Deeply Virtual Compton Scattering at COMPASS

Anatolii Koval

on behalf of the COMPASS collaboration

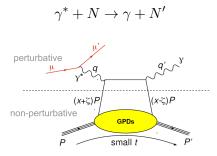
September 10, 2022

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- 1. Generalized Parton Distribution functions
- 2. Measurements at COMPASS and experimental setup
- 3. DVCS cross-section and steps for its extraction
- 4. Analysis of the cross section and its t-dependence

- Provide comprehensive description of 3-D partonic structure of the nucleon.
- Can be viewed as correlation functions between different partonic states.
- Allows to study decomposition of the total nucleon spin.

Deeply Virtual Compton Scattering



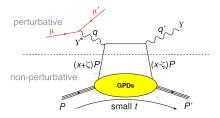
 $q=(p_{\mu}-p_{\mu'})$: 4-mom. of virt. photon $Q^2=-q^2$: virt. photon virtuality $t=(p_P-p_{P'})^2$: mom. transfer to nucleon squared

x: avg. long. mom. fraction

 ξ : half of long. mom. fraction transfer

Deeply Virtual Compton Scattering

 $\gamma^* + N \to \gamma + N'$



No nucleon spin flip $H^{f}(x,\xi,t)$ $\tilde{H}^{f}(x,\xi,t)$

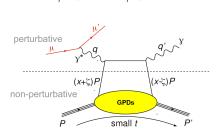
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GPDs are not experimentally accessible, but related to Compton Form Factors (CFFs)

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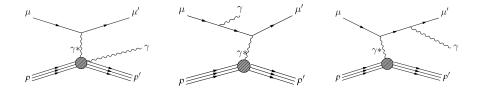
With nucleon spin flip $E^{f}(x,\xi,t)$ $\tilde{E}^{f}(x,\xi,t)$

CFFs are observables in cross section measurements

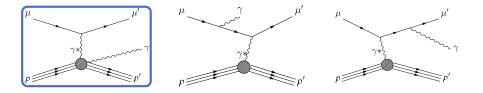
$$\mathcal{H}(\xi,t) = \int_{-1}^{1} \frac{H(x,\xi,t)}{x-\xi-i\epsilon} dx$$

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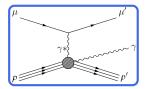
$\mu p \rightarrow \mu' p' \gamma \mbox{ processes}$

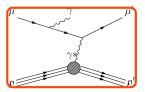


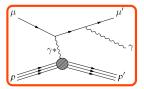
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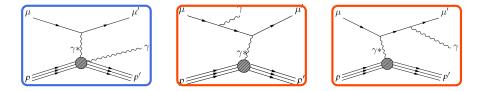
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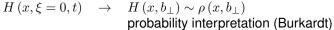
The observable products of these reactions are identical, therefore they can not be separated on per-event basis.

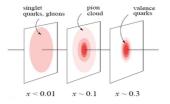
$$\sigma_\gamma \propto |A_{\rm DVCS}|^2 + |A_{\rm BH}|^2 + {\rm Interference Term}$$

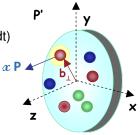
Interference Term $\equiv A_{\text{DVCS}}A_{\text{BH}}$ - allows to study DVCS on the amplitude level.

Most attractive goals

3D tomography via GPD H



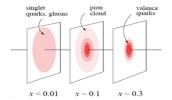




Most attractive goals

3D tomography via GPD H

 $H(x,\xi=0,t) \rightarrow H(x,b_{\perp}) \sim \rho(x,b_{\perp})$ probability interpretation (Burkardt)



Contribution to the nucleon spin puzzle $\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + \langle L_z^q \rangle + \langle L_z^g \rangle$

by constraining GPD H and E

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$$J^{q} = \frac{1}{2} \lim_{t \to 0} \int_{-1}^{+1} x \left[H^{q} \left(x, \xi, t \right) + E^{q} \left(x, \xi, t \right) \right] dx$$

GPD E related to the orbital angular momentum ICNFP2022

P

Z

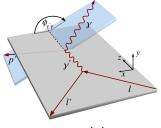
 $x \mathbf{P}$

×

Measurement at COMPASS

Diff. cross section
$$rac{d\sigma^4}{dQ^2 d
u d|t| d\phi}$$

 $\begin{array}{l} \mbox{Kinematic dependence:} \\ Q^2 = -q^2: \mbox{virtuality} \\ \nu = E_\mu - E_{\mu'}: \mbox{ ency of virt. photon} \\ t = (p_P - p_{P'})^2: \mbox{mom. transfer to nucleon squared} \\ \phi: \mbox{ angle between scattering and production planes} \end{array}$



 $\mu p \rightarrow \mu' p' \gamma$

Identify exclusive photon events:

- μ : beam muon
- μ' : scattered muon
- P': recoil proton
- γ : real photon

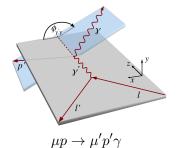
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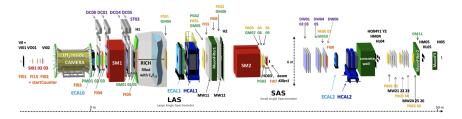
2012 pilot run for 4 weeks

 \rightarrow analysis finished and published

 2016/17 long runs (2 × 6 months) dedicated to DVCS

 \rightarrow analysis ongoing, preliminary results

COMPASS experiment setup



COmmon Muon and Proton Apparatus for Structure and Spectroscopy

2.5m long Liquid Hydrogen target

 $\begin{array}{lll} \text{Beam energy is } 140-180 \text{GeV} & \pi^+ \rightarrow \mu^+ + \nu_\mu & P_{\mu^+} \approx -80\% \\ \text{Beam polarisations: } \mu^{+\downarrow} \text{ and } \mu^{-\uparrow} & \pi^- \rightarrow \mu^- + \overline{\nu}_\mu & P_{\mu^-} \approx +80\% \end{array}$

COMPASS experiment setup



Two stage forward spectrometer SM1 + SM2

- Beam flux determined using true Random trigger, $\approx 1\%$ precission
- ECAL0, ECAL1 and ECAL2 for photon detection
- Muon trigger system ~ 300 tracking detector planes
- μ ID for muon identification

CAMERA



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Vertex candidates:

- $\mu\,$ Beam muon
- $\mu^\prime~{\rm Scattered}$ muon

Real photon candidate γ :

Single photon with the energy above DVCS threshold $E_{\gamma}>4,5,10~{\rm GeV}$ in ECAL0, 1, 2

Recoil proton candidate P': $|t|_{\max}^{\exp} = 0.64(\text{GeV}/c)^2$

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Exclusivity selections:

- $|\Delta p_T| < 0.3 {\rm GeV/c}$
- $|\Delta \phi| < 0.4 {\rm rad}$
- $|\Delta z_A| < 16 {\rm cm}$
- $|M^2_{\rm Undet}| < 0.3 ({\rm GeV/c}^2)^2$
- $0.08({\tt GeV/c})^2 < |t_{\tt fit}| < 0.64({\tt GeV/c})^2$

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Perform kinematic fit:

- constrain on kinematic variables $\chi^2 < 10$

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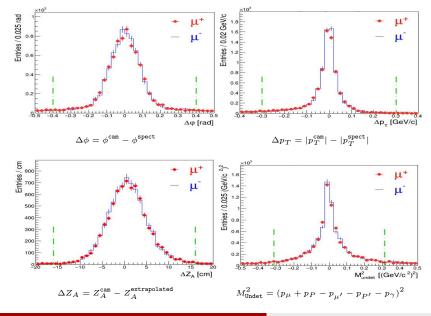
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Only events with single valid combination

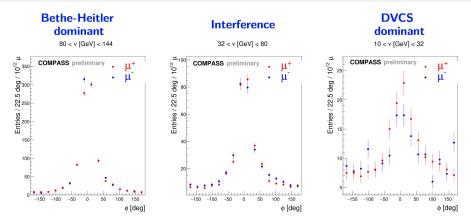
 $Vertex \ candidate \times \ Real \ photon \ candidate \times \ Recoil \ proton \ candidate$

Exclusive selections (COMPASS 2016 preliminary results)



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ϕ distribution of single γ events at different ν



Number of reconstructed single-photon events as a function of angle ϕ .

left. $80 \text{GeV} < \nu < 144 \text{GeV}$ BH dominates, DVCS - negligiblemiddle. $32 \text{GeV} < \nu < 80 \text{GeV}$ BH and DVCS are comparableright. $10 \text{GeV} < \nu < 32 \text{GeV}$ DVSC dominates BHAnatolii Koval

13/25

DVCS cross section in bins of t, ϕ , Q^2 , ν :

$$\begin{split} \left\langle \frac{d\sigma_{\rm DVCS}}{d|t|d\phi dQ^2 d\nu} \right\rangle_{t_i \phi_j Q_k^2 \nu_l}^{\pm} = \\ \frac{1}{\mathcal{L}^{\pm} \Delta t_i \Delta \phi_j \Delta Q_k^2 \Delta \nu_l} \left[\left(a_{ijkl}^{\pm} \right)^{-1} \left(\text{data} - \text{BH}_{\rm MC} - \pi_{\rm MC}^0 \right) \right] \end{split}$$

