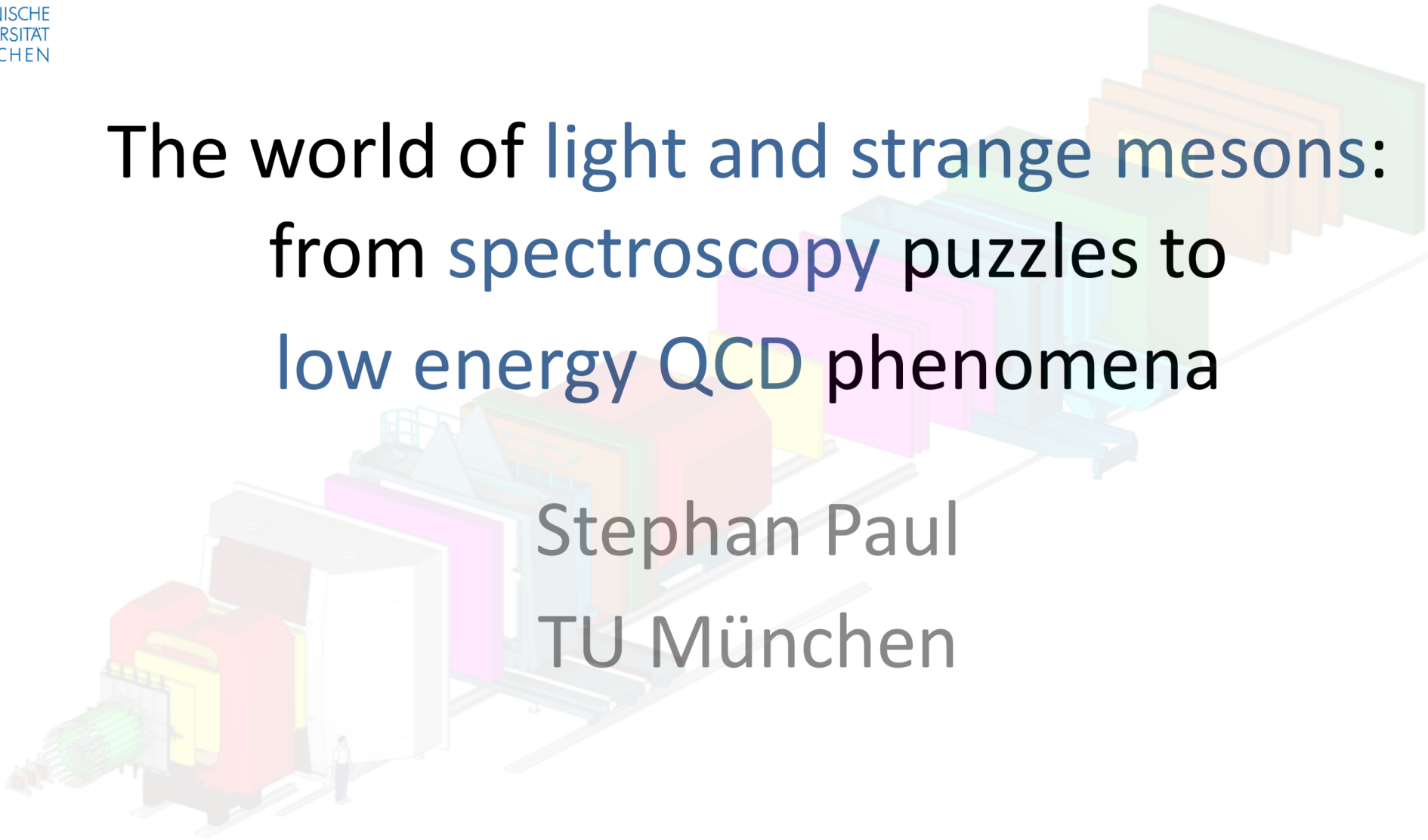
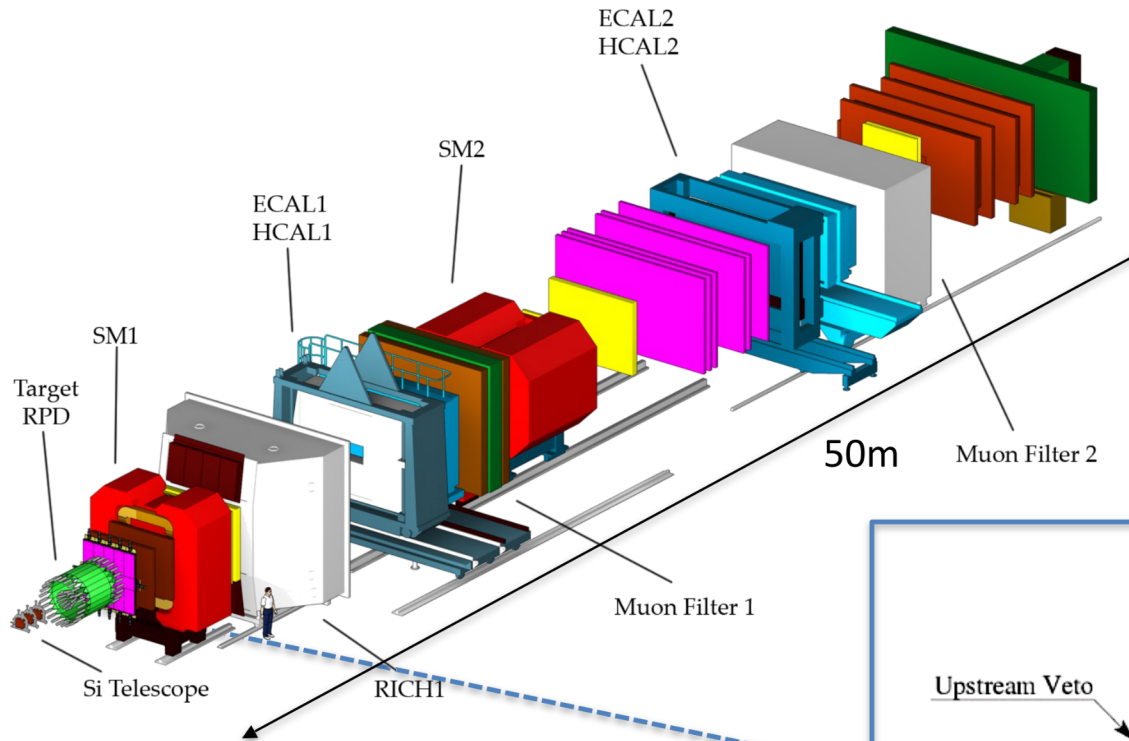


The world of light and strange mesons: from spectroscopy puzzles to low energy QCD phenomena

Stephan Paul
TU München



The COMPASS Experiment

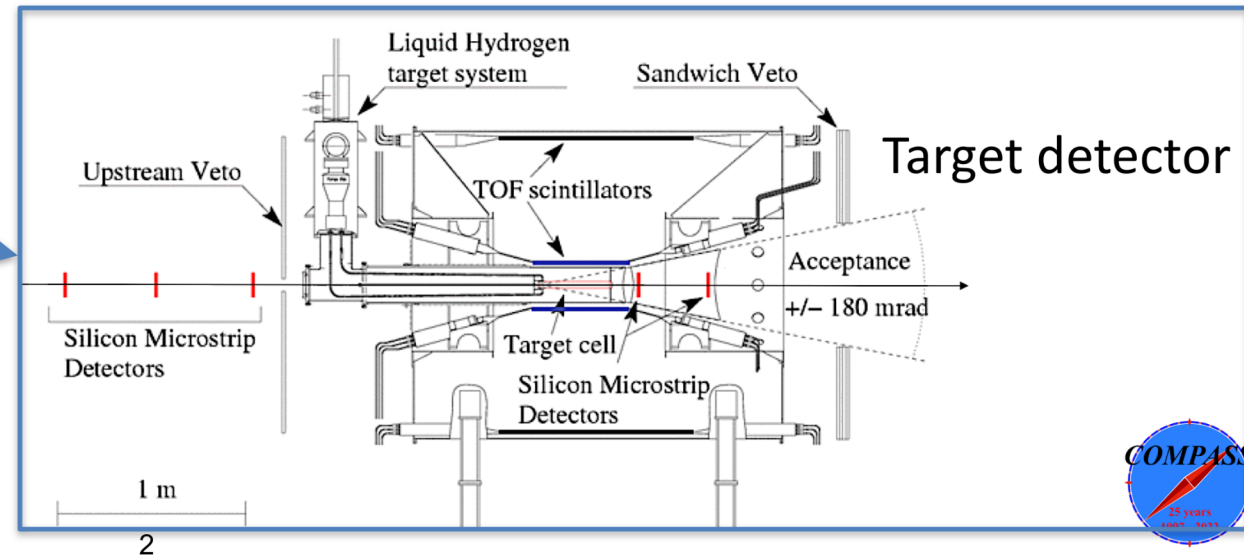


CERN SPS

Hadron beam:

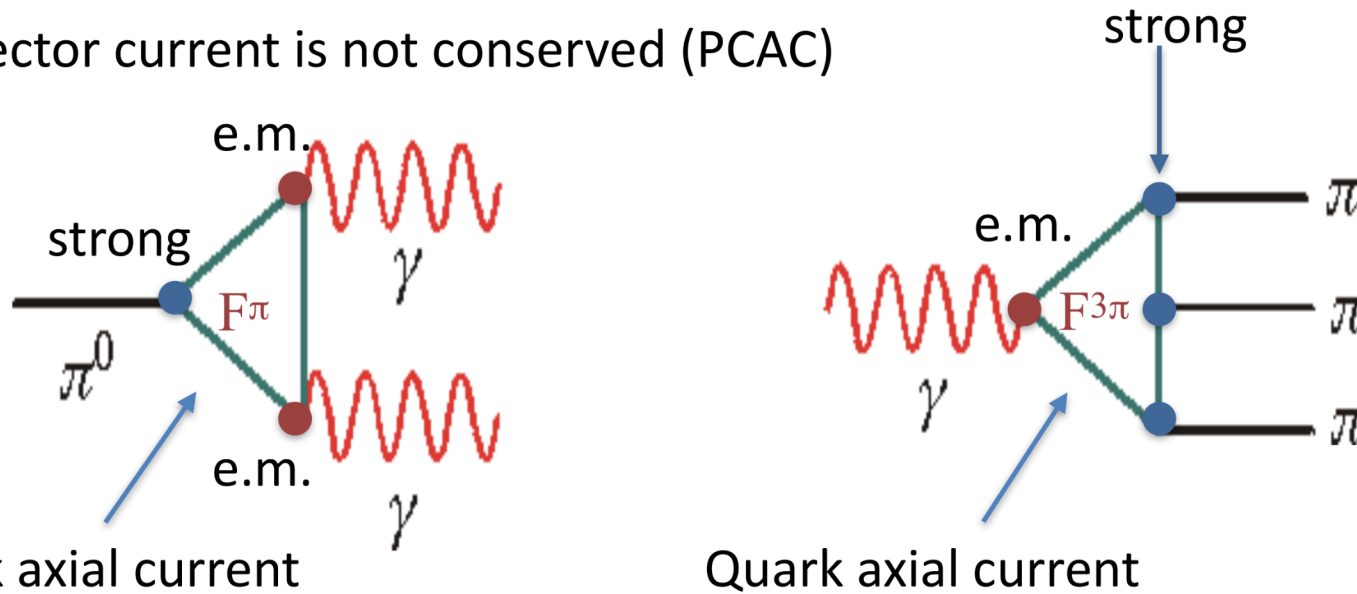
- 190 GeV/c π , K, p
- $5 \cdot 10^7$ particles/SPS-spill
- LH_2 or Ni/W-target

operated 2002-2022



The Chiral Anomaly

in QCD axial-vector current is not conserved (PCAC)

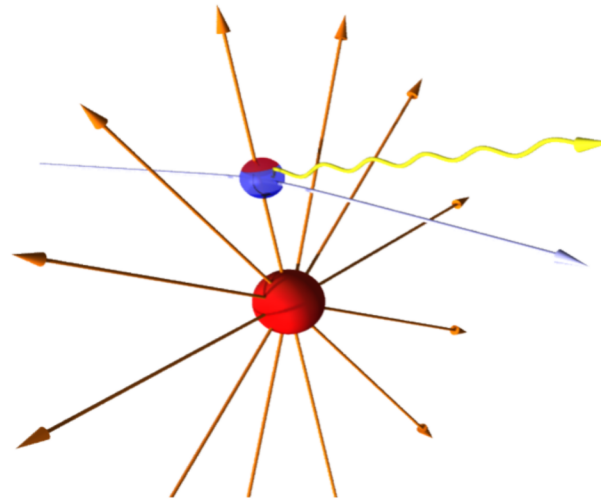


- triangle diagram reveals breaking of classical symmetries → **chiral anomaly**
- Chiral anomaly taken into account χ EFT by Wess-Zumino-Witten term:
Describes coupling of odd number of Goldstone bosons (π, η, K)

$\pi^0 \rightarrow \gamma\gamma$ and $\gamma \rightarrow 3\pi$ ($\pi^- \gamma \rightarrow \pi^- \pi^0$) determined by chiral anomaly of QCD

Principle of Measurement

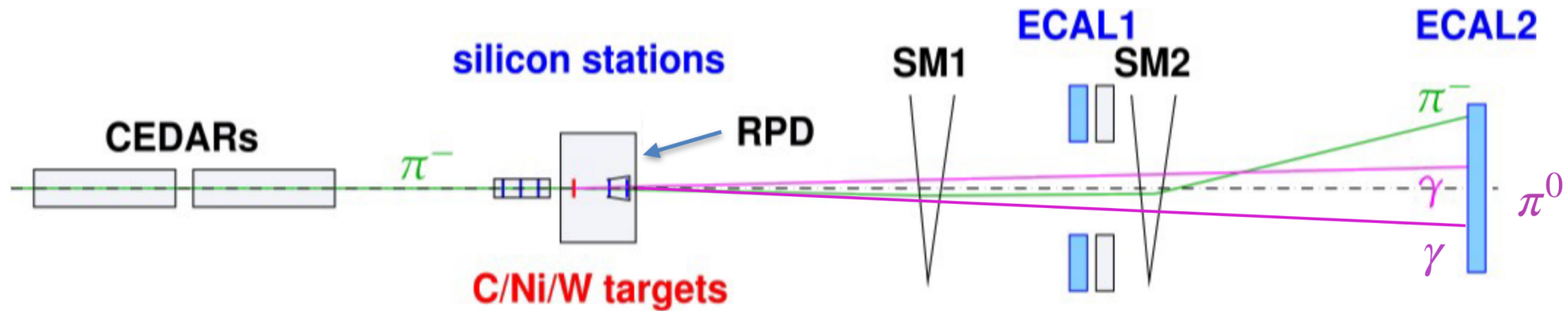
$$\pi^- + \gamma^* \rightarrow \pi^- \pi^0 \text{ via } \pi^- + (A, Z) \rightarrow \pi^- \pi^0 + (A, Z) \text{ at } Q^2 < 10^{-3}$$



Primakoff process

Principle of Measurement

$$\pi^- + \gamma^* \rightarrow \pi^- \pi^0 \text{ via } \pi^- + (A, Z) \rightarrow \pi^- \pi^0 + (A, Z) \text{ at } Q^2 < 10^{-3}$$



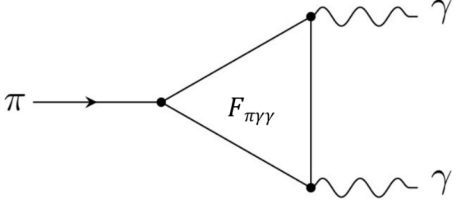
- identify beam particle: 96.8% π^- or 2.4% K^- (190 GeV)
- 4mm Ni target disk $\approx 25\% X/X_0$
- select exclusive $\pi^- \gamma$ final state at very low Q^2
- Luminosity determination via beam Kaon decay

$$(K^- \rightarrow \pi^- \pi^0 \text{ or } K^- \rightarrow \pi^- \pi^0 \pi^0)$$



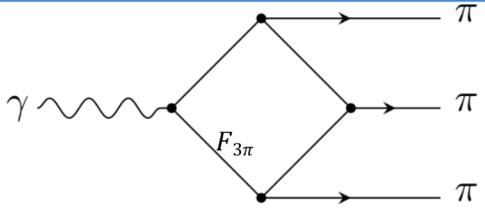
$F_{\pi\gamma\gamma}$

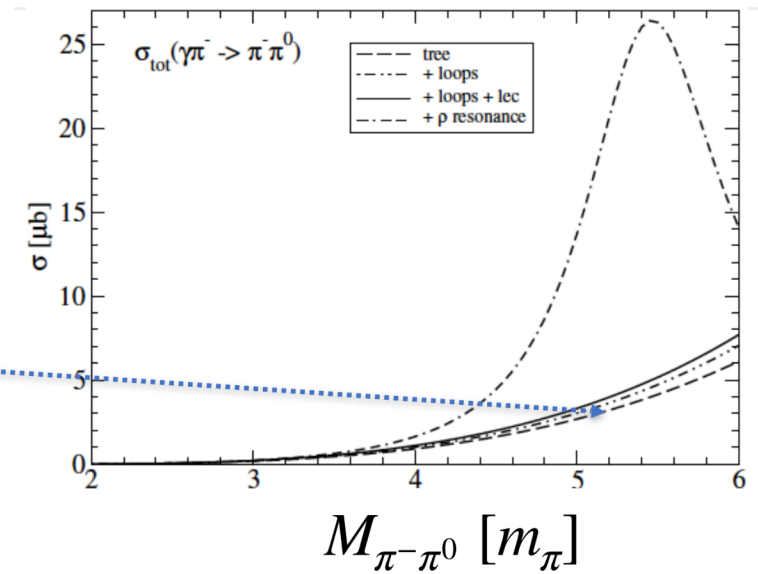
$N_c = 3$

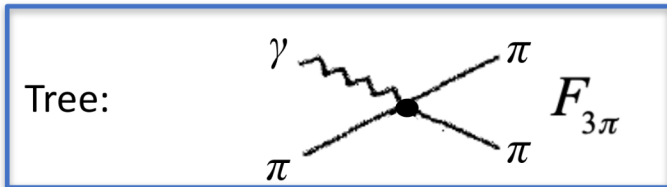


$$F_{\pi\gamma\gamma} = \frac{e^2 N_c}{12\pi^2 f_\pi} = 2.52 \cdot 10^{-2} \text{ GeV}^{-1}$$

