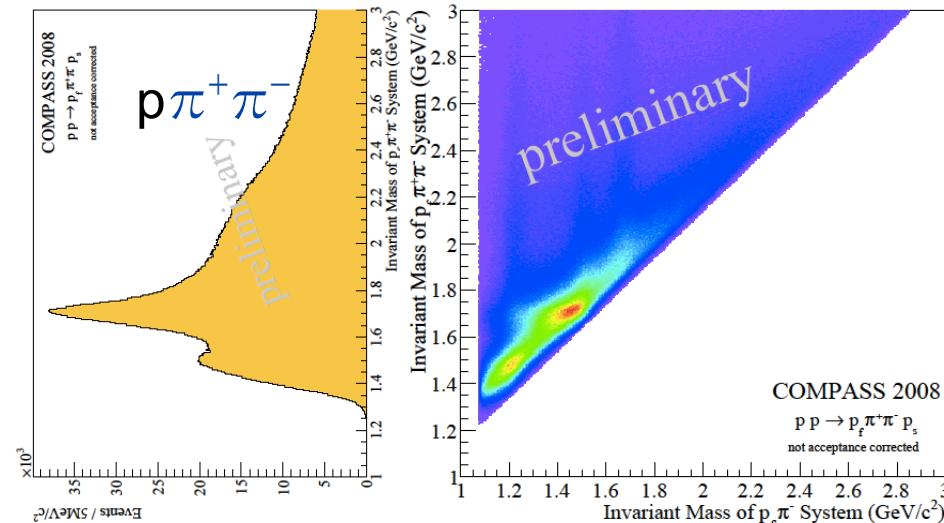


# Baryon Spectroscopy

$$pp \rightarrow p_f \pi^+ \pi^- p_s$$

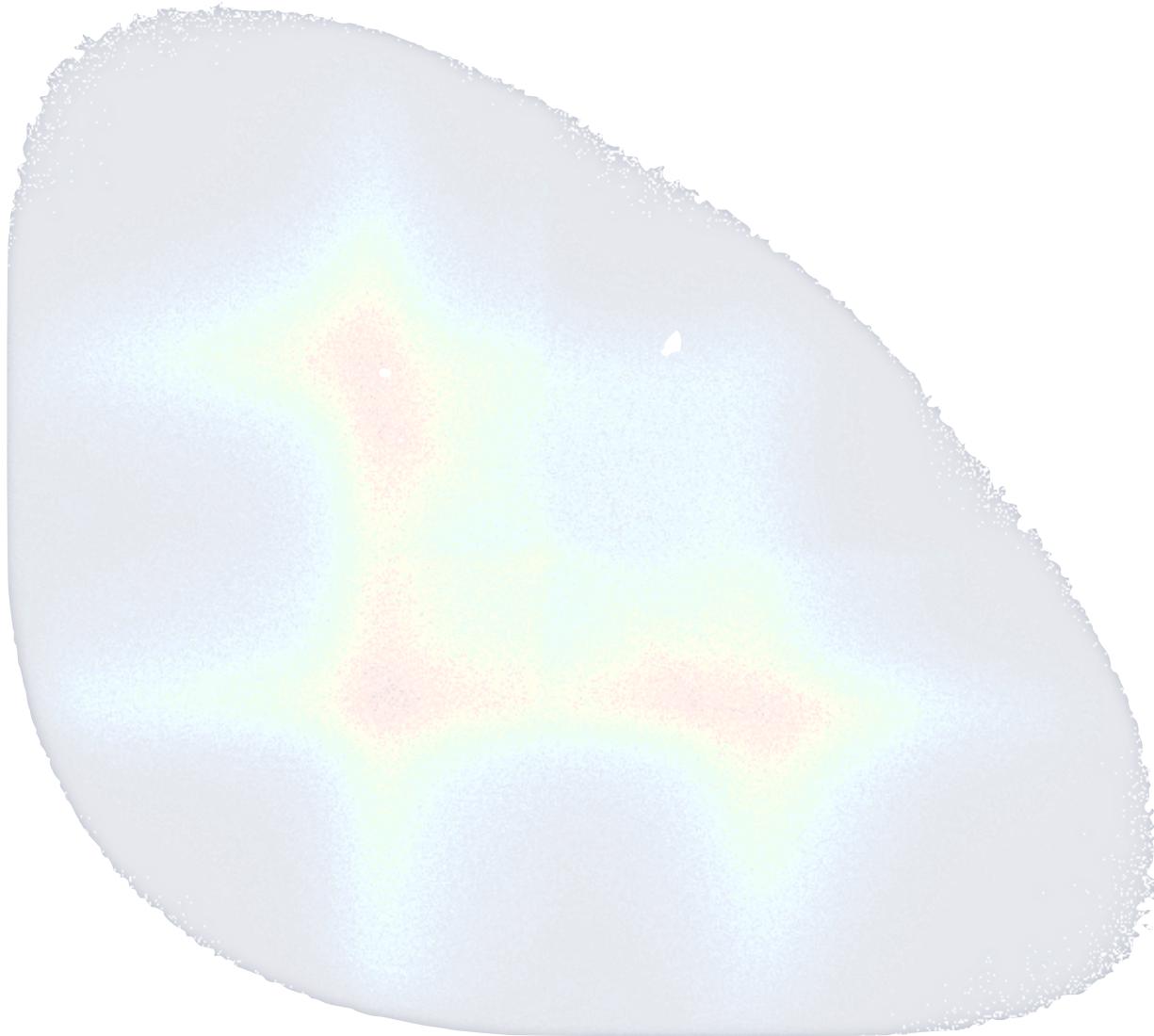


# Baryon Spectroscopy



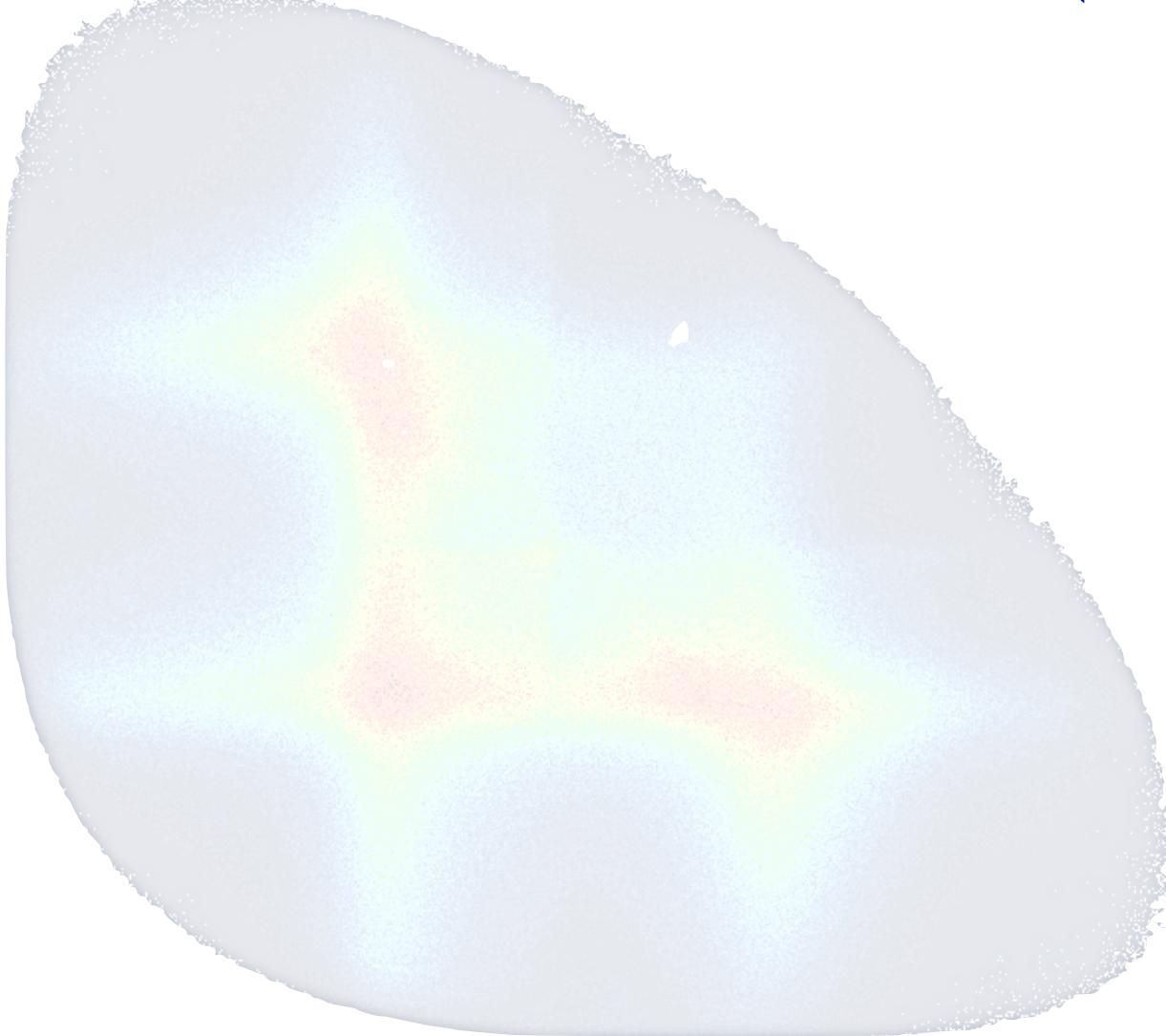
- final states containing charged and neutral particles
- Masses up to  $\sim 3 \text{ GeV}/c^2$  accessible

# Photo-Induced Reactions



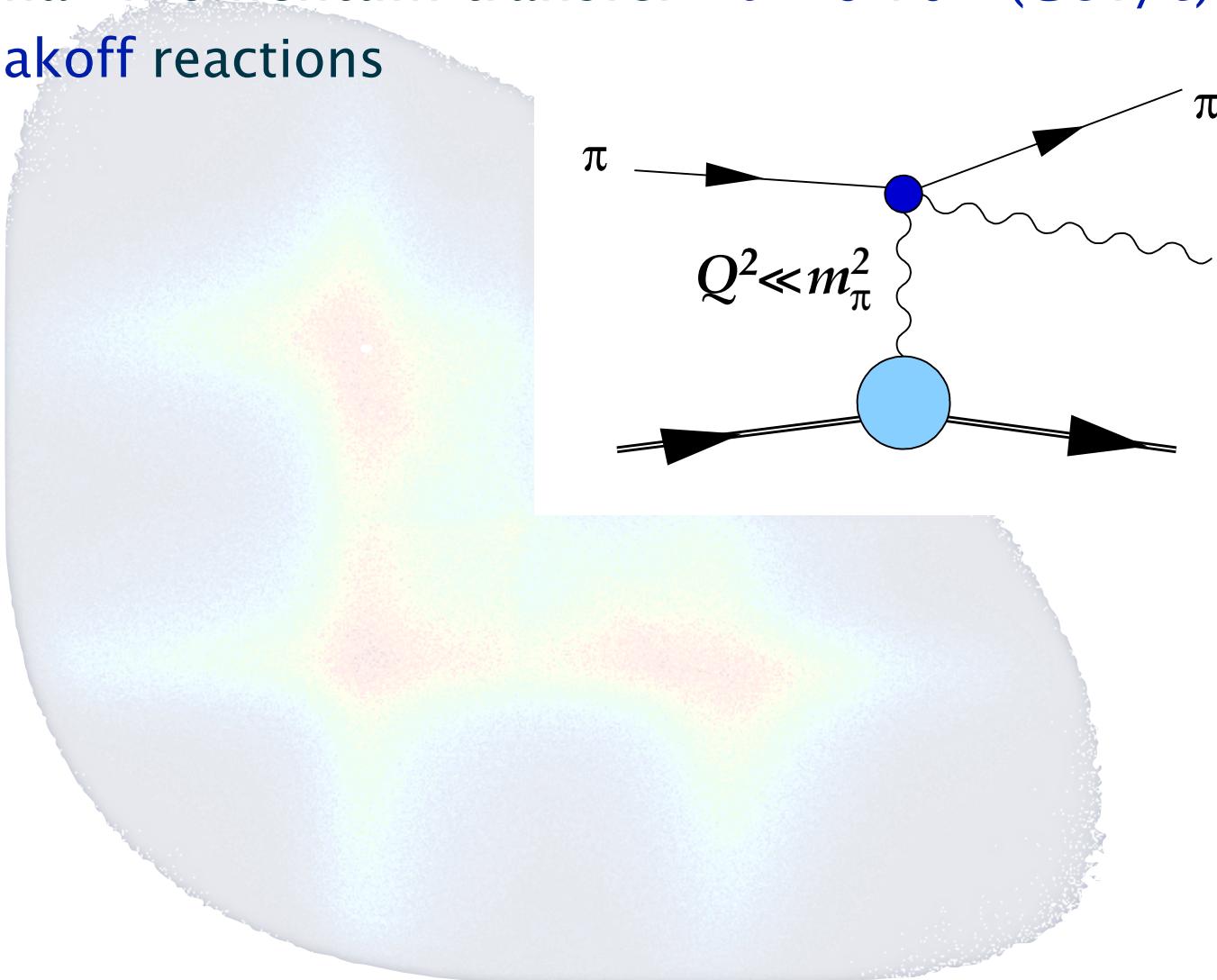
# Photo-Induced Reactions

- Very small momentum transfer -  $t < 6 \cdot 10^{-4} (\text{GeV}/c)^2$



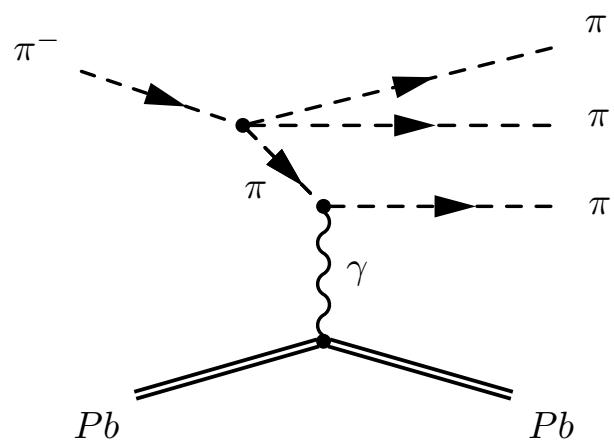
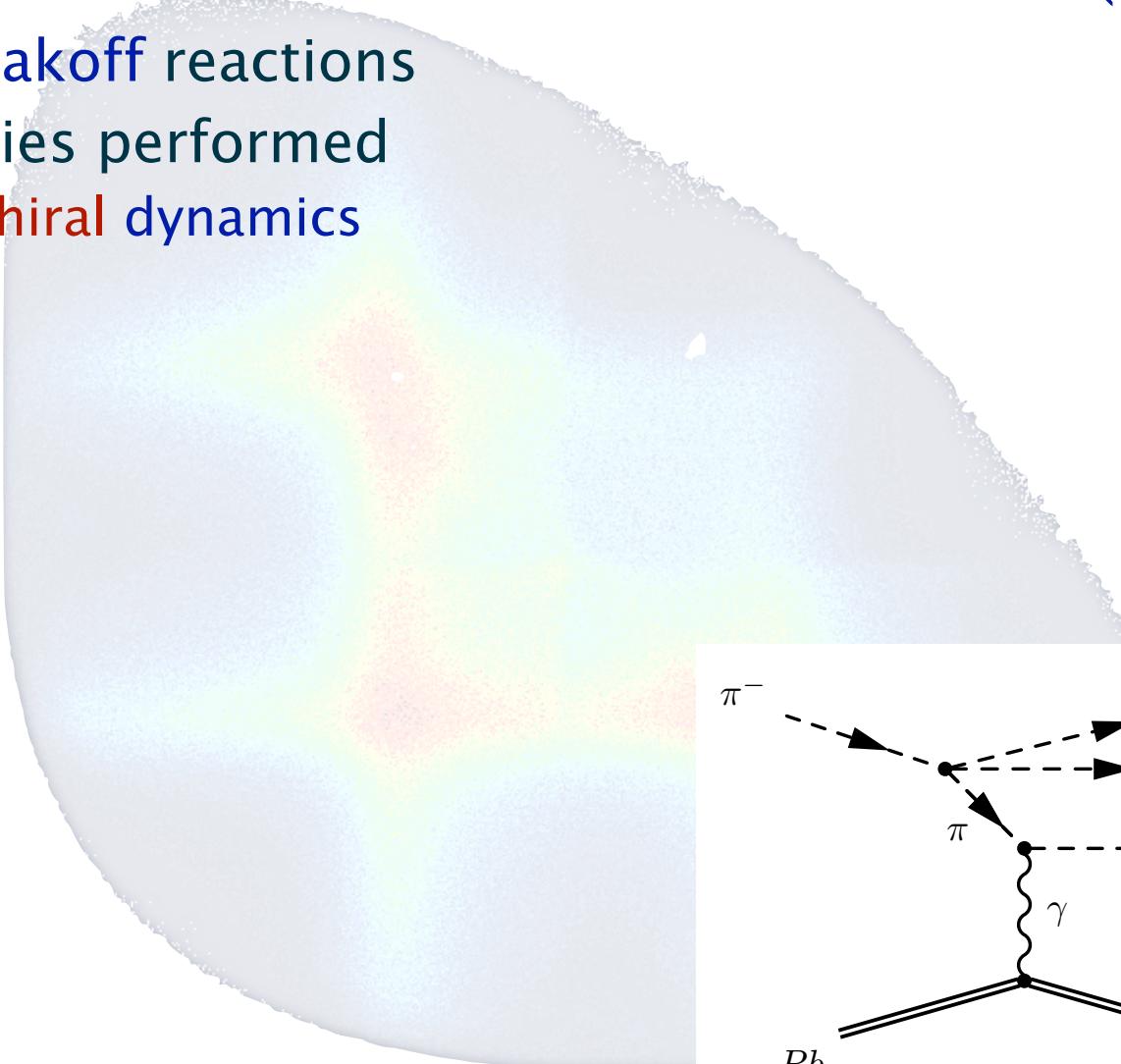
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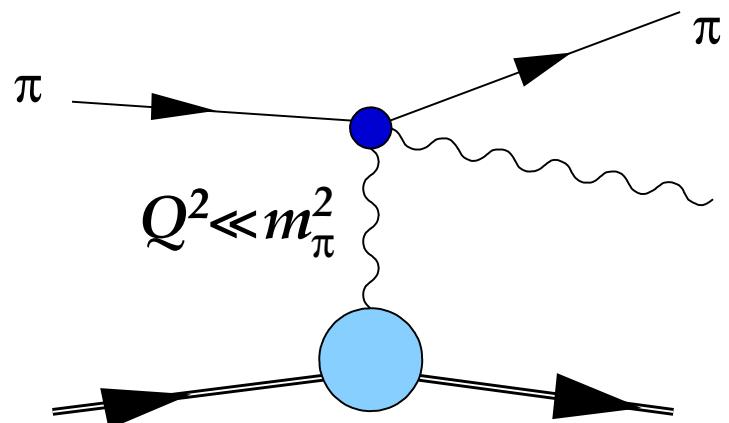
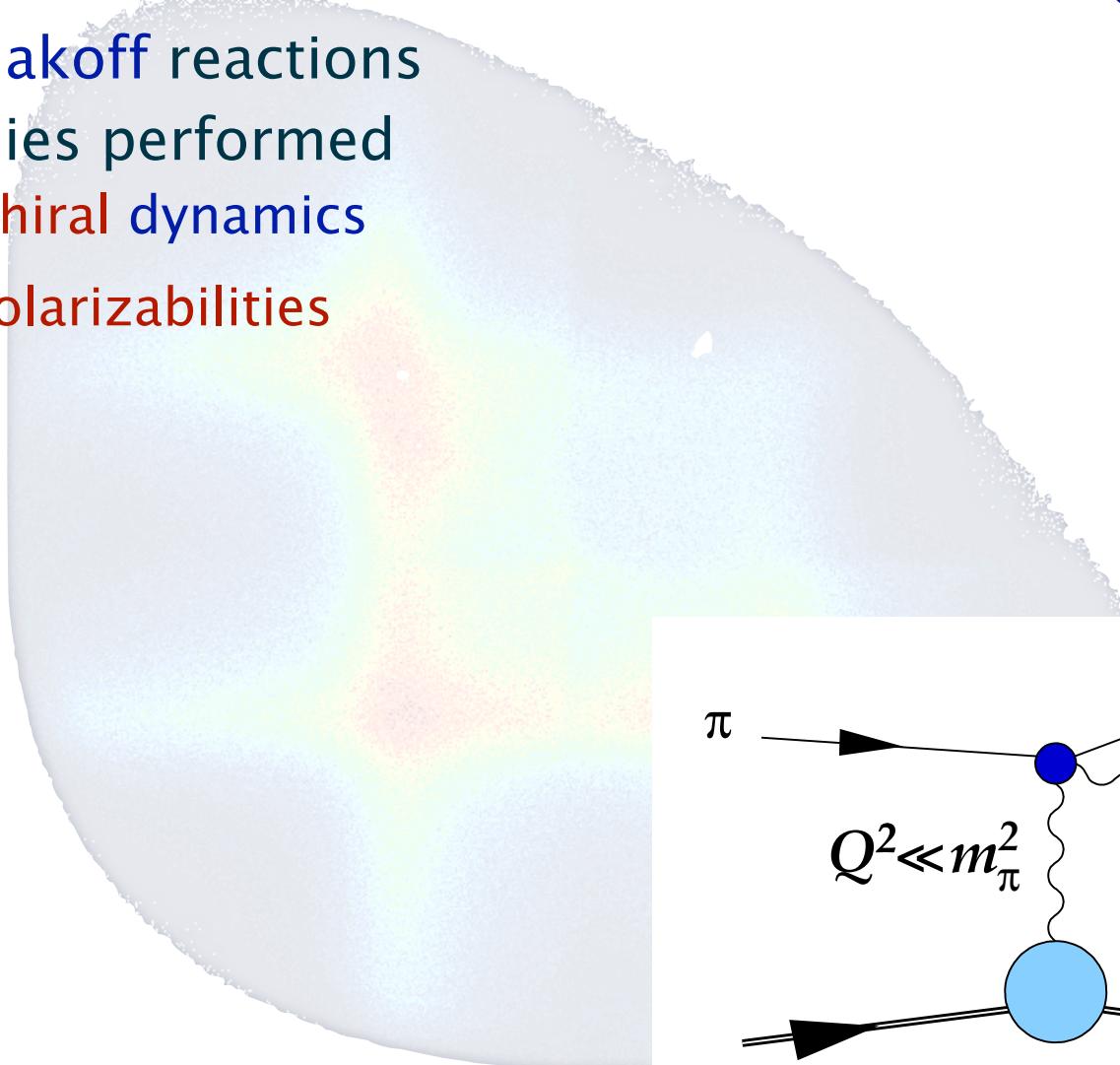
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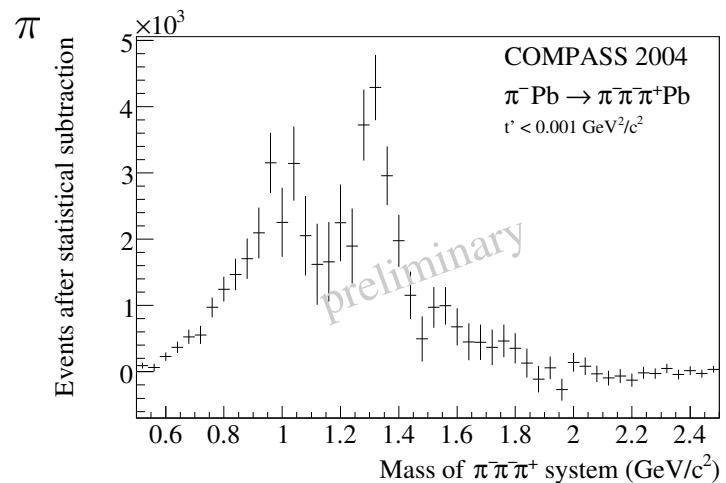
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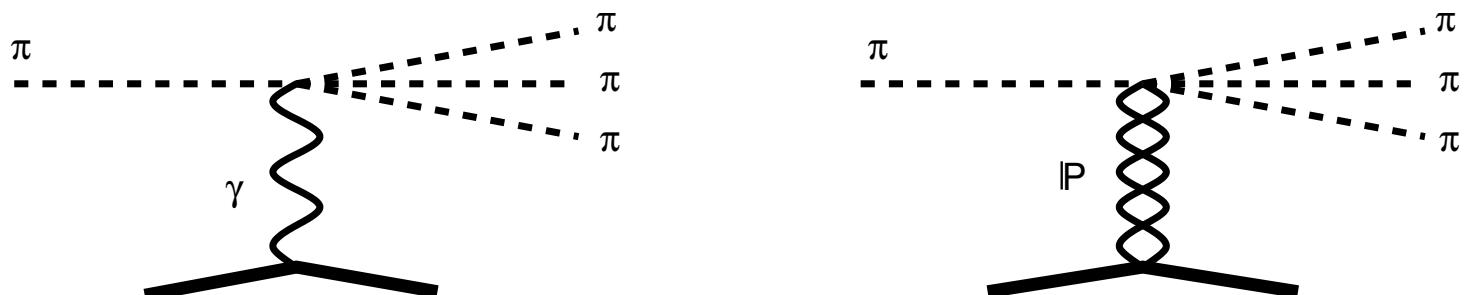
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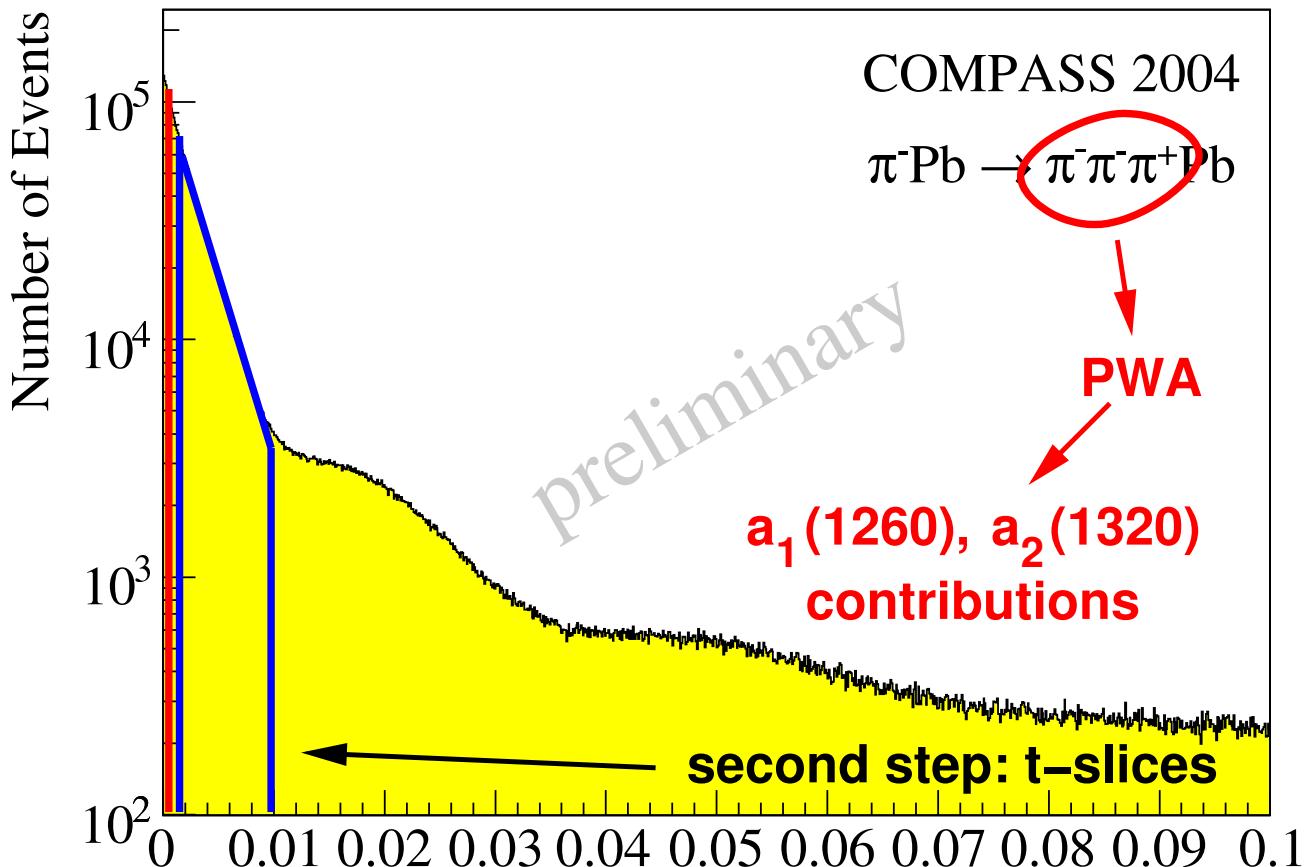
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  - Studies performed
    - Chiral dynamics
    - Polarizabilities
    - Radiative widths
    - Production of resonances



# Photo-Induced Reactions

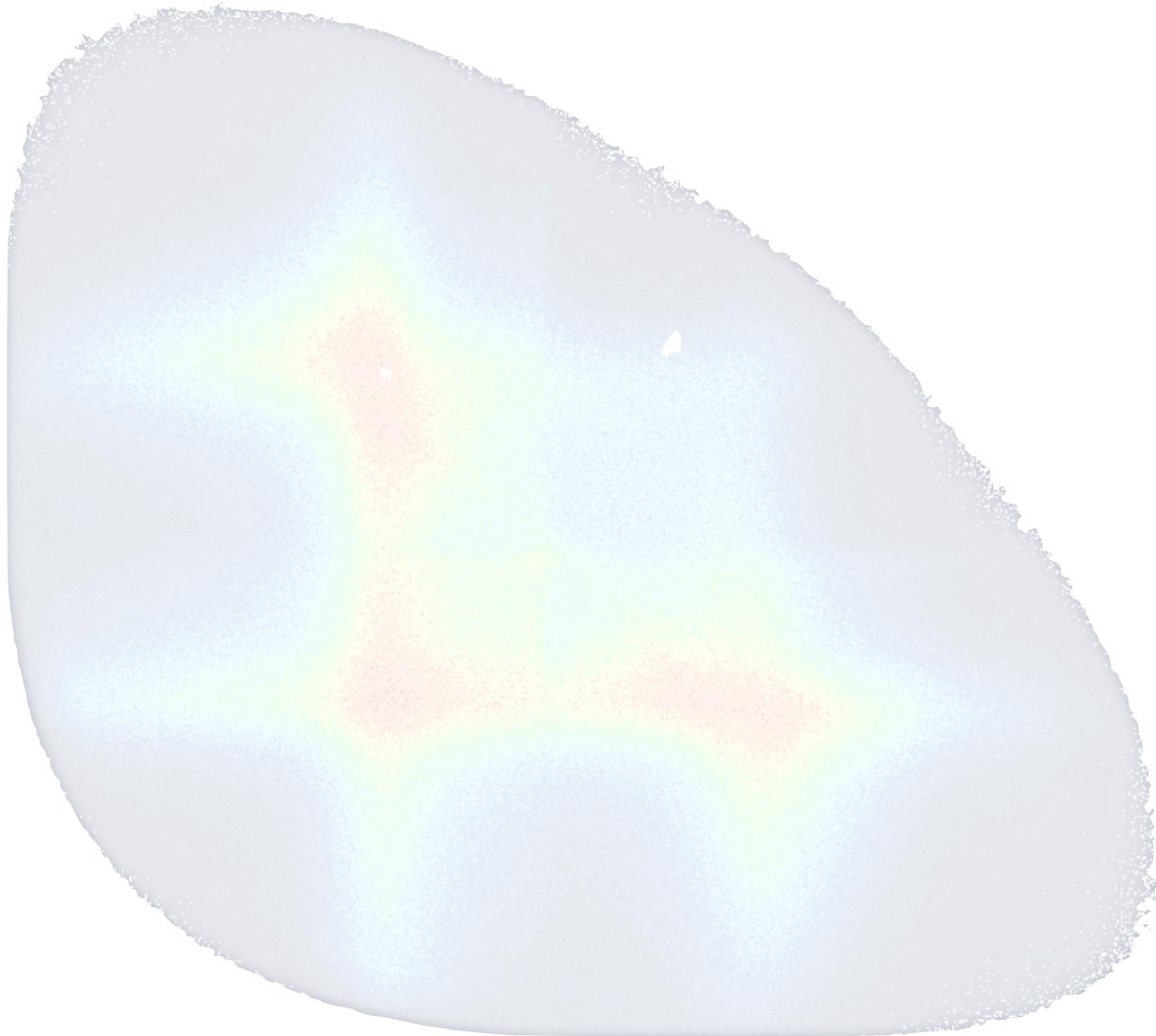
- Very small momentum transfer -  $t < 6 \cdot 10^{-4} (\text{GeV}/c)^2$ 
  - Primakoff reactions
  - Studies performed
    - Chiral dynamics
    - Polarizabilities
    - Radiative widths
    - Production of resonances
    - Nuclear-Coulomb interference





- "Low  $t'$ ":  $10^{-3} (\text{GeV}/c)^2 < t' < 10^{-2} (\text{GeV}/c)^2$   $\sim 2\,000\,000$  events
- "Primakoff region":  $t' < 10^{-3} (\text{GeV}/c)^2$   $\sim 1\,000\,000$  events

# Nuclear-Coulomb Interference



# Nuclear-Coulomb Interference

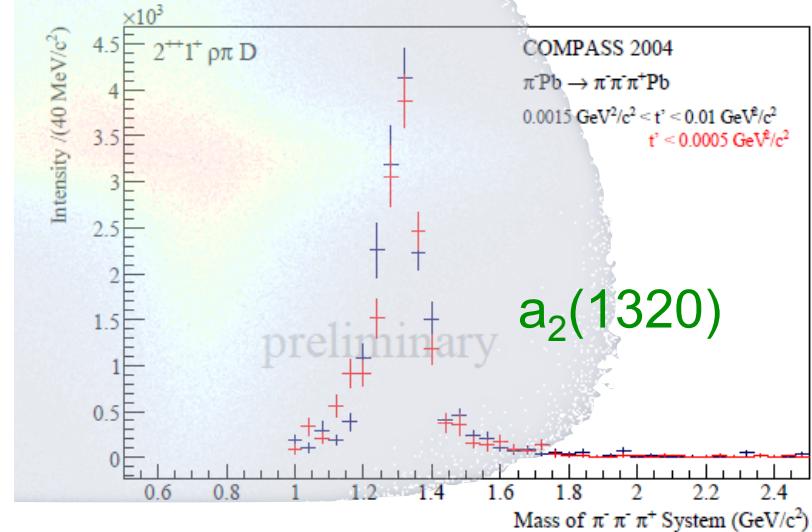
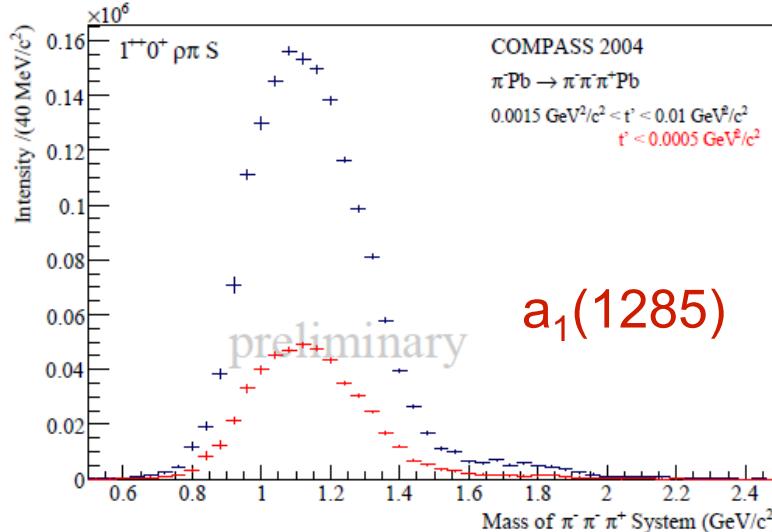
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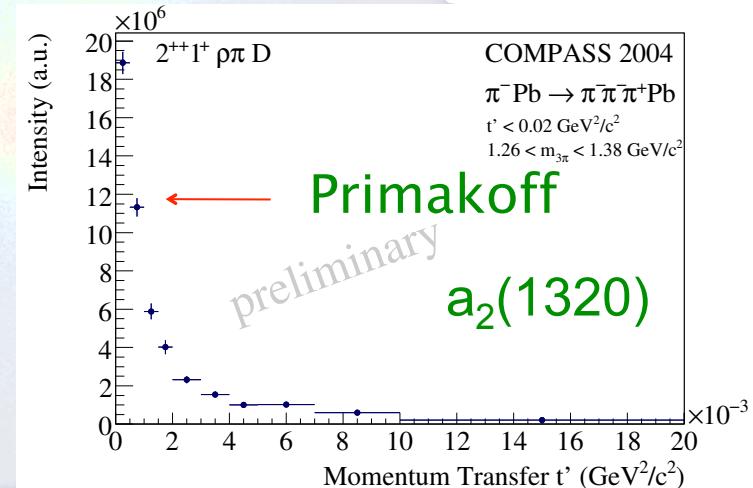
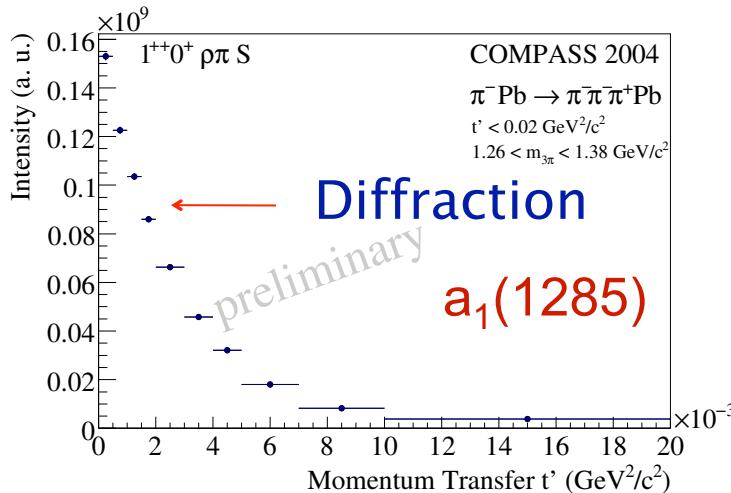
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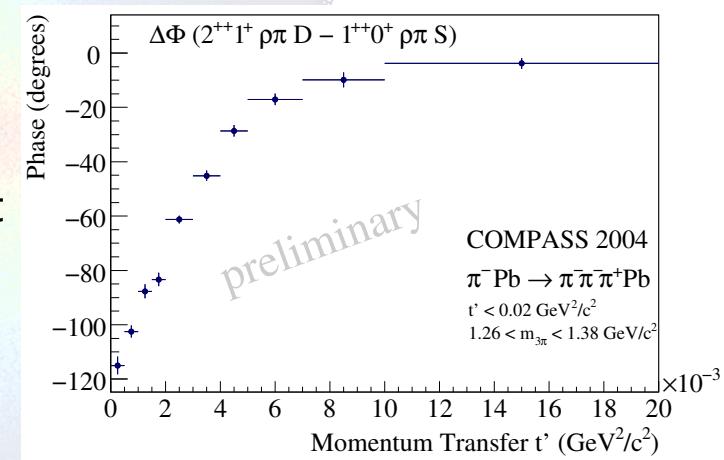
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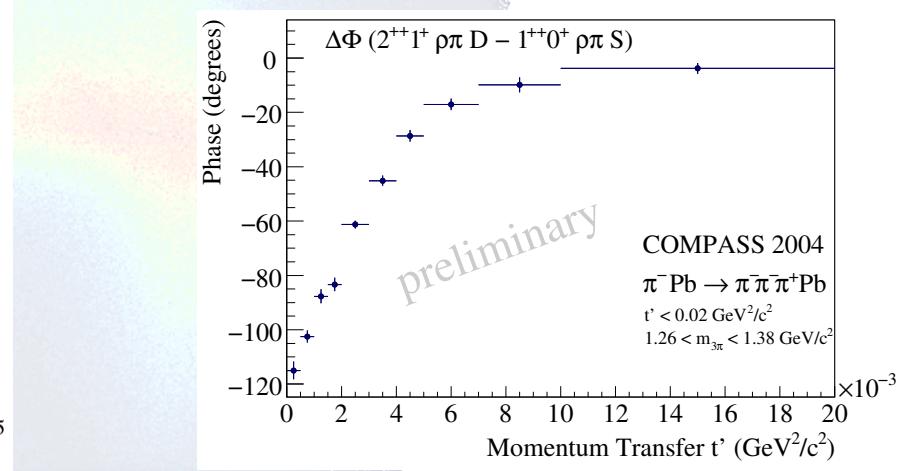
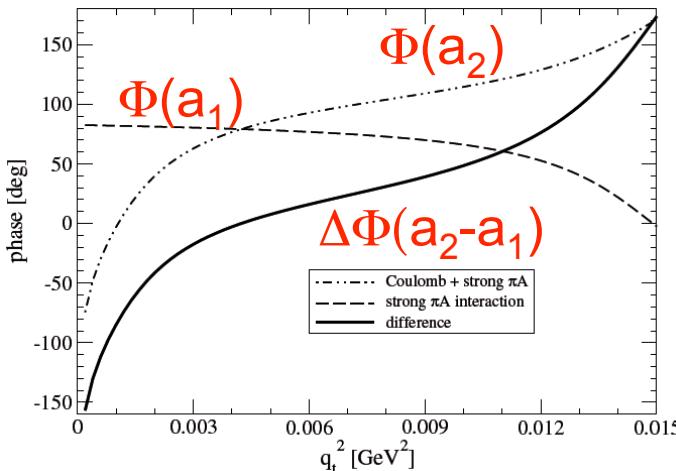
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- $t \sim 0$ :
  - $\Delta\phi$  (Coulomb/diffractive)  $\sim 90^\circ$
  - diffractive amplitude purely imaginary
- for  $t$ :  $0 \rightarrow 10^{-2}$  Diffraction becomes dominant  
Coulomb  $\sim 1/t^2$
- Exchange processes well identifiable

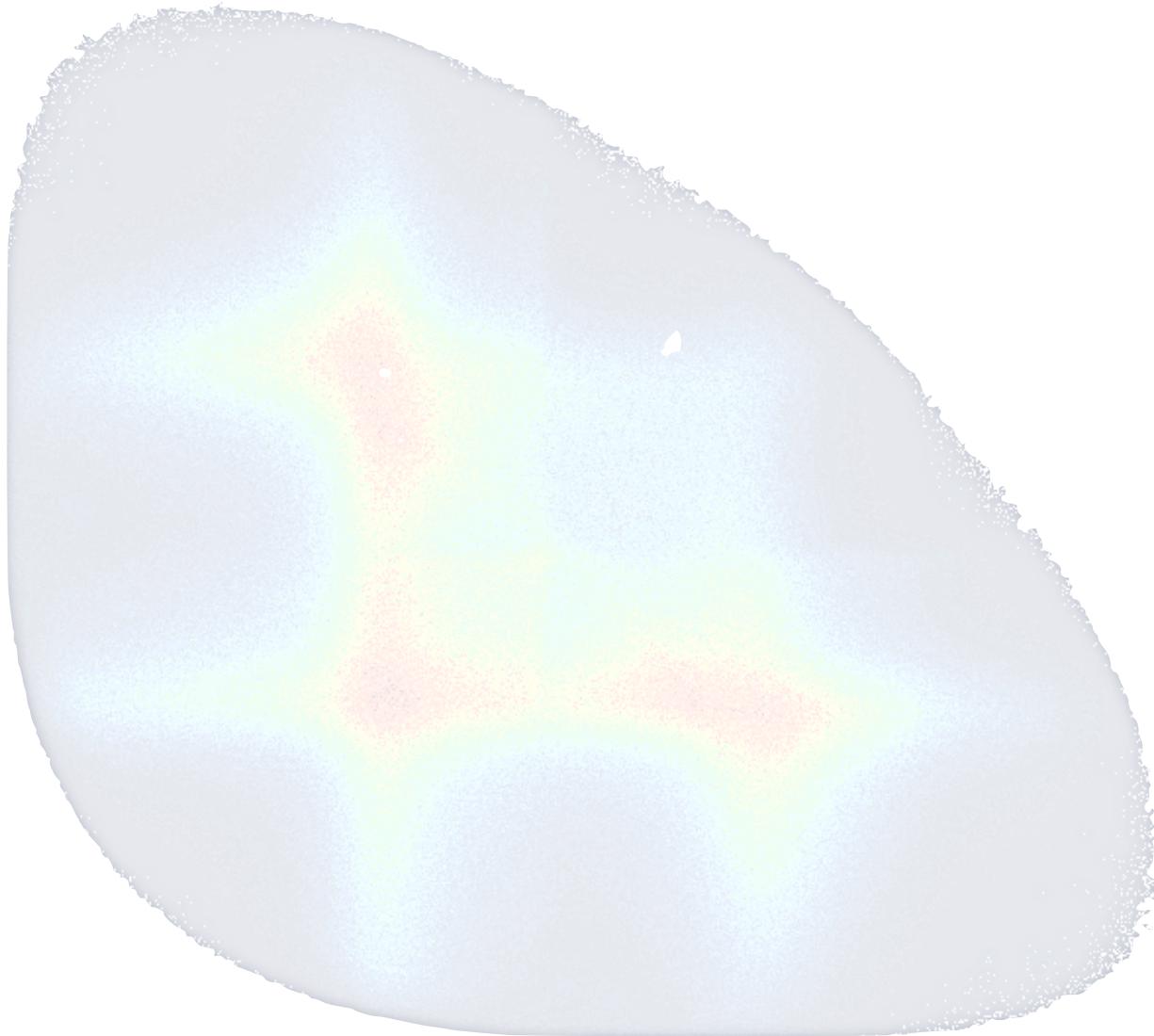


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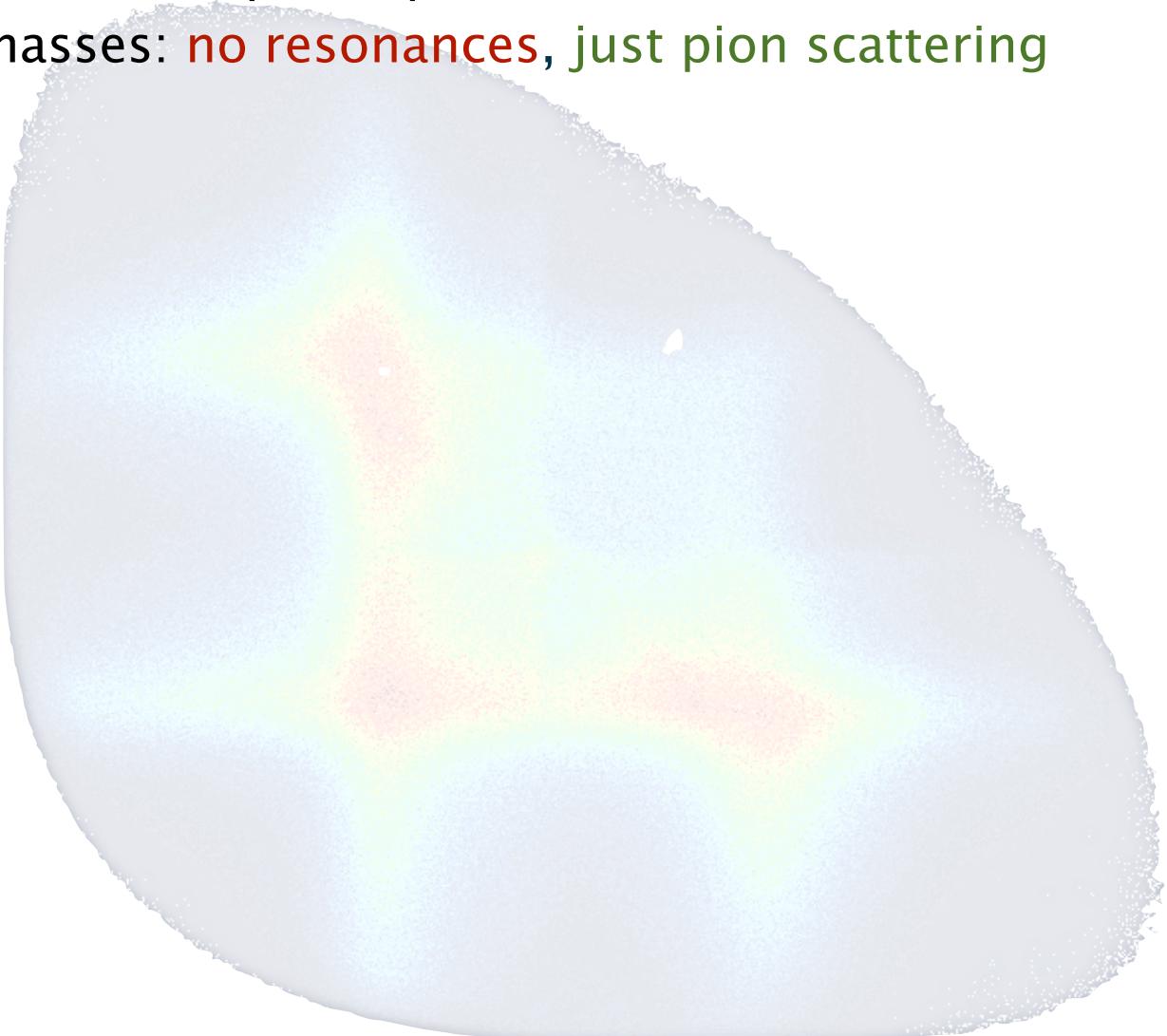


# Chiral Dynamics



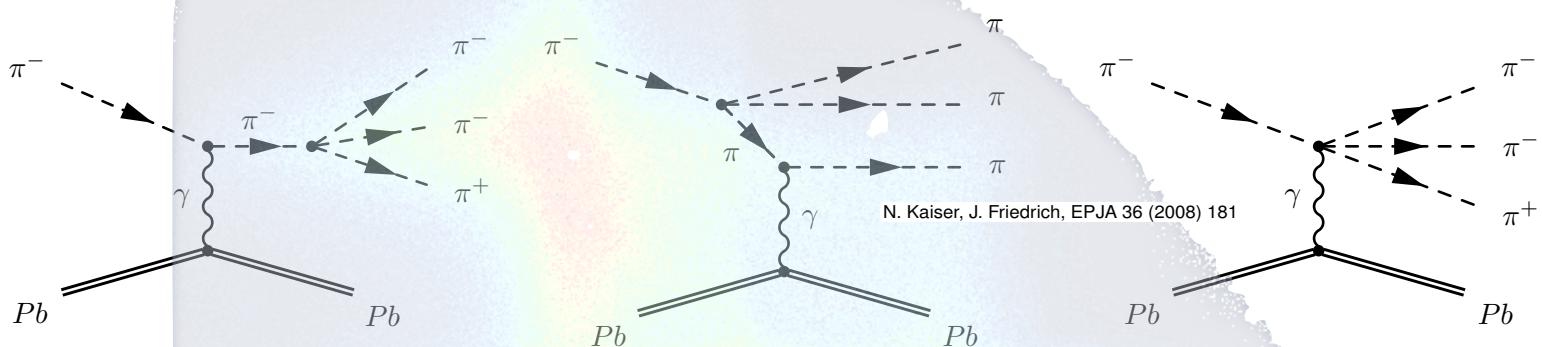
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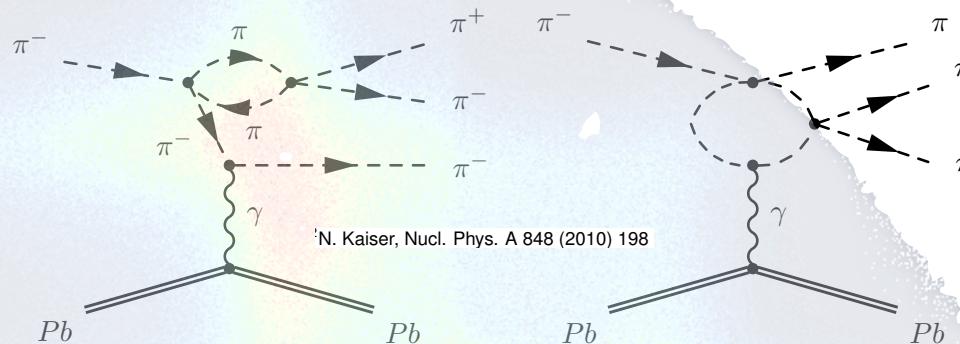
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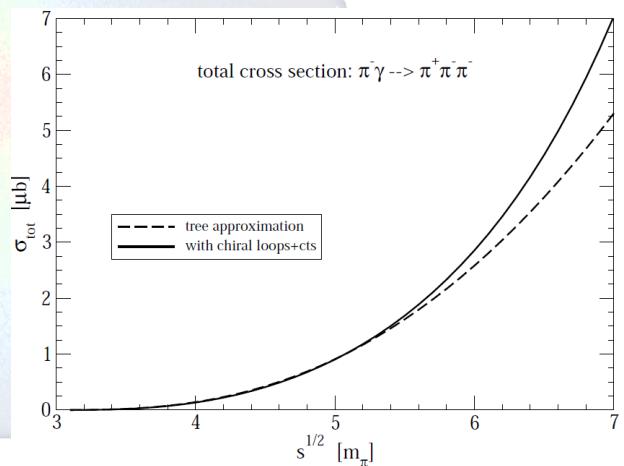
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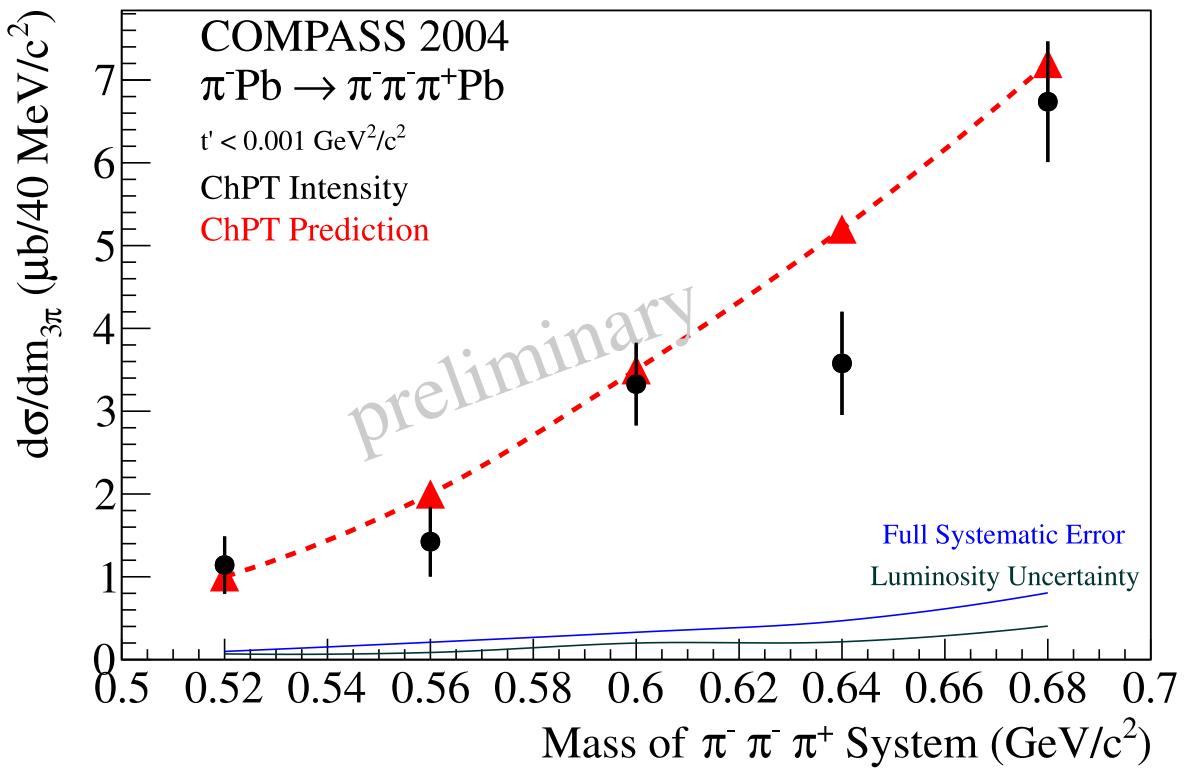


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  - Low masses: **no resonances**, just pion scattering  
→ **tree diagrams** from ChPT predictions
  - **loop diagrams**
- ChPT Amplitude introduced as **single partial wave**
  - Not orthogonal to waves in isobar model
  - Replaces (up to 6)  $(\pi\pi)_s \pi.$  And  $\rho\pi$  waves by **single amplitude**
- ChPT valid (at least)  $0.5 \text{ GeV/c}^2 < m_{3\pi} < 0.7 \text{ GeV/c}^2$
- Higher masses: Isobaric decays



# Chiral Dynamics



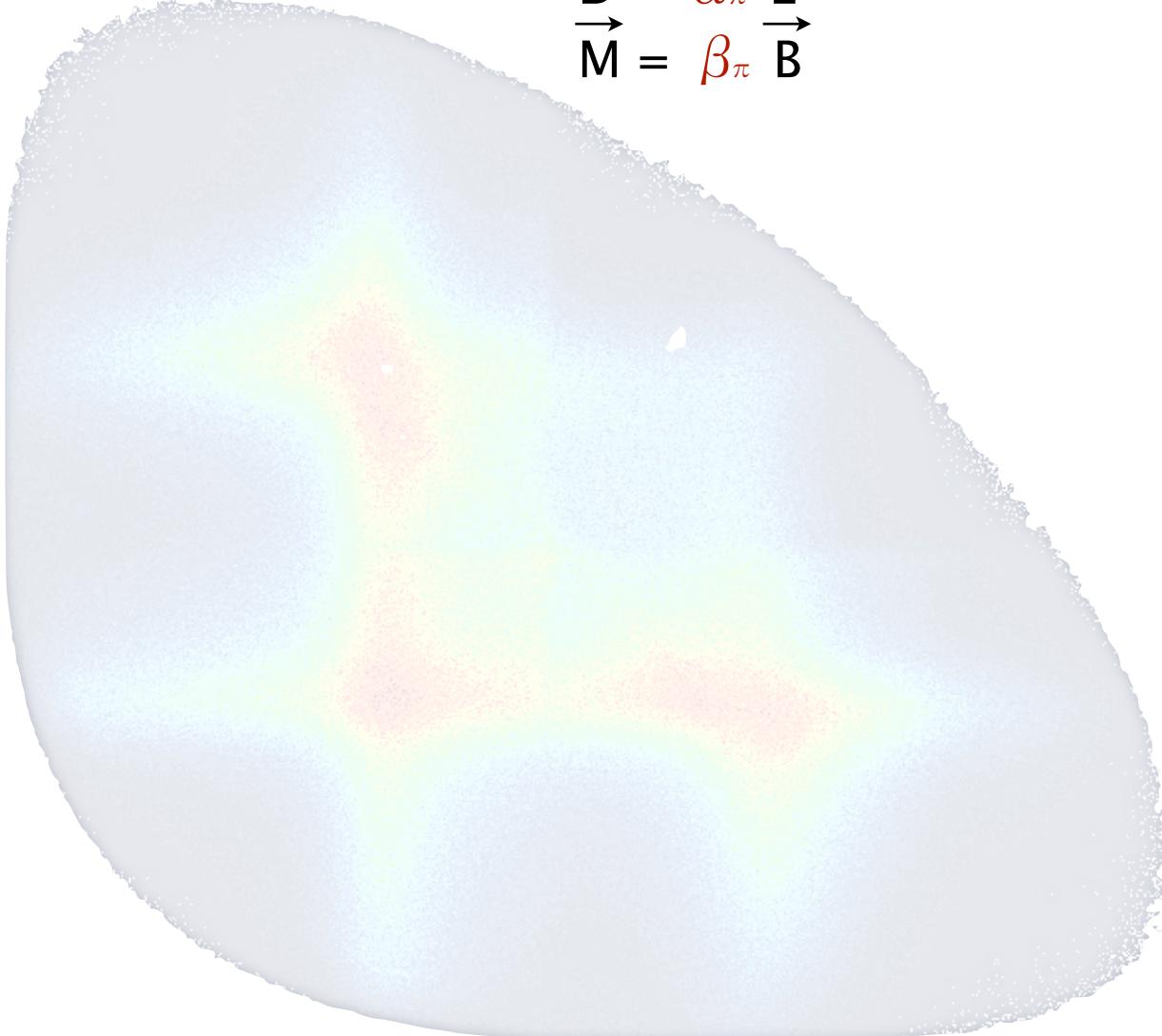
- Fits nicely....