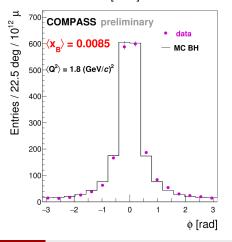
 a_{ijkl}^{\pm} Acceptance BH_{MC} Exclusive single photon MC sample $\pi_{MC}^{0} \pi^{0}$ MC sample (background estimation)

The Bethe-Heitler contribution

Bethe-Heitler process is well known, pure QED

 \rightarrow evaluated using Monte-Carlo sample for BH

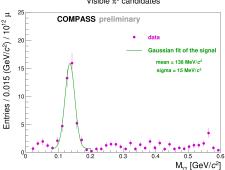
- Kinematic range where BH is dominant
 - \rightarrow use data/MC luminosities for absolute normalization
- BH substracted from the data in the DVCS region (small ν)



80 < v [GeV] < 144

The π^0 background contamination

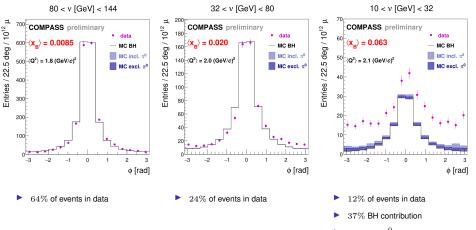
- > Photons from π^0 decay
- One photon identified as exclusive photon event \rightarrow above DVCS energy threshold in ECALs
- Visible (both γ are detected) - substracted Combine $\gamma_{\rm he}$ and $\gamma_{\rm le}$ (below DVCS energy threshold)
- **Invisible** (second γ lost)
 - estimated by MC
 - Inclusive: LEPTO
 - **Exclusive:** HEPGEN π^0



Visible π^0 candidates

ϕ distribution of exclusive photon events

 $1 < Q^2 < 10 ({\rm GeV/c})^2$



• 10% inv. π^0 contribution

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BH_{MC}: BH MC sample

• π^0_{HEPGEN} : exclusive π^0 MC sample • π^0_{LEPTO} : inclusive π^0 MC sample

DVCS cross section in bins of t, ϕ , Q^2 , ν :

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$$\pi^0_{ ext{MC}} = (1-R) imes \pi^0_{ ext{HEPGEN}} + R imes \pi^0_{ ext{LEPTO}}$$

BH_{MC}: BH MC sample

- π^0_{HEPGEN} : exclusive π^0 MC sample
- π^0_{LEPTO} : inclusive π^0 MC sample
 - ► R: relative contrib. of LEPTO (≈ 40%)
 - a_{ijkl}^{\pm} : acceptance

Acceptance studies limit to region with mostly flat acceptance

avg. acc. $\approx 40\%$, good agreement between μ^+ and μ^-

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$$\pi^0_{ ext{MC}} = (1-R) imes \pi^0_{ ext{HEPGEN}} + R imes \pi^0_{ ext{LEPTC}}$$

BH_{MC}: BH MC sample

Binning and kinematic range:

- 4 bins in |t| between 0.08 and 0.64(GeV/c)² (equistatistics)
- ▶ 4 bins v between 10 and 32 GeV (equidistant)
- 4 bins Q² between 1 and 5(GeV/c)² (equidistant)
- 8 bins φ between -π and +π (equidistant)

- π^0_{HEPGEN} : exclusive π^0 MC sample
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From
$$\mu p$$
 to $\gamma^* p$: $\frac{d\sigma^{\mu p}}{dt dt \phi dQ^2 d\nu} = \Gamma\left(Q^2, \nu\right) \times \frac{d\sigma^{\gamma^* p}}{dt dt \phi dQ^2 d\nu}$

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by weighting each event in data and MC by the inverse flux of the transverse polarized photons

$$\Gamma\left(Q^{2},\nu\right) = \frac{\alpha_{EM}\left(1-x_{Bj}\right)}{2\pi Q^{2} y E} \left[y^{2} \left(1-2\frac{2m_{\mu}^{2}}{Q^{2}}\right) + \frac{2}{1+\left(Q^{2}/\nu^{2}\right)} \left(1-y-\frac{Q^{2}}{4E^{2}}\right)\right]$$

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t-dependence for μ^+ and μ^-

$$\left\langle \frac{d\sigma_{\text{DVCS}}}{d|t|} \right\rangle_{t_i}^{\pm} = \left(\Delta Q^2 \Delta \nu \right)^{-1} \Sigma_{k,l} \left\langle \frac{d\sigma_{\text{DVCS}}}{d|t|dQ^2 d\nu} \right\rangle_{t_i Q_k^2 \nu_l}^{\pm} \Delta Q_l^2 \Delta \nu_l$$

