

Study of $\pi^- p \rightarrow \pi^- \eta(\eta) p$ at 190 GeV with the COMPASS experiment



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on behalf of the COMPASS collaboration

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- Lightest scalar nonet and beyond.



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- COMPASS Detector description.
- η reconstruction.



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- A first glimpse of $f_0(1500) \rightarrow \eta \eta$
- PWA description and comparison with standard formalisms.

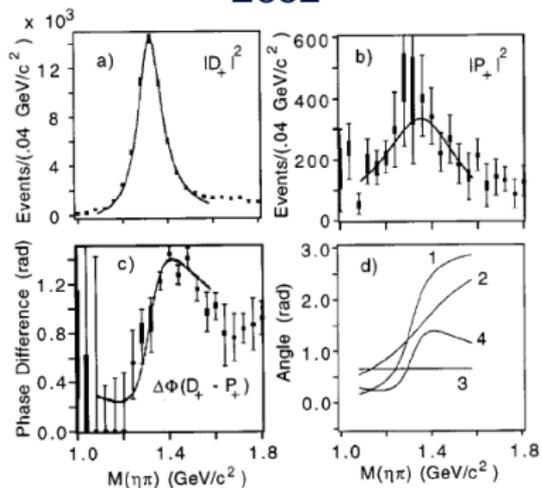


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- PWA description and comparison with standard formalisms.
- Conclusion and outlook.

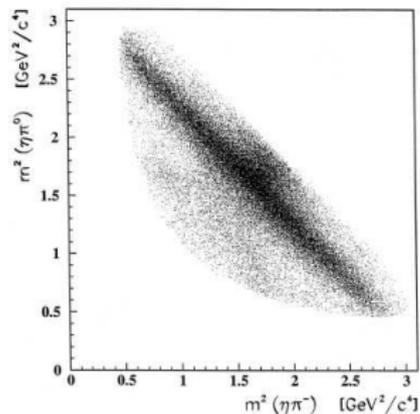


Exotic $\pi(1400)$

E852



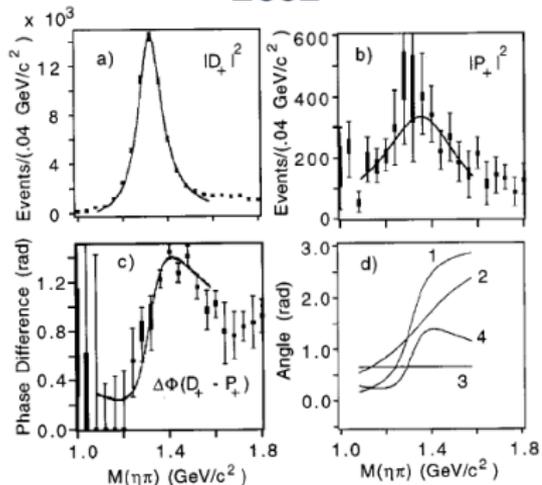
CBAR



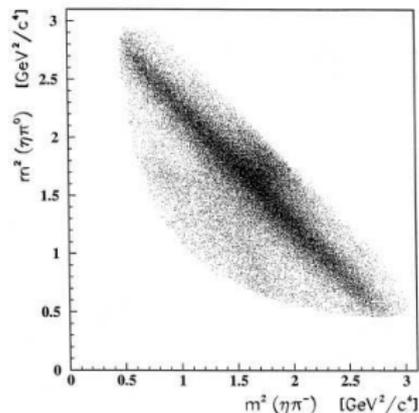
Seen by E852 exp. in $\pi^- p \rightarrow \eta\pi^- p$ at 18 GeV/c (publ. in 1997) and by CBAR exp. in $\bar{p}d \rightarrow \pi^- \pi^0 \eta p_{\text{spectator}}$ (publ. in 1998).



E852



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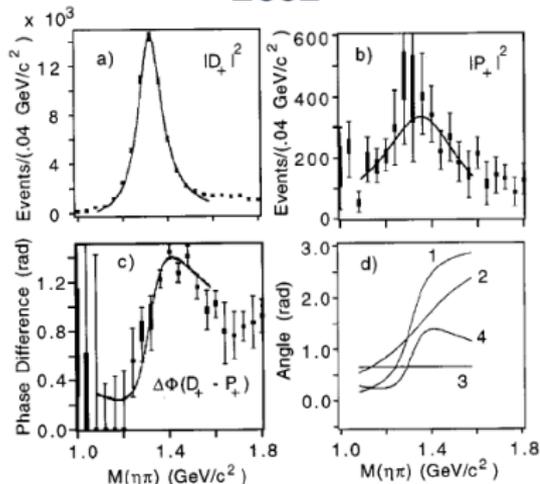


