

# COMPASS Results on Pion and Kaon Multiplicities from SIDIS on Proton Target

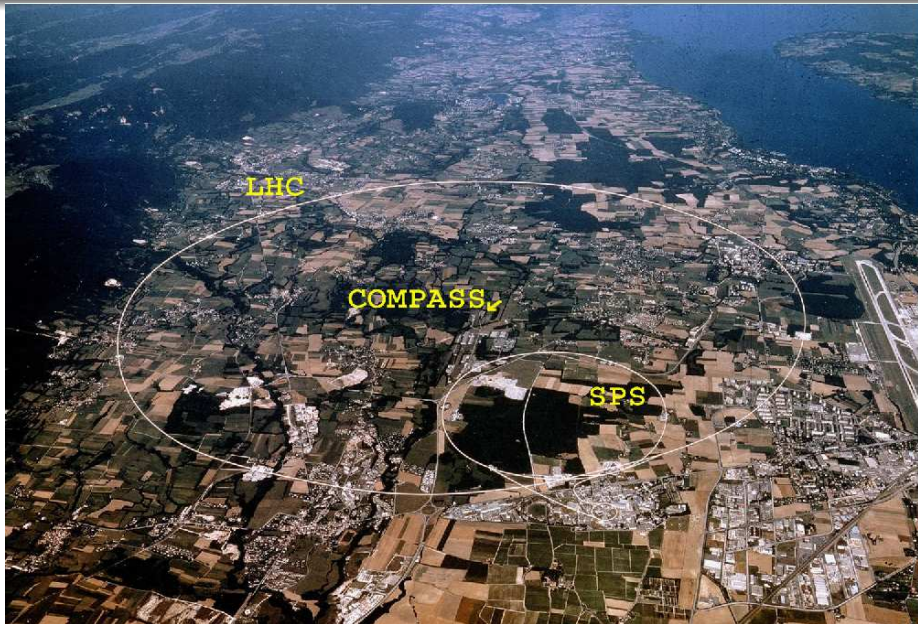
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LIP

On behalf of the COMPASS Collaboration

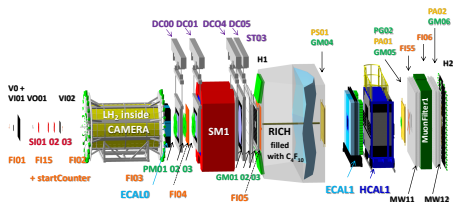
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# COMPASS at CERN



# COMPASS Spectrometer 2016



- COLLABORATION

- about 210 physicists
- 27 institutes

- DETECTOR

- two stage spectrometer
- 60 m length
- about 350 detector planes

- TARGET

- Liquid H target
- 250 cm - total length

- BEAM

- $\mu^\pm$  at 160 GeV/c

- FEATURES

- angular acceptance:  $\pm 180$  mrad
- track reconstruction:  
 $p > 0.5$  GeV/c
- identification  $h, e, \mu$ : calorimeters and muon filters
- identification:  $\pi, K, p$  (RICH)  
 $p > 2, 9, 18$  GeV/c respectively

