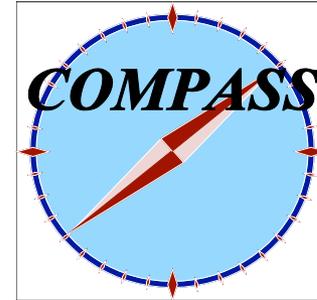


# *NLO QCD predictions for gluon polarization from open-charm asymmetries measured at COMPASS*

Krzysztof Kurek  
SINS, Warsaw



- Part I - *Open-charm results on gluon polarization from COMPASS - on behalf of the COMPASS Collaboration*



- Part II - *NLO QCD predictions for gluon polarization from open-charm asymmetries measured at COMPASS*

# COMPASS Collaboration at CERN

Common Muon and Proton Apparatus

for Structure and Spectroscopy

**Czech Rep., France, Germany, India, Israel, Italy,  
Japan, Poland, Portugal, Russia and CERN**

Bielefeld, Bochum, Bonn, Burdwan and Calcutta, CERN, Dubna, Erlangen,  
Freiburg, Lisbon, Mainz, Moscow, Munich, Prague, Protvino, Saclay,  
Tel Aviv, Torino, Trieste, Warsaw, Yamagata

~240 physicists, 30 institutes

Beam:  $2 \cdot 10^8 \mu^+$ / spill (4.8s / 16.2s)

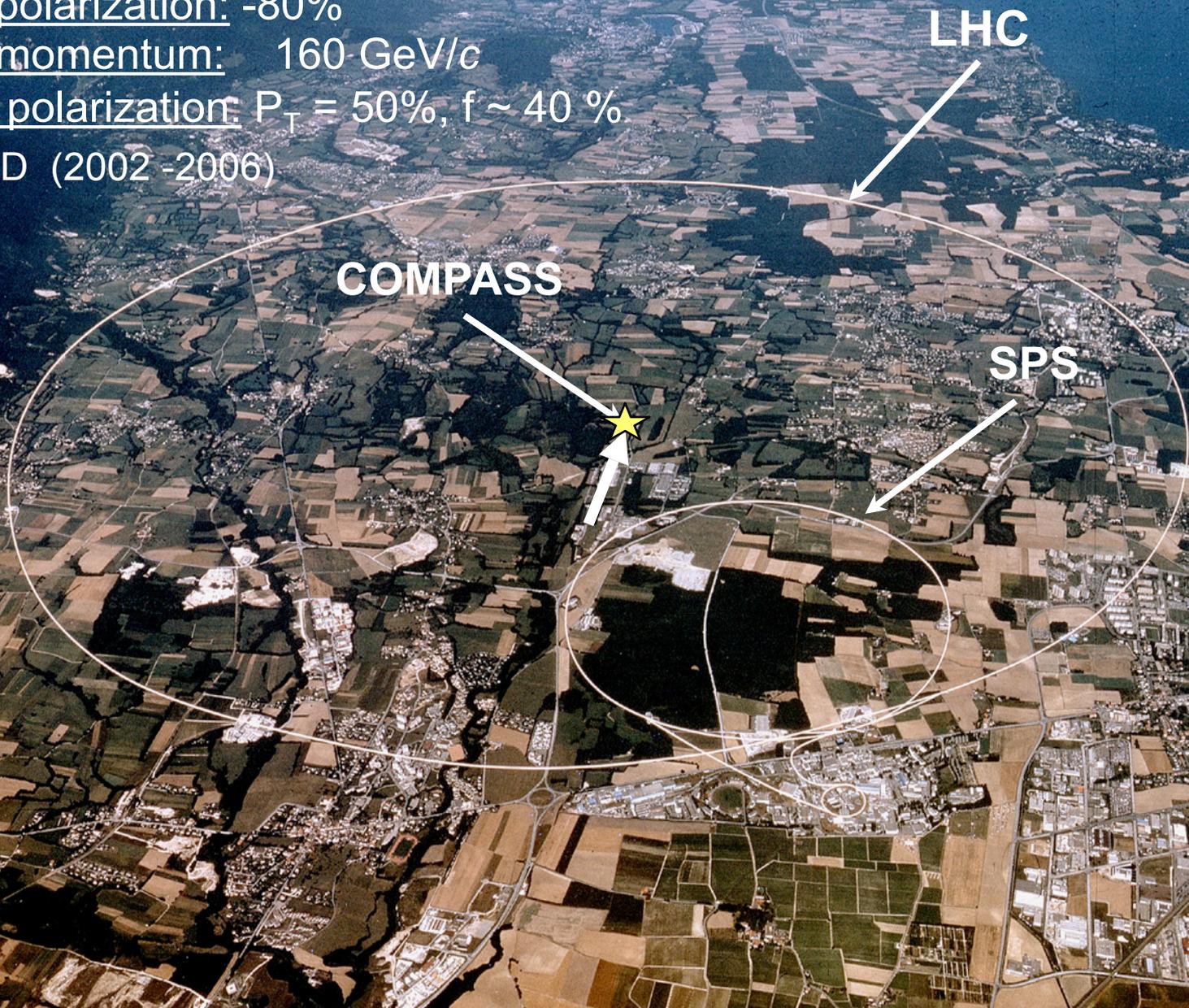
Luminosity  $\sim 5 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$

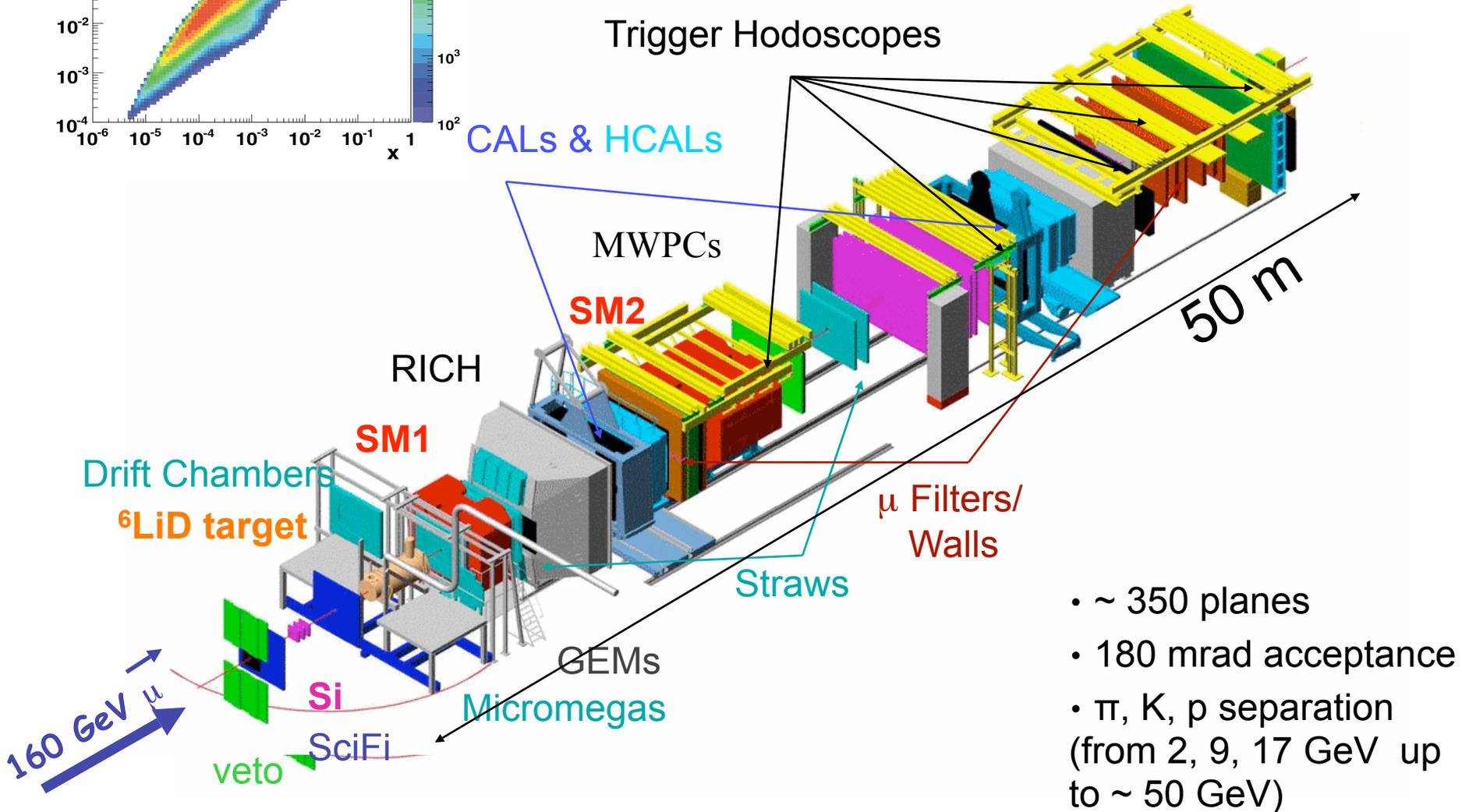
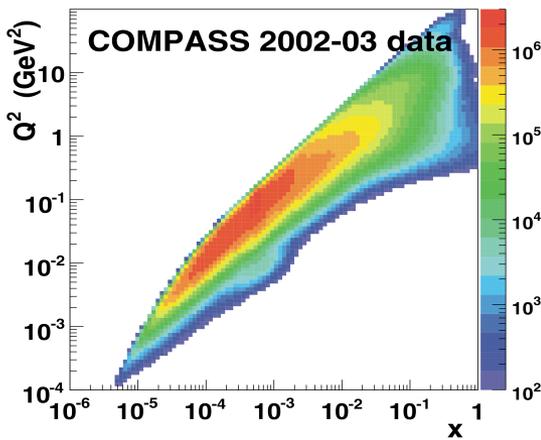
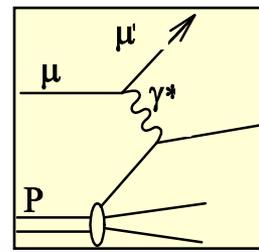
Beam polarization: -80%

Beam momentum: 160 GeV/c

Target polarization:  $P_T = 50\%$ ,  $f \sim 40\%$

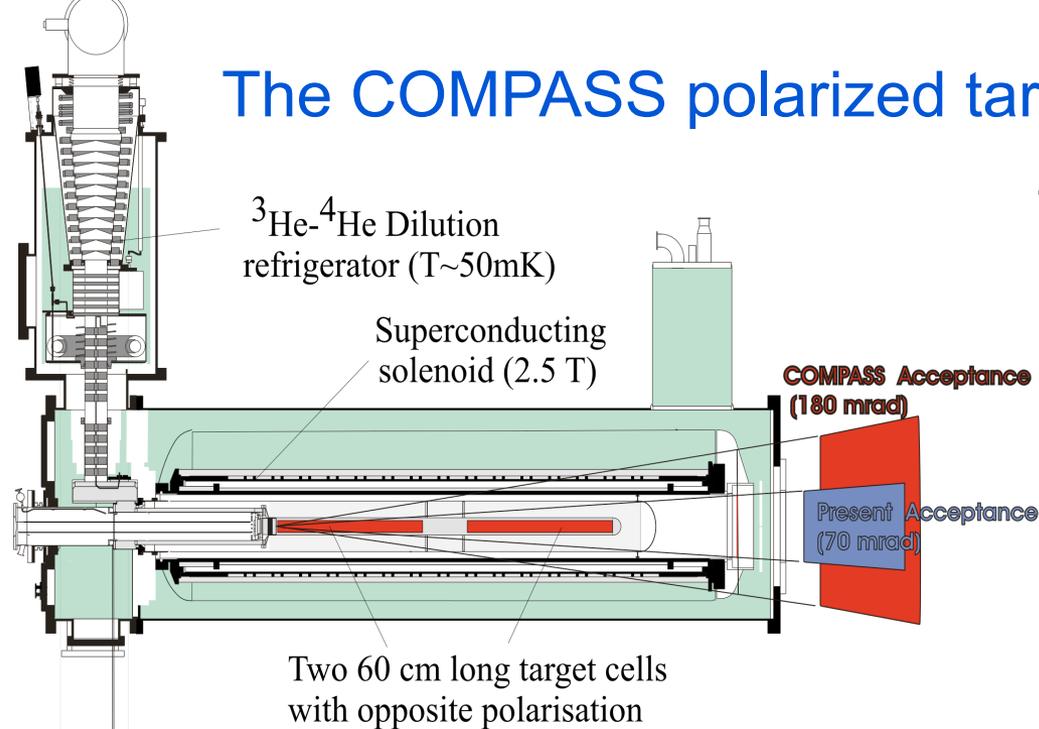
for  ${}^6\text{LiD}$  (2002 - 2006)





- ~ 350 planes
- 180 mrad acceptance
- $\pi$ , K, p separation (from 2, 9, 17 GeV up to ~ 50 GeV)

