

# Transverse Spin Effects in Semi-Inclusive Deep Inelastic Scattering

**Anna Martin**

***Trieste University and INFN Trieste***



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Hadron Structure and Spectroscopy**

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# Content of the talk

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- **SIDIS Experiments with transversely polarised tgt**  
**HERMES and COMPASS**
- **Results on asymmetries**
  - **transversity Distribution Function**
  - **Sivers Distribution Function**
  - **Other TMD Distribution Functions**
- **Conclusions**

**mainly experimental results**

also,

**FANTASTIC PROGRESS IN THEORY, IN THE LAST FEW YEARS**

**→ *V. Barone, A. Efremov, A. Prokudin***



- **SIDIS Experiments with transversely polarised tgt  
HERMES and COMPASS**
- Results on asymmetries
  - transversity Distribution Function
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  - Other TMD Distribution Functions
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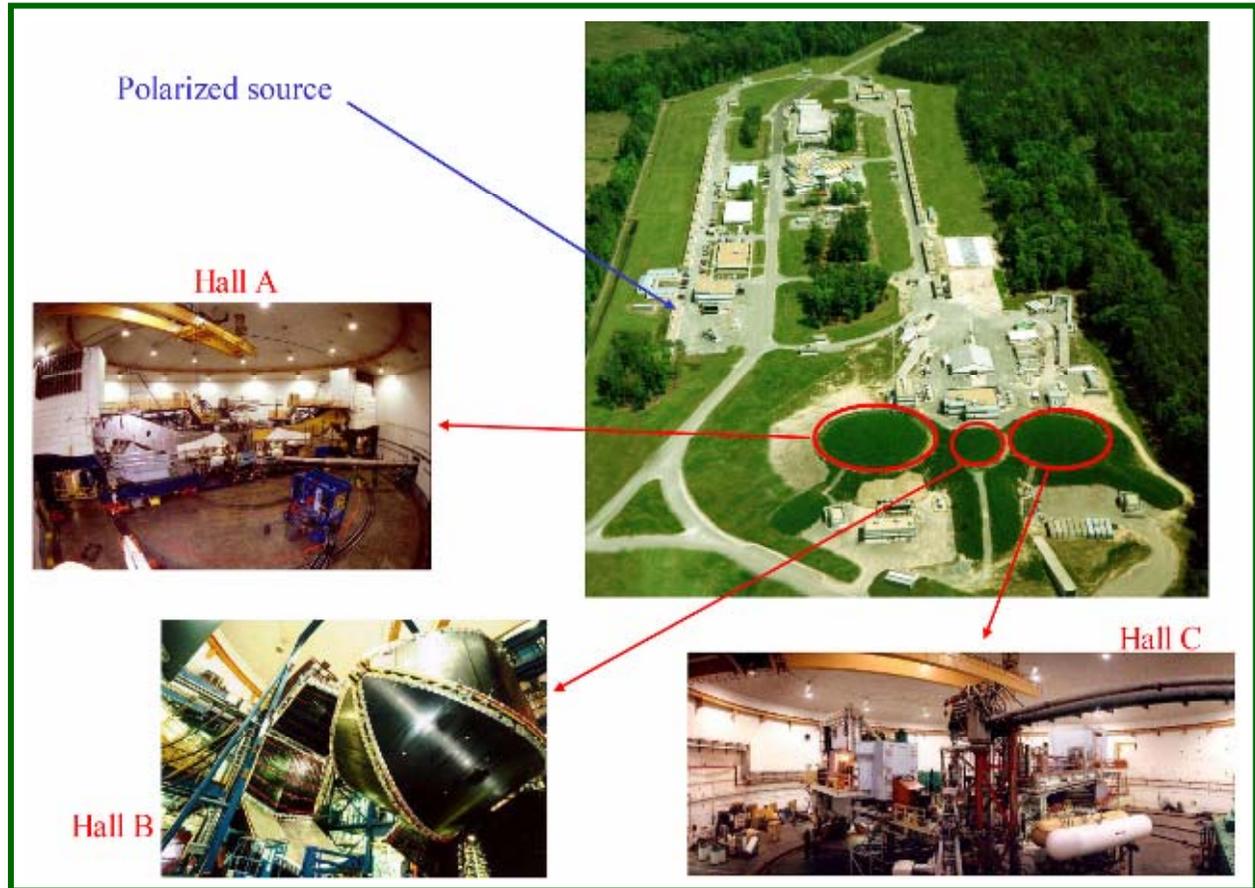
# SIDIS Experiments with transversely polarised targets

transverse spin effects are an important part of the program of the experiments

**HERMES at DESY**  
electron beam,  
energy 27.5 GeV

**COMPASS**  
at CERN  
long pol  $\mu$  beam,  
energy 160 GeV

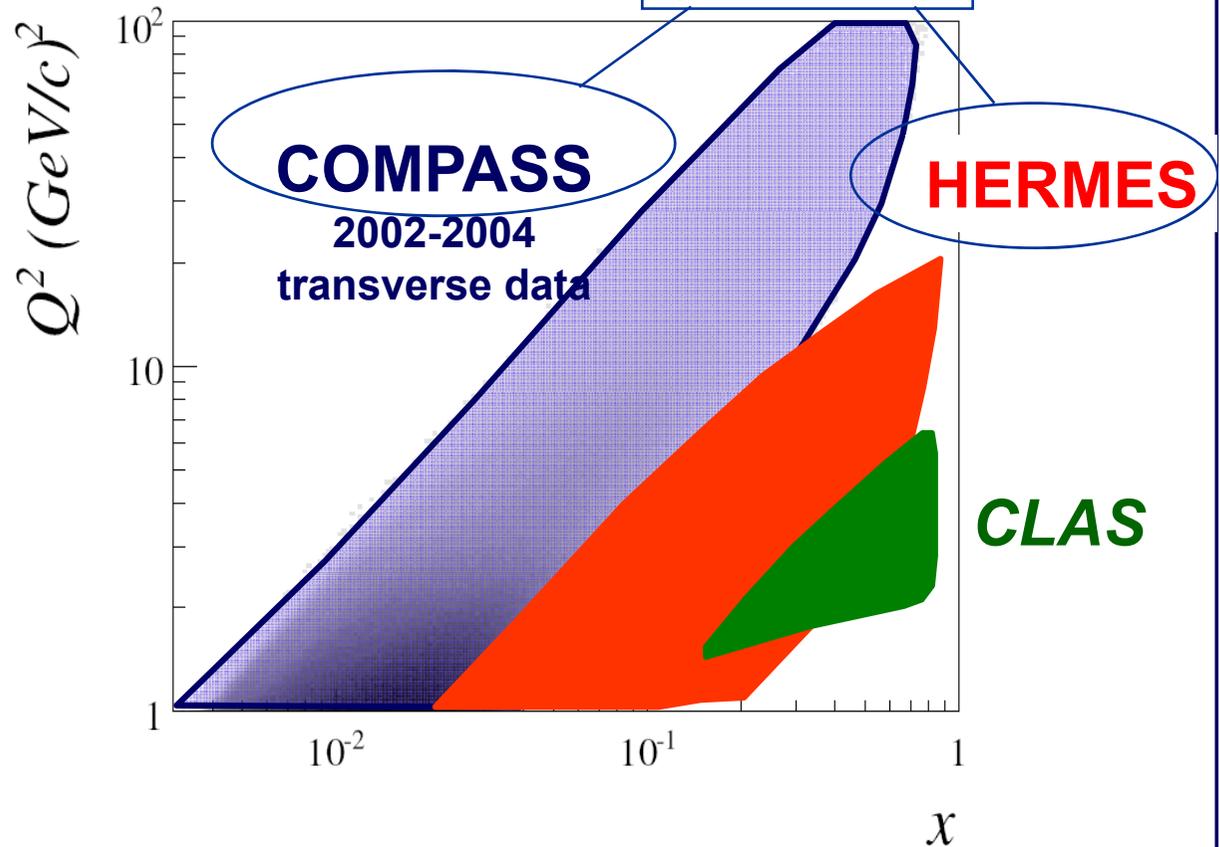
**JLAB experiments**  
electron beam,  
energy 6 GeV to be upgraded to 12 GeV  
(longitudinally polarised target, till now)





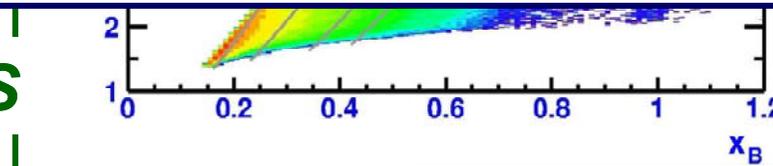
COMPASS 2002-03 data  $10^6$

given the different beam energies, the  $Q^2 - x$  range is different  
→ **complementary information**, needed to study energy dependence and to disentangle higher order effects



Anna Martin

CLAS

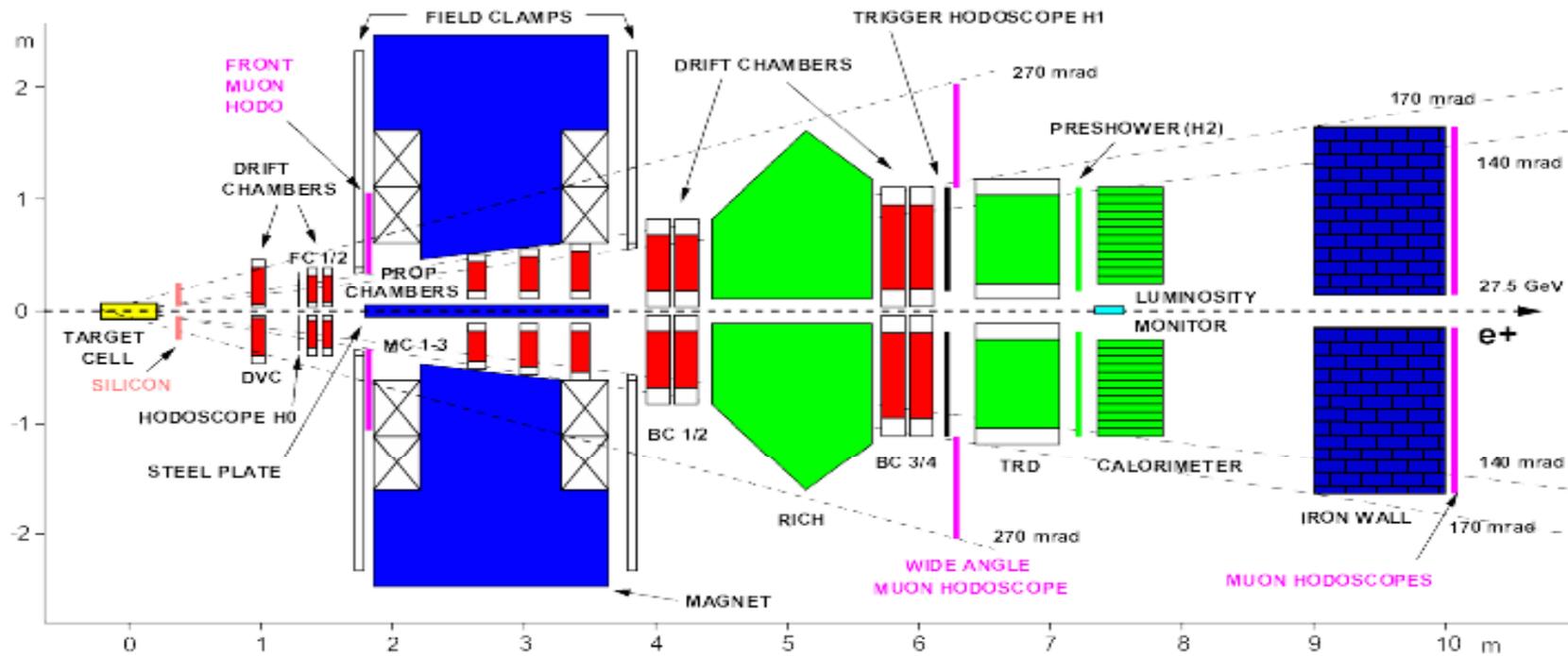


# HERMES



27.5 GeV e<sup>+</sup>

$$\sqrt{s} = 7 \text{ GeV}$$

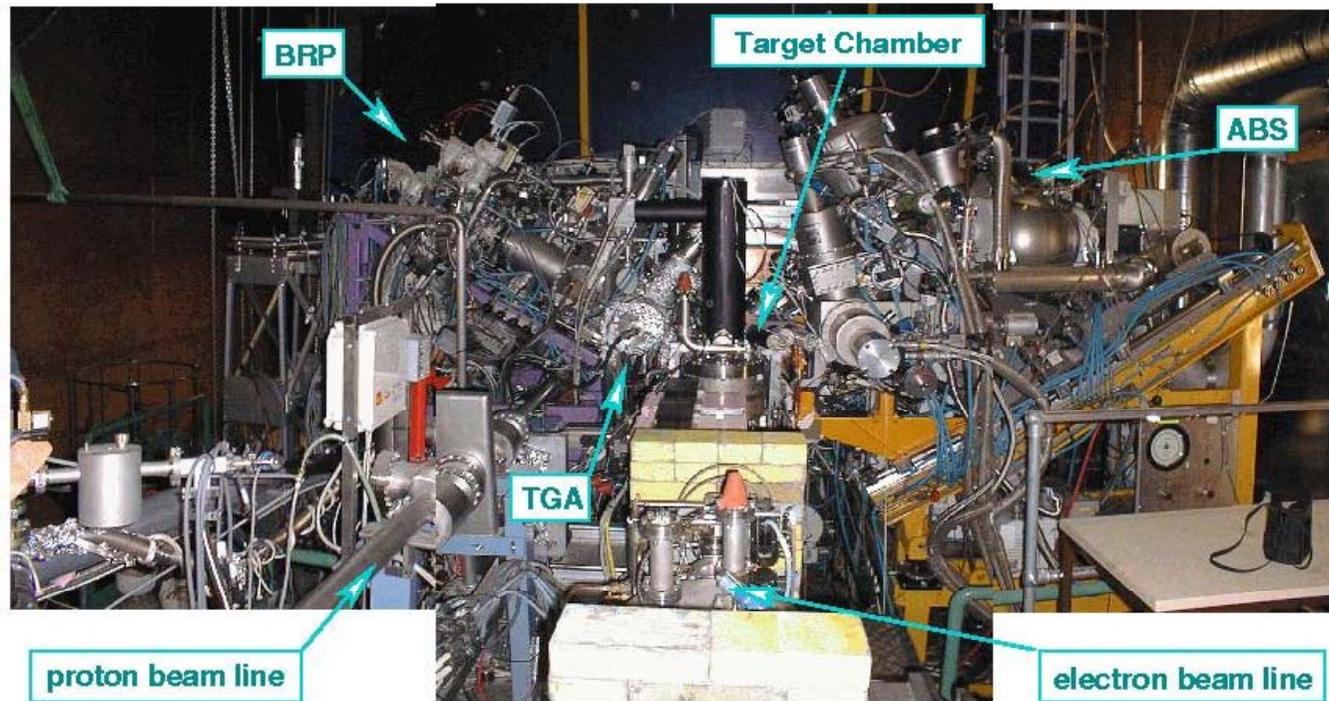


particle ID: lepton ID with  $\epsilon \sim 98\%$ ,  
 hadron contamination  $< 1\%$   
 RICH:  $\pi$ , K, p ID



# the HERMES polarised target

pure hydrogen gas target



flipped at high frequency (60- 90 s)

$${}^1\text{H} \rightarrow \langle |P_t| \rangle \sim 85 \pm 3.8 \%$$

$${}^2\text{H} \rightarrow \langle |P_t| \rangle \sim 84 \pm 3.5 \%$$

$${}^1\text{H} \uparrow \langle |P_t| \rangle \sim 74 \pm 4.2 \%$$



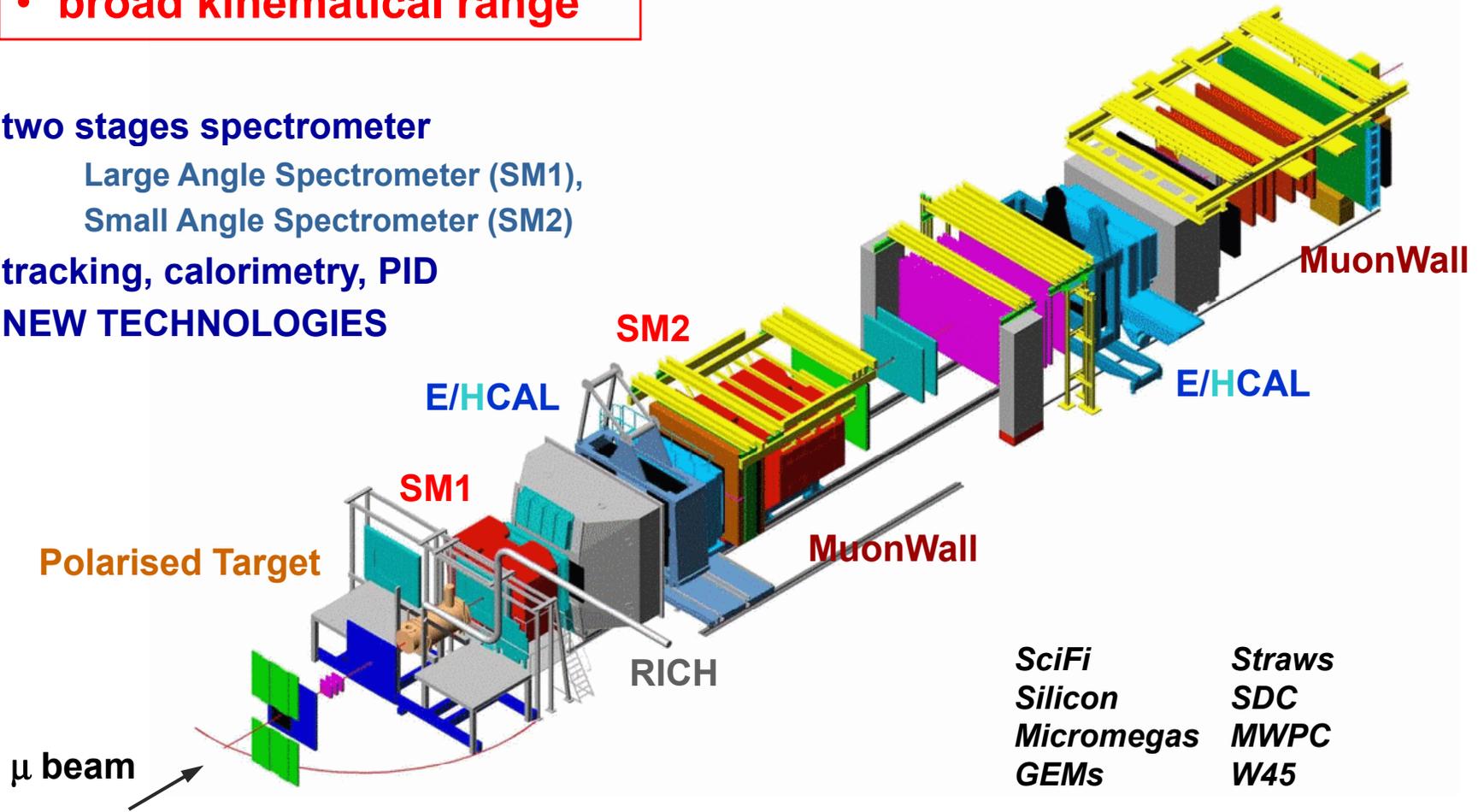
# COMPASS



- high energy beam
- large angular acceptance
- broad kinematical range

beam: 160 GeV/c  
 longitudinal polarisation -76%  
 intensity  $2 \cdot 10^8 \mu^+/\text{spill}$  (4.8s/16.2s)