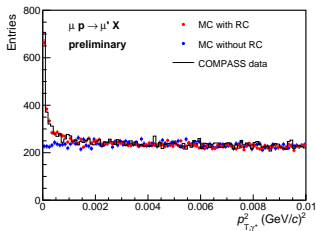
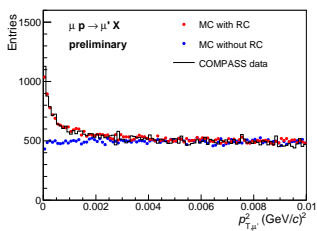
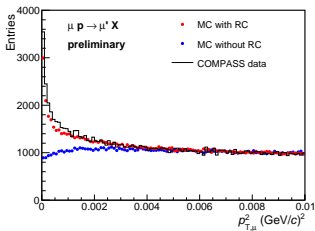
- Fragmentation functions ( $FF(s)$ ,  $D_q^h$ ) describe parton fragmentation into hadrons
- FFs are needed in analyses which deal with a hadron(s) in the final state
- In Leading Order QCD  $D_q^h$  describes probability density for a quark of flavour  $q$  to fragment into a hadron of type  $h$
- The cleanest way to access FFs is in  $e^+e^-$  annihilation. However,
  - only sensitive to the sum of  $q + \bar{q}$  fragmentation
  - flavour separation possibilities are limited
- In the SIDIS ( $\mu^\pm + p \rightarrow \mu^{\pm'} + h + X$ ) data, FF are convoluted with PDFs. However,
  - possibility to separate fragmentation from  $q$  and  $\bar{q}$
  - full flavour separation possible
- By studying  $pp$  collisions with high  $p_T$  hadrons, access to gluon fragmentation functions
- SIDIS data are crucial to understand quark fragmentation process

# Multiplicity Measurement

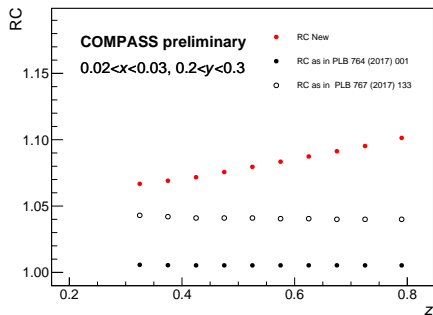
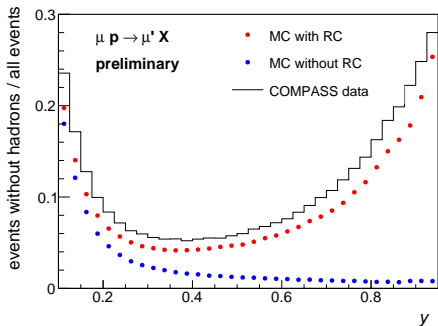
- Fragmentation studies in SIDIS can be done using hadron multiplicity data
- Hadron multiplicities are defined as number of observed hadrons per DIS event
- $$\frac{dM^h(x,z,Q^2)}{dz} = \frac{d^3\sigma^h(x,z,Q^2)/dx dQ^2 dz}{d^2\sigma^{DIS}(x,Q^2)/dx dQ^2}$$
- Experimentally measured hadron multiplicities need to be corrected for various effects e.g.
  - spectrometer acceptance and reconstruction program efficiency
  - RICH efficiency and purity (for  $\pi$  and  $K$ )
  - radiative corrections
  - diffractive vector meson production
- COMPASS already published several articles based on isoscalar target data
  - PLB 764 (2017) 001
  - PLB 767 (2017) 133
  - PRD 97 (2018) 032006
  - PLB 786 (2018) 390
  - PLB 807 (2020) 135600
- Today, preliminary results from the proton target are presented

# Radiative Corrections

- Correction due to radiative effects is a multiplicative factor to the multiplicity itself, and can be large, especially at low  $x$  and high  $y$
- The DJANGO program is used for RC simulations
- It was tested against COMPASS data and the TERAD program
- Some early results were shown already in 2019



