

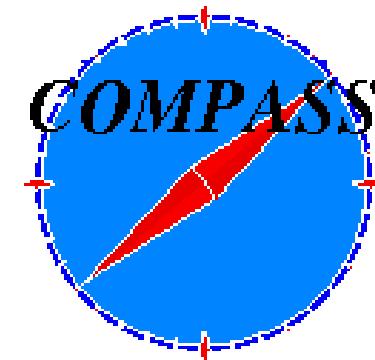
# $\Delta G/G$ results from the COMPASS experiment for $Q^2 > 1(\text{GeV}/c)^2$ using high $p_T$ hadrons

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On behalf of the COMPASS Collaboration

1 Oct 2010



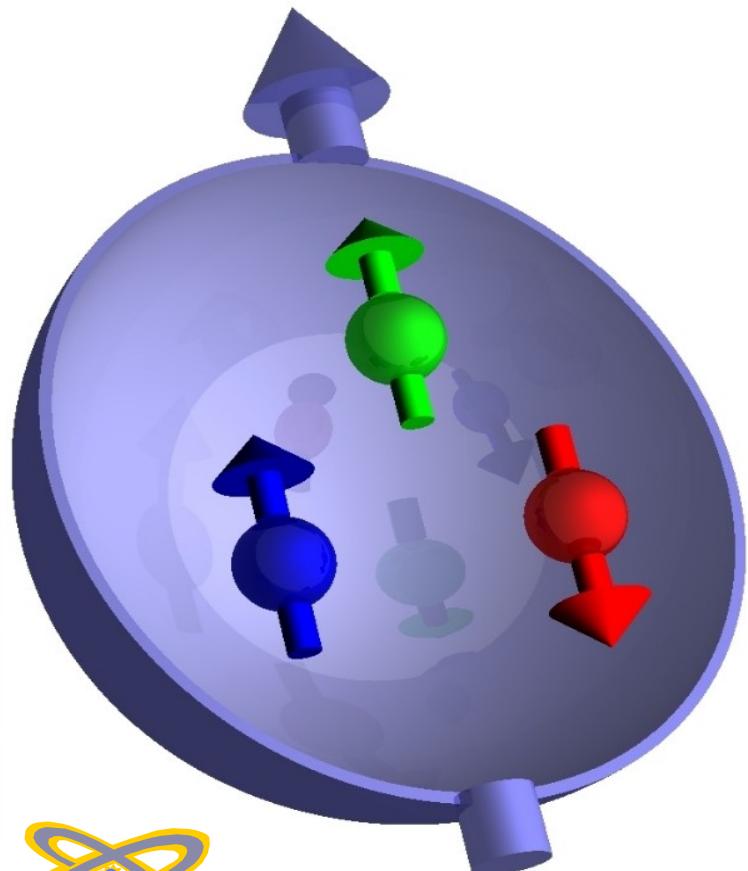
# Outline



- Motivation
- COMPASS experiment
- Direct measurement of  $\Delta G/G$
- High  $p_T$  analysis,  $Q^2 > 1 \text{ (GeV/c)}^2$
- $\Delta G/G$  results
- Summary and Conclusions

# The Nucleon Spin

$$S_N = \frac{1}{2} = \frac{1}{2} \Delta \Sigma$$



Spin crisis !

The naïve Quark-Parton Model (QPM) considers only the contribution from quarks

$$\Rightarrow \Delta \Sigma = 1$$

Using the Ellis-Jaffe Sum rule, Hyperon decays and Relativistic Corrections

$$\Rightarrow \Delta \Sigma \approx 0.6$$

In 1988 EMC measured

$$\Rightarrow \Delta \Sigma = 0.12 \pm 0.17 \text{ (Phys.Lett.B206,364)}$$

Today world data result, including COMPASS, gives:

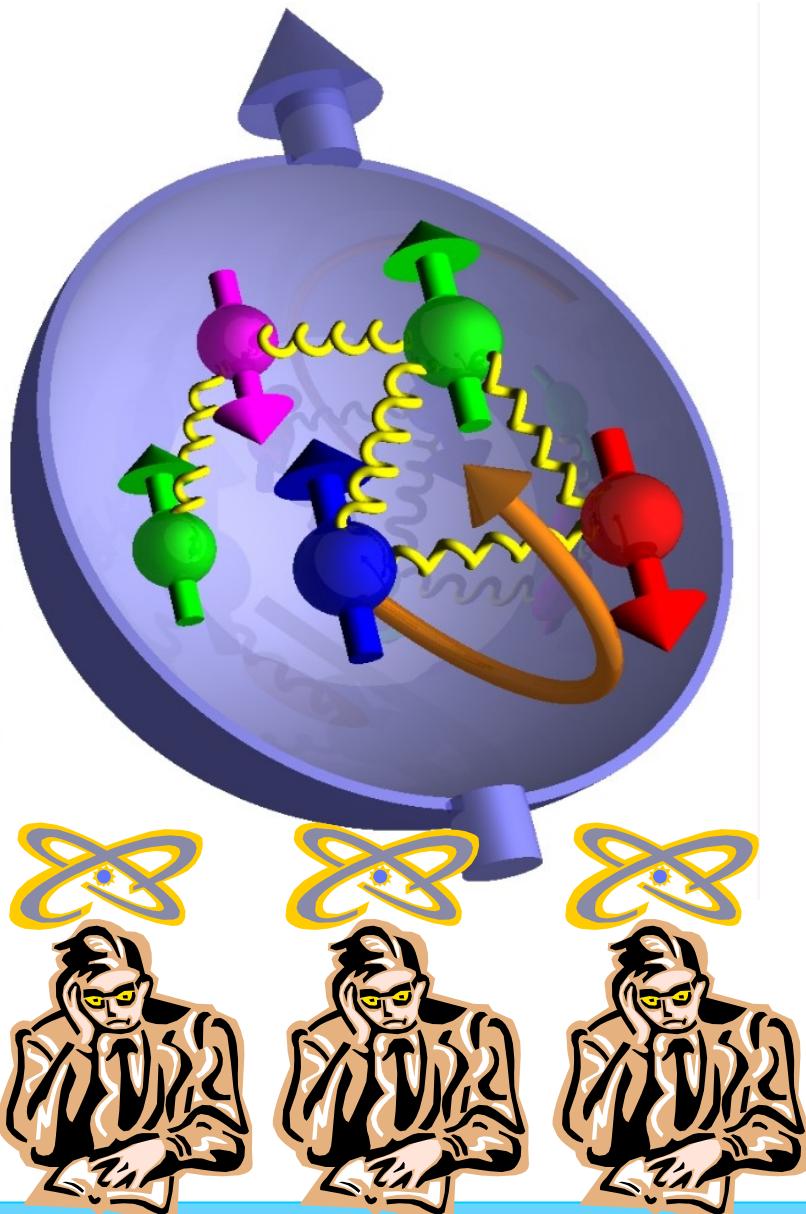
$$\Rightarrow \Delta \Sigma = 0.30 \pm 0.01 \text{ (stat.)} \pm 0.02 \text{ (evol.)}$$

$$@ \langle \mu^2 \rangle = 3 \text{ (GeV/c)}^2$$

(using QCD NLO fits) Phys.Lett.B647, (2007)8

# The Nucleon Spin

$$S_N = \frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L$$



The missing part could be accounted by the following contributions:

$\Delta G$  – from gluons

$L = L_g + L_q$  – from orbital angular momenta of quarks and gluons

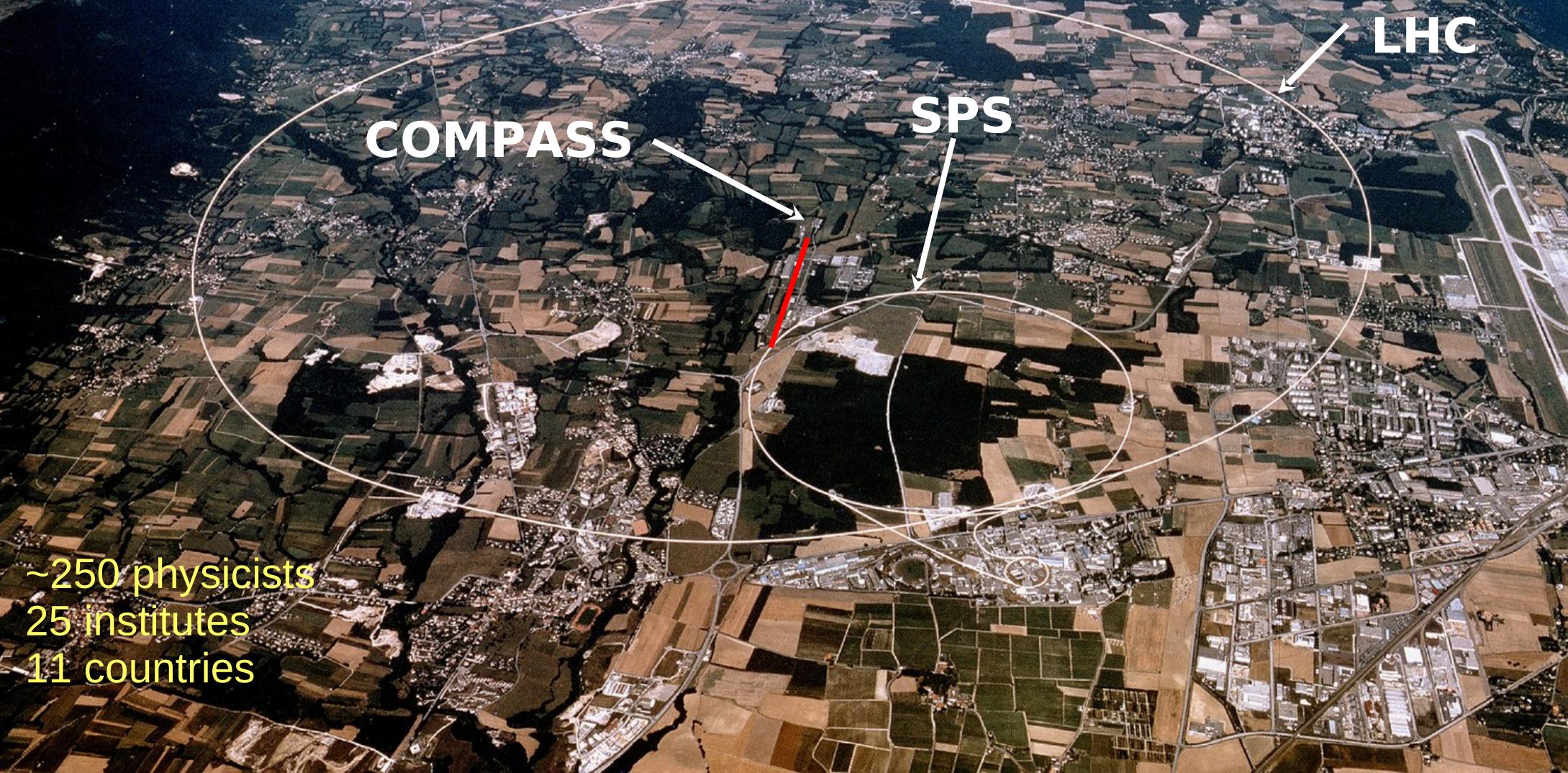
How much is the contribution from gluons and from  $L$ ?