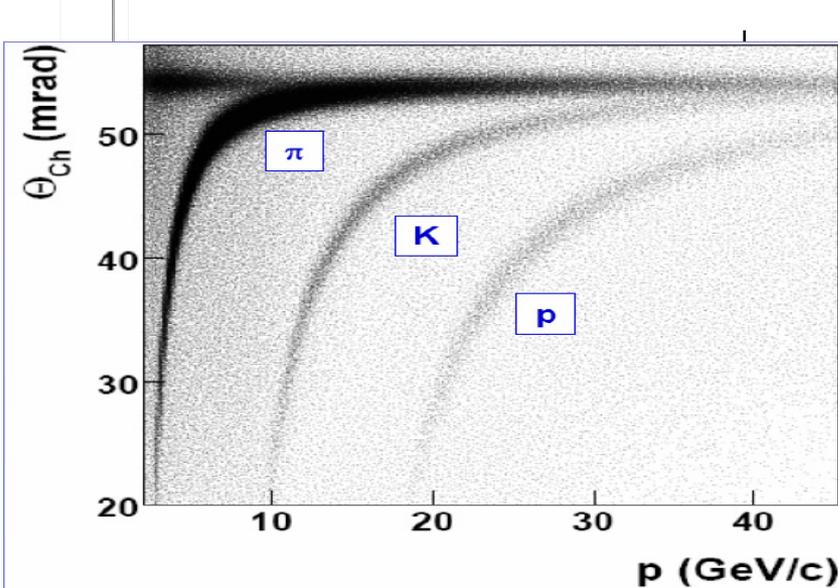
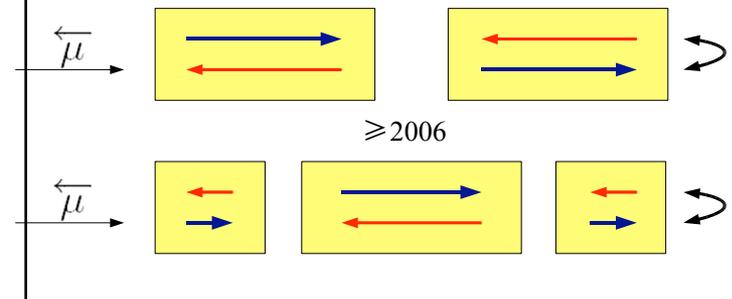
# The COMPASS polarized target



Target material:  $^6\text{LiD}$   
 Polarisation:  $>50\%$   
 Dilution factor:  $\sim 0.4$   
 Dynamic Nuclear Polarization

2006 - new solenoid with acceptance 180 mrad  
 3 target cells (reduce false asymmetries)

2002 - 2004



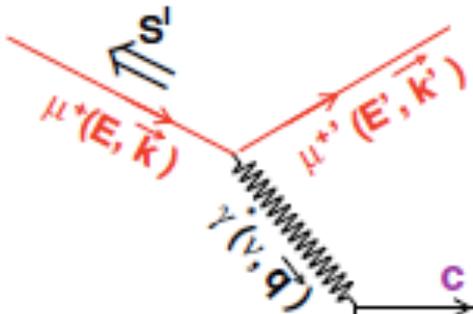
RICH 2006 upgrade : better PID

MAPMTs in central region

APV electronics in periphery

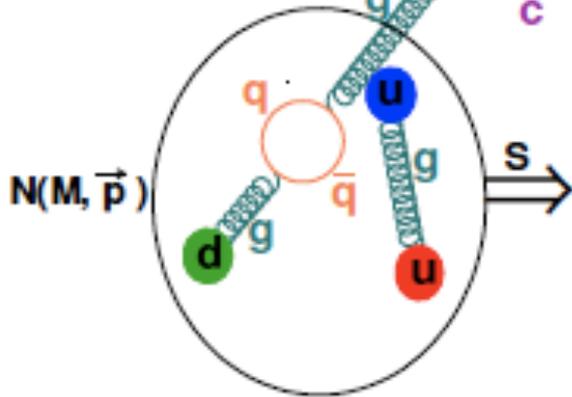
# Contents

- COMPASS experiment
- Charmed meson reconstruction at COMPASS
- Signal to background parameterization
  
- New channels from  $D^*$ :  $\pi^0$  reflection “bump” and “RICH sub-threshold kaons events”
- Neural network approach to signal/background parameterization
- New  $\Delta G/G$  result in LO
  
- Asymmetries from open-charm
- $\Delta G/G$  in LO approximation from COMPASS main  $D^0$  and  $D^*$  channels
- Summary and plans



Idea: tag  $\gamma^*g \rightarrow c\bar{c}$  via open-charm production mechanism

COMPASS:  
PLB676(2009)31



- Clean channel (less MC dependent) under the assumption that production mechanism is PGF only (true in LO pQCD)
- Resolved photon and “intrinsic” charm production mechanism negligible in COMPASS kinematics
- Limited statistics (no vertex detector - long polarized target)
- Huge combinatorial background
- NLO corrections potentially important

$$A^{\text{raw}} = \frac{N^{\uparrow\downarrow} - N^{\uparrow\uparrow}}{N^{\uparrow\downarrow} + N^{\uparrow\uparrow}} = P_B P_T f a_{LL} \frac{\sigma_{PGF}}{\sigma_{PGF} + \sigma_{bgd}} \frac{\Delta g}{g} + A^{\text{bgd}}$$

$P_B, P_T$  - are beam and target polarizations,

$f$  - dilution factor ( $\sim 0.4$  for  ${}^6\text{LiD}$  target)

$a_{LL}$  is a partonic asymmetry (analyzing power) for subprocess:  $\mu g \rightarrow c\bar{c}_{\text{bar}} \mu'$

- $\frac{\sigma_{PGF}}{\sigma_{PGF} + \sigma_{bgd}}$  is parameterized in terms of 10 variables, not just as a function of the reconstructed mass.
- each event is weighted with its analyzing power:

$$f P_B a_{LL} \frac{\sigma_{PGF}}{\sigma_{PGF} + \sigma_{bgd}}$$

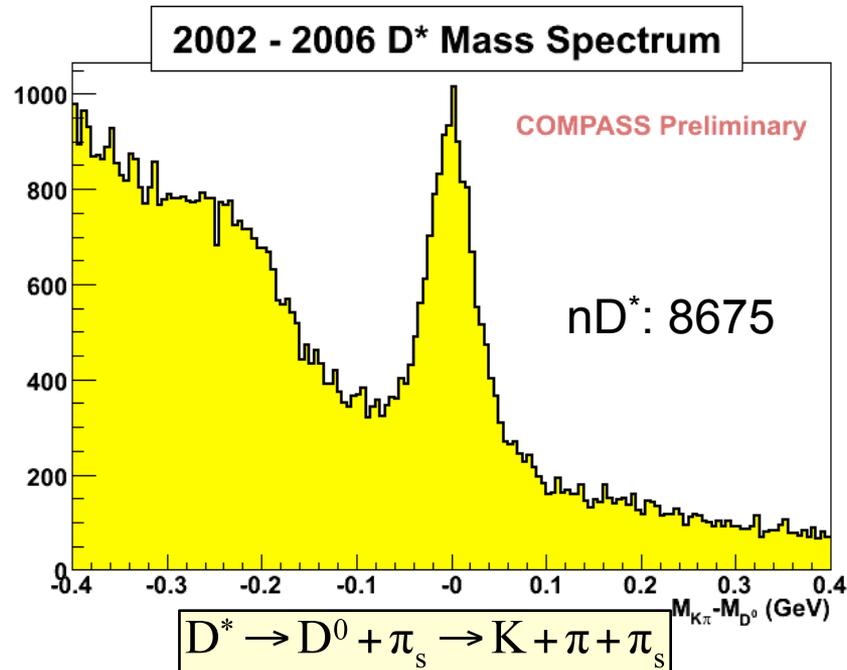
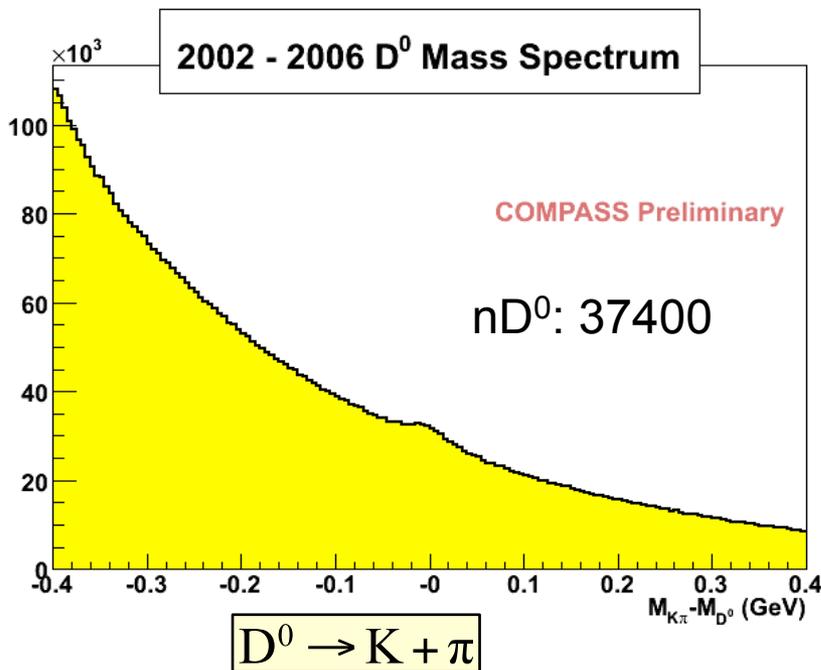
Large gain in statistics ( $a_{LL}$  has positive and negative values)

- events are simultaneously weighted with  $(\dots \frac{\sigma_{BGD}}{\sigma_{PGF} + \sigma_{bgd}})$   
 $\Rightarrow$  allows simultaneous extraction of signal and background asymmetries,  
 more efficient than side band subtraction

- **Events considered** (*resulting from c quarks fragmentation*):
  - $D^0 \rightarrow K\pi$  (BR: 4%)
  - $D^* \rightarrow D^0\pi_s \rightarrow K\pi\pi_s$  (30%  $D^0$  tagged with  $D^*$ )
- **Selection to reduce the combinatorial background:**
  - Kinematical cuts:  $Z_D$ ,  $D^0$  decay angle, K and  $\pi$  momentum
  - RICH identification: K and  $\pi$  ID + electrons rejected from the  $\pi_s$  sample

Thick target - no D<sup>0</sup> vertex reconstruction

D<sup>0</sup> reconstruction: Kπ invariant mass + cuts on D<sup>0</sup> decay angle + z<sub>D</sub> + RICH particle identification (different likelihoods)



+2 more channels :

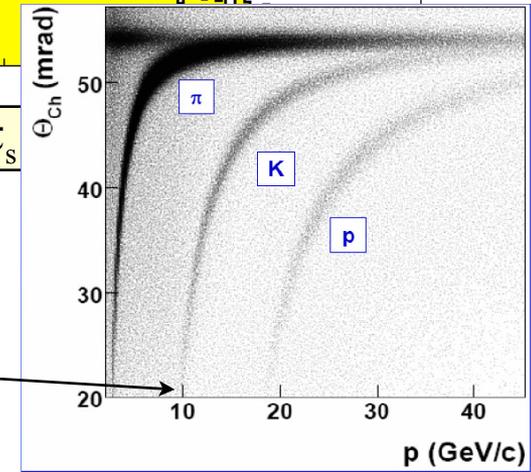
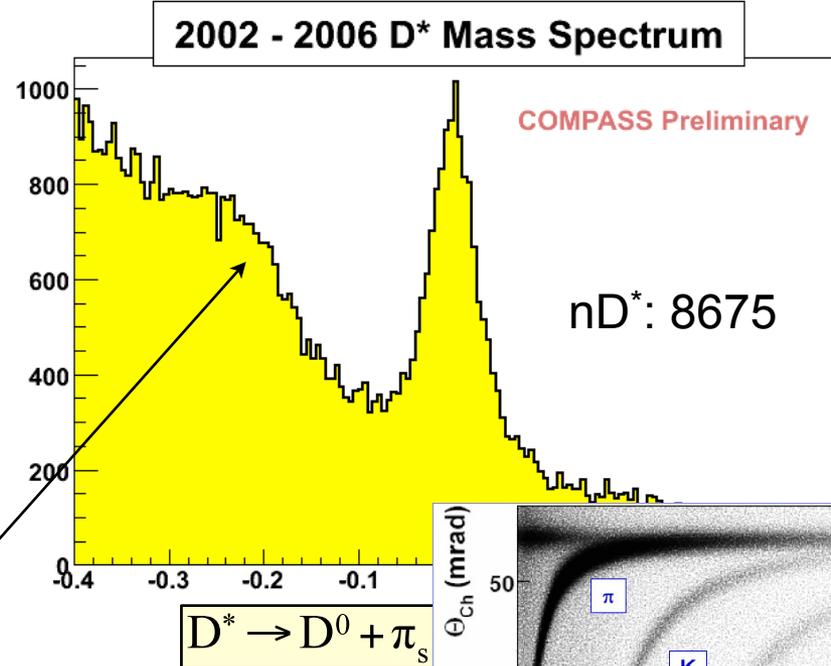
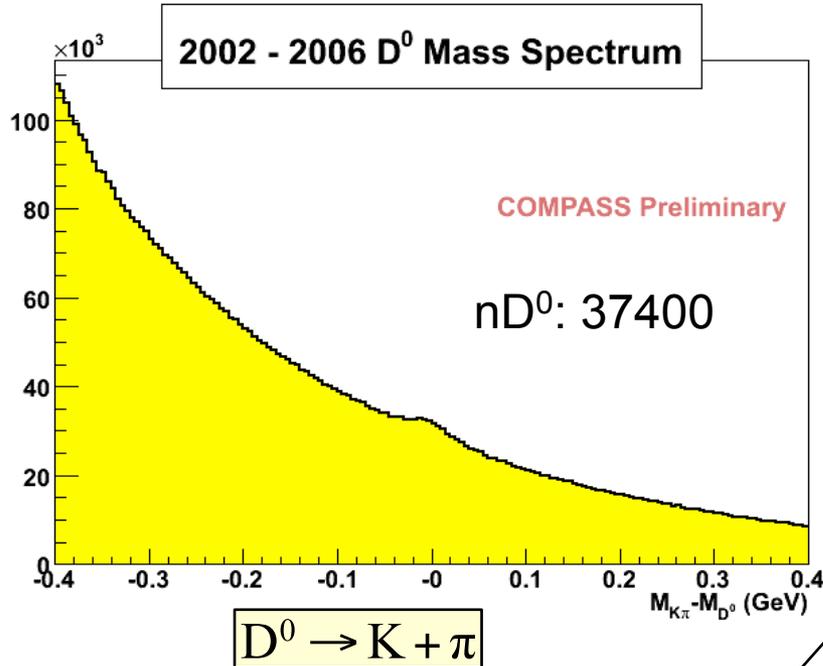
- $D^0 \rightarrow K^- \pi^+ + (\pi^0)$
- $D^{*+} \rightarrow D^0 \pi_{soft}^+ \rightarrow K^- \pi^+ \pi_{soft}^+$

(with kaons below RICH threshold of 9 GeV)

New!

