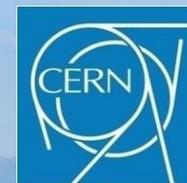




Spin measurements in lepton scattering

G. K. Mallot
CERN/PH



Workshop on
High-energy hadron physics with hadron beams

KEK, Tsukuba, January 2010

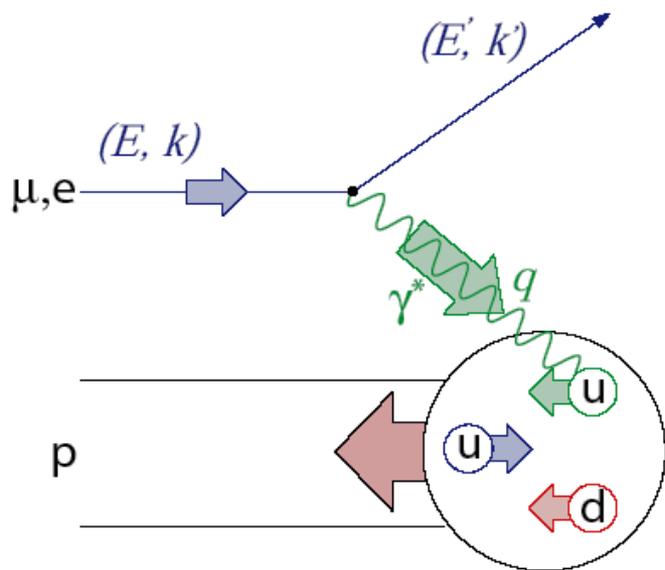


Plan

- Introduction
 - DIS
 - Experiments
- Helicity structure of the nucleon
 - Quarks
 - Gluons
- Transverse spin-structure of the nucleon
- Outlook



Deep Inelastic Scattering



$$Q^2 = -(k - k')^2 \stackrel{lab}{=} 4EE' \sin^2 \frac{\vartheta}{2}$$

$$P \cdot q \stackrel{lab}{=} M\nu = M(E - E')$$

$$P \cdot k \stackrel{lab}{=} ME$$

$$x \stackrel{lab}{=} \frac{Q^2}{2M\nu} = \frac{-q^2}{2P \cdot q}$$

$$y \stackrel{lab}{=} \frac{\nu}{E} = \frac{P \cdot q}{P \cdot k}$$

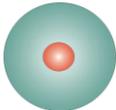
$$0 \leq x, y \leq 1$$



Parton Distribution Functions

Three twist-2 PDFs

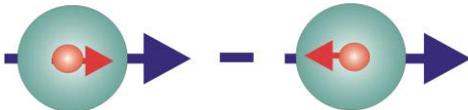
$q(x)$
 $f_1^q(x)$



unpolarised PDF

quark with momentum xP in a nucleon
well known – unpolarised DIS

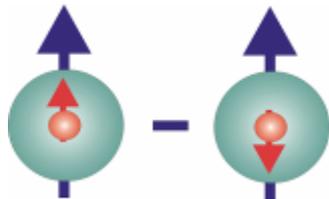
$\Delta q(x)$
 $g_1^q(x)$



helicity PDF

quark with spin parallel to the nucleon
spin in a longitudinally polarised nucleon
known – polarised DIS

$\Delta_T q(x)$
 $h_1^q(x)$



transversity PDF

quark with spin parallel to the nucleon
spin in a transversely polarised nucleon

chiral odd, poorly known



Longitudinal asymmetries

Inclusive scattering

$$A_1 = \frac{\sum_q e_q^2 \Delta q(x, Q^2)}{\sum_q e_q^2 q(x, Q^2)}$$

with

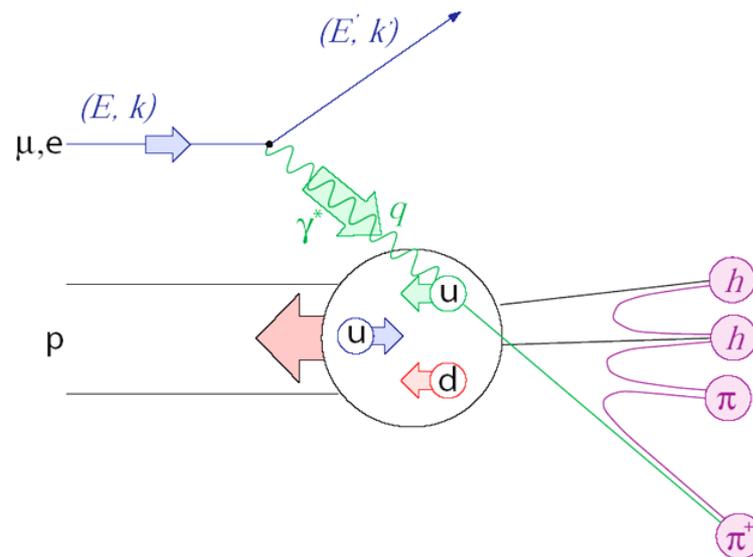
$$\Delta q = q^+ - q^-$$

$$A_1 = g_1 / F_1$$

Semi-inclusive scattering

$$A_1^h = \frac{\sum_q e_q^2 \Delta q(x, Q^2) D_q^h(z, Q^2)}{\sum_q e_q^2 q(x, Q^2) D_q^h(z, Q^2)}$$

with $z = E_h / \nu$





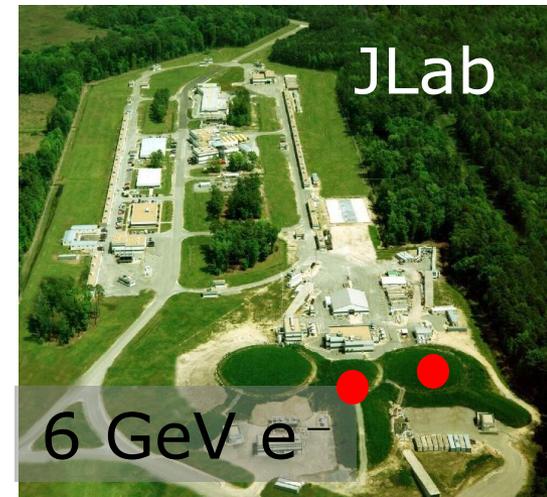
TMD parton distributions

- 8 intrinsic transverse momentum dependent PDFs at LO
- Asymmetries with different angular dependences on hadron and spin azimuthal angles, Φ_h and Φ_s

		nucleon polarization			
		U	L	T	
quark polarization	U	f_1 number density		f_{1T}^\perp -	Sivers
	L		g_1 -	g_{1T} -	
Boer-Mulders	T	h_1^\perp -	h_{1L}^\perp -	h_1 - transversity h_{1T}^\perp -	Transversity



Laboratories





Experiments

	1970	1980	1990	2000
SLAC				
	E80	E130	E142/3 E154/5	
CERN				
		EMC	SMC	COMPASS
DESY				
			HERMES	
JLab				
				CLAS/HALL-A

A worldwide effort since decades



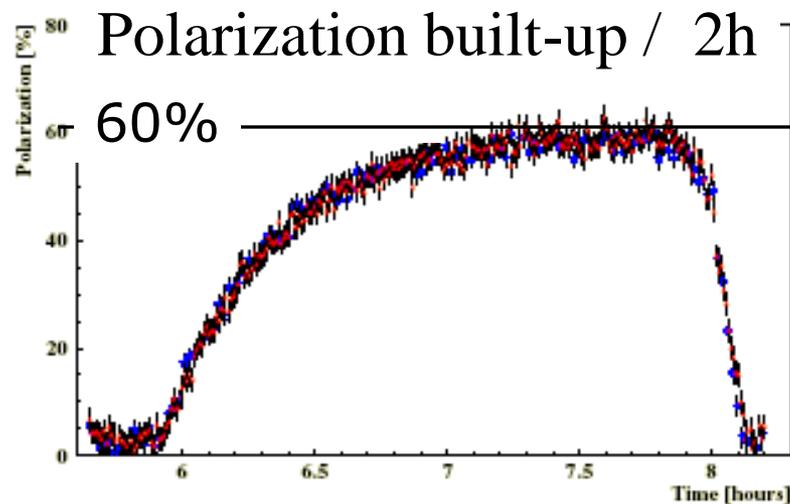
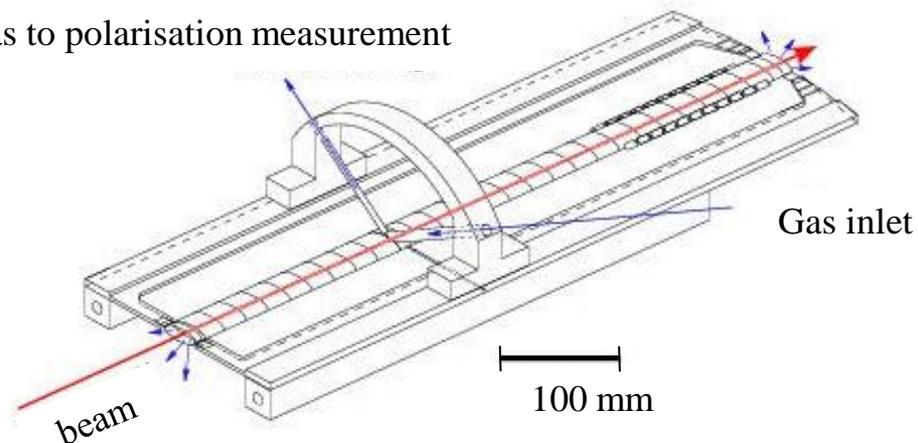
HERMES



Target: atomic beam source +
internal storage cell
 10^{14} atoms/cm²
p, d, ³He (~90% pol.)

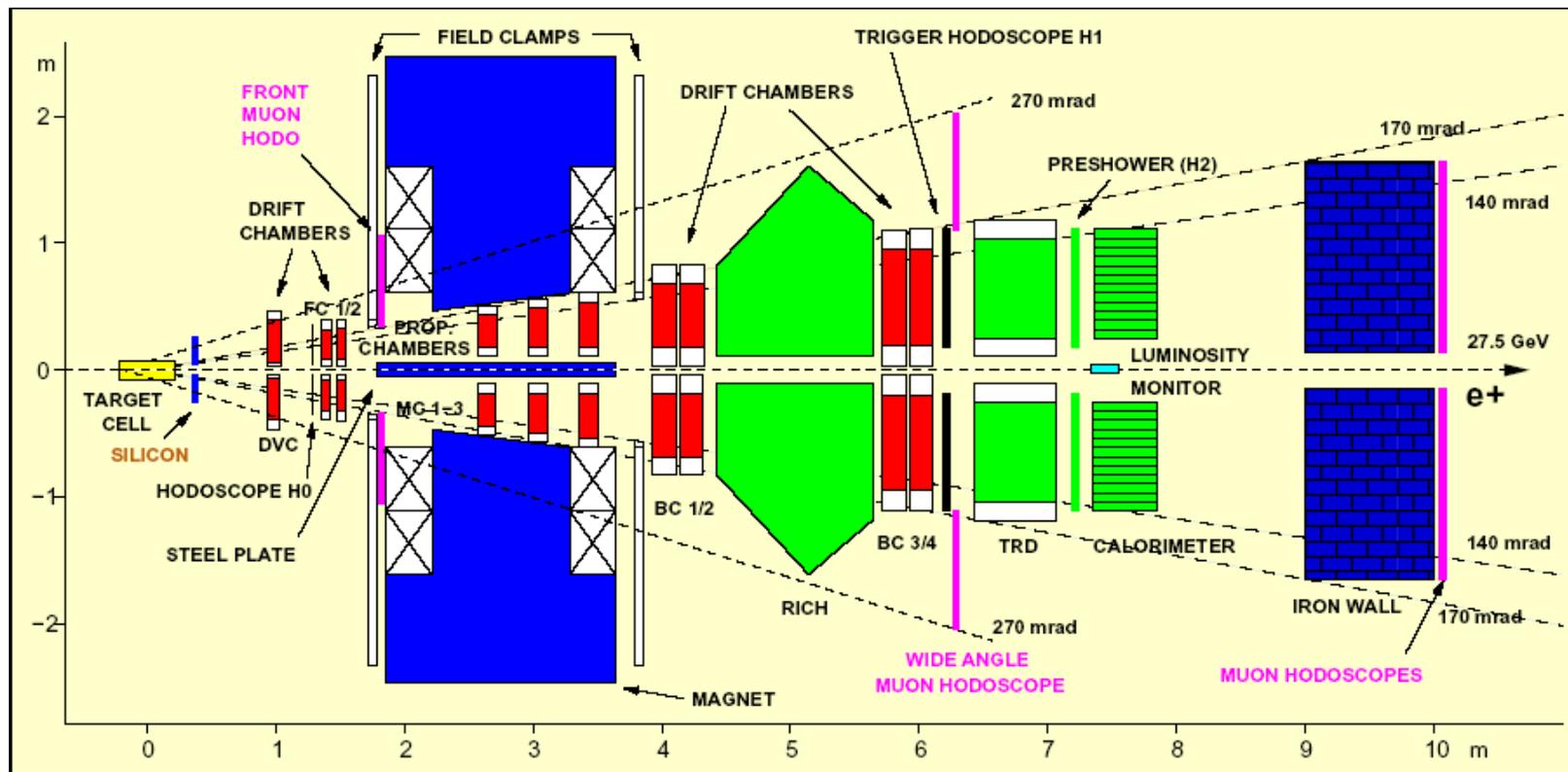
Beam: 27 GeV, electrons,
polarized by the
[Sokolov-Ternov](#) effect +
spin rotators