Spin Puzzle

# THE COMPASS EXPERIMENT

Beam:  $2 \cdot 10^8 \mu^+$ /spill  
Luminosity:  $\sim 5 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$   
Beam polarisation: 80%  
Beam momentum: 160 GeV/c

Data taken: 2002 - 2010, ...

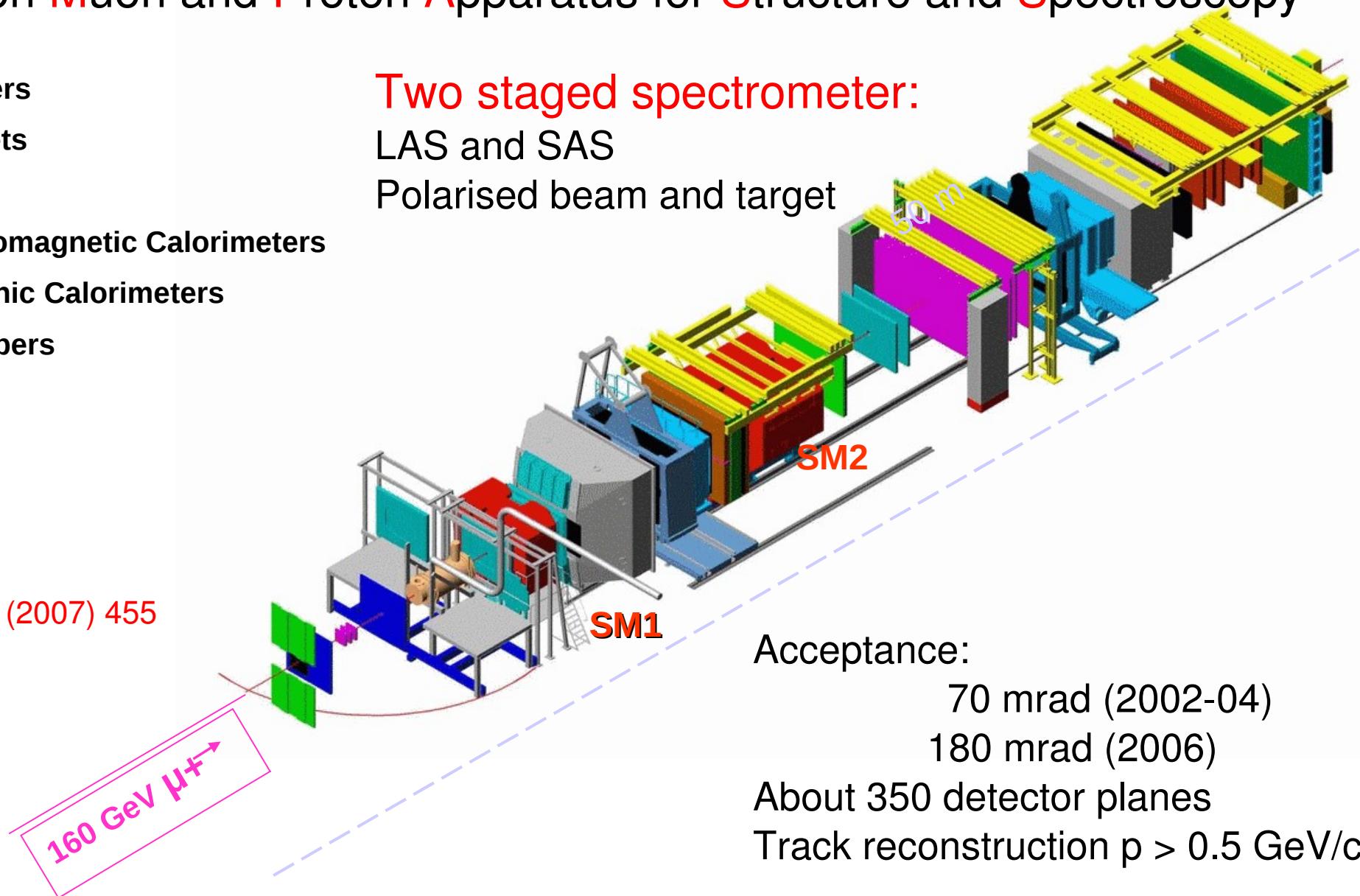


# The COMPASS Spectrometer

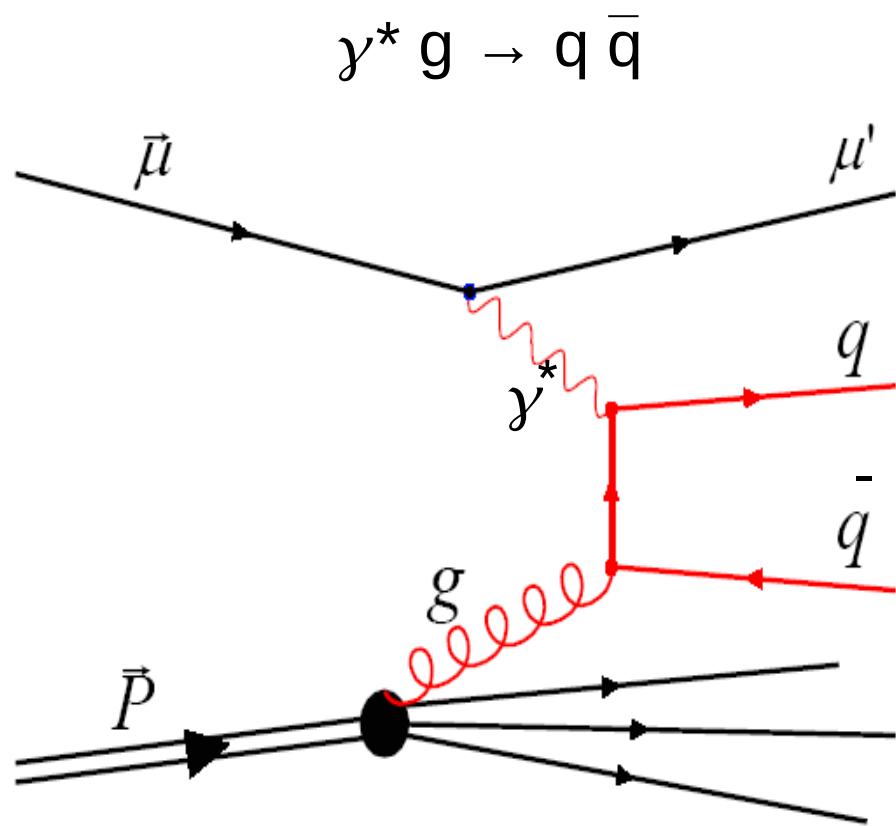
Common Muon and Proton Apparatus for Structure and Spectroscopy

-  Trackers
-  Magnets
-  RICH
-  Electromagnetic Calorimeters
-  Hadronic Calorimeters
-  Absorbers
-  Target

Two staged spectrometer:  
LAS and SAS  
Polarised beam and target

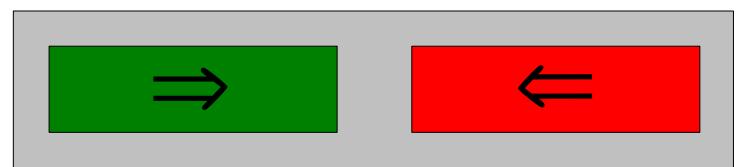


# Direct measurement of $\Delta G/G$



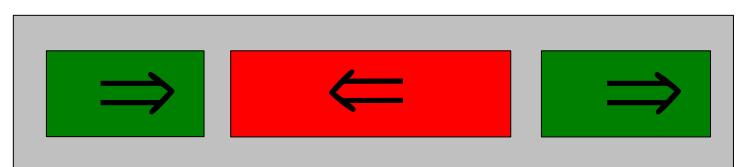
Photon-gluon fusion process (PGF)

