

# COMPASS results on nucleon spin and structure

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- **Nucleon longitudinal & transverse spin**
- **Quark Fragmentation functions**
- **Generalized parton distributions**
- **$\pi$  induced Drell-Yan and J/Psi production**

# COMPASS at CERN

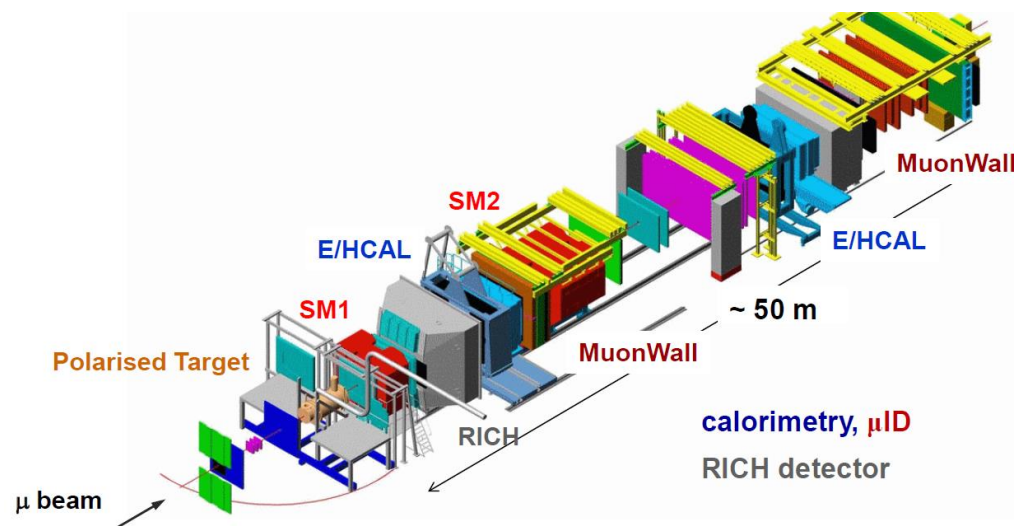
160-200 GeV

polarized muon beam DIS

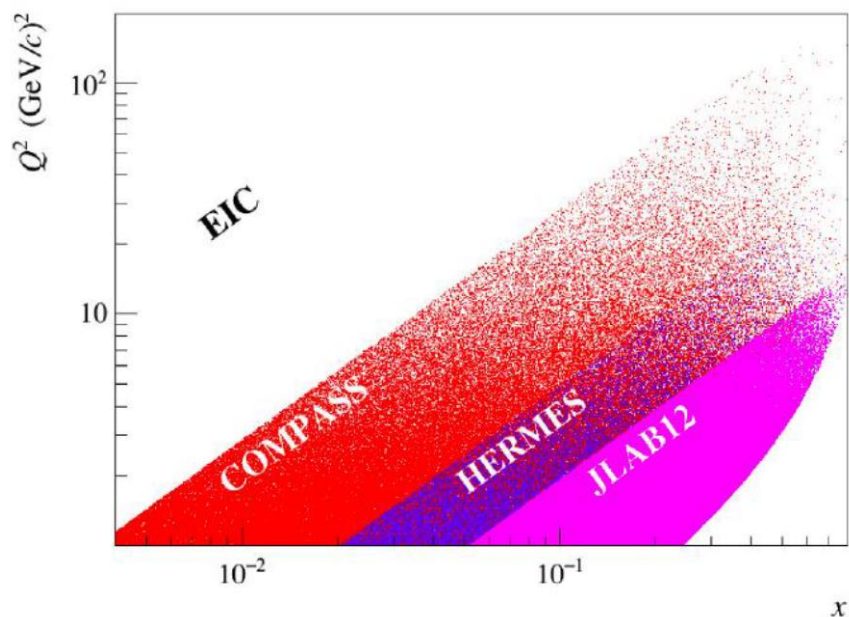
pion beam: Drell-Yan

Long solid polarized targets,  
LH2 target

& nuclear targets for DY



DIS kinematics



# Nucleon spin - longitudinal

How is the nucleon spin distributed among its constituents?