Gas to polarisation measurement





HERMES

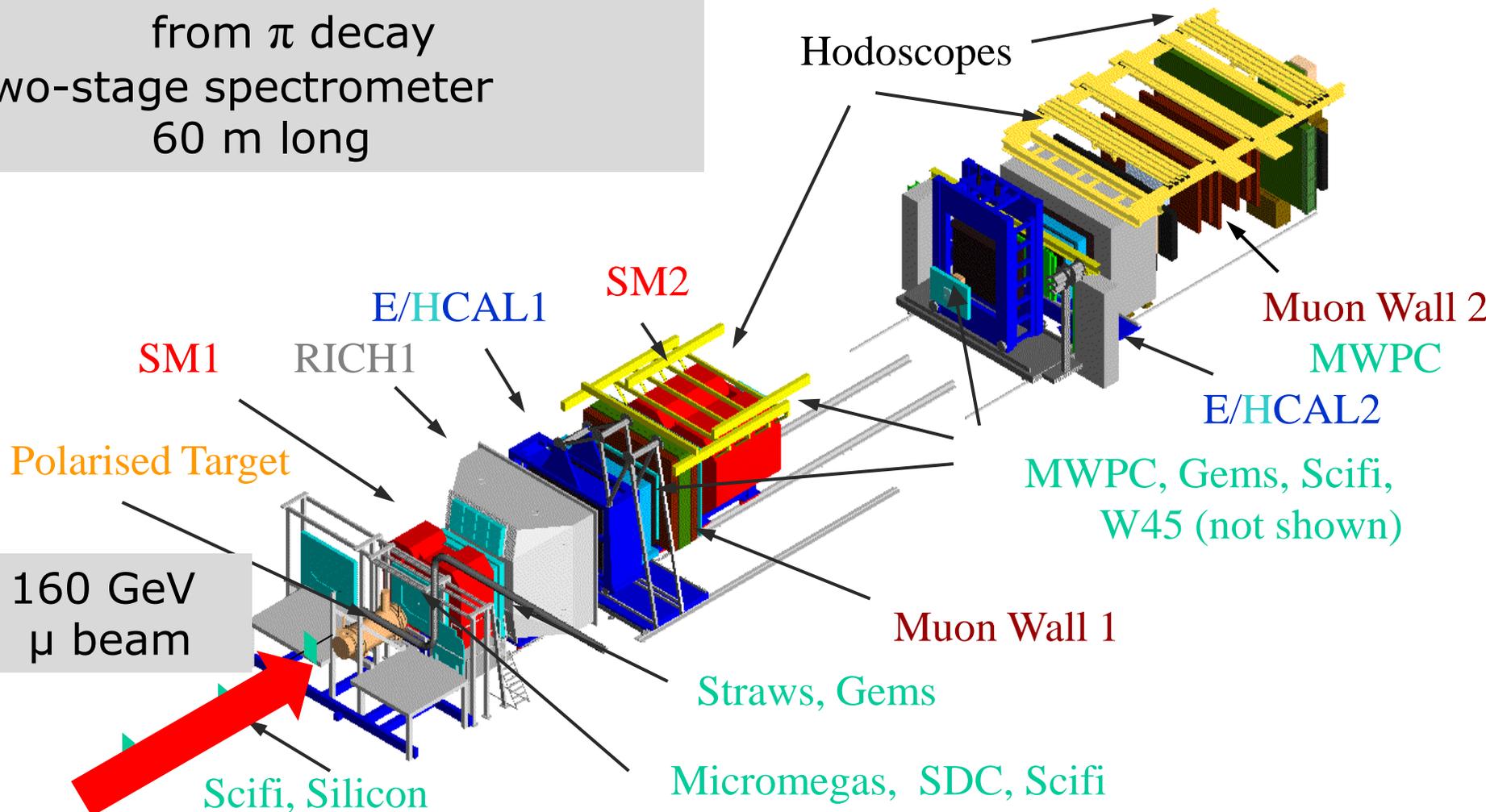




COMPASS



Beam: 160 GeV μ^+ , pol. 80%
from π decay
Two-stage spectrometer
60 m long





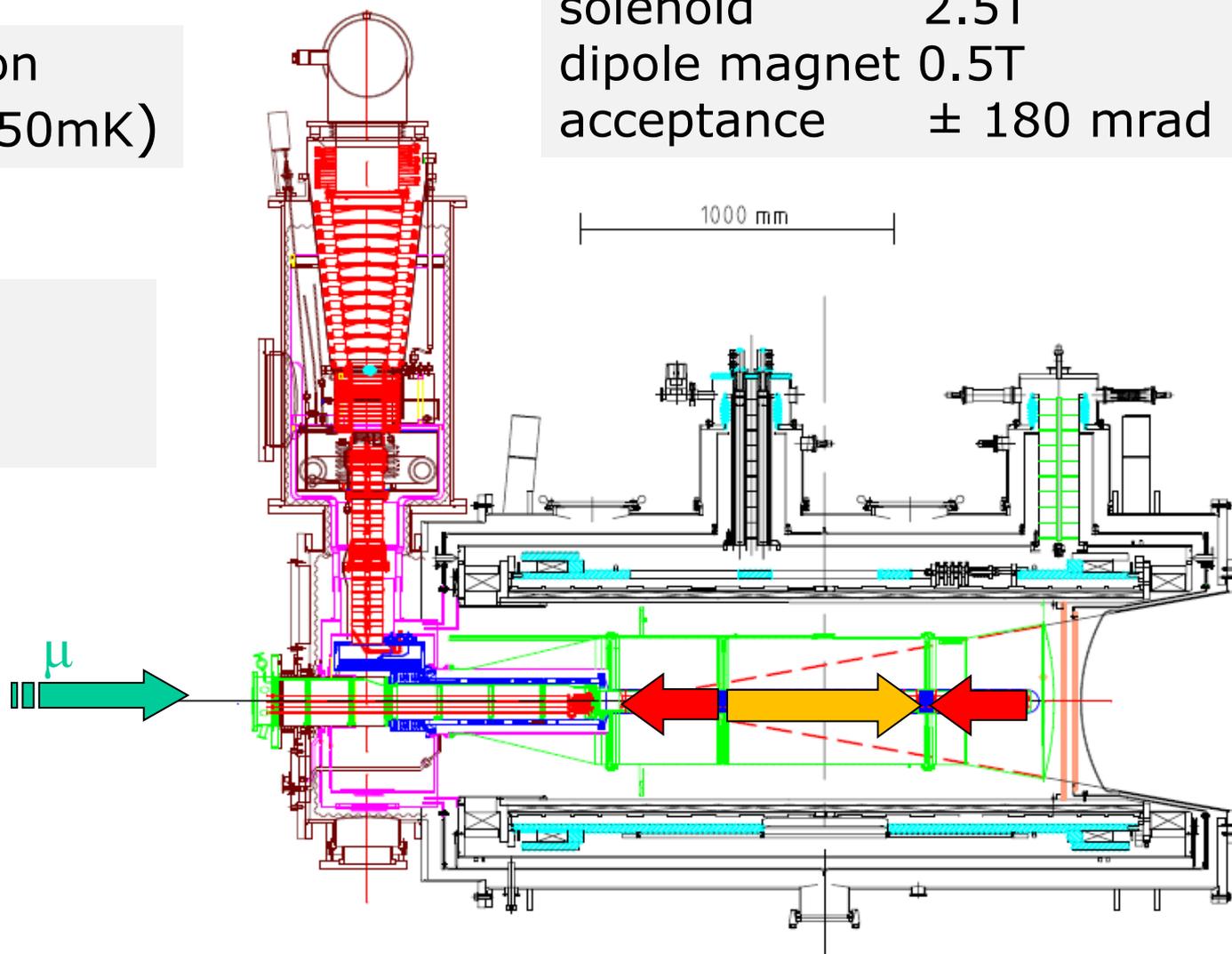
COMPASS Target system



^3He - ^4He dilution
refrigerator ($T \sim 50\text{mK}$)

$^6\text{LiD}/\text{NH}_3$
50/90% pol.
40/16% dil. f.

solenoid 2.5T
dipole magnet 0.5T
acceptance ± 180 mrad





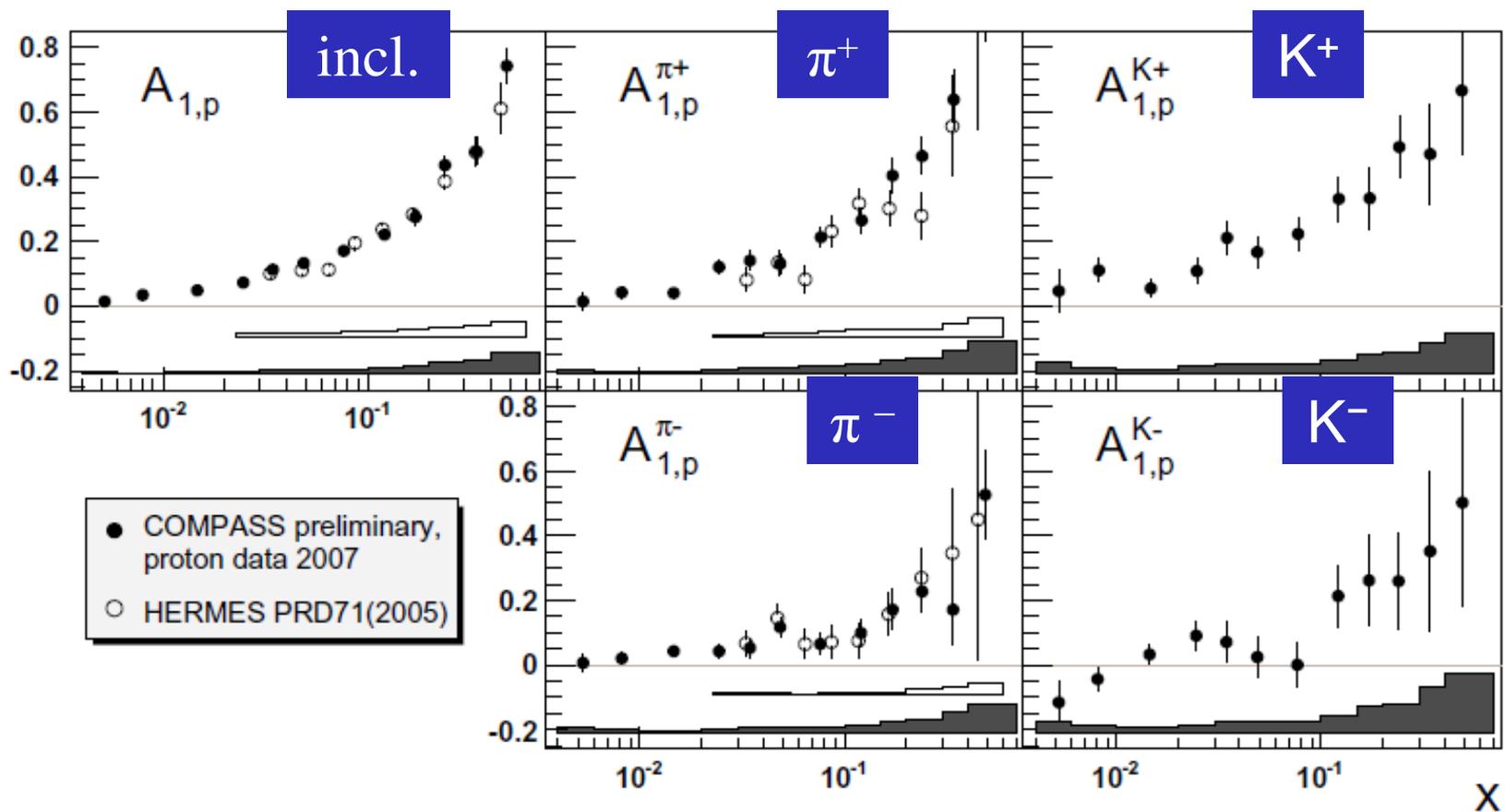
Helicity structure





Proton helicity structure

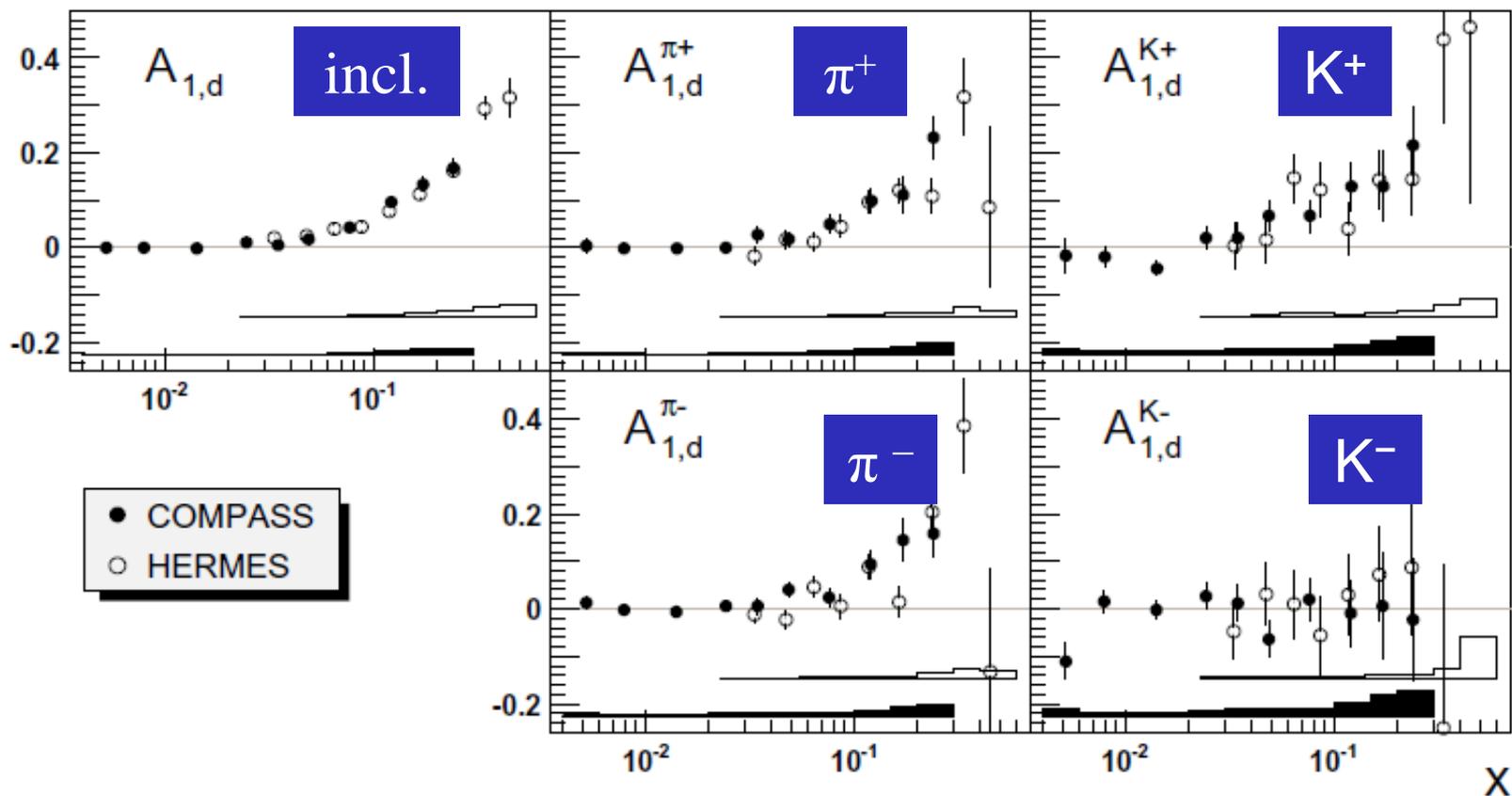
- incl. & semi-incl. asymmetries,
- first measurement of A^K





