

Transverse-momentum distributions of hadrons produced in DIS at COMPASS

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on behalf of the COMPASS collaboration



CHARLES UNIVERSITY
Faculty of mathematics
and physics



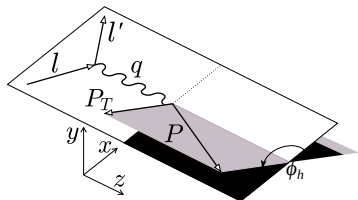


The cross section for producing a hadron h in DIS on unpolarised target $\ell N \rightarrow \ell' h X$:

[A. Bacchetta *et al.*, JHEP 0702 (2007)]

$$\begin{aligned} \frac{d\sigma}{dx dy dz d\phi_h dP_T^2} &= \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{2xM^2}{Q^2}\right) \left(F_{UU,T} + \varepsilon F_{UU,L} \right. \\ &\quad \left. + \sqrt{2\varepsilon(1+\varepsilon)} F_{UU}^{\cos\phi_h} \cos\phi_h + \varepsilon F_{UU}^{\cos 2\phi_h} \cos 2\phi_h + \lambda \sqrt{2\varepsilon(1-\varepsilon)} F_{LU}^{\sin\phi_h} \sin\phi_h \right) \\ &= \sigma_0 \left(1 + \varepsilon_1 A_{UU}^{\cos\phi_h} \cos\phi_h + \varepsilon_2 A_{UU}^{\cos 2\phi_h} \cos 2\phi_h + \lambda \varepsilon_3 A_{LU}^{\sin\phi_h} \sin\phi_h \right) \end{aligned}$$

- where x, y, Q^2 are usual DIS variables,
- λ is the beam polarisation (≈ 0.8 at COMPASS),
- z is the fraction of γ^* energy carried by h .
- P_T is the transverse momentum of h in the γN frame, ϕ_h is its azimuthal angle.
- $F_{XU}^{f(\phi_h)}(x, z, P_T^2, Q^2)$ are structure functions.
- $A_{XU}^{f(\phi_h)}(x, z, P_T^2, Q^2)$ are commonly called azimuthal asymmetries.



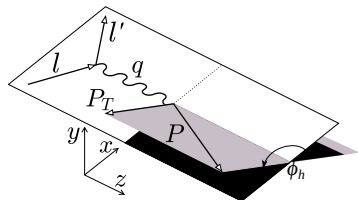
SIDIS in the γ -nucleon frame.

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The unpolarised structure function in terms of TMD PDFs and TMD FFs:

$$F_{UU,T} = \mathcal{C} [f_1 D_1],$$

Gaussian ansatz:

$$f_1^q(x, k_T^2) = f_1^q(x) \frac{1}{\pi \langle k_{Tq}^2 \rangle} e^{-\frac{k_T^2}{\langle k_{Tq}^2 \rangle}}$$

$$D_1^{h/q}(z, p_\perp^2) = D_1^{h/q}(z) \frac{1}{\pi \langle p_{\perp h/q}^2 \rangle} e^{-\frac{p_\perp^2}{\langle p_{\perp h/q}^2 \rangle}}$$

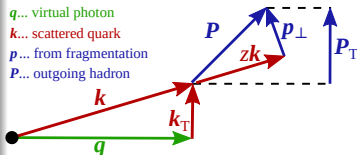
Assuming flavour independence of $\langle k_T^2 \rangle$ and $\langle p_\perp^2 \rangle$:

$$F_{UU,T} = x \sum_q e_q^2 f_1^q(x) D_1^{h/q}(z) \frac{1}{\pi \langle P_T^2 \rangle} e^{-\frac{P_T^2}{\langle P_T^2 \rangle}}$$

where

$$\langle P_T^2 \rangle = z^2 \langle k_{Tq}^2 \rangle + \langle p_{\perp h/q}^2 \rangle.$$

- $f_1(x, k_T^2, Q^2)$ unpolarised TMD PDF,
- $D_1(z, p_\perp^2, Q^2)$ unpolarised TMD FF,
- \mathcal{C} = sum over flavours and convolution over $\mathbf{p}_\perp, \mathbf{k}_T$,