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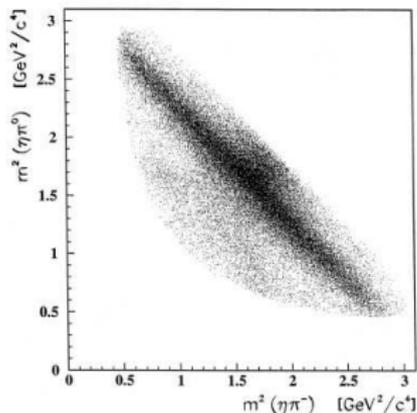
Questioned by Dzierba et al. in 2003 in $\pi^- p \rightarrow \eta\pi^0 n$ at 18 GeV/c.



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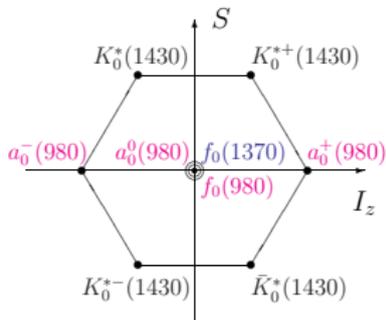
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Confirmed again by E852 in 2007 in $\pi^- p \rightarrow \eta\pi^0 n$ at 18 GeV/c , but with a lower mass ($M = 1257 \pm 20 \pm 25 \text{ MeV}$).

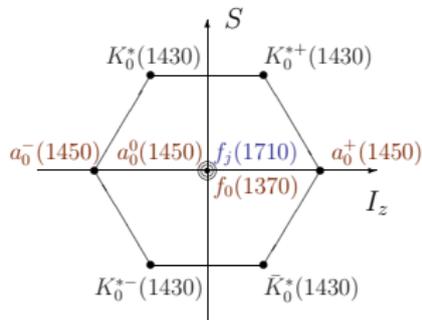


Hypothetical lightest scalar nonets configurations and beyond

Hypo 1 for 0^{++} Nonet

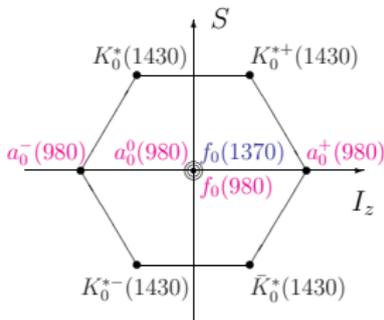


Hypo 2 for 0^{++} Nonet

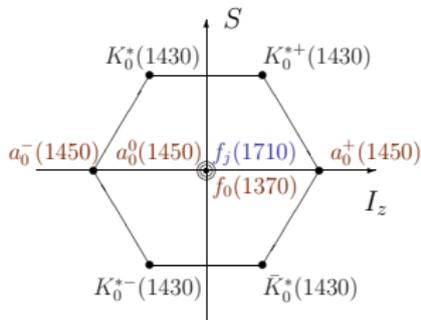


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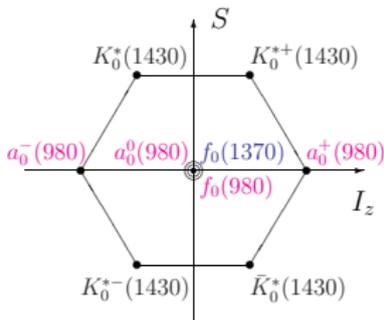


Hypo 3: $f_0(1500)$ supernumerary and therefore may be a glueball

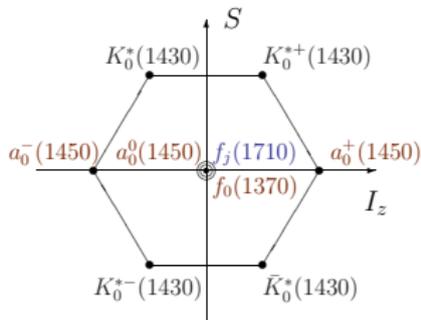


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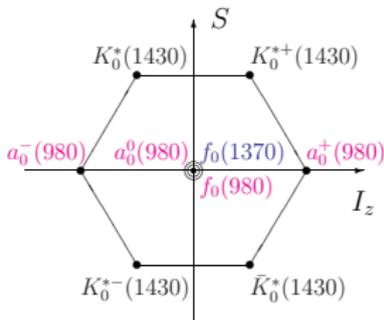
Hypo 3: $f_0(1500)$ supernumerary and therefore may be a glueball

Hypo 4: $a_0(980)$, $f_0(980)$ cusps or members of a **tetraquark** nonet.

