

hard photon &  
meson  
production  
workshop

European Centre for  
Theoretical studies  
Trento, Italy  
10th-15th October

# Studies of TMDs at *COMPASS*

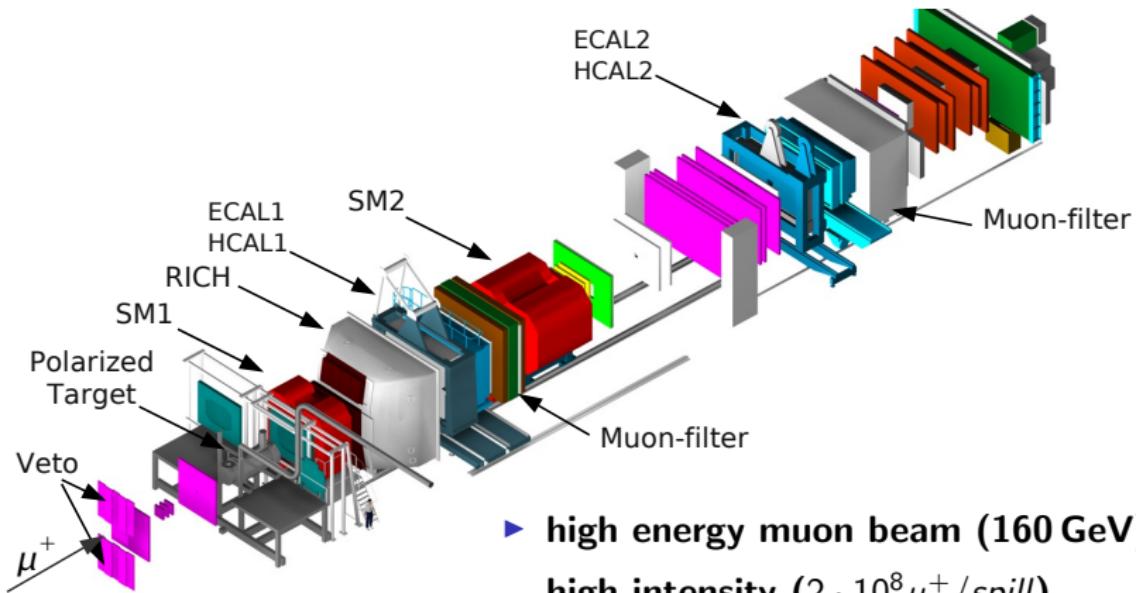
Heiner Wollny  
CEA-Saclay Irfu/SPhN  
on behalf of COMPASS



## Outline:

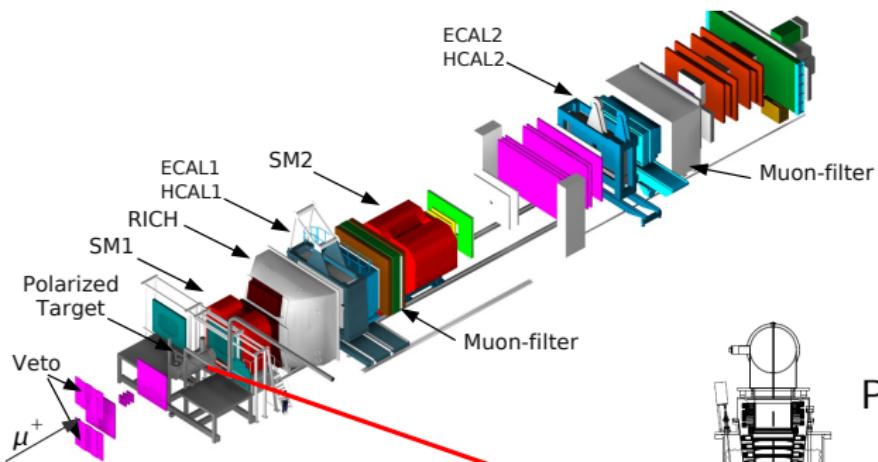
- ▶ Transversity: single hadrons, hadron pairs,  $\Lambda$  baryons
- ▶ TMDs: measured with transversely, longitudinally and unpolarized nucleons

# COMPASS Detector (muon setup)

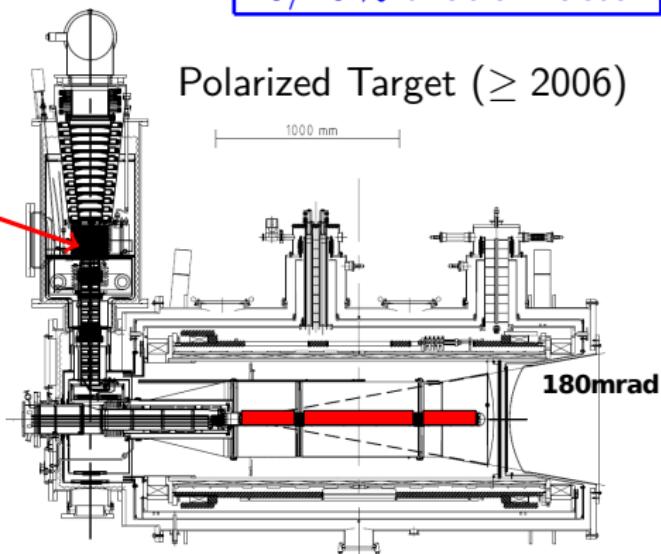
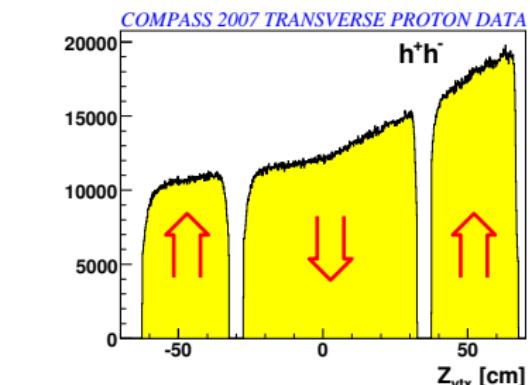


- ▶ **high energy muon beam (160 GeV)**
- ▶ **high intensity ( $2 \cdot 10^8 \mu^+/\text{spill}$ )**
- ▶ **naturally polarized ( $\sim 80\%$ )**
- ▶ **two stages spectrometer:**
  - ~ **large angular acceptance ( $0 \leq \theta_{\text{lab}} \leq 180 \text{ mrad}$ )**
  - ~ **broad kinematical range in  $x$  and  $Q^2$**

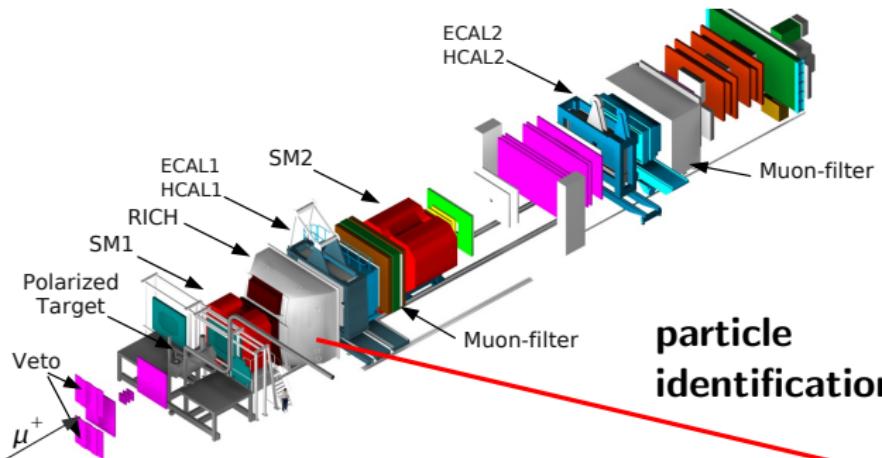
# COMPASS Polarized Target



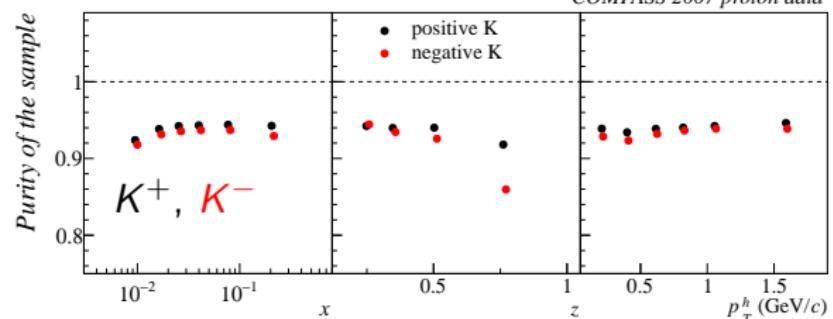
${}^6\text{LiD}$  or  $\text{NH}_3$   
50/90 % polarization  
40/16 % dilution factor



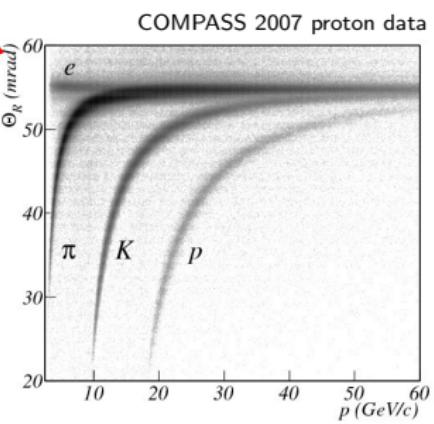
# COMPASS RICH



## particle identification



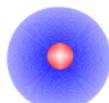
purity of  $\pi^\pm$  sample > 99 %



# Nucleon in Leading Order

In leading order three parton distributions are needed to describe the structure of the nucleon:

$q(x)$



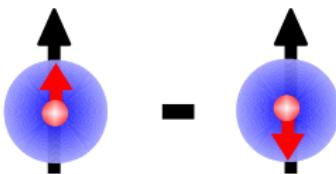
quark distribution  
in unpolarized DIS  
 $\ell N \rightarrow \ell' X$

$\Delta q(x)$



helicity distribution  
in polarized DIS  
 $\vec{\ell} \vec{N} \rightarrow \ell' X$

$\Delta_T q(x) = q^{\uparrow\uparrow}(x) - q^{\uparrow\downarrow}(x)$



transversity distribution  
in polarized SIDIS

1.  $\ell N^\uparrow \rightarrow \ell' h X$  Collins FF
2.  $\ell N^\uparrow \rightarrow \ell' hh X$  Interference FF
3.  $\ell N^\uparrow \rightarrow \ell' \Lambda^\uparrow X$  FF of  $q^\uparrow \rightarrow \Lambda^\uparrow$

# 1. Collins Asymmetry: $\ell N^\uparrow \rightarrow \ell' h X$

## Measuring transversity with Collins-FF $\Delta_T^0 D_q^h$ :

fragmentation of a transversely polarized quark into an unpolarized hadron

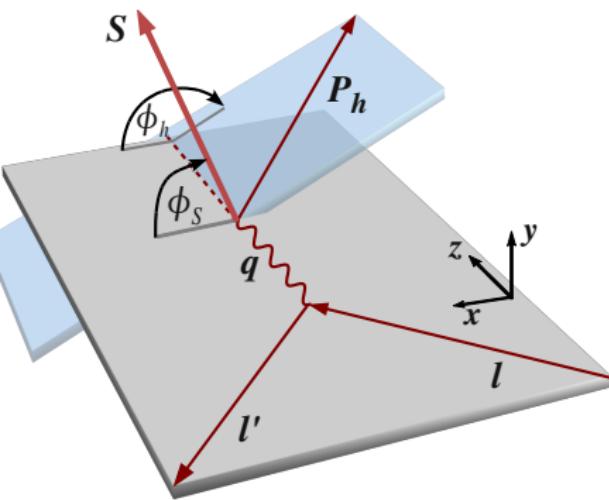
$\leadsto$  azimuthal asymmetry:

$$N_h \propto 1 \pm A \cdot \sin \phi_{Coll}$$

$$\phi_{Coll} = \phi_h + \phi_s - \pi$$

$\phi_h$ : azimuthal angle of hadron

$\phi_s$ : azimuthal angle of spin of initial quark



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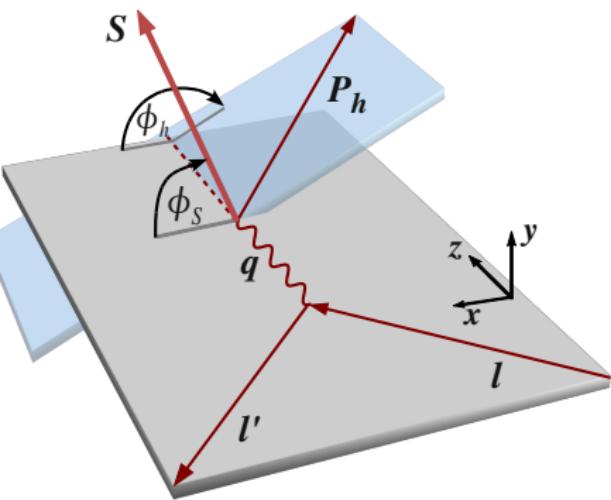
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$\phi_s$ : azimuthal angle of spin of initial quark



$$A_{Coll} = \frac{A}{f P_T D_{nn}} \propto \sum_q e_q^2 \cdot \Delta_T q \otimes \Delta_T^0 D_q^h$$

