

# $\Delta G$ from high $p_T$ events at COMPASS

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# COMPASS experiment

COMmon Muon and Proton Apparatus for Structure and Spectroscopy

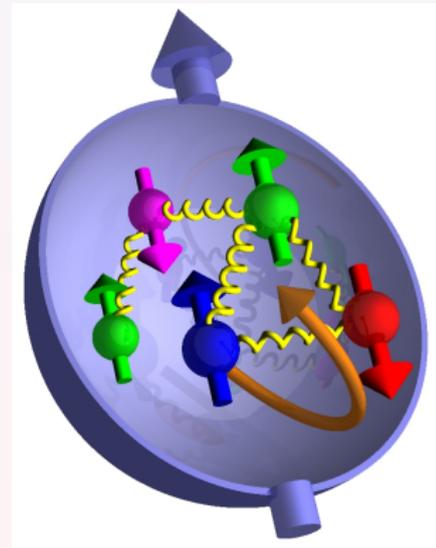


# Nucleon spin

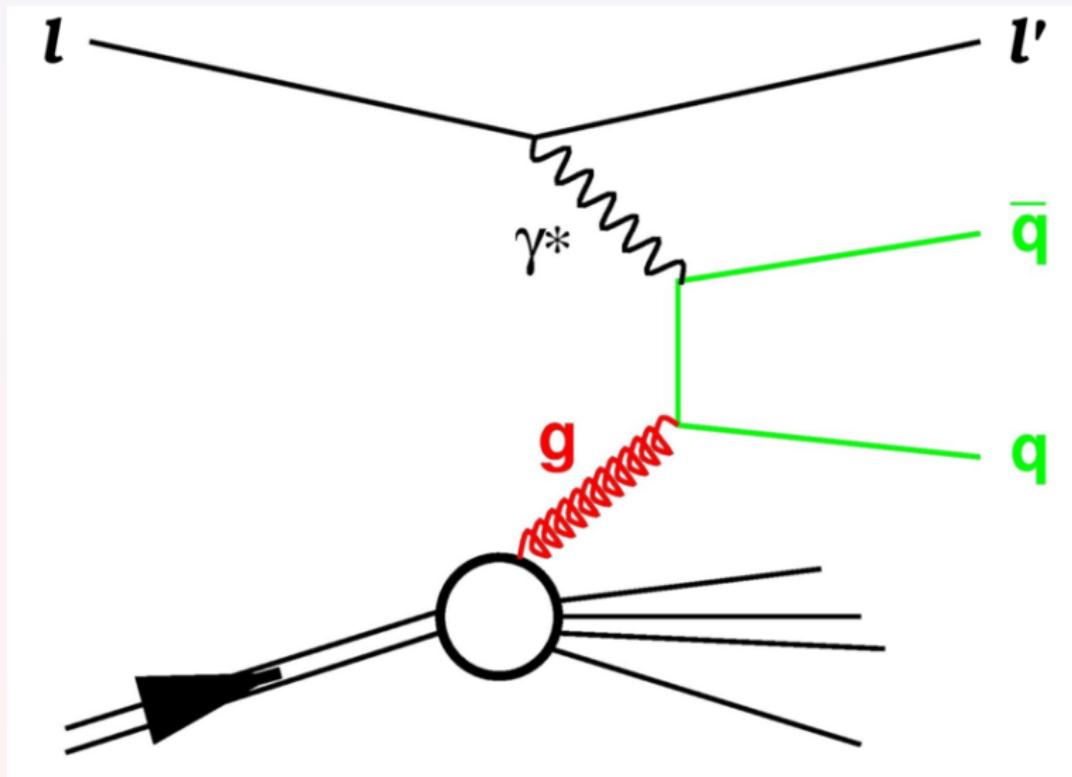
$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$

## "Spin Crisis"

- Only a small fraction of nucleon spin is carried by quarks  
 $\Delta\Sigma = 0.30 \pm 0.01(\text{stat.}) \pm 0.02(\text{evol.})$   
 (QCD NLO fits)
- How big is the contribution of gluons and orbital momentum?
- Precision of  $\Delta G$  determined from QCD fits is poor.
- Answer: directly measure polarization of the gluons and orbital momentum of partons.



# Photon Gluon Fusion - PGF



# Experimental asymmetry

- Extract asymmetry (asymmetries are sensitive to small effects):

$$A_{exp} = \frac{N_U - N_D}{N_U + N_D}$$



- One cell polarized parallel and one cell polarized antiparallel to the beam.
- Both cells exposed to same beam flux.
- Spectrometer acceptance is not the same for both cells.