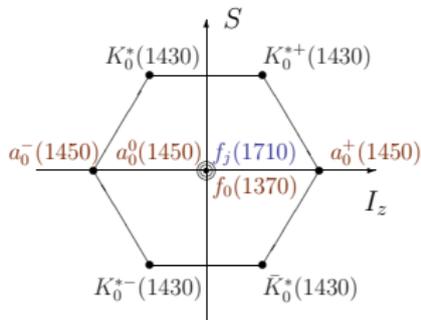


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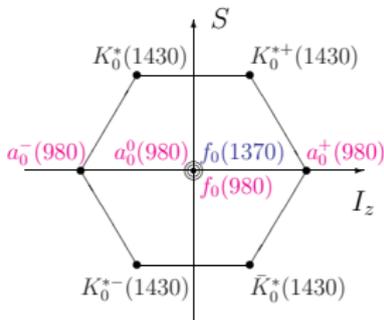
Hypo 4: $a_0(980)$, $f_0(980)$ cusps or members of a tetraquark nonet.

Hypo 5: $f_0(1370)$, $f_0(1500)$, $f_0(1710)$ are the result of the mixing of the glueball (and a tetraquark) with ordinary mesons.

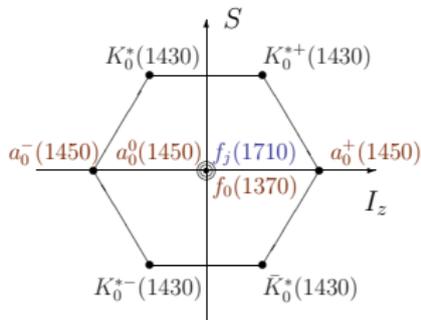


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Mixing scheme is based mainly on the results of WA102 experiment.

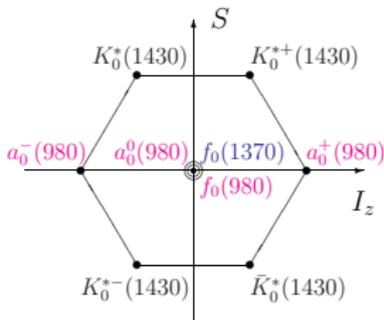
COMPASS goal in centrally produced data is to confirm and improve the observation of WA102:

measure the decay branching widths in $K\bar{K}$, $\pi\pi$, $\eta\eta$, $\eta\eta'$, 4π , $\eta'\eta'$, ...

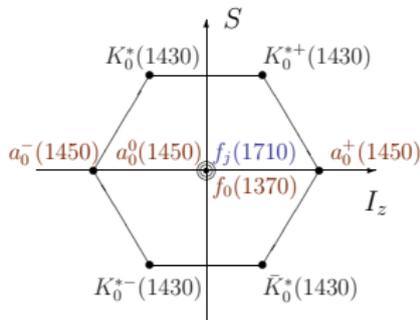


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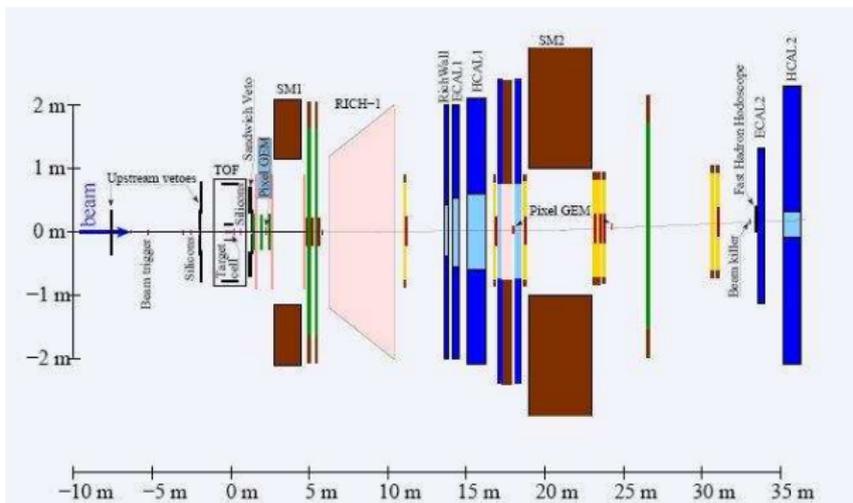
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$\pi^- p \rightarrow \pi^- \eta \eta p$ very selective: $X \rightarrow \eta\eta$ has $I(J^{PC}) = 0(0^{++}, 2^{++}, 4^{++}, \dots)$



