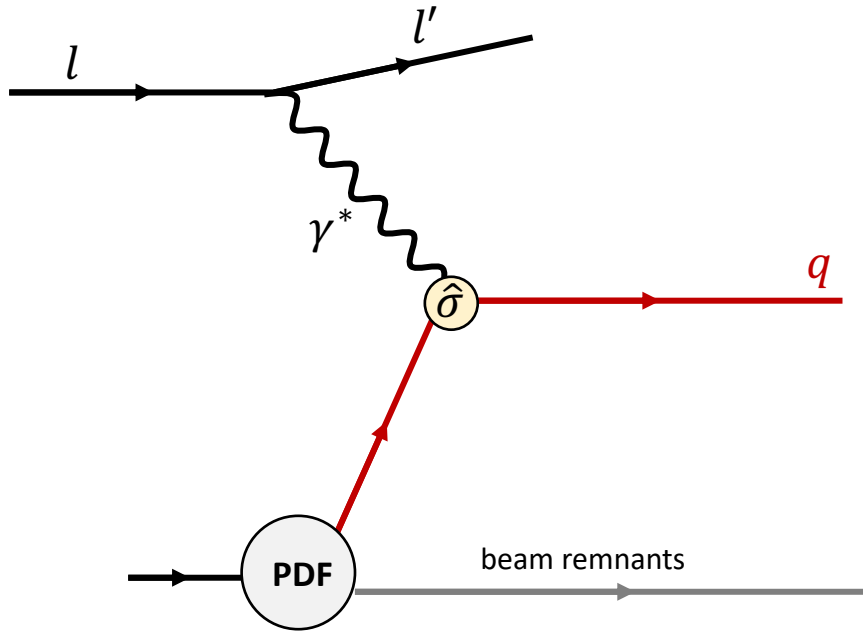


March 9, 2022  
Duke University

## Correlations in Partonic and Hadronic Interactions

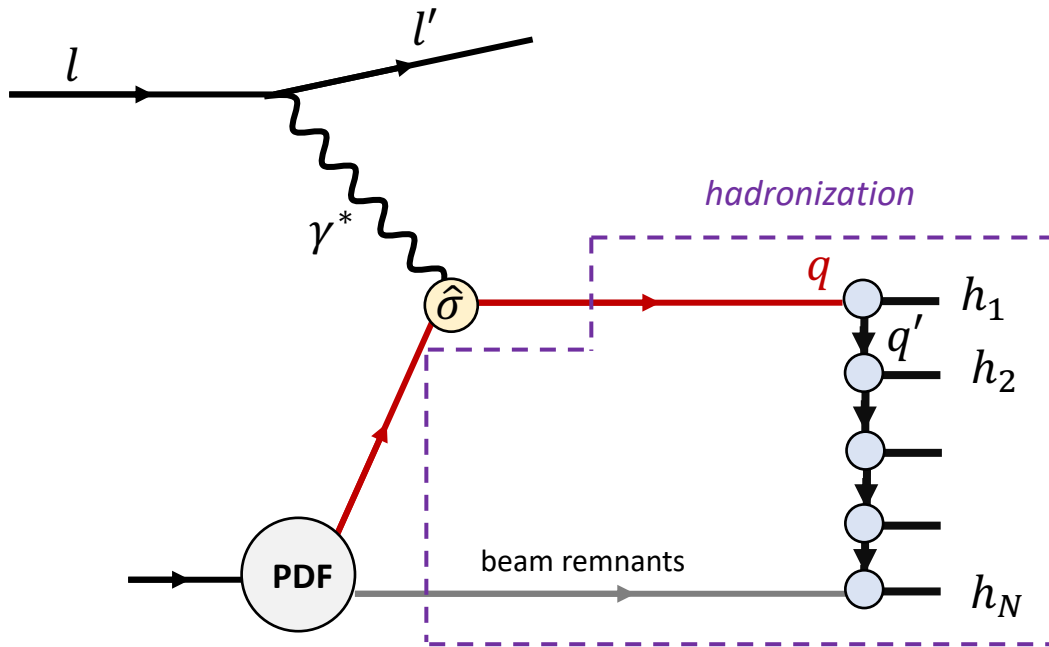
# Simulation of quark spin effects with Monte Carlo event generators

Albi Kerbizi



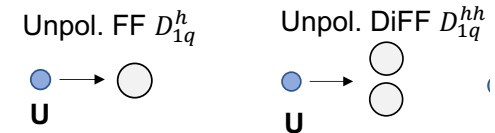
## PDFs input to the generator

- $f_1^q(x, Q^2)$  used to generation  $x, Q^2$ , struck quark flavor
- intrinsic  $\vec{k}_T$  treated as part of beam remnants



## Hadronization

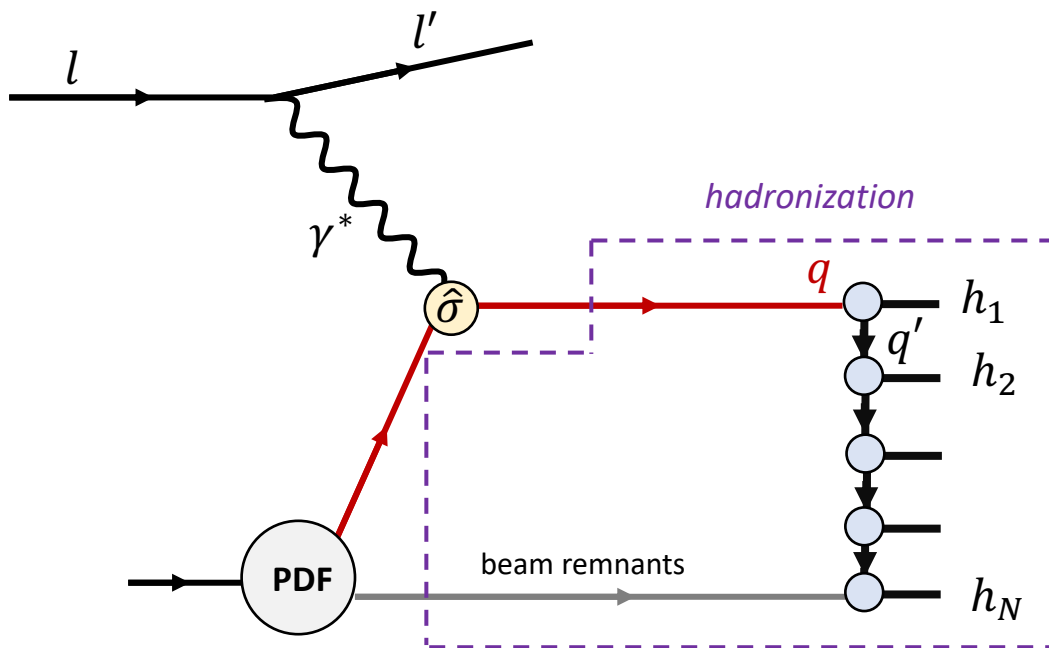
- A model must be utilized  
*Lund string Model (Pythia, Lepto,..)*  
*cluster model (Herwig,..)*  
 ..
- Can be used to simulate FFs  
*1h, 2h or more exclusive final states*
- **No spin by default!**



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# Polarized SIDIS process in a Monte Carlo Event Generator ~ the goal



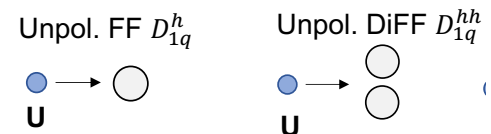
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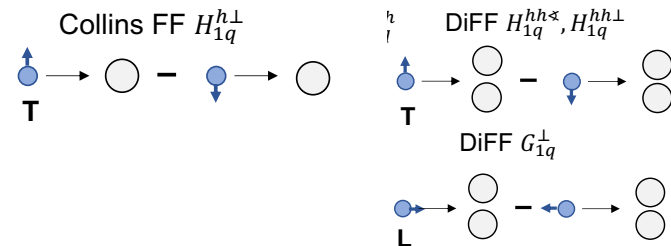
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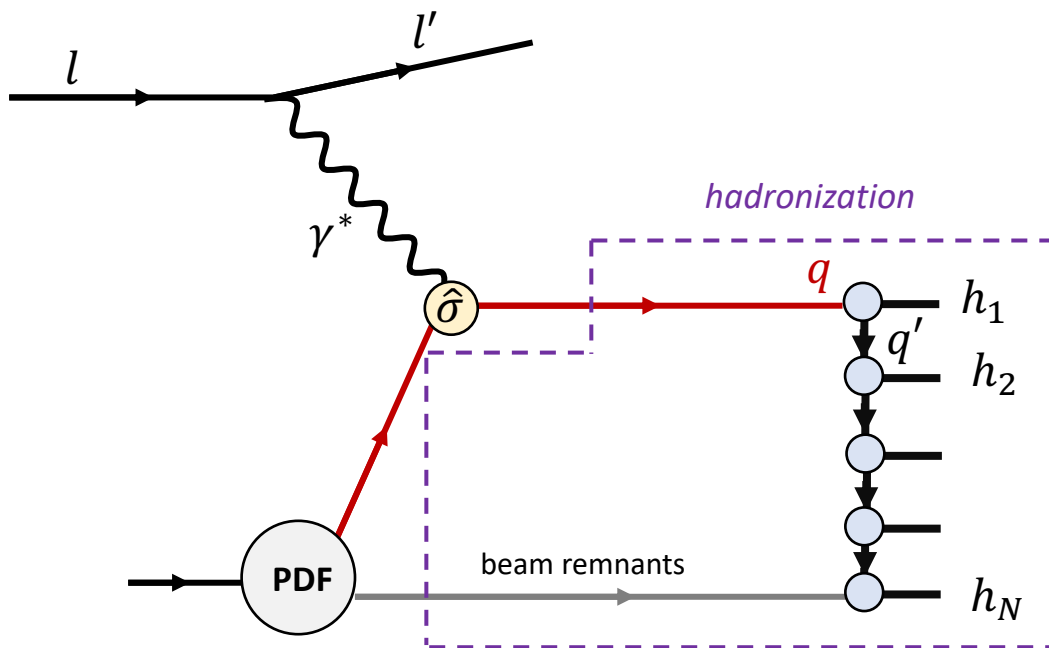
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### Including the spin of q



# Polarized SIDIS process in a Monte Carlo Event Generator ~ the goal



## PDFs input to the generator

- $f_1^q(x, Q^2)$  used to generation  $x, Q^2$ , struck quark flavor
- intrinsic  $\vec{k}_T$  treated as part of beam remnants

