

Correlations in partonic and hadronic interactions
Duke University (NC), March 7-12, 2022


Generalized parton distributions at


inclusive or semi-inclusive lepton-proton deep-inleastic scattering

deeply virtual Compton scattering (DVCS)

## Physics questions

How do quarks \& gluons, and their dynamics, make up proton spin?

$$
\underbrace{1 / 2=\mathbf{g l u o n} \text { spin }}_{\text {quark spin }} \begin{gathered}
\text { orbital angular momenta } \\
\text { of quarks and gluons }
\end{gathered}
$$

How is the proton spin correlated with the motion of quarks/gluons?


## Nucleon tomography



How does the proton spin influence
the spatial distribution of partons?


## Generalized Parton Distributions




$$
\int_{-1}^{1} H^{q}(x, \xi, t) \mathrm{d} x=F^{q}(t)
$$


transverse parton positions
longitudinal parton momenta


$$
H^{q}(x, 0,0)=q(x)
$$

PDFs from deep-inelastic
scattering

## Hard exclusive reactions


exclusive measurement = detection of entire final state
(or assumed to be known)

Standard channels to access generalized parton distributions are DVCS \& DVMP

$$
\begin{array}{cc}
\ell p \rightarrow \ell p \gamma & \begin{array}{c}
\text { Deeply Virtual Compton } \\
\text { Scattering (DVCS) }
\end{array} \\
\ell p \rightarrow \ell p M & \text { Deeply Virtual } \\
\text { Meson Production (DVMP) }
\end{array}
$$

- $\quad x, \xi$ : longitudinal momentum fractions of probed quark - skewness $\boldsymbol{\xi} \simeq \boldsymbol{x}_{\boldsymbol{B}} /\left(\mathbf{2}-\mathbf{x}_{\boldsymbol{B}}\right)$ in Bjorken limit ( $Q^{2}$ large \& $x_{B}, t$ fixed) - average momentum $x$ : mute variable, not accessible in DVCS \& DVMP. Is not $x$-Bjorken!
- $t$ : squared 4-momentum transfer to target


## Experimental access to GPDs

- Different exclusive final-state particles allow to probe different GPDs
- 4 chiral-even GPDs (conserve quark helicity)
- 4 chiral-odd GPDs (flip quark helicity)


From HERMES \& JLab-6 \& HERA to COMPASS \& JLab12 \& RHIC to the EIC
$Q^{2}\left[\mathrm{GeV}^{2}\right]$
Start ${ }^{10^{3}}$ 2001 After ${ }^{10}$
2016


## DVCS: Compton form factors (CFFs) $\leftrightarrow$ GPDs

In DVCS, the experimentally accessed quantity is a (complex) Compton Form Factor (CFF):

$$
\mathcal{H}(\xi, t)=\mathcal{P} \int_{-1}^{+1} \mathrm{~d} x \frac{H(x, \xi, t)}{x-\xi}-i \pi H(\xi, \xi, t)
$$

$$
\begin{array}{cc}
\text { CFF hard scattering kernel } \otimes \mathrm{GPD} \\
\mathcal{F}(\xi, t)= & \sum_{q} \int_{-1}^{1} \mathrm{~d} x C_{q}^{\mp}(\xi, x) F^{q}(x, \xi, t)
\end{array}
$$



Dispersion relation with D-term $D(t)$ : related to shear forces and radial distribution of pressure inside the nucleon

$$
\mathcal{R} e \mathcal{H}(\xi, t)=\mathcal{P} \int_{-1}^{+1} \mathrm{~d} x \frac{\operatorname{I} m \mathcal{H}(x, t)}{x-\xi}+D(t)
$$

$\operatorname{Im}\left(\tau_{\mathrm{DVCS}}\right)$
$|x|<\xi$
DDVCS
$\operatorname{Re}\left(\tau_{\mathrm{DVCs}}\right)$ integral over $\boldsymbol{x}$


CERN SPS polarized muon beams and COMPASS polarized target


- Polarization determined with Nuclear Magnetic Resonance (NMR)


COMPASS GPD measurements 2012 \& 2016/17


## Selection of exclusive event sample

DVMP without recoil-proton detection: missing energy technique assuming proton mass

## Exclusive $\varrho^{\mathbf{0}}{ }^{\text {p }}$ production

$$
\mu p^{(\uparrow)} \rightarrow \mu p \varrho^{0}
$$

with simulated exclusive signal \& SIDIS background

In case of transverse target polarization: additional azimuthal angle $\phi_{S}$ defined by direction of transverse target-polarization vector