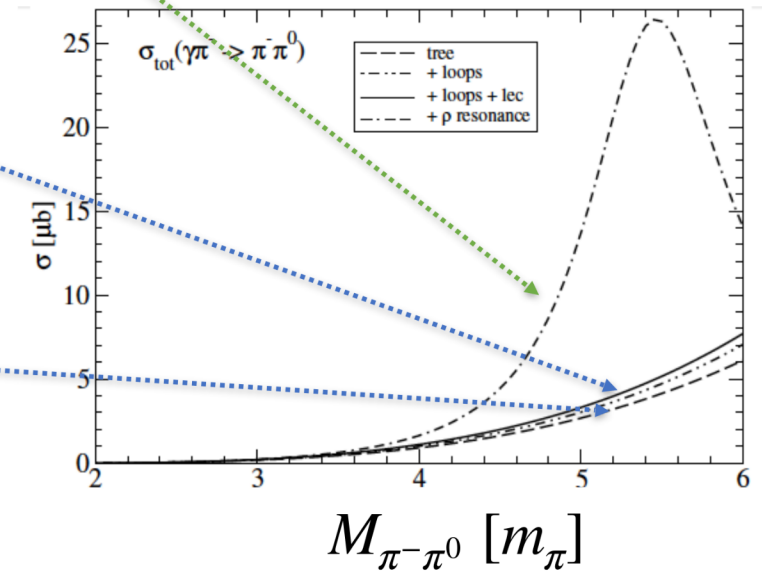
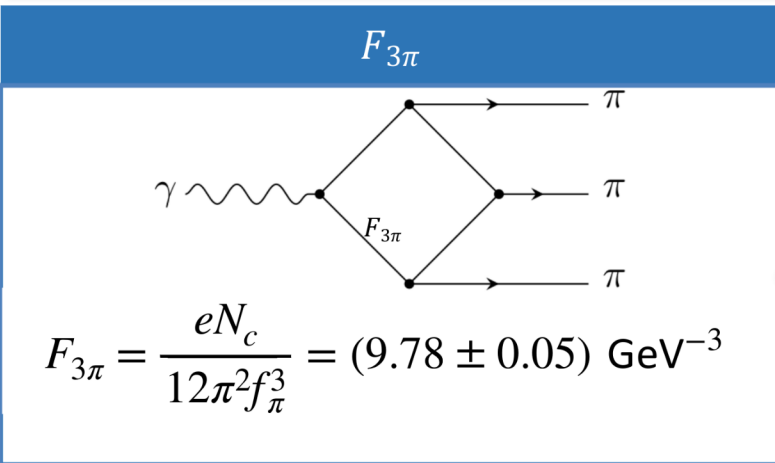
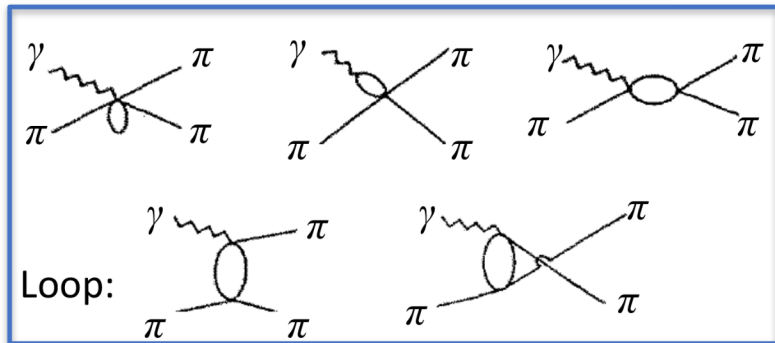
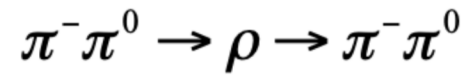
$F_{3\pi}$

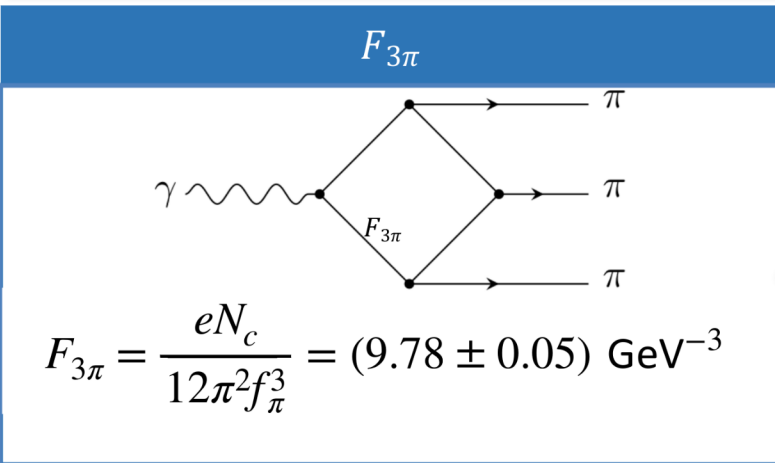
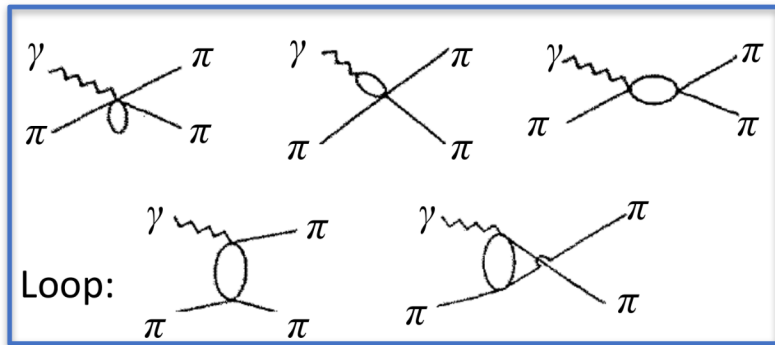
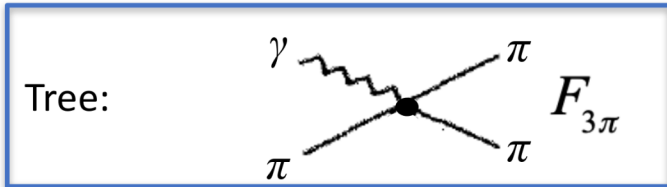


$$F_{3\pi} = \frac{e N_c}{12\pi^2 f_\pi^3} = (9.78 \pm 0.05) \text{ GeV}^{-3}$$


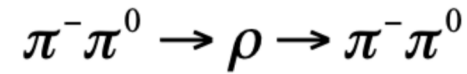


Strong final state interaction (FSI)

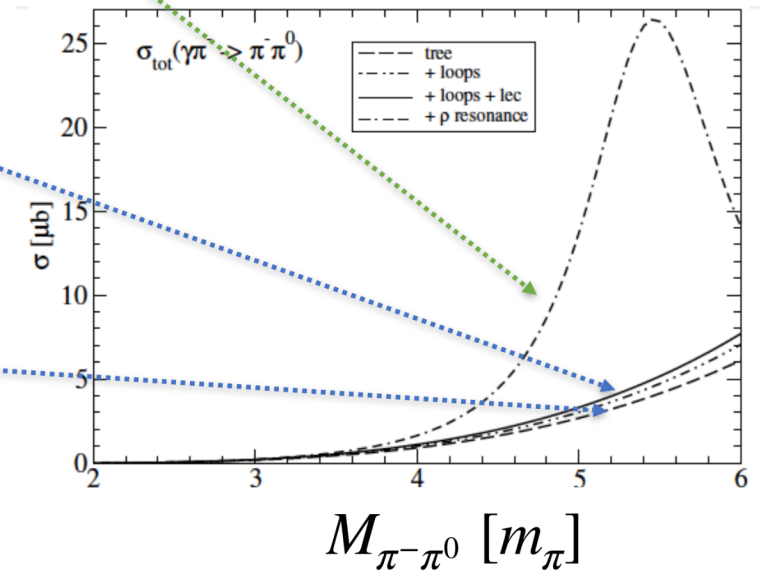




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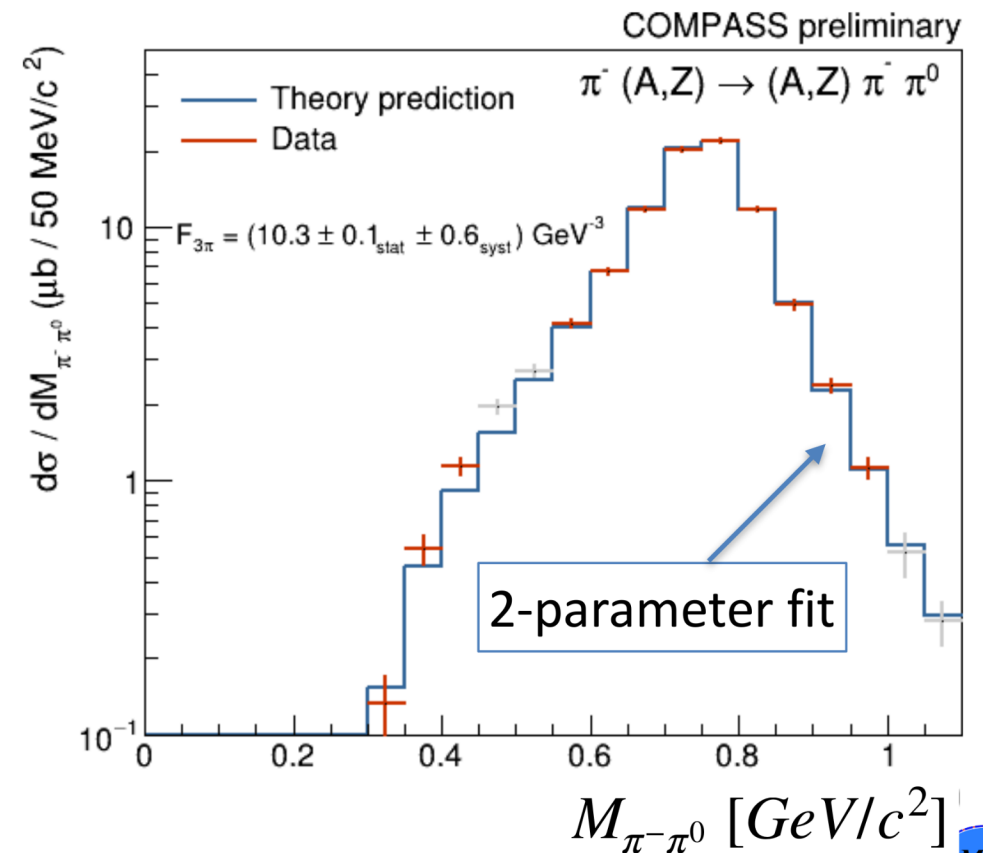


Antipov et al in Serpukhov:
 $F_{3\pi} = 12.9 \pm 0.9 \pm 0.5 \text{ GeV}^{-3}$
reanalyzed - many systematics



Results of Dispersive fits $\pi^- \gamma^* \rightarrow \pi^- \pi^0$

- Selection: $Q^2 < 1.3 \cdot 10^{-3} \text{ GeV}^2/c^2$
- Dispersive framework*: deduce $F_{3\pi}$ and $\Gamma_{\rho \rightarrow \pi\gamma}$ from fit to $\pi^- \pi^0$ mass distribution up to 1.0 GeV with FSI including $\rho(770)$ -resonance:



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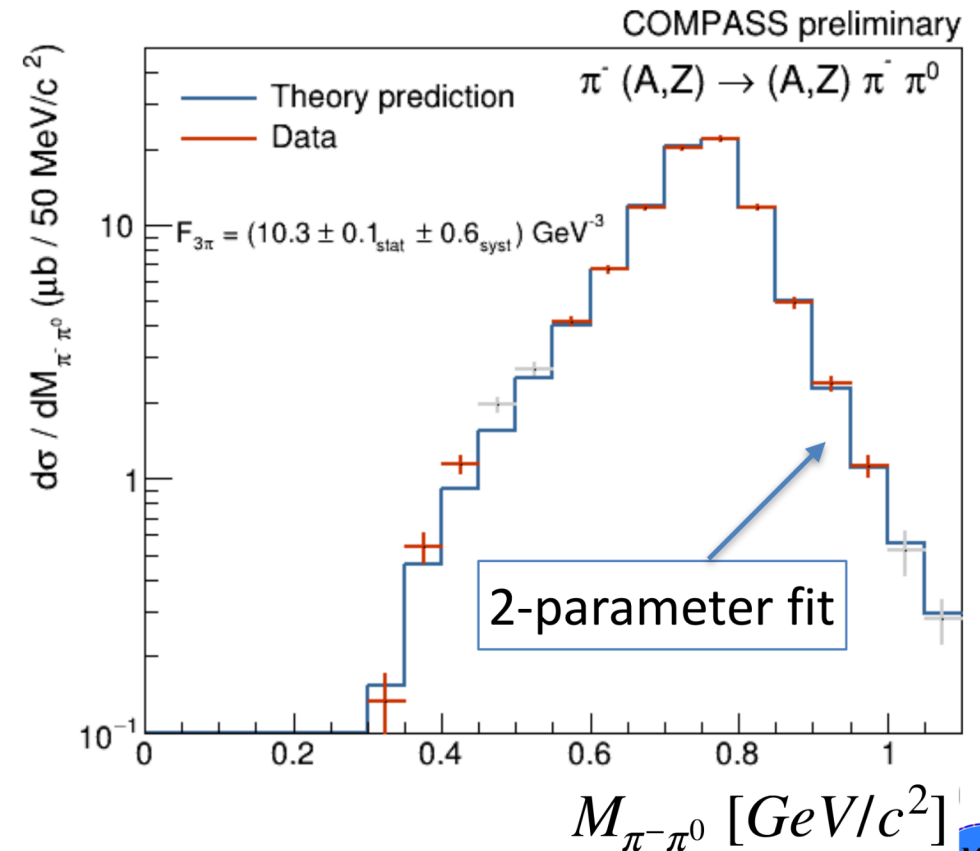
$$F_{3\pi} = (10.3 \pm 0.1_{\text{stat}} \pm 0.6_{\text{syst}}) \text{ GeV}^{-3}$$

$$\Gamma_{\rho \rightarrow \pi\gamma} = (76 \pm 1_{\text{stat}}^{+10}_{-8} \text{ syst}) \text{ keV}$$

- Preliminary result for $F_{3\pi}$ in agreement with χ PT prediction

$$F_{3\pi}^{\text{Th}} = (9.78 \pm 0.05) \text{ GeV}^{-3}$$

- Final systematic uncertainties expected: 4-5%



*M. Hoferichter, B. Kubis, and D. Sakkas, *PRD* **86** (2012) 116009

χ PT versus Experiments

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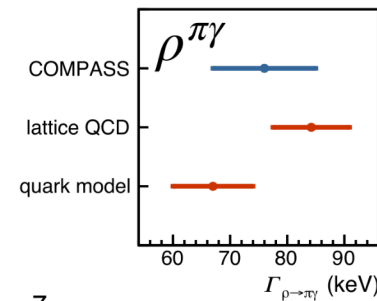
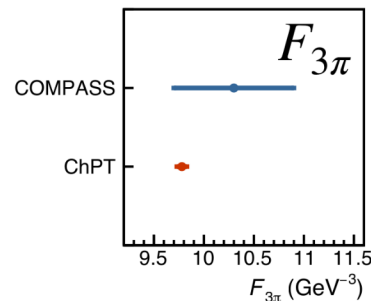
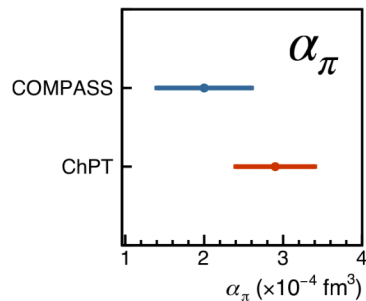
χ PT is consistent low energy effective theory for strong interaction

- Excellent agreement with experimental data:
 - So far: description of $\pi\pi$ scattering length, π^0 lifetime...