## Once spin effects in hadronization are treated correctly

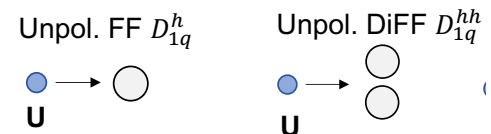
- other (TMD) PDFs can (in principle) be included
- possible to simulate the rich structure of azimuthal asymmetries in SIDIS

q\N	U	L	T
U	$f_1$		$f_{1T}$
L		$g_1$	$g_{1T}$
T	$h_1^\perp$	$h_{1L}^\perp$	$h_{1T}, h_{1T}^\perp$

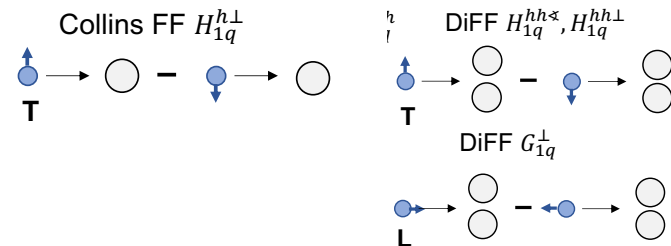
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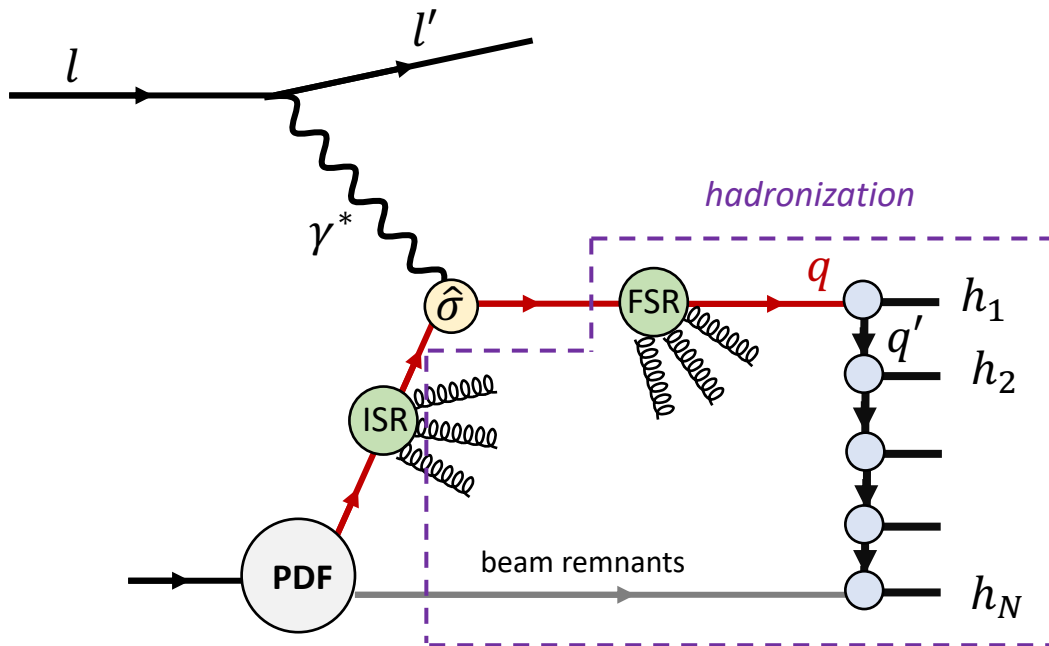
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# Polarized SIDIS process in a Monte Carlo Event Generator ~ the goal



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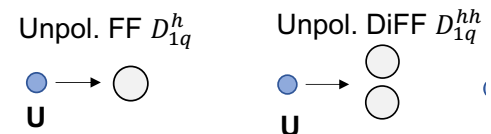
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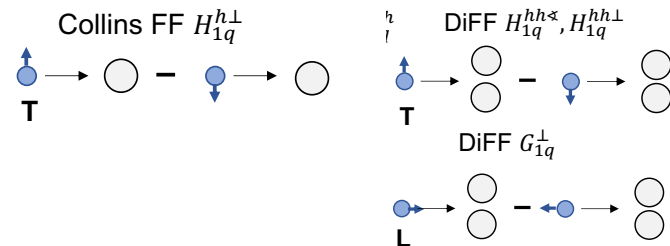
## Hadronization

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..
- Can be used to simulate FFs  
*1h, 2h or more exclusive final states*

### No spin by default!



### Including the spin of q



- evolution effects: spin in parton showers  
see e.g. Richardson, Webster, EPJ, C (2020) 80:83  
→ **still no match with polarized hadronization**

## polarized hadronization model is crucial

→ must start from here!

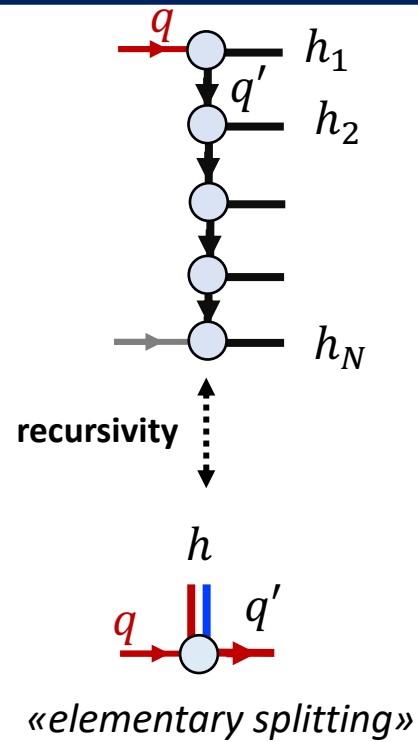
*understand hadronization, implement in MCEGs*

# Current models of polarized hadronization

## → The string+ ${}^3P_0$ model

- recursive model

AK, Artru, Belghobsi, Bradamante, Martin, PRD97 (2018) 7, 074010  
AK, Artru, Belghobsi, Martin, PRD100 (2019) no.1, 014003  
AK, Artru, Martin, PRD104 (2021) 11, 114038

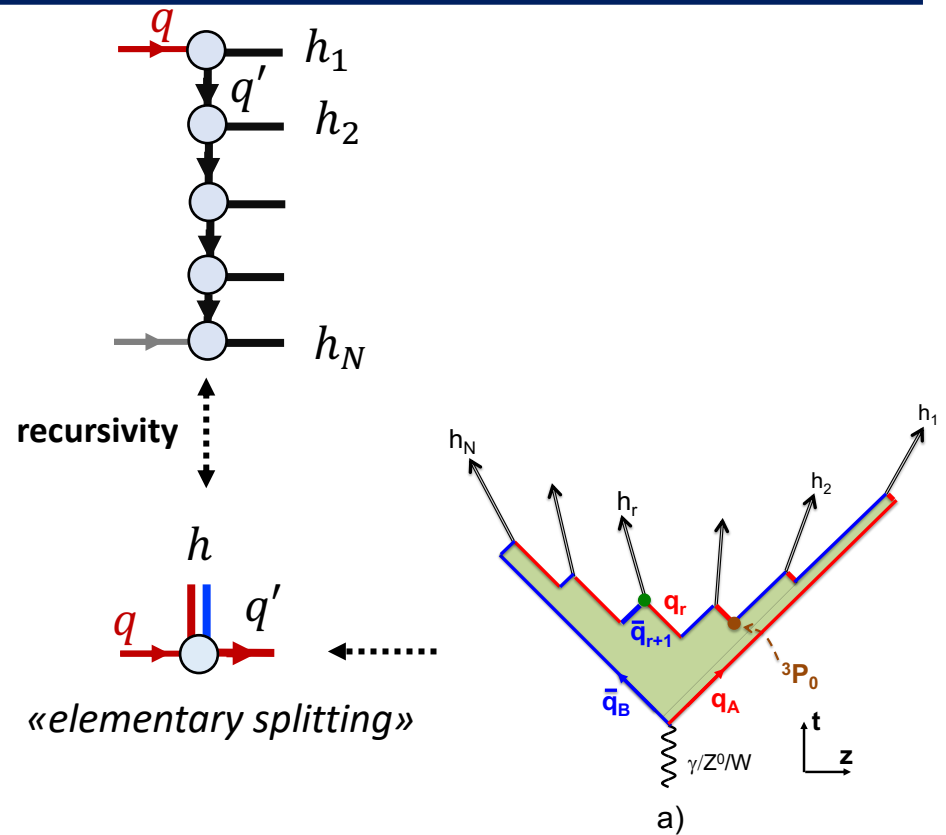


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AK, Artru, Belghobsi, Bradamante, Martin, PRD97 (2018) 7, 074010  
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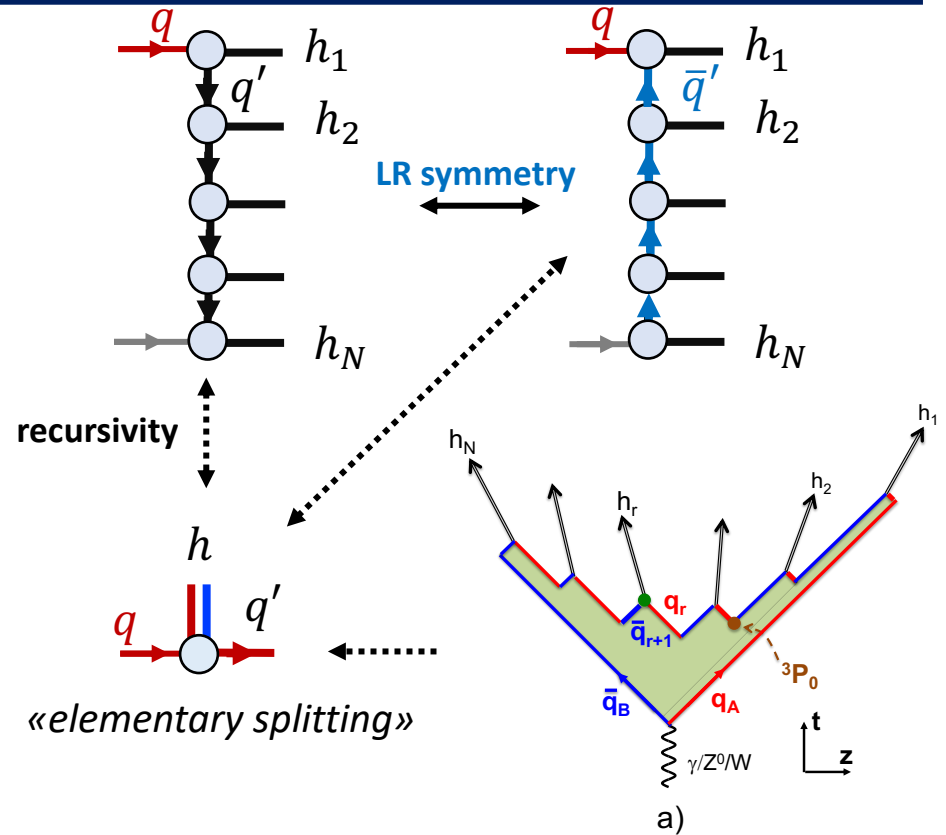