$$\text{Nucleon Spin } \frac{1}{2} = \underbrace{\frac{1}{2}\Delta\Sigma}_{\text{quark}} + \underbrace{\Delta G}_{\text{gluon}} + \underbrace{L}_{\text{orbital momentum}}$$

$\Delta\Sigma$  : sum over u, d, s,  $\bar{u}$ ,  $\bar{d}$ ,  $\bar{s}$   
can take non half-integer value:  
superposition of several spin states

$$\Delta q = \overrightarrow{q} - \overleftarrow{q}$$

Parton spin parallel or anti parallel to nucleon spin

$\Delta\Sigma$  Today:

Precise world data on polarized DIS:  $g_1 + \text{SU}_f(3) \quad a_0 = \Delta\Sigma \sim 0.3$   
Quark spin contribution  $\sim 30\%$

Confirmed by results from Lattice QCD on  $\Delta\Sigma_{u,d,s}$

Large experimental effort on :

-  **$\Delta G$  measurement**

also because  $a_0 = \Delta\Sigma - n_f (\alpha_s/2\pi) \Delta G$  (AB scheme)

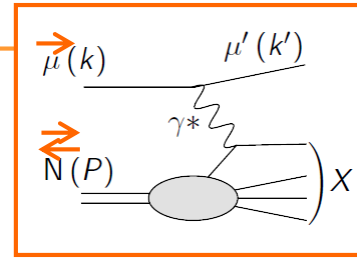
- **3D mapping of nucleon and constraining L**

through DVCS and Hard Exclusive Meson Production

# QCD fits- World data on $g_1^p$ and $g_1^d$

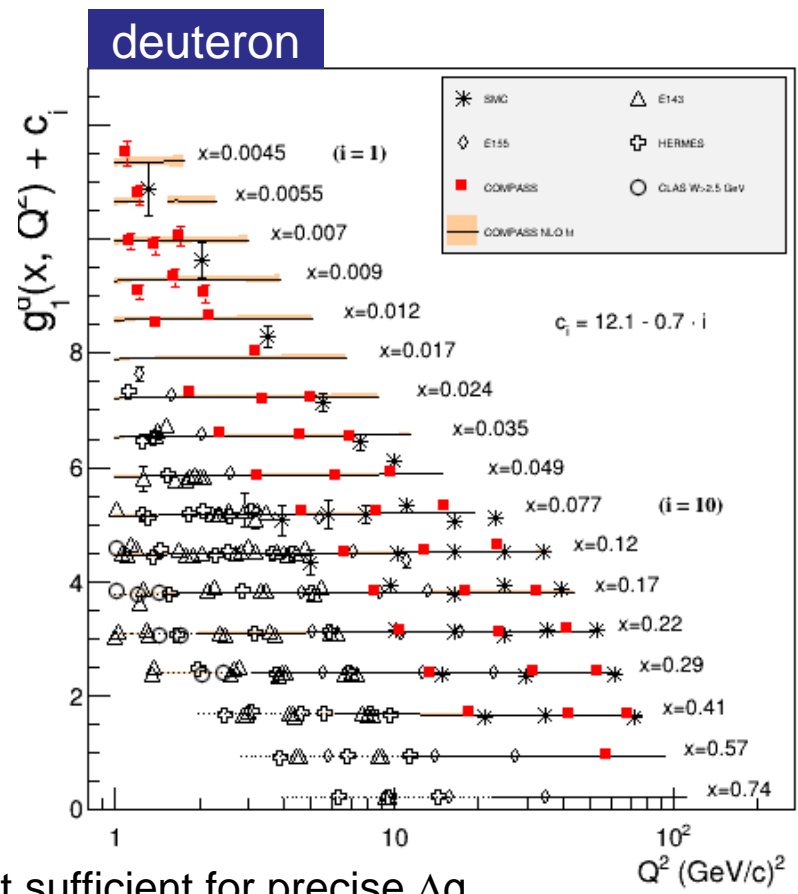
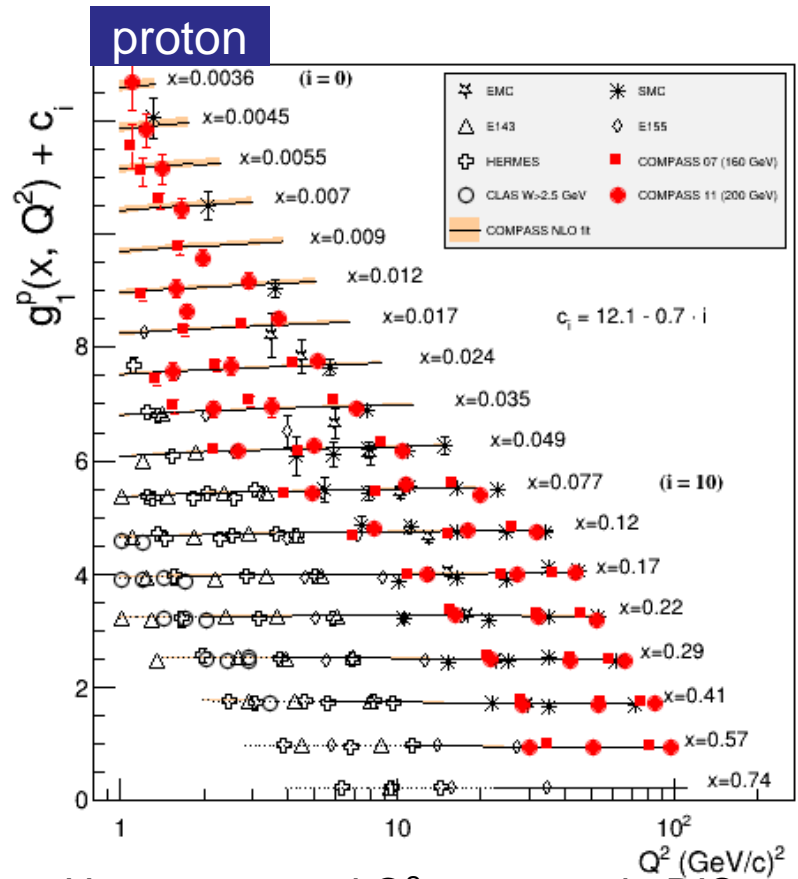
DIS