Deuteron helicity structure

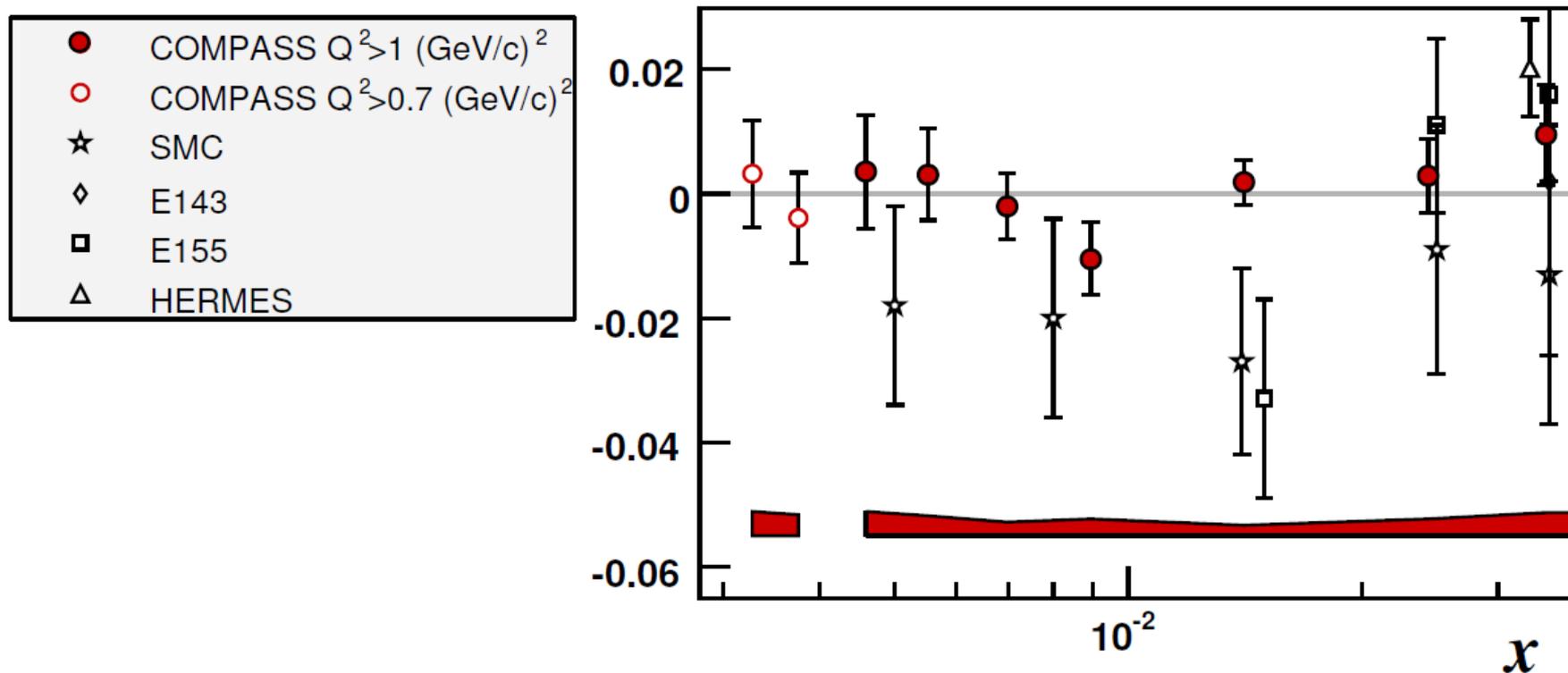
- incl. & semi-incl. asymmetries





Incl. deuteron asymmetry

- most precise measurement for $x < 0.03$ and $Q^2 > 1 \text{ GeV}^2$





Structure function $g_1(x, Q^2)$

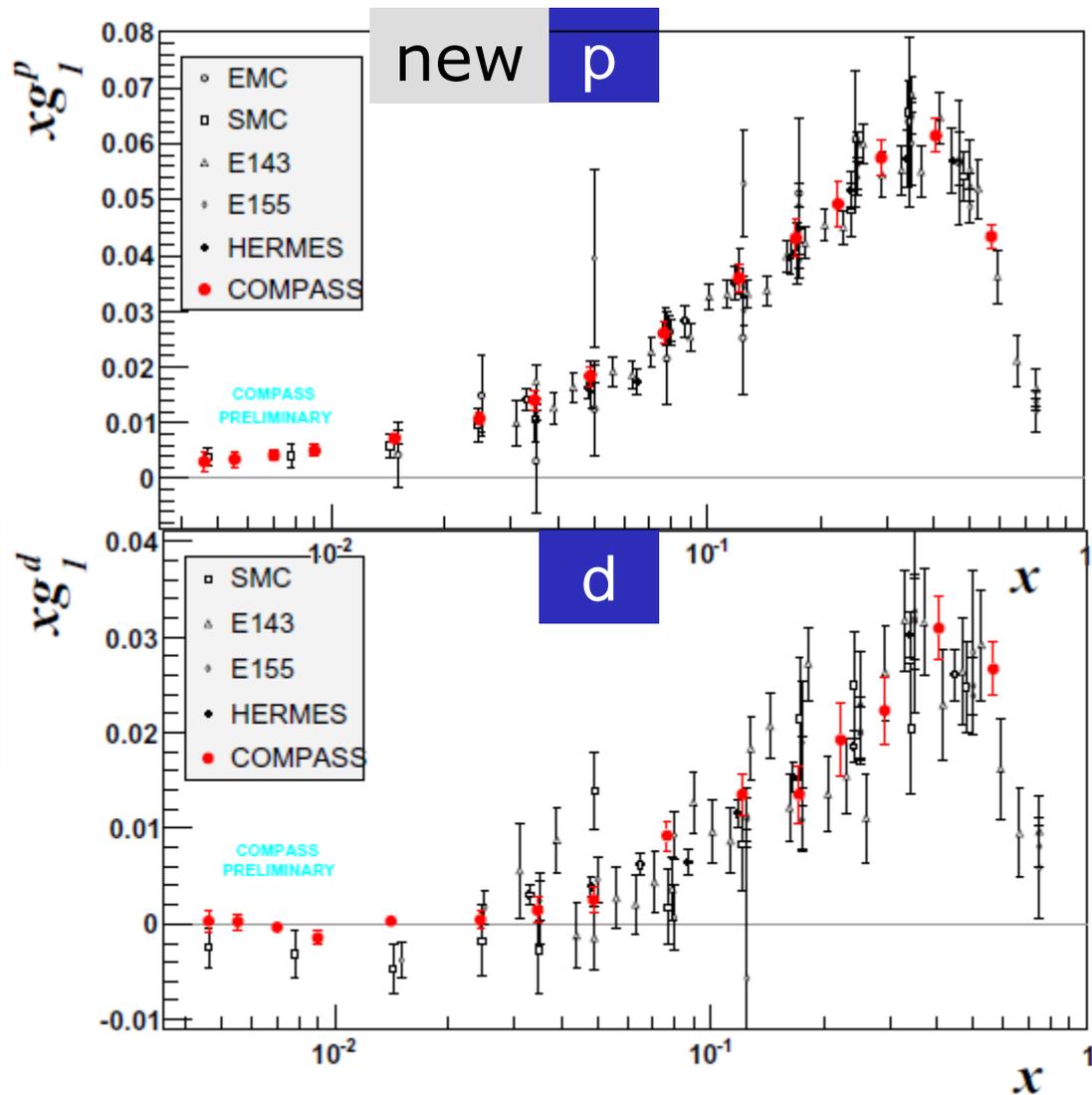
- very precise data
- only data below $x < 0.01$ ($Q^2 > 1$)

- deuteron data:

$$a_0 = \begin{matrix} 0.33 & 0.03 & 0.05 \\ \Delta s + \Delta \bar{s} \\ = -0.08 & 0.01 & 0.02 \end{matrix}$$

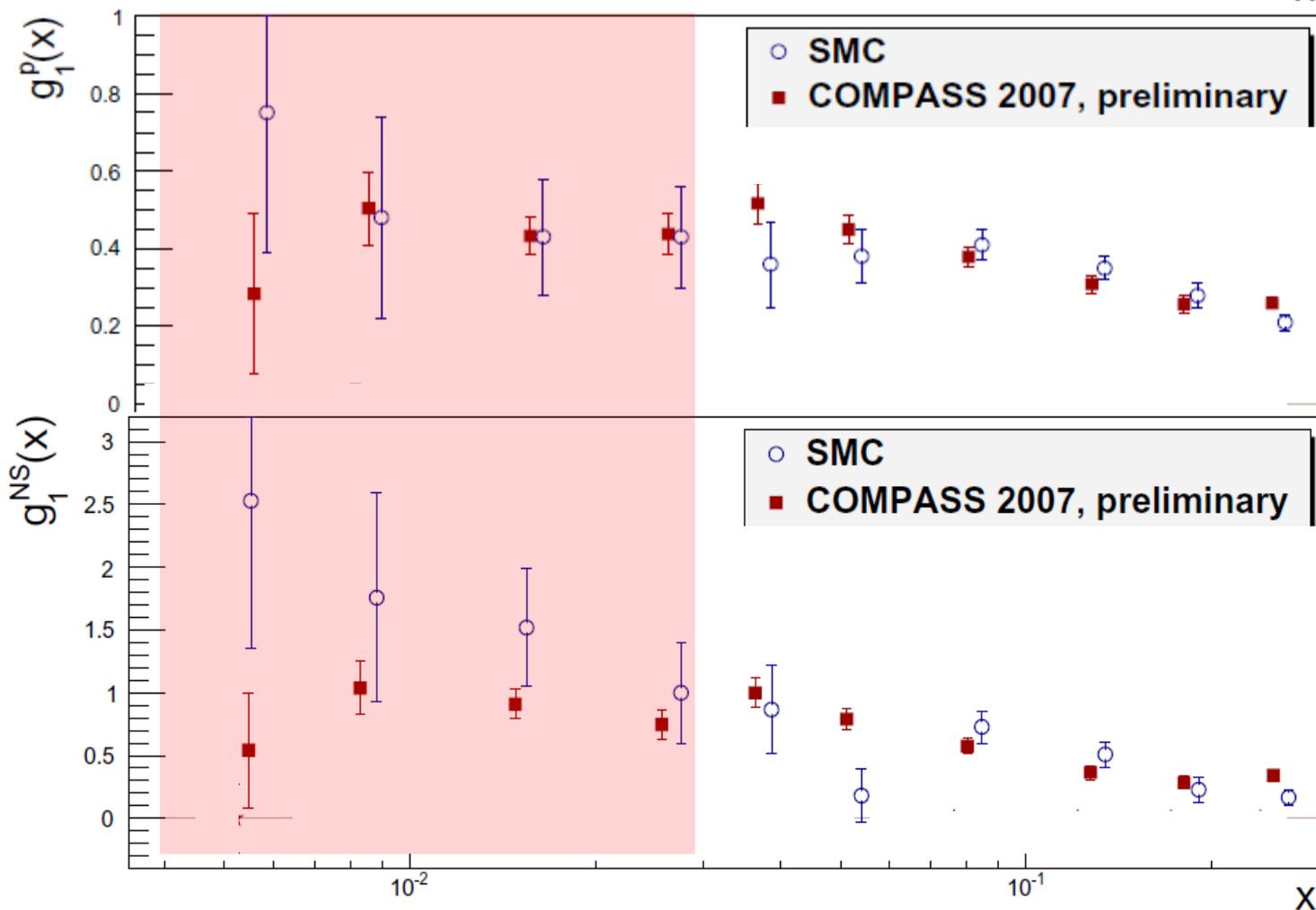
$$\begin{matrix} \Delta s + \Delta \bar{s} \\ = -0.08 & 0.01 & 0.02 \end{matrix}$$