# Radiative Corrections cont.



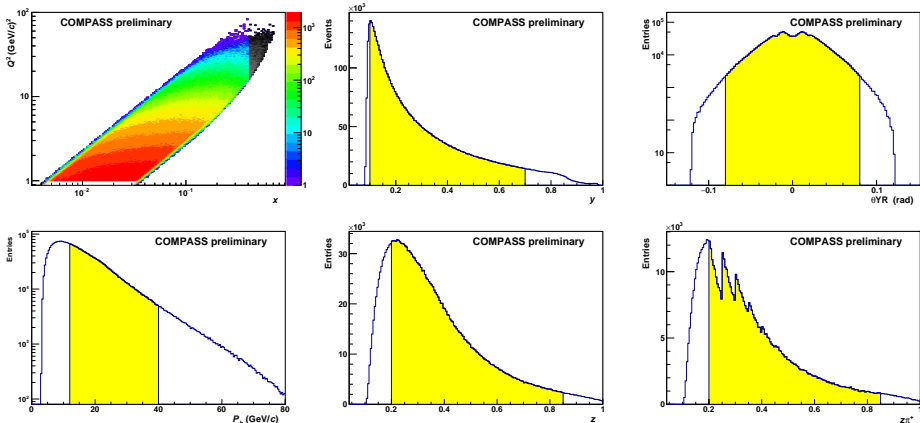
- COMPASS was always showing results with and without our estimate for RC
- Thus, new results can be easily implemented to older COMPASS multiplicity papers
- Note: according to our present knowledge the data from PLB 764 (2017) 001 ( $\pi^\pm, h^\pm$ ) need correction sometimes above 10%

# Data Selection - Main Cuts

- DIS selection:
  - Reconstructed  $\mu$  and  $\mu'$ ,
  - $Q^2 > 1 \text{ (GeV/c)}^2$
  - $W > 5 \text{ GeV/c}^2$ ,
  - $0.1 < y < 0.7$ , fraction of beam energy,  $E$ , carried by virtual gamma
- Hadron cuts:
  - $0.2 < z < 0.85$ , fraction of the virtual photon energy carried by a hadron
  - $12 \text{ GeV/c} < p < 40 \text{ GeV/c}$ , momentum cut due to RICH PID acceptance,
  - $\theta < 0.12$ ,  $|dy/dz| < 0.08$ , RICH acceptance
- Analysis is performed in 9 bins of Bjorken  $x$ , 5 bins of  $y$  and 12 bins of  $z$
- To avoid the "zero-acceptance" region, DIS sample is bin-by-bin restricted using
  - $\nu_{max} = \frac{\sqrt{p_{max}^2 + m_h^2}}{z_{max}}$ ,
  - $\nu_{min} = \frac{\sqrt{p_{min}^2 + m_h^2}}{z_{min}}$ ,
    - where  $\nu = E - E'$ ,
    - $p_{min} = 12 \text{ GeV/c}$  and  $p_{max} = 40 \text{ GeV/c}$ ,
    - $z_{min}$  and  $z_{max}$  - correspond to the edges of a given bin in  $z$  variable.