Polarized Deep Inelastic Scattering  
 → Nucleon spin structure functions  $g_1$



$$\frac{d g_1}{d \text{Log}(Q^2)} \propto -\Delta g(x, Q^2)$$

→  $g_1(x, Q^2)$  as input to global QCD fits for extraction of  $\Delta q_f(x)$  and  $\Delta g(x)$



However  $x$  and  $Q^2$  coverage in DIS not yet sufficient for precise  $\Delta g$   
 Need to use constraint from pp data (as in DSSV, NNPDF... fits)

PLB753 (2016) 18

# NLO pQCD fit to $g_1$ DIS world data

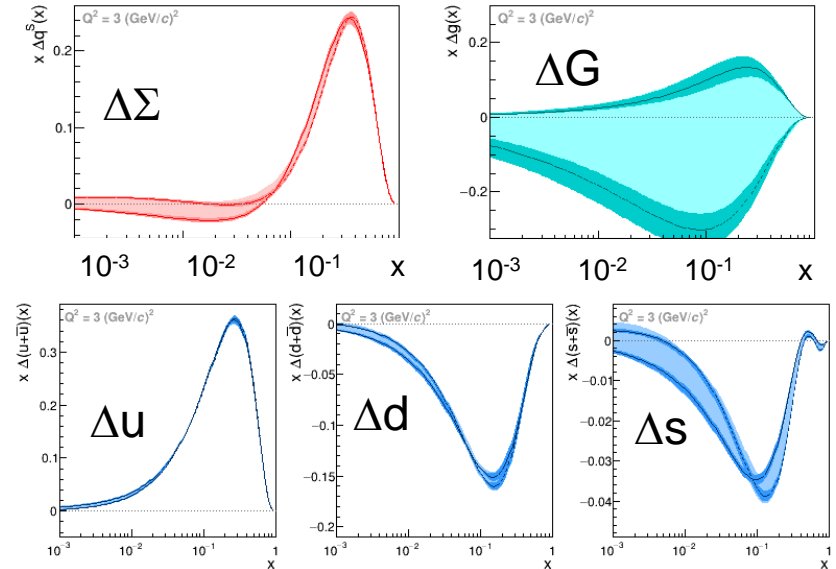
- Assume functional forms for  $\Delta\Sigma$ ,  $\Delta G$  and  $\Delta q^{\text{NS}}$
- Use DGLAP equations, relating  $\Delta\Sigma$ ,  $\Delta G$  evolutions .
- Fit  $g_1^p$ ,  $g_1^d$ ,  $g_1^n$  DIS world data. ( $SU_3$ )