$f$  = target dilution

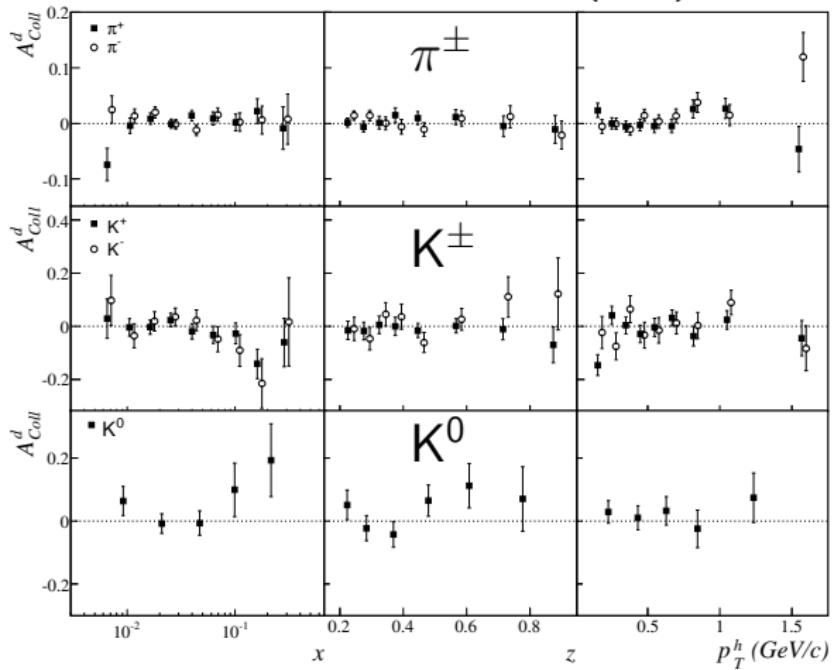
$P_T$  = target polarization

$$D_{nn} = \frac{1-y}{1-y+\frac{y^2}{2}} = \text{transverse spin transfer}$$

# Collins Asymmetries: ${}^6\text{LiD}$ (2003-2004)



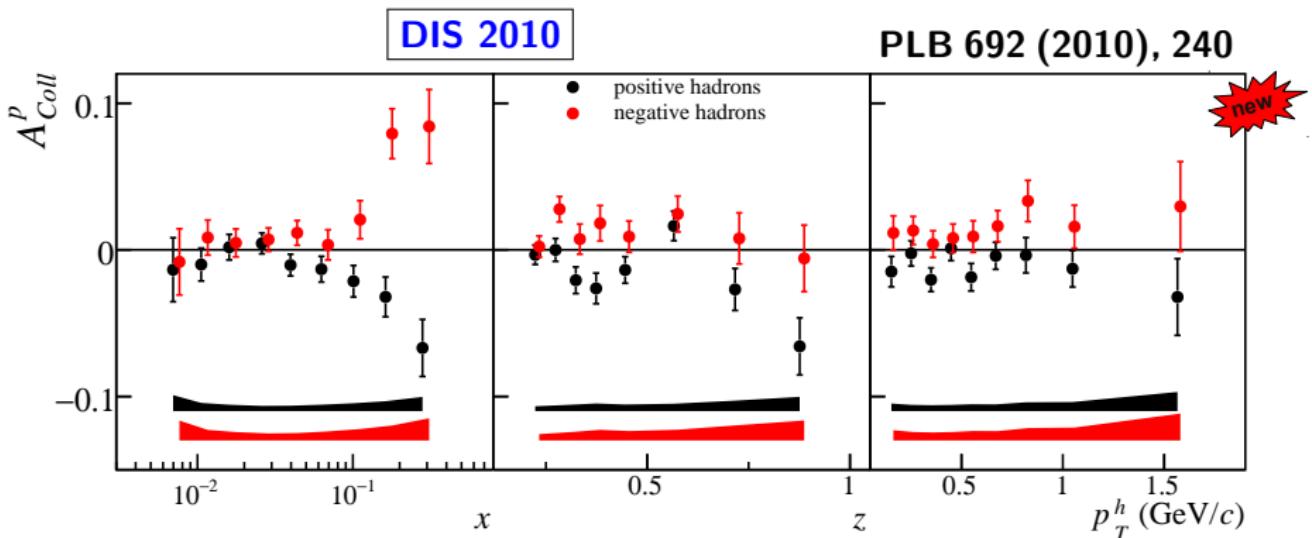
PLB 673 (2009) 127-135



all asymmetries are small,  
compatible with zero

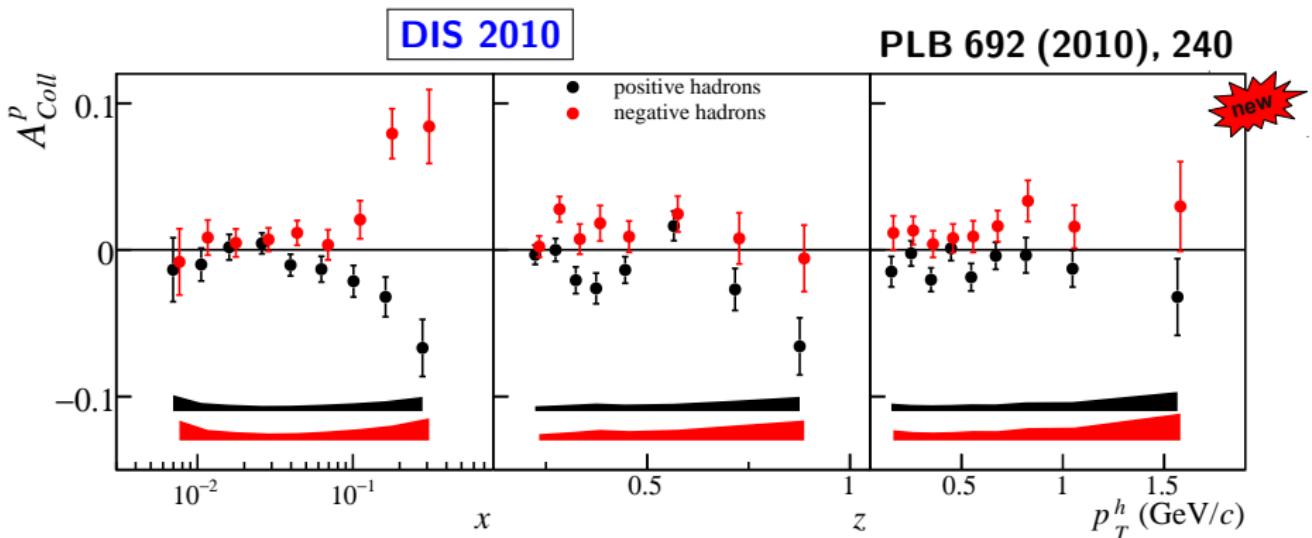
systematical error:  $\sigma_{\text{sys}} \leq 0.3 \sigma_{\text{stat}}$

# Collins Asymmetries: NH<sub>3</sub> (2007)



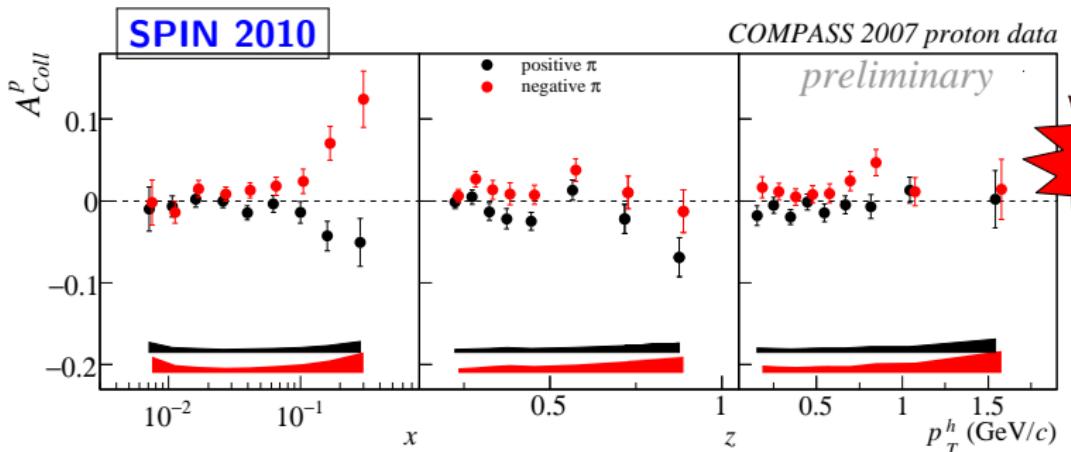
- Large asymmetries for proton  $\sim 10\%$

# Collins Asymmetries: NH<sub>3</sub> (2007)

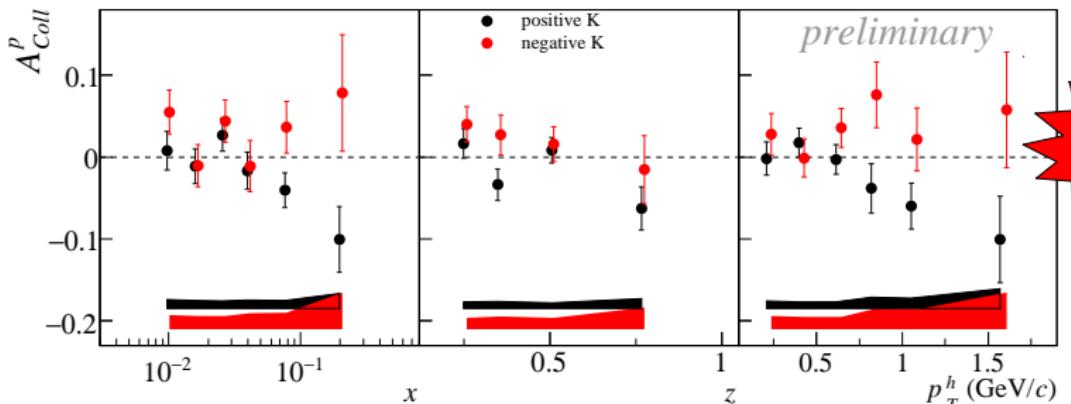


- ▶ Large asymmetries for proton  $\sim 10\%$
- ▶ Small asymmetries for deuteron  
 $\leadsto$  cancellation of  $\Delta_T u$  and  $\Delta_T d$

# Collins Asymmetries for $\pi^\pm$ and $K^\pm$ : NH<sub>3</sub> (2007)

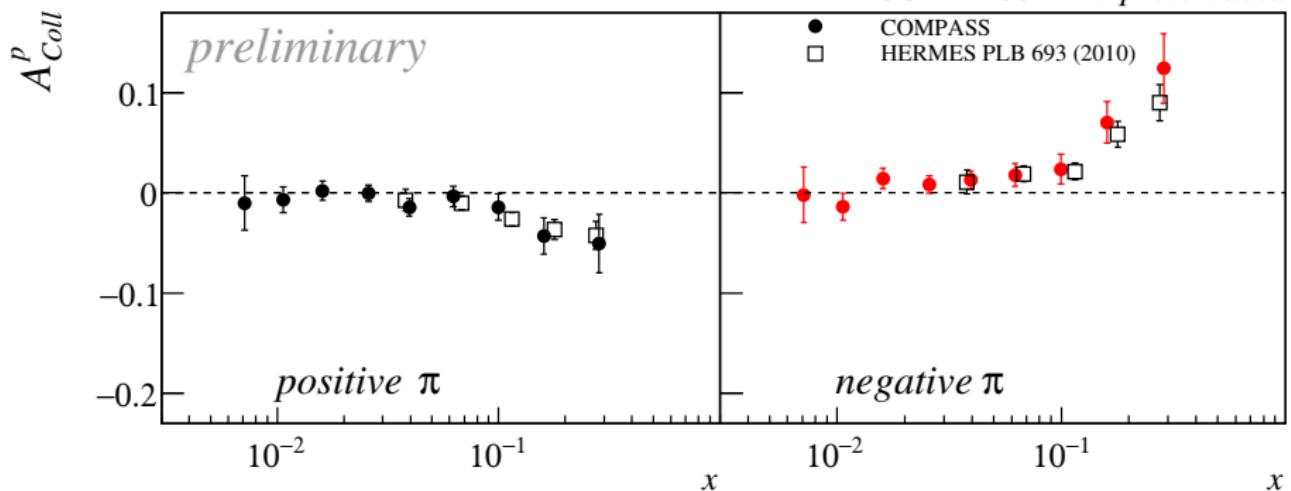


**new**



**new**

# Collins Asymmetries for $\pi^\pm$ : NH<sub>3</sub> (2007)

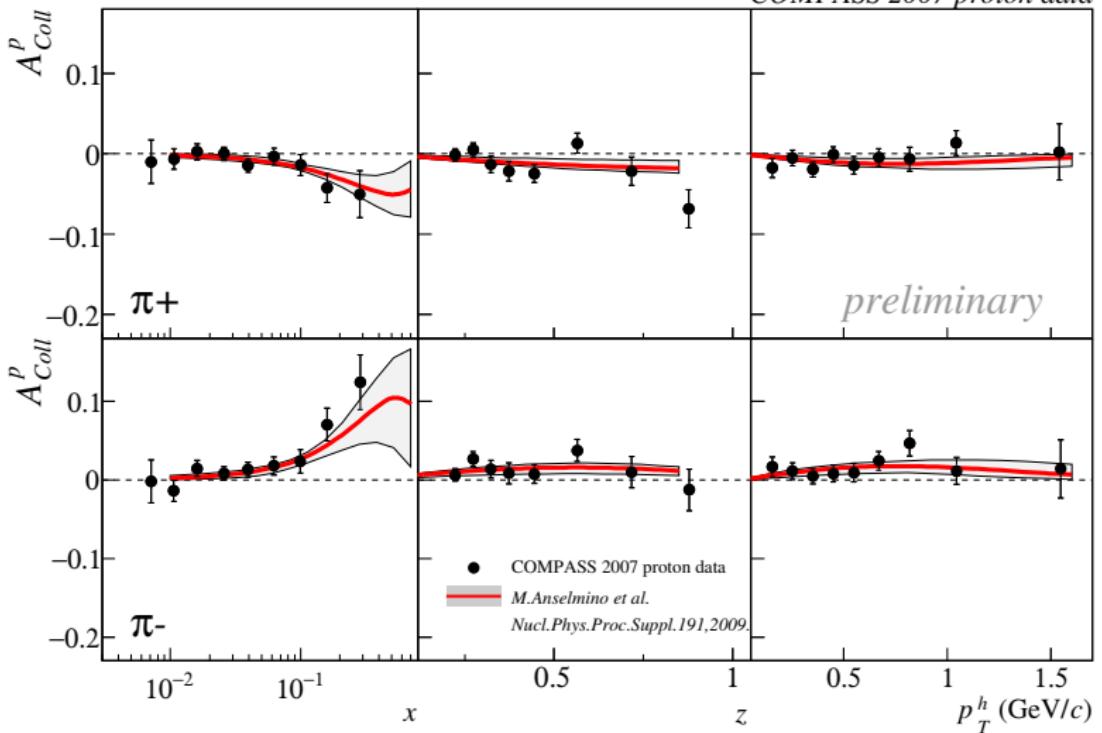


- Good agreement in overlap region  
(HERMES results are not  $D_{nn}$  corrected)

# Collins Asymmetries for $\pi^\pm$ : NH<sub>3</sub> (2007)

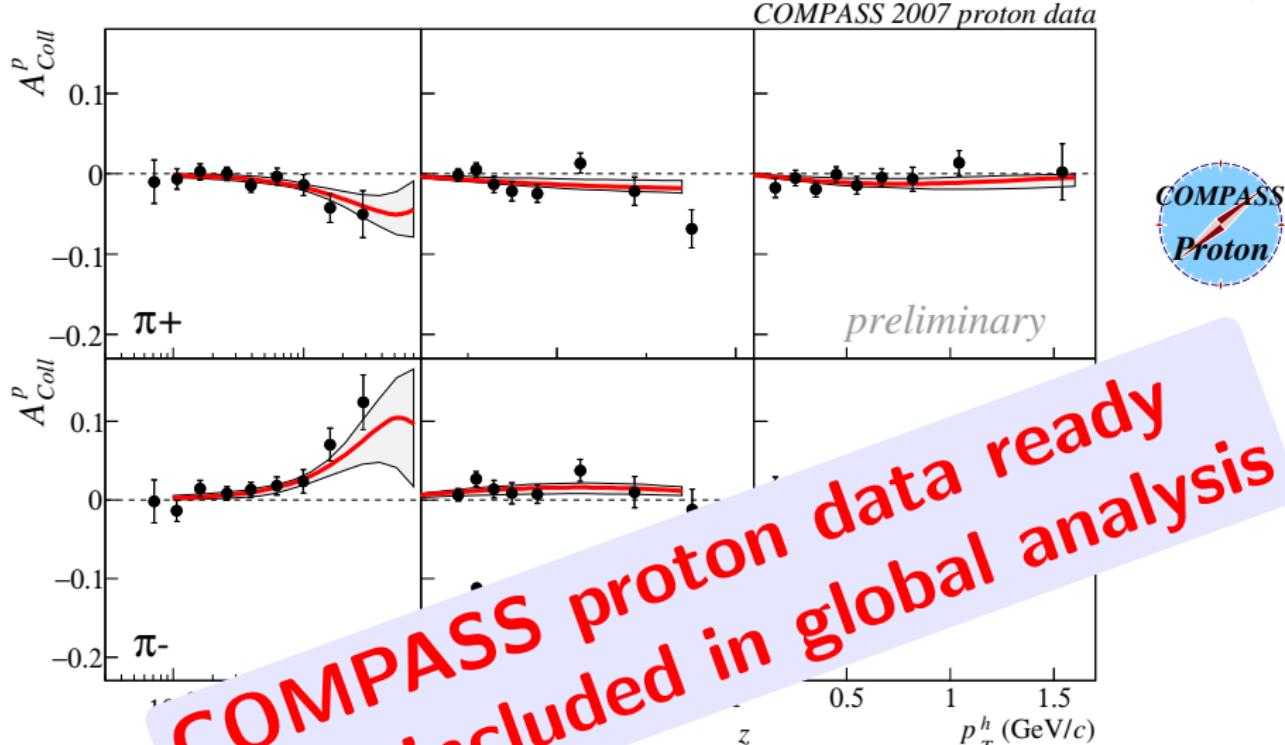


COMPASS 2007 proton data



Predictions from fit to COMPASS deuteron, HERMES proton and Belle  $e^+e^-$  data

# Collins Asymmetries for $\pi^\pm$ : NH<sub>3</sub> (2007)



Predictions  
and Belle  
data

COMPASS deuteron, HERMES proton



## 2. Dihadron Interference: $\ell N^\uparrow \rightarrow \ell' hhX$

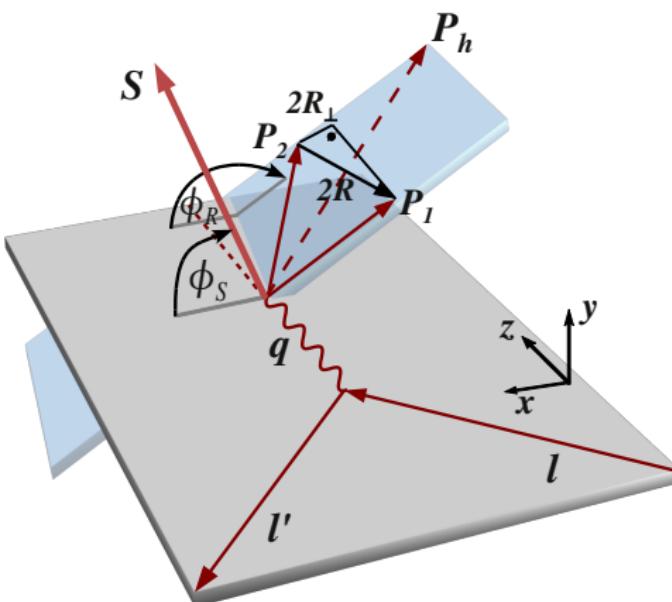
### Measuring transversity with polarized Dihadron-Interference-FF $H_1^<$ :

fragmentation of transversely polarized quark  
into two unpolarized hadrons and rest X