χ PT versus Experiments

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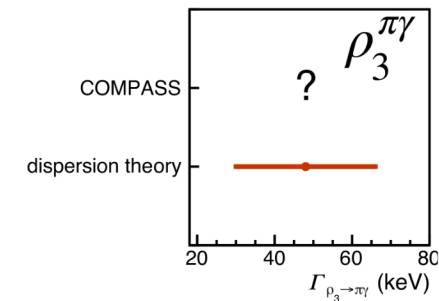
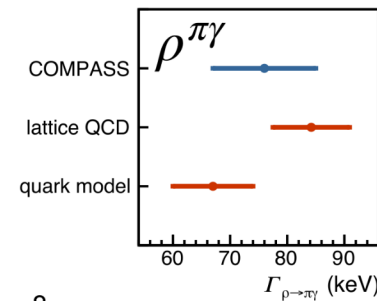
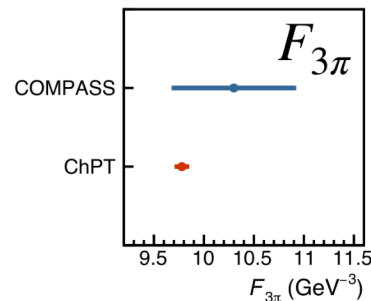
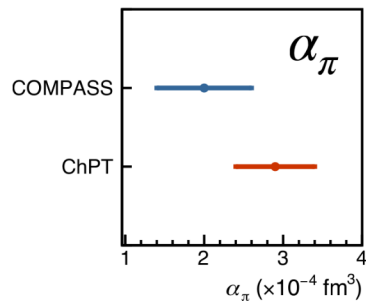
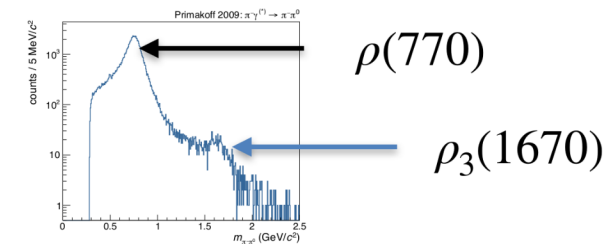
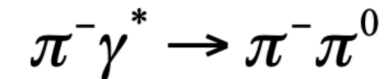
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 - **Now: Chiral anomaly ($F_{3\pi}$)** agrees well with data
 - Now: Excellent agreement with $O(p^6)$ for π -polarisability ($\alpha_\pi - \beta_\pi$ not shown)
 - Now: First „precision“ tests of hadron-hadron dynamics ($\pi^- \gamma^* \rightarrow \pi^- \pi^- \pi^+$ not shown)



χ PT versus Experiments

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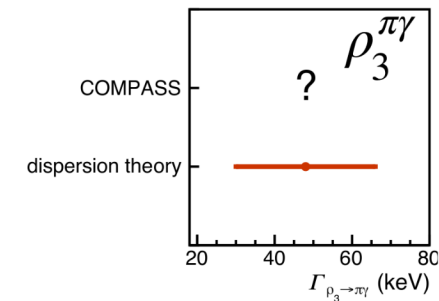
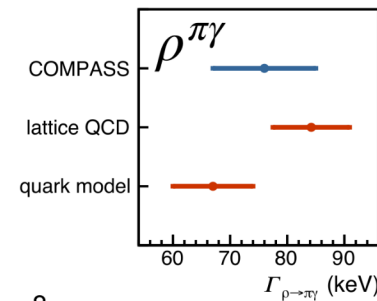
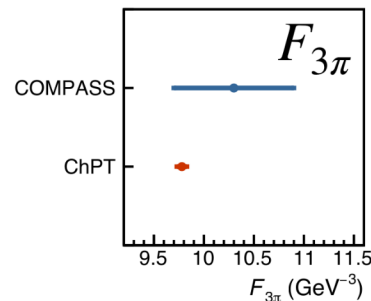
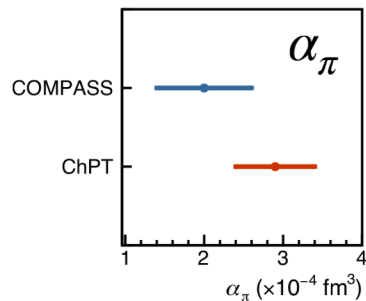
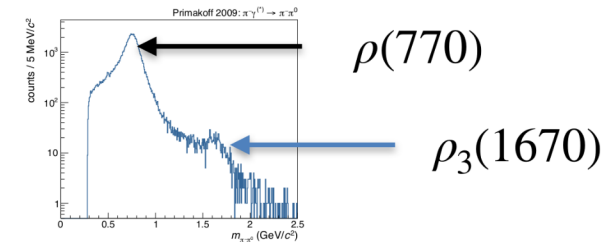
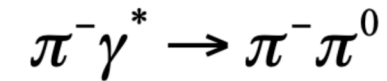
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 - Radiative width of $\rho(770)$ extracted „model independently“
- Pions are Goldstone bosons of spontaneous chiral symmetry breaking
- Pions are the only active degrees of freedom

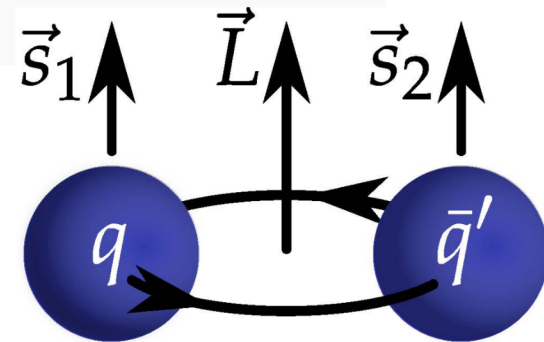


Meson Spectroscopy

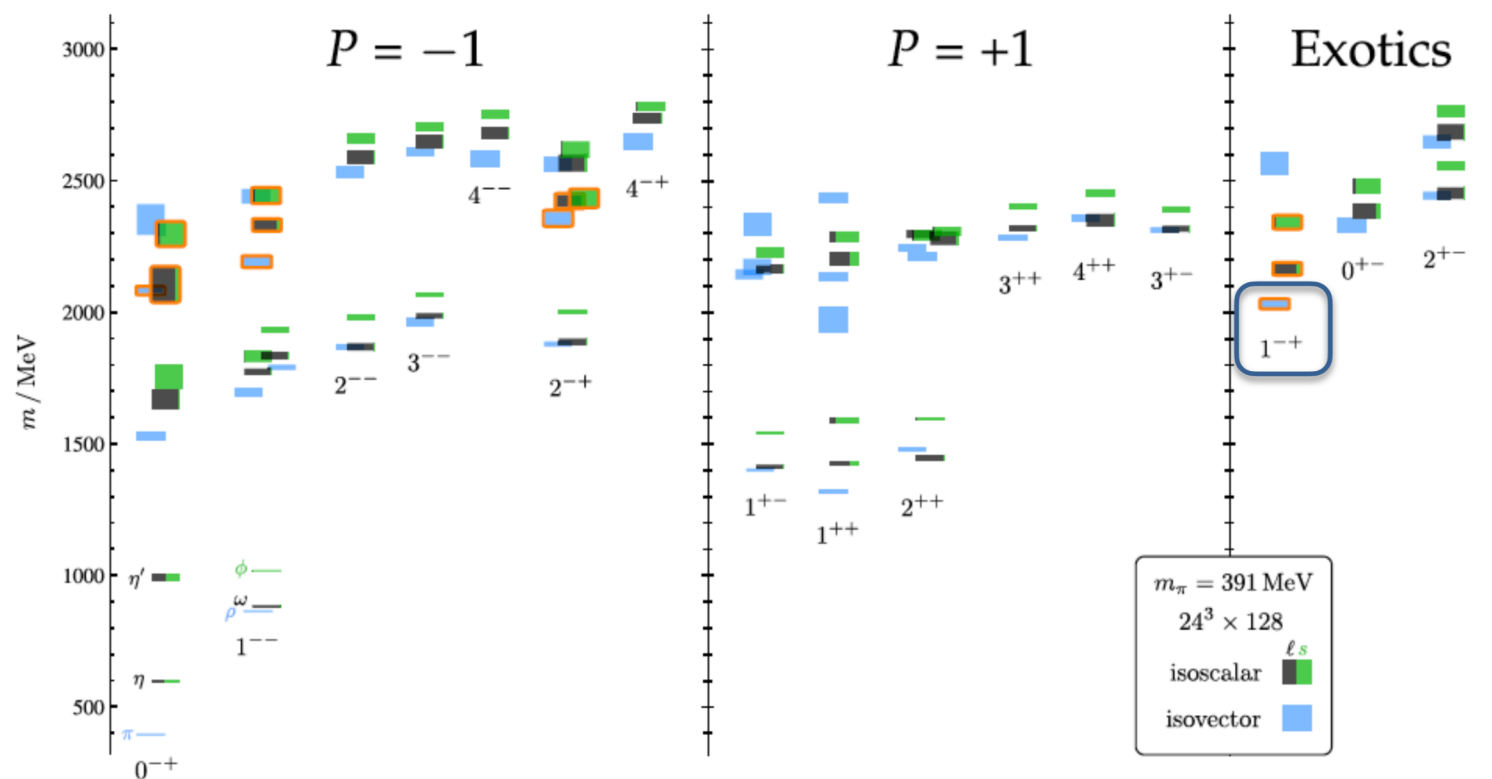
Constituent Quark Model Mesons

Spin-Parity selection rules for bound $q\bar{q}$ ' system

- Quark spins couple to total **intrinsic spin S** : $S = 0$ (singlet) or $S=1$ (triplet)
- Relative **orbital angular momentum L** couples with total **spin S** to **Meson spin**: $\vec{J} = \vec{L} + \vec{S}$
- Parity: $P = (-1)^{L+1}$
- Charge conjugation: $C = (-1)^{L+S}$
- G-parity: $G = C \cdot e^{i\pi I_z} = (-1)^{L+S}$
- **Allowed J^{PC} combinations**:
 - $L = 0 \rightarrow$ pseudo-scalar 0^{-+} , Vector 1^{-}
 - $L = 1 \rightarrow$ scalar 0^{++} , axial-vector 1^{+-} , 1^{++} and tensor 2^{++}
- **Forbidden J^{PC} combinations**: 0^{-} , 0^{+} , 1^{-+} , 2^{+-} , 3^{+}



- lattice calculations predict mass spectrum (also for exotics)
- future: lattice predicts width and couplings



Why Searching for Light Mesons II

At high energies:

- **Restoration** of chiral symmetry $E > 4\pi \cdot f_\pi \approx 1.2 \text{ GeV}$
- **Degeneration** of different parity states
- **Disappearance of mass-splitting** of parity multiplets

Requires precise spectroscopy at higher masses ($M > 2 \text{ GeV}/c^2$)

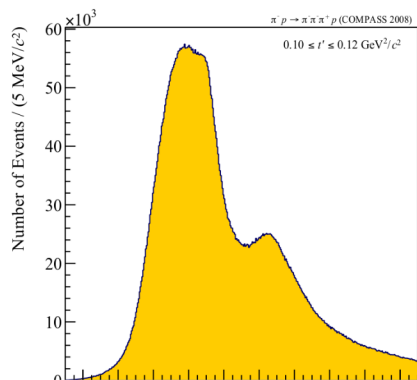
Meson Spectroscopy

- Most reactions studied with COMPASS are diffractive beam dissociation;
 $h^-p \rightarrow 3 \text{ hadrons e.g. } h'\pi \pi + p$ 3-body final state
 $h^-p \rightarrow 2 \text{ hadrons e.g. } \pi^-\eta^{(\prime)} + p$ 2-body final state

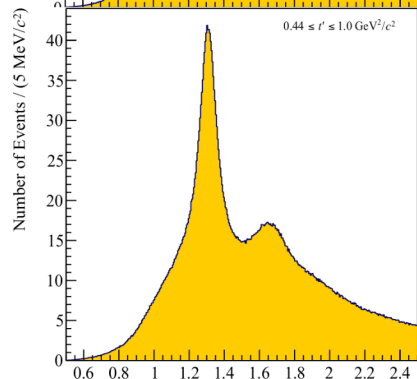
How to Search: Final State Examples

- Mass spectra of inclusive final states give small fraction of information
- Production dependence (4-momentum transfer) adds **separation power**
- Final states contain 10-20 different resonances - **from peak hunting to PWA**

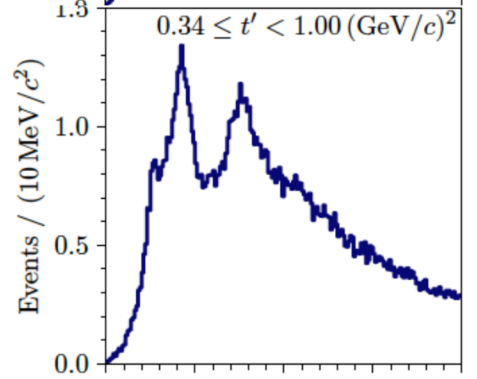
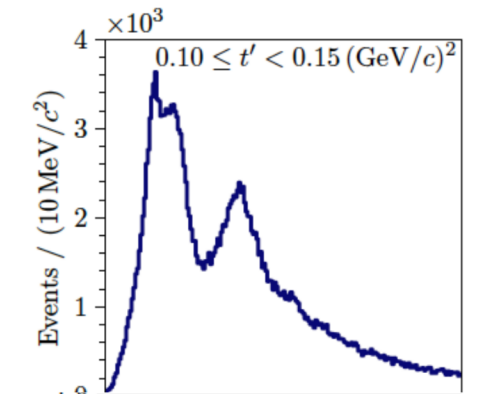
low t'



high t'

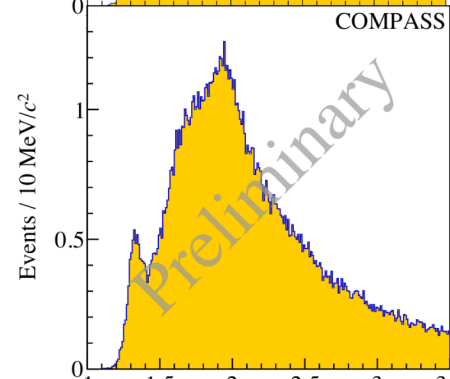
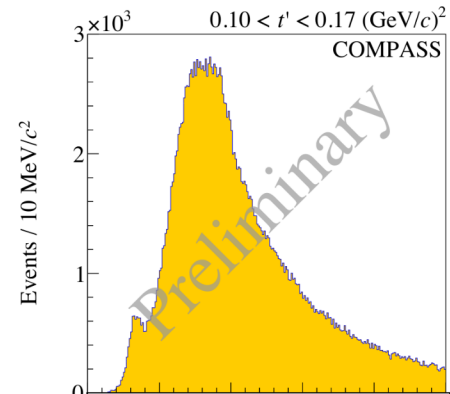


$m_{\pi^- \pi^- \pi^+} [GeV/c^2]$

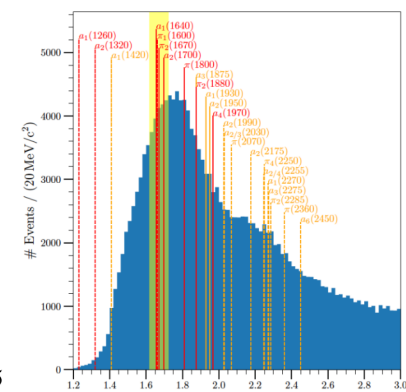


$m_{K\pi\pi} [GeV/c^2]$

14



$m_{\omega\pi\pi} [GeV/c^2]$



$m_{K_S^0 K_S^0 \pi} [GeV/c^2]$

Hass HK 29.4
Wagner HK 29.3



Partial Wave Analysis

- Decomposition of a complex System (**without interference**)

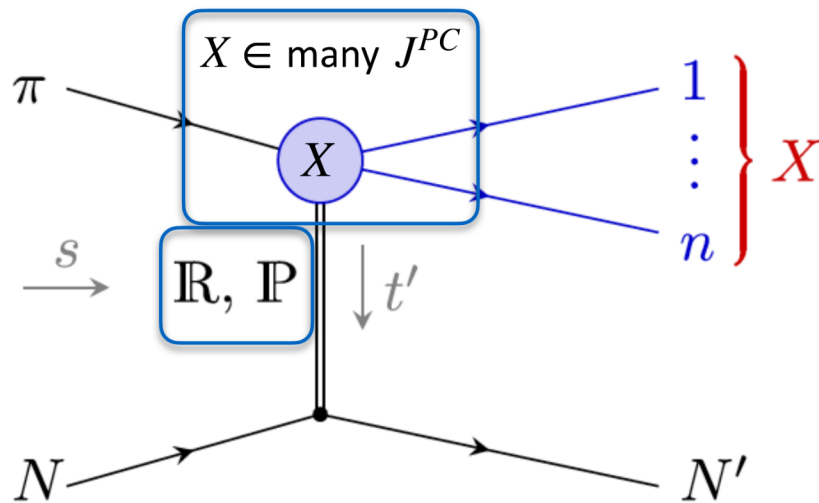
inspired by M. Pennington



Art taken from Urs Wehrli: "Kunst aufgeräumt"