COMPASS, PLB 753 (2016) 18

- Extract  $\Delta\Sigma$  Quarks  $\Delta G$  Gluons

## $\Delta G$ not well constrained using DIS only

Obtain solutions with  $\Delta G > 0$  and  $\Delta G < 0$   
 Solution with  $\Delta G > 0$  agrees with result from DSSV++ which uses RHIC pp data



$$0.82 \leq \Delta U \leq 0.85 \quad -0.45 \leq \Delta D \leq -0.42 \quad -0.11 \leq \Delta S \leq -0.08$$

$\Delta\Sigma$  well constrained in valence region

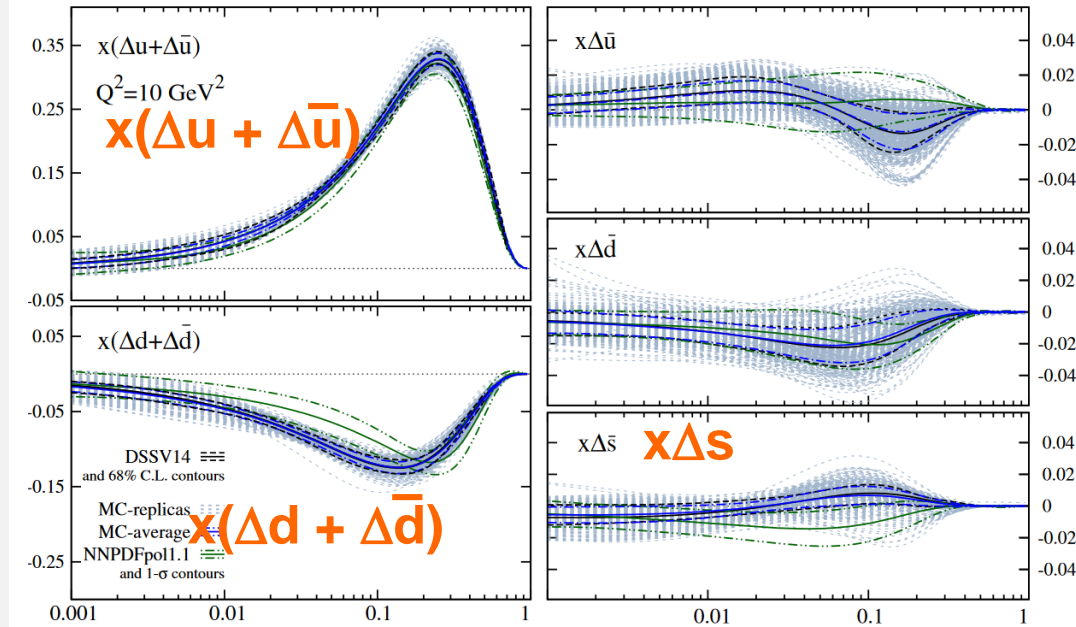
$$\Delta\Sigma = 0.31 (5) \text{ at } Q^2=3 \text{ (GeV/c)}^2$$