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AK, Artru, Belghobsi, Bradamante, Martin, PRD97 (2018) 7, 074010  
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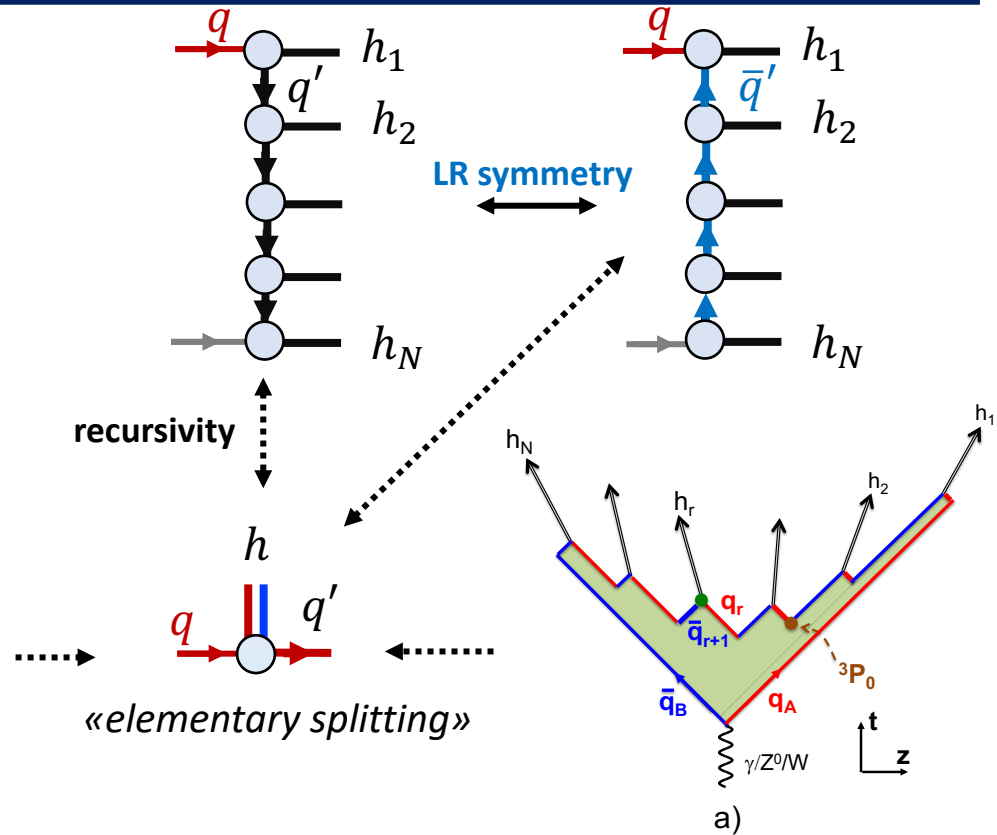
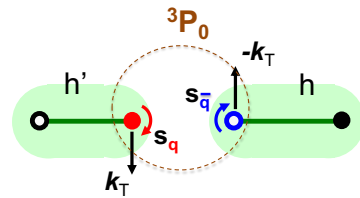


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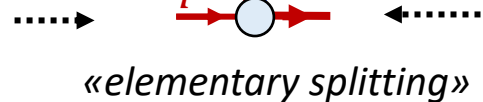
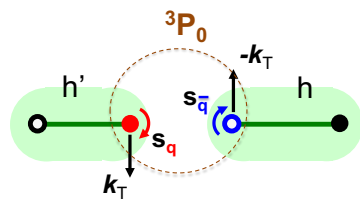
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- formulated at the amplitude level
- density matrix formalism to propagate spin effects
- PS mesons, VM

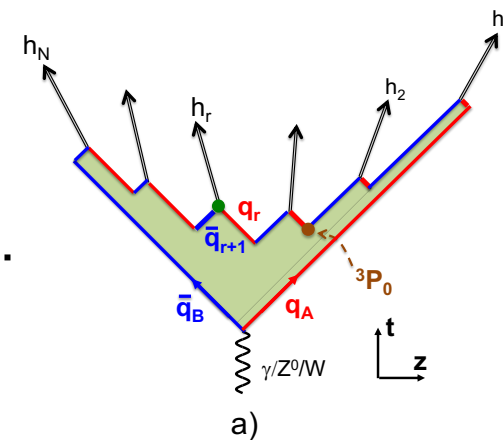
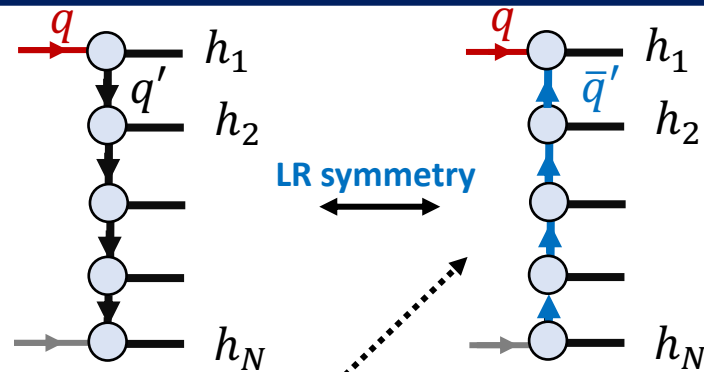
AK, Artru, Belghobsi, Bradamante, Martin, PRD97 (2018) 7, 074010

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AK, Artru, Martin, PRD104 (2021) 11, 114038



recursivity

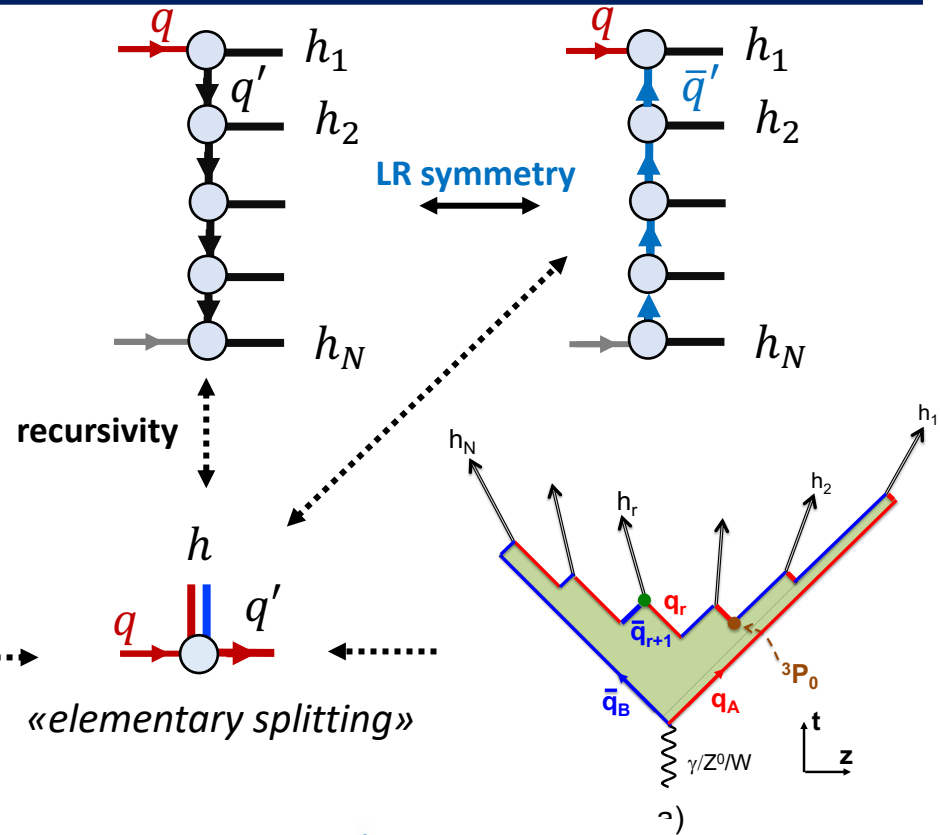
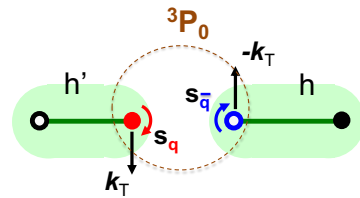


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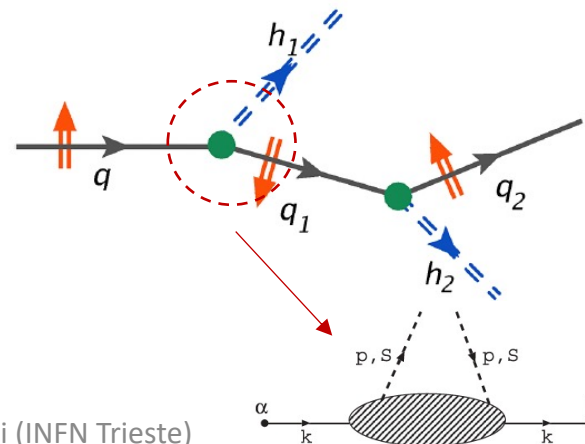
AK, Artru, Belghobsi, Bradamante, Martin, PRD97 (2018) 7, 074010  
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## → The quark-jet model