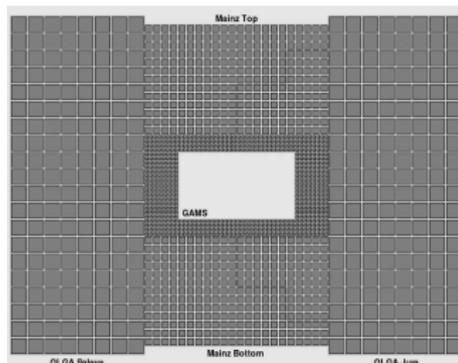
COMPASS setup and detector description



- Two arm spectrometer
- Tracking: Straw, Drift chambers, [MicroMegas](#), [PixelGEM](#), [Recoil Proton Detector](#)
- Calorimetry: [ECAL1 \(2006\)](#), [ECAL2](#), [HCAL1](#), [HCAL2](#), [Sandwich Veto](#)
- Cherenkov: [CEDAR](#), [RICH](#)

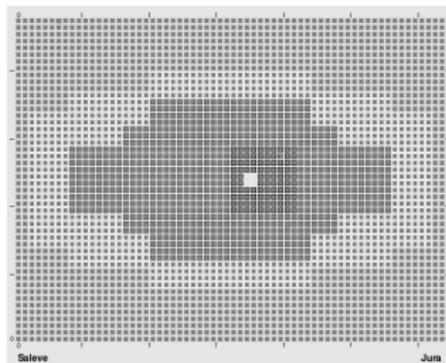


ECAL1



- 11.1 m downstream, low energetic photon detection, $L \times H$: $3.97 \times 2.86 \text{ m}^2$
- 1500 channels:
- OLGA: 302 cells, $14.3 \times 14.3 \text{ cm}^2$
- MAINZ: 572 cells, $7.5 \times 7.5 \text{ cm}^2$
- GAMS: 608 cells, $3.8 \times 3.8 \text{ cm}^2$

ECAL2



- 33.2 downstream, high energetic photon detection, $L \times H$: $2.45 \times 1.94 \text{ m}^2$
- 3068 channels:
- peripheral area: GAMS lead glass blocks $3.8 \times 3.8 \text{ cm}^2$
- central area: new ~ 900 radiation hard SHASHLYK modules $3.8 \times 3.8 \text{ cm}^2$
- New ADC (2008) with 32 sample converters



Pre-selection of exclusive events

- Trigger dedicated to diffractive and "central" reactions.
- Loop to all primary vertexes.
- Interaction in the target: $-69 < z_{\text{vertex}} < -29$ cm and $r_{\text{vertex}} < 1.5$ cm.
- 1 outgoing negative track with $E_{\text{track}} < 180$ GeV.
- 2 and 4 **good** clusters in **ECAL1** and in **ECAL2** for the 2γ and 4γ channels, respectively:



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 - ▶ not pointed by a track.
 - ▶ noise suppression.
 - ▶ $E_{clus_{min}} > 1$ GeV in **ECAL1** and $E_{clus_{min}} > 4$ GeV in **ECAL2**.
 - ▶ in time with the beam: $-3 < t_{cluster} - t_{beam} < 5$ ns.

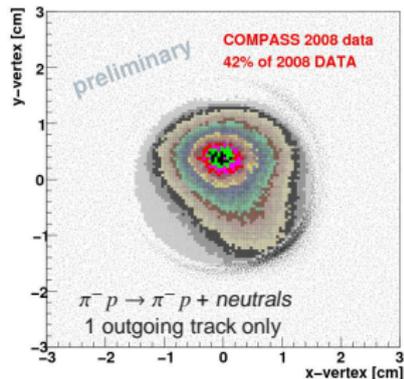
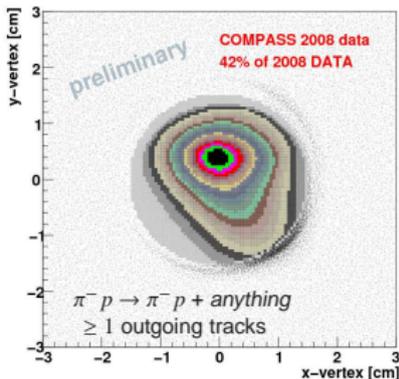
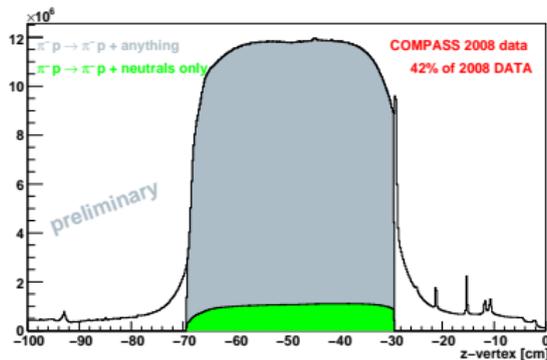