Still large uncertainty coming from the bad knowledge of functional forms

# Global fits to polarized PDFs (I)

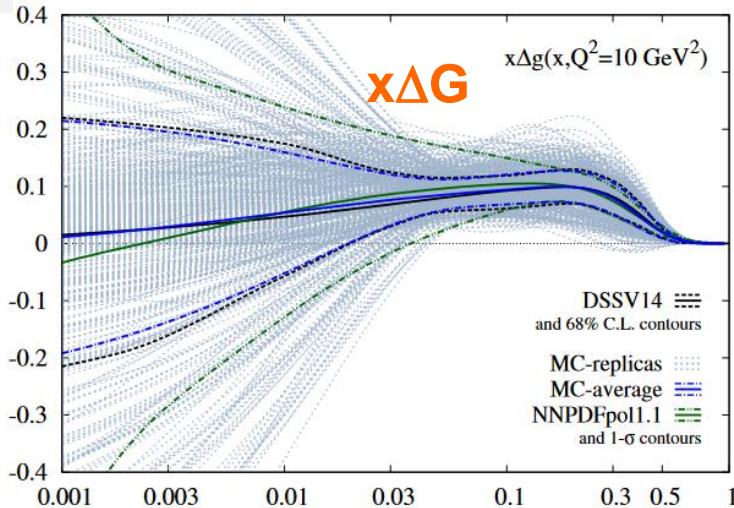
Fits to world data, including  $\vec{p}\vec{p}$  collider data. Many fitters. Some examples:

DLSSV: PRD100, 114027 (2019)



Blue: **DSSLV**  
from DSSV14 w. replicas  
and MC average

Green: **NNPDFpol1.1**



**More realistic evaluation of uncertainties**

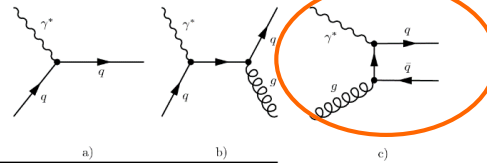
Still some discrepancies in  **$\Delta s$  sign**  
and in  **$\Delta d$  position of minimum**

~ unknown  **$\Delta G$** , below  $x \sim 0.05$

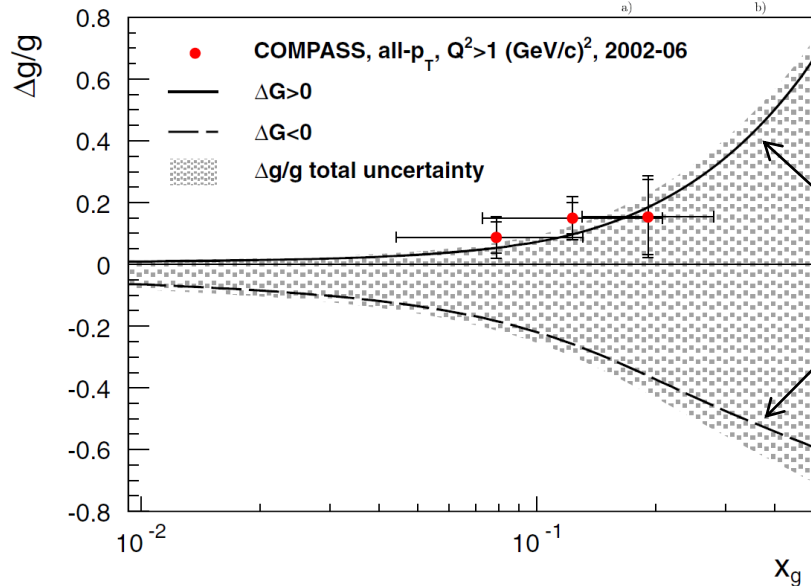
# Gluon helicity $\Delta G/G$ direct measurement

$Q^2 > 1 (\text{GeV}/c)^2$

$$\vec{\mu} \quad \vec{p} \rightarrow \mu' \quad h + h + X$$



## Photon Gluon Fusion



Extraction at LO:

$$\Delta g/g (x=0.1) = 0.11 \pm 0.04 \pm 0.04$$

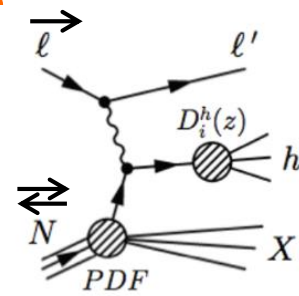
Solutions from COMPASS NLO  
QCD fit of  $g_1$  world data (see before)