- recursive model
- generalization of Field-Feynman fragmentation model
- field-theoretic calculation of elementary splitting functions (T-even and T-odd functions treated differently)
- density matrix formalism to propagate spin effects
- spin effects for PS mesons

see e.g. Matevosyan, Kotzinian, Thomas, PRD95 (2017) 1, 014021

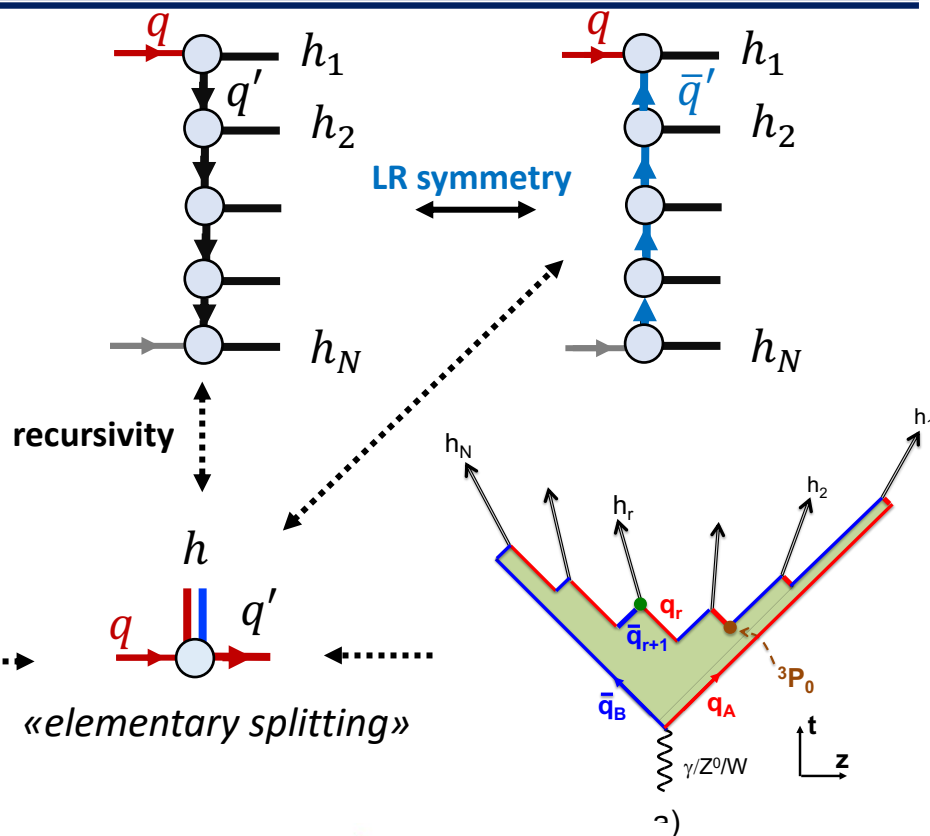
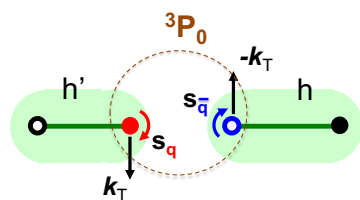


# Current models of polarized hadronization

## → The string+ $^3P_0$ model next slides

- recursive model
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(respects quark-Line Reversal symmetry)
- spin effects via  $^3P_0$  mechanism
- formulated at the amplitude level
- density matrix formalism to propagate spin effects
- PS mesons, VM

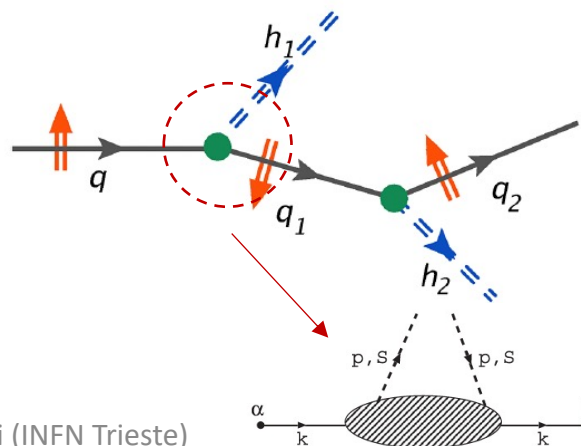
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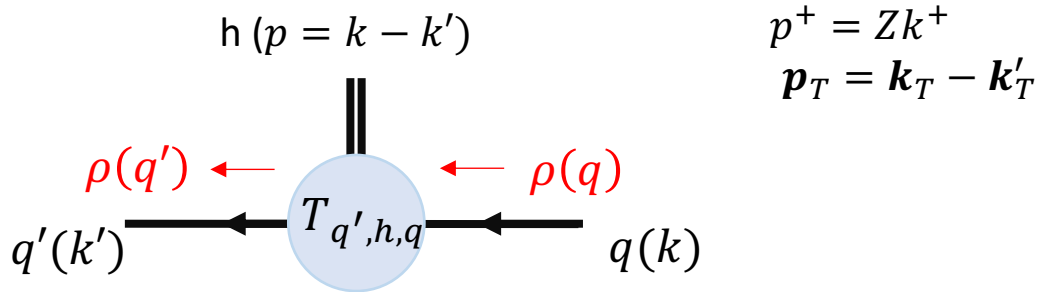
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# Elementary splitting in the string+ $^3P_0$ model



## M19: Emission of a PS meson ( $\pi, K, \eta, \eta'$ )

AK, Artru, Belghobsi, Martin, PRD100 (2019) no.1, 014003

i) Introduce the Splitting Amplitude ( $2 \times 2$  matrix)

$$T_{q',h,q}(Z, \mathbf{p}_T | \mathbf{k}_T) = F_{\text{Lund}}^{1/2} \times \Gamma_h \times (\mu + \sigma_z \boldsymbol{\sigma} \cdot \mathbf{k}'_T)$$

coupling  $^3P_0$  wave func.

ii) Generate  $h$  according to the Splitting Function

$$F_{q'hq}(Z, \mathbf{p}_T | \mathbf{k}_T, \mathcal{S}_q) = \text{tr} T_{q',h,q} \rho(q) T_{q',h,q}^\dagger$$

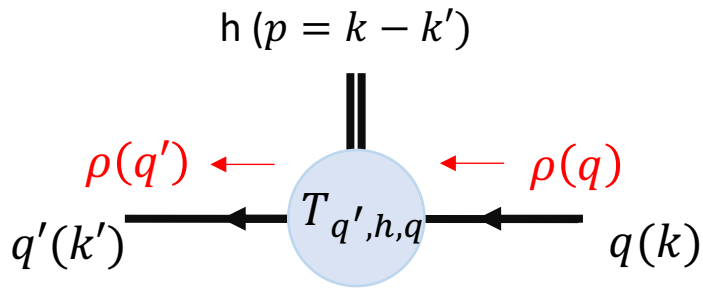
iii) Calculate the density matrix of  $q'$

$$\rho(q') \propto T_{q',h,q} \rho(q) T_{q',h,q}^\dagger$$

## Couplings:

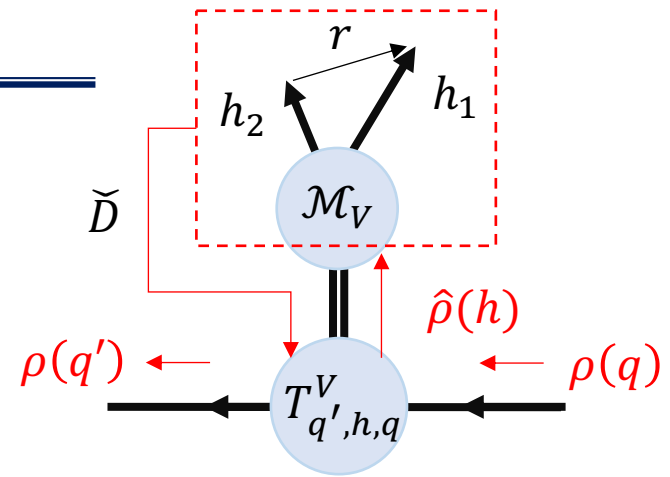
$$\Gamma_h = \sigma_z \quad \rightarrow \text{PS meson}$$

# Elementary splitting in the string+ $^3P_0$ model



$$p^+ = Zk^+$$

$$\mathbf{p}_T = \mathbf{k}_T - \mathbf{k}'_T$$



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## Couplings:

$$\Gamma_h = \sigma_z \rightarrow \text{PS meson}$$

$$\Gamma_{h,V} = G_L V_L^* \mathbf{1} + G_T \mathbf{V}_T^* \cdot \boldsymbol{\sigma}_T \sigma_z \rightarrow \text{VM with pol. V}$$

## M20: Emission of a VM ( $\rho, K^*, \omega, \phi$ )

AK, Artru, Martin, PRD104 (2021) 11, 114038

i) Introduce the Splitting Amplitude ( $2 \times 2$  matrix)

$$T_{q',h,q}^V(M, Z, \mathbf{p}_T, s_h | \mathbf{k}_T) = F_{\text{Lund}}^{1/2} \times \Gamma_{h,V} (\mu + \sigma_z \boldsymbol{\sigma} \cdot \mathbf{k}'_T)$$

use the recipe of Collins '88 and Knowles '88 to

ii) Generate h according to the Splitting Function

$$F_{q'hq}(M, Z, \mathbf{p}_T | \mathbf{k}_T, \mathbf{S}_q) = \text{tr} T_{q',h,q}^V \rho(q) T_{q',h,q}^{V\dagger}$$

iii) Calculate density matrix of h

$$\hat{\rho}_{VV'}(h) \propto \text{tr} T_{q',h,q}^V \rho(q) T_{q',h,q}^{V'\dagger}$$

iv) Simulate the polarized decay

$$dN/d\Omega \propto \mathcal{M}_V \hat{\rho}_{VV'} \mathcal{M}_{V'}^\dagger$$

v) Bring decay information back to  $q'$

$$\check{D}_{V'V} = \mathcal{M}_{V'}^\dagger \mathcal{M}_V$$

vi) Calculate density matrix of  $q'$

$$\rho(q') = \check{D}_{VV'} T_{q',h,q}^{V'} \rho(q) T_{q',h,q}^{V\dagger}$$

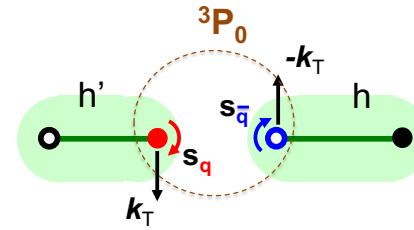
# The free parameters of the string+ $^3P_0$ model

## Spin effects

complex mass  $\mu$  from  $^3P_0$  wave function

$Im(\mu) \rightarrow$  T spin effects (Collins, dihadron)

$Re(\mu) \rightarrow$  L spin effects (jet-handedness)





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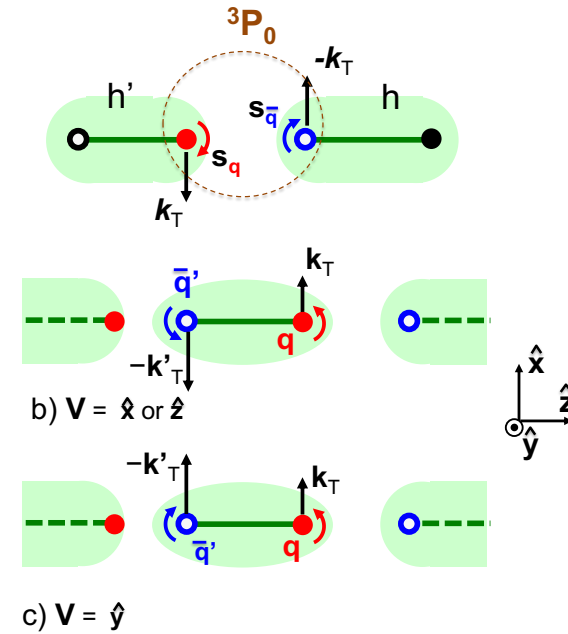
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## Coupling to VM