DVCS with recoil-proton detector (RPD): comparison of proton kinematics measured in RPD vs. expected in spectrometer (from $\mu \gamma$ )


+ kinematically complete event reconstruction via kinematic event fitting
$\phi$-modulation in cross section (azimuthal asymmetry analysis)

DVCS


Analysis of azimuthal modulations (HERMES- and JLab-type) on DVCS on the unpolarized proton in progress

$$
\text { DVCS } \quad \text { Bethe-Heitler }(\mathrm{BH})
$$

dominant at small $X_{\mathrm{B}}$ (remainder $\sim 5 \%$ from KM / GK model)

The DVCS / Bethe-Heitler interference term allows to disentangle $\operatorname{Re}\left(\tau_{\text {DVCS }}\right)$ and $\operatorname{Im}\left(\tau_{\text {DVCS }}\right)$ magnitude and phase of DVCS amplitude $\tau_{\text {DVCS }}$

$$
\mathcal{S}_{C S, U} \equiv \mathrm{~d} \sigma^{ \pm}+\mathrm{d} \sigma^{\ddagger}
$$

$$
\mathcal{D}_{C S, U} \equiv \mathrm{~d} \sigma^{ \pm}-\mathrm{d} \sigma^{\rightrightarrows}
$$

$$
\mathcal{A}_{C S, U} \equiv \frac{\mathrm{~d} \sigma^{ \pm}-\mathrm{d} \sigma^{\bar{\mp}}}{\mathrm{d} \sigma^{ \pm}+\mathrm{d} \sigma^{\mp}}=\frac{\mathcal{D}_{C S, U}}{\mathcal{S}_{C S, U}}
$$

Spin-independent DVCS cross section $\propto$

$$
4\left(\mathcal{H} \mathcal{H}^{*}+\tilde{\mathcal{H}} \tilde{\mathcal{H}}^{*}\right)+\frac{t}{M^{2}} \mathcal{E E}^{*}
$$

$\operatorname{Im}\left(F_{1} \mathcal{H}+\xi\left(F_{1}+F_{2}\right) \tilde{\mathcal{H}}-\frac{t}{4 M^{2}} F_{2} \mathcal{E}\right)$
$\operatorname{Re}\left(F_{1} \mathcal{H}+\varepsilon\left(F_{1}+F_{2}\right) \tilde{\mathcal{H}}-\frac{t}{4 M_{2}} F_{2} \mathcal{E}\right)$
leading twist (twist 2)
on the proton


Sign \& magnitude of $\cos \phi$ amplitude for beam-charge asymmetry? (changes sign between HERMES and HERA)

Kroll, Moutarde, Sabatié, Eur. Phys. J. C (2013) 73:2278

Test of GPD universality: use DVMP data to constrain GPD parameters

DVCS cross section / transverse imaging

Impact-parameter representation of parton distribution function:
$q^{f}\left(x, \boldsymbol{b}_{\perp}\right)=\int \frac{\mathrm{d}^{2} \boldsymbol{\Delta}_{\perp}}{(2 \pi)^{2}} e^{-i \boldsymbol{\Delta}_{\perp} \cdot \boldsymbol{b}_{\perp}} H^{f}\left(x, 0,-\boldsymbol{\Delta}_{\perp}^{2}\right)$
[Burkardt, Int. J. Mod. Phys. A18 (2003) 173]
"spatial parton density = Fourier transform of GPD"
$\boldsymbol{b}_{\perp}$ is the impact parameter,
$\boldsymbol{\Delta}_{\perp}$ is the difference of initial and final transverse momenta,
$\boldsymbol{\Delta}_{\perp}{ }^{2}$ is related to the Mandelstam- $t$
The differential DVCS cross section allows to probe the transverse extension of partons in the nucleon:

$$
\frac{\mathrm{d} \sigma^{\mathrm{DVCS}}}{\mathrm{~d} t} \propto e^{-b|t|}
$$

$\mathrm{b}=$ " $t$-slope" = average impact parameter

## Extraction of pure DVCS yield at COMPASS

DVCS cross section / transverse imaging

$$
\left|\mathcal{T}_{\mathrm{BH}}\right|^{2}+\left(\mathcal{T}_{\mathrm{DVCS}} \mathcal{T}_{\mathrm{BH}}^{*}+\mathcal{T}_{\mathrm{DVCS}}^{*} \mathcal{T}_{\mathrm{BH}}\right)+\left|\mathcal{T}_{\mathrm{DVCS}}\right|^{2}
$$