2002-2004



$\mu$ -beam

2006



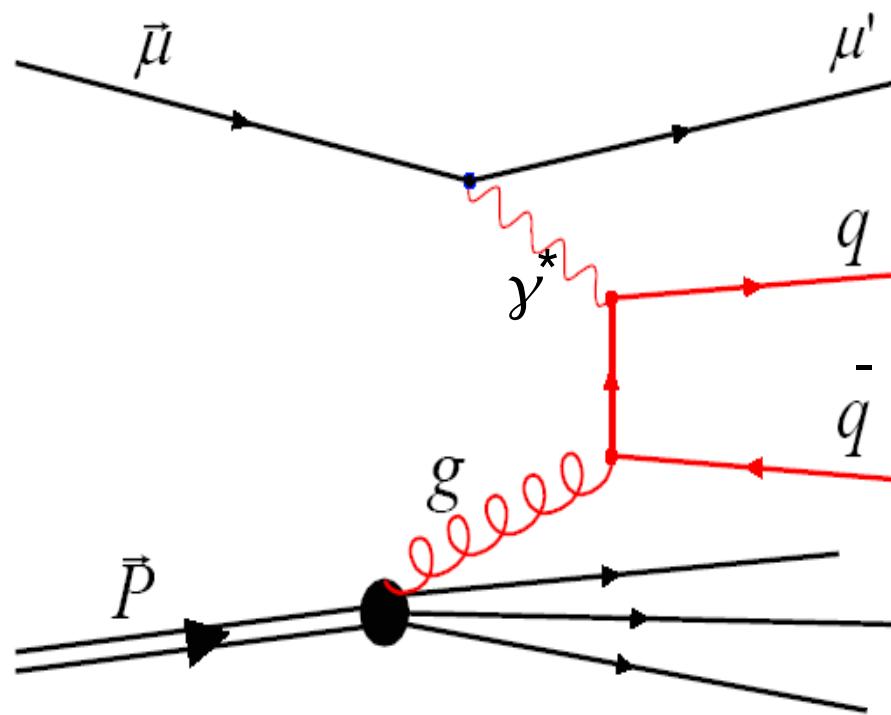
$$A_{PGF} = \frac{N_{PGF}^{\rightarrow} - N_{PGF}^{\leftarrow}}{N_{PGF}^{\rightarrow} + N_{PGF}^{\leftarrow}}$$



Experiments with polarised beam and target could be sensitive to gluon helicity

# Direct measurement of $\Delta G/G$

$$\gamma^* g \rightarrow q \bar{q}$$



To tag this process there are two procedures concerning event selection :

- **Open-charm meson** (cf. K.Kurek talk)
  - ☺ Provides the purest sample of PGF events, almost free from background contamination. Small dependence on MC.
  - ☹ Low statistics.
- **High transverse momentum hadrons** ( $Q^2 < 1$  and  $Q^2 > 1$  (GeVc) $^2$ )
  - ☺ Much more statistics.
  - ☹ Physical background: strongly model dependent, requires a very good agreement between MC and Data.

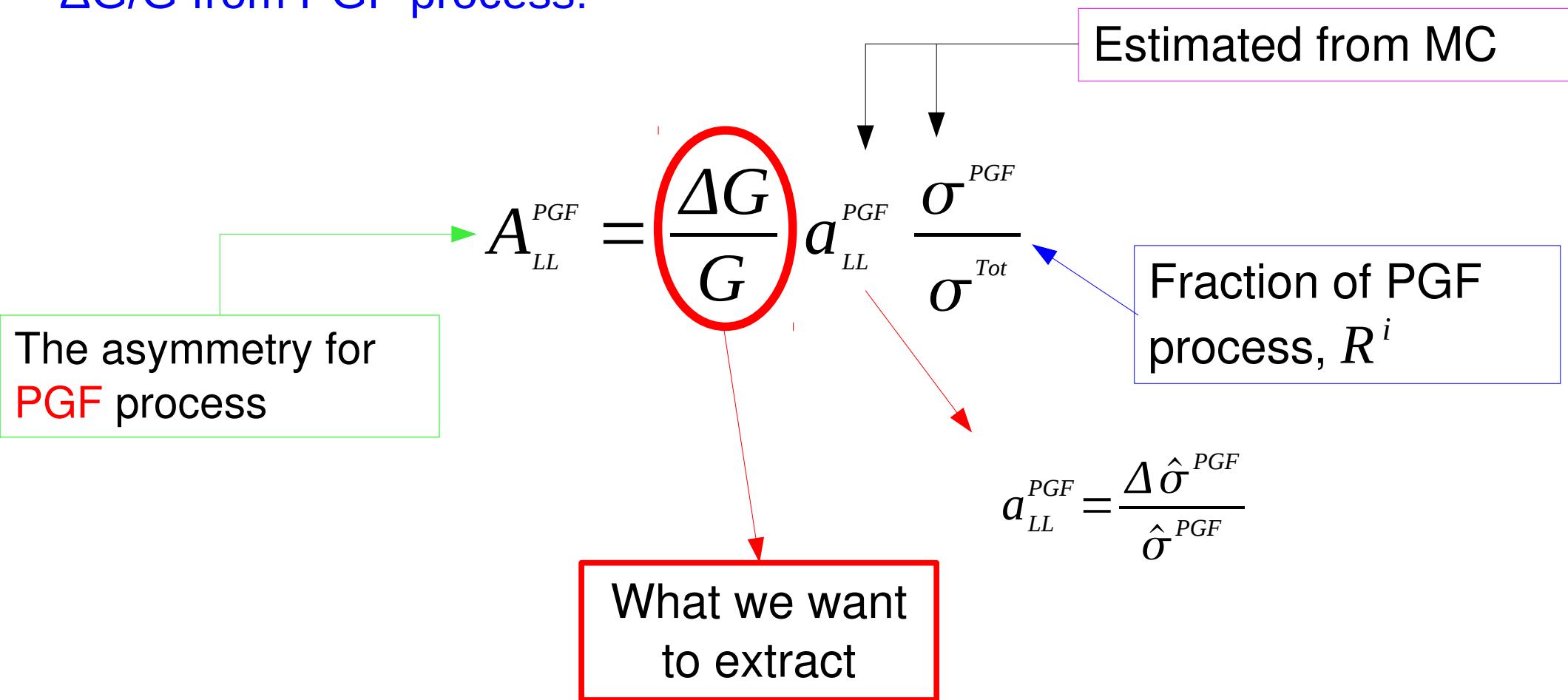
Photon-gluon fusion process (PGF)

# High $p_T$ Analysis



How is  $\Delta G/G$  measured?

$\Delta G/G$  from PGF process:

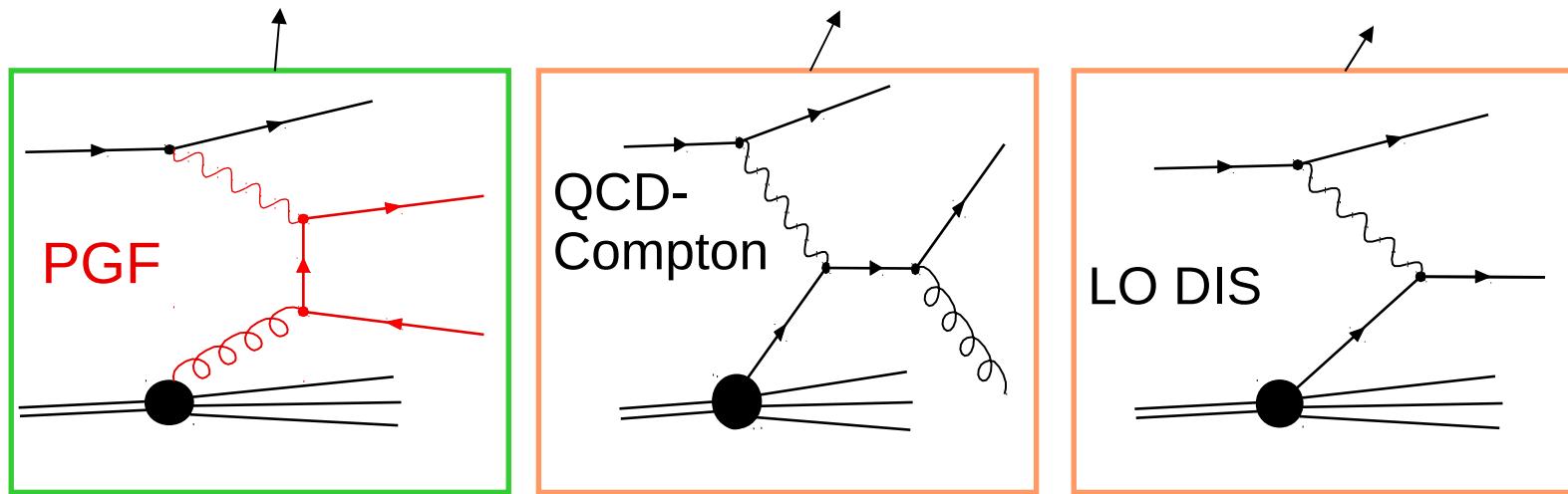


# High $p_T$ Analysis



We access  $A^{PGF}$  by measuring the helicity asymmetry in a sample of events with **two high- $p_T$  hadrons** produced at large  $Q^2$ . This measurement includes also contributions from other physical processes:

$$A_{LL}^{2h}(x) = \frac{\Delta G}{G}(x_g) a_{LL}^{PGF} \frac{\sigma^{PGF}}{\sigma^{Tot}} + A_1^{LO}(x_C) a_{LL}^C \frac{\sigma^C}{\sigma^{Tot}} + A_1^{LO}(x_{Bj}) D \frac{\sigma^{LO}}{\sigma^{Tot}}$$



$A_1^{LO}$  is estimated by the measured  $A_1$  asymmetry on **inclusive sample**

$D$  is the fraction of polarisation transferred from the muon to the virtual photon

# $\Delta G/G$ from High $p_T$



To extract the gluon polarisation, information from two samples is needed: the **two high  $p_T$  hadrons** and the **inclusive** data samples.

The final formula for the gluon polarisation is the following:

$$\frac{\Delta G}{G}(x_g^{av}) = \frac{1}{\beta} \left[ A_{LL}^{2h}(x_{Bj}) + A_{corr} \right]$$

$$\beta = a_{LL}^{PGF} R_{PGF} - a_{LL}^{PGF, incl} R_{PGF}^{incl} \frac{R_{LO}}{R_{LO}^{incl}} - a_{LL}^{PGF, incl} \frac{R_C R_{PGF}^{incl}}{R_{LO}^{incl}} \frac{a_{LL}^C}{D}$$

$$A_{corr} = - \left( A_1(x_{Bj}) D \frac{R_{LO}}{R_{LO}^{incl}} - A_1(x_C) \beta_1 + A_1(x_C') \beta_2 \right)$$

- $A_{LL}^{2h}$  is the measured asymmetry in the 2-h sample.
- $\beta_1$  and  $\beta_2$  are factors depending on  $a_{LL}^i$  and  $R^i$
- Where  $i$  stands for **signal** or **background** processes.