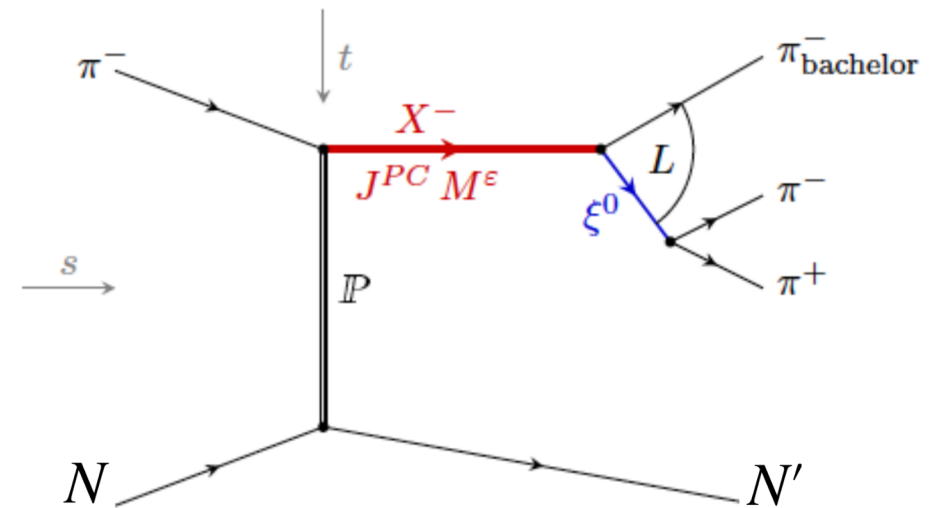
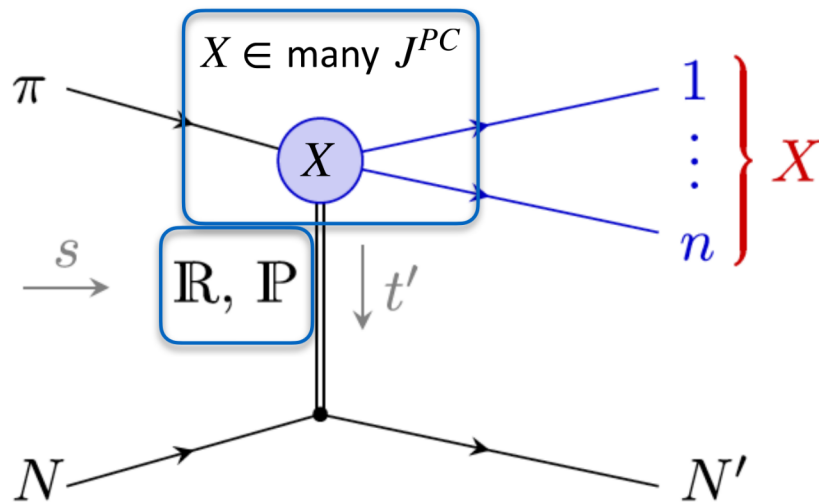
Partial Wave Analysis

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- But: quantum mechanics involves interference



Partial Wave Analysis

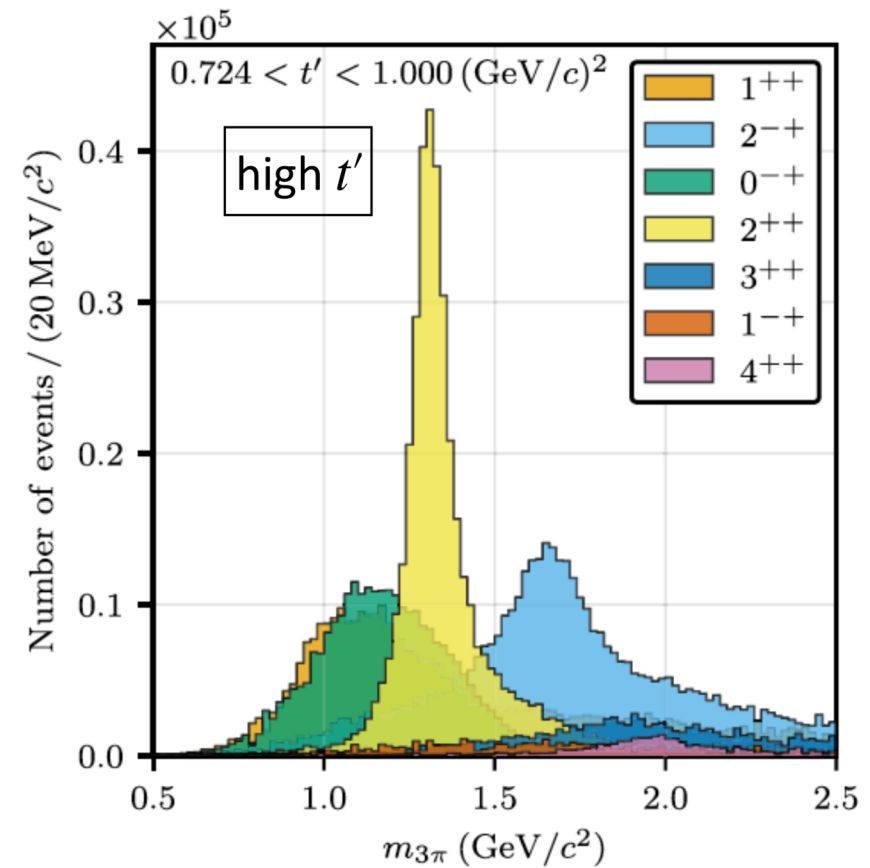
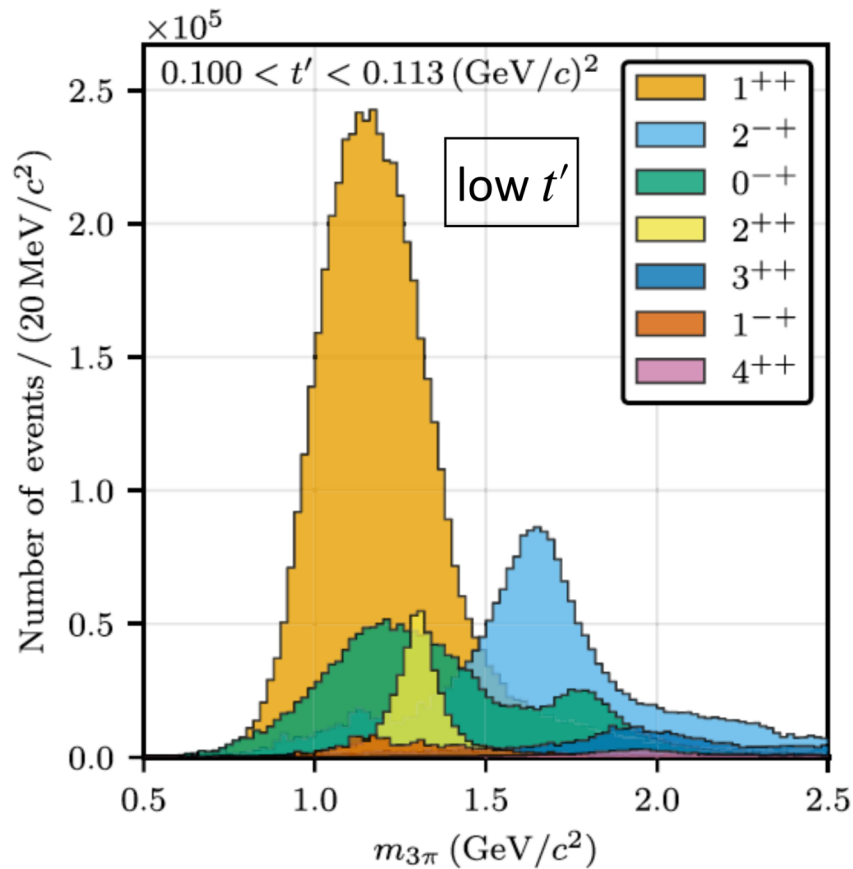
- Decomposition of a complex System (**without interference**)
- But: quantum mechanics involves interference
- Model reaction as multi-step process: production X and subsequent 2-body decays



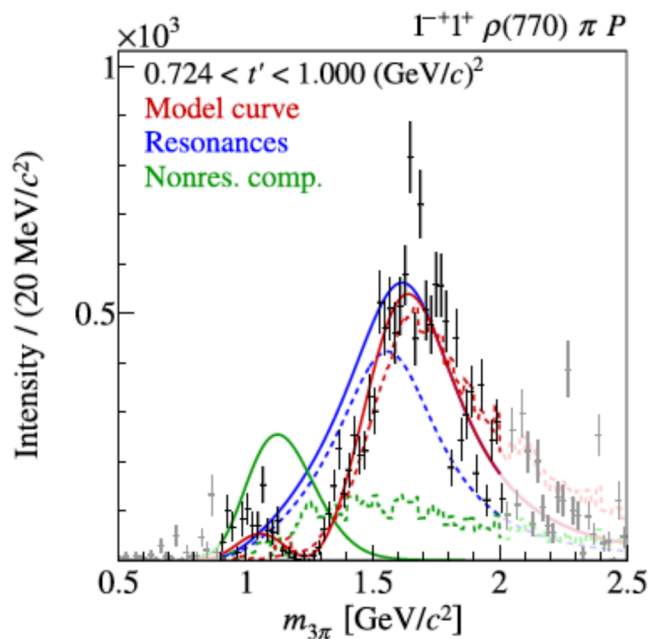
$J^{PC}(X^-)M^\epsilon \rightarrow \xi\pi \rightarrow 3\pi$ is called "wave"

PWA Result („spin totals“)

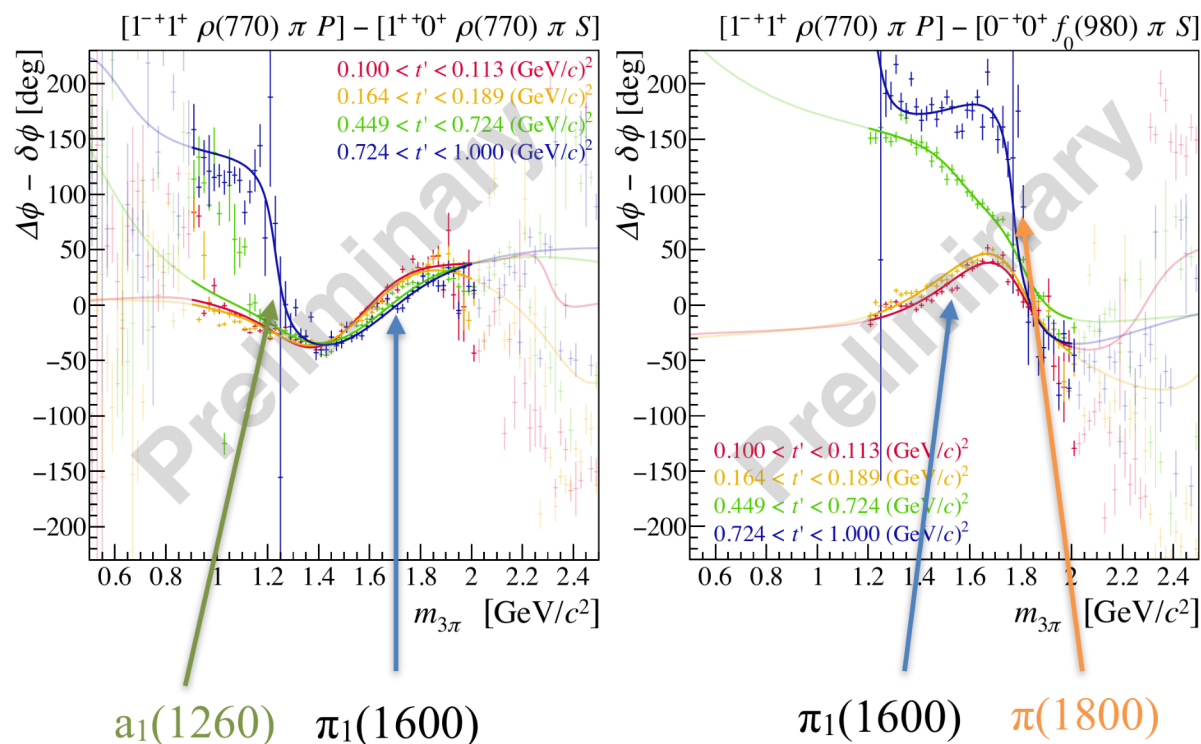
- Decomposition of the mass spectrum in terms of J^{PC}



Intensity



Relative Phases (interference terms)

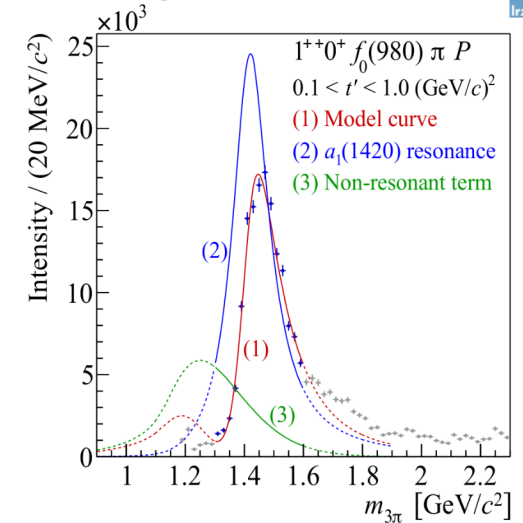


Clear Establishment of exotic meson !
 COMPASS could reconcile dispute from previous experiment : analysis artifact

Exotic: Observation of $a_1(1420)$

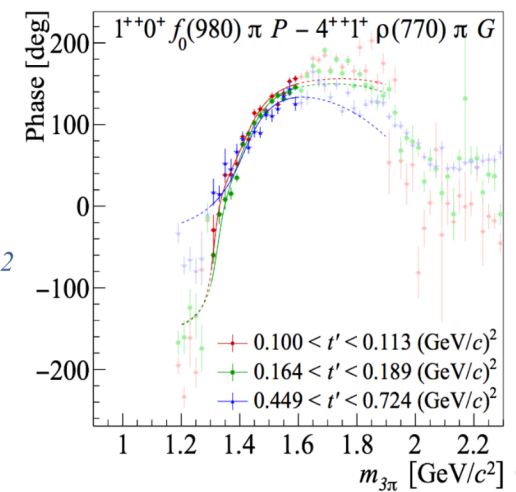
axialvector ($J^{PC} = 1^{++}$) decaying into $f_0(980)\pi$ (P-wave)

- small signal (10^{-3}) compared to dominant $\rho(770)\pi$ (S-wave)
- large phase variation
- „narrow“ signal : $\Gamma/M \approx 10\%$



Observation:

- Decay only : $[f_0(980)] \pi P$
- *Mass* : $1413 \pm 15 \pm 13 \text{ MeV/c}^2$
- *Width*: $157 \pm 8 \pm 23 \text{ MeV/c}^2$



Observation of $a_1(1420)$

Observation of $a_1(1420)$

Various explanations proposed for interpretation:

– Dynamics

- Interference of $a_1(1260)$ with Deck amplitude ($\Delta\phi = 180^\circ$ shifted by 100 MeV)
(Berger et al.)