(evol. to $Q^2 = \infty$)





g_1 proton and g_1^{NS}



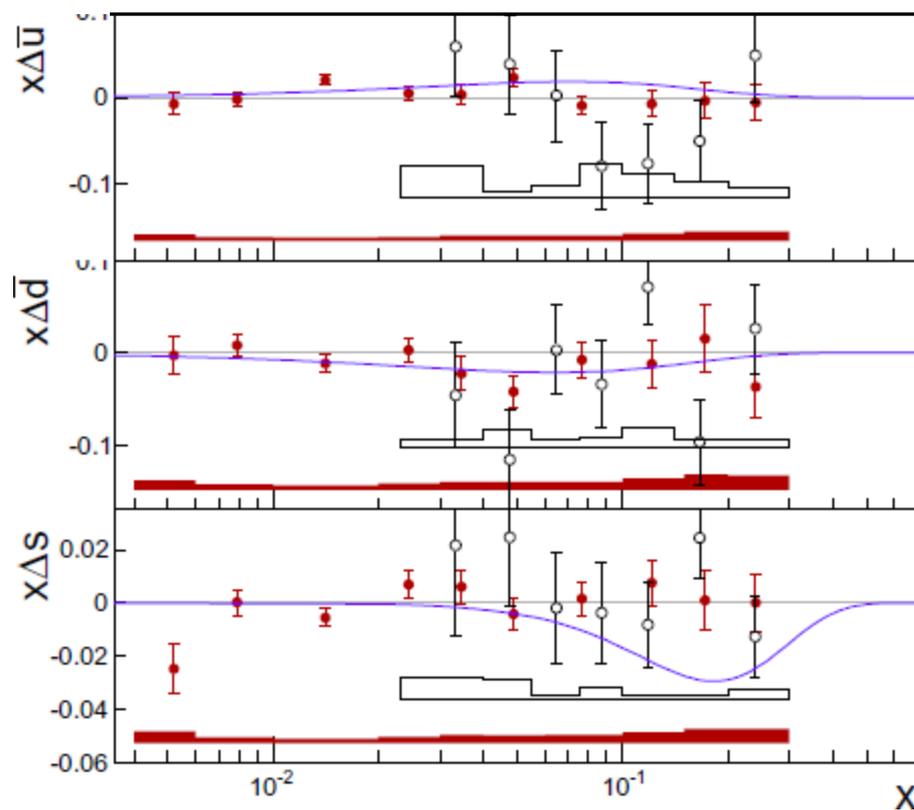
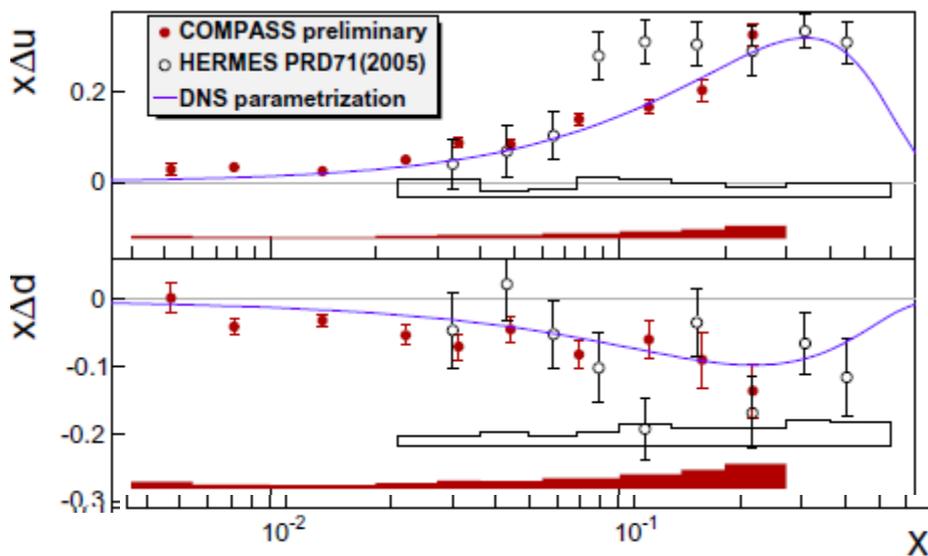
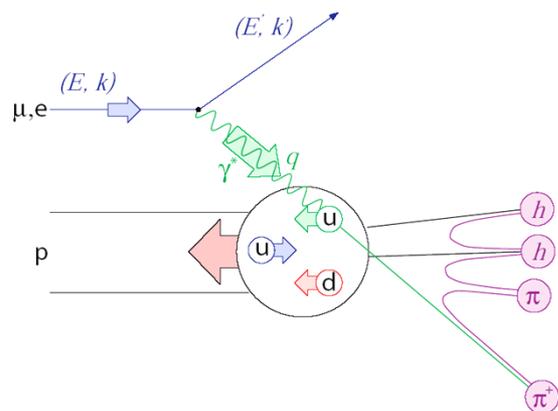
new





The role of quark flavours

LO semi-inclusive data analysis

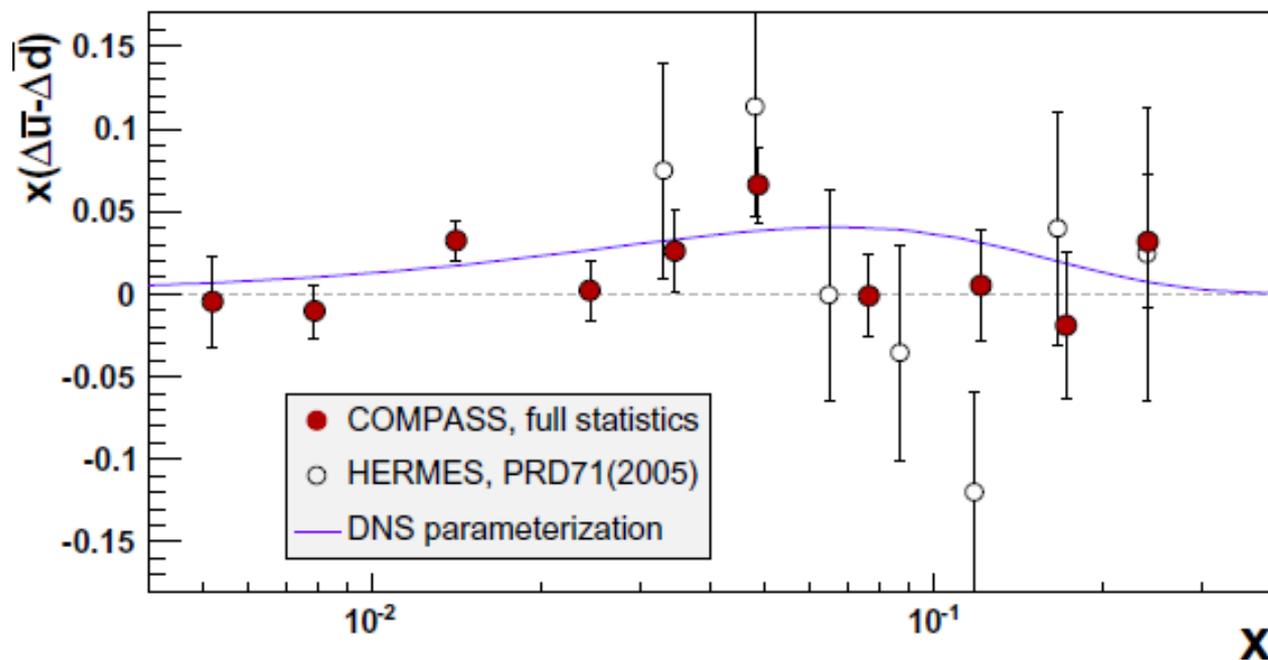




Flavour asymmetry?

$$\Delta\bar{u} - \Delta\bar{d}$$

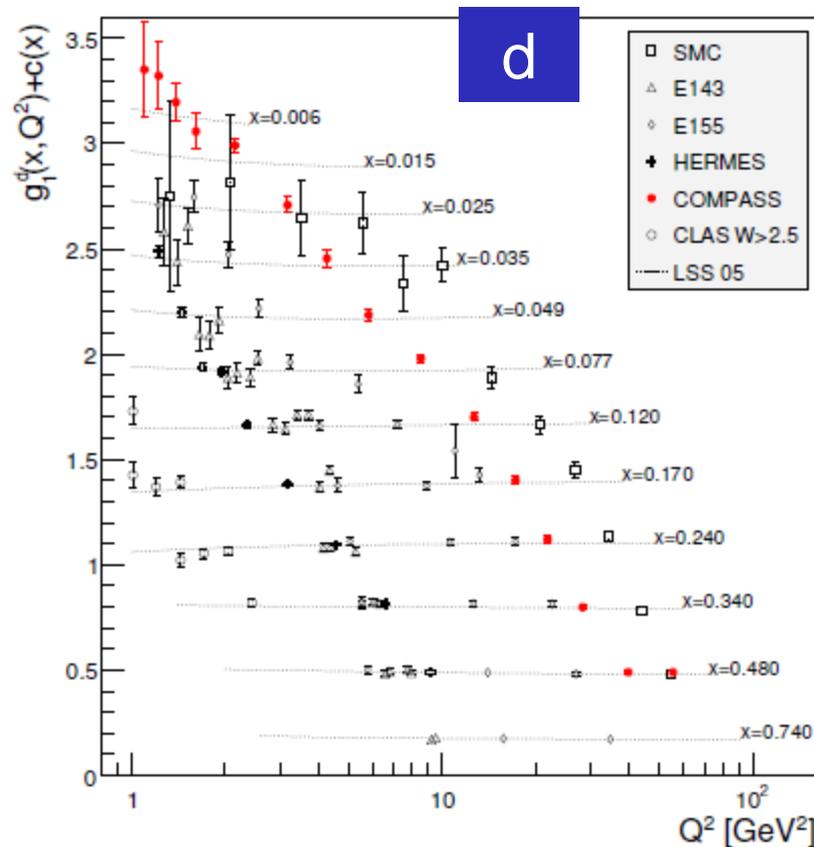
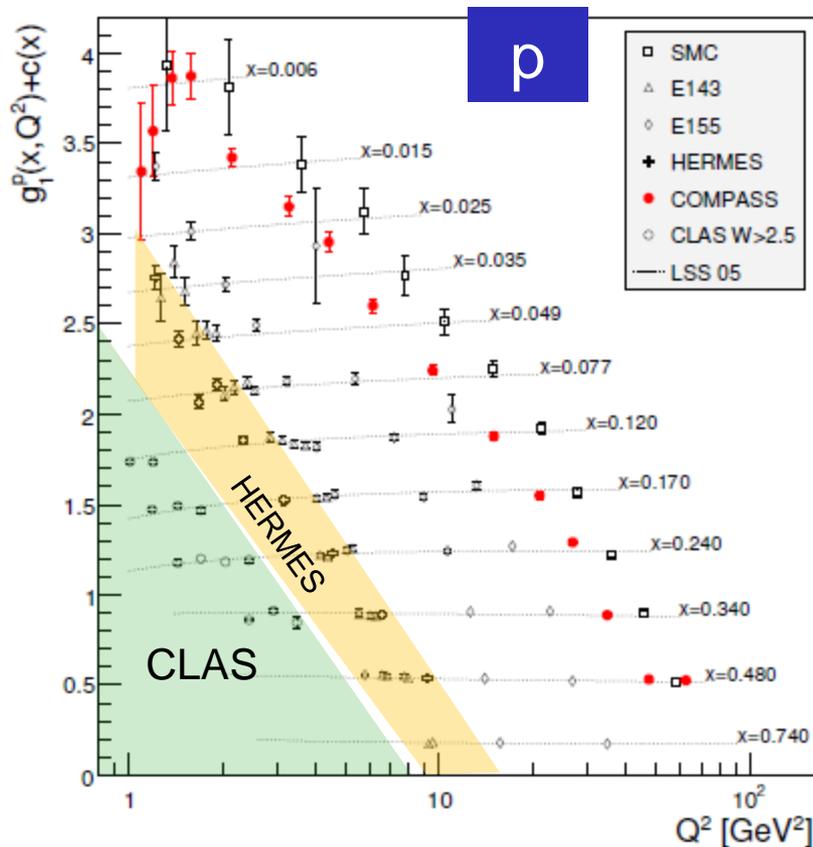
- considerable asymmetry in the unpolarised case
- model predicts naturally asymmetry for pol. case
- Rather small effect, $\bar{u} > \bar{d}$





QCD analyses

- Q^2 dependence g_1 or A_1 data described in QCD
- Nice data, but limited kinematic ranges (c.f. unpol. HERA)





Gobal NLO QCD analysis

$$\frac{d}{d \ln Q^2} \Delta q^{ns} = \Delta \mathcal{P}_{qq}^{ns} \otimes \Delta q^{ns}$$
$$\frac{d}{d \ln Q^2} \begin{pmatrix} \Delta q^s \\ \Delta g \end{pmatrix} = \begin{pmatrix} \Delta \mathcal{P}_{qq}^s & \Delta \mathcal{P}_{qg}^s \\ \Delta \mathcal{P}_{gq}^s & \Delta \mathcal{P}_{gg}^s \end{pmatrix} \otimes \begin{pmatrix} \Delta q^s \\ \Delta g \end{pmatrix}$$

DGLAP

- choose scheme ($\overline{\text{MS}}$, AB, jet) and Q_0^2
- optionally fix ns moments from hyperon decays (a_3, a_8)
- fit PDFs for quark non-singlet and **singlet** and **gluon** to data
- extra problems in polarized case
 - no positivity condition, no momentum sum rule