# Polarisabilities

- Determine properties of pion

$$\vec{D} = \alpha_\pi \vec{E}$$

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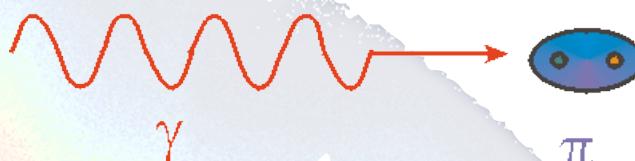


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$\Delta V \sim 10 \text{ MV}$



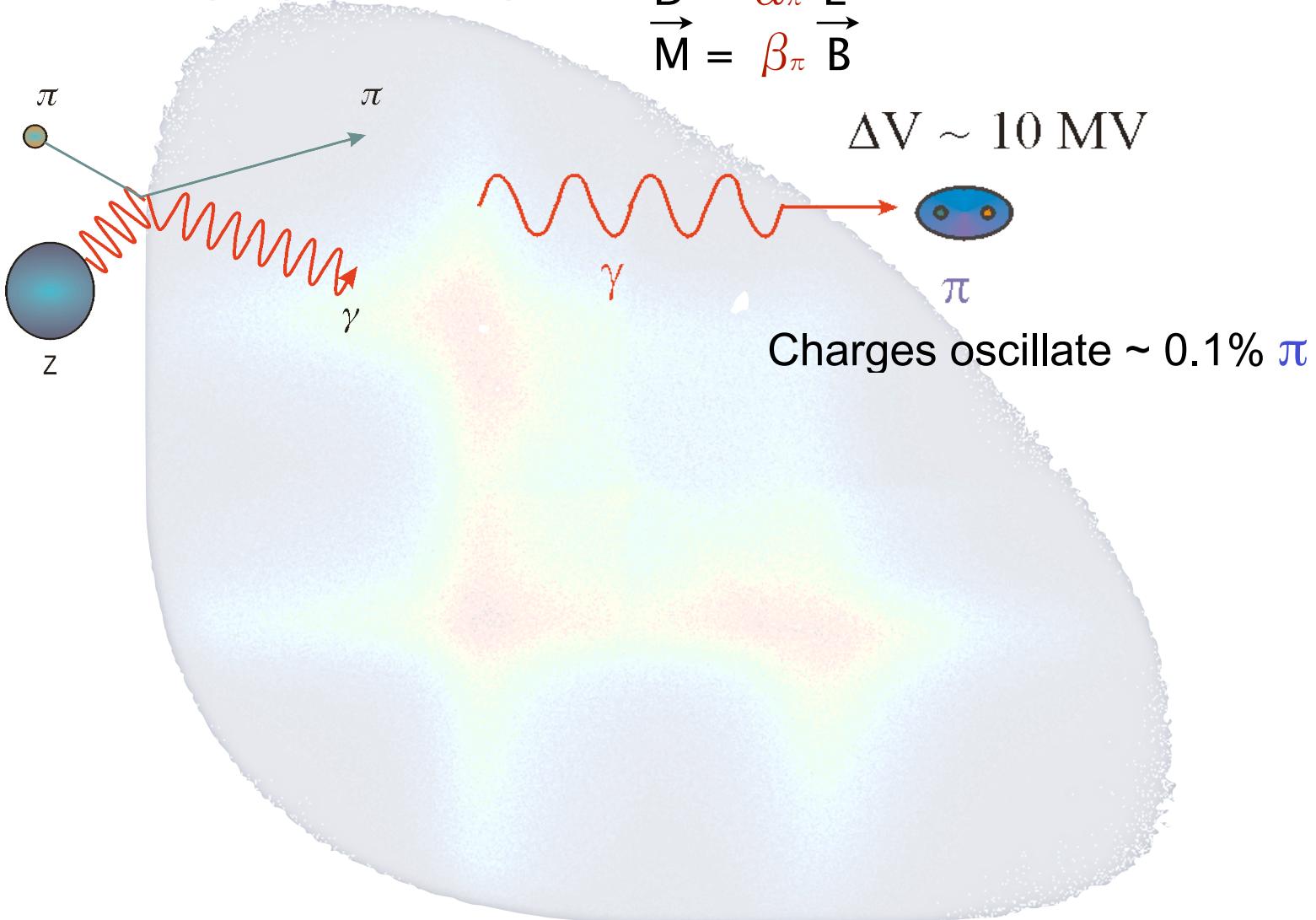
Charges oscillate  $\sim 0.1\% \pi$

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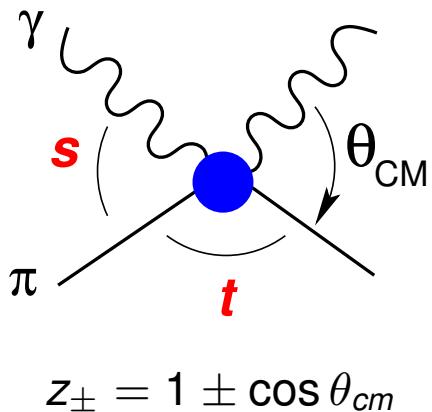


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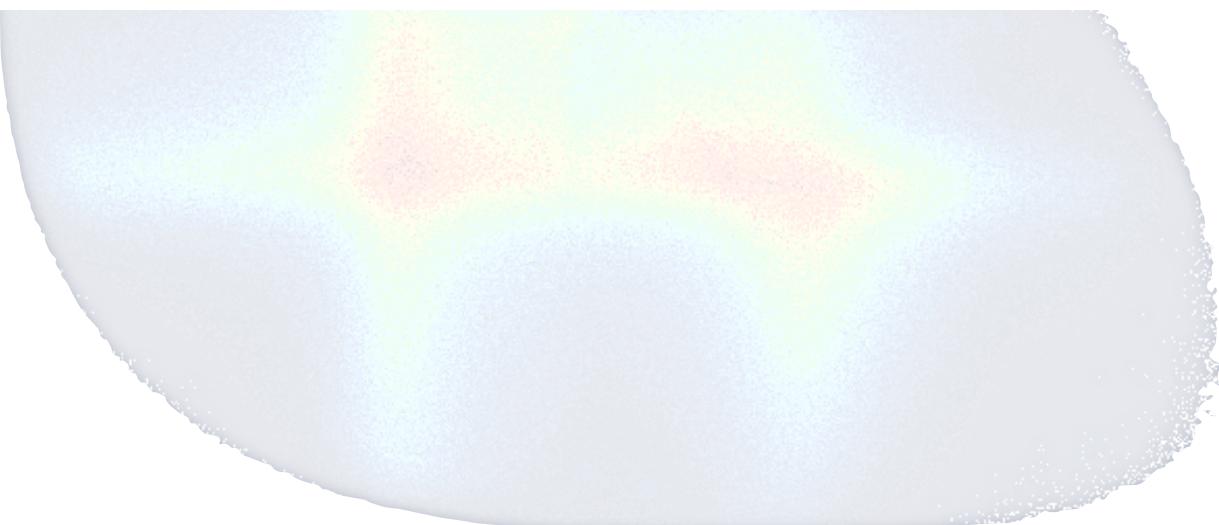
$$\begin{aligned}\vec{D} &= \alpha_\pi \vec{E} \\ \vec{M} &= \beta_\pi \vec{B}\end{aligned}$$



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where

$$\mathcal{P} = z_-^2(\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+^2(\alpha_\pi + \beta_\pi) - \frac{(s - m_\pi^2)^2}{24s} z_-^3(\alpha_2 - \beta_2)$$



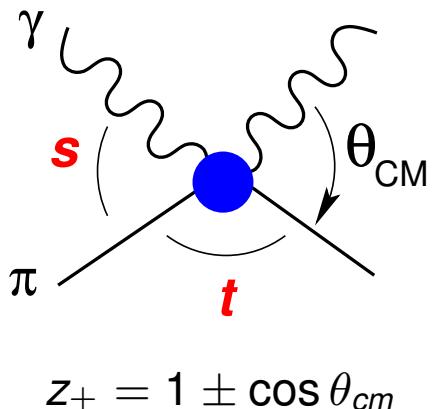
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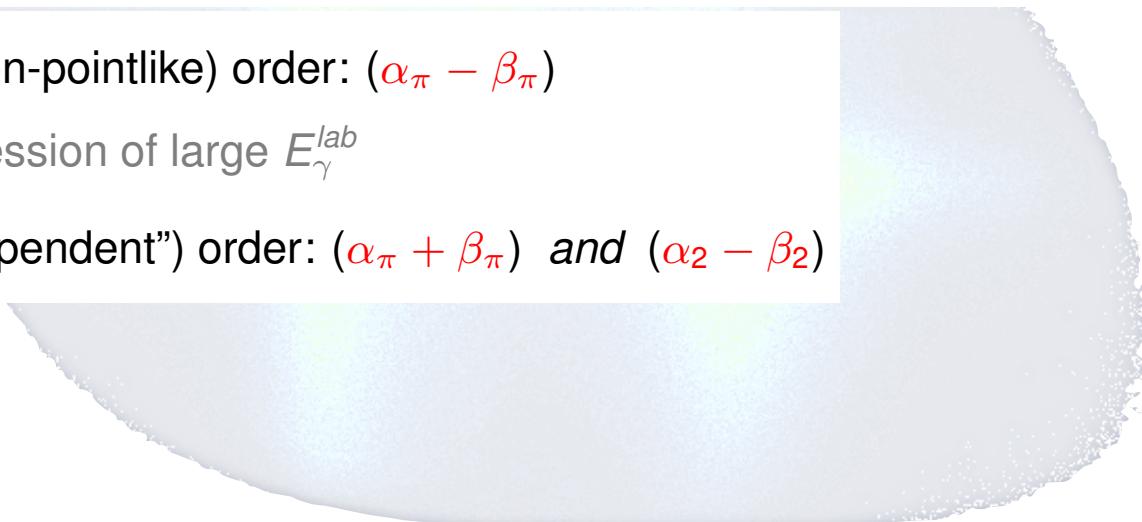


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- leading (non-pointlike) order:  $(\alpha_\pi - \beta_\pi)$   
→ suppression of large  $E_\gamma^{lab}$
- next (“s-dependent”) order:  $(\alpha_\pi + \beta_\pi)$  and  $(\alpha_2 - \beta_2)$



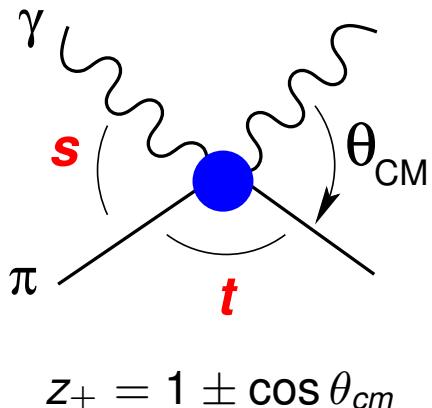
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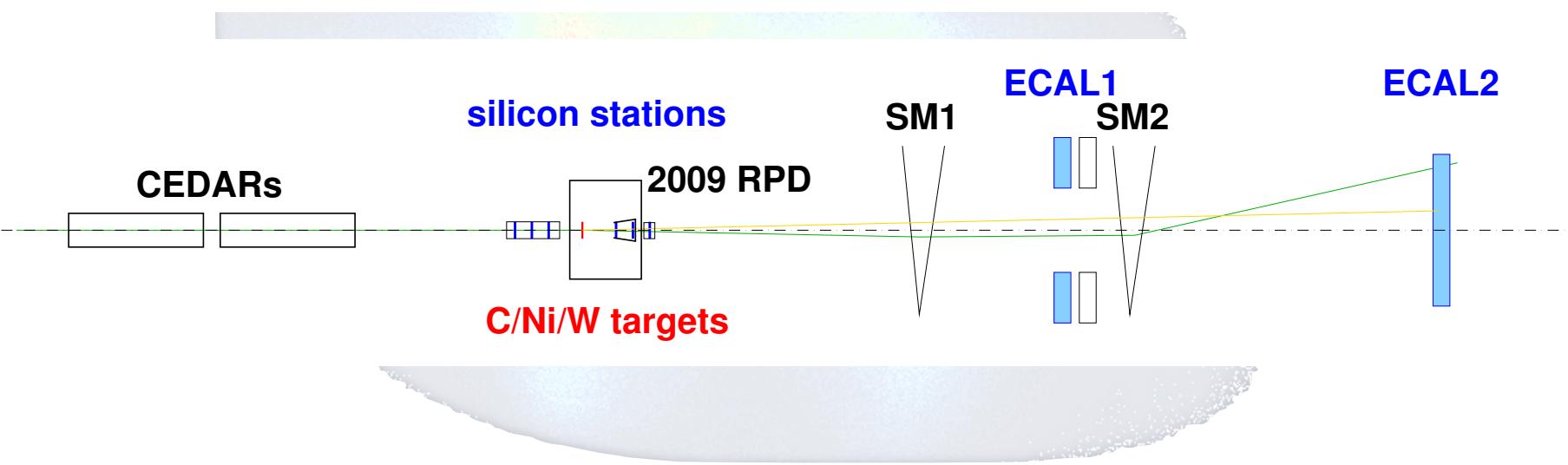
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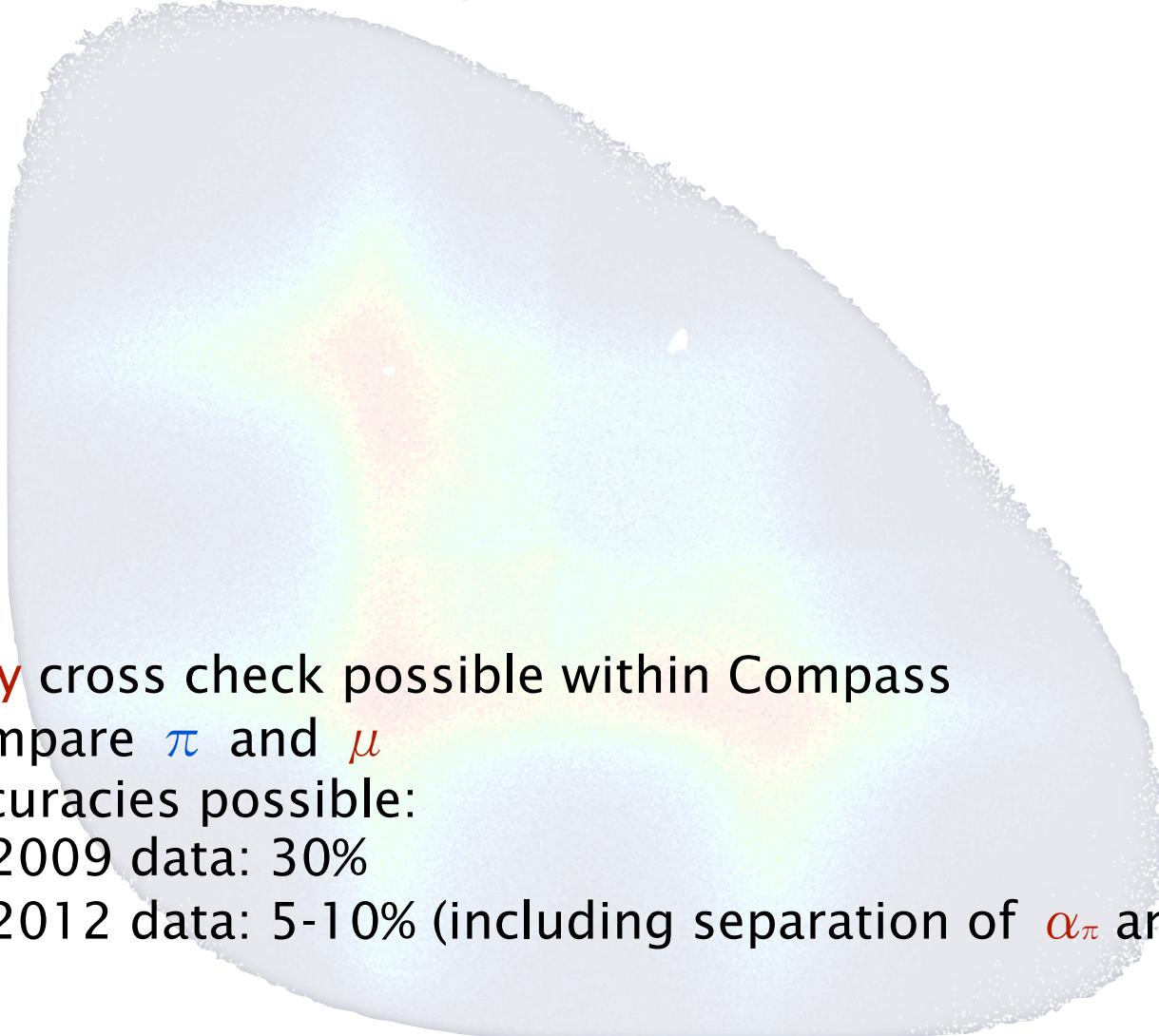
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# Polarisabilities II

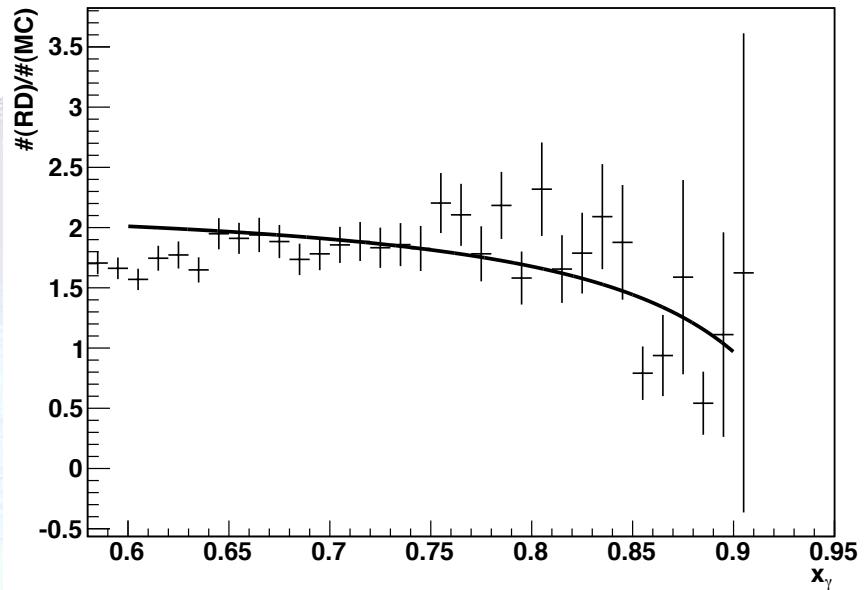
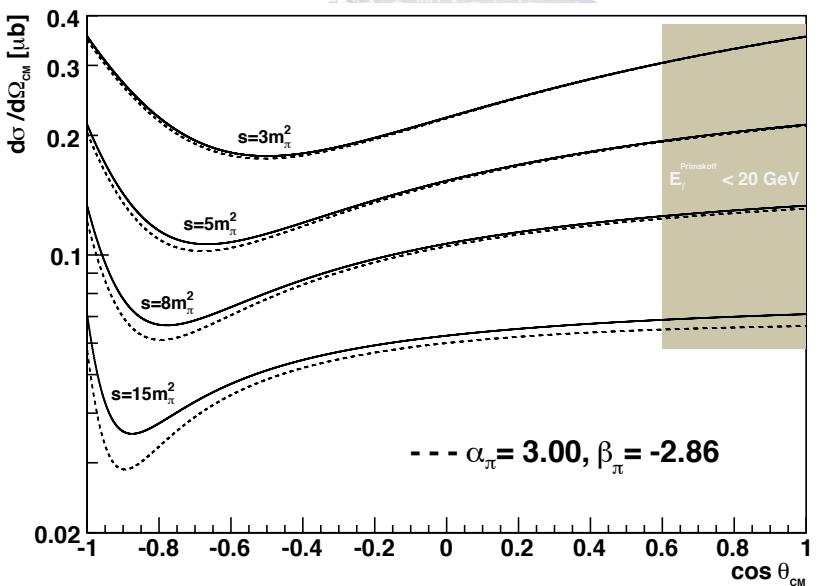
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- Quality cross check possible within Compass
  - Compare  $\pi$  and  $\mu$
  - Accuracies possible:
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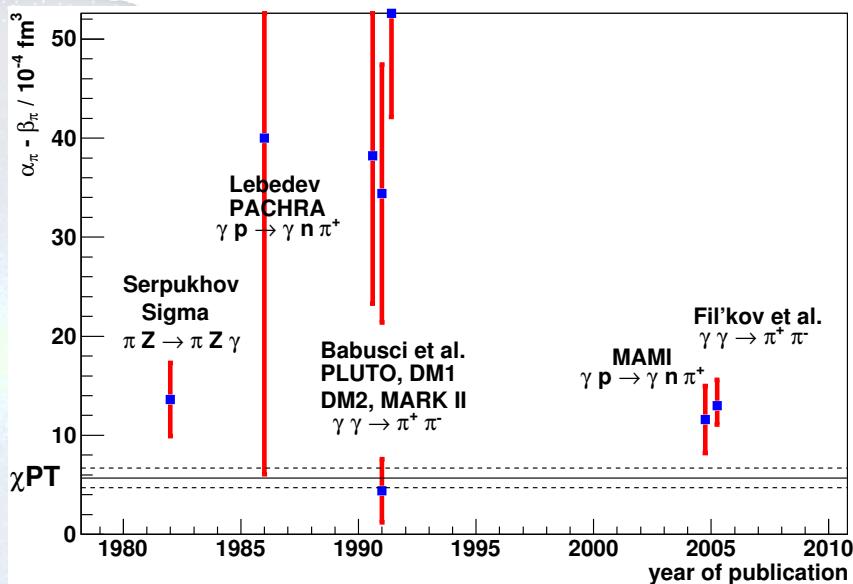
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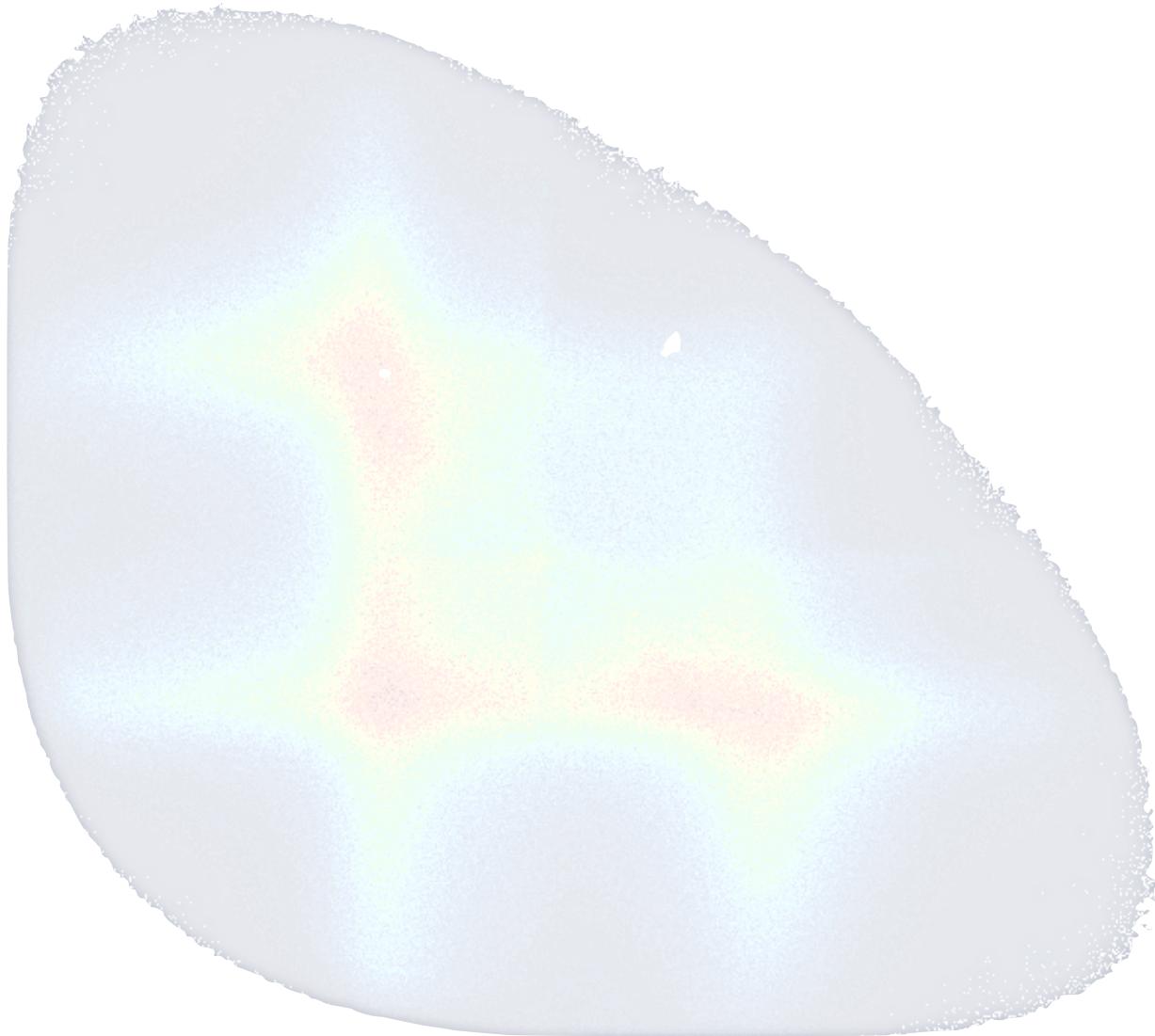
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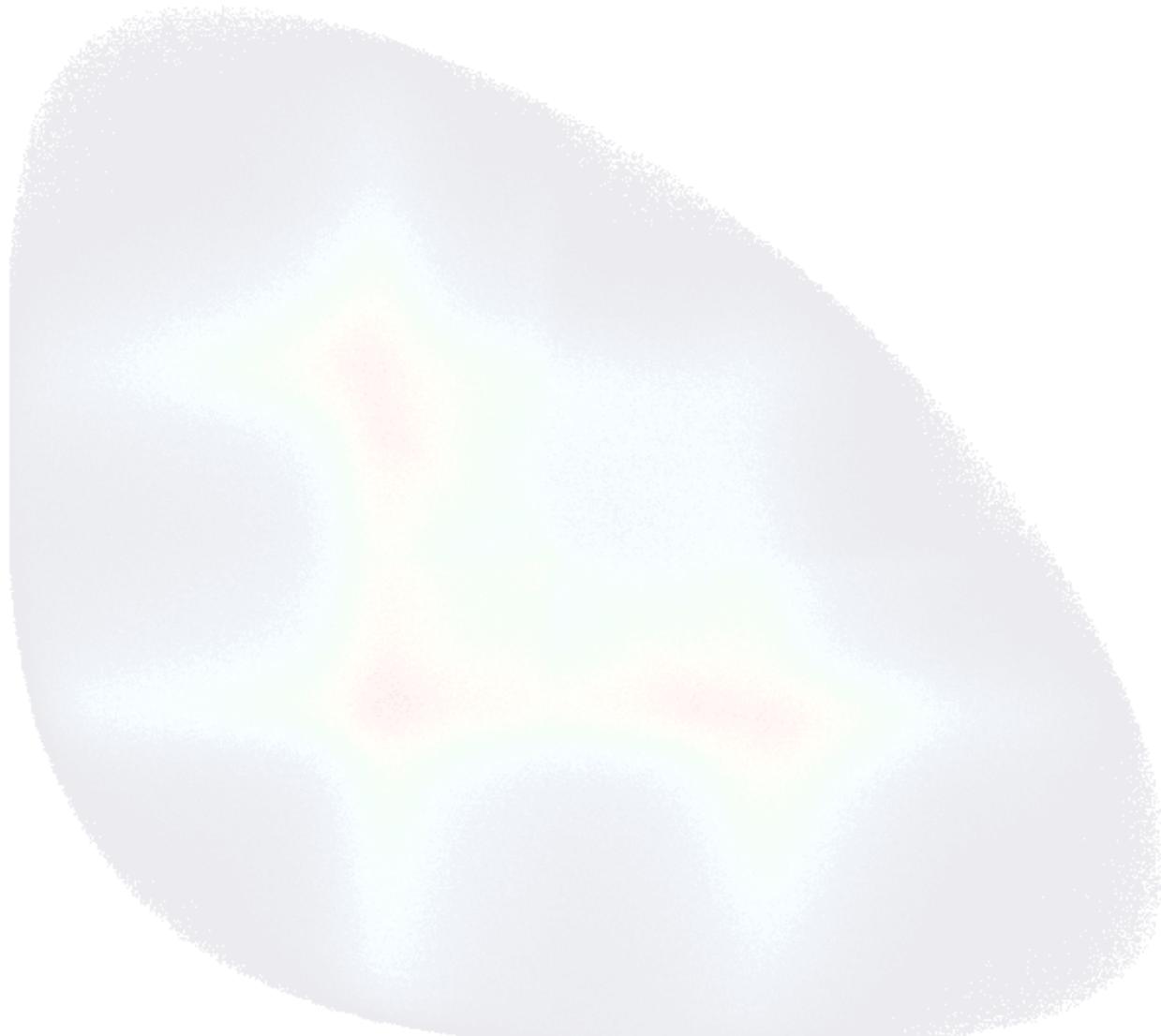
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# Conclusions

- COMPASS has active spectroscopy program
  - PWA Tools developed
  - More refined PWA underway: larger wave set, Deck effect
  - **High statistics** (partly > 200 times previous work) in many channels
- Results:
  - Observe consistent signal on **exotic  $\pi_1(1600)$**  in diffraction ( $3\pi$ )
  - Nuclear dependence of production characteristics (also seen in 2009)
  - Neutral channels show consistent signals  $\pi^-\pi^0\pi^0$
  - $5\pi$  analysis ongoing (complex analysis)
  - Central production analysis in  $4\pi$  and kaonic channels underway
  - Baryon spectroscopy may be add on
  - Primakoff physics reveals many aspects (also new)
  - Coulomb-nuclear interference
- Analysis future: address high mass region, chiral dynamics, polarisability (run 2012)



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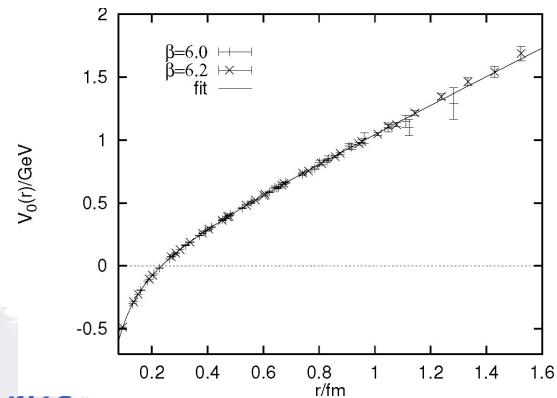
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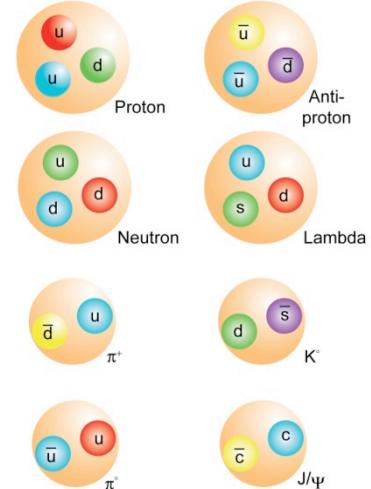
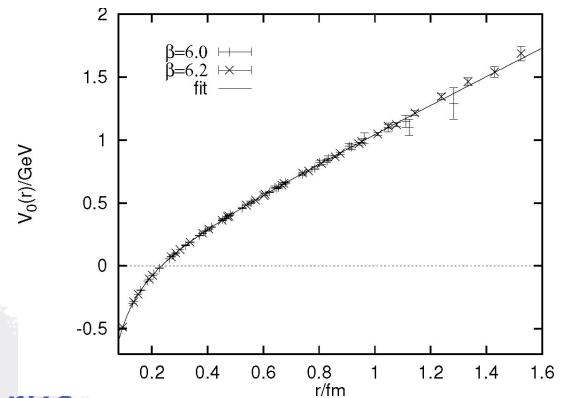


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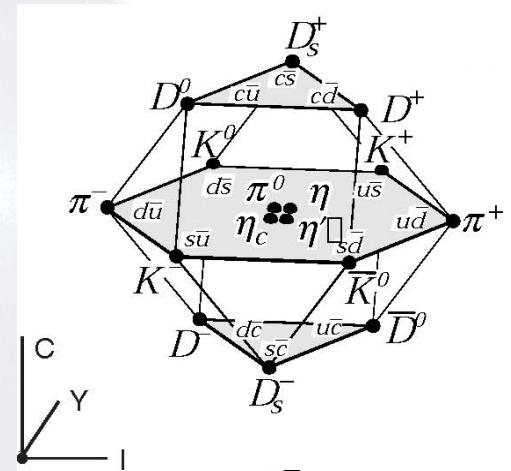
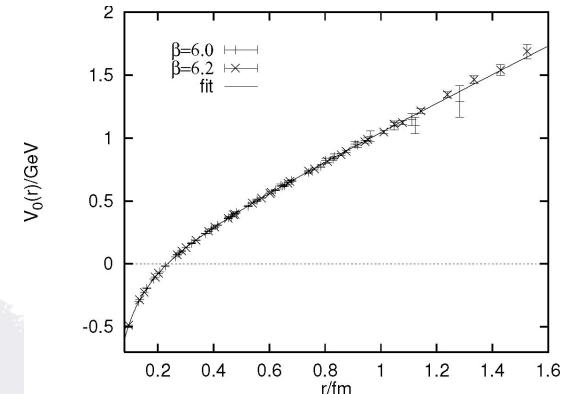


- effective  $q\bar{q}$  potential

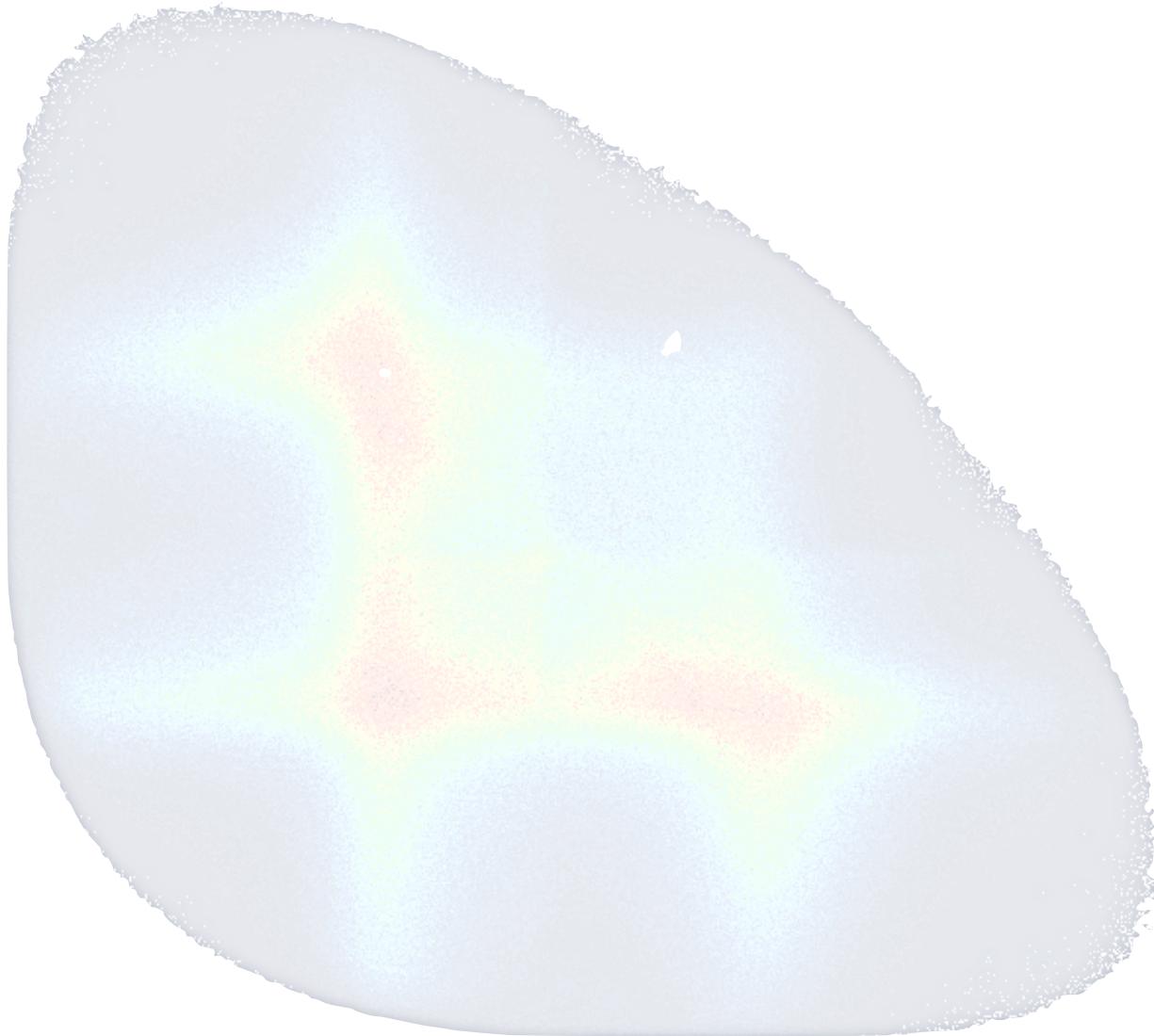


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  - Classify into **multiplets**  
  
**Hadron masses** are sum of quark masses
  - Use **hyperfine-interaction** (spin-spin interaction)  
**mass spectrum** surprisingly well **described**

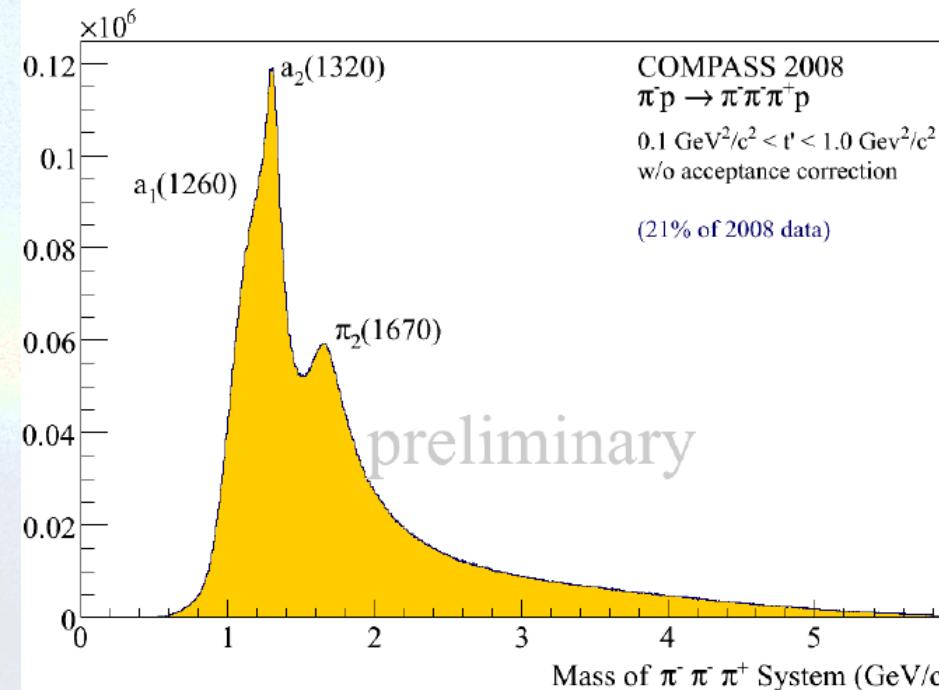
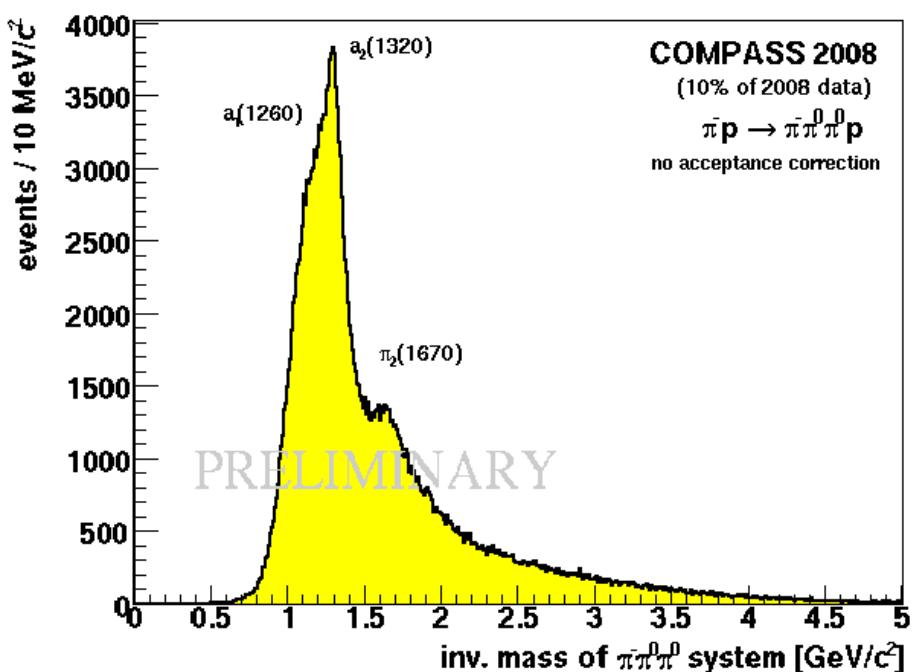


# 3 $\pi$ Final State: $\pi^- p \rightarrow \pi^-\pi^0\pi^0 p$



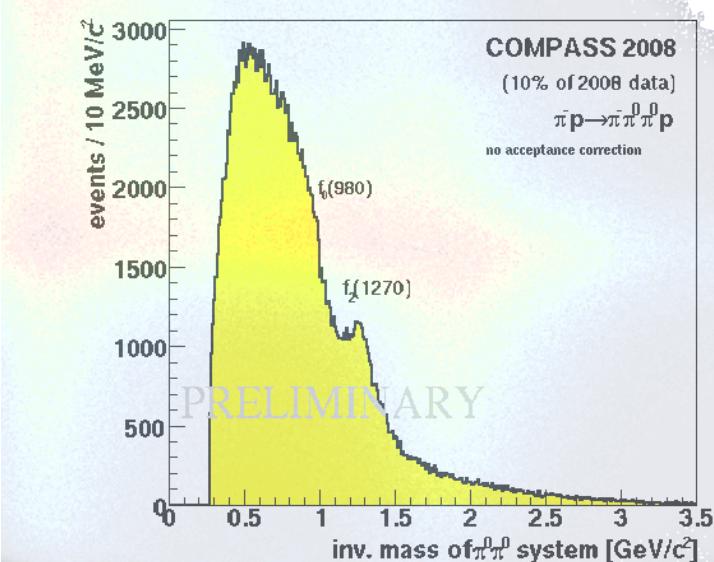
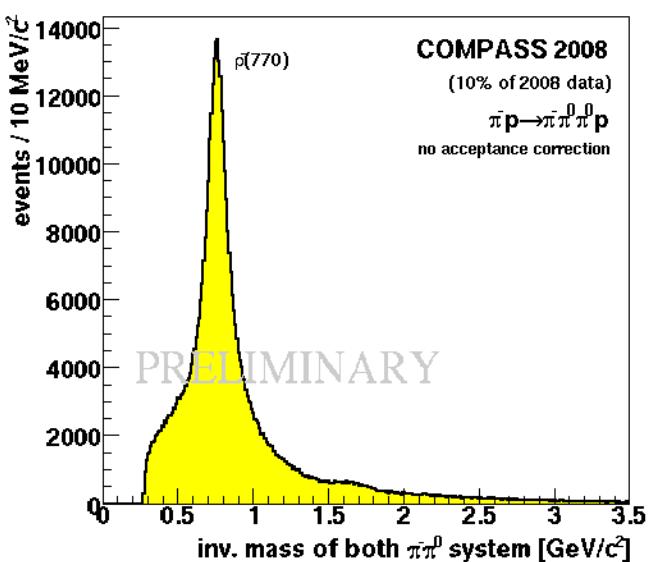
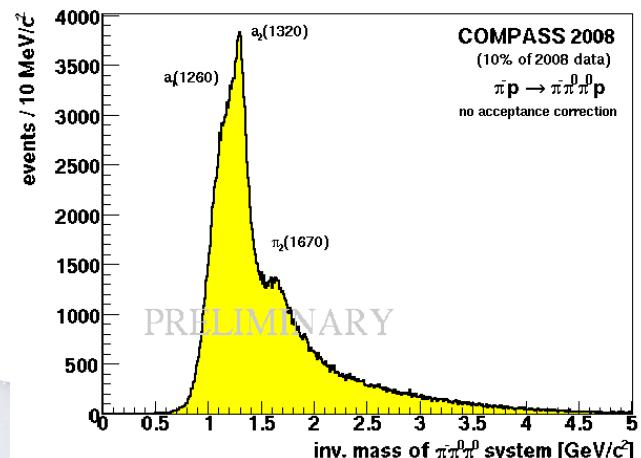
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- Isospin partner to  $\pi^- p \rightarrow \pi^-\pi^+\pi^- p$ 
  - Consistency check
  - Different isobars in decay chain
  - Isospin information