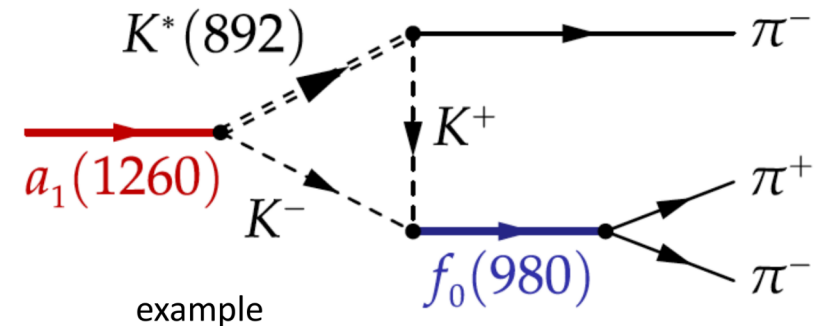
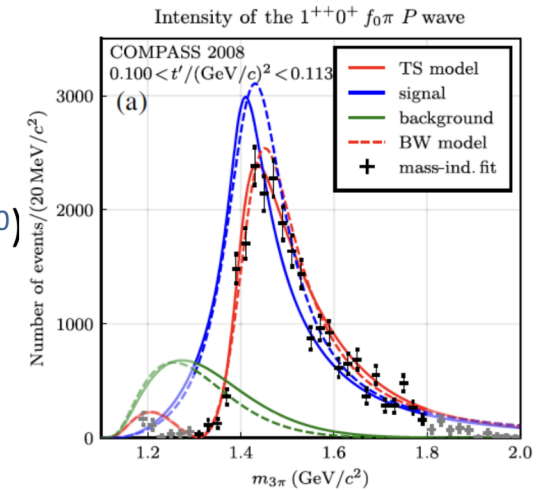
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 $a_1(1260) \rightarrow f_0(980)\pi$ decay shows up 200 MeV above $a_1(1260)$ (Mikhasenko et al.; Aceti et al.)
- Requires same kinematic t dependence for $a_1(1260)$ and $a_1(1420)$

– Molecular structure



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– Molecular structure

- Partner of $f_1(1420)$

– Fit quality equivalent for **BW** and triangular diagram

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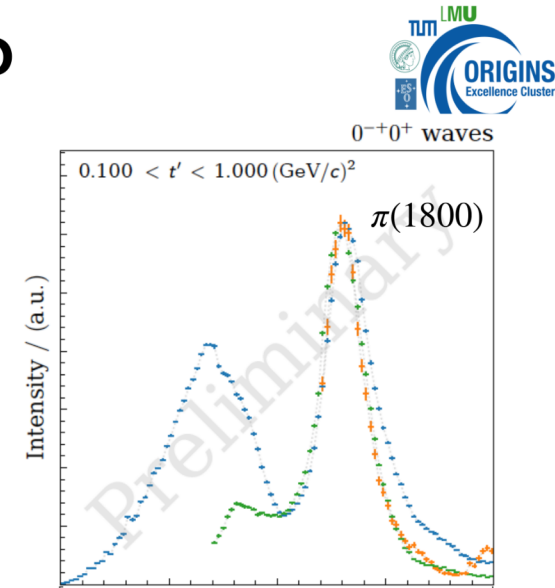
Analysis of 3π τ lepton decays crucial

- ongoing using Belle/Belle 2 data (TUM)

Rabusov HK 29.2

Exotic: A **New** Pionic State ?

- Ground state and radially excited pions have $J^{PC} = 0^{-+}$
- known states: $\pi(140)$, $\pi(1300)$, $\pi(1800)$

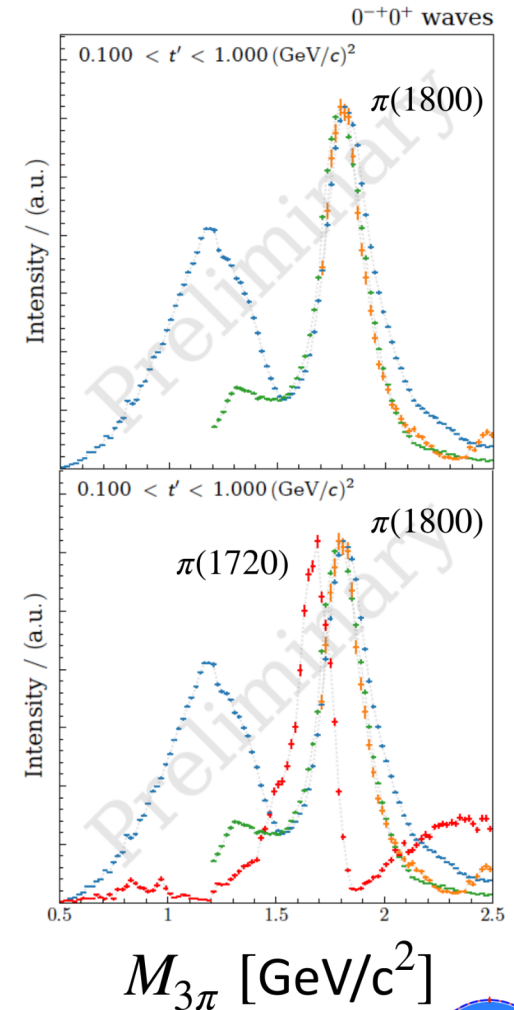


$M_{3\pi}$ [GeV/c²]



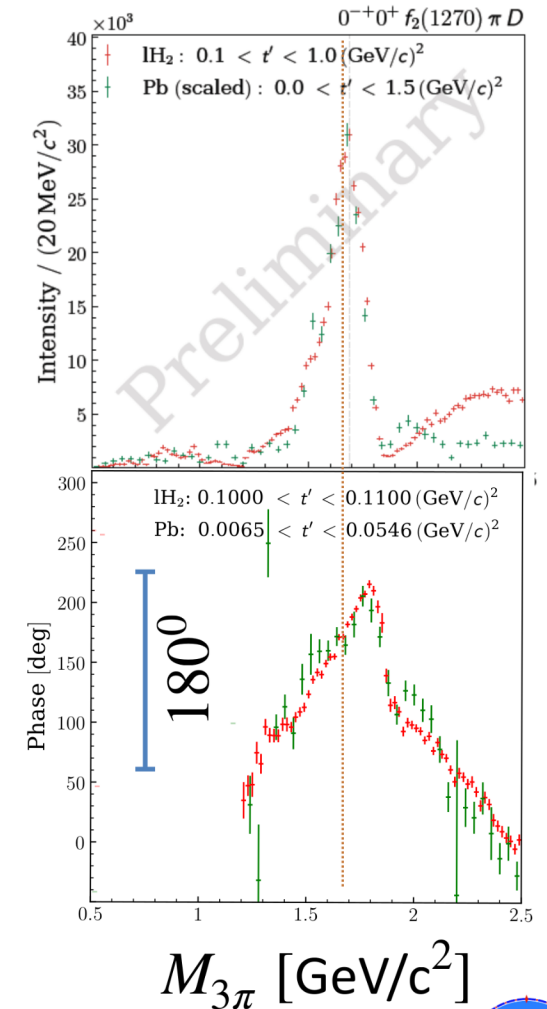
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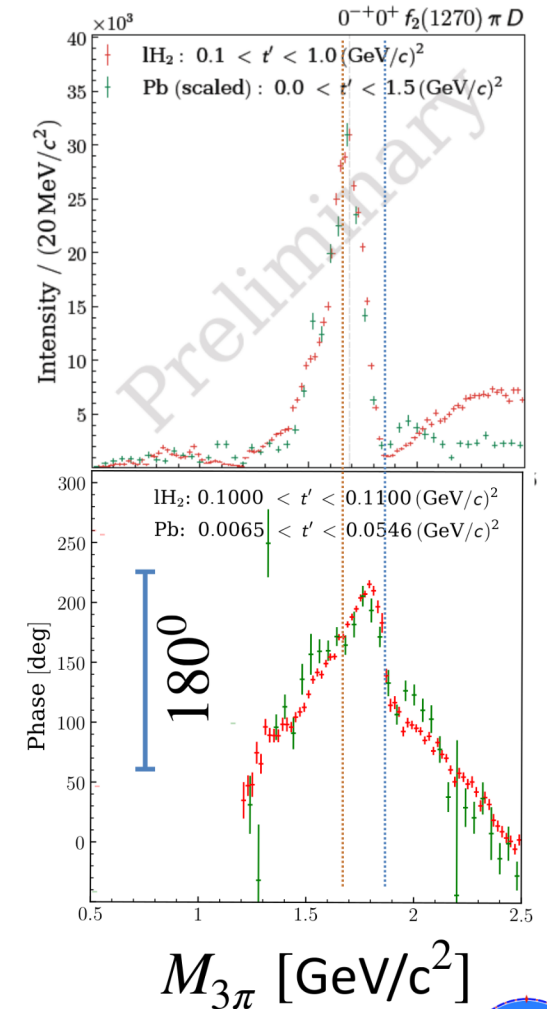
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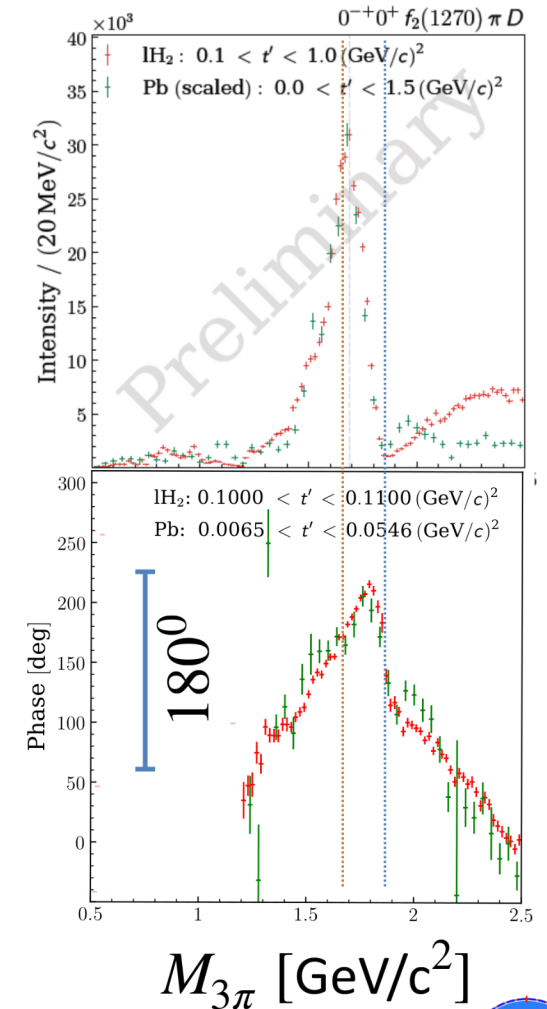
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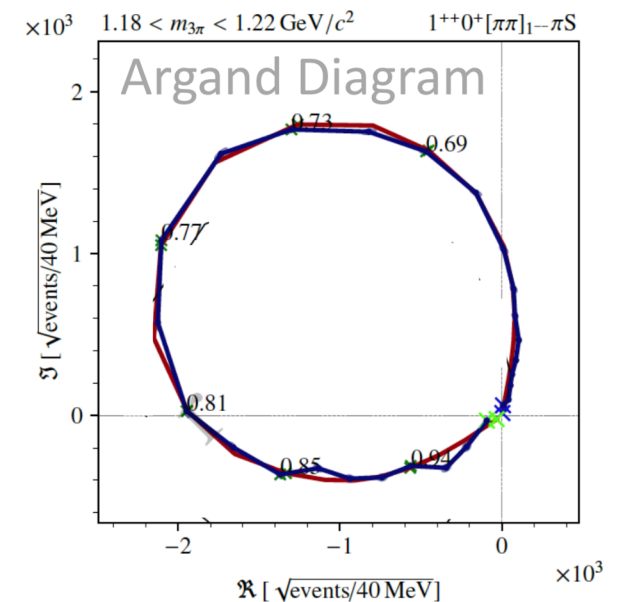
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- Interpretation unclear



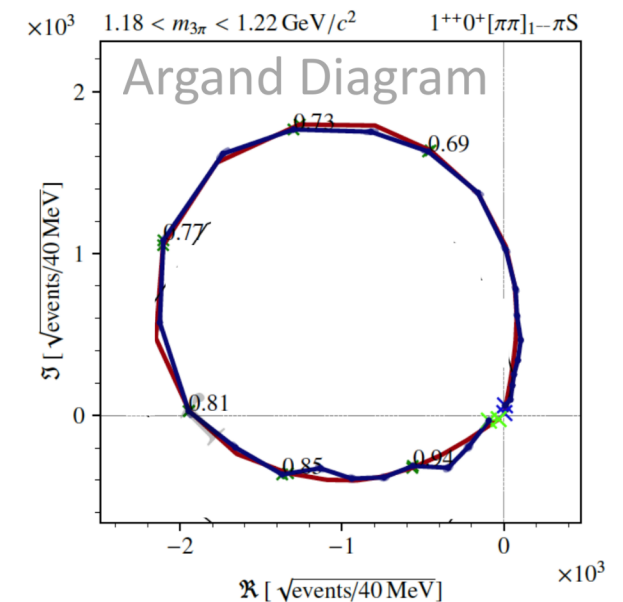
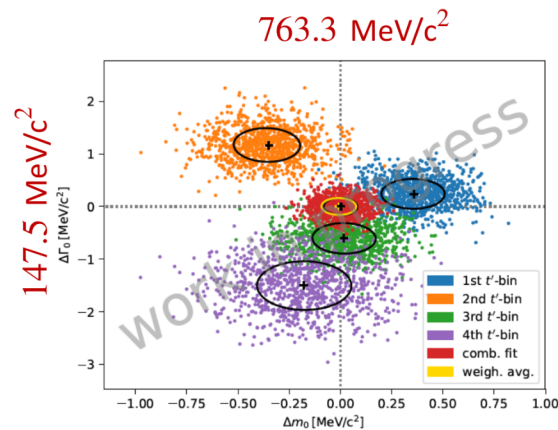
Analyzing the Isobaric Structure

- Novel analysis technique to extract complex amplitudes for 2-body isobars from data
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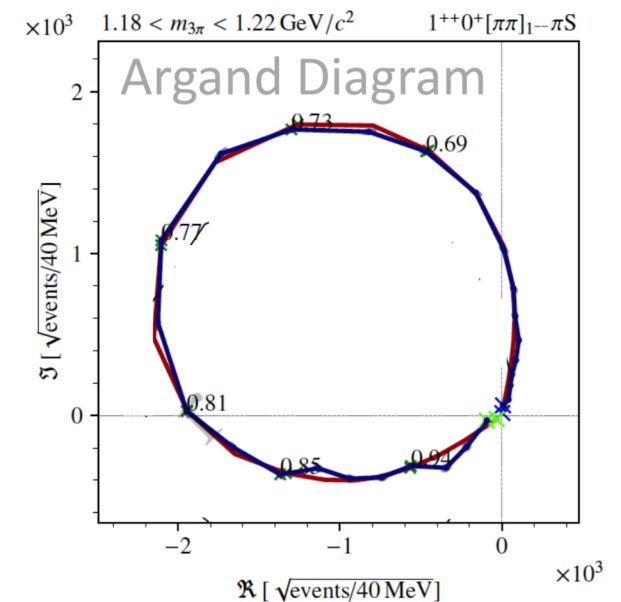
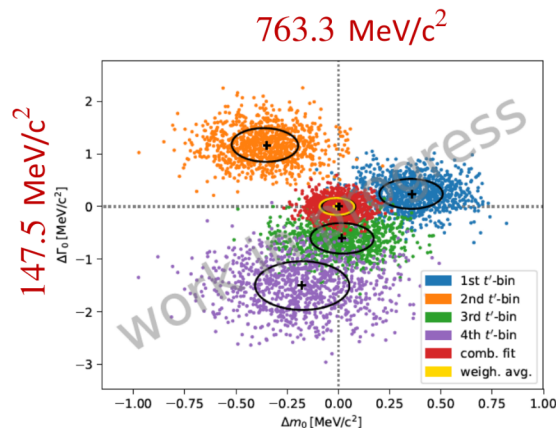


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3-body systematics to be understood



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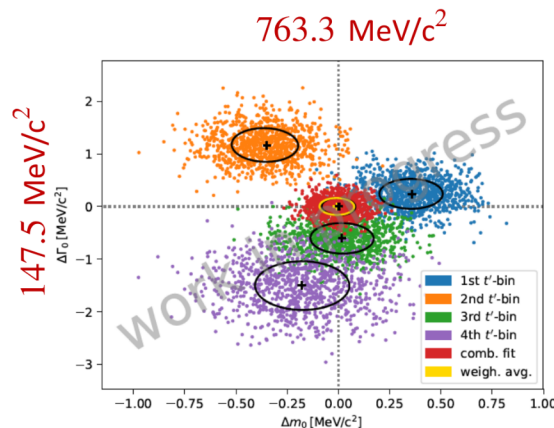
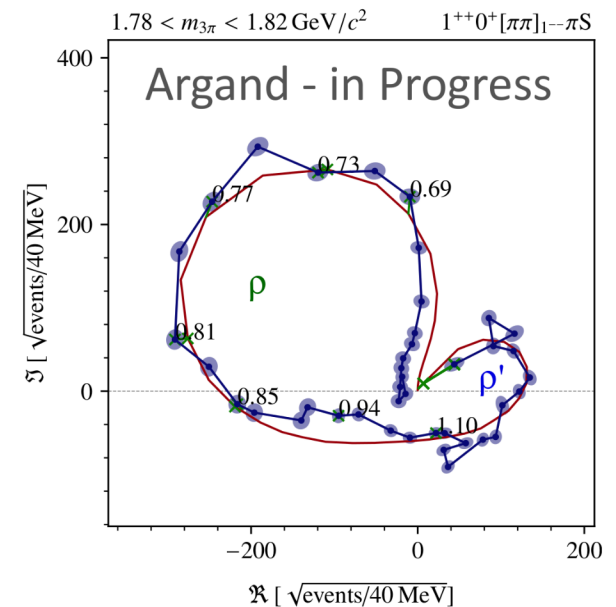
Bartl HK 74.33

*e.g. G. Colangelo, J. Gasser and H. Leutwyler, Nucl. Phys. B **603**, 125 (2001) [hep-ph/0103088].