## Experimental asymmetry

- Solution: reverse polarization every 8 hours.

$$A_{exp} = 1/2 \left( \frac{N_U - N_D}{N_U + N_D} + \frac{N'_D - N'_U}{N'_D + N'_U} \right)$$

- Experimental asymmetry is related to cross-section asymmetry:

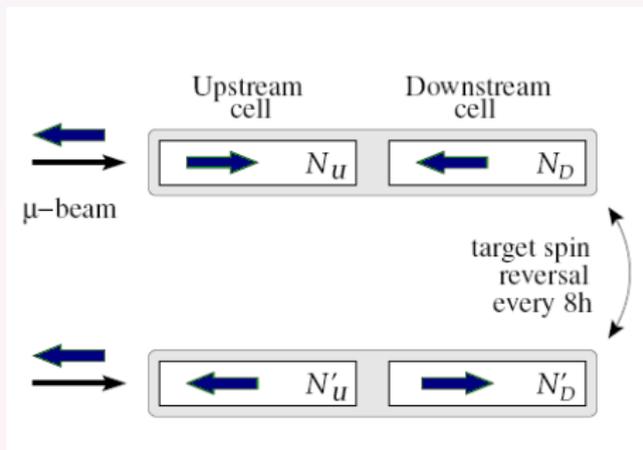
$$A_{exp} = P_T P_B f A_{||}$$

where:

$P_T$  - Target polarization  
 (measured with NMR probes)

$P_B$  - Beam polarization  
 (parametrization)

$f$  - dilution factor  
 (parametrisation)



# $\Delta G/G$ from PGF

$$A^{IN} \equiv A_{||} \equiv \frac{\Delta\sigma}{\sigma} \equiv \frac{\sigma^{\downarrow\uparrow} - \sigma^{\downarrow\downarrow}}{\sigma^{\downarrow\uparrow} + \sigma^{\downarrow\downarrow}}$$

- $\Delta\sigma = \Delta F \otimes \Delta\hat{\sigma} \otimes \tilde{D}$ ;  $\sigma = F \otimes \hat{\sigma} \otimes \tilde{D}$

$\Delta F, F$ :  $\Delta G, \Delta q, G, q$

$$\Delta q = \sum_f e_f^2 (\Delta q_f(x) + \Delta \bar{q}_f(x))$$

$$q = \sum_f e_f^2 (q_f(x) + \bar{q}_f(x))$$

$\Delta\hat{\sigma}, \hat{\sigma}$  - hard process cross-sections

$\tilde{D}$  - fragmentation functions

- $A_{||} = R_{sig} \langle a_{LL}^{sig} \rangle \frac{\Delta G}{G} + R_{bg} A_{bg}$

$R_i$  - fraction of process "i"

$$\langle a_{LL} \rangle = \langle \Delta\hat{\sigma}/\hat{\sigma} \rangle$$

$A_{bg}$  - background asymmetry

- To minimise statistical error a weighting method is used**

Events are weighted with  $w = fDP_B$  instead of using mean values

D - depolarisation factor of the virtual photon

$$\frac{A_{||}}{D} = -\frac{1}{2|P_t|} \left( \frac{\sum w_u - \sum w_d}{\sum w_u^2 + \sum w_d^2} - \frac{\sum w'_u - \sum w'_d}{\sum w'^2_u + \sum w'^2_d} \right)$$

$$\delta \left( \frac{A_{||}}{D} \right) = \frac{1}{2|P_t|} \sqrt{\frac{1}{\sum w_u^2 + \sum w_d^2} - \frac{1}{\sum w'^2_u + \sum w'^2_d}}$$

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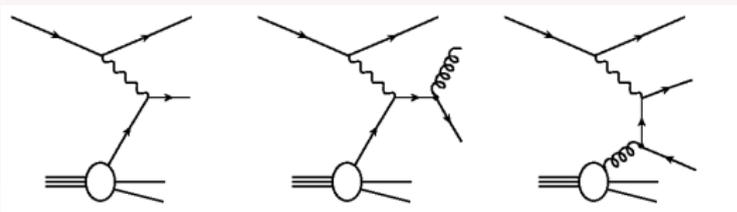
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## PGF selection

- Open charm production
  - $c\bar{c}$  production
  - hard scale set by  $4m_c^2$
  - no background asymmetry
  - limited statistics
- 2 high  $p_T$  hadrons ( $Q^2 > 1\text{GeV}^2$ )
  - hard scale set by  $Q^2$
  - large statistics
  - contamination by other processes
- 2 high  $p_T$  hadrons ( $Q^2 < 1\text{GeV}^2$ )
  - hard scale set by  $p_T$
  - very large statistics
  - contamination by other processes (resolved photon not negligible)