- Recent analyses include semi-inclusive and RHIC data

- DSSV 2009

arXiv:0904.3821

- Hirai, Kumano

arXiv:0808.0413

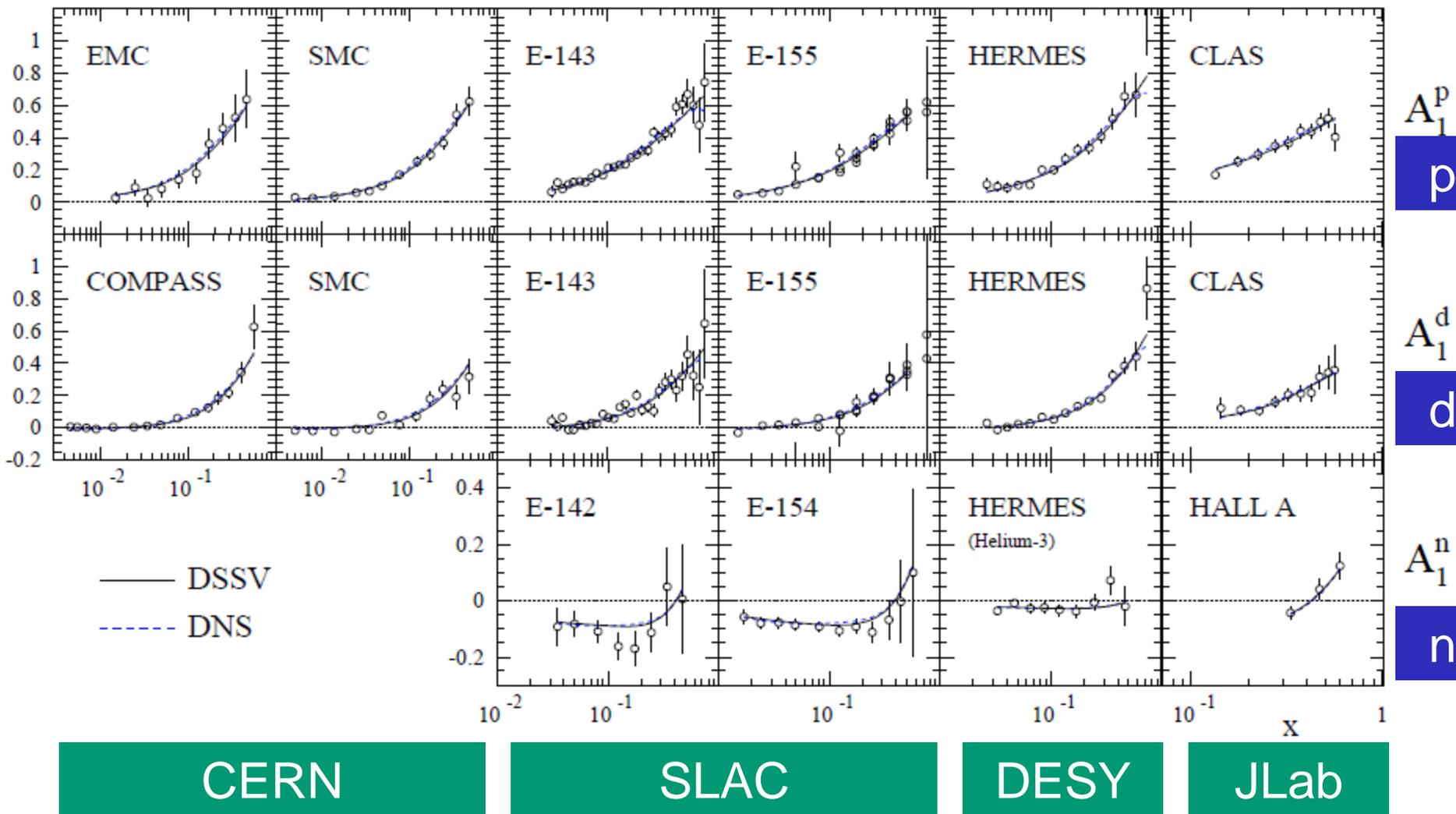


Global NLO QCD analyses

- Recent analyses of DIS and RHIC data
 - **DSSV 2009** [arXiv:0904.3821](https://arxiv.org/abs/0904.3821)
DIS and SIDIS data,
RHIC π^0 and inclusive jets
 - **Hirai, Kumano** [arXiv:0808.0413](https://arxiv.org/abs/0808.0413)
DIS data,
RHIC π^0 data
- Pol. gluon PDFs with node allowed
- Detailed studies of systematic uncertainties
- SIDIS data very sensitive to used fragmentation functions
- “PGF” hadron data not yet included (s. below)



DSSV fit to inclusive asymmetries

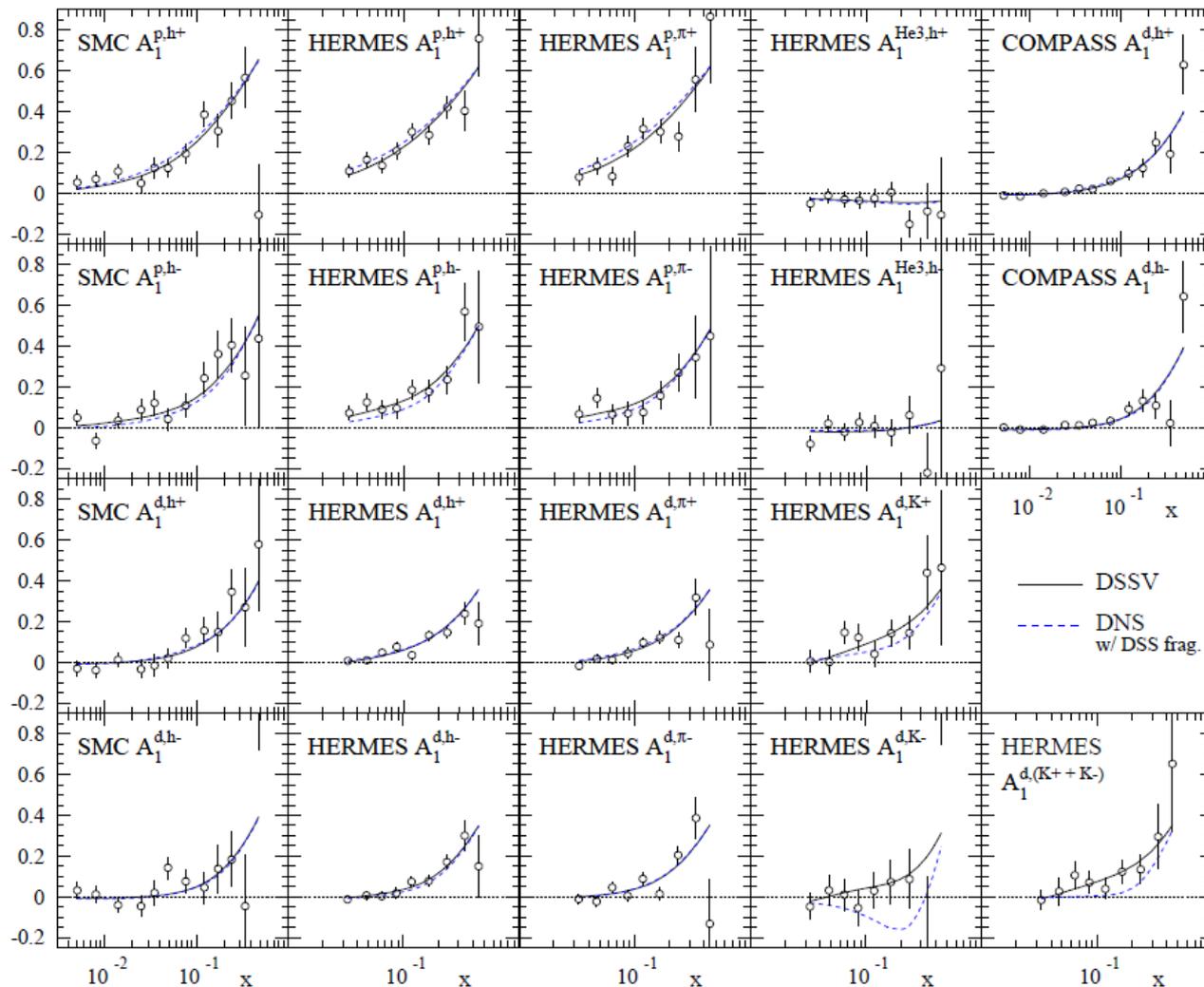




DSSV (semi-inclusive data)

- Most data from HERMES
- COMPASS proton data not yet in
- DSS fragmentation functions

PRD 75, 114010
PRD 76, 074033

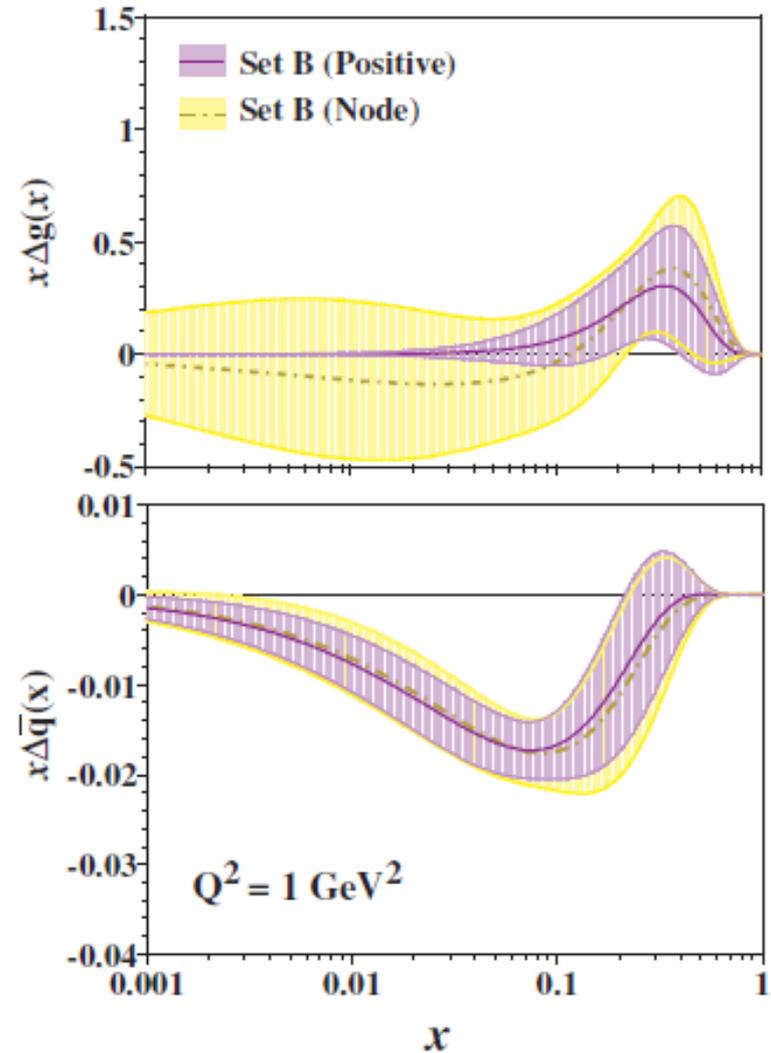
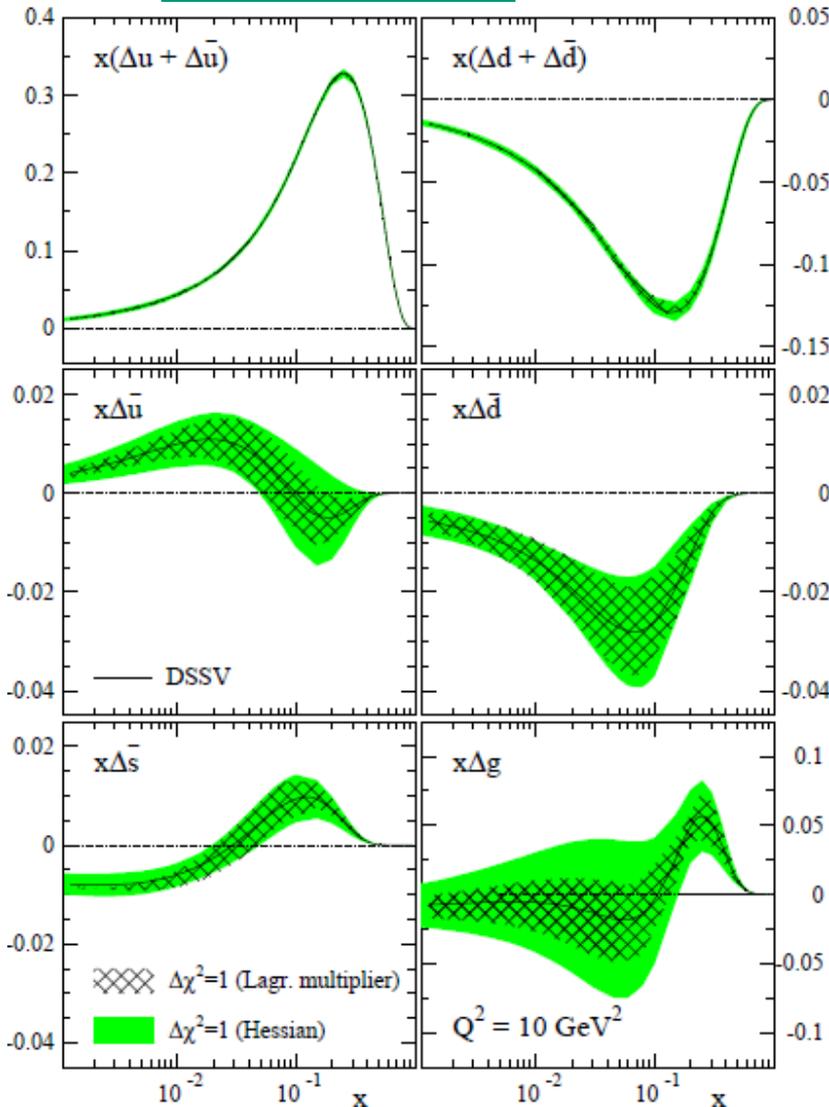