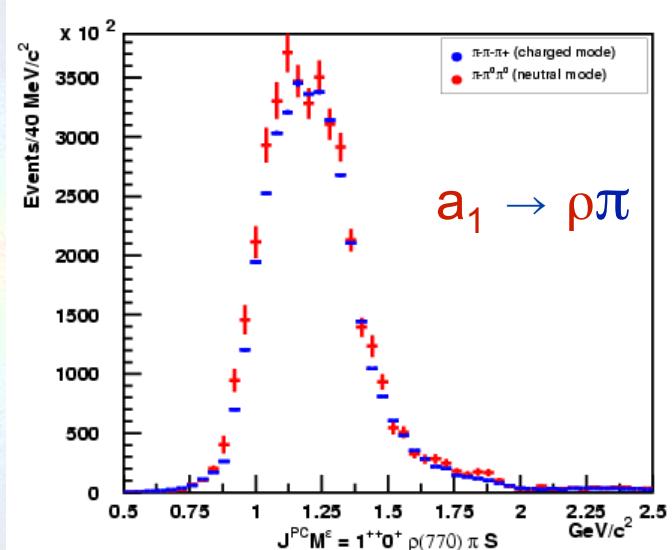
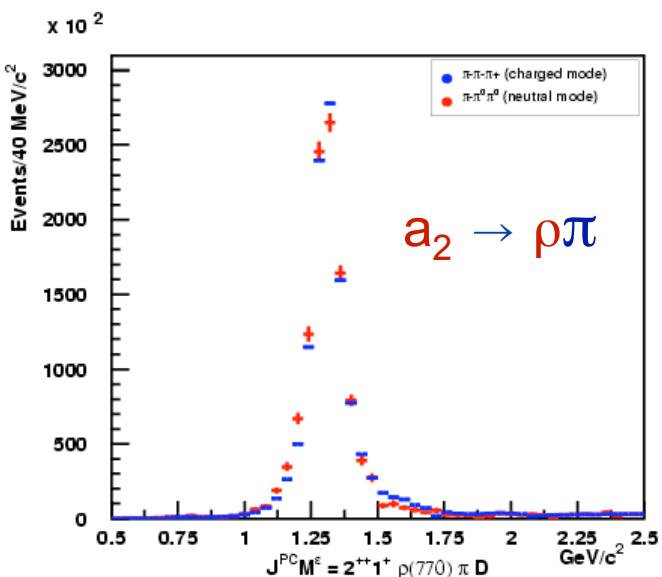
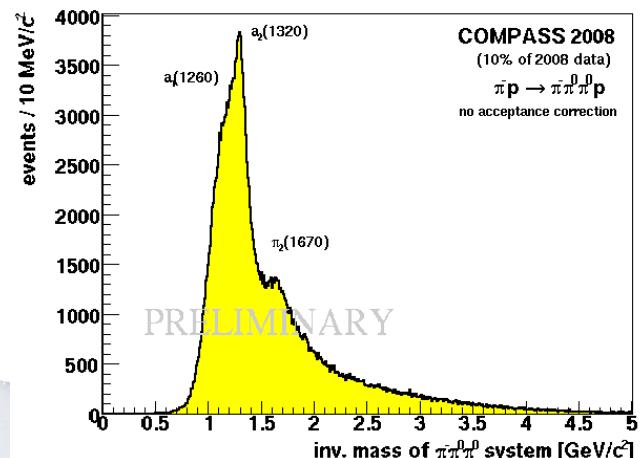
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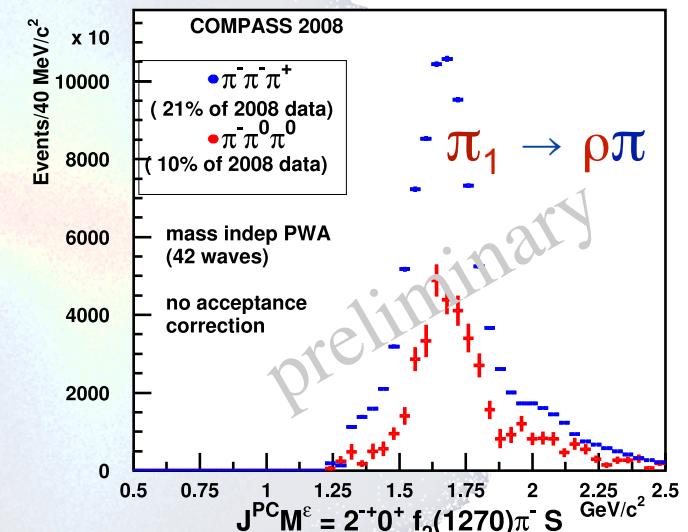
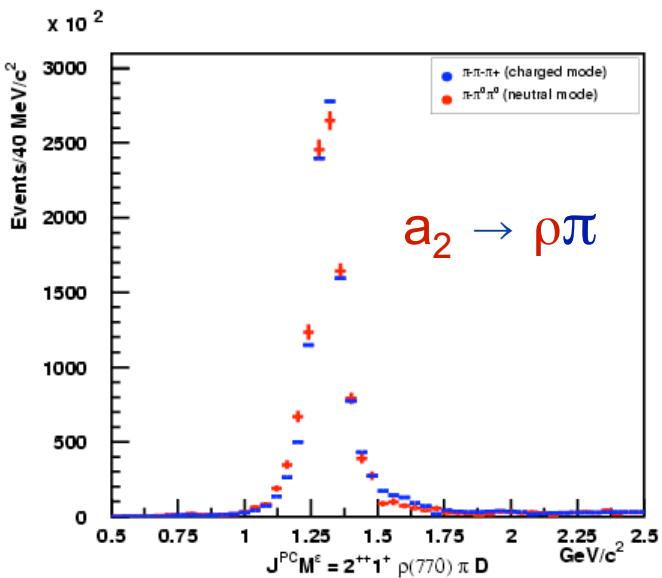
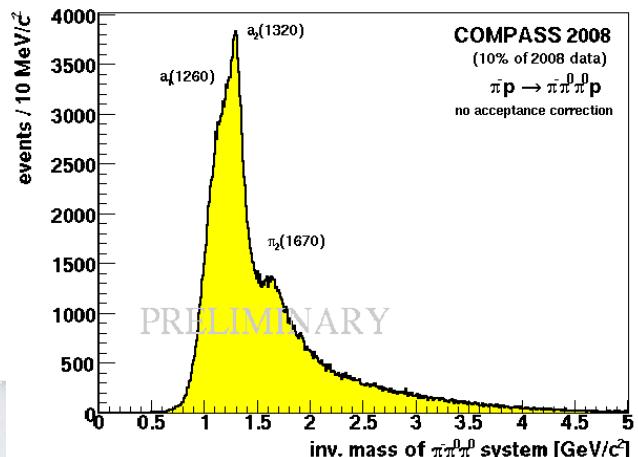
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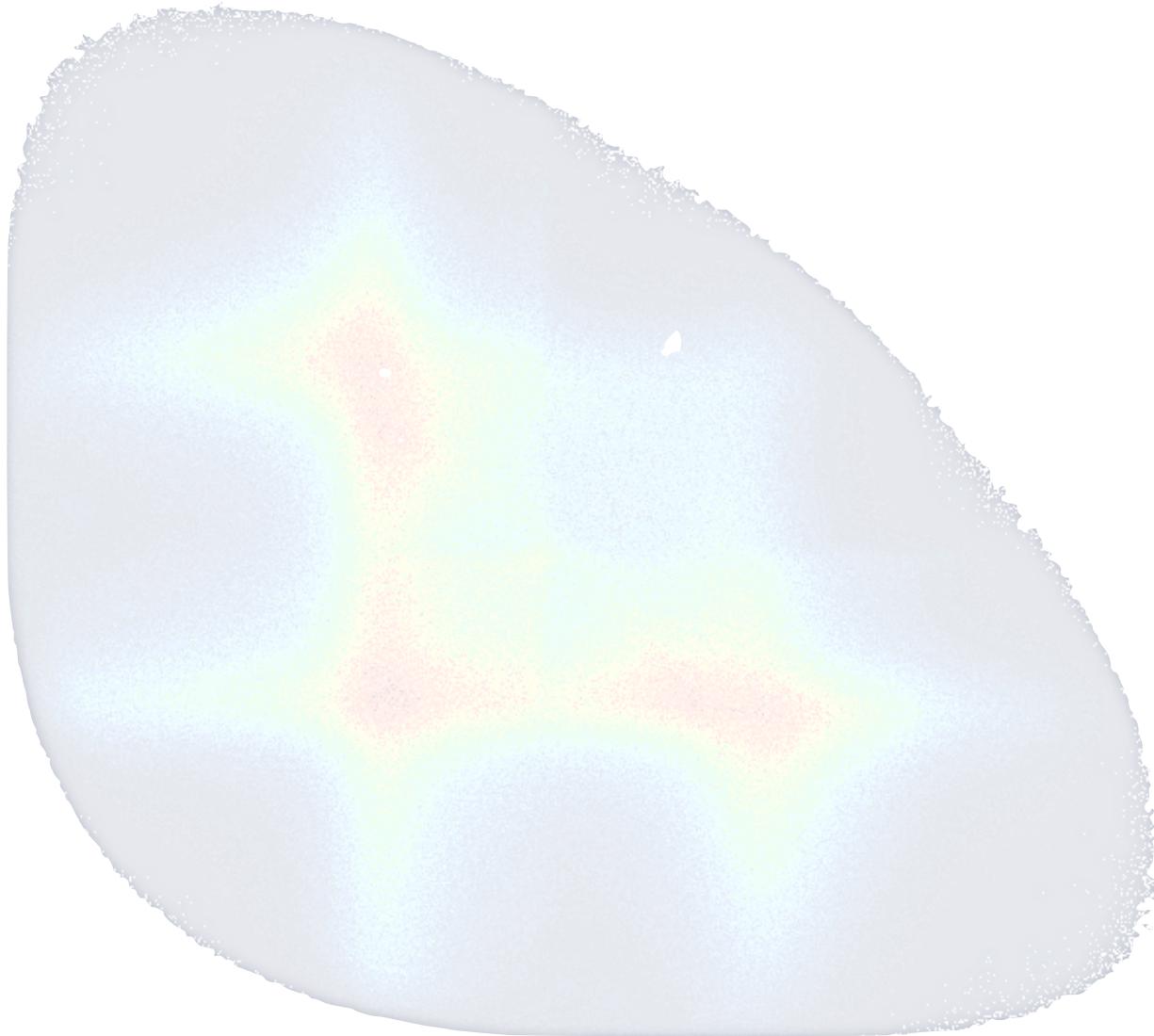


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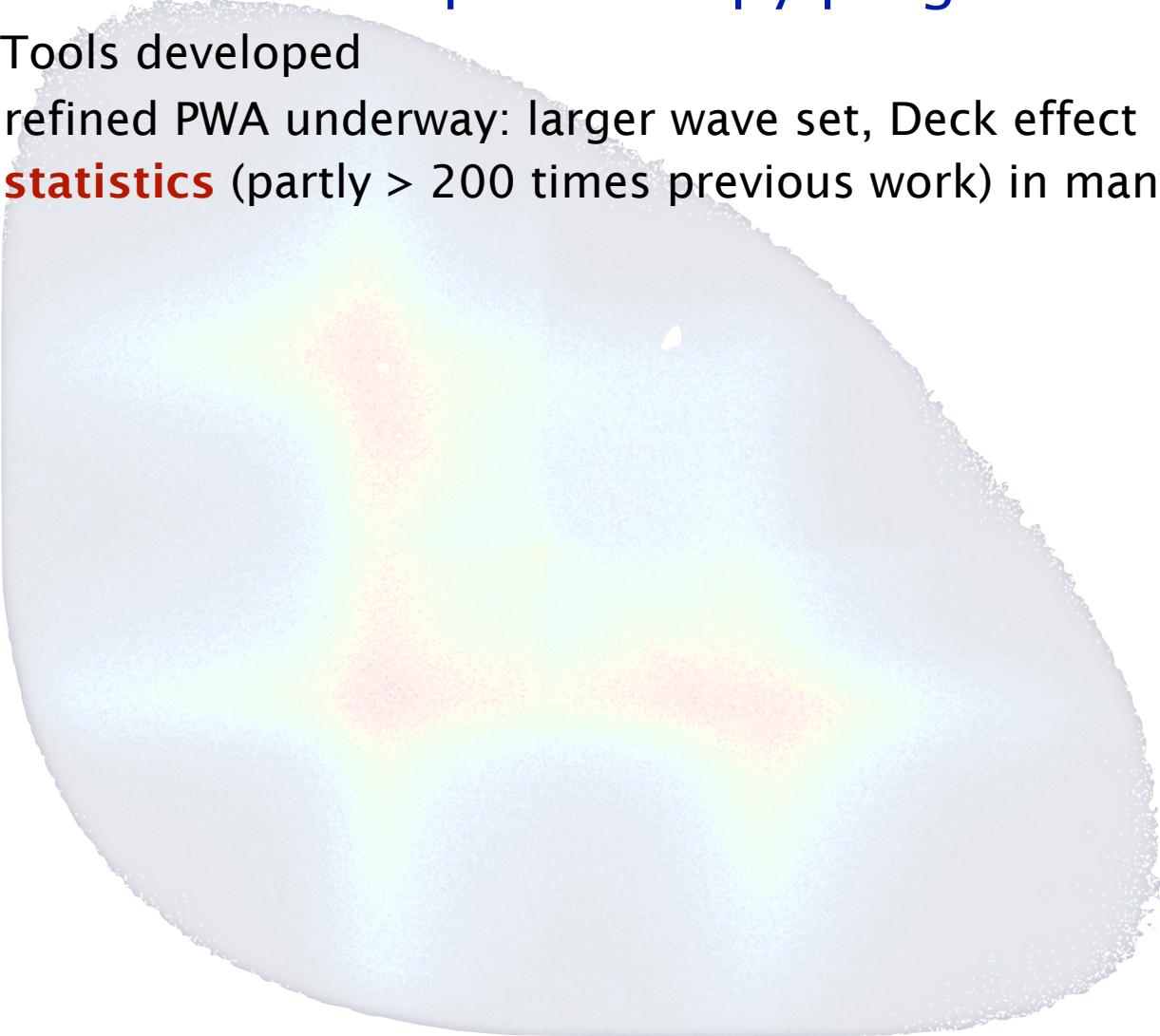


# Conclusions



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  - More refined PWA underway: larger wave set, Deck effect
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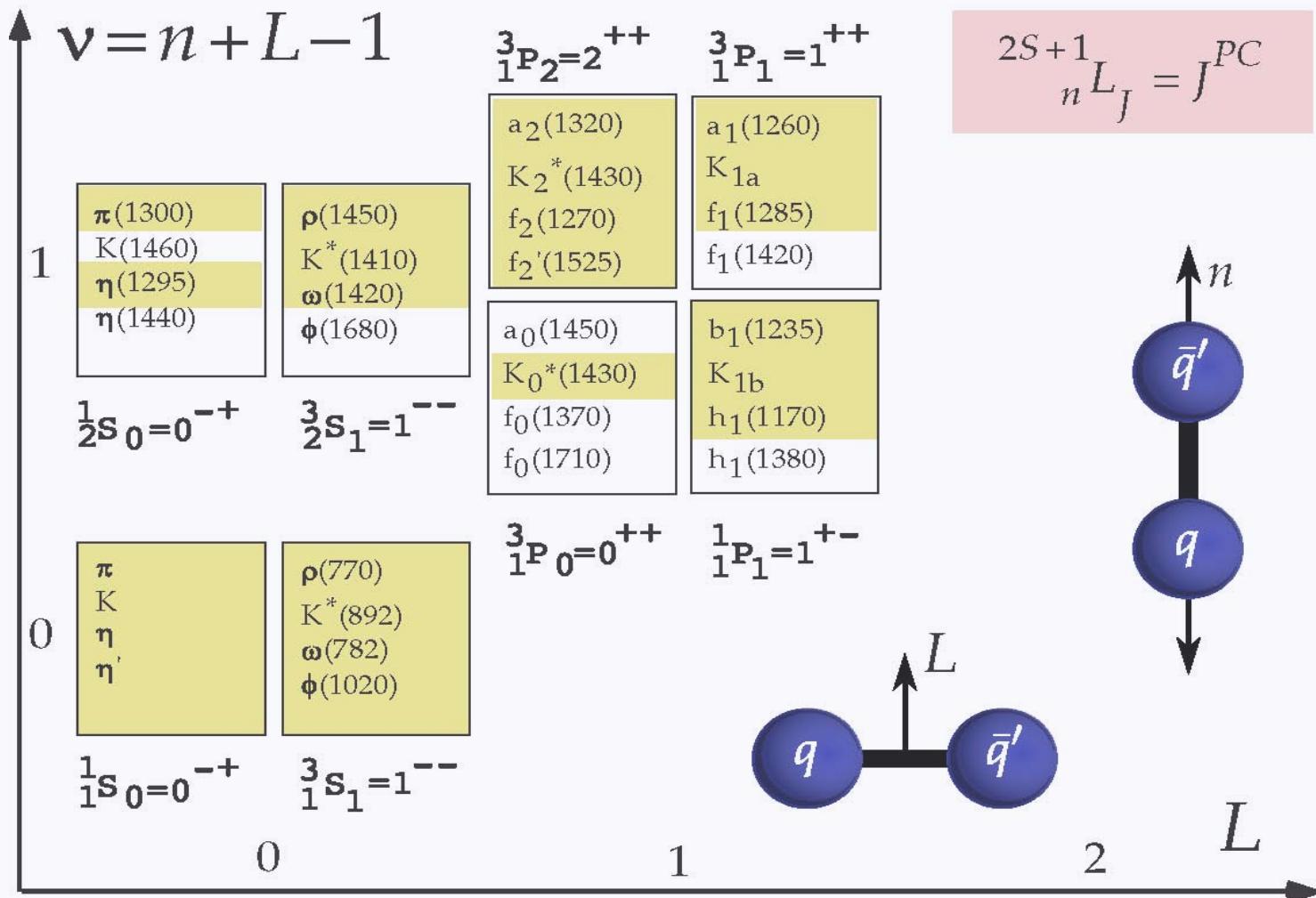
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- Analysis future: address high mass region, chiral dynamics, polarisability

# Constituent Quark Model III

Spectrum light mesons:

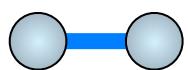


C. Amsler *et al.*, Phys. Rept. 389, 61 (2004)

# Meson-Spectroscopy



=

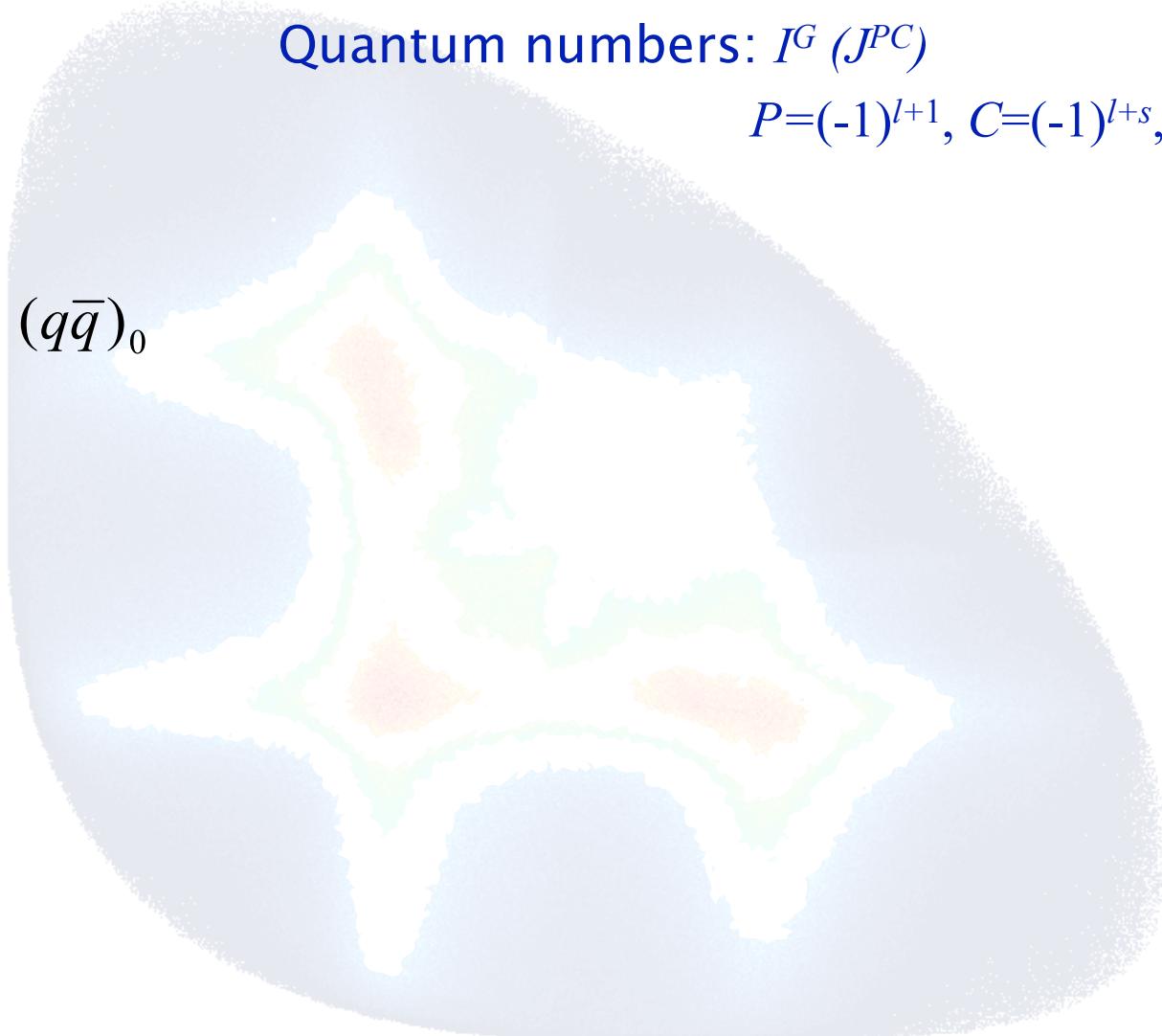


$(q\bar{q})_0$

**Quark model:** bound states of  $q\bar{q}$

Quantum numbers:  $I^G (J^{PC})$

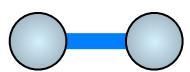
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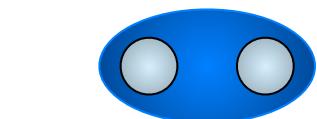
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=



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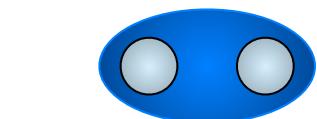
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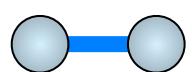
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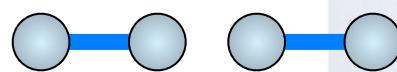
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=


 $(q\bar{q})_0$ 

+


 $(q\bar{q})(q\bar{q})$ 

+


 $(q\bar{q})_8 g$   
Hybrids

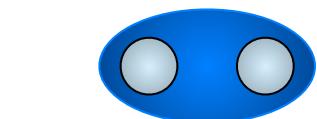
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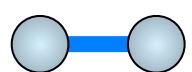


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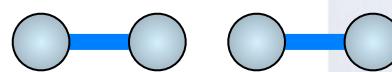
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+



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$gg$

**Glueballs**

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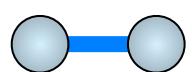


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**Glueballs**  
dynamics

+ ...

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=



+



+



+



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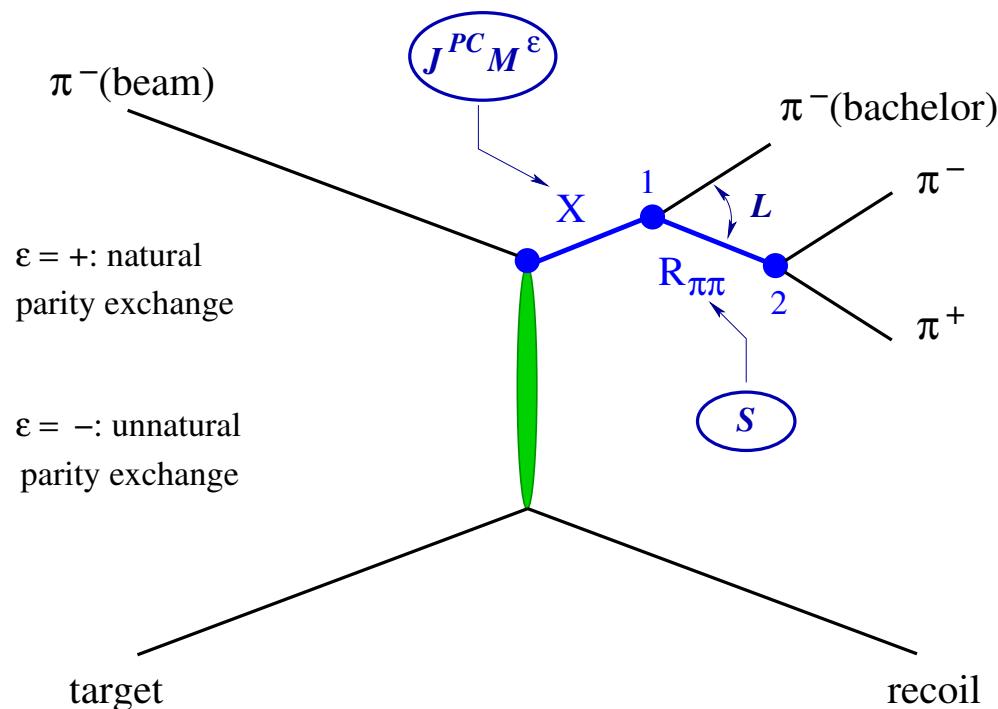
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**Decoupling** only possible for

- narrow states
- No leading  $q\bar{q}$  term  
 $\Rightarrow$  spin-exotic  $J^{PC}$ :  $0^{--}, 0^{+-}, 1^{-+}, 2^{+-}, \dots$

# Analysis Inelastic Final State IV

- Decay amplitudes  $\psi_i(\tau, m)$  calculable
  - 3 variables for each 2-body vertex  $m_{\text{mother}}, (\theta, \varphi)$  in mother r.f.
  - $3\pi$  decay:  $m, \{\theta_{\text{GJ}}, \phi_{\text{GJ}}, m_R, \theta_{\text{H}}, \phi_{\text{H}}\} \equiv \tau$
  - contain angular distributions and isobar parameterizations

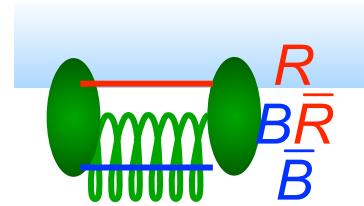


# Hybrids

**Sector light mesons** : exotic  $J^{PC}=1^{-+}$ :

- $\pi_1(1400)$  (VES, E852, Crystal Barrel)
- $\pi_1(1600)$  (E852, VES)
- $\pi_1(2000)$

still disputed...

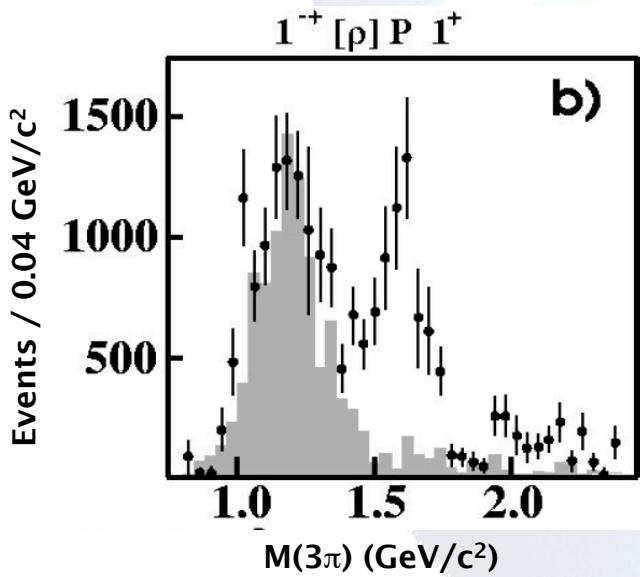


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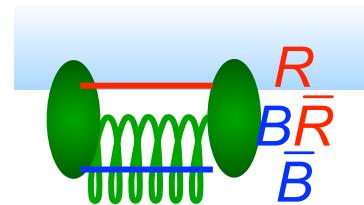
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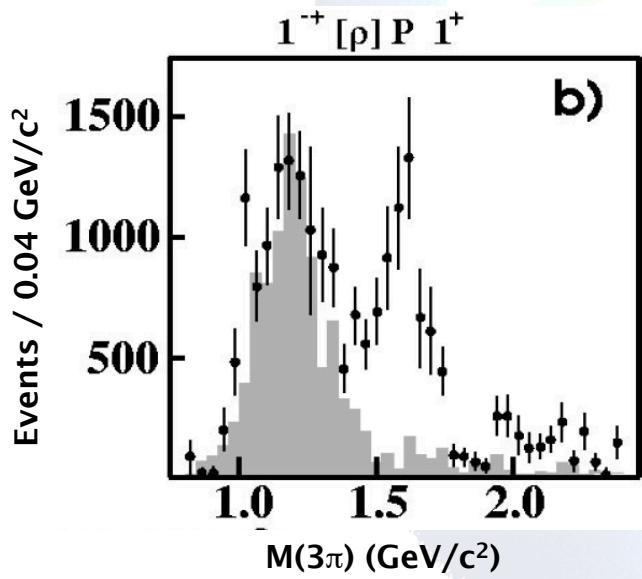


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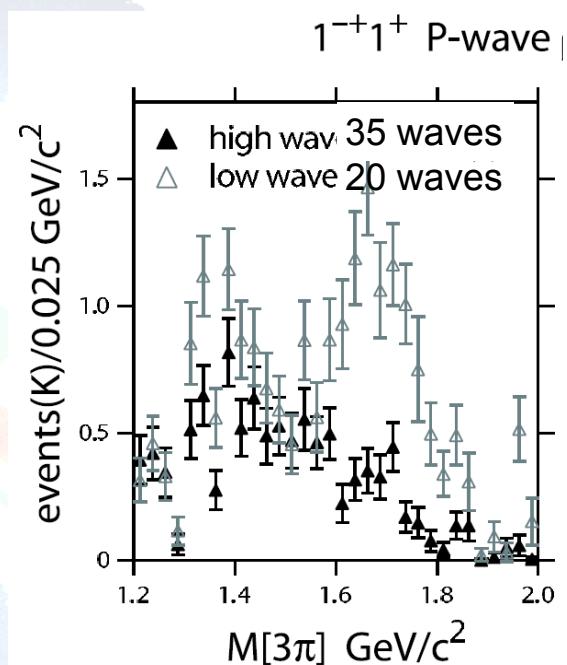
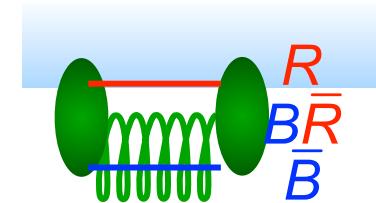
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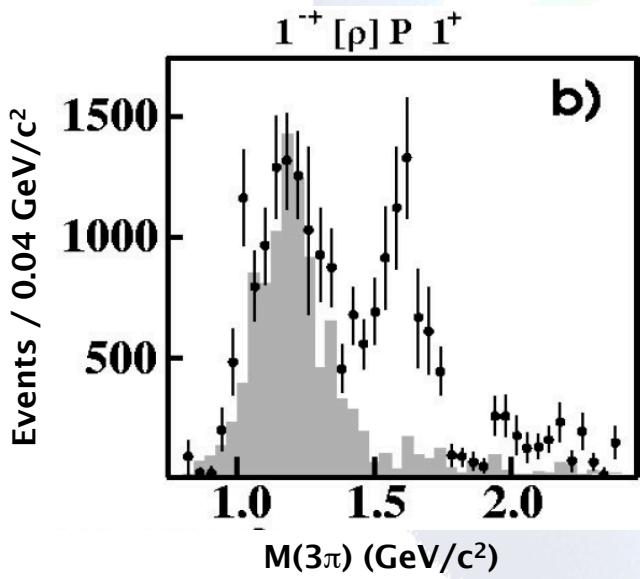
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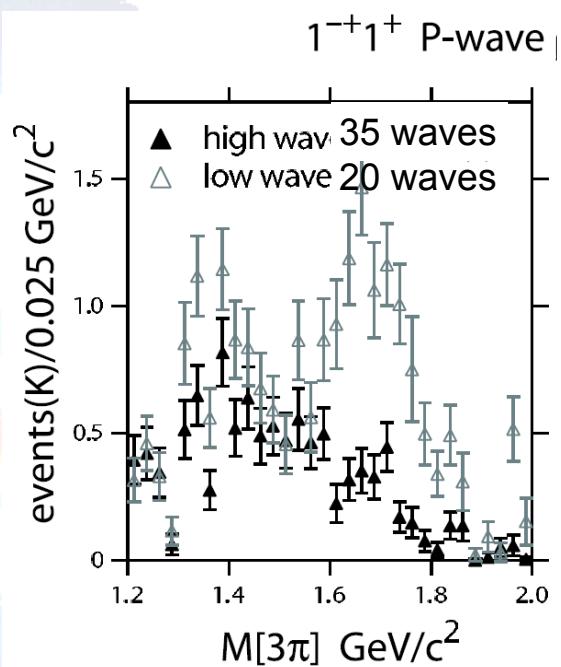
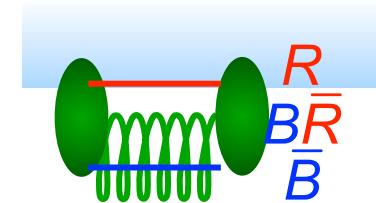
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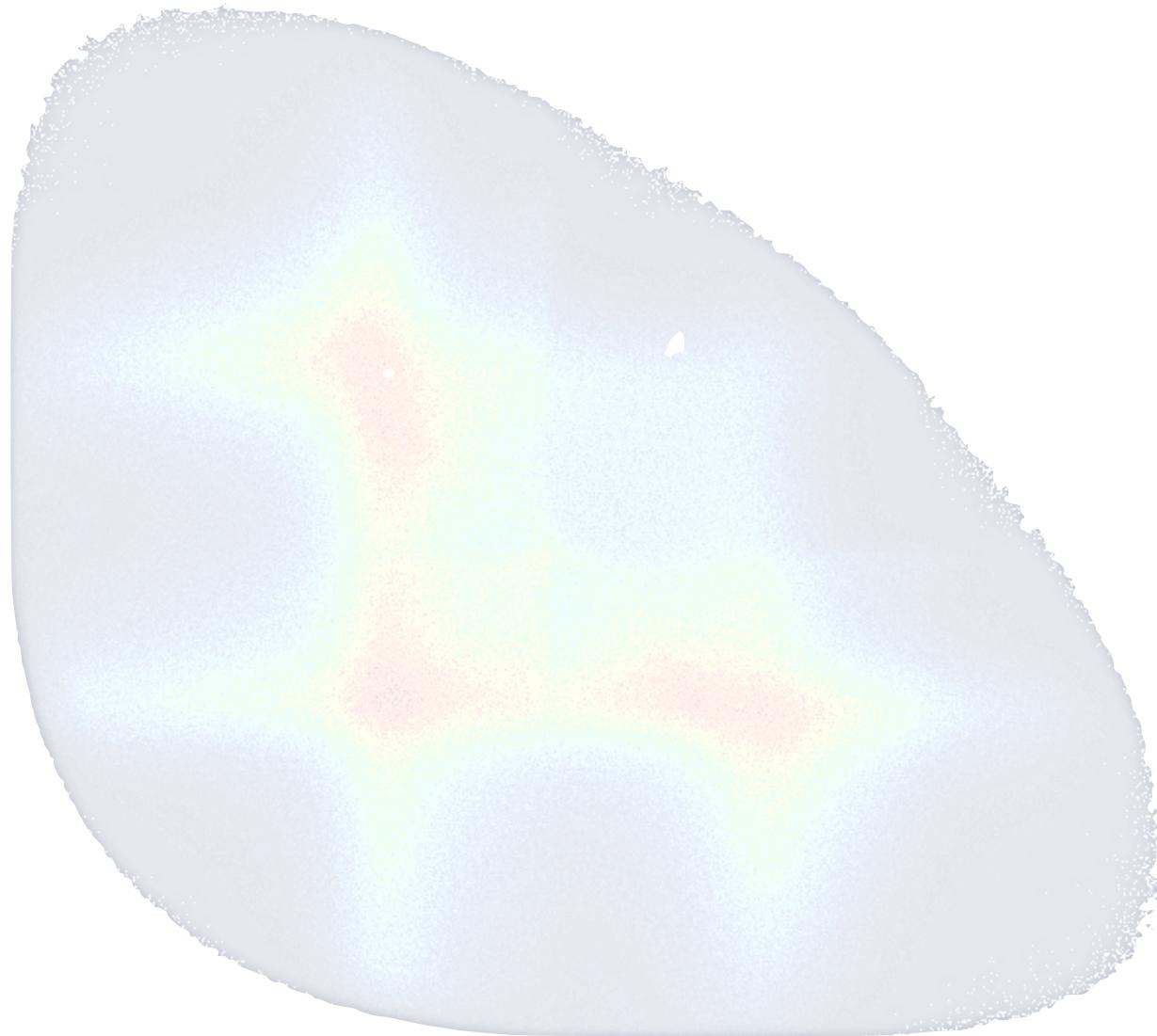
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⇒ COMPASS

# Analyse Inelastic Final State III

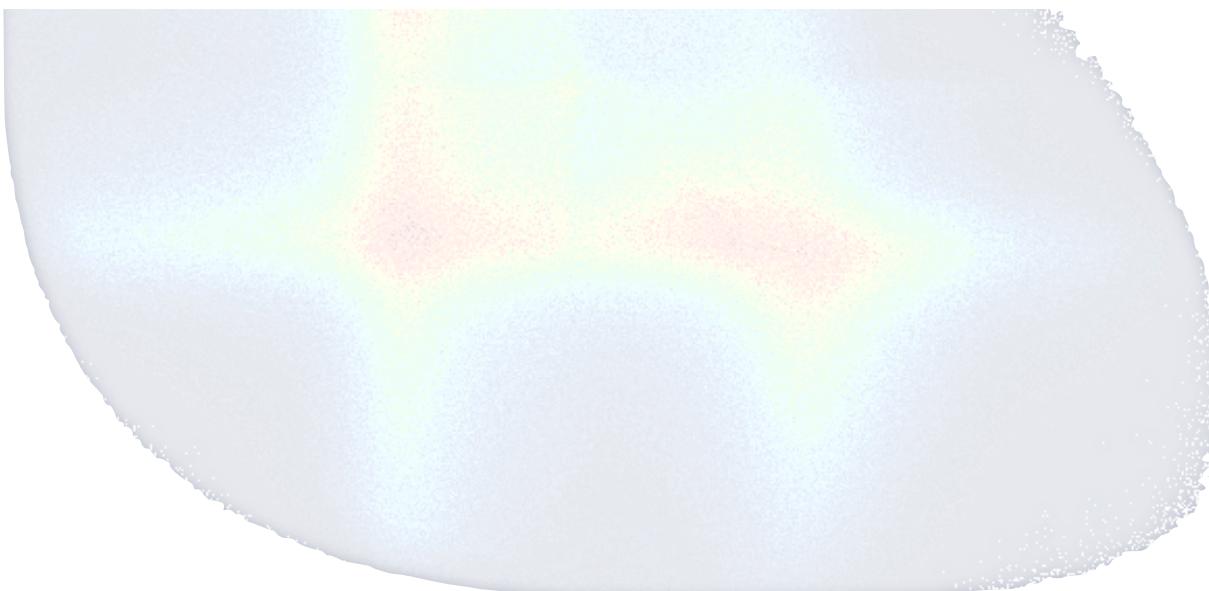


## Mass-Independent PWA

- Fit angular distributions + isobar systems  
in independent mass bins

$$\sigma(\tau, m) = \sum_{\epsilon=\pm 1} \sum_{r=1}^{N_r} \left| \sum_i T_{ir}^{\epsilon}(m) f_i^{\epsilon}(t') \psi_i^{\epsilon}(\tau, m) \right|^2$$

- Production amplitude
- $t'$ -dependence (helicity “flip”)
- Decay amplitude (Helicity formalism, reflectivity basis)



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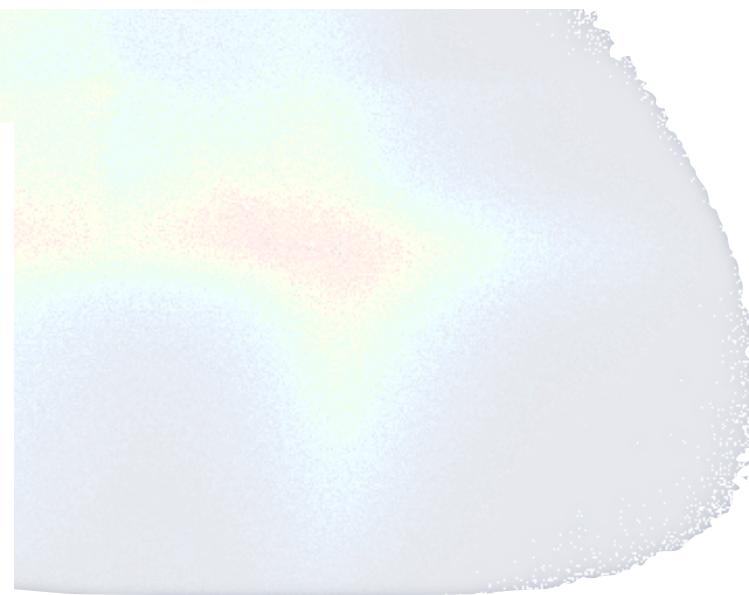
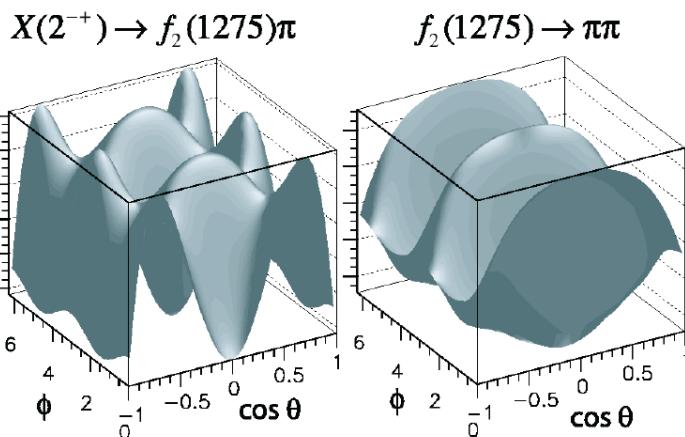
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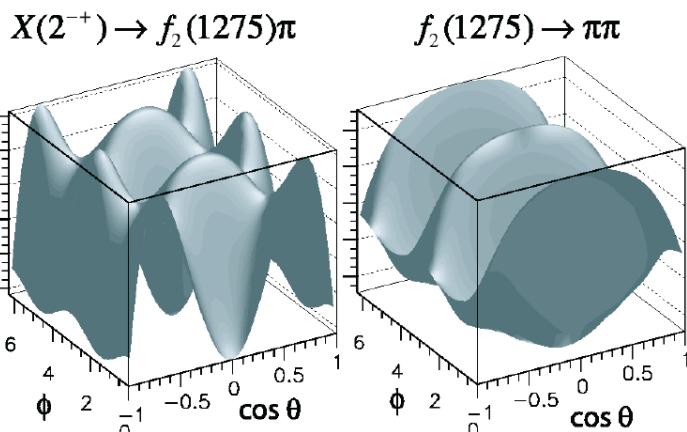
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## Example:



Obtain info about:

$$\text{Im}(T_i), \text{Re}(T_i), |T_i|^2$$

$$T_i(E) = T_i(m_x)$$

- Make **hypothesis** about all  $i \rightarrow$  fit
- Vary hypothesis**

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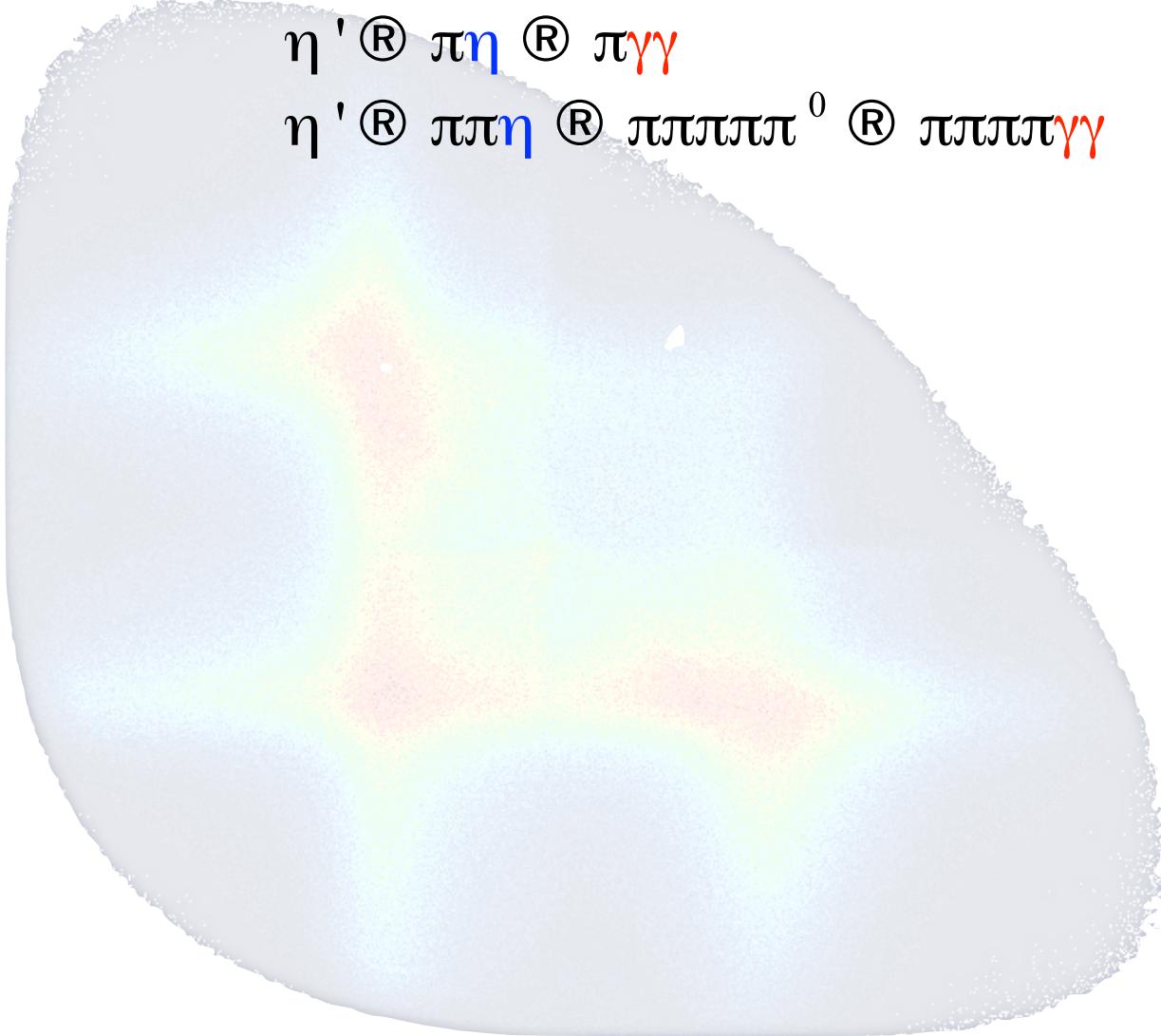
## Mass-Dependent $\chi^2$ fit → Extract Resonance Parameters

- Parameterization of spin-density matrix elements  $\sum_r T_{ir}^{\epsilon} T_{jr}^{\epsilon*}(m_x)$
- Takes into account **interference terms**
- Coherent background for some waves

# Zukünftige Arbeiten

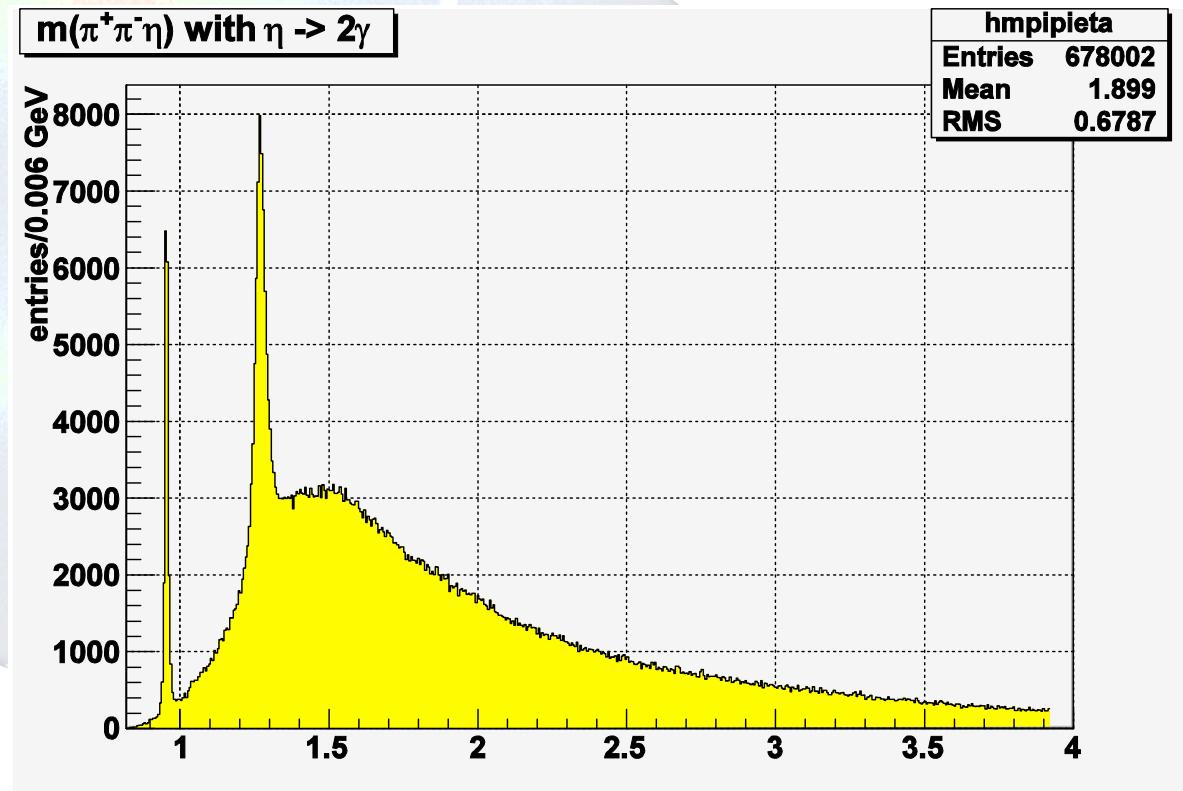
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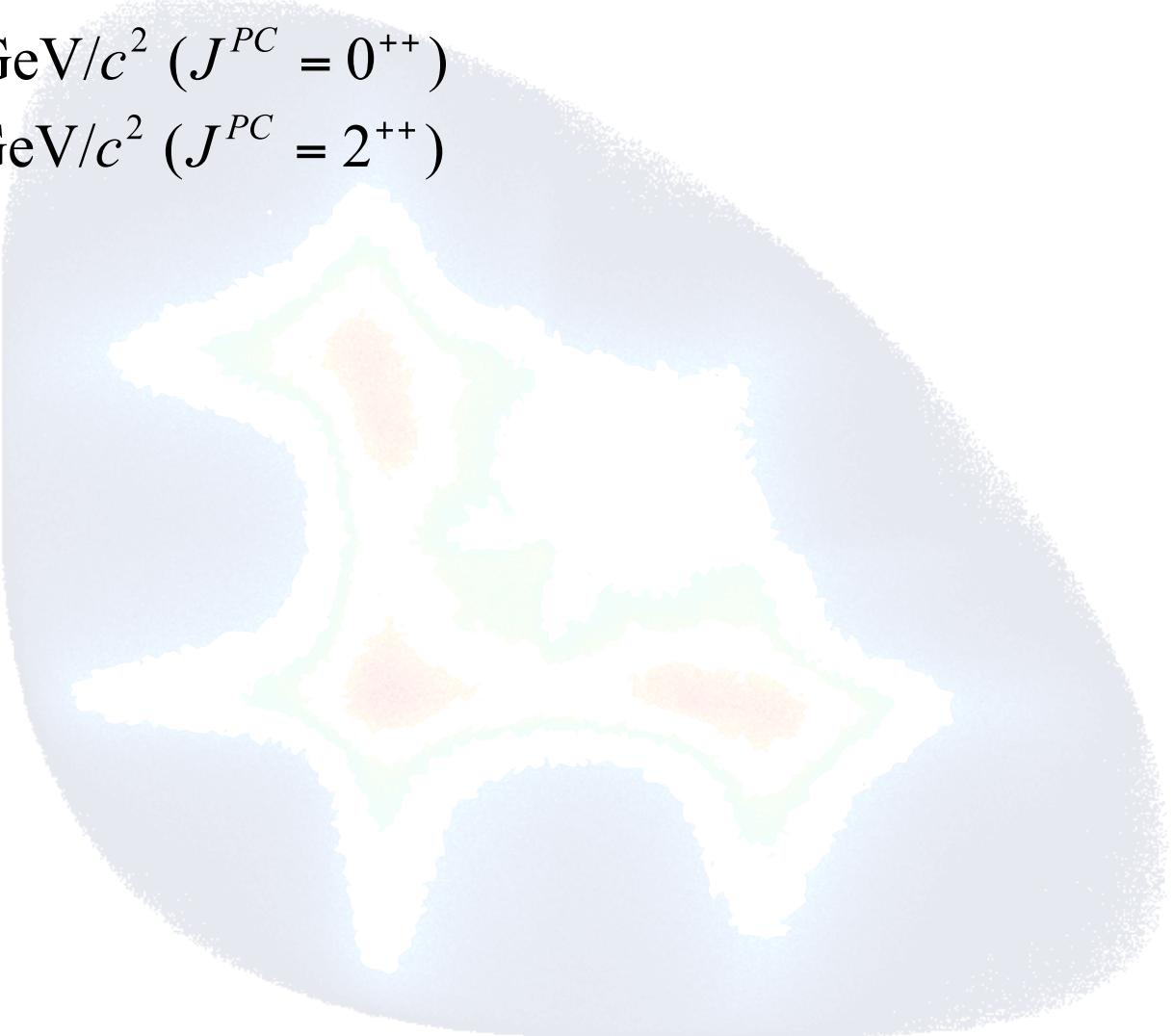
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- Reaction:  $p p \rightarrow p_f X p_s$ 
  - central production of  $X^0$
  - diffractive production of  $N^*$