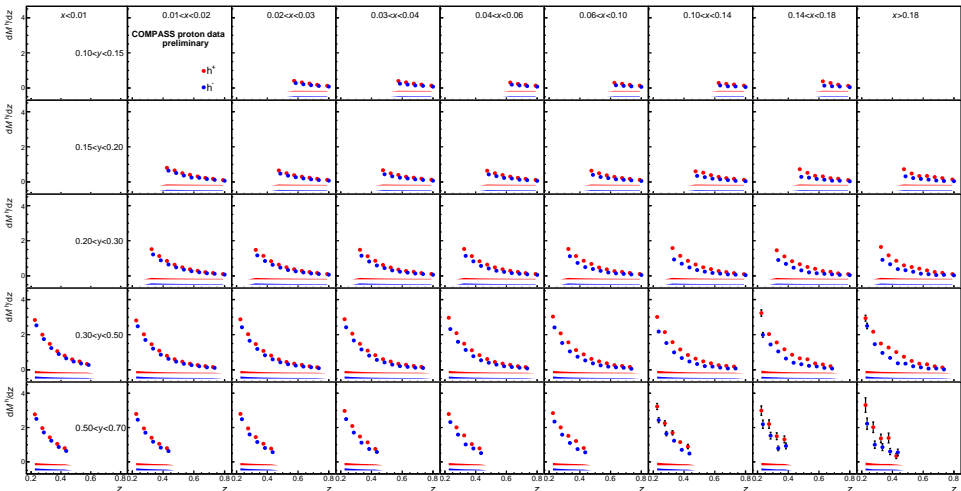
# Kinematic Distributions



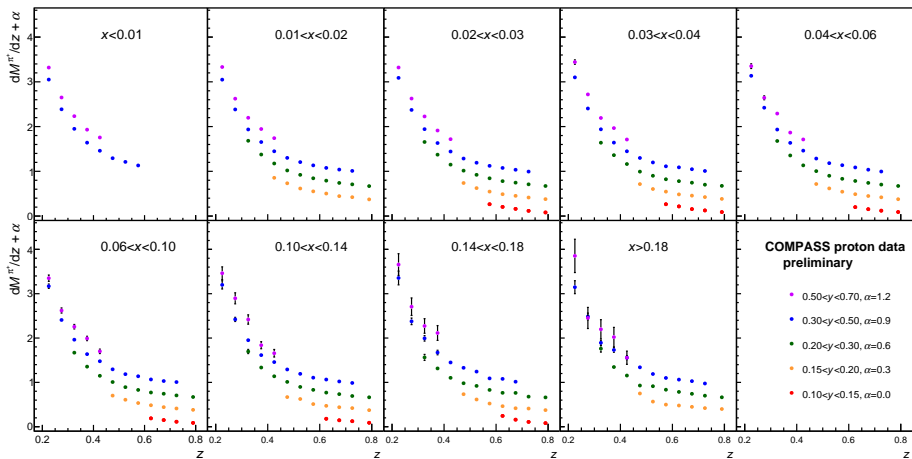
- The bottom right plot shows the impact of the  $\nu$  cuts on  $z$  distribution
- Total sample of events:
  - DIS: 5.5M
  - unidentified hadrons: 1.7M ( $\pi$ : 1.3M, K: 280k)

# RESULTS

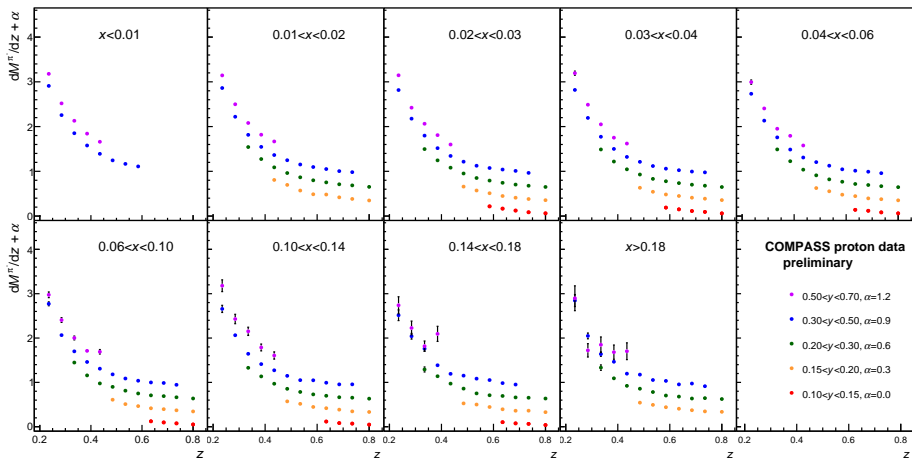
# Multiplicities of Unidentified Hadrons