Thick target - no D<sup>0</sup> vertex reconstruction

D<sup>0</sup> reconstruction: Kπ invariant mass + cuts on D<sup>0</sup> decay angle + z<sub>D</sub> + RICH particle identification (different likelihoods)



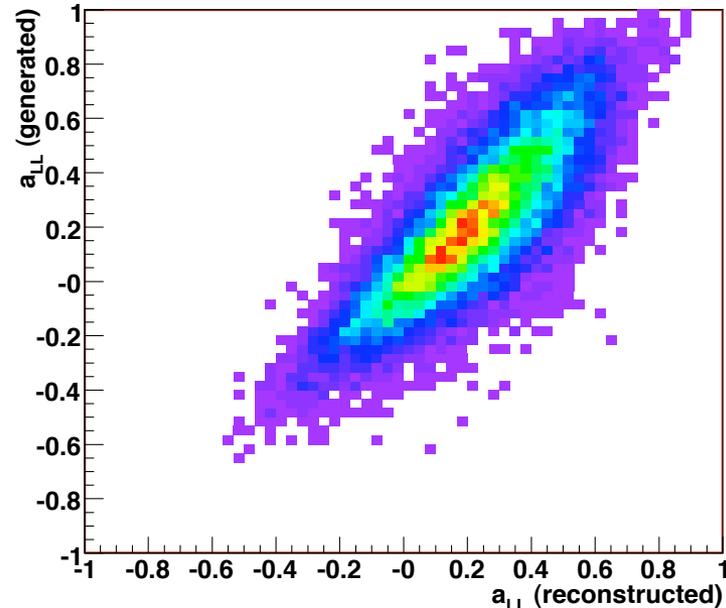
- +2 more channels :
- $D^0 \rightarrow K^- \pi^+ + (\pi^0)$
  - $D^{*+} \rightarrow D^0 \pi_{soft}^+ \rightarrow K^- \pi^+ \pi_{soft}^+$
- (with kaons below RICH threshold of 9 GeV)

- $a_{LL}$  is dependent on full knowledge of partonic kinematics:

$$a_{LL} = \frac{\Delta \sigma^{PGF}}{\sigma_{PGF}}(y, Q^2, x_g, z_C, \phi)$$

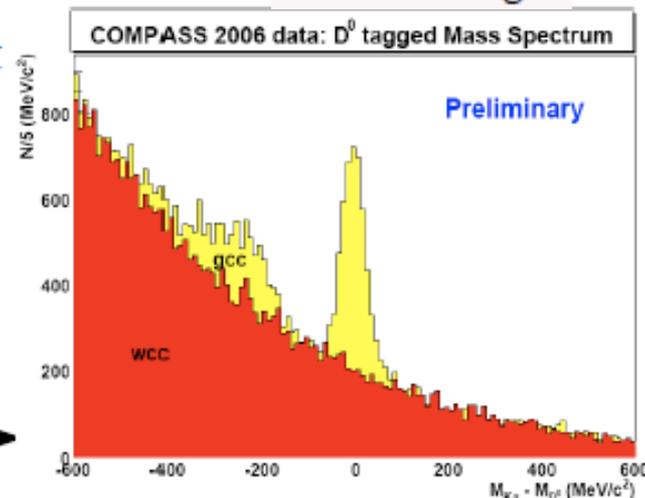
- Can't be experimentally obtained!  $\Rightarrow$  only one charmed meson is reconstructed
- $a_{LL}$  is obtained from Monte-Carlo (*in LO*), to serve as input for a Neural Network parameterization on reconstructed kinematical variables:  $y, x_{Bj}, Q^2, z_D$  and  $p_{T,D}$

- 82% correlation NN/MC
- very large dispersion of values, even change of sign: weighting essential



- **Two real data samples (with same cuts) are compared by the Neural Network (giving as input some kinematic variables as a learning vector):**
  - **Signal model**  $\rightarrow$  **gcc** =  $\mathbf{K}^+\pi^-\pi_s^- + \mathbf{K}^-\pi^+\pi_s^+$  ( $D^*$  spectrum: signal + bg.)
  - **Background model**  $\rightarrow$  **wcc** =  $\mathbf{K}^+\pi^+\pi_s^- + \mathbf{K}^-\pi^-\pi_s^+$
- **If the background model is good enough: Net is able to distinguish the signal from the combinatorial background on a event by event basis!**
- **$\Sigma$  is built in the same way as for main channels, BUT:**
  - Only 1 variable is used: Neural Network output
    - Sorts the events according to similar kinematic dependences (thus improving our statistical precision)
    - Results from 2 real data samples comparison, in a mass window around the meson mass

$$\Sigma = \frac{\sigma_{PGF}}{\sigma_{PGF} + \sigma_{bgd}}$$



New preliminary result including all channels

$$\Delta G/G = -0.39 \pm 0.24 \text{ (stat)}$$

published:  $\Delta G/G = -0.49 \pm 0.27 \text{ (stat)} \pm 0.11 \text{ (syst)}$

$$\left\langle x_g \right\rangle = 0.11^{+0.11}_{-0.05}$$
$$\left\langle \mu^2 \right\rangle = 13 \text{ GeV}^2$$

10% gain in statistical precision!

# Summary

- Small value of  $\Delta G/G$  is preferred -  $\Delta G/G$  compatible with 0 within  $2\sigma$
- Under study:
  - pure NN approach (fit independent)
  - 2007 data (proton)
  - others channels (4 particles from decay)
  - NLO analysis

- Part II - *NLO QCD predictions for gluon polarization from open-charm asymmetries measured at COMPASS*

- Model independent asymmetries were extracted from data only

$$A_{\text{exp}} = P_B P_T f \left[ R_{PGF} DA^{\gamma N \rightarrow DX} + (1 - R_{PGF}) A_{bkg} \right]$$

- $\frac{\Delta g}{g}$  can be extracted using  $a_{LL}^{PGF}$  calculated at LO :

published:  
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$$A_{\text{exp}} = P_B P_T f \left[ R_{PGF} a_{LL}^{PGF} \frac{\Delta g}{g} + (1 - R_{PGF}) A_{bkg} \right]$$

- Similar analysis, but with weight

$$w = f P_B \frac{S}{S+B} a_{LL}$$

instead of

$$w = f P_B \frac{S}{S+B} D$$

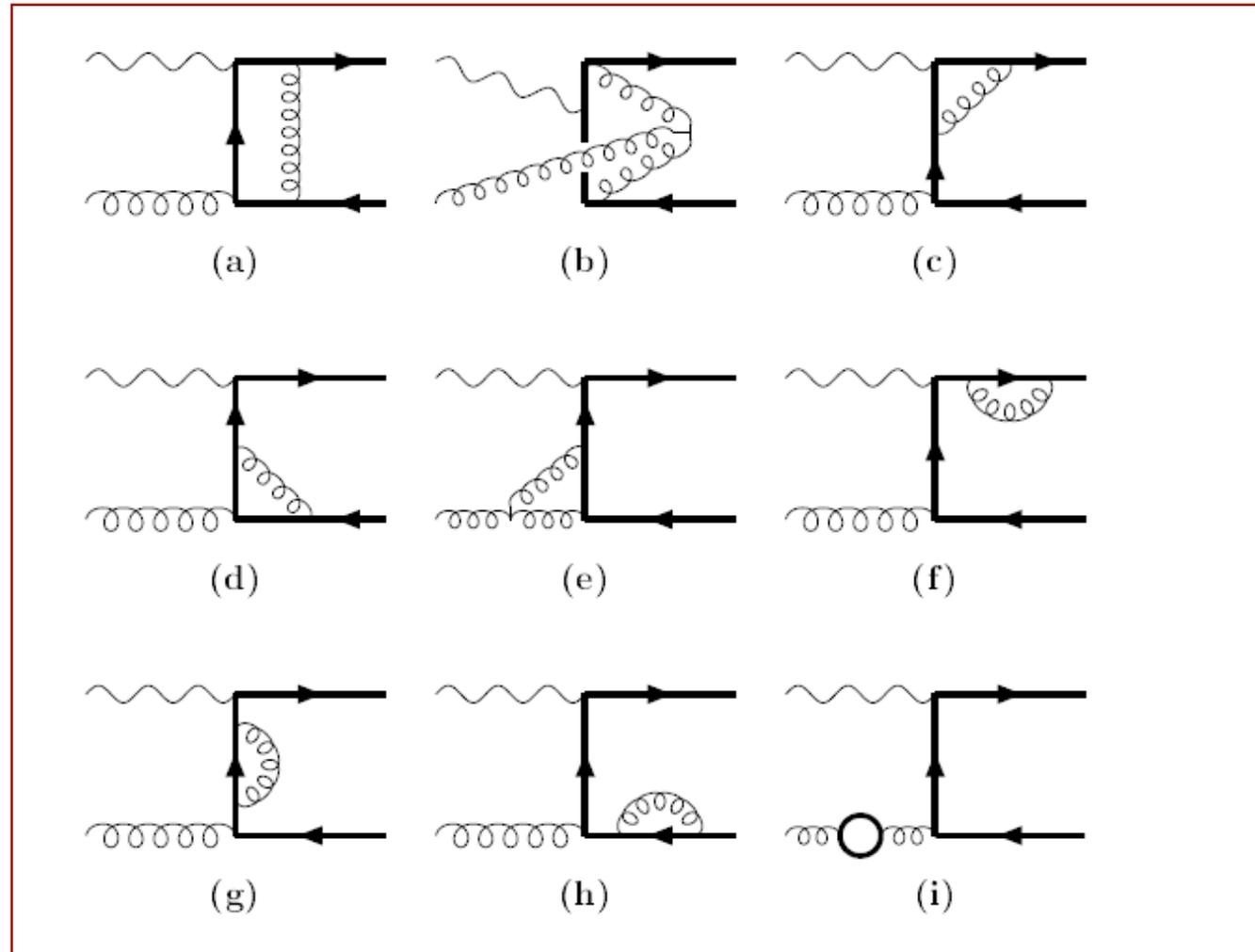
# Contents

- LO and NLO QCD processes for open-charm production
- The role of MC in the COMPASS open-charm analysis
- NLO corrections and the MC approach
- $\Delta G/G$  in the NLO approximation from COMPASS open-charm asymmetries
- Summary



NLO calculations for partonic cross sections – much more complicated. Here Feynmann diagrams for „virtual +soft” corrections are presented.

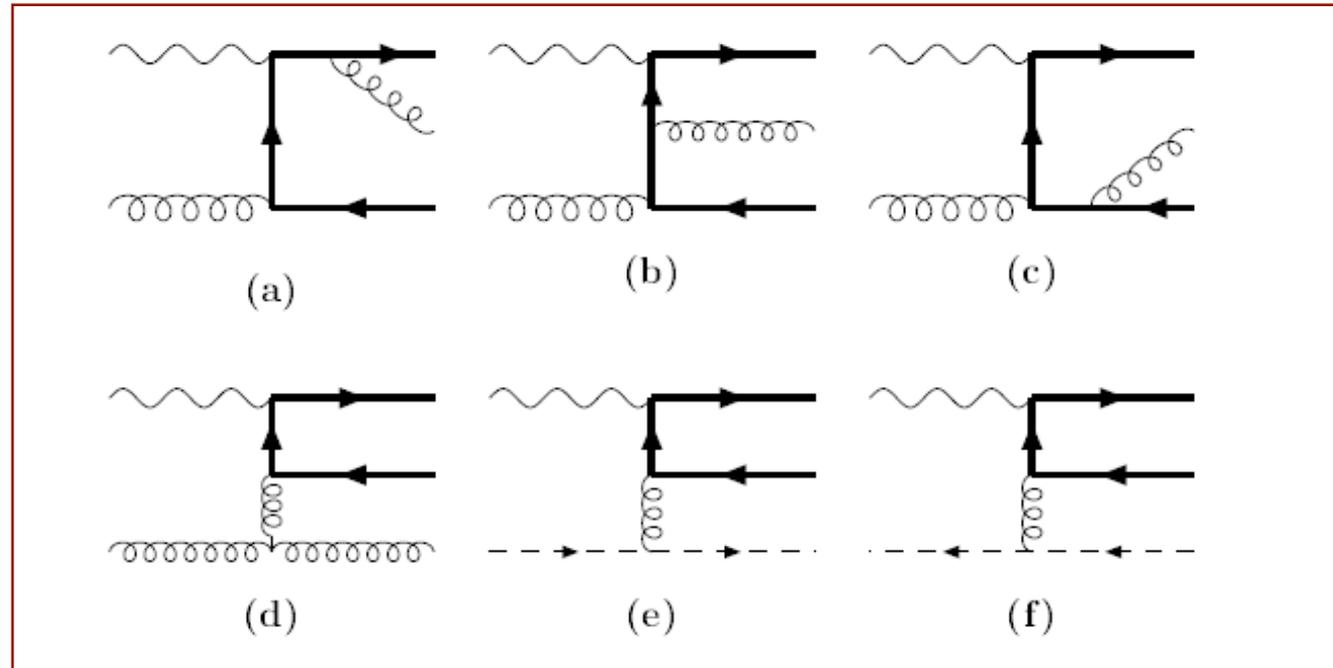
Loops produce divergences:  
 UV – removed by renormalization procedure,  
 IR - related to „zero” momenta of Internal loop particles



NLO calculations for partonic cross sections.