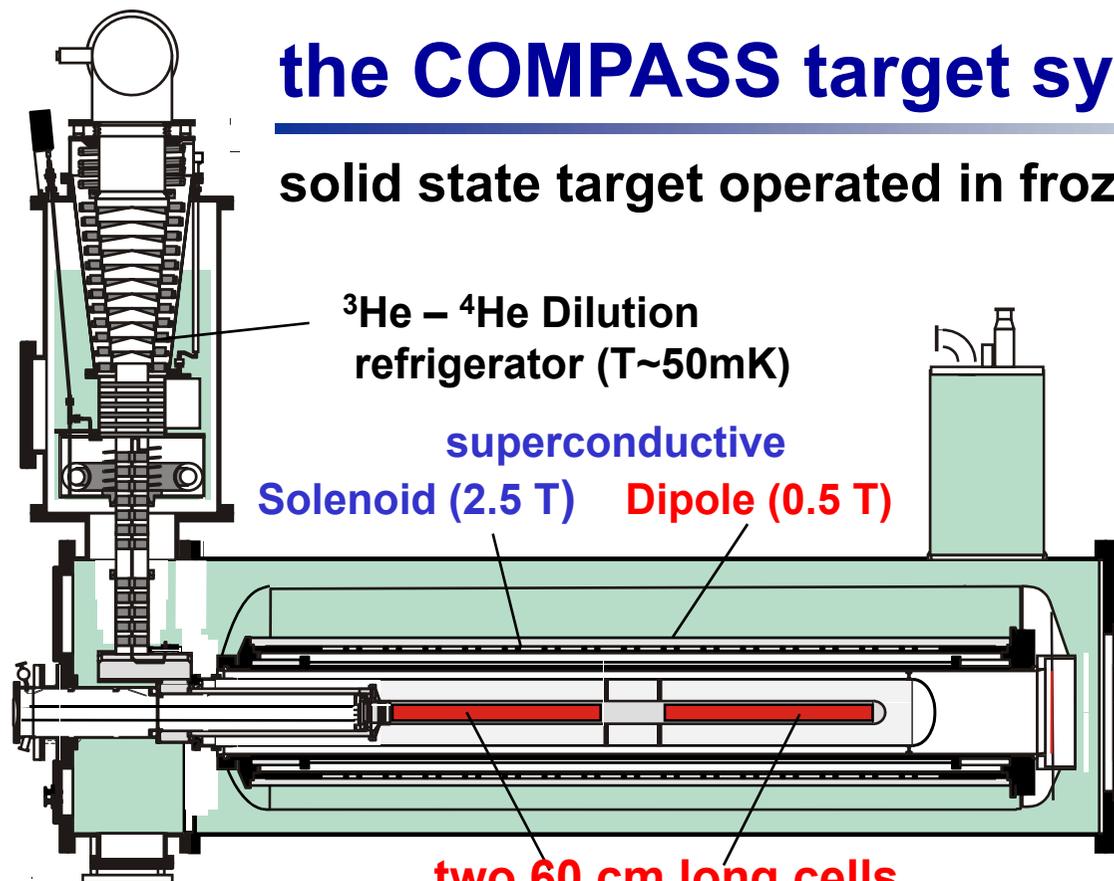
two stages spectrometer  
 Large Angle Spectrometer (SM1),  
 Small Angle Spectrometer (SM2)  
 tracking, calorimetry, PID  
 NEW TECHNOLOGIES



# the COMPASS target system (2002-2004)



solid state target operated in frozen spin mode

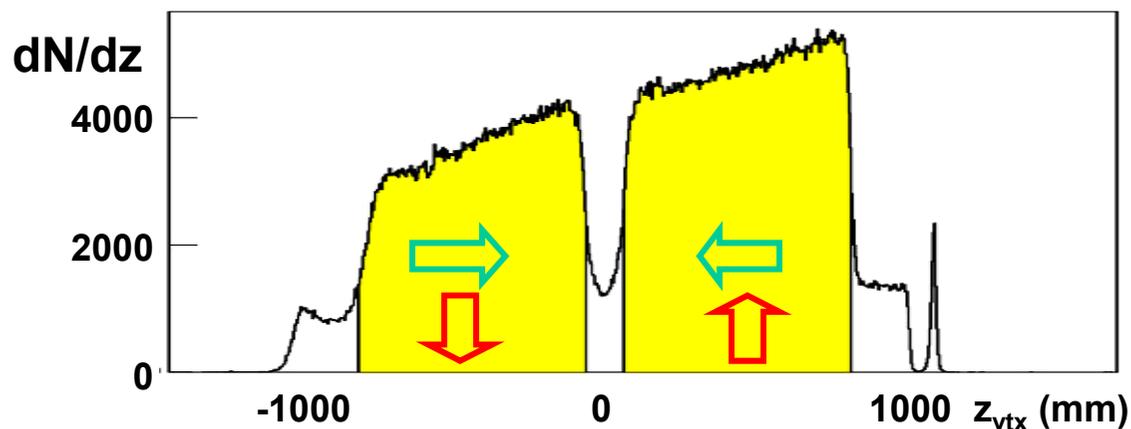


$^3\text{He} - ^4\text{He}$  Dilution refrigerator ( $T \sim 50\text{mK}$ )

superconductive Solenoid (2.5 T) Dipole (0.5 T)

two 60 cm long cells with opposite polarisation (systematics)

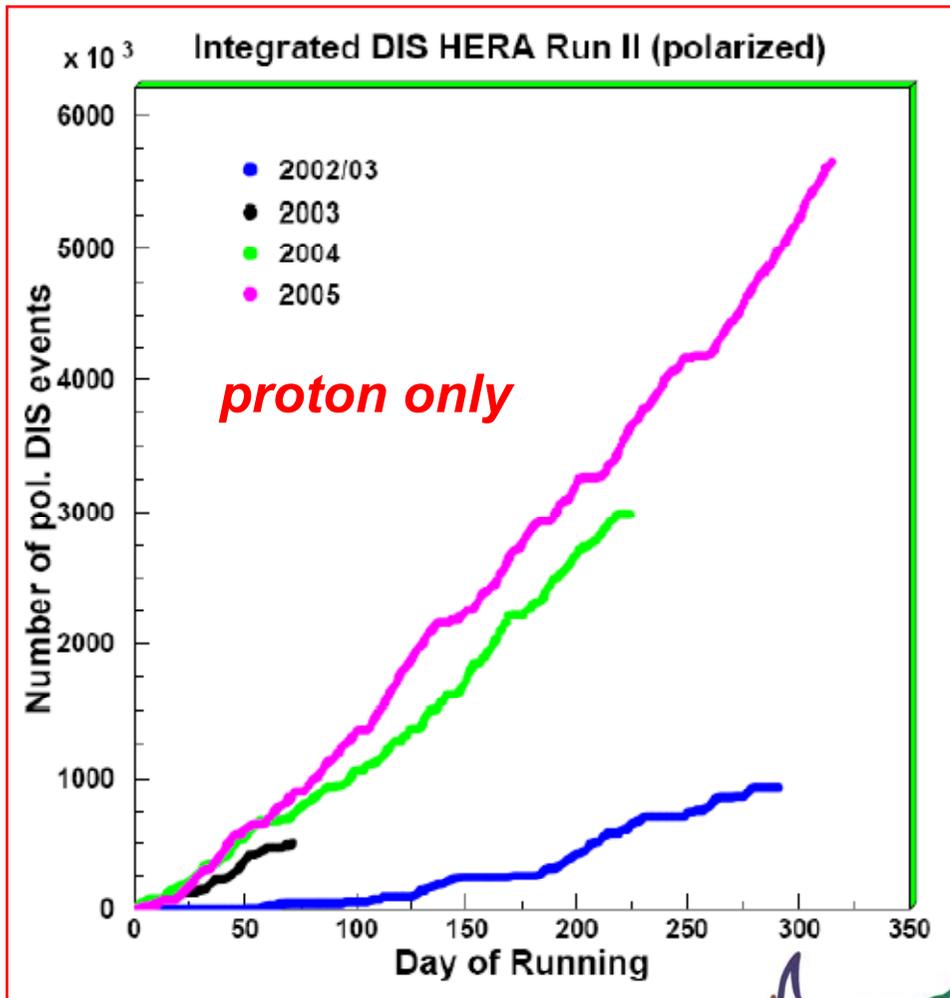
**2002-2004:  $^6\text{LiD}$**   
dilution factor  $f = 0.38$   
polarization  $P_T = 50\%$   
 **$\sim 20\%$  of the time transversely polarised**



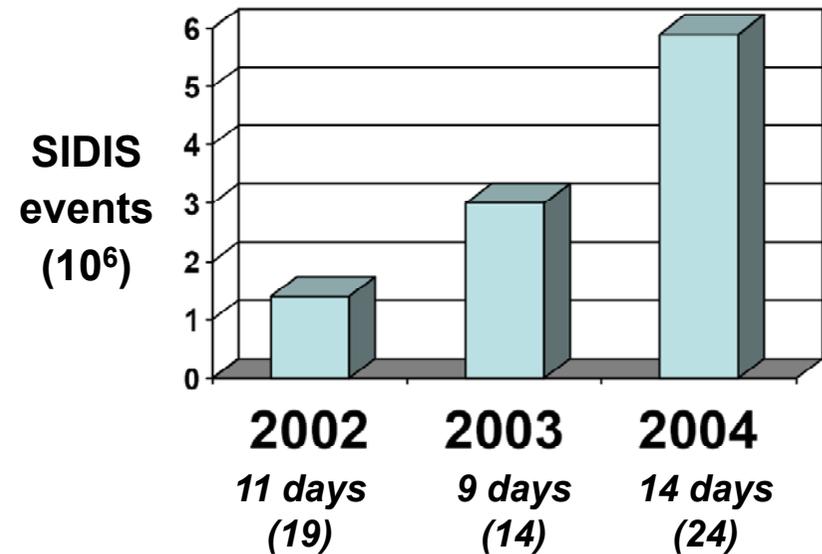
during data taking with transverse polarization

- dipole field always  $\uparrow$
- polarization reversal in the 2 cells after  $\sim 5$  days

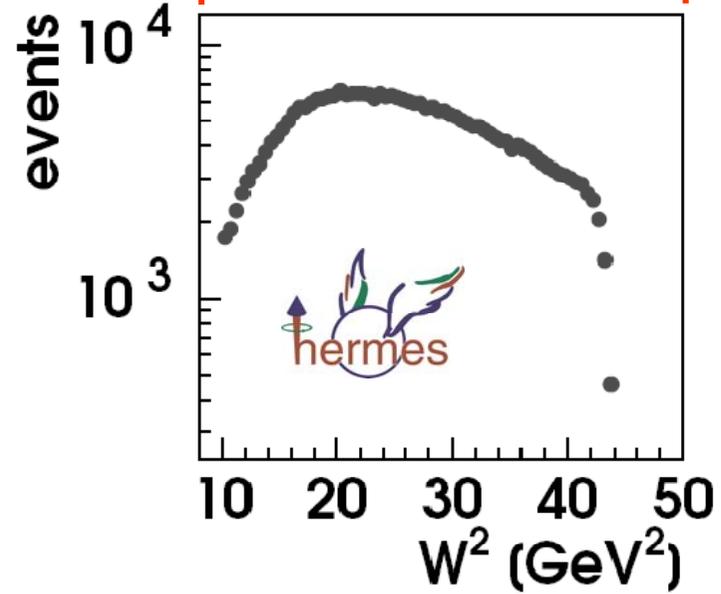
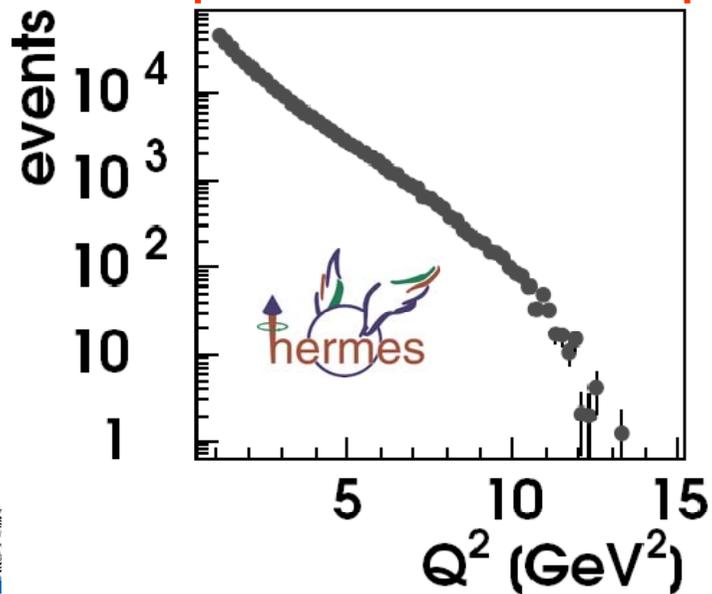
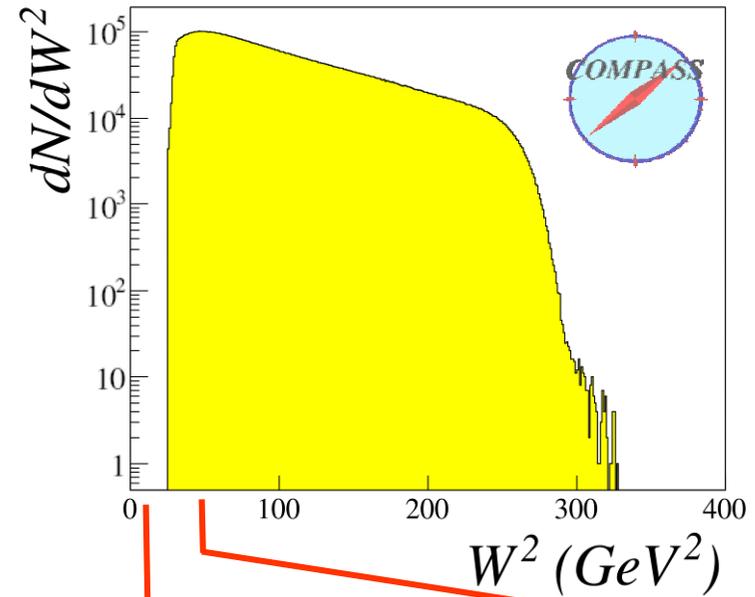
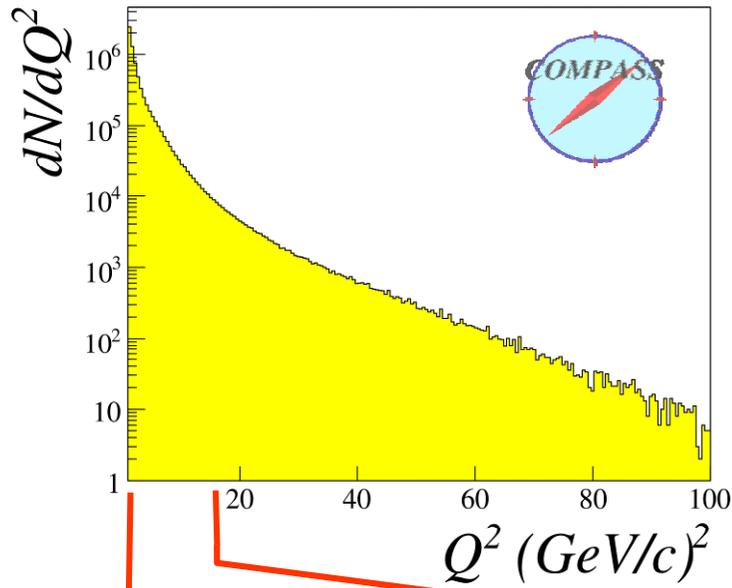
# data taking with transversely polarised target



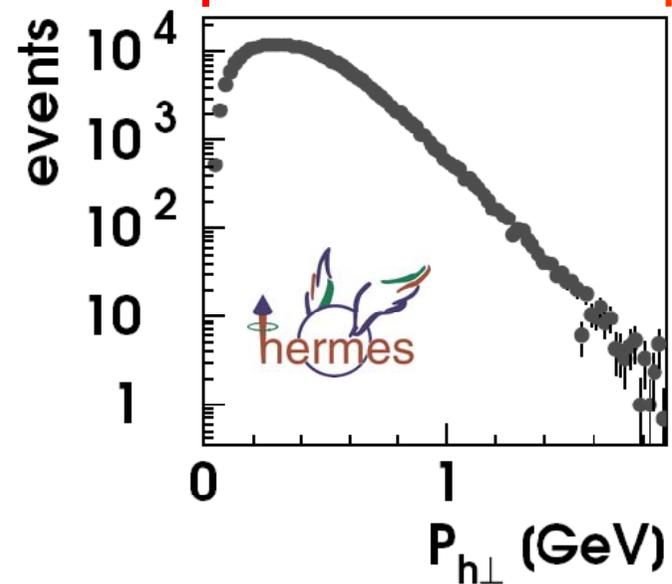
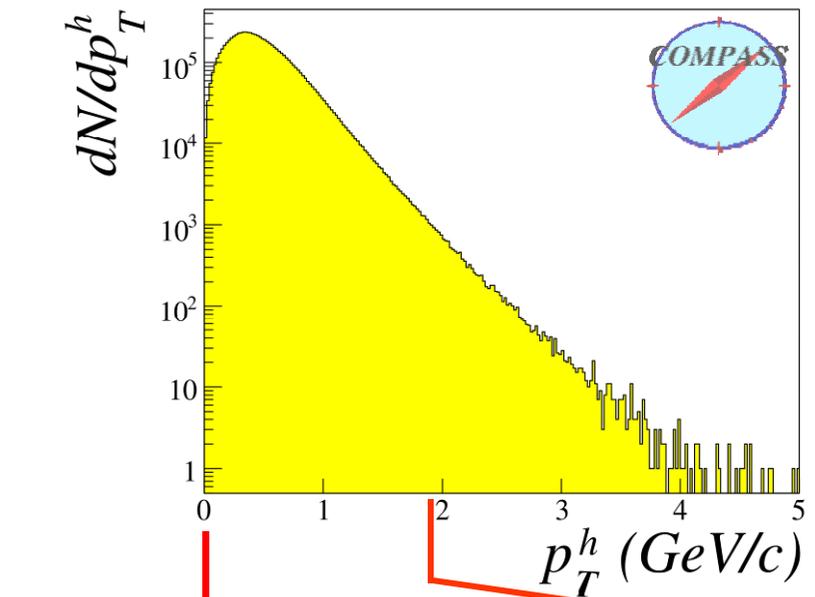
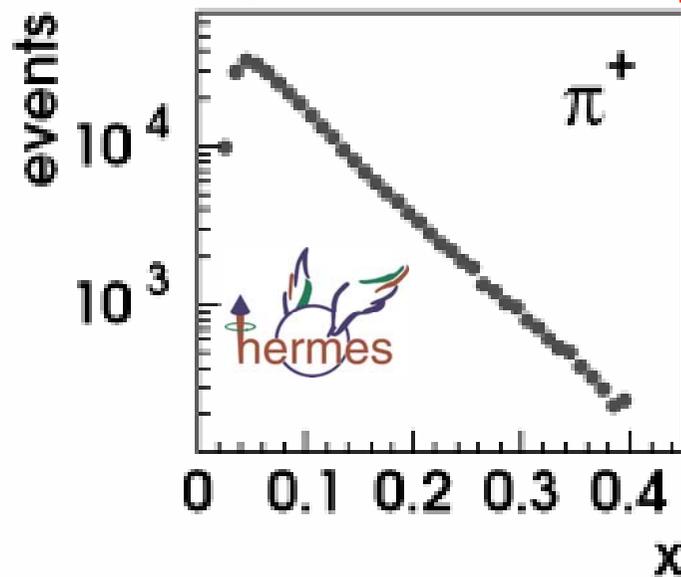
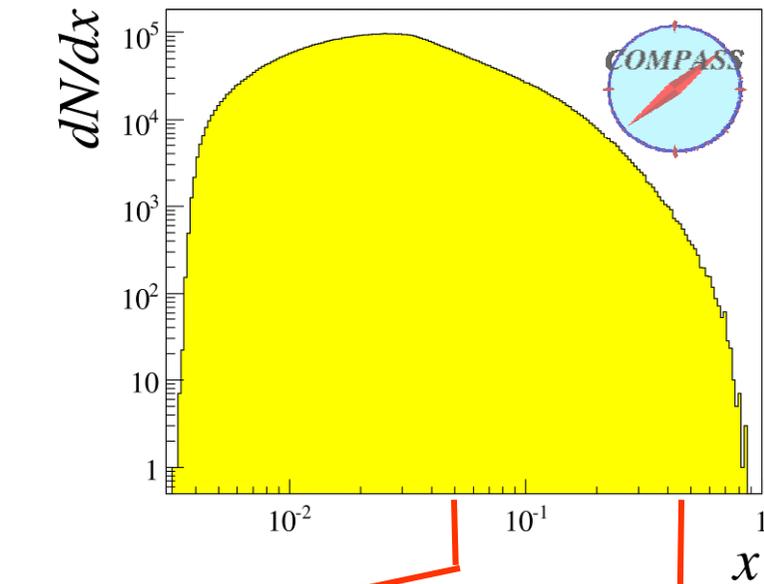
## 2002-2004: $^6\text{LiD}$ only