$G_L \rightarrow$  VM with L pol. along the string axis

$G_T \rightarrow$  VM with T pol. w.r.t the string axis



# The free parameters of the string+ $^3P_0$ model

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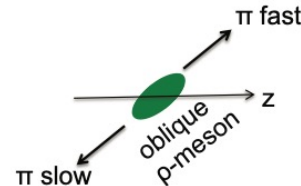
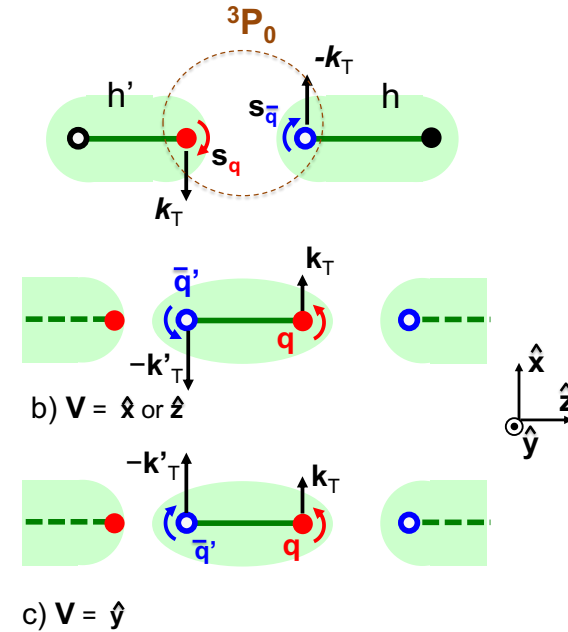
$G_T \rightarrow$  VM with T pol. w.r.t the string axis

## Effective parameters for VM production

$$|G_L|^2 + 2|G_T|^2 = \frac{VM}{PS} = \begin{cases} 0.62 \text{ light mesons.} \\ 0.725 \text{ strange mesons} \end{cases} \rightarrow \text{as in Pythia 8}$$

$|G_L/G_T| \rightarrow$  spin alignment, Collins effect of the VM

$\theta_{LT} = \arg(G_L/G_T) \rightarrow$  oblique polarisation



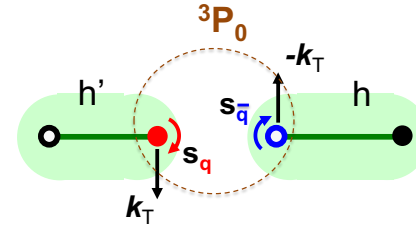
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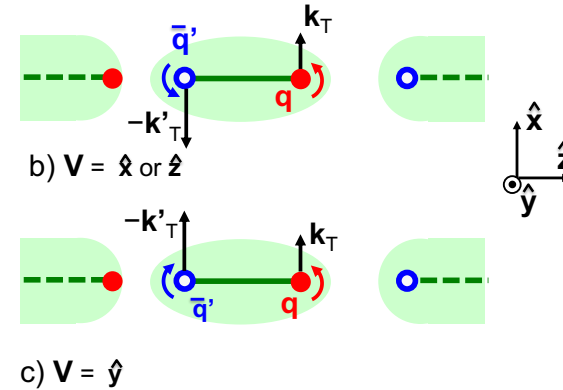
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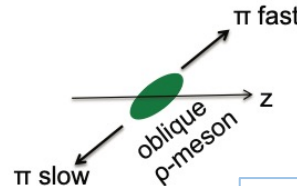


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+ Parameters for spin-less Lund splitting Function

$\rightarrow$ parametrize the string decay process (*see backup slides*)

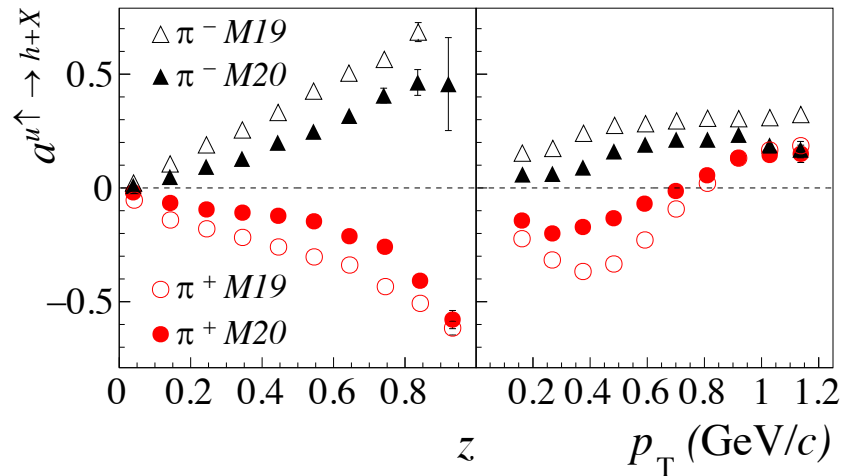
Following slides, simulations with  $u$  quarks with full T pol. along  $\hat{y}$   
no primordial  $\vec{k}_T$

# Effect of VM production on TSA

M19 = only PS

M20 = PS, VM

## Collins analysing power



Different trends as compared to M19

Dilution of about 50%

Large effect on Collins

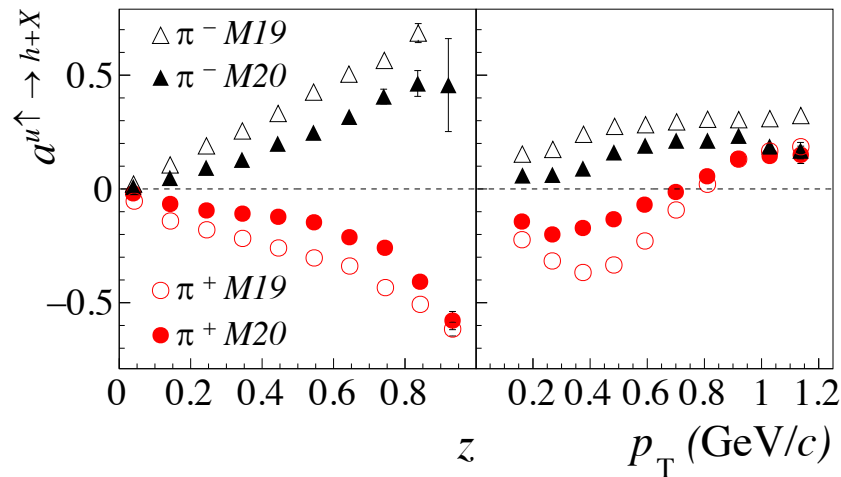
→ VM important to understand how the observed asymmetries arise

# Effect of VM production on TSA

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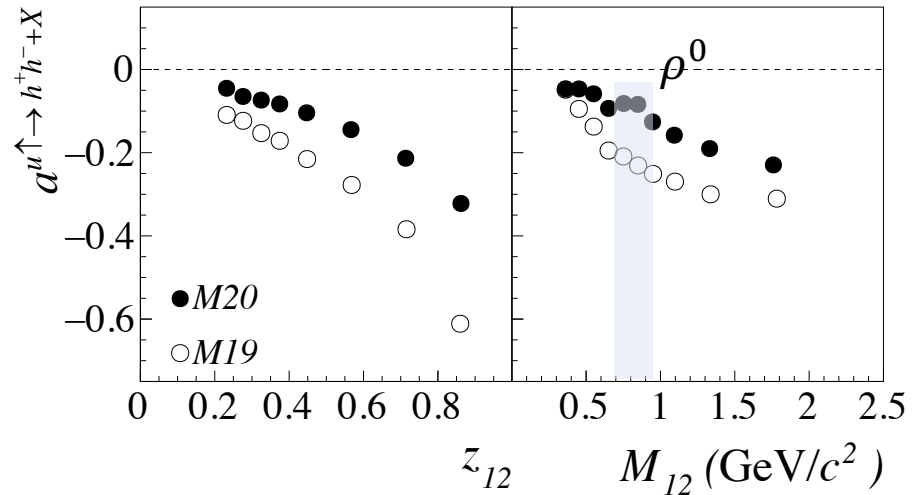
M20 = PS, VM

## Collins analysing power



Different trends as compared to M19  
Dilution of about 50%

## Di-hadron analysing power



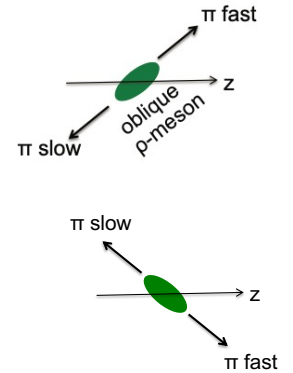
VM decays do not contribute to the 2h asymmetry  
(decay symmetric w.r.t  $\mathbf{R} \leftrightarrow -\mathbf{R}$ )  
50% dilution w.r.t M19  
→ stronger dilution around  $\rho^0$

Large effect on Collins and dihadron analysing powers  
→ VM important to understand how the observed asymmetries arise