Momentum vectors

$$\mathbf{P}_T = z\mathbf{k}_T + \mathbf{p}_\perp$$



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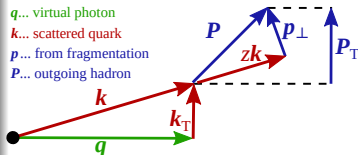
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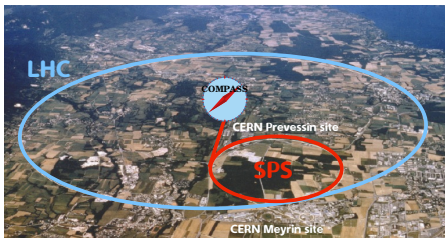
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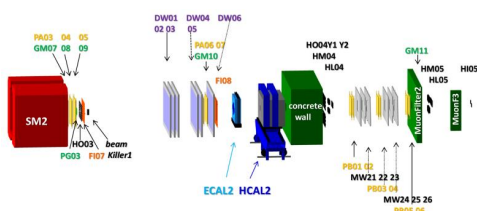
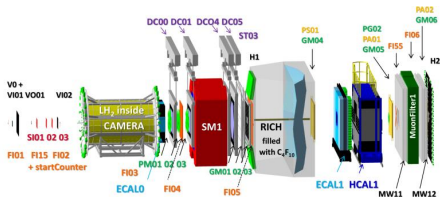
Momentum vectors

$$\mathbf{P}_T = z\mathbf{k}_T + \mathbf{p}_\perp$$



It is located at M2 beamline of CERN's SPS.

- Collaboration: 24 institutes, 13 countries.
- Fixed target, multi-purpose.
- Broad research programme:
 - **SIDIS**: μ^+ beam and L/T-polarised proton (NH_3) or deuteron (${}^6\text{LiD}$) target (beam 160 GeV/c, 200 GeV/c in 2011)
Summary by F. Bradamante on Monday.
 - **Hadron spectroscopy**: hadron beams and nuclear targets.
 - **Drell-Yan**: 190 GeV/c π^- beam and p^\uparrow , Al and W targets – *R. Longo, Friday.*
 - **Hard exclusive processes and SIDIS**: 160 GeV/c μ^\pm beam and liquid H_2 target.
DVCS & HEMP – N. d'Hose, Wednesday.



2016–2017 setup with CAMERA recoil proton detector and ECAL0 calorimeter for DVCS studies.



Published unpolarised SIDIS results:

- Azimuthal asymmetries on ${}^6\text{LiD}$ target [COMPASS, Nucl.Phys.B 886 (2014)].
- P_{T} -dependent multiplicities on ${}^6\text{LiD}$ target [COMPASS, Phys.Rev.D97 (2018)]
- Background to the asymmetries from decays of exclusive vector mesons [COMPASS, Nucl.Phys.B 956 (2020)].

Ongoing analysis presented in this talk:

- 2016–2017 data taken with 2.5 m long LH_2 target.
- Primary goal: exclusive measurements, useful for SIDIS as well.
- Advantages:
 - pure proton target,
 - alternating μ^\pm beam with balanced statistics (stability tests for systematics),
 - MC development in synergy with DVCS analysis.
- Part of the data (about 11 %) used for these preliminary results.
- P_{T}^2 -distributions – this talk.
- Azimuthal asymmetries – A. Moretti (next talk).

Future:

- 2022 run with ${}^6\text{LiD}$ target (transversely polarised).