Here Feynmann diagrams for „hard gluon emissions” corrections.

**IR** - related to „soft” momenta of gluon emissions. Here there is also **colliner** divergency for 3-gluons coupling



„VS” and „Hard” parts contain so-called double pole:  $\sim \frac{1}{\epsilon_{UV}} \frac{1}{\epsilon_{IR}}$

These terms **MUST** cancell **Factorization**.



### The structure of the cross sections in NLO QCD

$$\frac{\sigma^{NLO}}{dt_1 du_1} = \frac{\alpha\alpha_s^2 e_q^2}{s^2} \left( \sigma_{Hard}^{non-abelian} + \sigma_{Hard}^{QED} + \sigma_{SV}^{non-abelian} + \sigma_{SV}^{QED} + \sigma^F \log\left(\frac{\mu_f^2}{m^2}\right) \right)$$

$$\frac{\Delta\sigma^{NLO}}{dt_1 du_1} = \frac{\alpha\alpha_s^2 e_q^2}{s^2} \left( \Delta\sigma_{Hard}^{non-abelian} + \Delta\sigma_{Hard}^{QED} + \Delta\sigma_{SV}^{non-abelian} + \Delta\sigma_{SV}^{QED} + \Delta\sigma^F \log\left(\frac{\mu_f^2}{m^2}\right) \right)$$

Kinematics:

$$s + t_1 + u_1 = 0 \quad \longleftarrow \text{for LO and „SV” NLO part}$$

$$s + t_1 + u_1 = s_4 \quad \longleftarrow \text{for „Hard” NLO part ( integration over } s_4 \text{)}$$

$$t_1 = t - m^2 \quad u_1 = u - m^2$$

I.Bojak, M.Stratmann, hep-ph/9807405,  
 Nucl.Phys.B 540 (1999) 345, I.Bojak, PhD thesis  
 J.Smith, W.L.Neerven, Nucl.Phys.B 374 (1992)36

W.Beenakker, H.Kuijf, W.L.Neerven,,J.Smith, Phys.Rev.D40(1989)54

1. NLO corrections available only for photo-production limit.  $Q^2 = 0$
2. No big problem for COMPASS: D – depolarization factor

$$a_{LL}^{LO} = D a_{LL}^{LO,\gamma g}$$

$$a_{LL}^{NLO} = D a_{LL}^{NLO,\gamma g}$$

Neglecting  $Q^2$  in this parts is not a big sin – unimportant effect ☺

$a_{LL}^{NLO,\gamma g}$  Calculated in NLO with the assumptions of photo-production.

$$A = \frac{\int \Delta G(x_g) \Delta \hat{\sigma}^{LO} du_1 dt_1}{\int G(x_g) \hat{\sigma}^{LO} du_1 dt_1} = \frac{\int \frac{\Delta G}{G} \frac{\Delta \hat{\sigma}^{LO}}{\hat{\sigma}^{LO}} G(x_g) \hat{\sigma}^{LO} du_1 dt_1}{\int G(x_g) \hat{\sigma}^{LO} du_1 dt_1}$$

$$A = \langle \frac{\Delta G}{G} \frac{\Delta \hat{\sigma}^{LO}}{\hat{\sigma}^{LO}} \rangle = \langle \frac{\Delta G}{G} \rangle \langle \frac{\Delta \hat{\sigma}^{LO}}{\hat{\sigma}^{LO}} \rangle = \langle \frac{\Delta G}{G} \rangle \langle a_{LL}^{LO} \rangle$$

$$\langle \frac{\Delta G}{G} \rangle = \frac{\int \frac{\Delta G}{G} a_{LL}^{LO} G(x_g) \hat{\sigma}^{LO} du_1 dt_1}{\int a_{LL}^{LO} G(x_g) \hat{\sigma}^{LO} du_1 dt_1} = \frac{\Delta G}{G} (\langle x_g \rangle)$$

$$\frac{\Delta G}{G} \approx a(x_g - \langle x_g \rangle) + b \quad b = \frac{\Delta G}{G} (\langle x_g \rangle)$$

$$\langle x_g \rangle = \frac{\int x_g a_{LL}^{LO} G(x_g) \hat{\sigma}^{LO} du_1 dt_1}{\int a_{LL}^{LO} G(x_g) \hat{\sigma}^{LO} du_1 dt_1}$$

$$\langle a_{LL}^{LO} \rangle = \frac{\int a_{LL}^{LO} G(x_g) \hat{\sigma}^{LO} du_1 dt_1}{\int G(x_g) \hat{\sigma}^{LO} du_1 dt_1}$$

## The role of MC and theoretical input

- $a_{LL}$  allows to calculate **gluon polarization from measured asymmetries**
- COMPASS is using **weighted method** - and  $a_{LL}$  (theory input) is used in the weight. To calculate  $a_{LL}$  MC generator with simulation of the apparatus + reconstruction is used; then  $a_{LL}$  is parameterized and run on real data to estimate  $a_{LL}$  event by event.
- The weight has impact on **value, statistical error and  $\langle x_G \rangle$  !**
- Changing approximation (from  $a_{LL}$  in LO to NLO) can have a serious consequence on importance and precision of the COMPASS result!

## Procedure in NLO

- MC with parton shower (MC PS on) to simulate phase space for real emissions
- events have  $s_1, u_1$  and  $t_1$  and  $s_1+t_1+u_1 \neq 0$
- Method 1:  
event is defined by  $cc_{bar}$  system:  $u_1$  and  $t_1$  define event.  
Integrations over  $s_4$  is performed from 0 up to  $s_1+t_1+u_1$
- Method 2:  
event is defined by  $s_1$  and  $t_1(u_1)$  - only one charm observed.  
Integration over  $s_4$  is performed from 0 up to  $s_1+t_1+u_1$

## method 1

- **Advantage:** similar to theoretical calculations in bins - gluons convoluted with hard part in the integration over  $s_4$  - good for collinear divergence removal procedure
- **Disadvantage:** shape of gluon distribution is required - model of gluon polarization needed!
- **Assumption done:** MC with PS on reproduces correctly the event distributions produced according to  $\sigma^{\text{NLO}} * G(s_1^{\text{el}})/G(s_1)$



## method 1 - examples

- Model of the gluon polarization:
  1.  $\Delta G/G = \text{const}$ ,  
COMPASS QCD fits:
  - 2 - positive gluons
  - 3 - negative gluons
- used to illustrate the potential differences between methods based on the same MC events, good for systematic studies

- This part of the talk **is not** on behalf of COMPASS - pure MC generator (aroma) has been used -no acceptance/reconstruction/apparatus simulation used.
- But - it is not crucial thanks to weighting!
- Tested and compared for LO results
- PDF unpolarized used: MRST2004 LO/NLO, GRV98 LO
- Scale:  $2m_c$
- No special cuts except cut on energy of the  $E_D$
- MC used only for signal simulation: PSoff/on (LO/NLO)
- $s/(s+b)$  assumed 1 (no background simulation) - therefore statistical error is smaller than in COMPASS analysis

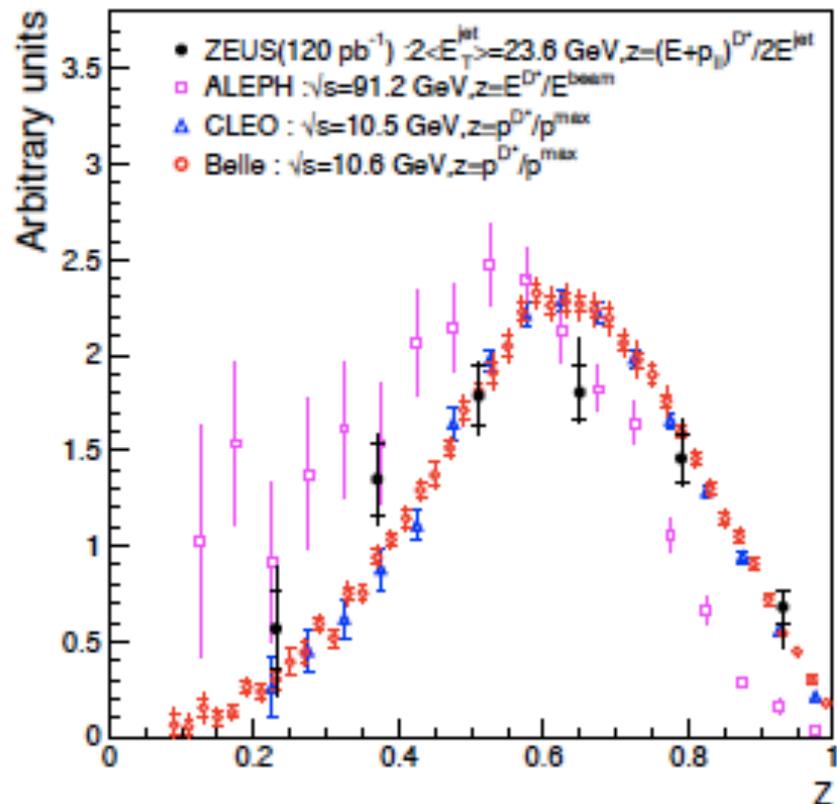
based on 2002-2006 COMPASS data and  
published asymmetries in bins (PLB 676(2009)31)

- LO weighted from PLB  $\Delta G/G = -0.49 \pm 0.27$
- LO (from asym. and  $a_{LL}$  from PLB)  $\Delta G/G = -0.42 \pm 0.28$
- LO (MC P<sub>Soff</sub>, asym. from PLB):  $\Delta G/G = -0.47 \pm 0.23$
  
- NLO (MC P<sub>Son</sub>, asym. from PLB)
- method 2:  $\Delta G/G = +0.032 \pm 0.231$
- $\Delta G/G = \text{const}$  (method 1):  $\Delta G/G = -0.051 \pm 0.239$
- $\Delta G/G > 0$ , Compass fit (method 1):  $\Delta G/G = -0.036 \pm 0.239$
- $\Delta G/G < 0$ , Compass fit (method 1):  $\Delta G/G = -0.057 \pm 0.240$

## Comment:

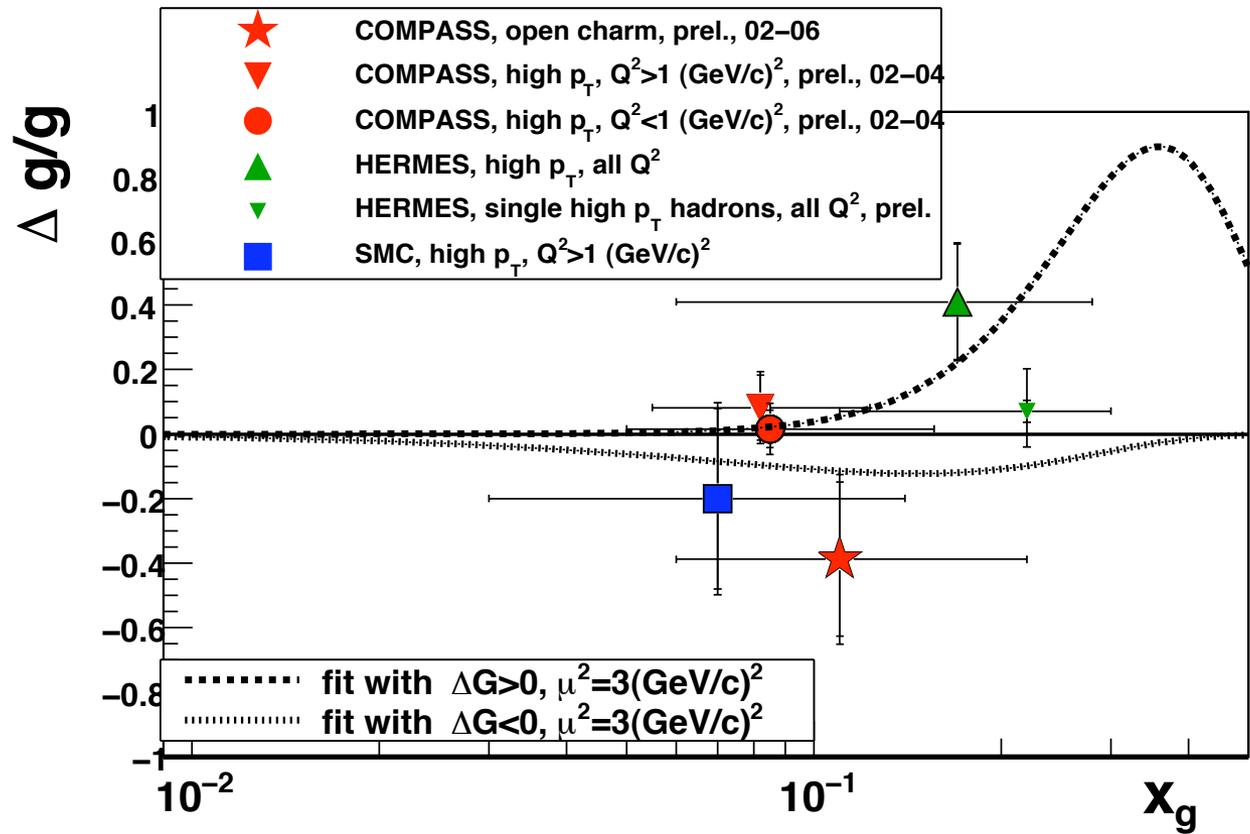
- MC with PS on simulates NLO kinematics of the event in the approximation (Sudakov formfactor approach)
- MC is in still in LO approx., PS - depends on MC steering parameters.
- Another approach: simple MC generator **weighted** by **correct NLO cross section**
- Belle  $D^*/D^0$  fragmentation function