# SIDIS kinematics



# SIDIS kinematics



- SIDIS Experiments with transversely polarised tgt  
HERMES and COMPASS
- Results on asymmetries
  - **transversity Distribution Function**
  - Sivers Distribution Function
  - Other TMD Distribution Functions
- Conclusions



# Transversity distribution function

reminder:

1993: first proposals to measure the transversity DFs:

the RHIC-Spin Collaboration, BNL	Drell-Yan
the HELP Collaboration, CERN	SIDIS

today: SIDIS

transversity (and transverse spin effects) is being studied at  
HERMES and COMPASS

proposals to measure it at JLAB (12 GeV)

Drell-Yan: measurements planned at RHIC

*Oleg Denissov* being planned at COMPASS  
proposed at GSI

*Christine Aidala*

complementary  
to SIDIS

flavour separation:  
unique feature in SIDIS



# Transversity Distribution Function

three quark distribution functions (DF) are necessary to describe the structure of the nucleon at LO

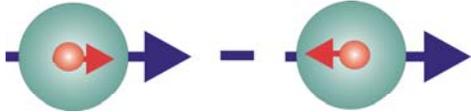
$q(x)$   
 $f_1^q(x)$



**unpolarised DF**

quark with momentum  $xP$  in a nucleon  
*well known – unpolarised DIS*

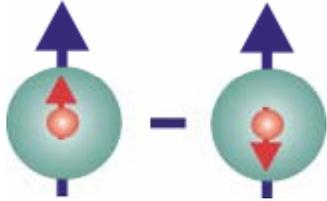
$\Delta q(x)$   
 $g_1^q(x)$



**helicity DF**

quark with spin parallel to the nucleon  
 spin in a longitudinally polarised nucleon  
*known – polarised DIS*

$\Delta_T q(x) = q^{\uparrow\uparrow}(x) - q^{\uparrow\downarrow}(x)$   
 $h_1^q(x),$   
 $\delta q(x),$   
 $\delta_T q(x)$



**transversity DF**

quark with spin parallel to the nucleon spin in a transversely polarised nucleon

*largely unknown*

**ALL 3 OF EQUAL IMPORTANCE**



# Transversity Distribution Function

$$\Delta_T \mathbf{q}(\mathbf{x}), h_1^q(x), \delta q(x), \delta_T q(x), \quad q=u_v, d_v, q_{\text{sea}}$$

properties:

- probes the relativistic nature of **quark dynamics**
- **no contribution from the gluons** → simple  $Q^2$  evolution

- **positivity (Soffer) bound**

$$2 |\Delta_T \mathbf{q}| \leq q + \Delta q$$

- first moments: **tensor charge**

$$\Delta_T \mathbf{q} \equiv \int dx \Delta_T \mathbf{q}(x)$$

- **sum rule** for transverse spin in Parton Model framework

$$\frac{1}{2} = \frac{1}{2} \sum \Delta_T \mathbf{q} + L_q + L_g$$

*Bakker, Leader, Trueman, PRD 70 (04)*

- it is related to **GPD's**

- is **chiral-odd**: decouples from inclusive DIS



# Transversity DF: how to measure it

the Transversity DF is **chiral-odd**:

observable effects are given only by the product of  $\Delta_T q(x)$  and another **chiral-odd function**

can be measured in SIDIS on a transversely polarised target via “quark polarimetry”

$I N^\uparrow \rightarrow I' h X$  “Collins” asymmetry

“Collins” Fragmentation Function

$I N^\uparrow \rightarrow I' h h X$  two-hadron asymmetry

“Interference” Fragmentation Function

$I N^\uparrow \rightarrow I' \Lambda X$   $\Lambda$  polarisation

Fragmentation Function of  $q^\uparrow \rightarrow \Lambda$

.....



# Measurement of the Transversity DF in SIDIS

“Collins asymmetry” in  $l N^\uparrow \rightarrow l' h^\pm X$

the “quark polarimetry” relies on the Collins effect

a quark moving “horizontally” and polarized “upwards” would emit the leading meson preferentially on the “left” side of the jet

→ the fragmentation function of a transversely polarised quark has a **spin dependent part**

$$D_q^h(z, \vec{p}_T^h) = D_q^h(z, p_T^h) + \underbrace{\Delta_T^0 D_q^h(z, p_T^h)}_{\text{“Collins” FF: } H_1^{\perp q}, \delta \hat{q}^h, \dots} \cdot \sin(\varphi_h - \varphi_s)$$



# Collins effect in SIDIS

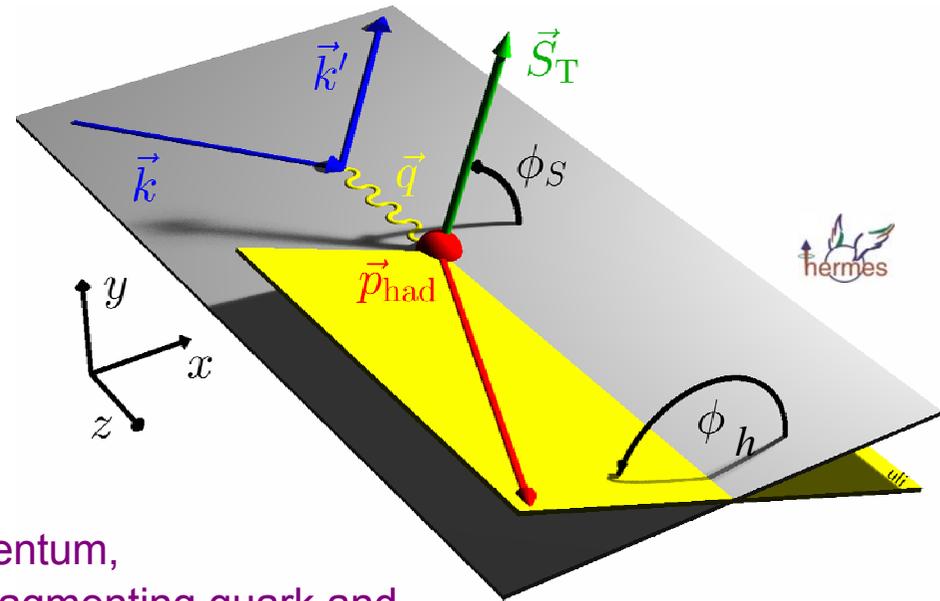
the “Collins angle” is



$$\begin{aligned}\Phi_C &= \phi_h - \phi_{s'} \\ &= \phi_h + \phi_S - \pi\end{aligned}$$



$$\Phi_C = \phi_h + \phi_S \quad (\text{Trento})$$



$\phi_{h,s',S}$  azimuthal angles of the hadron momentum,  
of the spin of the fragmenting quark and  
of the nucleon

**distribution of the hadrons:** 
$$\mathbf{N}_h^\pm(\Phi_C) = \mathbf{N}_h^0 \cdot \left[ \mathbf{1} \pm \mathbf{P}_T \cdot \mathbf{D}_{NN} \cdot \mathbf{A}_{\text{Coll}} \cdot \sin\Phi_C \right]$$

$\pm$  refer to the opposite orientation of the transverse spin of the nucleon

$\mathbf{P}_T$  ( $\mathbf{f} \cdot \mathbf{P}_T$ ) is the target polarisation;

$\mathbf{D}_{NN}$  is the transverse spin transfer coefficient initial  $\rightarrow$  struck quark



# Collins effect in SIDIS

distribution of the hadrons:  $N_h^\pm(\Phi_C) = N_h^0 \cdot [1 \pm \mathbf{P}_T \cdot \mathbf{D}_{NN} \cdot \mathbf{A}_{Coll} \cdot \sin\Phi_C]$

in each angular bin one measures the quantities



$$A_{UT}^{\pi^\pm}(\phi, \phi_S) = \frac{1}{\langle P_z \rangle} \cdot \frac{N_{\pi^\pm}^{\uparrow}(\phi, \phi_S) - N_{\pi^\pm}^{\downarrow}(\phi, \phi_S)}{N_{\pi^\pm}^{\uparrow}(\phi, \phi_S) + N_{\pi^\pm}^{\downarrow}(\phi, \phi_S)}$$



$$A_j(\phi_h, \phi_S) = \frac{N_{j,u}^+(\phi_h, \phi_S)}{N_{j,u}^-(\phi_h, \phi_S)} \cdot \frac{N_{j,d}^+(\phi_h, \phi_S)}{N_{j,d}^-(\phi_h, \phi_S)}$$

2 cells oppositely polarised:

- reduces acceptance variation effects
- at first order, spin independent effects cancel out

and fitting them the  
“Collins Asymmetry”  
is extracted

$$A_{Coll} \propto \frac{\sum_q e_q^2 \cdot \Delta_T \mathbf{q} \cdot \Delta_T^0 \mathbf{D}_q^h}{\sum_q e_q^2 \cdot \mathbf{q} \cdot \mathbf{D}_q^h}$$



# Collins Fragmentation Function

measurable in  $e^+e^-$  annihilation

- first attempts to measured it from the correlation between the azimuthal angles of  $\pi$ 's from  $e^+e^-$  annihilation using LEP data

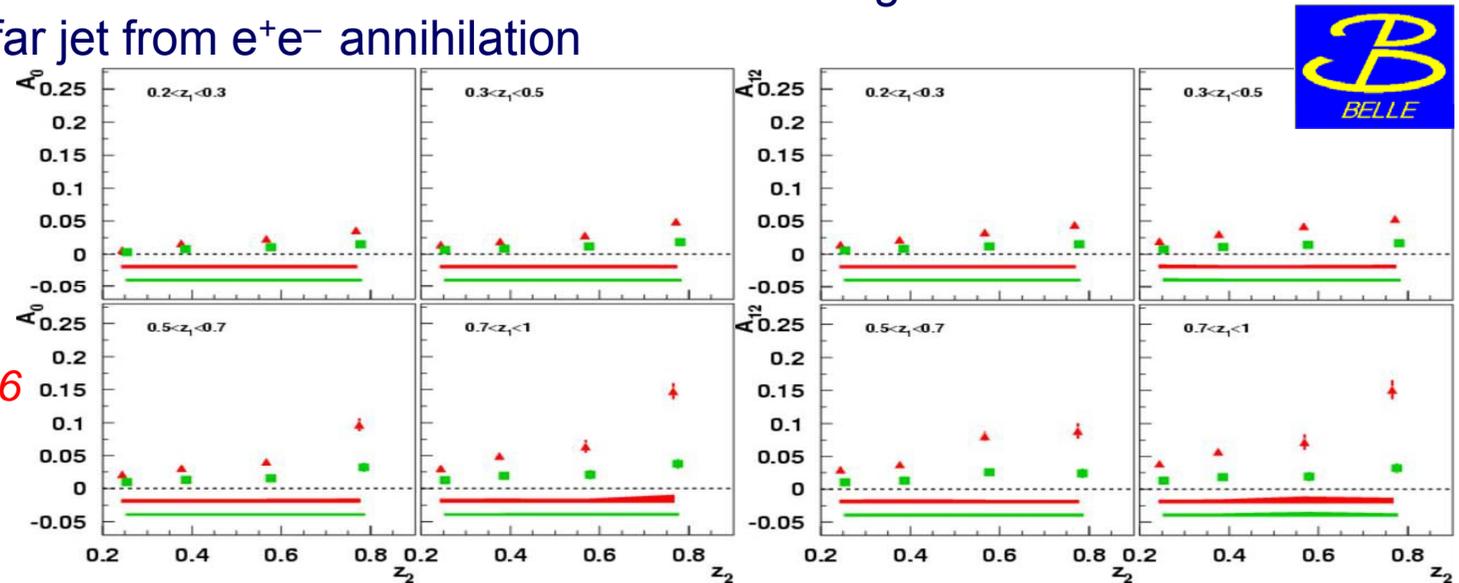
last year: great news from BELLE

the Collins FF is being measured in  $e^+e^-$  annihilation, and it is different from zero!

measurement of the correlation between the azimuthal angles of  $\pi$ 's in the near jet and in the far jet from  $e^+e^-$  annihilation

- 547  $\text{fb}^{-1}$  charm corrected data sample,
  - UL and UC double ratios
- R. Seidl, *SPIN2006*

Matthias GP

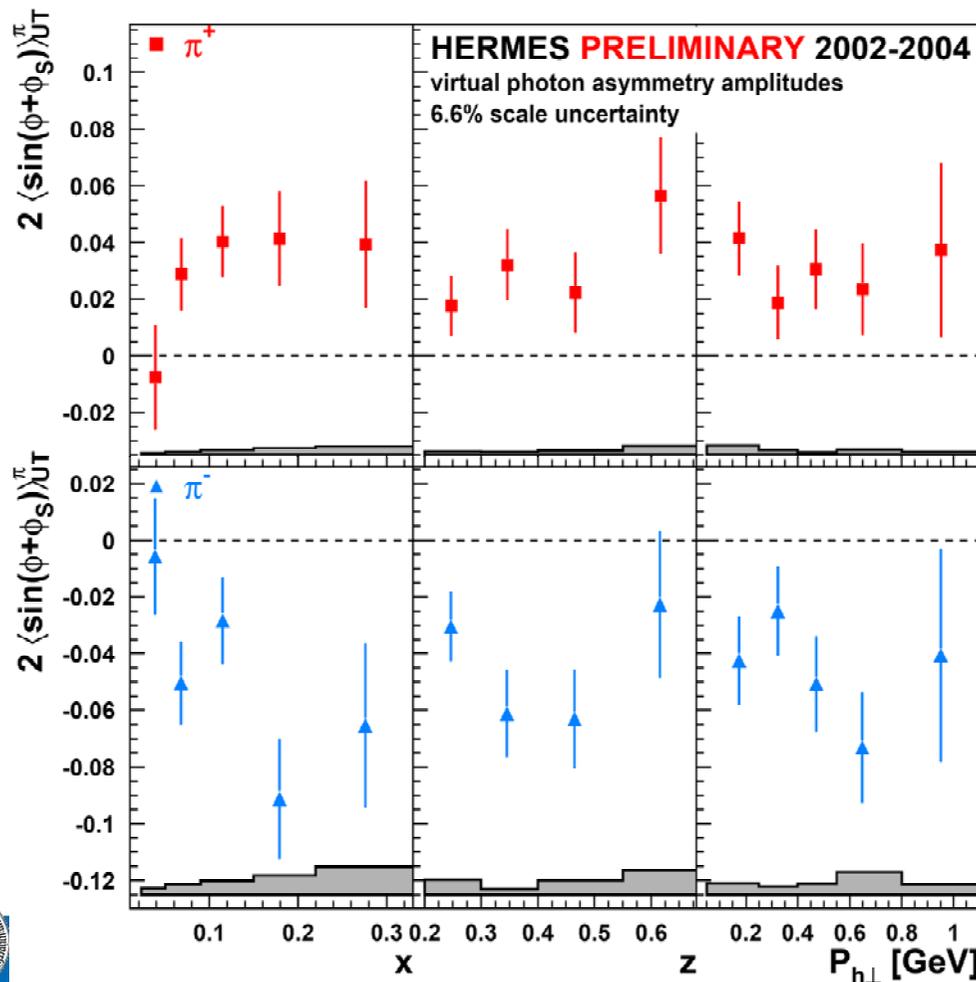


# Collins asymmetry



transversely polarised **proton target** - **charged pions**

- *first attempt with longitudinally polarised target*
- **2004: results from 2002-2003 data** PRL94 (2005) 012002 confirmed by
- **2005: results from 2002-2004 data**



**a very clear signal:  
transversity is  $\neq 0$ ,  
the Collins FF is  $\neq 0$**

**positive  $\pi^+$   
and  
negative  $\pi^-$  (unexpected large)  
asymmetries**



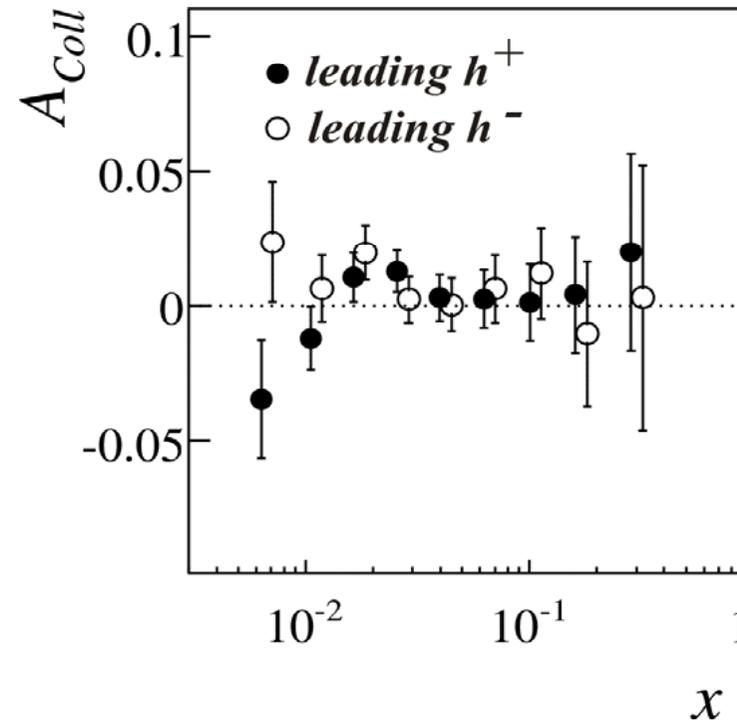
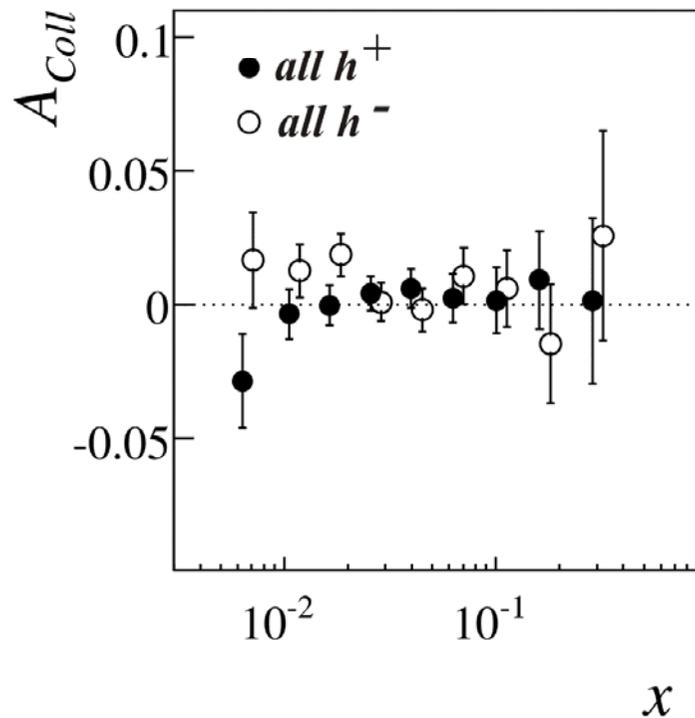
# Collins asymmetry



transversely polarised **deuteron target**  
**charged hadrons** (mostly pions)

- **2004**: first results from **2002 data** PRL94 (2005) 202002 confirmed by
- **2006**: final results from **2002-2004 data** NPB765 (2007)31

COMPASS 2002-2004



**asymmetries compatible with zero within the statistical errors**  
**(syst. errors much smaller)**

**the same with leading  $h$**



# Collins asymmetry

naïve interpretation of the data (parton model, valence region)