→ azimuthal asymmetry:

$$N_{h^+h^-} \propto 1 \pm A \cdot \sin \phi_{RS} \cdot \sin \theta$$

$$\phi_{RS} = \phi_R + \phi_S - \pi$$



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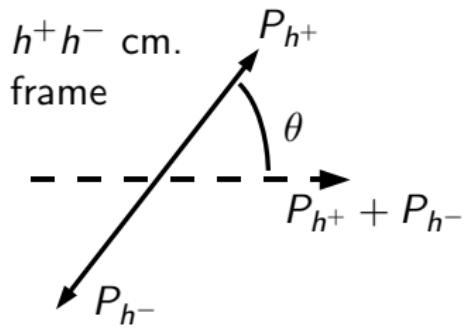
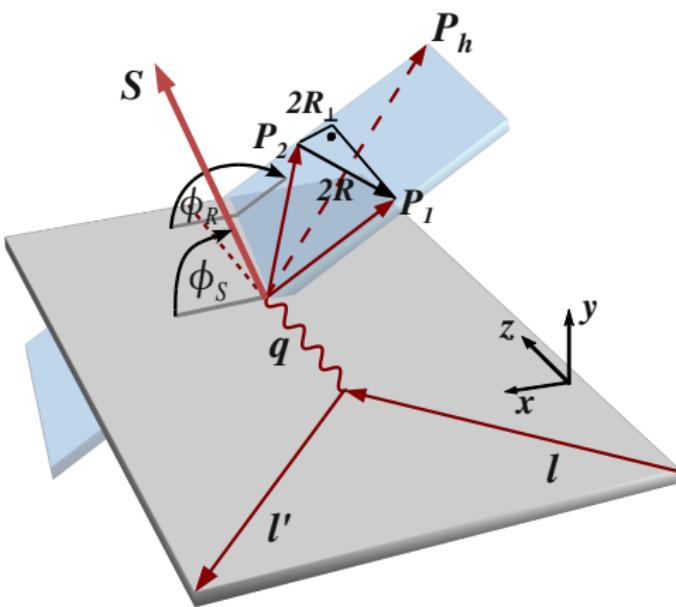
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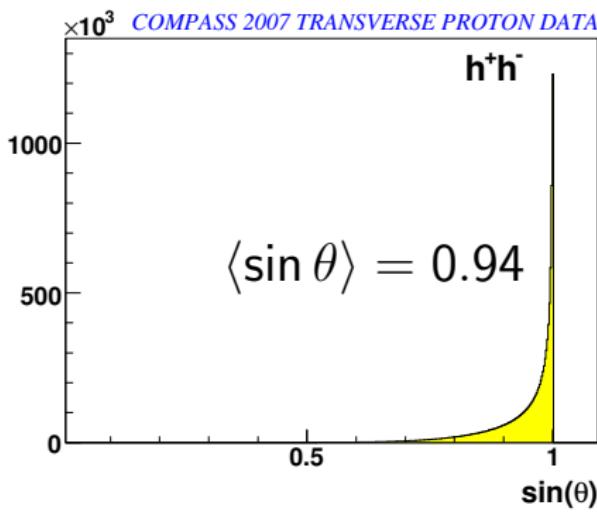
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For this analysis:  
 $\sin \theta$  can be neglected

## 2. Dihadron Interference: $\ell N^\uparrow \rightarrow \ell' hhX$

### Measuring transversity with polarized Dihadron-Interference-FF $H_1^\triangleleft$ :

fragmentation of transversely polarized quark  
into two unpolarized hadrons and rest X

→ azimuthal asymmetry:

$$N_{h^+ h^-} \propto 1 \pm A \cdot \sin \phi_{RS}$$

$$\phi_{RS} = \phi_R + \phi_S - \pi$$

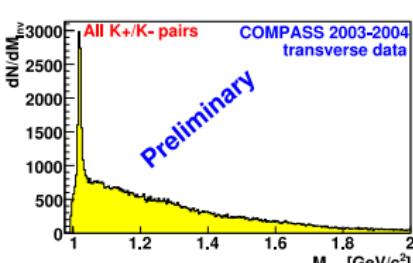
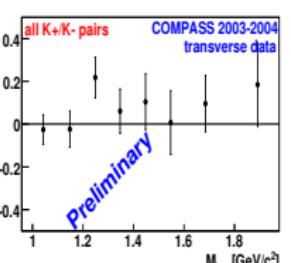
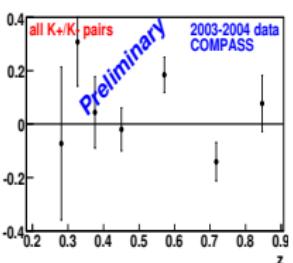
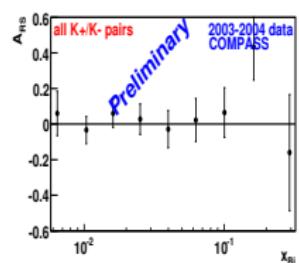
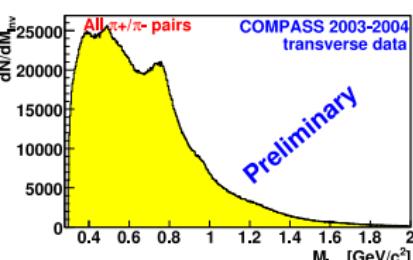
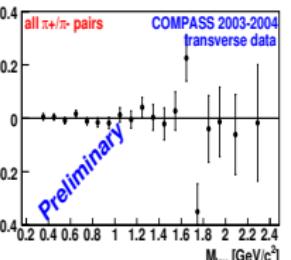
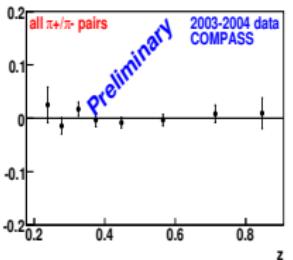
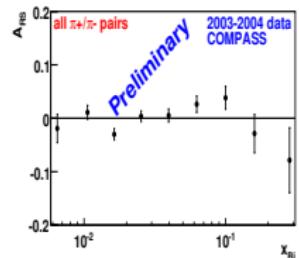
$$A_{RS} = \frac{A}{f P_T D_{nn}} \propto \sum_q e_q^2 \cdot \Delta_T q \cdot H_1^\triangleleft$$

$f$  = target dilution

$P_T$  = target polarization

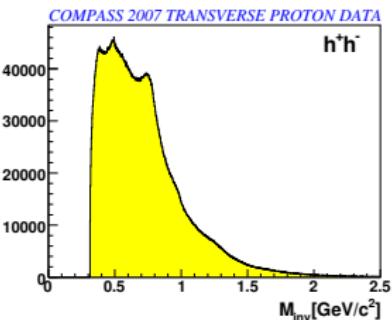
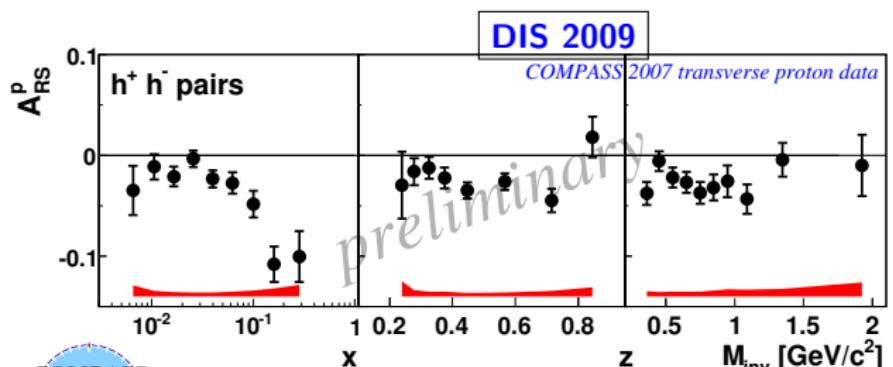
$D_{nn} = \frac{1-y}{1-y+\frac{y^2}{2}}$  = transverse spin transfer

# Dihadron Asymmetries: ${}^6\text{LiD}$ (2003-2004)



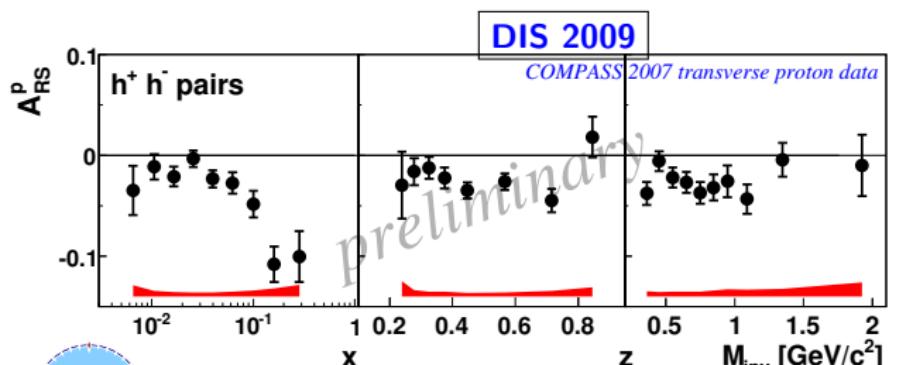
all asymmetries are small, compatible with zero

# Dihadron Asymmetries: NH<sub>3</sub> (2007)

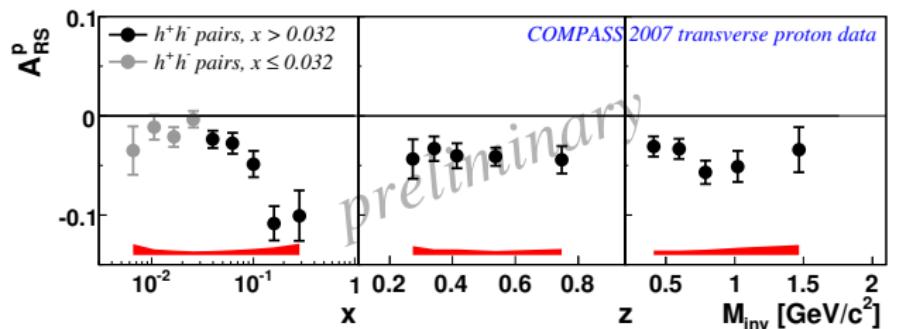
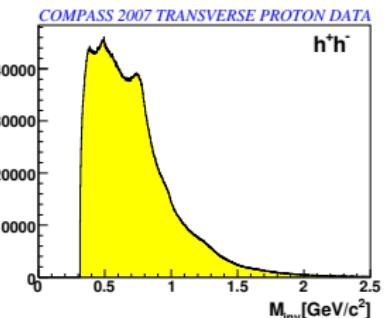


- ▶ Large asymmetries for proton  $\sim 10\%$

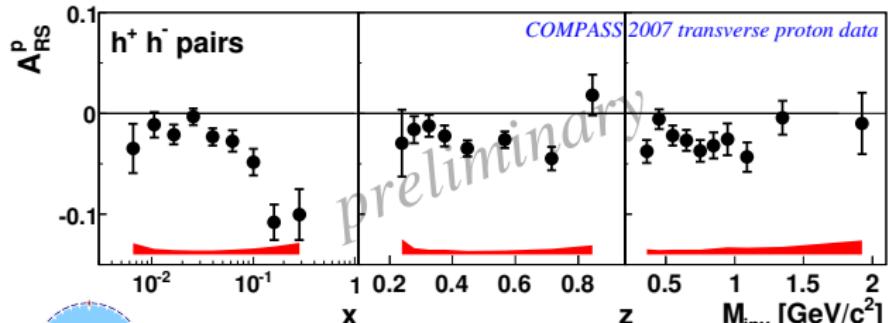
# Dihadron Asymmetries: NH<sub>3</sub> (2007)



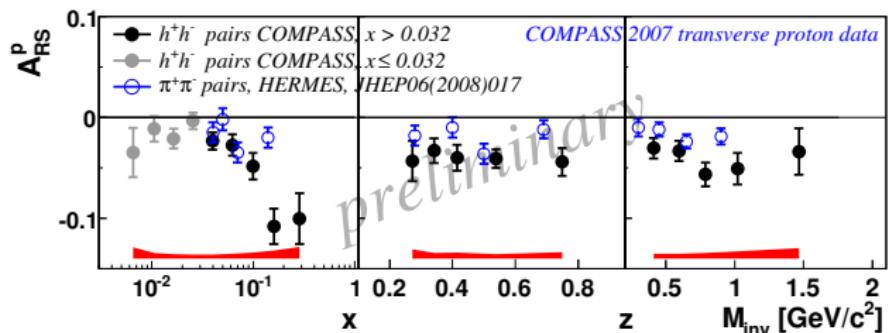
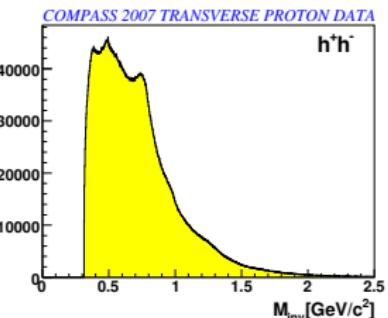
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# Dihadron Asymmetries: NH<sub>3</sub> (2007)

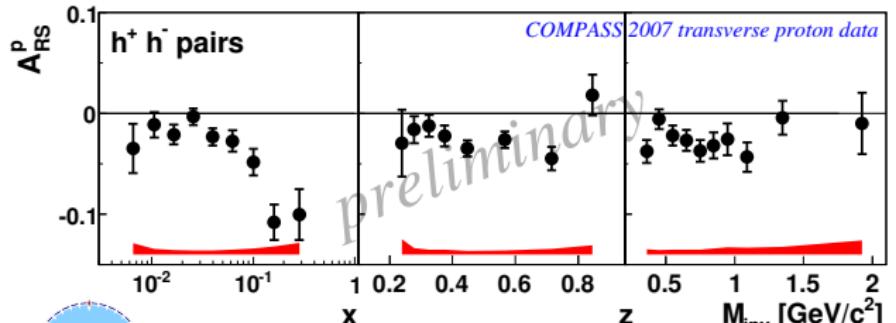


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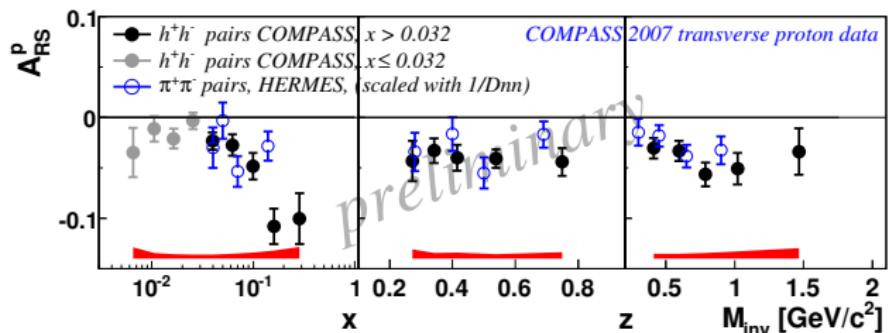
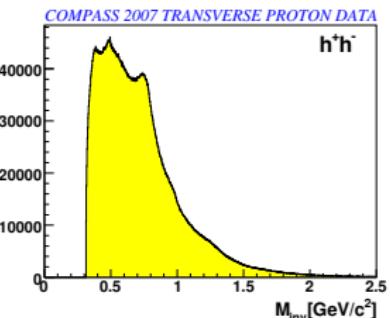


