



# Diffractive pion production at COMPASS – First results on $3\pi$ final states – neutral mode



Frank Nerling

*Universität Freiburg, Physikalisches Institut*

on behalf of the  
COMPASS Collaboration

*Hadron 2009, XIII Intern. Conf. on Hadron Spectroscopy,  
Nov 29th – Dec 4th 2009, Florida State University*

## Outline:

- The COMPASS experiment:
- Diffractive dissociation into  $3\pi$  final states
- First look into  $3\pi$  neutral mode
  - Event selection
  - First PWA fits, main waves



bmb+f - Förderschwerpunkt  
**COMPASS**  
Großgeräte der physikalischen  
Grundlagenforschung



# The COMPASS experiment

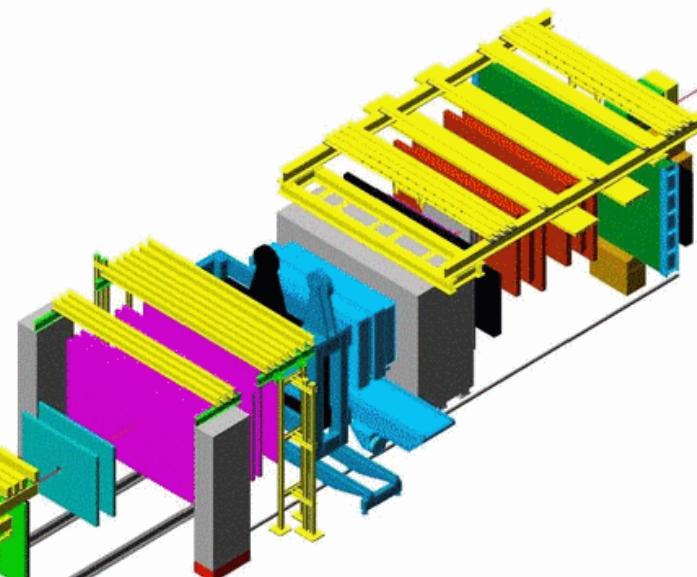
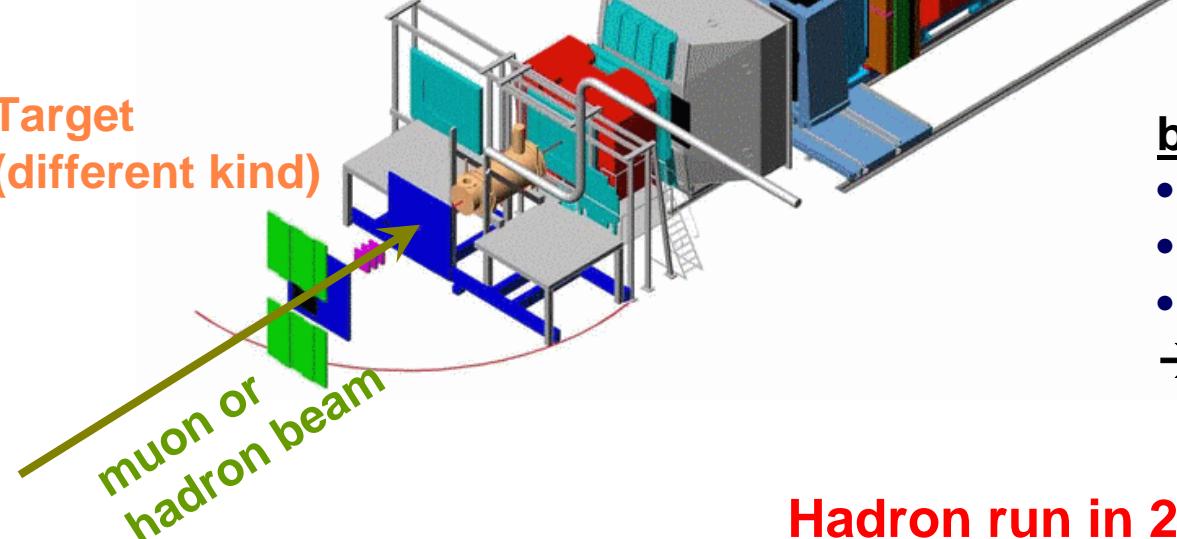


COmmon Muon Proton Apparatus for Structure and Spectroscopy  
(~270 physicists, 25 institutes, 12 countries)

## a) Nucleon spin structure:

- polarised muon beam ( $160 \text{ GeV}/c \mu^+$ )
- data taken 2002-04, 2006/07

Target  
(different kind)



## b) Nucleon & meson spectroscopy:

- Diffractive production
  - Central production
  - Primakoff
- Hadron beams ( $190 \text{ GeV}/c \pi^-, K^-$ )

Hadron run in 2008 & 2009 (after pilot run in 2004)



# The COMPASS experiment

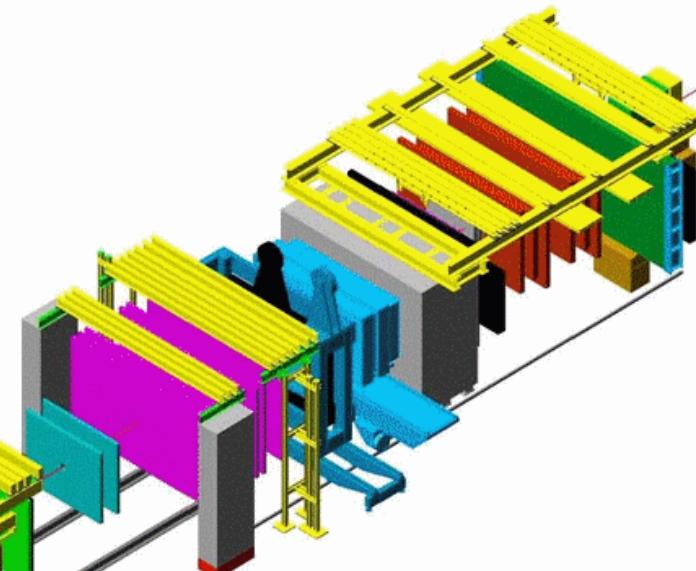


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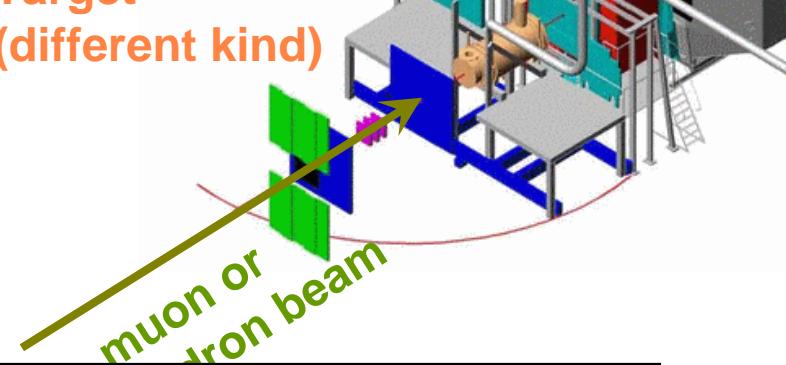
## a) Nucleon spin structure:

- polarised muon beam ( $160 \text{ GeV}/c \mu^+$ )
- data taken 2002-04, 2006/07

→ see 3D



Target  
(different kind)



## b) Nucleon & meson spectroscopy:

- Diffractive production
- Central production
- Primakoff

→ see 6D

→ see 7D,8C

→ Hadron beams ( $190 \text{ GeV}/c \pi^-, K^-$ )

[hep-ex/0703049, NIM A 577, 455 (2007)]

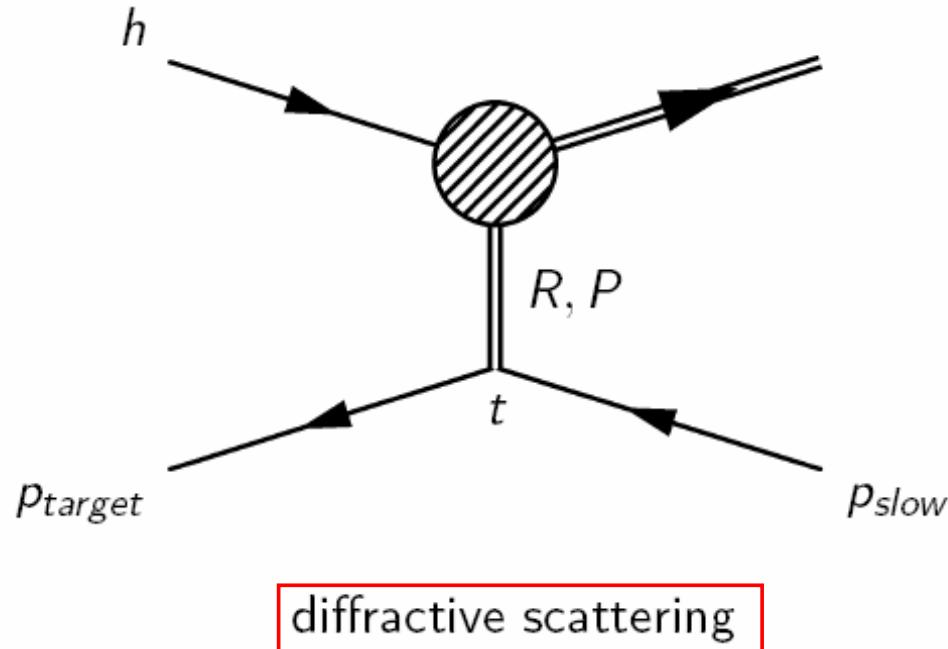
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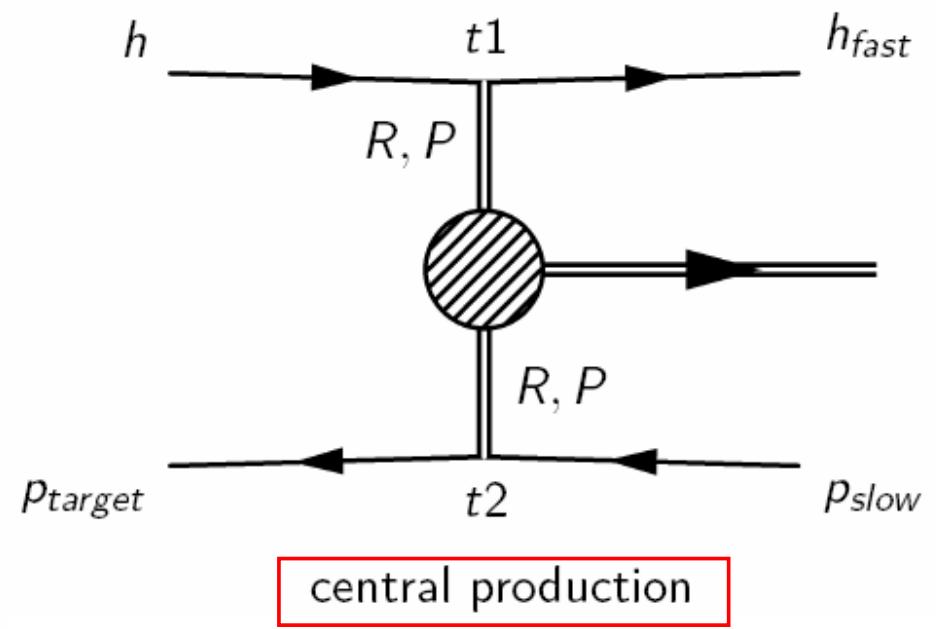
# COMPASS Hadron spectroscopy



- study of  $J^{PC}$  exotic mesons
- t-channel Reggeon Exchange
- forwards kinematics, target stays intact



- large rapidity gap between  $p_{\text{slow}}, h_{\text{fast}}, X$
- possible source of glueballs



## Light meson sector ( $< 2.2 \text{ GeV}/c^2$ ):

exotics  $J^{PC} = 1^{+-}$

- $\pi_1(1400)$ : VES, E852, Crystal Barrel
- $\pi_1(1600)$ : E852, VES

.... still controversial → COMPASS

Also: **photo-production**, e.g.  
 $\mu^- p \rightarrow \mu^- p_{\text{slow}} + X^0$



# COMPASS Hadron spectroscopy

## -- Diffractive pion dissociation

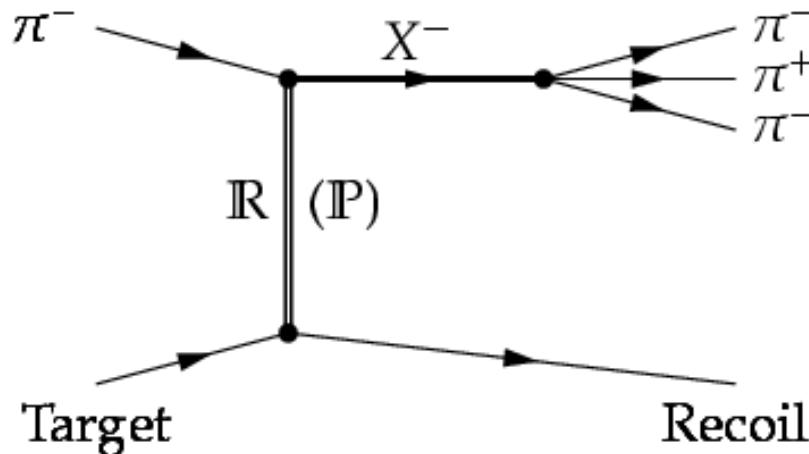


### Diffraction:

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### Diffr. pion dissociation:

- incoming  $\pi^-$  excited to resonance  $X^-$
- $X^-$  decays into final state, e.g.  $(3\pi)^-$ :  
 $\pi^- p \rightarrow \pi^-\pi^+\pi^- p$  (charged mode)



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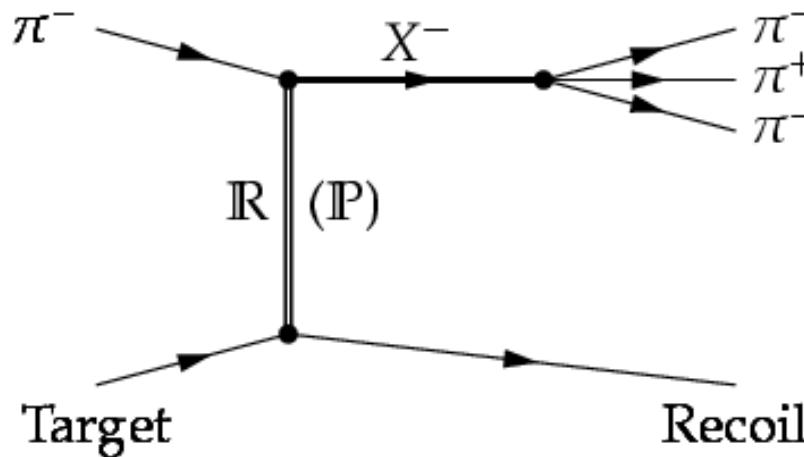


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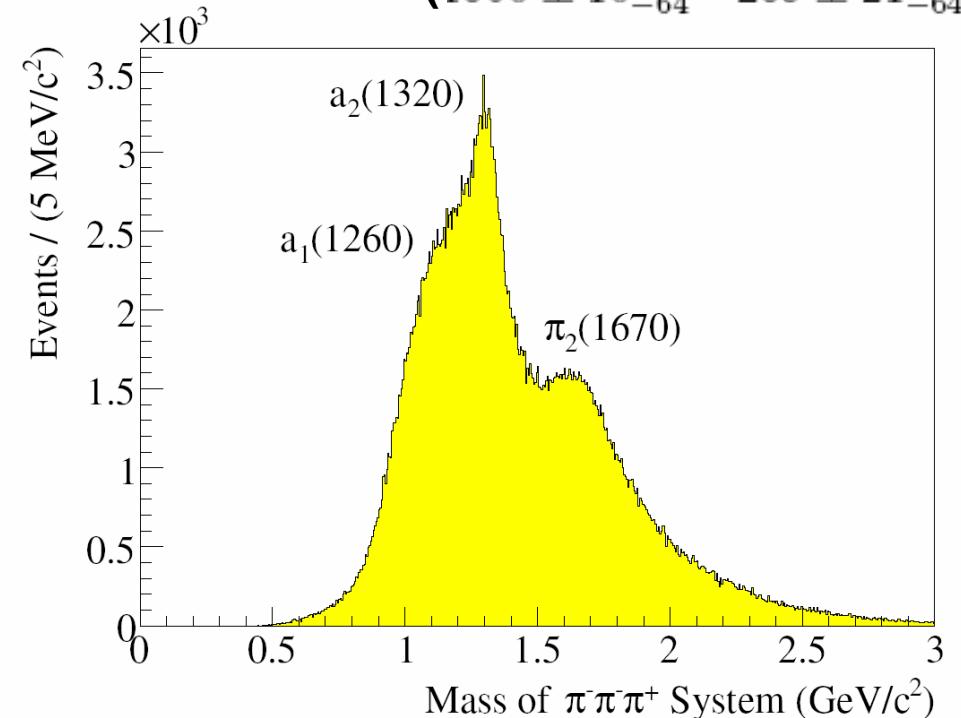
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### Submitted to Phys.Rev.Let:

$J^{PC}$  exotic  $\pi_1(1600)$  evidence in 2004 data (Pb):

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# COMPASS Hadron spectroscopy

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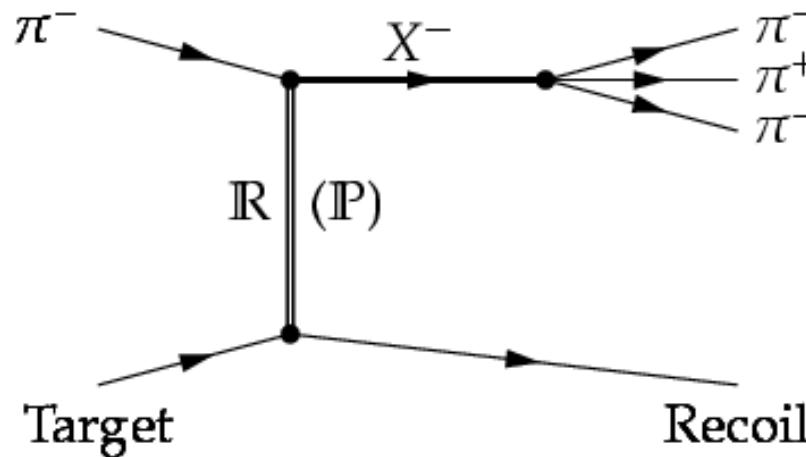


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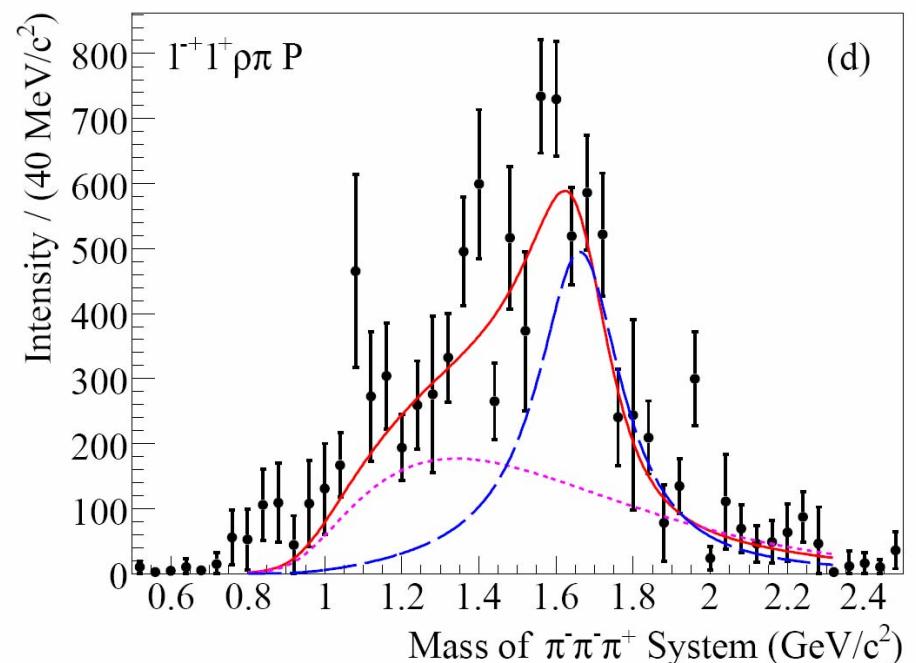
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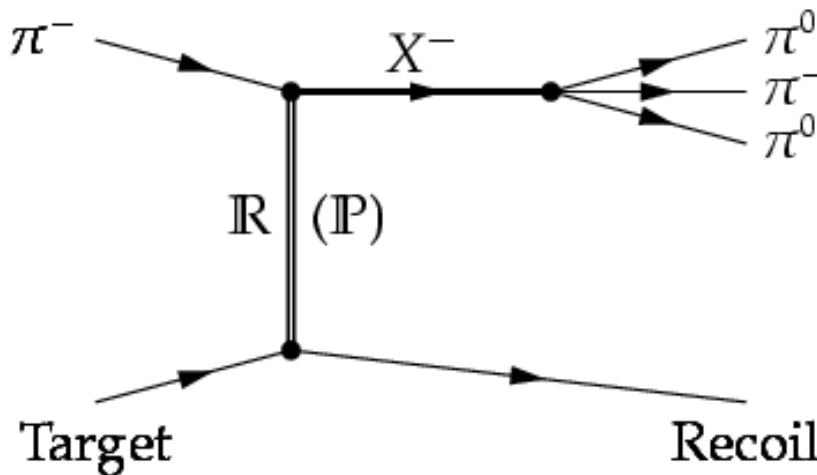
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## -- Diffractive pion dissociation



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- $X^-$  decays into final state, e.g.  $(3\pi)^-$ :  
 $\pi^- p \rightarrow \pi^- \pi^+ \pi^- p$  (charged mode)  
 $\pi^- p \rightarrow \pi^- \pi^0 \pi^0 p$  (neutral mode)

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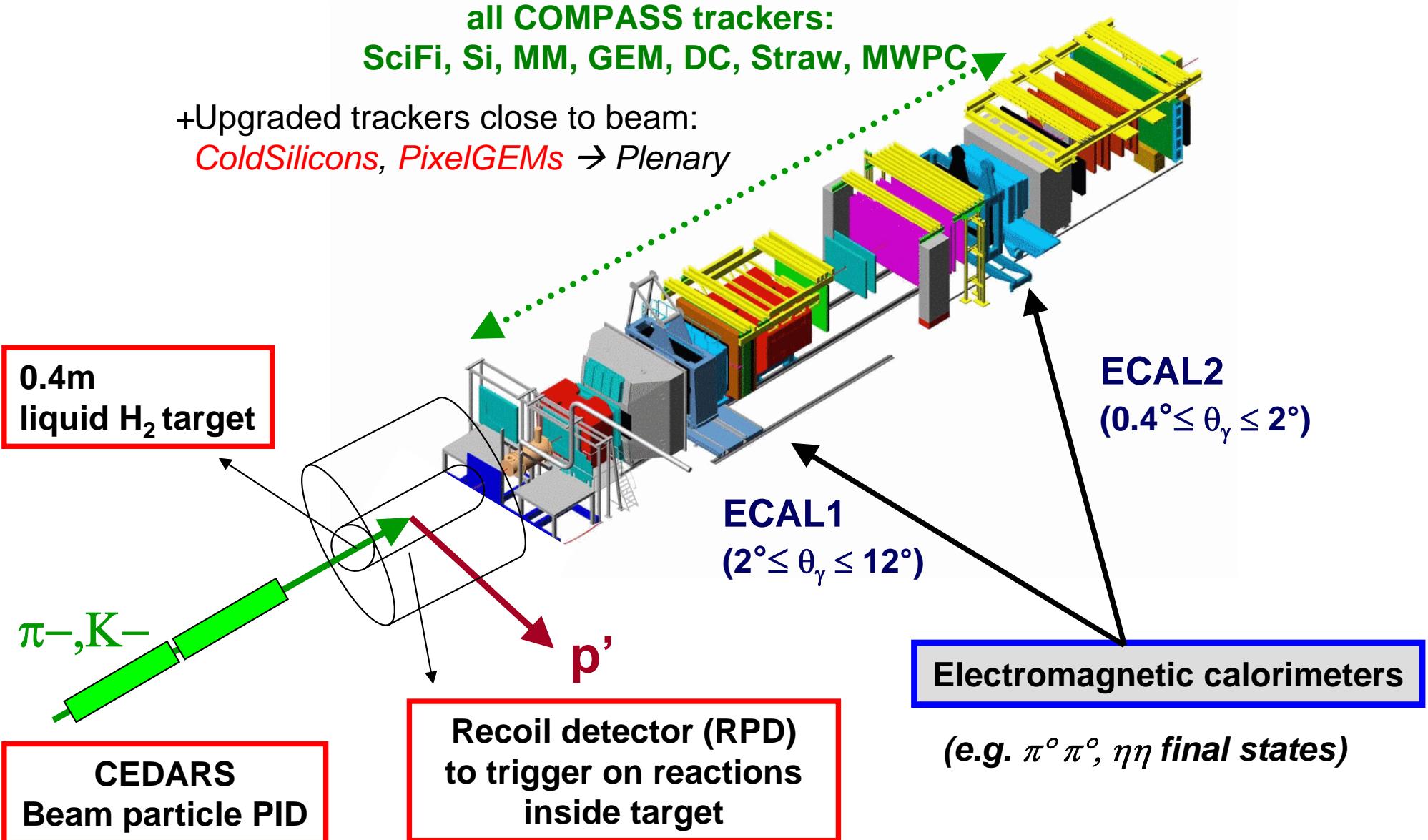
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- Analysis of 2008 data started (p-target)
  - Simultaneous observation in neutral mode
    - independent measurement (same apparatus)
    - => important cross check (understand acceptance)
- 1st look into neutral mode (main waves, isospin sym.)



# COMPASS spectrometer: Hadron setup 2008/09

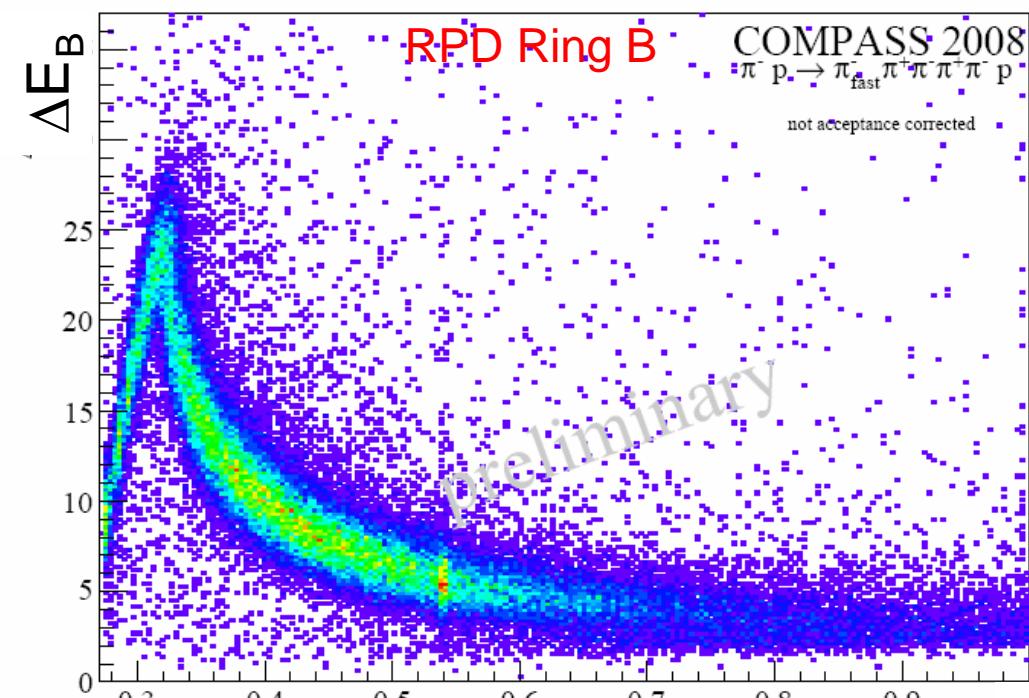
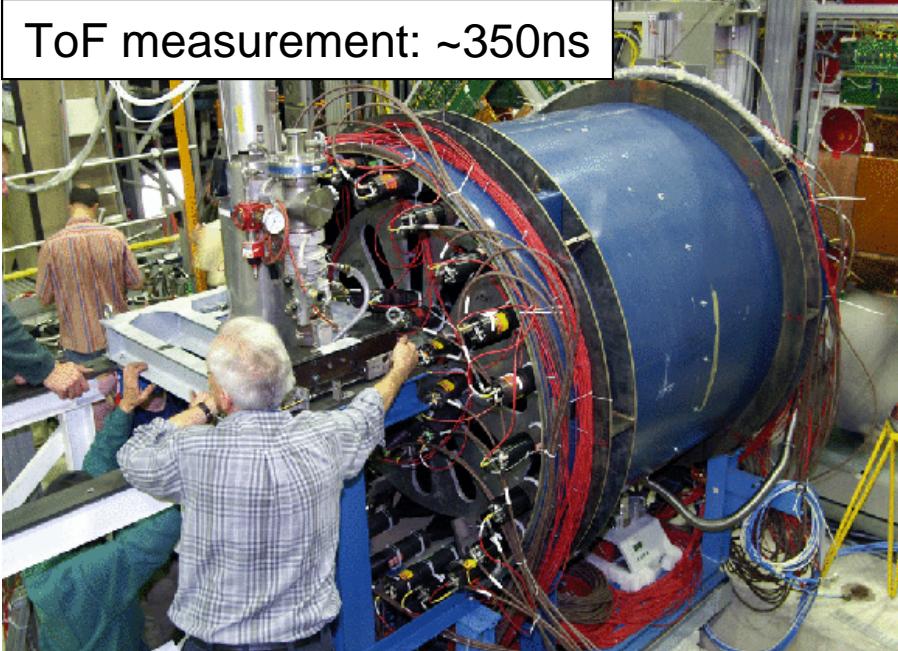




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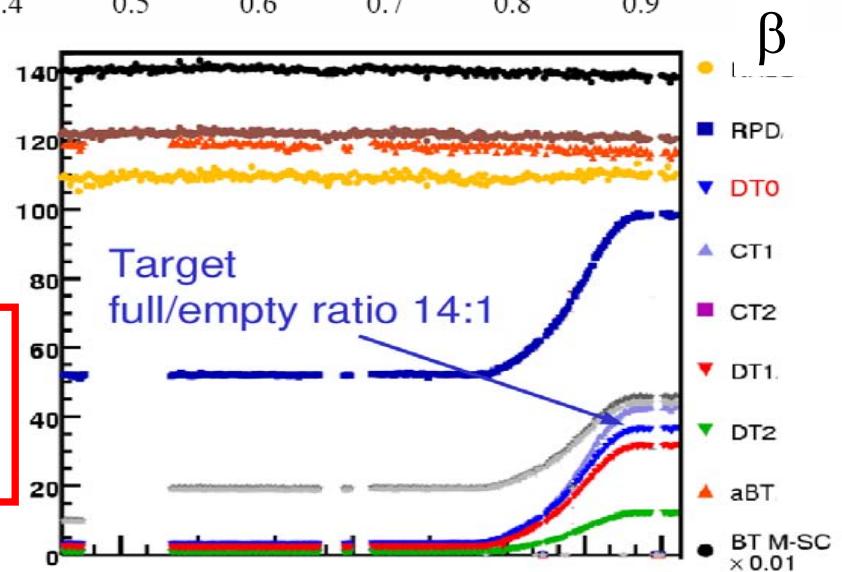