## Leichteste Gluebälle:

- $M \sim 1.7 \text{ GeV}/c^2$  ( $J^{PC} = 0^{++}$ )
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 $J^{PC} = 0^{++} \Rightarrow$  Mischung mit isoskalaren Mesonen

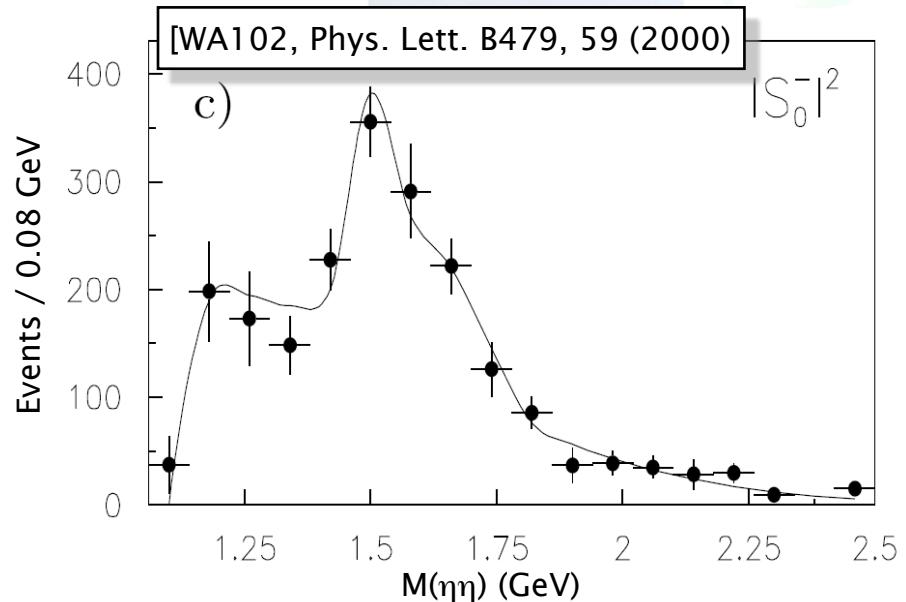
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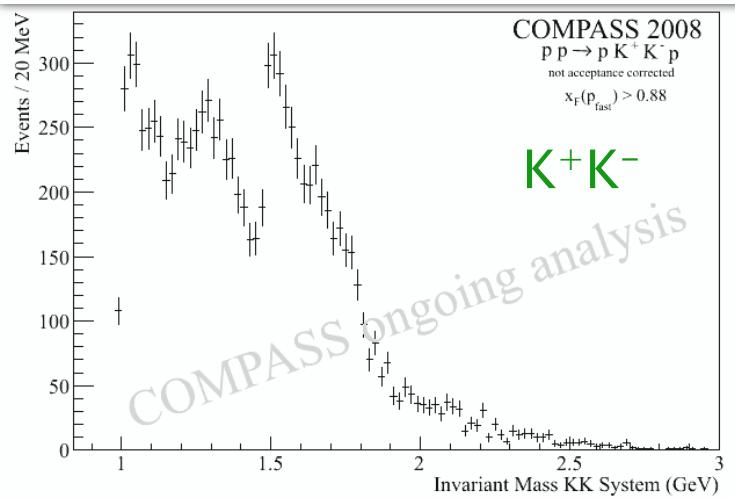
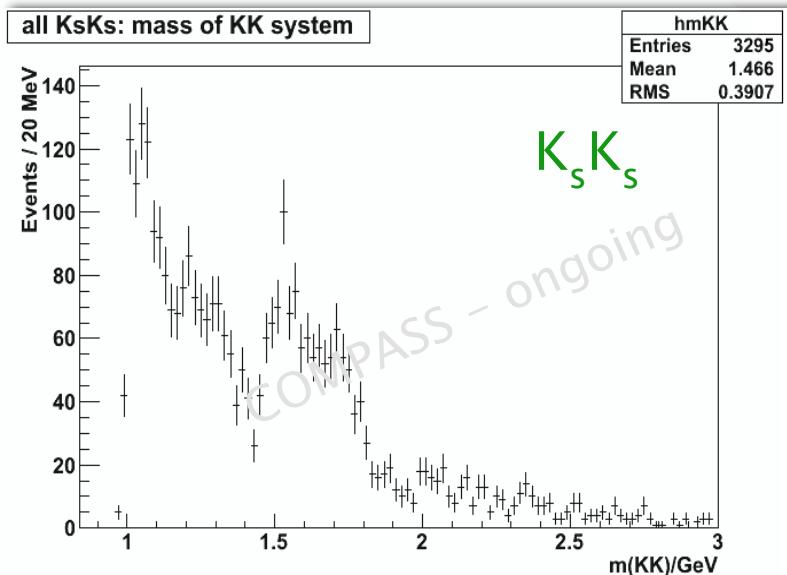
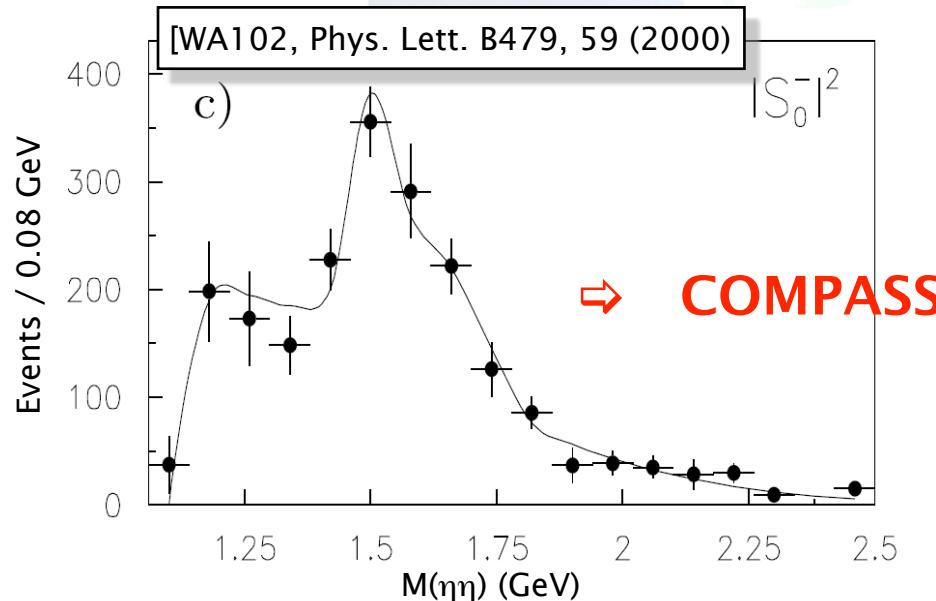
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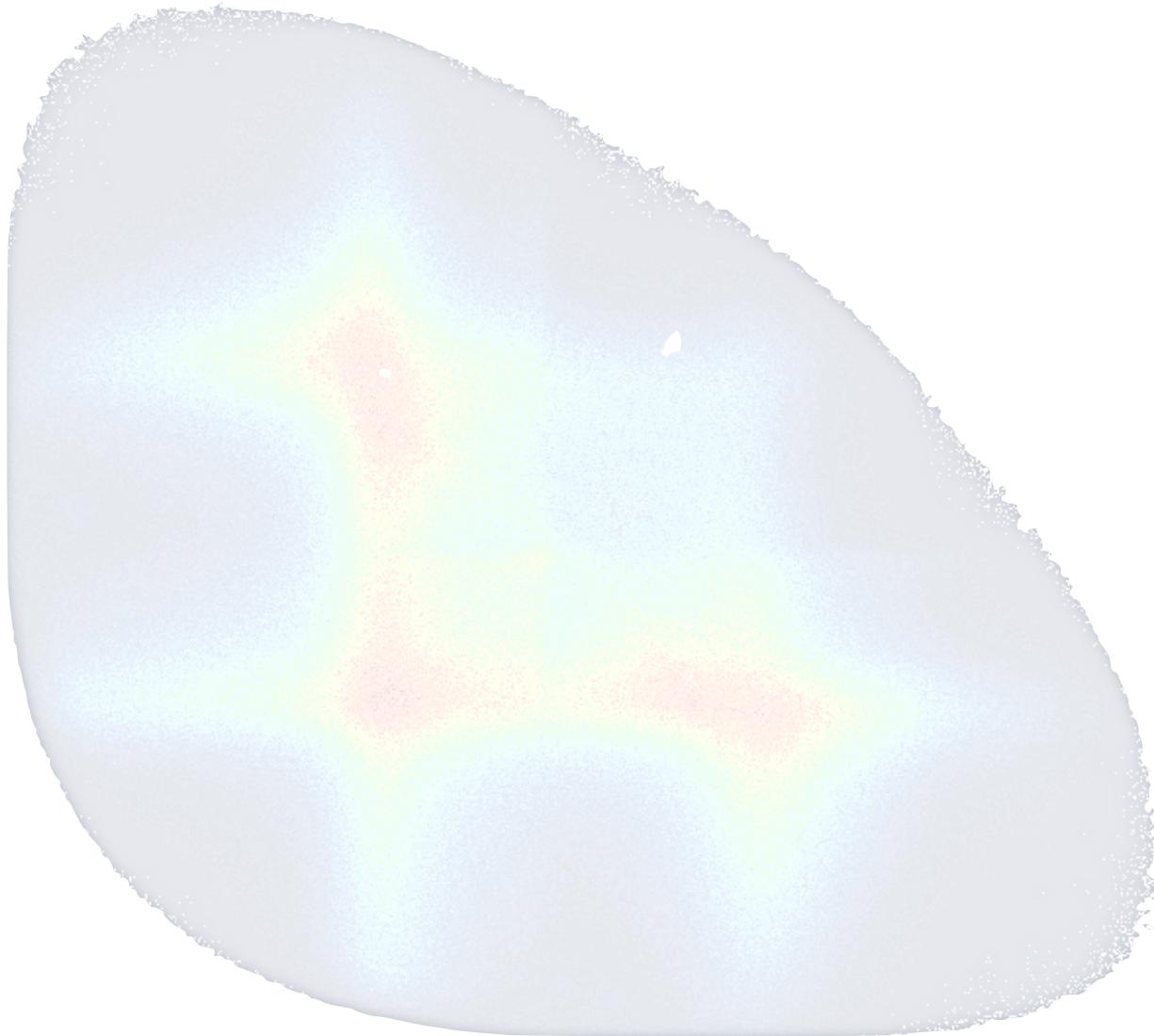
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Mesonen

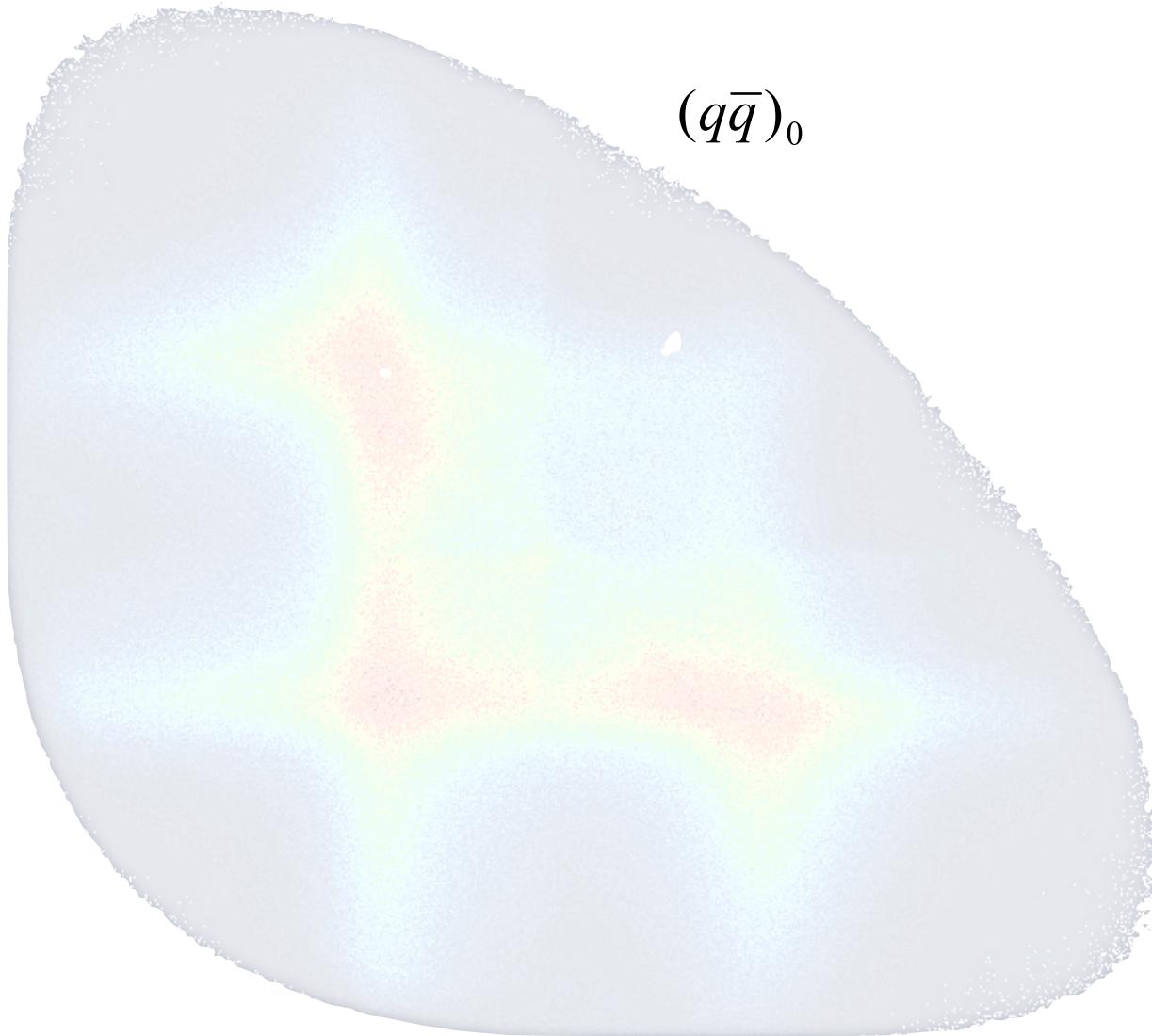


~ 10% der Statistik

# Coupling to Strangeness

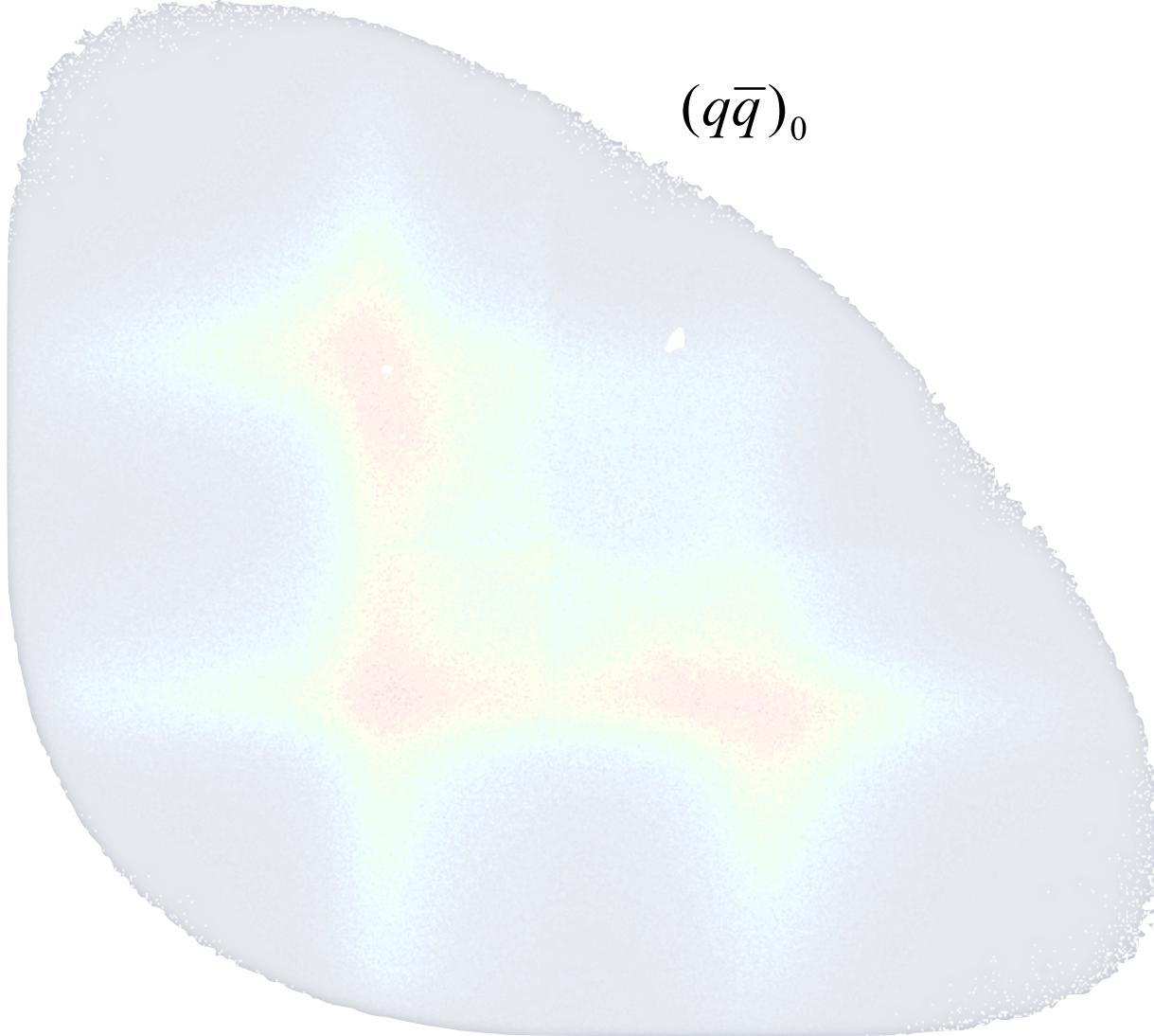


# Coupling to Strangeness



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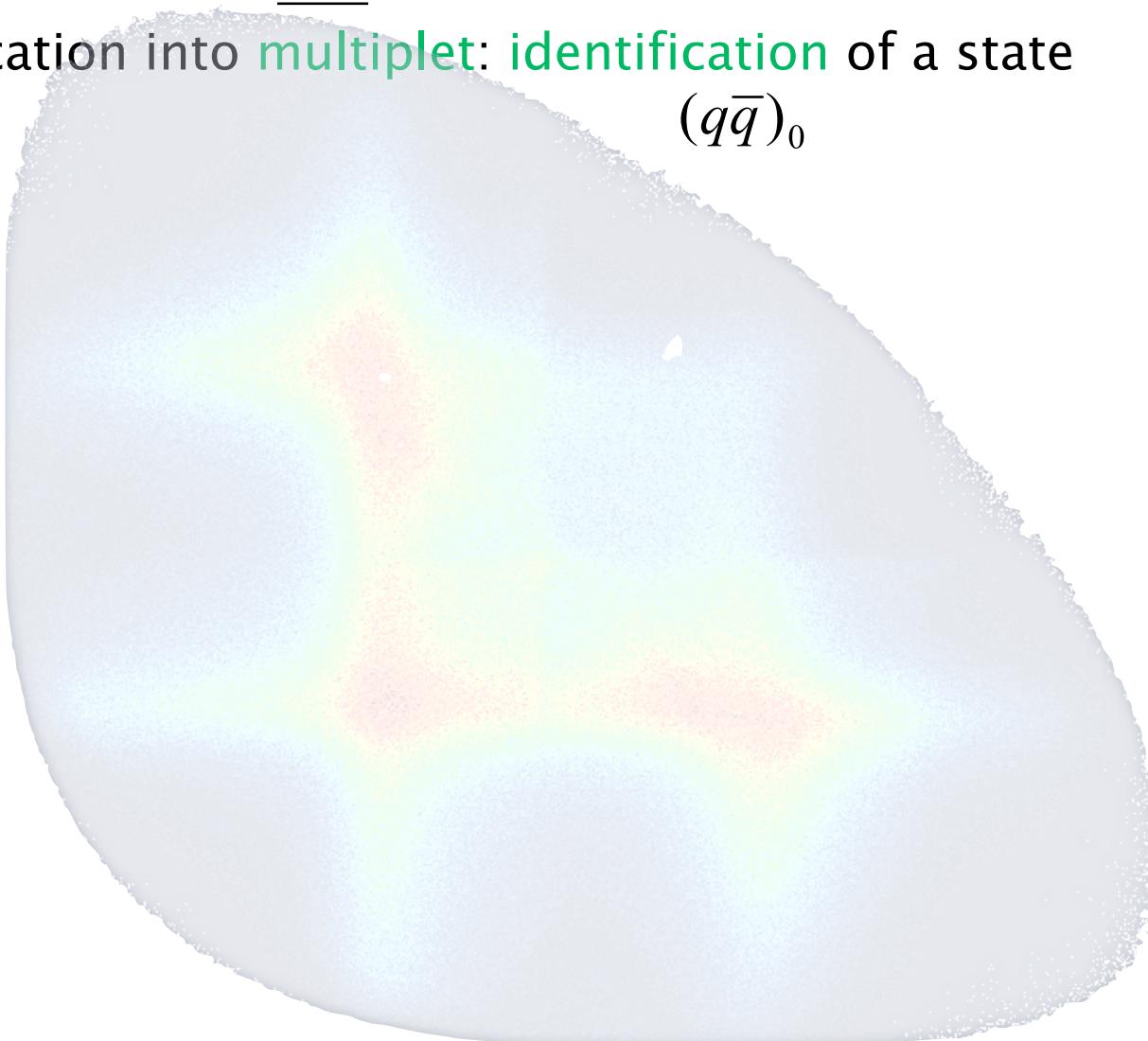
- Quantum numbers and flavour content of a state is relevant



# Coupling to Strangeness

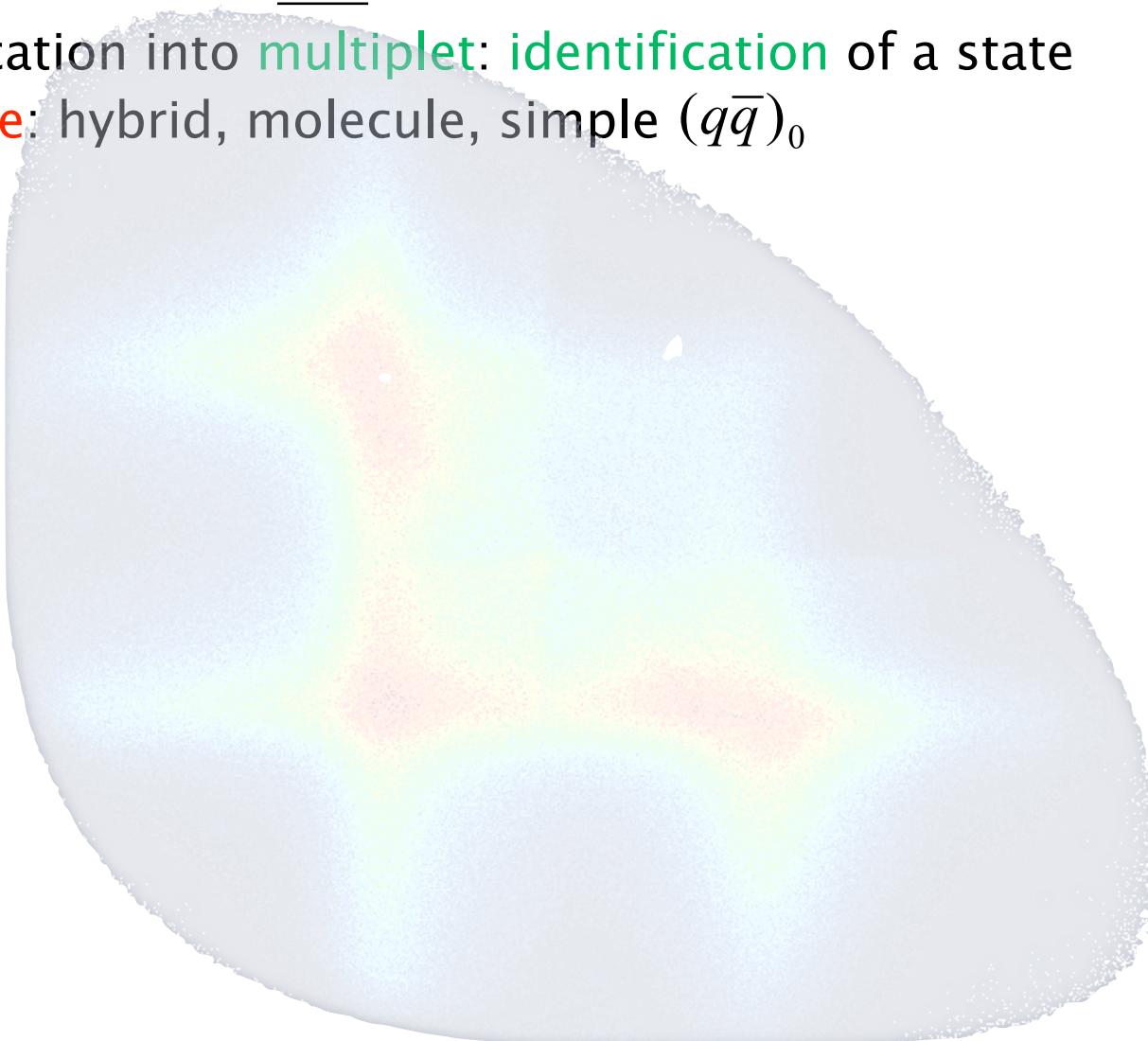
- Quantum numbers and flavour content of a state is relevant
- Classification into multiplet: identification of a state

$$(q\bar{q})_0$$



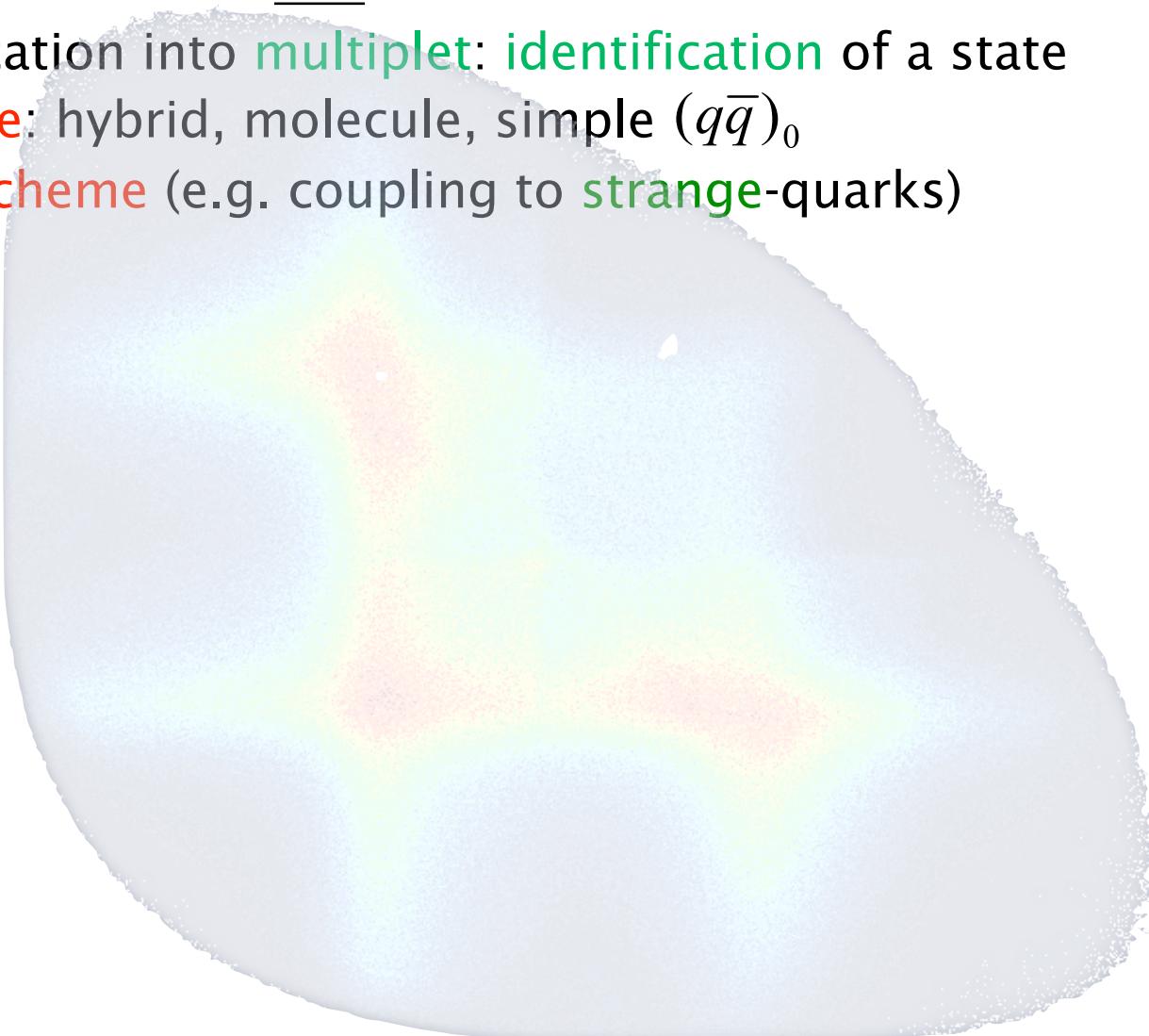
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- Structure: hybrid, molecule, simple  $(q\bar{q})_0$



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- Decay-scheme (e.g. coupling to strange-quarks)

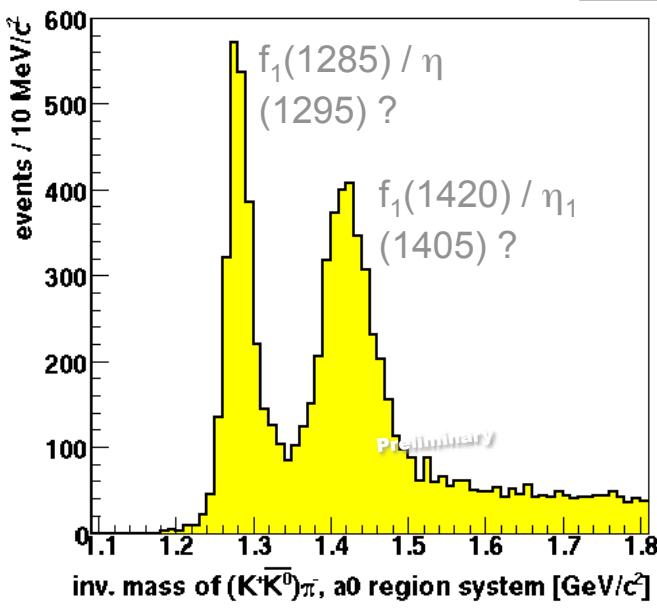


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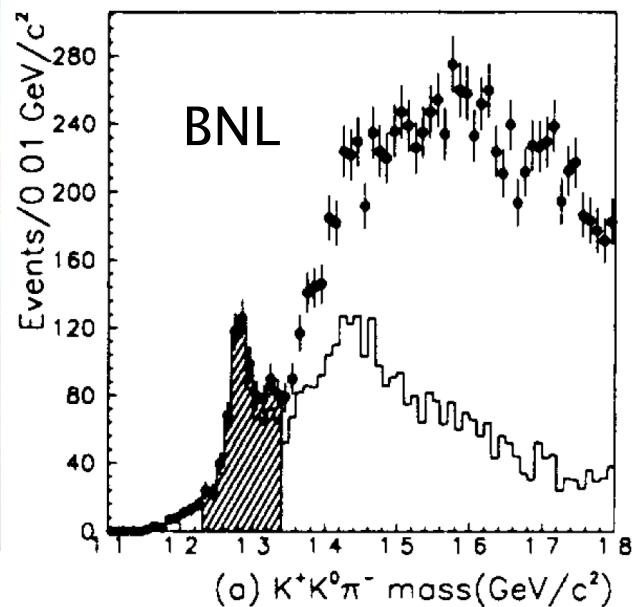
- Quantum numbers and flavour content of a state is relevant
- Classification into multiplet: identification of a state
- Structure: hybrid, molecule, simple  $(q\bar{q})_0$
- Decay-scheme (e.g. coupling to strange-quarks)
- Consider diffractive production

$$\pi^- p \circledR \bar{K} K \pi \pi^- p$$

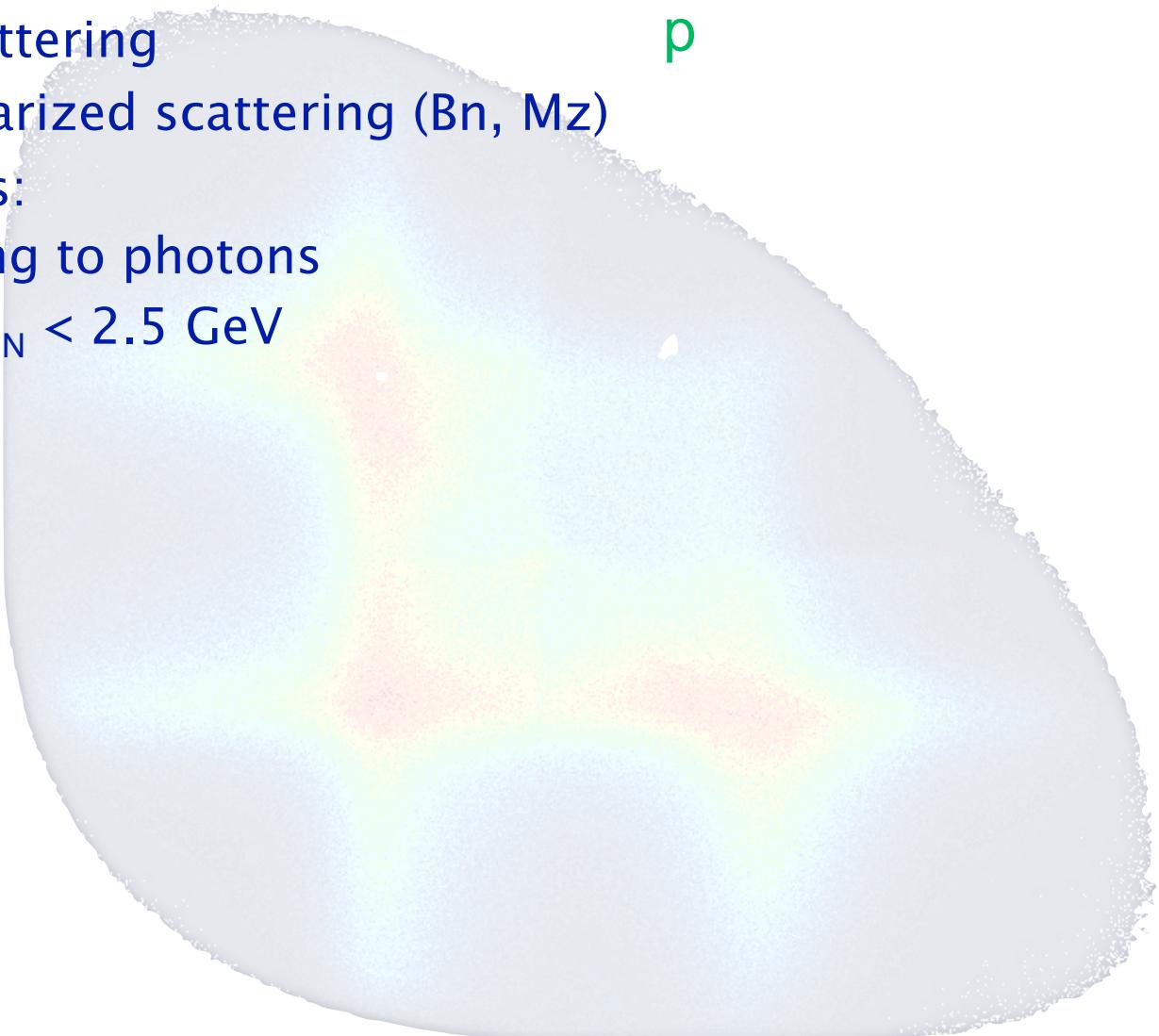
Endzustand:  $\bar{K}^0 K^+ \pi^- \pi^-$  und  $\bar{K}^- K^0 \pi^+ \pi^-$



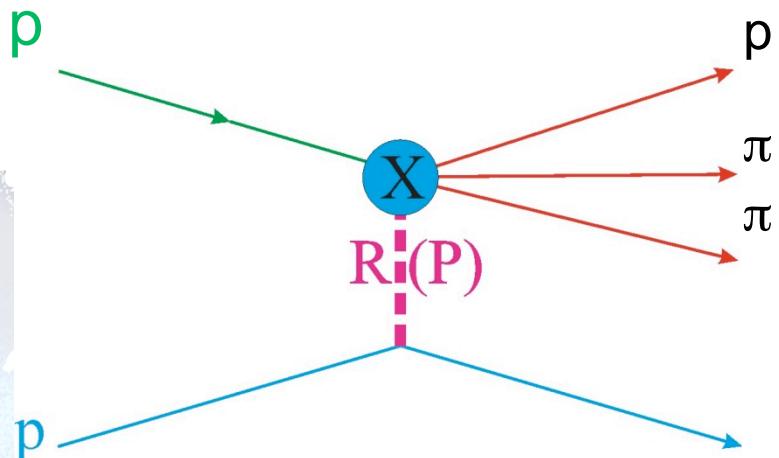
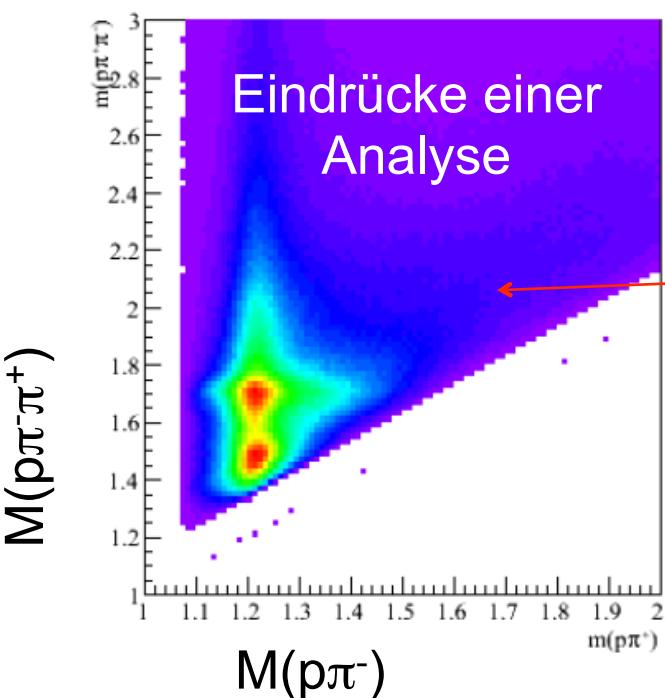
Physics Letters B 323 (1994) 227–232  
North-Holland



- Baryon spectroscopy in
  - $\pi N$  scattering
  - $\gamma N$  polarized scattering ( $B_N$ ,  $M_z$ )
- Limitations:
  - Coupling to photons
  - Mass  $M_N < 2.5$  GeV



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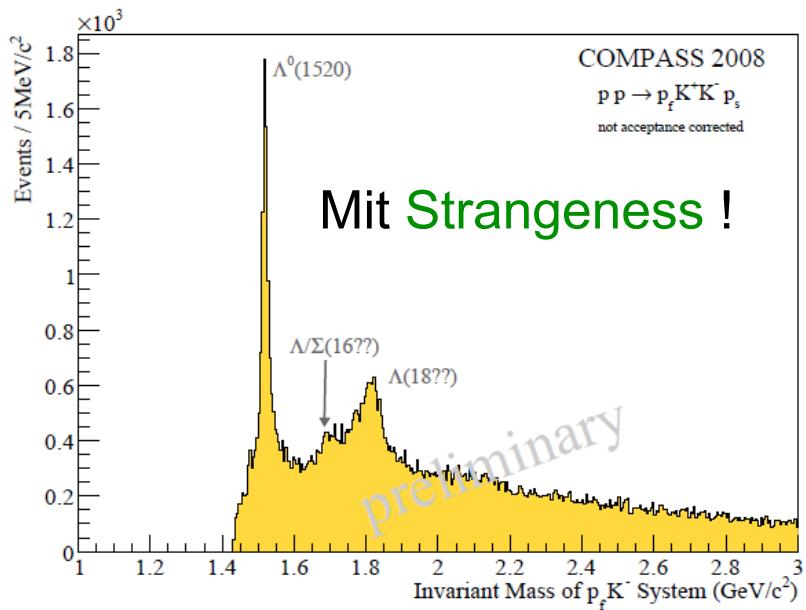
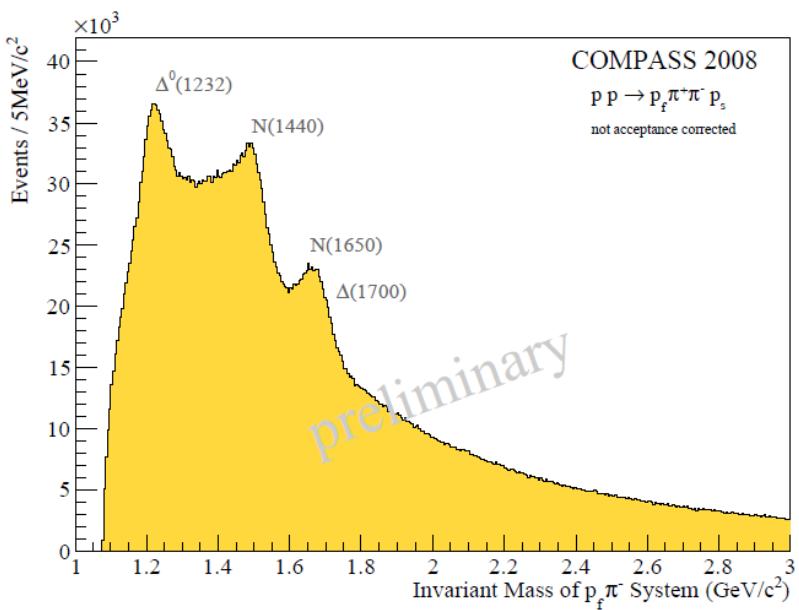
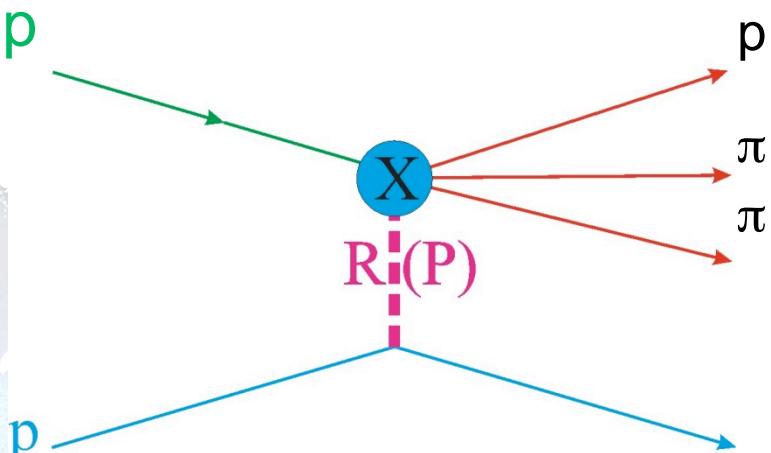


**COMPASS** can create high **masses**

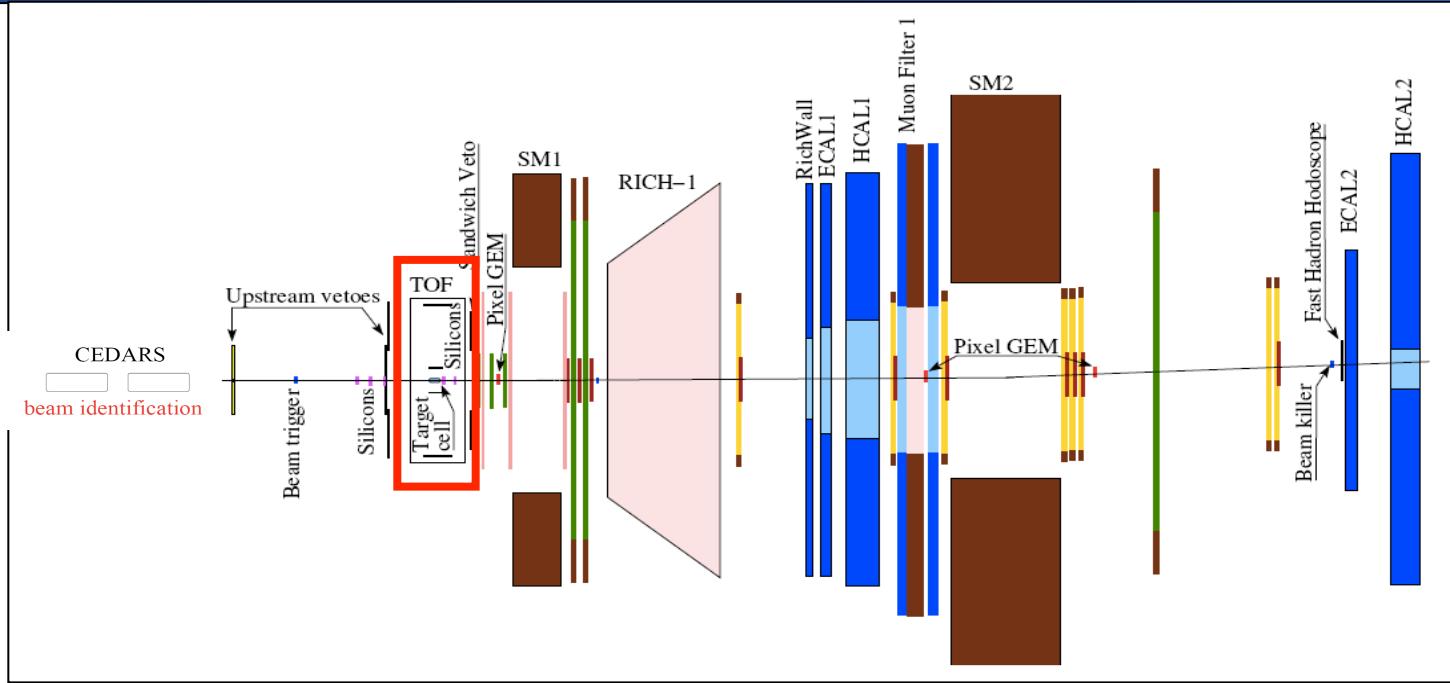
Ca. 15% of statistics

PWA formalism being developed

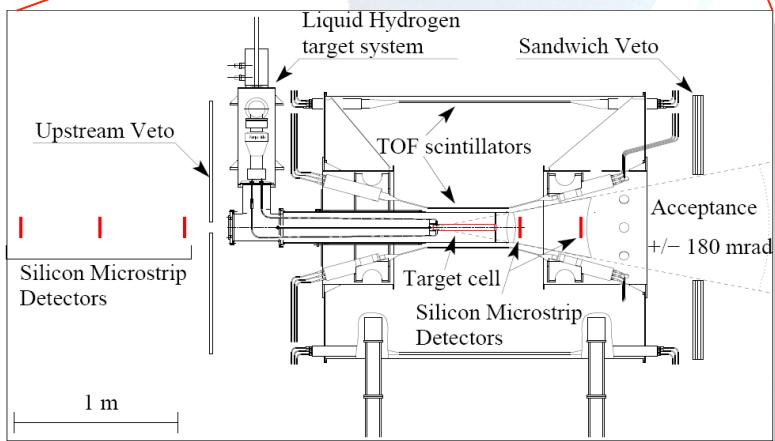
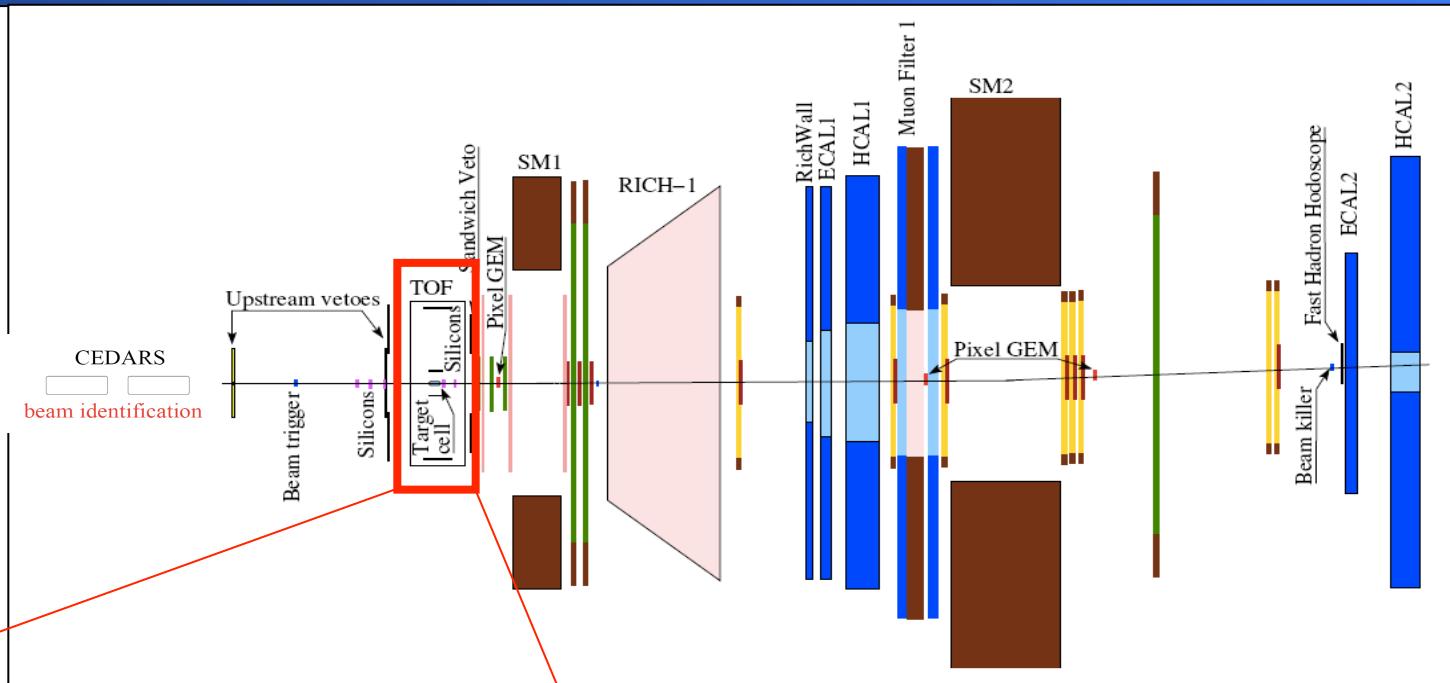
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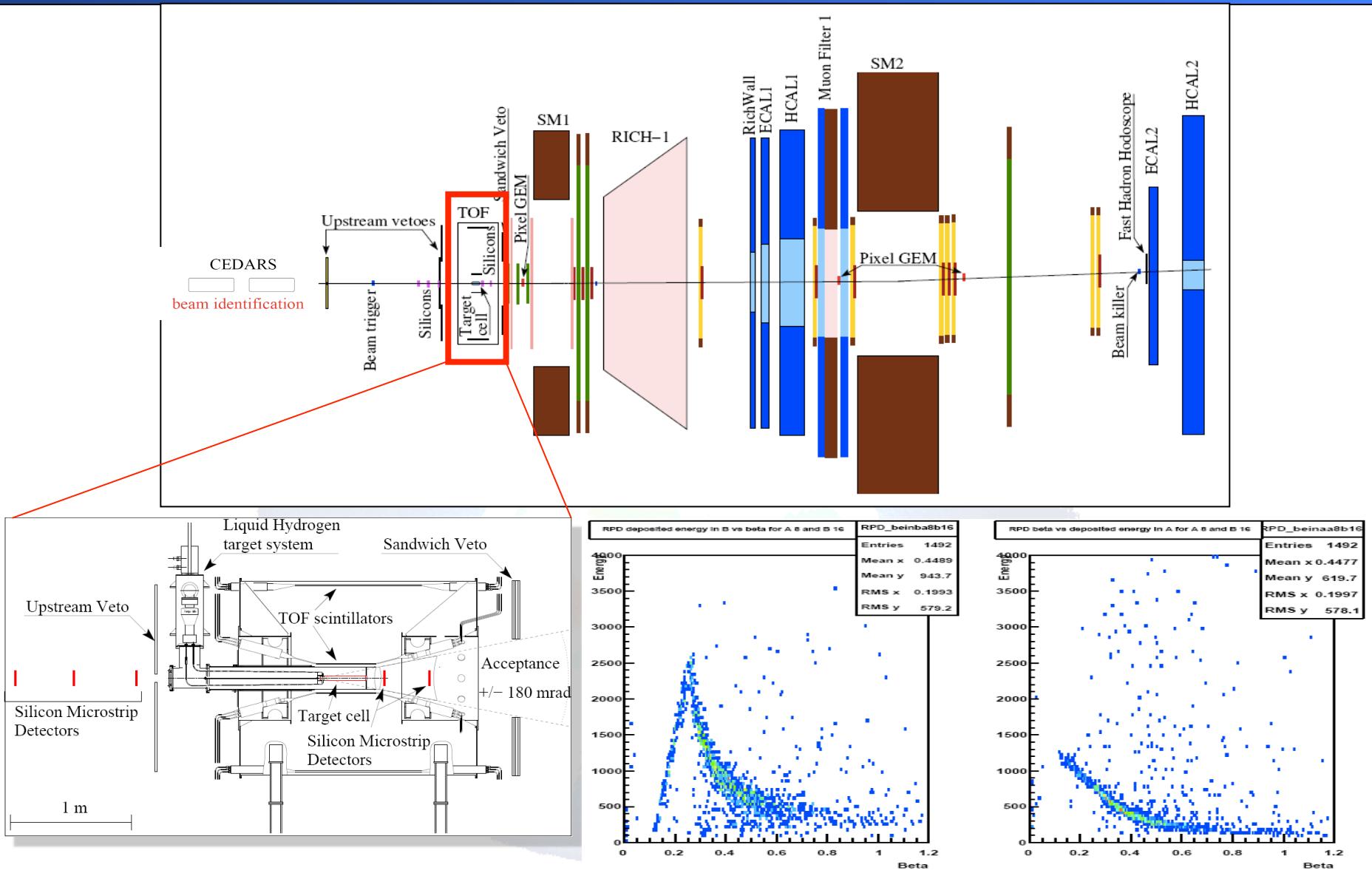
# COMPASS in 2008



