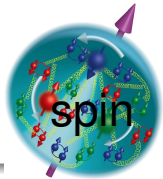


# Introduction to spin physics



Barbara Badelek  
University of Warsaw

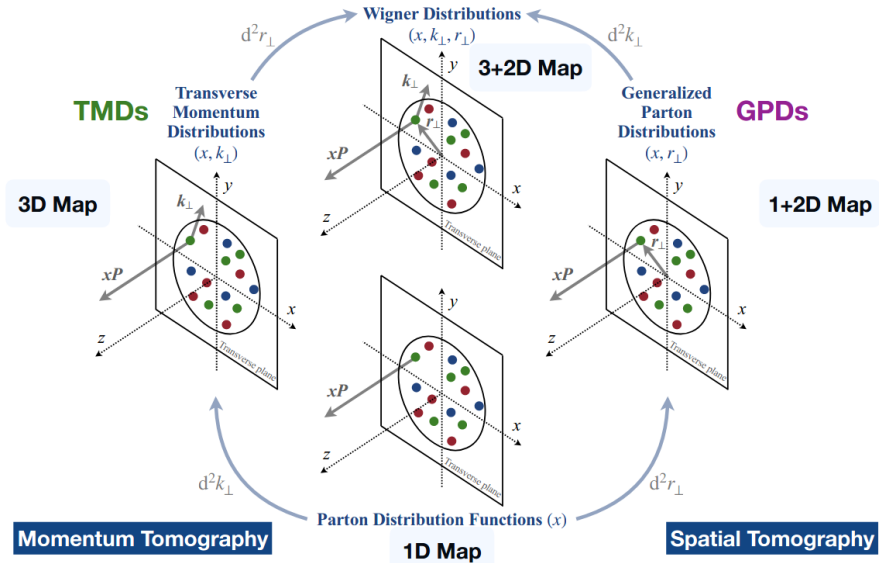


Epiphany2023

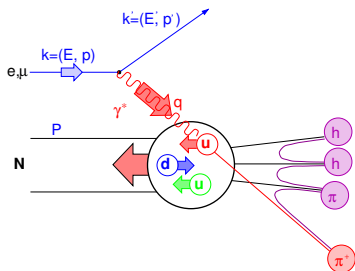
Cracow, 16 – 19 January, 2023



# Nucleon partonic structure (courtesy of Yu-Hsiang Lien, COMPASS)



# Nucleon spin structure in DIS: $\mu + N \rightarrow \mu' + X$

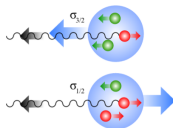


- $\frac{d^2\sigma}{d\Omega dE'} = \frac{\alpha^2}{2Mq^4} \frac{E'}{E} L_{\mu\nu} W^{\mu\nu}$
- Symmetric part of  $W^{\mu\nu}$  – unpolarised DIS, antisymmetric – polarised DIS
- Nominally  $F_{1,2}, q(x, Q^2) \rightarrow g_{1,2}, \Delta q(x, Q^2)$  where  $q = q^+ + q^-, \Delta q = q^+ - q^-$ , but...
  - ...anomalous gluon contribution to  $g_1(x, Q^2)$
  - ... $g_2(x, Q^2)$  has no interpretation in terms of partons.

Definitions of DIS variables...

$Q^2 = -q^2$	$\gamma^*$ virtuality
$x = Q^2/(2Pq)$	Bjorken variable
$y = Pq/(Pk)$	relative $\gamma^*$ energy
$W = P + q$	$\gamma^*$ -N cms energy

...and of the  $\gamma^*$ -N asymmetry (e.g. for  $\gamma^*$ -p):



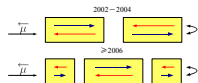
$$A_1(x, Q^2) = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}}$$

# Observables

- Inclusive asymmetry,  $A_{meas}(x, Q^2)$ ,  $\gamma^*$ -N asymmetry,  $A_1(x, Q^2)$ , and  $g_1(x, Q^2)$ :

$$A_{meas} = \frac{1}{f P_T P_B} \left( \frac{N^{\leftarrow} - N^{\rightarrow}}{N^{\leftarrow} + N^{\rightarrow}} \right) \approx D A_1 = D \frac{g_1(x, Q^2)}{F_1(x, Q^2)} \stackrel{\text{LO}}{=} D \frac{\sum_q e_q^2 \Delta q(x, Q^2)}{\sum_q e_q^2 q(x, Q^2)}$$