PDFs from global analyses

DSSV

Hirai, Kumano





Global analyses

- Gluon polarization still poorly known but much smaller than expected in axial anomaly scenario for solving the spin puzzle.
- Gluons can still make a major contribution to the nucleon spin.
- Many analyses indicate the possibility of a node around $x=0.1$ in $\Delta g(x)$
- Quark distributions well determined (apart from anti-quarks)
- Strange quark distribution is indeed strange: SIDIS data prefer $\Delta s > 0$ ($x > 0.01$) while incl data require with SU3 the first moment to be $\sim -0.1 \Rightarrow$ node in DSSV



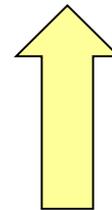
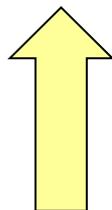
Angular momentum of the nucleon

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_z$$

quarks

gluons

orbital



small ~ 0.15

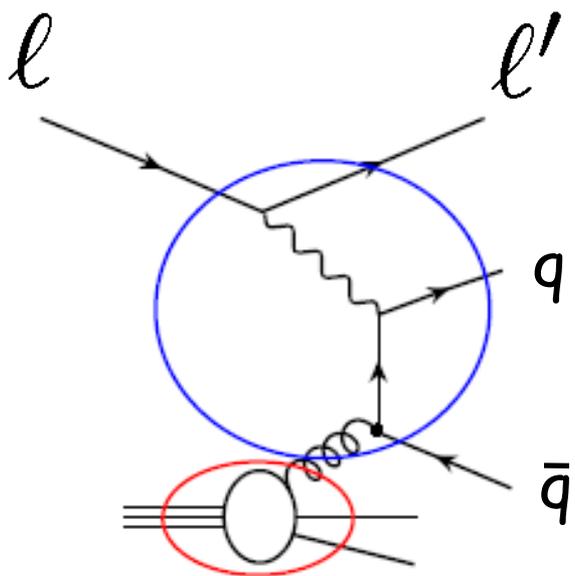
unknown

Still poorly known



Gluon polarization from PGF

Principle: Gluon polarisation enters via
photon-gluon fusion (PGF)



$$A_{||} = R_{pgf} \langle \hat{a}_{pdf} \rangle \left\langle \frac{\Delta g}{g} \right\rangle$$

- measure $A_{||}$
- calculate R_{pgf} , $\langle \hat{a}_{pgf} \rangle$ and background by Monte Carlo



Analysed channels

analysed data sets:

– high- p_T hadron pairs (no ID, pions/kaons)

- $Q^2 > 1 \text{ GeV}^2$

LEPTO



- $Q^2 < 1 \text{ GeV}^2$ / unmeasured 

PYTHIA



– high- p_T single hadron

- small Q^2 / unmeasured



PYTHIA



– single charmed meson

- quasi-real photons

AROMA, RAPGAP



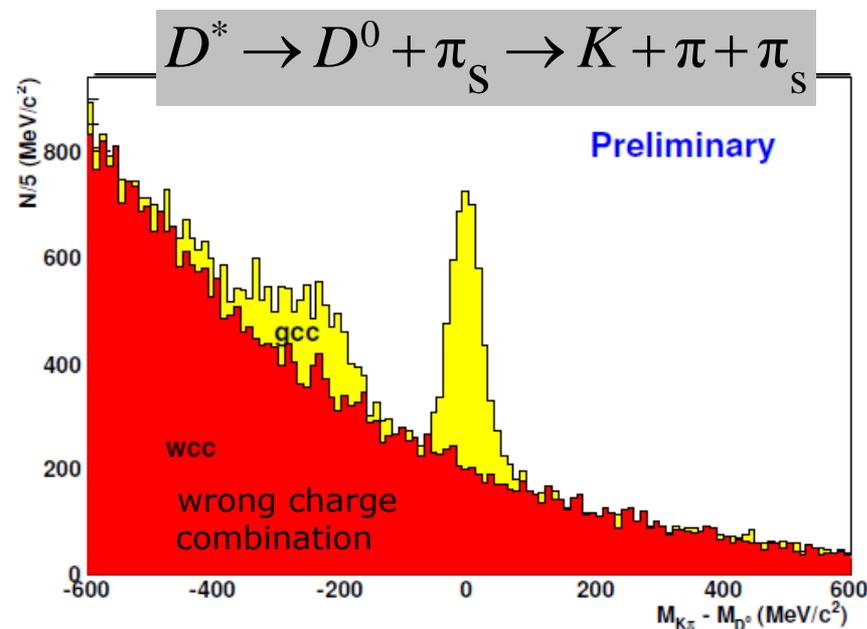
All analyses in LO till now (plus parton showers)



$\Delta g/g$ from open charm

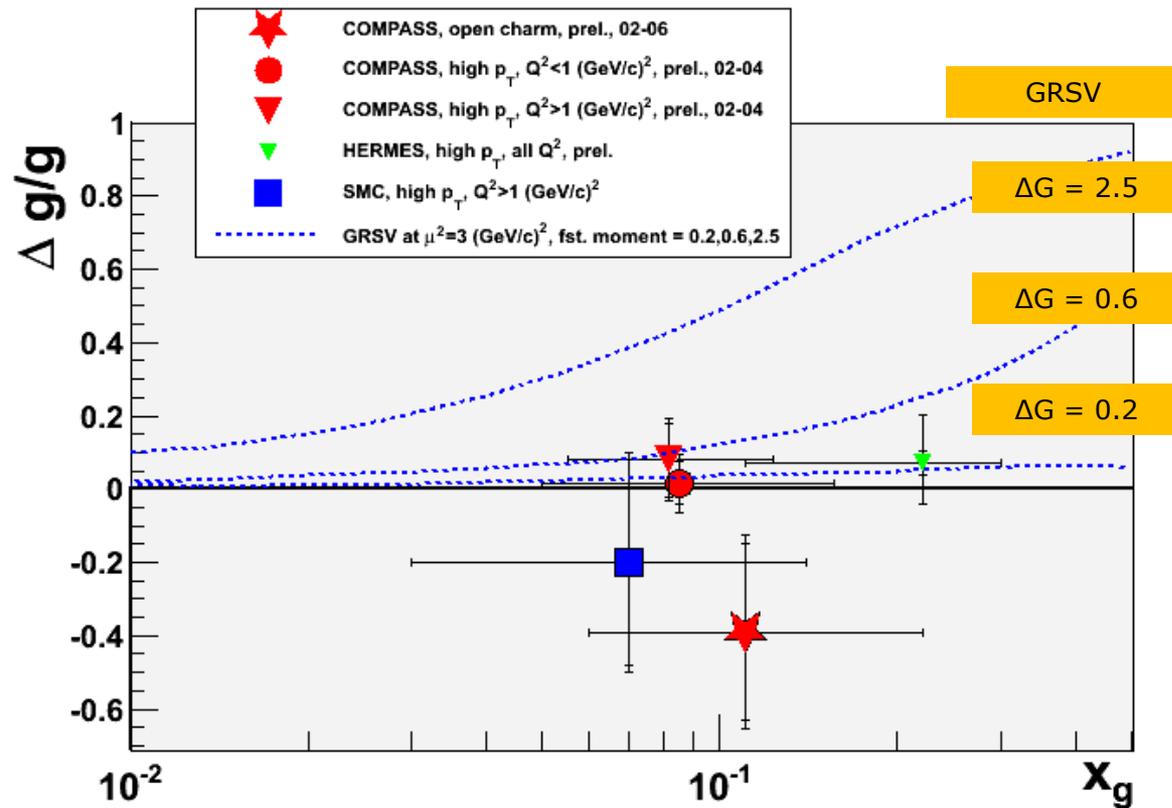
- Little physics background (LO, QCDC)
- Statistics limited, $D \rightarrow \pi K$ (BR $\sim 4\%$)
- Large combinatorial background, drastically reduced in D^* channel with slow π_s
- All **deuteron** data
- new channels in D^* sample
 - sub-threshold kaons
 - 3-body decay with non-observed π^0 (bump)

$$\langle \Delta g/g \rangle_x = -0.39 \pm 0.24 \text{ (stat.)}$$

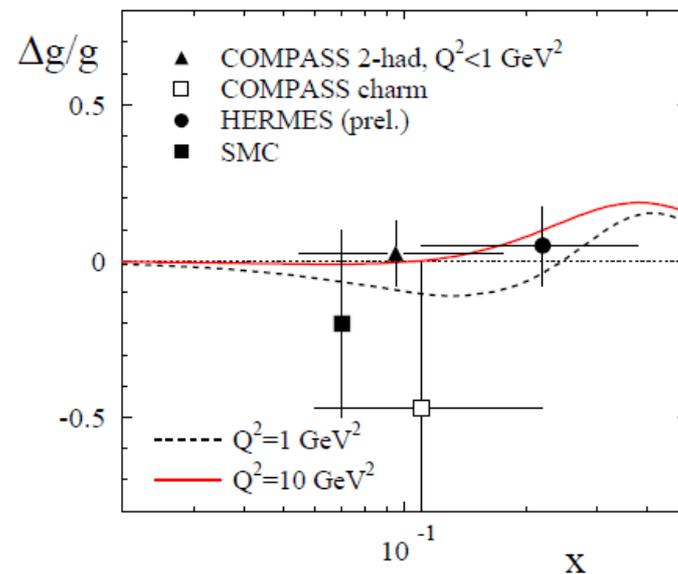




Gluon Polarization from LO PGF



Comparison with NLO DSSV





Transverse spin structure





Transversity PDF $\Delta_T^0 D_q^h$ or h_1

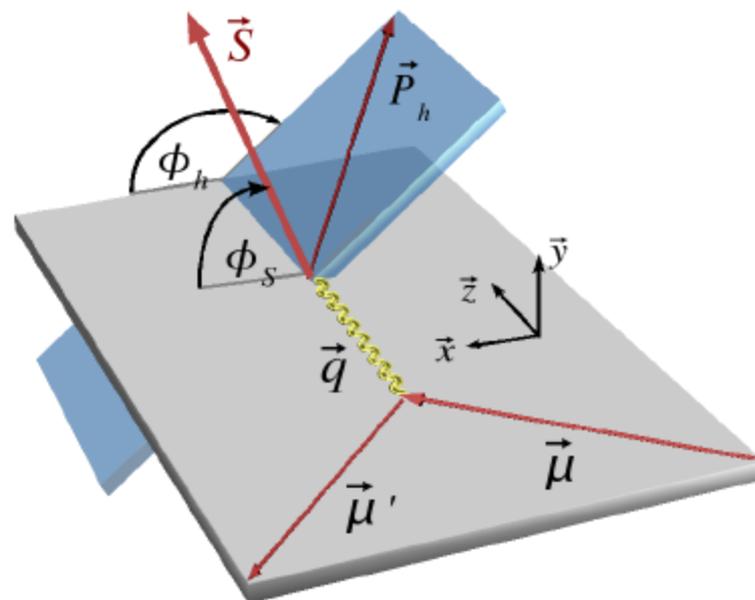
Couple $\Delta_T q$ to chiral odd Collins FF $\Delta_T^0 D_q^h$

$$A_{Coll} = \frac{\sum_q e_q^2 \Delta_T q(x) \Delta_T^0 D_q^h(z, p_T^h)}{\sum_q e_q^2 q(x) D_q^h(z, p_T^h)}$$

Azimuthal cross-section asymmetry:

$$\frac{\Delta\sigma}{\sigma} \propto A_{Coll} \sin \Phi_C$$

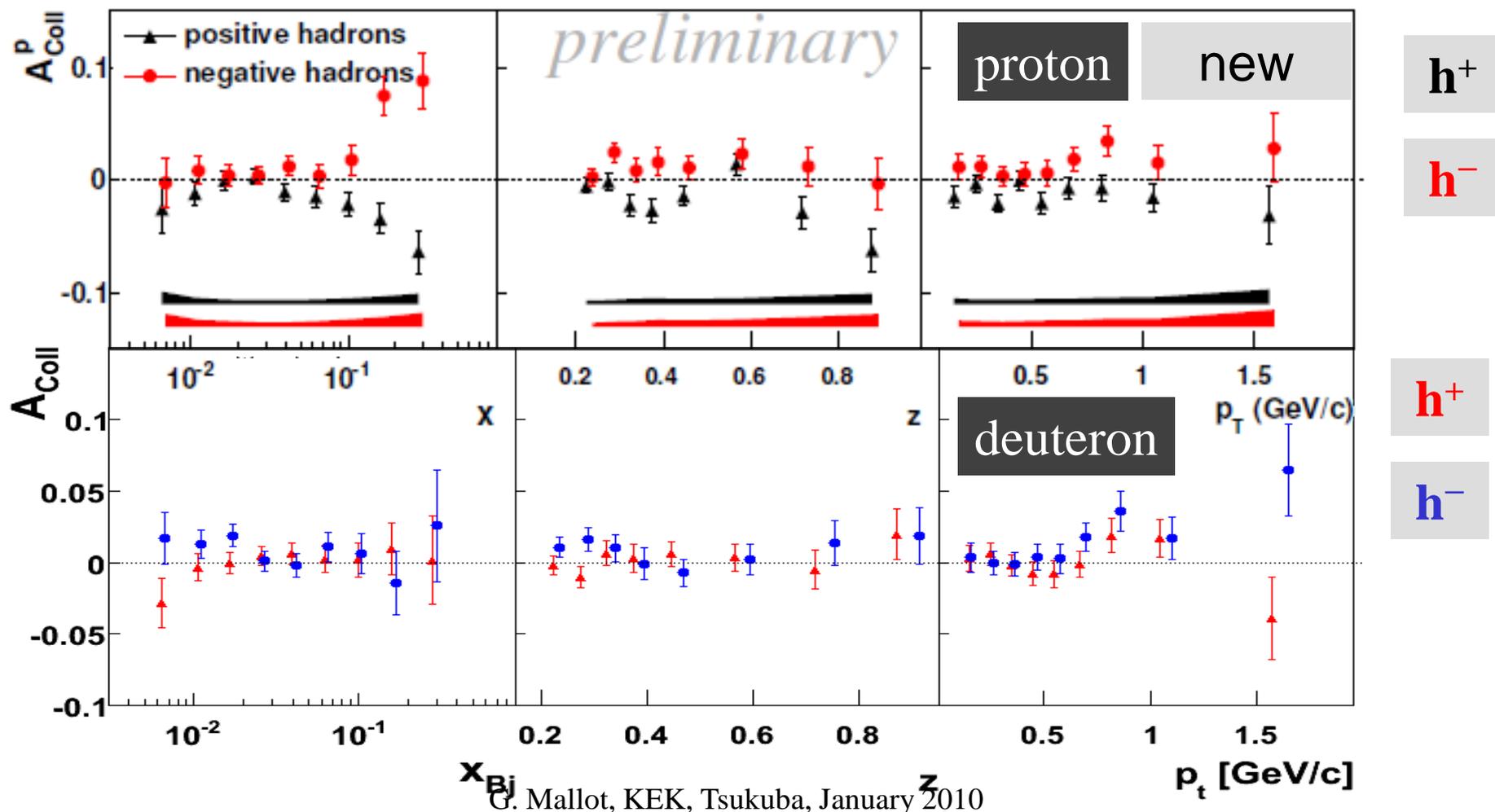
$$\Phi_C = \phi_h - \phi_s - \pi$$





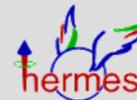
Collins Asymmetries

New from COMPASS: full 2007 proton data set (statistics tripled)