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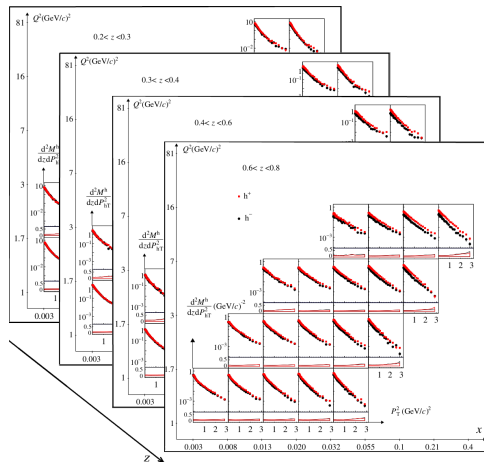
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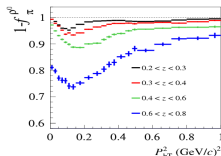
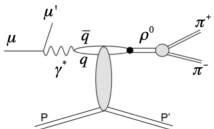


- [COMPASS, Phys.Rev.D97 (2018)]
- **4D analysis**
(bins in x , Q^2 , z and P_T^2)
- Unidentified charged hadrons studied.
- QED radiative effects taken into account.
- Contribution of the decay of exclusive vector mesons
 - Contamination estimated from HEPGEN MC generator [A. Sandacz & P. Sznajder, arXiv:1207.0333].
 - Subtracted in each bin.
 - ρ^0 : small P_T , large z , small Q^2 .
 - ϕ : tiny P_T , medium z , small Q^2 .

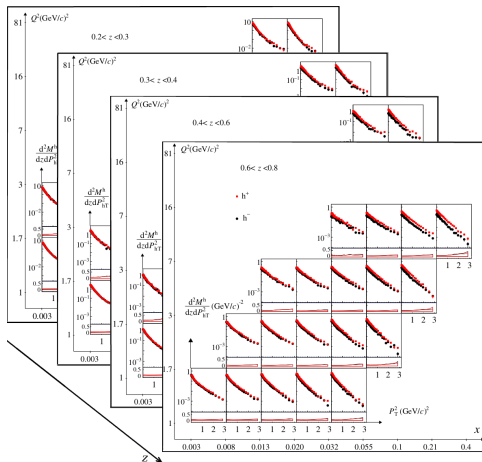




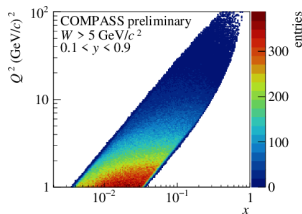
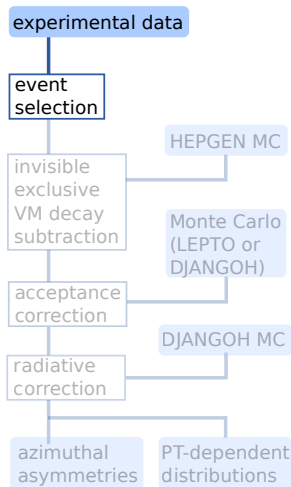
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$1 - \rho^0$ contamination fraction.



Diffractively produced $\rho^0 \rightarrow \pi^+\pi^-$, creating a background to SIDIS.



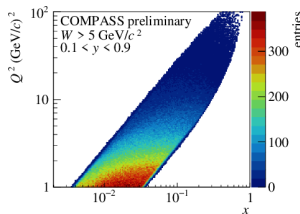
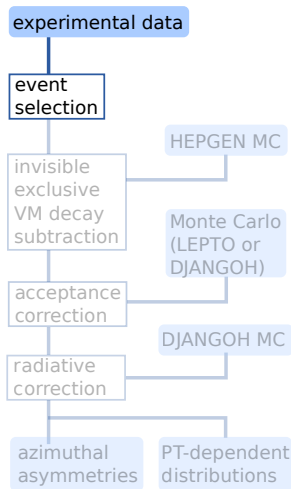
The x and Q^2 range covered.

DIS event selection

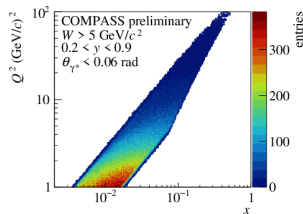
- $Q^2 > 1$ (GeV/c)²,
- $W > 5$ GeV/c²,
- $0.003 < x < 0.13$,
- $0.2 < y < 0.9$,
- $\theta_\gamma < 60$ mrad,
- Exclusive VM decay cut:
if only $\mu'h^+h^-$ outgoing,
 $z_1 + z_2 = z_t < 0.95$.

