

# Tests of Chiral Perturbation Theory in Primakoff Reactions at COMPASS

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*for the COMPASS collaboration*

SPIN-PRAHA-2010  
July 20

supported by: Maier-Leibnitz-Labor München,  
Excellenzcluster: Origin and Structure of the Universe, BMBF



Bundesministerium  
für Bildung  
und Forschung

 Outline

- Introduction: QCD and ChPT
- COMPASS at the CERN SPS
- Primakoff reactions
  - chiral anomaly
  - 3-pion final state
  - [ pion polarisabilities → dedicated talk by Alexey Guskov]

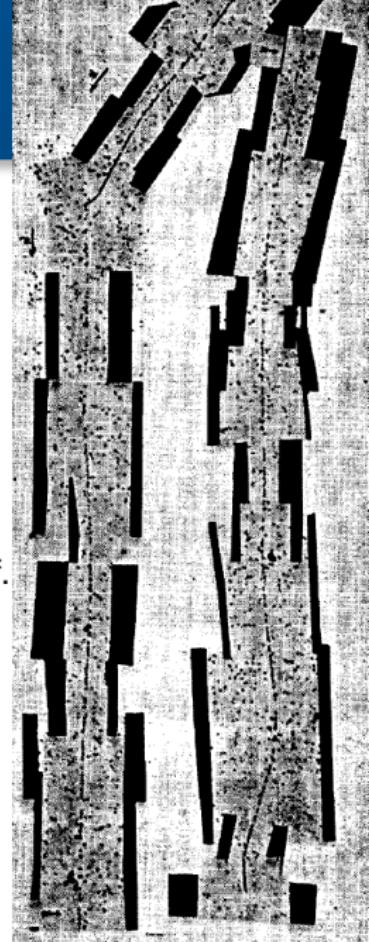


# The strong force, the pion and $\chi$ PT

- Yukawa's particle of the strong force
- development of QCD: quarks and gluons
- running coupling parameter, confinement
- $m_q \approx 0 \rightarrow$  chiral symmetry  
(spontaneously broken)

$$SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$$

- series expansion of QCD in particle momenta, inner d.o.f.  
are “condensed” into Low Energy Constants
- $\pi^+ \pi^\circ \pi^-$  (re-)appear as Goldstone bosons



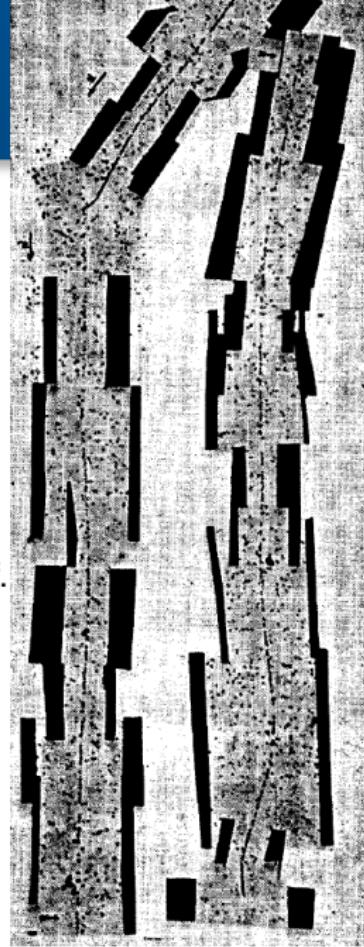


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# ChPT and Experiment

- Pion scattering lengths: 2-loop predictions

- $a_0^0 m_{\pi^+} = 0.220 \pm 0.005$  confirmed in  
 $K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$  (E865)
- $(a_0^0 - a_0^2) m_{\pi^+} = 0.264 \pm 0.006$  confirmed in  
 $K^+ \rightarrow \pi^+ \pi^\circ \pi^\circ$  (NA48:  $0.268 \pm 0.010$ )

- Electromagnetic structure

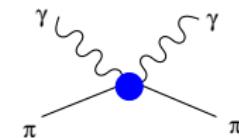
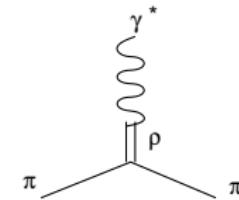
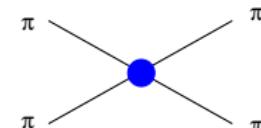
- Form factor described by coupling to  $\rho(770)$  (resonance effect, VMD)
- Polarisability

accessible as contribution to Compton scattering;  
prediction obtained by the LEC relation to  $\pi^+ \rightarrow e^+ \nu_e \gamma$

$$\alpha_\pi + \beta_\pi = (0.2 \pm 0.1) \cdot 10^{-4} \text{fm}^3$$

$$\alpha_\pi - \beta_\pi = (5.7 \pm 1.0) \cdot 10^{-4} \text{fm}^3$$

[Gasser, Ivanov, Sainio, Nucl. Phys. B745, 2006]

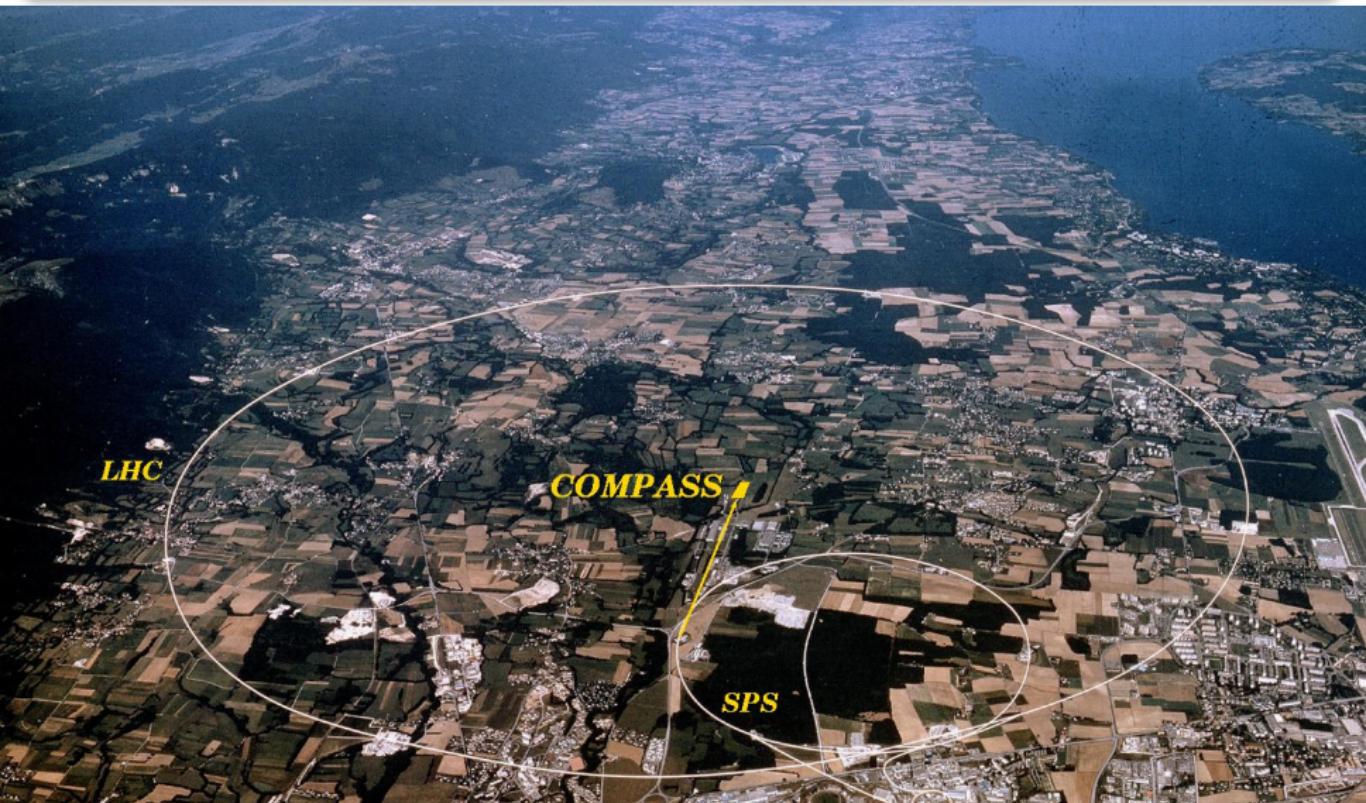




# COmmon Muon and Proton Apparatus for Structure and Spectroscopy



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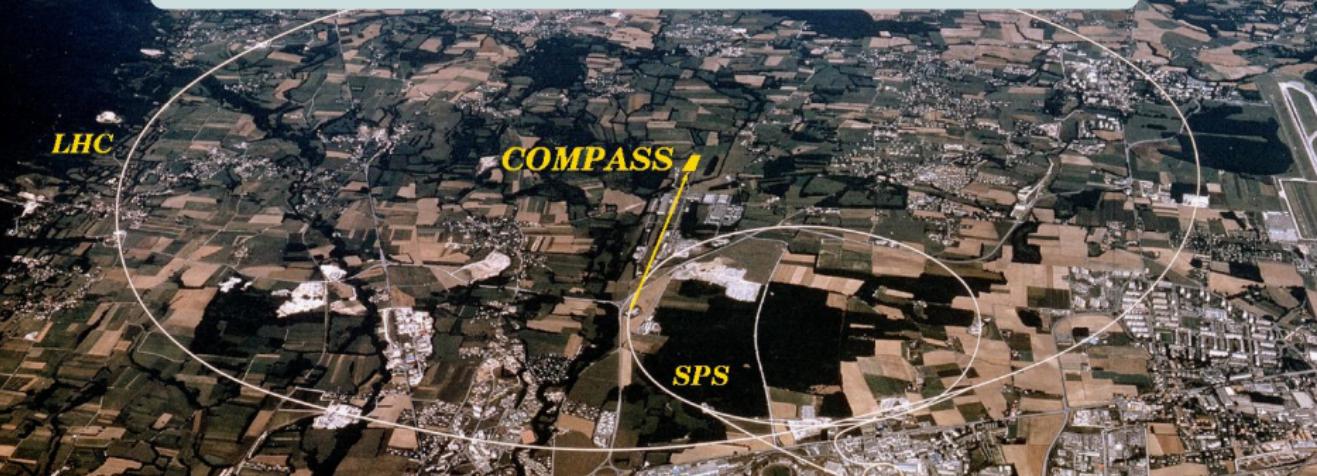




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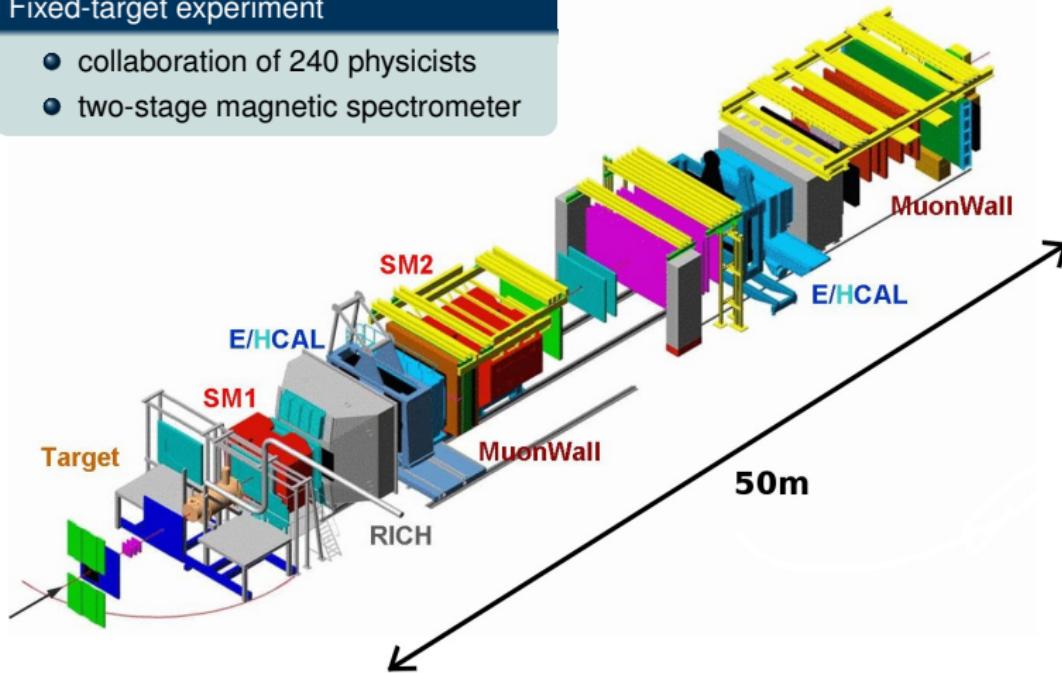
CERN SPS: protons  $\sim 400$  GeV

- tertiary muons:  $4 \cdot 10^7$  / s      (5 s spills)  
2002-04, 2006-07, 2010-11: spin structure of the nucleon
- secondary  $\pi, K, (\bar{p})$ :  $2 \cdot 10^7$  / s  
Nov. 2004, 2008-09: hadron spectroscopy