# Event selection

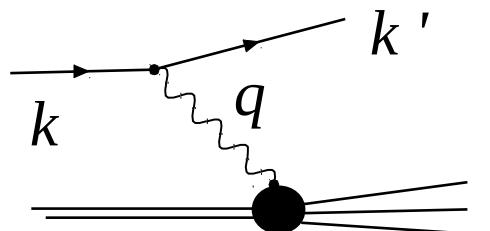


- Interaction vertex which contains an incoming and an outgoing **muon**
- For DIS variables:  $Q^2 > 1 \text{ (GeV/c)}^2$  and  $0.1 < y < 0.9$ 
  - ⇒ This selection constitutes the **inclusive** sample
- Events with at least **2** outgoing **hadrons** are selected
- The **hadrons** of the **high  $p_T$**  pair are required to have:

$$p_{T1} > 0.7 \text{ GeV/c}, \quad p_{T2} > 0.4 \text{ GeV/c}$$

$$z_1 + z_2 < 0.95$$

⇒ All this selection produces the **high  $p_T$**  sample



$$Q^2 = -q^2$$

$$q = k - k'$$

$$\nu = E - E'$$

$$y = \frac{\nu}{E}$$

$$x = \frac{Q^2}{2M\nu}$$

Years	2002	2003	2004	2006	all years
Statistics	450 K	1.3 M	2.8 M	2.7 M	<b>7.3 M</b>

Events

# Monte Carlo Simulation



This analysis uses **information** from the MC, thus a **strong effort** and **care** to ensure that the MC simulation describes as **good** as possible the **data** was undertaken.

Two **MC samples** were used in the analysis: **high  $p_T$**  and **inclusive** samples.

- Full chain of MC has been used:

Generator (LEPTO) + Apparatus Simulation (GEANT) +  
Reconstruction Program.

- PDF: MSTW2008LO.
- High  $p_T$  sample:

- MC with **parton shower ON** has been used in the analysis.
  - A **new tuning** was performed to **improve** the hadron description.

# MC Tuning

- The purpose of the **MC tuning** is to correct the shapes of the **hadron variables** (momenta) and **fragmentation** (multiplicity).
- In **LEPTO** this can be **achieved** by changing **JETSET** parameters:

PARJ(21)	PARJ(23)	PARJ(24)	PARJ(41)	PARJ(42)
Transverse momentum of the hadron fragmentation			Fragmentation function	

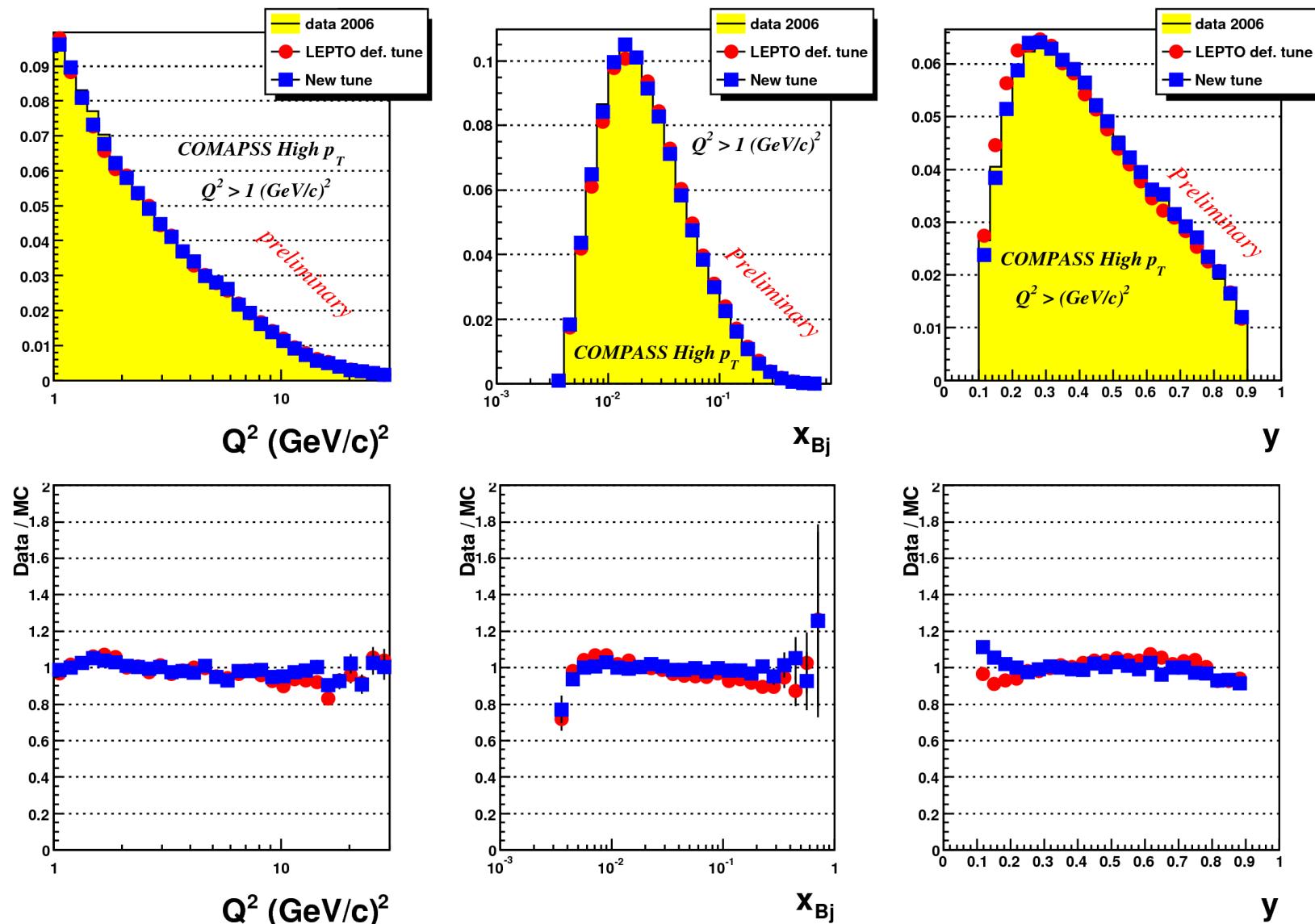
- These **parameters** can be **divided** into **two sets** regarding the **component** of the **trajectory** of the particles: **Transverse** and **longitudinal** variable components.
- The **sets** can be **tuned independently**.  
⇒ The tuning improves substantially the Data-MC agreement.



# Data – Monte Carlo comparison

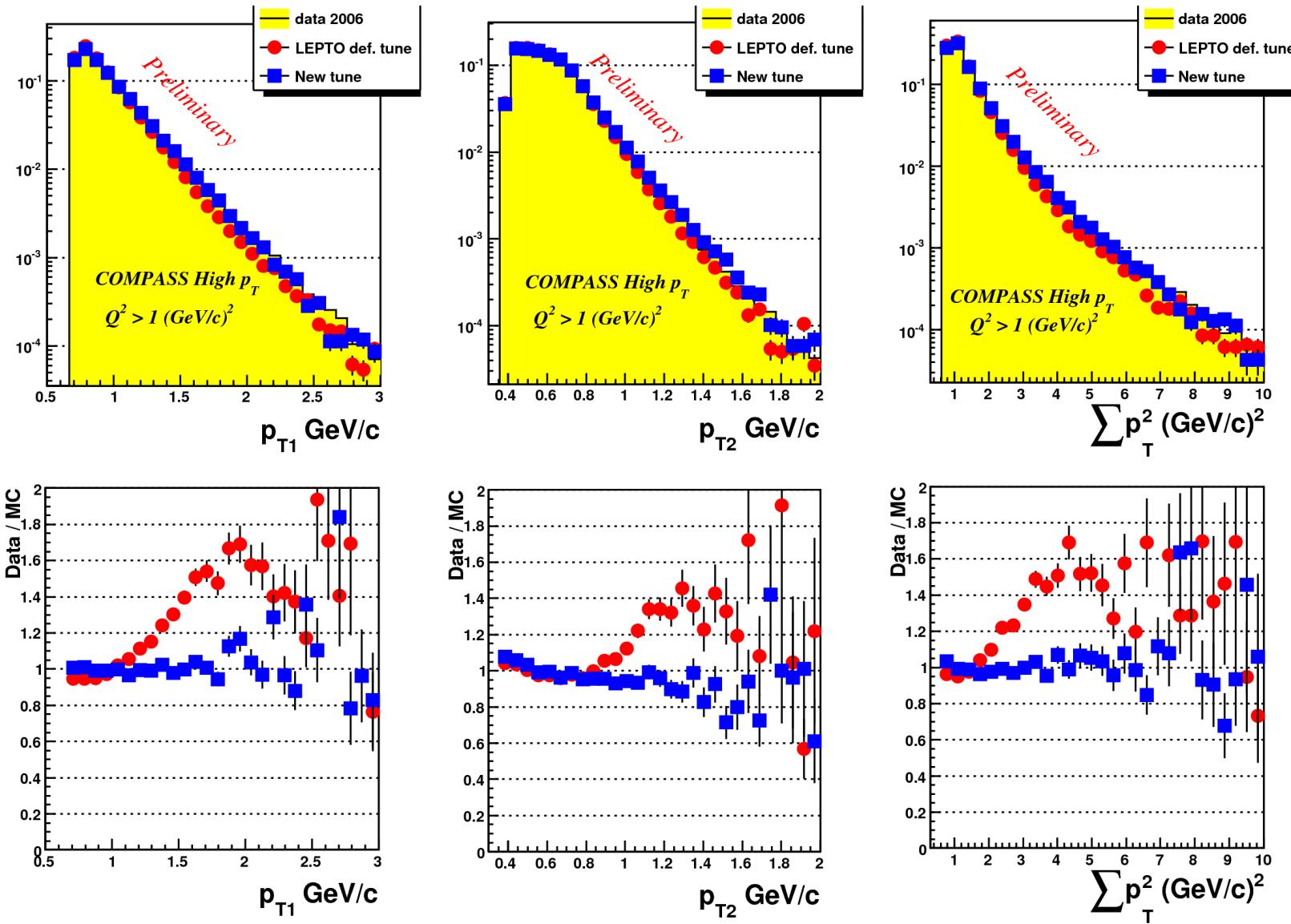


high- $p_T$  sample ( $Q^2$ ,  $x$  and  $y$ )