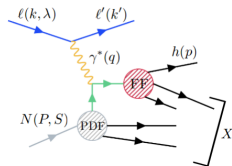
$f, D$ : dilution and depolarisation factors;  $P_T, P_B$ : target and beam polarisations;  
 $N^{\leftarrow, \rightarrow}$ : number of  $\vec{\mu}$  interactions in each target cell:  
 (upstream, downstream) or (outer, central)



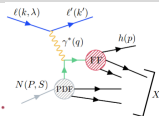
- Semi-inclusive asymmetry,  $A_1^h(x, z, Q^2)$ , at LO:

$$A_1^h(x, z, Q^2) \approx \frac{\sum_q e_q^2 \Delta q(x, Q^2) D_q^h(z, Q^2)}{\sum_q e_q^2 q(x, Q^2) D_q^h(z, Q^2)}, \quad z = \frac{E_h}{\nu}$$

$D_q^h \neq D_{\bar{q}}^h$



# THE 18 SIDIS STRUCTURE FUNCTIONS



Unpolarized structure function

$$\frac{d\sigma}{dx dy d\phi_S dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} \right.$$

$$\left. + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} + S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] \right.$$

$$f_1 \otimes D_1$$

Sivers structure function

$$+ S_L \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right]$$

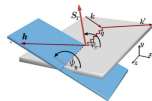
$$+ S_T \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon \sin(\phi_h - \phi_S) F_{T,L}^{\sin(\phi_h - \phi_S)} \right) + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \right.$$

$$\left. + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} \right.$$

$$\left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} + S_T \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} \right. \right.$$

$$\left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right]$$

$$f_{1T}^\perp \otimes D_1$$

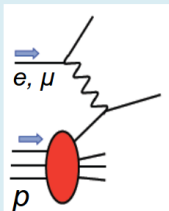


Collins structure function

$$h_1 \otimes H_1^\perp$$

Slide courtesy A. Bacchetta, IWHSS2022 (with changes)

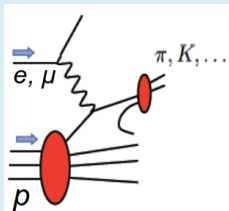
# Processes available for parton (helicity) distributions



**DIS:**

$$\Delta q + \Delta \bar{q}$$

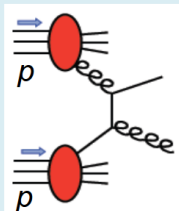
$\Delta g$  (From  $Q^2$  evolution of  $g_s$ )



**SIDIS:**

$$\Delta q, \Delta \bar{q}$$

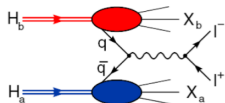
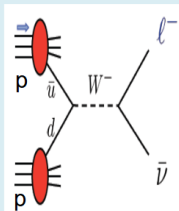
$\Delta g$



**pp:**

$$\Delta q, \Delta \bar{q}$$

$\Delta g$



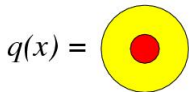
Drell-Yan process, complementary to SIDIS; COMPASS, FNAL, STAR, PHENIX

JLab  
(HERMES@HERA)  
COMPASS@CERN

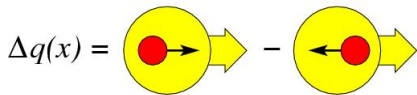
A. Bazilevsky, SPIN2016  
STAR@RHIC  
PHENIX@RHIC  
LHC/Spin  
⇒ talk by P.Di Nezza

# Partonic structure of the nucleon; distribution functions

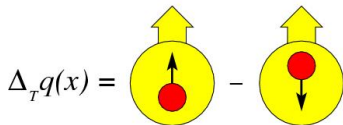
Three **twist-two** quark distributions in QCD and after integrating over the quark intrinsic  $k_t$



Quark momentum DF;  
**well known** (unpolarised DIS  $\rightarrow \mathbf{F}_{1,2}(x, Q^2)$ ).



Difference in DF of quarks with spin parallel or antiparallel to the nucleon's spin in a longitudinally polarised nucleon;  
**less well known** (polarised DIS  $\rightarrow \mathbf{g}_1(x, Q^2)$ ).  
 $\Rightarrow$  talk by M. Žurek



Difference in DF of quarks with spin parallel or antiparallel to the nucleon's spin in a transversely polarised nucleon;  
**poorly known** (polarised DIS  $\rightarrow \mathbf{h}_1(x, Q^2)$ ).