- proton data**

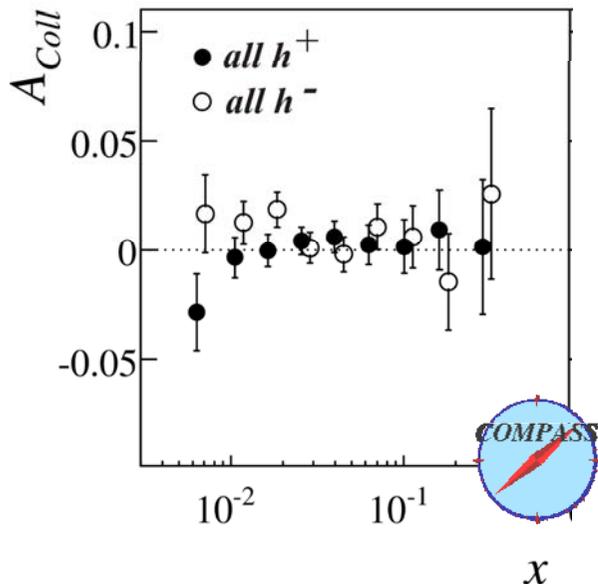
$$A_{Coll}^{p,\pi^+} \simeq \frac{4\Delta_T u_v \Delta_T^0 D_1 + \Delta_T d_v \Delta_T^0 D_2}{4u_v D_1 + d_v D_2} \quad A_{Coll}^{p,\pi^-} \simeq \frac{4\Delta_T u_v \Delta_T^0 D_2 + \Delta_T d_v \Delta_T^0 D_1}{4u_v D_2 + d_v D_1}$$

→ unfavored Collins FF ~ - favored Collins FF

$$\Delta_T^0 D_2 \approx -\Delta_T^0 D_1 \quad \text{at variance with unpol case}$$

**u quark dominance (d quark DF ~ unconstrained)**

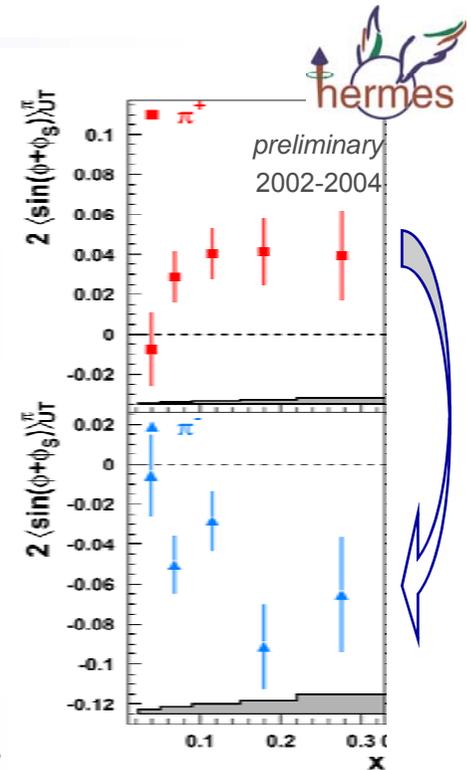
- deuteron data**



$$A_{Coll}^{d,\pi^+} \simeq \frac{\Delta_T u_v + \Delta_T d_v}{u_v + d_v} \frac{4\Delta_T^0 D_1 + \Delta_T^0 D_2}{4D_1 + D_2}$$

$$A_{Coll}^{d,\pi^-} \simeq \frac{\Delta_T u_v + \Delta_T d_v}{u_v + d_v} \frac{\Delta_T^0 D_1 + 4\Delta_T^0 D_2}{D_1 + 4D_2}$$

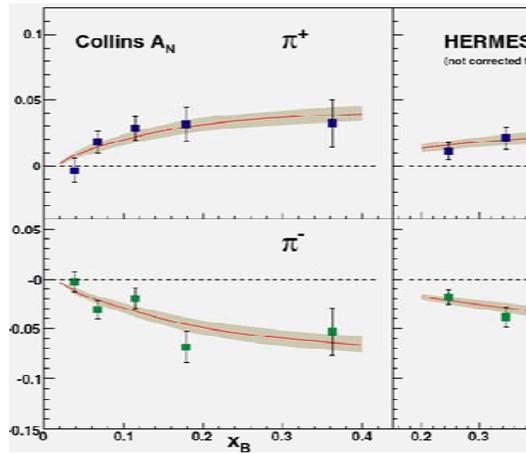
some (small) effect expected even if  $\Delta_T^0 D_2 \approx -\Delta_T^0 D_1$   
 → cancellation between  $\Delta_T u(x)$  and  $\Delta_T d(x)$   
**access to  $\Delta_T d(x)$**



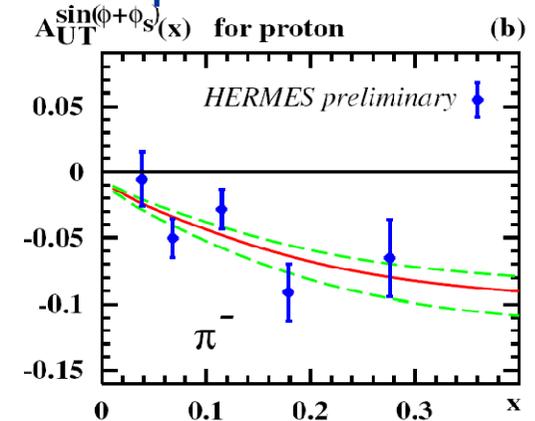
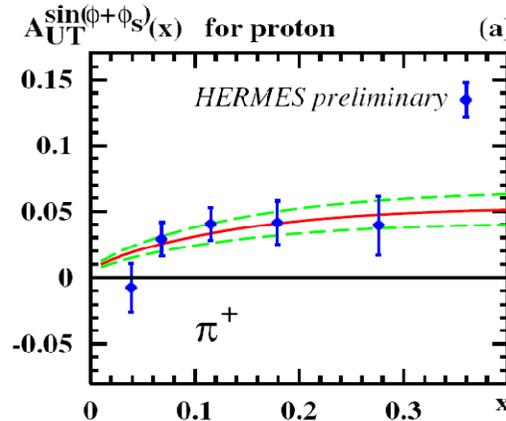
# Collins asymmetry

2005-2006: theoretical work mainly

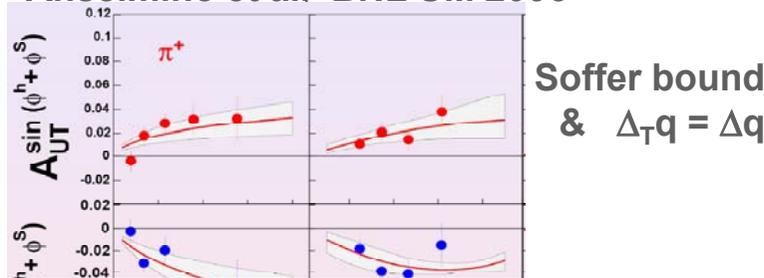
Vogelsang Yuan, PRD 71



Efremov et al, PRD 73, 094025 (2006)  
chiral quark-soliton model



Anselmino et al. BNL UM 2006



- favored Collins FF ~  
– unfavored Collins FF
- u-dominance
- agreement with the first Belle and COMPASS 2002 data
- *marginal agreement with the new deuterium data*

using the new Belle, the HERMES and the COMPASS 2002-2004 data  
first extraction from transversity from a global analysis

Anselmino et al (2007) → A. Prokudin

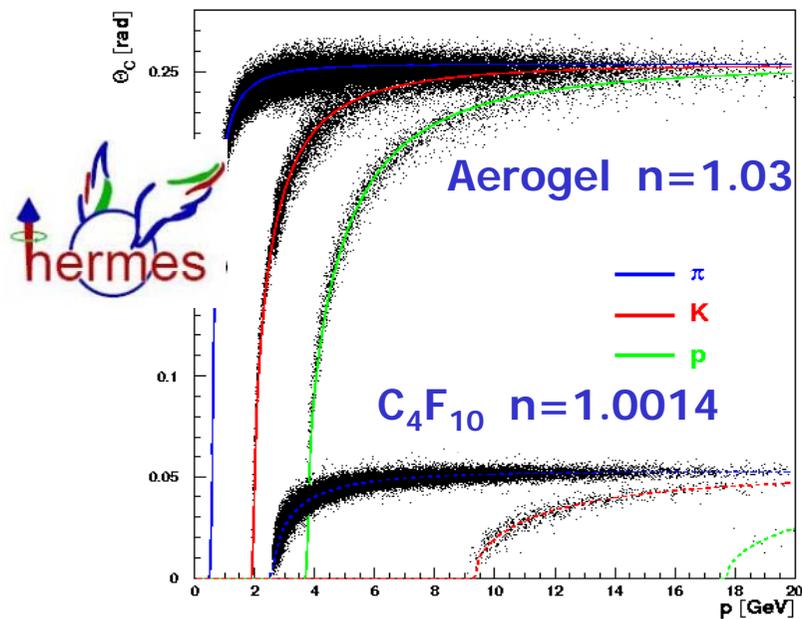


# Also new: Collins asymmetry for $K^\pm$

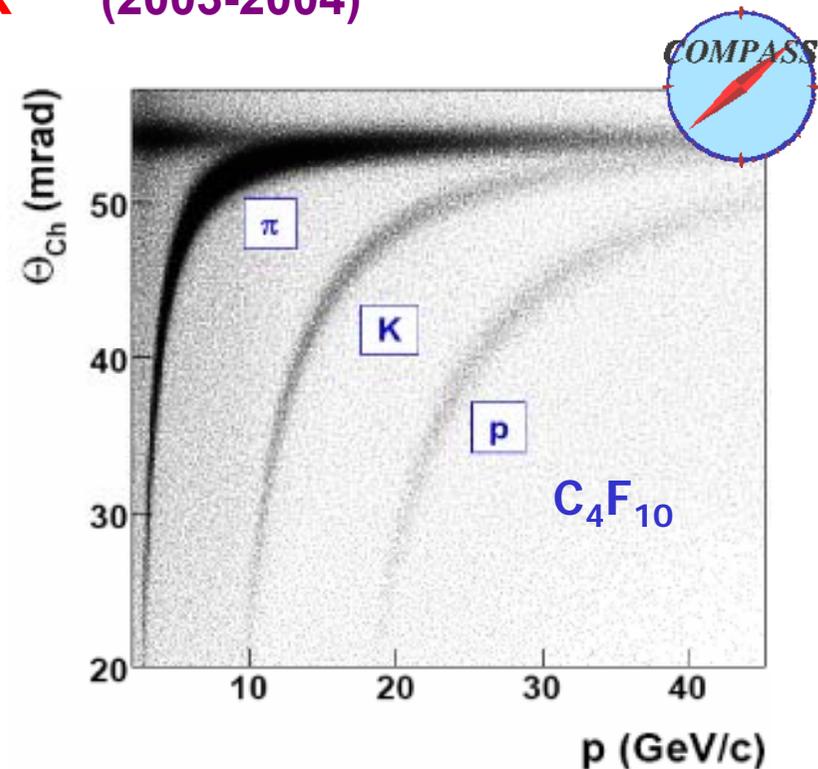
together with measurements on different targets,  
relevant for flavour decomposition

there are very recent results for the Collins asymmetry

- on **proton** for  $K^+$  and  $K^-$
- on **deuteron** for  $\pi^+$  and  $\pi^-$ ,  $K^+$  and  $K^-$  (2003-2004)



$\pi, K, p$  ID within  $2 < E_h < 15$  GeV



threshold:  $\pi \sim 2$  GeV/c  
 $K \sim 10$  GeV/c



# Collins Asymmetry for pions and kaons

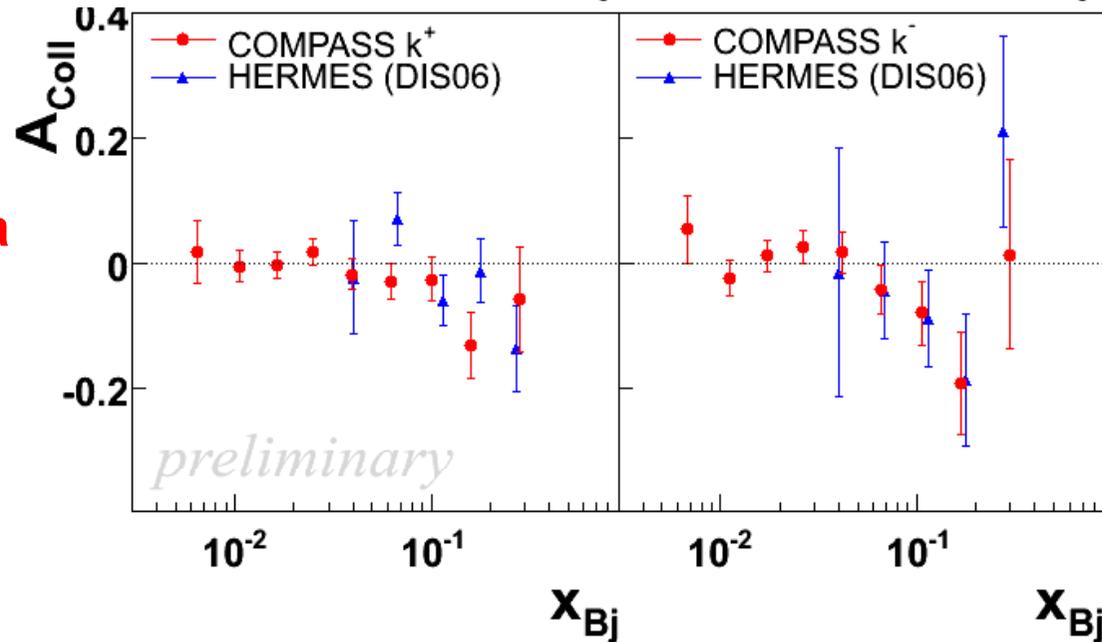
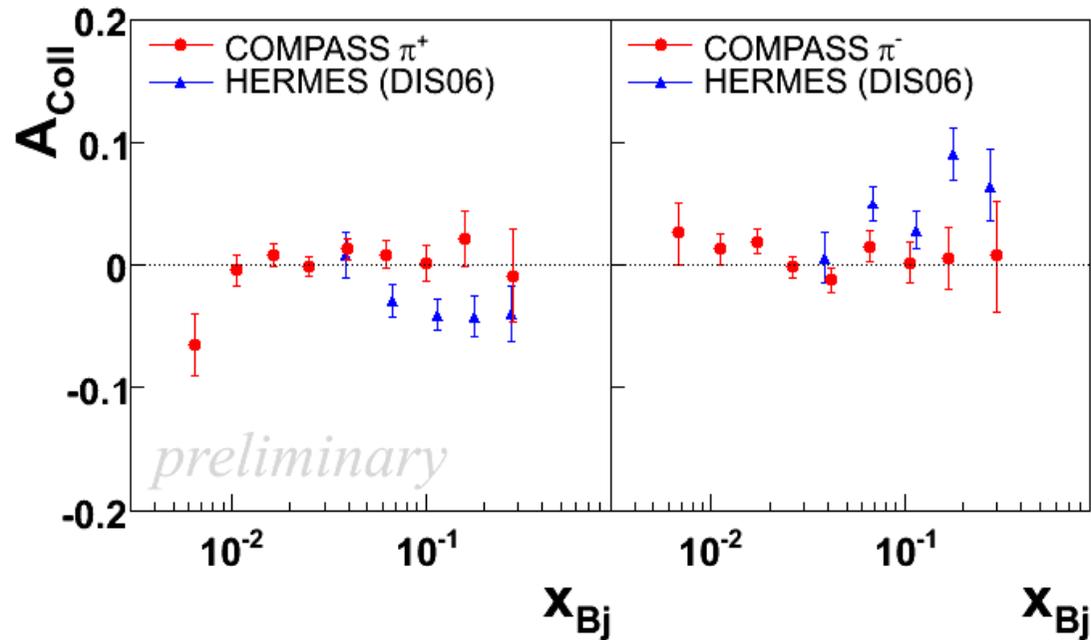


preliminary  
2002-2004 data  
proton



preliminary  
2003-2004 data  
deuteron

COMPASS  
sign  
convention



# Transversity DF: how to measure it

can be measured in SIDIS on a transversely polarised target via “quark polarimetry”

$I N^{\uparrow} \rightarrow l' h X$  “Collins” asymmetry  
“Collins” Fragmentation Function

$I N^{\uparrow} \rightarrow l' h h X$  two-hadron asymmetry  
“Interference” Fragmentation Function

$I N^{\uparrow} \rightarrow l' \Lambda X$   $\Lambda$  polarisation  
Fragmentation Function of  $q^{\uparrow} \rightarrow \Lambda$

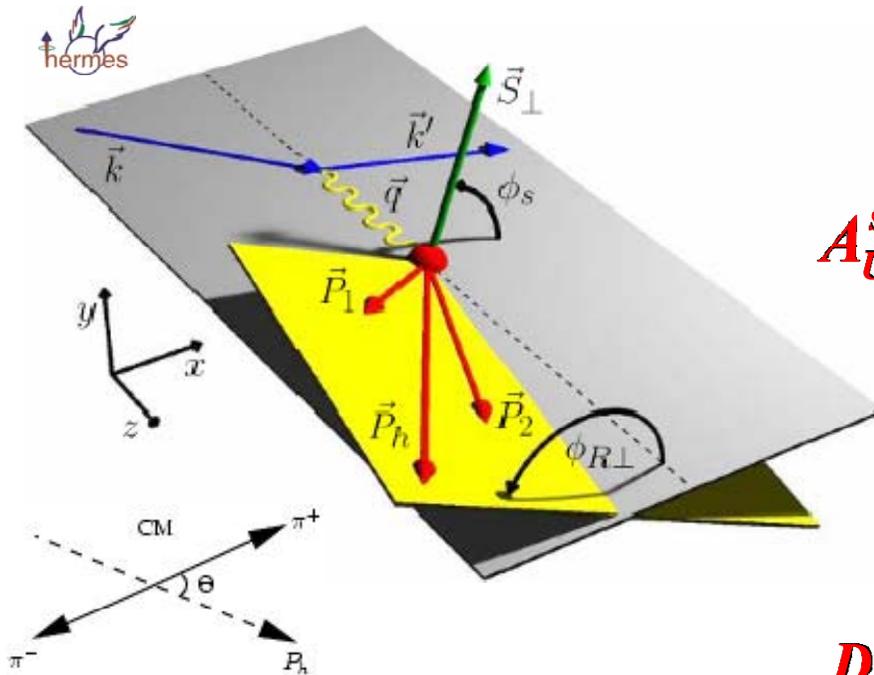
alternative way to access transversity  
not sensible to transverse momenta

*M. Radici*



# two-hadron asymmetries

in inclusive production of hadron pairs, one can define the angle  $\phi_{R\perp}$  and measure an **azimuthal asymmetry** from the modulation of the number of events in  $\phi_{RS} = \phi_{R\perp} - \phi_S$ ,  
 or  $\phi_{RS} = \phi_{R\perp} + \phi_S$



$$A_{UT}^{\sin(\phi_{R\perp} + \phi_S) \sin\theta} \propto \frac{\sum h_1(x) H_1^{\perp\perp}(z)}{\sum q(x) D_1(z)}$$