COMPASS measurement covers much larger range in  $x$

# Dihadron Asymmetries: NH<sub>3</sub> (2007)



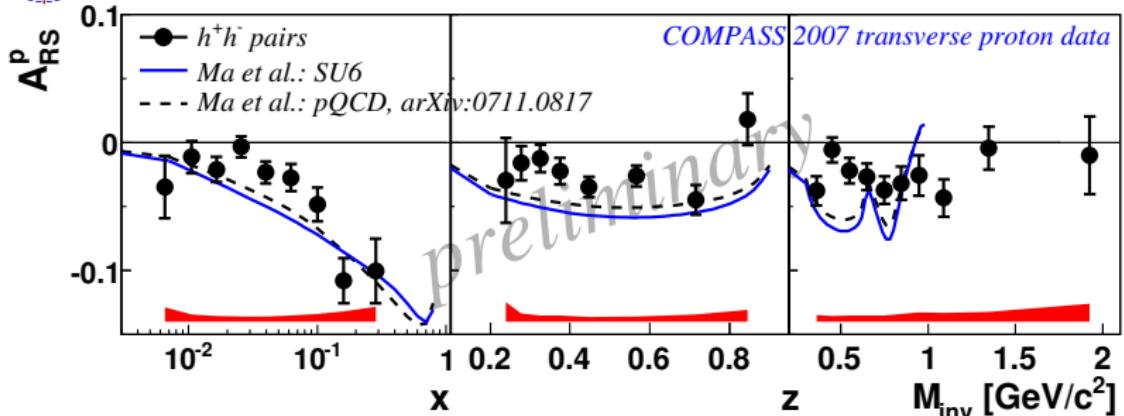
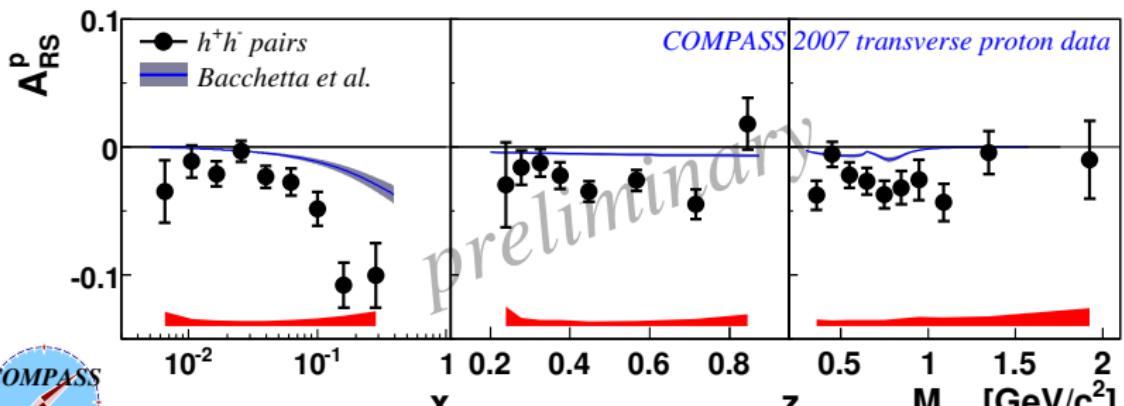
► Large asymmetries for proton  $\sim 10\%$



HERMES values scaled with  $1/D_{nn}$

COMPASS measurement covers much larger range in  $x$

# Dihadron Asymmetry: NH<sub>3</sub> (2007)



### 3. Transverse $\Lambda$ -Polarization: $\ell N^\uparrow \rightarrow \ell' \Lambda^\uparrow X$

**Measuring transversity with polarized  $\Lambda$ -FF  $\Delta_T D_q^\Lambda$ :**

transversely polarized quark transfers its spin to  $\Lambda$ -Baryon

$\Lambda$ -Polarization:  $P_\Lambda \propto f P_T D_{nn} \sum_q e_q^2 \cdot \Delta_T q \cdot \Delta_T D_q^\Lambda$

measured via parity violating decay

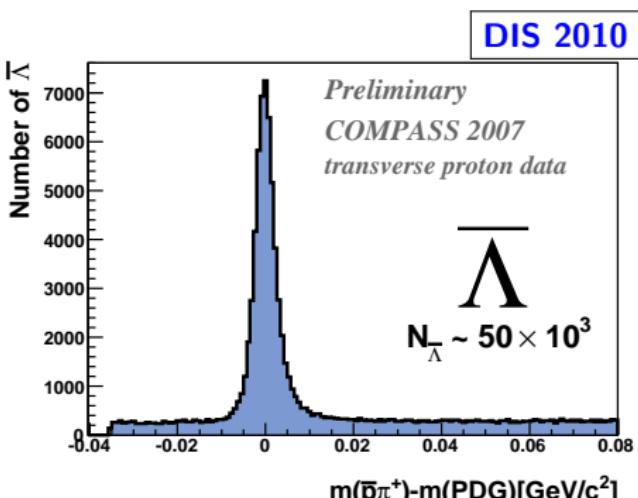
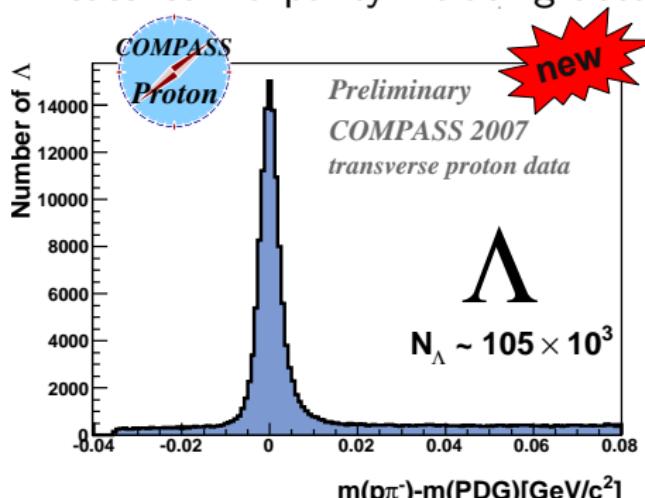
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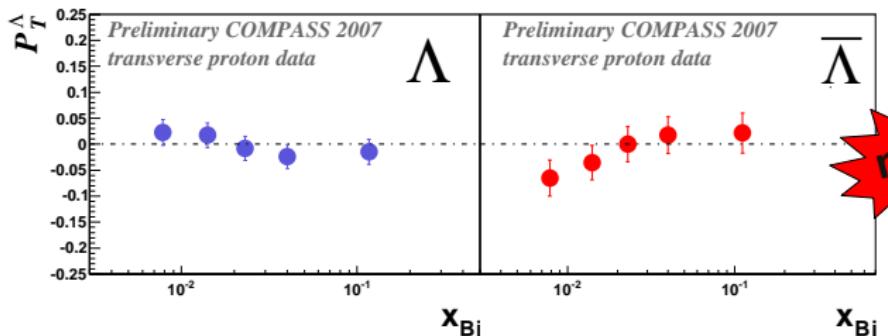
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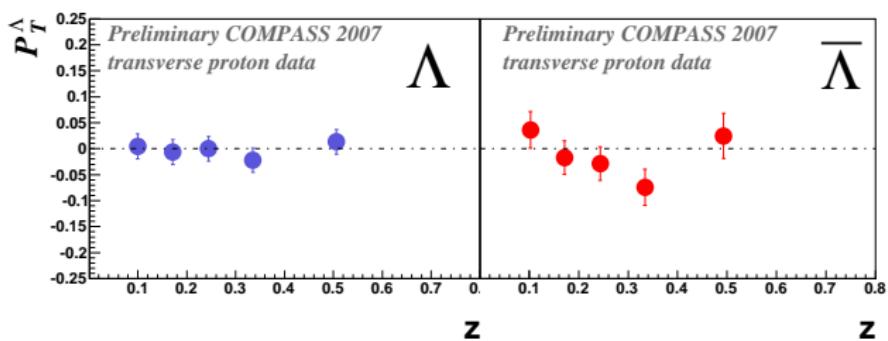
measured via parity violating decay



# Transverse $\Lambda$ -Polarization: $\text{NH}_3$ (2007)



DIS 2010



systematical error:  $\sigma_{\text{sys}} \leq 0.74 \sigma_{\text{stat}}$

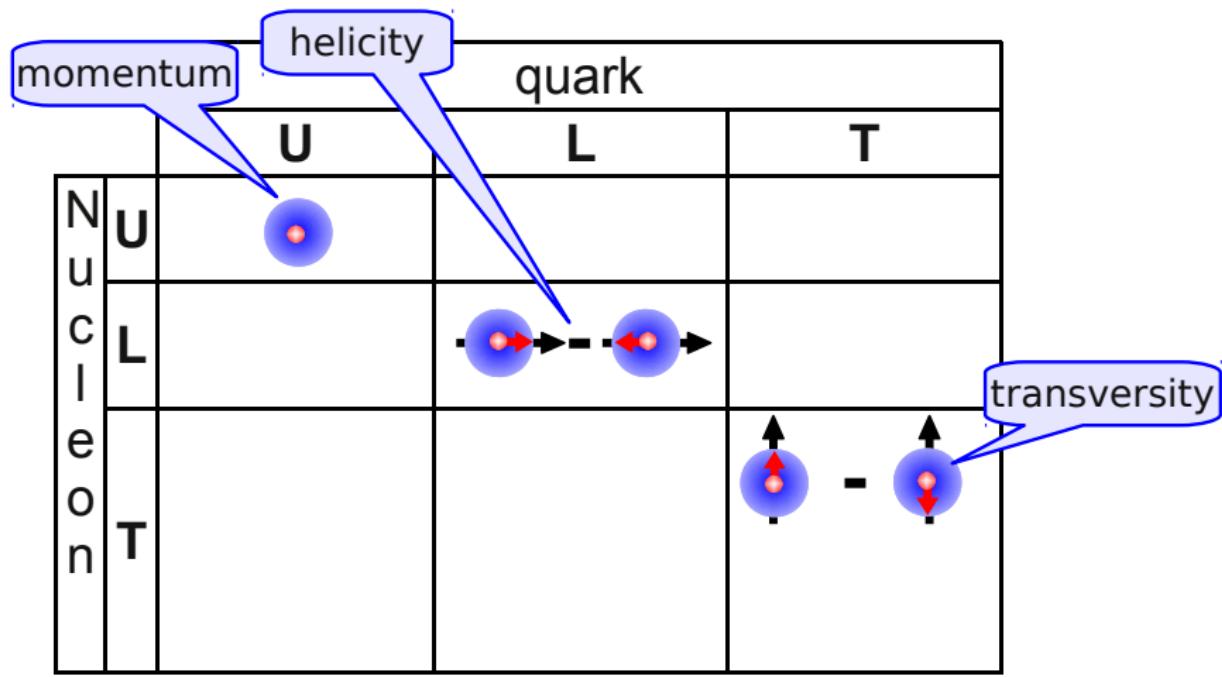
$P_T^\Lambda, P_T^{\bar{\Lambda}}$  small, compatible with zero  $\sim$  small analyzing power of  $\Delta_T D_q^\Lambda$

$P_T^\Lambda, P_T^{\bar{\Lambda}}$  for deuteron also compatible with zero

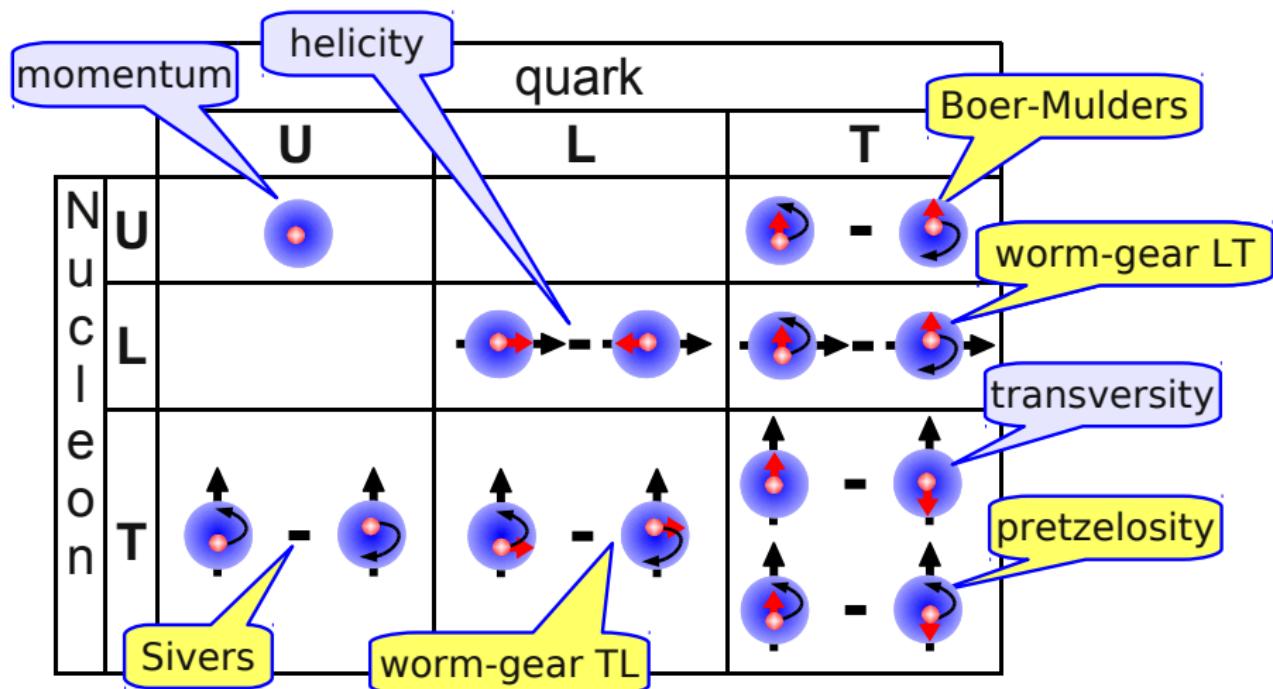


# TMDs

Three parton distribution functions when integrating over  $k_{\perp}$



Eight parton distribution functions when taking into account  $k_{\perp}$



# General Expression of polarized SIDIS Cross-Section

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} \right.$$

$$\left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin \phi_h F_{LU}^{\sin \phi_h} \right\}$$

unpolarized target

$$+ S_{\parallel} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_h F_{UL}^{\sin \phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right]$$

$$+ S_{\parallel} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_h F_{LL}^{\cos \phi_h} \right]$$

$$+ |S_{\perp}| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right.$$

$$+ \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)}$$

$$+ \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \left. \right]$$

$$+ |S_{\perp}| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} \right. \\ \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},$$

longitudinally polarized target

transversely polarized target

A. Bacchetta et al

JHEP 0702:093,2007

E-print number: hep-ph/0611265

# SIDIS Cross-Section: Transversely Polarized Target

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ \dots \right.$$

twist-2

twist-3

$$+ |\mathbf{S}_\perp| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right.$$

$$+ \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)}$$

$$+ \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)}$$

$$+ |\mathbf{S}_\perp| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} \right]$$

$$+ \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \left. \right\},$$

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E-print number: hep-ph/0611265



# SIDIS Cross-Section: Transversely Polarized Target

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ \dots \right.$$

twist-2

twist-3

$$+ |\mathbf{S}_\perp| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right]$$

Collins ✓

$$+ \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)}$$

$$+ \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)}$$

$$+ |\mathbf{S}_\perp| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} \right]$$

$$+ \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right\},$$

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## SIDIS Cross-Section: Transversely Polarized Target

$$\begin{aligned}
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 & \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ \dots \right. \\
 & + |\mathbf{S}_\perp| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \left. + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \right] \\
 & + \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \\
 & + |\mathbf{S}_\perp| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} \right. \\
 & \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \left. \right\},
 \end{aligned}$$

twist-2  
twist-3

**Sivers**      **Collins ✓**

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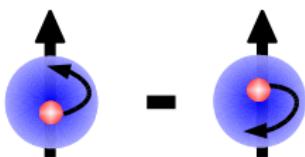
JHEP 0702:093,2007

E-print number: hep-ph/0611265

# Sivers Asymmetry

$$F_{UT,T}^{\sin(\phi_h - \phi_S)} \propto \Delta_0^T q \otimes D_q^h$$

Sivers PDF  $\Delta_0^T q$ :

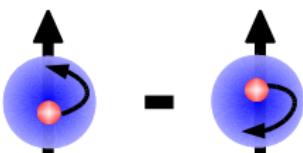


correlation between intrinsic transverse momentum  
of the quarks and the transverse polarization of the nucleon

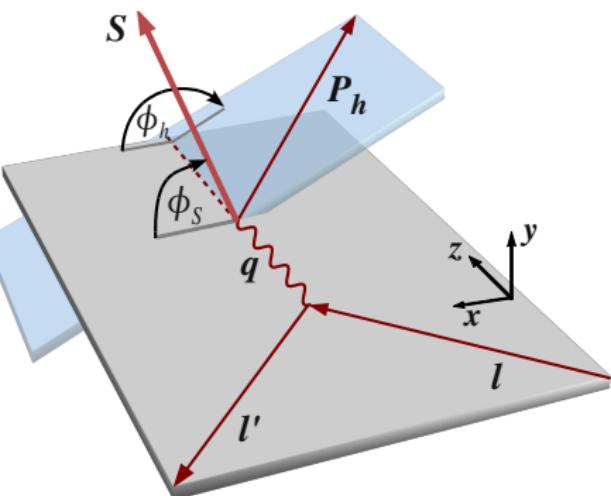
# Sivers Asymmetry

$$F_{UT,T}^{\sin(\phi_h - \phi_s)} \propto \Delta_0^T q \otimes D_q^h$$

Sivers PDF  $\Delta_0^T q$ :



correlation between intrinsic transverse momentum  
of the quarks and the transverse polarization of the nucleon