## Extraction of pure DVCS yield at COMPASS




## DVCS / BH: $\mu \mathrm{p} \rightarrow \mu \mathrm{p} \gamma$

$\pi^{0}$ production: $\mu \mathrm{p} \rightarrow \mu \mathrm{p} \pi^{0} \rightarrow \mu \mathrm{p} \gamma(\gamma)(\mathrm{X})$ exclusive or SIDIS $\gamma \gamma$ : "visible $\pi^{0 "}$ " $\gamma$ : invisible $\pi^{0}$ background

Determine BH reference yield at low- $x_{B} \Leftrightarrow$ high-v: tune MC to data


## COMPASS $\phi$-integrated DVCS cross section

- Relation between parton average squared transverse extension and slope

$$
\left\langle r_{\perp}^{2}\left(x_{\mathrm{Bj}}\right)\right\rangle \approx 2\left\langle B\left(x_{\mathrm{Bj}}\right)\right\rangle \hbar^{2}
$$

- Sea-quark domain between gluons and valence-quarks
- Pilot run: $<Q^{2}>=1.8 \mathrm{GeV}^{2} \&<x_{\mathrm{Bj}}>=0.056$ 2016/17 run: $<Q^{2}>=1.8 \mathrm{GeV}^{2} \&<x_{\mathrm{Bj}}>=0.063$ (ECalO extension)
- So far, $\lesssim 30 \%$ of COMPASS cross-section data analyzed.

2016/17 ( $\approx 23 \%$ )
2012

- COMPASS: $\left\langle Q^{2}\right\rangle=1.8(\mathrm{GeV} / c)^{2} \quad$ This Analysis


DVCS cross section / transverse imaging

$$
\frac{\mathrm{d} \sigma^{\mathrm{DVCS}}}{\mathrm{~d} t} \propto e^{-b|t|}
$$

Differential DVCS cross section with $b($ or $B)=" t$-slope" = average impact parameter

COMPASS: $\left\langle Q^{2}\right\rangle=1.8(\mathrm{GeV} / \mathrm{c})^{2} \quad$ Phys. Lett. B793 (2019) 188 ZEUS: $\left.\quad<Q^{2}\right\rangle=3.2(\mathrm{GeV} / \mathrm{c})^{2} \quad$ JHEP 0905 (2009) 108 H1: $\left.\quad<Q^{2}\right\rangle=4.0(\mathrm{GeV} / \mathrm{c})^{2}$ \} Eur. Phys. C44 (2005) 1
$\left\langle Q^{2}\right\rangle=10 .(\mathrm{GeV} / \mathrm{C})^{2} \quad$ Phys. Lett. B 681 (2009) 391 $\left.\left\langle Q^{2}\right\rangle=8.0(\mathrm{GeV} / c)^{2}\right\}$


## Exclusive meson production

| chiral-even GPDs at leading twist |  | chiral-odd GPDs at higher twist |
| :---: | :---: | :---: |
| H, E | JP $=1$ <br> vector <br> mesons |  |
| $\tilde{\mathrm{H}}$ | $\begin{gathered} \mathrm{JP}^{\mathrm{P}}=\mathrm{O}^{-} \\ \text {pseudoscalar } \\ \text { mesons } \end{gathered}$ | $\overline{\mathrm{E}}_{\mathrm{T}}=2 \mathrm{H}_{\mathrm{T}}+\mathrm{E}_{\mathrm{T}}$ |
| longitudinally polarized virtual photon \& vector meson) |  |  |

- Different mesons filter different quark flavors and have different sensitivity to gluon GPDs.

$$
\begin{aligned}
E^{\rho^{0}} & =\frac{1}{\sqrt{2}}\left(\frac{2}{3} E^{u}+\frac{1}{3} E^{d}+\frac{3}{4} E^{g}\right) \\
E^{\omega} & =\frac{1}{\sqrt{2}}\left(\frac{2}{3} E^{u}-\frac{1}{3} E^{d}+\frac{3}{4} E^{g}\right) \\
E^{\phi} & =-\frac{1}{3} E^{s}+\frac{1}{8} E^{g}
\end{aligned}
$$



## Spin density matrix elements in $\mu p \rightarrow \mu p V M$



- Tests of hierarchy of helicity amplitudes
- Cross-section ratio $R$ of longitudinal to transverse vector mesons,...
$R^{\prime}=\frac{1}{\varepsilon} \frac{r_{00}^{04}}{1-r_{00}^{04}}$
- Sensitivity to chiral-odd GPDs $\boldsymbol{H}_{\mathrm{T}}$ and $\overline{\boldsymbol{E}}_{\mathrm{T}}$.