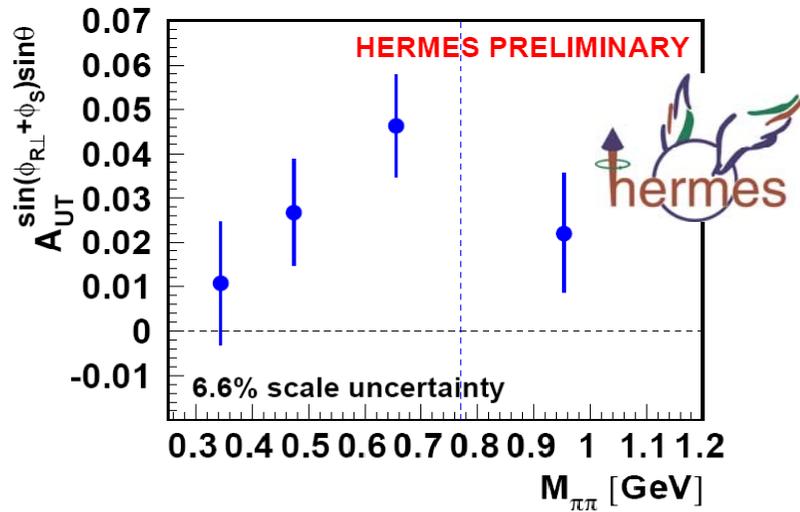
$D_1, H_1^{\perp\perp}$  presently unknown  
 being measured in  $e^+e^-$  (BELLE)

expected to depend on the hadron pair invariant mass

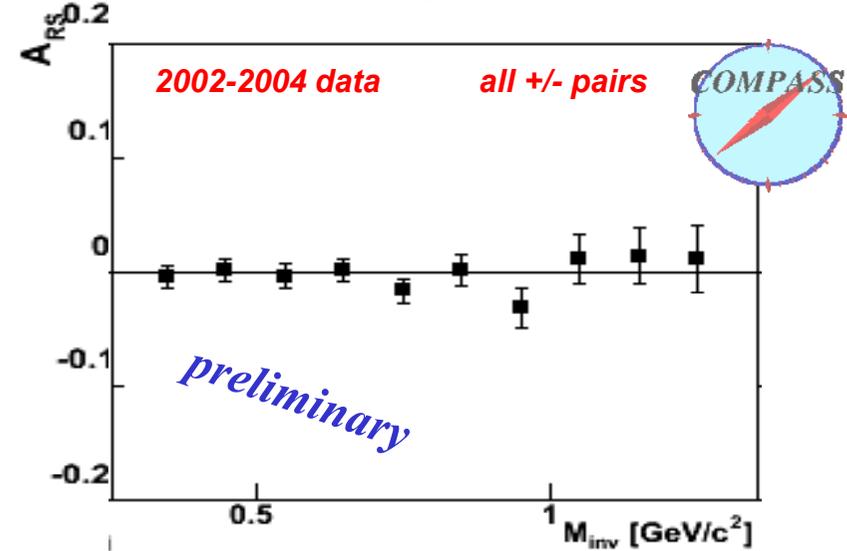


# two-hadron asymmetries

proton target

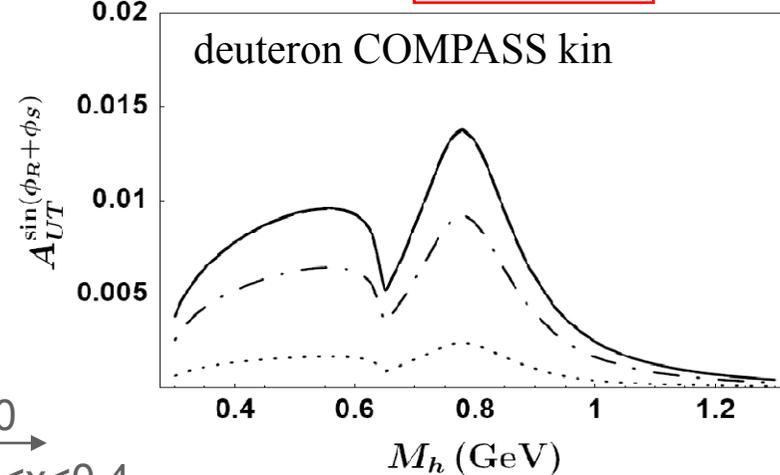
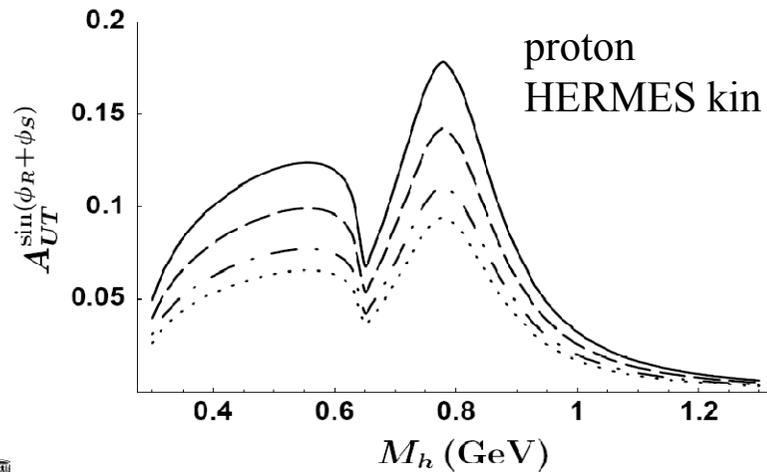


deuteron target



A. Bacchetta, M. Radici PRD74(2006)114007 model for DiFF

M. Radici



1/10  
0.004 < x < 0.4

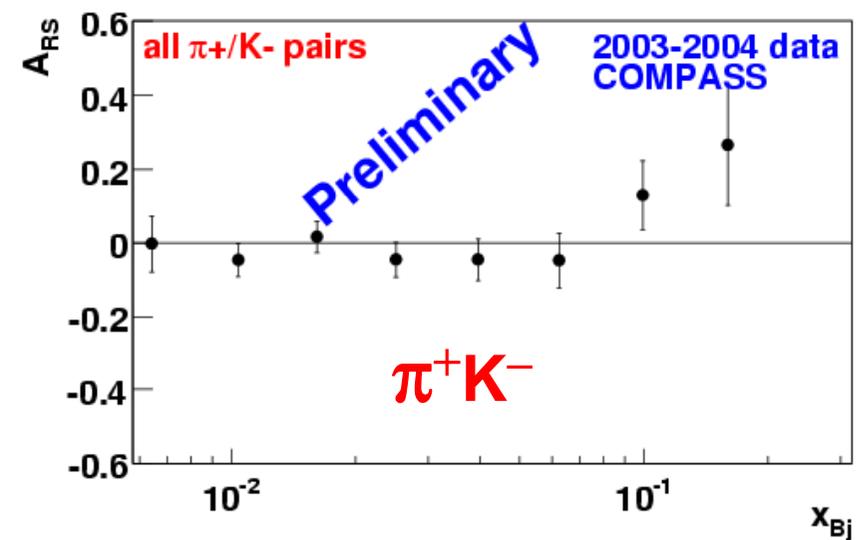
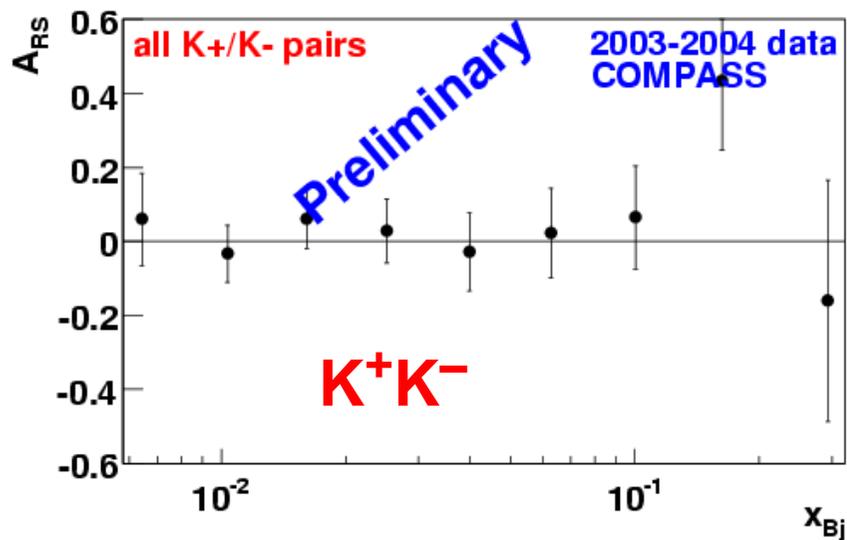
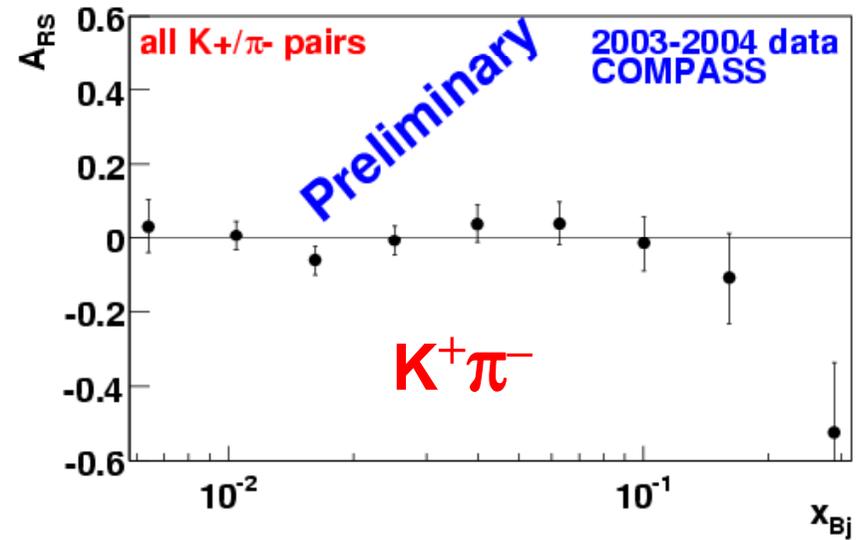
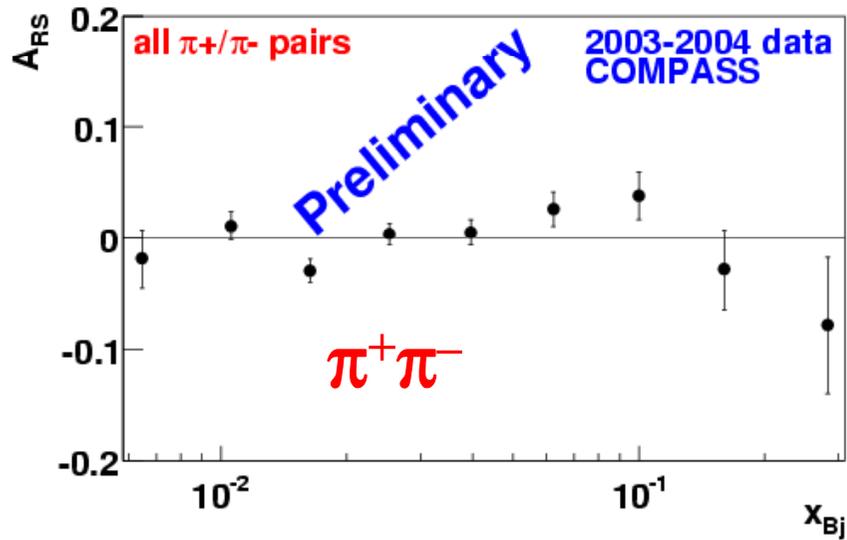
AND deuteron target



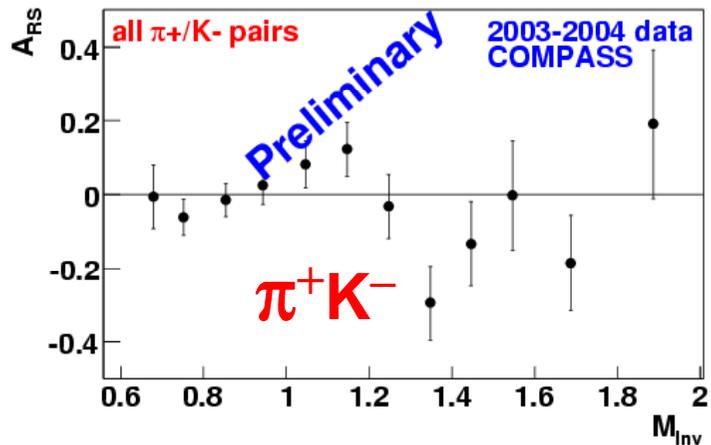
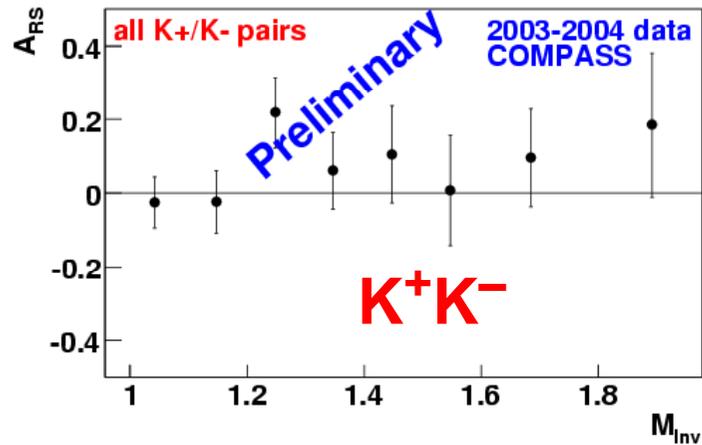
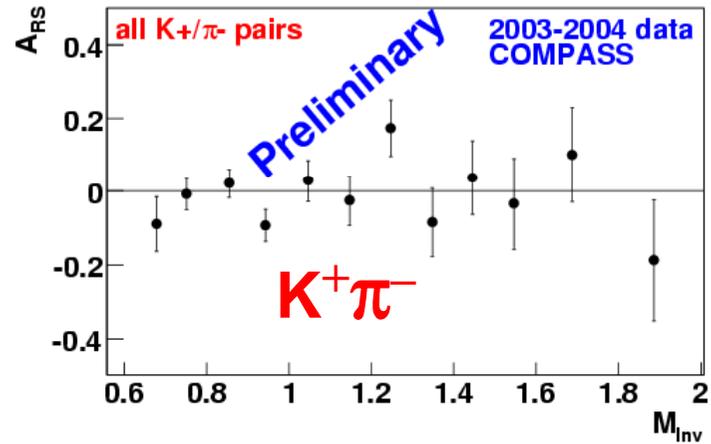
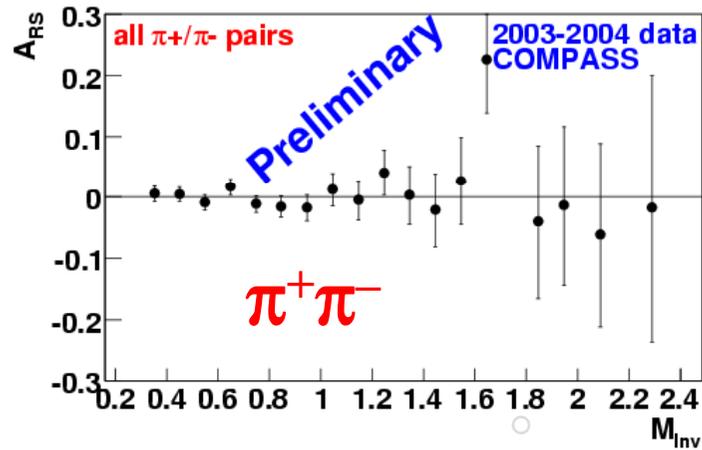
# two-hadron asymmetries



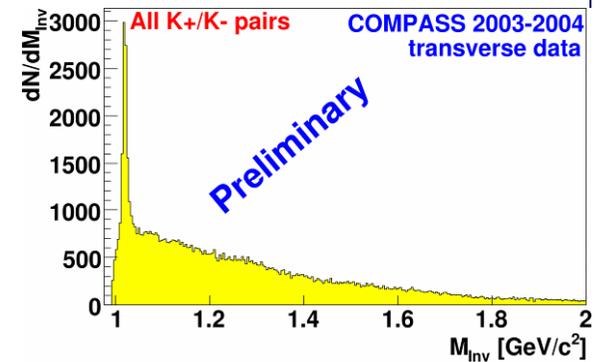
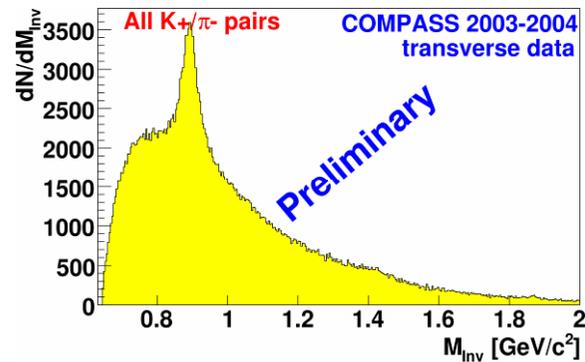
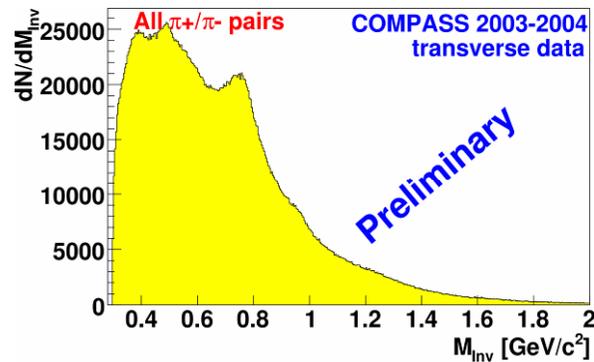
**new results** from COMPASS with **deuteron target** (2007)



# two-hadron asymmetries



deuteron  
target



# Transversity DF: how to measure it

can be measured in SIDIS on a transversely polarised target via “quark polarimetry”

$I N^{\uparrow} \rightarrow I' h X$  “Collins” asymmetry  
“Collins” Fragmentation Function

$I N^{\uparrow} \rightarrow I' h h X$  two-hadron asymmetry  
“Interference” Fragmentation Function

$I N^{\uparrow} \rightarrow I' \Lambda X$   $\Lambda$  polarisation  
Fragmentation Function of  $q^{\uparrow} \rightarrow \Lambda$

alternative way to access transversity  
independent on Transverse Momentum ...  
the favorite in some models  
(statistics)



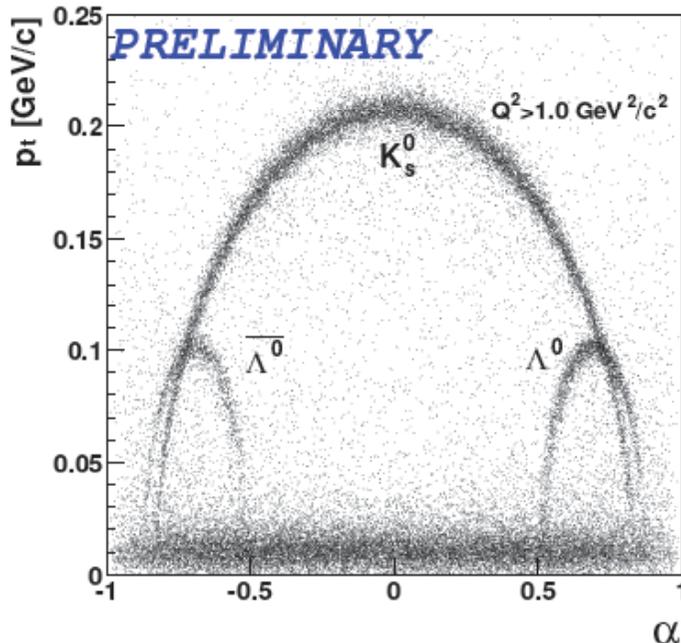
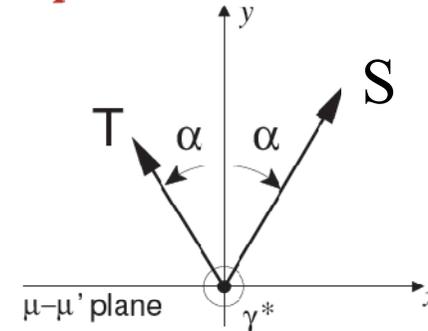
# $\Lambda$ polarimetry