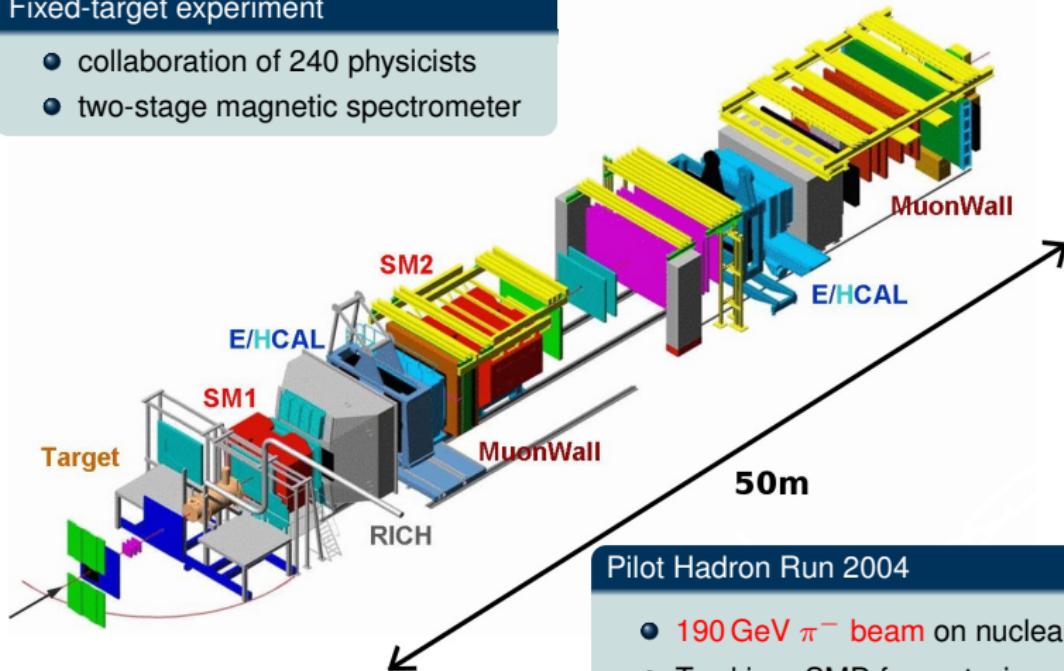
## Fixed-target experiment

- collaboration of 240 physicists
- two-stage magnetic spectrometer



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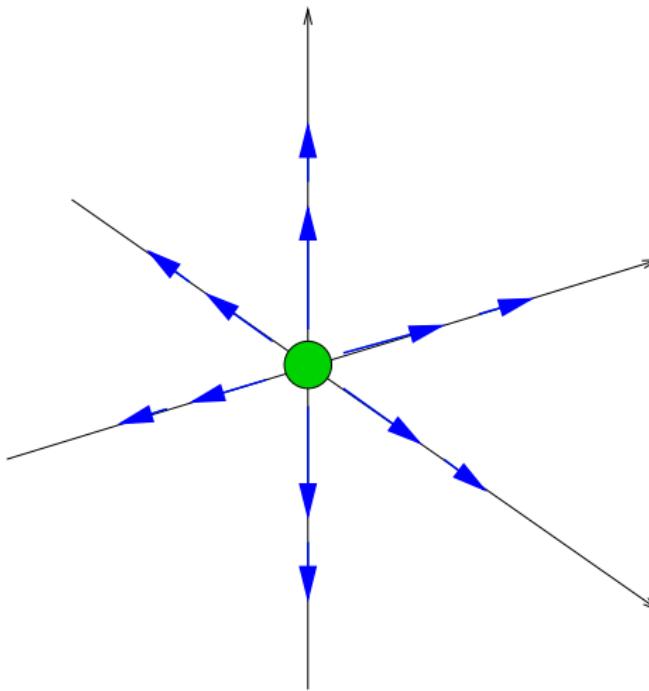


## Pilot Hadron Run 2004

- 190 GeV  $\pi^-$  beam on nuclear targets
- Tracking: SMD for vertexing
- Trigger: Multiplicity trigger, ECAL trigger

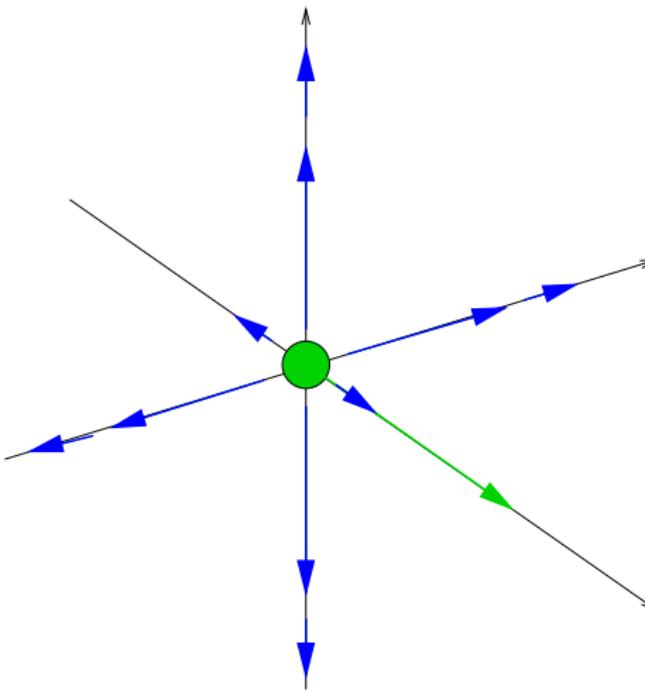


## Electric charge at rest



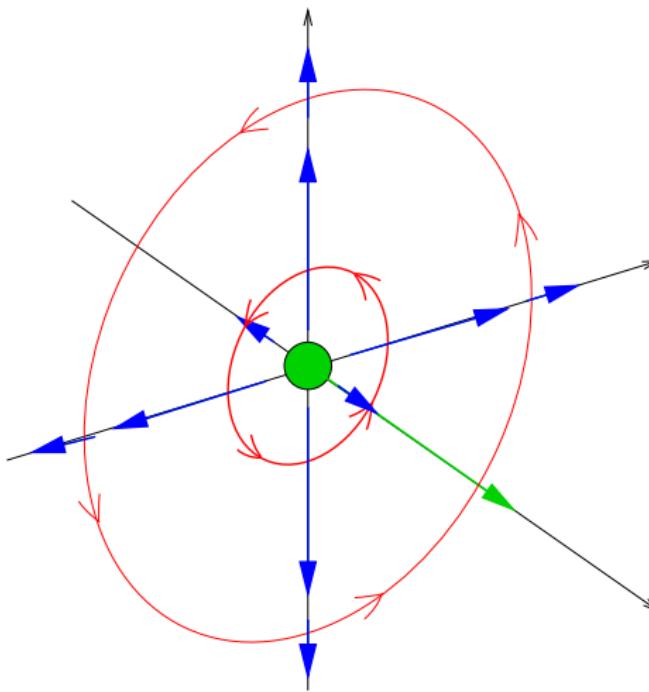


Electric charge moving



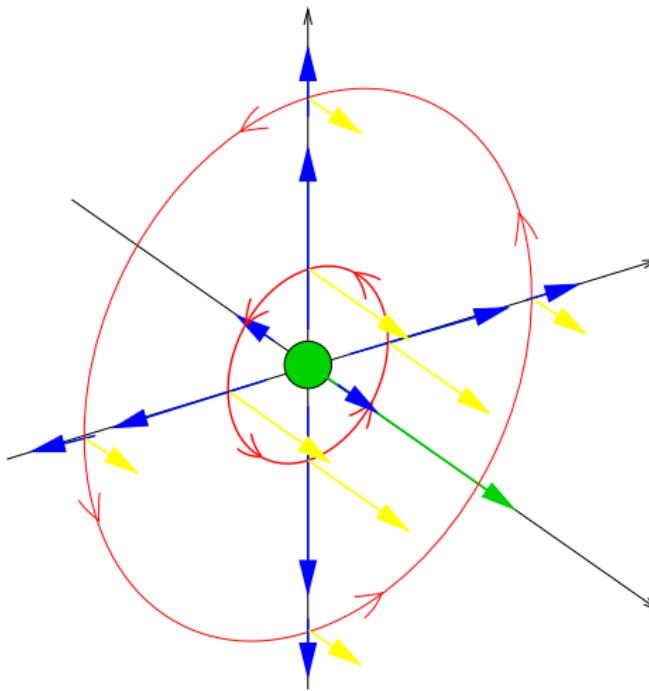


## Electromagnetic field





(almost) real photons



 Key to ChPT: Primakoff reactions

Access to  $\pi + \gamma$  reactions via the **Primakoff effect**:

At small momentum transfer to the nucleus, high-energetic particles scatter predominantly off the **el.mag. field** quanta ( $\sim Z^2$ )

$$\pi^- + \gamma \rightarrow \left\{ \begin{array}{l} \pi^- + \gamma \\ \pi^- + \pi^0 \\ \pi^- + \pi^0 + \pi^0 \\ \pi^- + \pi^- + \pi^+ \\ \pi^- + \dots \end{array} \right.$$

analogously: **Kaon-induced reactions**  $K^- + \gamma \rightarrow \dots$

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$$\pi^- + \gamma \rightarrow \begin{cases} \pi^- + \gamma \\ \pi^- + \pi^0 \\ \pi^- + \pi^0 + \pi^0 \\ \pi^- + \pi^- + \pi^+ \\ \pi^- + \dots \end{cases}$$

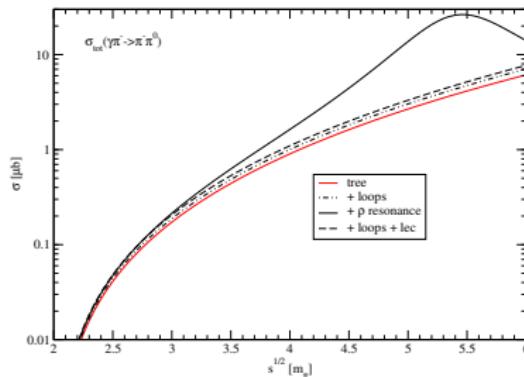
analogously: **Kaon-induced reactions**  $K^- + \gamma \rightarrow \dots$

Chiral anomaly  $\pi^- \gamma \rightarrow \pi^- \pi^0$ 

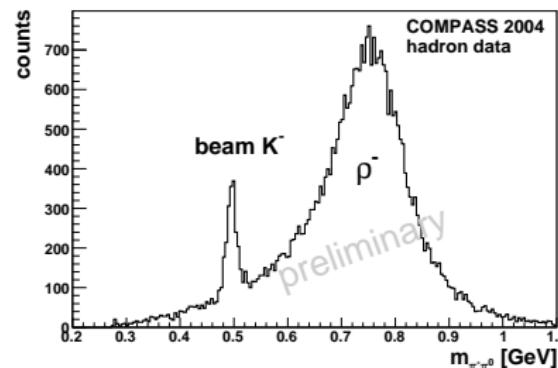
$\frac{e}{4\pi^2 f_\pi^3} \epsilon_{\mu\nu\alpha\beta} \varepsilon^\mu q_1^\nu q_2^\alpha q_3^\beta$

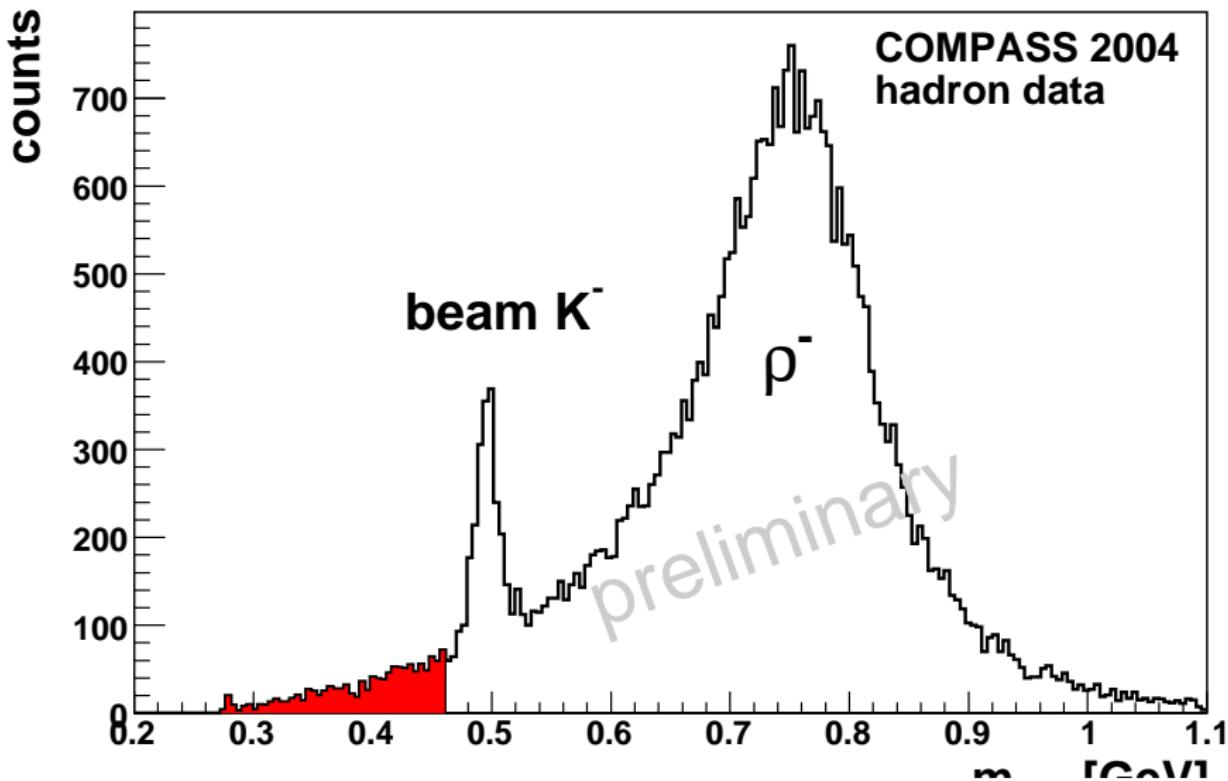
$$F_{3\pi}^{\chi PT} = 9.72 \text{ GeV}^{-3} \quad F_{3\pi}^{\text{Serpukhov}} = 12.9 \pm 1.4 \text{ (10.7} \pm 1.2) \text{ GeV}^{-3}$$