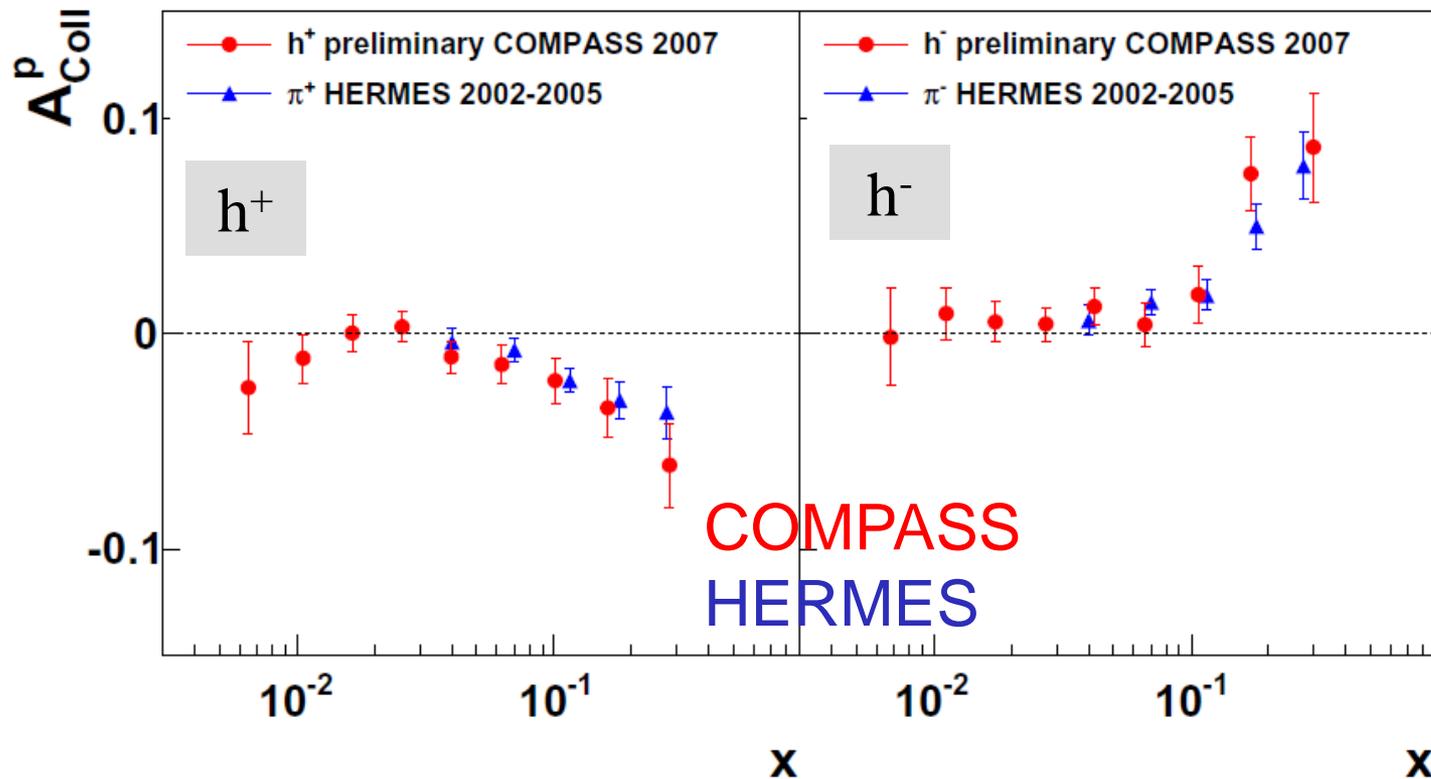




Comparison



proton



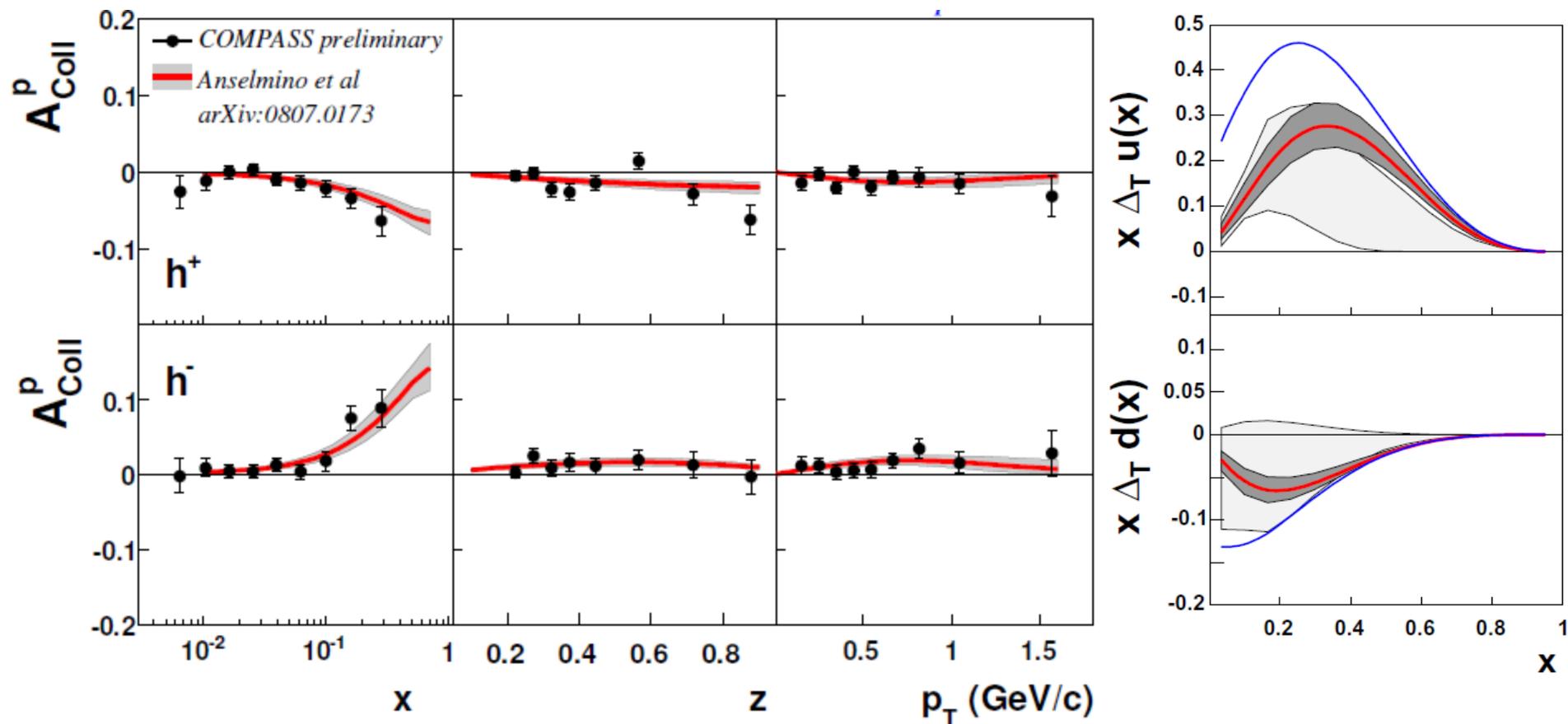
sign change and $D_{nn} \cong y$ applied for HERMES data

- large asymmetry $\sim 10\%$
- good agreement in common x range
- zero deuteron result important \Rightarrow opposite sign of u and d quark transversity PDF



Global Fit

Fit to COMPASS d , HERMES, BELLE (FF, e^+e^-)
in good agreement with new proton data





Transversity PDF $\Delta_T q(x)$

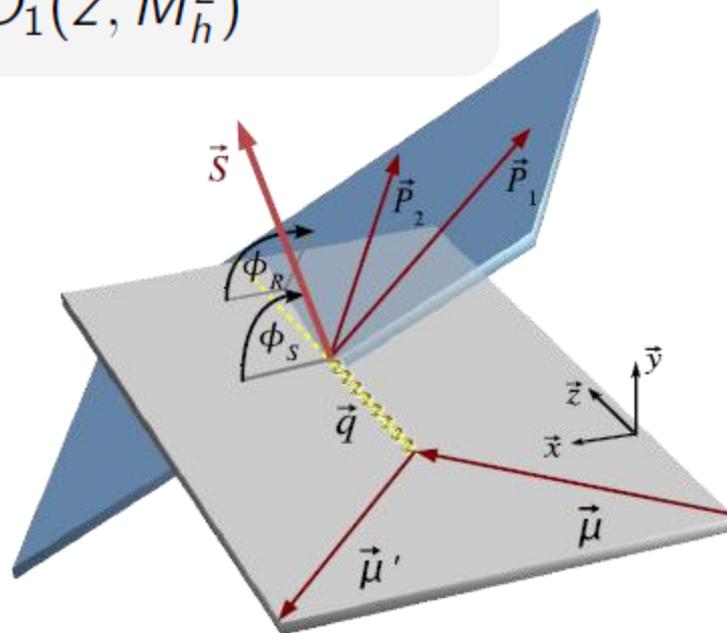
Alternative: couple $\Delta_T q$ to chiral odd 2-hadron interference FF H_1^\triangleleft

$$A_{RS} \propto \frac{\sum_q e_q^2 \Delta_T q(x) H_1^\triangleleft(z, M_h^2)}{\sum_q e_q^2 q(x) D_1(z, M_h^2)}$$

cross-section
asymmetry:

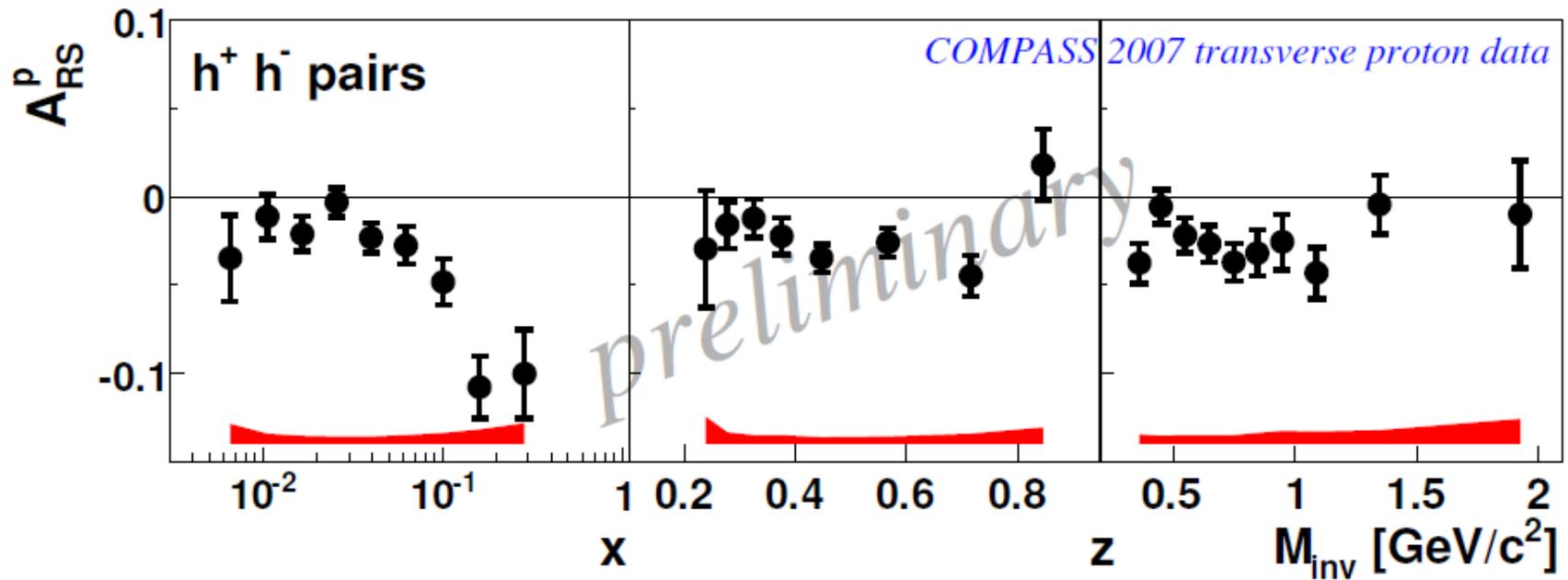
$$\frac{\Delta\sigma}{\sigma} \propto A_{RS} \sin \phi_{RS} \sin \theta$$