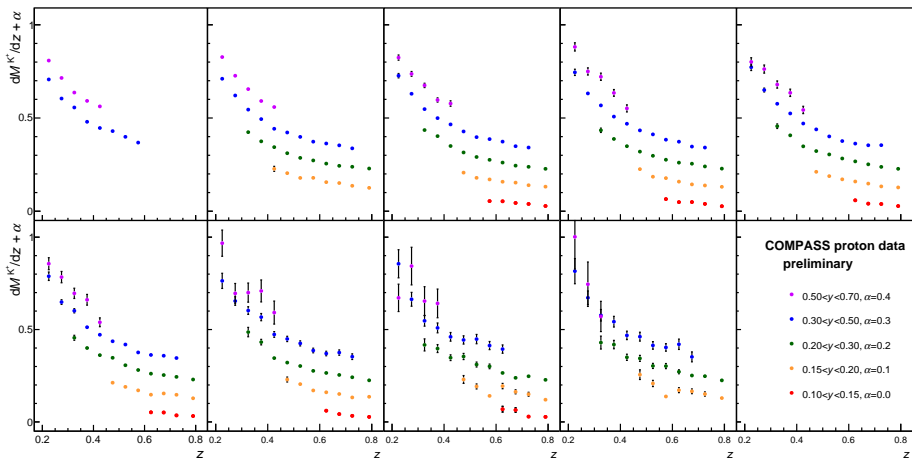
# Multiplicities of $\pi^+$



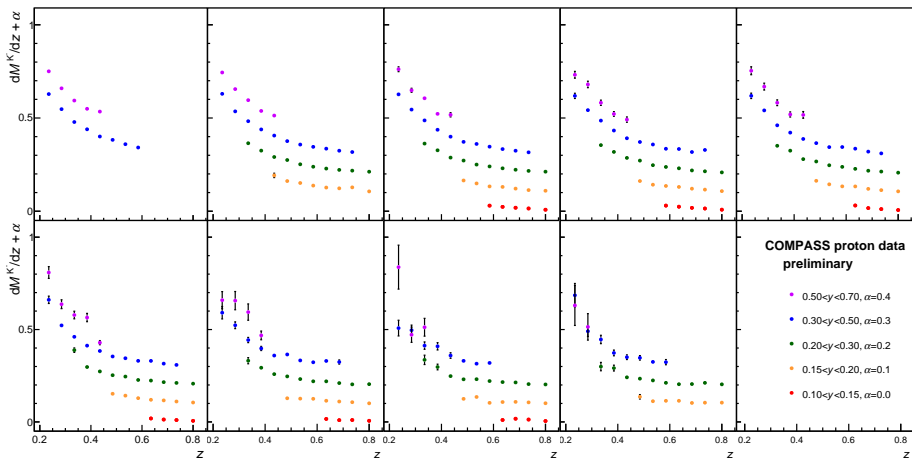
# Multiplicities of $\pi^-$



# Multiplicities of $K^+$

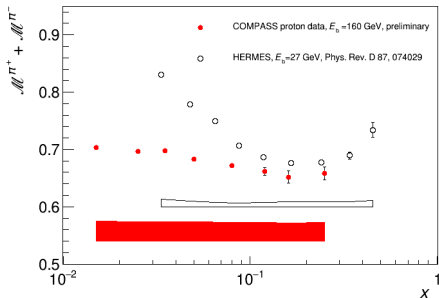
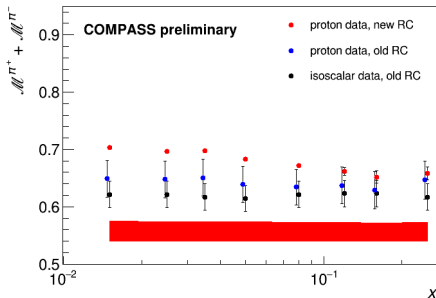