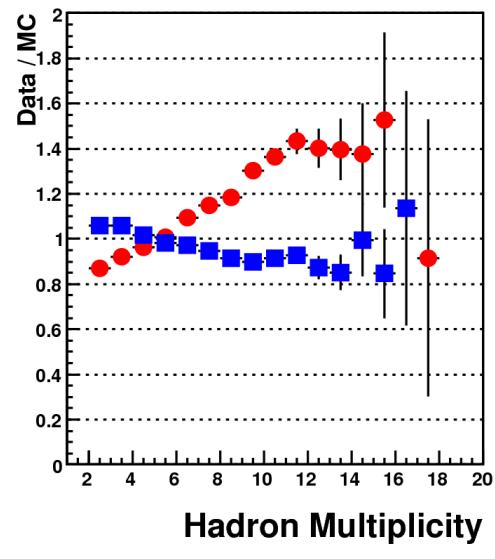
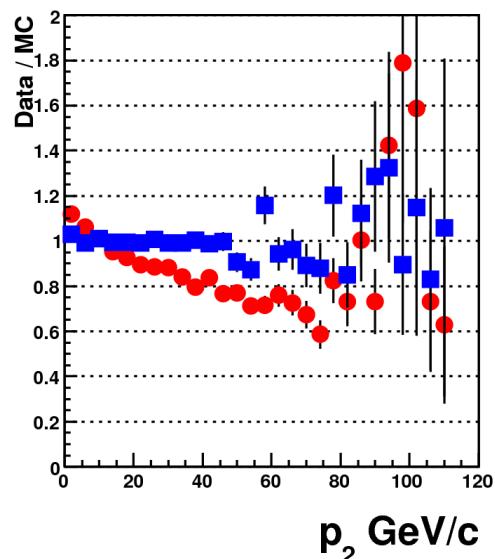
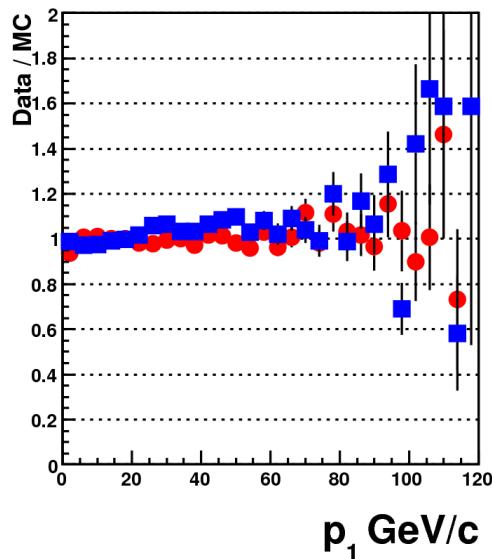
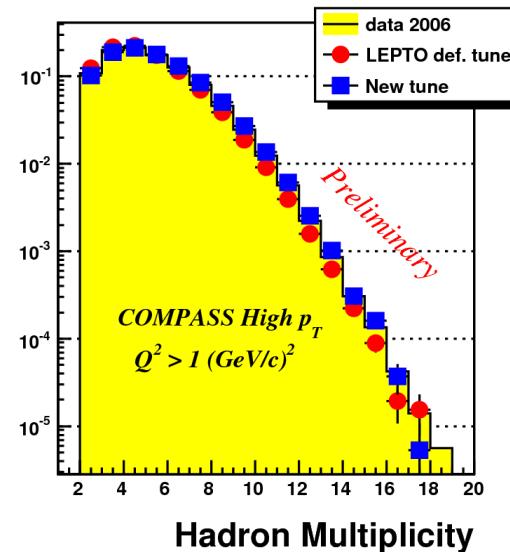
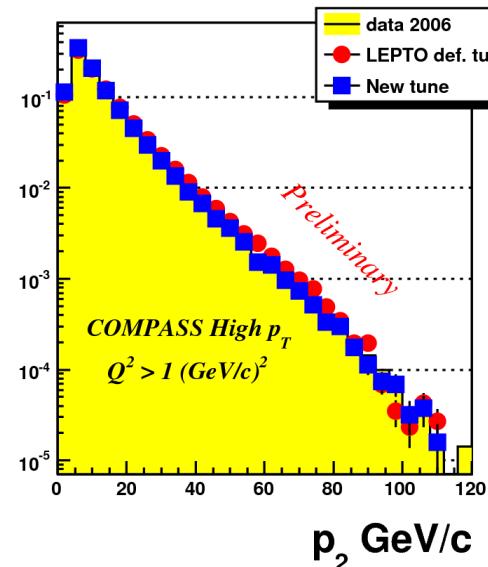
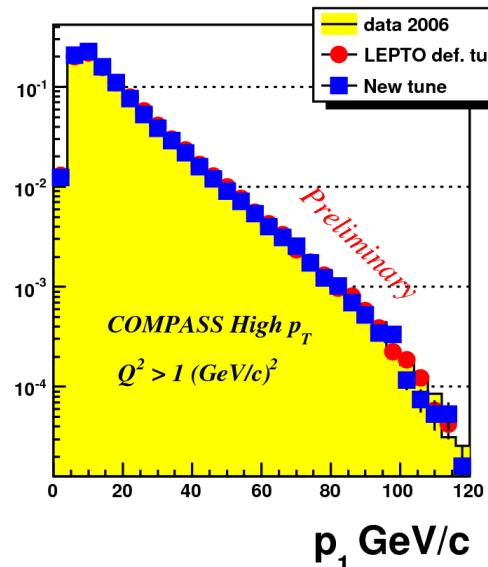
# Data – Monte Carlo comparison

high- $p_T$  sample: hadron variables ( $p_{T1}$ ,  $p_{T2}$  and  $\sum p_T^2$ )



# Data – Monte Carlo comparison

high- $p_T$  sample: hadron variables ( $p_1$ ,  $p_2$  and multiplicity)



# Weighted method

- A weight is applied on event-by-event basis:

$W = fDP_b\beta$  , where  $\beta$  is a factor depending on  $a_{LL}^i$  and  $R^i$

- Therefore for every event we have to know:

$R_{PGF}, R_C, R_{LO}, R_{PGF}^{incl}, R_C^{incl}, R_{LO}^{incl},$

$a_{LL}^{PGF}, a_{LL}^C, a_{LL}^{PGF,incl}, a_{LL}^{C,incl},$

$x_C, x_G,$

$f, D, P_b$

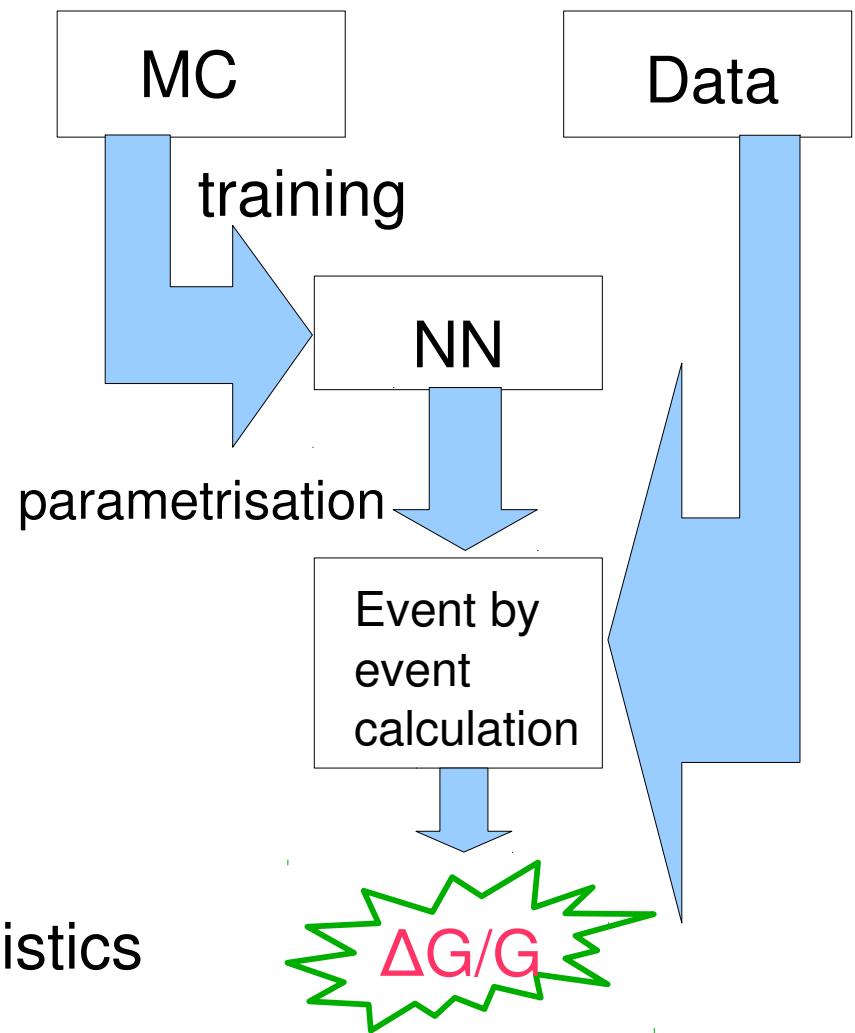
$f, D, P_b$  are directly obtained from data.

The all the others variables have to be estimated/parametrised.

# Weighted method

A Neural Network is used to assign to each event a probability to be originated from each of the three processes (LO, PGF or Compton).