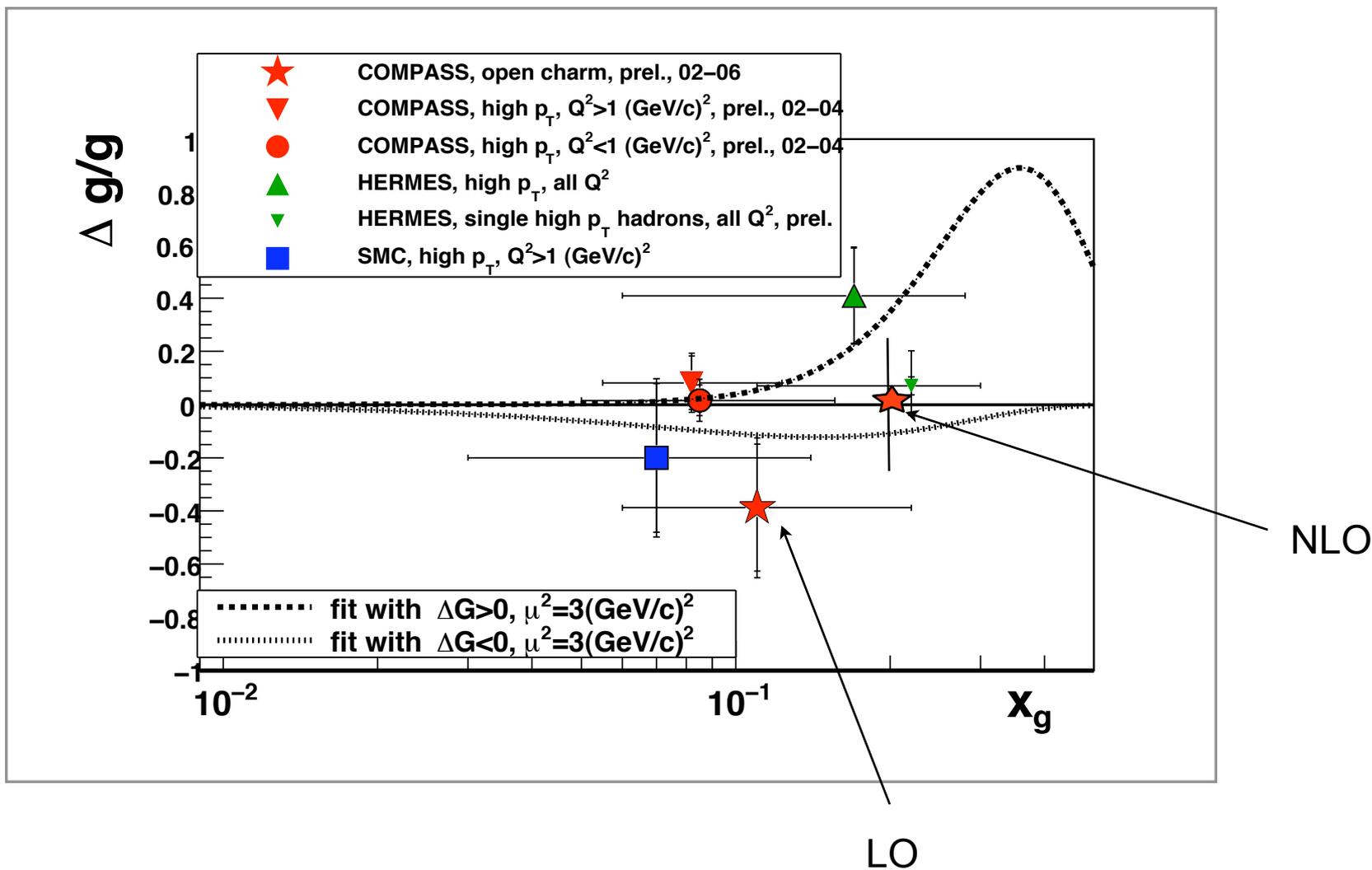
Peterson set with slightly modified parameters to describe Belle data



Fragmentation function	Functional form	Comment
Bowler	$N \frac{1}{z^{1+bm^2}} (1-z)^a \exp(-\frac{bm^2}{z})$	$a, b$ identical for all quarks
Lund	$N \frac{1}{z} (1-z)^a \exp(-\frac{bm^2}{z})$	$a, b$ identical for all quarks
Kartvelishvili	$N z^{\alpha_c} (1-z)$	
Collins-Spiller	$N (\frac{1-z}{z} + \frac{(2-z)\epsilon'_c}{1-z})(1+z^2)(1-\frac{1}{z} - \frac{\epsilon'_c}{1-z})^{-2}$	
Peterson	$N \frac{1}{z} (1 - \frac{1}{z} - \frac{\epsilon_c}{1-z})^{-2}$	widely used



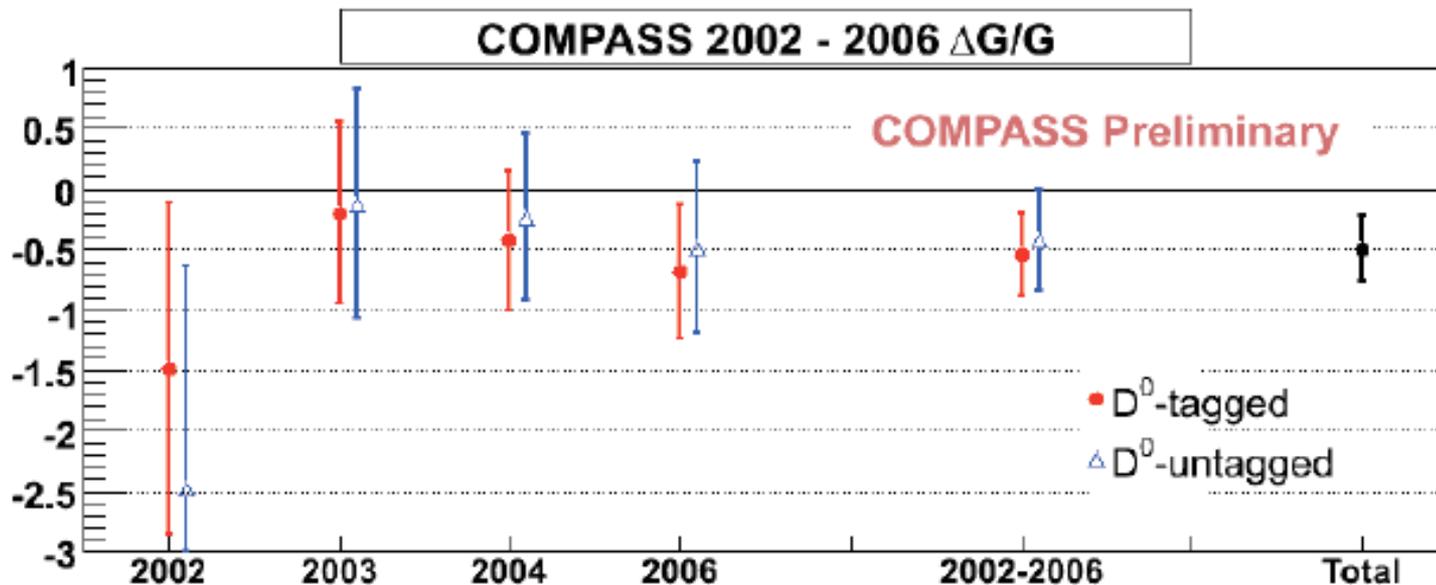




## Conclusions

- NLO corrections for  $a_{LL}$  (PGF channel) for COMPASS open-charm asymmetry bins have been computed based on MC PS on and MC weighted by correct NLO cross section
- Preliminary result for gluon polarization has been shown - gluon polarization consistent with 0.
- Missing NLO corrections - quark initiated processes - are under consideration

# Spares



$\Delta G/G = -0.49 \pm 0.27$  (stat)  $\pm 0.11$  (syst)

Systematics :

Source	$D^0$	$D^*$
Beam polar	0.025	0.025
Target polar	0.025	0.025
Dil. Fact.	0.025	0.025
False asymmetry	0.05	0.05
Signal extraction ( $\Sigma$ )	0.07	0.01
$a_{11}$ (charm mass)	0.05	0.03
<b>TOTAL</b>	<b>0.11</b>	<b>0.07</b>

$\langle x_g \rangle = 0.11^{+0.11}_{-0.05}$   
 $\langle \mu^2 \rangle = 13 \text{ GeV}^2$

published:  
PLB676(2009)31

# Open-charm signal - per year

$K\pi$  invariant mass

weighted spectra

2002

2003

2004

2006

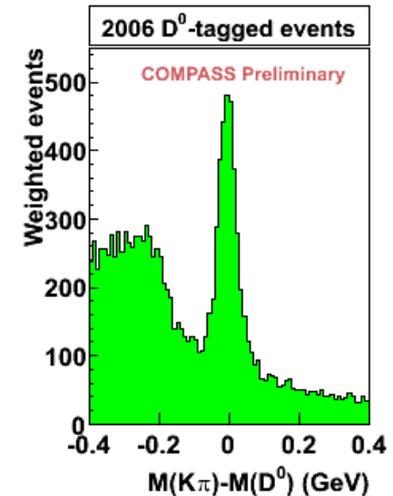
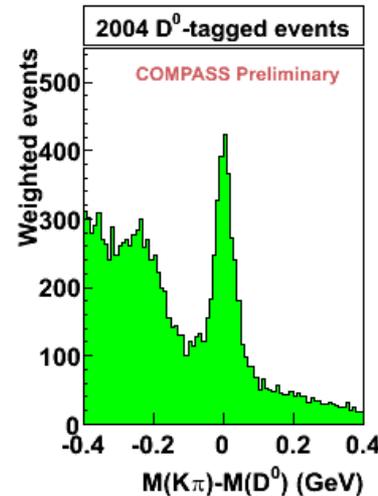
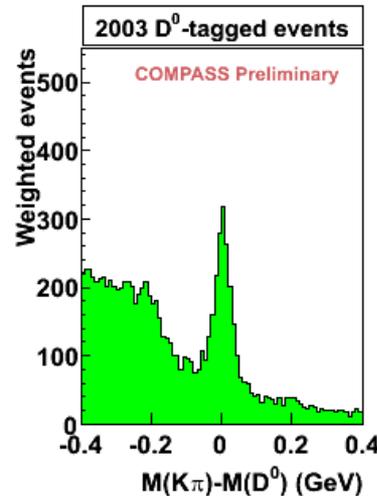
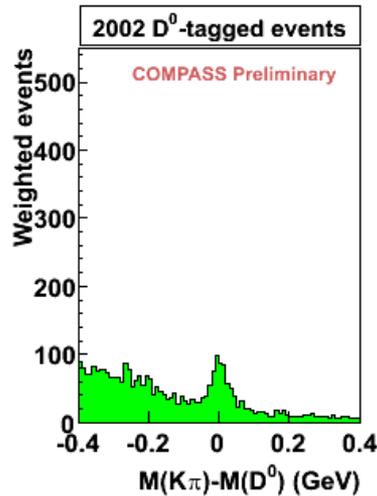
$0.43 \text{ fb}^{-1}$

$0.58 \text{ fb}^{-1}$

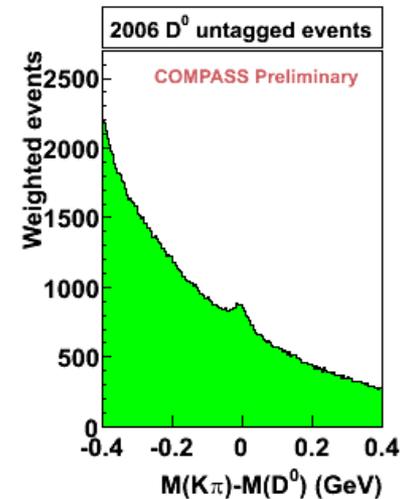
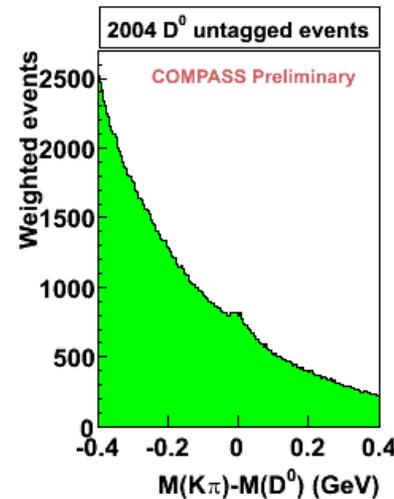
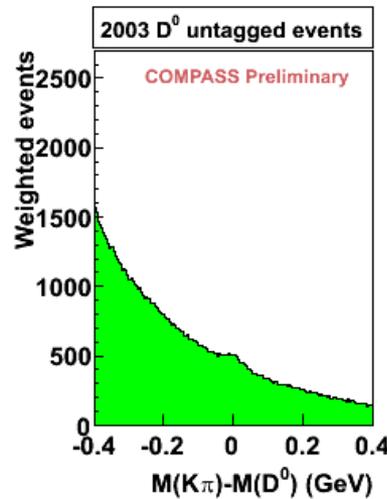
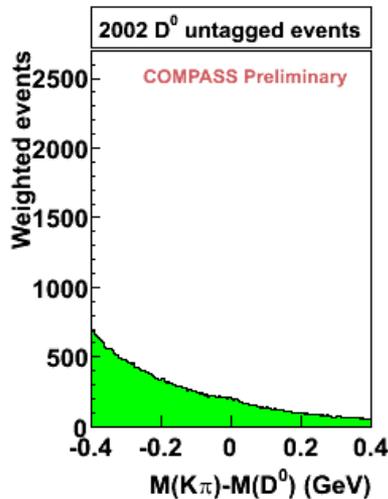
$0.92 \text{ fb}^{-1}$