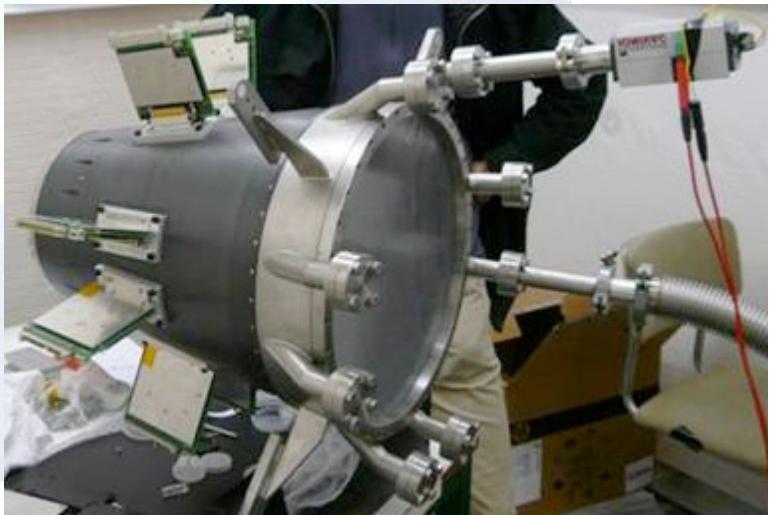
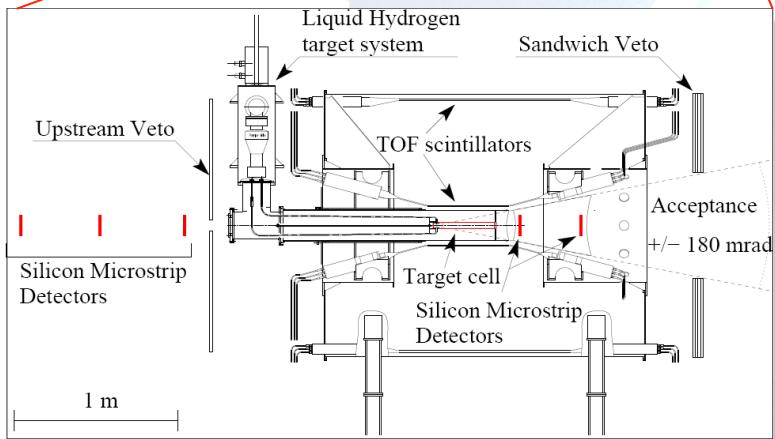
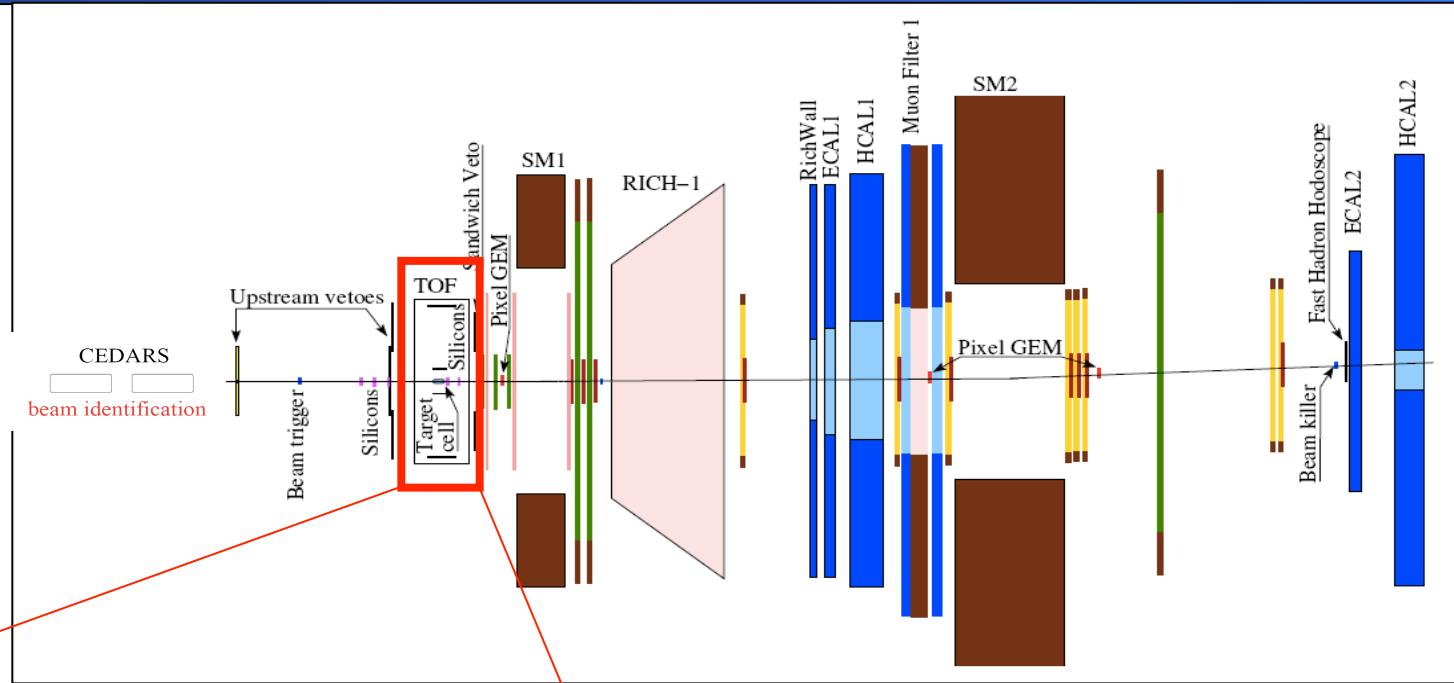
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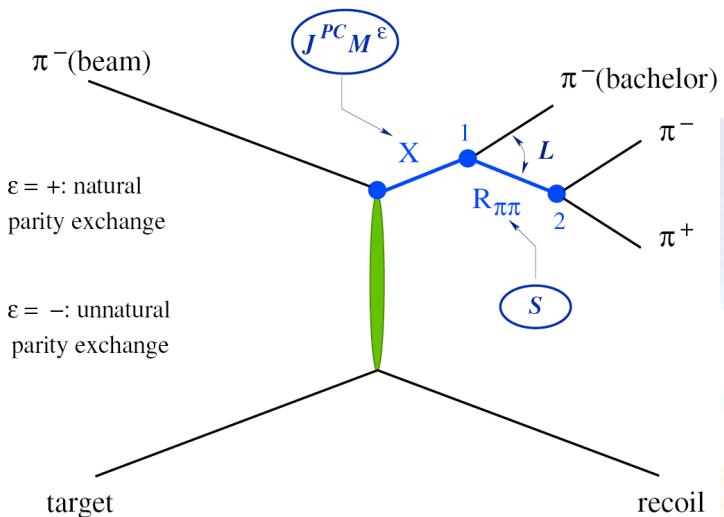
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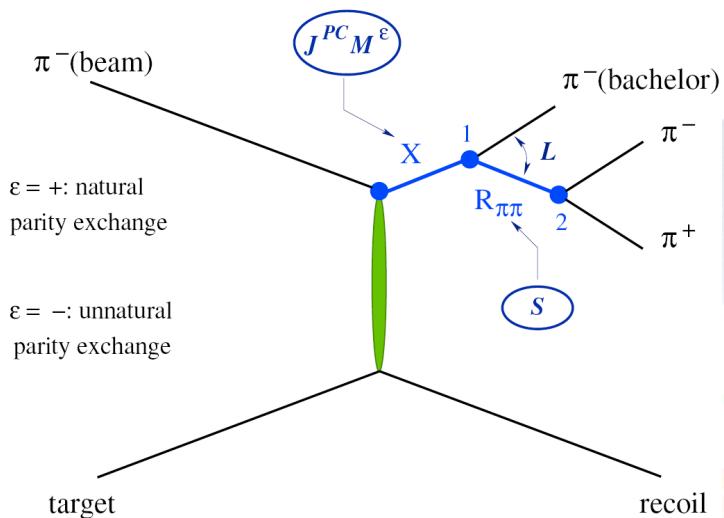


# PWA Technique



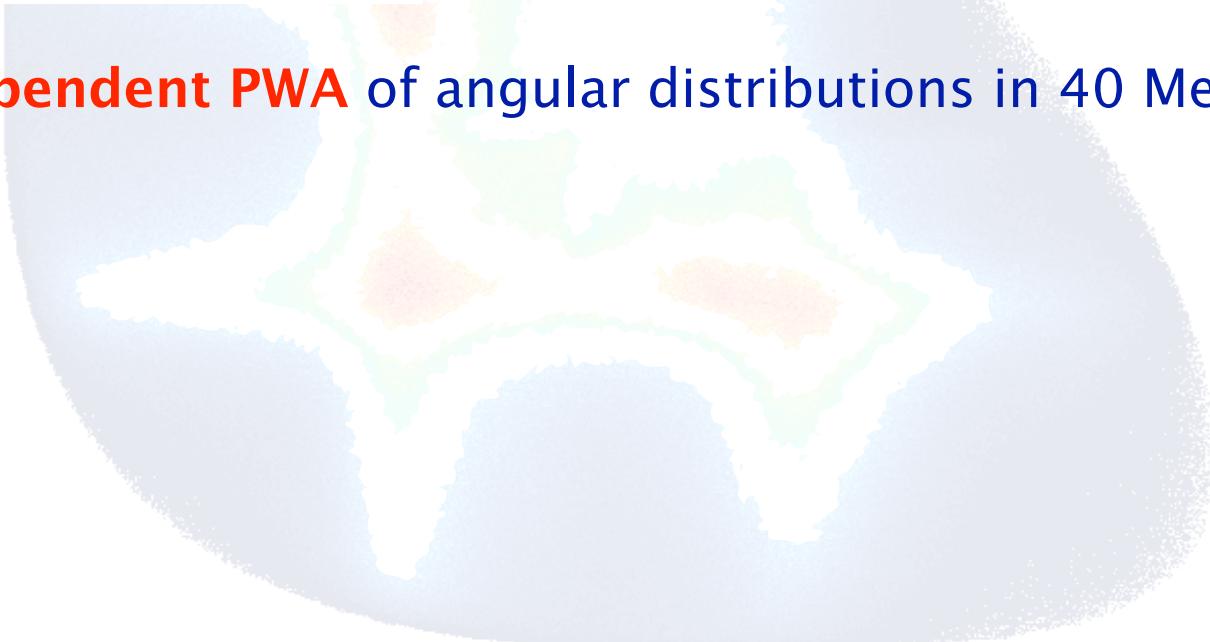
- high  $s$ : t-channel Reggeon exchange
- Reflectivity basis in G-J frame
- $\epsilon = \eta$  of Regge trajectory
- Isobar model

# PWA Technique

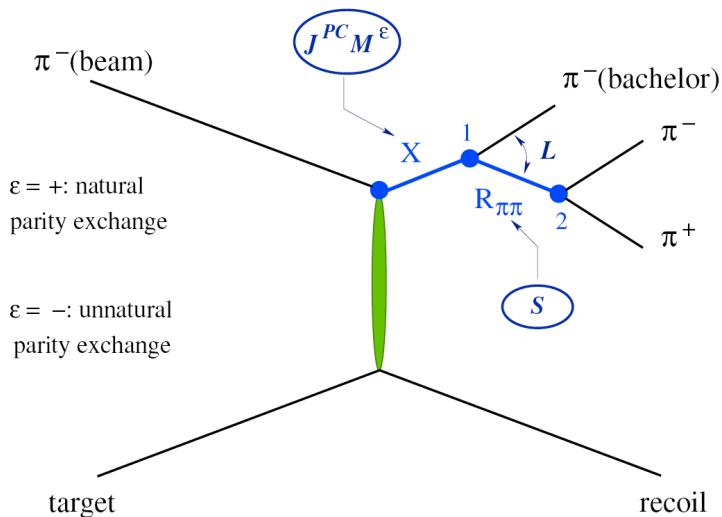


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## 1. Mass-independent PWA of angular distributions in 40 MeV mass bins



# PWA Technique



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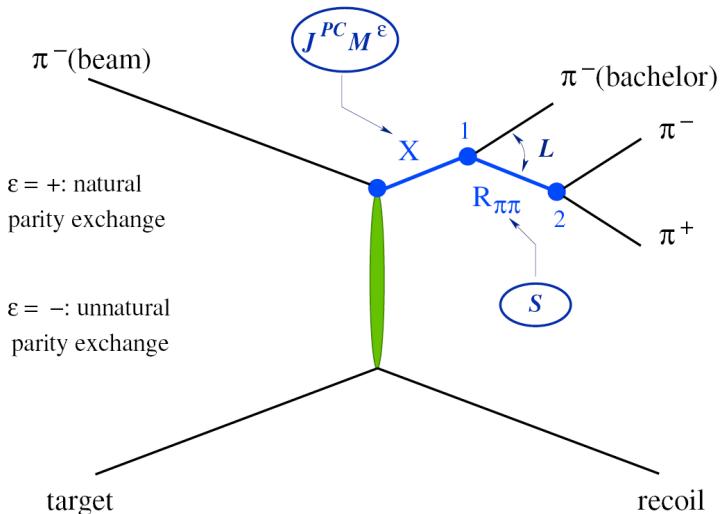
$$\sigma_{\text{indep}}(\tau) = \sum_{\epsilon=-1}^1 \sum_{r=1}^{N_r} \left| \sum_i T_{ir}^\epsilon \psi_i^\epsilon(\tau) \Big/ \sqrt{\int |\psi_i^\epsilon(\tau')|^2 d\tau'} \right|^2$$

•  $T_{ir}^\epsilon$  production amplitudes - determined by fit

• 42 partial waves  $i = J^{PC} M^\epsilon [...] L$

$[...] = \text{isobar}: (\pi\pi)_S, f_0(980), \rho(770), f_2(1270), \rho_3(1690)$

# PWA Technique



- high  $s$ : t-channel Reggeon exchange
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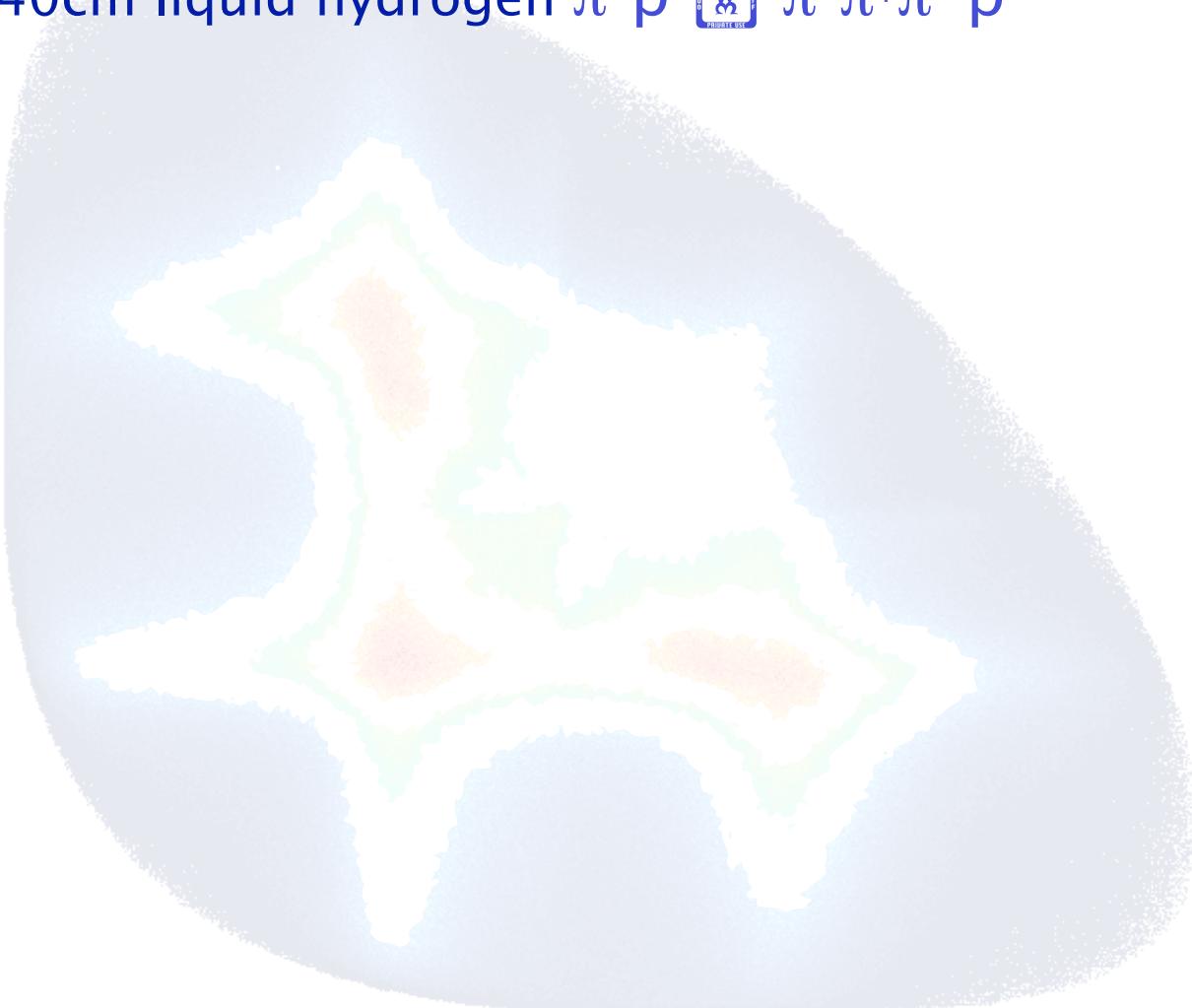
1. **Mass-independent PWA** of angular distributions in 40 MeV mass bins

2. **Mass-dependent  $\chi^2$  fit** to results of step 1

- 6 waves
- Parameterized by BW (incl. barrier factors and  $\Gamma(m)$ )
- Coherent background for some waves

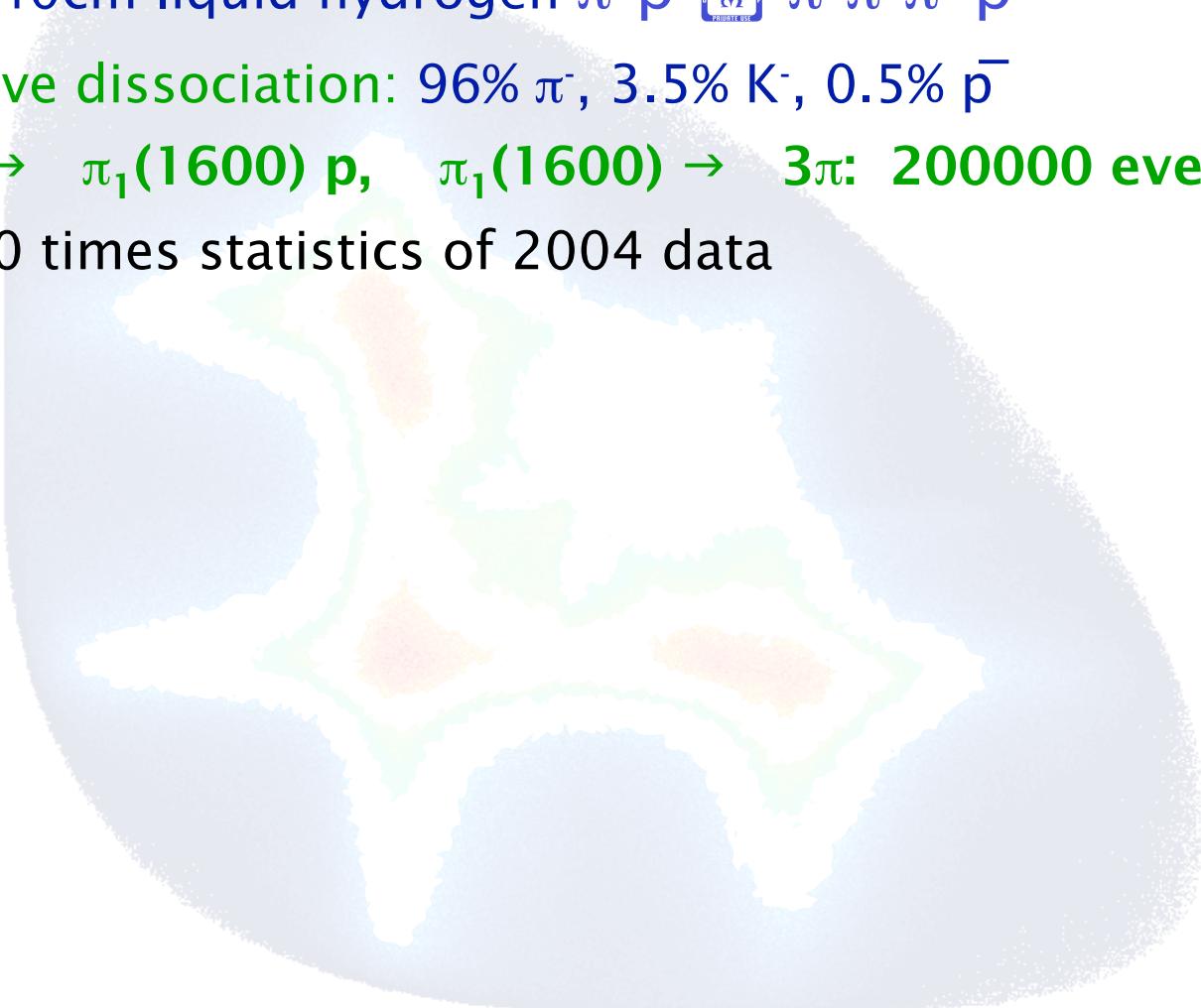
# $\pi^-\pi^+\pi^-$ in 2008

- 190 GeV/c hadron beam
- Target: 40cm liquid hydrogen  $\pi^- p \rightarrow \pi^-\pi^+\pi^- p$

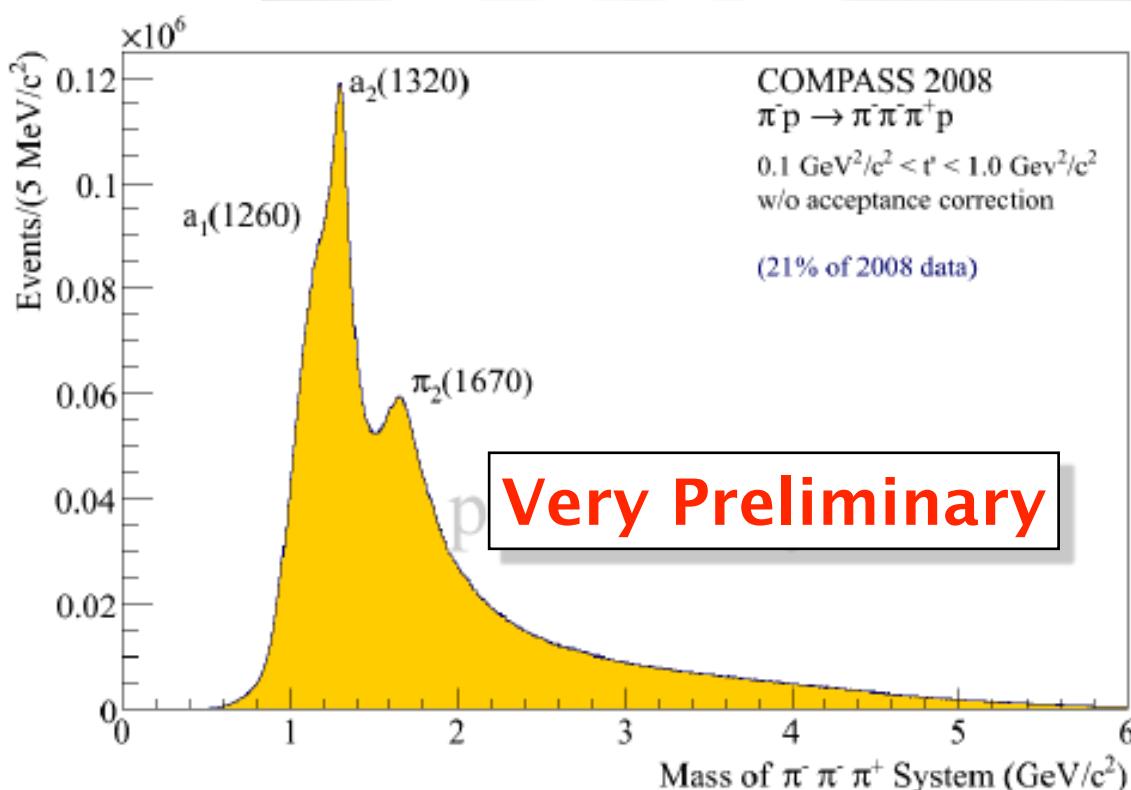


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- Diffractive dissociation: 96%  $\pi^-$ , 3.5%  $K^-$ , 0.5%  $p^-$ 
  - $\pi^- p \rightarrow \pi_1(1600) p, \pi_1(1600) \rightarrow 3\pi$ : **200000 events exp.** ✓
  - >200 times statistics of 2004 data

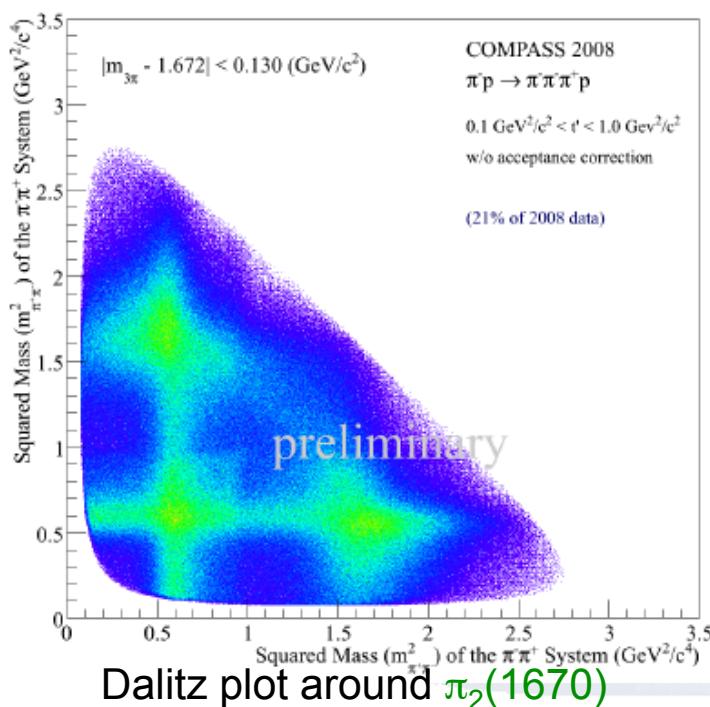


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see talk by S. Neubert

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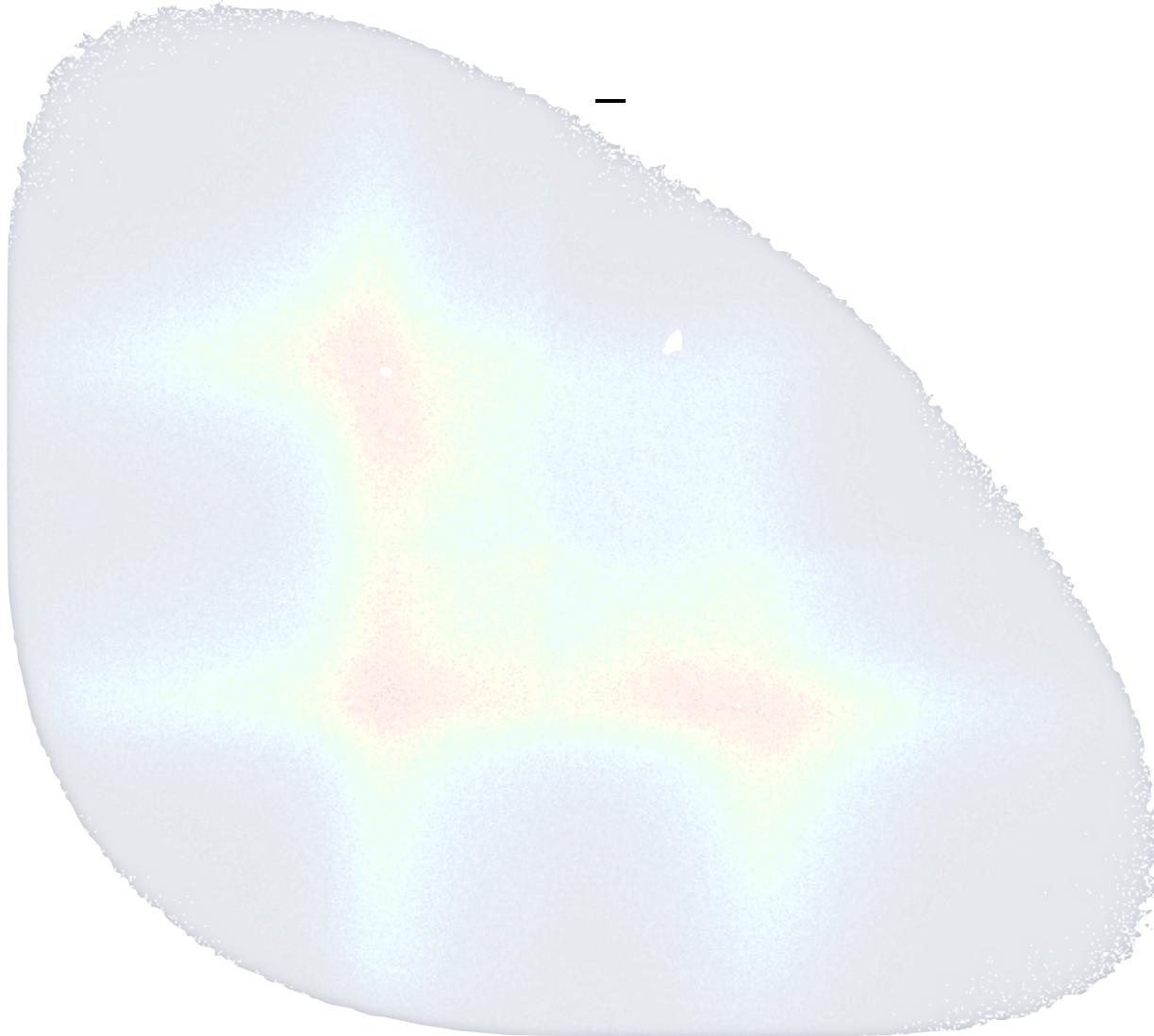
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  - ! High statistics requires perfect understanding of physics
  - Deck effect (under study)
  - Up to date parametrization of  $\pi\pi$  scattering

see talk by S. Neubert

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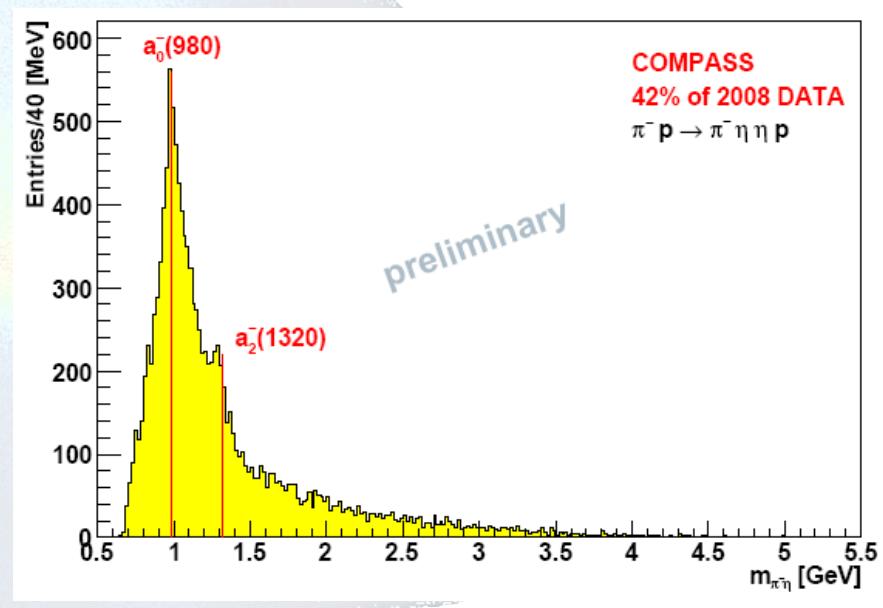
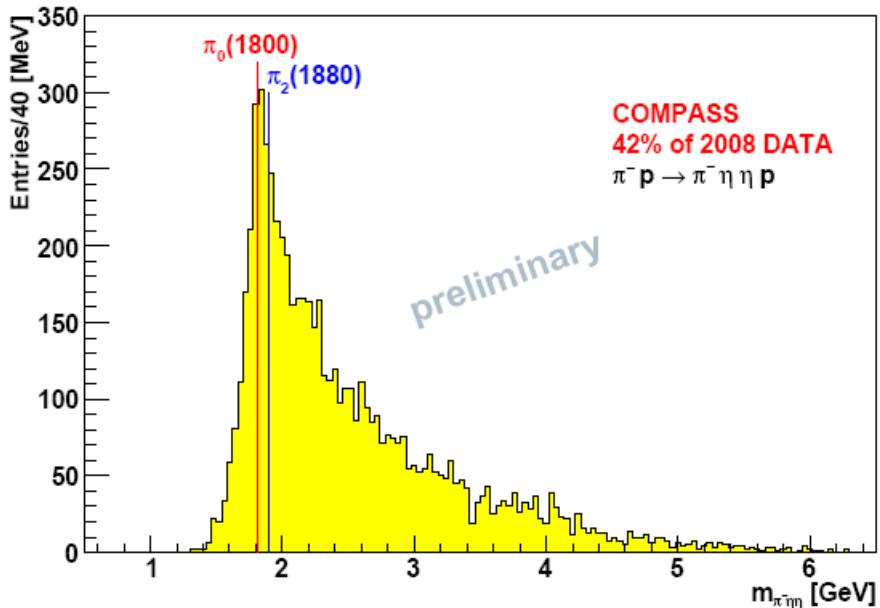
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  - Up to date parametrization of  $\pi\pi$  scattering
- First result: compare production on proton and lead
  - ! m-population is different: Pb prefers higher m values

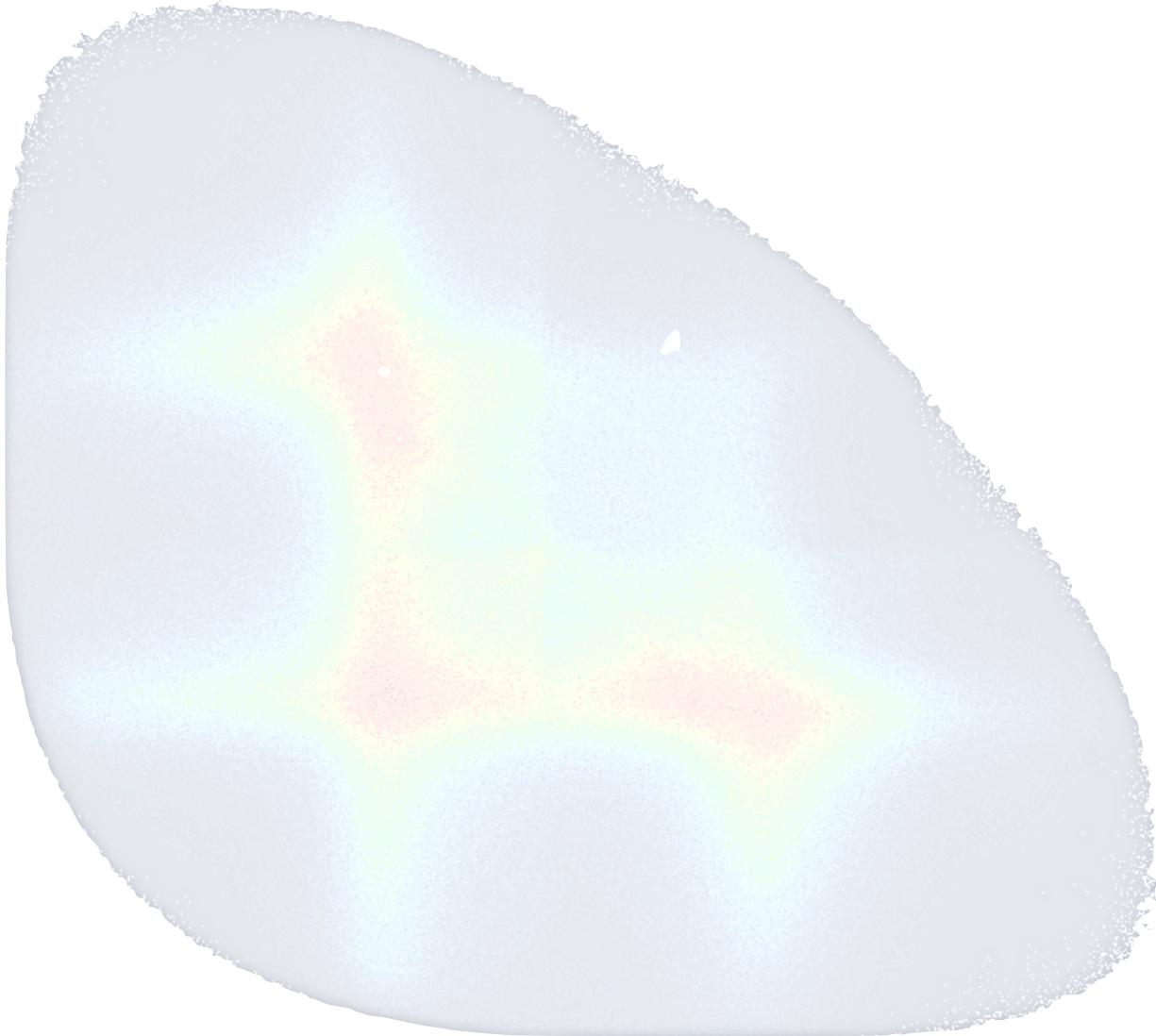
see talk by S. Neubert



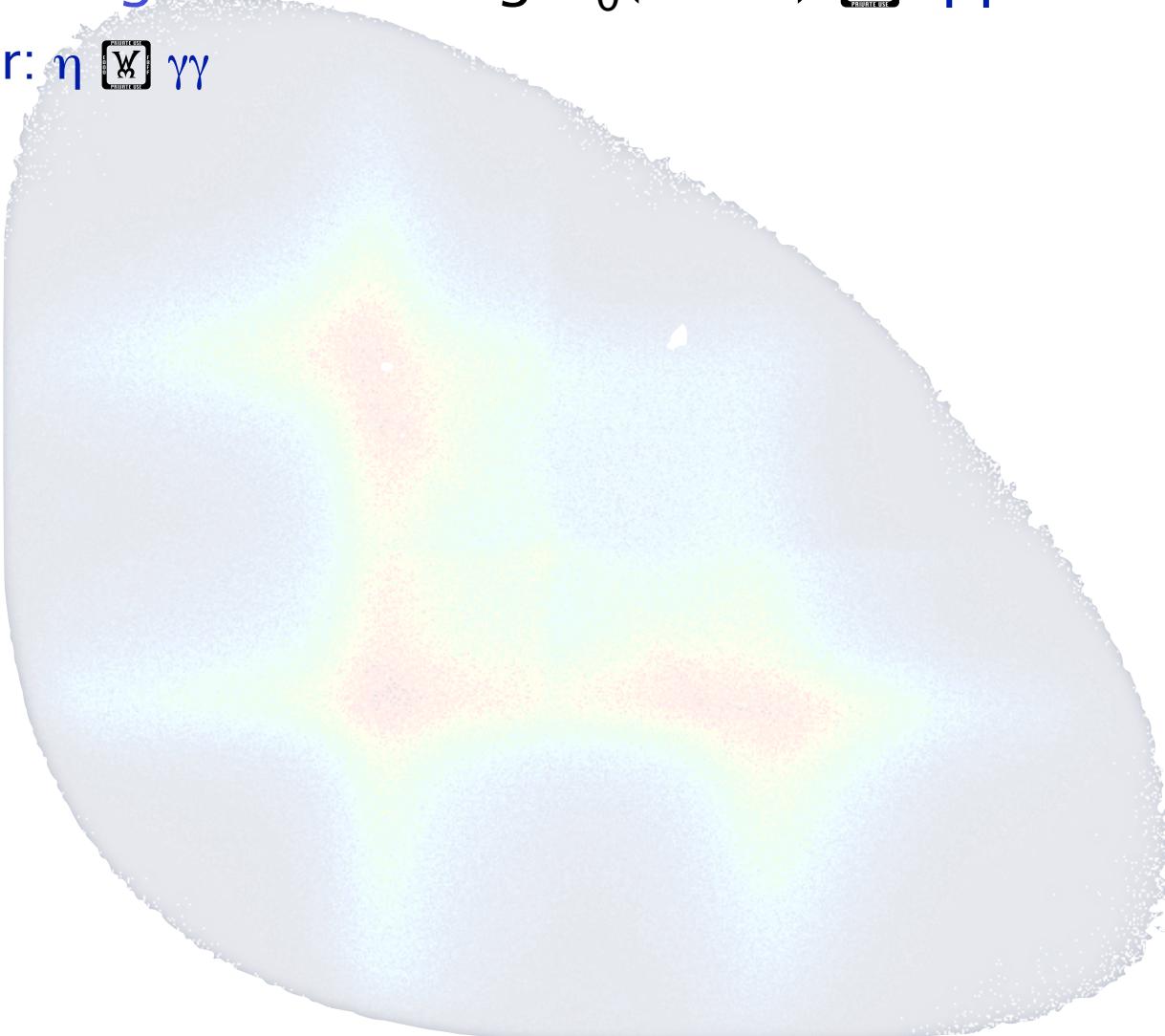
- Search for **exotics** - e.g.  $\pi(1400)$   $\pi^- \eta$ 
  - **Seen** by E852 exp. in 1997  $\pi^- p \rightarrow \pi^- \eta$   $p$  at 18 GeV/c
  - **Confirmed** by CBAR exp. in 1998 in  $pd \rightarrow \pi^- \eta \pi^0 p_{spectator}$
  - **Questioned** by Dzierba et al. in 2003 in  $\pi^- p \rightarrow \pi^0 \eta \eta$  at 18 GeV/c

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- Diffractive production:

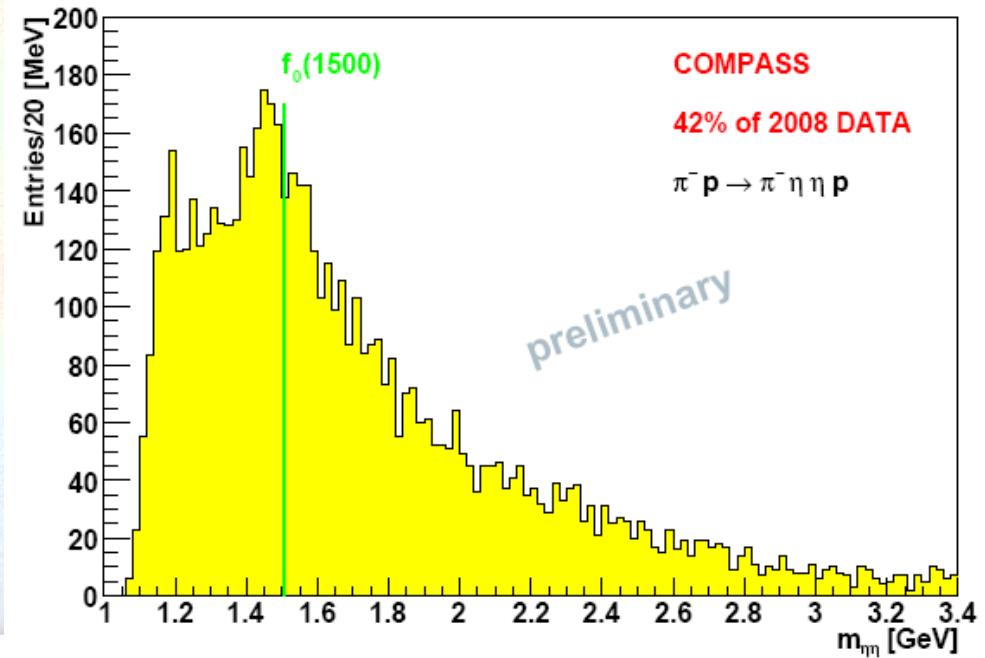
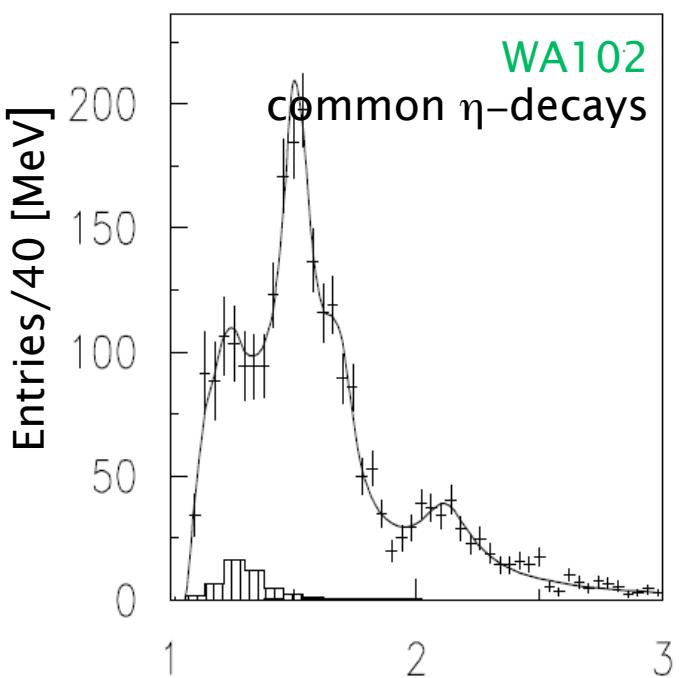




- Search for glueballs - e.g.  $f_0(1500)$    $\eta\eta$ 
  - So far:  $\eta$    $\gamma\gamma$

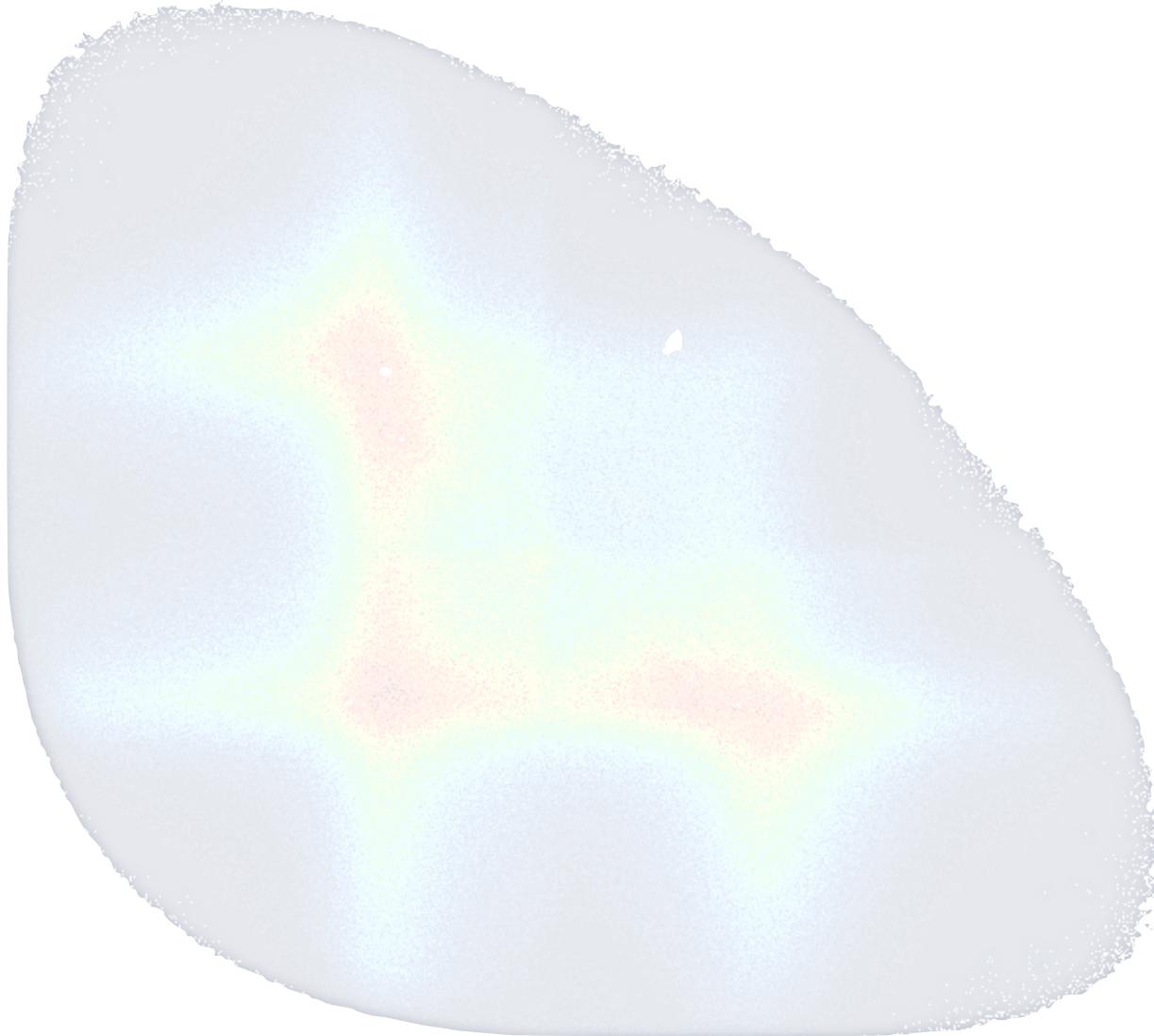


- Search for glueballs - e.g.  $f_0(1500)$   $\eta\eta$ 
  - So far:  $\eta$   $\gamma\gamma$
- Central Production assumed:
  - Structure consistent with  $f_0(1500)$  observed
  - > 10 times statistics of WA102