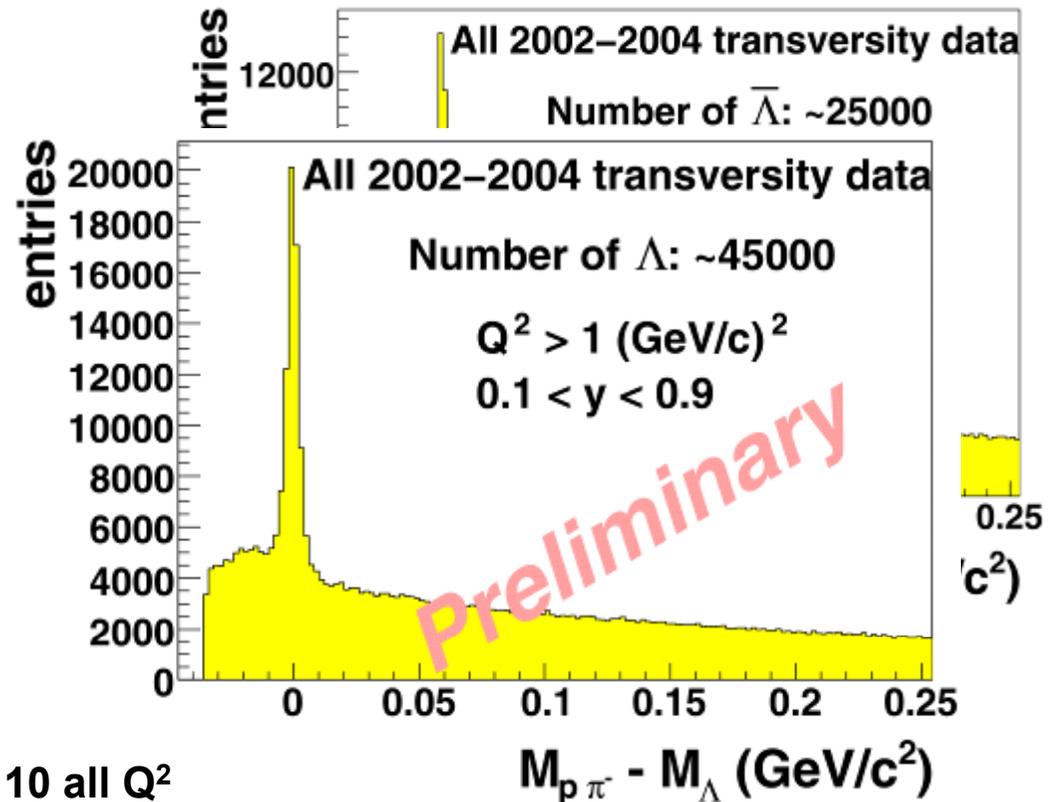
$$P_{T,exp}^{\Lambda} = \frac{d\sigma^{\mu N^{\uparrow} \rightarrow \mu' \Lambda^{\uparrow} X} - d\sigma^{\mu N^{\downarrow} \rightarrow \mu' \Lambda^{\uparrow} X}}{d\sigma^{\mu N^{\uparrow} \rightarrow \mu' \Lambda^{\uparrow} X} + d\sigma^{\mu N^{\downarrow} \rightarrow \mu' \Lambda^{\uparrow} X}}$$

$$= f P_N D(y) \frac{\sum_q e_q^2 \Delta_T q(x) \Delta_T D_{\Lambda/q}(z)}{\sum_q e_q^2 q(x) D_{\Lambda/q}(z)}$$

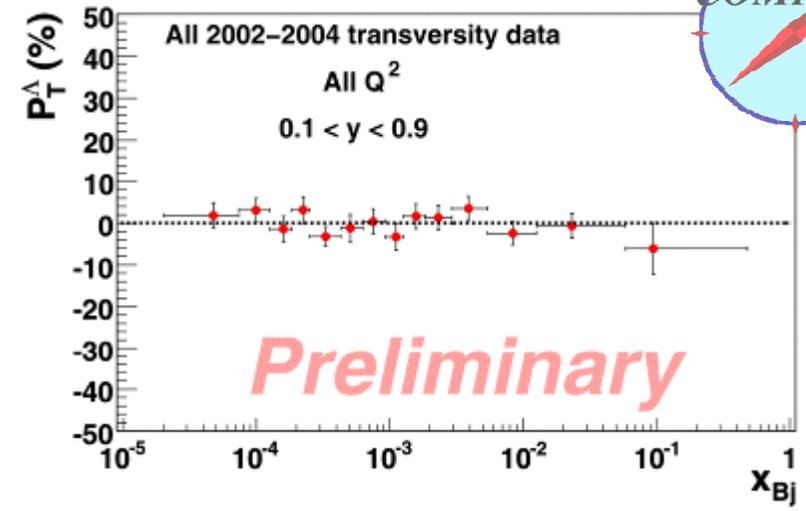
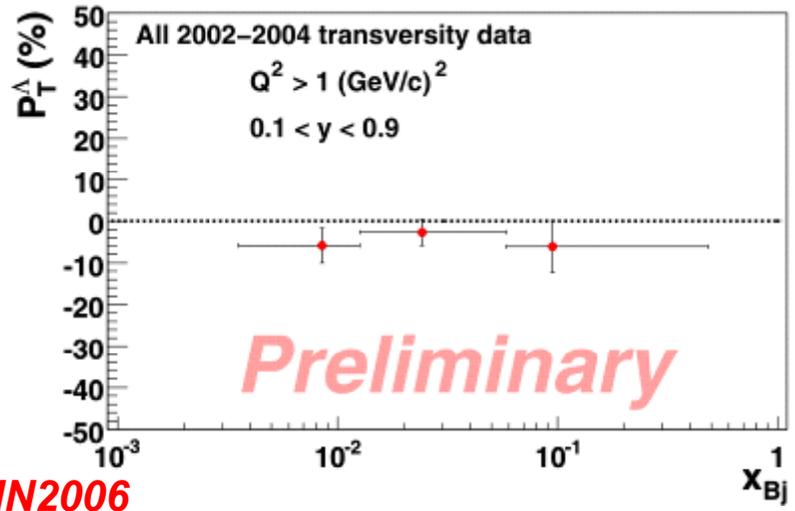
$\Lambda$  polarization axis



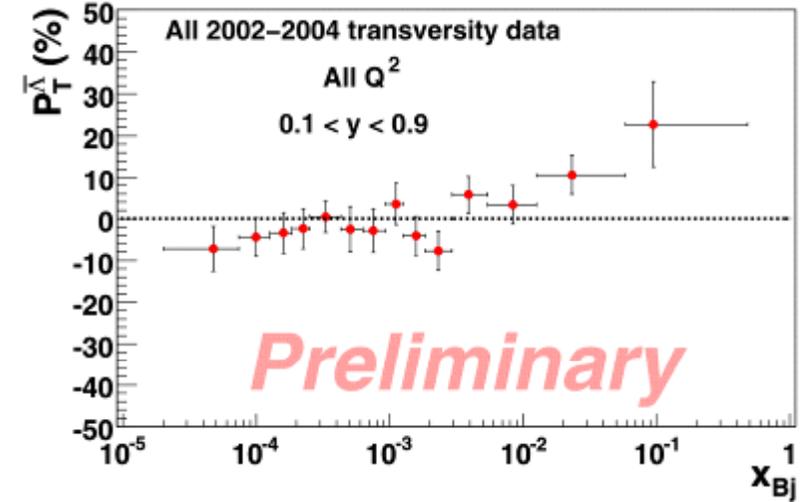
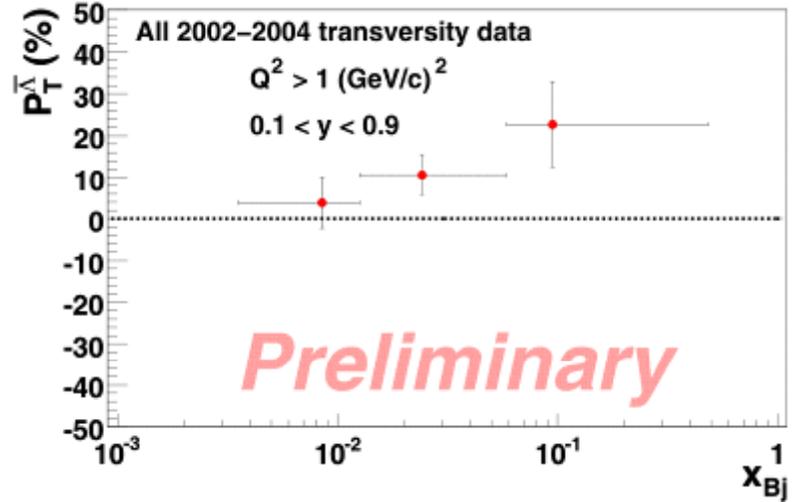
$\times 10$  all  $Q^2$



# $\Lambda$ polarimetry



SPIN2006



systematic errors not larger than statistical errors

**RICH ID not used yet; someother improvement in selection still foreseen**



Anna Martin

- SIDIS Experiments with transversely polarised tgt  
HERMES and COMPASS
- Results on asymmetries
  - transversity Distribution Function
  - **Sivers Distribution Function**
  - Other TMD Distribution Functions
- Conclusions



# Measurement of the **Sivers DF** in SIDIS

---

$$\Delta_0^T \mathbf{q} \text{ (or } \Delta^N f_{q/N\uparrow} \text{ or } f_{1T}^{\perp q} \text{ or } q_T)$$

it is the most famous of the TMD parton distribution functions

it is related to an intrinsic asymmetry in the parton transverse momentum distribution induced by the nucleon spin

- requires final/initial-state interactions  
quark rescattering via soft gluon exchange
- should change sign from SIDIS to DY
- it is related to the parton orbital angular momentum in a transversely polarized nucleon



# Sivers asymmetry

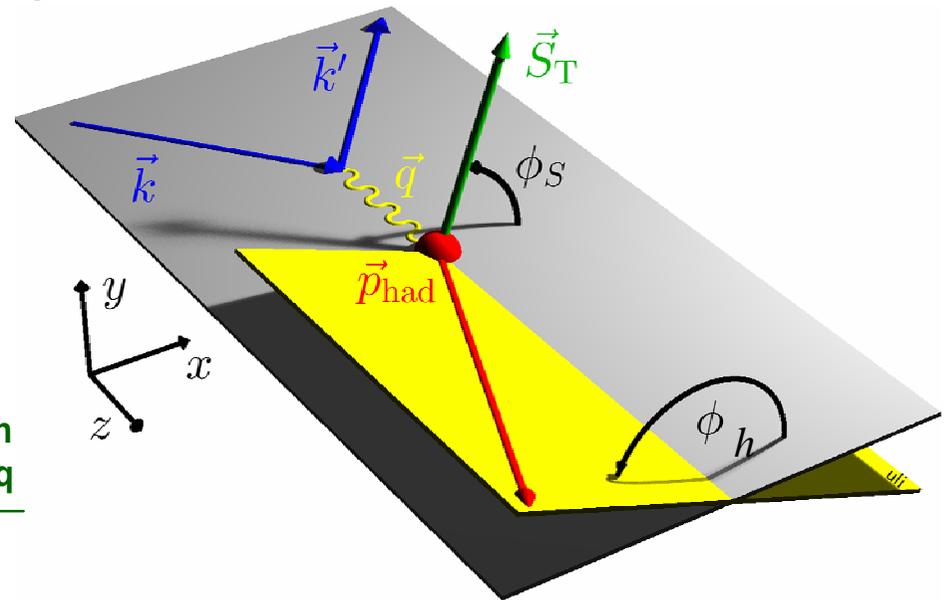
appears in SIDIS as a modulation in the “Sivers angle”  $\Phi_S$

$$\mathbf{N}_h^\pm(\Phi_S) = \mathbf{N}_h^0 \cdot [1 \pm \mathbf{P}_T \cdot \mathbf{A}_{\text{Siv}} \cdot \sin\Phi_S]$$

$$\Phi_S = \phi_h - \phi_S$$

$\phi_h$  azimuthal angle of hadron momentum  
 $\phi_S$  azimuthal angle of the spin of the nucleon

$$\mathbf{A}_{\text{Siv}} \approx \frac{\sum_q e_q^2 \cdot \Delta_0^T \mathbf{q} \cdot \mathbf{D}_q^h}{\sum_q e_q^2 \cdot \mathbf{q} \cdot \mathbf{D}_q^h}$$



the “Sivers angle”  $\Phi_S$  and the “Collins angle”  $\Phi_C$  are independent

→ the Collins and Sivers asymmetries can be disentangled and extracted from the same data in SIDIS

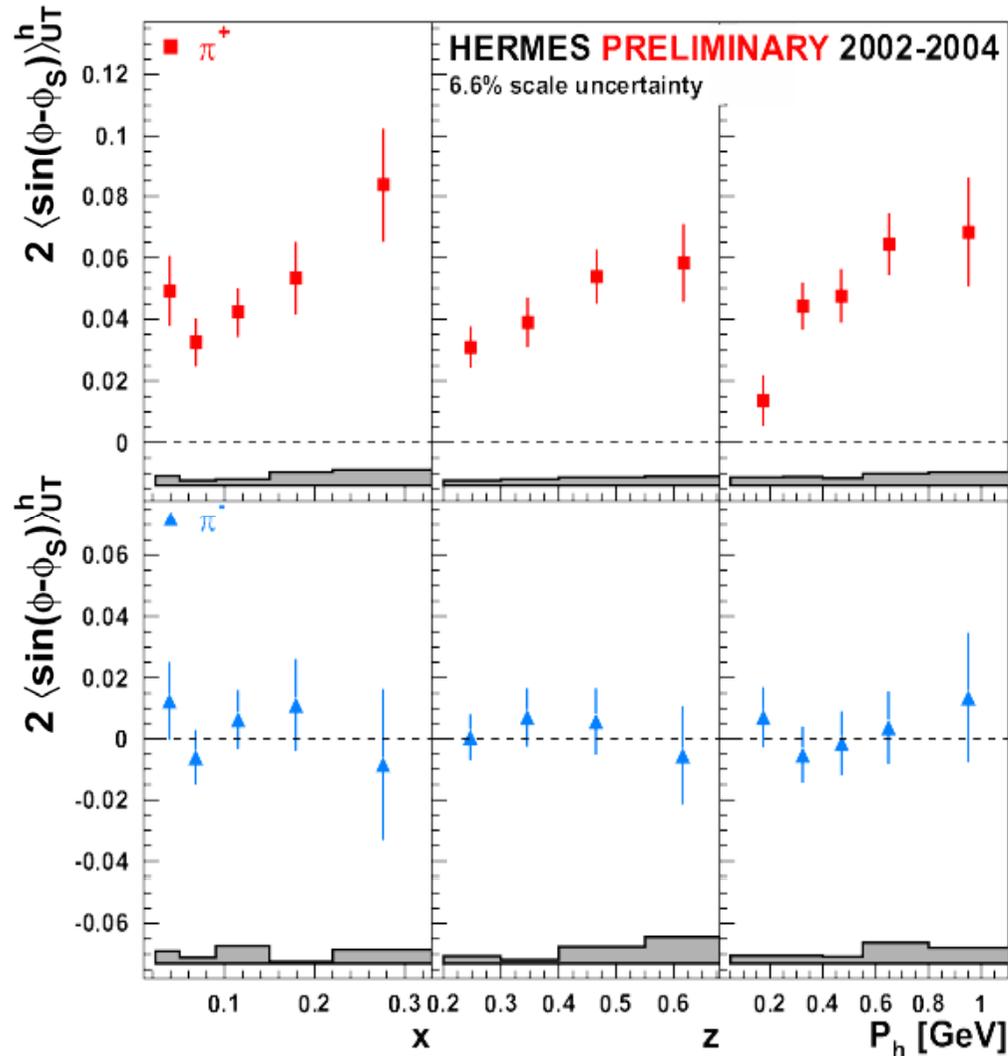


# Sivers asymmetry



proton target transversely polarised – charged pions

- 2004: results from 2002-2003 data PRL94(2005)012002 confirmed by
- 2005: results from 2002-2004 data



$\pi^+$  asymmetry  $> 0$   
**VERY CLEAR SIGNAL**  
 $\pi^-$  asymmetry  $\sim 0$

**the Sivers effect is a  
real effect !**

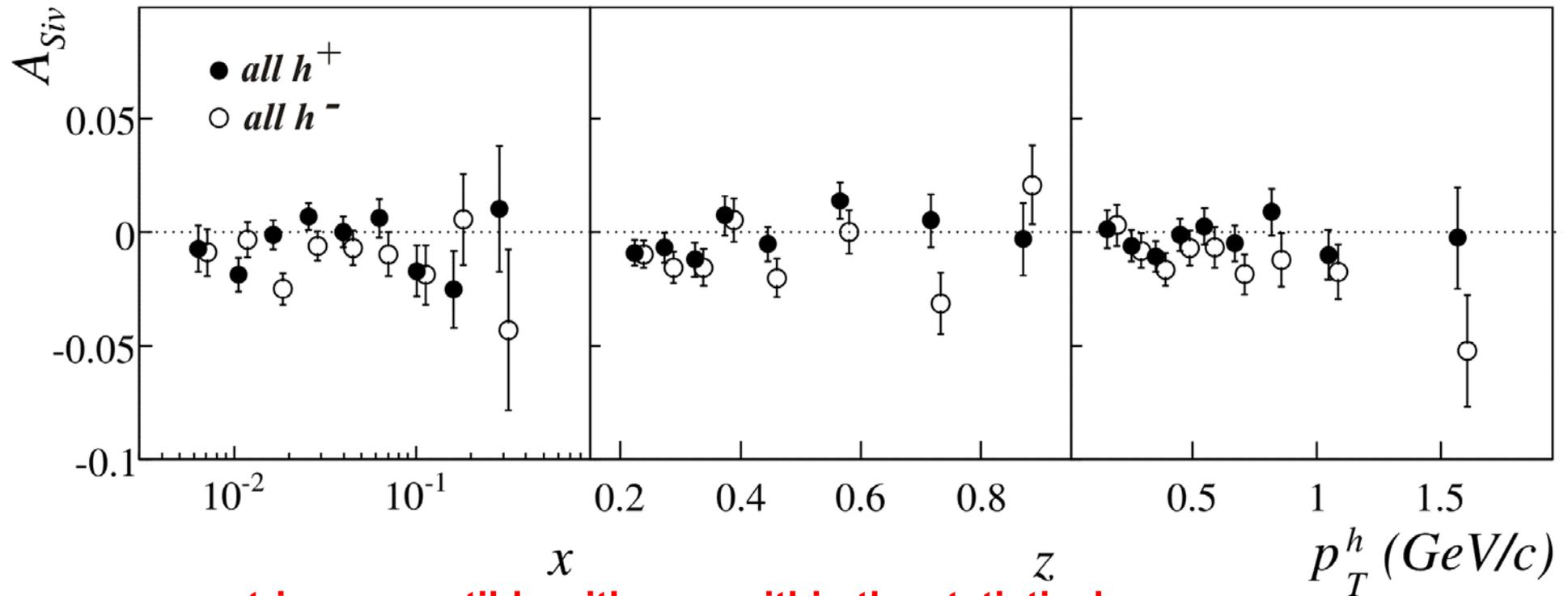
# Sivers asymmetry



deuteron target transversely polarised  
charged hadrons (mostly pions)

- 2004: results from 2002 data PRL94(2005)202002 confirmed by
- 2006: results from 2002-2004 data NPB765(2007)31

COMPASS 2002-2004



asymmetries compatible with zero within the statistical errors  
(syst. errors much smaller)