Hadron selection

- $0.1 < z < 0.85$,
- $0.1 < P_T / (\text{GeV}/c) < 1.73$.



The x and Q^2 range covered.



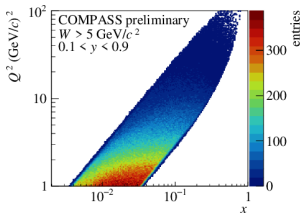
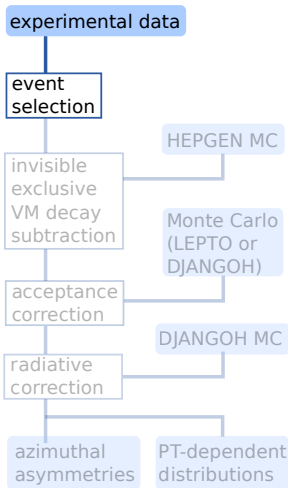
Selected range with moderate acceptance corrections.

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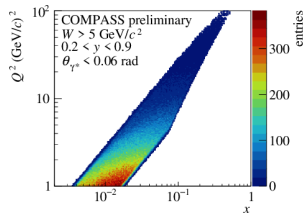
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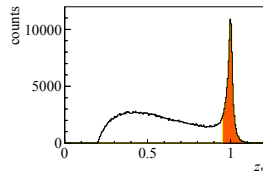
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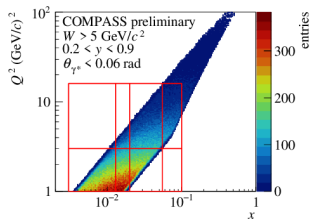
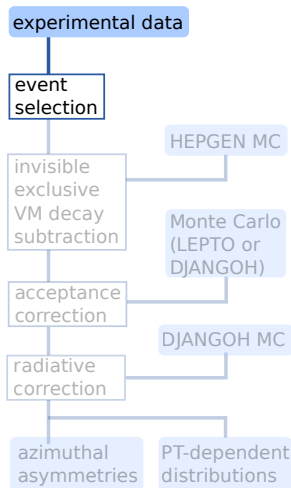
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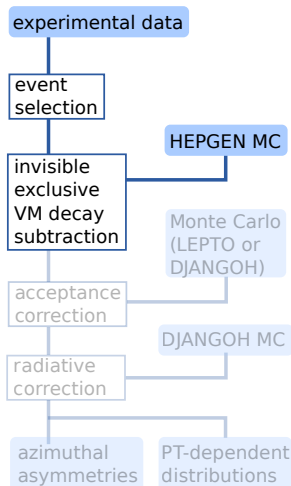
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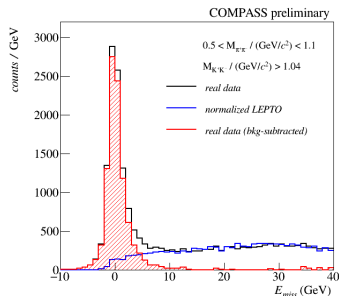
Q^2 and x bins for the P_T -dependent distributions.

Binning

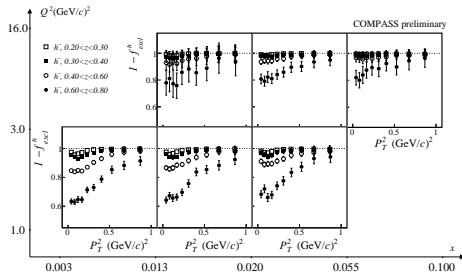
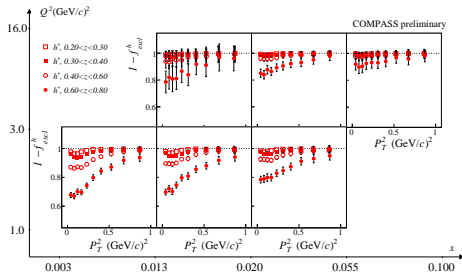
- Based on the published results on ⁶LiD.
- Asymmetries:
 - 1D in x , z and P_T .
 - 3D in x , z and P_T
- P_T -dependent distributions
 - 4D in x , Q^2 , z and P_T^2 .
 - Larger bins w.r.t the publication
 - $4x \times 2Q^2 \times 4z$
 - $4x \times 2Q^2 \times 7z$
 - Additional binning in W
 - $4x \times 3Q^2 \times 4z \times 2W$