# High $p_T$ background processes

Contributing diagrams ( $Q^2 > 1 \text{ GeV}^2$ )



LP  
 Leading Process

QCDC  
 QCD Compton

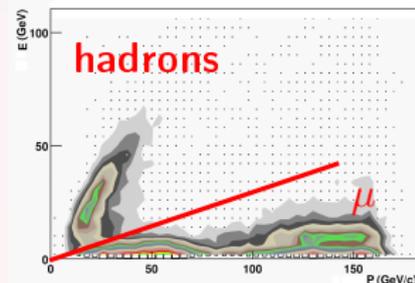
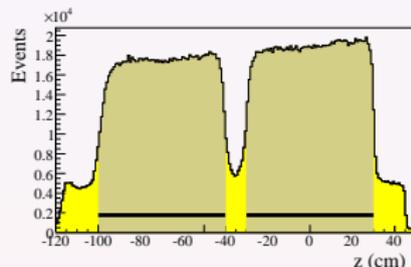
PGF  
 Photon Gluon  
 Fusion

- For Leading Process struck quark goes along photon direction
- $p_T$  of hadron in the final state is small
- Non zero  $p_T$  can originate from fragmentation or intrinsic  $p_T$  of quark
- Selection of events with high  $p_T$  suppresses Leading Process

## High $p_T$ selection

Event selection:

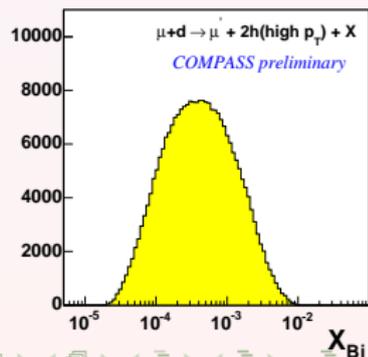
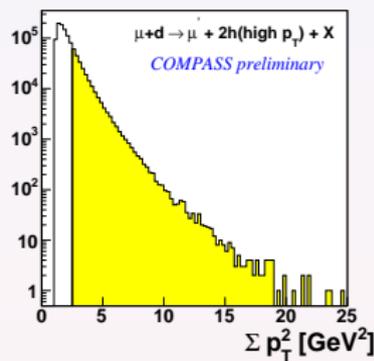
- Primary vertex is reconstructed within target volume.
- Extrapolated beam track goes through both target cells.
- Hadron identification
  - For hadron candidates that have an energy measurement in calorimeter:  $E_{cal}/p > 0.3$
  - Hadron candidates don't have associated clusters behind muon filters



# High $p_T$ selection

Kinematic cuts:

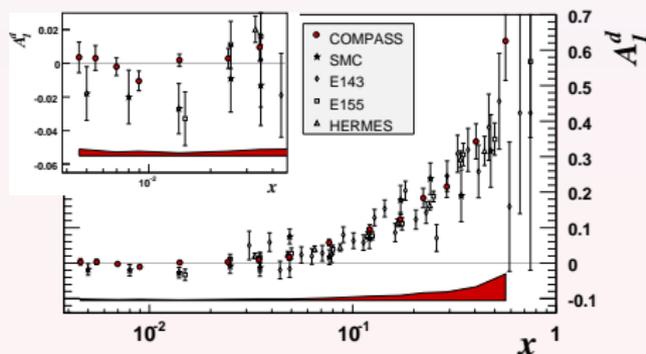
- Enhance PGF contribution also ensure factorisation for  $Q^2 < 1 \text{ GeV}^2$  sample:
  - $p_T > 0.7 \text{ GeV}$  (for both hadrons)
  - $\Sigma p_T^2 > 2.5 \text{ GeV}^2$
- $0.1 < y: Q^2 > 1 \text{ GeV}^2$   
 $0.35 < y: Q^2 < 1 \text{ GeV}^2$   
 - suppress region with low contribution to  $\Delta G/G$
- $y < 0.9$  - suppress region with large radiative corrections
- $x_F, z > 0.1$  : current fragmentation region
- $m(h_1, h_2) > 1.5 \text{ GeV}$  : remove  $\rho$  resonance