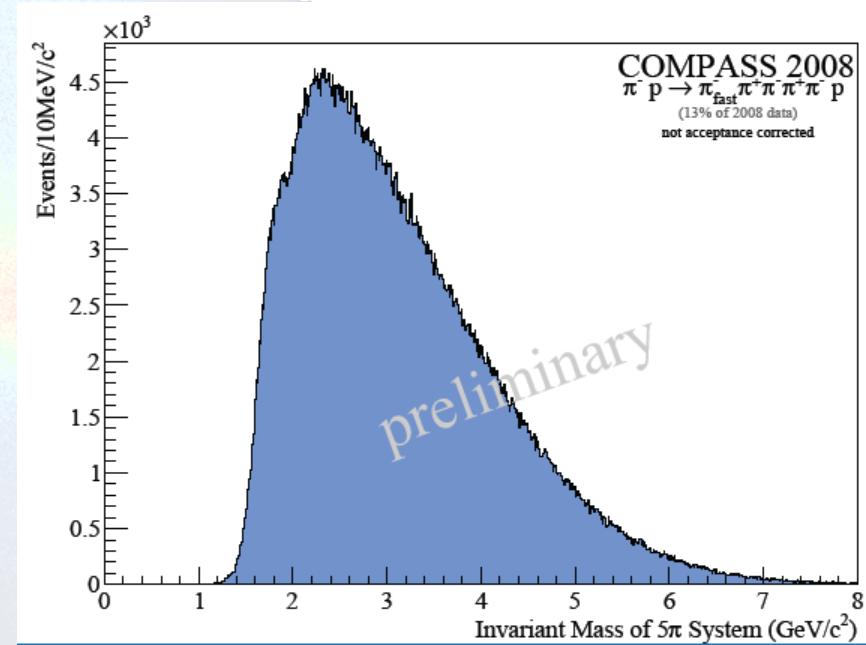
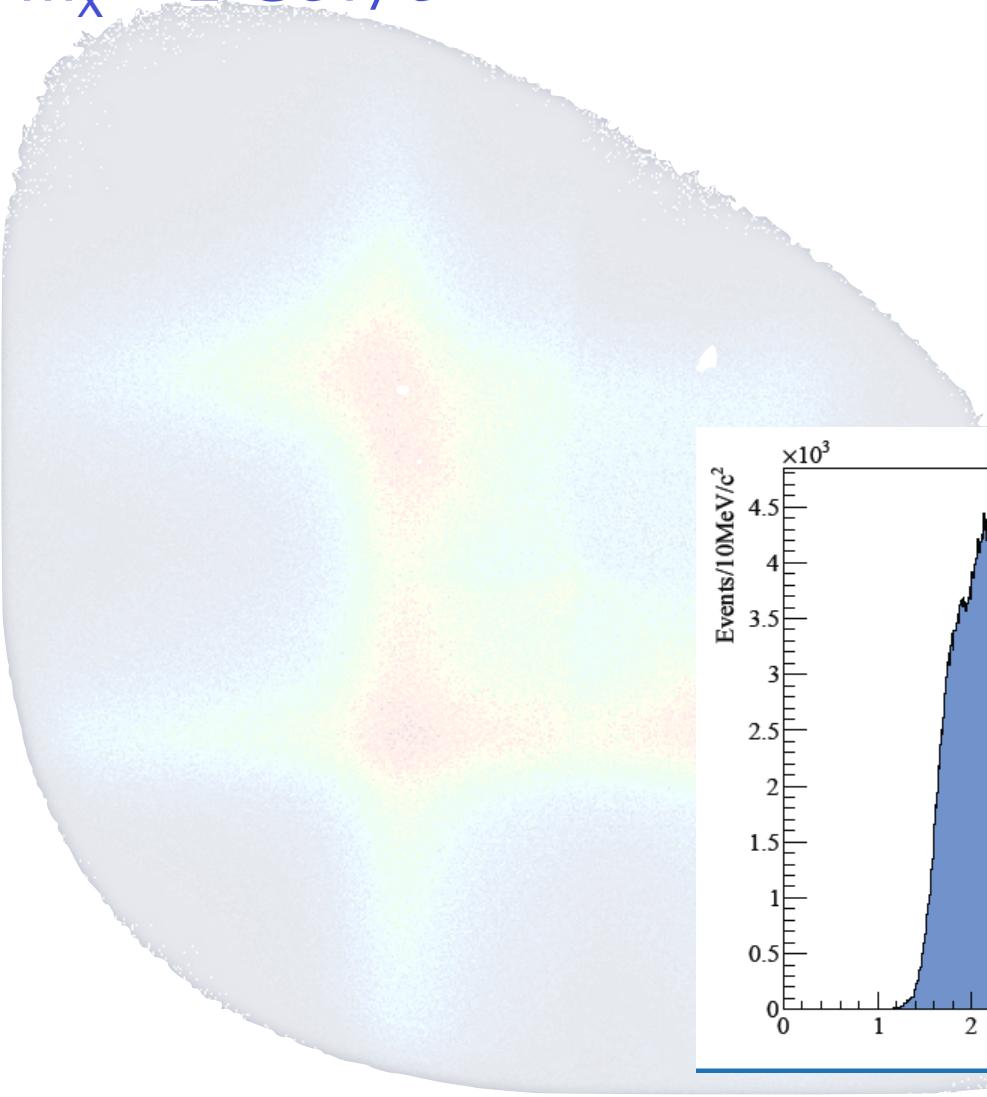




# Multi $\pi$ final states $\pi^- p \rightarrow \pi^-\pi^+\pi^-\pi^+\pi^- p$

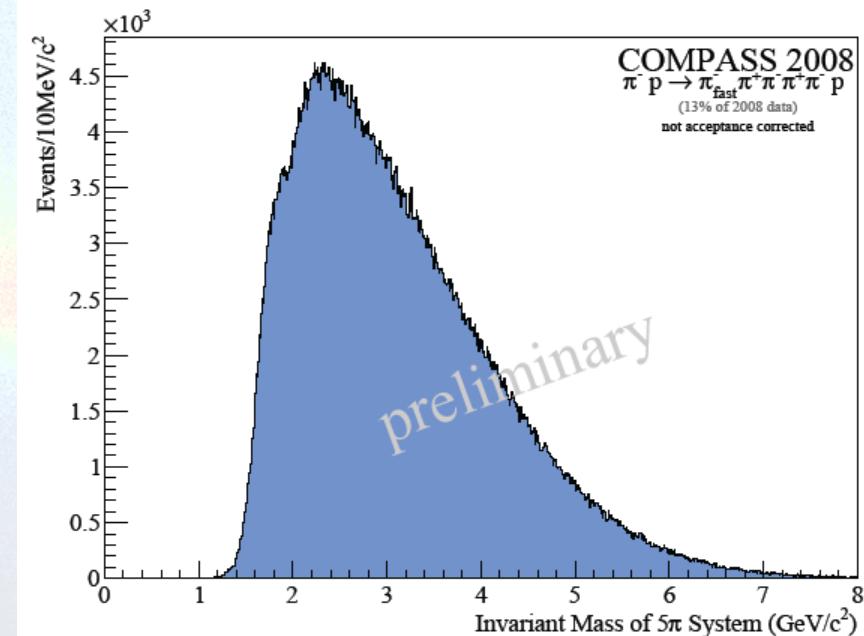


- Access  $m_x > 2 \text{ GeV}/c^2$



see talk by S. Neubert

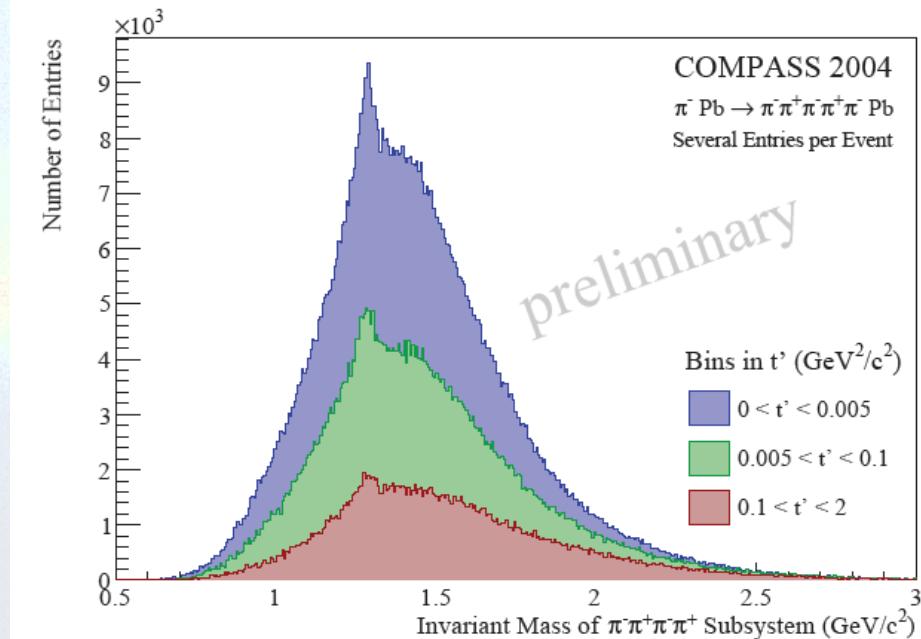
- Access  $m_X > 2 \text{ GeV}/c^2$
- Understand mass range  $m_X [1.6-2] \text{ GeV}/c^2$ 
  - Start with existing observations
    - Study  $\pi_1(1600)$
    - Study  $\pi(1800)$



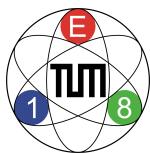
see talk by S. Neubert

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Cut 4 $\pi$  spectrum:



see talk by S. Neubert



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- Use high mass isobars
  - $b_1, f_1, \eta', \rho(1450) \dots$

see talk by S. Neubert

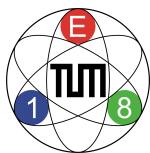


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- Combinatorics is huge

see talk by S. Neubert

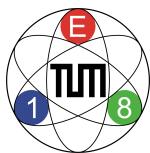


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- Combinatorics is huge
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- PWA being started – **high statistics**

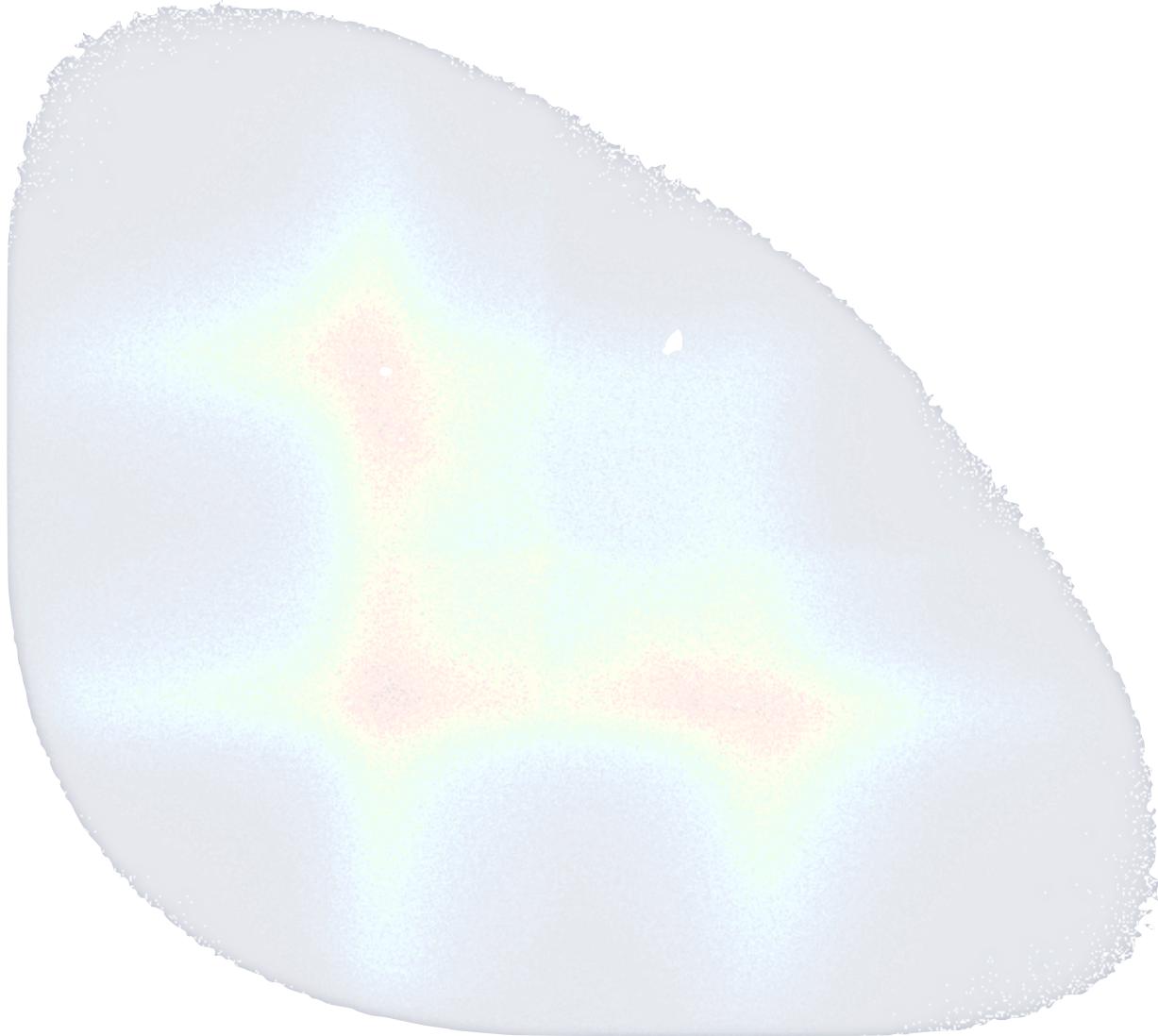
see talk by S. Neubert

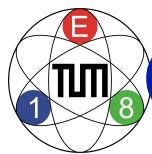


# Central production $\pi^- p$

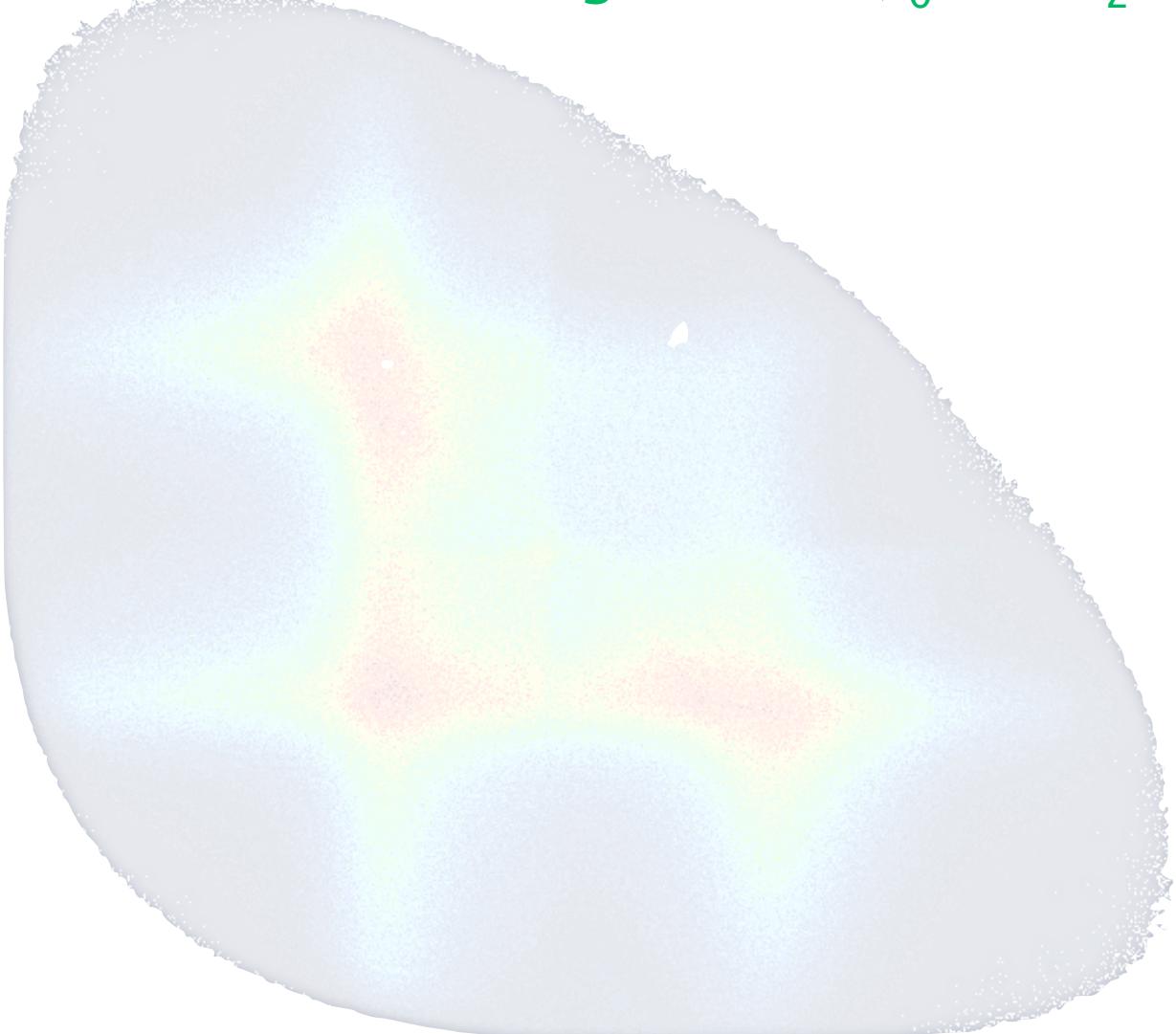


$\pi^-\pi^+\pi^-\pi^+\pi^-p$



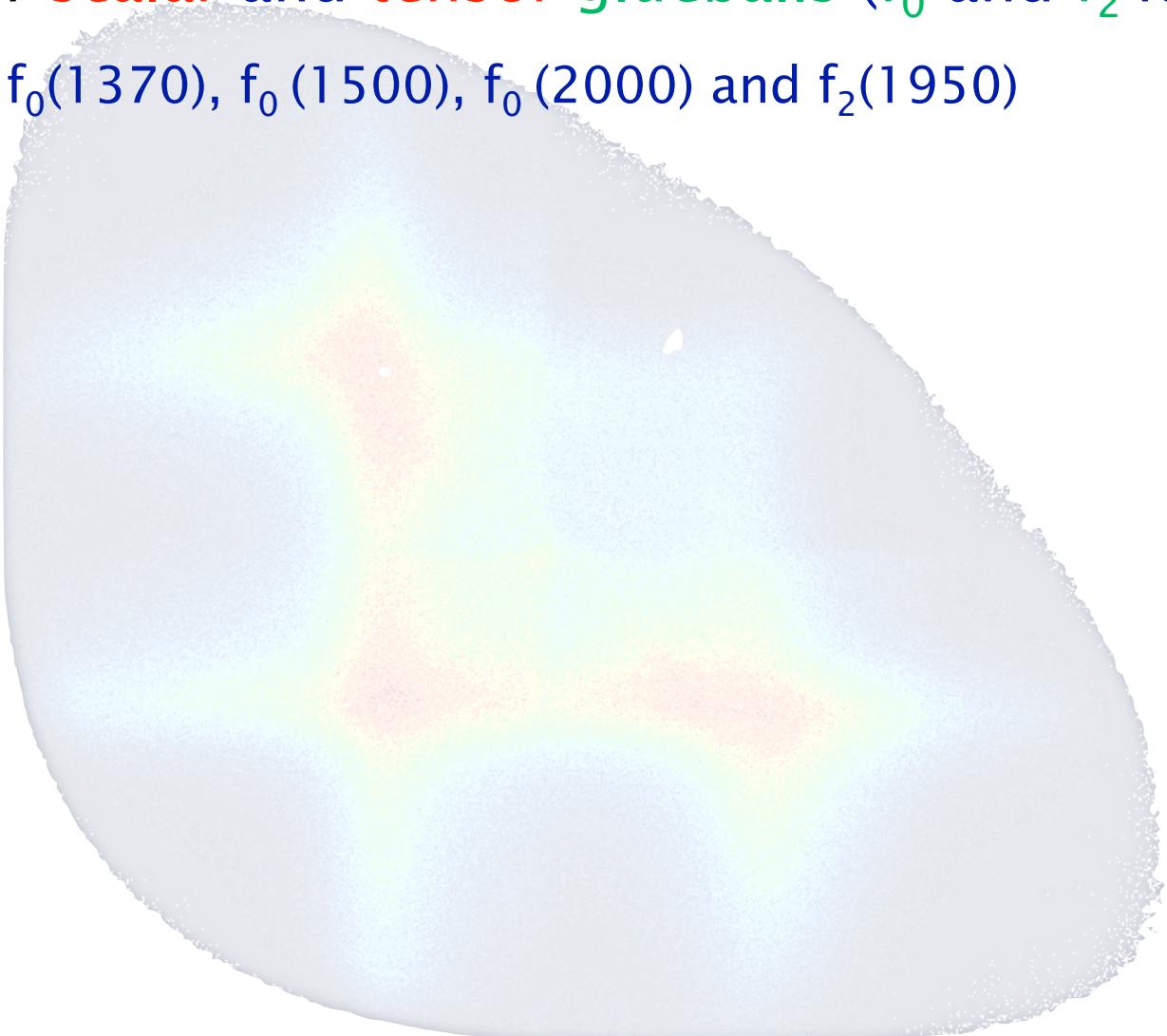


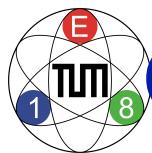
Search for **scalar** and **tensor** glueballs ( $f_0$  and  $f_2$  family)



## Search for scalar and tensor glueballs ( $f_0$ and $f_2$ family)

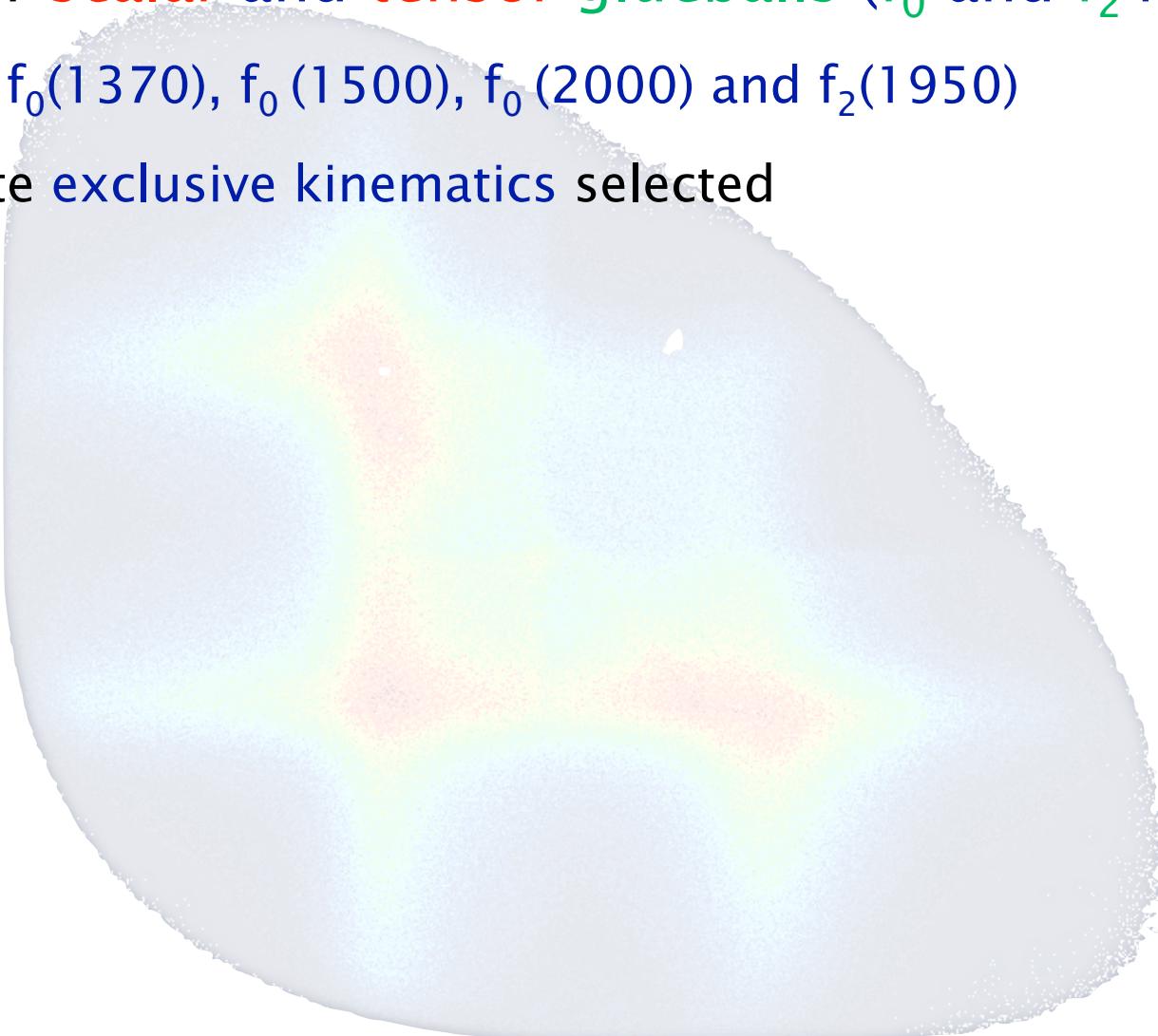
- WA102:  $f_0(1370)$ ,  $f_0(1500)$ ,  $f_0(2000)$  and  $f_2(1950)$

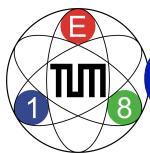




Search for **scalar** and **tensor** glueballs ( $f_0$  and  $f_2$  family)

- WA102:  $f_0(1370)$ ,  $f_0(1500)$ ,  $f_0(2000)$  and  $f_2(1950)$
- Complete **exclusive kinematics** selected





# Central production $\pi^- p$ $\pi^-\pi^+\pi^-\pi^+\pi^- p$

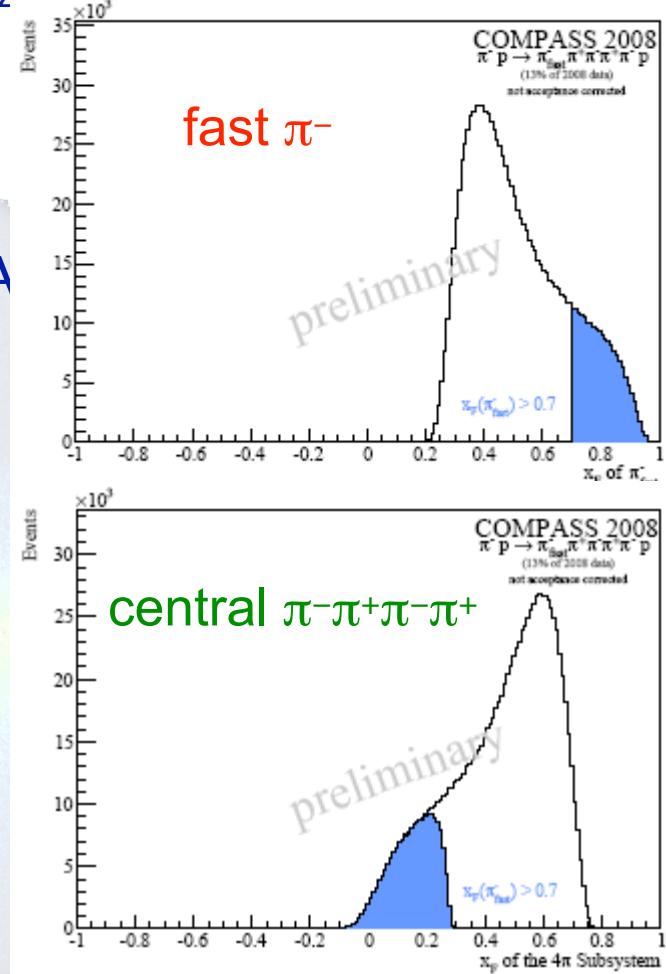


Search for **scalar** and **tensor** glueballs ( $f_0$  and  $f_2$  family)

- WA102:  $f_0(1370)$ ,  $f_0(1500)$ ,  $f_0(2000)$  and  $f_2(1950)$
- Complete **exclusive** kinematics selected
- Select  $(\pi^-)_{\text{fast}} \pi^+\pi^-\pi^+\pi^- (p_{\text{slow}})$

## Search for scalar and tensor glueballs ( $f_0$ and $f_2$ family)

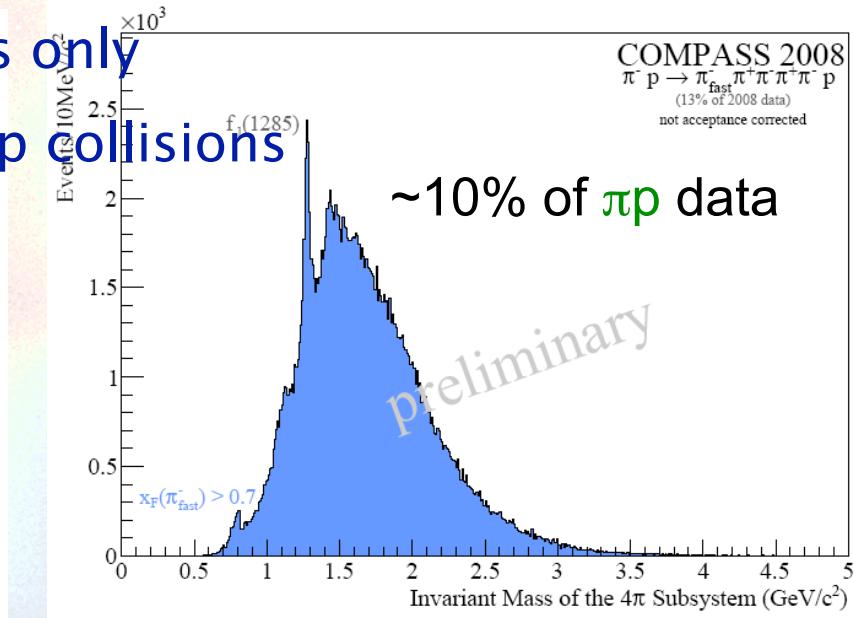
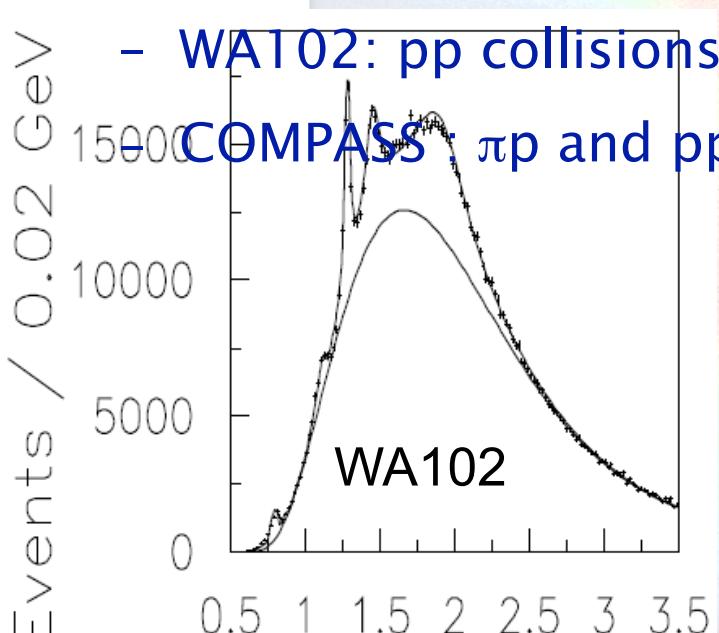
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- Select  $(\pi^-)_{\text{fast}} \pi^+\pi^-\pi^+\pi^- (p_{\text{slow}})$
- Compass has  $\sim 100$  times stastistics of WA102
  - WA102: pp collisions only
  - COMPASS :  $\pi p$  and pp collisions



see talk by J. Bernhard

## Search for scalar and tensor glueballs ( $f_0$ and $f_2$ family)

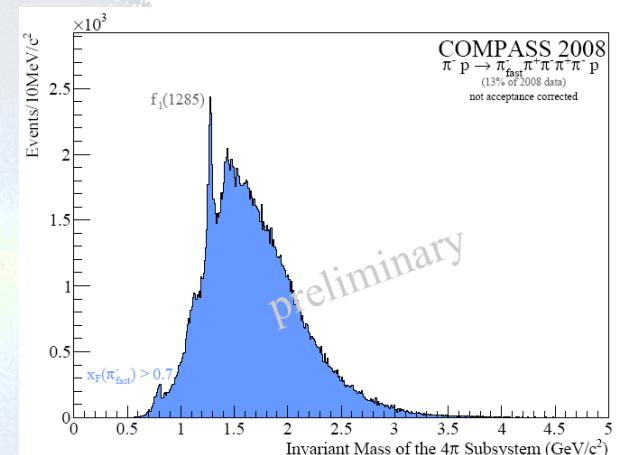
- WA102:  $f_0(1370)$ ,  $f_0(1500)$ ,  $f_0(2000)$  and  $f_2(1950)$
- Complete **exclusive kinematics** selected
- Select  $(\pi^-)_{\text{fast}} \pi^+ \pi^- \pi^+ \pi^- (p_{\text{slow}})$
- Compass has  $\sim 100$  times stastistics of WA102



see talk by J. Bernhard

## Search for scalar and tensor glueballs ( $f_0$ and $f_2$ family)

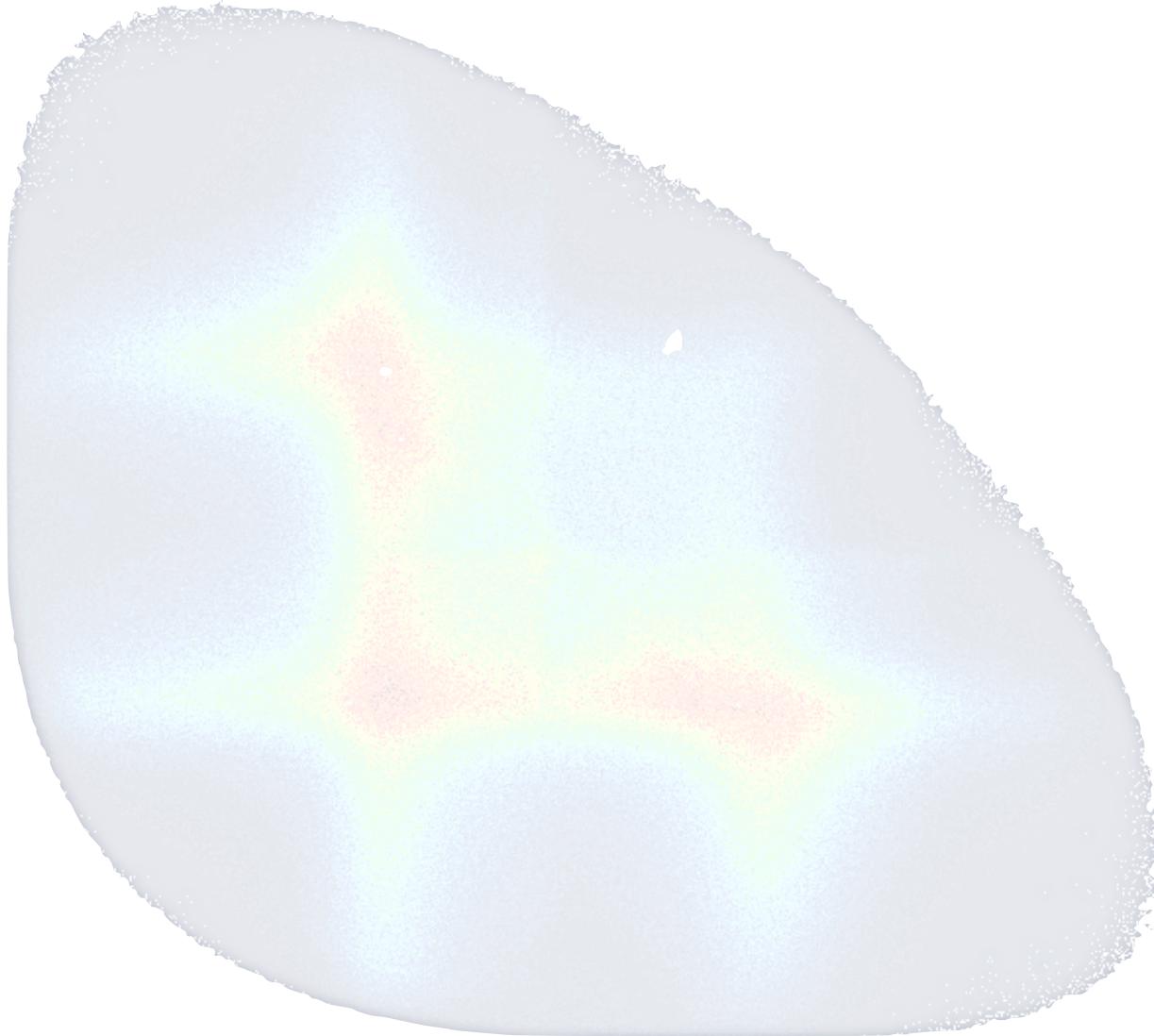
- WA102:  $f_0(1370)$ ,  $f_0(1500)$ ,  $f_0(2000)$  and  $f_2(1950)$
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- Select  $(\pi^-)_{\text{fast}} \pi^+ \pi^- \pi^+ \pi^- (p_{\text{slow}})$
- Compass has  $\sim 100$  times statistics of WA102
  - WA102: pp collisions only
  - COMPASS :  $\pi p$  and pp collisions



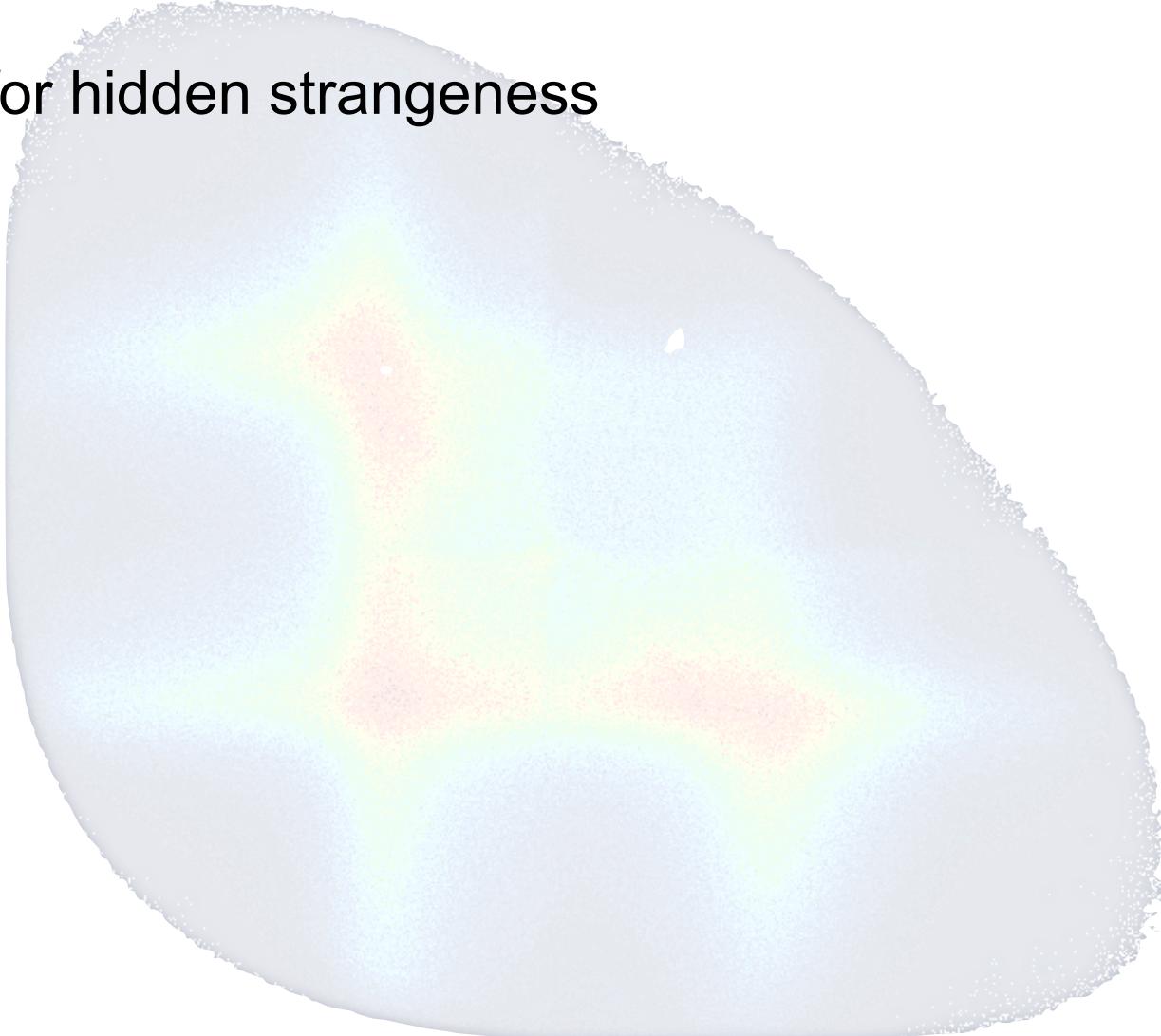
see talk by J. Bernhard



# Strangeness in final states $\pi p$ $\pi K K p$

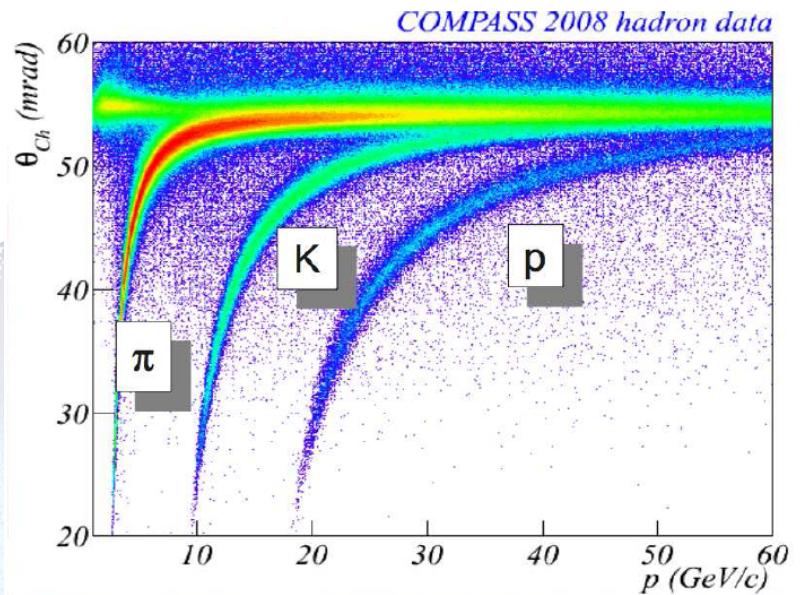


Search for hidden strangeness



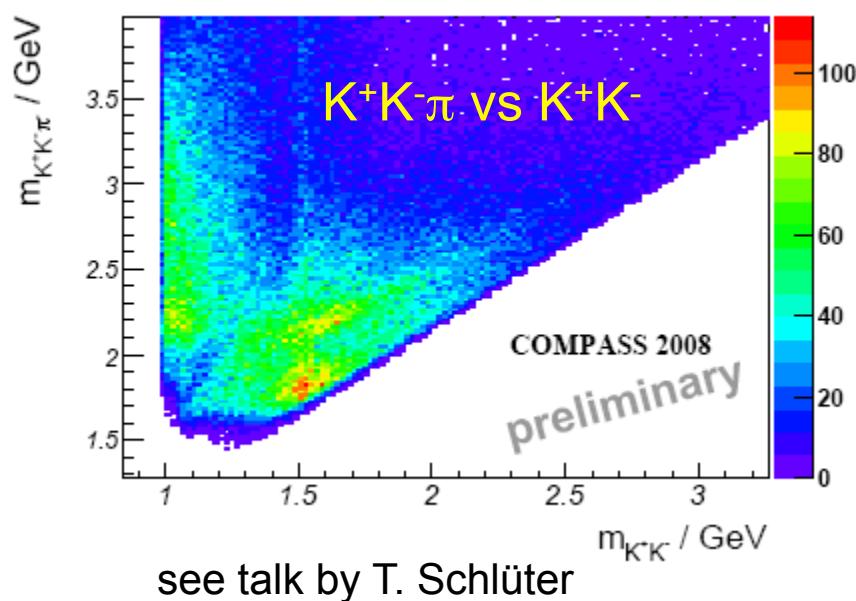
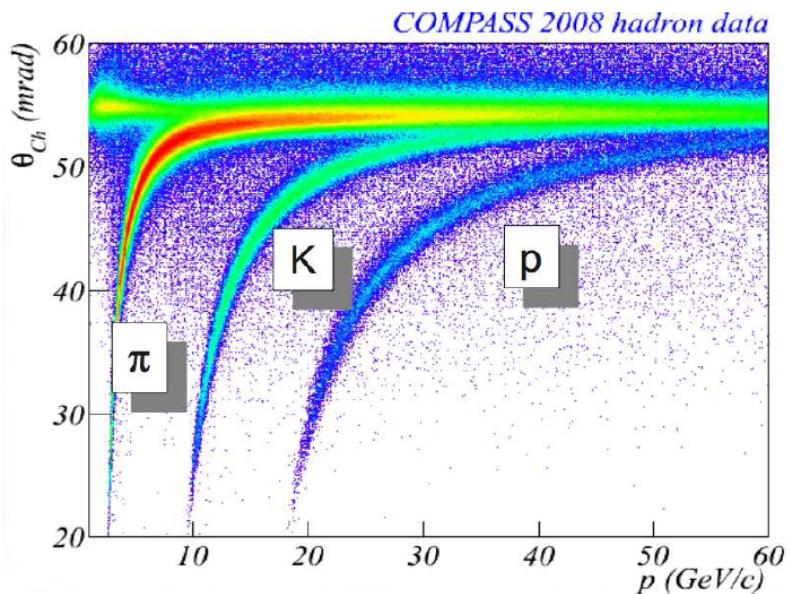
## Search for hidden strangeness

- Neutral and charged kaon channels



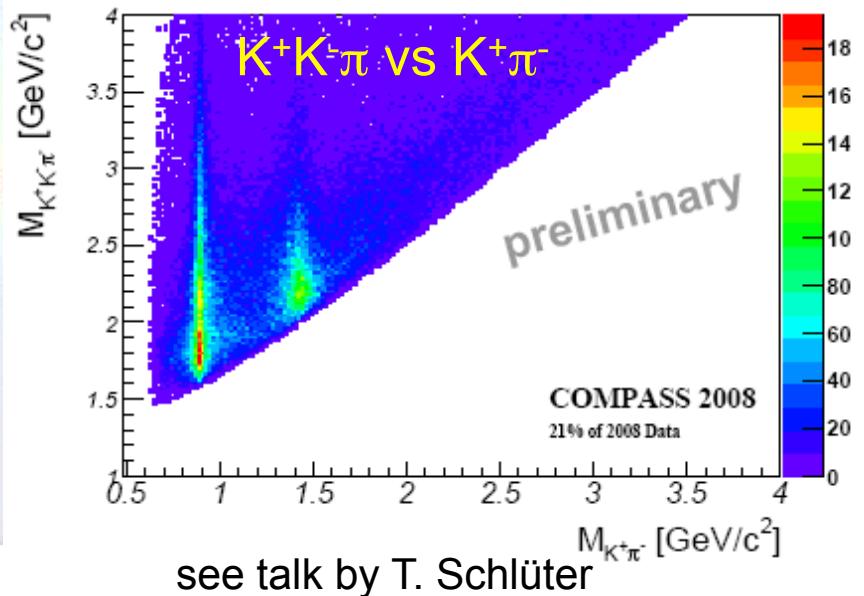
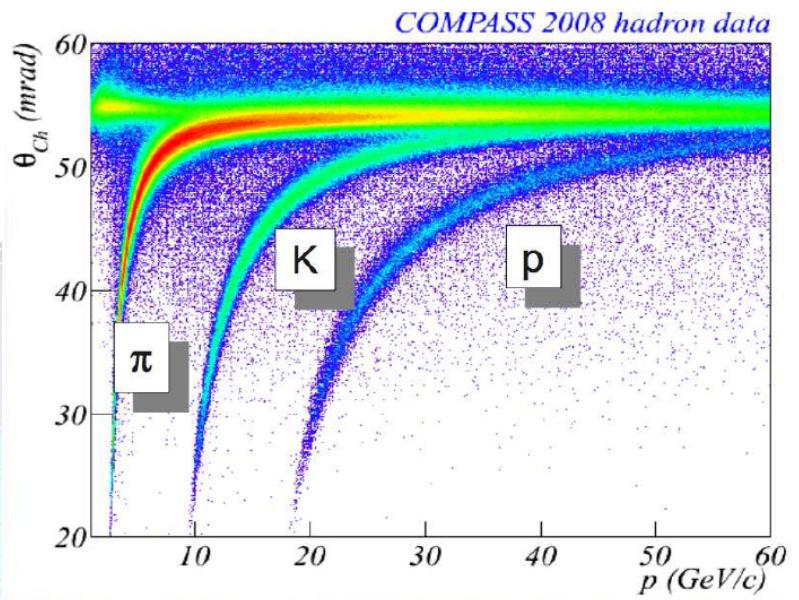
## Search for hidden strangeness

- Neutral and charged kaon channels
- High mass isobars observed cleanly
- Glueball search decaying into  $KK$
- Hybrids decaying into  $KK\pi$
- Information on nature of states
  - branching fraction
  - decay chain



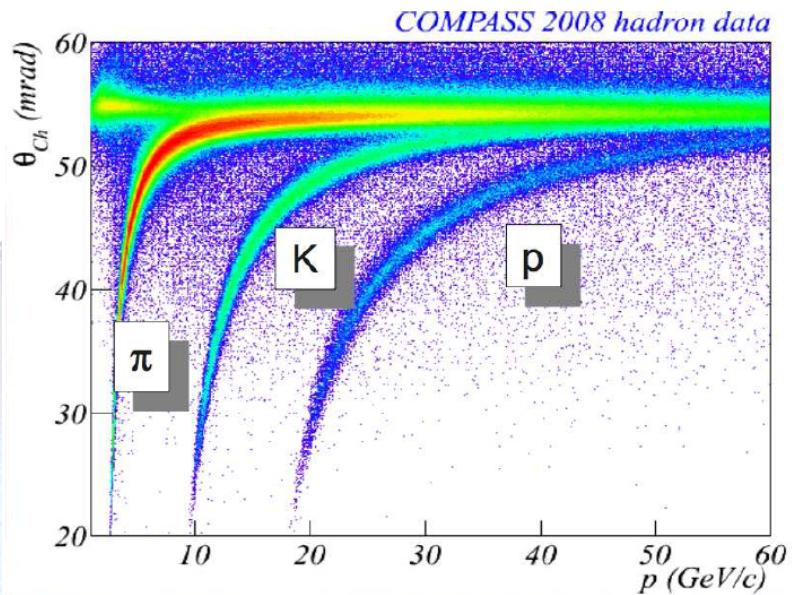
## Search for hidden strangeness

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## Search for hidden strangeness