$$\phi_{RS} = \phi_R + \phi_S - \pi; \quad \sin \theta \simeq 1$$





two-hadron asymmetry

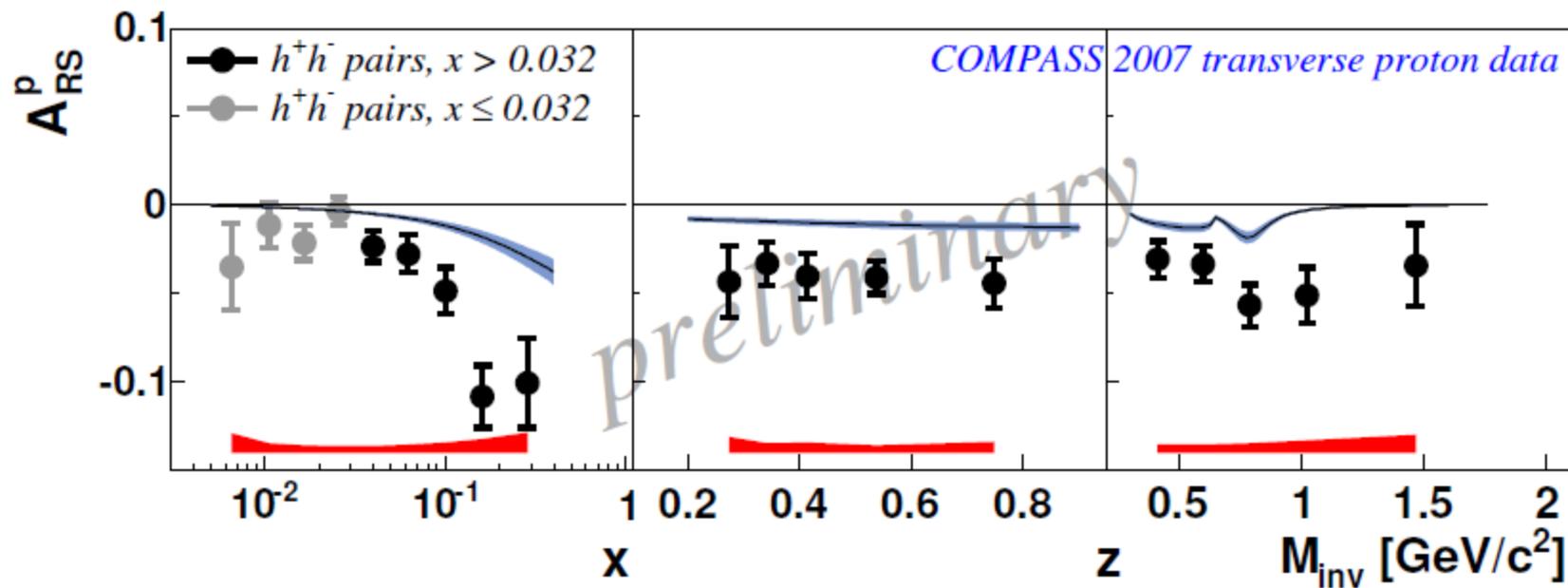


- large asymmetries
- interference FF and transversity sizable



Comparison to a recent Fit

- Recent fit (dominated by HERMES, COMPASS p not yet in)



Very recent prediction (Bacchetta, Radici Phys.Rev.D79:034029,2009)



Sivers function $\Delta_0^T q$ or f_{1T}^\perp

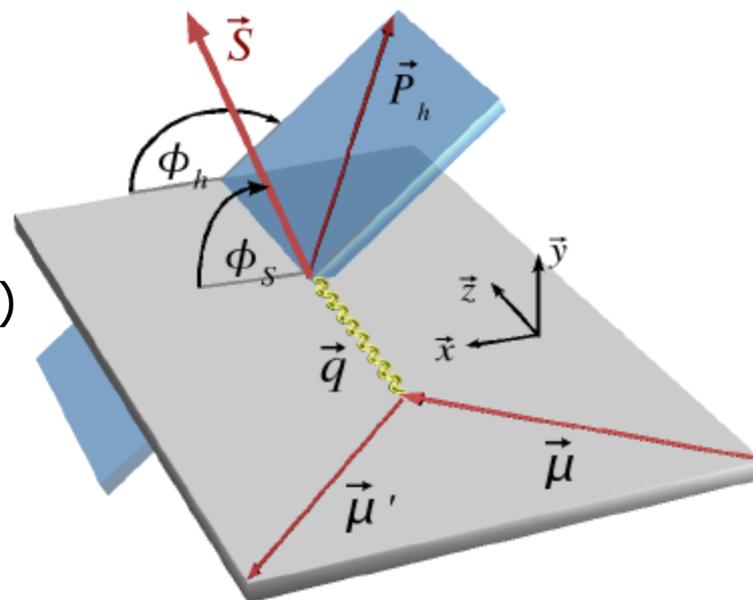
Sivers Asymmetry:

$$A_{Siv} = \frac{\sum_q e_q^2 \Delta_0^T q(x, p_T^h/z) D_q^h(z)}{\sum_q e_q^2 q(x, p_T^h/z) D_q^h(z)}$$

$$\frac{\Delta\sigma}{\sigma} \propto A_{Siv} \sin \Phi_S$$

$$\Phi_S = \phi_h - \phi_S$$

- proposed (1990, Sivers)
- thought to vanish (1993, Collins)
- resurrected (2002, Brodsky, Hwang, Schmitt)
- different sign in DY and SIDIS



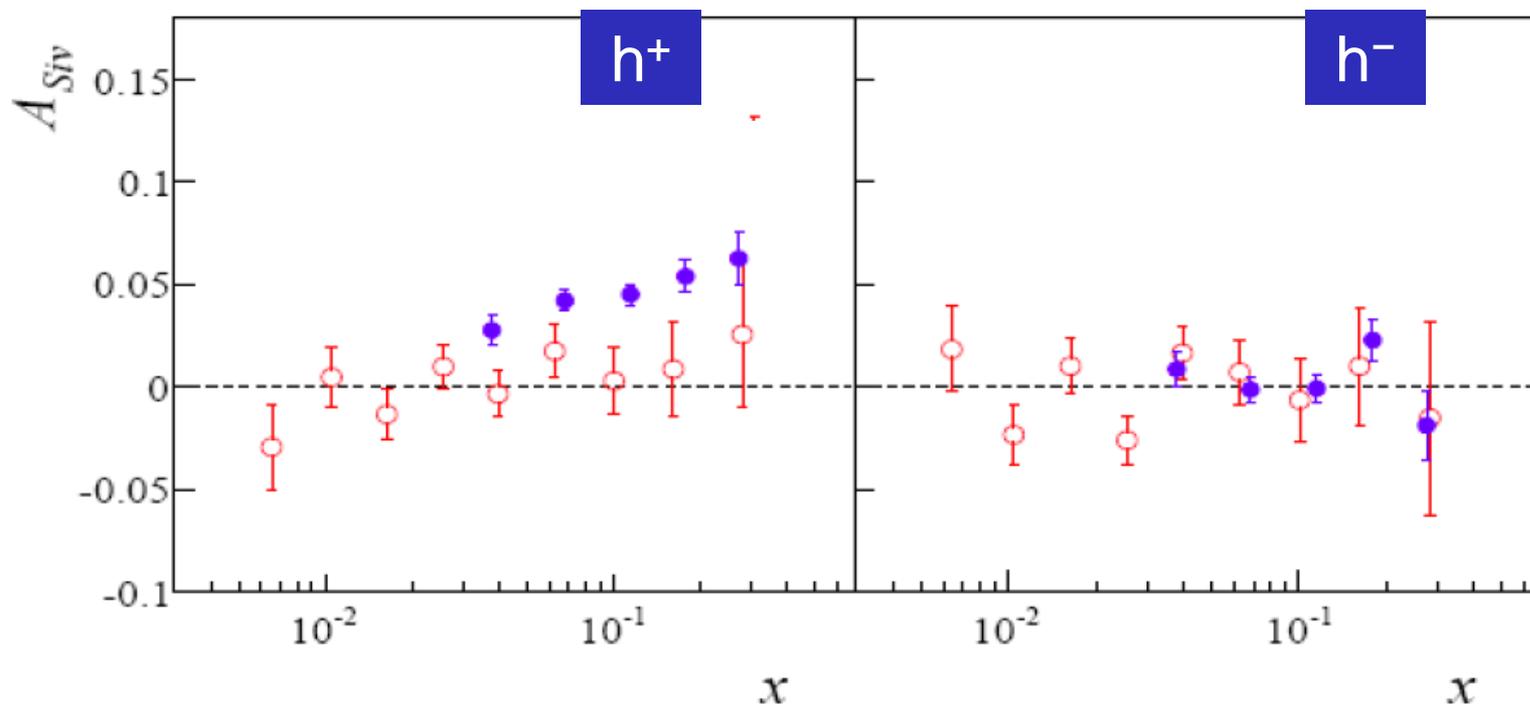


Proton Sivers Asymmetry

- compatible with zero for the deuteron
- large effect seen by HERMES, not confirmed by COMPASS
- clarification needed

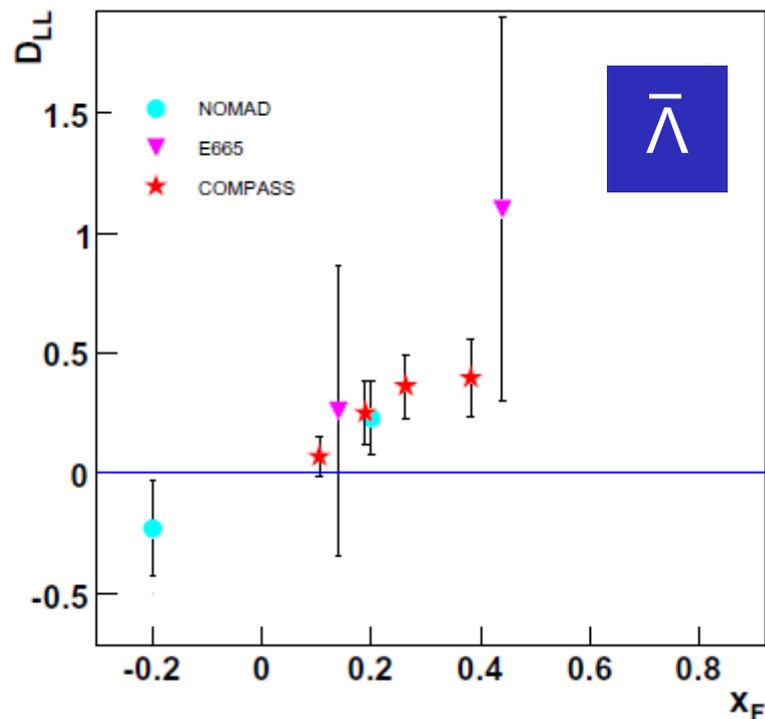
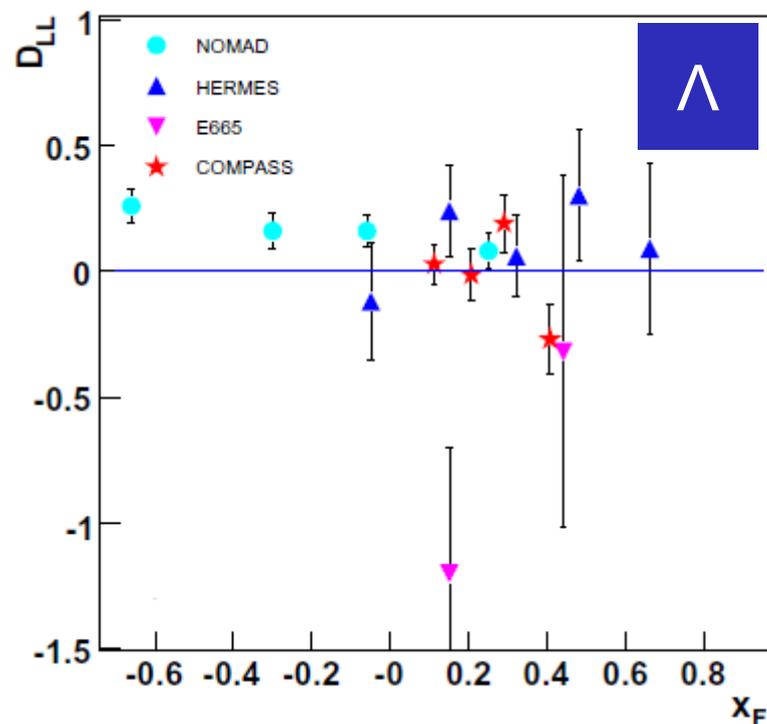
○ COMPASS 2007

● HERMES 2002-2005





Longitudinal spin transfer to Λ & $\bar{\Lambda}$



- non-zero D_{LL} related to polarisation of strange (anti) quarks (?)



Outlook

Goals: Precise determination of $\Delta g(x)$
Generalized parton distributions (GPD)
Orbital angular momentum

Experimental prospects:

Short term: More lepton data from COMPASS & Jlab
More hadron data from RHIC (500 GeV!)

Longer term: COMPASS GPD & DY programme
RHIC upgrade
JLab 12 GeV

Long term: Electron-Ion Colliders: eRHIC, ELIC, ENC