→ azimuthal asymmetry:

$$N_h \propto 1 \pm A \cdot \sin(\phi_h - \phi_s)$$

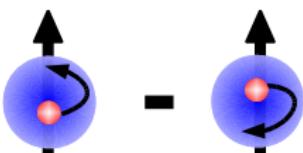
$\phi_h$ : azimuthal angle of hadron

$\phi_s$ : azimuthal angle of spin of initial quark

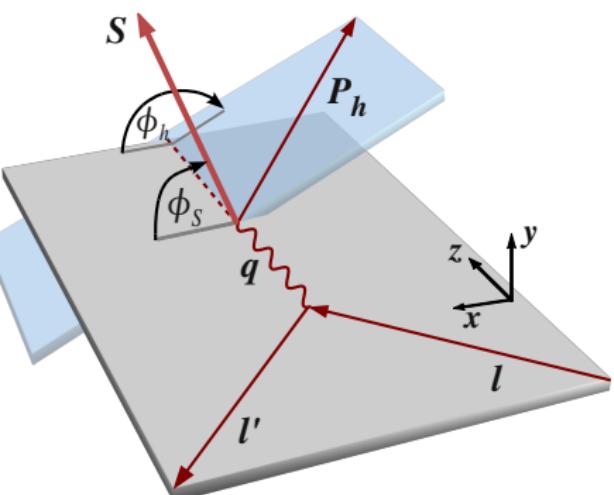
# Sivers Asymmetry

$$F_{UT,T}^{\sin(\phi_h - \phi_S)} \propto \Delta_0^T q \otimes D_q^h$$

Sivers PDF  $\Delta_0^T q$ :



correlation between intrinsic transverse momentum  
of the quarks and the transverse polarization of the nucleon



~ azimuthal asymmetry:

$$N_h \propto 1 \pm A \cdot \sin(\phi_h - \phi_S)$$

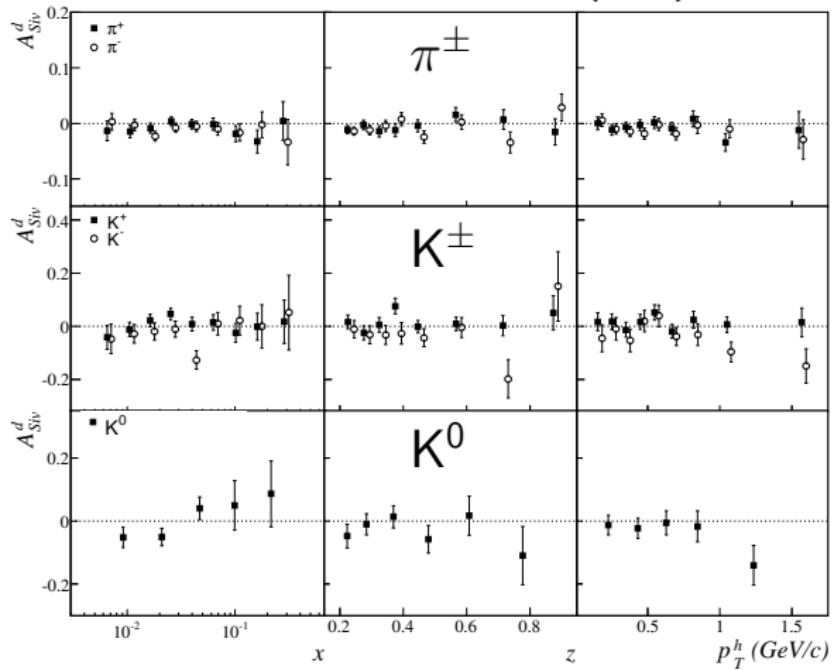
$\phi_h$ : azimuthal angle of hadron

$\phi_S$ : azimuthal angle of spin of initial quark

$$A_{Siv} = \frac{A}{f P_T} \propto \sum_q e_q^2 \cdot \Delta_0^T q \otimes D_q^h$$

# Sivers Asymmetries: ${}^6\text{LiD}$ (2003-2004)

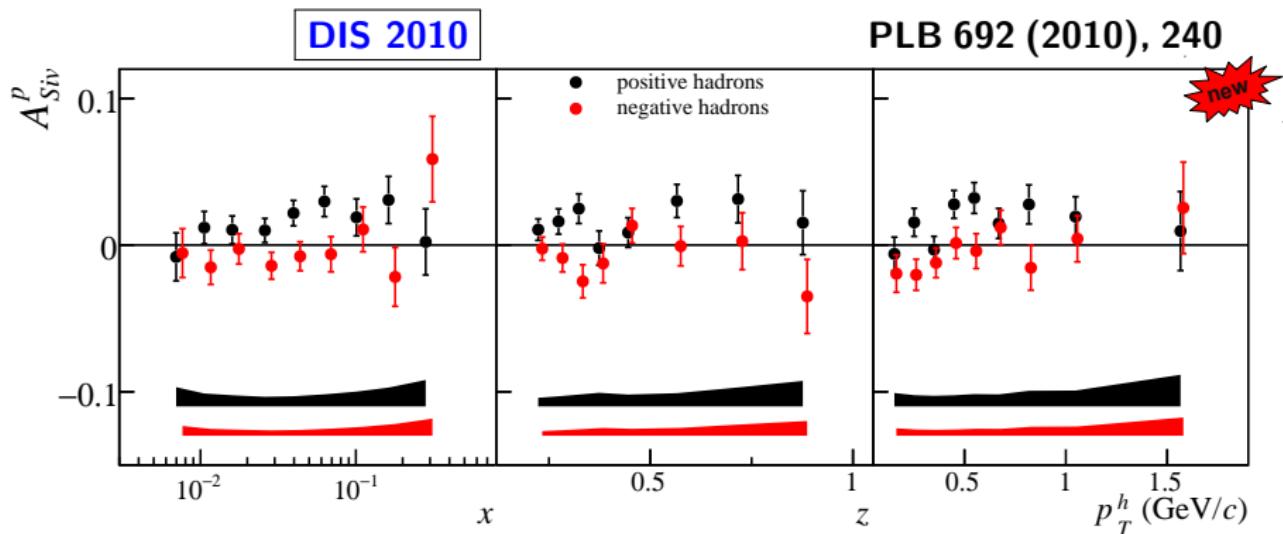
PLB 673 (2009) 127-135



all asymmetries are small,  
compatible with zero

systematical error:  $\sigma_{sys} \leq 0.3 \sigma_{stat}$

# Sivers Asymmetries: NH<sub>3</sub> (2007)

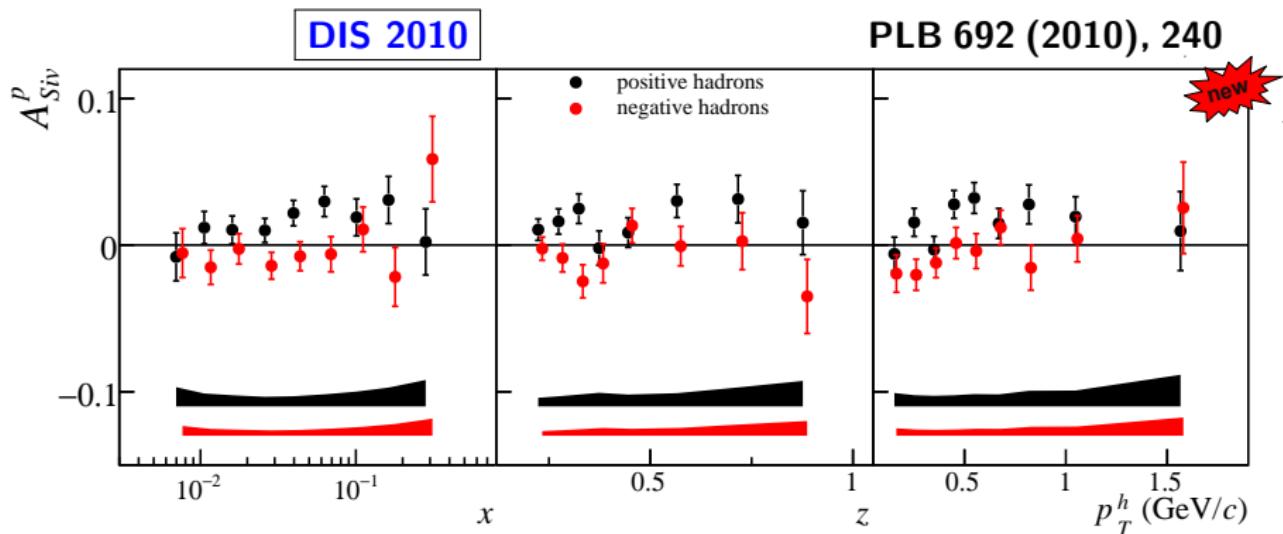


for  $h^+$  additional absolute systematical uncertainty of  $\pm 0.01$



- ▶ positive asymmetry for  $h^+$
- ▶ asymmetry for  $h^-$  small, compatible with zero

# Sivers Asymmetries: NH<sub>3</sub> (2007)

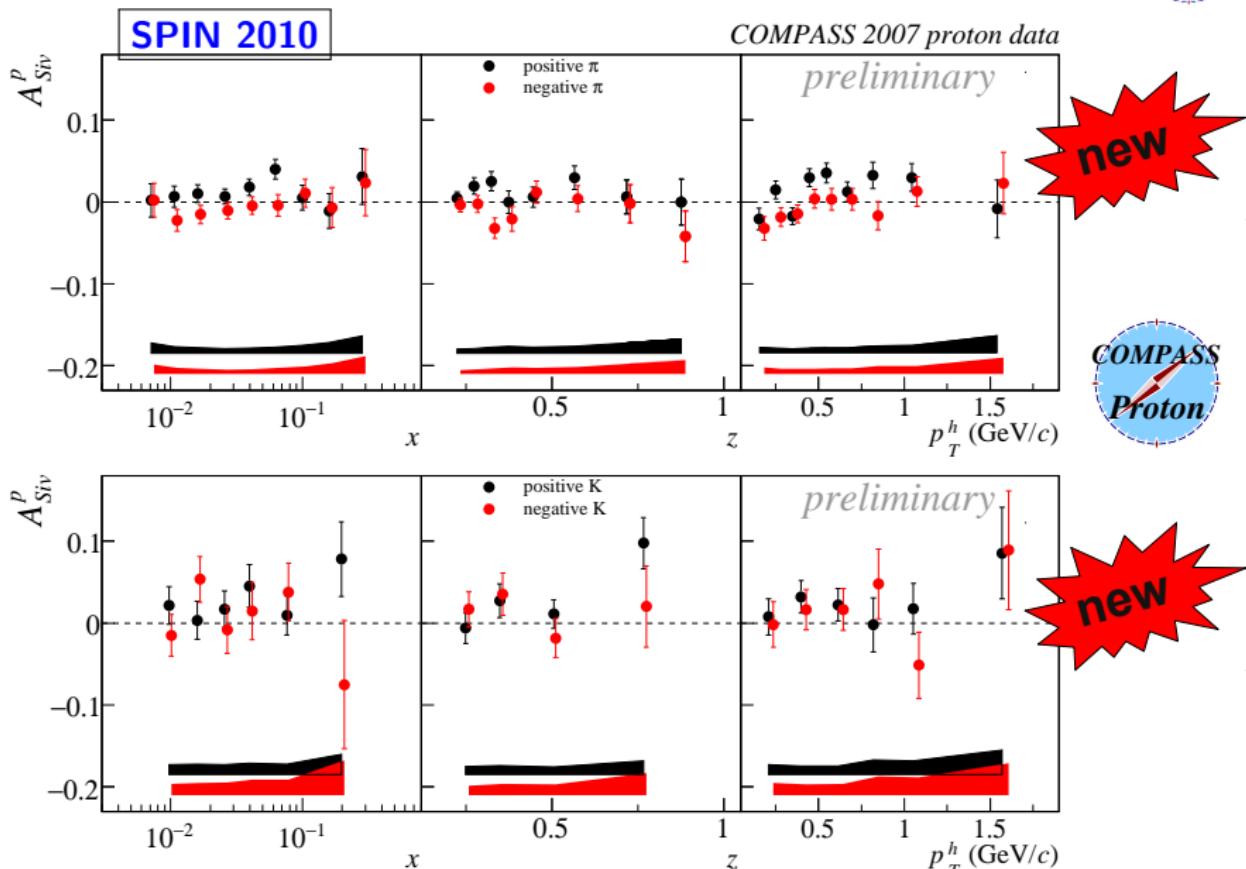


for  $h^+$  additional absolute systematical uncertainty of  $\pm 0.01$

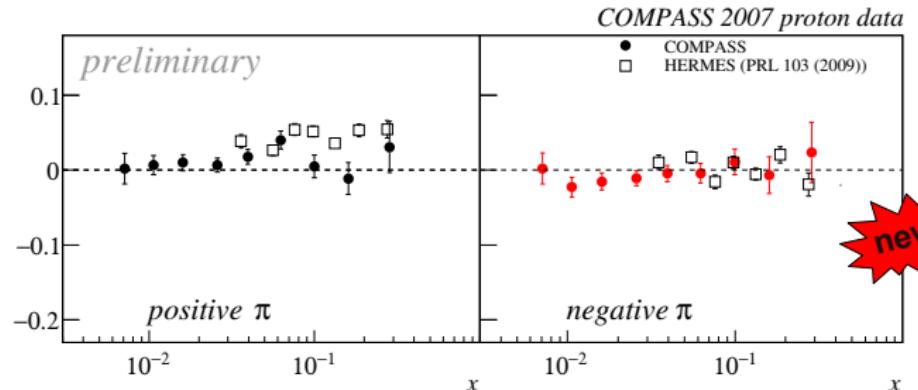


- ▶ positive asymmetry for  $h^+$
- ▶ asymmetry for  $h^-$  small, compatible with zero
- ▶ Small asymmetries for deuteron  
 $\sim$  opposite sign of  $\Delta_0^T u$  and  $\Delta_0^T d$

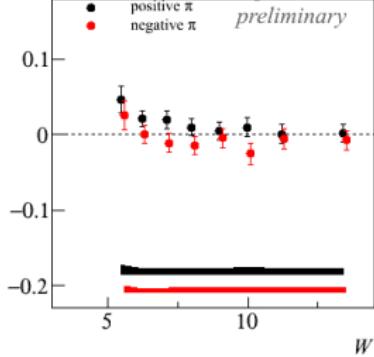
# Sivers Asymmetries for $\pi^\pm$ and $K^\pm$ : NH<sub>3</sub> (2007)



# Sivers Asymmetries: NH<sub>3</sub> (2007)

 $A_{Siv}^p$ **new** $A_{Siv}^p$ 

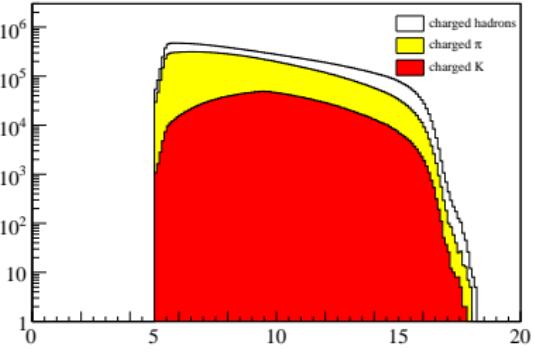
*COMPASS 2007 proton data*  
● positive  $\pi$   
● negative  $\pi$       *preliminary*



possible  $W$  dependence

 $dN/dW$ 

*COMPASS 2007 transverse proton data*



$W(GeV/c^2)$

# SIDIS Cross-Section: transversely polarized target

$$\begin{aligned}
 & \frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \\
 & \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ \dots \right. \\
 & + |\mathbf{S}_\perp| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & \quad \left. + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \right] \\
 & + \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \\
 & + |\mathbf{S}_\perp| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} \right. \\
 & \quad \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \left. \right\},
 \end{aligned}$$

twist-2

twist-3

Sivers ✓

Collins ✓

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JHEP 0702:093,2007

E-print number: hep-ph/0611265

## SIDIS Cross-Section: transversely polarized target

$$\begin{aligned}
 \frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = & \\
 \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \Bigg\{ & \dots \\
 + |\mathbf{S}_\perp| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. & \xrightarrow{\text{Sivers } \checkmark} \\
 + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} & \xrightarrow{\text{Collins } \checkmark} \text{pretzelosity} \\
 + \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} & \\
 + |\mathbf{S}_\perp| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} \right. & \\
 \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \Bigg\}, &
 \end{aligned}$$

twist-2  
twist-3

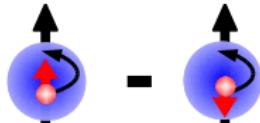
**pretzelosity**  
**worm-gear**

A. Bacchetta et al  
JHEP 0702:093,2007  
E-print number: hep-ph/0611265

# Pretzelosity

$$F_{UT}^{\sin(3\phi_h - \phi_S)} \propto h_{1T}^{\perp,q} \otimes \Delta_T^0 D_q^h,$$

Pretzelosity PDF  $h_{1T}^{\perp,q}$ :

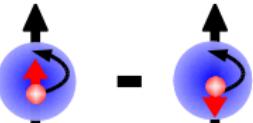


correlation of parton transv. momentum and transv.  
polarization in a transversely polarized nucleon