# High $p_T$ ( $Q^2 > 1 \text{ GeV}^2$ ): $\Delta G/G$ extraction

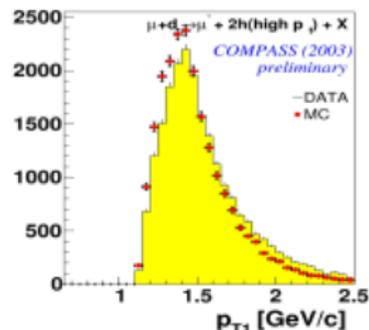
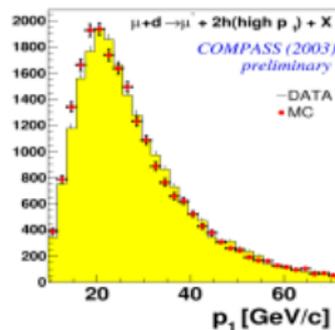
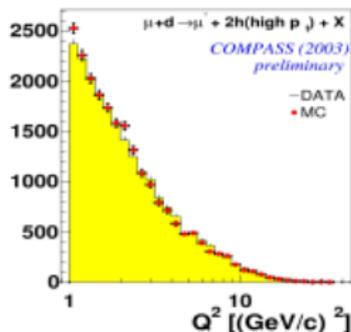
$$\frac{A_{||}}{D} = A_1 \left( \left\langle \frac{a_{LL}^{LP}}{D} \right\rangle R_{LP} + \left\langle \frac{a_{LL}^{QCDC}}{D} \right\rangle R_{QCDC} \right) + \frac{\Delta G}{G} \left\langle \frac{a_{LL}^{PGF}}{D} \right\rangle R_{PGF}$$

- For region  $x < 0.05$   $A_1$  is small - we can neglect contribution from LP and QCDC (included in systematic error)
- $R_{PGF}$  - fraction of PGF events - determined from MC simulations



## High $p_T$ ( $Q^2 > 1 \text{ GeV}^2$ ): Monte Carlo

- Monte Carlo generator: LEPTO
- Reasonable agreement with data



## High $p_T$ ( $Q^2 > 1 \text{ GeV}^2$ ): result

- Result based on data collected in 2002-2003:

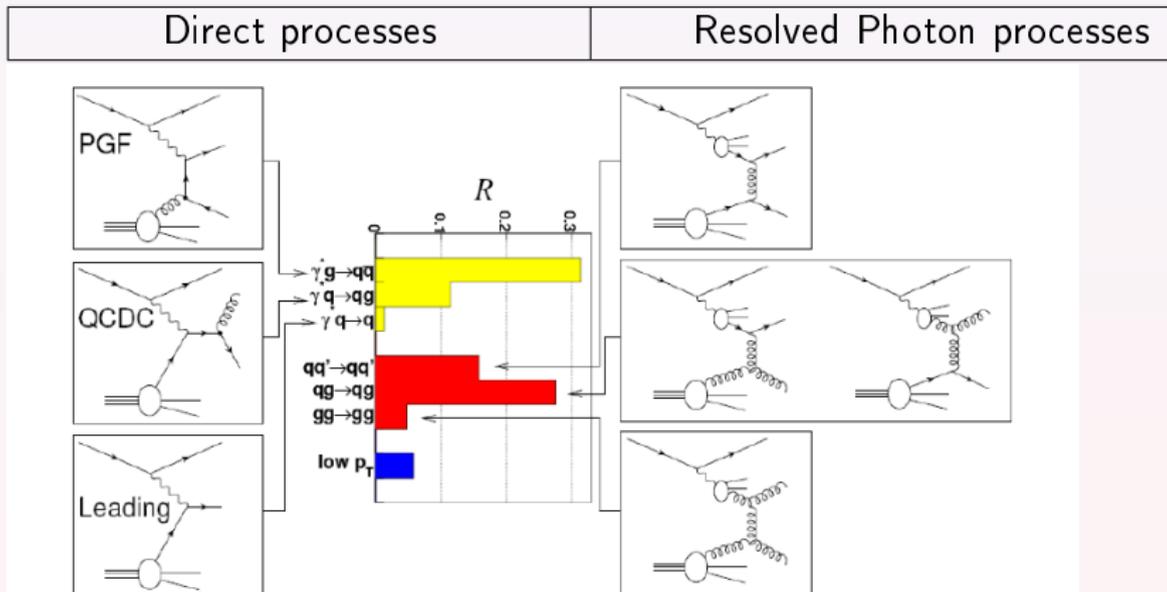
$$\frac{\Delta G}{G} = 0.06 \pm 0.31(\text{stat.}) \pm 0.06(\text{syst.})$$

$$R_{PGF} = 0.34 \pm 0.7$$

$$\langle x_g \rangle = 0.13$$

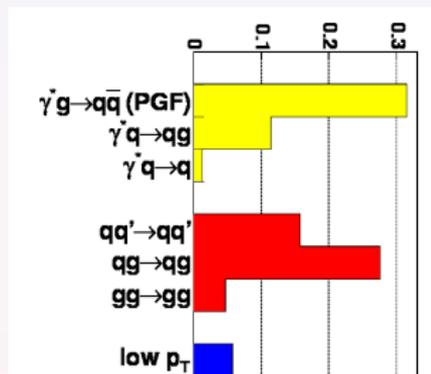
- Analysis of 2004 and 2006 data ongoing.
- We are working on methods to improve sample selection.