# Multiplicities of $K^-$



# Sum of Pion Multiplicities

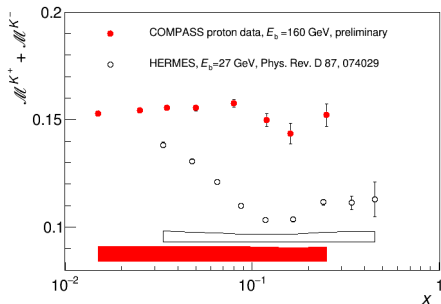
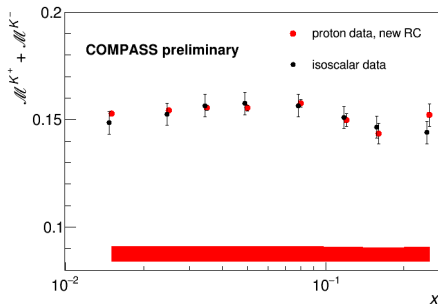
- Let  $D_{fav,(unf)} = D_q^h$  where  $q$  is (not) the valence quark of  $h$ , in LO pQCD:
- For proton target in LO pQCD:
  - $\frac{dM^{\pi^+}}{dz} + \frac{dM^{\pi^-}}{dz} = D_{fav} + D_{unf} - \frac{s+\bar{s}}{4u+4\bar{u}+d+\bar{d}+s+\bar{s}}(D_{fav} - D_{unf}) \approx D_{fav} + D_{unf}$
- For isoscalar target in LO pQCD:
  - $\frac{dM^{\pi^+}}{dz} + \frac{dM^{\pi^-}}{dz} = D_{fav} + D_{unf} - \frac{2(s+\bar{s})}{5(u+\bar{u}+d+\bar{d})+2(s+\bar{s})}(D_{fav} - D_{unf}) \approx D_{fav} + D_{unf}$
- Results for proton and isoscalar targets are expected to be very similar
- $D(Q^2, z) \rightarrow$  obtained from multiplicity sum is effectively independent of  $x$
- $\mathcal{M}^{\pi^+} + \mathcal{M}^{\pi^-} = \int_{0.2}^{0.85} \left( \frac{dM^{\pi^+}}{dz} + \frac{dM^{\pi^-}}{dz} \right) dz$



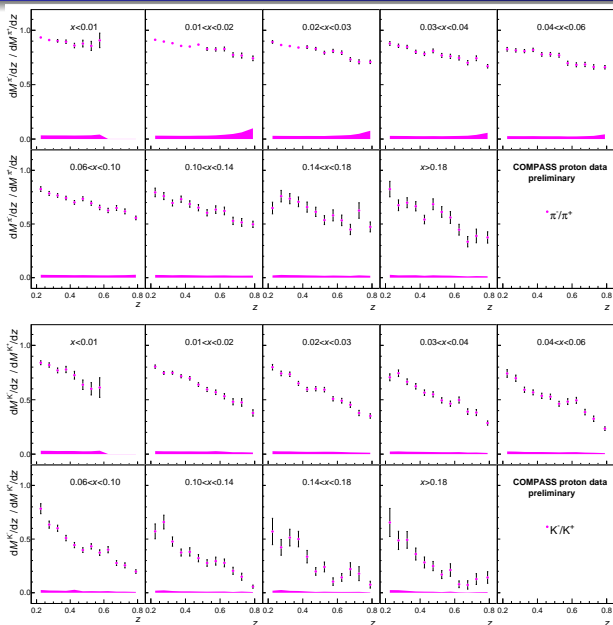


# Sum of Kaon Multiplicities

- Contrary to pion case, here  $D_s^{K^-}$ ,  $D_{\bar{s}}^{K^+}$  are dominant, larger than e.g.  $D_u^{K^+}$
- Since there are not too many  $s, \bar{s}$  at high  $x$ , we should see some turn-on effect related to the increased density of strange quark PDFs at lower  $x$
- Perhaps  $x$  values accessed by COMPASS is too low to assure low density of  $s, \bar{s}$
- $\mathcal{M}^{K^+} + \mathcal{M}^{K^-} = \int_{0.2}^{0.85} \left( \frac{dM^{K^+}}{dz} + \frac{dM^{K^-}}{dz} \right) dz$