- Neutral and charged kaon channels
- High mass isobars observed cleanly
- Glueball search decaying into  $KK$
- Hybrids decaying into  $KK\pi$
- Information on nature of states
  - branching fraction
  - decay chain
- PWA being prepared



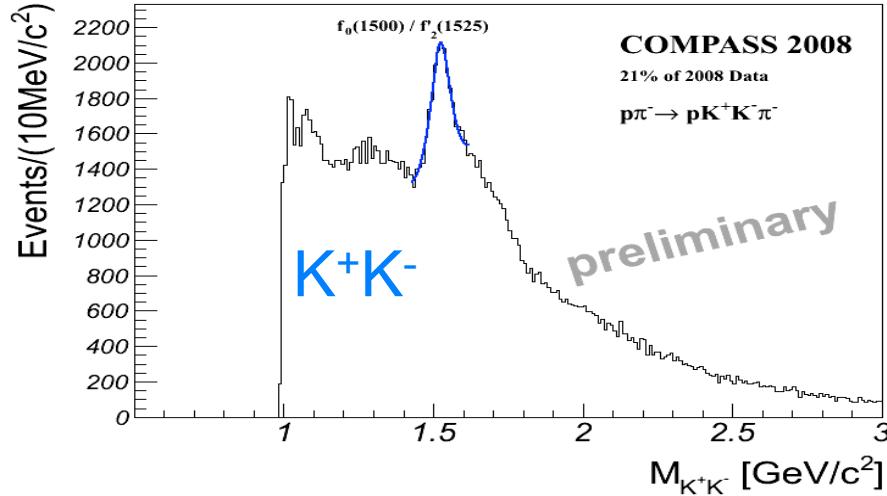
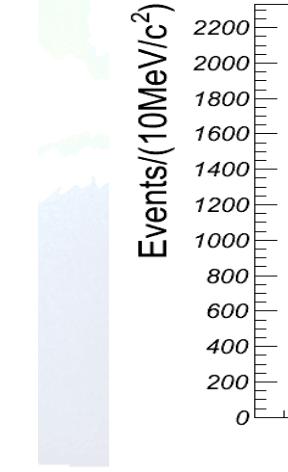
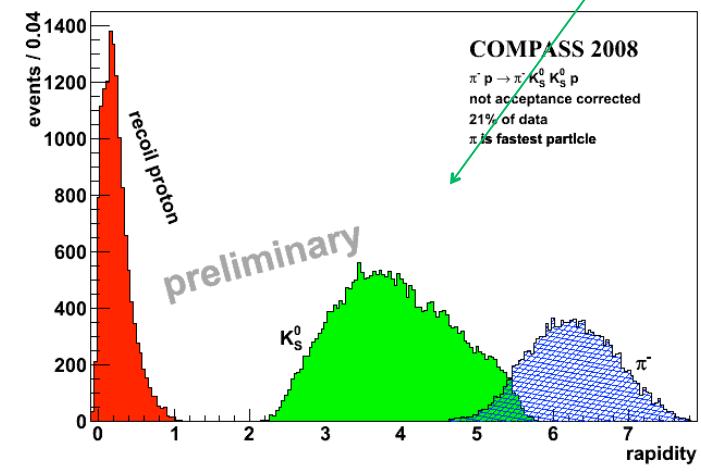
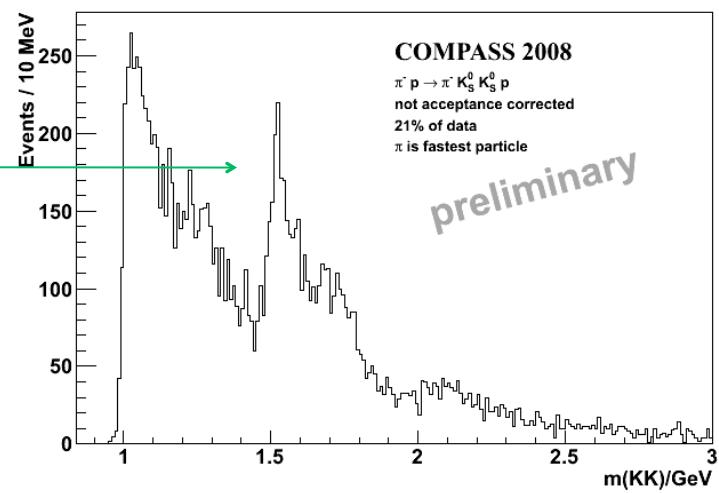
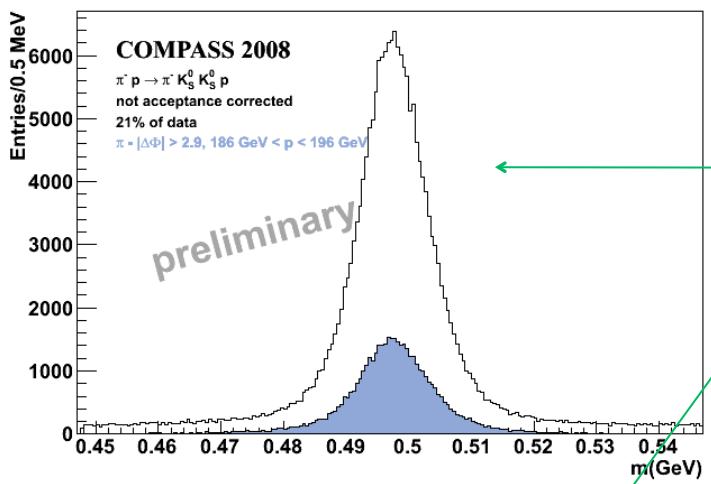
see talk by T. Schlüter

# Central Production (KK)

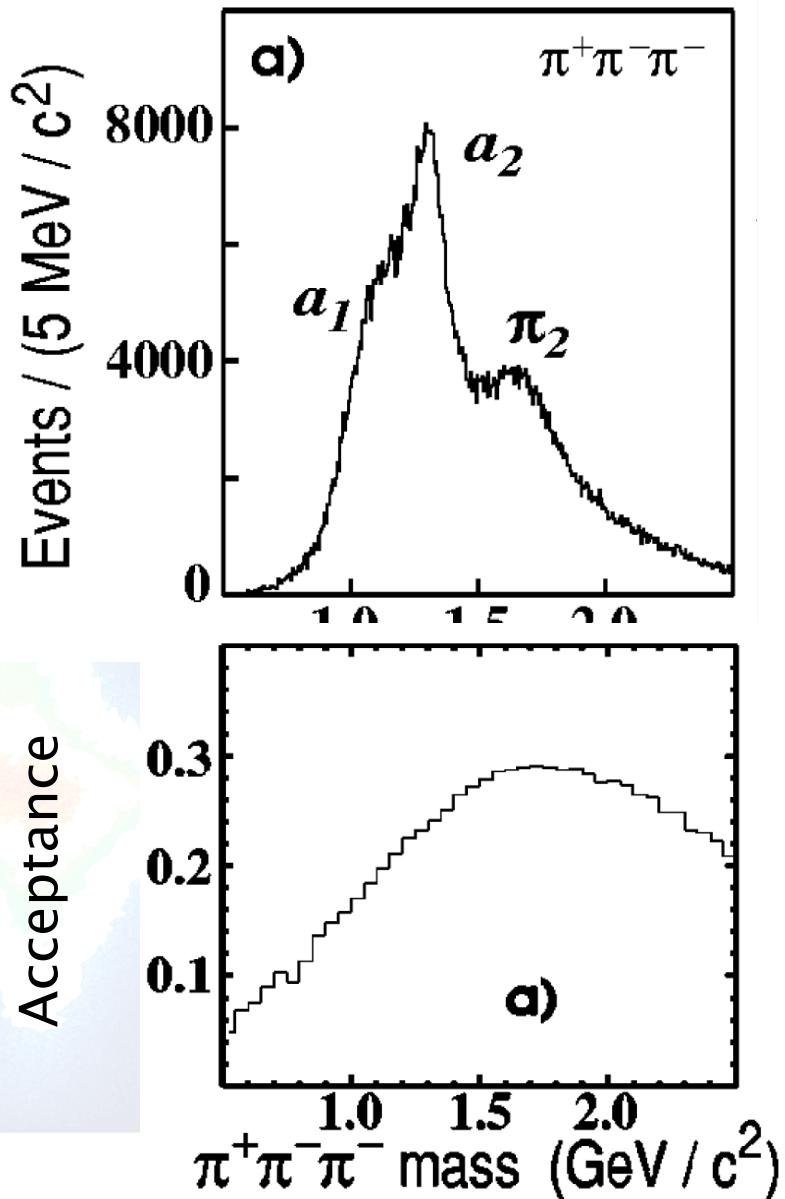
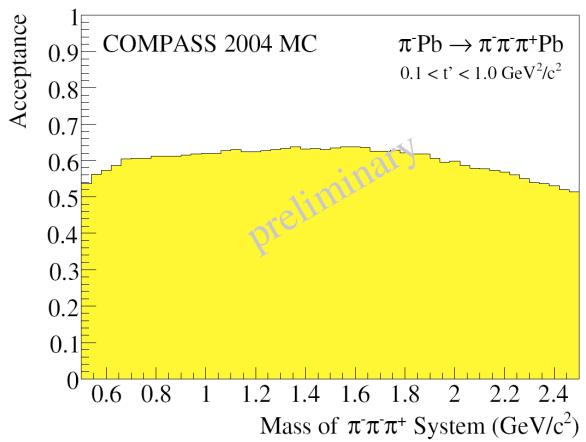
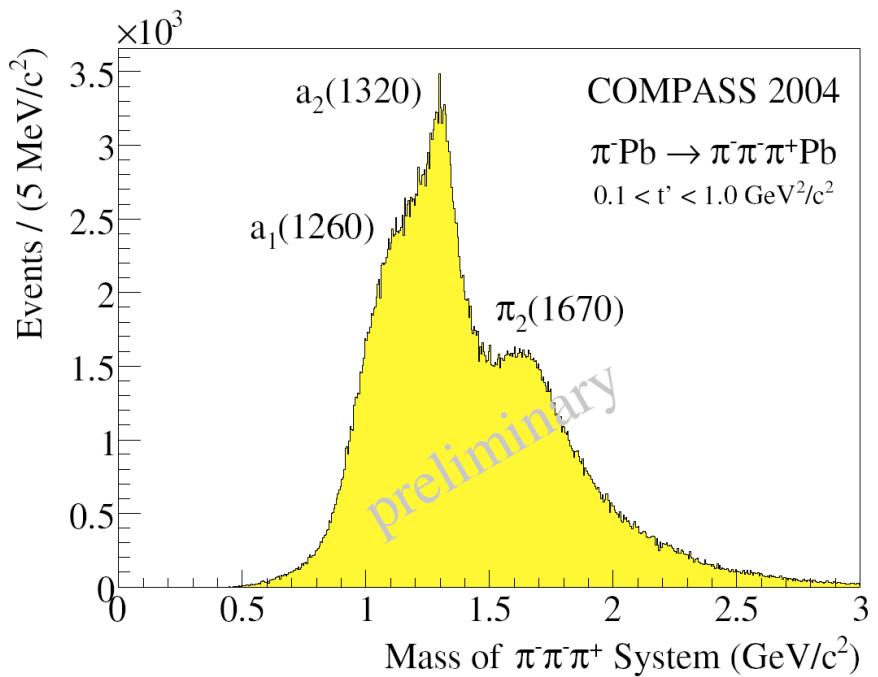
- Central production used to search for glue-rich states
  - WA102 was successful studying  $f_0$  mixing scheme
- Study central production with mesons and protons
  - In ideal world: production very similar (except for spin effects)
  - At COMPASS: Pomeron-Pomeron (DPE) not clearly separable from simple Reggeon exchange
  - Mixture of diffraction and central production
- Kaons are promising selective final states

state	allowed $J^{PC}$			
$K_S^0 K_S^0$	$0^{++}$	$2^{++}$	$4^{++}$	
$K_S^0 K_L^0$		$1^{--}$	$3^{--}$	
$K^+ K^-$	$0^{++}$	$1^{--}$	$2^{++}$	$3^{--}$ $4^{++}$

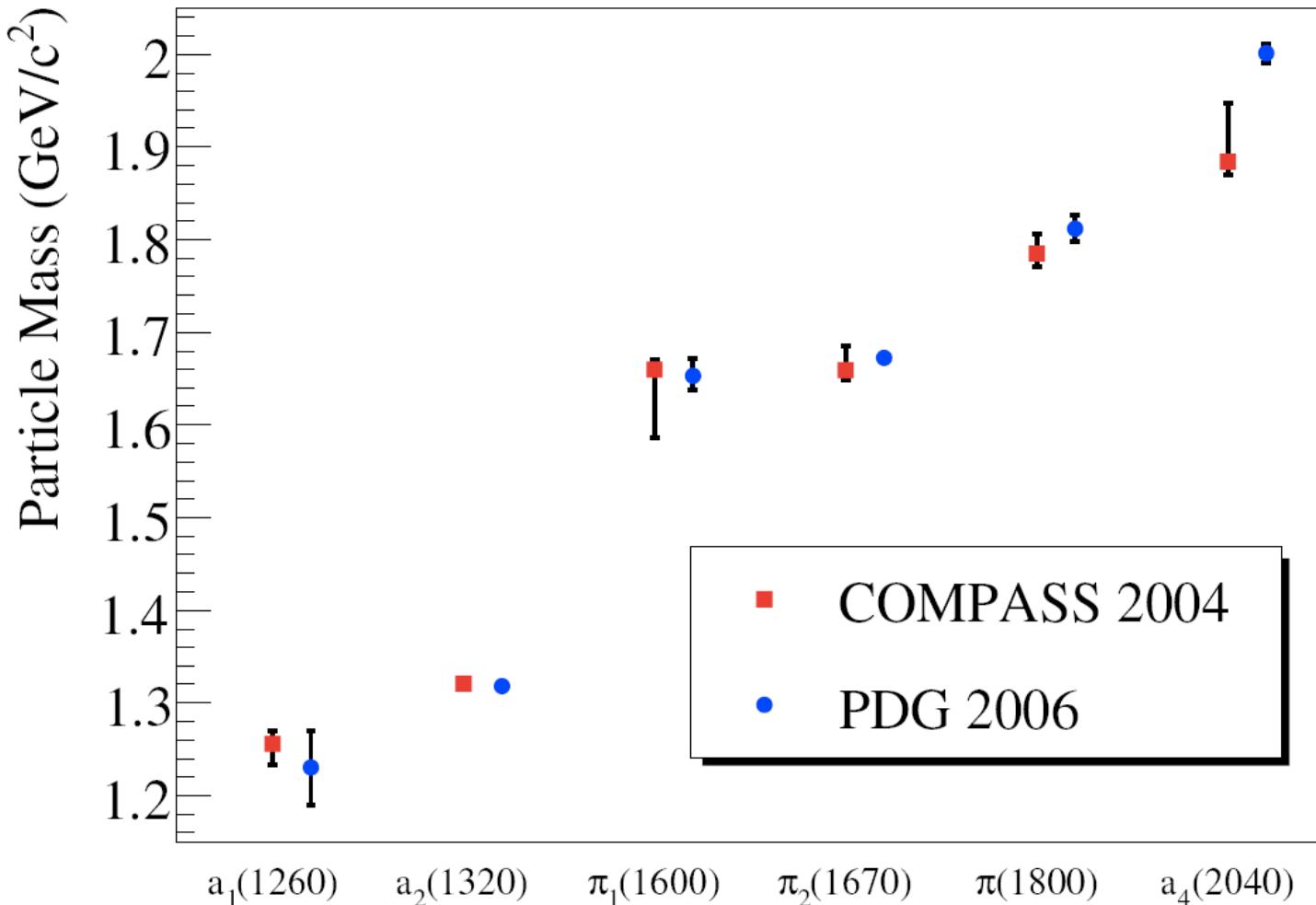
# Central Production (KK)



# Invariant Mass of 3 $\pi$ System '04



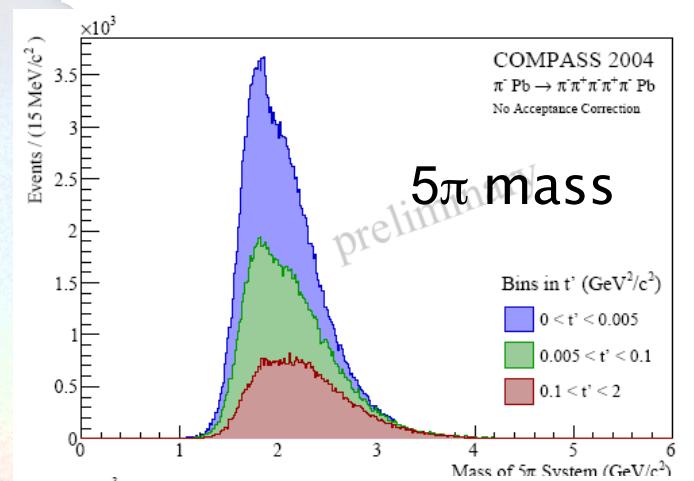
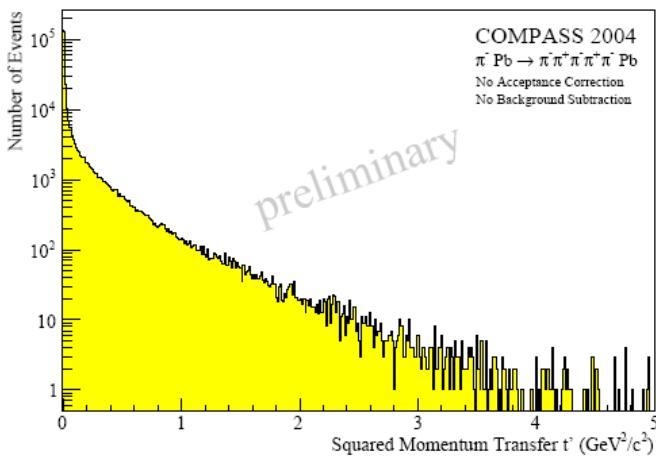
# Summary of Waves



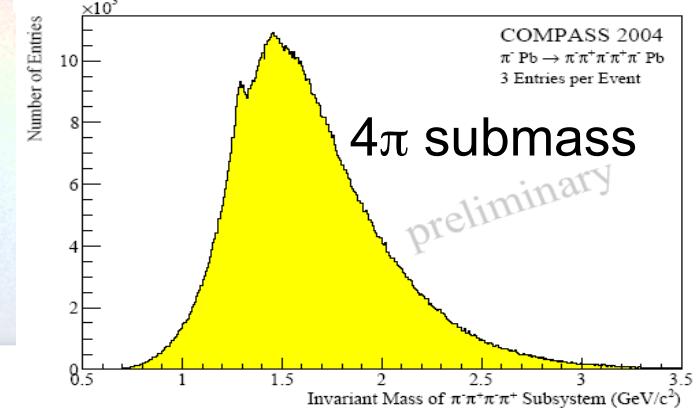
Publication submitted to CERN (preprint) and to PRL

# Analysis of $5\pi$

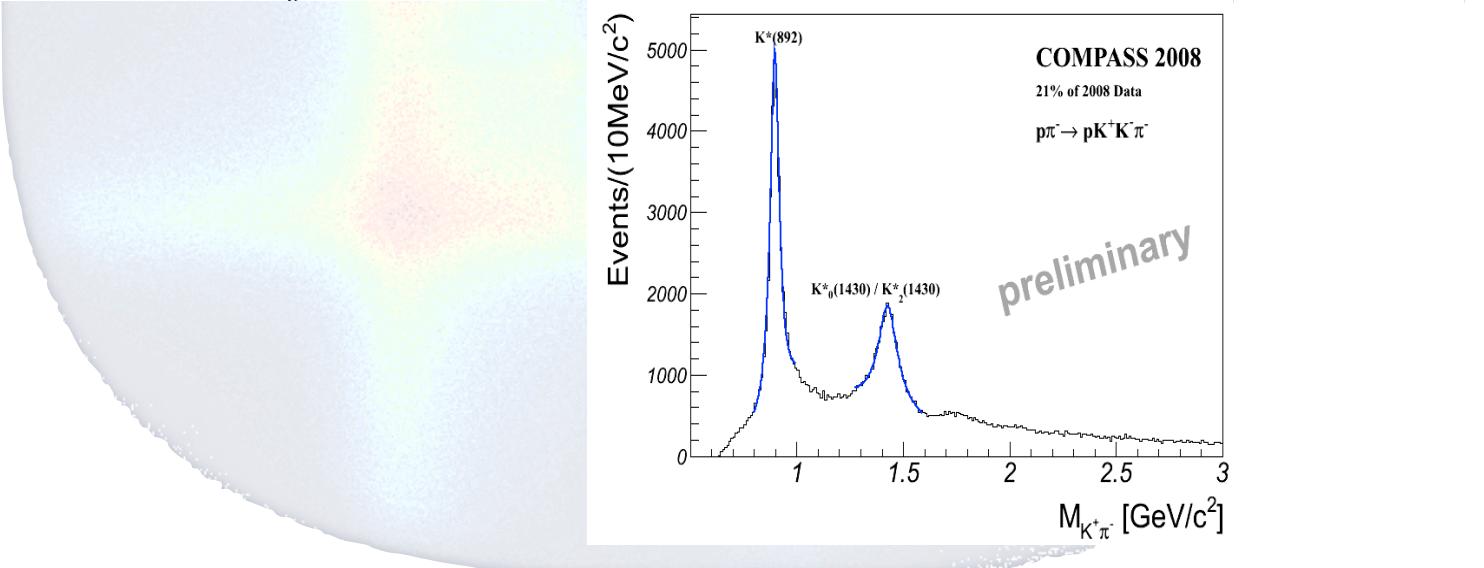
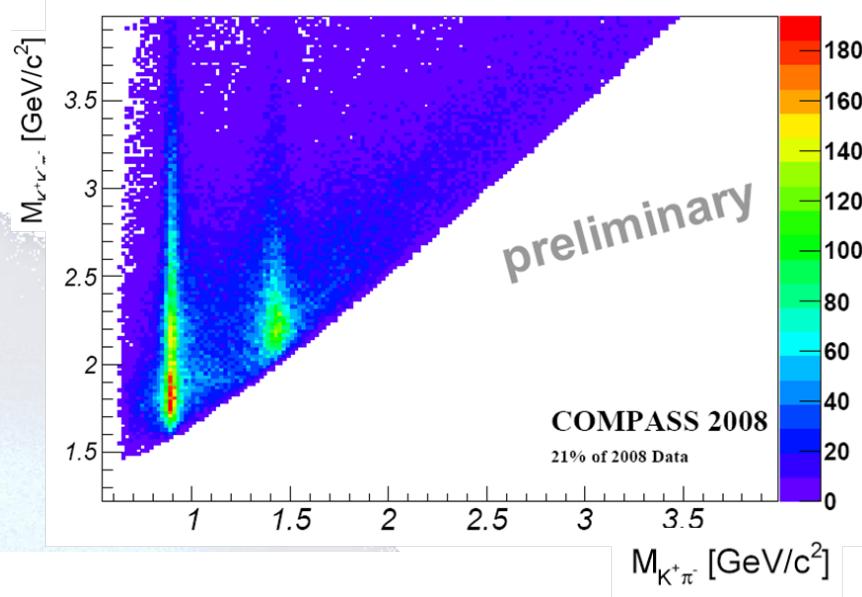
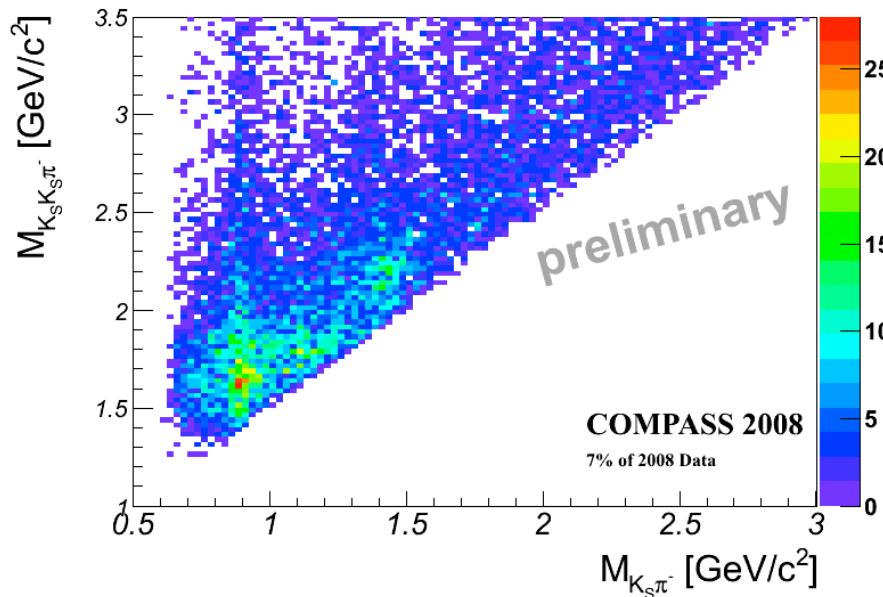
- Need to extend study to high masses
  - Decay of heavy resonances into high mass isobars
  - Multi pion final states
  - Complex analysis (106 waves)



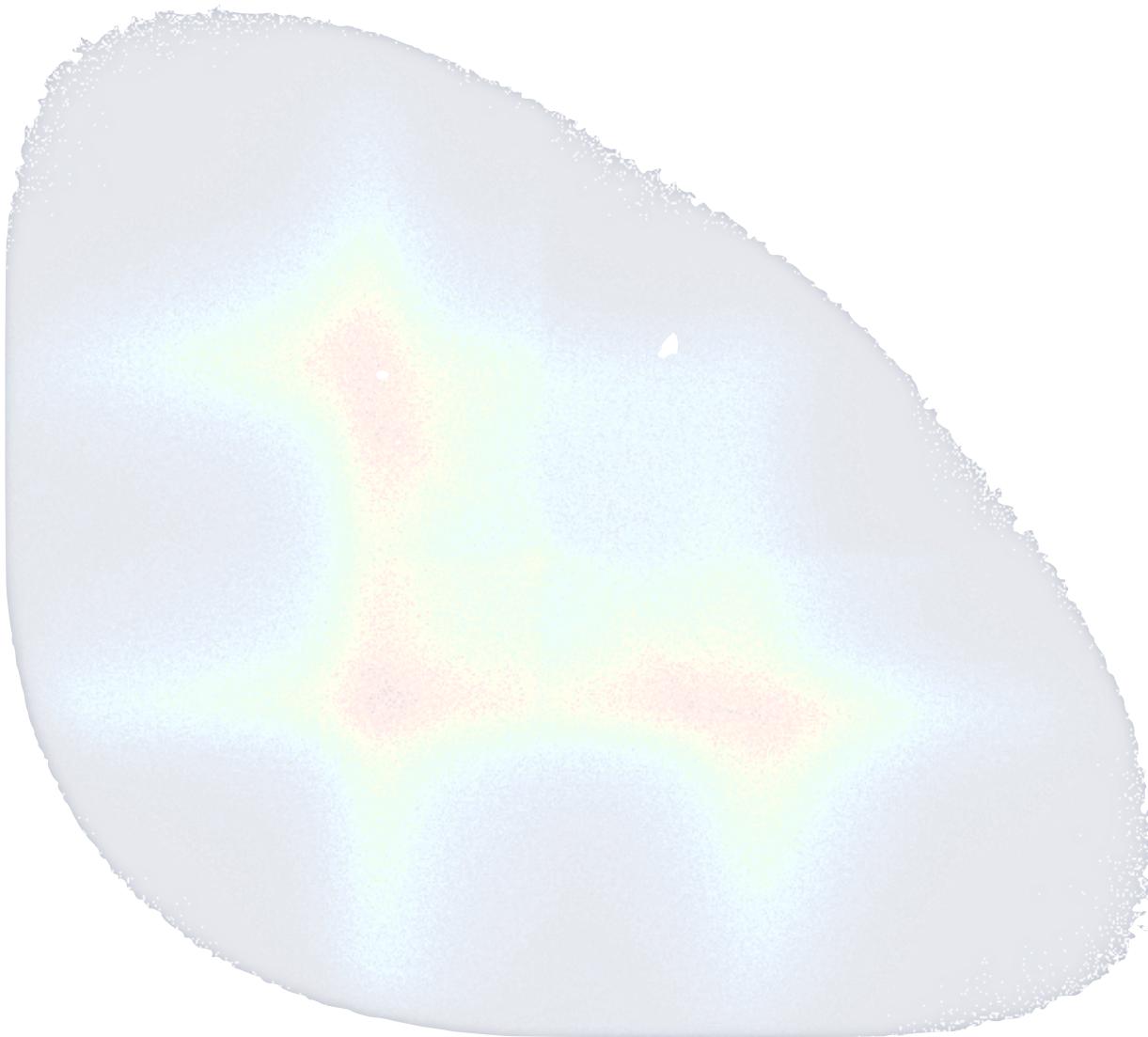
4π Isobars ( $G = +1$ )			3π Isobars ( $G = -1$ )		
Name	Mass ( $\text{MeV}/\text{c}^2$ )	$I^G(J^{PC})$	Name	Mass ( $\text{MeV}/\text{c}^2$ )	$I^G(J^{PC})$
$f_0$	1370 / 1700	$0^+(0^{++})$	$a_1$	1270	$1^-(1^{++})$
$\eta'$	1403	$0^+(0^{-+})$	$a_2$	1320	$1^-(2^{++})$
$\rho'$	1450	$1^+(1^{--})$	$\pi'$	1300	$1^-(0^{-+})$
$b_1$	1235 / 1800	$1^+(1^{+-})$	$\pi_2$	1670	$1^-(2^{-+})$
$f_1$	1285 / 1450	$0^+(1^{++})$	$\pi_1$	1600	$1^-(1^{-+})$
$\eta'_2$	1645	$0^+(2^{-+})$			
$f_2$	1565	$0^+(2^{++})$			
$\rho_3$	1690	$1^+(3^{--})$			
$\eta_1$	1600	$0^+(1^{-+})$			
More Exotics	???	$1^+(0^{+-}), 1^+(2^{+-})$			



# Central Production (KK)



# Wave Set Included into Fit



# Wave Set Included into Fit

Notation of Partial Waves:  $J^P C M^\epsilon [\dots] L$

- Spin  $J$ , parity  $P$ ,  $C$ -parity  $C$ , spin projection  $M$ , reflectivity  $\epsilon$ , decay particles  $[\dots]$  and their relative orbital angular momentum  $L$
- E. g.:  $\pi_2(1670)$ :  $2^{-+} 1^+ [f_2 \pi] S$ ,  $2^{-+} 0^+ [\rho \pi] P$ ,  $a_2(1320)$ :  $2^{++} 1^+ [\rho \pi] D$
- Intensity is a **coherent** and **incoherent** ( $\epsilon = \pm 1$ , flat) sum of partial waves

# Wave Set Included into Fit

$J^{PC} M^\epsilon$	$L$	Isobar $\pi$	Cut [GeV]	$J^{PC} M^\epsilon$	$L$	Isobar $\pi$	Cut [GeV]
$0^{-+0^+}$	$S$	$f_0\pi$	1.40	$2^{++1^+}$	$P$	$f_2\pi$	1.50
$0^{-+0^+}$	$S$	$(\pi\pi)_s\pi$	-	$2^{++1^+}$	$D$	$\rho\pi$	-
$0^{-+0^+}$	$P$	$\rho\pi$	-	$3^{++0^+}$	$S$	$\rho_3\pi$	1.50
$1^{-+1^+}$	$P$	$\rho\pi$	-	$3^{++0^+}$	$P$	$f_2\pi$	1.20
$1^{++0^+}$	$S$	$\rho\pi$	-	$3^{++0^+}$	$D$	$\rho\pi$	1.50
$1^{++0^+}$	$P$	$f_2\pi$	1.20	$3^{++1^+}$	$S$	$\rho_3\pi$	1.50
$1^{++0^+}$	$P$	$(\pi\pi)_s\pi$	0.84	$3^{++1^+}$	$P$	$f_2\pi$	1.20
$1^{++0^+}$	$D$	$\rho\pi$	1.30	$3^{++1^+}$	$D$	$\rho\pi$	1.50
$1^{++1^+}$	$S$	$\rho\pi$	-	$4^{-+0^+}$	$F$	$\rho\pi$	1.20
$1^{++1^+}$	$P$	$f_2\pi$	1.40	$4^{-+1^+}$	$F$	$\rho\pi$	1.20
$1^{++1^+}$	$P$	$(\pi\pi)_s\pi$	1.40	$4^{++1^+}$	$F$	$f_2\pi$	1.60
$1^{++1^+}$	$D$	$\rho\pi$	1.40	$4^{++1^+}$	$G$	$\rho\pi$	1.64
$2^{-+0^+}$	$S$	$f_2\pi$	1.20	$1^{-+0^-}$	$P$	$\rho\pi$	-
$2^{-+0^+}$	$P$	$\rho\pi$	0.80	$1^{-+1^-}$	$P$	$\rho\pi$	-
$2^{-+0^+}$	$D$	$f_2\pi$	1.50	$1^{++1^-}$	$S$	$\rho\pi$	-
$2^{-+0^+}$	$D$	$(\pi\pi)_s\pi$	0.80	$2^{-+1^-}$	$S$	$f_2\pi$	1.20
$2^{-+0^+}$	$F$	$\rho\pi$	1.20	$2^{++0^-}$	$P$	$f_2\pi$	1.30
$2^{-+1^+}$	$S$	$f_2\pi$	1.20	$2^{++0^-}$	$D$	$\rho\pi$	-
$2^{-+1^+}$	$P$	$\rho\pi$	0.80	$2^{++1^-}$	$P$	$f_2\pi$	1.30
$2^{-+1^+}$	$D$	$f_2\pi$	1.50				
$2^{-+1^+}$	$D$	$(\pi\pi)_s\pi$	1.20				
$2^{-+1^+}$	$F$	$\rho\pi$	1.20				
				FLAT			

# PWA Method

$$\sigma(\tau) = \left| \sum_i T_i \Psi_i(\tau) \right|^2$$

$\tau$  = kinetische variable (für jedes Ereignis gemessen)

$\Psi_i(\tau)$  = Zerfallsamplitude : parametrisiert im Isobarmodell

$T_i$  = Produktionsamplitude (aus Fit)

$i$  = Liste aller Zerfallswege im Massenbin  $M_x$

# PWA Method

- Use mass independent fit to angular distributions and sub-mass

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# PWA Method

- Use mass independent fit to angular distributions and sub-mass

Differential Cross-Section (mass-independent, 40 MeV bins)

$\tau$  = kinetische variable (für jedes Ereignis gemessen)

$$\sigma_{\text{indep}}(\tau) = \sum_i \left| \sum_e T_e \Psi_e(\tau) / \sqrt{\int |\Psi_i(\tau)|^2 d\tau} \right|^2$$

$T_i$  = Produktionsamplitude (aus Fit)

$i$  = Liste aller Zerfallswege im Massenbin  $M_x$

- $e$ : reflectivity,     $r$ : rank of density matrix,     $i$ : different partial waves
- $T$ : complex production amplitudes (**fit parameters!**)
- $\psi$ : complex decay amplitudes (coded inside program)
- $\tau$ : phase space coordinates (5 parameters for 3-body decay)

# PWA Method

- Use mass independent fit to angular distributions and sub-mass
- Use mass dependent fit using results from step 1

$$\sigma(\tau) = \left| \sum_i T_i \Psi_i(\tau) \right|^2$$

$\tau$  = kinetische variable (für jedes Ereignis gemessen)

$\Psi_i(\tau)$  = Zerfallsamplitude : parametrisiert im Isobarmodell

$T_i$  = Produktionsamplitude (aus Fit)

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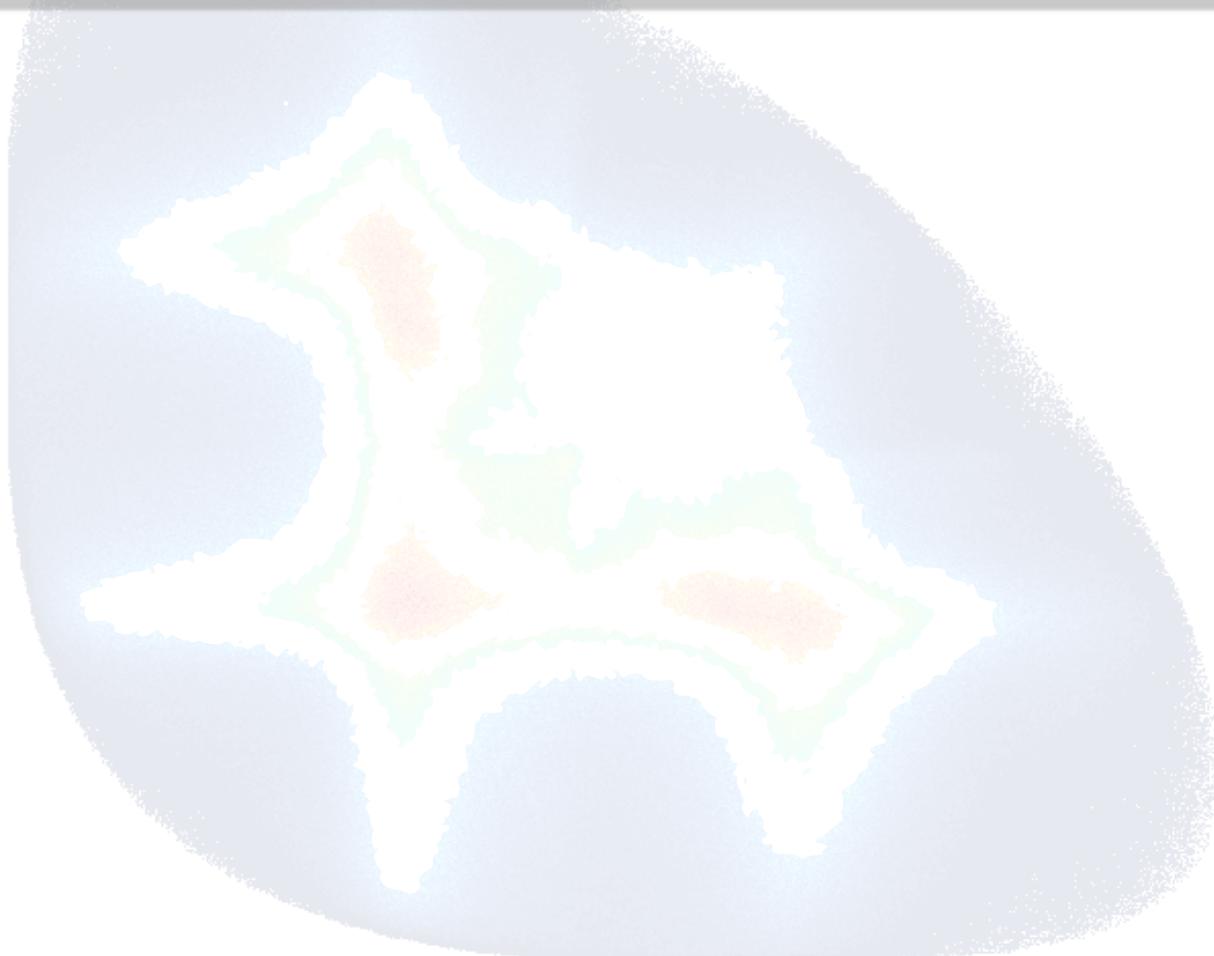
Mass-Dependent Fit using Breit-Wigners (simplified!, precise → note)

$$T_{ir}^\epsilon(M_{3\pi}) = \frac{1}{M_{3\pi}} \sum_k C_{k,ir}^\epsilon \text{BW}_{k,i}(M, M_{0,k,i}, \Gamma_{0,k,i}) \sqrt{\int |\psi_i^\epsilon(\tau')|^2 d\tau'}$$

# The Goal

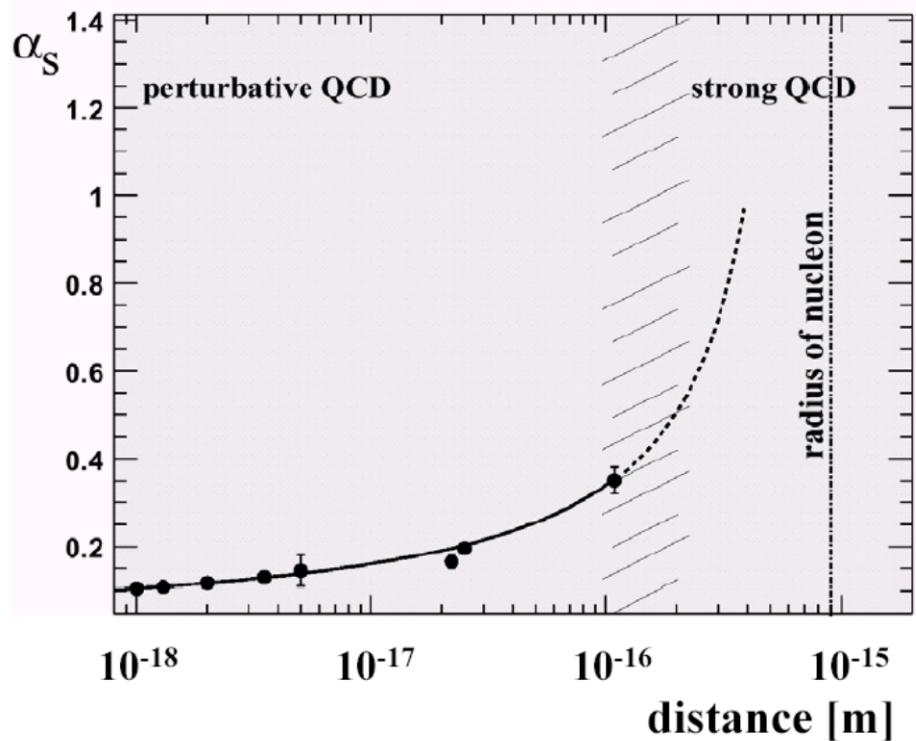


**Understand hadrons from the dynamics  
of quarks and gluons**



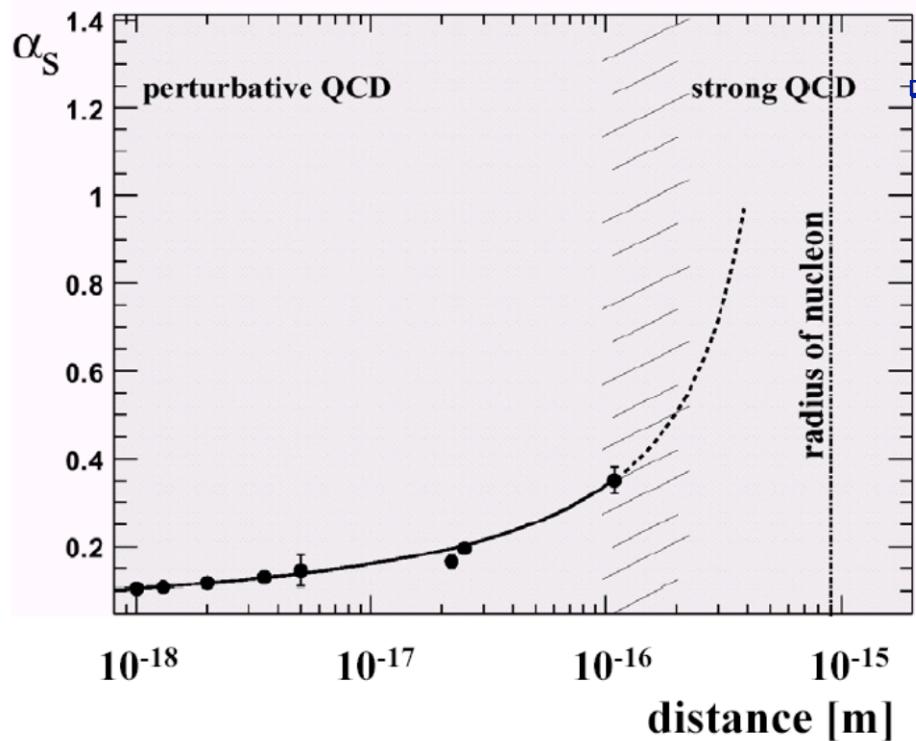
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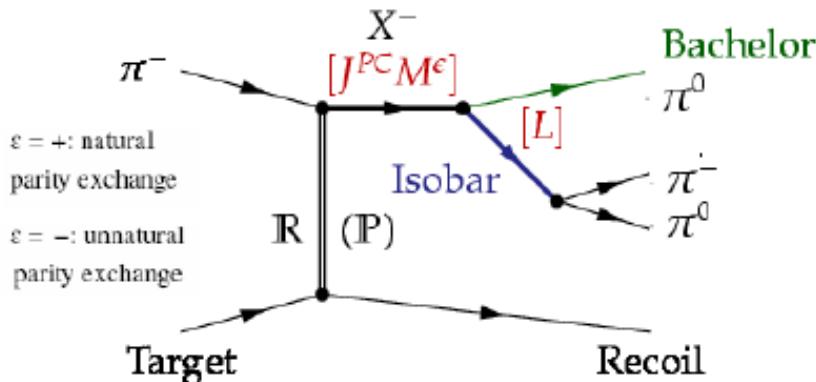
**Understand hadrons from the dynamics  
of quarks and gluons**



⇒ **non-perturbative regime of QCD**

- Models: QM, bag, flux tube, ...
- Effective theories:  $\chi$ PT, ...
- Lattice-QCD

## PWA using isobar model



$X^-$  decay described using isobar model:

- Intermediate di-pion resonance (isobar)
- *Spin S and rel. orbital angular momentum L w.r.t bachelor  $\pi^-$*
- *L+S couple to J*
- Partial waves:  $J^{PC} M^\epsilon$  [isobar] L

### PWA:

- program: Illinois/Protvino/Munich (D.Ryabchikov) software (IHEP/VES, TUM/COMPASS)
- Isobars:  $(\pi\pi)_S$  [broad  $f_0(600)+f_0(1370)$ ],  $f_0(980)$ ,  $\rho(770)$ ,  $f_2(1270)$ ,  $\rho_3(1690)$
- No acceptance correction yet (assumed flat)

### Assumptions:

- *factorisation* of beam & target vertex, *no final state interactions*
- $I^G$  conserved at *beam vertex* ( $\pi^-$  beam:  $I^G = 1^-$ )
- *Scattering on nucleons*: helicity flip & non-flip amps at target vertex (*rank 2*)
- Using *reflectivity basis* in Gottfried Jackson frame (at high CM energies: reflectivity  $\varepsilon$  = naturality of  $R$ )

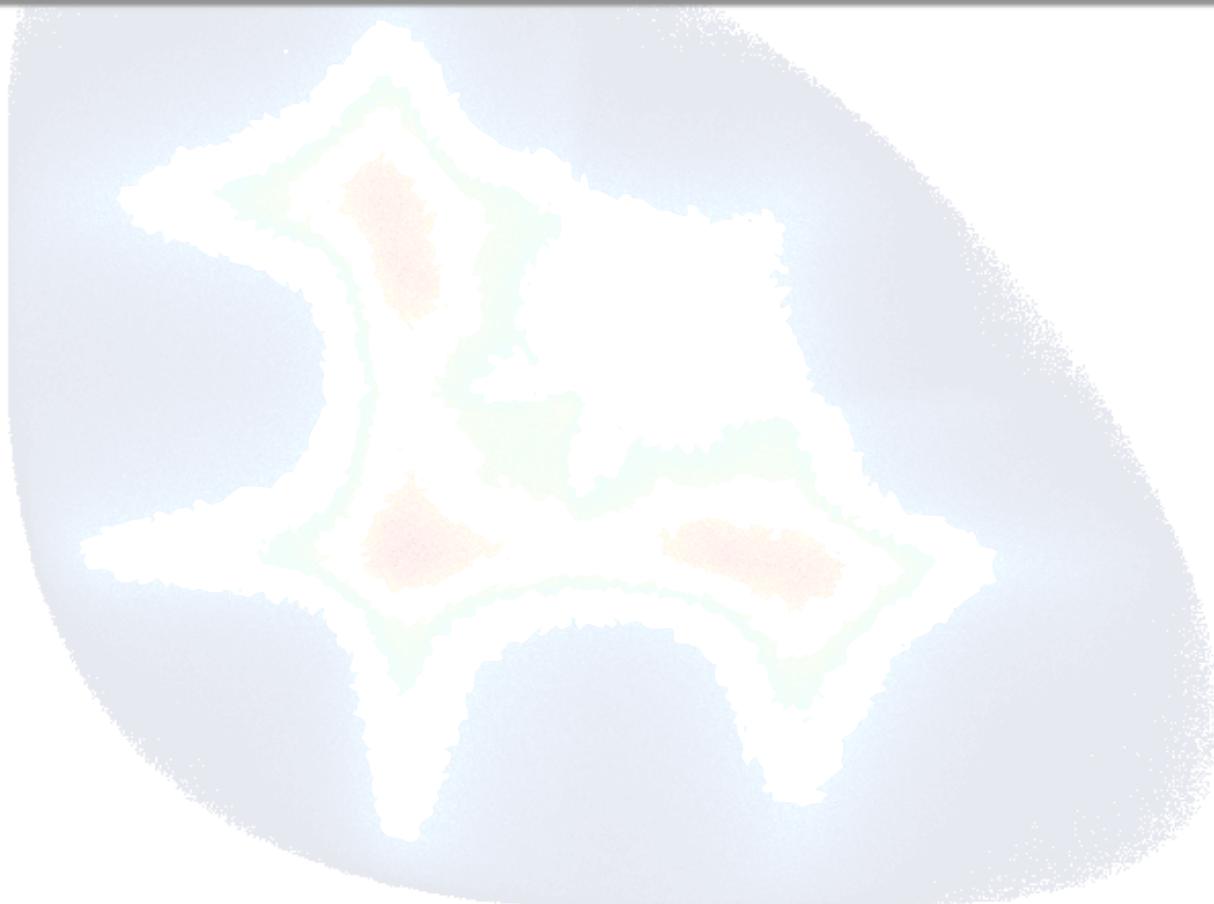
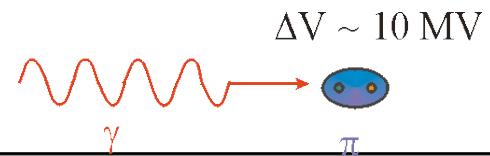
### Isospin symmetry: neutral / charge mode

- isobar decaying into  $f_2 \pi$ : 1/2 intensity expected
- isobar decaying into  $\rho \pi$ : 1/1 intensity expected

# Pion Polarizabilities

Describe response to external e.m. fields  $\Rightarrow$  stiffness of system

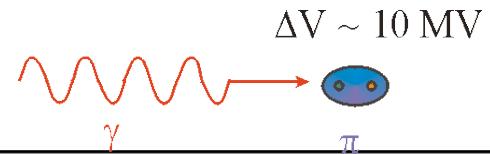
- electric polarizability  $\vec{d} = \bar{\alpha} \vec{E}$
- magnetic polarizability  $\vec{\mu} = \bar{\beta} \vec{H}$



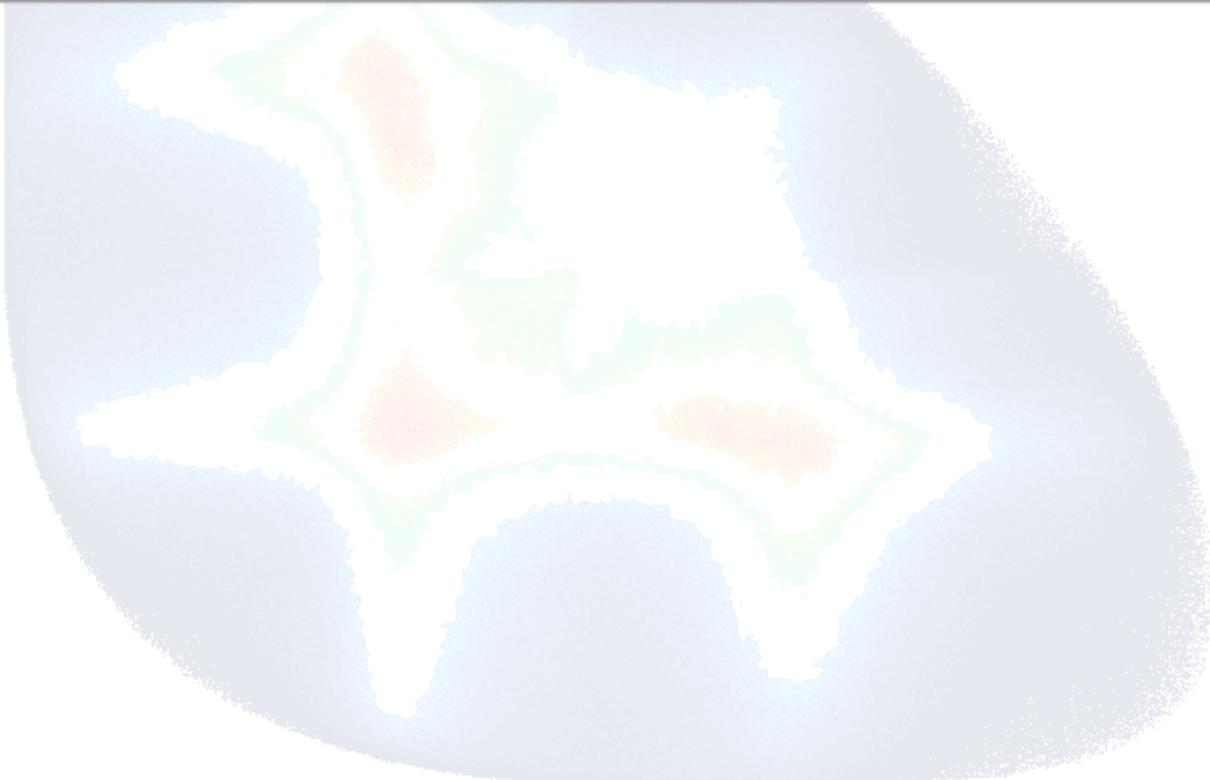
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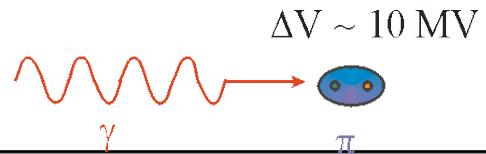
**$\chi$ PT (2-loop):**  $\bar{\alpha}_\pi = (2.9 \pm 0.5) \times 10^{-4} \text{ fm}^3$        $\bar{\beta}_\pi = (-2.8 \pm 0.5) \times 10^{-4} \text{ fm}^3$