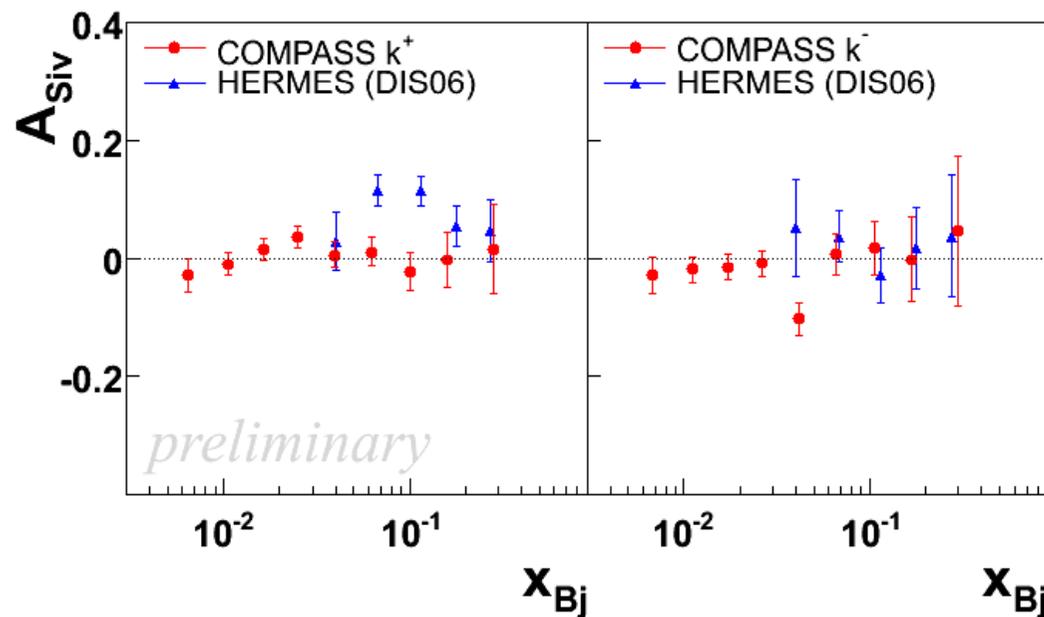
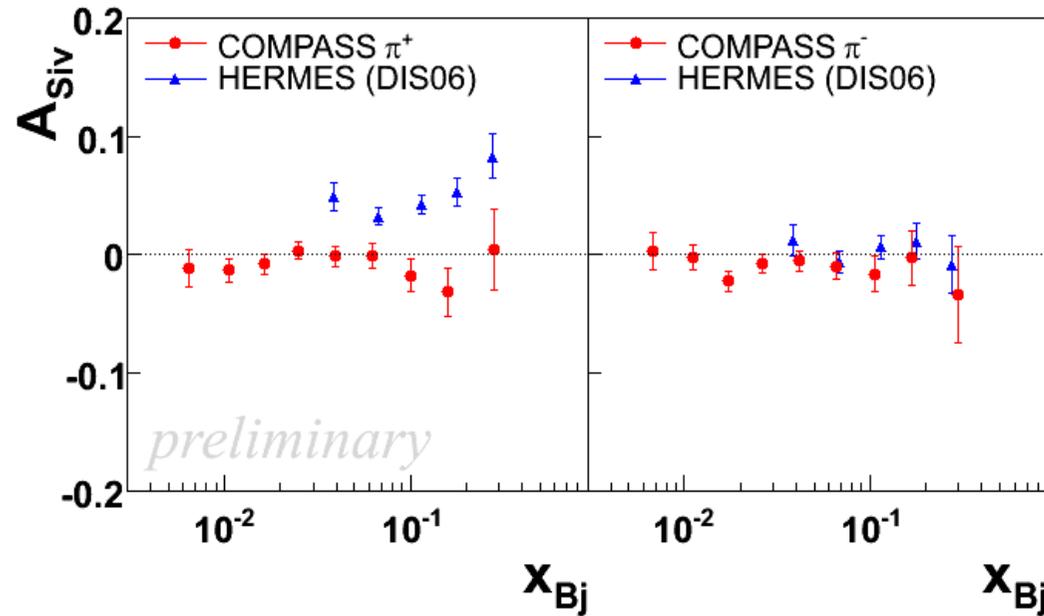
# Also new: Sivers asymmetry for $\pi^\pm, K^\pm$



**HERMES**  
*preliminary 2002-2004*  
 **$K^+$  and  $K^-$  on proton**  
 (DIS06)



**COMPASS**  
*preliminary 2003-2004*  
 **$\pi^+$  and  $\pi^-$ ,  $K^+$  and  $K^-$**   
**on deuteron**  
 (GPD06)



# Sivers asymmetry

naïve interpretation of the data (parton model, valence region)

- proton data**

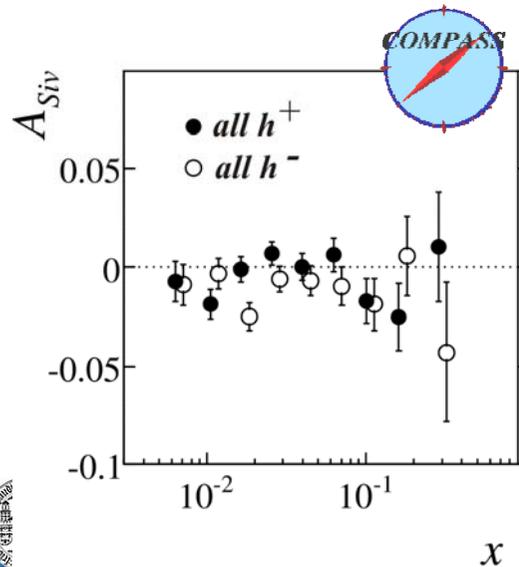
$$A_{Siv}^{p,\pi^+} \simeq \frac{4\Delta_0^T u_v D_1 + \Delta_0^T d_v D_2}{4u_v D_1 + d_v D_2} \quad A_{Siv}^{p,\pi^-} \simeq \frac{4\Delta_0^T u_v D_2 + \Delta_0^T d_v D_1}{4u_v D_2 + d_v D_1}$$

asymmetry for  $\pi^+$  > 0, asymmetry for  $\pi^- \approx 0$

→ Sivers DF for d-quark  $\approx -2$  Sivers DF for u-quark

$$\Delta_0^T d_v \simeq -2 \Delta_0^T u_v$$

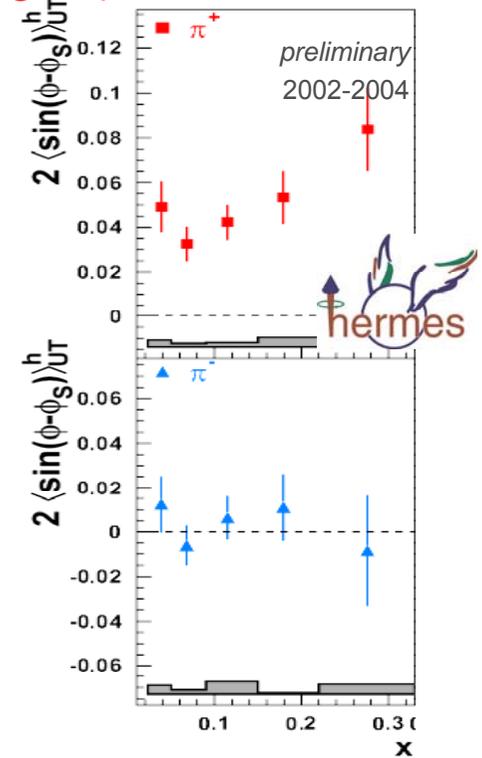
- deuteron data**



$$A_{Siv}^{d,\pi^+} \simeq A_{Siv}^{d,\pi^-} \simeq \frac{\Delta_0^T u_v + \Delta_0^T d_v}{u_v + d_v}$$

the measured asymmetries compatible with zero suggest

$$\Delta_0^T d_v \simeq -\Delta_0^T u_v$$

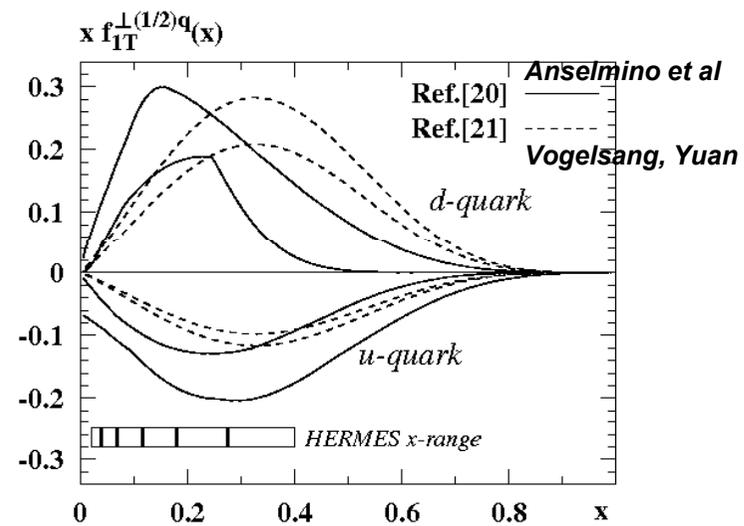
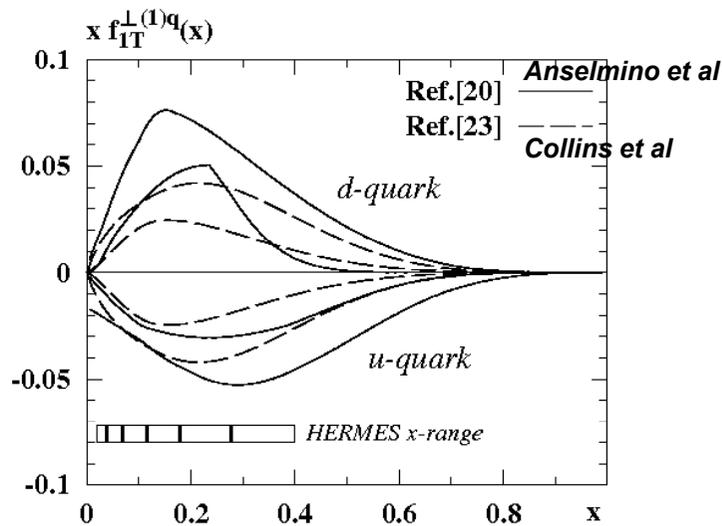


# Sivers asymmetry

2005-2006: theoretical work on the interpretation of the data  
 use of the new HERMES results to extract the Sivers DF

*Vogelsang Yuan (2005), Anselmino et al (2005), Collins et al (2006)*

- good fits to the new proton from HERMES
- comparison (or fit) with the deuteron COMPASS 2002 data ok  
 with  $\Delta_0^T d$  ranging from  $-\Delta_0^T u$  to  $-2\Delta_0^T u$



*Anselmino et al., hep-ph/0511017*

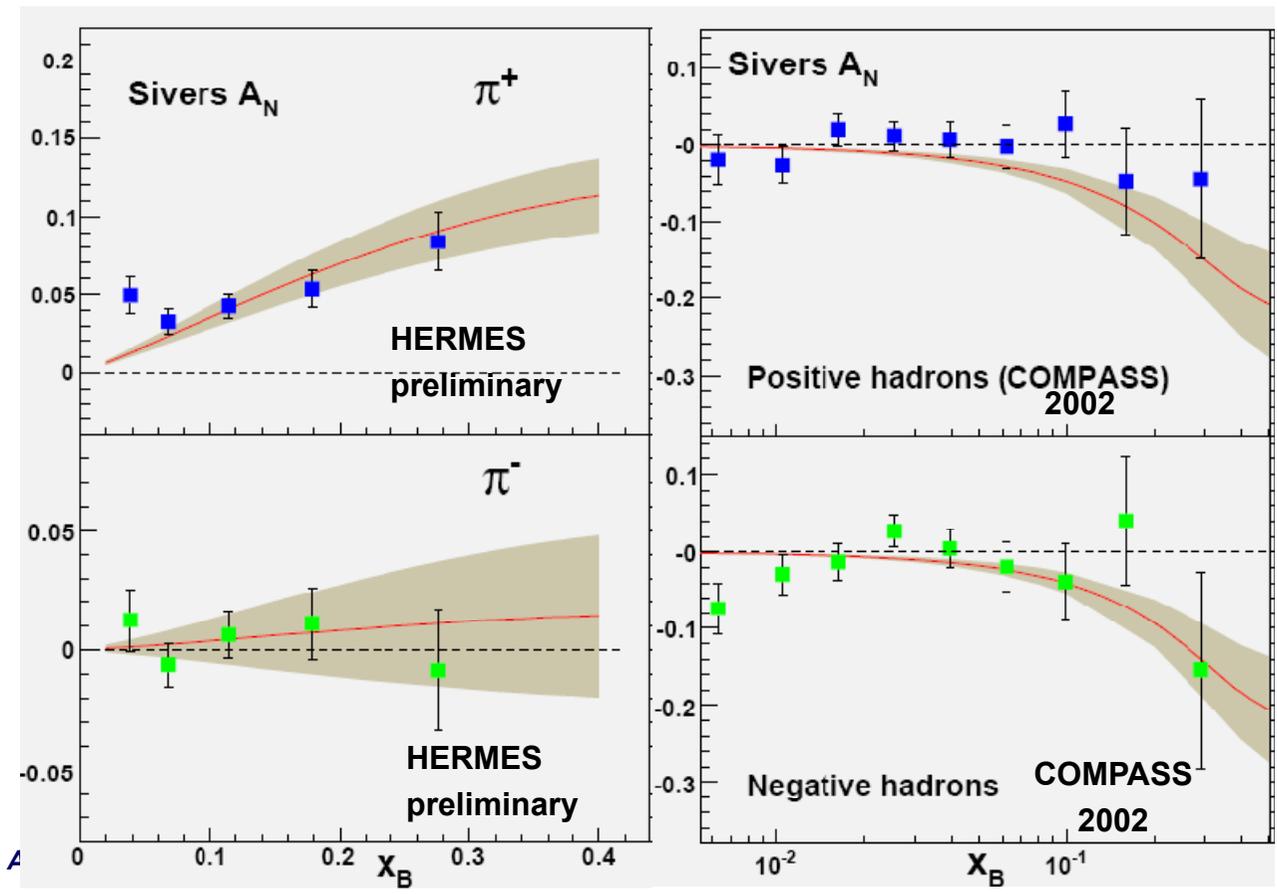


# Siver asymmetry – flavour separation

to have a hint about the **relevance of the 2002-2004 deuteron data**,  
 same fit as in Vogelsang and Yuan, PRD 72, 054028(2005)

$$\Delta_0^T u = S_u x(1-x)u(x) \quad \text{with HERMES data only:} \quad S_u = -0.81 \pm 0.07$$

$$\Delta_0^T d = S_d x(1-x)u(x) \quad S_d = 1.86 \pm 0.28$$



$$S_u = -0.76 \pm 0.07$$

$$S_d = 1.83 \pm 0.29$$

**[Trieste, 2006]**



# Siver asymmetry – flavour separation

$$\Delta_0^T u = S_u x(1-x)u(x)$$

$$\Delta_0^T d = S_d x(1-x)u(x)$$

**HERMES only**

$$S_u = -0.76 \pm 0.07$$

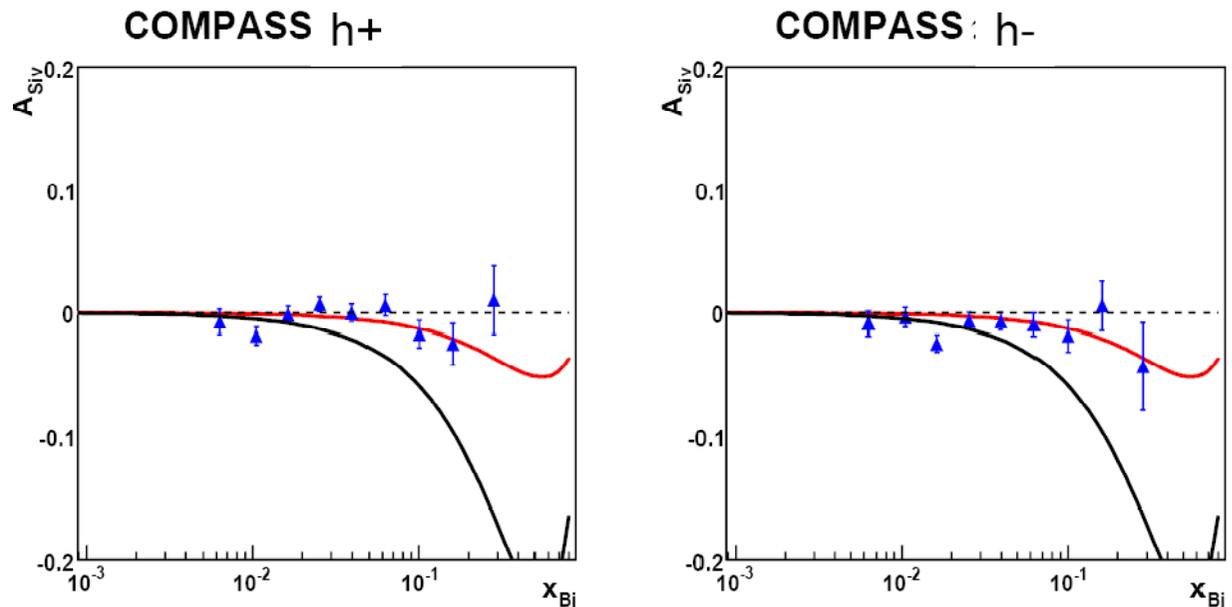
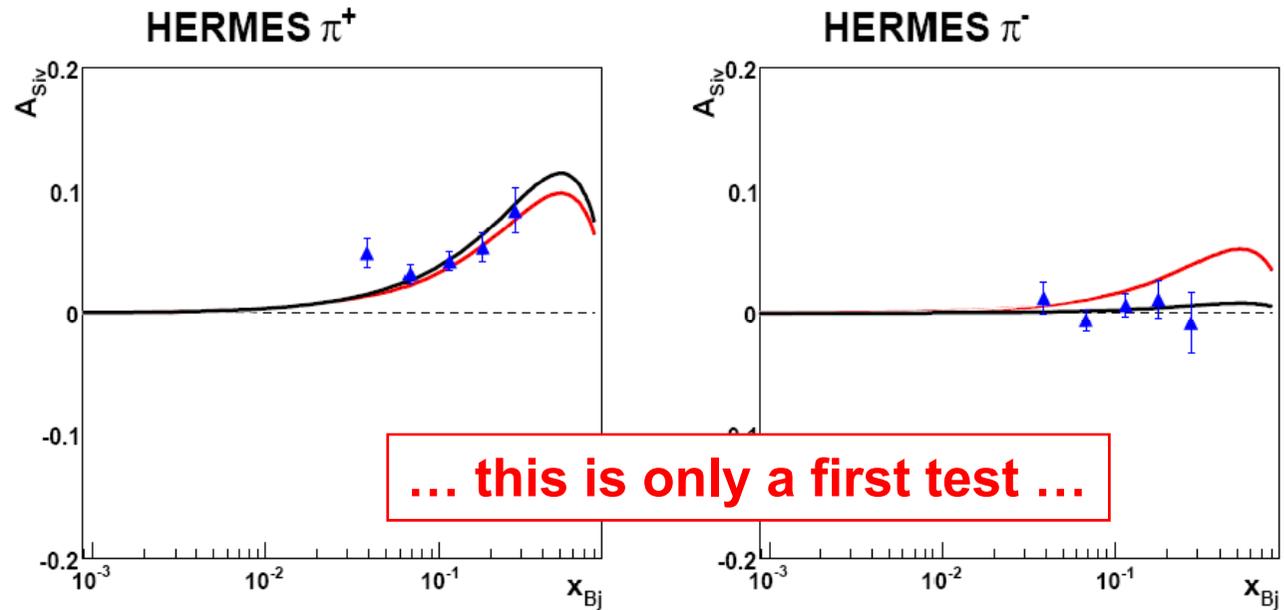
$$S_d = 1.83 \pm 0.29$$

**HERMES and  
COMPASS 02-04**

$$S_u = -0.52 \pm 0.05$$

$$S_d = 0.76 \pm 0.10$$

**[Trieste, 2006]**



# Sivers asymmetry

---

the measured asymmetry on **deuteron** compatible with zero  
has been interpreted as

## **Evidence for the Absence of Gluon Orbital Angular Momentum in the Nucleon**

**S.J. Brodsky and S. Gardner, PLB643 (2006) 22**

..... The approximate cancellation of the SSA measured on a deuterium target suggests that the gluon mechanism, and thus the orbital angular momentums carried by gluons in the nucleon, is small.