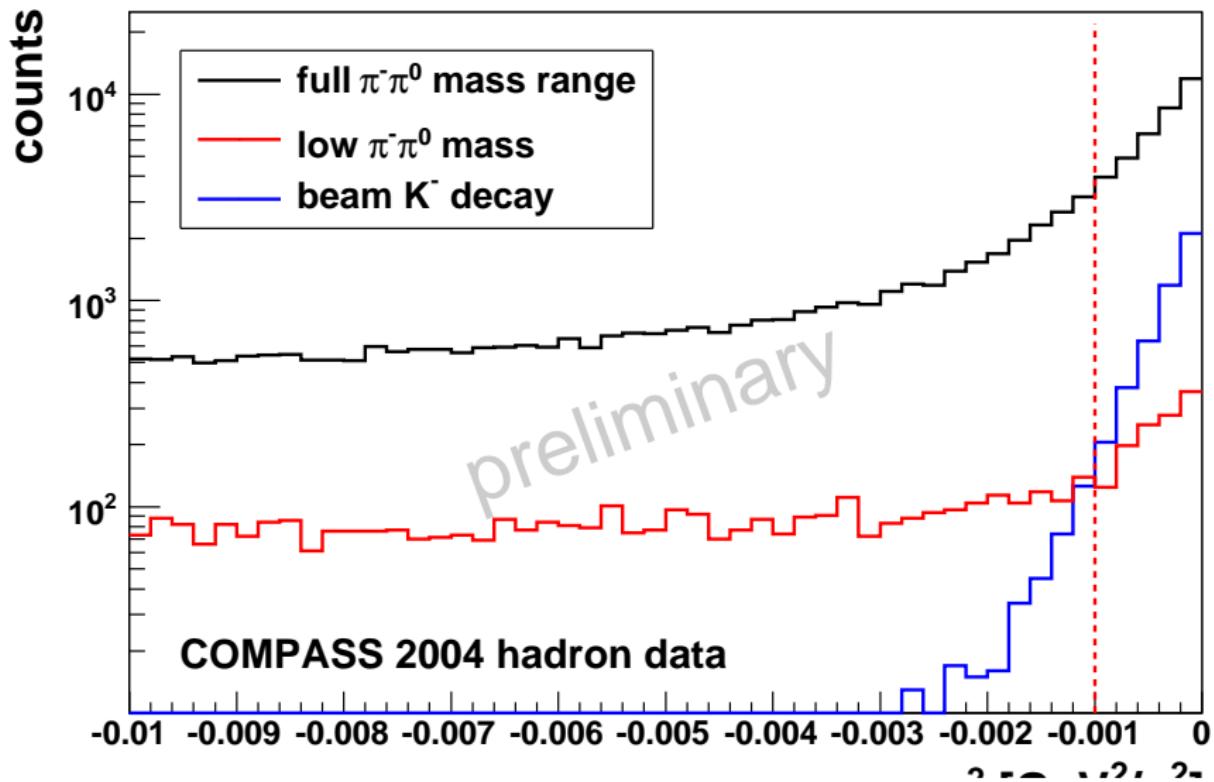
(theory: real photons)

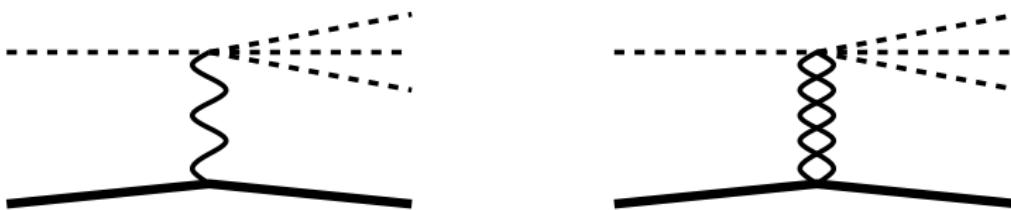


(data: quasi-real)





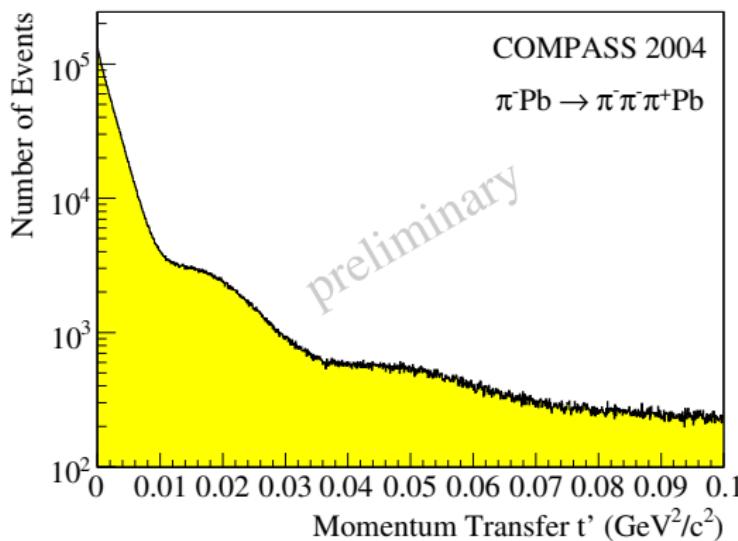




- Production via **photon** and strong (**pomeron**) exchange
  - separable by different  $t$ -dependence
- e.g. resonance  $a_2(1320)$  is produced both ways
  - radiative width
  - phase between the photon and strong amplitudes
- low-mass region  $\rightarrow$  ChPT



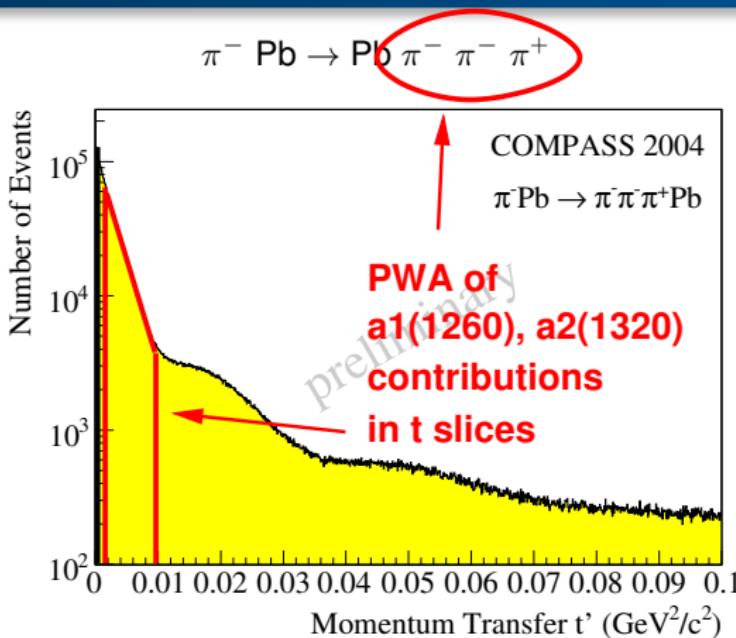
# 2004 Primakoff results (diffractive trigger)



- "Low  $t'$ ":  $10^{-3} (\text{GeV}/\text{c})^2 < t' < 10^{-2} (\text{GeV}/\text{c})^2$   $\sim 2\,000\,000$  events
- "Primakoff region":  $t' < 10^{-3} (\text{GeV}/\text{c})^2$   $\sim 1\,000\,000$  events



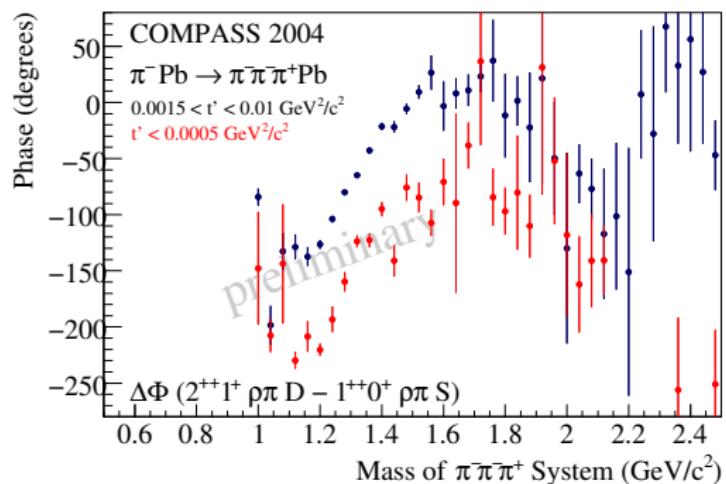
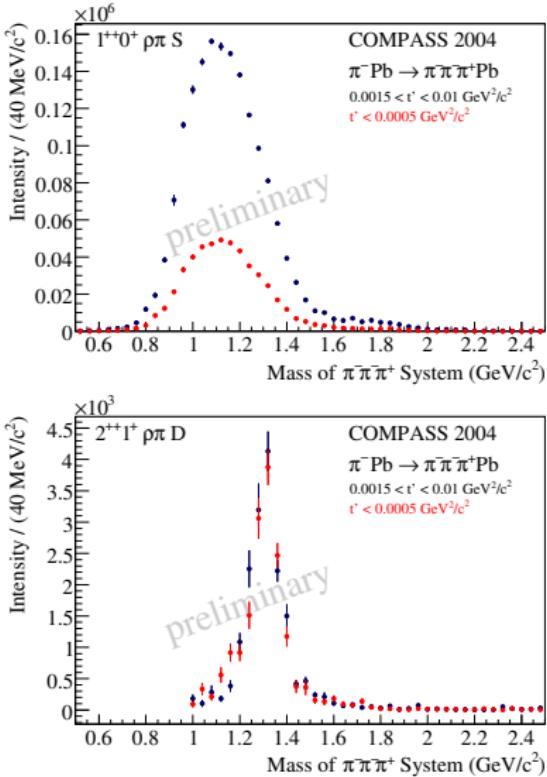
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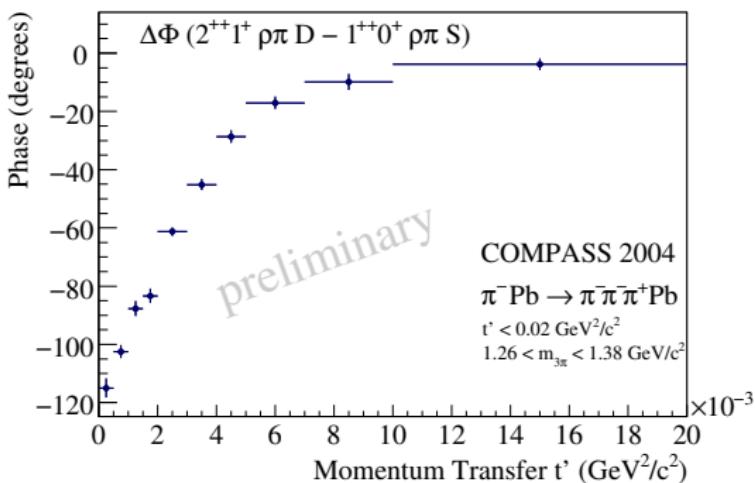
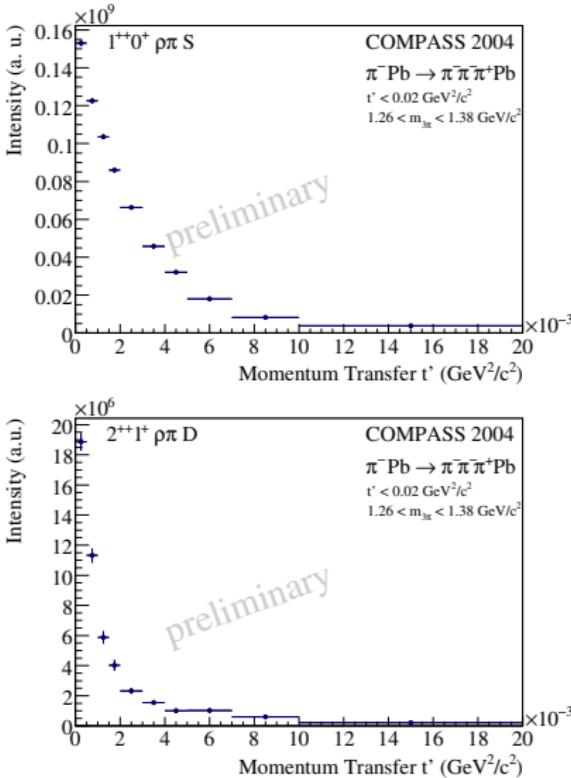


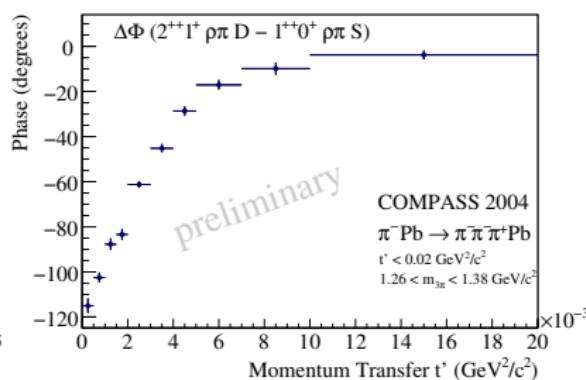
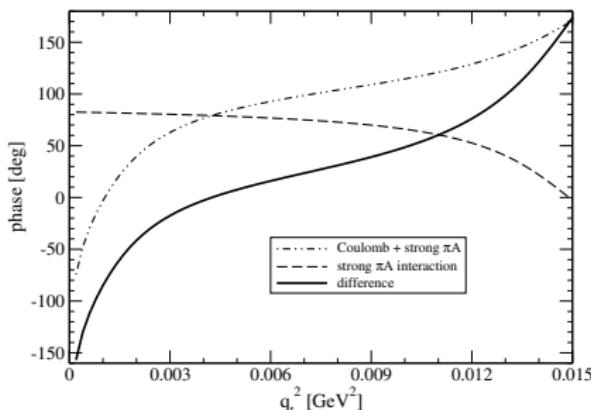
# PWA: $a_1$ , $a_2$ and $\Delta\Phi$ in separated $t'$ regions