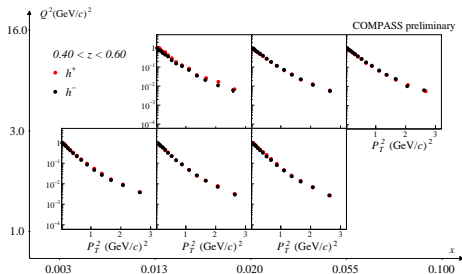
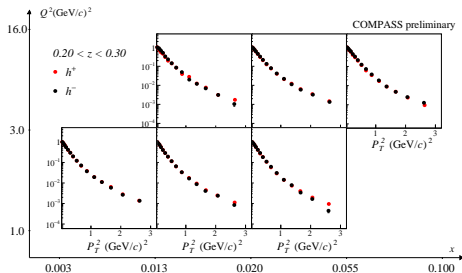
- Different approach w.r.t published d asymmetries.
- ‘Visible’ exclusive h^+h^- removed in event selection.
 - About 80 % of the decays are ‘visible’.
- ‘Invisible’ decays (only one h observed)
 - HEPGEN MC generator with azimuthal modulations.
 - Normalised to the data using E_{miss} distribution of the ‘visible’ decays.
 - Subtracted in every bin.



The number of signal events in the peak after SIDIS (from LEPTO) background subtraction is used to normalise HEPGEN.



The impact of the VM-subtraction (the sum of ‘visible’ and ‘invisible’) on the P_T -dependent distributions.

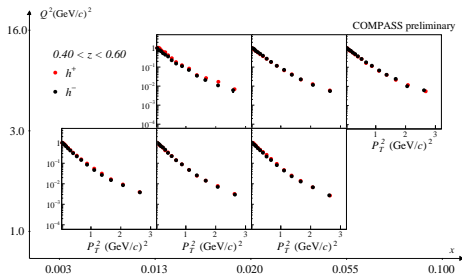
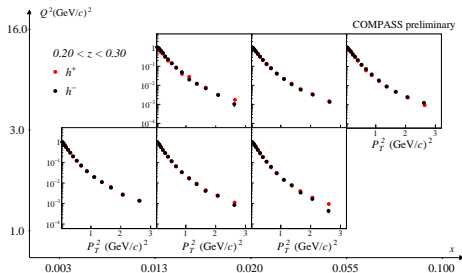


- Distributions normalised to the first bin.
- The shape almost the same for h^\pm – no sign of flavour dependence of k_T , p_\perp .
- Clear z and Q^2 dependence.
- Gaussian model for f_1 and D_1 :

$$\frac{d^2 N}{dz dP_T} \propto \exp\left(-\frac{P_T^2}{\langle P_T^2 \rangle}\right)$$

$$\langle P_T^2 \rangle = z^2 \langle k_T^2 \rangle + \langle p_\perp^2 \rangle.$$

- Deviation from the simple exponential visible at $P_T > 1$ (GeV/c)².