$0.85 \text{ fb}^{-1}$

$D^*$

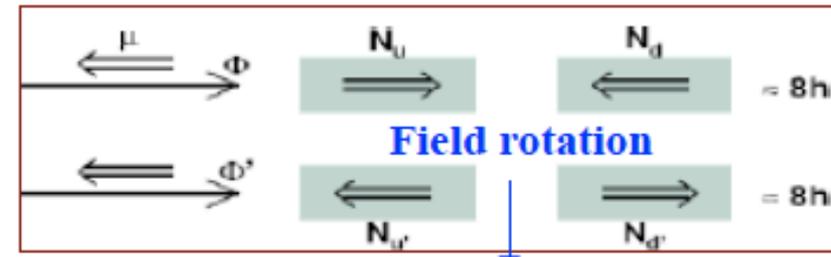


$D^0$



Considering  $A_B = 0$

$$\frac{\Delta G}{G} = \frac{1}{2P_T P_\mu f a_{LL} \frac{S}{S+B}} \times \left( \frac{N^u - N^d}{N^u + N^d} + \frac{N^{d'} - N^{u'}}{N^{u'} + N^{d'}} \right)$$



$a_{LL}$  → partonic asymmetry  
 $\frac{S}{S+B}$  → event weight  
 $\left( \frac{N^u - N^d}{N^u + N^d} + \frac{N^{d'} - N^{u'}}{N^{u'} + N^{d'}} \right)$  → signal strength of Open-Charm events

equal acceptance for both cells

- Using →  $A_1 = \langle a_{LL} \rangle \langle \frac{\Delta G}{G} \rangle$  with  $a_{LL} = \frac{\Delta \sigma^{PGF}}{\sigma^{PGF}}$

asymmetries are less sensitive to experimental changes than cross section differences

- Events with small  $(P_\mu \cdot P_T \cdot f \cdot a_{LL} \cdot (S/S+B))$  factors contain less information about the asymmetry:

- Weighting the events with the option chosen minimizes de statistical error

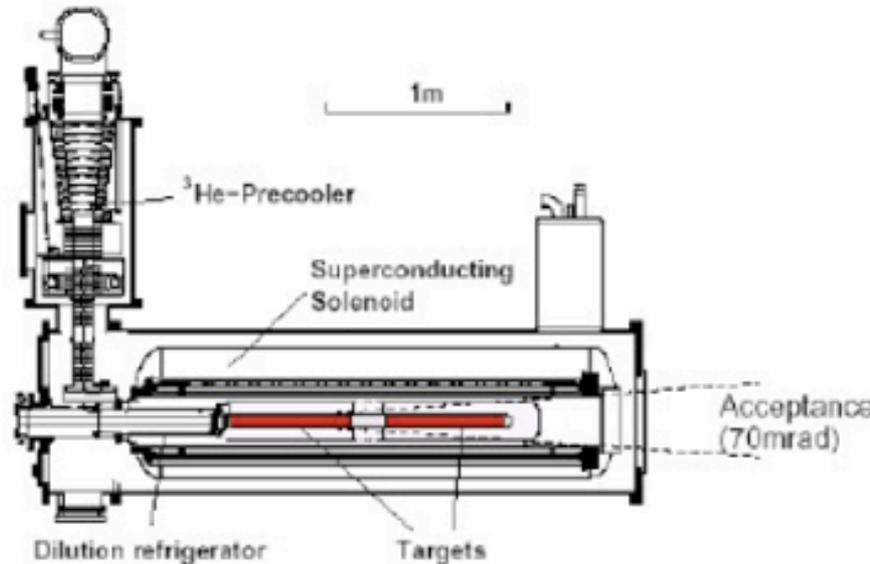
$$\frac{\Delta G}{G} = \frac{1}{2P_T} \times \left( \frac{\omega_u - \omega_d}{\omega_u^2 + \omega_d^2} + \frac{\omega_{u'} - \omega_{d'}}{\omega_{u'}^2 + \omega_{d'}^2} \right) \text{ with a statistical gain: } \frac{\langle \omega^2 \rangle}{\langle \omega \rangle^2}$$

# How to parameterize $\Sigma$ ?

- A function to build  $\Sigma_p = S/B$  is defined, and parameterized for every event:
  - $\Sigma_p$  is built (*iteratively*) over some kinematic variables and RICH response:
    - $(\Sigma_p)_{\text{initial}} = 1$
    - Mass spectra is divided in bins of each variable (*binning needed for statistical gain*)
    - Fit all  $D^0$  and  $D^*$  mass spectra inside each bin of each variable
    - $\Sigma_p$  is adjusted (*for every event inside each bin*) to  $(S/B)_{\text{fit}}$
  - After convergence, parameterization is checked:
    - No artificial peak produced in wrong charge mass spectra
  - Mass dependence  $\Rightarrow$  Included in  $\Sigma$  after convergence of  $\Sigma_p$
- $(\Sigma = \Sigma_p / (\Sigma_p + 1))$  in the weight  $\longrightarrow$  **probability for a given event to be background or Open-Charm**

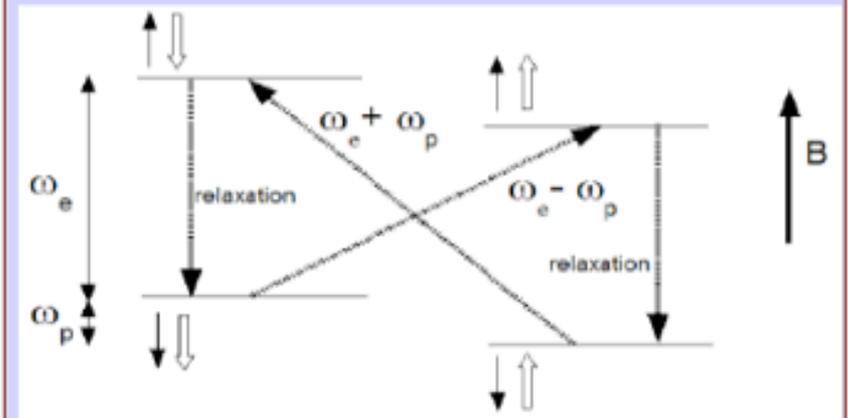
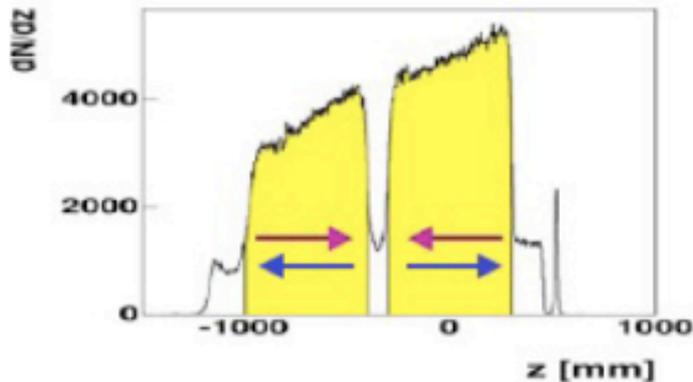
# Polarised target

- Target material:  ${}^6\text{LiD}$
- Solenoid field: 2.5 T
- Dilution factor:  $f \sim 0.4$
- Polarisation:  $P_T > 50\%$
- ${}^3\text{He}/{}^4\text{He}$ :  $T_{\min} \sim 50 \text{ mK}$



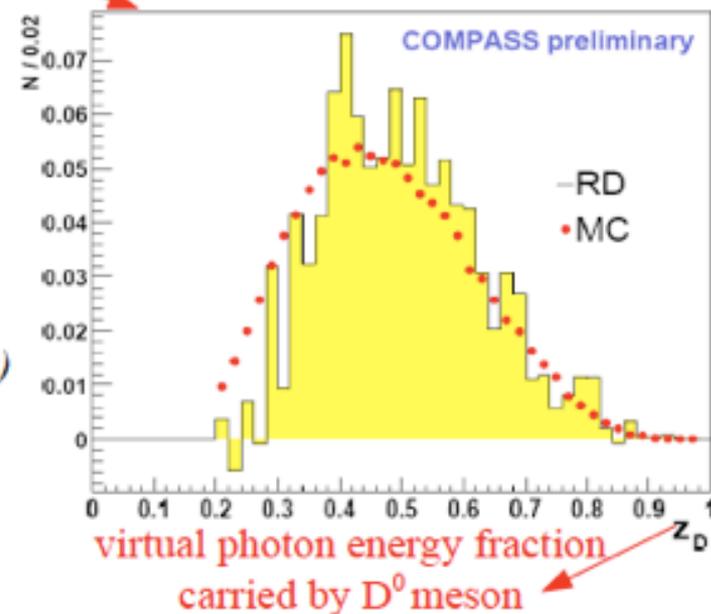
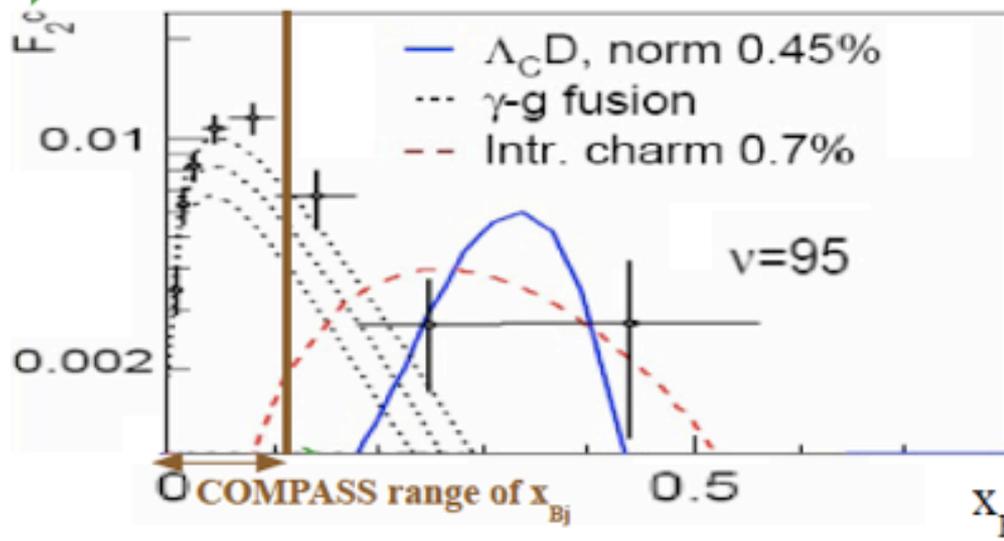
## Dynamic nuclear polarisation:

- High electron polarisation (high magnetic moment)
- Microwave irradiation of material, for simultaneous flip of electron and nucleon spin
- After spin flip, electron relaxates to lower energy state
- Nucleon has long relaxation time (low magnetic moment)