**EPJC 77 (2017) 209**

Results are in agreement with fits from NNPDF and DSSV++ using RHIC  $\vec{p}\vec{p}$  data, which gave:

$$\int_{0.05}^{0.2} \Delta g(x) dx \simeq 0.20$$

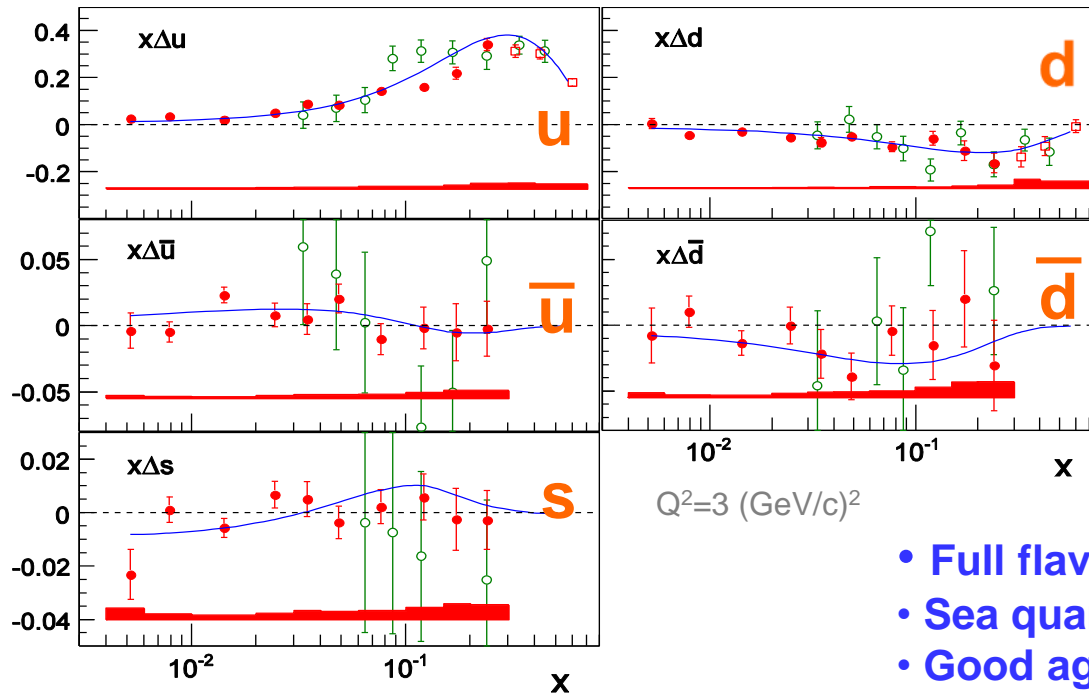
# Quark helicities from semi-inclusive DIS



$$l \rightarrow p \rightarrow l h^{+/-} X$$

Outgoing hadron tags quark flavor  
(via quark fragmentation functions)

Flavour separation of quark helicities:



- HERMES  
PRD71(2005)012003
- COMPASS  
PLB693(2010)227, using DSS-07 FFs
- DSSV at NLO