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 \rightarrow Integrating over ϕ dependence **removes interference and** ϕ -dependent DVCS contribution

$$\begin{split} \mathcal{S}_{CS,U} &= d\sigma^{+\downarrow} + d\sigma^{-\uparrow} = \\ & 2 \left[d\sigma^{\text{BH}} + c_0^{\text{DVCS}} + c_1^{\text{DVCS}} \cos\phi + c_2^{\text{DVCS}} \cos2\phi + s_1^{\text{I}} \sin\phi + s_2^{\text{I}} \sin2\phi \right] \end{split}$$

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t-dependence of the cross section:

$$\left\langle \frac{d\sigma_{\rm DVCS}}{d|t|} \right\rangle_{t_i} = \frac{1}{2} \left(\left\langle \frac{d\sigma_{\rm DVCS}}{d|t|} \right\rangle_{t_i}^+ + \left\langle \frac{d\sigma_{\rm DVCS}}{d|t|} \right\rangle_{t_i}^- \right)$$

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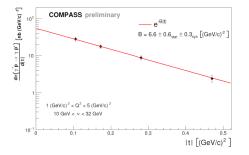
Analyse the cross section *t*-slope

$$d\sigma^{\rm DVCS}/dt \sim e^{-B|t|} \propto c_0^{\rm DVCS} = (Im\mathcal{H})^2$$

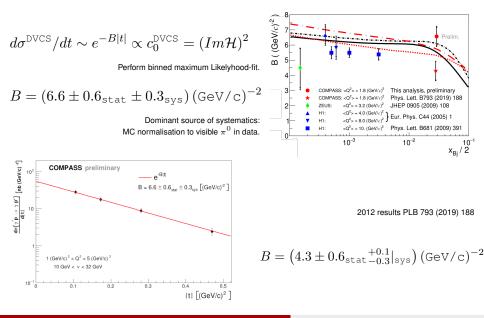
Perform binned maximum Likelyhood-fit.

$$B = (6.6 \pm 0.6_{\rm stat} \pm 0.3_{\rm sys}) \, ({\rm GeV/c})^{-2}$$

Dominant source of systematics: MC normalisation to visible π^0 in data.



Analyse the cross section *t*-slope



Outlook

- Analyse full statistics of 2016 and 2017 (3 times more data than 2016)
- More detailed studies of systematic uncertainties
- Cross section study in few x_{Bj} regions \rightarrow tomography
- ▶ Study the azimuthal dependence of the cross section → Determine c_0^{DVCS} , c_1^{DVCS} , c_2^{DVCS} , s_1^{I} and s_2^{I}
- Cross section difference $\mathcal{D}_{CS,U} = d\sigma^{+\downarrow} d\sigma^{-\uparrow}$ \rightarrow Access to $Re\mathcal{H}$

Thank you for your attention!

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Backup

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Cross section

$$d\sigma \propto |A_{\rm BH}|^2 + |A_{\rm DVCS}|^2 + \text{Interference Term}$$

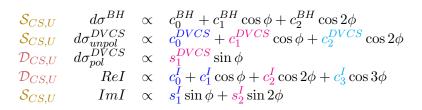
$$\frac{d^4\sigma(lp \to lp\gamma)}{dx_{Bj}dQ^2d|t|d\phi} = d\sigma^{BH} + \left(d\sigma^{DVCS}_{unpol} + P_ld\sigma^{DVCS}_{pol}\right) + \left(e_lReI + e_lP_lImI\right)$$

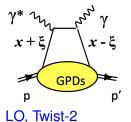
$$\mathcal{D}_{CS,U} = d\sigma^{+\downarrow} - d\sigma^{-\uparrow} = 2 \left[e_{\mu} a^{BH} Re A^{DVCS} + |P_{\mu}| d\sigma^{DVCS}_{pol} + ReI \right]$$
$$= 2 \left[s_1^{DVCS} \sin \phi + c_0^I + c_1^I \cos \phi + c_2^I \cos 2\phi + c_3^I \cos 3\phi \right]$$

$$\begin{aligned} \mathcal{S}_{CS,U} &= d\sigma^{+\downarrow} + d\sigma^{-\uparrow} = 2 \left[d\sigma^{BH} + d\sigma^{DVCS}_{unpol} - |P_{\mu}|ImI \right] \\ &= 2 \left[d\sigma^{BH} + c_0^{DVCS} + c_1^{DVCS} \cos\phi + c_2^{DVCS} \cos 2\phi + s_1^I \sin\phi + s_2^I \sin 2\phi \right] \end{aligned}$$

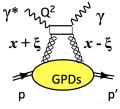
Cross section

$$\mathcal{S}_{CS,U} = d\sigma^{+\downarrow} + d\sigma^{-\uparrow} \qquad \qquad \mathcal{D}_{CS,U} = d\sigma^{+\downarrow} - d\sigma^{-\uparrow}$$





 γ^{*} γ^{*} γ^{*} γ^{*} $x - \xi$ $x + \xi$ $x - \xi$ p p'LO, Twist-3



NLO, Twist-2