# High $p_T$ ( $Q^2 < 1 \text{ GeV}^2$ ): additional processes



# High $p_T$ ( $Q^2 < 1 \text{ GeV}^2$ ): additional processes

$$\begin{aligned}
 A_{\parallel}/D &= R_{PGF} \left\langle \frac{a_{LL}^{PGF}}{D} \right\rangle \frac{\Delta G}{G} \\
 &+ R_{QCDC} \left\langle \frac{a_{LL}^{QCDC}}{D} \right\rangle A_1 \\
 &+ R_{qq} \left\langle \frac{a_{LL}^{qq}}{D} \right\rangle \frac{\Delta q}{q} \frac{\Delta q^\gamma}{q^\gamma} \\
 &+ R_{qg} \left\langle \frac{a_{LL}^{qg}}{D} \right\rangle \frac{\Delta q}{q} \frac{\Delta G^\gamma}{G^\gamma} \\
 &+ R_{gq} \left\langle \frac{q}{D} \right\rangle \frac{\Delta G}{G} \frac{\Delta q^\gamma}{q^\gamma} \\
 &+ R_{gg} \left\langle \frac{a_{LL}^{gg}}{D} \right\rangle \frac{\Delta G}{G} \frac{\Delta G^\gamma}{G^\gamma}
 \end{aligned}$$



- $R_i$  - process fraction (MC).
- $a_i$  - hard process asymmetry (QCD).
- $A_1$ ,  $q$ ,  $\Delta q$  - parton distributions in the nucleon (parametrisation).
- $q^\gamma$ ,  $G^\gamma$  - unpolarised PDFs in photon (parametrisation).
- $\Delta q^\gamma$ ,  $\Delta G^\gamma$  - polarised PDFs in photon (min-max scenario).

## High $p_T$ ( $Q^2 < 1 \text{ GeV}^2$ ): Parametrisations

- $A_1$  - parametrisation based on the E143 and SMC data.
- $q$ ,  $\Delta q$  - parametrisations GRV98LO and GRSV2000 respectively.
- $q^\gamma$ ,  $G^\gamma$  - parametrisation by *Glück, Reya, and Schienbein* [Phys. Rev. **D60**, 054019]
- $\Delta q^\gamma$ ,  $\Delta G^\gamma$ - can be decomposed into two terms:

$$\Delta f^\gamma = \Delta f_{VMD}^\gamma + \Delta f_{pl}^\gamma$$

$\Delta f_{pl}^\gamma$  - photon fluctuates into  $q\bar{q}$  pair  
 - term calculable in QCD + QED

$\Delta f_{VMD}^\gamma$  - photon fluctuates into a vector meson  
 - this term is non perturbative.

We can only estimate it via max-min scenarios:

$$-f_{VMD}^\gamma < \Delta f_{VMD}^\gamma < f_{VMD}^\gamma$$

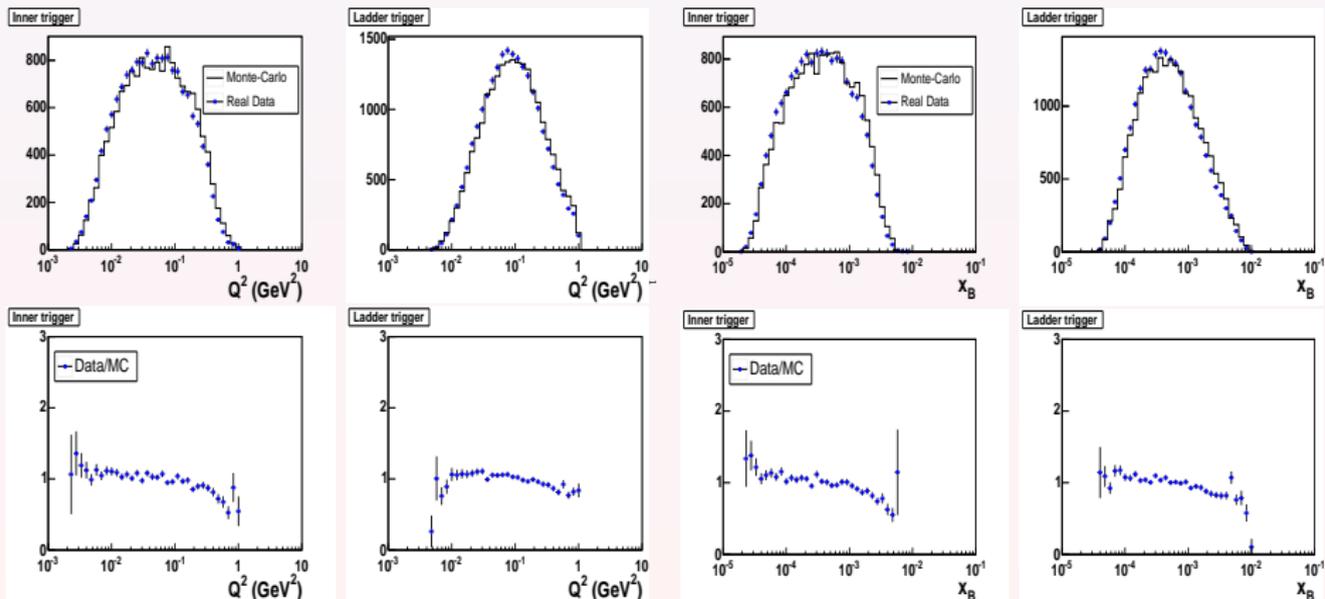
Unpolarised distribution are constrained by data.

[Ref: *Glück, Reya, and Sieg*, Eur. Phys. J. **C20**, 271-281]

# High $p_T$ ( $Q^2 < 1 \text{ GeV}^2$ ): Monte Carlo

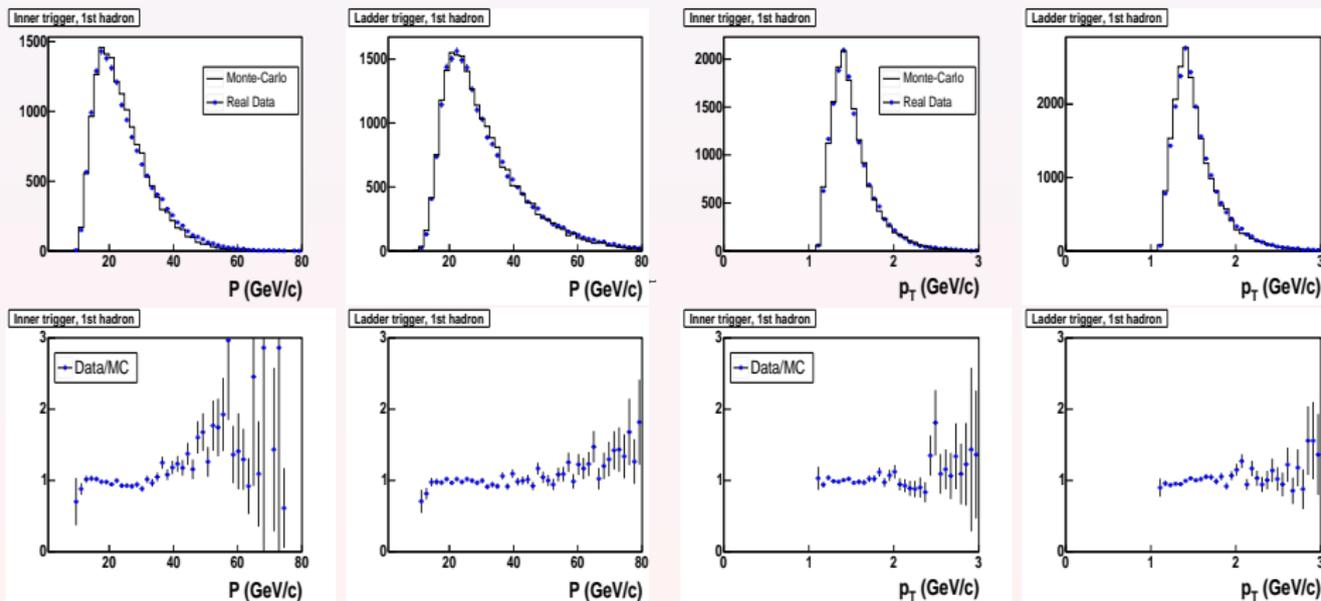
Monte Carlo generator: PYTHIA (GRV98LO)

Agreement between Real Data (blue points) and Monte Carlo



# High $p_T$ ( $Q^2 < 1 \text{ GeV}^2$ ): Monte Carlo (*cont'd*)

Intrinsic  $k_T^\gamma$  in the resolved photon was tuned to obtain agreement in  $p$  and  $p_T$  for both leading and second hadrons.