ToF measurement: ~350ns



Diffractive Trigger = BT  $\wedge$  RPD  $\wedge$  !Veto

Recoil detector (RPD)  
to trigger on reactions  
inside target

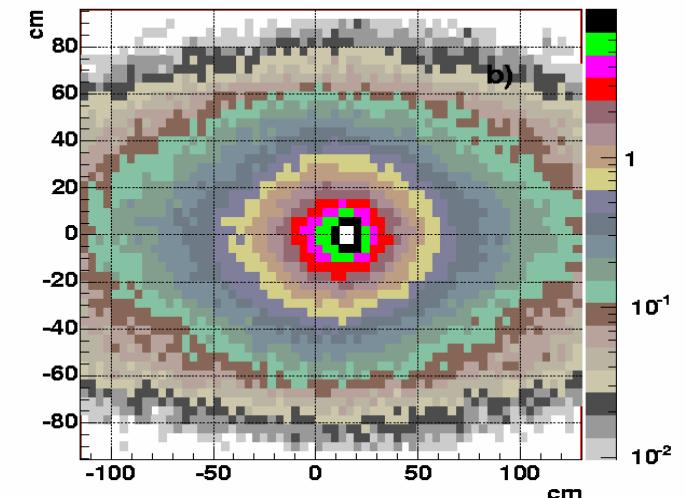




# COMPASS spectrometer: Hadron setup 2008/09



Radiation doses deposited in the ECal2



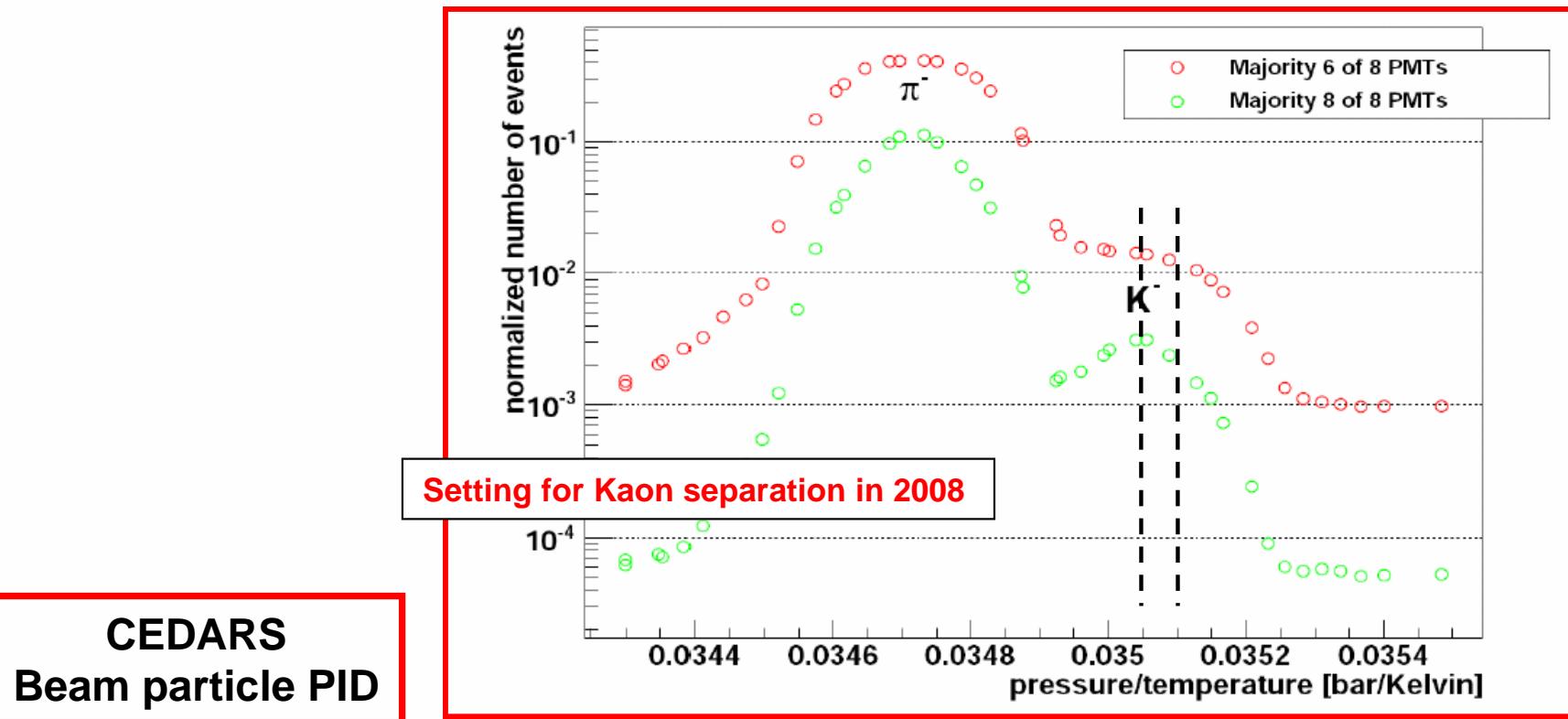
## Electromagnetic calorimeters

### ECal2:

- rad. hard shashlik counter
- 10bit SADC → 12bit MSADC
- DSP → timing info



# COMPASS spectrometer: Hadron setup 2008/09





# Event selection: $\pi^- p \rightarrow \pi^-\pi^0\pi^0 p$



~10% of 2008 data

Type of cut applied	Nb of events	Remaining [%]
All events	$6.98800 \times 10^8$	100.00
DT0	$5.07415 \times 10^8$	72.61
NbPV==1	$4.02453 \times 10^8$	57.59
NbOutPar==1	$2.25624 \times 10^8$	32.29
TargetCut	$1.80785 \times 10^8$	25.87
ChargeSum	$1.76766 \times 10^8$	25.30
$N_\gamma == 4$	$9.75743 \times 10^6$	1.40
$2\pi^0$ within $m_{\pi^0}(\text{PDG}) \pm 20$ MeV	$9.15084 \times 10^5$	0.13
exactly one $2\pi^0$ combination within $m_{\pi^0}(\text{PDG}) \pm 20$ MeV	$8.99705 \times 10^5$	0.13

Table 1: Remaining statistics after cuts - Preselection.

Type of cut applied	Nb of events	Remaining [%]
All events - preselected	$8.99705 \times 10^5$	100.00
$E_{\pi^-} < 185 \text{ GeV}/c^2$	$8.20096 \times 10^5$	91.15
RPDtracks==1 && $p_{\text{recoil}} > 250$ MeV	$5.85308 \times 10^5$	65.06
$\Delta\Phi < 0.2$	$3.95250 \times 10^5$	43.93
Tightened cut on $\pi^0$ mass ( $m_{\pi^0}(\text{PDG}) \pm 16$ MeV)	$3.25001 \times 10^5$	36.12
Exclusivity $\pm 6$ GeV	$2.41406 \times 10^5$	26.83
CEDAR Veto on Kaons	$2.39511 \times 10^5$	26.62

Table 2: Remaining statistics after further cuts applied on preselected events, cf. Tab. 1 - Final Selection.



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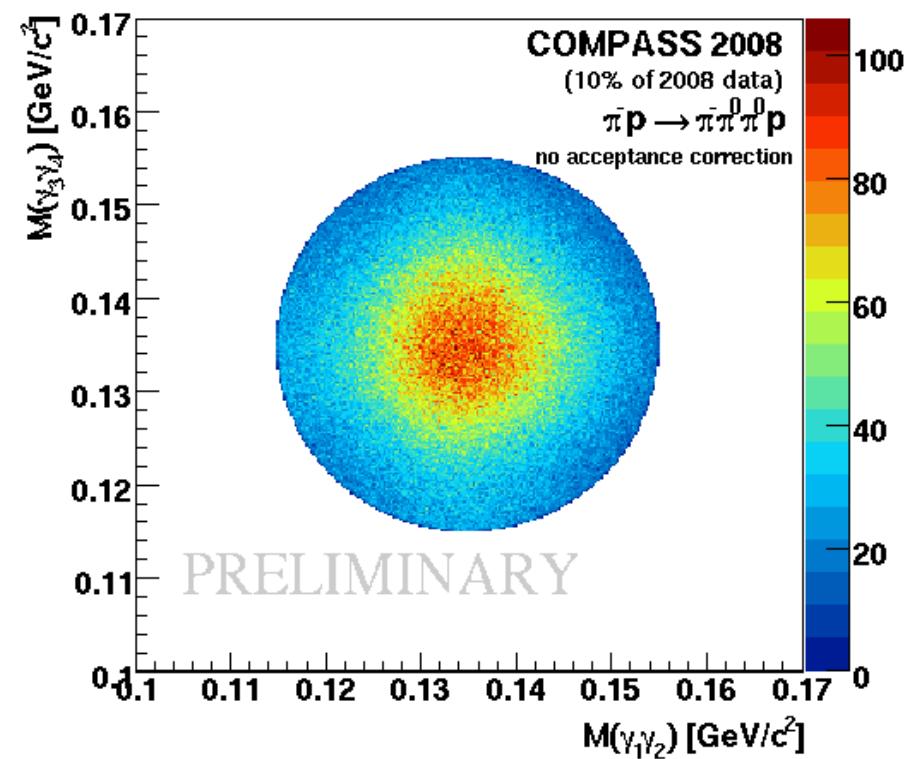
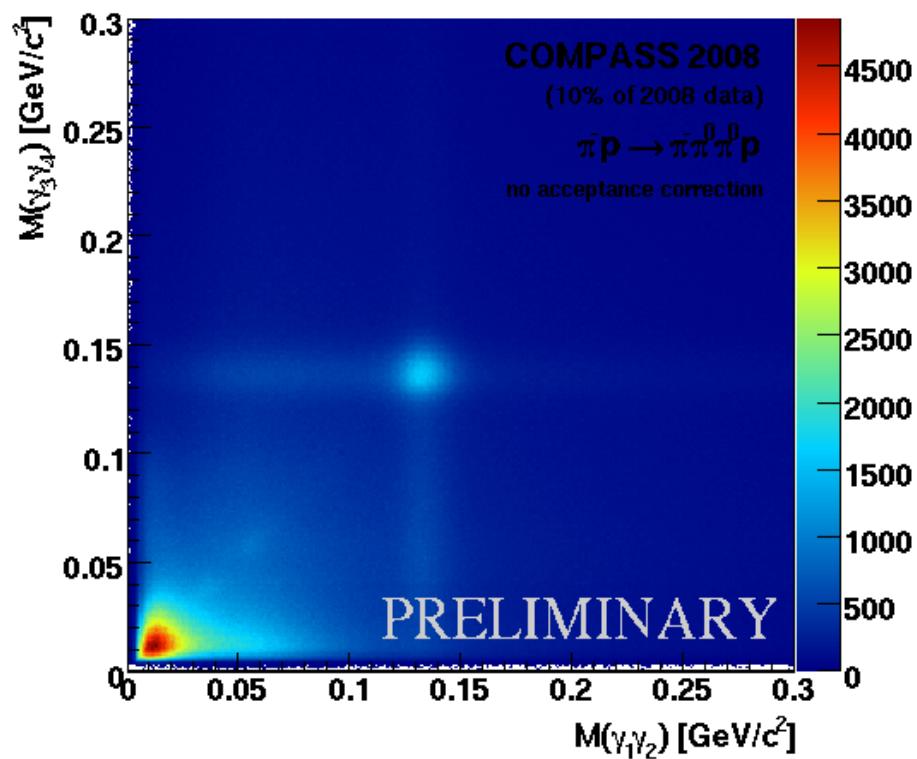
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Main cuts for exclusive events:  
=> in terms of sigma ( $\pm 2\sigma$ )

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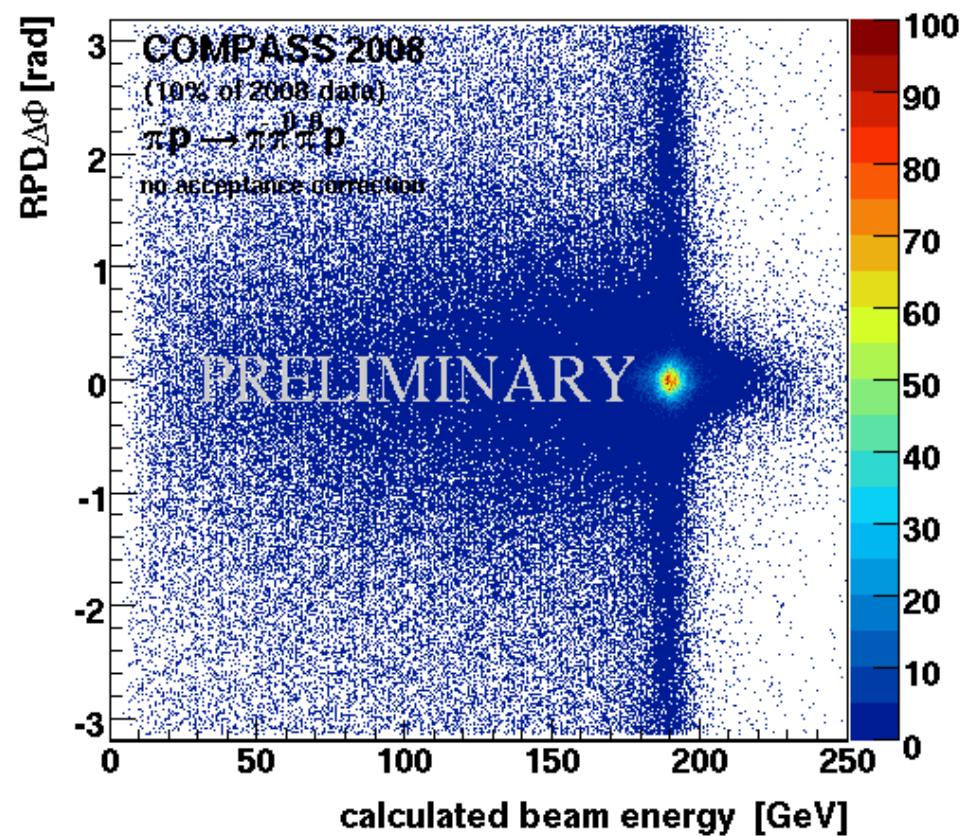
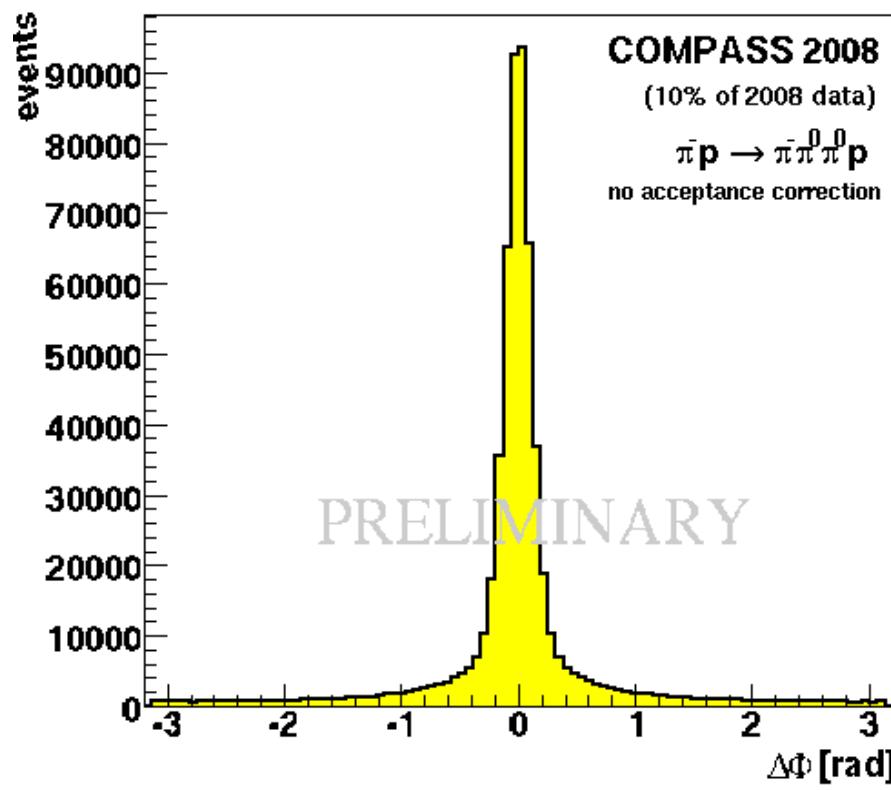
# All & Preselected gg pairs, circular cut on PDG $\pi^0$ mass



$2\pi^0$  evt := exactly 4 clusters, exactly one  $2\pi^0$  combi within PDG  $\pm$  20 MeV