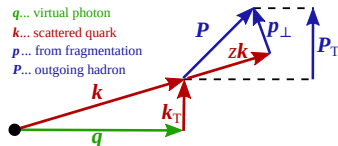


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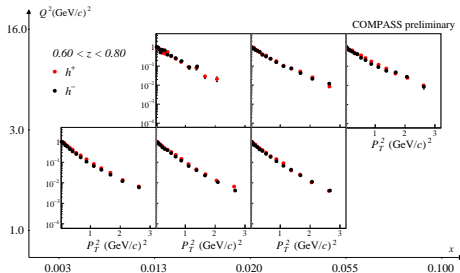
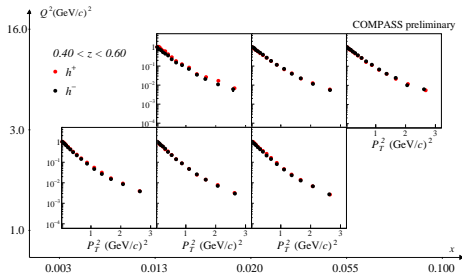
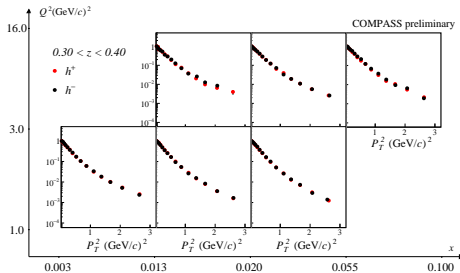
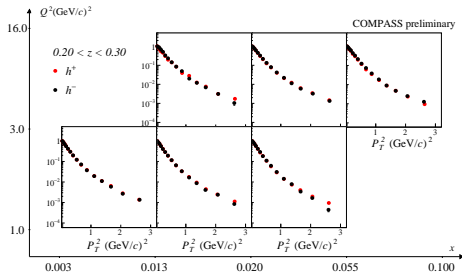
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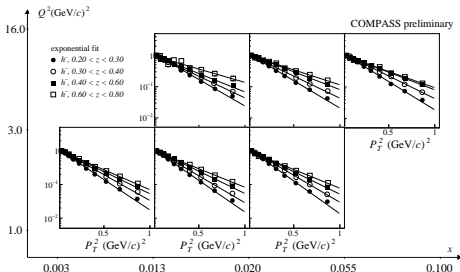
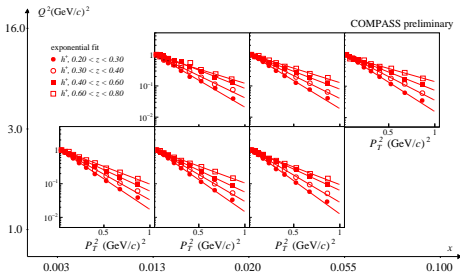


Measurement on LH₂: Results for the P_T -distributions





$$\frac{d^2N}{dzdP_T} \propto \exp\left(-\frac{P_T^2}{\langle P_T^2 \rangle}\right)$$



Exponential fit in $P_T < 1$ (GeV/c)² range.

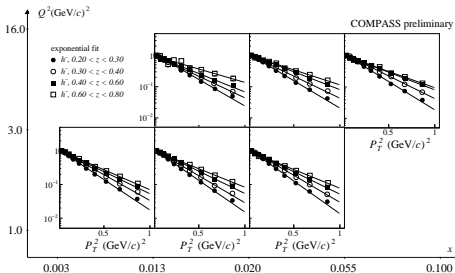
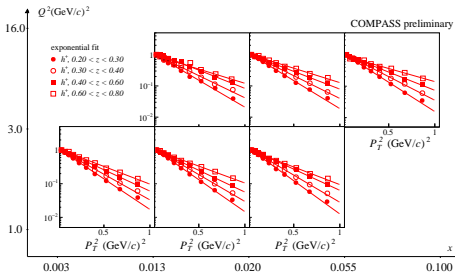
- Linear trend in z^2 expected from the simple Gaussian model

$$\langle P_T^2 \rangle = z^2 \langle k_T^2 \rangle + \langle p_{\perp}^2 \rangle.$$

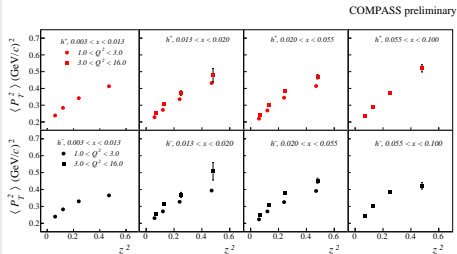
- Possible dependence of $\langle p_{\perp}^2 \rangle$ on z or of $\langle k_T^2 \rangle$ on x .
- Momentum conserv.: $P_T \rightarrow 0$ at $z \rightarrow 1$.



$$\frac{d^2 N}{dz dP_T} \propto \exp\left(-\frac{P_T^2}{\langle P_T^2 \rangle}\right)$$



Exponential fit in $P_T < 1$ (GeV/c)² range.