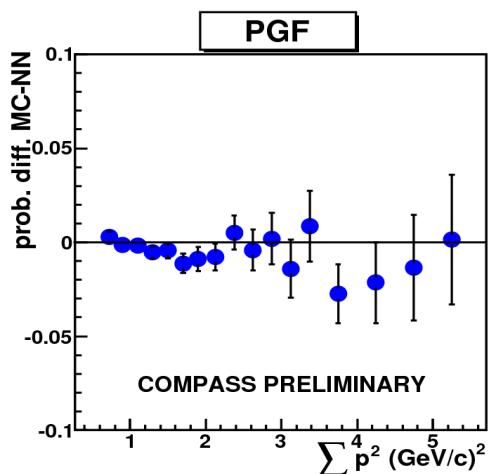
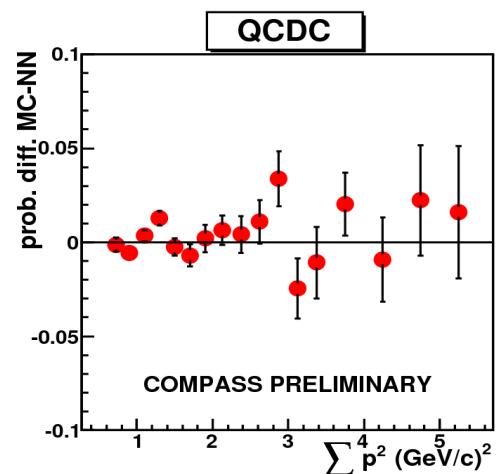
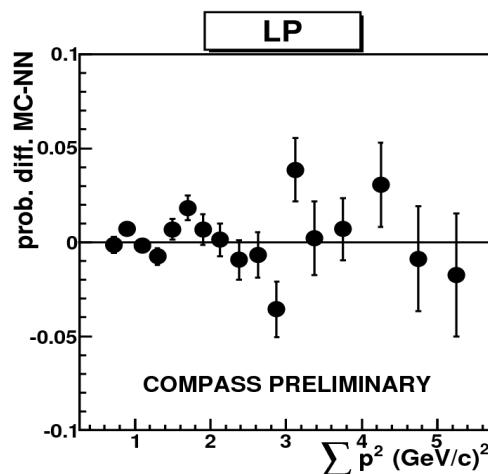
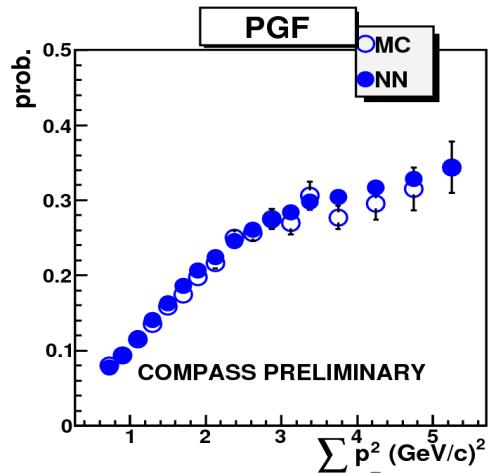
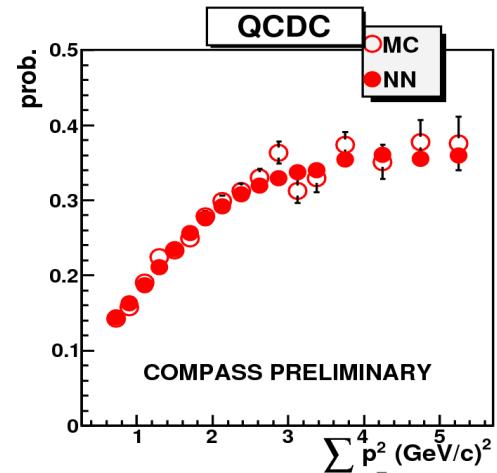
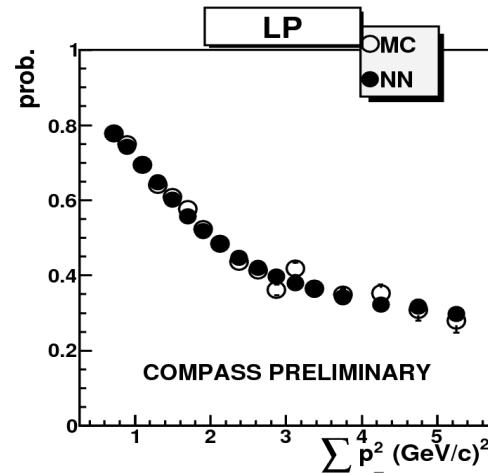
- A **MC** sample is used to train the Neural Network (NN).
- A parametrisation is constructed for all variables involved in the weight.
- A **Data** sample is weighted on an event-by-event basis.



Optimal usage of the data sample statistics

# Example: Stability plots for NN

We parametrise the  $R^i$  fractions as probabilities.



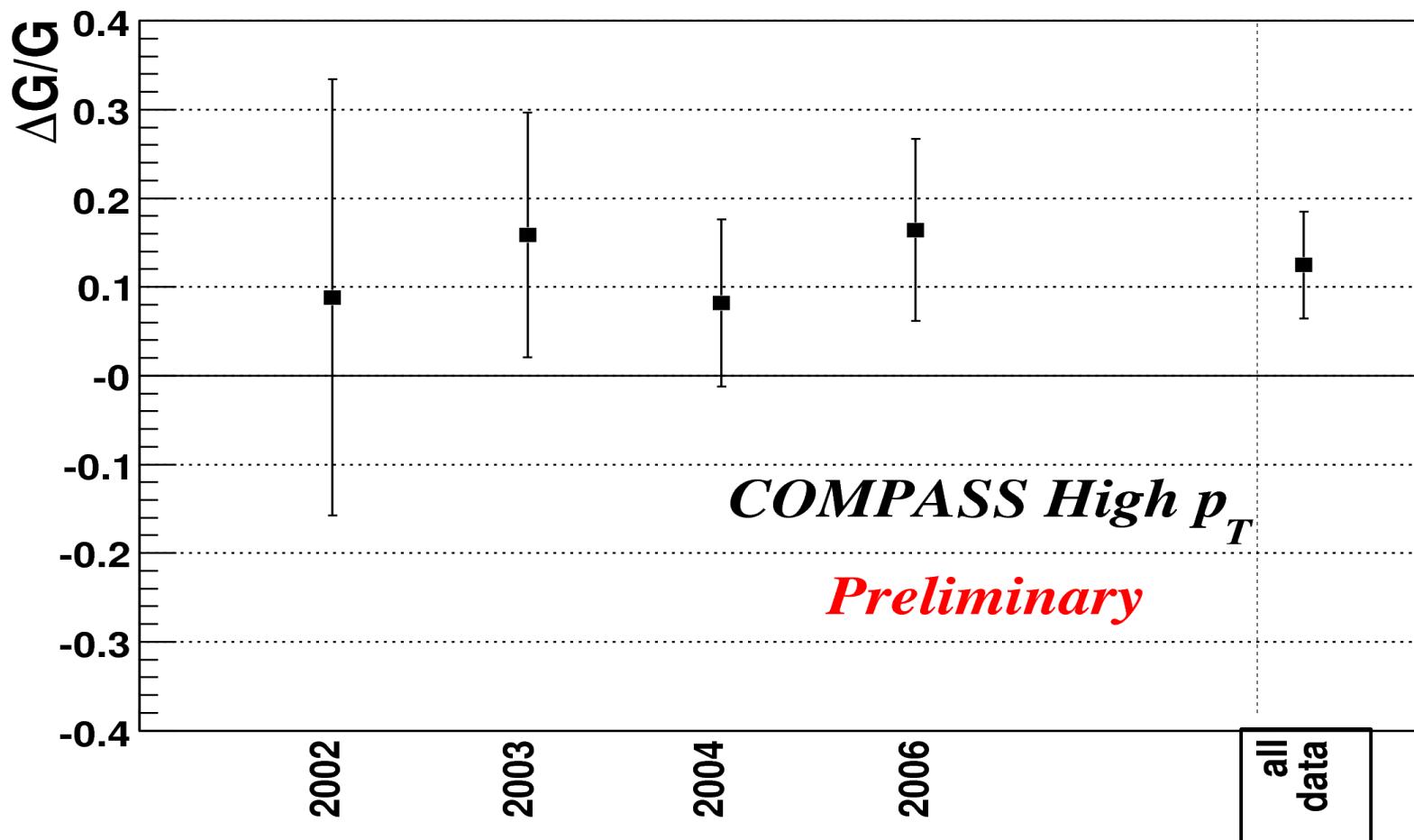
# Results



$$\frac{\Delta G}{G} = 0.125 \pm 0.060 \pm 0.063$$

$$x_{_G} = 0.09^{+0.08}_{-0.04}$$

$$\langle \mu^2 \rangle = 3.4 \text{ (GeV/c)}^2$$



# Results



$$\frac{\Delta G}{G} = 0.125 \pm 0.060 \pm 0.063 \quad x_g = 0.09^{+0.08}_{-0.04} \quad \langle \mu^2 \rangle = 3.4 \text{ (GeV/c)}^2$$

- The whole statistics was divided, for the first time, in 3 independent samples, having each one its own  $x_g$  distribution.

	1 <sup>st</sup> point	2 <sup>nd</sup> point	3 <sup>rd</sup> point
$\Delta G/G$	$0.15 \pm 0.09 \pm 0.09$	$0.08 \pm 0.10 \pm 0.08$	$0.19 \pm 0.17 \pm 0.14$
$\langle x_g \rangle$	$0.07^{+0.05}_{-0.03}$	$0.10^{+0.07}_{-0.04}$	$0.17^{+0.10}_{-0.06}$

⇒ Within the errors the 3 points show no  $x_g$  dependence

# Systematic errors Study



What has been checked?