# Pion Polarizabilities

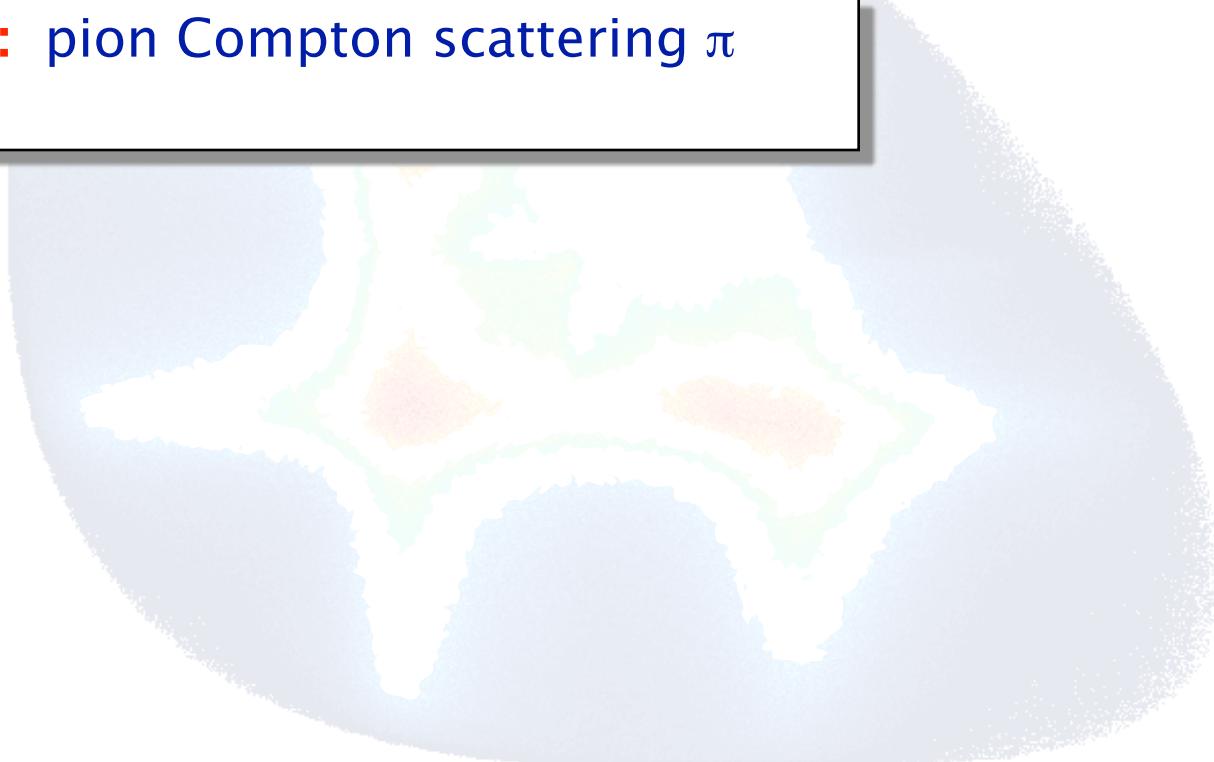
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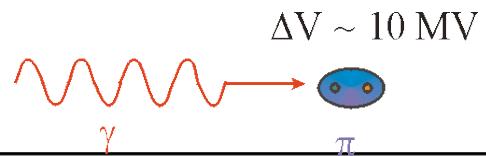
**Experiments:** pion Compton scattering  $\pi^- \gamma \rightarrow \pi^- \gamma$



# Pion Polarizabilities

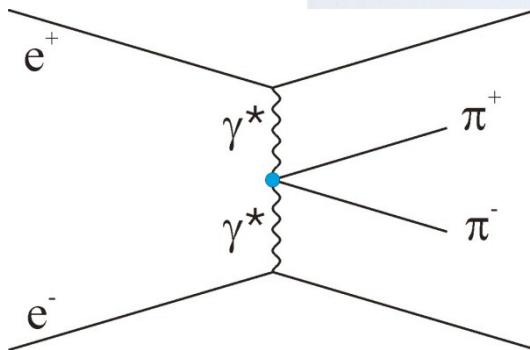
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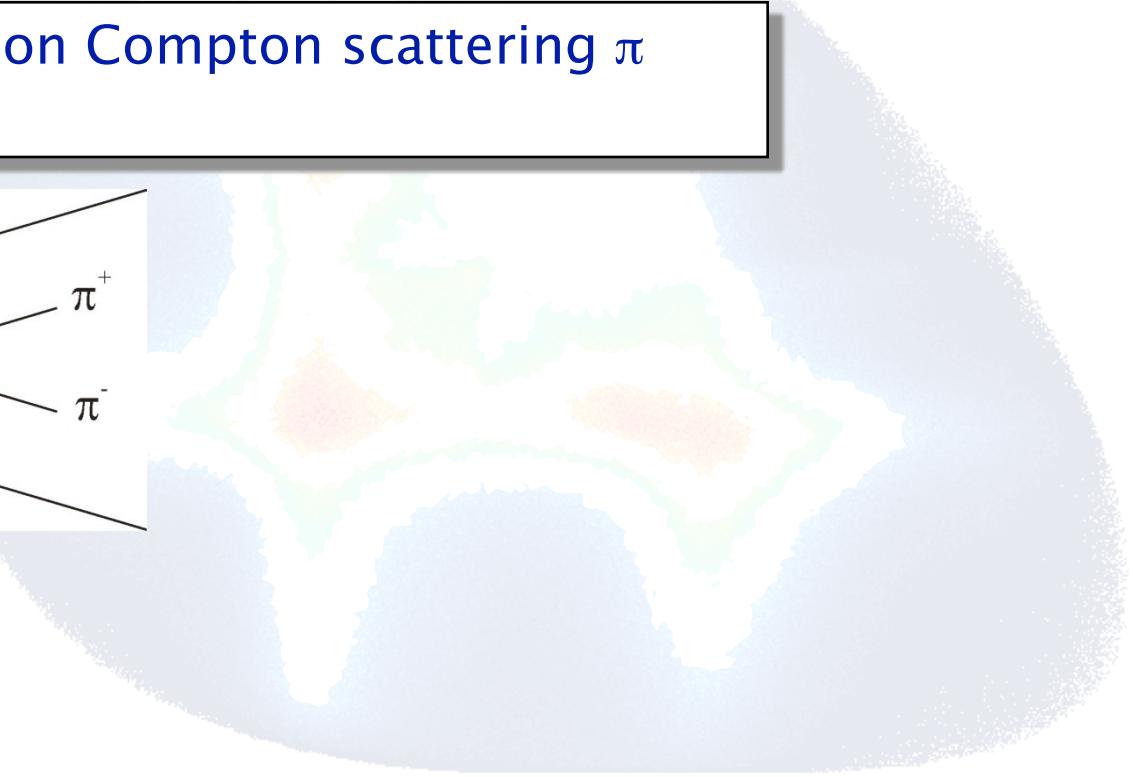


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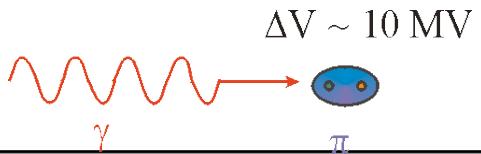
PLUTO  
DM1  
DM2  
Mark II



# Pion Polarizabilities

Describe response to external e.m. fields  $\Rightarrow$  stiffness of system

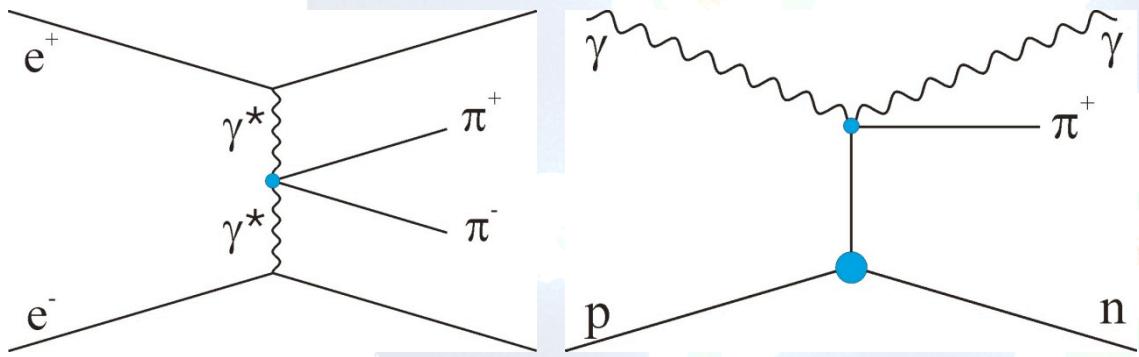
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$$\chi\text{PT (2-loop)}: \quad \bar{\alpha}_\pi = (2.9 \pm 0.5) \times 10^{-4} \text{ fm}^3 \quad \bar{\beta}_\pi = (-2.8 \pm 0.5) \times 10^{-4} \text{ fm}^3$$

Experiments: pion Compton scattering  $\pi^-$

$$-\gamma \rightarrow \pi^- \gamma$$



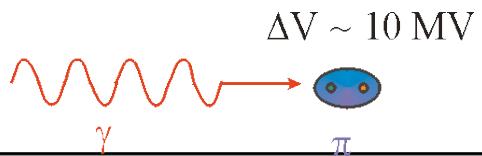
PLUTO  
DM1  
DM2  
Mark II

Lebedev  
Mami A2

# Pion Polarizabilities

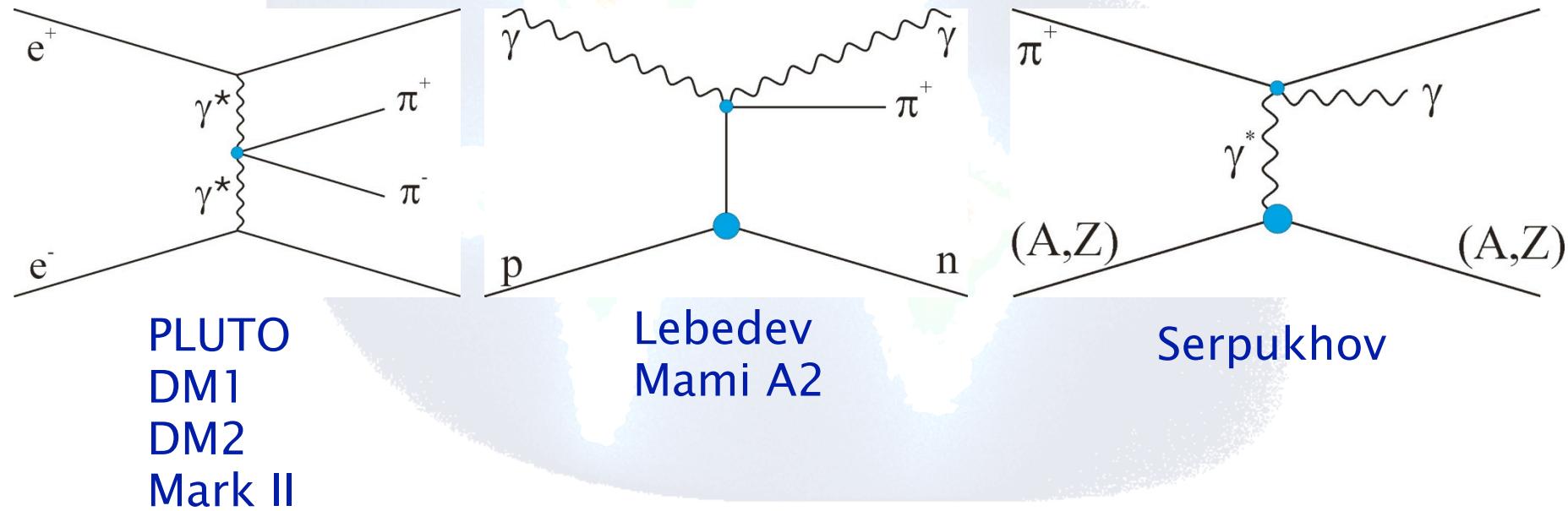
Describe response to external e.m. fields  $\Rightarrow$  stiffness of system

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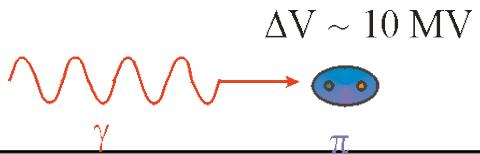
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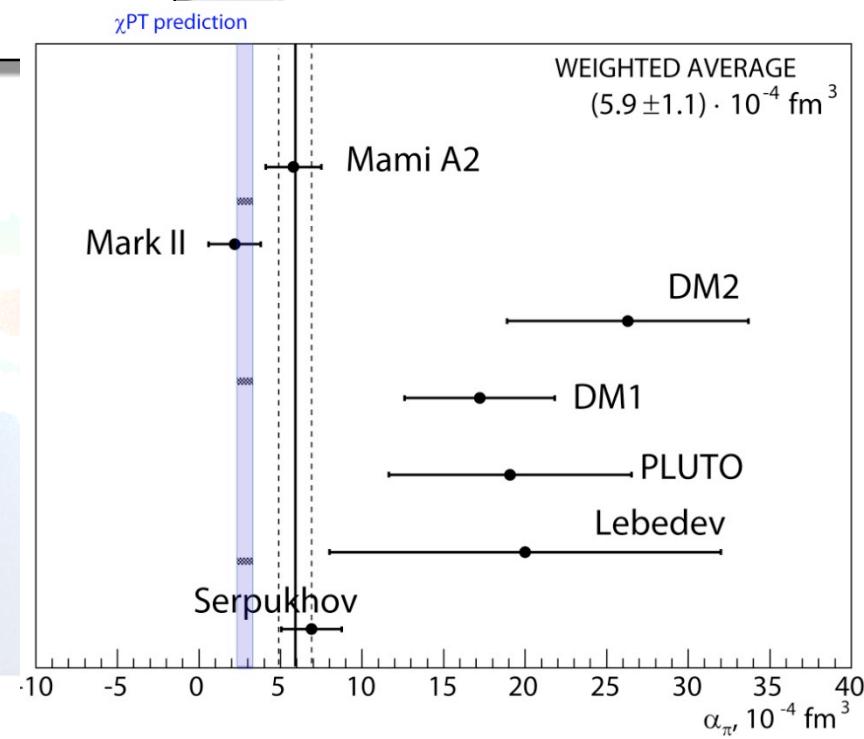
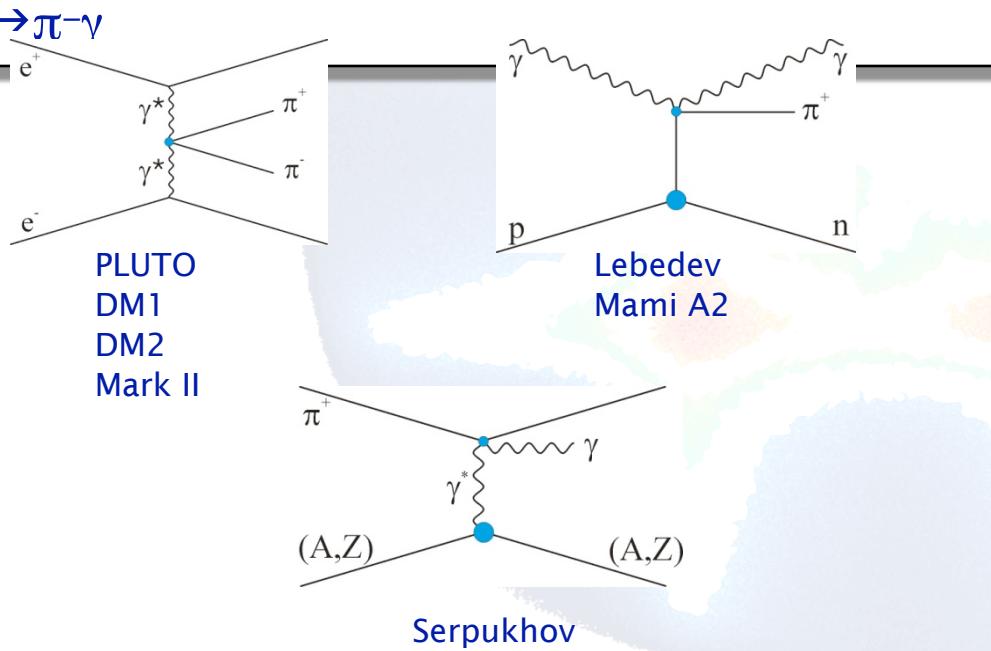
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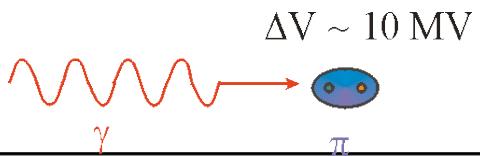
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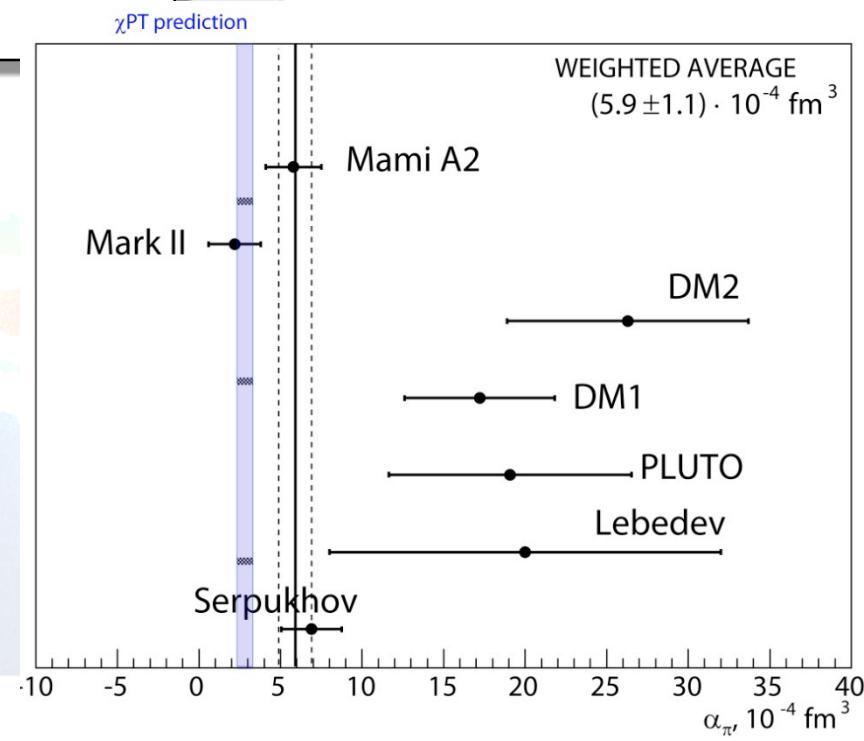
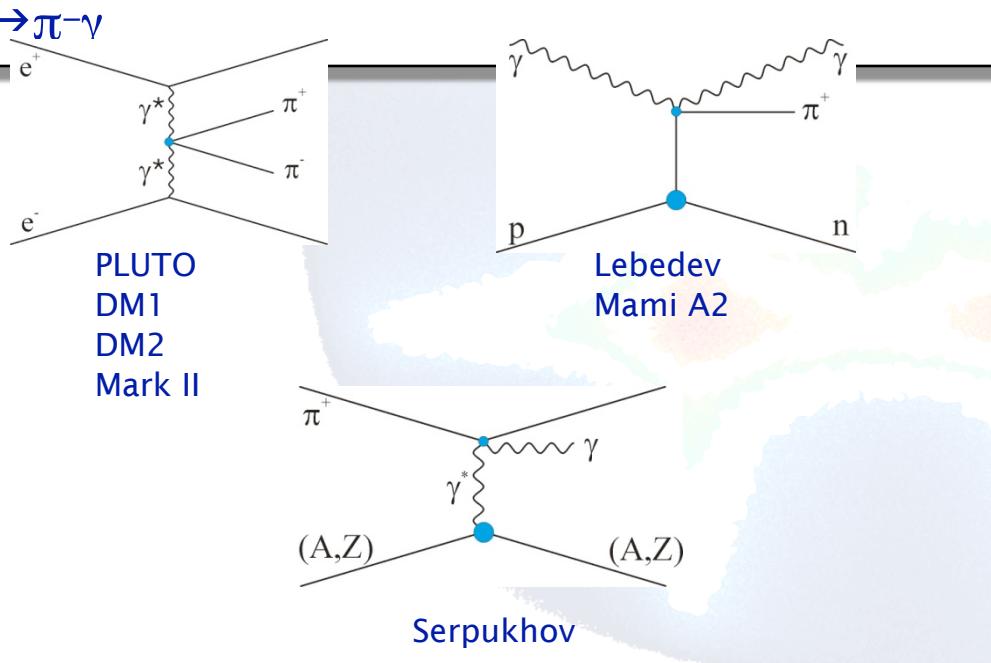
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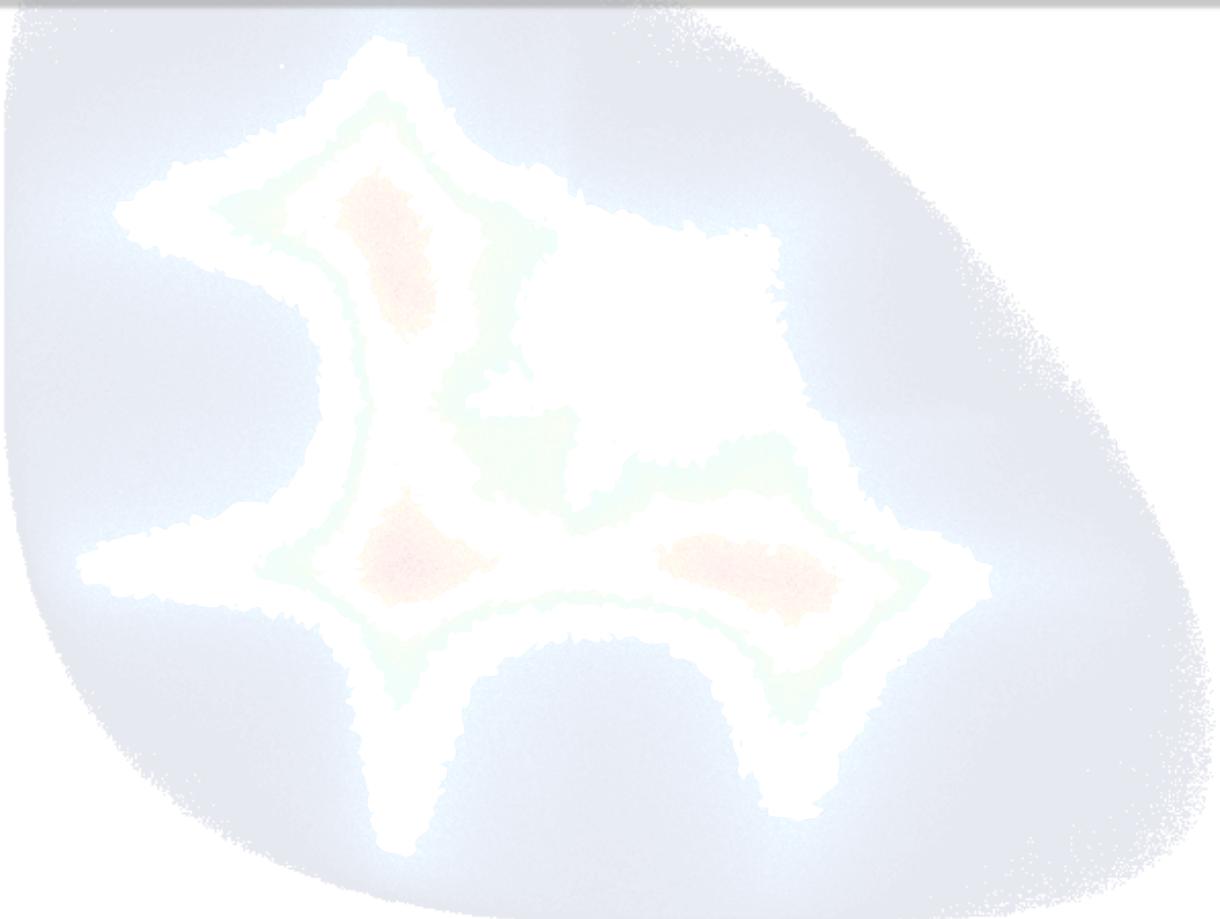
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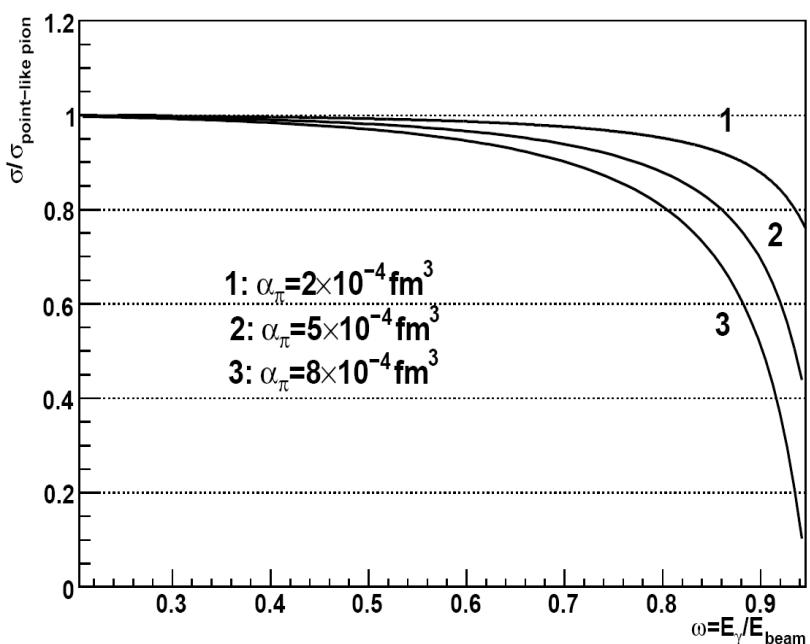
# Cross Section Ratio

$$R(\omega) = \frac{N_{\text{exp}}(\omega)}{N_{\text{MC}}(\omega)} = \frac{d\sigma_{\gamma\pi}^{\text{Prim}}}{d\sigma_{\gamma\pi}^{\text{Thomson}}} \approx 1 + \frac{3}{2} \frac{m_\pi^3}{\alpha} \frac{\omega^2}{1-\omega} \bar{\beta}_\pi, \quad (\bar{\alpha}_\pi + \bar{\beta}_\pi = 0)$$



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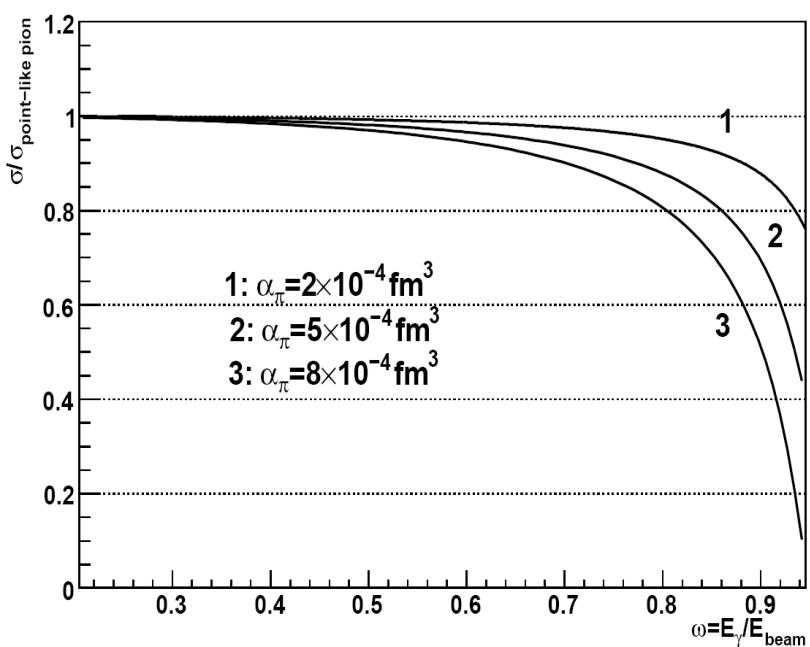
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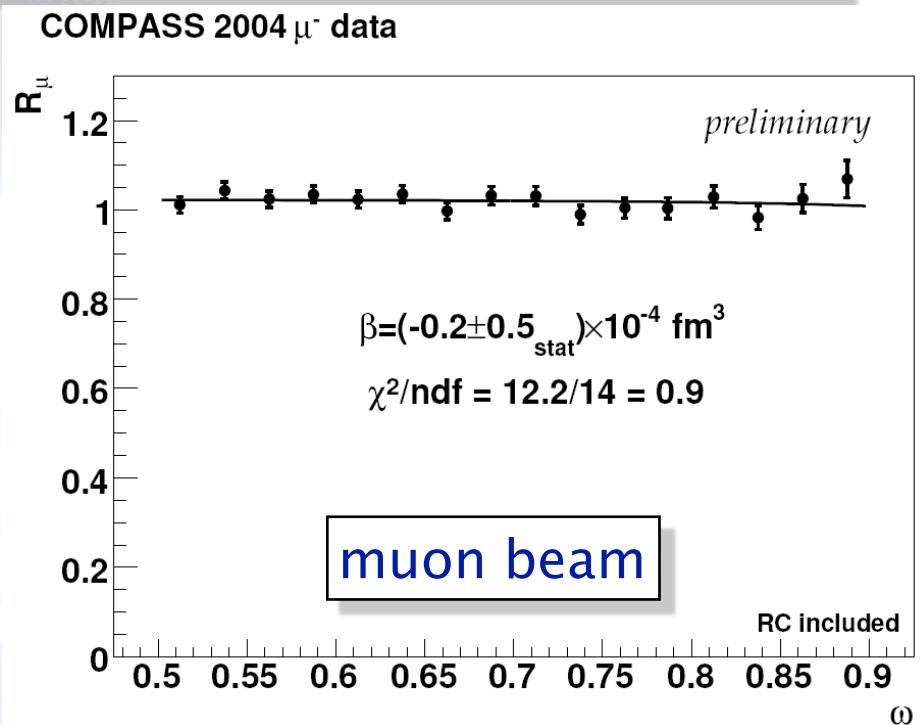
$R(\omega)$  for different values  
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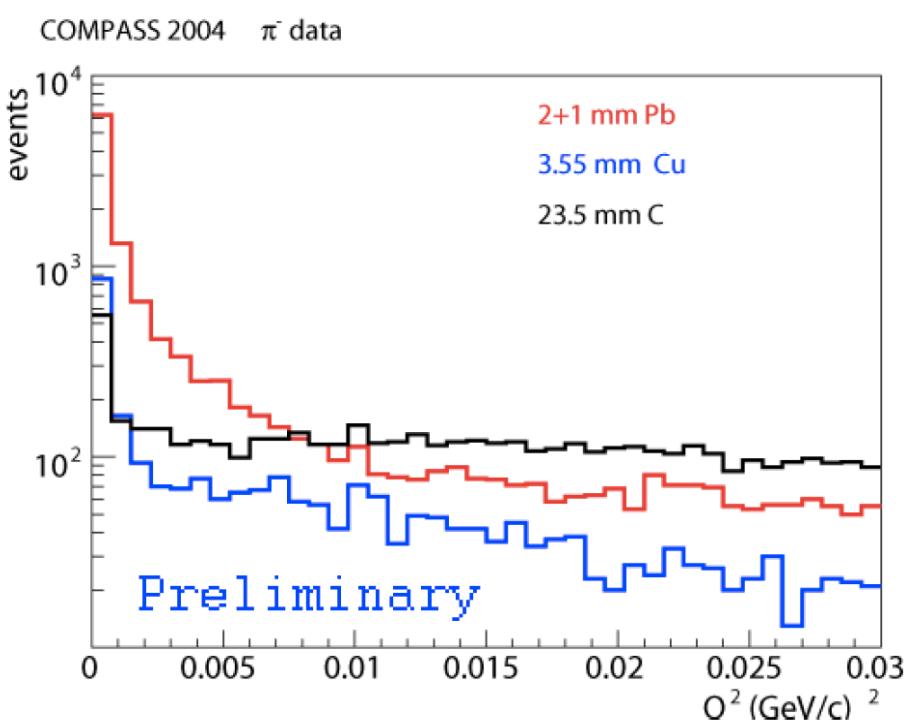
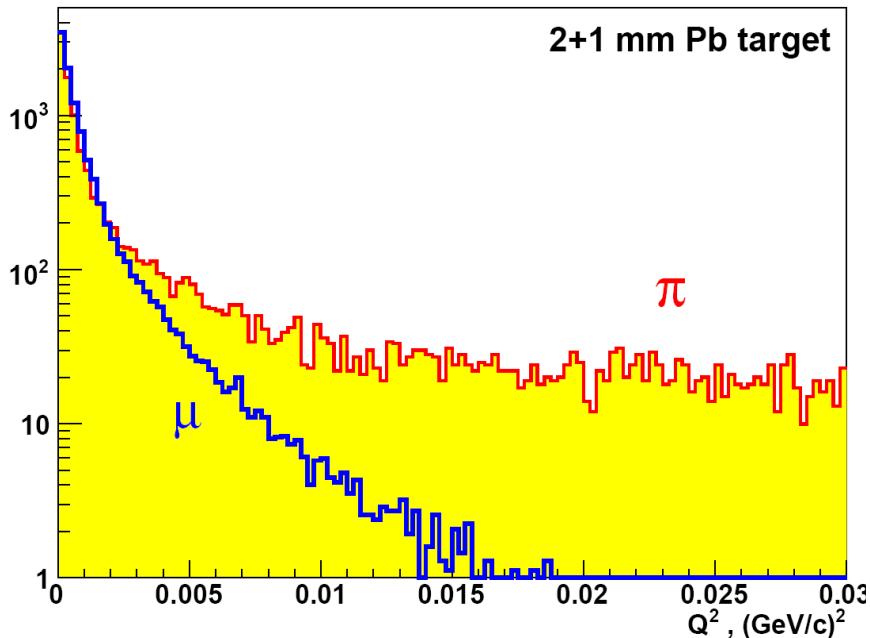
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Cross check with  $\mu$  beam

# $Q^2$ Distributions from Pilot Run

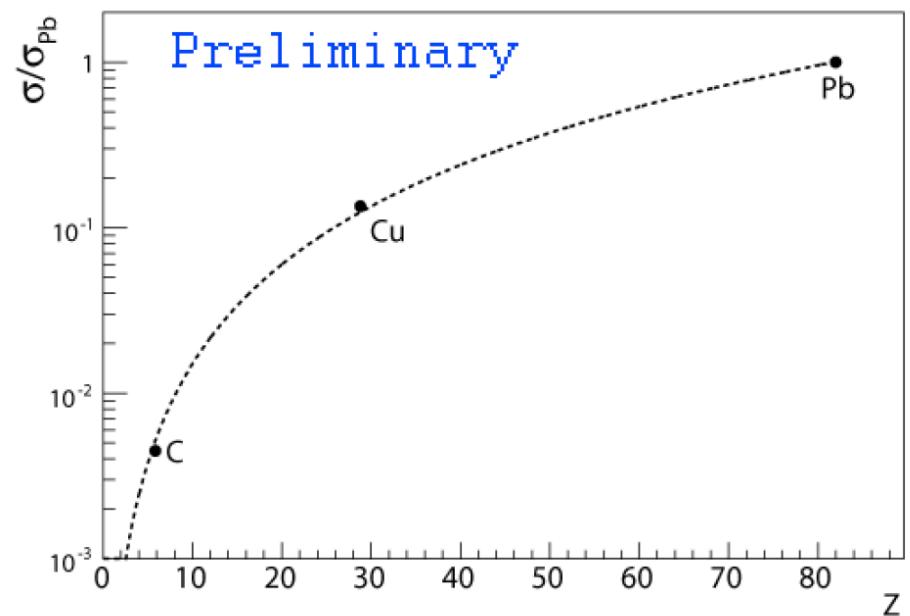
$$\frac{d^3\sigma}{dQ^2 d\omega d\cos\theta} = \frac{\alpha Z^2}{\pi\omega} \times \frac{Q^2 - Q_{\min}^2}{Q^4} \times F_Z(Q^2)^2 \times \frac{d\sigma_{\gamma\pi}(\omega, \theta)}{d\cos\theta}$$



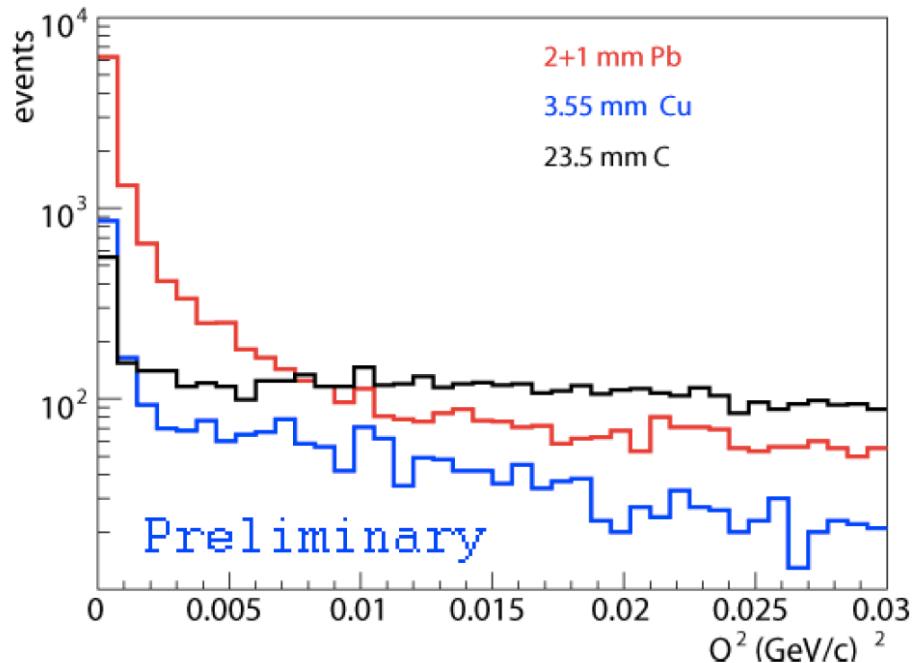
# $Z^2$ Dependence of Cross Section

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COMPASS 2004  $\pi^-$  data



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## Major improvements:

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- Optimized target:  $^{58}\text{Ni}$
- Radiative corrections
- Beyond Weizsäcker-Williams approach
- Interference with diffractive amplitudes
- Suppression of  $\pi^-\pi^0$  background
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## Prospects (4 weeks):

- $\sigma_{\text{stat}} \sim 0.33 \cdot 10^{-4} \text{ fm}^3$
- $\sigma_{\text{sys}} \sim 0.16 \cdot 10^{-4} \text{ fm}^3$
- independent extraction of  $\alpha_\pi$ ,  $\beta$  with  $\sigma_{\text{stat}} \sim 0.5 \cdot 10^{-4} \text{ fm}^3$
- $\alpha_\pi(s)$
- first measurement of  $\alpha_K$

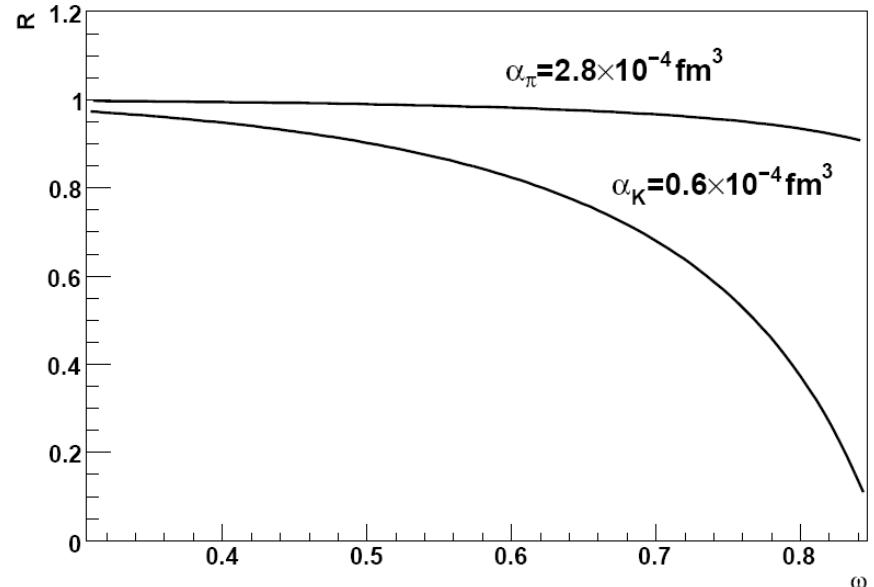
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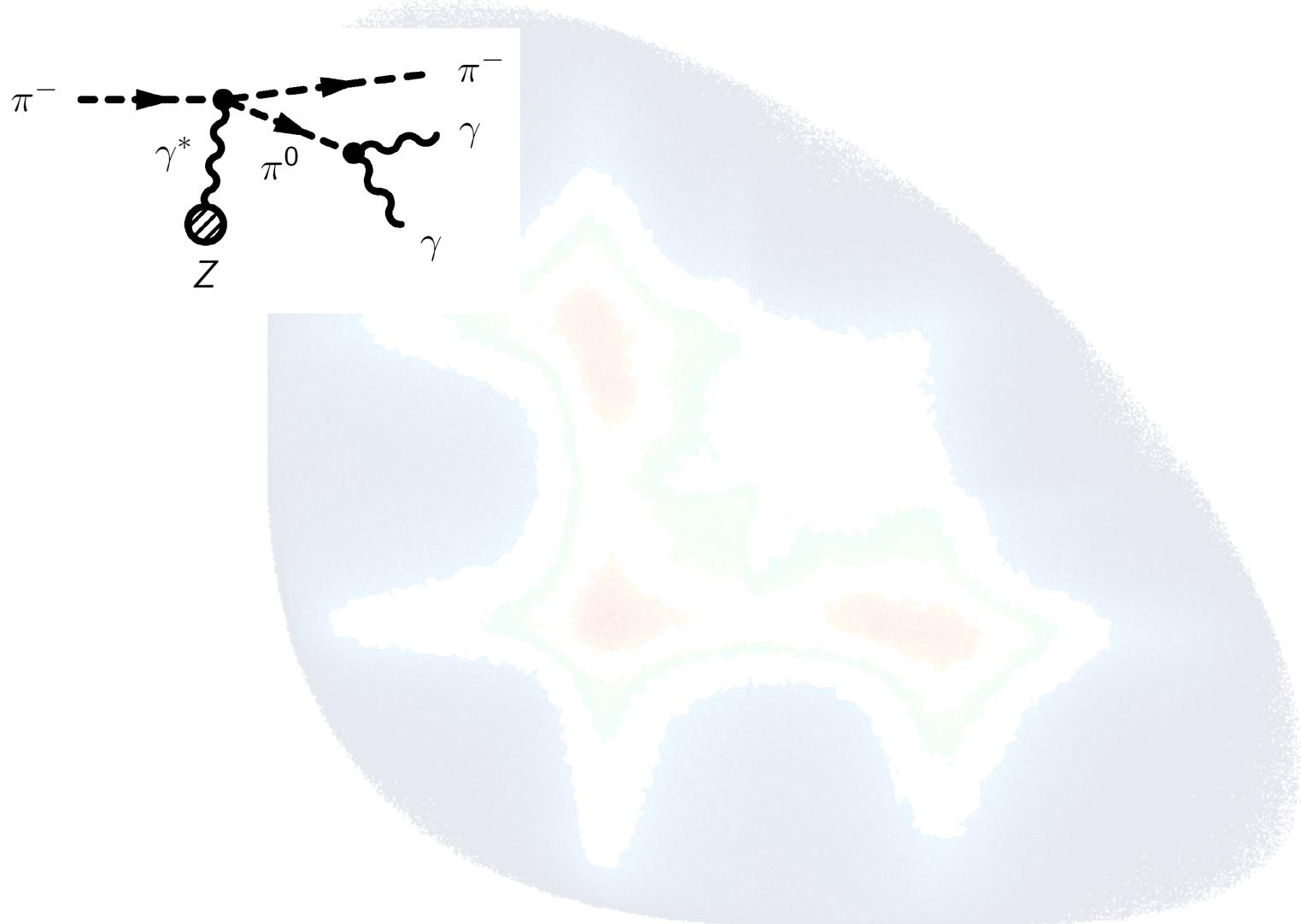
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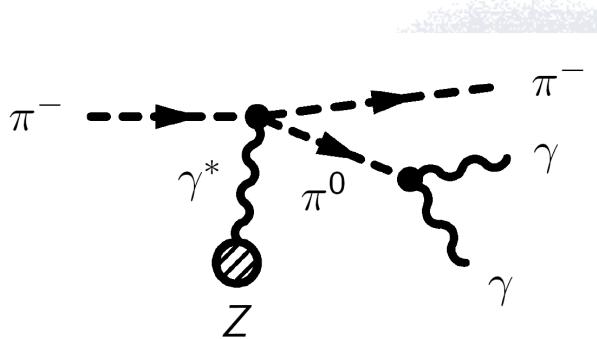
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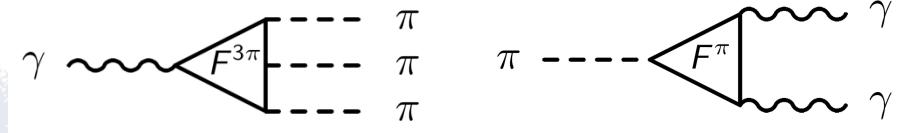
## Primakoff $\pi^0$ production



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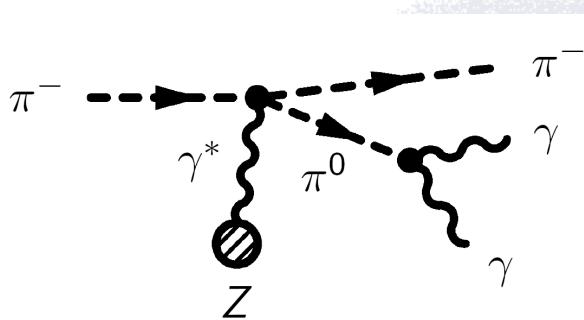


## Chiral Perturbation Theory

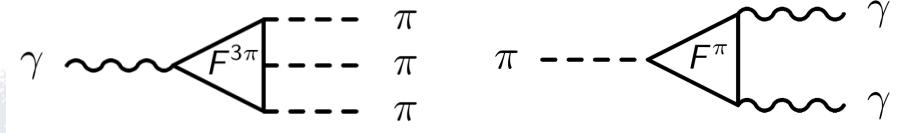


$$F^{3\pi}(0) = \frac{F^\pi(0)}{\sqrt{\pi\alpha} f_\pi^2}, f_{\pi^\pm} = (130.7 \pm 0.4) \text{ MeV}$$

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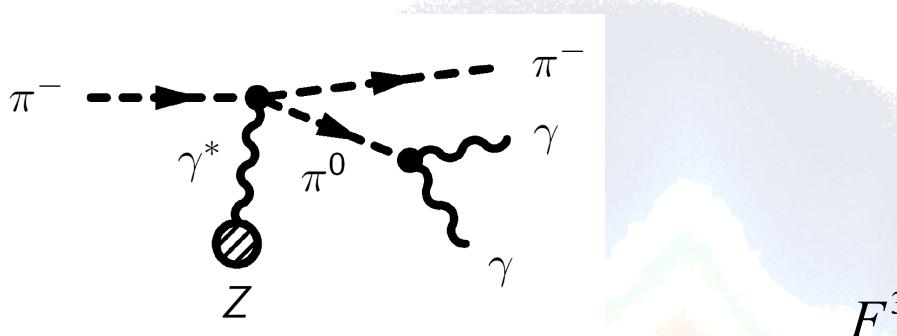
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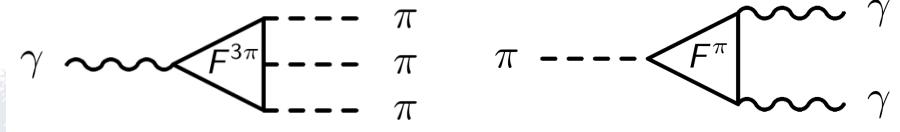
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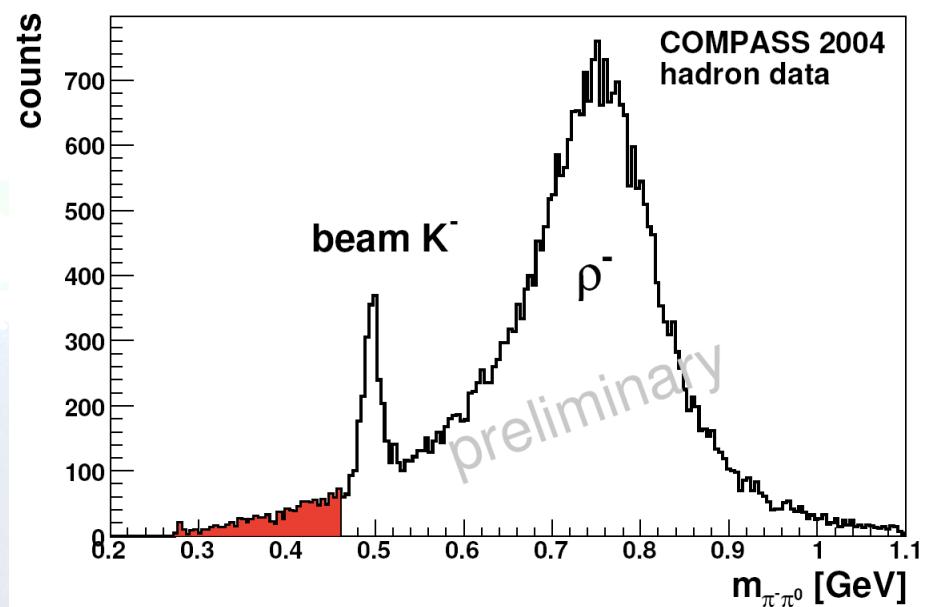
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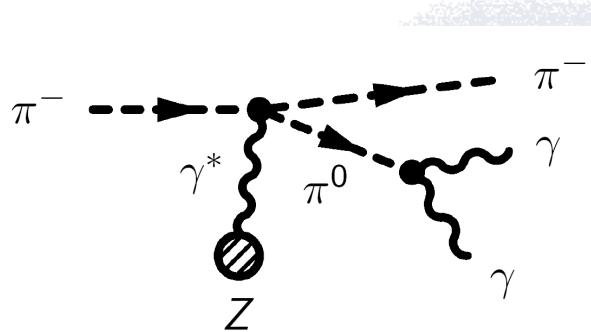
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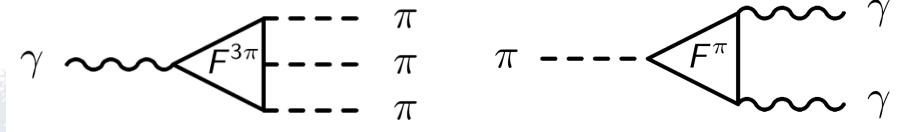
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- Further reactions channels studied in COMPASS:  $\pi^- Z \circledcirc \pi^- Z \pi^0 \pi^0$

$$\pi^- Z \circledcirc \pi^- Z \eta$$