[COMPASS EPJC (2021) 81126]

SDMEs $\mu$ p $\rightarrow \mu$ p $^{0}$ to be published


Dip at small $|t|$ indicative of large effect by chiral-odd GPD $\bar{E}_{\mathrm{T}}$

$$
\left[\left(1-\xi^{2}\right)|\langle\tilde{H}\rangle|^{2}-2 \xi^{2} \operatorname{Re}\left[\langle\tilde{H}\rangle^{*}\langle\tilde{E}\rangle\right]-\frac{t^{\prime}}{4 M^{2}} \xi^{2}|\langle\tilde{E}\rangle|^{2}\right]
$$




## Summary and outlook: GPDs at

- 2012 GPD pilot run \& 2016/17 GPD runs with recoil-proton detector Transverse runs without recoil-proton detector
- DVCS: transverse extension of partons in the proton
- $t$-slope of DVCS cross section in the kinematic domain between the other fixed-target experiments and HERA ep collider
- Azimuthal asymmetry analysis ongoing
- DVMP: input for GPD constraints, in particular chiral-odd GPDs
- Transverse target spin asymmetries for $\varrho^{0}$ and $\omega$ vector mesons
- SDMEs for $\varrho^{0}$ and $\omega$ vector mesons
- $\pi^{0}$ cross section
- More data are being analyzed.


## References

HEPGEN:
M.Gorzellik, PhD thesis, University of Freiburg (2018)
A. Sandacz and P. Sznajder, arXiv:1207.0333[hep-ph]

GK model:
S. V. Goloskokov and P. Kroll, Eur. Phys. J. C 42 (2005) 281 S. V. Goloskokov and P. Kroll, Eur. Phys. J. C 53 (2008) 367 S. V. Goloskokov and P. Kroll, Eur. Phys. J. C 65 (2010) 137 KM15 model:
K. Kumericki and D. Müller, Nucl. Phys. B 841 (2010) 1
K. Kumericki and D. Müller, EPJ Web Conf. 112 (2016) 01012

## Backup

## COMPASS DVCS 2016 data - 1D exclusivity cuts



COMPASS DVCS 2016 data - BH data vs. MC, $80<n u<144 \mathrm{GeV}$

(incoming muon)
exclusive variables






## COMPASS DVCS 2016 data - invariant mass of visible $\pi^{0}$



## COMPASS DVCS 2016 data - $\phi \gamma^{* *}$ distributions


$32<v[\mathrm{GeV}]<80$


$$
10<v[\mathrm{GeV}]<32
$$



## Selection of exclusive data sample



HERMES \& COMPASS excl. @:



## closs

CLAS DVCS:
no Inner Calo: ep or ep $\gamma$
with Inner Calo: ep $\gamma$
zeus
H1/ZEUS DVCS:
e $\gamma+$ forward veto
ZEUS subsample: ep $\gamma$

## Experimental access to CFFs at HERMES \& JLab

## DVCS




$$
\sigma\left(\phi ; P_{B}, C_{B}\right)=\sigma_{\mathrm{UU}}(\phi) \cdot\left[1+P_{B} \mathcal{A}_{\mathrm{LU}}^{\mathrm{DVCS}}(\phi)+P_{B} C_{B} \mathcal{A}_{\mathrm{LU}}^{\mathcal{I}}(\phi)+C_{B} \mathcal{A}_{C}(\phi)\right]
$$

Different experimental configurations (beam polarization, beam charge, target polarization, and their combinations) provide access to different parts or aspects of CFFs.