# Why measure gluon spin from Open-Charm?

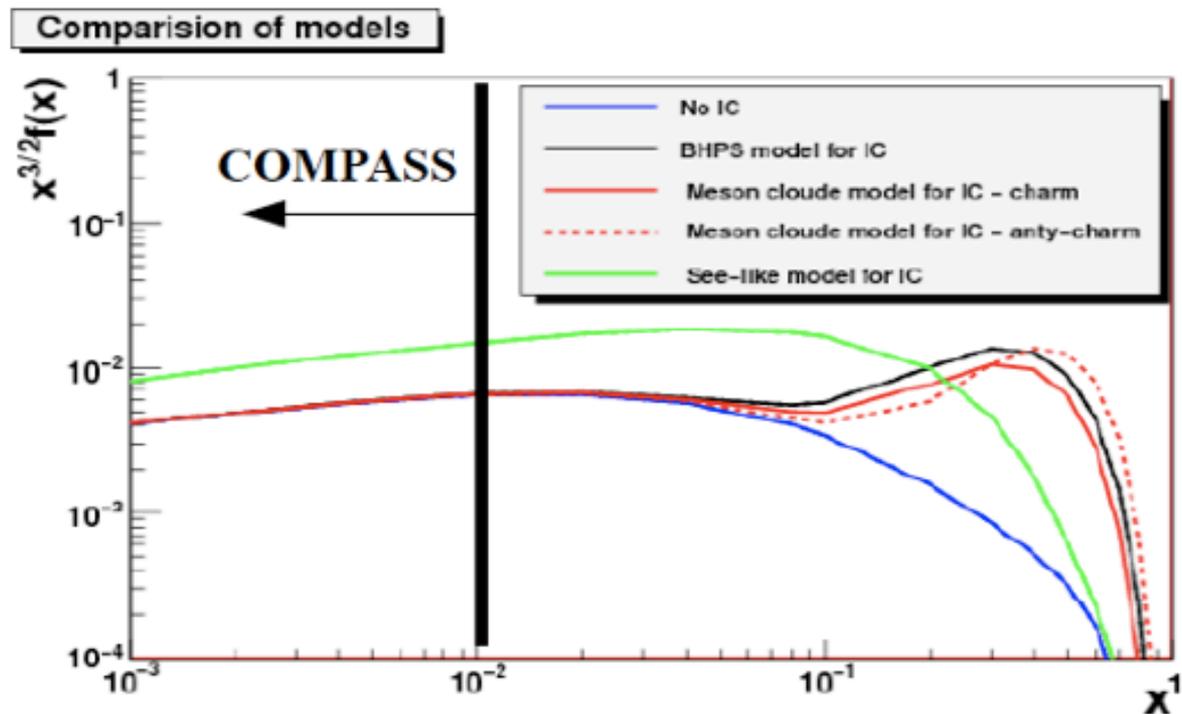
- $c\bar{c}$  production is dominated by the PGF process, and free from physical background (ideal for probing gluon polarisation)
  - In our center of mass energy, the contribution from intrinsic charm ( $c$  quarks not coming from hard gluons) in the nucleon is negligible
  - Perturbative scale set by charm mass  $4m_c^2$
  - Nonperturbative sea models predict at most 0.7% for intrinsic charm contribution
    - Expected at high  $x_{Bj}$  (compass  $x_{Bj} < 0.1$ )
  - $c\bar{c}$  suppressed during fragmentation (at our energies)



Ref. Hep-ph/0508126 and hep-ph/9508403  
 Phys. Lett. B93 (1980) 451  
 Data from EMC: Nucl. Phys. B213, 31 (1983)

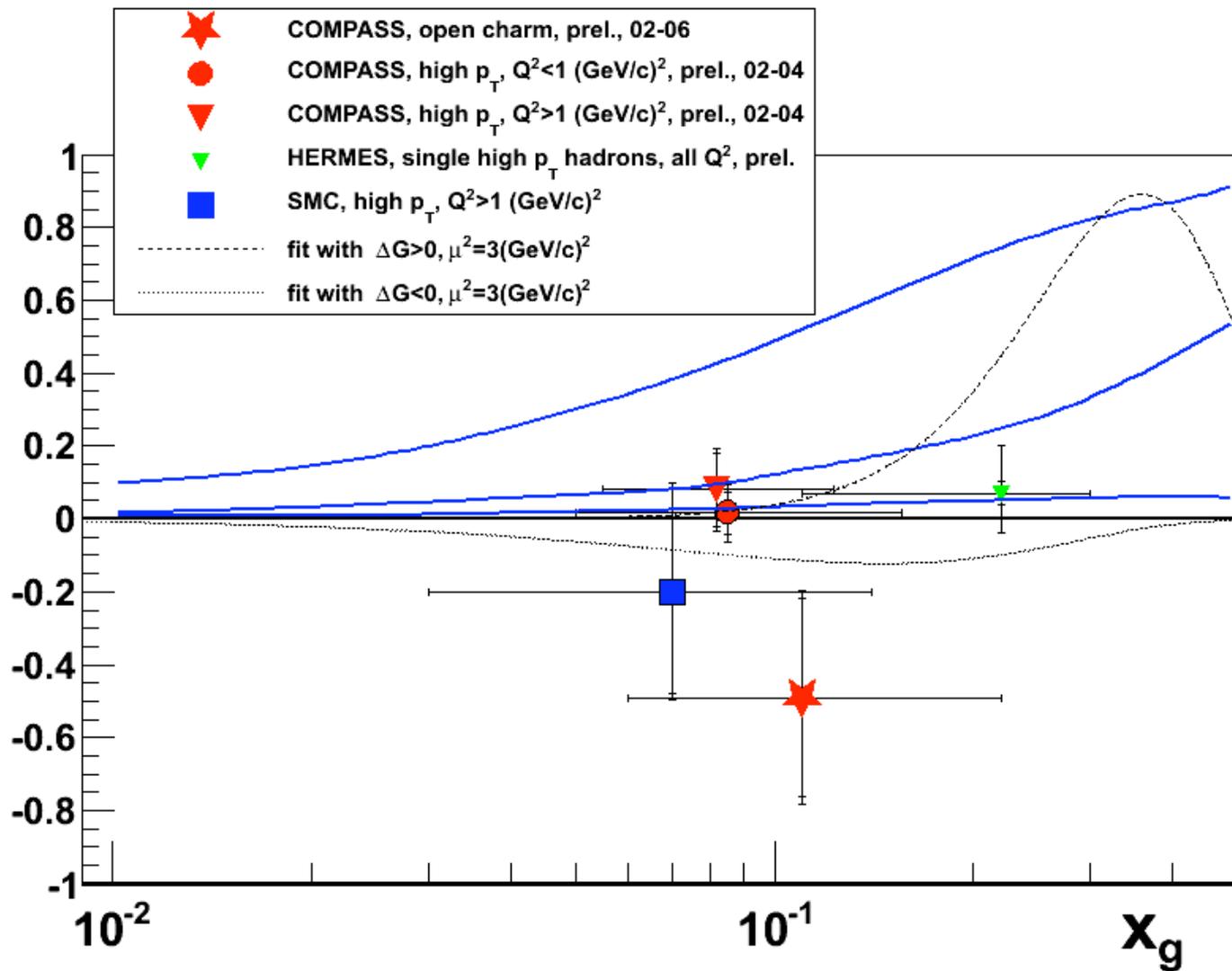
# Intrinsic charm predictions: CTEQ6.5c

- In the COMPASS kinematic domain:
  - No intrinsic charm contamination is predicted by the theory driven results
  - Only the more phenomenological “See-like” scenario should be taken into account (*under study*)



# GRSV, $\Delta G$

$\Delta g/g$



max, 2.5

std, 0.6

min, 0.2

# Method for $\Delta G/G$ and polarised $A_B$ extraction

- The number of events comes from asymmetries in the following way:

$$N_{u,d} = a \phi n (S+B) \left( 1 + P_T P_\mu f \left( a_{LL} \frac{S}{S+B} \frac{\Delta G}{G} + a_{LL}^B \frac{B}{S+B} A_B \right) \right)$$

$a$  = acceptance,  $\phi$  = muon flux,  $n$  = number of target nucleons

- We have 4 cell configurations (2 cells oppositely polarised + field reversal for acceptance normalization):

- Weight the 4  $N_{u,d}$  equations by  $\omega_s$  and by  $\omega_B = P_\mu f \cdot D(y) (B/S+B)$

$$\langle \sum_{k=1}^{N_{\text{cell}}} \omega_i^k \rangle = \hat{a}_{\text{cell},i} \left( 1 + (\langle \beta_{\text{cell},S} \rangle \omega_i) A_S + (\langle \beta_{\text{cell},B} \rangle \omega_i) A_B \right) = f_{\text{cell},i}$$

(cell = u, d, u', d')

( $\Delta G/G$ )

(i = S, B)

$$\hat{a} = a \phi n \sigma = a \phi n (\sigma_{\text{PGF}} + \sigma_B) = a \phi n (S+B)$$

$$\beta_S = P_B P_T f a_{LL} \frac{S}{S+B} \quad \beta_B = P_B P_T f D \frac{B}{S+B}$$

**8 eq. with 10 unknowns**

# How to solve equations for simultaneous $\Delta G/G$ and $A_B$ extraction?

- Possible acceptance changes with time are the same for both cells (*also the muon flux is the same for both cells*):

10  $\Rightarrow$  8 unknowns: 6  $\hat{a}$ ,  $A_S$  and  $A_B$   $\longrightarrow$

$$\frac{\hat{a}_{u,S} \hat{a}_{d',S}}{\hat{a}_{u',S} \hat{a}_{d,S}} = 1, \quad \frac{\hat{a}_{u,B} \hat{a}_{d',B}}{\hat{a}_{u',B} \hat{a}_{d,B}} = 1$$

- Signal and background events are affected in same way before and after a field reversal:

8  $\Rightarrow$  7 unknowns: 5  $\hat{a}$ ,  $A_S$  and  $A_B$   $\longrightarrow$

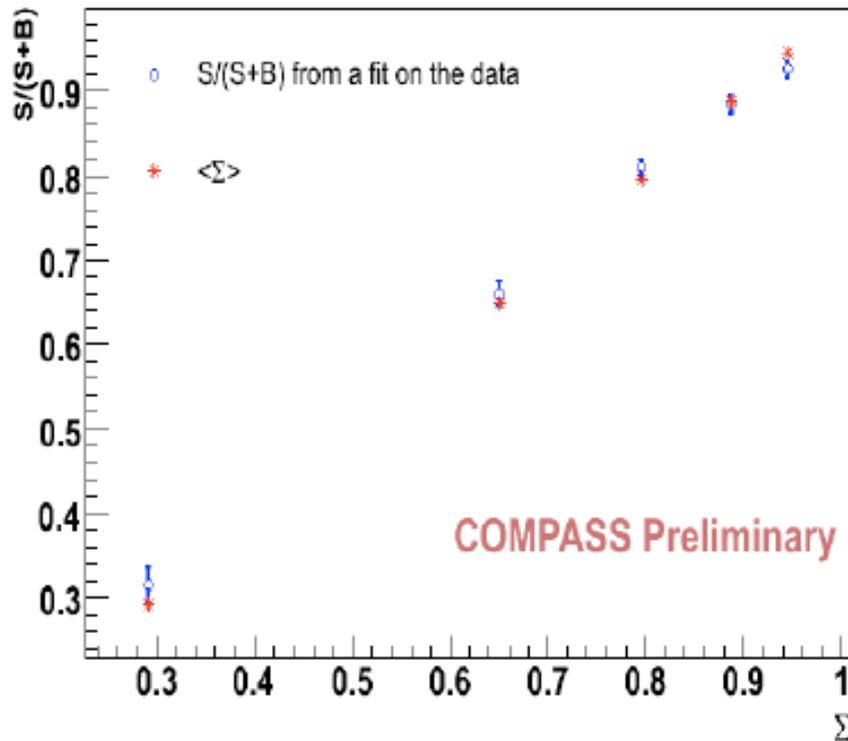
$$\frac{\hat{a}_{u,S}}{\hat{a}_{u,B}} = \frac{\hat{a}_{u',S}}{\hat{a}_{u',B}}, \quad \frac{\hat{a}_{d,S}}{\hat{a}_{d,B}} = \frac{\hat{a}_{d',S}}{\hat{a}_{d',B}}$$

- Unknowns are obtained by a  $\chi^2$  minimization:

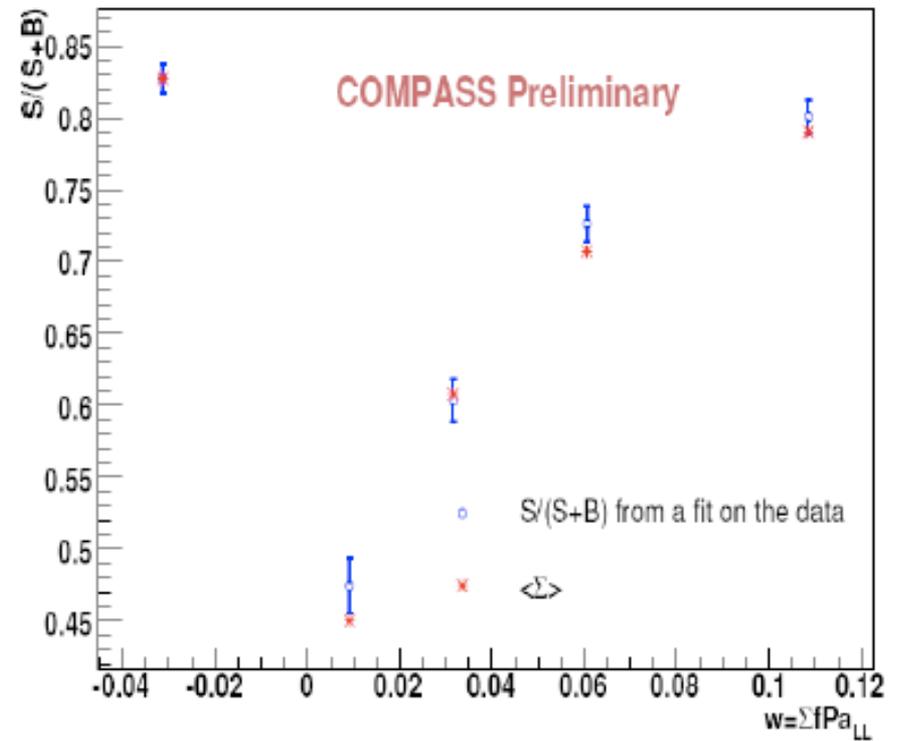
$$\chi^2 = (\vec{N} - \vec{f})^T \text{Cov}^{-1} (\vec{N} - \vec{f})$$