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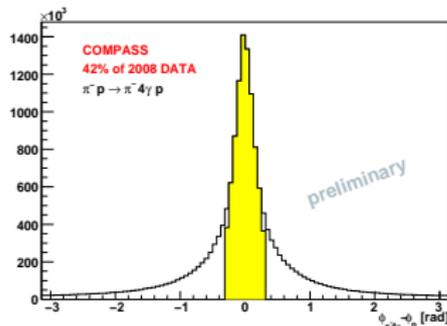
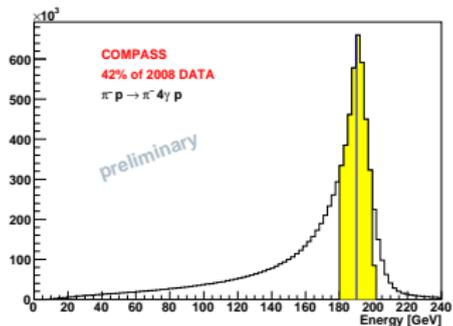
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 - ▶ in time with the beam: $-3 < t_{cluster} - t_{beam} < 5ns$.
- Correction of the photons momenta assuming they originate from the primary vertex.
- Correlation with RPD: $-0.3 < \phi_{\pi^{-n\gamma}} - \phi_p < 0.3$ rad.
- Energy balance: $180 < E_{\pi^{-n\gamma}} < 200$ GeV assuming the track to be a pion.
- $\pi^0, \eta \rightarrow \gamma_1\gamma_2$: 1 combination.
 $\pi_1^0, \eta_1 \rightarrow \gamma_i\gamma_j, \pi_2^0, \eta_2 \rightarrow \gamma_k\gamma_m$: 3 combinations.



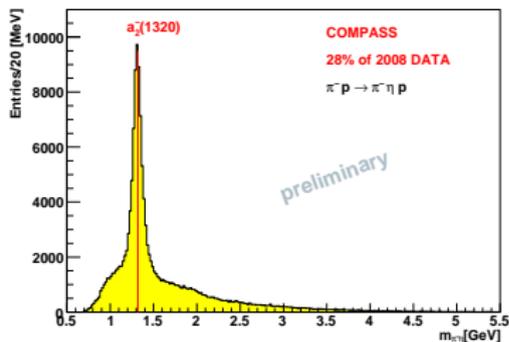
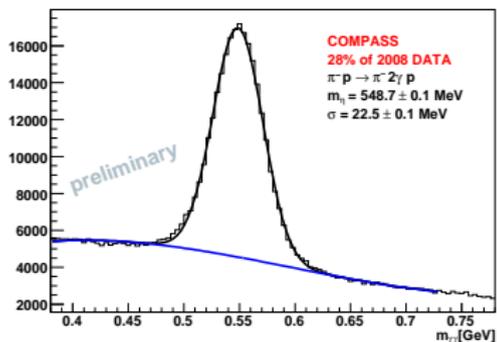
Vertex distributions



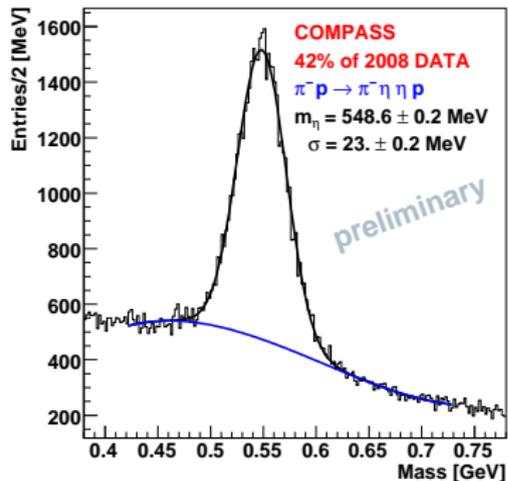
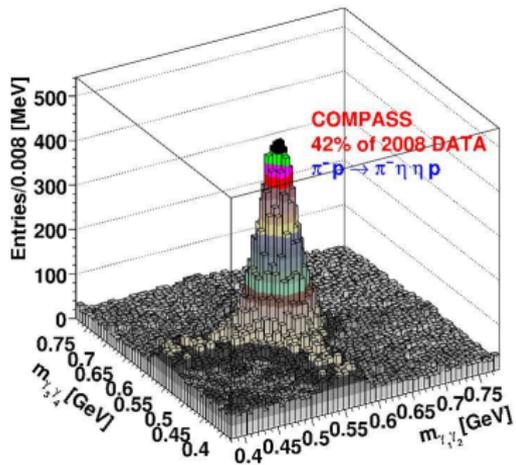
Recoil Proton Detector and exclusivity cuts