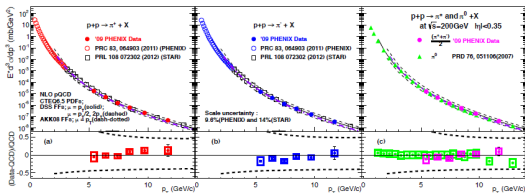
Nonrelativistically:  $\Delta_T q(x, Q^2) \equiv \Delta q(x, Q^2)$ . OBS.!  $\Delta_T q(x, Q^2)$  are C-odd and chiral-odd

If the  $k_t$  taken into account  $\Rightarrow$  8 TMD distr.; e.g.  $f_{1T}^\perp$  (accessible through "Sivers asymmetry").

# Transverse Single Spin asymmetry (SSA) in $pp \rightarrow \pi X$

mid-rapidity RHIC data, unpolarised cross sections  
(arXiv:1409.1907 [hep-ex], Phys. Rev. D91 (2015) 3, 032001)

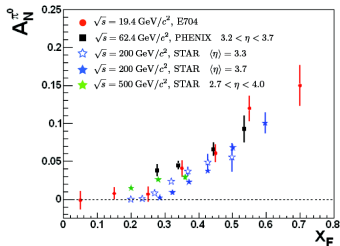
large  $P_T$  single pion production  $pp \rightarrow \pi X$



good agreement between RHIC data  
and collinear pQCD calculations

BUT for  $\perp$  polarised p

$A_N$  large and persistent at high energies ...



...but QCD at quark level:  $A_N \sim \frac{m_q}{E_q} \alpha_s$

Many other spin effects @ high energies  
cannot be understood in the collinear QCD...



## 1987: European Muon Collaboration at CERN:

J. Ashman et al., Phys. Lett. B **206** (1988) 364

J. Ashman et al., Nucl. Phys. B **328** (1989) 1

$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma(\mu) + \Delta G(\mu) + L_q(\mu) + L_g(\mu) \quad \text{Jaffe-Manohar}$$

$$\Delta\Sigma(Q^2) = \int_0^1 dx [\Delta u + \Delta\bar{u} + \Delta d + \Delta\bar{d} + \Delta s + \Delta\bar{s}](x, Q^2), \quad \Delta G(Q^2) = \int_0^1 dx \Delta g(x, Q^2)$$

$$\text{(with } \int_0^1 dx [\Delta s + \Delta\bar{s}] < 0)$$

EMC measured:  $\Delta\Sigma \sim 0.1!$  and broken Ellis-Jaffe sum rule

papers cited **4099** times (2 XII 2022)

# Nucleon in 3-D

(two approaches)

# Partonic structure of the nucleon; distribution functions

- In LT and considering  $k_T$ , 8 PDF describe the nucleon  
 $\implies$  Transverse Momentum Dependent PDF

- QCD-TMD approach valid  $k_T \ll \sqrt{Q^2}$

- After integrating over  $k_T$  only 3 survive:  $f_1, g_1, h_1$

- TMD accessed in SIDIS and DY by measuring azimuthal asymmetries with different angular modulations

- SIDIS: e.g.  $A_{\text{Sivers}} \propto \text{PDF} \otimes \text{FF}$

- DY: e.g.  $A_{\text{Sivers}} \propto \text{PDF}^{\text{beam}} \otimes \text{PDF}^{\text{target}}$

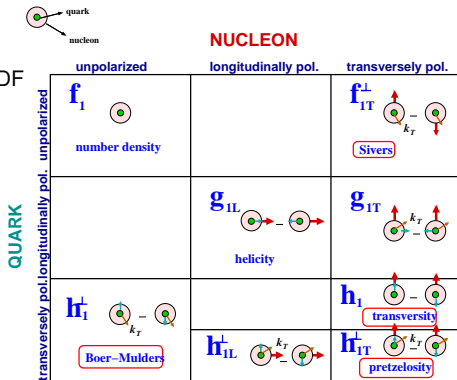
- OBS! Boer-Mulders and Sivers PDF are T-odd, i.e. process dependent

$$h_1^\perp(\text{SIDIS}) = -h_1^\perp(\text{DY})$$

$$f_{1T}^\perp(\text{SIDIS}) = -f_{1T}^\perp(\text{DY})$$

- OBS! transversity PDF is chiral-odd; may only be measured with another chiral-odd partner, e.g. fragmentation function.