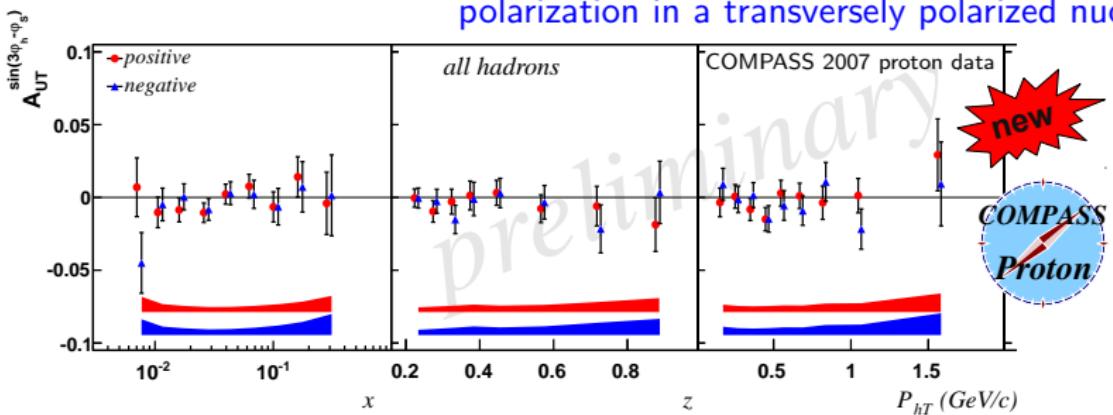
# Pretzelosity: NH<sub>3</sub> (2007)

$$F_{UT}^{\sin(3\phi_h - \phi_S)} \propto h_{1T}^{\perp, q} \otimes \Delta_T^0 D_q^h,$$

Pretzelosity PDF  $h_{1T}^{\perp, q}$ :



correlation of parton transv. momentum and transv.  
polarization in a transversely polarized nucleon

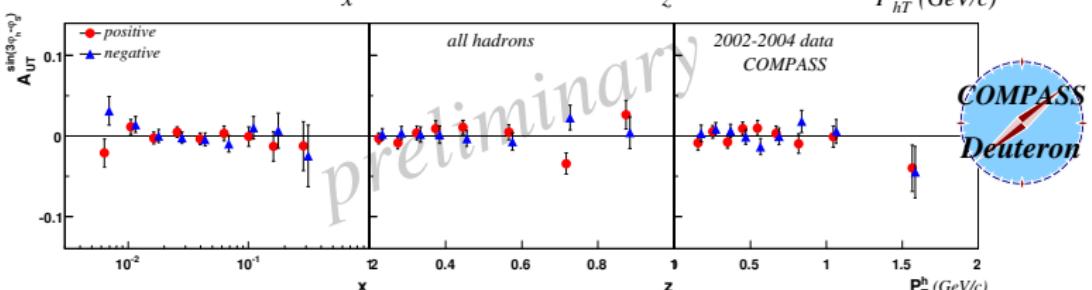
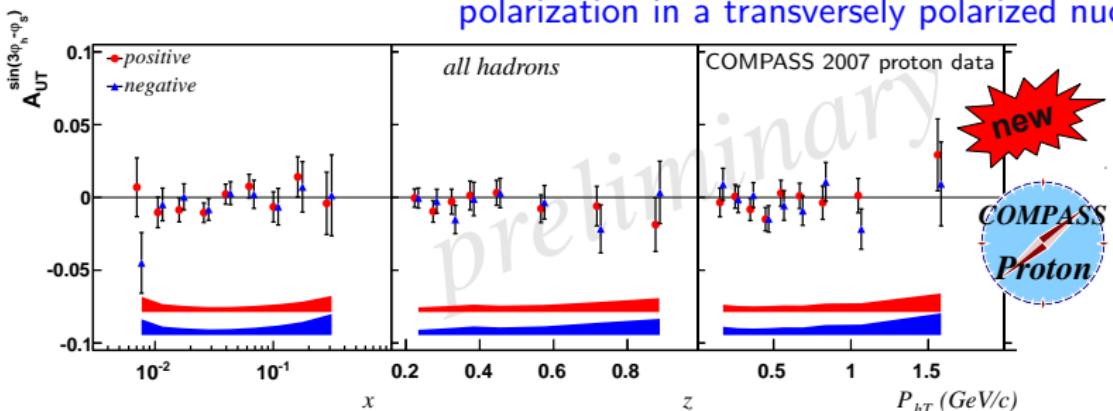


# Pretzelosity: NH<sub>3</sub> (2007) & <sup>6</sup>LiD (2002-2004)

$$F_{UT}^{\sin(3\phi_h - \phi_S)} \propto h_{1T}^{\perp, q} \otimes \Delta_T^0 D_q^h, \quad \text{Pretzelosity PDF } h_{1T}^{\perp, q}:$$



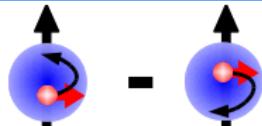
correlation of parton transv. momentum and transv.  
polarization in a transversely polarized nucleon



# Worm-gear (TL)

$$F_{LT}^{\cos(\phi_h - \phi_S)} \propto g_{1T}^q \otimes D_q^h,$$

worm-gear PDF  $g_{1T}^q$ :



correlation of parton transv. momentum and long.  
polarization in a transversely polarized nucleon

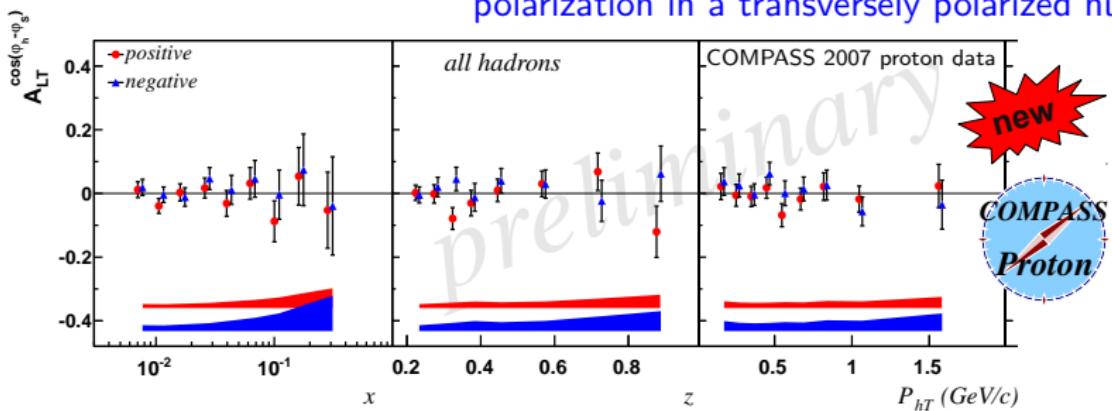
# Worm-gear (TL): NH<sub>3</sub> (2007)

$$F_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_q^h,$$

worm-gear PDF  $g_{1T}^q$ :



correlation of parton transv. momentum and long.  
polarization in a transversely polarized nucleon



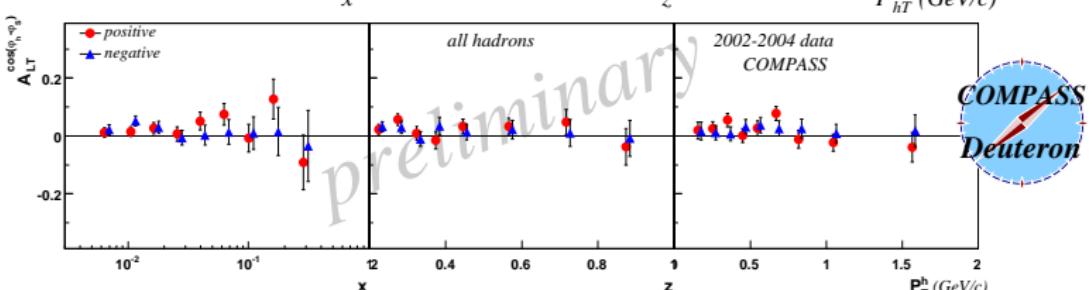
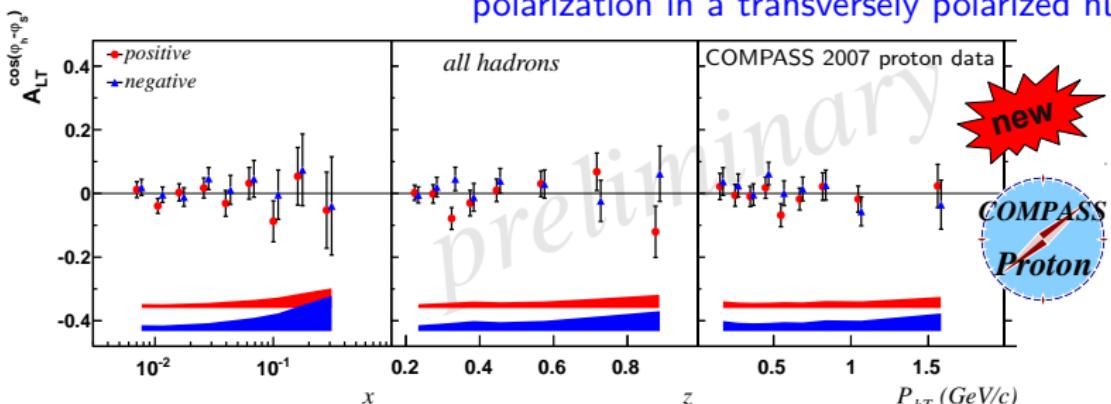
# Worm-gear (TL): NH<sub>3</sub> (2007) & <sup>6</sup>LiD (2002-2004)

$$F_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_q^h,$$

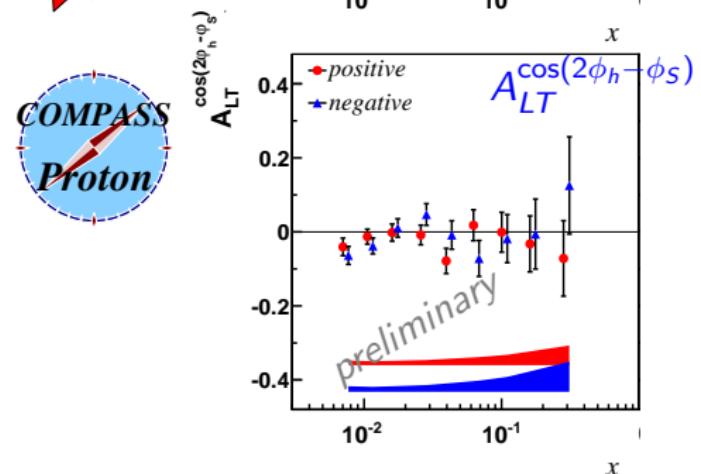
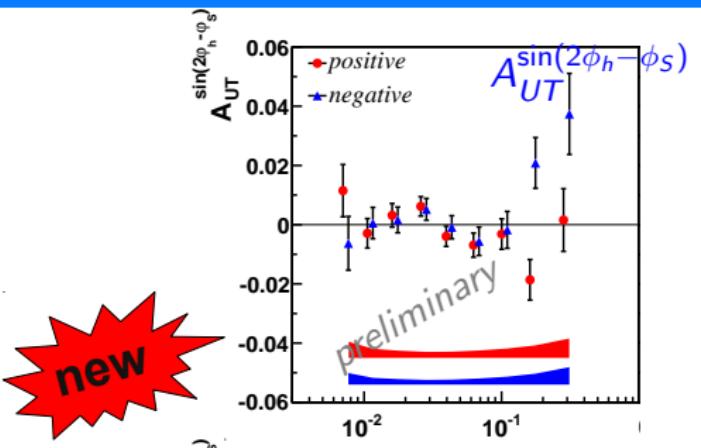
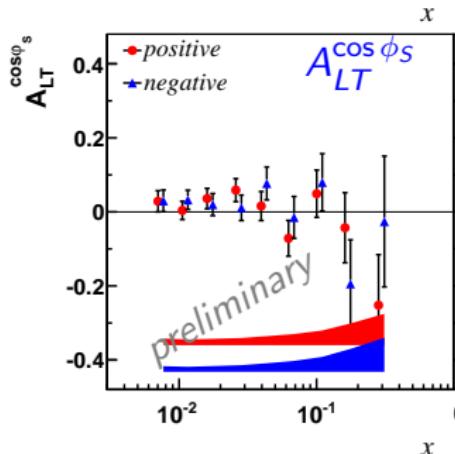
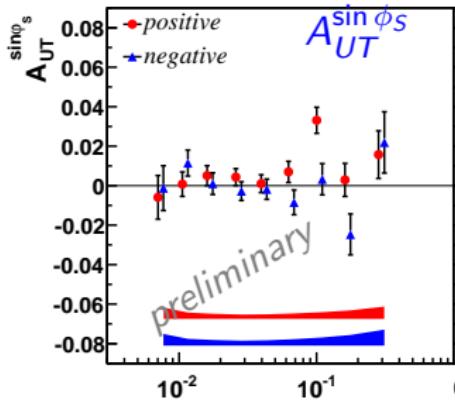
worm-gear PDF  $g_{1T}^q$ :



correlation of parton transv. momentum and long. polarization in a transversely polarized nucleon



# Twist-3 Structure Functions: NH<sub>3</sub> (2007)



# SIDIS Cross-Section: unpolarized target

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} \right.$$

$$\left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin \phi_h F_{LU}^{\sin \phi_h} \right\}$$

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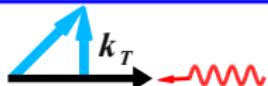
E-print number: hep-ph/0611265

- $F_{UU}^{\cos \phi}$  and  $F_{UU}^{\cos 2\phi}$ : Cahn Effect + Boer-Mulders (~~pQCD~~)
- $F_{LU}^{\sin \phi_h}$ : beam asymmetry (beam polarization:  $P_{\mu^+} \approx -80\%$ )

# SIDIS Cross-Section: unpolarized target

$$\frac{d\sigma}{dx dy dz d\psi_h d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} \right. \\ \left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin \phi_h F_{LU}^{\sin \phi_h} \right\}$$

Cahn Effect



kinematical effect due to transv. mom-  
entum of partons in the nucleon

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- ▶  $F_{UU}^{\cos \phi}$  and  $F_{UU}^{\cos 2\phi}$ : Cahn Effect + Boer-Mulders (~~pQCD~~)
- ▶  $F_{LU}^{\sin \phi_h}$ : beam asymmetry (beam polarization:  $P_{\mu^+} \approx -80\%$ )

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Cahn Effect

kinematical effect due to transv. mom-  
entum of partons in the nucleonBoer-Mulders  $h_1^\perp$ :correlation of parton transv. momentum  
and transv. polarization in an unpolarized  
nucleon

- $F_{UU}^{\cos\phi}$  and  $F_{UU}^{\cos 2\phi}$ : Cahn Effect + Boer-Mulders (~~pQCD~~)
- $F_{LU}^{\sin\phi_h}$ : beam asymmetry (beam polarization:  $P_{\mu^+} \approx -80\%$ )

# SIDIS Cross-Section: unpolarized target

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} \right. \\ \left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin \phi_h F_{LU}^{\sin \phi_h} \right\}$$

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Cahn Effect

kinematical effect due to transv. momentum of partons in the nucleon

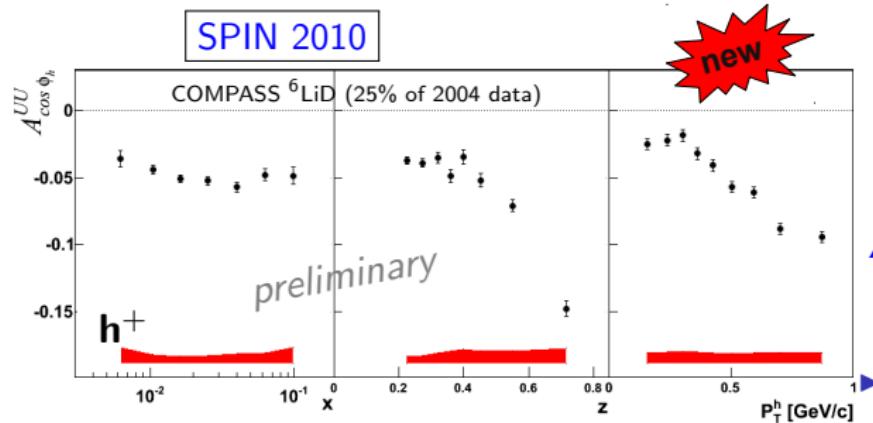


Boer-Mulders  $h_1^\perp$ :

correlation of parton transv. momentum and transv. polarization in an unpolarized nucleon

- ▶  $F_{UU}^{\cos \phi}$  and  $F_{UU}^{\cos 2\phi}$ : Cahn Effect + Boer-Mulders (~~+ pQCD~~)
- ▶  $F_{LU}^{\sin \phi_h}$ : beam asymmetry (beam polarization:  $P_{\mu^+} \approx -80\%$ )
- ▶ Target polarization canceled by event weighting
- ▶ Detector acceptance corrected by MC simulation