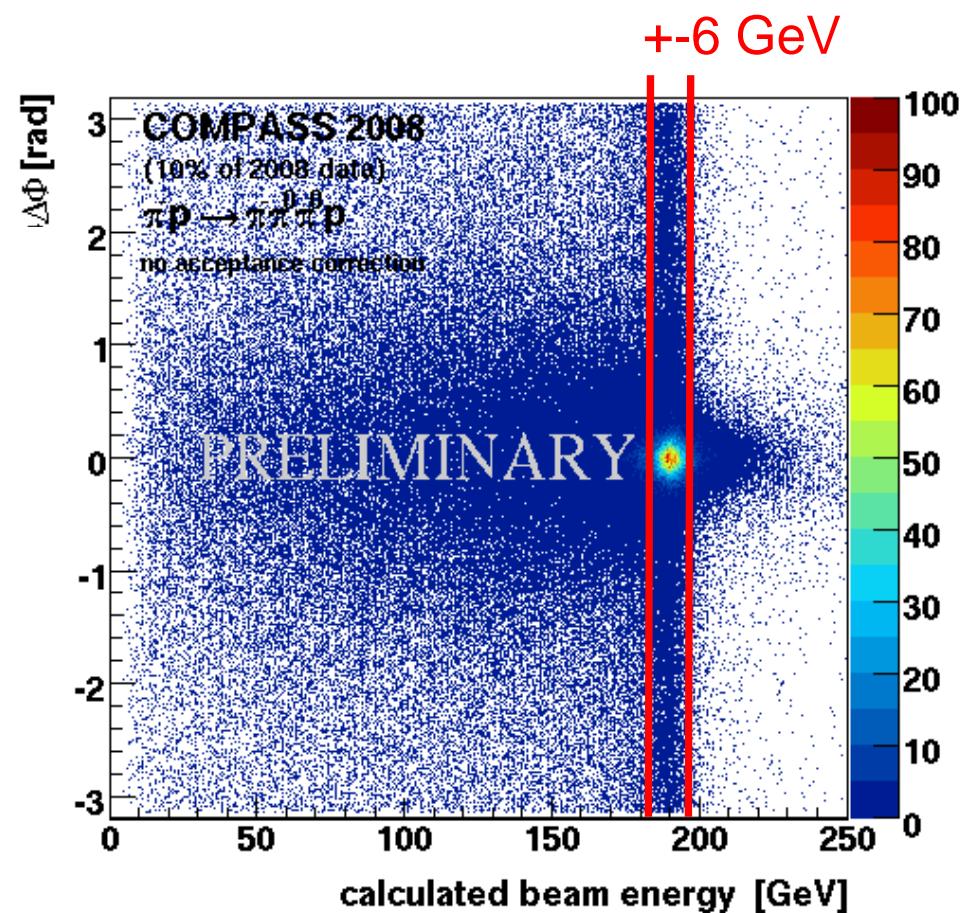
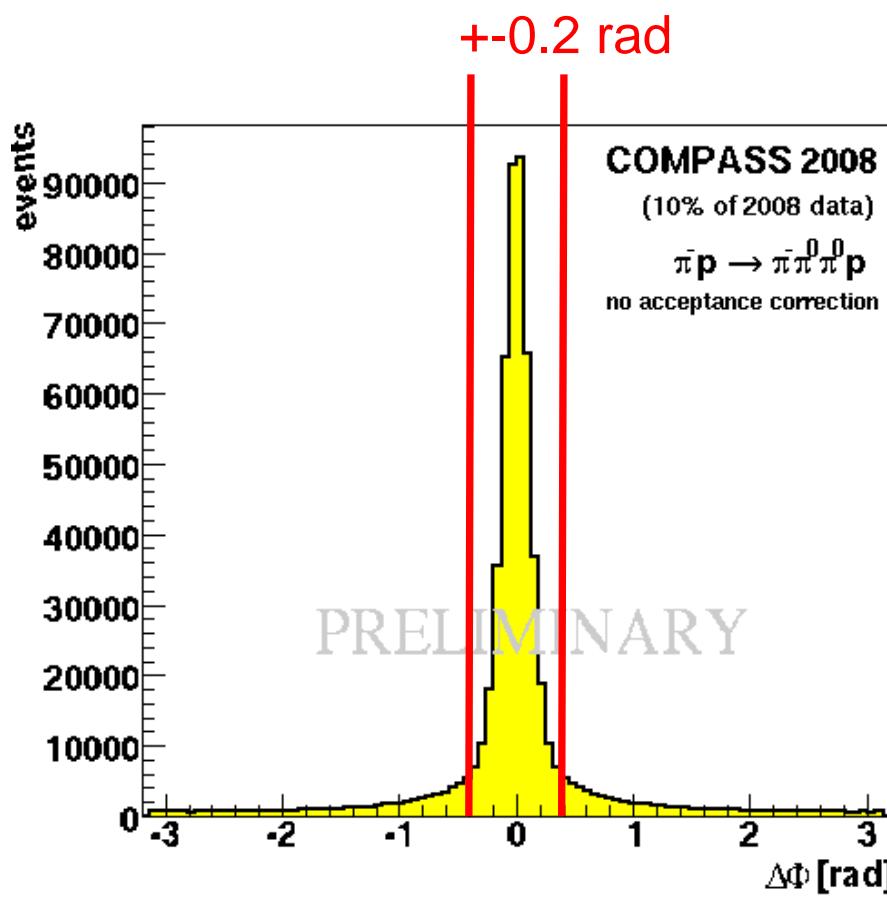


# $\Delta\Phi$ (RPD-Spectro) vs. $E_{\text{beam}}$





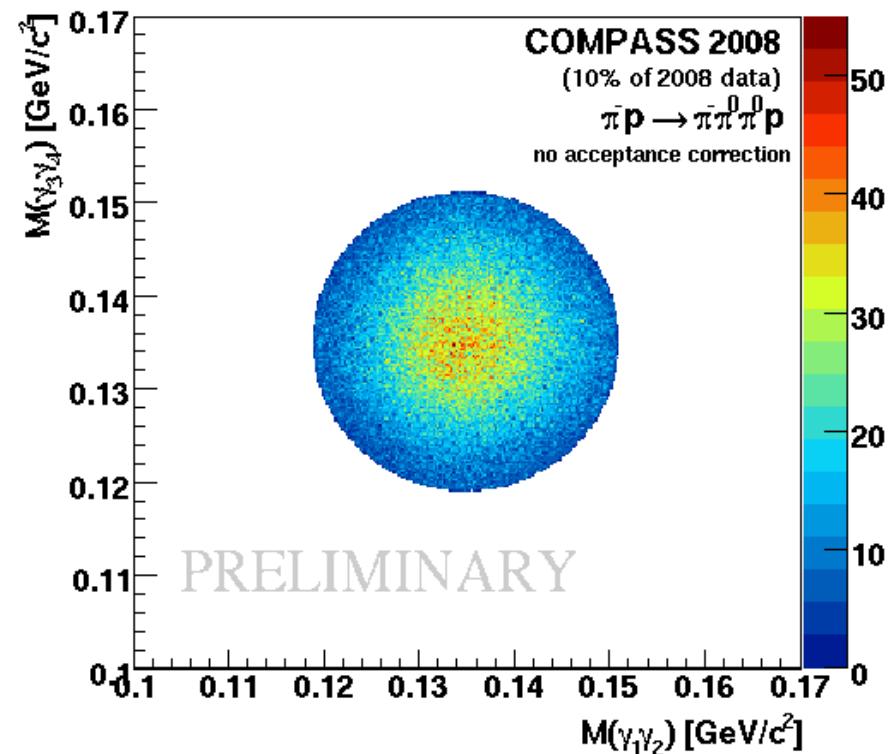
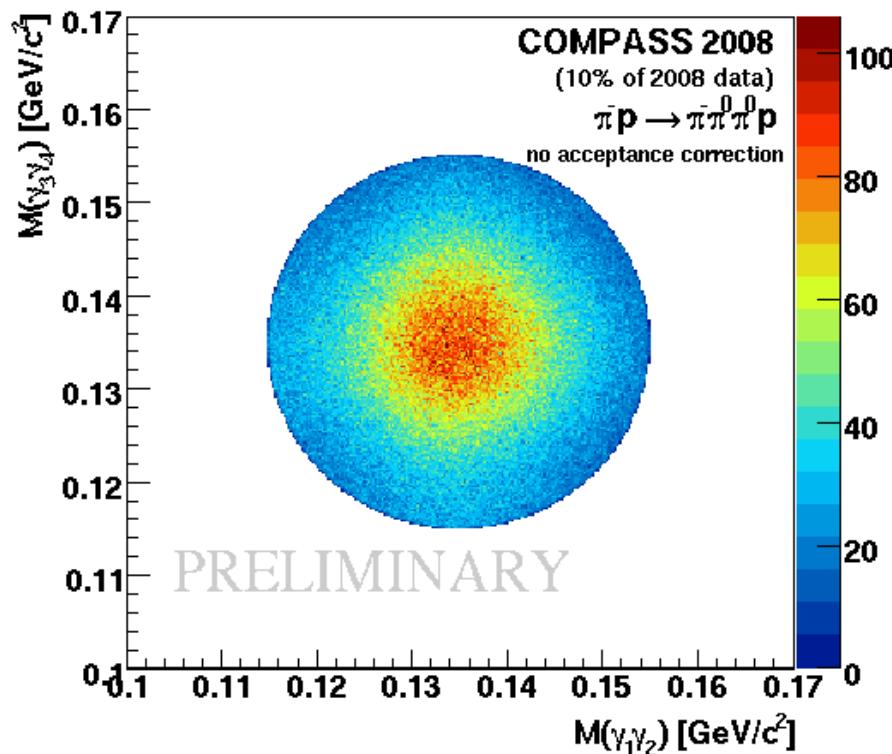
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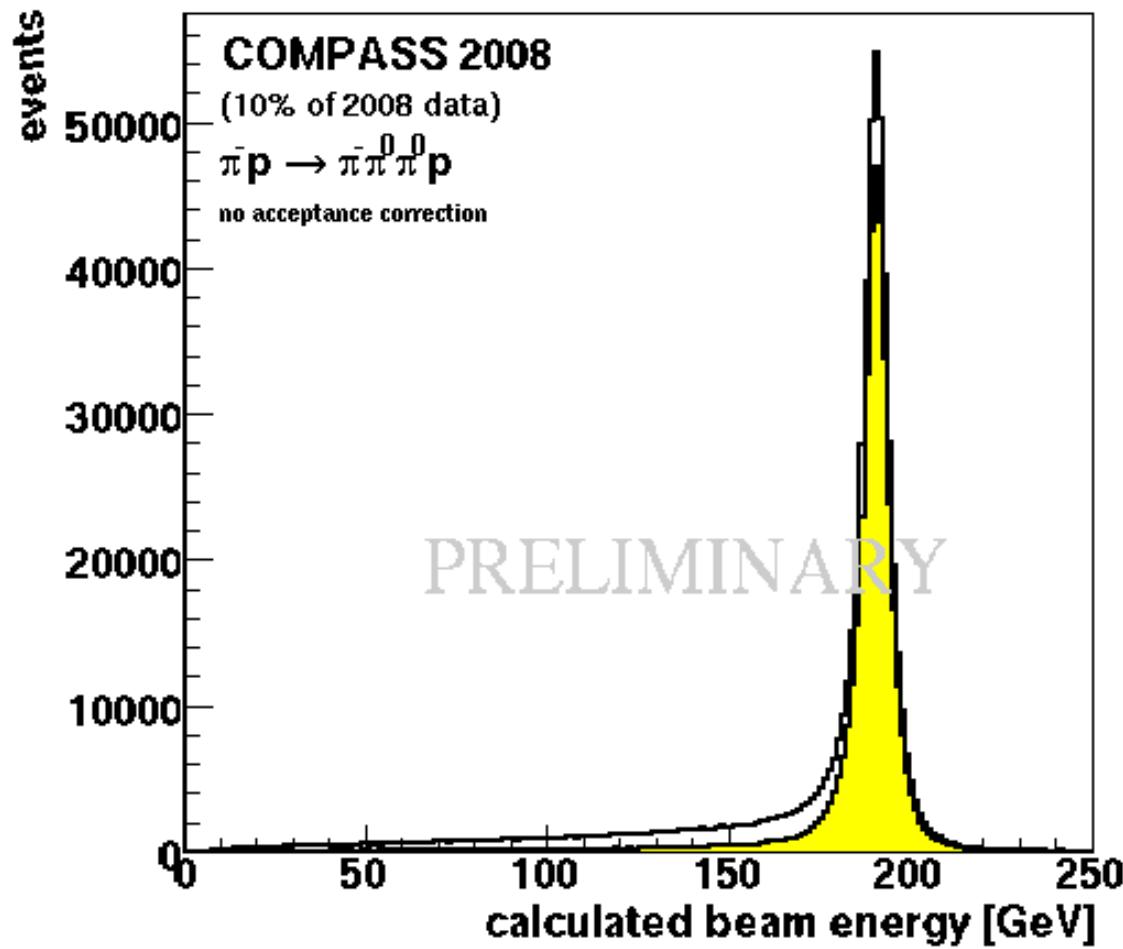
After final cuts on  $\Delta\Phi$  and exclusivity



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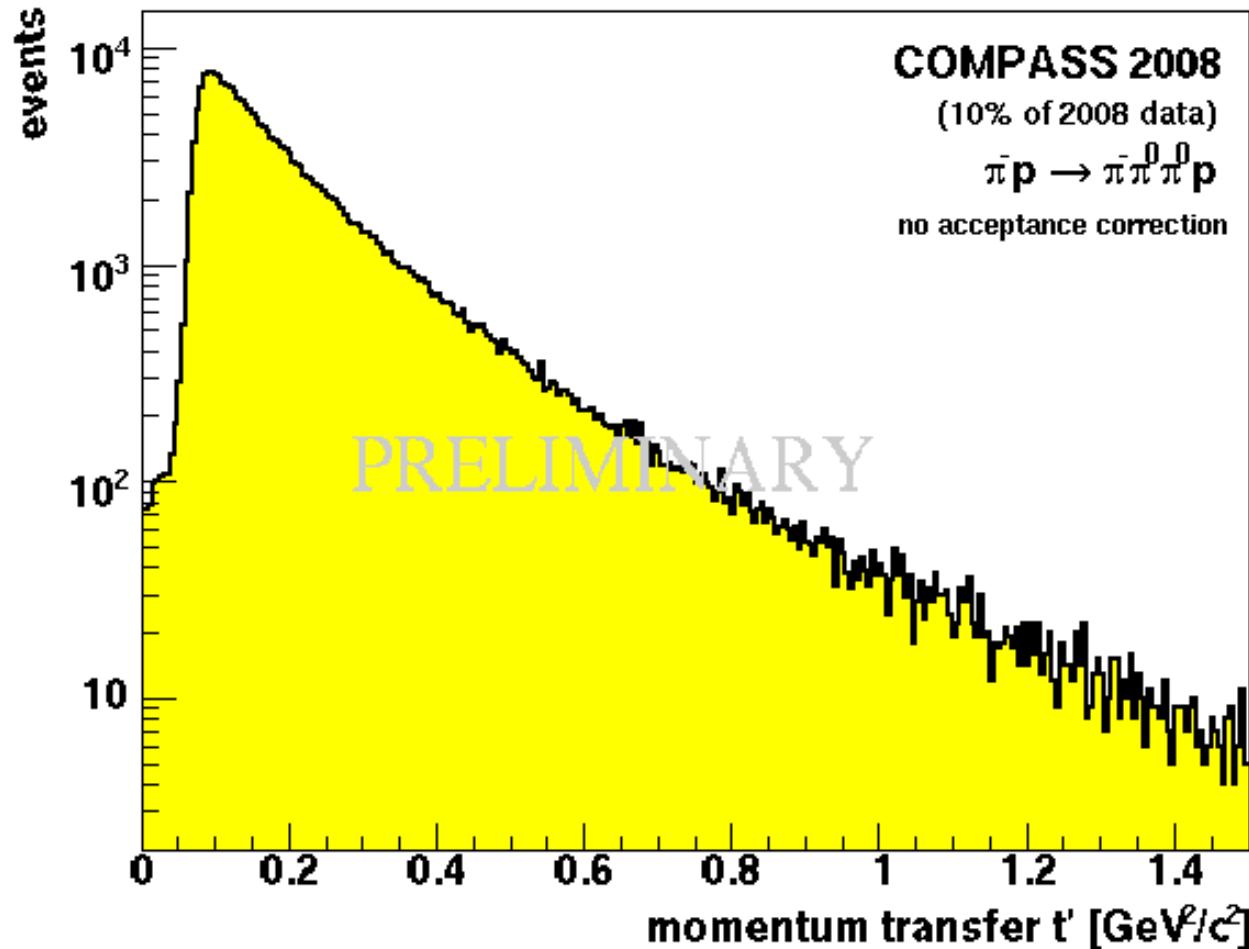