## High $p_T$ ( $Q^2 < 1 \text{ GeV}^2$ ): systematics

### Main contributions to systematic errors

- False asymmetries (experimental systematics): 0.014
- Resolved photon contribution (min - max scenario): 0.013
- Monte Carlo: 0.052

- False Asymmetries (FA) can be decomposed into:

- Reproducible FA - appears if properties of the apparatus depend on the sign of solenoid field.

- Almost completely cancelled out thanks to two MW settings:

$$A_{\text{rep}} = \frac{1}{2}(A_+ - A_-); \quad A_{\text{R}} = A_{\text{rep}} \times \frac{(a_+)^2 - (a_-)^2}{(a_+)^2 + (a_-)^2}$$

- Random FA - originate from random fluctuation.

- Estimated using "pulls" method on large number of data groups, after correction for  $A_{\text{rep}}$ .

- Systematic FA - eg. efficiency of a detector degrades in time.

- Constant on-line monitoring during data taking.

- Can be decomposed into  $A_{\text{rep}}$  and  $A_{\text{R}}$ .

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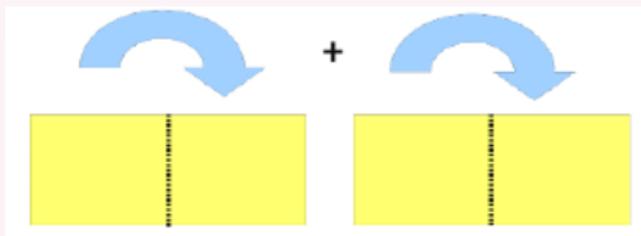
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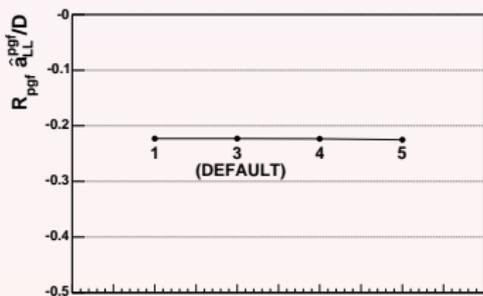
## High $p_T$ ( $Q^2 < 1 \text{ GeV}^2$ ): systematics

- False asymmetries (*cont'd*)
  - Studied on low  $p_T$  sample:  $\sim 250 \otimes$  more statistics
  - Considered scenarios:
    - Microwave setting “+” vs “-”
    - Upper vs Lower part of spectrometer
    - Left vs Right part of the spectrometer
    - Asymmetries within one target cell

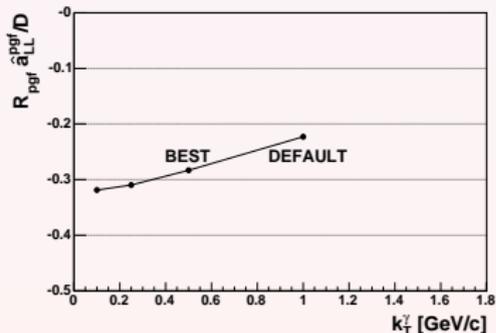
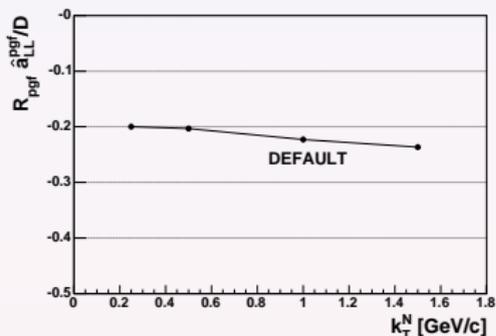


# High $p_T$ ( $Q^2 < 1 \text{ GeV}^2$ ): MC systematics

- MC parameters were varied in a range with reasonable Data/MC agreement:
  - parton fragmentation
  - $k_T$  of partons in nucleon and in photon
  - renormalisation and factorisation scales
  - parton showers