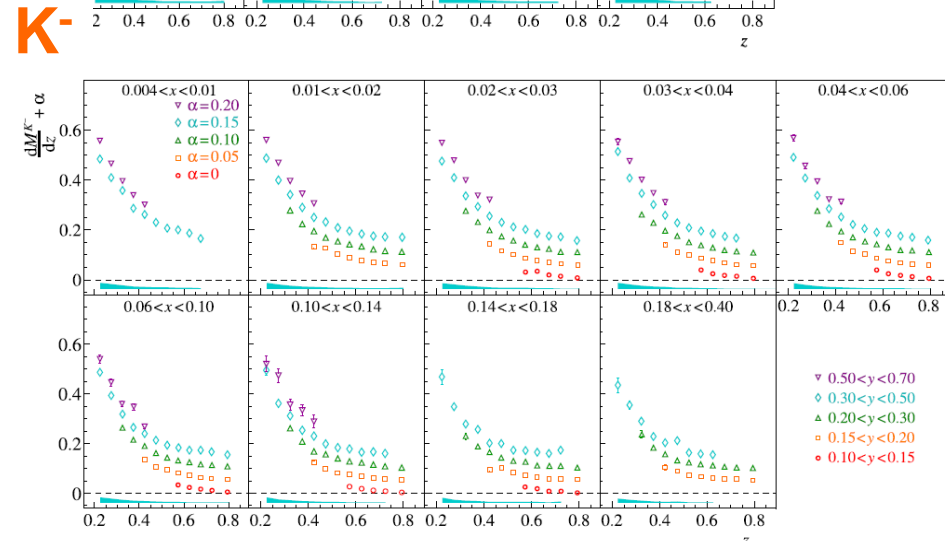
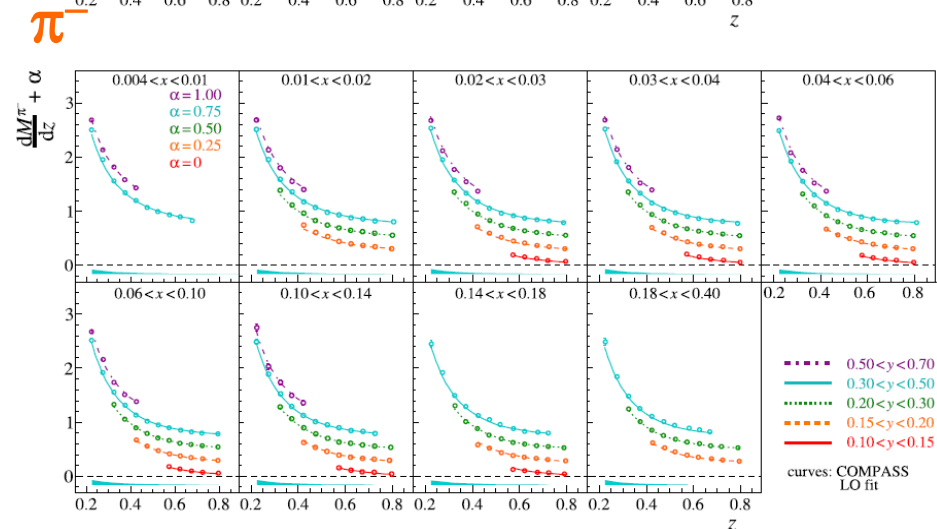
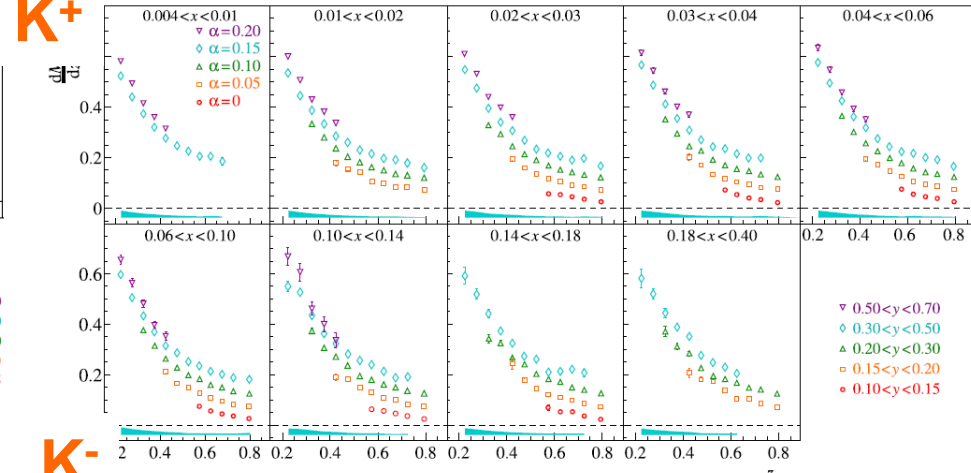
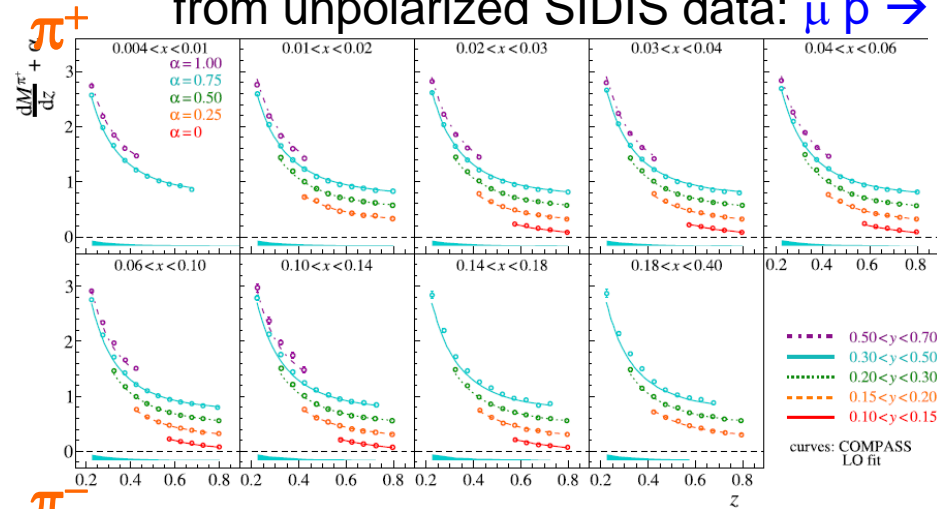
- Full flavour separation →  $x \sim 0.004$
- Sea quark distributions ~ zero
- Good agreement with global fits