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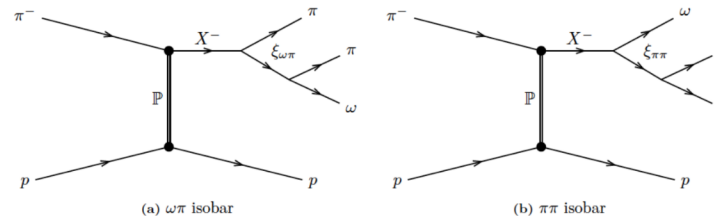
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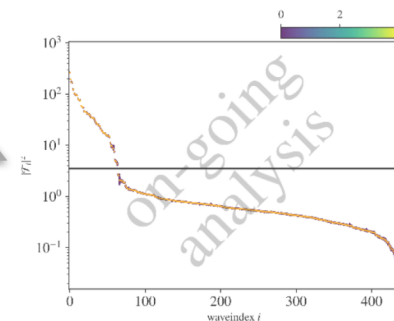


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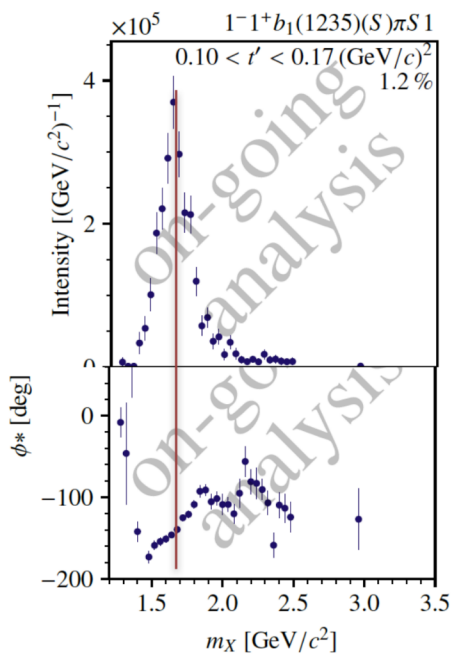
$$\omega\pi\pi \rightarrow 2\pi^-2\pi^0\pi^+$$



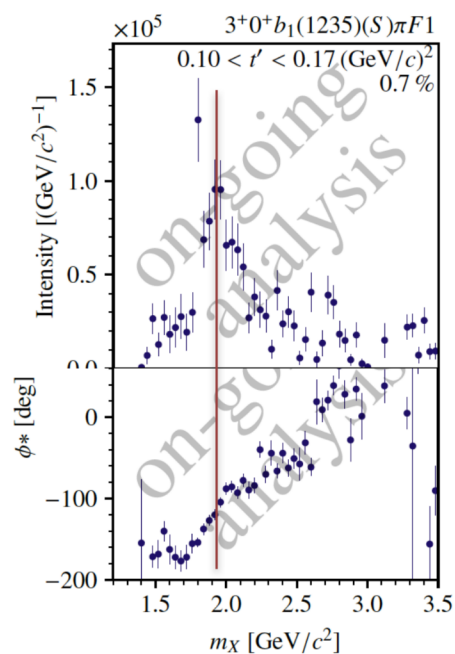
- PWA: automatic wave selection: select 80(*) waves from pool of 434
- most exciting examples in $b_1(1235)\pi \rightarrow (\omega\pi)\pi$:



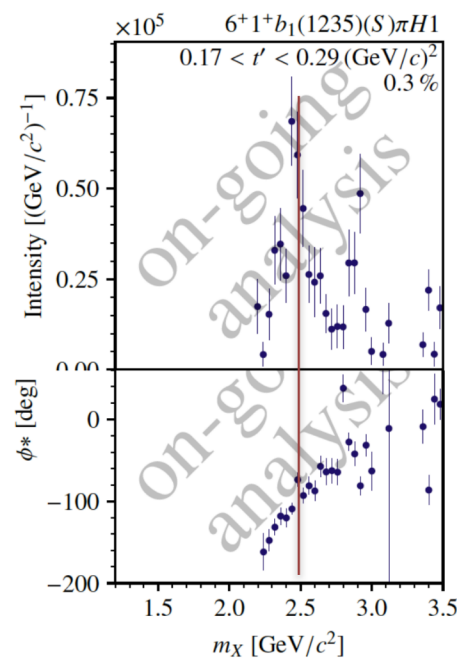
1^{-+} spin-exotic



a_3



a_6



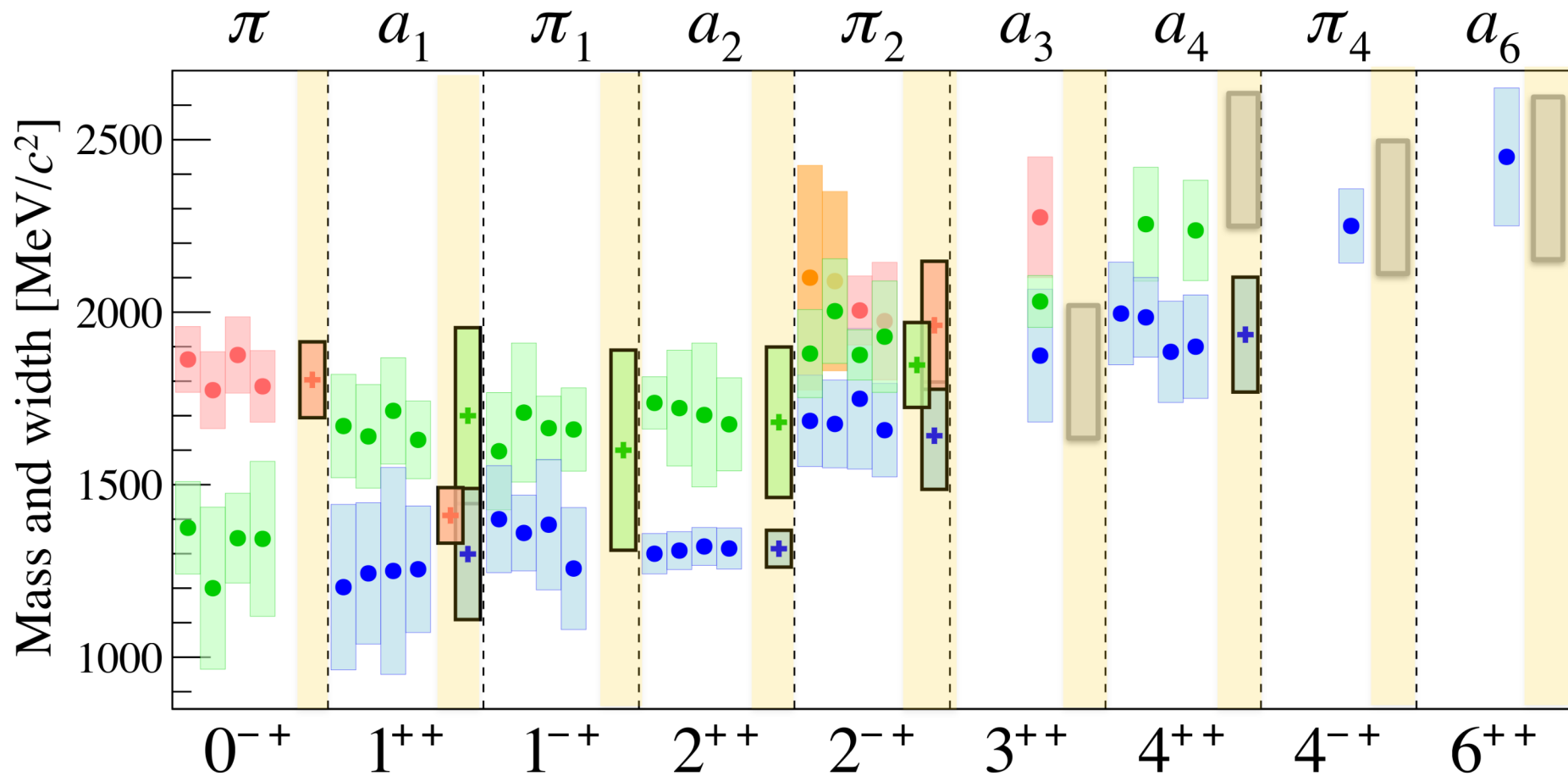
* in total 150 waves appear in various mass ranges

Developments

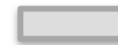
1. Wave selection: use **computer algorithm** and **regularization** on very large „wave pools“
2. **bin-correlated analysis** using NIFTY* (program package used by cosmology)
3. One step data fitting for resonances (**parametric**) and **non-parametric** background across full mass range
4. **Variational inference** (variational Bayes) to estimate uncertainties

*numerical information field theory

The Light Isovector Meson System



- COMPASS found 15 states in a consistent analysis (more on the horizon)

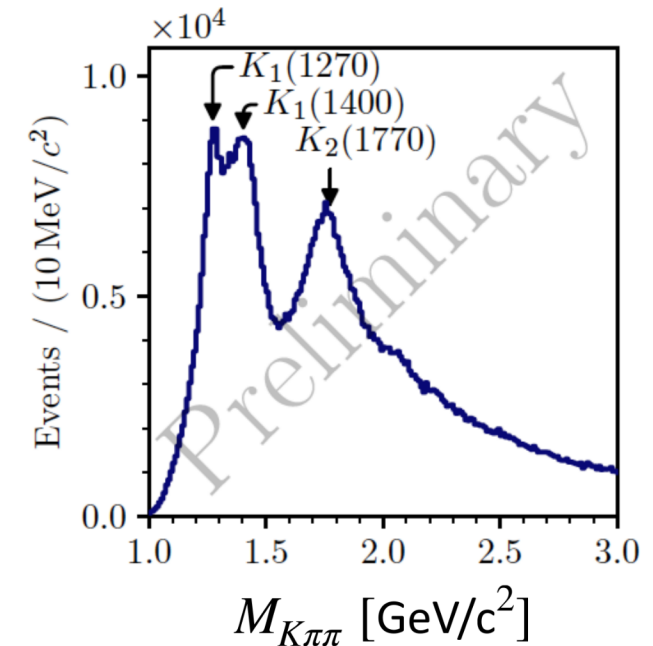


Strangeness

Strange-Meson Spectroscopy

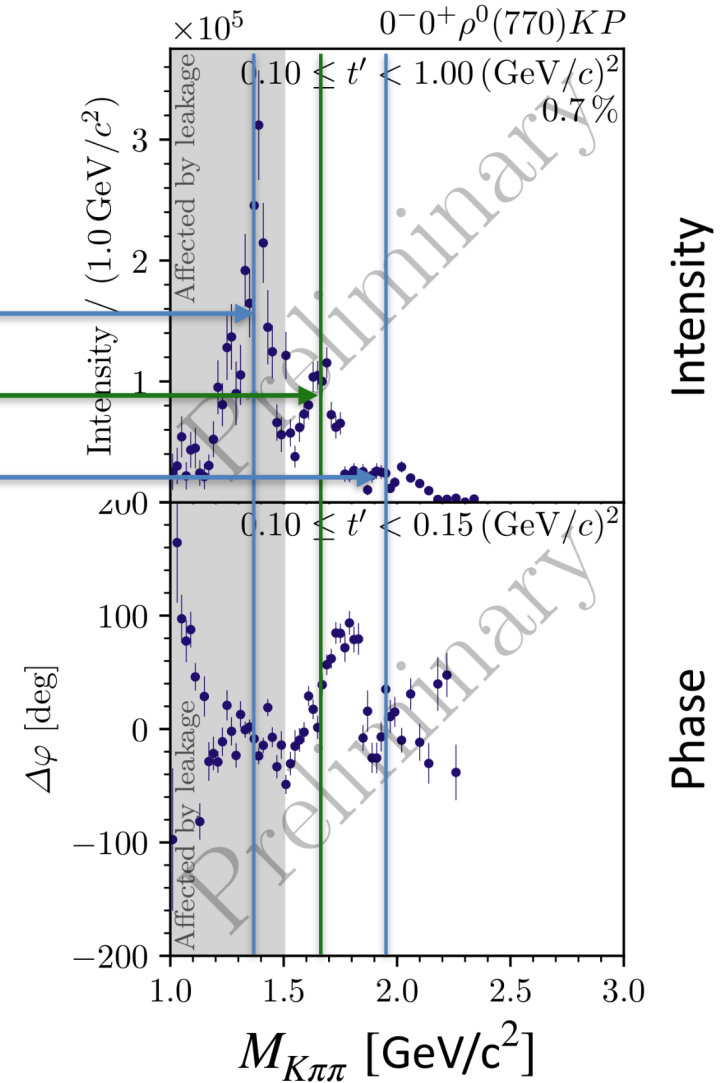
COMPASS hadron beam contains 2.4 % kaons

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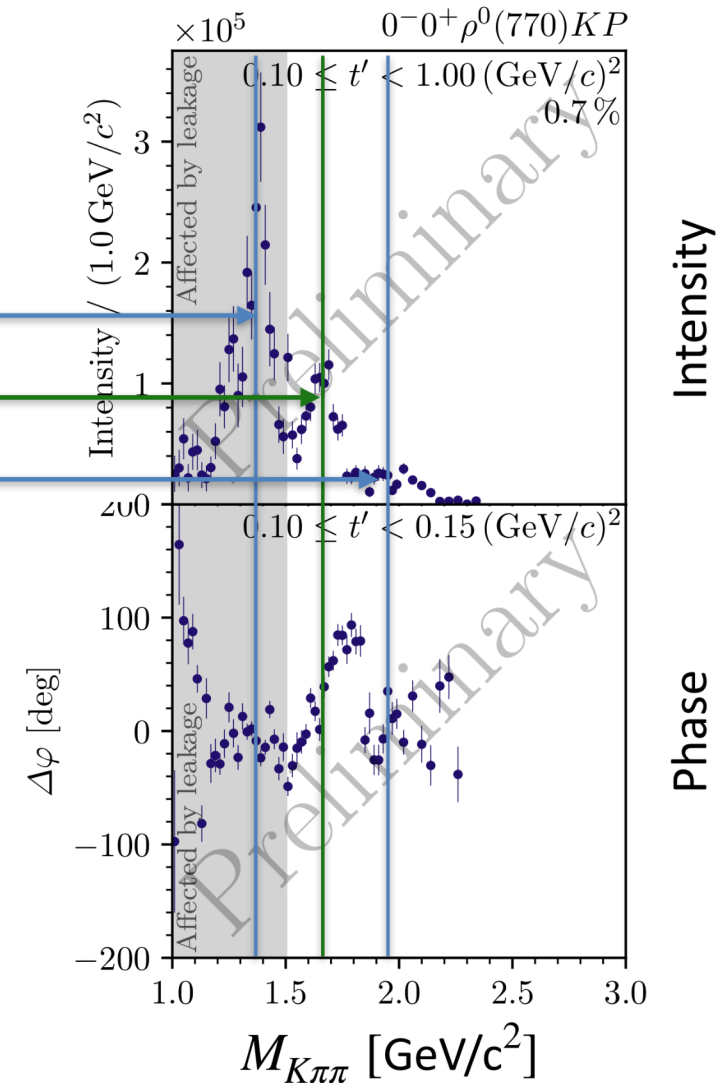
Examples for Excited (and Exotic) Kaons

- $J^P = 0^-$: $K^*(892)\pi$ and $[K\pi]_S\pi$ and $\rho(770)K$
 - $K(1460)$
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Examples for Excited (and Exotic) Kaons

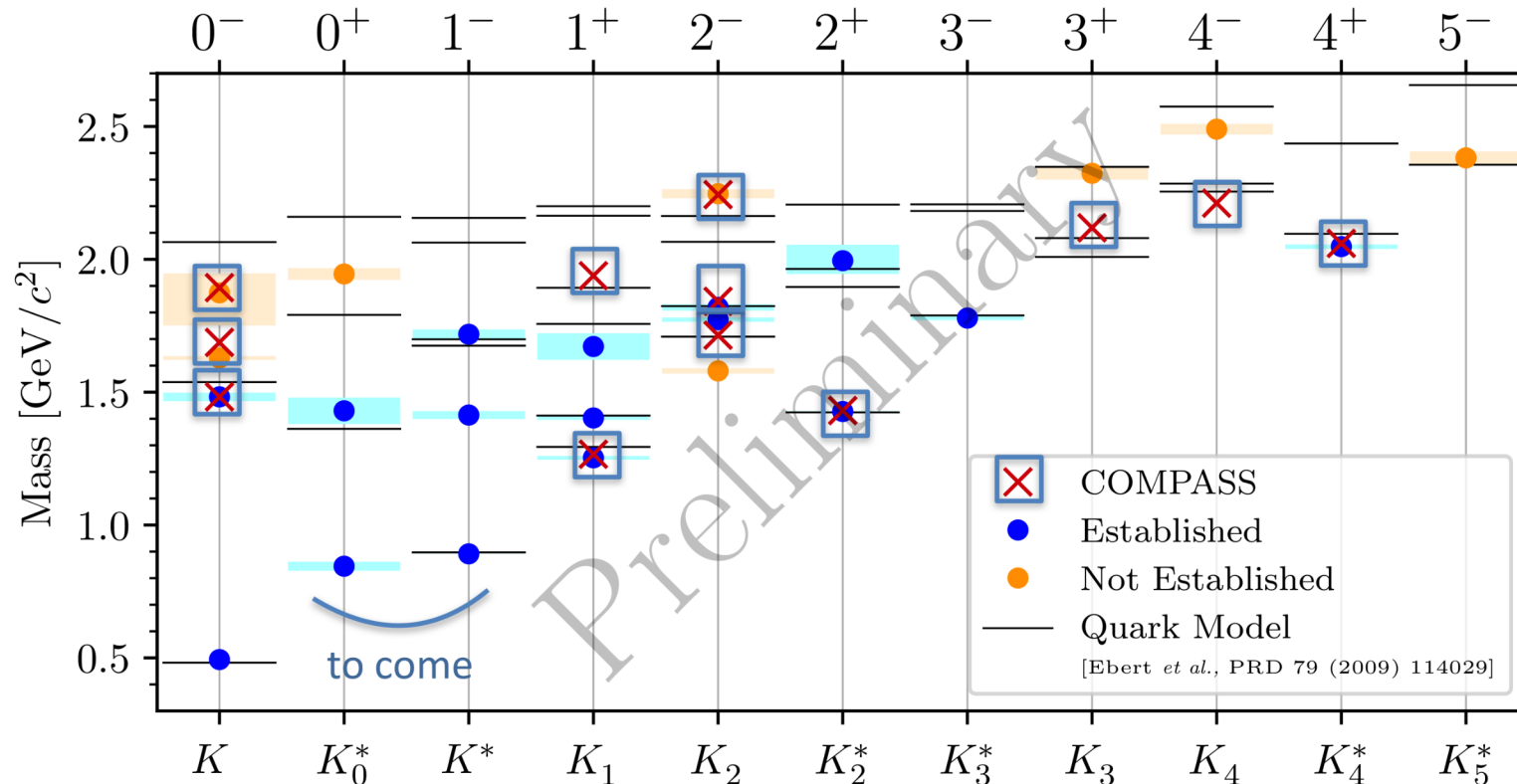
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- supernumerous state likely to be of exotic nature



Summary Strange Mesons

COMPASS will release m_0/Γ of 11 strange mesons using $K^- \pi^- \pi^+$

- $K, K_1, K_2^*, K_2, (K_3^*), K_3, K_4^*, K_4$



- COMPASS found 11 strange mesons - ONE **supernumerous** State (exotic ?)