The fitted $\langle P_T^2 \rangle$ versus z^2 in the x and Q^2 bins.

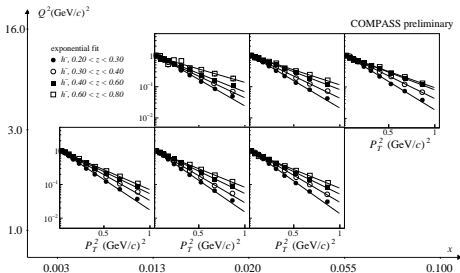
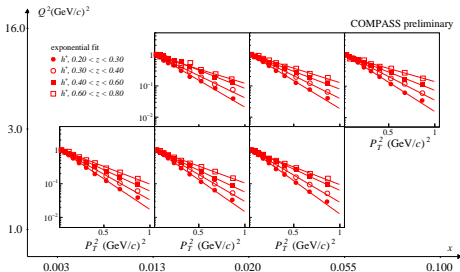
- Linear trend in z^2 expected from the simple Gaussian model

$$\langle P_T^2 \rangle = z^2 \langle k_T^2 \rangle + \langle p_{\perp}^2 \rangle.$$

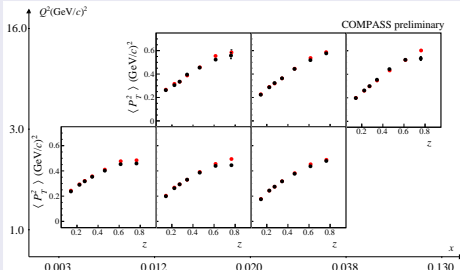
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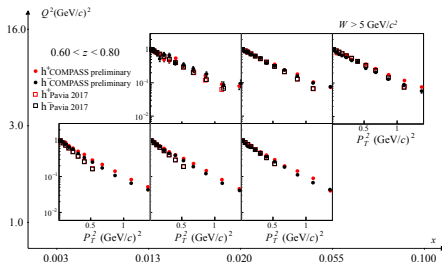
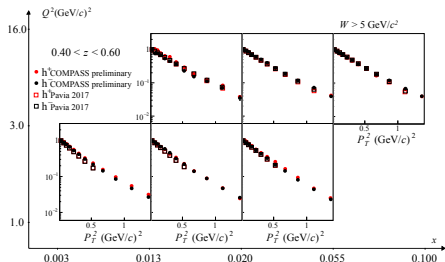
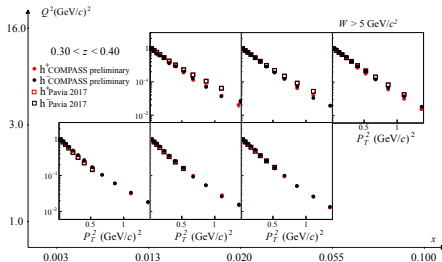
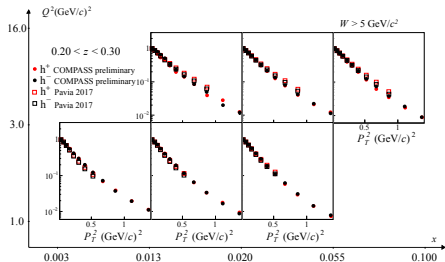
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Comparison with Pavia 2017 fit [A. Bacchetta *et al.*, JHEP 06 (2017) 081]

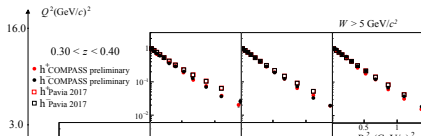
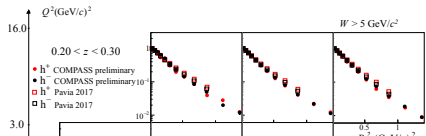
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- Z boson production (CDF, D0)