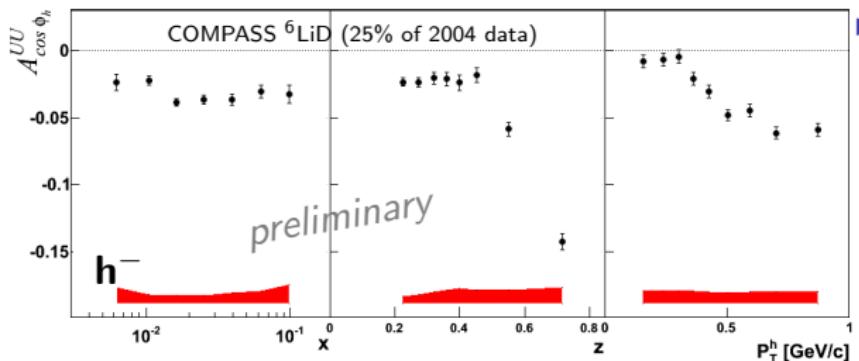
# Unpolarized Asymmetries: ${}^6\text{LiD}$ (2004 part)



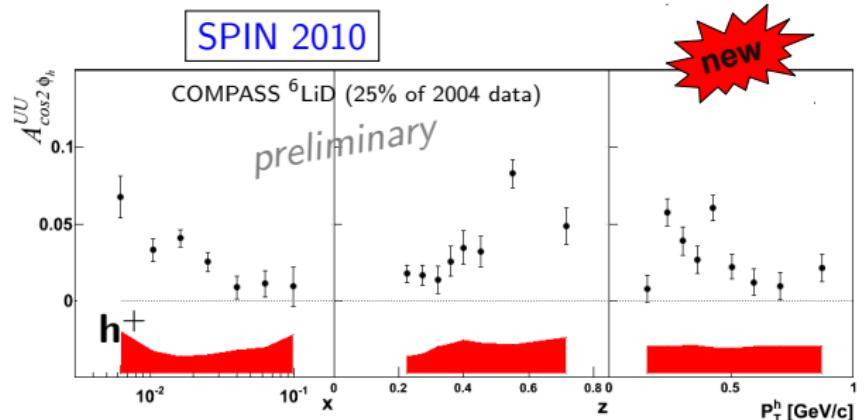
$A_{\cos \phi}^{UU}$ : Mainly Cahn effect

► Large negative asymmetries

► Charge dependent

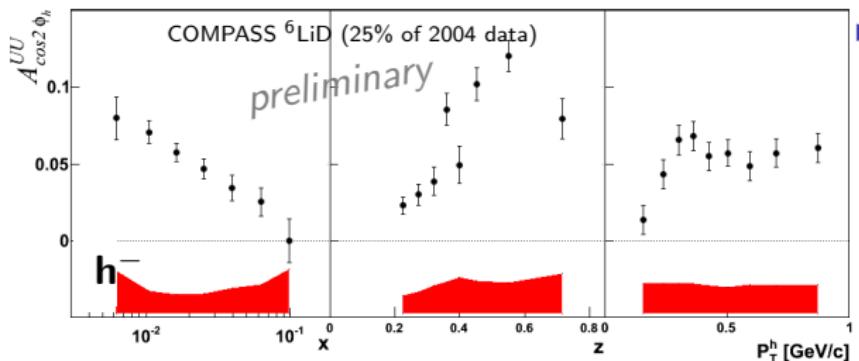


# Unpolarized Asymmetries: ${}^6\text{LiD}$ (2004 part)

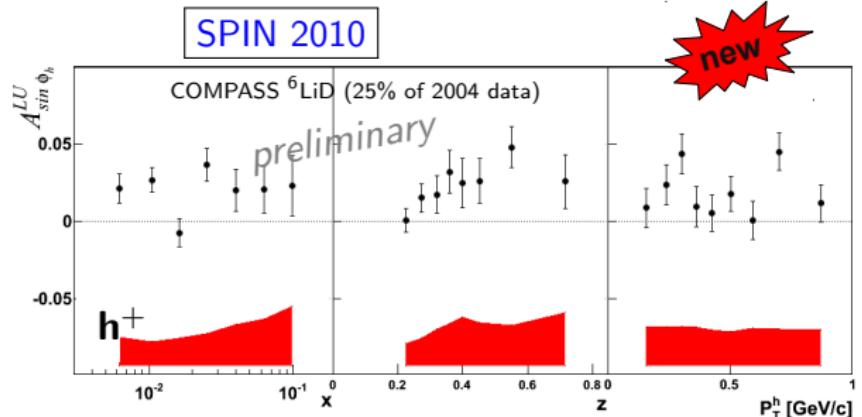


$A_{\cos 2 \phi}^{UU}$ : Boer-Mulders TMD  
+ Cahn  $\propto \left(\frac{k_\perp}{Q}\right)^2$

- ▶ Large positive asymmetries
- ▶ Charge dependent

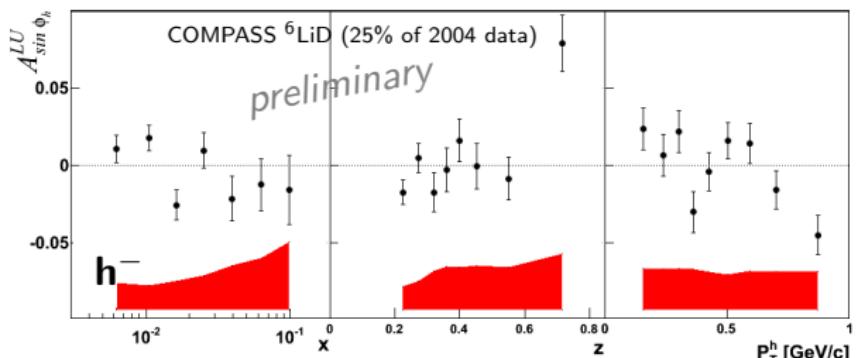


# Unpolarized Asymmetries: ${}^6\text{LiD}$ (2004 part)



$A_{\sin \phi}^{LU}$ : twist-3 effect due to beam polarization

- ▶  $h^+$  positive asymmetry
- ▶  $h^-$  small asymmetry, compatible with zero



# Summary

## Many new results from COMPASS:

- ▶ **Collins asymmetries** for  $\pi^\pm$  and  $K^\pm$  for deuteron and proton target
  - ~ New proton results ready to be used in a global analysis
- ▶ **Dihadron asymmetries** for deuteron and proton target
  - ~ Ultimate cross-check for Transversity extraction
- ▶ **Sivers asymmetries** for  $\pi^\pm$  and  $K^\pm$  for deuteron and proton target
  - ~ New proton results ready to be used in a global analysis
- ▶ Large **azimuthal asymmetries** of charged hadrons produced scattering off unpolarized deuterons

# Summary

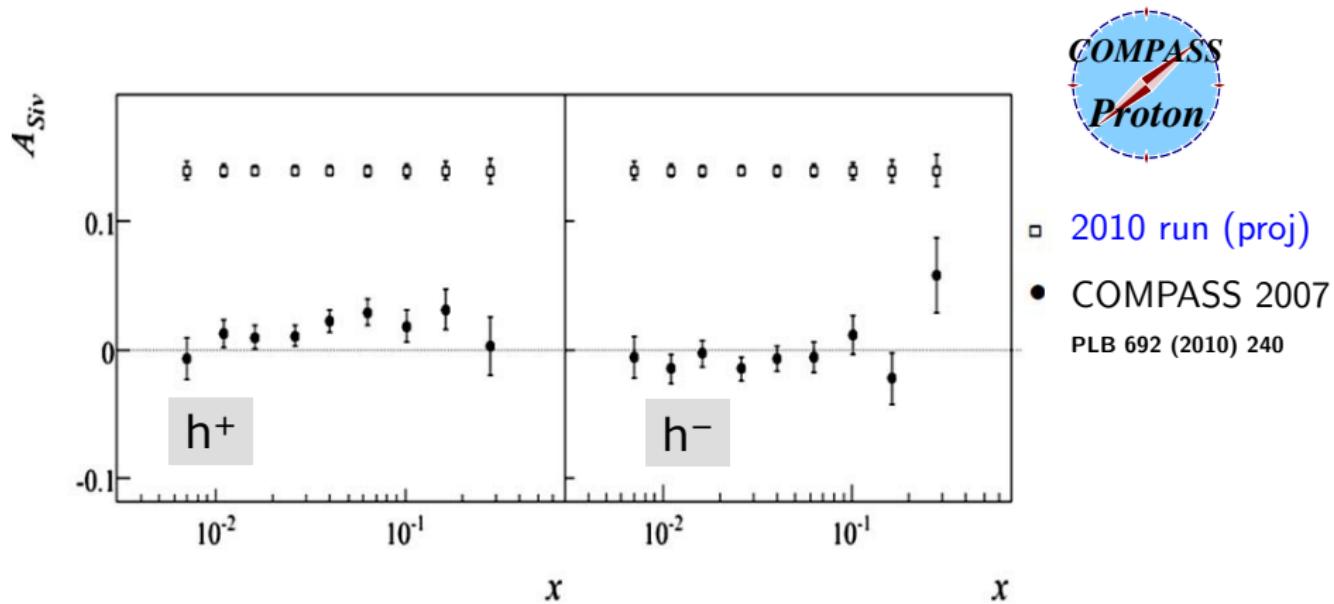
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COMPASS is a major player in nucleon spin physics

# Outlook: 2010 NH<sub>3</sub>

One full year with transverse data taking has nearly finished



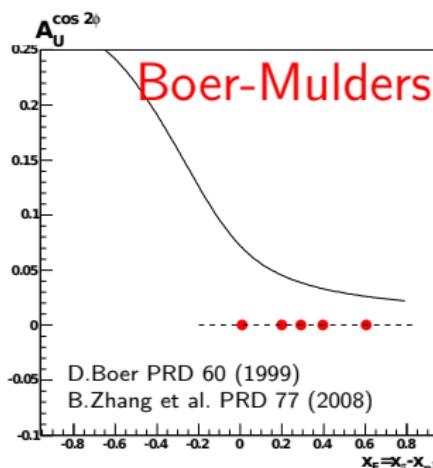
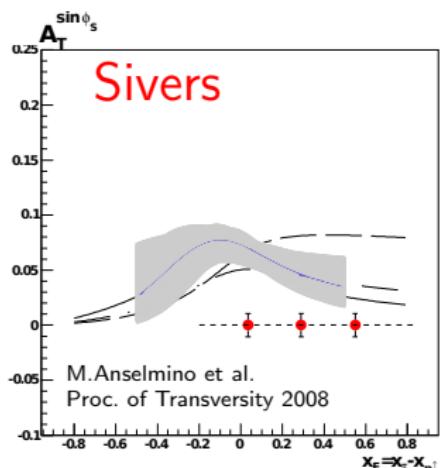
# Outlook: 2013 and beyond

COMPASS-II proposal approved by SPSC

...proposal for two years GPD and **two years DY...**

$$\pi P^\uparrow \rightarrow \mu \bar{\mu} X$$

Predictions and expected statistical errors ( $2 \text{ GeV}/c^2 < M_{\mu\mu} < 2.5 \text{ GeV}/c^2$ )





End

# Thank You

email: [heiner.wollny@cern.ch](mailto:heiner.wollny@cern.ch)



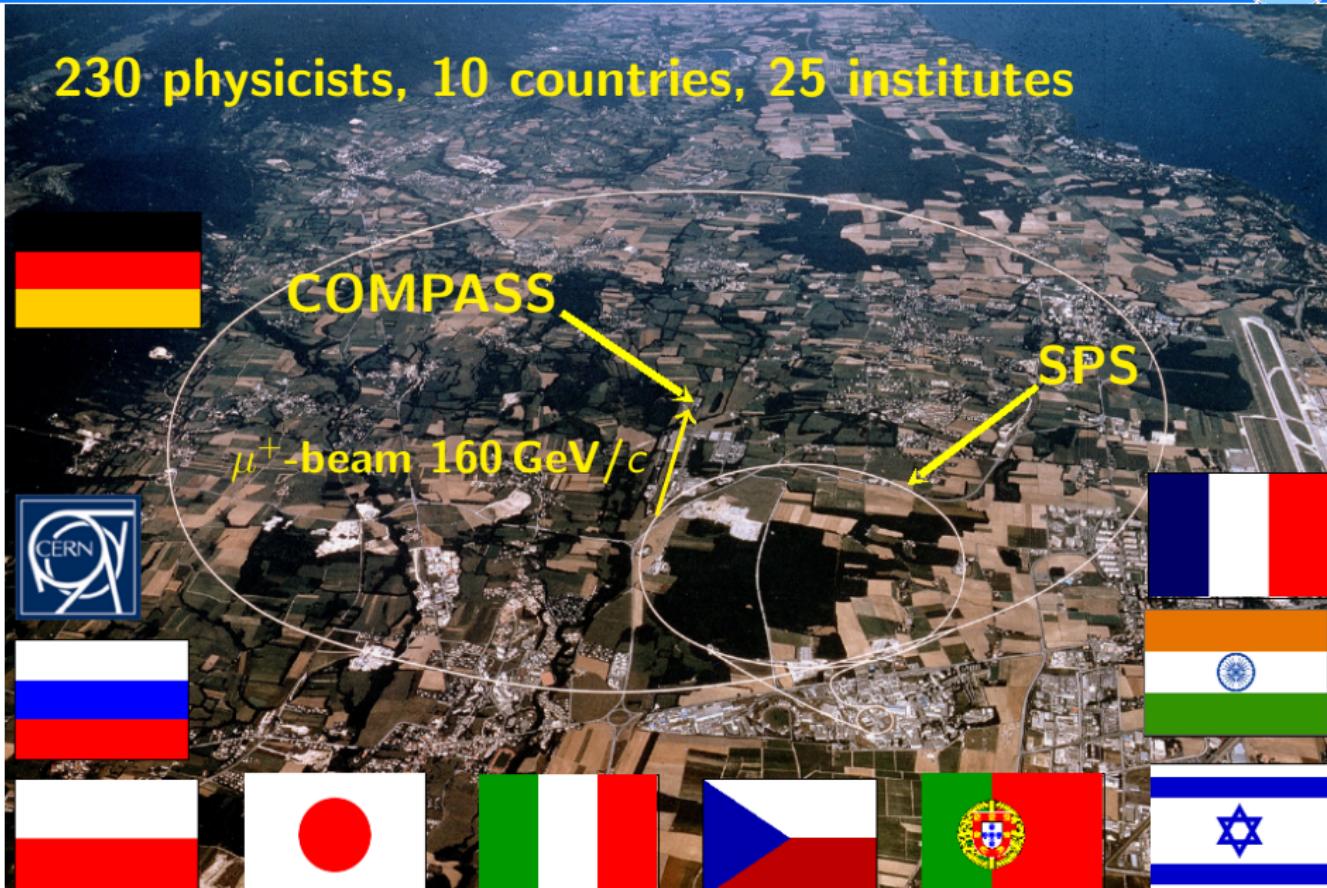
# Back up

# Back Up



# COMPASS Experiment

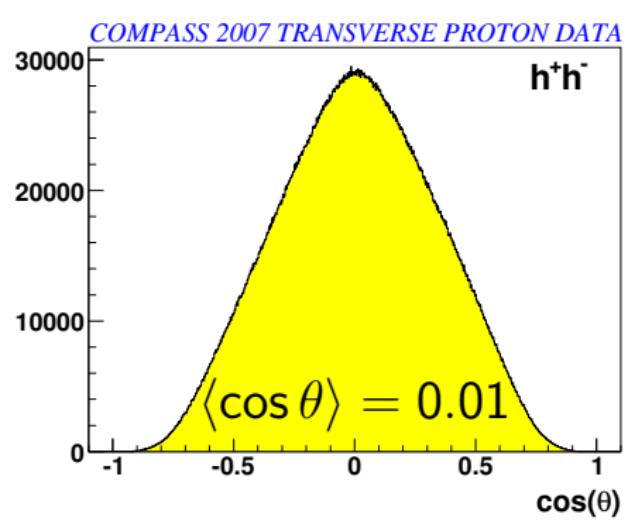
230 physicists, 10 countries, 25 institutes



# Dihadron Interference

## Measuring transversity with polarized Dihadron-Interference-FF $H_1^{\triangleleft}$ :

~ azimuthal asymmetry:



$$N_{h^+h^-} \propto 1 \pm A \cdot \sin \phi_{RS} \cdot \sin \theta$$

$$\phi_{RS} = \phi_R + \phi_S - \pi$$

$$A_{RS} = \frac{A}{f P_T D_{nn}} \propto \sum_q e_q^2 \cdot \Delta_T q \cdot H_1^{\triangleleft}$$

$$H_1^{\triangleleft} = H_1^{\triangleleft, sp} + \cos \theta H_1^{\triangleleft, pp}$$