η and two-body $\eta\pi^-$ invariant masses in the 2γ channel



η masses in the 4γ channel



Preliminary statistics of $\pi^- p \rightarrow \pi^- \pi^0(\eta)p$

Amount of processed data (28% of 2008 data)	100.00%
DT0 trigger	73.17%
Majority < 6 for CEDAR1 and CEDAR2	71.75%
Primary vertex	66.15%
$-69 < z_{vertex} < -29$ cm	54.44%
$r_{vertex} < 1.5$ cm	52.92%
1 negative track	4.89%
Two golden clusters	0.93%
$-0.3 < \phi_{\pi^- 2\gamma} - \phi_p < 0.3$	0.25%
Exclusivity ($180 < E_{\pi^- 2\gamma} < 200$ GeV)	0.06%
$100 < m_{\pi^0} < 170$ MeV	31.2% of excl. events
π^0 1C $CL > 10\%$ (π^0 mass)	14.6% of excl. events
$450 < m_{\eta} < 650$ MeV	21.6% of excl. events
η 1C $CL > 10\%$ (η mass)	8.1% of excl. events

- A preliminary sample of about 150K fitted $\pi^- p \rightarrow \pi^- \eta p$ events is used for the amplitude analysis.
- Better statistics will be achieved with improved calorimeter calibration (2008 data) and additional LASER and LED calorimeter monitoring system (2009 DATA).



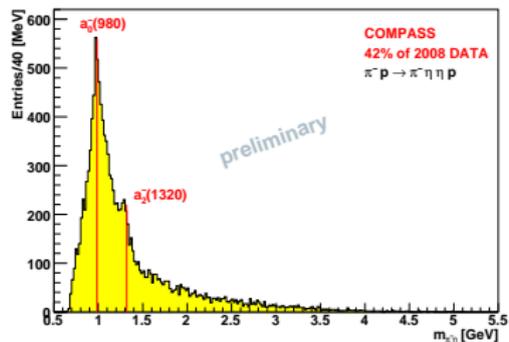
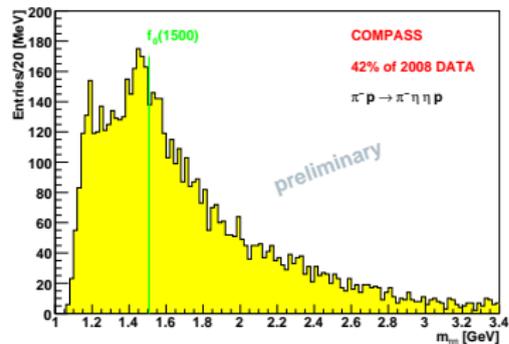
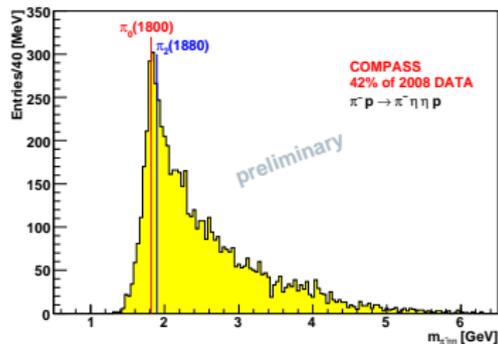
Preliminary statistics of $\pi^- p \rightarrow \pi^- \eta \eta p$

Amount of processed data (42% of 2008 data)	100.00%
DT0 trigger	73.78%
Majority < 6 for CEDAR1 and CEDAR2	72.49%
Primary vertex	66.91%
$-69 < z_{vertex} < -29$ cm	54.81%
$r_{vertex} < 1.5$ cm	53.36%
1 negative track	4.94%
Four good clusters	0.61%
$-0.3 < \phi_{\pi^- 4\gamma} - \phi_p < 0.3$	0.21%
Exclusivity ($180 < E_{\pi^- 4\gamma} < 200$ GeV)	0.10%
$\sqrt{(m_{\gamma_1\gamma_2} - m_{\pi^0})^2 + (m_{\gamma_3\gamma_4} - m_{\pi^0})^2} < 25$ MeV	69.78% of excl. events
$2\pi^0$ 2C CL > 10% (π^0 mass)	27.39% of excl. events
$\sqrt{(m_{\gamma_1\gamma_2} - m_{\eta})^2 + (m_{\gamma_3\gamma_4} - m_{\eta})^2} < 25$ MeV	0.17% of excl. events
2η 2C CL > 10% (η mass)	0.13% of excl. events

- A preliminary sample of about 5K fitted $\pi^- p \rightarrow \eta \eta p$ events is used for the amplitude analysis.
- Comparable amount of data is available in $\pi^- p$ and in $p p$ at 190 GeV in the 2009 run.
- Better statistics will be achieved with improved calorimeter calibration (2008 data) and additional LASER and LED calorimeter monitoring system (2009 DATA).
- The statistics will be further increased by using the mixed decay mode of one of both η s in $\pi^+ \pi^- \pi^0$.