- Neural Network stability
- MC
- False Asymmetries
- $\delta P_b, \delta P_t, \delta f$
- $A_1$  parametrisation
- Simplification of the Formula for  $\Delta G/G$

$\delta(\Delta G/G)_{NN}$	0.010
$\delta(\Delta G/G)_{MC}$	0.045
$\delta(\Delta G/G)_{\text{false}}$	0.019
$\delta(\Delta G/G)_{f,Pb,Pt}$	0.004
$\delta(\Delta G/G)_{A1}$	0.015
$\delta(\Delta G/G)_{\text{formula}}$	0.035
Total	0.063

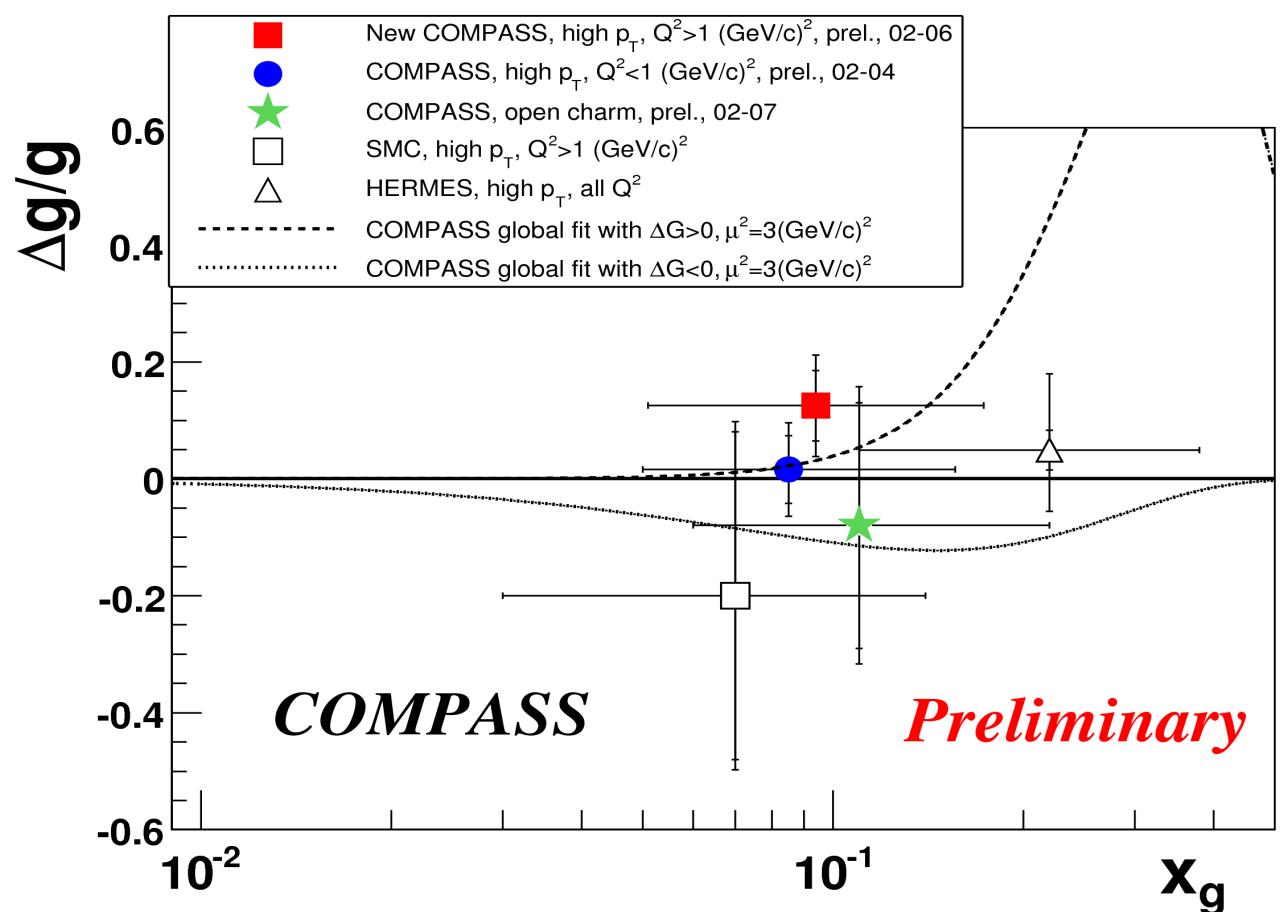
# $\Delta G/G$ Results

$$\frac{\Delta G}{G} = 0.125 \pm 0.060 \pm 0.063$$

$$x_g = 0.09^{+0.08}_{-0.04}$$

$$\langle \mu^2 \rangle = 3.4 \text{ (GeV/c)}^2$$

- All points at  $x_g \sim 0.1$  are compatible with each other
- All points are compatible with the COMPASS QCD fits and other predictions.
- At  $x_g \sim 0.1 \Rightarrow \Delta G/G \sim 0$

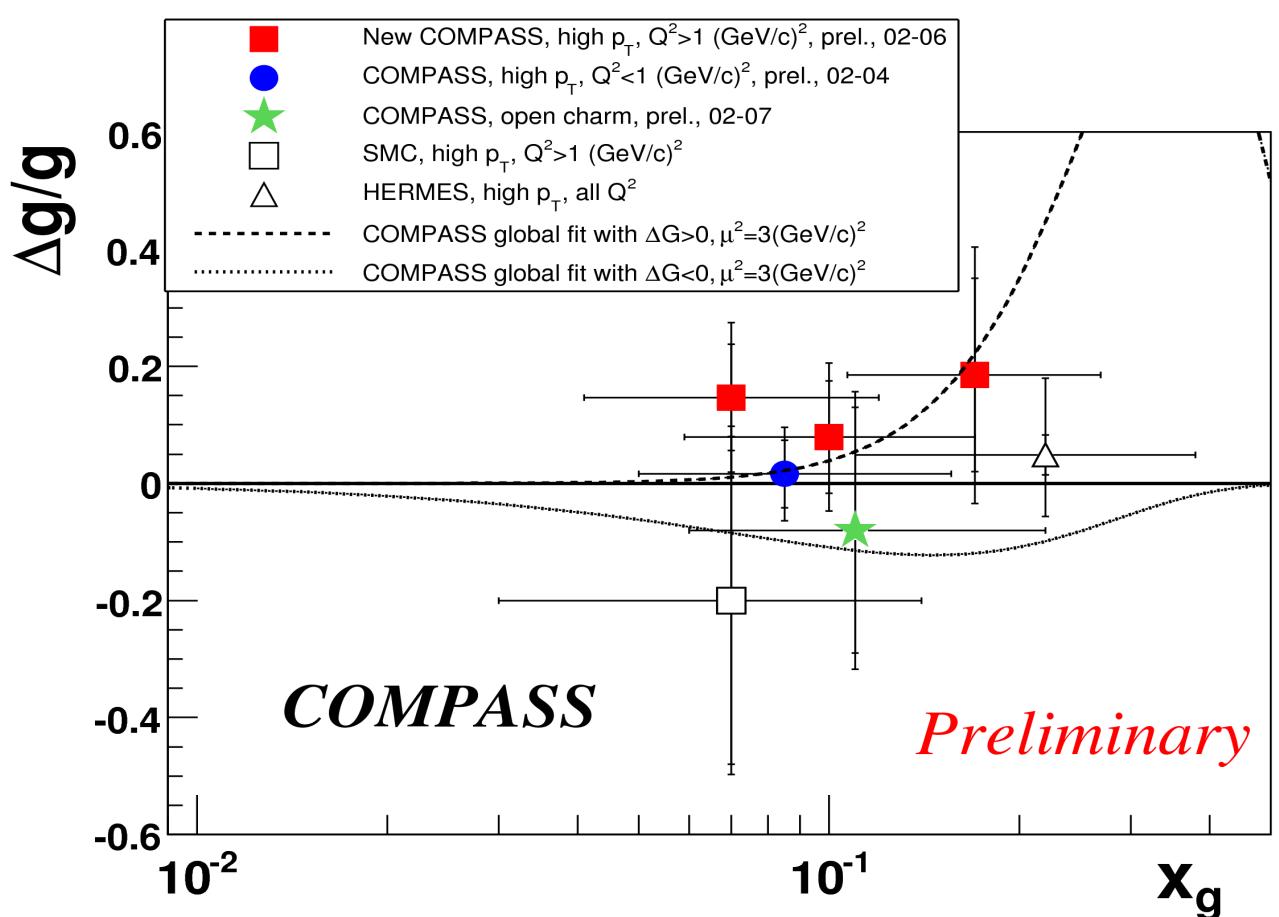


# $\Delta G/G$ Results

1<sup>st</sup> point :  $0.147 \pm 0.091_{\text{stat}} \pm 0.088_{\text{sys}}$  @  $x_g = 0.07^{+0.05}_{-0.03}$   
 2<sup>nd</sup> point :  $0.079 \pm 0.096_{\text{stat}} \pm 0.082_{\text{sys}}$  @  $x_g = 0.10^{+0.07}_{-0.04}$   
 3<sup>rd</sup> point :  $0.185 \pm 0.165_{\text{stat}} \pm 0.143_{\text{sys}}$  @  $x_g = 0.17^{+0.10}_{-0.06}$

First experiment giving a measurement in 3 points in

$x_g$



# Spares



# $\Delta G/G$ for High $p_T$ , $Q^2 > 1 \text{ GeV}^2$

The final formula for the gluon polarization:

$$\frac{\Delta G}{G}(x_g^{av}) = \frac{A_{LL}^{2h}(x_{Bj})}{\beta} - \frac{A_1(x_{Bj})}{\beta} D \frac{R_{LO}}{R_{LO}^{incl}} - \frac{A_1(x_C)}{\beta} \beta_1 + \frac{A_1(x_C')}{\beta} \beta_2$$

$$\beta = a_{LL}^{PGF} R_{PGF} - a_{LL}^{PGF,incl} R_{PGF}^{incl} \frac{R_{LO}}{R_{LO}^{incl}} - a_{LL}^{PGF,incl} \frac{R_C}{R_{LO}^{incl}} \frac{R_{PGF}^{incl}}{D} \quad R_i = \frac{\sigma^i}{\sigma^{Tot}}$$

$$\beta_1 = \frac{1}{R_{LO}^{incl}} (a_{LL}^C R_C - a_{LL}^{C,incl} R_C^{incl} \frac{R_{LO}}{R_{LO}^{incl}}) \quad \beta_2 = a_{LL}^{C,incl} \frac{R_C}{(R_{LO}^{incl})^2} \frac{R_C^{incl}}{D} \frac{a_{LL}^C}{D}$$