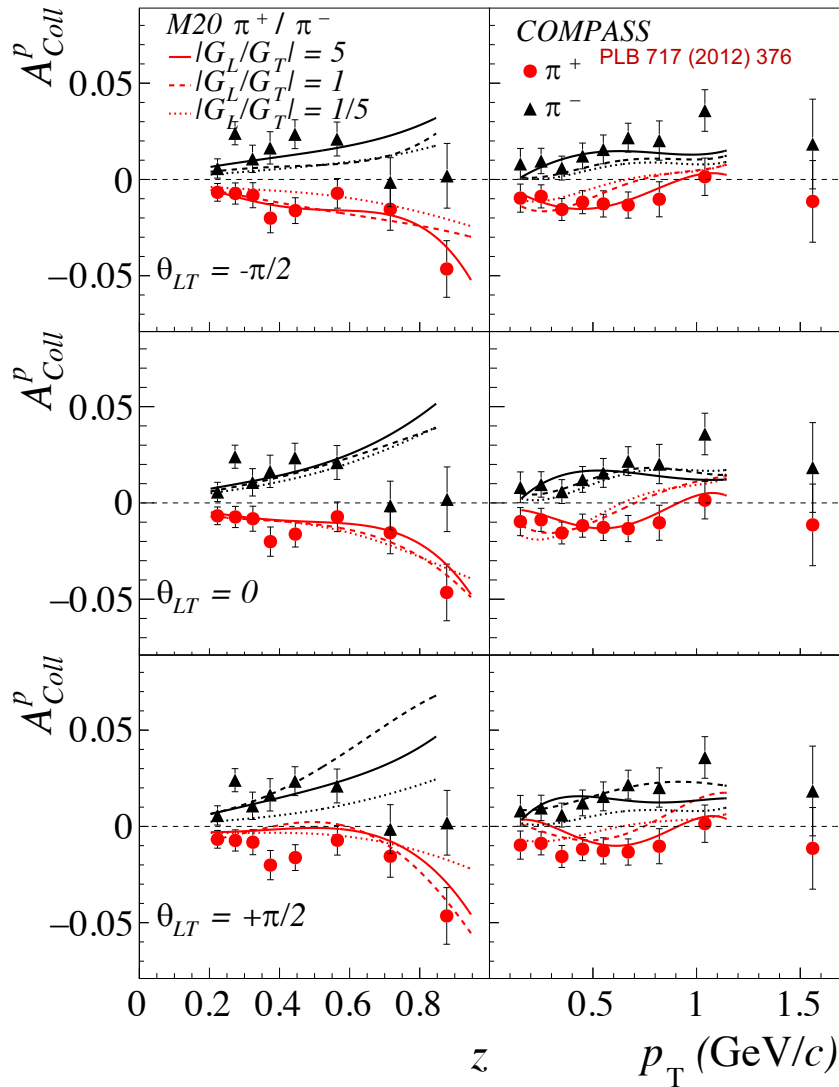
Different combinations of free parameters

$$\left| \frac{G_L}{G_T} \right| = \begin{cases} 5 & \text{L pol. VM} \\ 1 & \text{T, L pol. VM} \\ 1/5 & \text{T pol. VM} \end{cases}$$

$$\theta_{LT} = \begin{cases} -\frac{\pi}{2} & \text{VM with oblique pol.} \\ 0 & \text{VM with no oblique pol.} \\ +\frac{\pi}{2} & \text{VM with oblique pol.} \end{cases}$$



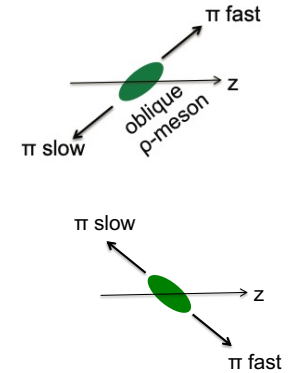
# Comparison with SIDIS data



Different combinations of free parameters

$$\left| \frac{G_L}{G_T} \right| = \begin{cases} 5 & \text{L pol. VM} \\ 1 & \text{T, L pol. VM} \\ 1/5 & \text{T pol. VM} \end{cases}$$

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MC scaled by a constant for each combination

Large variations for different values of  $|G_L|/|G_T|$  and  $\theta_{LT}$   
 → **both parameters important**

hint for  $|G_L/G_T| = 5, \theta_{LT} = -\pi/2$

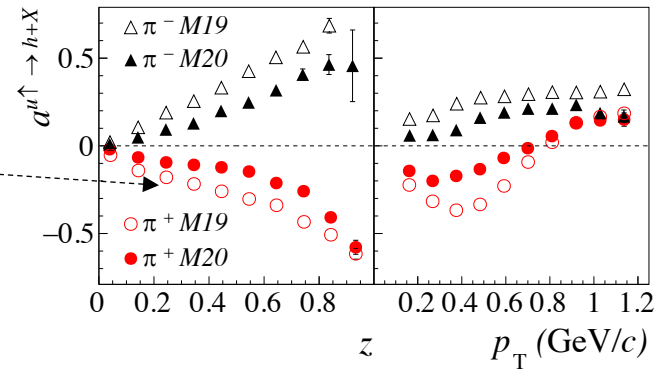
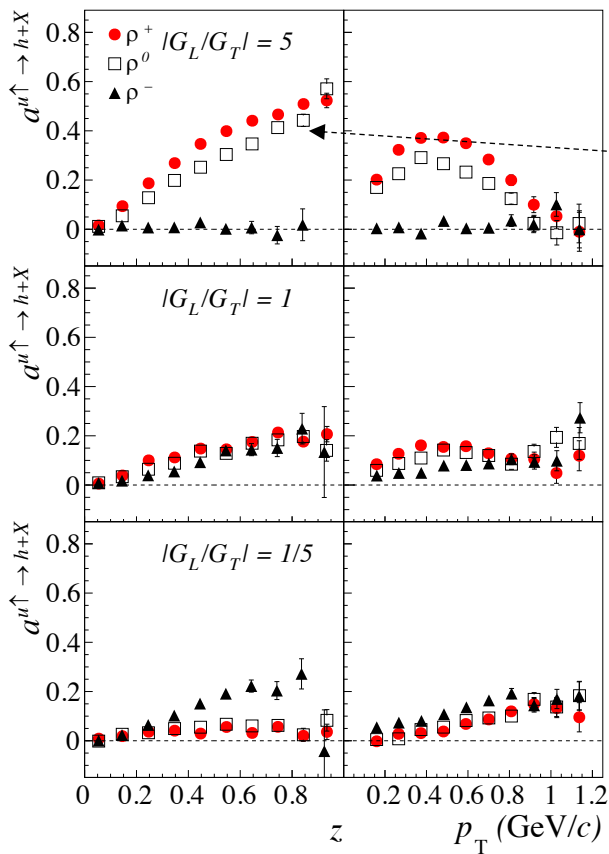
or  $|G_L/G_T| = 1, \theta_{LT} = 0$

→ more precise data needed to fix the free parameters

comparison with 2h asymmetry OK

less sensitive to  $|G_L/G_T|$  and  $\theta_{LT}$

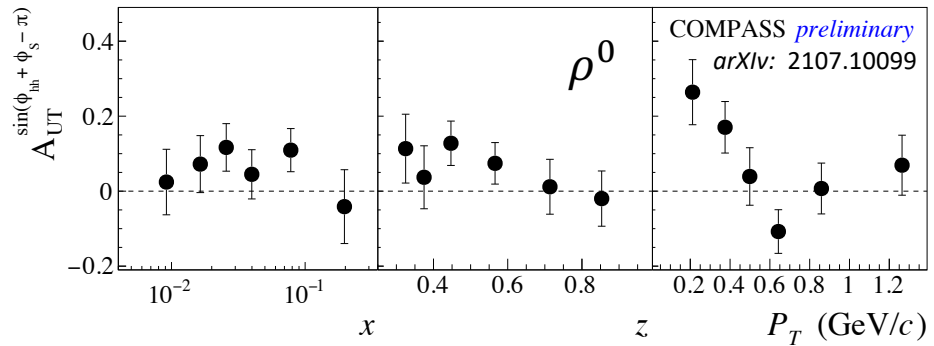
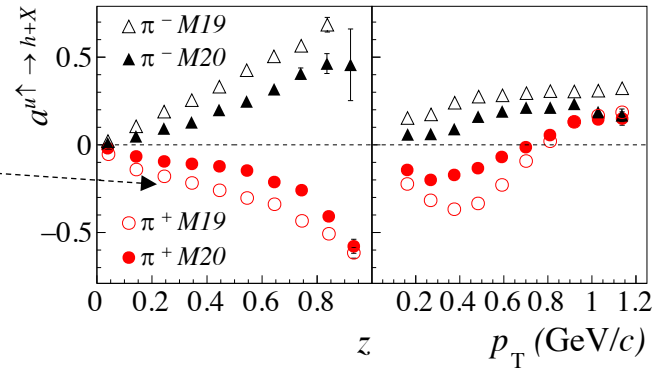
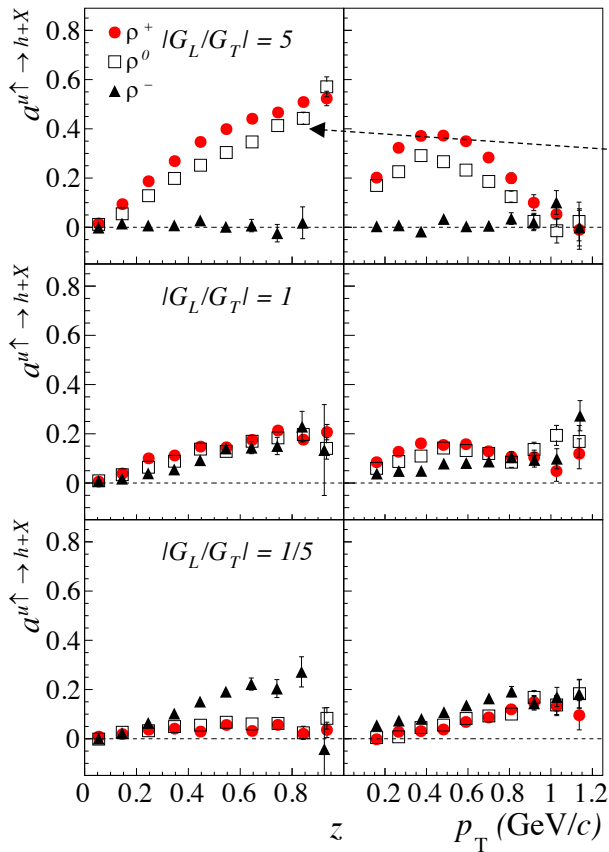
# Collins effect for $\rho$ mesons



- Opposite sign w.r.t  $\pi^+$   
(in agreement with Czyzewski '96)
- Strong dependence on  $|G_L/G_T|$   
→ both size and shapes change



# Collins effect for $\rho$ mesons



First measurement by COMPASS

→ Hint for  $\frac{|G_L|}{|G_T|} > 1$  ?

→ Measurements feasible

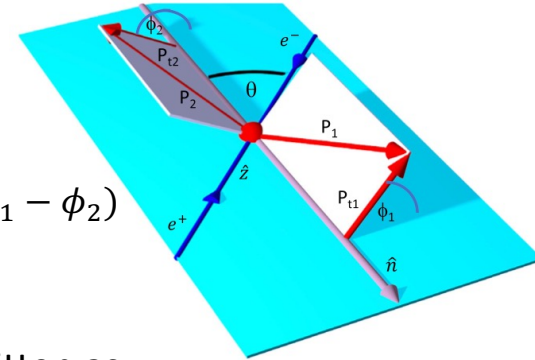
more precise data are needed,  
 $e^+e^-$  data would be wellcome!