Two and three-body inv. masses in the 4γ channel

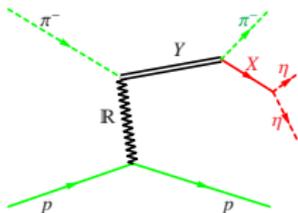


Production mechanisms

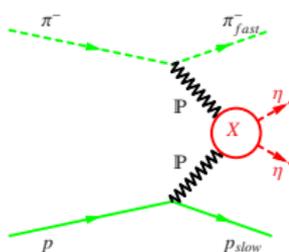
At 190 GeV incoming beam energy two compelling mechanisms for the production process of a state X are possible:

- as a product of the decay of a diffractively produced state Y : $\pi^- p \rightarrow Y p$, $Y \rightarrow \pi^- X$, $X \rightarrow \eta\eta$
- centrally produced via Double Pomeron Exchange: $\pi^- p \rightarrow \pi^-_{fast} X p$, $X \rightarrow \eta\eta$

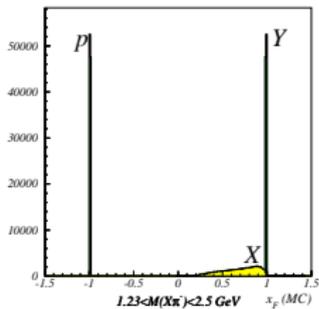
Diffractive dissociation



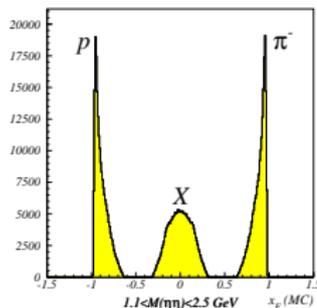
Central production



MC of diffractive dissociation



MC of central production



x_f and rapidities overlap: both processes have to be fitted simultaneously!



Amplitude Ansatz for the decay process

- Amplitude (isobar model):

$$A_J^\lambda = G_\lambda e^{i\delta_\lambda} F_J(q) \frac{Y_J^\lambda(\alpha, \beta)}{m_0^2 - s - im_0\Gamma(m)}$$

- Blatt-Weisskopf barrier factors
- Angular part: spherical harmonics, decay angles α, β after "Wick rotations" (no D-functions needed).
- Relativistic Breit Wigner

$$\Gamma(m) = \Gamma_0 \left(\frac{m_0}{m} \frac{q}{q_0} \frac{F_J^2(q)}{F_J^2(q_0)} \right)$$

$$w(m, m_0, m_1) = \sum_J [|A_{X_J}^\lambda(m, m_0)|^2 + |A_{Y_J}^\lambda(m, m_1)|^2 + 2 c_{\lambda} \Re(A_{X_J}^\lambda(m, m_0) A_{Y_J}^{\lambda*}(m, m_1))]$$



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- Relativistic Breit Wigner**

- Relativistic mass dependent width:

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$$w(m, m_0, m_1) = \sum_J [|A_{X_J}^\lambda(m, m_0)|^2 + |A_{Y_J}^\lambda(m, m_1)|^2 + 2 c_{\lambda} \Re(A_{X_J}^\lambda(m, m_0) A_{Y_J}^{\lambda*}(m, m_1))]$$



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Minimization and comparison with standard PWA

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 $G_\lambda, \delta_\lambda, c_\lambda$: free parameters of the fit
With this definition, and for a fixed set of parameters, a reduction of $\ln\mathcal{L}$ by 0.5 is statistically significant and corresponds to one standard deviation in mass and width optimizations.
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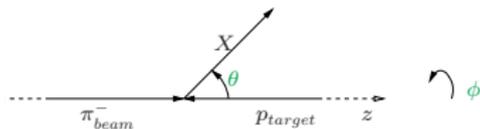
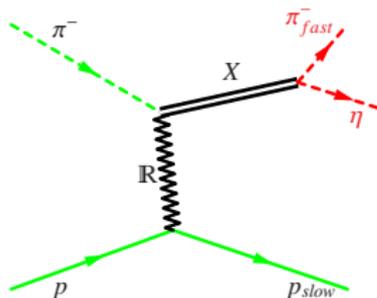
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Backup Slides