  
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# Phase $a_2 - a_1$ in detail: $t'$ dependence





## Glauber model

G. Fäldt and U. Tengblad, Phys. Rev. C79, 014607 (2009)

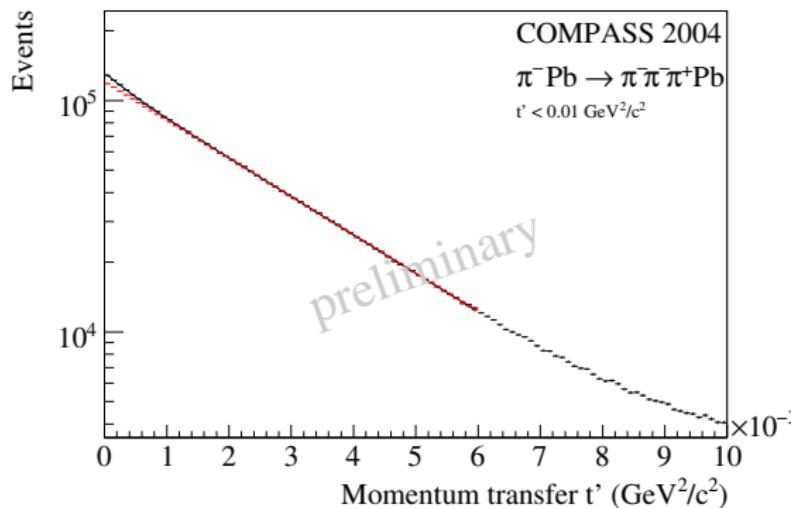
Plot: N. Kaiser (TU München)

- ⇒ indicates confirmation of interference Coulomb-interaction - strong interaction
- ⇒ detailed studies of the nature of resonances



# Primakoff contribution at $t' < 10^{-3} (\text{GeV}/c)^2$

Primakoff:  $\sigma(t') \propto e^{-b_{\text{Prim}} t'}$ ,  $b_{\text{Prim}} \approx 2000 (\text{GeV}/c)^{-2}$  (mainly resolution)  
 Diffractive:  $\sigma(t') \propto e^{-b_{\text{diff}} t'}$ ,  $b_{\text{diff}} \approx 400 (\text{GeV}/c)^{-2}$  for lead target



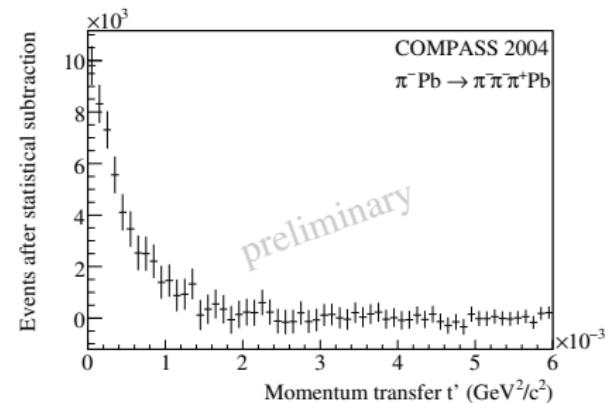
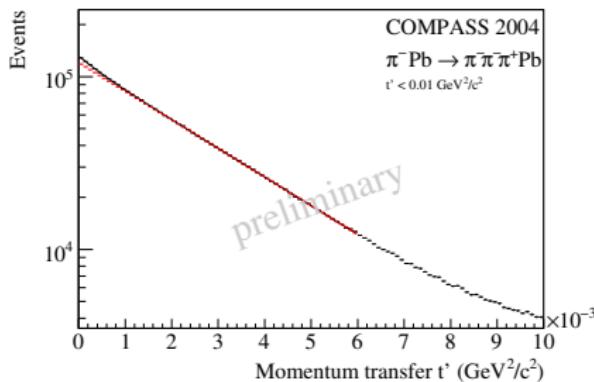
(Mass) spectrum of this Primakoff contribution?

⇒ Statistical subtraction of diffractive background (for bins of  $m_{3\pi}$ )



# Basic features of the statistical subtraction

- Fit of  $t'$  spectrum with sum of both exponentials for  $0 < t' < 0.006 \text{ (GeV}/c)^2$   
 $(0.5 < m_{3\pi} < 2.5 \text{ GeV}/c^2)$
- Subtraction of “diffractive” exponent from  $t'$  spectrum



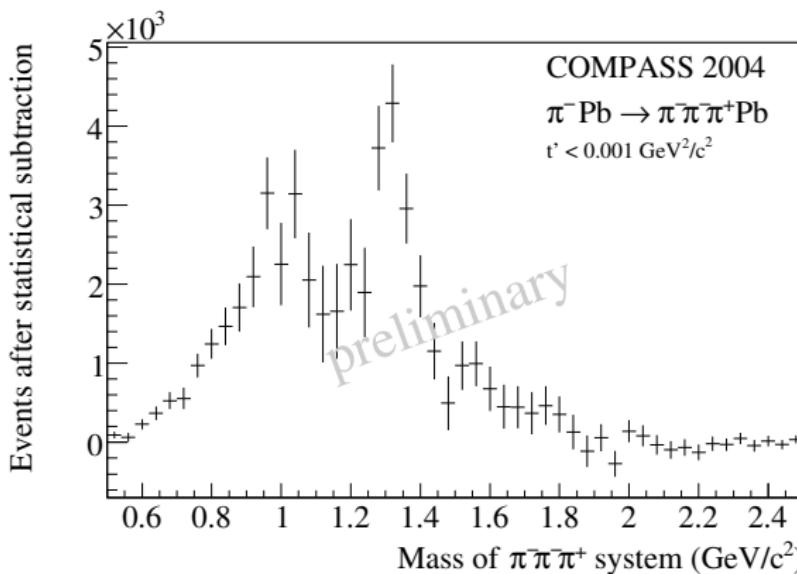
- Fit and subtraction in  $3\pi$  mass bins:
  - $b_{\text{Prim}} = 2050 \text{ (GeV}/c)^{-2}$  fixed
  - $b_{\text{diff}}$  as fit parameter

Primakoff contribution

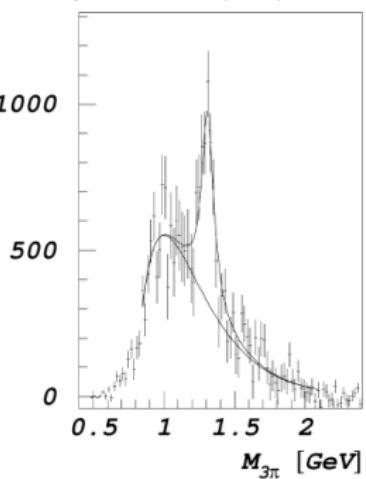


# Mass spectrum from statistical subtraction

- Statistical subtraction separately in  $40 \text{ MeV}/c^2$  mass bins
- Integrate Primakoff contribution of the  $t'$  spectra for  $t' < 10^{-3} (\text{GeV}/c)^2$

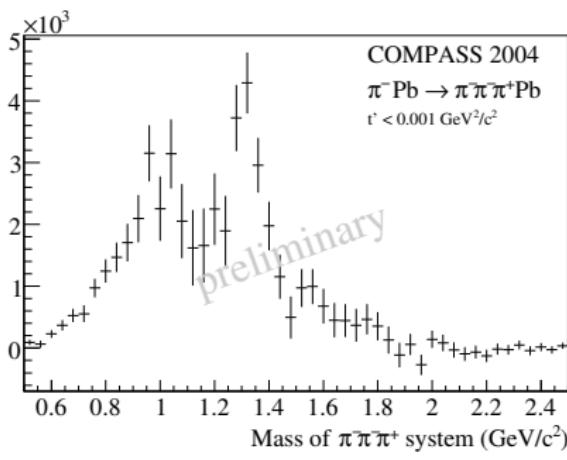


Selex, Phys. Lett. B 521(2001), 171-180

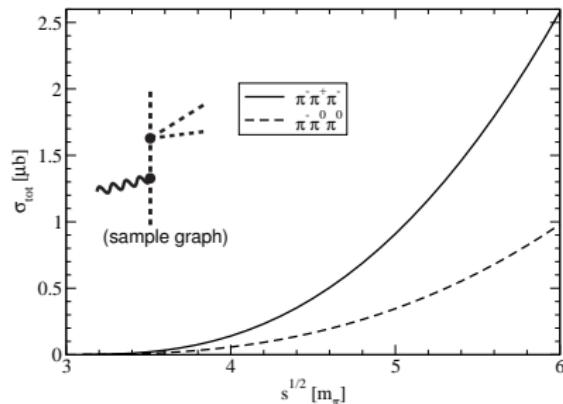
Fig. 3.  $M_{3\pi}$  mass distribution for the Cu target after subtraction of diffractive background. The curve shows fit with a sum of pure Coulomb contribution and smooth background.



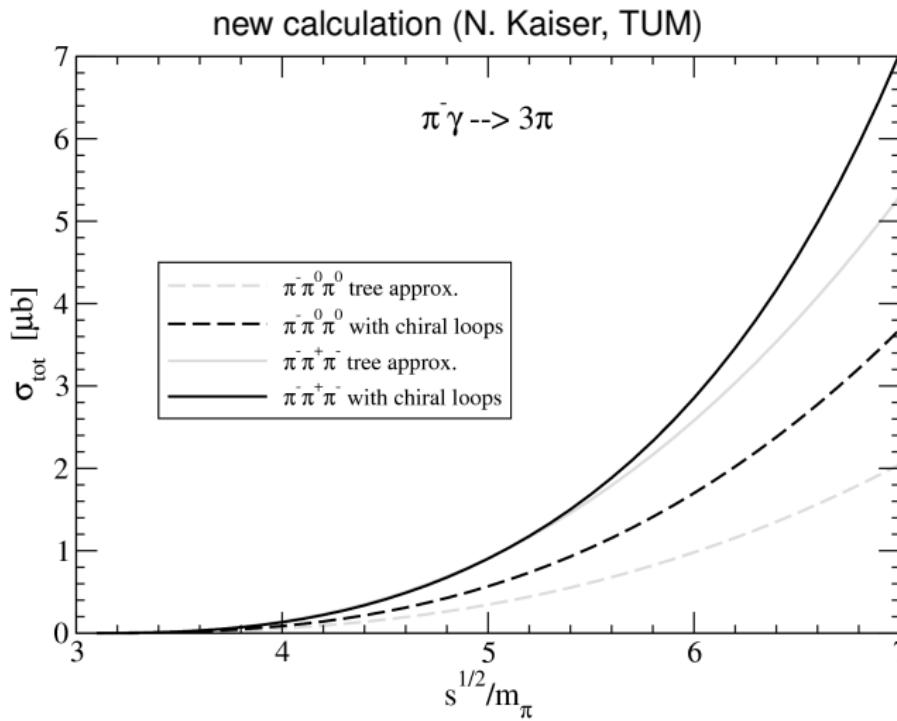
Events after statistical subtraction



preliminary



- Simple approach: look at Primakoff mass spectrum by statistical subtraction
- Chiral Perturbation Theory prediction: tree diagrams calculation 2008
- Formula for (absolute) total cross section: N. Kaiser, JF, EPJA 36 (2008) 181

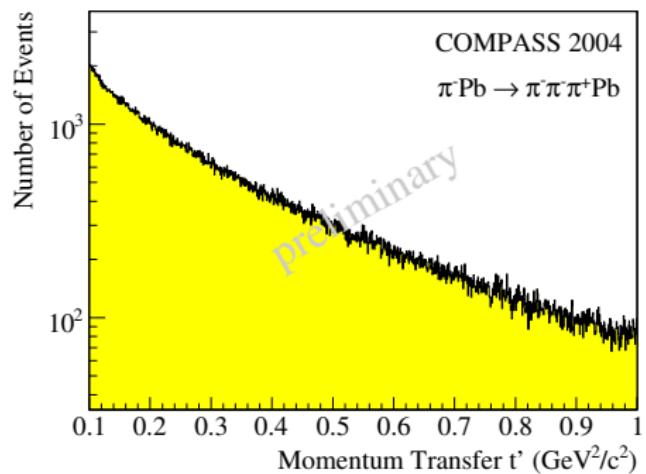
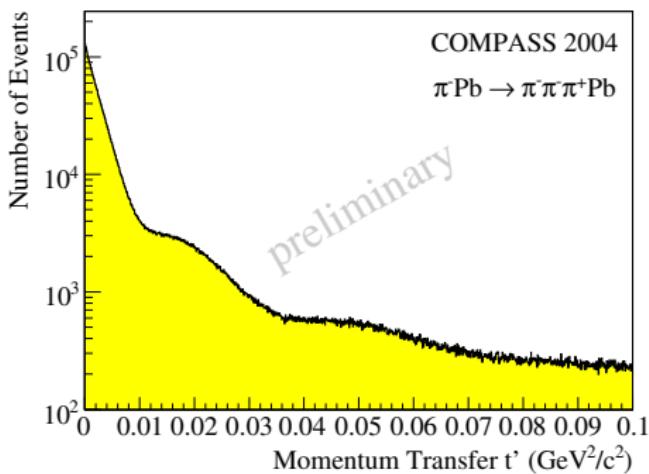