# Exclusivity w/wo $\Delta\Phi$ (RPD-Spectro) cut



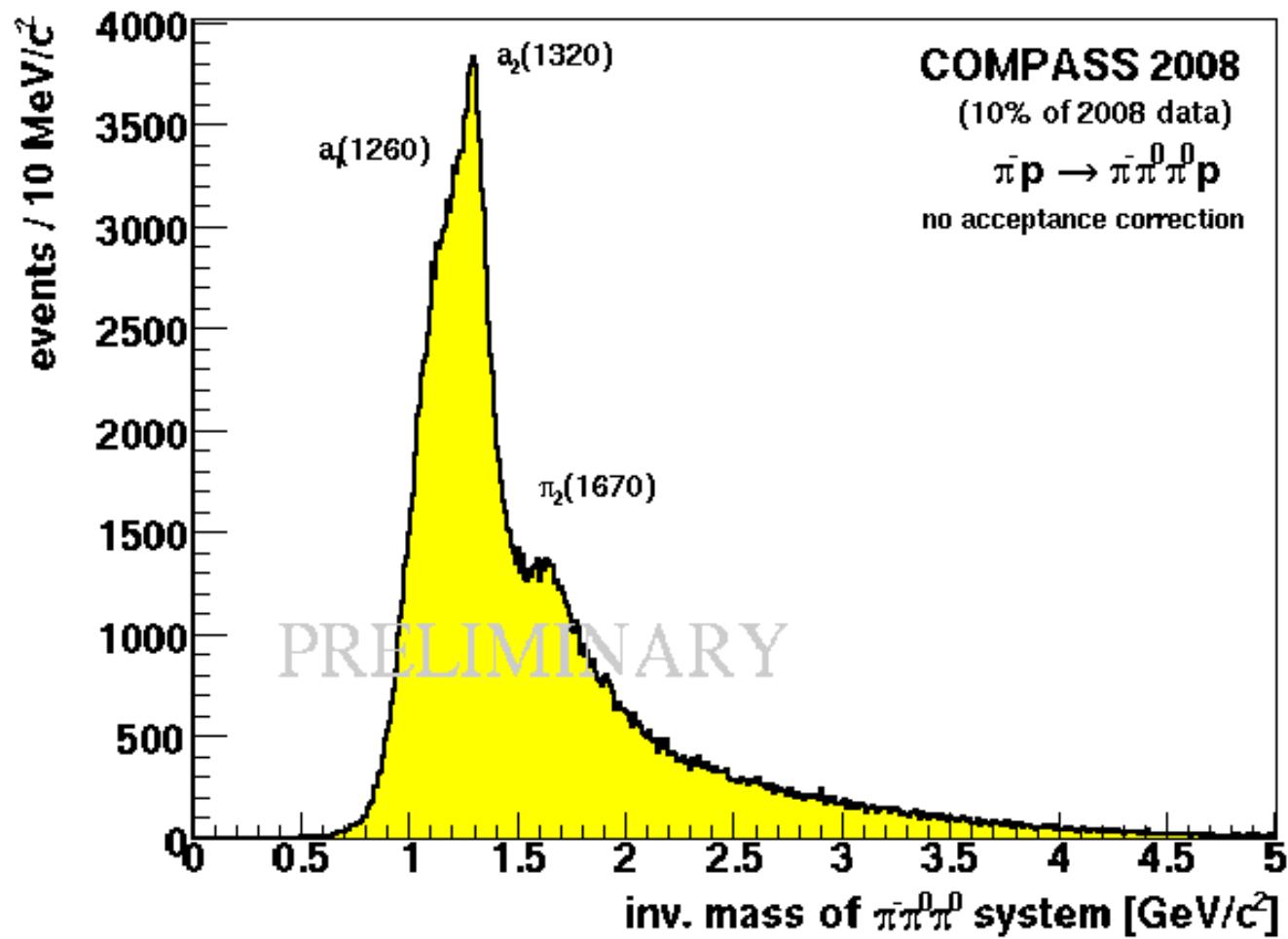


# **t' distribution**



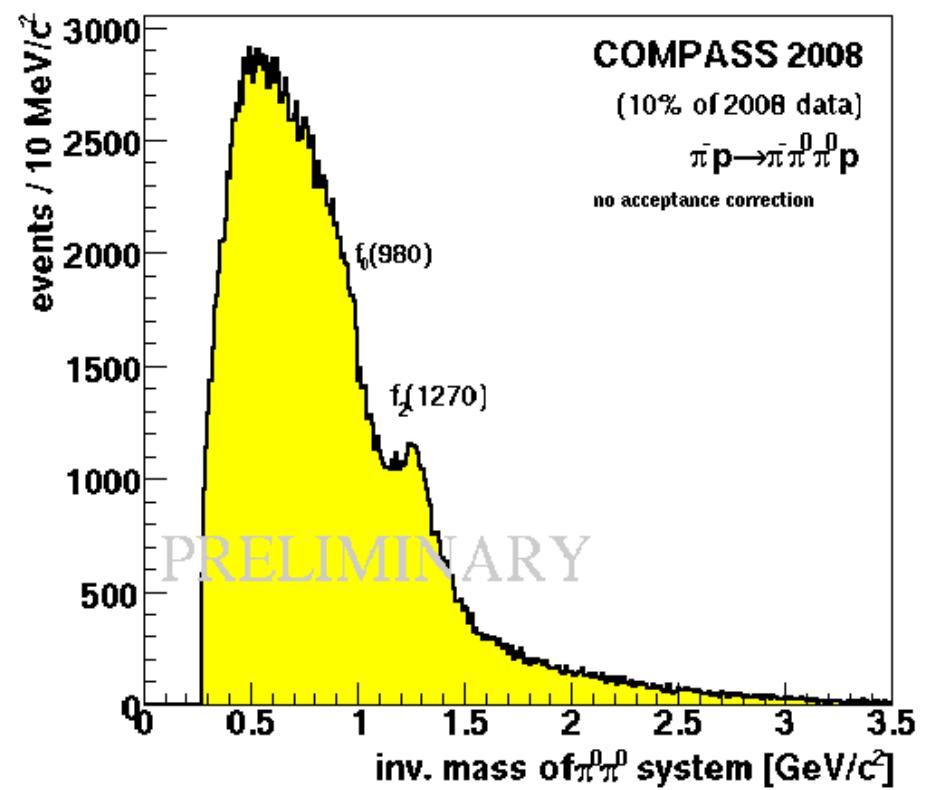
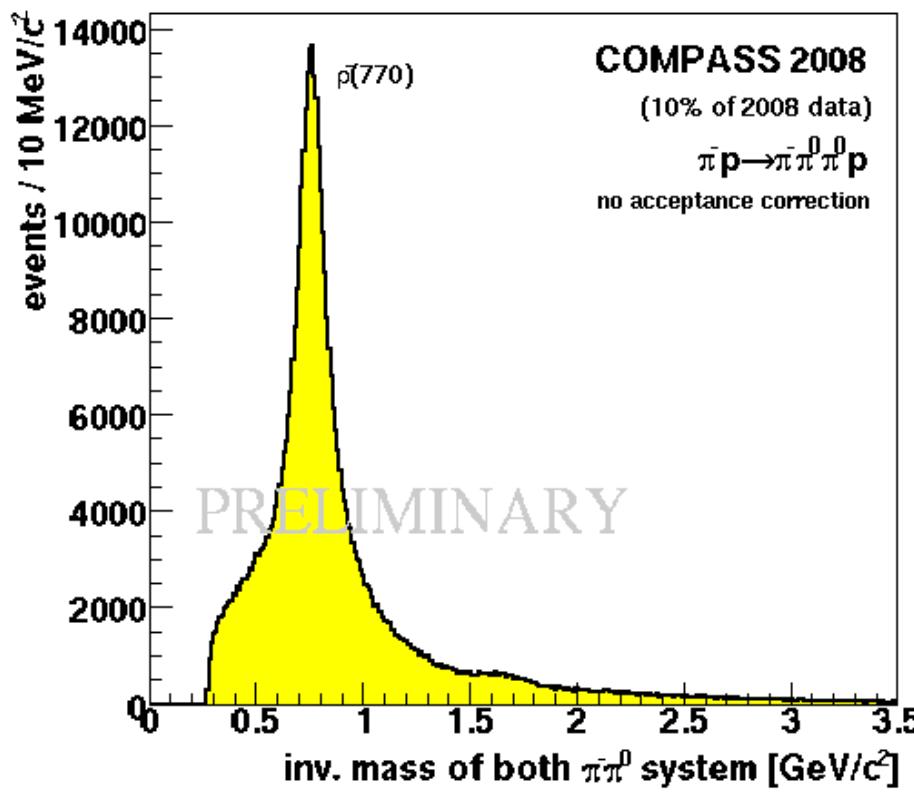


# Mass spectrum of $\pi^-\pi^0\pi^0$ final state



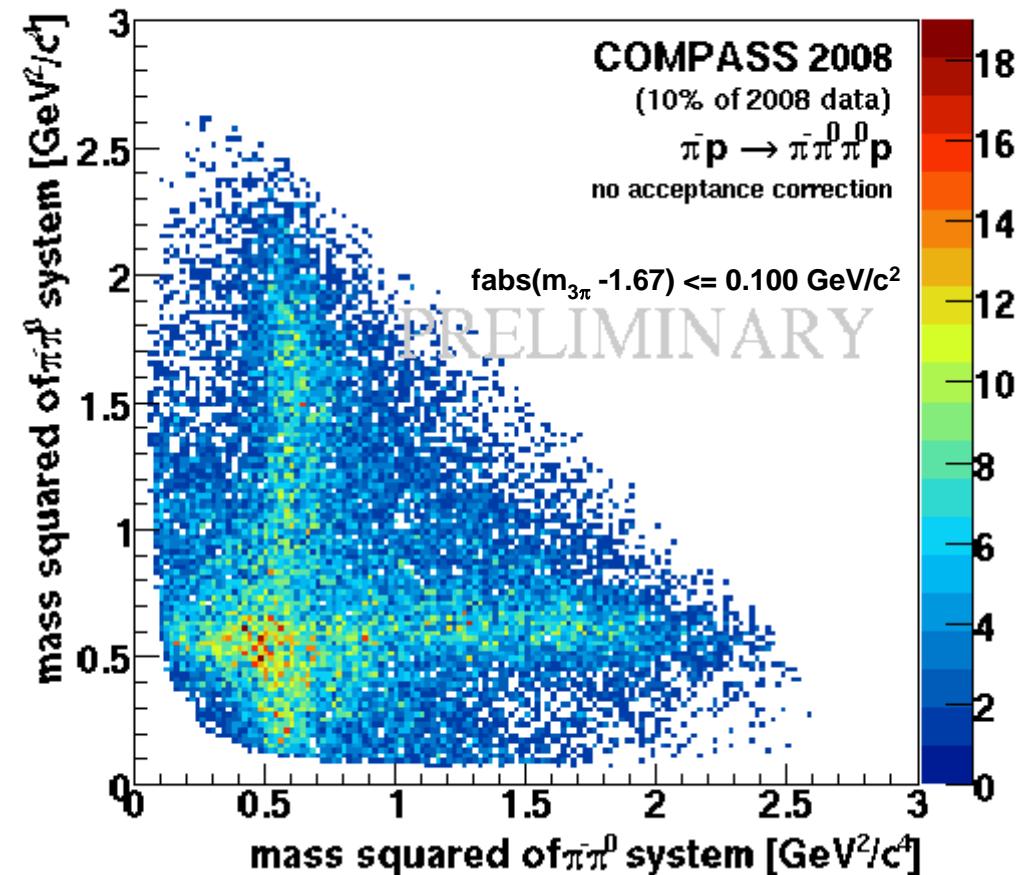
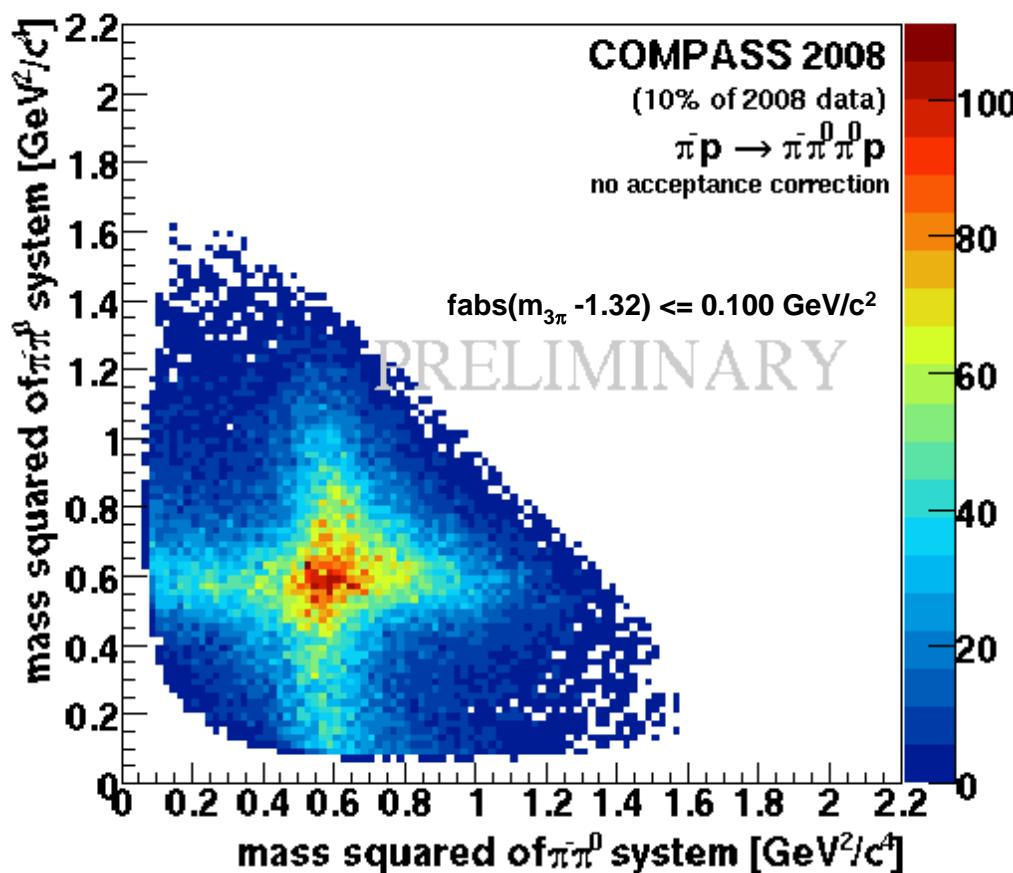