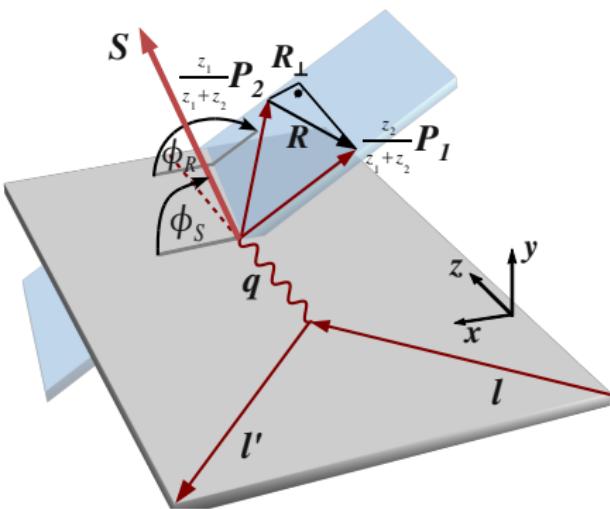
~ only sensitive to  $H_1^{\triangleleft, sp}$

# Definition of $R_T$ and $\phi_R$

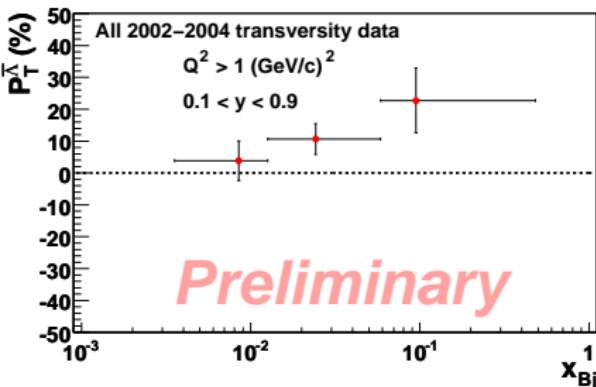
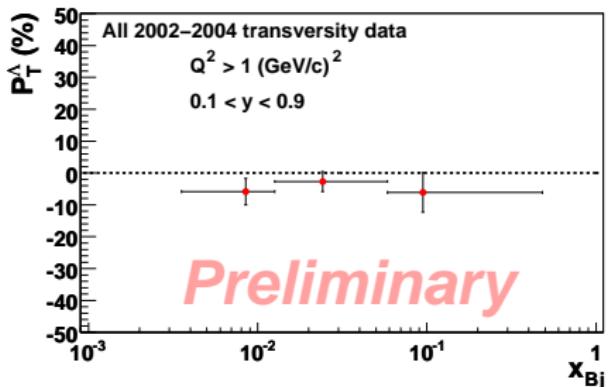
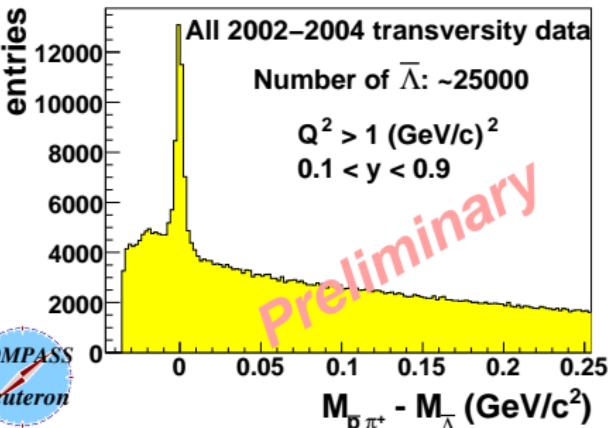
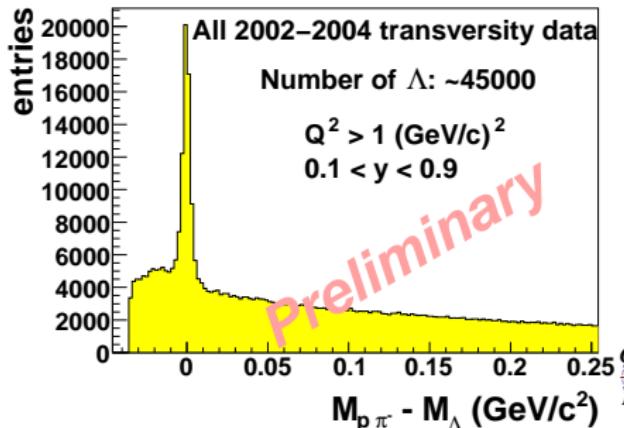
$$R_T = \frac{z_2 \mathbf{P}_{1T} - z_1 \mathbf{P}_{2T}}{z_1 + z_2}$$

$$\cos \phi_R = \frac{\vec{q} \times \vec{\ell}}{|\vec{q} \times \vec{\ell}|} \cdot \frac{\vec{q} \times \vec{R}_T}{|\vec{q} \times \vec{R}_T|},$$

$$\sin \phi_R = \frac{(\vec{\ell} \times \vec{R}_T) \cdot \hat{q}}{|\hat{q} \times \vec{\ell}| |\hat{q} \times \vec{R}_T|}$$

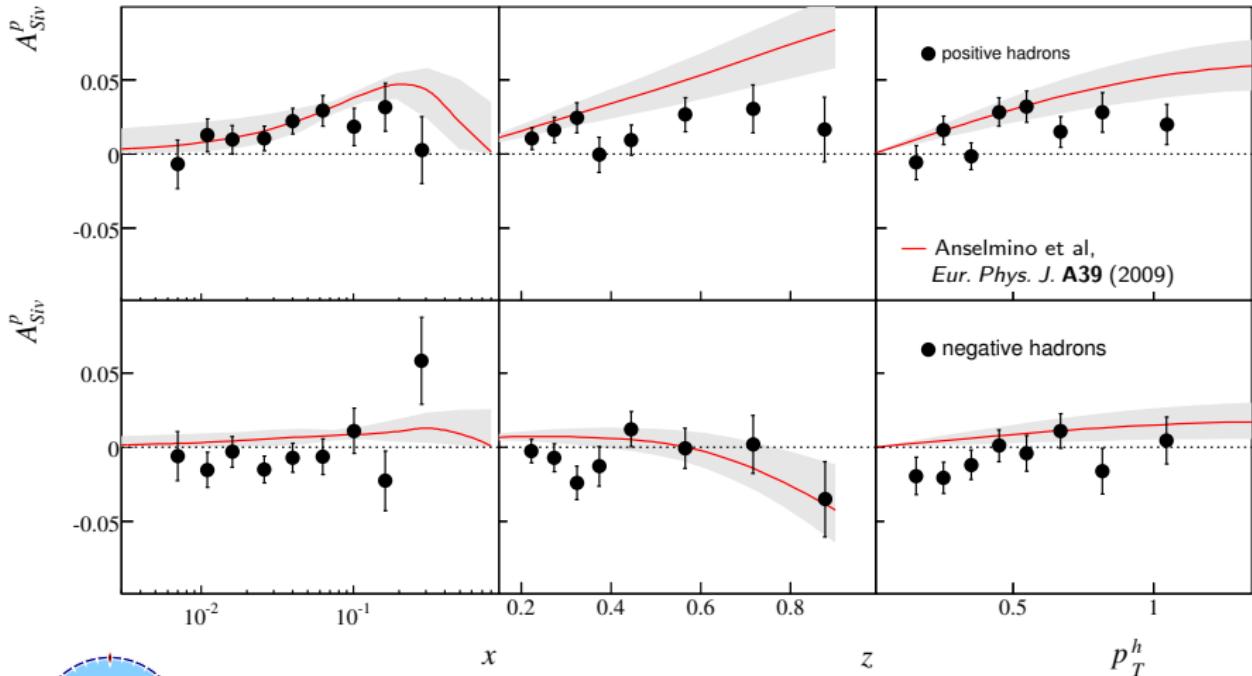


# Transverse $\Lambda$ -Polarization: ${}^6\text{LiD}$ (2002-2004)



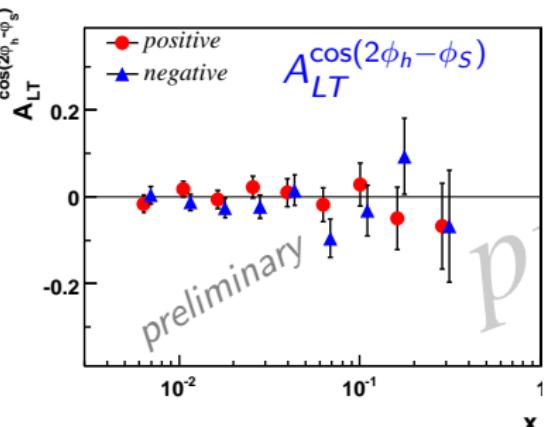
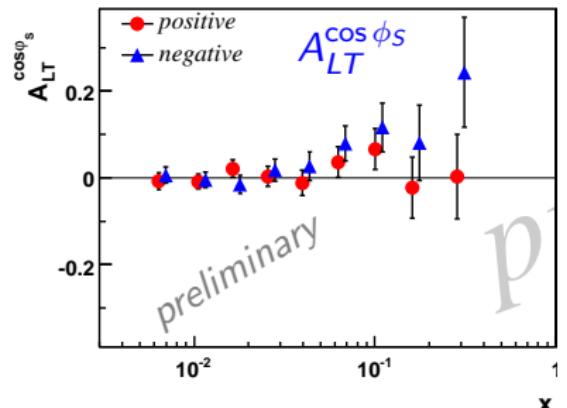
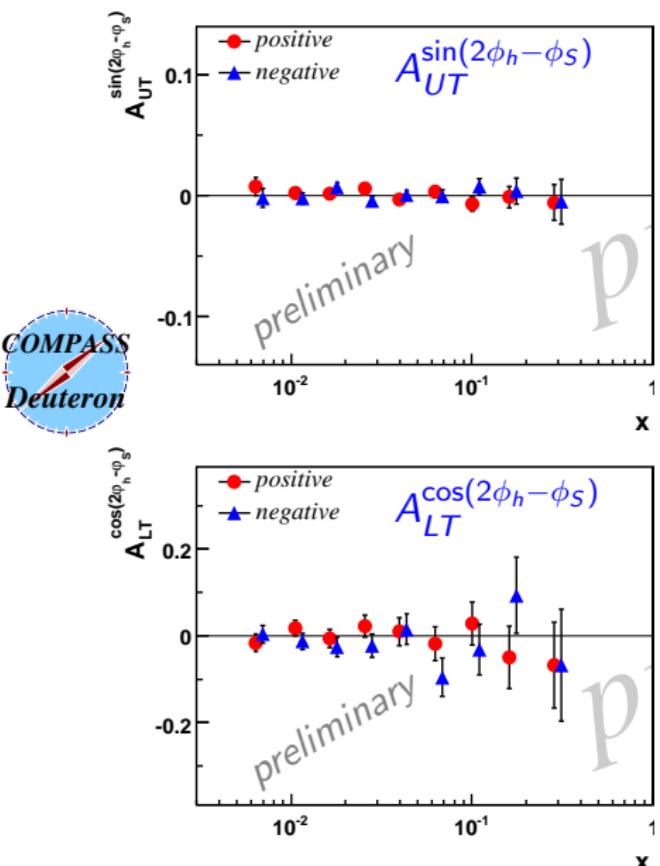
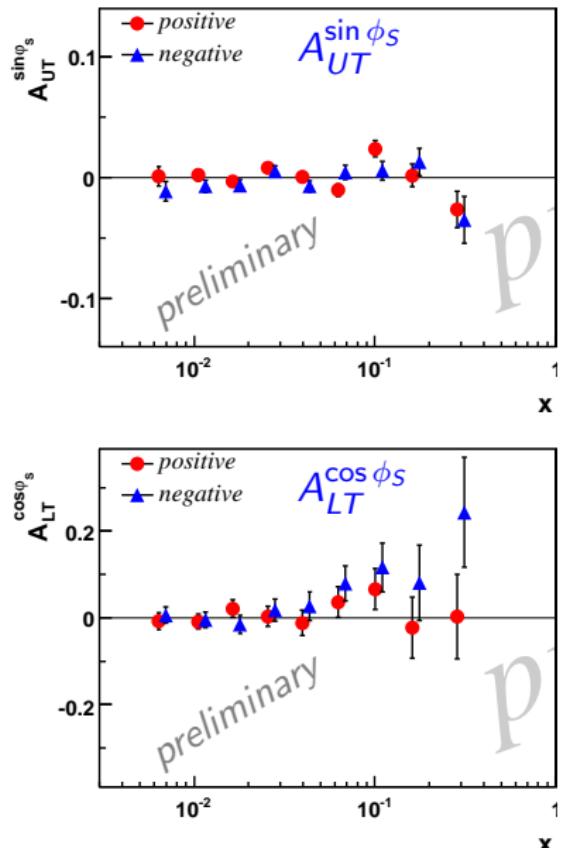
systematical errors are smaller than the statistical ones

# Sivers Asymmetries: NH<sub>3</sub> (2007)



Predictions from fit to COMPASS deuteron  
and HERMES proton SIDIS data

# Twist-3 Structure Functions: ${}^6\text{LiD}$ (2002-2004)



# SIDIS Cross-Section: Longitudinally Polarized Target

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xy Q^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ \dots \right.$$

$$+ S_{\parallel} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_h F_{UL}^{\sin \phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right]$$

$$+ S_{\parallel} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos \phi_h F_{LL}^{\cos \phi_h} \right]$$

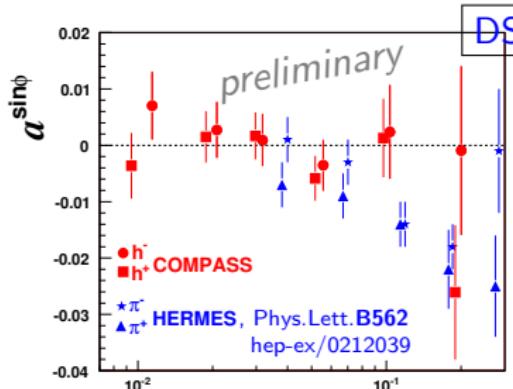
A.Bacchetta et al

JHEP 0702:093,2007

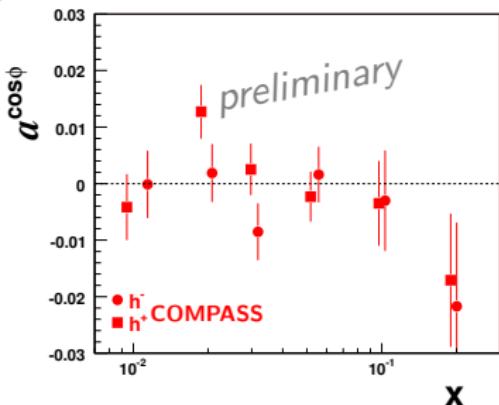
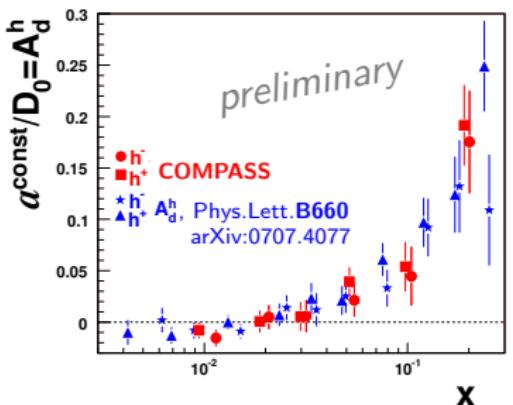
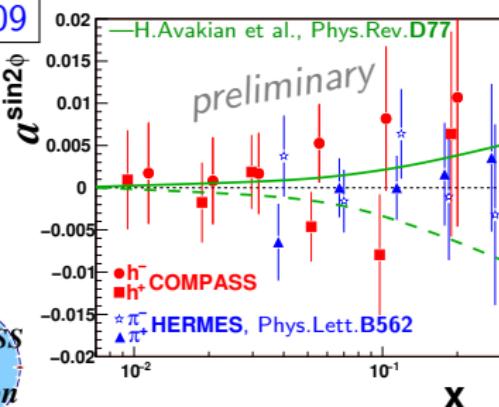
E-print number: hep-ph/0611265

- ▶  $F_{LL} \propto \Delta q \otimes D_q^h$
- ▶  $F_{UL}^{\sin \phi_h}$ ,  $F_{UL}^{\sin 2\phi_h}$ ,  $F_{LL}^{\cos \phi_h}$ : twist-3, complex parton picture

# Longitudinally Polarized Target: ${}^6\text{LiD}$ (2002-2004)



DSPIN 2009



Publication is on the way



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