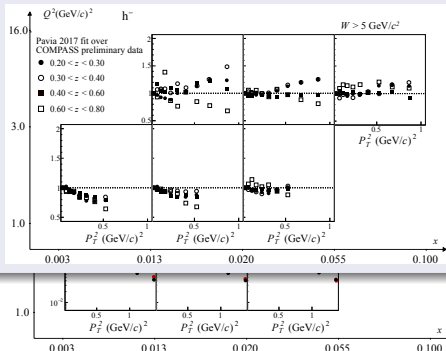
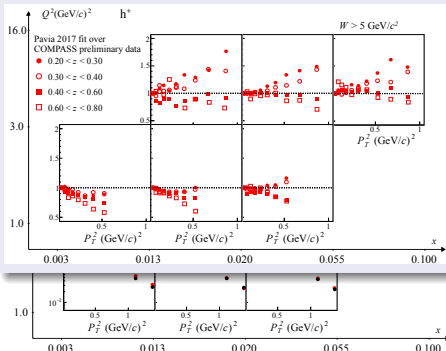


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The ratio of the prediction from the fit over the preliminary data:





Interesting observables in unpolarised SIDIS

- **Azimuthal asymmetries:** sensitive to k_T (via Cahn effect) and to Boer–Mulders function.
- **2h-asymmetries** – additional information on Boer–Mulders and Cahn.
- **P_T -dependent distributions:** sensitive to k_T and p_\perp dependence of f_1 and D_1 .
- Contamination from decays of exclusive VMs – an important role in some regions.

COMPASS measurements

- Published results on ${}^6\text{LiD}$ target: [COMPASS, Nucl.Phys.B 886 (2014)], [COMPASS, Phys.Rev.D97 (2018)], [COMPASS, Nucl.Phys.B 956 (2020)].
- New preliminary results (August 2020) on liquid H_2 target.
 - 11 % of the statistics,
 - More robust method for exclusive VM subtraction.
 - Alternating μ^\pm beam – systematic check.
 - Qualitative agreement with deuteron.
 - Two-exponential shape, the same for h^\pm .
 - More results will come.
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These measurements provide important input to general understanding of the **transverse-momentum-dependent structure of the nucleon** and of the **fragmentation process**.



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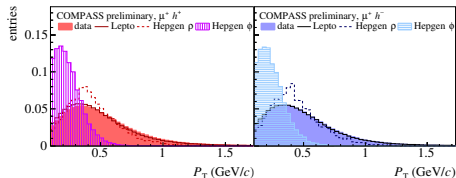
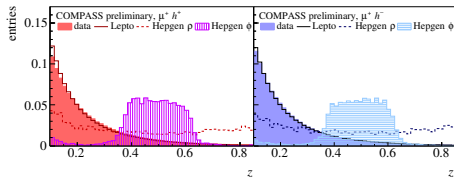
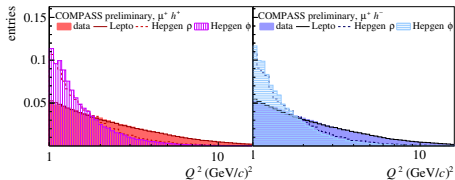
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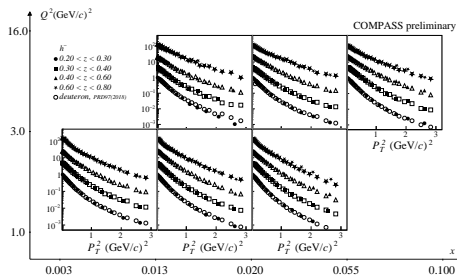
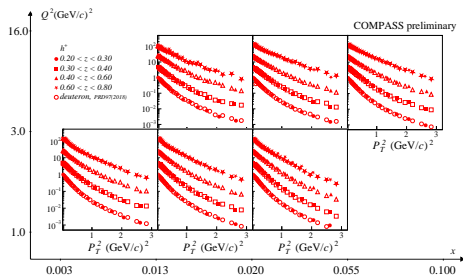
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Thank you for your attention!



Normalised kinematic distributions: real data, LEPTO, HEPGEN ρ^0 and HEPGEN ϕ .



Backup: Distributions of q_T and q_T^2



$$q_T = P_T/z$$