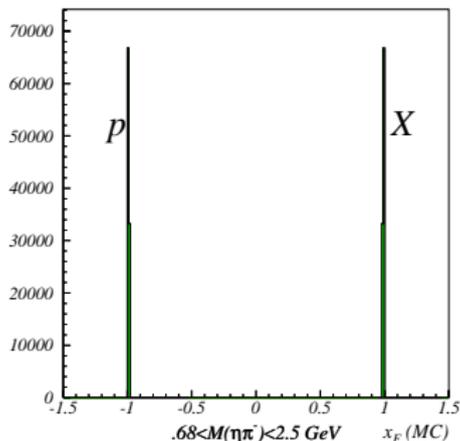
Simulation of the production of a diffractive X in $\pi^- p \rightarrow X p$ with $X \rightarrow \pi^- \eta$



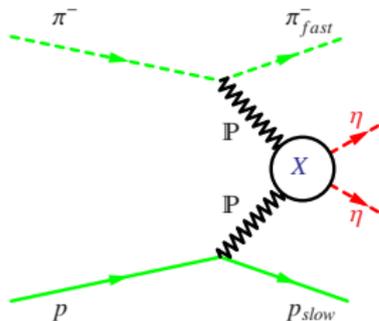
- M_X uniformly from $m_\pi + m_\eta$ to 3.5 GeV
- t_X as e^{-bt} with $b = 6 \text{ GeV}^{-2}$ with $0 < t < 1 \text{ GeV}^2$. To take into account a resonance dependent production mechanism the shape of the t -distribution will be optimized from the data in different mass ranges around the resonance masses.
- $\phi_X(\phi_p)$ uniformly from 0 to 2π

$$1 - x_X = \frac{M_X^2 - m_{\pi^-}^2}{s}$$

$$p_{T,X}^2 = -t_X$$



Simulation of the production of a central X in $\pi^- p \rightarrow X p$ with $X \rightarrow \eta\eta$



$$x_{P_1} - \frac{M^2}{s} \frac{1}{x_{P_1}} = \frac{M_T}{\sqrt{s}} (e^y - e^{-y})$$

Solution:

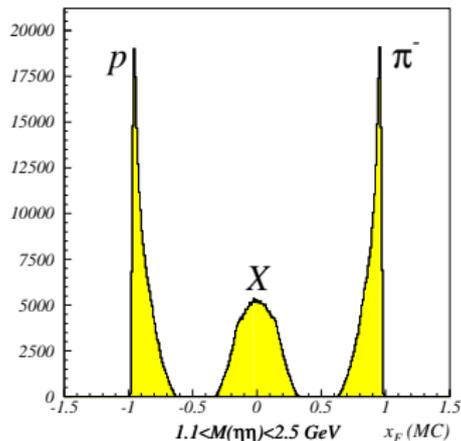
$$x_{P_1} = \frac{M_T}{\sqrt{s}} \left[\pm \sqrt{\left(\frac{M_X}{M_T}\right)^2 + (\sinh y)^2} + \sinh y \right]$$

- M_X uniformly from $2m_\eta$ to 3.5 GeV
- t_X as e^{-bt} with an average $b = 6 \text{ GeV}^{-2}$ with $0 < t < 1 \text{ GeV}^2$. The optimization of a resonance dependent t-distribution will be obtained from the data.
- Flat rapidity distribution $-1 < y(X) < 1$
- $\phi_X(\phi_p)$ uniformly from 0 to 2π

$$M_X^2 = -x_{P_1} x_{P_2} s$$

$x_{P_2} = 1 - x_\pi$ on the π side, $x_{P_1} = x_p - 1$ on the p side
In the center of mass

$$x_p + x_\pi + x_X = 0 \quad x_X = M_T \frac{e^y - e^{-y}}{\sqrt{s}} = \frac{2M_T \sinh y_{cm}}{\sqrt{s}}$$



Wick rotation and amplitude Ansatz



Definition of angles for a diffractive X in $\pi^- p \rightarrow \pi^- X p$, $X \rightarrow \pi^- \eta p$:

- The z axis is defined in the πp c.m. frame. The x, y axes are defined by the angle formed by the production plane and the decay plane.
- The Wick rotation by angles $-\phi$ and θ to the direction of flight of the diffractive X are followed by a Lorentz boost to the its rest frame (x', y', z') and by another rotation by $-\theta$ and $-\phi$ so that the direction of the new reference frame x'', y'', z'' correspond to one of x, y, z .
- α, β define the direction of one η in the rest frame of X after the Wick rotations. The effect of the Lorentz boost is to leave the η with final momenta different from those in the overall πp rest frame.

The angles α, β obtained in this reference frame after Wick rotations enter in the decay amplitude definition:

- $$A_J^\lambda = G_\lambda e^{i\delta_\lambda} F_J(q) \frac{Y_J^\lambda(\alpha, \beta)}{m_0^2 - s - im_0 \Gamma(m)}$$