# Multiplicity Ratios $\pi^-/\pi^+$ and $K^-/K^+$



# Multiplicity Ratios $K^-/K^+$ and $\bar{p}/p$ from Isoscalar Target

- In the multiplicity ratio a lot experimental and theoretical uncertainties cancel
- In LO pQCD one can calculate a lower limit for the ratio

$$R_K(x, Q^2, z) = \frac{dM^{K^-}(x, Q^2, z)/dz}{dM^{K^+}(x, Q^2, z)/dz} = \frac{4(\bar{u}+\bar{d})D_{fav} + (5u+5d+\bar{u}+\bar{d}+s+\bar{s})D_{unf} + (s+\bar{s})D_{str}}{4(u+d)D_{fav} + (5\bar{u}+5\bar{d}+u+d+s+\bar{s})D_{unf} + (s+\bar{s})D_{str}}$$

$$R_p(x, Q^2, z) = \frac{dM^{\bar{p}}(x, Q^2, z)/dz}{dM^p(x, Q^2, z)/dz} = \frac{(5\bar{u}+5\bar{d})D_{fav} + (5u+5d+2s+2\bar{s})D_{unf}}{(5u+5d)D_{fav} + (5\bar{u}+5\bar{d}+2s+2\bar{s})D_{unf}}$$

- $D_{unf}$  is expected to be small at large  $z$ , thus can be neglected

$$R_K = \frac{4(\bar{u}+d)D_{fav} + (s+\bar{s})D_{str}}{4(u+d)D_{fav} + (s+\bar{s})D_{str}}$$

$$R_p = \frac{\bar{u}+\bar{d}}{u+d}$$

- since  $(s+\bar{s})D_{str}$  is positive, it can also be neglected for the **lower limit calculation**

$$R_K > \frac{\bar{u}+\bar{d}}{u+d}$$

$$R_p > \frac{\bar{u}+\bar{d}}{u+d}$$

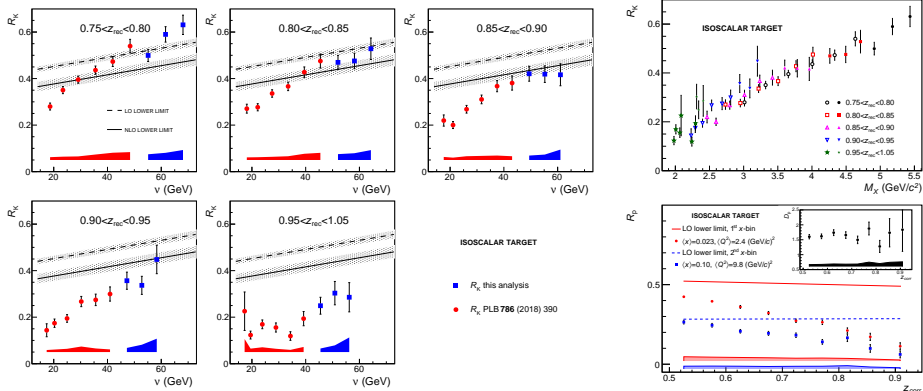
- The lower limits predicted by LO pQCD for  $R_K$  and  $R_p$  are the same

- $R_K$  expected to be 10-15% higher than  $R_p$  because of  $D_{str}$

- $R_\pi$  suffers from large contamination of decay products of diffractive  $\rho^0$

# Multiplicity Ratios $K^-/K^+$ and $\bar{p}/p$ from Isoscalar Target cont.

- Results published PLB 786 (2018) 390 and PLB 807 (2020) 135600
- At high  $z$  multiplicity ratio for  $K^-/K^+$  and  $\bar{p}/p$  in data are below lower limits expected from pQCD in (N)LO
- Kaon results presented for  $x < 0.05$
- Effect more pronounced for  $\bar{p}/p$  and starts at lower  $z$



- SIDIS data are crucial for understanding quark fragmentation into hadrons
- COMPASS already published several papers based on isoscalar data analysis
- Today, results for  $h^\pm, \pi^\pm, K^\pm$  multiplicities on proton target were shown
- Impact of Radiative Correction is larger than originally anticipated in early isoscalar data analyses
- Otherwise, there is a good agreement between proton and isoscalar data
- Analysis is considered as finished - paper is in preparation