- TMD parton distributions need TMD Fragmentation Functions!



talks by V.Bertone, A.Bressan

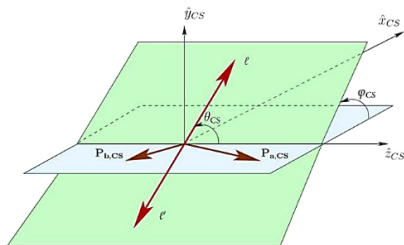
# SIDIS and Drell-Yan compatibility

$$A_{SIDIS} \propto PDF_p \otimes FF$$

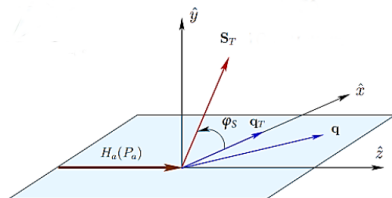
$$A_{DY} \propto PDF_\pi \otimes PDF_p$$

$A_{UU}^{\cos(2\phi_h)} \propto h_{1,p}^{\perp q} \otimes H_{1q}^{\perp h}$	<b>Boer-Mulders</b>	$A_U^{\cos(2\varphi_{CS})} \propto h_{1,\pi}^{\perp,q} \otimes h_{1,p}^{\perp,q}$
$A_{UT}^{\sin(\phi_h - \phi_S)} \propto f_{1T,p}^{\perp q} \otimes D_{1q}^h$	<b>Sivers</b>	$A_T^{\sin\varphi_S} \propto f_{1,\pi}^q \otimes f_{1T,p}^{\perp q}$
$A_{UT}^{\sin(3\phi_h - \phi_S)} \propto h_{1T,p}^{\perp q} \otimes H_{1q}^{\perp h}$	<b>Pretzelosity</b>	$A_T^{\sin(2\varphi_{CS} + \varphi_S)} \propto h_{1,\pi}^{\perp q} \otimes h_{1T,p}^{\perp q}$
$A_{UT}^{\sin(\phi_h + \phi_S)} \propto h_{1,p}^q \otimes H_{1q}^{\perp h}$	<b>Transversity</b>	$A_T^{\sin(2\varphi_{CS} - \varphi_S)} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^q$

(courtesy of R. Longo, COMPASS)

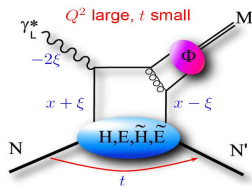


Collins-Soper ref. frame (CS)



Target rest frame (S)

# Generalised Parton Distributions



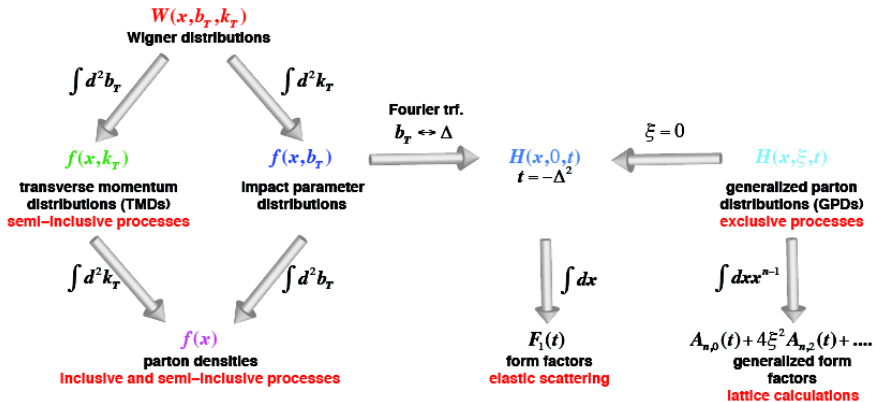
- Accessible via DVCS/DVMP:  $\mu p \rightarrow \mu p \gamma(M)$
- 4 GDPs ( $H, E, \tilde{H}, \tilde{E}$ ) for each flavour and for gluons plus 4 chiral odd ones ( $H_T, E_T, \tilde{H}_T, \tilde{E}_T$ )
- All depend on 4 variables:  $x, \xi, t, Q^2$ ; DIS @  $\xi = t = 0$ ; **Careful ! Here  $x \neq x_B$ !**
- $H, \tilde{H}$  conserve nucleon helicity  
 $E, \tilde{E}$  flip nucleon helicity
- $H, E$  refer to unpolarised distributions  
 $\tilde{H}, \tilde{E}$  refer to polarised distributions
- $H^q(x, 0, 0) = q(x), \tilde{H}^q(x, 0, 0) = \Delta q(x)$

**Important:**

$$J_z^q = \frac{1}{2} \int dx x [H^q(x, \xi, t = 0) + E^q(x, \xi, t = 0)] = \frac{1}{2} \Delta \Sigma + L_z^q \quad (\text{X. Ji})$$