Topics Not Mentioned

- Measurement of pion polarizability ✓
- Measurement of $\gamma\pi^- \rightarrow \pi^-\pi^+\pi^-, \pi^-\pi^0\pi^0$ (χ EFT fit) ✓
- Measurement of radiative width of excited mesons $a_2(1320)$ and $\pi_2(1670)$ ✓
- $\eta\pi, \eta'\pi$ analysis and the state of $\pi_1(1400)$ and $\pi_1(1600)$ ✓
- Kaon polarizability ✓
- SU(3) χ EFT ✓
- Nuclear effects in π scattering ✓
- Determination of $(K\pi) S - , P - , D -$ wave scattering ✓
- Spectroscopy in 16+ final states ✓

COMPASS Phys.Rev.Lett. 114
(2015) 062002

COMPASS Phys.Rev.Lett. 108
(2012) 192001

COMPASS Eur.Phys.J.A 50
(2014) 79

COMPASS Phys.Rev.Lett. 114 (2015) 062002,
JPAC-COMPASS Phys.Lett.B 779 (2018) 464-472

Vast number of measurements with polarized muons and polarized target on longitudinal and transversal structure of the nucleon

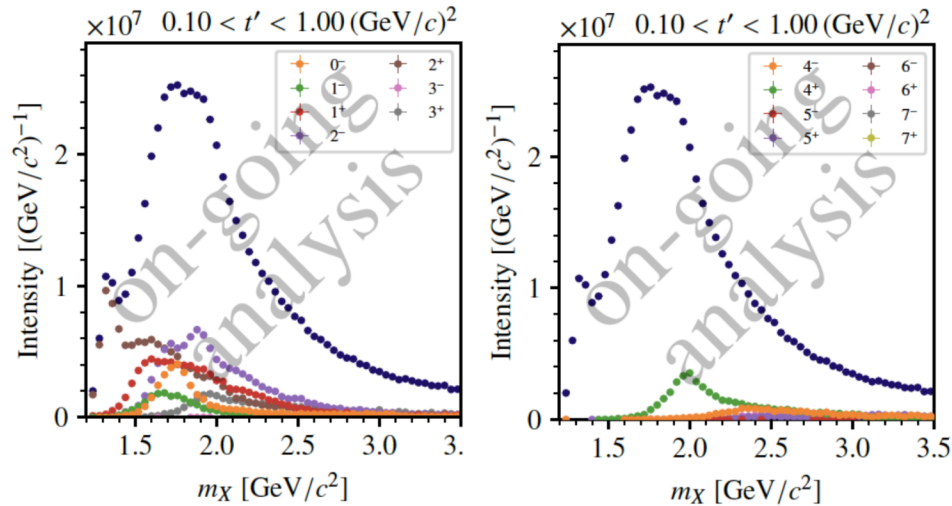
Summary

- COMPASS has made numerous **key measurements**
 - **low energy QCD** phenomena
 - light meson **spectroscopy**
 - systematic exploration of ordinary meson systems
 - **exotic mesons**
 - **new undiscovered phenomena**
- Development of tools necessary
 - **precision measurements** around χ EFT
 - complex **partial wave analysis** and high mass mesons
 - **export technology** to heavy flavor facilities (e.g. D, B-meson decays, τ -lepton decays)
- COMPASS explores **full $SU(3)$ flavor space** (many results to come)
- **AMBER II** offers extension to strangeness sector (10-fold data sample)

Backup $\omega\pi\pi \rightarrow 2\pi^-2\pi^0\pi^+$

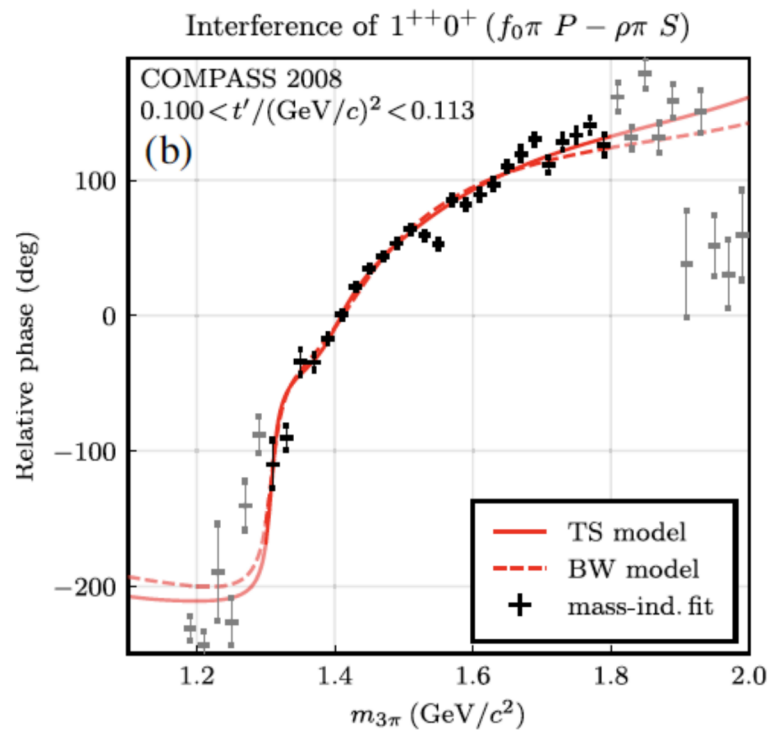
- include $L \leq 7$ for $\xi'\xi$ and use the following isobars

Isobar	Decay channel	m [MeV/ c^2]	Γ [MeV/ c^2]
$\rho(770)^0$	$\pi\pi$	769.0	150.9
$\rho(770)^-$	$\pi\pi$	766.5	150.2
$\rho(1450)$	$\omega\pi$	1465	400
$\rho_3(1690)$	$\omega\pi, \pi\pi$	1688.8	161
$b_1(1235)$	$\omega\pi$	1229.5	142



Backup a1(1420)

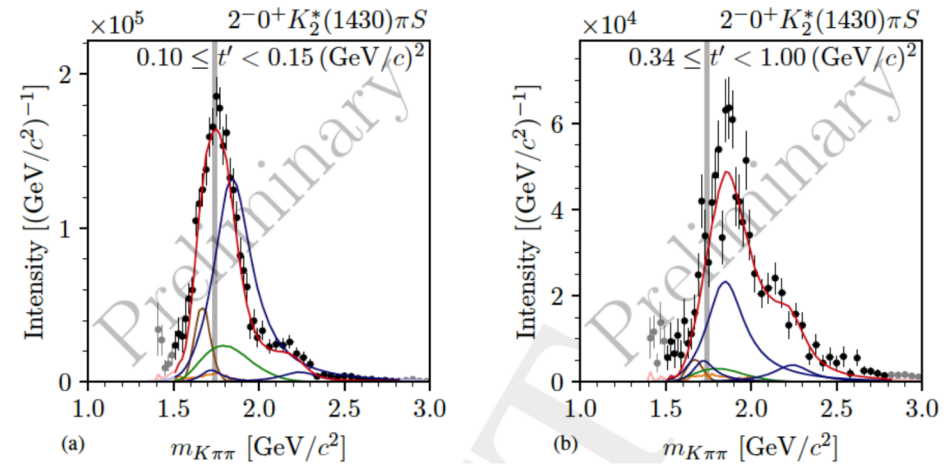
- phase variation w.r.t. main wave



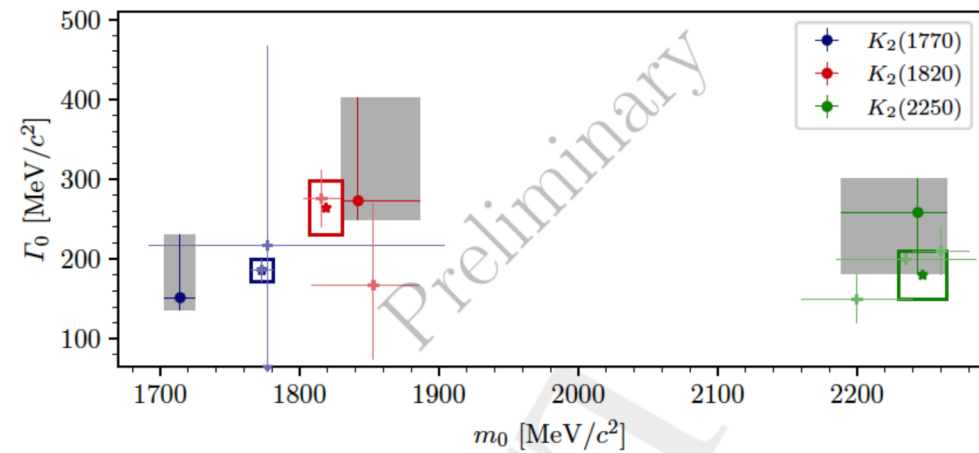
- same fit quality for resonance and triangular singularity

Backup strange mesons K_2

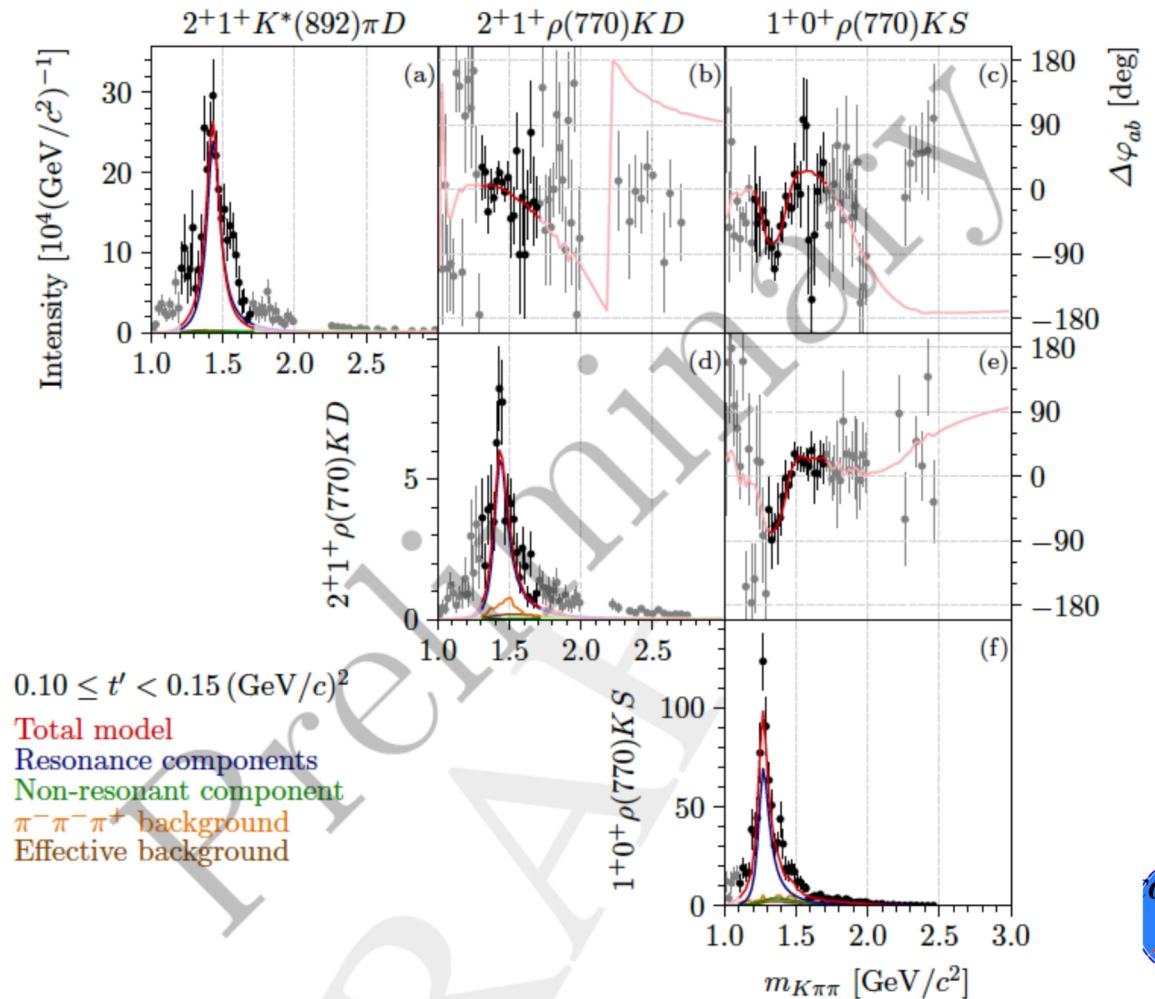
- K_2 : t' dependence (4 t' bins)



- BW parameters: Systematics of fit:



Backup strange mesons K_2^*



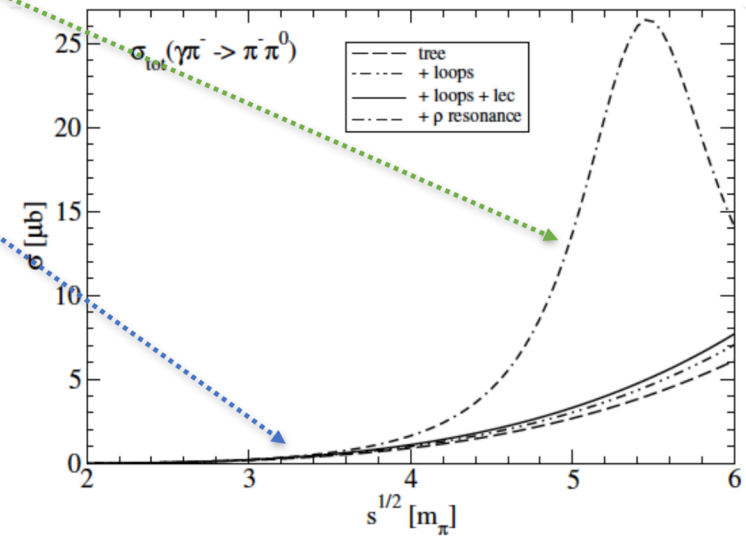
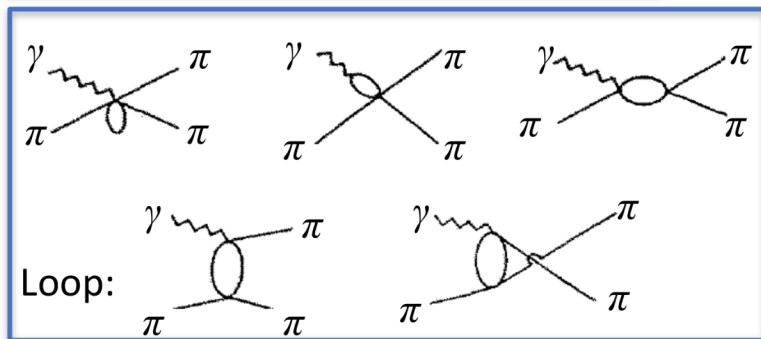
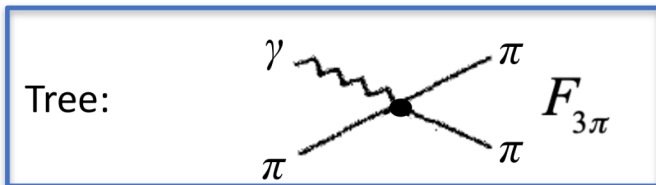
$$\pi^- \gamma^* \rightarrow \pi^- \pi^0$$

$$T_{\gamma 3\pi} \propto \frac{e}{4\pi^2 f_\pi^2} = F_{3\pi} \text{ determined by chiral anomaly of QCD}$$