- Opposite sign w.r.t  $\pi^+$   
 (in agreement with Czyzewski '96)
- Strong dependence on  $|G_L/G_T|$
- both size and shapes change

# Comparison with $e^+e^-$ data

Comparison with Collins asymmetries for back-to-back pions measured recently by BELLE

*BELLE, PRD 100, 092008 (2019)*



$$R_{12}^{UL} = \frac{N_{\pi^+\pi^-} + N_{\pi^-\pi^+}}{N_{\pi^+\pi^+} + N_{\pi^-\pi^-}} \approx 1 + A_{12}^{UL} \cos(\phi_1 - \phi_2)$$

The  $A_{12}^{UL}(z, p_T)$  asymmetry can be written as

$$A_{12}^{UL}(z, p_T) = \underbrace{\left\langle \frac{\sin^2 \theta}{1 + \cos^2 \theta} \right\rangle}_{0.91} \times \underbrace{|a^{fav}(z, p_T)|^2}_{\text{Collins analyzing power for fav. fragmentation}} \times \underbrace{\left( \frac{5 + 5\alpha^2 + 2\alpha'^2}{5 + 5\beta^2 + 2\beta'^2} - \frac{5\alpha + \alpha'^2}{5\beta + \beta'^2} \right)}_{\text{isospin + charge congj.}}$$

$z_1 = z_2 \equiv z$   
 $p_{1T} = p_{2T} \equiv p_T$

$\alpha = H_1^{fav} / H_1^{unfav}$      $\alpha' = H_{1,s}^{unfav} / H_1^{unfav}$   
 $\beta = D_1^{fav} / D_1^{unfav}$      $\beta' = D_{1,s}^{unfav} / D_1^{unfav}$

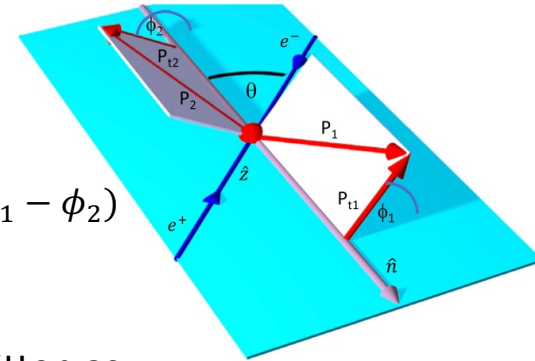
Belle data corrected for charm production

$A_{12}^{UL}$  has been **evaluated** using M20 (cuts as in data, MC not rescaled)

# Comparison with e<sup>+</sup>e<sup>-</sup> data

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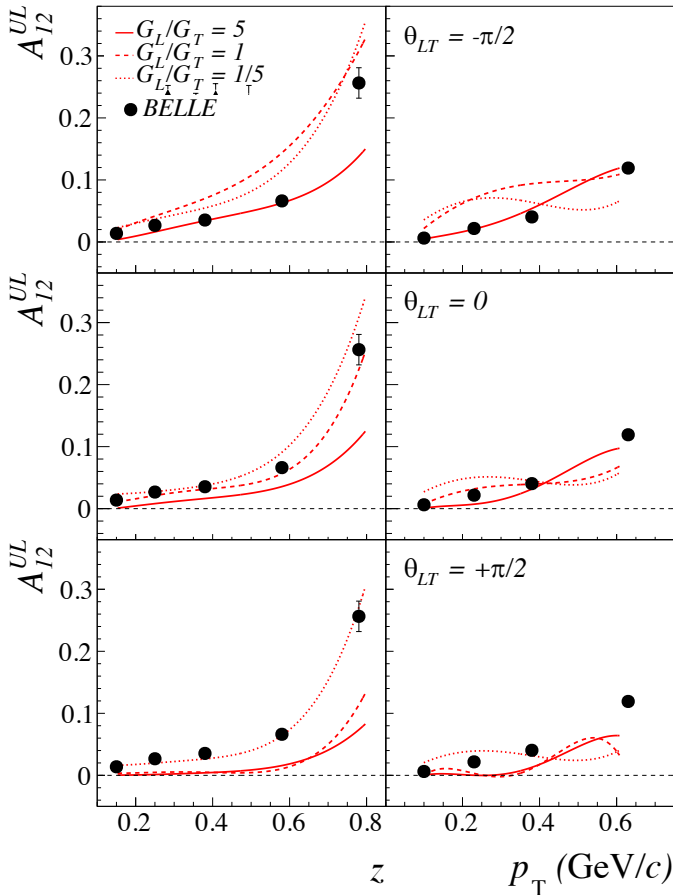
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Belle data corrected for charm production

$A_{12}^{UL}$  has been **evaluated** using M20 (cuts as in data, MC not rescaled)

→ satisfactory description for  $\left| \frac{G_L}{G_T} \right| = 5, \theta_{LT} = -\frac{\pi}{2}$  and  $\left| \frac{G_L}{G_T} \right| = 1, \theta_{LT} = 0$  as for SIDIS data

## A new di-hadron asymmetry

---

VMs do not contribute to the standard dihadron asymmetry

They contribute to the z-ordered di-hadron asymmetry, namely

$$a^{u\uparrow\rightarrow h_1 h_2 + X} = 2\langle \sin(\phi_R - \phi_{S_u}) \rangle, \mathbf{R}_T = z_2 \mathbf{p}_{1T}/z - z_1 \mathbf{p}_{2T}/z, z_1 > z_2 \text{ (z-ordering)}$$

→ Due to the oblique polarization which depends on  $\theta_{LT}$

**z-ordered 2h analysing power in the decay  $\rho^0 \rightarrow \pi^+ \pi^-$**

# A new di-hadron asymmetry

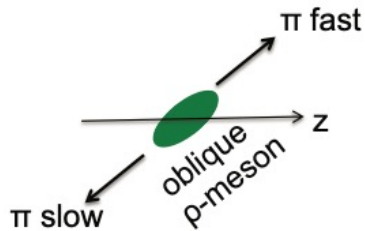
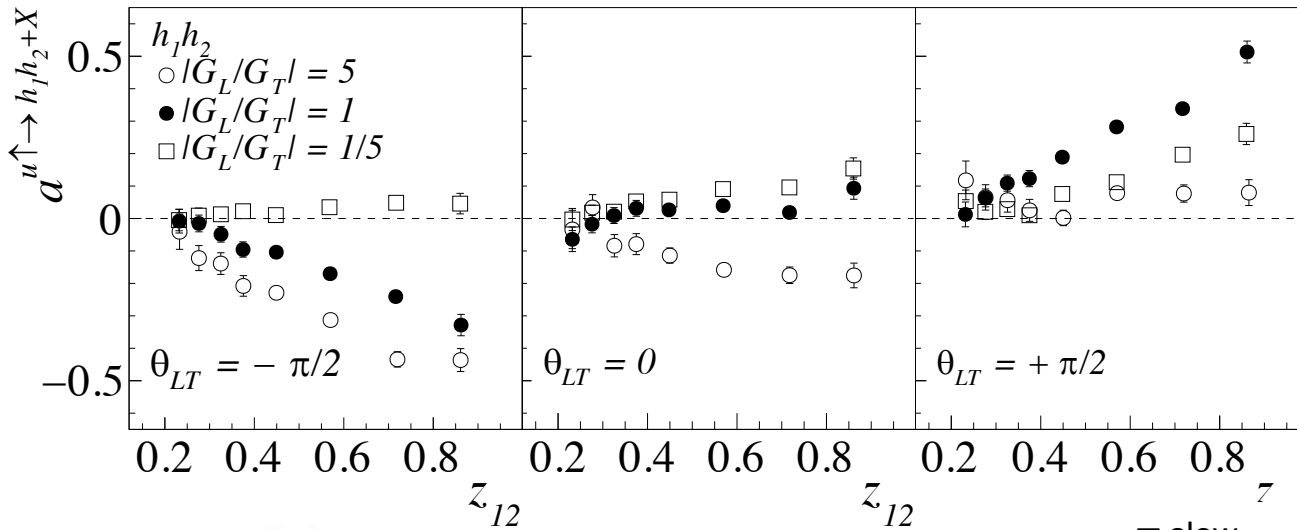
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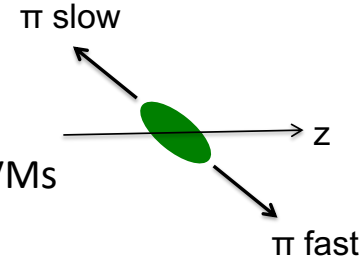
**z-ordered 2h analysing power in the decay  $\rho^0 \rightarrow \pi^+ \pi^-$**



Relevant to study the oblique polarization of VMs

→ asymmetry still large below the  $\rho^0$  region

→ interesting measurement in SIDIS and  $e^+e^-$



## Interface of the string+ $^3P_0$ model to PYTHIA hadronization

---

The simulation of complete scattering events requires many physics ingredients (PDF, hard scattering, parton showers, hadronization, decays .. )

Existing general purpose event generators include all these effects (for spin-less processes)

→ **introducing spin effects on top of them as an external additional feature is very convenient**

decoupled from new releases of the generator

must be done systematically, and with compromises

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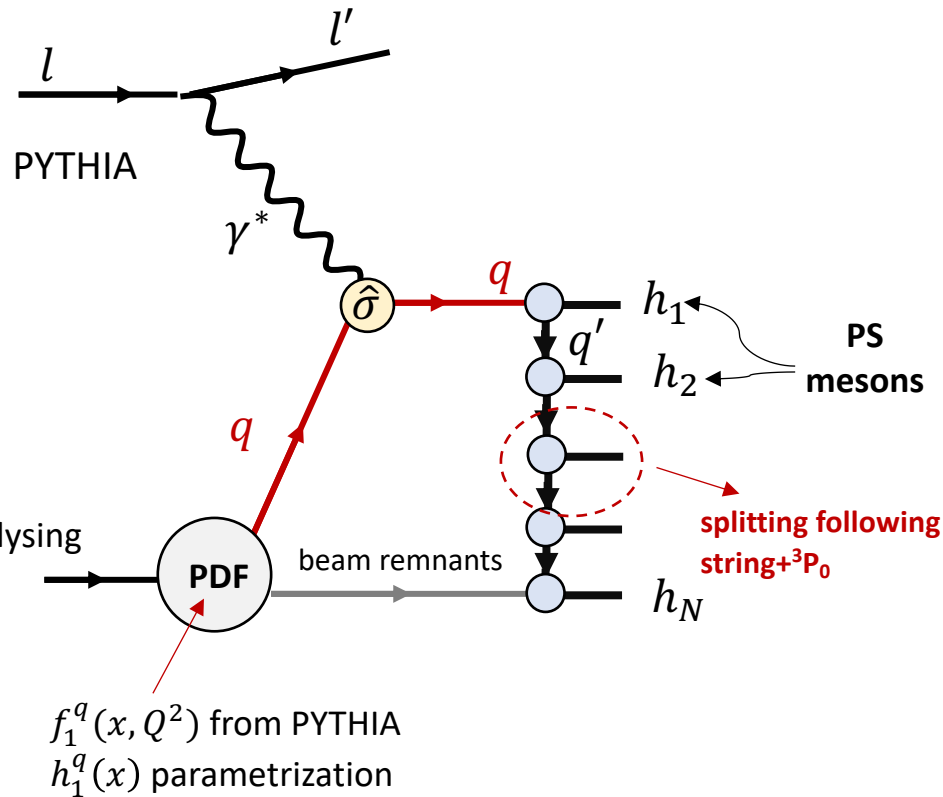
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## StringSpinner:

*an external «plug-in» which interfaces string+<sup>3</sup>P<sub>0</sub> with PYTHIA 8.2 for SIDIS*

*AK, L. Lönnblad, CPC 272 (2022) 108234*

- ISR/FSR switched OFF
- spin effects in string fragmentation to PS mesons
- parametrizations of transversity PDFs introduced (for  $u^v$  and  $d^v$ , can be changed by the user)
- also possible to chose the quark polarization by hand (analysing power)

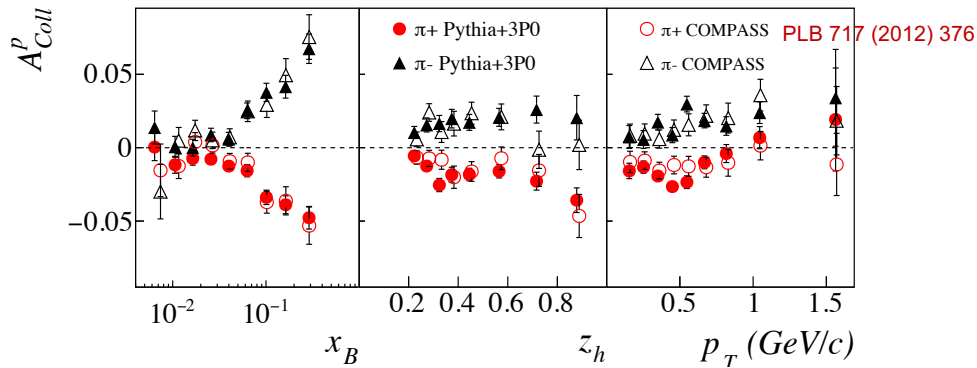


# Transverse spin asymmetries from StringSpinner

Simulations of SIDIS off protons in the COMPASS kinematics  
(no intrinsic  $\vec{k}_T$ ,  $\mu = (0.78 + i0.38) \text{ GeV}/c^2$ )

Code of StringSpinner available in  
<https://gitlab.com/albikerbizi/stringspinner.git>

## Collins asymmetry from StringSpinner



- Satisfactory description of TSA  
.. **promising tool!**

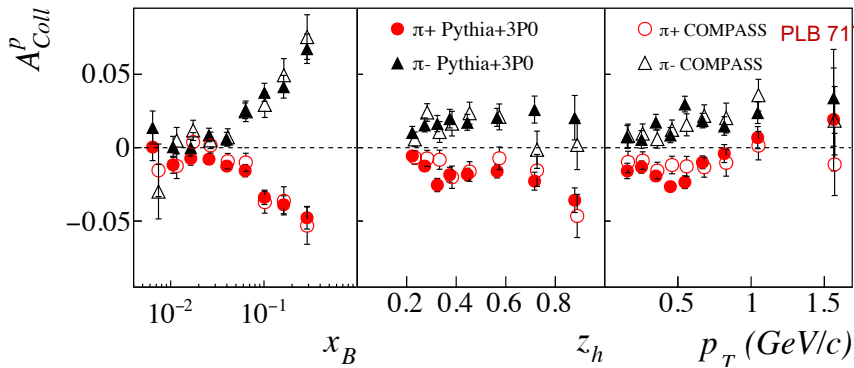


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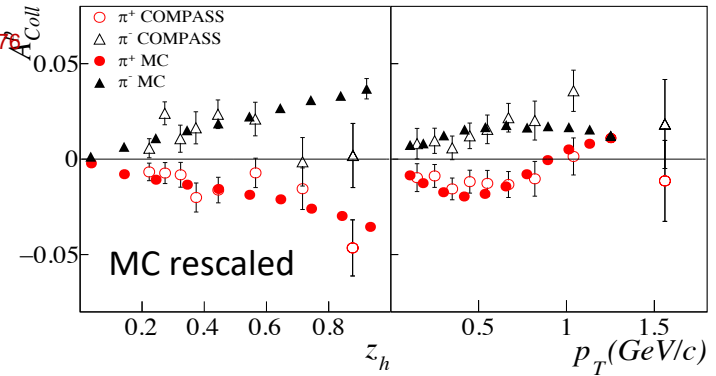
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## from Standalone MC



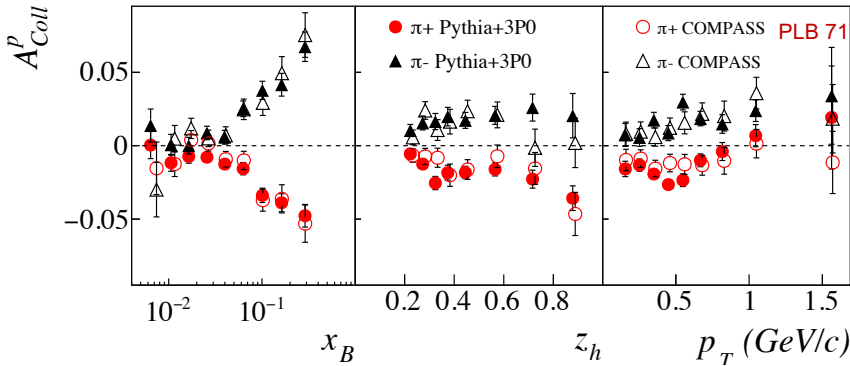
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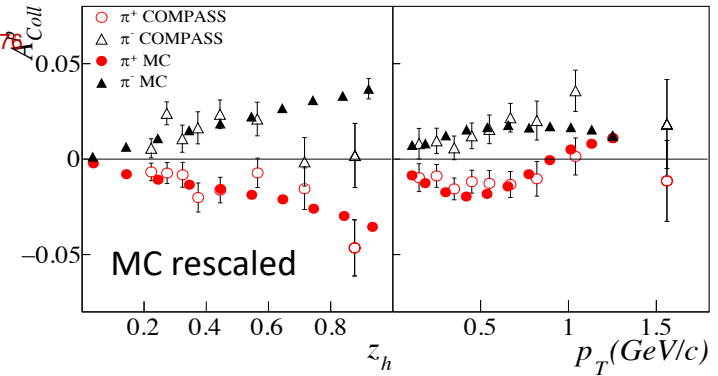
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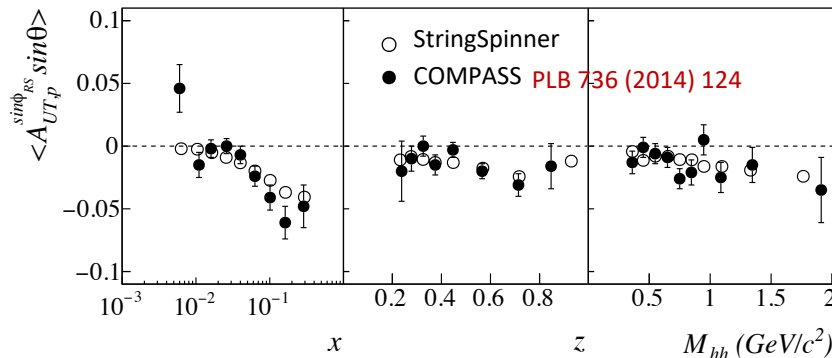
## Collins asymmetry from StringSpinner



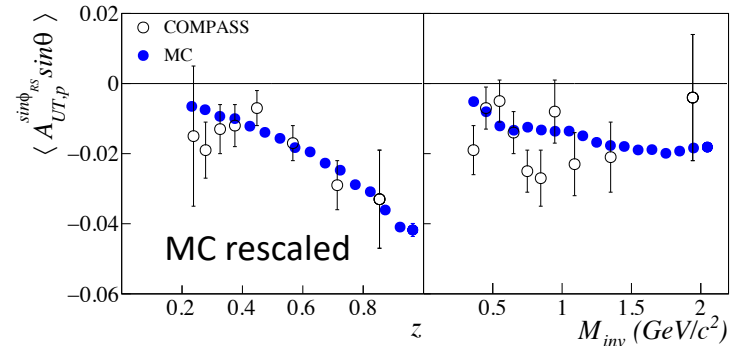
## from Standalone MC



## Dihadron asymmetry from StringSpinner



## from Standalone MC



- Satisfactory description of TSA  
.. promising tool!

## Conclusions

The string+ $^3P_0$  model includes PS meson and VM emission and has been studied in detail

→ describes the main features of Collins and di-hadron asymmetries!

→ hints for values of the free parameters related to VM

more precise data would help ( COMPASS 2022 d run, JLab12 .. )

and also new measurements, e.g. Collins asymmetries for  $\rho$  mesons,

$z$ -ordered 2h asymmetry in  $e^+e^-$  annihilation!

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.. the base for the systematic inclusion of spin effects in a MCEG has been laid!

**now is time to move on!**

include VM production in StringSpinner

apply the string+ $^3P_0$  model to the  $e^+e^-$  annihilation event

...

**backup**

# List of free parameters in the string+ $^3P_0$ model

---

## Spin effects

$$\mu = (0.42 + i0.76) \text{ GeV}/c^2$$

## Spinless Lund splitting Function

Elementary splitting

$$q(k) \rightarrow h(p) + q'(k')$$

Spinless Splitting Function

$$F_{\text{Lund}}^{1/2}(Z, \mathbf{p}_T) = C_{q',h,q}^{1/2} (1-Z)^{a/2} \exp\left(-\frac{b_L \varepsilon_h^2}{2Z}\right) \exp -b_T \mathbf{k}'^2$$

$$\varepsilon_h^2 = m_h^2 + \mathbf{p}_T^2, \quad \mathbf{p}_T = \mathbf{k}_T - \mathbf{k}'_T, \quad Z = p^+ / k^+$$

$$a = 0.9$$

$$b_L = 0.5 (\text{GeV}/c^2)^{-2}$$

$$b_T = 8.43 (\text{GeV}/c)^{-2}$$

## Vector Meson production

$$2|G_T|^2 + |G_L|^2 = \begin{cases} 0.62 & \text{light mesons} \\ 0.725 & \text{strange mesons} \end{cases}$$

$$|G_L/G_T| = 5, 1, 1/5$$

$$\theta_{LT} = -\frac{\pi}{2}, 0, +\frac{\pi}{2}$$