# Mass spectrum of both $\pi^-\pi^0$ systems & the $\pi^0\pi^0$ system



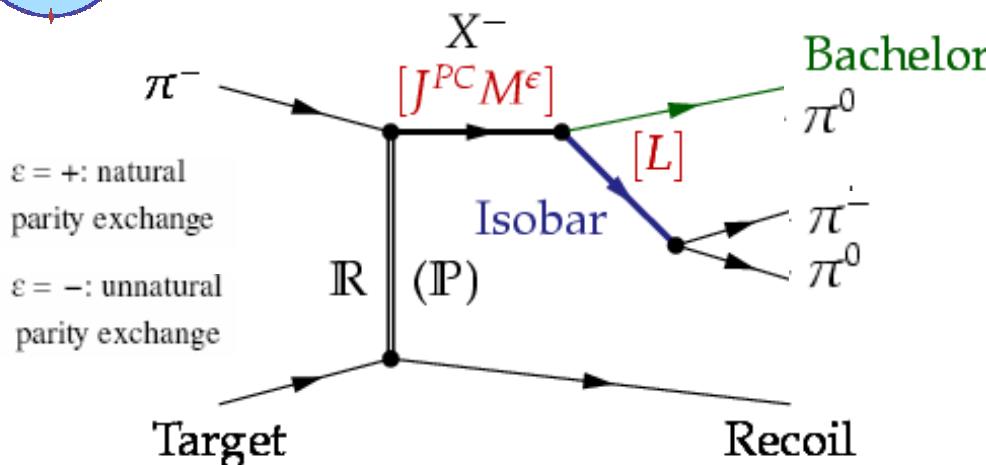


# Dalitz plots: $a_2$ & $\pi_2$ region





# PWA using isobar model



## $X^-$ decay described using isobar model:

- Intermediate di-pion resonance (isobar)
  - Spin  $S$  and rel. orbital angular momentum  $L$  w.r.t bachelor  $\pi^-$
  - $L+S$  couple to  $J$
- Partial waves:  $J^{PC} M^\epsilon$  [isobar]  $L$

## PWA:

- program: Illinois/Protvino/Munich (D.Ryabchikov) software (IHEP/VES, TUM/COMPASS)
- Isobars:  $(\pi\pi)_S$  [broad  $f_0(600)+f_0(1370)$ ],  $f_0(980)$ ,  $\rho(770)$ ,  $f_2(1270)$ ,  $\rho_3(1690)$
- No acceptance correction yet (assumed flat)

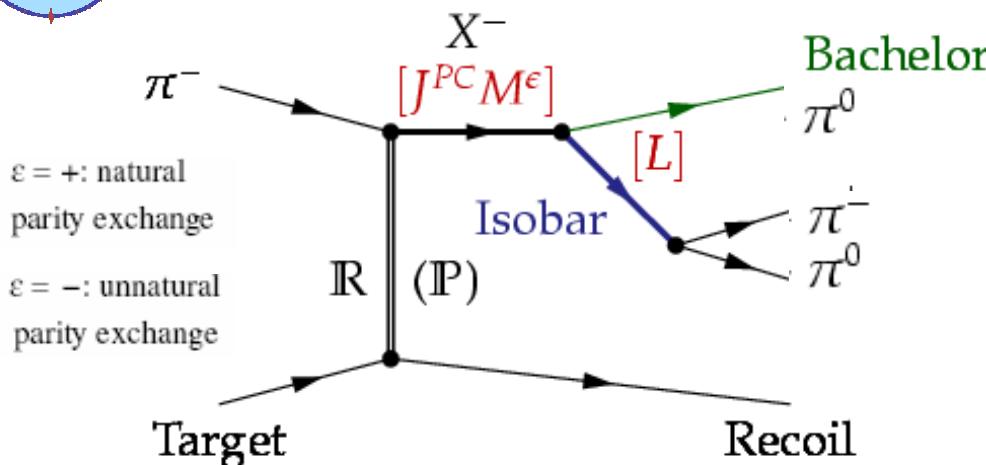
## Mass independent PWA: (40 MeV/c<sup>2</sup> bins, same waveset as used for 2004 data)

$$\sigma_{indep}(\tau, m, t') = \sum_{\epsilon=\pm 1} \sum_{r=1}^{N_r} \left| \sum_i T_{ir}^\epsilon f_i^\epsilon(t') \psi_i^\epsilon(\tau, m) / \sqrt{\int |\psi_i^\epsilon(\tau', m)|^2 d\tau'} \right|^2$$

- Production amplitudes  $T_{ir}^\epsilon$  → extended maximum likelihood fit
- Decay amplitudes  $\psi_i^\epsilon(\tau, m)$  (Zemach tensors, D functions)



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## Assumptions:

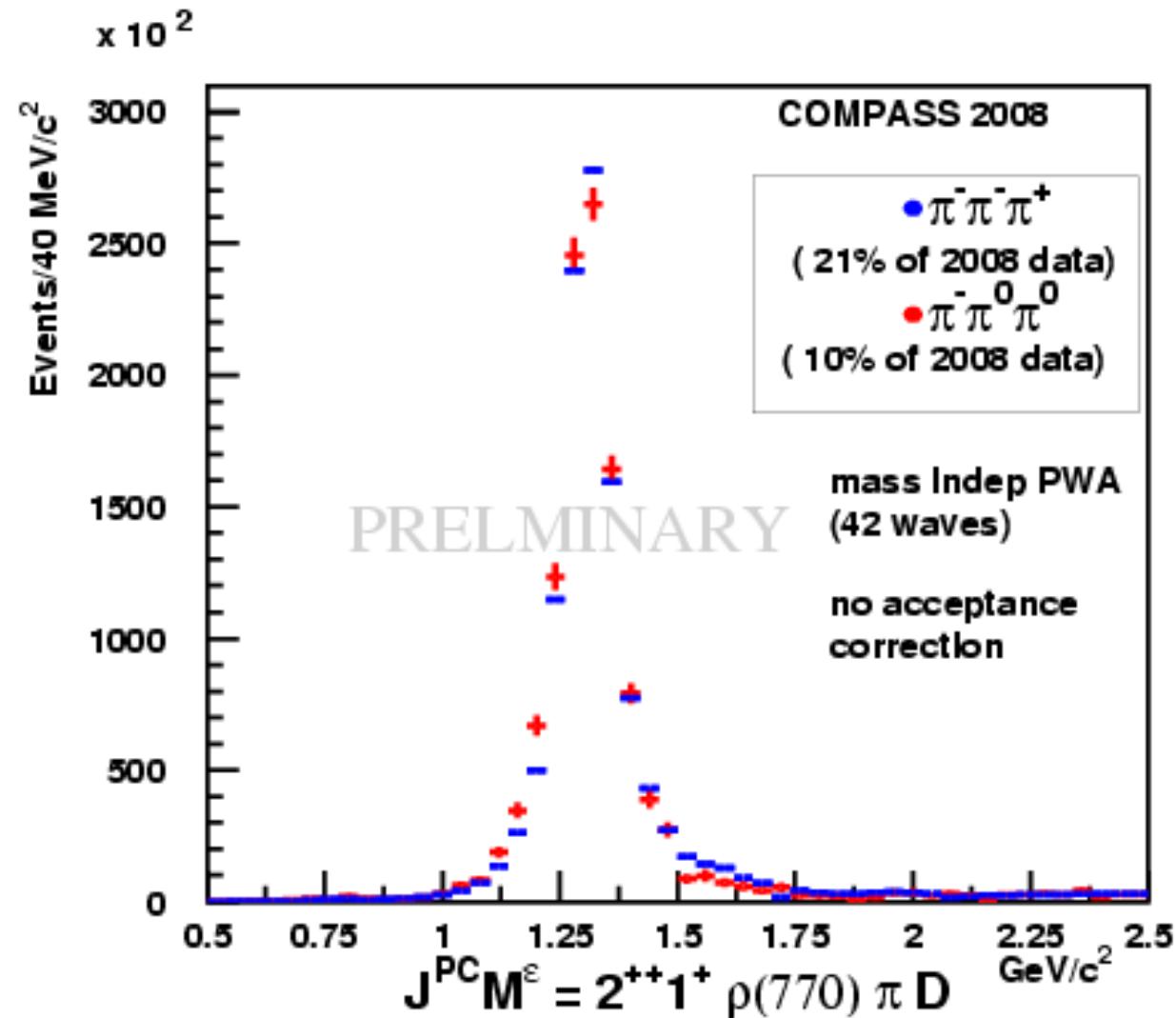
- factorisation of beam & target vertex, no final state interactions
- $I^G$  conserved at beam vertex ( $\pi^-$  beam:  $I^G = 1^-$ )
- Scattering on nucleons: helicity flip & non-flip amps at target vertex (rank2)
- Using reflectivity basis in Gottfried Jackson frame (at high CM energies: reflectivity  $\varepsilon$  = naturality of  $R$ )

## Isospin symmetry: neutral / charge mode

- isobar decaying into  $f_2 \pi$ : 1/2 intensity expected
- isobar decaying into  $\rho \pi$ : 1/1 intensity expected