## Different experimental configurations to map out CFFs

$\underset{\text { polarization }}{$| $\mathcal{A}_{\text {LU }}$ |
| :---: | :---: |
| $\downarrow \downarrow$ |
|  Bear  |$}$| $\rightarrow$ target spin |
| :---: |
| $\rightarrow$ beam spin |
| + beam charge |

unpolarized target:


$$
\left.\mathcal{A}_{\mathrm{LU}}(\phi) \equiv \frac{d \sigma^{\rightarrow}-d \sigma^{\leftarrow}}{d \sigma^{\rightarrow}+d \sigma^{\leftarrow}} \quad \begin{array}{c}
\text { Beam-helicity } \\
\text { asymmetry } \\
\text { More Fourier coefficients accessible } \\
\text { with } 2 \text { beam charges }
\end{array}\right]
$$

## Compton Form Factors (CFFs)

longitudinally polarized target:

$$
\begin{array}{r}
\frac{x_{B}}{2-x_{B}}\left(F_{1}+F_{2}\right)\left(\mathcal{H}+\frac{x_{B}}{2} \mathcal{E}\right) \\
+F_{1}\left(\tilde{\mathcal{H}}-\frac{x_{B}}{2-x_{B}}\left(\frac{x_{B}}{2} F_{1}+\frac{t}{4 M^{2}} F_{2}\right) \widetilde{\mathcal{E}}\right.
\end{array}
$$

$\mathcal{A}_{\mathrm{UL}}\left(\phi, e_{\ell}\right) \equiv$ Longitudinal target-spin asymmetry
$\frac{\left[\sigma^{\leftarrow \Rightarrow}\left(\phi, e_{\ell}\right)+\sigma^{\rightarrow \Rightarrow}\left(\phi, e_{\ell}\right)\right]-\left[\sigma^{\leftarrow \Leftarrow}\left(\phi, e_{\ell}\right)+\sigma^{\rightarrow \Leftarrow}\left(\phi, e_{\ell}\right)\right]}{\left[\sigma^{\leftarrow \Rightarrow}\left(\phi, e_{\ell}\right)+\sigma^{\rightarrow \Rightarrow}\left(\phi, e_{\ell}\right)\right]+\left[\sigma^{\leftarrow \Leftarrow}\left(\phi, e_{\ell}\right)+\sigma^{\rightarrow \Leftarrow}\left(\phi, e_{\ell}\right)\right]}$
analog: Double-spin (LL) asymmetry
transversely polarized target:
$\frac{t}{4 M^{2}}\left[\left(2-x_{B}\right) F_{1} \mathcal{E}-4 \frac{1-x_{B}}{2-x_{B}} F_{2} \mathcal{H}\right]$

## H1 \& HERMES: DVCS beam-charge asymmetry

```
            Re(\mp@subsup{\tau}{DVCS}{*}}>
        for HERA (small x)
            Re(\tau (\tauVCS) <0
for HERMES (larger x)
```

Where is the zero crossing? COMPASS measurement at intermediate energy

- $\varrho=\boldsymbol{R e}\left(\tau_{D V C S}\right) / \mathbf{I m}\left(\tau_{D V C S}\right)$
- $\varrho=0.20 \pm 0.05$ (stat) $\pm 0.08$ (sys)
- In good agreement with theoretical calculation (dispersion relation)
- H1@HERA/DESY: first and only measurement at collider
- low $\mathrm{x}_{\mathrm{B}}=10^{-4} \ldots 10^{-2}$
- $6.5<\mathrm{Q}^{2}<80 \mathrm{GeV}^{2}$
- $30<W<140 \mathrm{GeV}$
- $|\mathbf{t}|<1 \mathrm{GeV}^{2}$




## GPD $E$ linked to orbital angular momentum

Measurements sensitive to GPD E allow (in principle) to access the total angular momentum of partons, $J_{q}$.

Ni sum rule for the nucleon:
[Jj, PRL 78 (1997) 610]

$$
J_{\mathrm{q}}=\frac{1}{2} \lim _{t \rightarrow 0} \int_{-1}^{1} \mathrm{~d} x x\left[H^{\mathrm{q}}(x, \xi, t)+E^{\mathrm{q}}(x, \xi, t)\right]
$$


[Hall A PRL 99, 242501 (2007)]

HERMES and Hall-A DVCS asymmetries
(A) HERMES: ep ${ }^{\uparrow} \rightarrow \mathbf{e p} \gamma$ :
$H-E$ (transversely polarized proton target) $\mathcal{A}_{\mathrm{UT}}$
(B) Hall A: $\overrightarrow{\mathbf{e}} \mathbf{n} \rightarrow \mathbf{e} \mathbf{n} \boldsymbol{\gamma}$ :
$\boldsymbol{E}$ dominant for the neutron
 J/Psi asymmetry

- More data from JLab12 and RHIC (STAR) to come.
- STAR: exclusive J/Psi production in ultra-peripheral $\mathrm{p} \uparrow \mathrm{p}$ collisions (UPC) $\rightarrow$ gluon GPD $E$


Vector meson production and decay