Diffraction 2004:  $\pi^- \text{Pb} \rightarrow \pi^- \pi^- \pi^+ \text{Pb}$ 

## Momentum Transfer Distributions

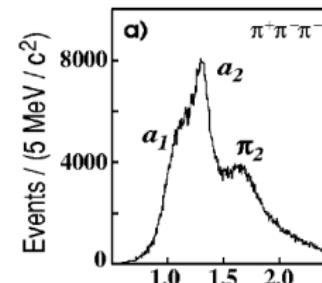
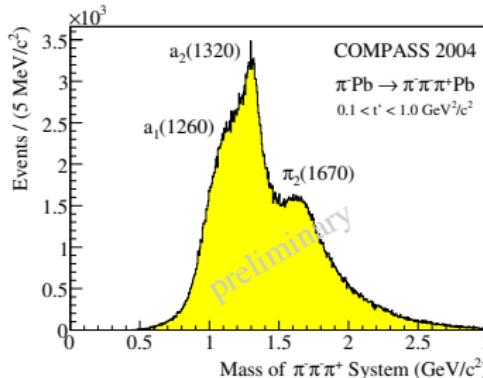


- 4-pion vertex in Pb target
- Exclusive in the energy within resolution
- Momentum transfer:  $-t = Q^2 - (p_{\text{beam}} - p_{(\pi^- \pi^- \pi^+)})^2$

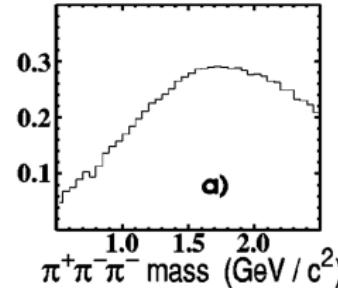
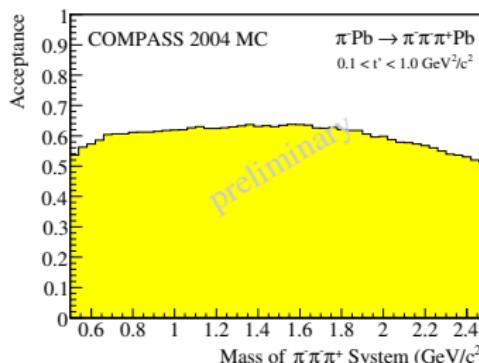


# 3 $\pi$ Data in the range $0.3 < t'/(GeV^2/c^2) < 1$

## $\pi^- \pi^- \pi^+$ Mass Distributions and Acceptance



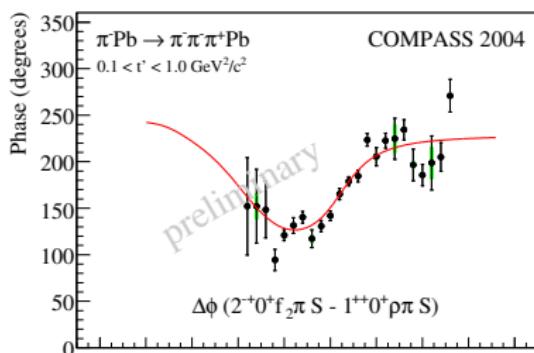
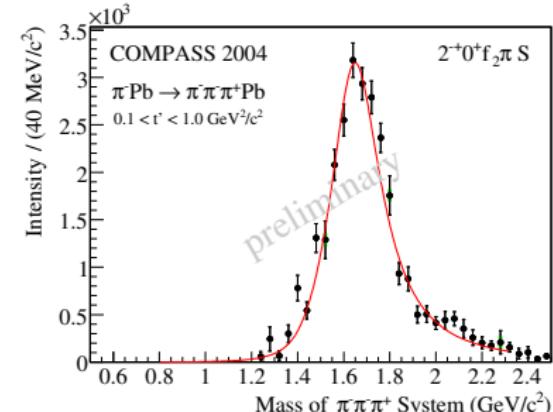
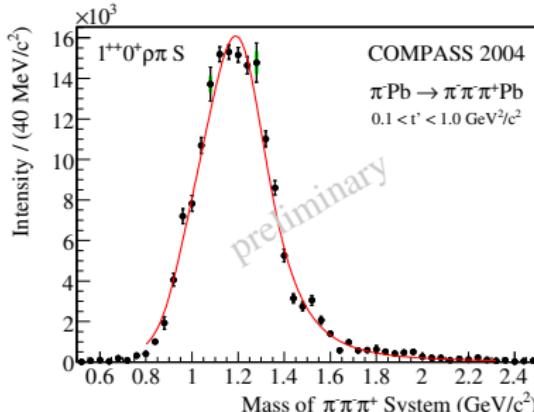
BNL-E852, Phys. Rev. **D65**, 072001, 2002



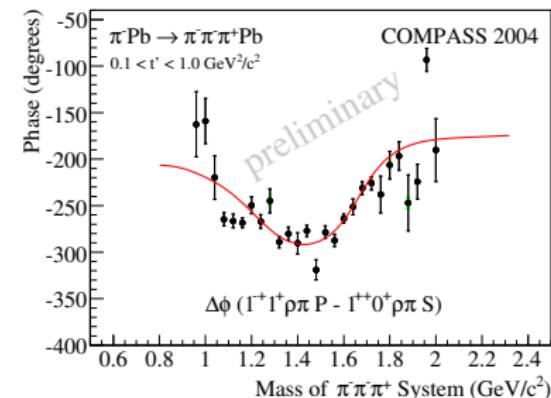
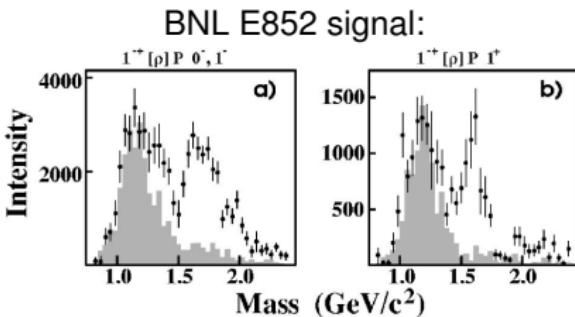
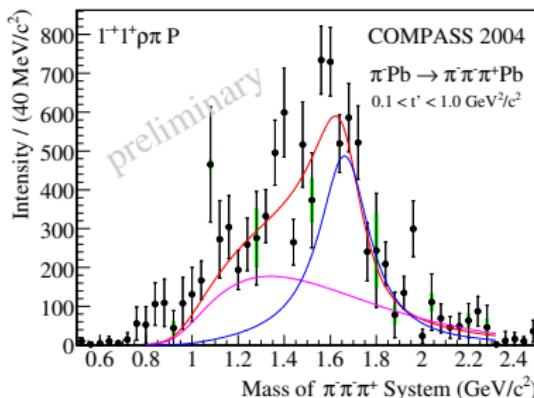


# PWA Results

$1^{++}0^+\rho\pi S$  and  $2^{-+}0^+f_2\pi S$



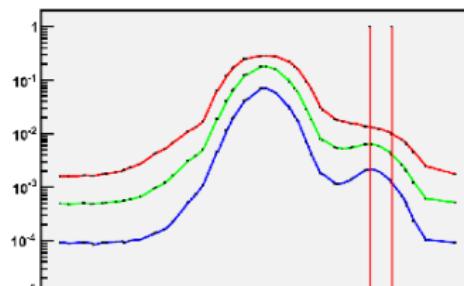
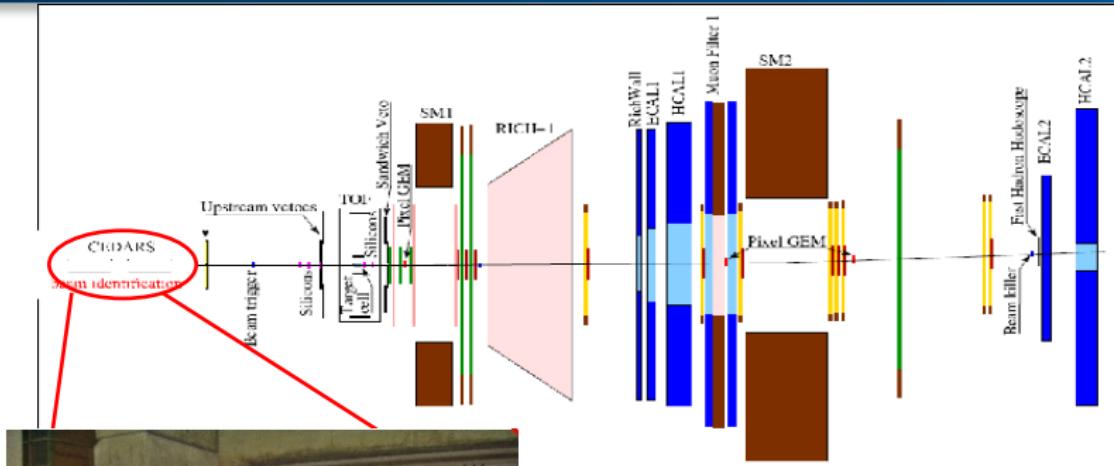
- BW for  $a_1(1260)$  + background:  
 $M = (1.256 \pm 0.006 {}^{+0.007}_{-0.017}) \text{ GeV}$   
 $\Gamma = (0.366 \pm 0.009 {}^{+0.028}_{-0.025}) \text{ GeV}$
- BW for  $\pi_2(1670)$ :  
 $M = (1.659 \pm 0.003 {}^{+0.024}_{-0.008}) \text{ GeV}$   
 $\Gamma = (0.271 \pm 0.009 {}^{+0.022}_{-0.024}) \text{ GeV}$

 PWA Results
Exotic  $1^{-+} 1^+ \rho\pi P$  Wave

- Significant  $1^{-+}$  amplitude consistent with resonance at  $\sim 1.6 \text{ GeV}$
- No leakage observed
- BW for  $\pi_1(1600)$  + background:  
 $M = (1.660 \pm 0.010 {}^{+0.000}_{-0.064}) \text{ GeV}$   
 $\Gamma = (0.269 \pm 0.021 {}^{+0.042}_{-0.064}) \text{ GeV}$

# COMPASS Setup 2008

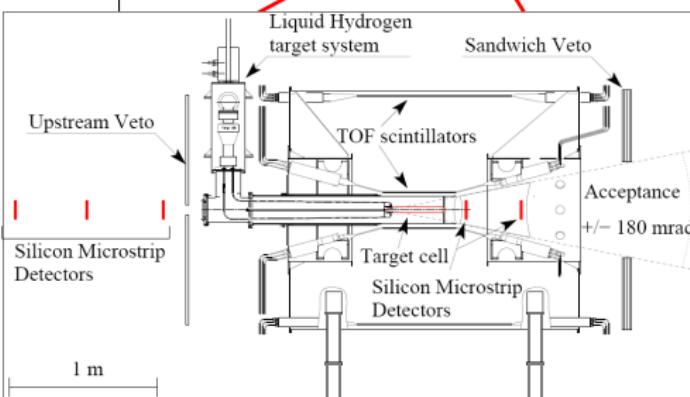
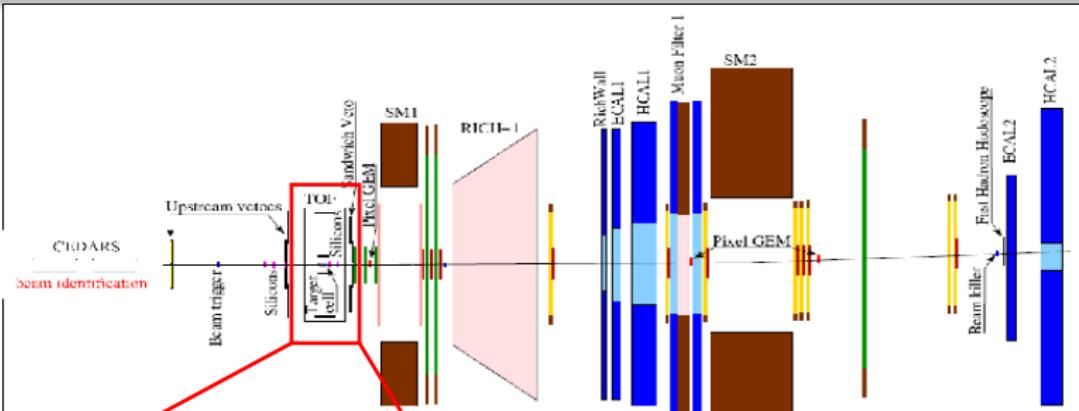
## CEDARs