# Validation of parameterization (2006 example)

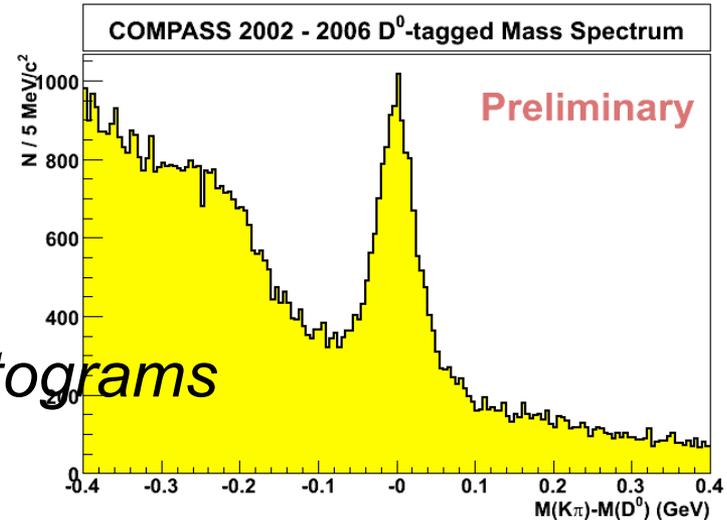
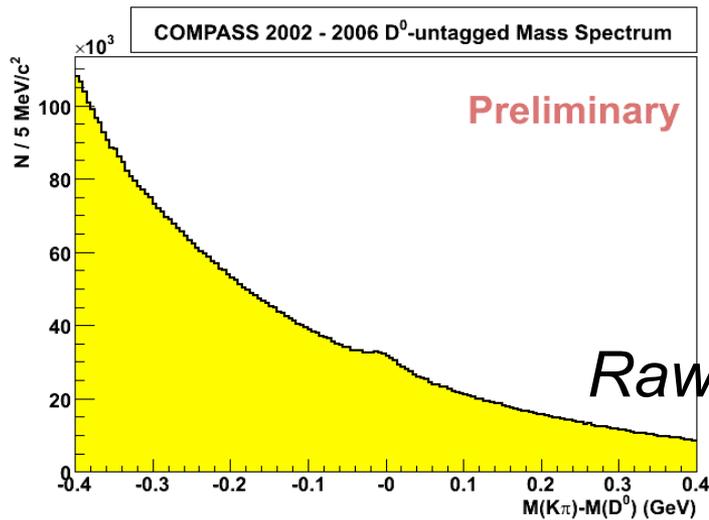
Data vs.  $\Sigma$ -Parameterization in  $\Sigma$  bins (2006  $D^0$ -tagged)



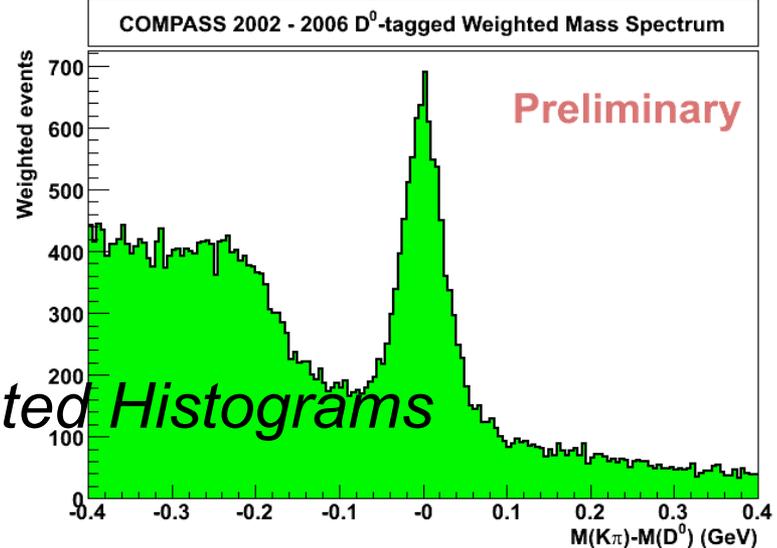
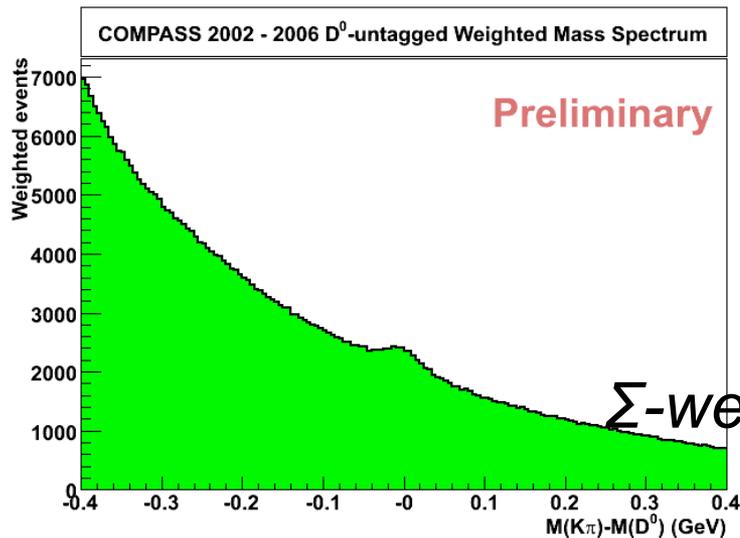
Data vs.  $\Sigma$ -Parameterization in weight bins (2006  $D^0$ -tagged)



# Invariant mass of $K\pi$ pairs - $S/(S+B)$ weighting



*Raw Histograms*



*$\Sigma$ -weighted Histograms*

$$A = \frac{\int \Delta G(x_g)(\Delta \hat{\sigma}^{LO} + \Delta \hat{\sigma}_{SV}^{NLO}) ds_1 dt_1 + \int \Delta G(x'_g) \Delta \hat{\sigma}_{hard}^{NLO} ds_4 ds_1 dt_1}{\int G(x_g)(\hat{\sigma}^{LO} + \hat{\sigma}_{SV}^{NLO}) ds_1 dt_1 + \int G(x'_g) \hat{\sigma}_{hard}^{NLO} ds_4 ds_1 dt_1}$$

$$\hat{\sigma}^{NLO}(t_1, s_1) = \hat{\sigma}^{LO} + \hat{\sigma}_{SV}^{NLO} + \int \hat{\sigma}_{hard}^{NLO} ds_4$$

$$\Delta \hat{\sigma}^{NLO}(t_1, s_1) = \Delta \hat{\sigma}^{LO} + \Delta \hat{\sigma}_{SV}^{NLO} + \int \Delta \hat{\sigma}_{hard}^{NLO} ds_4$$

$$A = \frac{\int \frac{\Delta G}{G} \frac{\Delta \hat{\sigma}^{NLO}(t_1, s_1)}{\hat{\sigma}^{NLO}(t_1, s_1)} G(x_g) \hat{\sigma}^{NLO}(t_1, s_1) dt_1 ds_1}{\int G(x_g) \hat{\sigma}^{NLO}(t_1, s_1) dt_1 ds_1}$$

$$A = \frac{\int \frac{\Delta G}{G} a_{LL}^{NLO} G(x_g) \hat{\sigma}^{NLO}(t_1, s_1) dt_1 ds_1}{\int G(x_g) \hat{\sigma}^{NLO}(t_1, s_1) dt_1 ds_1}$$

NLO - method 2  
event is defined  
by  $s_1$  and  $t_1(u_1)$   
 $s_1$  define  $x_g$

$$A = \frac{\int \Delta G(x_g) (\Delta \hat{\sigma}^{LO} + \Delta \hat{\sigma}_{SV}^{NLO}) du_1 dt_1 + \int \Delta G(x'_g) \Delta \hat{\sigma}_{hard}^{NLO} ds_4 du_1 dt_1}{\int G(x_g) (\hat{\sigma}^{LO} + \hat{\sigma}_{SV}^{NLO}) du_1 dt_1 + \int G(x'_g) \hat{\sigma}_{hard}^{NLO} ds_4 du_1 dt_1}$$

$$= \frac{\int \Delta G(x_g) \left[ \Delta \hat{\sigma}^{LO} + \Delta \hat{\sigma}_{SV}^{NLO} + \int \frac{\Delta G(x'_g)}{\Delta G(x_g)} \Delta \hat{\sigma}_{hard}^{NLO} ds_4 \right] du_1 dt_1}{\int G(x_g) \left[ \hat{\sigma}^{LO} + \hat{\sigma}_{SV}^{NLO} + \int \frac{G(x'_g)}{G(x_g)} \hat{\sigma}_{hard}^{NLO} ds_4 \right] du_1 dt_1}$$

$$\hat{\sigma}^{NLO}(t_1, u_1) = \hat{\sigma}^{LO} + \hat{\sigma}_{SV}^{NLO} + \int \frac{G(x'_g)}{G(x_g)} \hat{\sigma}_{hard}^{NLO} ds_4$$

$$\Delta \hat{\sigma}^{NLO}(t_1, u_1) = \Delta \hat{\sigma}^{LO} + \Delta \hat{\sigma}_{SV}^{NLO} + \int \frac{\Delta G(x'_g)}{\Delta G(x_g)} \Delta \hat{\sigma}_{hard}^{NLO} ds_4$$

$$A = \frac{\int \frac{\Delta G}{G} \frac{\Delta \hat{\sigma}^{NLO}(t_1, u_1)}{\hat{\sigma}^{NLO}(t_1, u_1)} G(x_g) \hat{\sigma}^{NLO}(t_1, u_1) du_1 dt_1}{\int G(x_g) \hat{\sigma}^{NLO}(t_1, u_1) du_1 dt_1}$$

$$A = \frac{\int \frac{\Delta G}{G} a_{LL}^{NLO} G(x_g) \hat{\sigma}^{NLO}(t_1, u_1) du_1 dt_1}{\int G(x_g) \hat{\sigma}^{NLO}(t_1, u_1) du_1 dt_1}$$

NLO - method 1  
event is defined  
by  $u_1$  and  $t_1$   
 $s_1^{el} = -u_1 - t_1$  define  $x_g$

$$2 \rightarrow 2 \quad \Rightarrow \quad g(k_1) + \gamma(k_2) \rightarrow c(p_1) + \bar{c}(p_2)$$

$$2 \rightarrow 3 \quad \Rightarrow \quad g(k_1) + \gamma(k_2) \rightarrow c(p_1) + \bar{c}(p_2) + g(k_3)$$

$$s_1 = (k_1 + k_2)^2 + Q^2 = 2k_1k_2$$

$$t_1 = (k_2 - p_2)^2 - m^2 = -2p_2k_2$$

$$u_1 = (k_1 - p_2)^2 - m^2 = -2p_2k_1$$

$$s_4 = (k_3 + p_1)^2 - m^2 = 2k_3p_1$$

$$x_g = \frac{s_1}{2Pq} = \frac{s_4 - t_1 - u_1}{2MEy}$$

$$2 \rightarrow 2 \quad \Rightarrow \quad s_1 + t_1 + u_1 = 0$$

$$2 \rightarrow 3 \quad \Rightarrow \quad s_1 + t_1 + u_1 = s_4$$

# Asymmetries in bins in $p_T$ and $E$ of $D^0$

**Table 2**  
The asymmetries  $A^{\gamma N \rightarrow D^0 X}$  in bins of  $p_T^{D^0}$  and  $E_{D^0}$  for the  $D^0$  and  $D^*$  sample combined, together with the averages of several kinematic variables. Only the statistical errors are given. The relative systematic uncertainty is 20% which is 100% correlated between the bins.

Bin limits		$A^{\gamma N \rightarrow D^0 X}$	$\langle y \rangle$	$\langle Q^2 \rangle$ (GeV/c) <sup>2</sup>	$\langle p_T^D \rangle$ (GeV/c)	$\langle E_D \rangle$ (GeV)	$D(\langle X \rangle)$	$\epsilon_{LL}(\langle X \rangle)$
$p_T^D$ (GeV/c)	$E_D$ (GeV)							
0–0.3	0–30	$-1.34 \pm 0.85$	0.47	0.50	0.19	24.8	0.57	0.37
0–0.3	30–50	$-0.27 \pm 0.52$	0.58	0.75	0.20	39.2	0.70	0.48
0–0.3	> 50	$-0.07 \pm 0.66$	0.67	1.06	0.20	60.0	0.80	0.61
0.3–0.7	0–30	$-0.85 \pm 0.51$	0.47	0.47	0.50	25.1	0.56	0.26
0.3–0.7	30–50	$0.09 \pm 0.29$	0.58	0.65	0.51	39.4	0.71	0.34
0.3–0.7	> 50	$-0.20 \pm 0.37$	0.67	0.68	0.50	59.6	0.80	0.46
0.7–1	0–30	$-0.47 \pm 0.56$	0.48	0.53	0.85	25.2	0.58	0.13
0.7–1	30–50	$-0.49 \pm 0.32$	0.58	0.66	0.85	39.1	0.70	0.17
0.7–1	> 50	$1.23 \pm 0.43$	0.68	0.73	0.84	59.4	0.81	0.26
1–1.5	0–30	$-0.87 \pm 0.48$	0.50	0.49	1.21	25.7	0.60	0.01
1–1.5	30–50	$-0.24 \pm 0.25$	0.60	0.62	1.22	39.5	0.73	0.00
1–1.5	> 50	$-0.18 \pm 0.34$	0.69	0.77	1.22	59.3	0.83	0.04
> 1.5	0–30	$0.83 \pm 0.71$	0.52	0.51	1.77	26.2	0.63	-0.13
> 1.5	30–50	$0.18 \pm 0.28$	0.61	0.68	1.87	40.0	0.74	-0.20
> 1.5	> 50	$0.44 \pm 0.33$	0.71	0.86	1.94	59.9	0.84	-0.24

weighted!

$$w = f P_B \frac{S}{S + B} D$$

published:

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