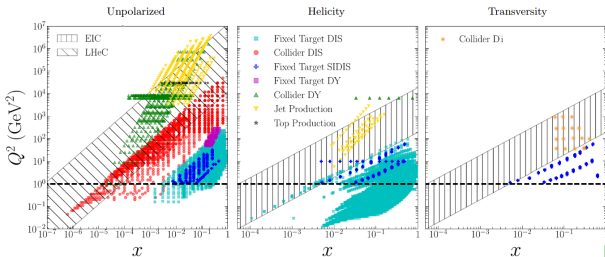
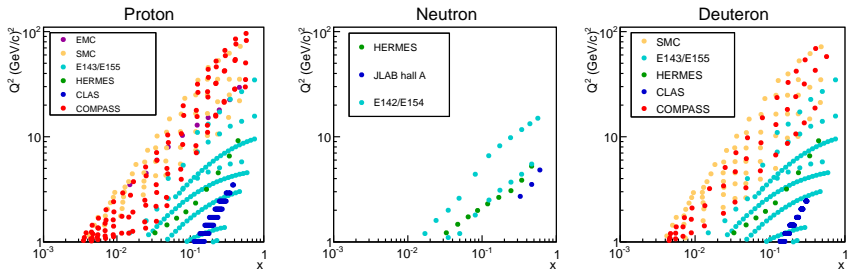
⇒ talks by J.Wagner, F.Kunne, K.Cichy (lattice)

# Descriptions of $pdf^s$ in the nucleon



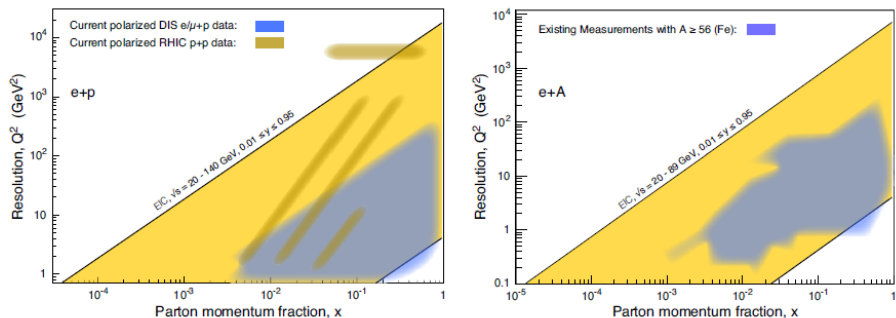
From "White paper", arXiv:1212.1701

# Map of present experimental results



hep-ph 2006.08636v2

# The EIC perspective



**Figure 2.1:** Left: The  $x$ - $Q^2$  range covered by the EIC (yellow) in comparison with past and existing polarized  $e/\mu+p$  experiments at CERN, DESY, JLab and SLAC, and  $p+p$  experiments at RHIC. Right: The  $x$ - $Q^2$  range for  $e+A$  collisions for ions larger than iron (yellow) compared to existing world data.



# OPEN QUESTIONS

to be addressed in the near/LHC-Spin/EIC  future

(originally formulated with Umberto D'Alesio  
at the “2022 Diffraction and Low  $x$ ” workshop)

- **Spin as a goal** (nucleon spin structure) **and as a tool** (fundamental properties of QCD);
- **Three fundamental electromagnetic interactions: SIDIS, DY,  $e^+e^- \rightarrow h_1 h_2 X$ :**  
TMD factorization proven; azimuthal modulations to access separately all TMDs;  
test of factorisation, evolution and (modified) universality properties;
  - **SIDIS:** (un)polarised TMDs; Sivers, Collins, Boer-Mulders;
  - **DY:** clear channels for TMD-PDFs; bridge DY  $\iff$  SIDIS;  
recent extractions unpolarised TMDs from a global fit on SIDIS and DY;
  - **$e^+e^-$ :** clear channel for TMD Fragmentation Functions;  
universality of TMDs; spontaneous  $\Lambda$  polarisations;  
single and double hadron production; new advancements in TMD factorization;
- **$pp \rightarrow h(\text{jet}) X$ ;  $ep \rightarrow h(\text{jet}) X$ :** complementary processes to learn on TMD-FFs  
and check their universality;
- **$pp \rightarrow h X$ ,  $pp \rightarrow \text{jet} X$ ,  $pp \rightarrow \gamma X$ :** twist-3 parton-hadron correlators  
and their relation with TMDs;
- **TMD factorisation:** interplay of perturbative (calculable) and nonperturbative effects;  
matching low and high scales, improvements in Collins-Soper-Sterman formalism;