- **SIDIS Experiments with transversely polarised tgt**  
HERMES and COMPASS
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  - transversity Distribution Function
  - Sivers Distribution Function
  - **Other TMD Distribution Functions**  
*taking into account transverse momentum,  
more terms appear in the SIDIS cross-section*
- **Conclusions**



# semi-inclusive cross-section

## 18 structure functions

A. Metz

$$\begin{aligned}
 \frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = & \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right. \\
 & + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \\
 & + S_{\parallel} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] \\
 & + S_{\parallel} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right] \\
 & + |S_{\perp}| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & \quad + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & \quad \left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \\
 & + |S_{\perp}| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\
 & \quad \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \left. \right\},
 \end{aligned}$$

4

1

2

2

6

3

A Bacchetta, M Diehl, K Goeke, A Metz, P Mulders, M Schlegel (06)



# semi-inclusive cross-section

## 18 structure functions

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right.$$

**Cahn**

**EMC**  
**E665**  
**ZEUS**  
**CLAS**  
**HERMES**

**Boer-  
Mulders**

$$\begin{aligned} & + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \\ & + S_{\parallel} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] \\ & + S_{\parallel} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right] \\ & + |S_{\perp}| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\ & \quad + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\ & \quad \left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \\ & + |S_{\perp}| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\ & \quad \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \left. \right\}, \end{aligned}$$



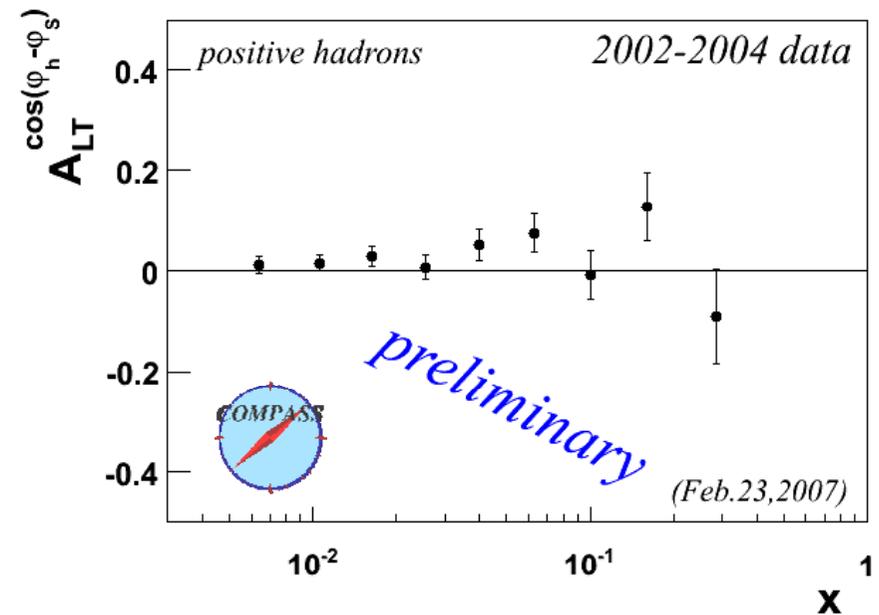
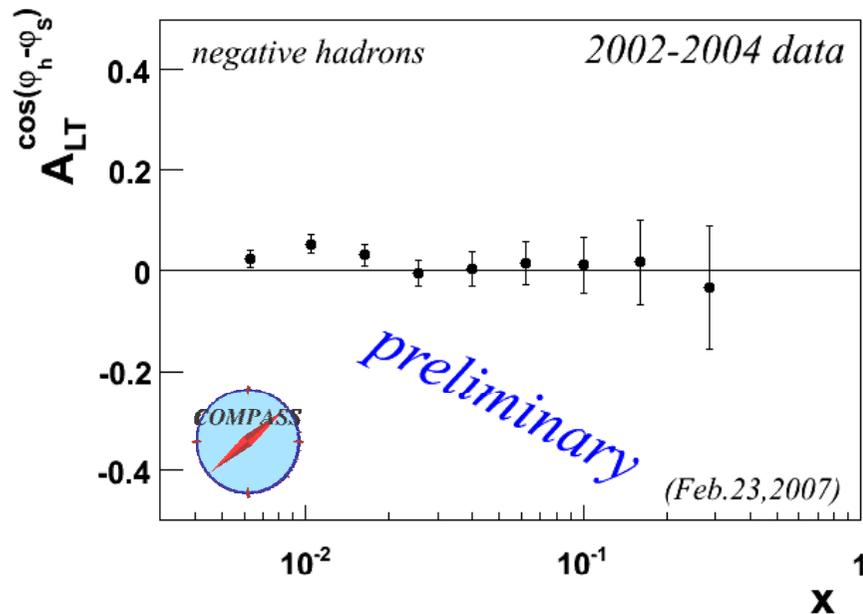


# target transverse spin dependent asymmetries (LO)

/1

$$F_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$$

$g_{1T}$  is the only parton DF which is  
chiral-even, T-even, leading twist function  
in addition to the unpolarised DF and to the helicity DF

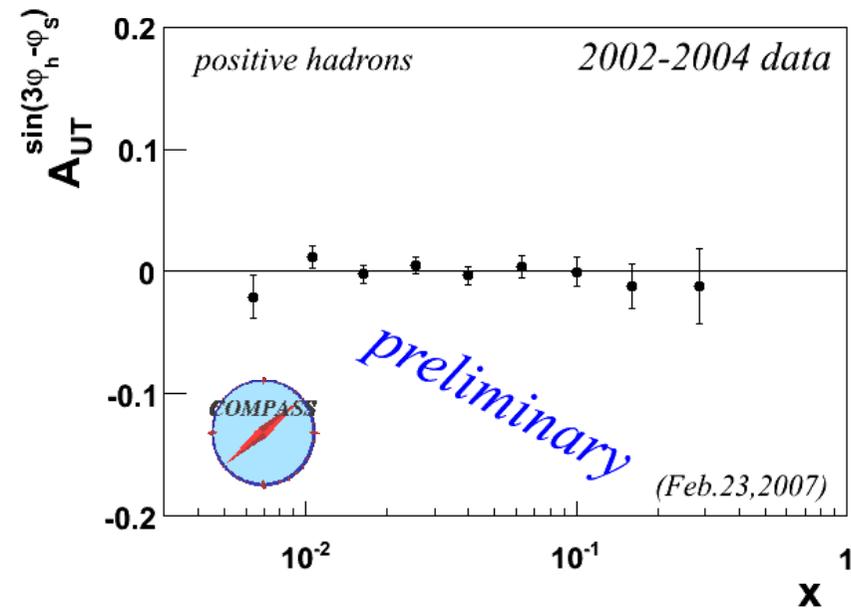
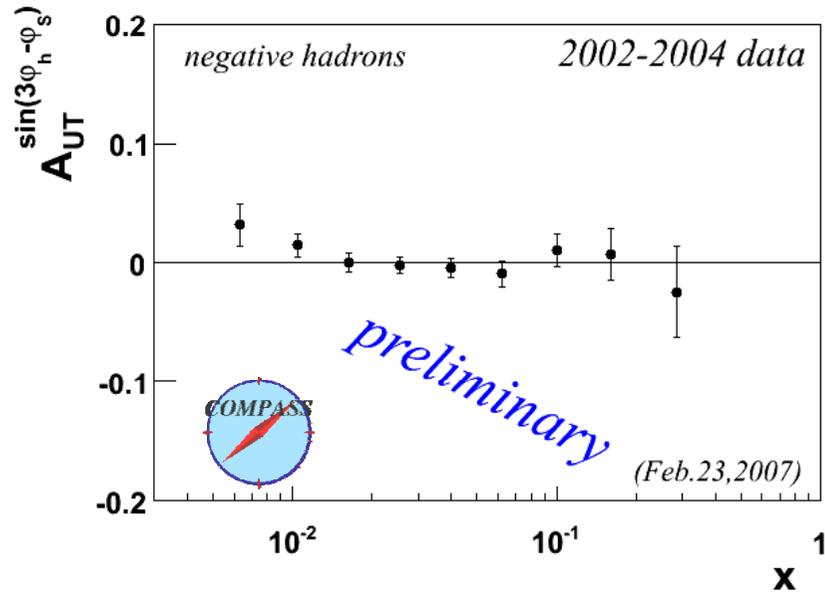


# target transverse spin dependent asymmetries (LO)

/1

$$F_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$$

$$F_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

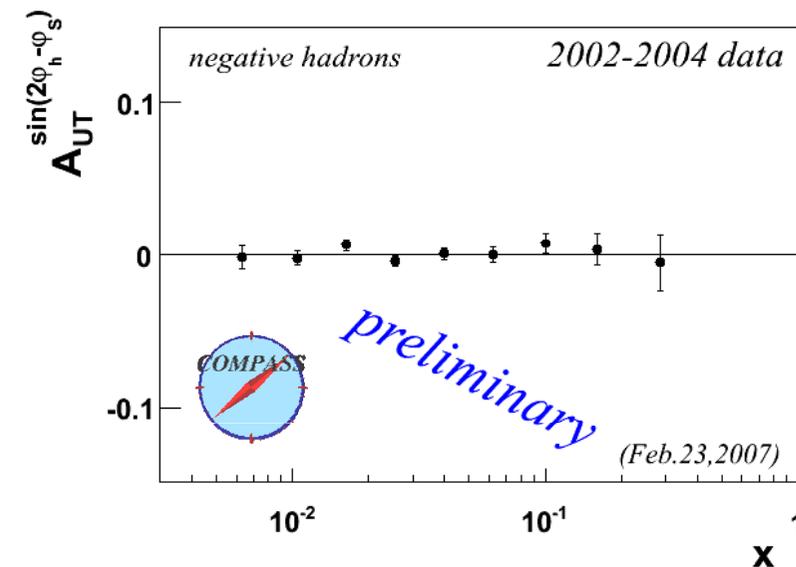
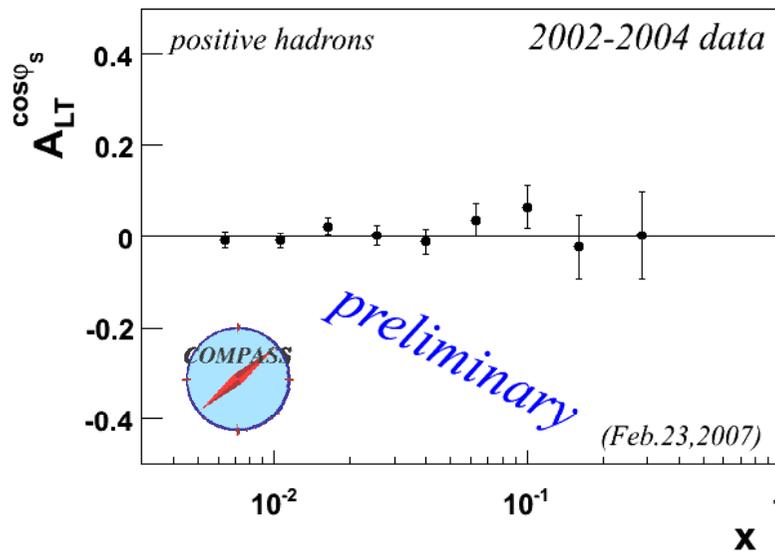
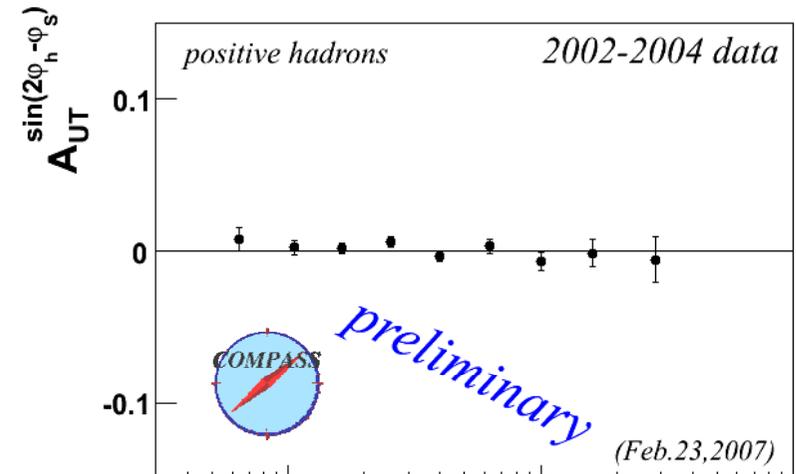
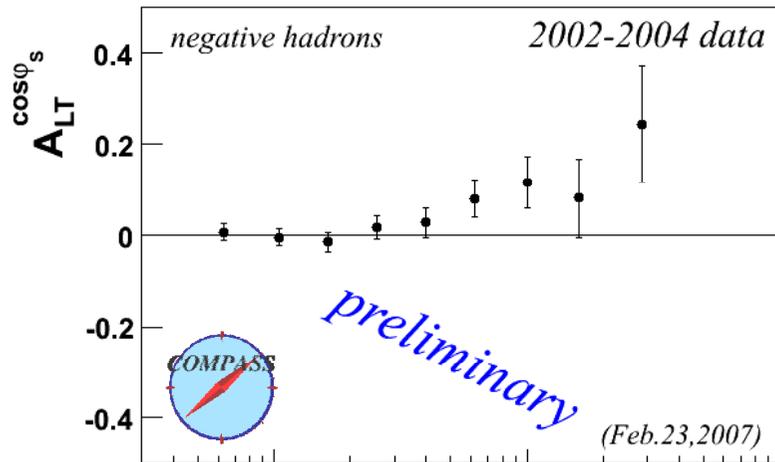


# target transverse spin dependent asymmetries

12

$$F_{LT}^{\cos(\phi_s)} \propto \frac{M}{Q} g_{1T}^q \otimes D_{1q}^h$$

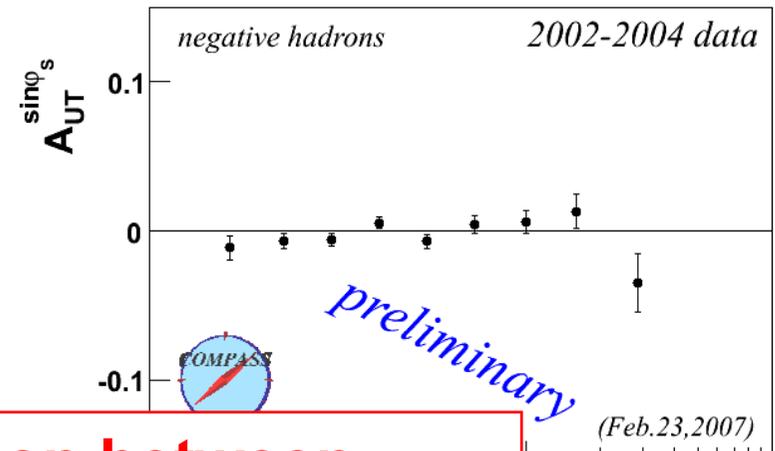
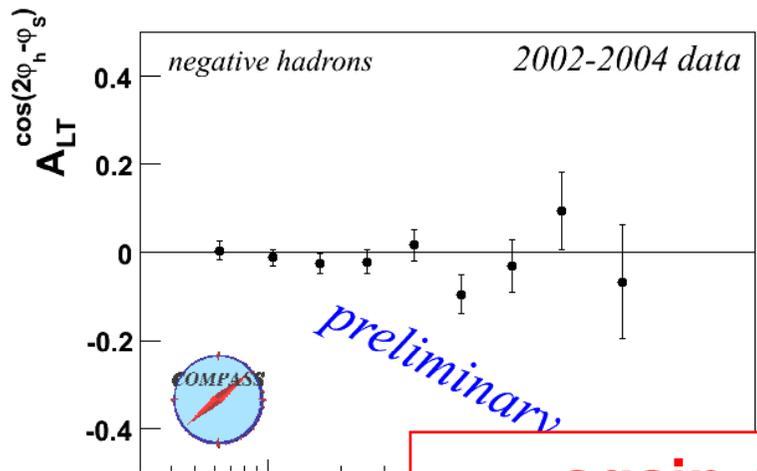
$$F_{LT}^{\cos(2\phi_h - \phi_s)} \propto \frac{M}{Q} g_{1T}^q \otimes D_{1q}^h$$



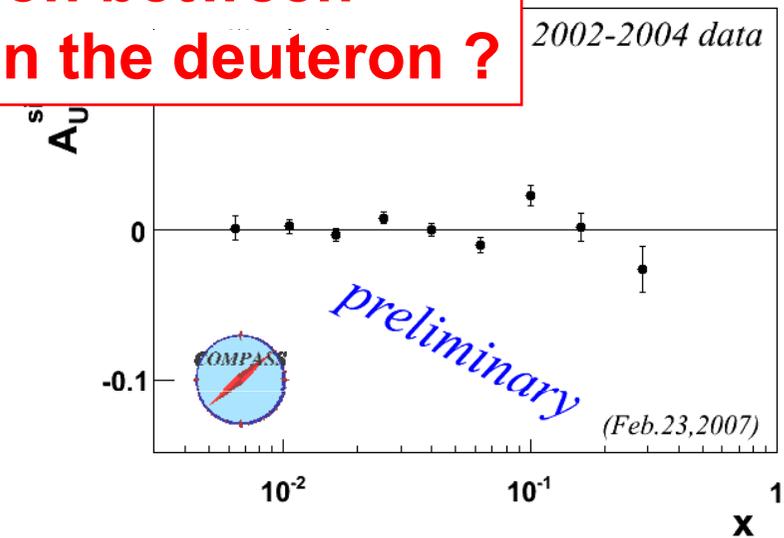
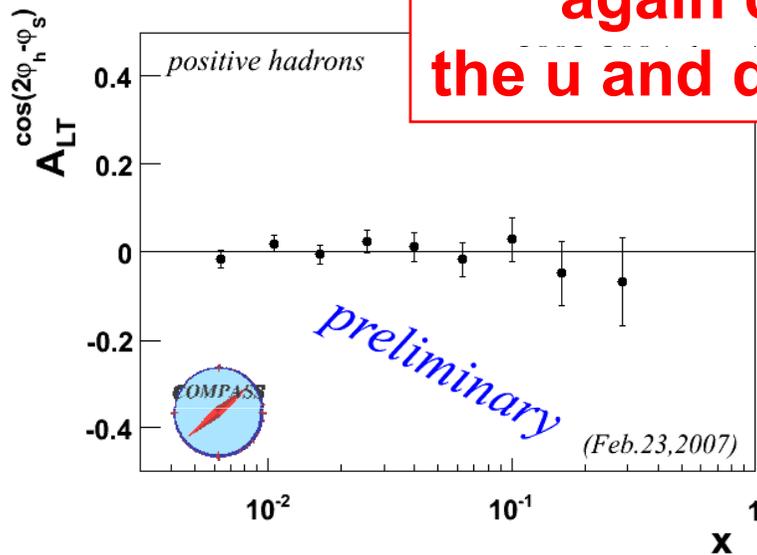
# target transverse spin dependent asymmetries

$$F_{UT}^{\sin(2\phi_h - \phi_s)} \propto \frac{M}{Q} \left( h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h \right)$$

$$F_{UT}^{\sin(\phi_s)} \propto \frac{M}{Q} \left( h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h \right)$$



**again cancellation between the u and d quarks in the deuteron ?**



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# summary

after many years of work,

since 2004 measurements of

- Collins asymmetries on p and d
- Collins FF in  $e^+e^-$  from Belle

} transversity DF

transversity DFs  $\neq 0$ , Collins FF  $\neq 0$ , a new property of matter

- 2hadron asymmetries on p and d
- $\Lambda$  polarisation on d

}

- Sivers asymmetries on p and d

Sivers DF  $\neq 0$ , a real effect

first extractions of the u and d quark DFs

- six more target transverse spin asymmetries have been measured on the deuteron

a complete description of the spin structure of the nucleon is emerging  
the work is starting now!



# summary 2

---

new SIDIS data are coming

very soon:

- new results from HERMES from 2005 data (factor 2 in statistics)

soon:

- $K^0$  asymmetries on deuteron from COMPASS
- exclusive  $\rho^0$  asymmetries on deuteron from COMPASS  $\rightarrow$  GPDs
- Cahn and Boer-Mulders asymmetries  $\rightarrow$  unpol
- proton asymmetries from COMPASS (the run is about to start)

afterwards, there should be:

- (neutron) data from JLab experiments
- further measurements at CERN (COMPASS2)

and

the measurements of Drell-Yan pairs in  $\pi p$  (COMPASS) and pbar-p (FAIR) scattering

*Oleg Denissov*

in addition to the transverse spin effects measurements in pp hard scattering at RHIC

*Christine Aidala*



**ALL IN ALL,**

**A HUGE EXPERIMENTAL EFFORT**

**and**

**A CHALLENGING GOAL FOR THEORY**