Antipov et al in Serpukhov:
 $F_{3\pi} = 12.9 \pm 0.9 \pm 0.5 \text{ GeV}^{-3}$
reanalyzed - many systematics

- strong final state interaction:

$$\pi^- \pi^0 \rightarrow \rho \rightarrow \pi^- \pi^0$$



Comparison to Previous Measurements

- COMPASS: First combined measurement of $F_{3\pi}$ and $\Gamma_{\rho \rightarrow \pi\gamma}$

$$F_{3\pi} = (10.3 \pm 0.1_{stat} \pm 0.6_{syst}) \text{GeV}^{-3}$$

$$\Gamma_{\rho \rightarrow \pi\gamma} = (76 \pm 1 \text{ (stat)} \pm_{-8}^{+10} \text{ (syst)}) \text{ keV}$$

- Intensive **study of systematics**:
 - multiple K^- decay modes
 - Various background studies (ω and π exchange)
- Detailed $\pi^- \text{Ni} \rightarrow \pi^- \pi^0 \pi^0 \text{Ni}$ analysis for **diffractive background subtraction**

Expect final uncertainties $\sim 4\%$

Previous measurements (80's):

$$*\Gamma_{\rho \rightarrow \pi\gamma} = (81 \pm 4 \pm 4) \text{ keV}$$

separation of nuclear and Coulomb processes from $d\sigma/dt$

- **Neglect chiral contribution** to $\pi^- \pi^0$
- **No detailed 3π diffractive background** study
- Unresolved beam composition

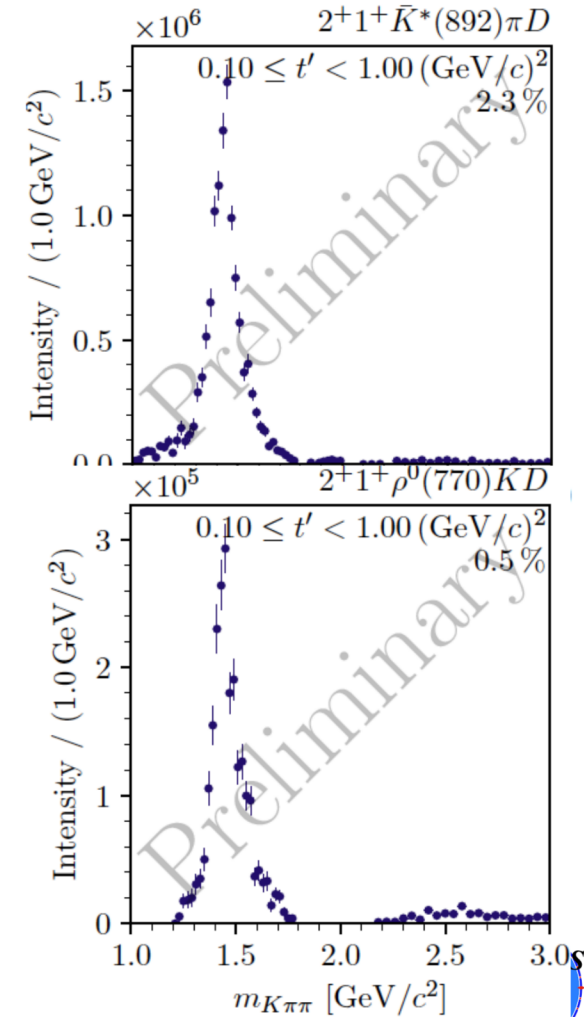
$$**F_{3\pi} = (10.7 \pm 1.2) \text{ GeV}^{-3}$$

- Neglect s -channel production of ρ meson
- No proper consideration of systematics

Examples for Excited (and **Exotic**) Kaons

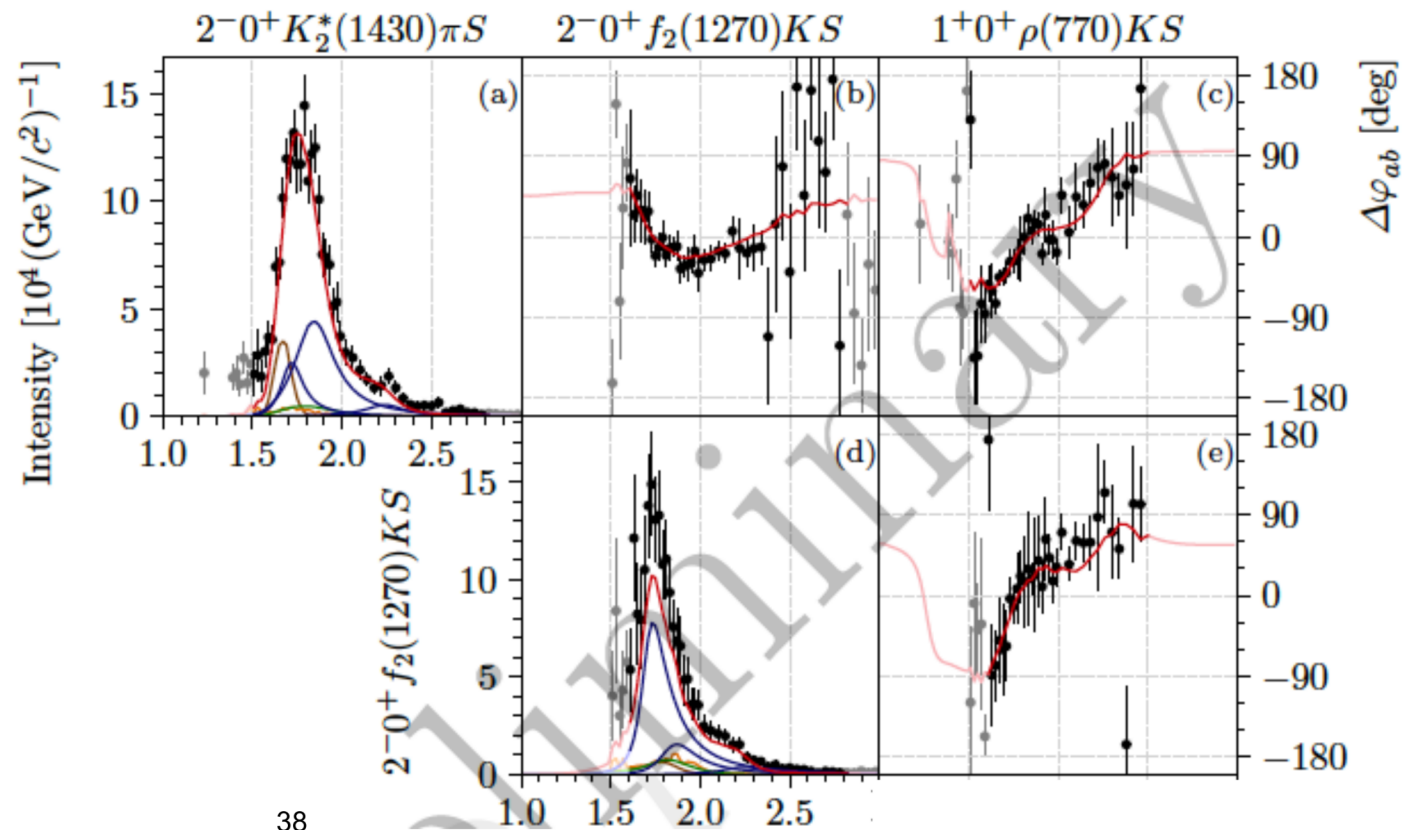
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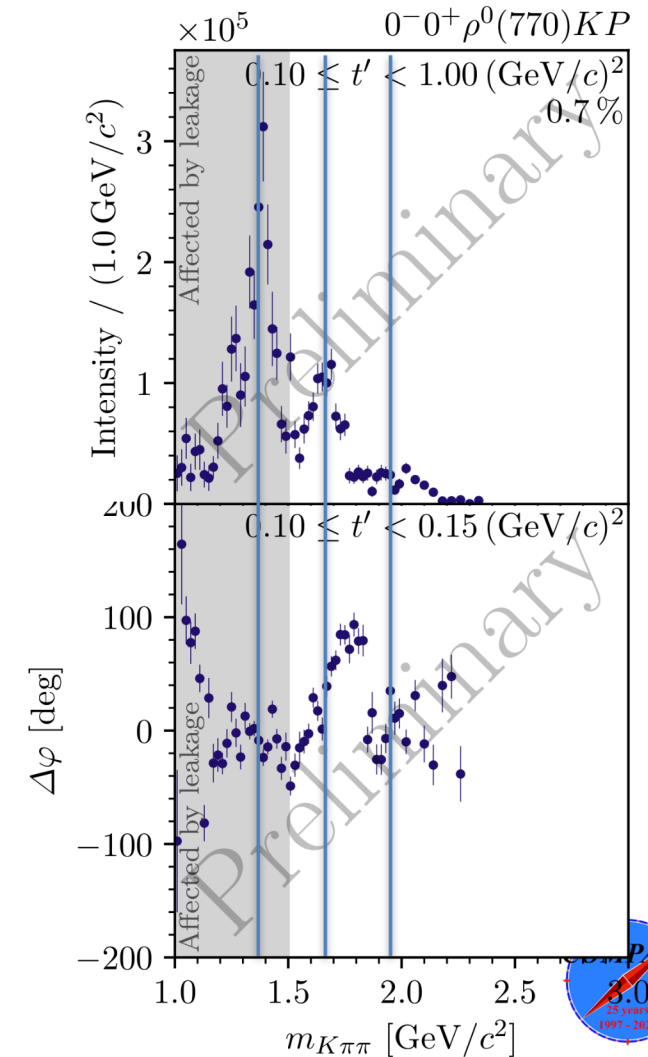
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- $K_2(2250)$ (confirmation)
- coherent fit including all



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Strange-Meson Spectroscopy

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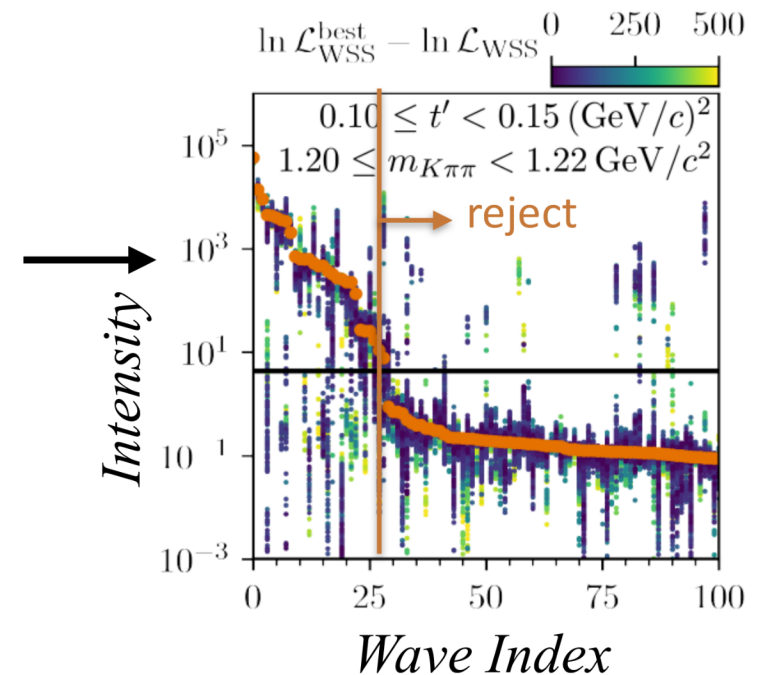
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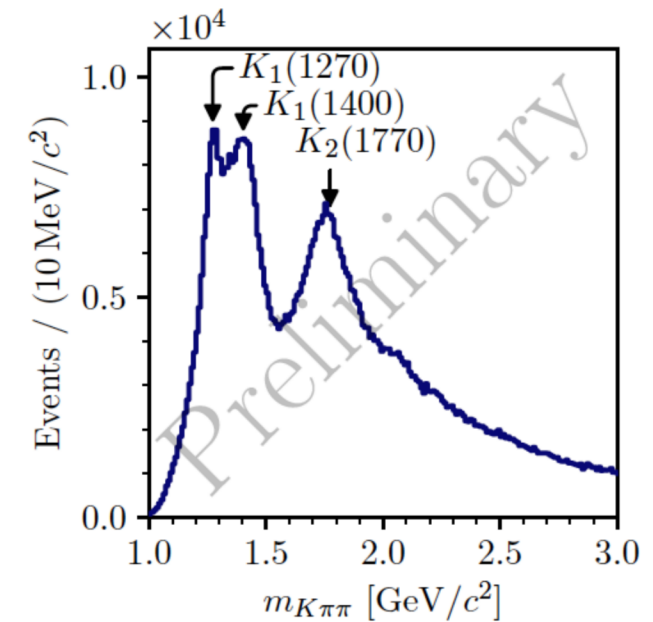
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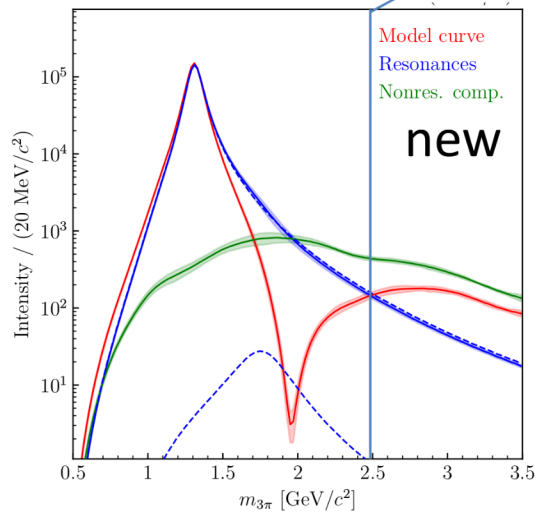
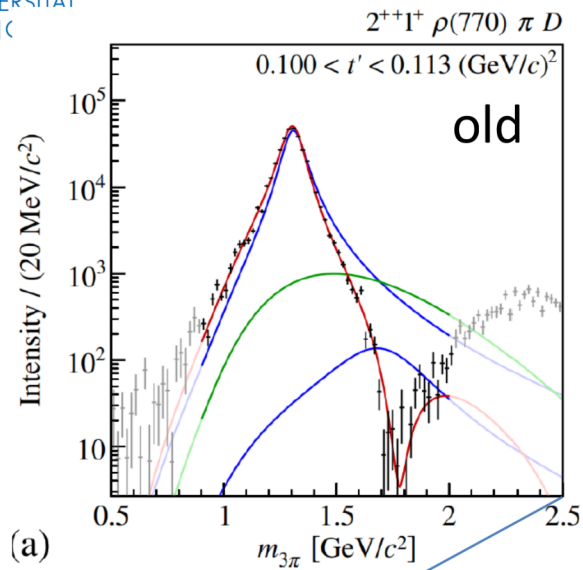
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through incoherent wave set in PWA (novel)



COMPASS Spectroscopic reactions

- $\pi^- p \rightarrow \pi^- \pi^- \pi^+ + p$ ✓
- $\pi^- p \rightarrow \pi^- \pi^0 \pi^0 + p$ ✓
- $\pi^- p \rightarrow \omega \pi^- \pi^0 + p$ ✓
- $\pi^- p \rightarrow \pi^- \pi^- \pi^+ \eta + p$ ✓
- $\pi^- p \rightarrow \pi^- \eta + p$ ✓
- $\pi^- p \rightarrow \pi^- \eta' + p$ ✓
- $\pi^- p \rightarrow \pi^- f_1(1285) + p$ ✓
- $\pi^- p \rightarrow K_s^0 K_s^0 \pi^- + p$ ✓
- $\pi^- p \rightarrow K^- K_s^0 + p$ ✓
- $K^- p \rightarrow K^- \pi^- \pi^+ + p$ ✓
- $K^- p \rightarrow K_s^0 \pi^- + p$ ✓
- $K^- p \rightarrow \Lambda \bar{p} + p$ ✓
- $\pi^- \gamma^* \rightarrow \pi^- \pi^- \pi^+$ ✓
- $\pi^- \gamma^* \rightarrow \pi^- \pi^0 \pi^0$ ✓
- $\pi^- \gamma^* \rightarrow \pi^- \pi^0$ ✓
- $K^- \gamma^* \rightarrow K^- \pi^0$ ✓

Prove of new PWA-Scheme



Prove of new PWA-Scheme

Error bands obtained from
variational Bayes