- $A_{LL}^{2h}$  is the measured 2-h asymmetry.
- $a_{LL}$  and  $R$  are estimated using MC.
- The  $A_1$  are taken using a parametrisation on inclusive data. (EPJ C52 (2007)255)



# $\Delta G/G$ for High $p_T$ , $Q^2 > 1 \text{ GeV}^2$

The final formula for the gluon polarization:

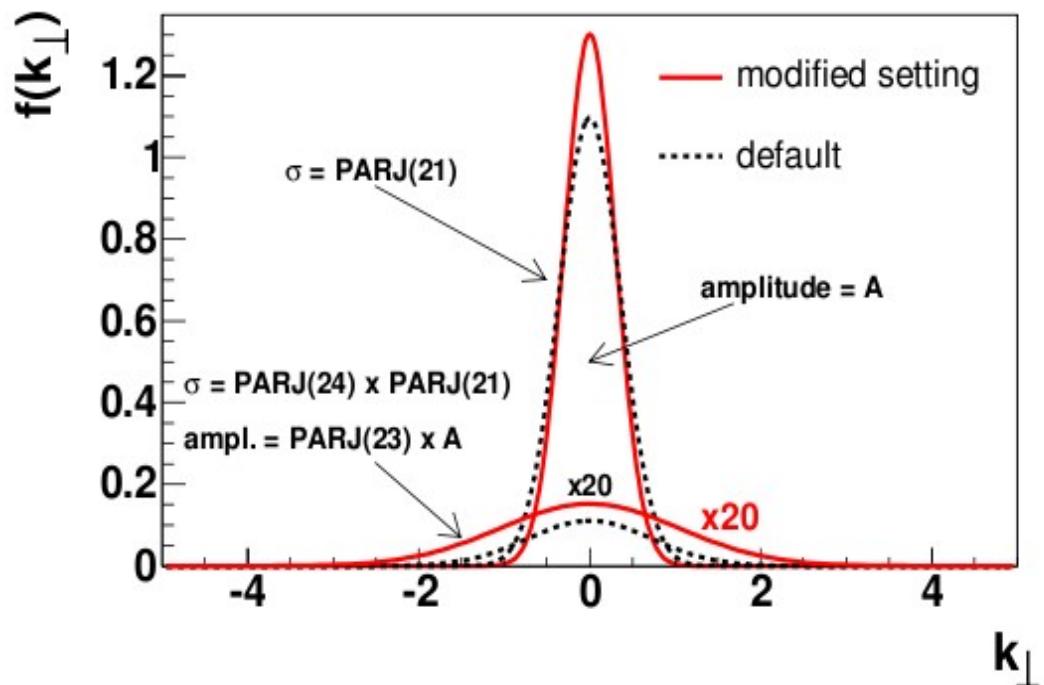
$$\frac{\Delta G}{G}(x_g^{av}) = \frac{1}{\beta} \left[ A_{LL}^{2h}(x_{Bj}) + A_{corr}(x_{Bj}) \right]$$

- $A_{LL}^{2h}$  is the measured 2-h asymmetry.
- $\beta$  is composed by  $a_{LL}$  and  $R$ . They are estimated using MC.
- $A_{corr}$  is a corrective factor for Compton-QCD and LO processes:
  - $a_{LL}$  and  $R$  are estimated using MC.
  - The  $A_1$  are taken using a parametrization on inclusive data.

(EPJ C52 (2007) 255)

$$A_{corr} = - \left( A_1(x_{Bj}) D \frac{R_{LO}}{R_{LO^{incl}}} - A_1(x_C) \beta_1 + A_1(x_C') \beta_2 \right)$$

# Monte Carlo Simulation



$a = \text{PARJ}(41)$

$b = \text{PARJ}(42)$

$$f(z) \propto \frac{1}{2} (1-z)^a \exp\left(-\frac{b m_T^2}{z}\right)$$

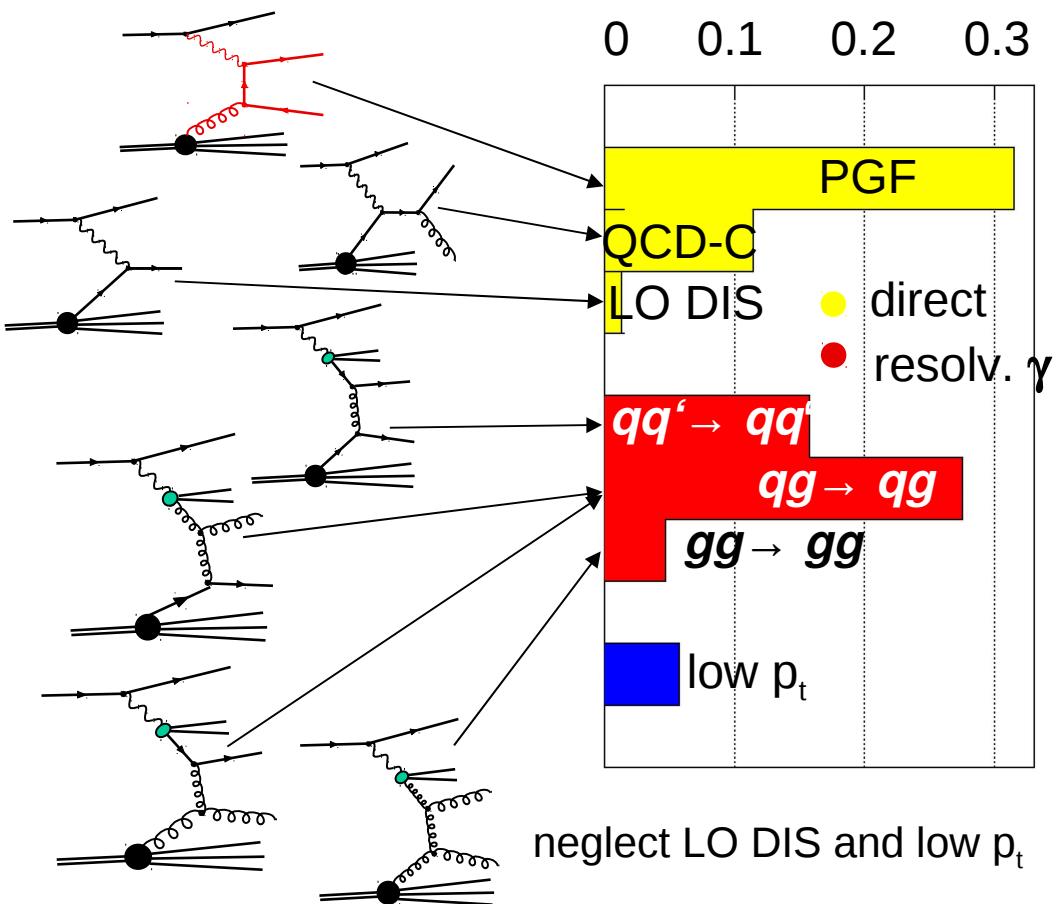
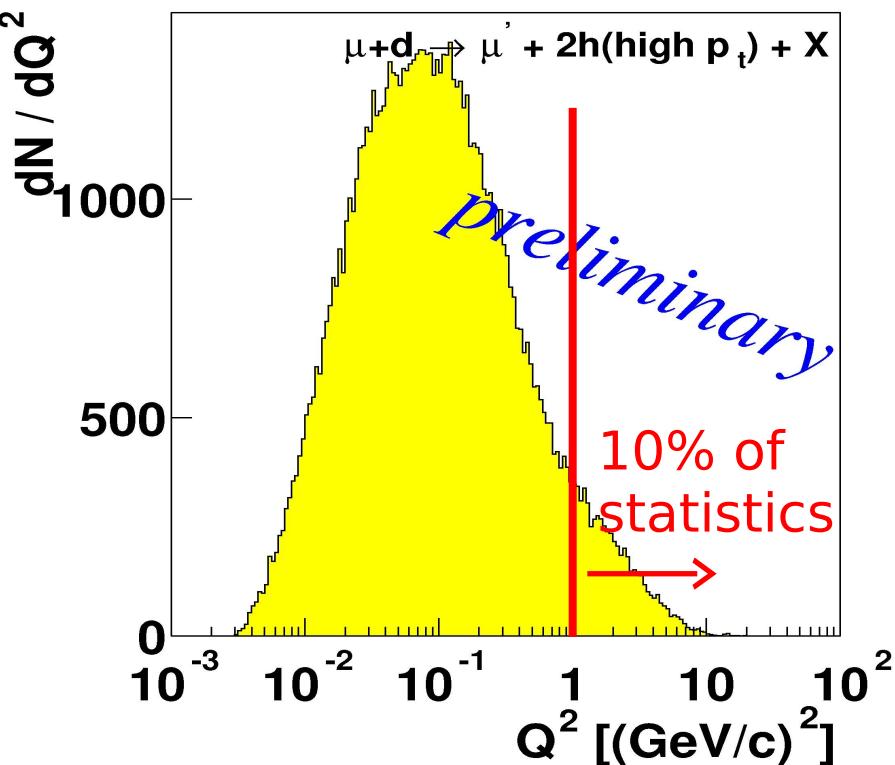
COMPASS new tuning  
LEPTO default tuning

PARJ(21)	PARJ(23)	PARJ(24)	PARJ(41)	PARJ(42)
0.34	0.04	2.8	0.025	0.075
0.36	0.01	2.0	0.3	0.58
Transverse momentum of the hadron fragmentation			Fragmentation function	

# High $p_T$ Analysis, $Q^2 < 1 \text{ (GeV/c)}^2$



~90 % of our statistics in this sample



2002-2004 Preliminary:

$$\Delta G/G = 0.016 \pm 0.058(\text{stat}) \pm 0.055(\text{syst})$$

2002-2003 Published:

$$\Delta G/G = 0.024 \pm 0.089(\text{stat}) \pm 0.057(\text{syst})$$

*Phys. Lett. B 633 (2006) 25 - 32*