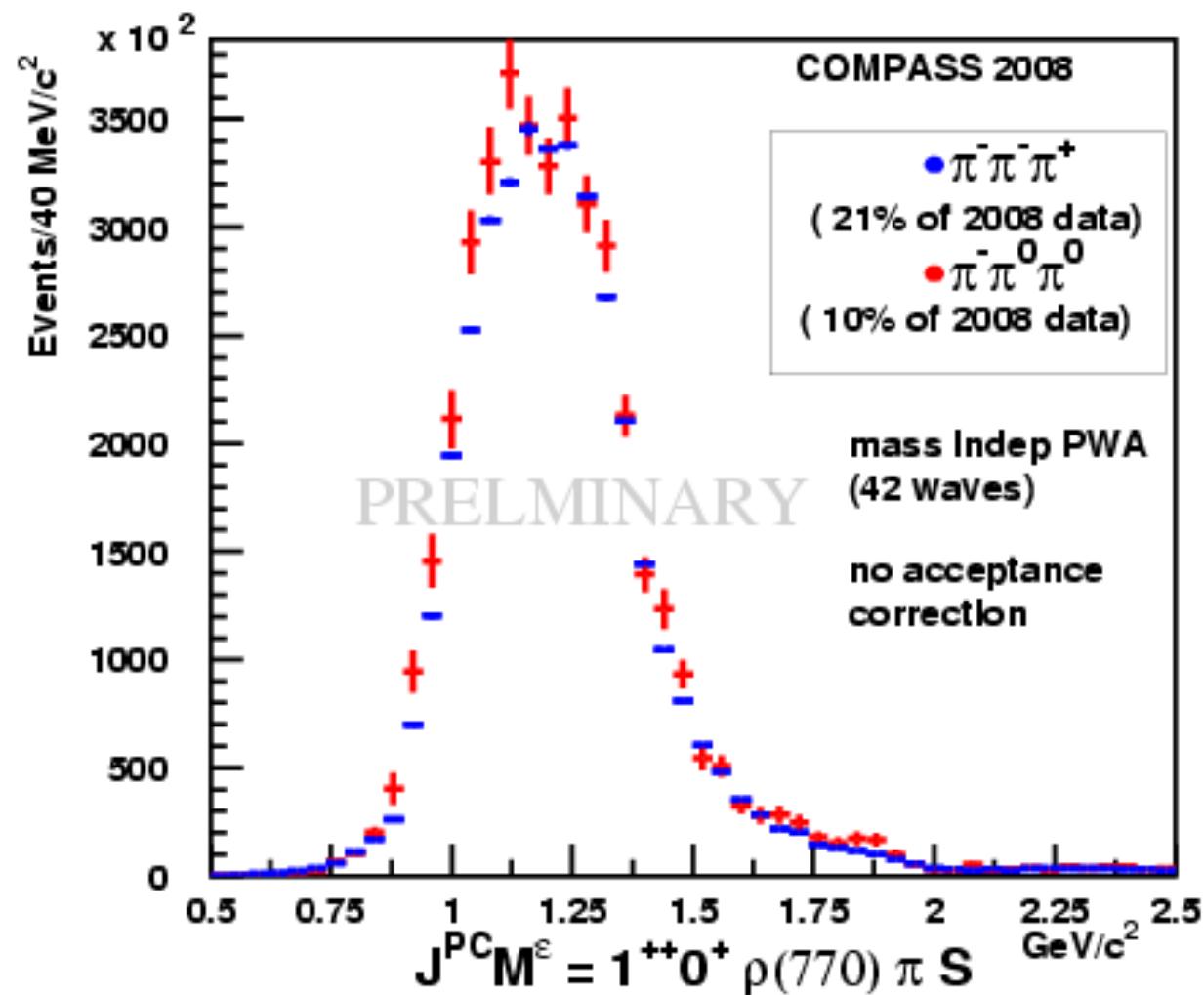


# First PWA fits – normalisation to a<sub>2</sub>



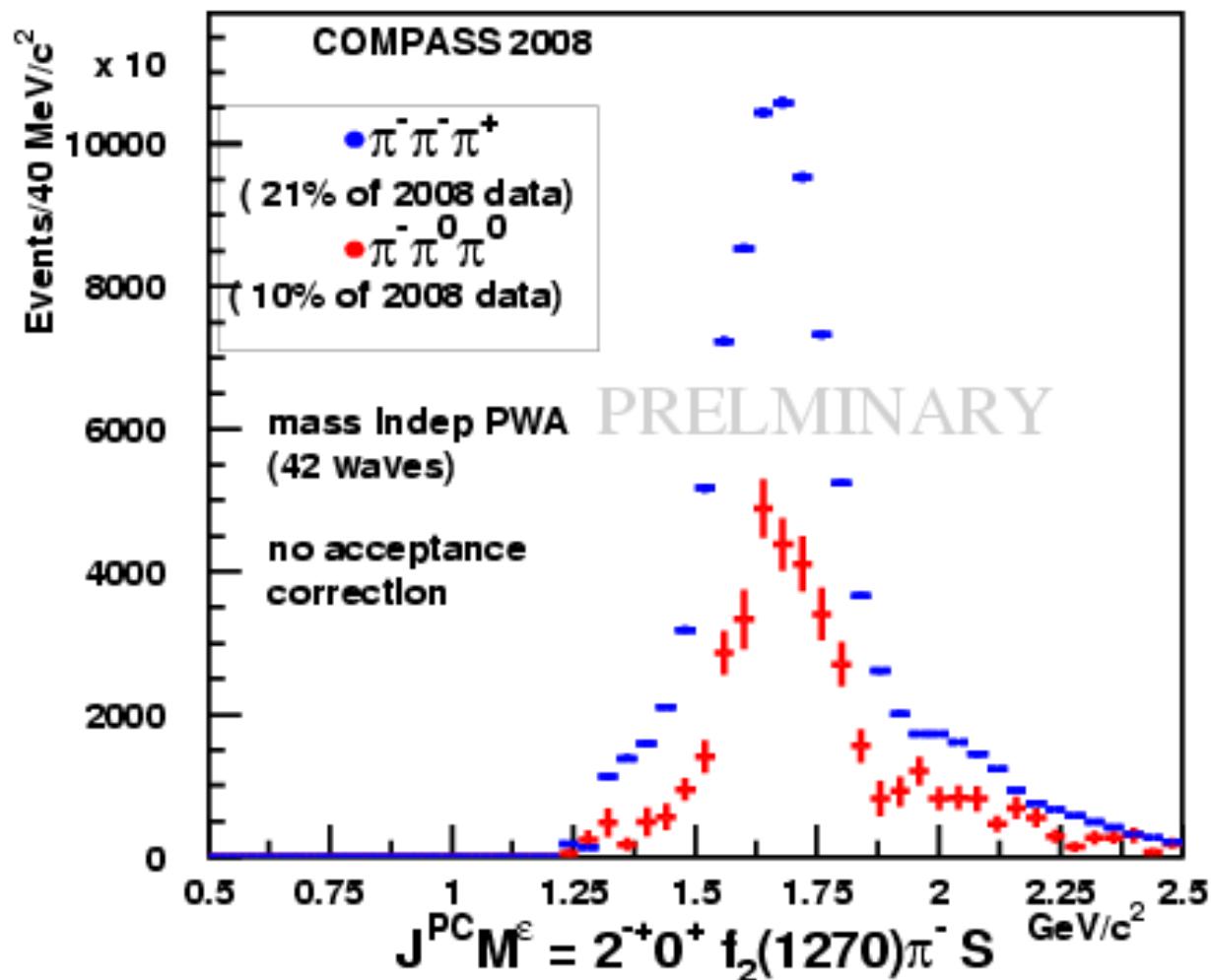


# First PWA fits – check intensities a1 to rho pi



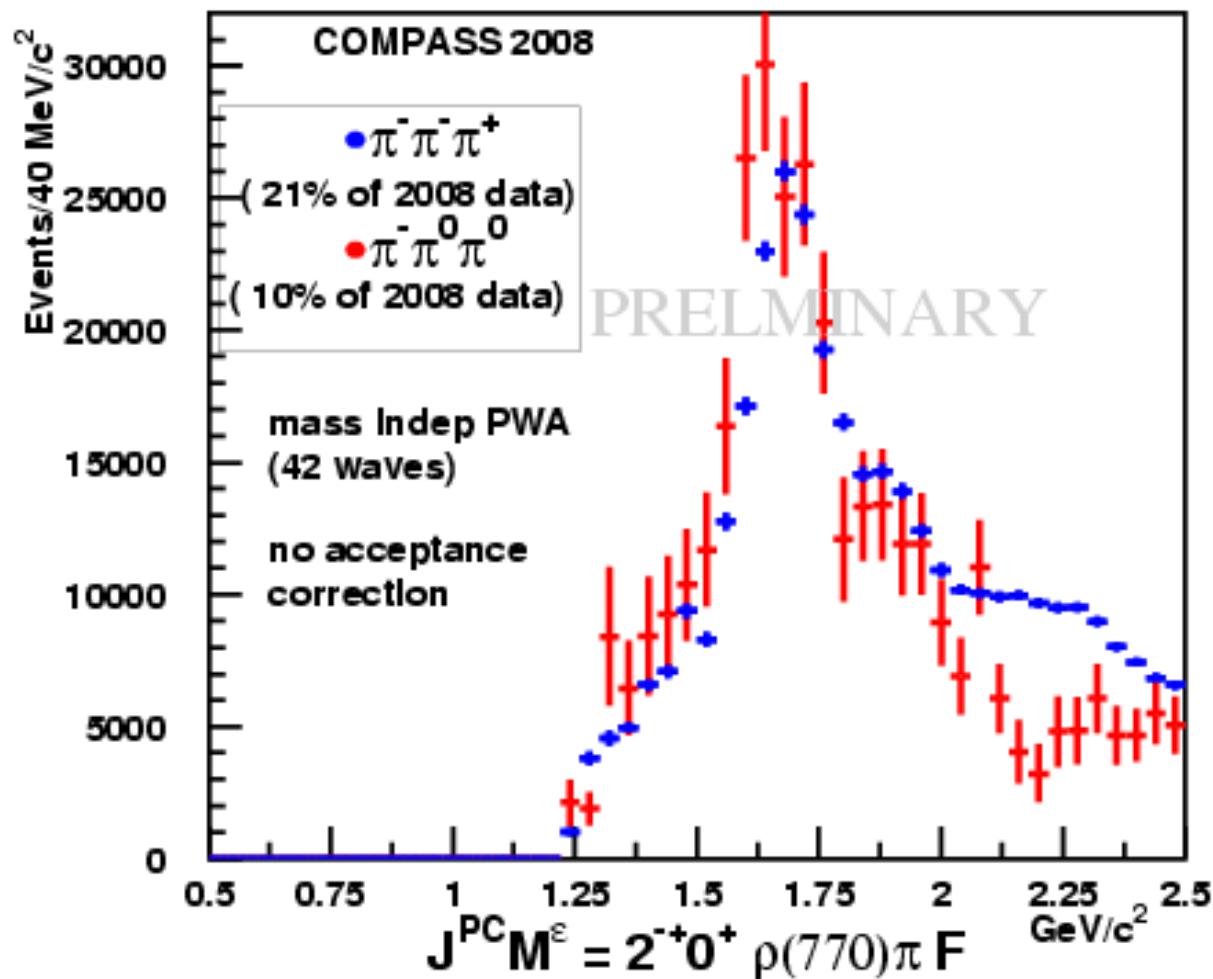


# First PWA fits – check intensities pi2 to f2pi





# First PWA fits – check intensities a1 to rho pi



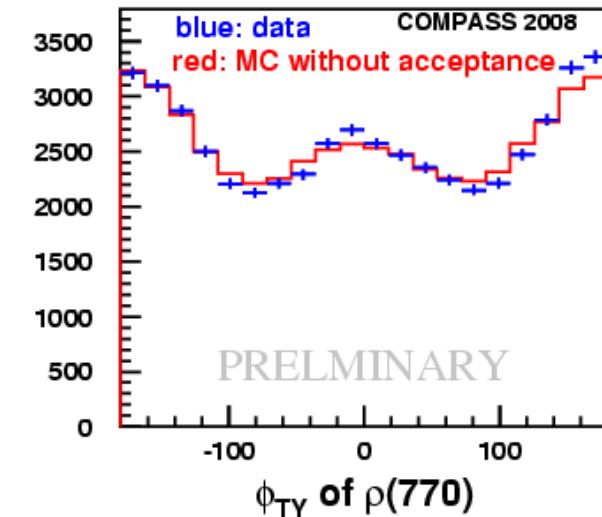
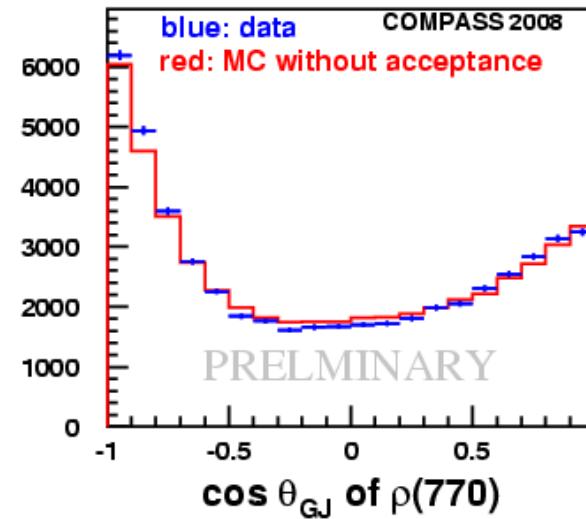


# Decay angles in G.J. frame: Full PhaseSpace

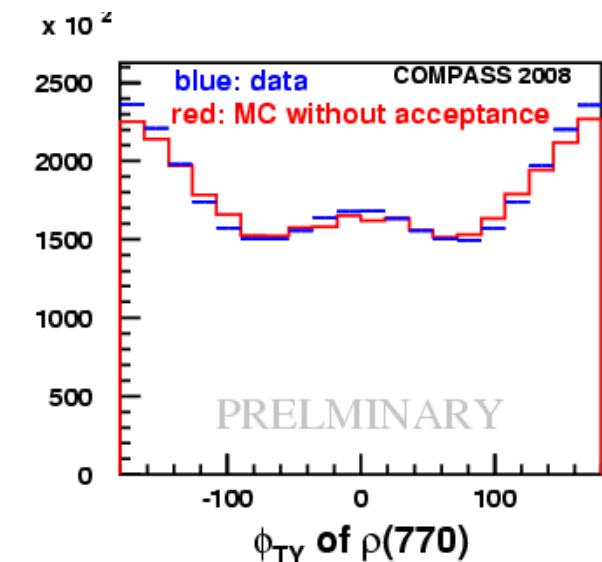
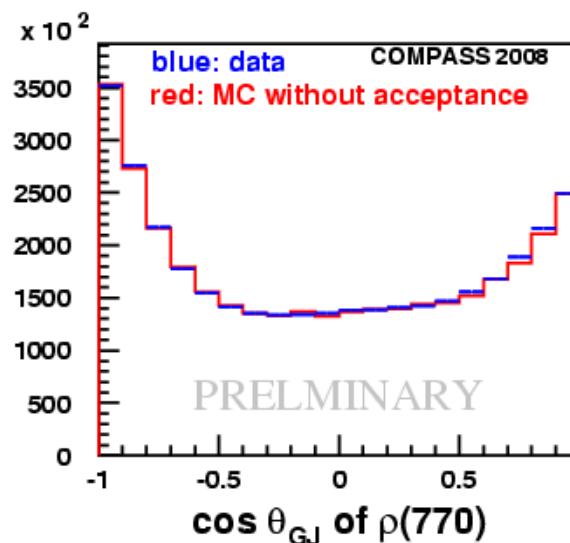
## Generated Prediction vs. fitted data



a1/a2 mass region - neutral  
(1.22 - 1.38 GeV/c<sup>2</sup>)



a1/a2 mass region - charged  
(1.22 - 1.38 GeV/c<sup>2</sup>)





# Conclusions & outlook



- **COMPASS spectrometer well suited for Hadron Spectroscopy**  
→ *Data taken with hadron beams on p target in 2008 & 09*
- **COMPASS measures Neutral & Charged channels**
- **First results on  $3\pi$  final state -- neutral mode (diffr. dissociation)**
  - + Evt selection & 1st PWA fits (*mass independent*)
  - + *First look promising: mass spectra, main waves, isospin symmetry*

=> Important cross-checks & independent confirmation of any new state observed
- **Statistics less than charged mode**
  - event selection presently limited to (exactly)  $4\gamma$  events
  - will improve (allowing 5th => gain ~20%)
  - *Ecals reconstruction under redevelopment*
- **Next steps:**
  - Further development of Ecals reconstruction → MSADC info, DSP etc
  - Increase statistics, acceptance corrections, extend waveset, ...



# Backup





# First PWA fits on $\pi-\pi^0\pi^0$

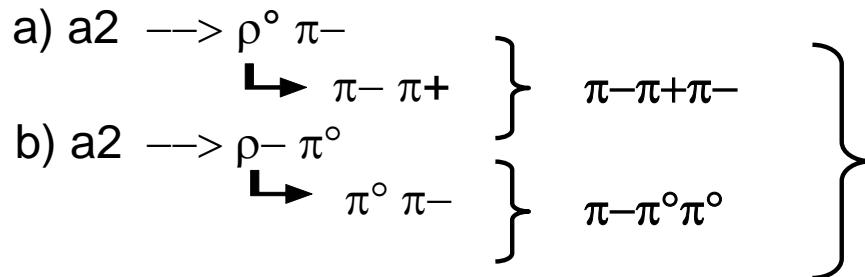


**Theoretical expectation:** neutral / charge mode

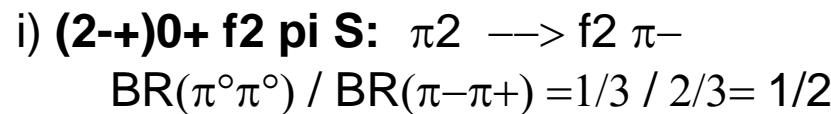
- isobar decay into **f2**  $\pi$ : 1/2 intensity expected
- isobar decay into  **$\rho$**   $\pi$ : 1/1 intensity expected

Examples,  $(J^{PC}) M^{\epsilon}$  [isobar] L notation:

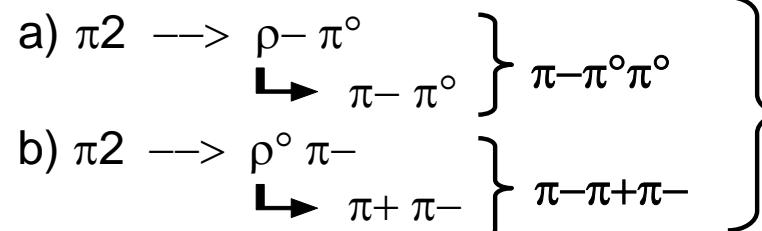
- **a2: (2++)1+ rho pi D**



- **$\pi 2$ :**



**$\pi 2$  intensity expected (neutral/charged): 1/2  
(plus reduced acc.  $\rightarrow$  eff x eff for neutrals)**





# First PWA fits on $\pi-\pi^0\pi^0$



**Theoretical expectation:** neutral / charge mode

- isobar decay into  $f2 \pi$ : 1/2 intensity expected
- isobar decay into  $\rho \pi$ : 1/1 intensity expected

Examples,

- General:** Branching not only from Clebsch-Gordon coeff., but also from Bose-Symmetrisation w bachelor  $\pi$
- $a2: (2++)1+$ 
    - a)  $a2 \rightarrow \rho \pi$   
=> IsospinSym. holds for isobars going to  $\rho\pi$  (same effect)  
=> - " - needs to be modified, BR may differ
    - b)  $a2 \rightarrow \pi\pi$   
Calculated / checked:  $BR = N(\pi-\pi^0\pi^0)/N(\pi-\pi^+\pi^-)$   
 $BR(0-+ f0(1400) \pi S) = 0.26$  (at 1.3 GeV)  
 $BR(0-+ f0(980) \pi S) = 0.44$  (at 1.8 GeV)
  - $\pi2:$ 
    - i)  $(2-+)0$   $BR(2-+ f2(1270) \pi S) = 0.50$  (at 1.67 GeV =  $\pi2$  mass)

$$BR(\pi^0\pi^0) / BR(\pi^-\pi^+) = 1/3 / 2/3 = 1/2 \quad \left. \right\} \quad \text{find very good agreement with experiment}$$

*(plus reduced acc.  $\rightarrow$  eff x eff for neutrals )*

ii)  $(2-+)0+$  rho pi F

$$\begin{aligned} a) \pi2 &\rightarrow \rho^-\pi^0 \\ &\quad \downarrow \\ &\quad \pi^-\pi^0 \end{aligned} \quad \left. \right\} \quad \pi-\pi^0\pi^0$$
  
$$\begin{aligned} b) \pi2 &\rightarrow \rho^0\pi^- \\ &\quad \downarrow \\ &\quad \pi^+\pi^- \end{aligned} \quad \left. \right\} \quad \pi-\pi^+\pi^-$$

**$\pi2$  intensity expected** (neutral/charged): 1



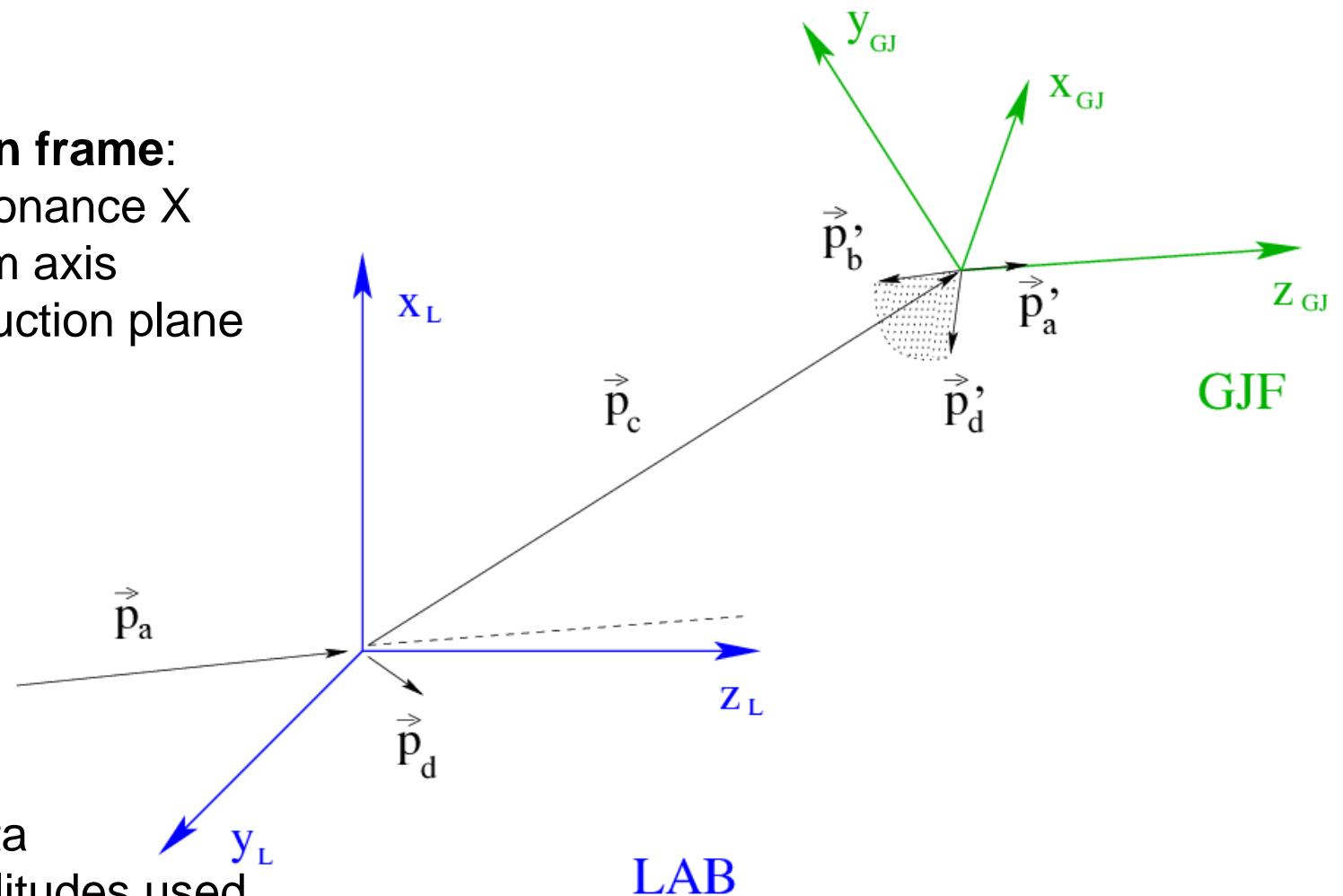
# Decay angles in G.J. frame

## Full PhaseSpace Generated Prediction



**Gottfried-Jackson frame:**

- rest frame of resonance X
- z parallel to beam axis
- y normal to production plane