# COMPASS Setup 2008

Target region: Recoil Proton Detector

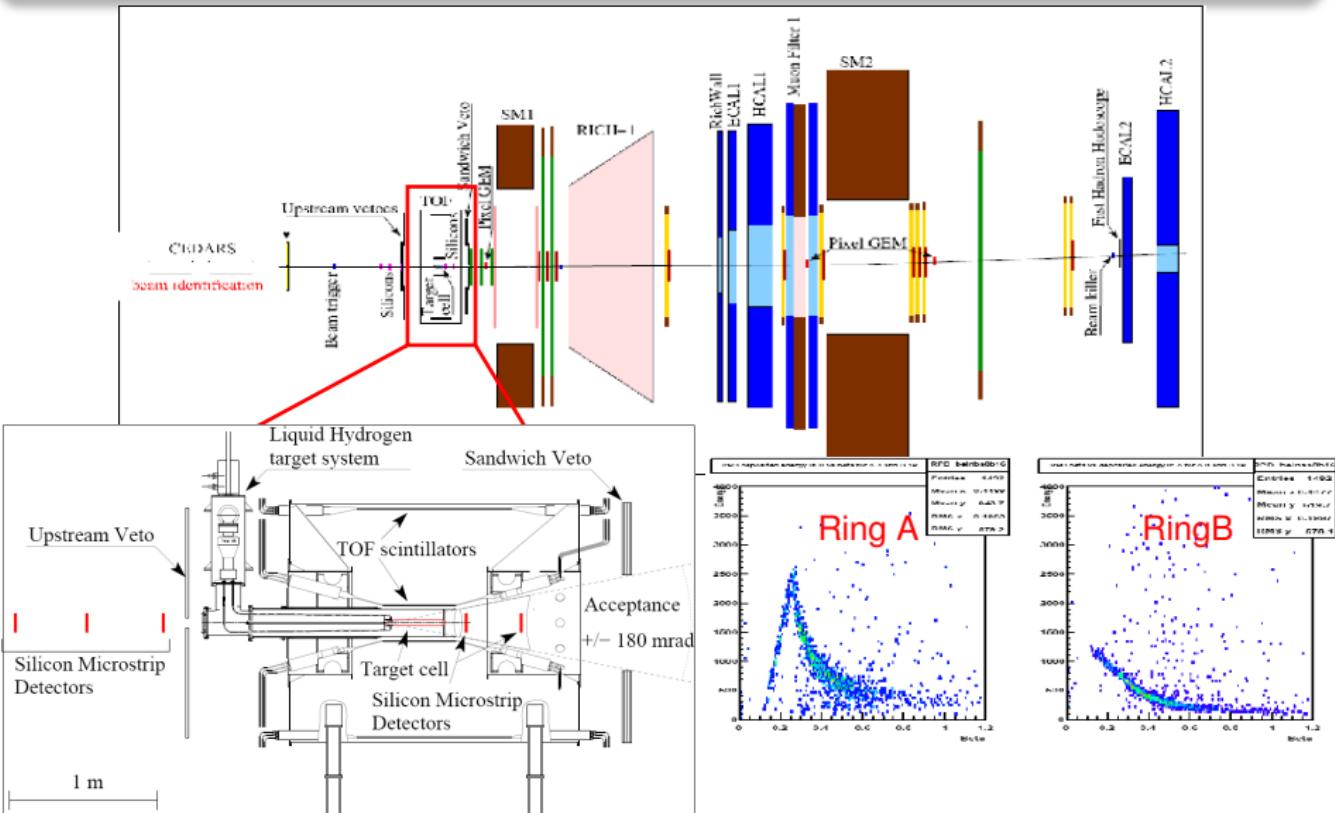


# COMPASS Setup 2008

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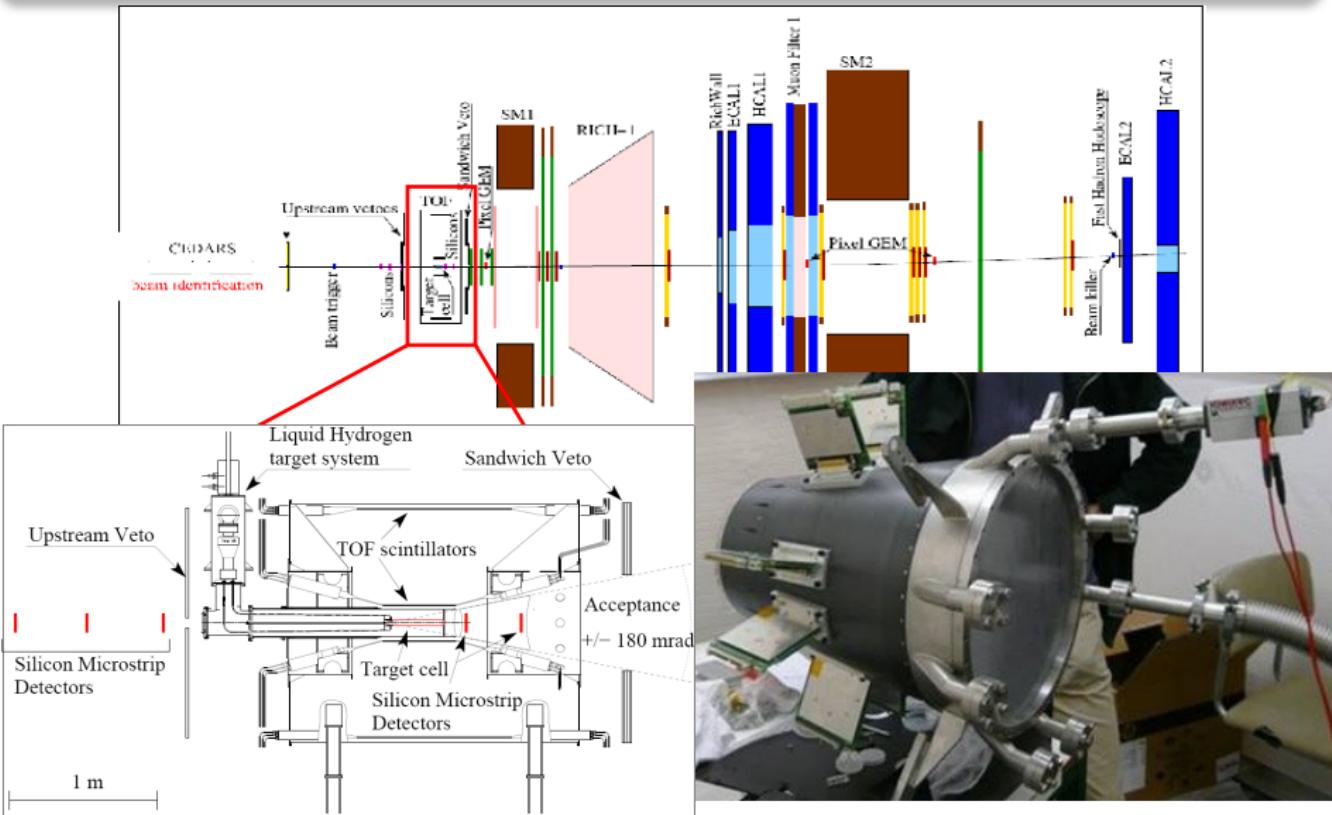


Target region: RPD Signals



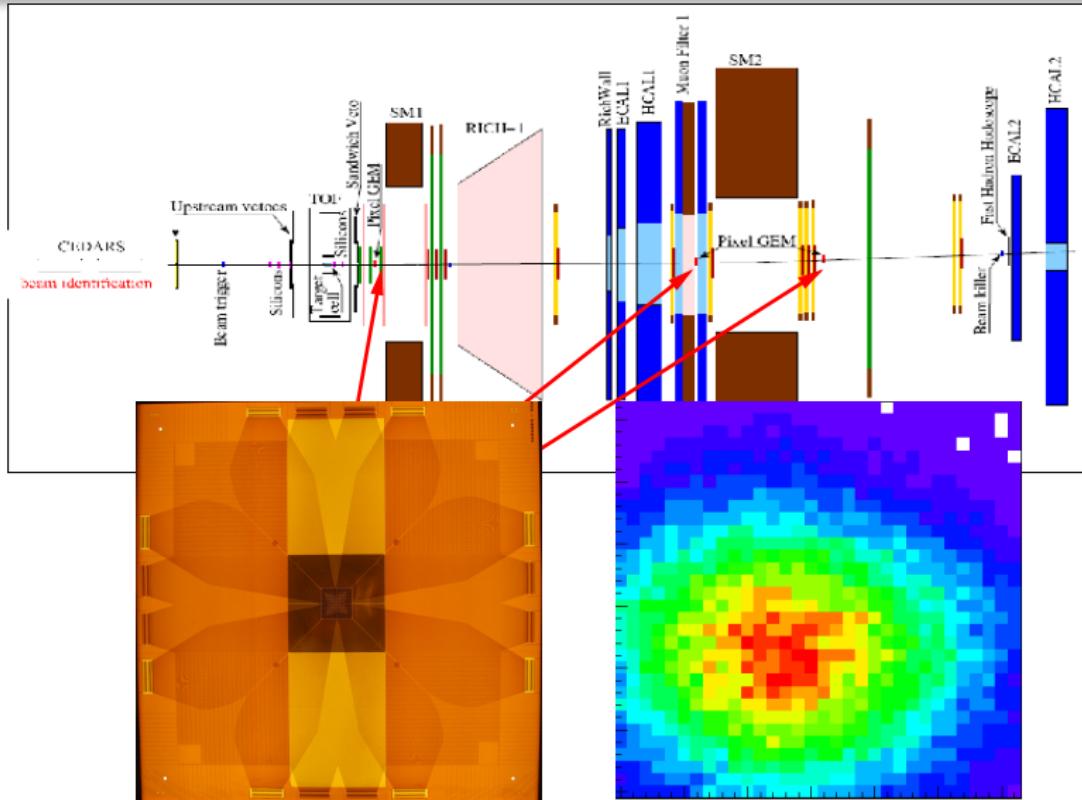
# COMPASS Setup 2008

Target region: Silicon detectors



# COMPASS Setup 2008

Target region: Pixel GEM detectors

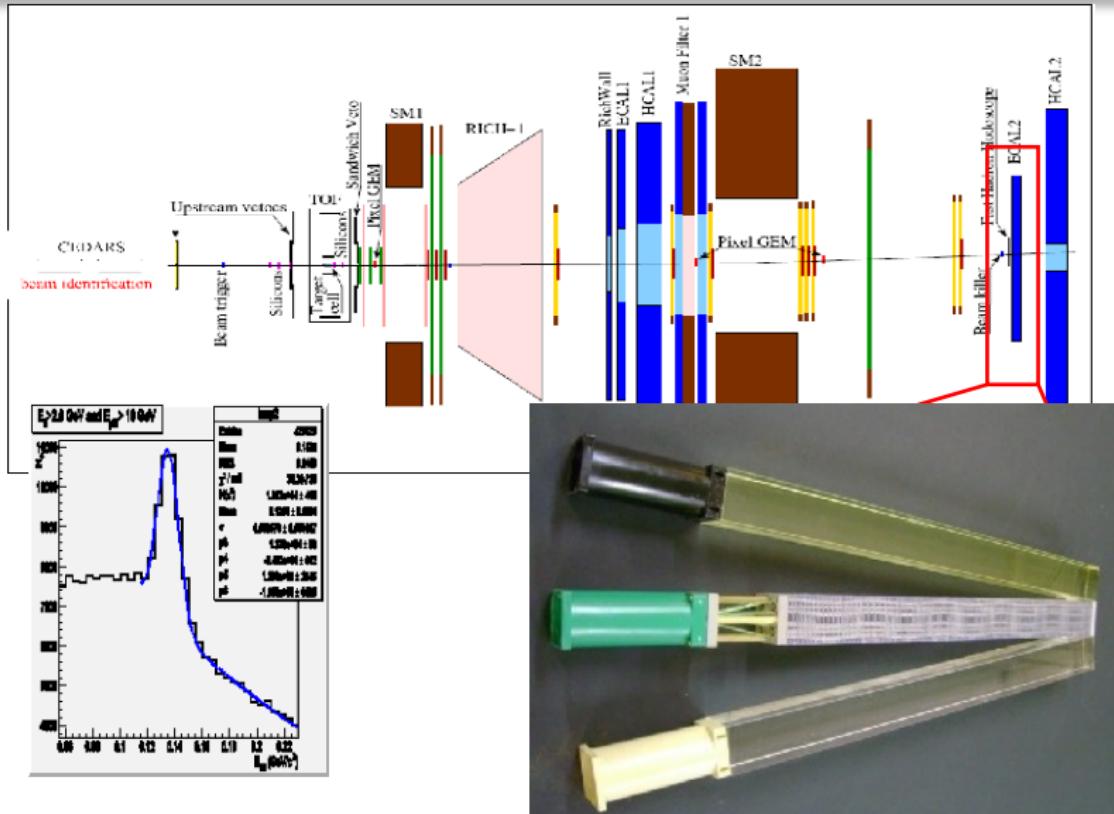


# COMPASS Setup 2008

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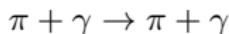


## Calorimetry:

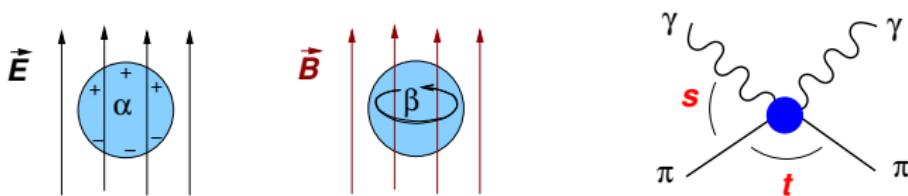




# Compton scattering and polarisability



Leading deviation from pointlike particle  $\leftrightarrow$  e.m. polarisability



for  $\alpha_\pi - \beta_\pi$  [10 $^{-4}$  fm $^3$ ]:  $(\alpha_\pi \approx -\beta_\pi)$

ChPT: 5.7±1.0  
experiments: 4 — 14



# Compton cross section

$$\frac{d\sigma_{\pi\gamma}}{d\Omega_{cm}} = \frac{\alpha^2(s^2 z_+^2 + m_\pi^4 z_-^2)}{s(sz_+ + m_\pi^2 z_-)^2} - \frac{\alpha m_\pi^3 (s - m_\pi^2)^2}{4s^2(sz_+ + m_\pi^2 z_-)} \cdot \mathcal{P}$$

with (quadrupole polarisability  $\alpha_2 - \beta_2$ )