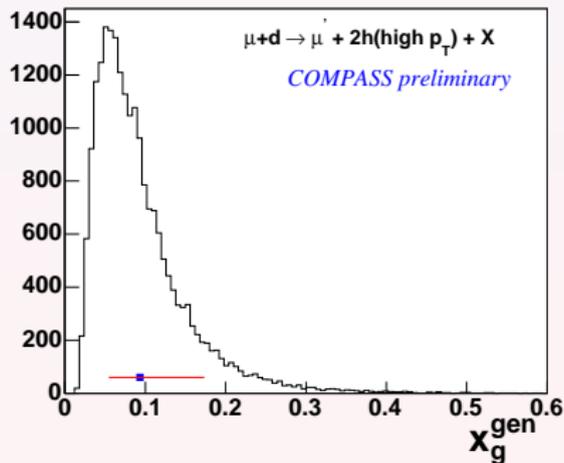


Fragmentation tuning



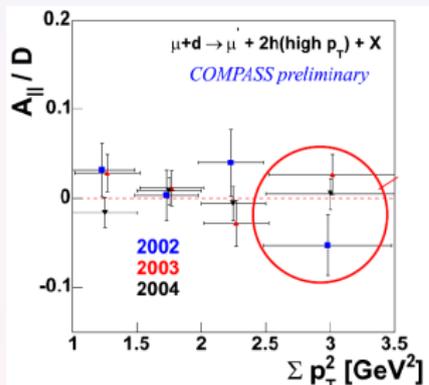
## High $p_T$ ( $Q^2 < 1 \text{ GeV}^2$ ): estimation of $x_g$

- $x_g$  estimated using MC.
- Each process probes  $\Delta G/G$  at different  $x_g$ .
- Contributions from processes are weighted by sensitivity to  $\Delta G/G$ .



$$x_g \approx 0.085^{+0.071}_{-0.035} \text{ (RMS 0.8)}$$

# High $p_T$ ( $Q^2 < 1 \text{ GeV}^2$ ): result



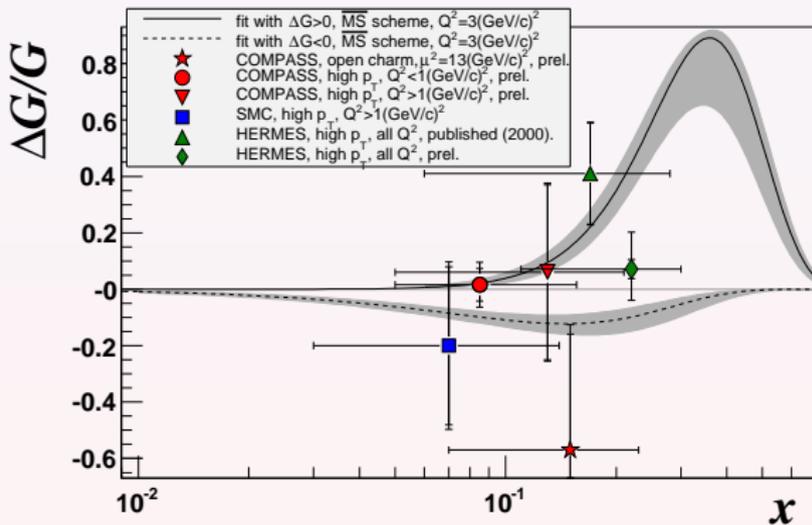
- 2002-2003 data (PLB 633 (2006) 25-32)  
 $\frac{\Delta G}{G} = 0.024 \pm 0.089(\text{stat.}) \pm 0.057(\text{syst.})$
- 2004 data:  
 $\frac{\Delta G}{G} = 0.015 \pm 0.077(\text{stat.}) \pm 0.056(\text{syst.})$

- Preliminary result based on 2002-2004 data:

$$\frac{\Delta G}{G} = 0.016 \pm 0.058(\text{stat.}) \pm 0.055(\text{syst.})$$

- $x_g \approx 0.085^{+0.071}_{-0.035}$  (RMS 0.8)
- Scale  $3\text{GeV}^2$

# $\Delta G/G$



## QCD fits:

- Lines obtained from NLO QCD fits including a new COMPASS deuteron results on  $g_1^d$  (PLB 647 (2007) 8-17).
- Two equally good solutions for  $\Delta G/G$  were found. For both  $|\Delta G| = 0.2 - 0.3$ .

## Prospects

- 2006 and 2007 data to be analysed
- Increased statistics in 2006 and 2007 due to new COMPASS magnet
- 2004 data for High  $p_T$  ( $Q^2 > 1 \text{ GeV}^2$ ) sample is being analysed
- Usage of neural networks is studied as a tool for selecting PGF events

## Summary

- Recent results of  $\Delta G/G$  from COMPASS were presented
- Present measurements indicate that  $\Delta G/G$  is consistent with zero at  $x_g \approx 0.1$
- We are working on further analysis and hope to show new results with even better precision in near future
- Measurement of orbital momentum of partons in nucleon is needed to solve “nucleon spin puzzle”