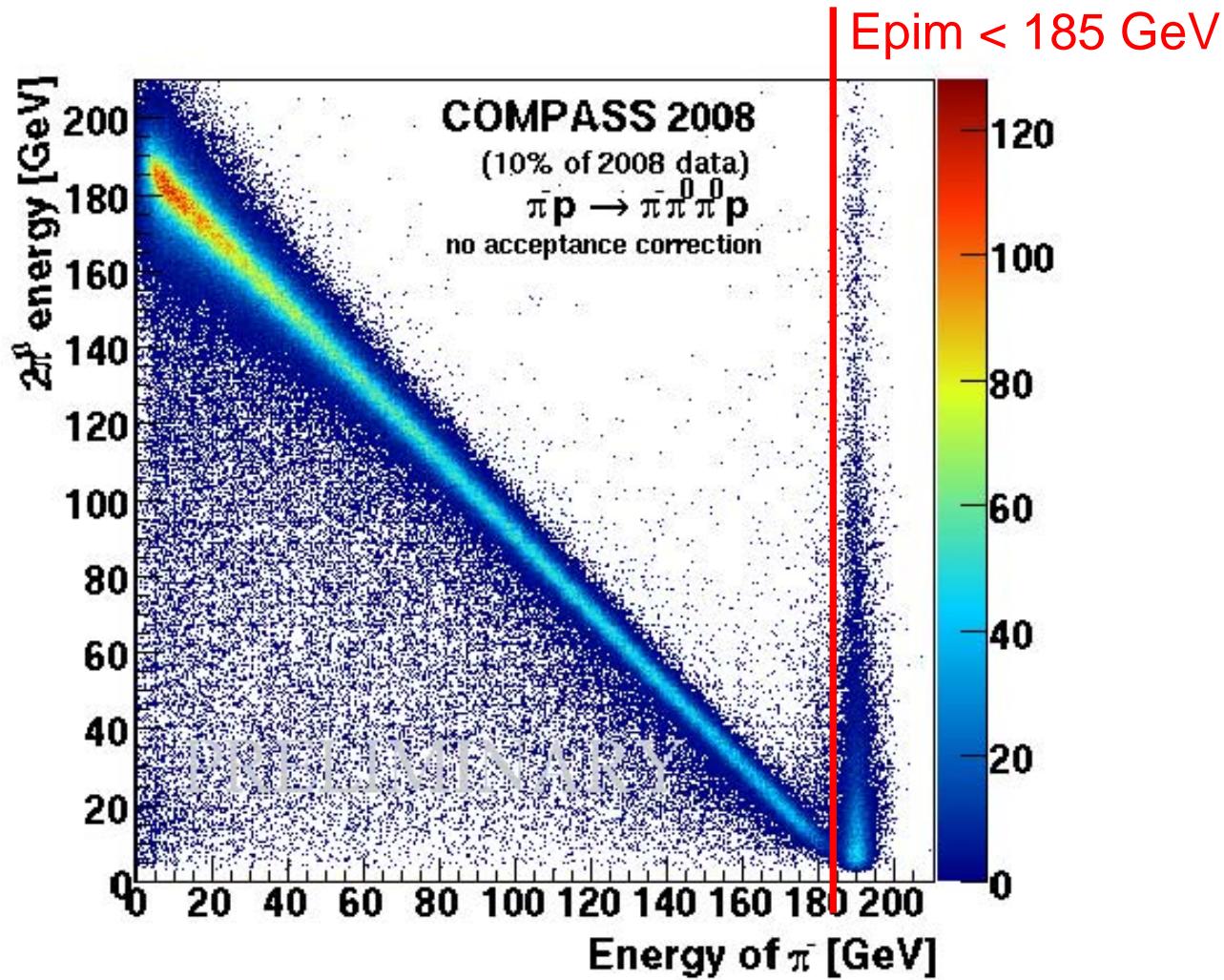


**„PREDICT“:**

- fit waveset to data
- fitted decay amplitudes used to calculate decay angles
- under assumption of uniform acceptance
- normalised per mass bin to data



# Cut on energy of $\pi^-$ (plot after RPDCut) (elastic events and background from e.g. pile-up)





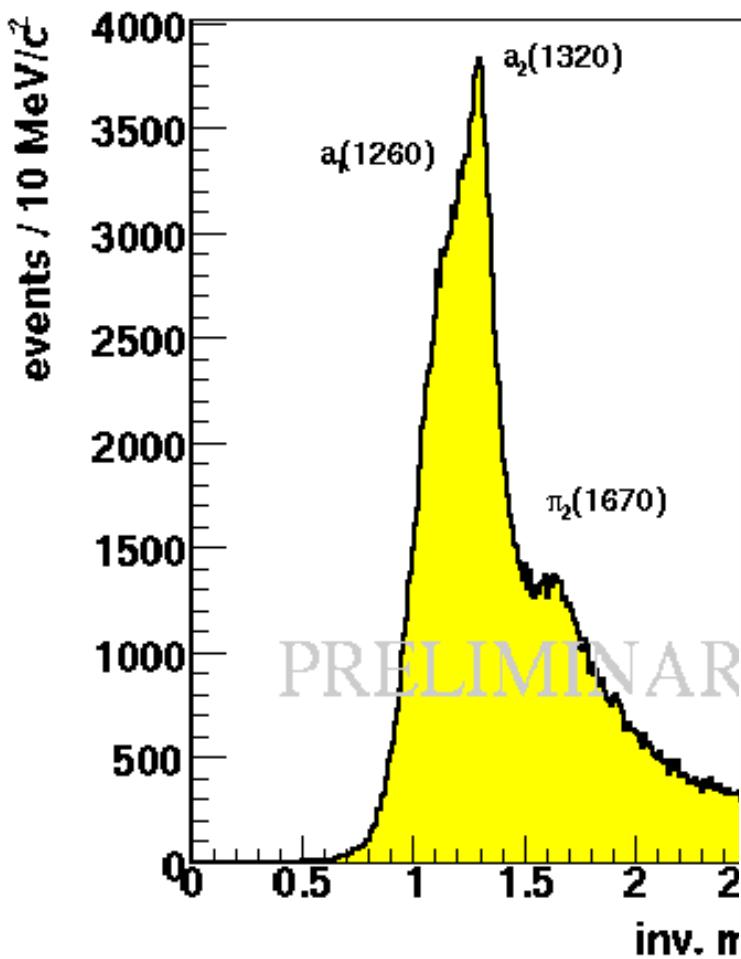
# Waveset used for the PWA

$J^{PC} M^\epsilon$	$L$	Isobar $\pi$	Threshold (GeV/ $c^2$ )
$0^{-+0^+}$	$S$	$f_0(980)\pi$	1.25
$0^{-+0^+}$	$S$	$(\pi\pi)_s\pi$	-
$0^{-+0^+}$	$P$	$\rho\pi$	-
$1^{-+1^+}$	$P$	$\rho\pi$	-
$1^{++0^+}$	$S$	$\rho\pi$	-
$1^{++0^+}$	$P$	$f_2\pi$	1.20
$1^{++0^+}$	$P$	$(\pi\pi)_s\pi$	0.94
$1^{++0^+}$	$D$	$\rho\pi$	1.30
$1^{++1^+}$	$S$	$\rho\pi$	-
$1^{++1^+}$	$P$	$f_2\pi$	1.40
$1^{++1^+}$	$P$	$(\pi\pi)_s\pi$	1.20
$1^{++1^+}$	$D$	$\rho\pi$	1.40
$2^{-+0^+}$	$S$	$f_2\pi$	1.20
$2^{-+0^+}$	$P$	$\rho\pi$	0.80
$2^{-+0^+}$	$D$	$(\pi\pi)_s\pi$	0.80
$2^{-+0^+}$	$D$	$f_2\pi$	1.50
$2^{-+0^+}$	$F$	$\rho\pi$	1.20
$2^{-+1^+}$	$S$	$f_2\pi$	1.20
$2^{-+1^+}$	$P$	$\rho\pi$	0.80
$2^{-+1^+}$	$D$	$(\pi\pi)_s\pi$	1.20
$2^{-+1^+}$	$D$	$f_2\pi$	1.50
$2^{-+1^+}$	$F$	$\rho\pi$	1.20
<hr/>			
<hr/>			
$2^{++1^+}$	$P$	$f_2\pi$	1.20
$2^{++1^+}$	$D$	$\rho\pi$	-
$3^{++0^+}$	$S$	$\rho_3\pi$	1.76
$3^{++0^+}$	$P$	$f_2\pi$	1.20
$3^{++0^+}$	$D$	$\rho\pi$	1.20
$3^{++1^+}$	$S$	$\rho_3\pi$	1.76
$3^{++1^+}$	$P$	$f_2\pi$	1.20
$3^{++1^+}$	$D$	$\rho\pi$	1.50
$4^{-+0^+}$	$F$	$\rho\pi$	1.00
$4^{-+1^+}$	$F$	$\rho\pi$	1.20
$4^{++1^+}$	$F$	$f_2\pi$	1.60
$4^{++1^+}$	$G$	$\rho\pi$	1.40
$1^{-+0^-}$	$P$	$\rho\pi$	-
$1^{-+1^-}$	$P$	$\rho\pi$	-
$1^{++1^-}$	$S$	$\rho\pi$	-
$2^{-+1^-}$	$S$	$f_2\pi$	1.20
$2^{++0^-}$	$P$	$f_2\pi$	1.30
$2^{++0^-}$	$D$	$\rho\pi$	-
$2^{++1^-}$	$P$	$f_2\pi$	1.30
<hr/>			
<hr/>			
FLAT			

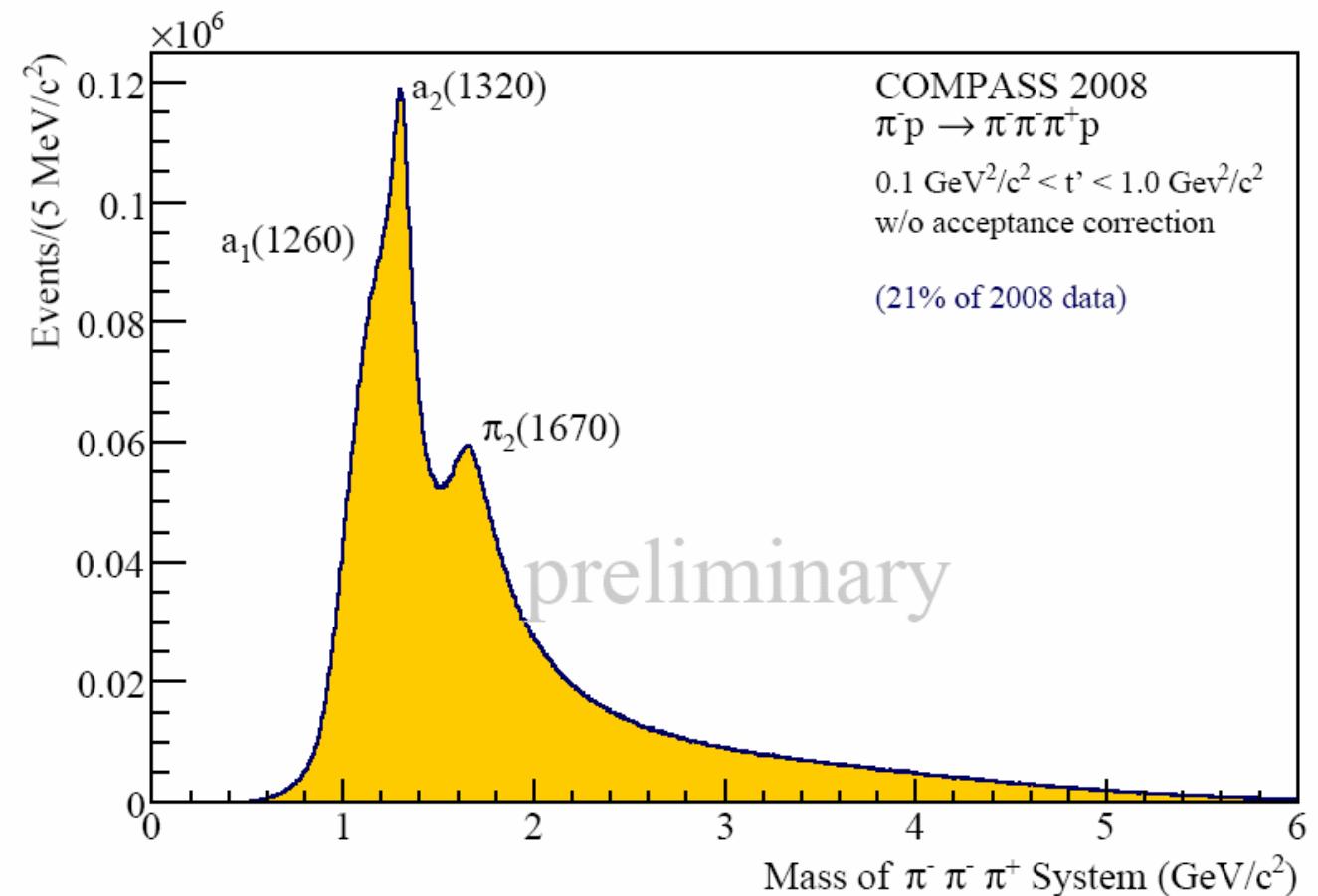
Table 5: List of the 42 waves used for the mass independent PWA.



# Mass spectrum of $\pi-\pi^0\pi^0$ final state



**COMPASS 2008**  
(10% of 2008 data)  
 $\pi^- p \rightarrow \pi^-\pi^0\pi^0 p$   
no acceptance correction



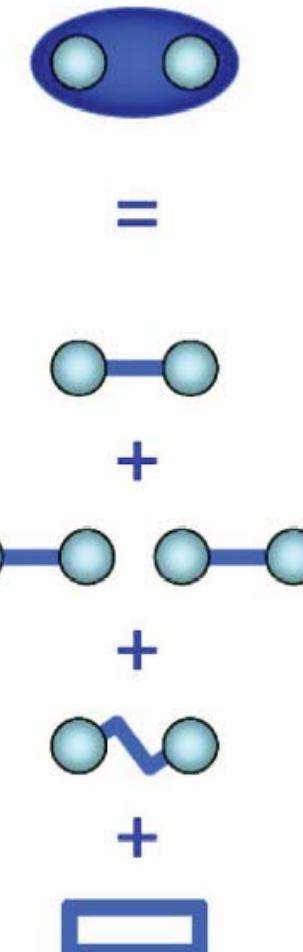


# Mesons and Spin Exotic States



## Constituent quark model

- color neutral qqbar systems
- Quantum numbers  $I^G J^{PC}$
- $P = (-1)^{L+1}$     $C = (-1)^{L+S}$     $G = (-1)^{I+L+1}$
- $J^{PC}$  multiplets:  $0^{++}$ ,  $0^{-+}$ ,  $1^{--}$ ,  $1^{+-}$ ,  $1^{++}$ ,  $2^{++}$ , ...
- **Forbidden:**  $0^{--}$ ,  $0^{+-}$ ,  $1^{+-}$ ,  $2^{+-}$ ,  $3^{--}$ , ...



## QCD: Additional color-neutral objects

- Tetraquarks (qqbar)(qqbar)
- Hybrids (qqbar)g
- Glueballs gg

## Spin Exotic States

- $J^{PC}$  forbidden  $\rightarrow$  no simple qqbar state
- No mixing with quark model states