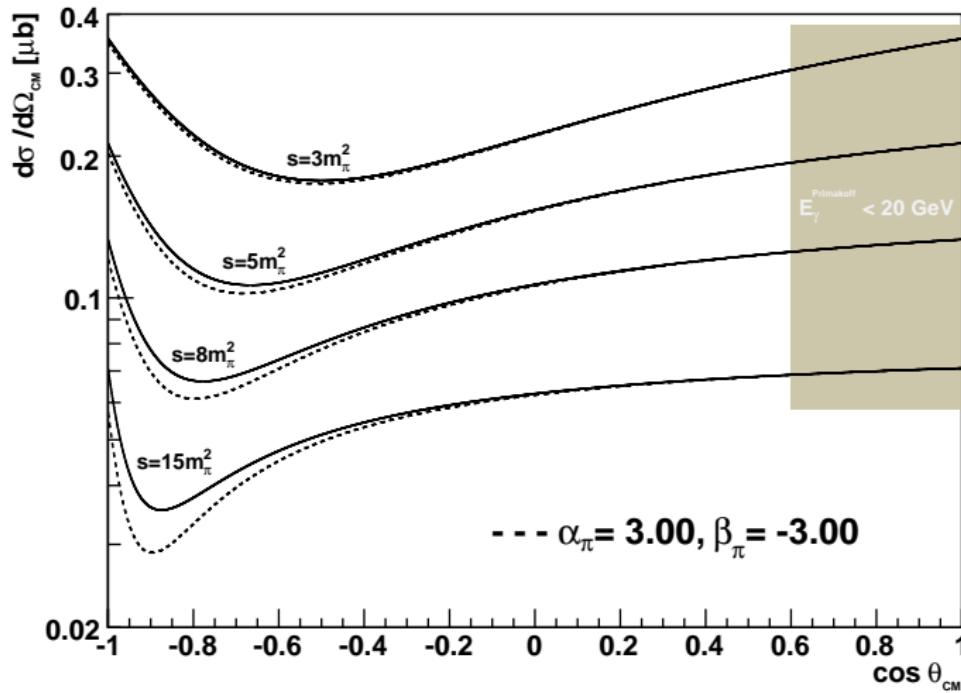
$$\mathcal{P} = z_-^2(\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+^2(\alpha_\pi + \beta_\pi) - \frac{(s - m_\pi^2)^2}{24s} z_-^3(\alpha_2 - \beta_2)$$

$$(z_\pm = 1 \pm \cos \theta_{cm})$$

**Measuring the differential cross section with high statistics allows to determine all three polarisability contributions**



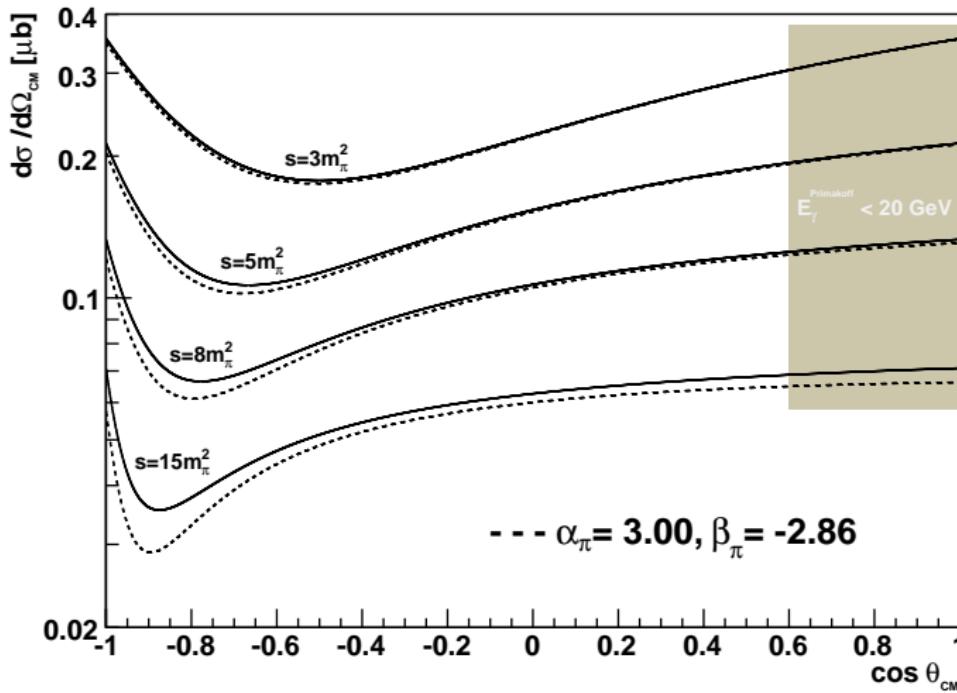
loop effects not shown





# Polarisability effect (NLO ChPT values)

loop effects not shown





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- recorded statistics (eff. 3 days) competitive to the Serpukhov measurement
- problems with the calorimeter (stability, trigger logic)  
→ large estimated systematic error

Nov. 2009

- major upgrade of calorimeter readout, new digital trigger
- fine tuning / offline corrections **ongoing**

2012 <http://wwwcompass.cern.ch> → New proposal

- COMPASS-II proposal for a high-statistics Primakoff run
- increase statistics by a factor > 30, uncertainty on  $\alpha_\pi - \beta_\pi$ :  $\pm 0.66$  (ChPT: 5.7)
- First measurement of polarisability **sum  $\alpha_\pi + \beta_\pi$**   
expected uncertainty  $\pm 0.025$  (ChPT: 0.16)



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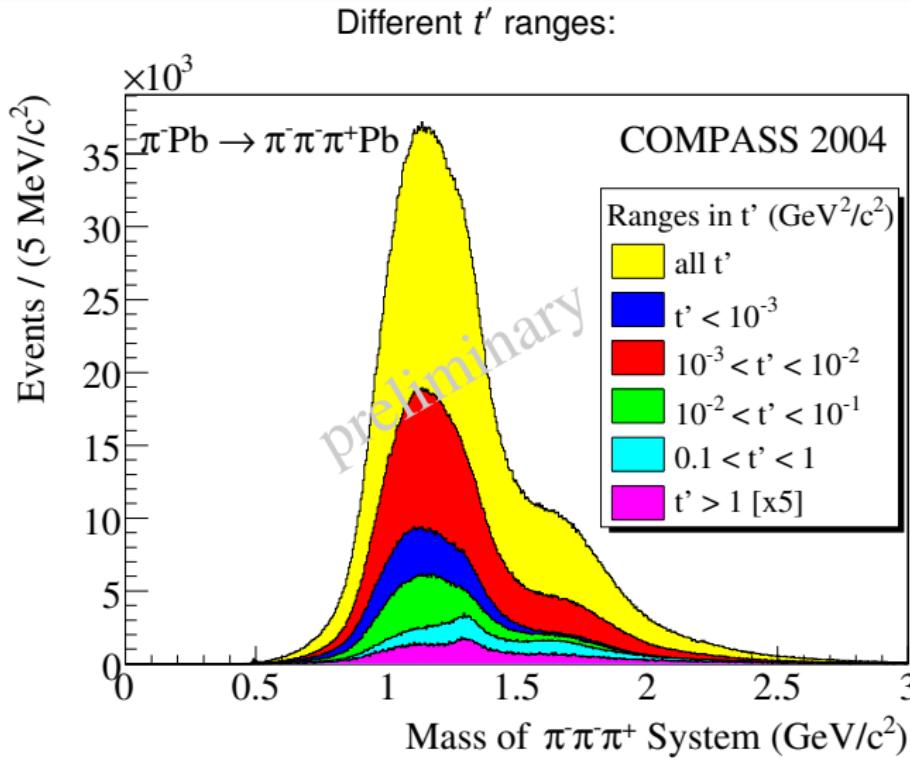
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 Summary and Outlook

- **COMPASS 2004** hadron run (few days) using a 190 GeV  $\pi^-$  beam
  - Primakoff: calorimetry problems
  - diffractive: spin-exotic  $\pi_1$  observation (PRL104), more results coming
- $\pi^- Pb \rightarrow \pi^- \pi^- \pi^+ Pb$  at (very) low momentum transfer
- Production phase of  $a_2(1320)$  dependent on  $t'$  shows interference of contributions from Coulomb and strong interaction
- Test of chiral diagrams in threshold mass region *coming up*
- **2009** data with extended spectrometer
  - diffractive on H, Pb, Ni
  - Primakoff on Ni
- High-statistics run **2012**

 BACKUP: 3 $\pi$  Data Sample (2004) $\pi^- \pi^- \pi^+$  mass distribution



- Mass-independent PWA (narrow mass bins):

$$\sigma_{\text{indep}}(\tau, m, t') = \sum_{\epsilon=\pm 1} \sum_{r=1}^{N_r} \left| \sum_i T_{ir}^{\epsilon} f_i^{\epsilon}(t') \psi_i^{\epsilon}(\tau, m) \right|^2 / \sqrt{\int |f_i^{\epsilon}(t')|^2 dt'} \sqrt{\int |\psi_i^{\epsilon}(\tau', m)|^2 d\tau'}$$

- Production strength assumed constant in single bins
  - Decay amplitudes  $\psi_i^{\epsilon}(\tau, m)$ , with  $t'$  dependence  $f_i^{\epsilon}(t')$
  - Production amplitudes  $T_{ir}^{\epsilon}$  → Extended log-likelihood fit
  - Acceptance corrections included
- Spin-density matrix:  $\rho_{ij}^{\epsilon} = \sum_r T_{ir}^{\epsilon} T_{jr}^{\epsilon*}$

→ Physical parameters:

$$\text{Intens}_i^{\epsilon} = \rho_{ii}^{\epsilon}, \\ \text{relative phase } \Phi_{ij}^{\epsilon}$$

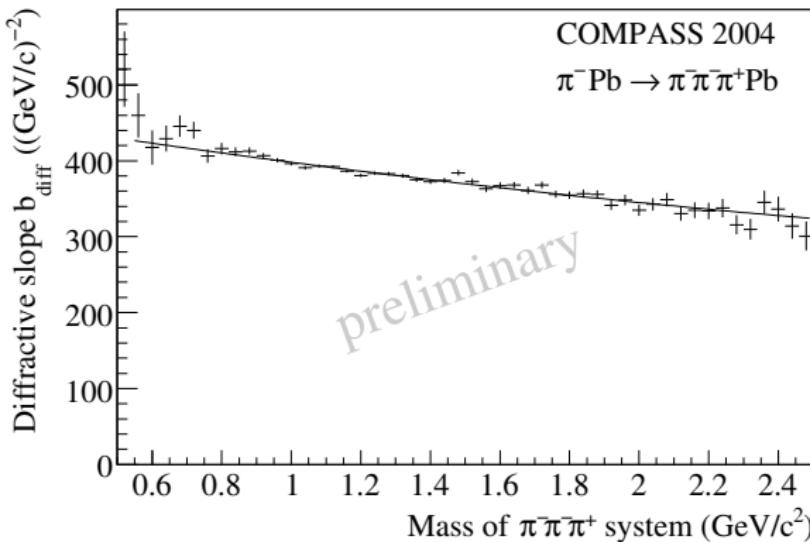
$$\text{Coh}_{i,j}^{\epsilon} = \sqrt{(\text{Re } \rho_{ij}^{\epsilon})^2 + (\text{Im } \rho_{ij}^{\epsilon})^2} / \sqrt{\rho_{ii}^{\epsilon} \rho_{jj}^{\epsilon}}$$

- Mass-dependent  $\chi^2$ -fit (not presented here):

- $X$  parameterized by Breit-Wigner (BW) functions
- Background can be added

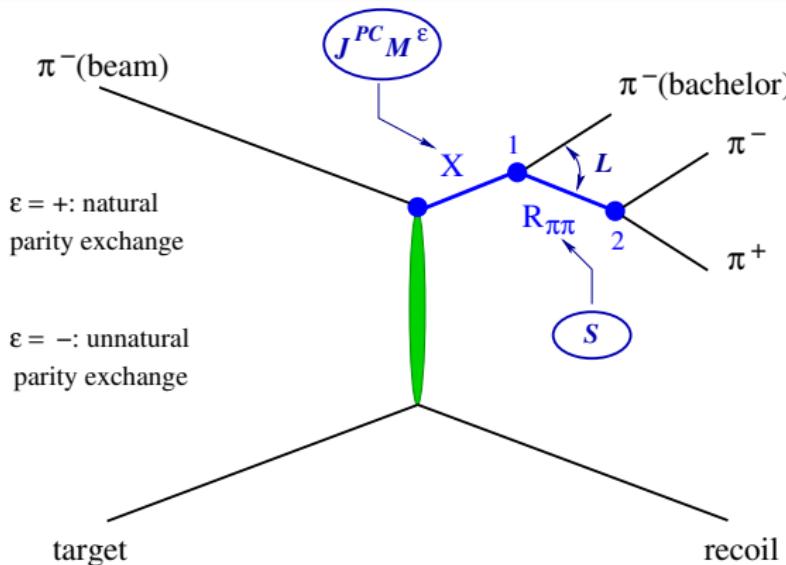


## Mass dependence of the diffractive slope



# Partial Wave Analysis Formalism

## Isobar Model



- Isobar model:  
Intermediate  
2-particle decays
- Partial wave in  
reflectivity basis:  
 $J^{PC} M^\epsilon [isobar] L$

- Mass-independent PWA (40 MeV/c<sup>2</sup> mass bins): **38 waves**  
Fit of angular dependence of partial waves, interferences
- Mass-dependent  $\chi^2$ -fit (Not presented here)

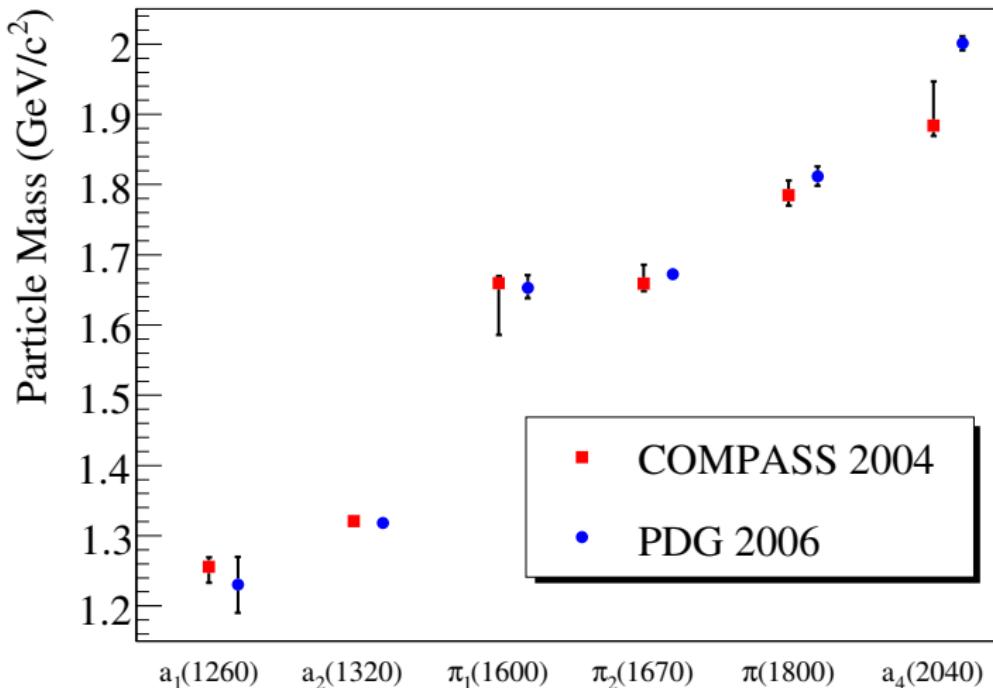


## Summary of Extracted States

Comparison with PDG values

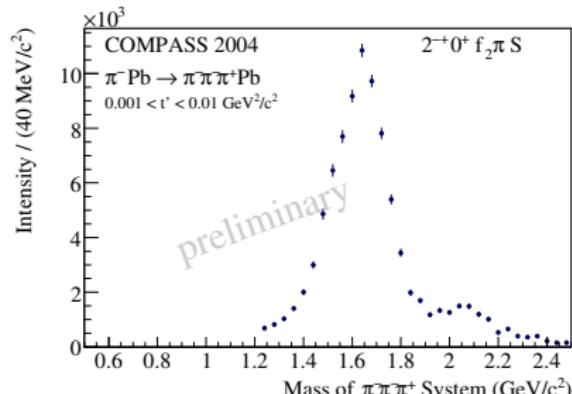
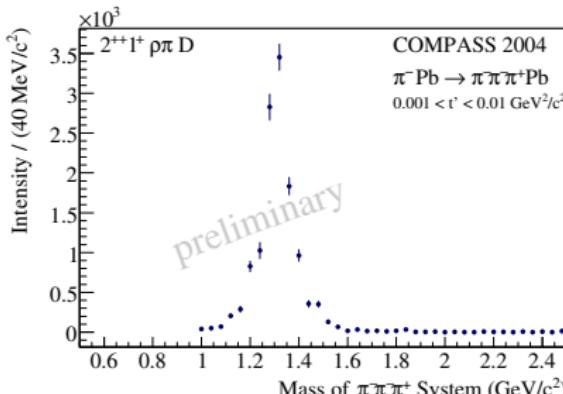
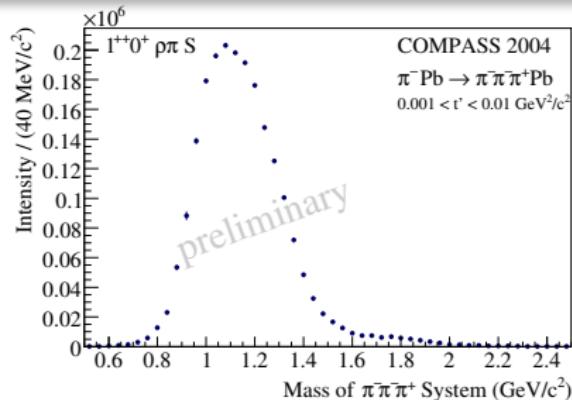
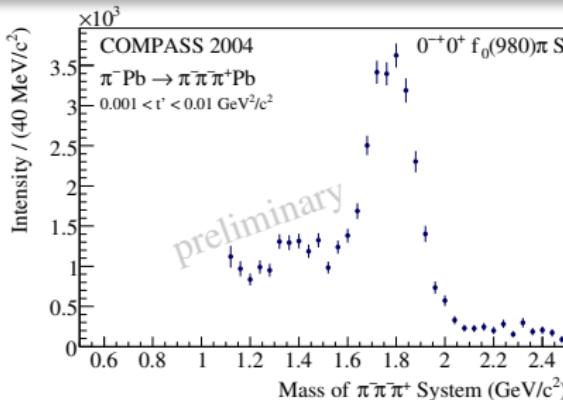


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# PWA of data with low $t'$

Intensity of selected waves:  $0^{-+}0^+ f_0(980)\pi S$ ,  $1^{++}0^+ \rho\pi S$ ,  $2^{++}1^+ \rho\pi D$ ,  $2^{-+}0^+ f_2(1270)\pi S$



# Spin Totals for $t' < 10^{-3}$ (GeV/c $^2$ )

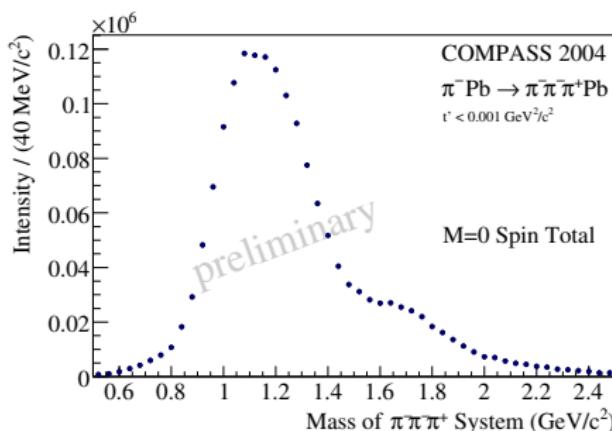
"Spin Totals": Sum of all contributions for given M (i.e. z-projection of J)

$t'$ -dependent amplitudes:

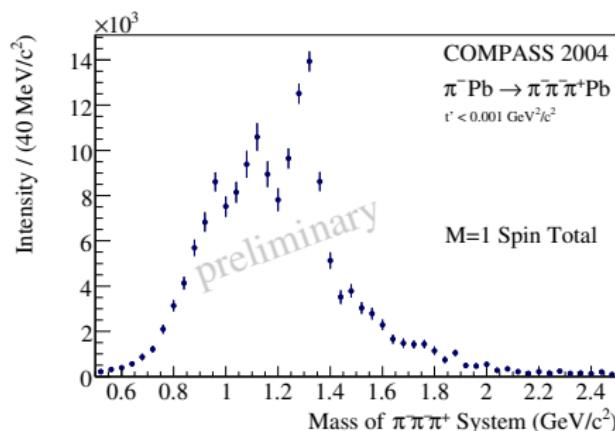
Primakoff production: **M=1**:  $\sigma(t') \propto e^{-b_{\text{Prim}}t'} \rightarrow$  arises at  $t' \approx 0$  (resolved shape!)

Diffractive production: **M=0**:  $\sigma(t') \propto e^{-b_{\text{diff}}(m)t'}$

**M=1**:  $\sigma(t') \propto t' e^{-b_{\text{diff}}(m)t'} \rightarrow$  vanishes for  $t' \approx 0$



**M=0**



**M=1**

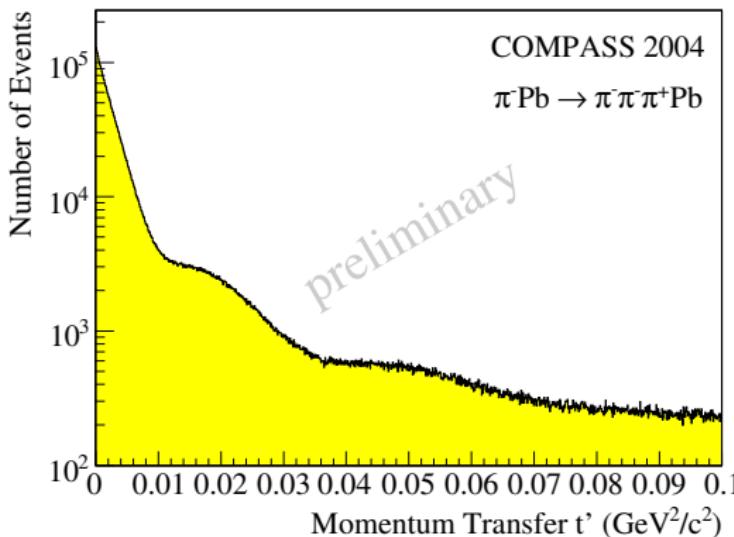


## 2004 Primakoff results (diffractive trigger)

Momentum Transfer

Momentum transfer to target:

$$-t = -(p_{\text{beam}} - p_{(\pi^-\pi^-\pi^+)})^2 \Rightarrow t' = |t| - |t|_{\min}$$



with

$$|t|_{\min} = \frac{(m_{3\pi}^2 - m_\pi^2)^2}{4|\vec{p}_{\text{beam}}|_{\text{lab}}^2}$$

**Diffraction pattern:**  
 Pb nucleus acts like  
 "black disc" in optics

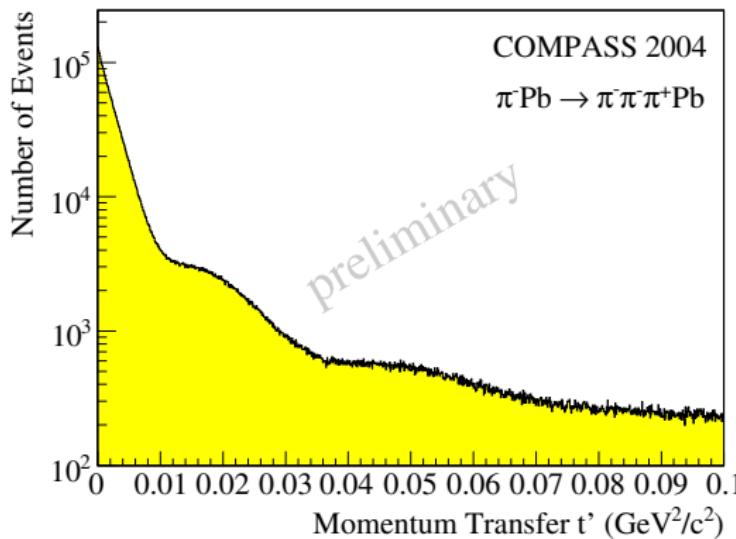


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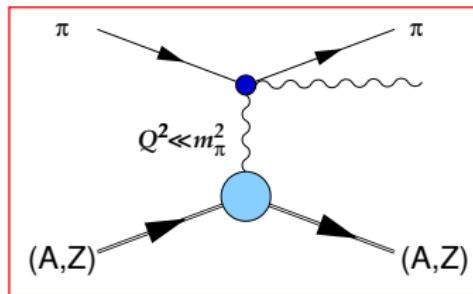
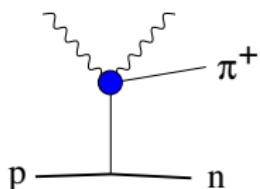
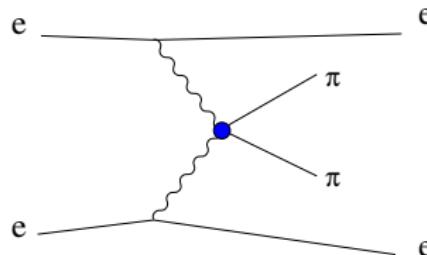
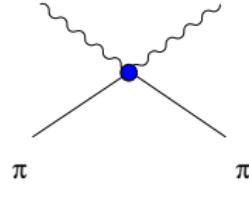
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- "Low  $t'$ ":  $10^{-3} (\text{GeV}/\text{c})^2 < t' < 10^{-2} (\text{GeV}/\text{c})^2$   $\sim 2\,000\,000$  events
- "Primakoff region":  $t' < 10^{-3} (\text{GeV}/\text{c})^2$   $\sim 1\,000\,000$  events



wanted:





M.R. Pennington in the 2<sup>nd</sup> DAΦNE Physics Handbook,  
“What we learn by measuring  $\gamma\gamma \rightarrow \pi\pi$  at DAΦNE”:

All this means that the only way to measure the pion polarisabilities is in the Compton scattering process near threshold and not in  $\gamma\gamma \rightarrow \pi\pi$ . Though the low energy  $\gamma\gamma \rightarrow \pi\pi$  scattering is seemingly close to the Compton threshold (...) and so the *extrapolation* not very far, the dominance of the pion pole (...) means that the energy scale for this continuation is  $m_\pi$ . Thus the polarisabilities cannot be determined accurately from  $\gamma\gamma$  experiments in a model-independent way and must be measured in the Compton scattering region.