NB: The SIDIS extraction uses input of quark Fragmentation Functions, not that well determined yet, especially for the strange quark sector.



# COMPASS $\pi$ and $K$ multiplicities vs $z$ in $(x,y)$ bins

from unpolarized SIDIS data:  $\mu p \rightarrow \mu' \pi/K X$



- More than 1200 points in total, various  $Q^2$  staggered vertically for clarity
- Strong  $z$  dependance
- $M(\pi^+) \sim M(\pi^-)$  and  $M(K^+) > M(K^-)$

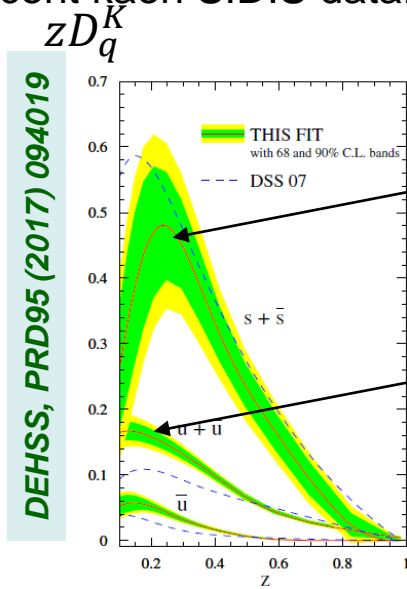
PLB 764 (2017) 001  
PLB 767 (2017) 133

# Kaons- Quark fragmentation functions from NLO fits

Extensive sets of SIDIS kaon data  
change significantly flavor decomposition of FFs (& PDFs)

COMPASS PLB 767 (2017) 133

Ex1: **DEHSS-17** fit to quark FF, includes recent kaon SIDIS data.

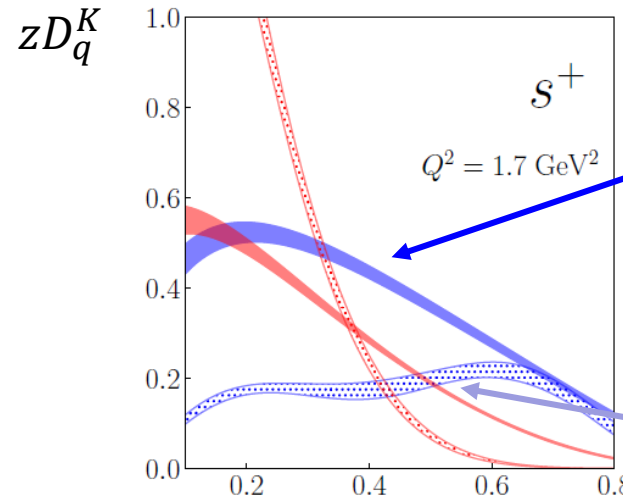


$D_S^K$   
smaller than  
in DSS-07

$D_U^K$   
larger than in  
DSS-07

Ex2: **JAM18 w/o SIDIS data**

Combined fit of PDFs and FFs (prelim)



$D_S^K$  w SIDIS  
agrees with  
DEHSS

$D_S^K$  w/o SIDIS

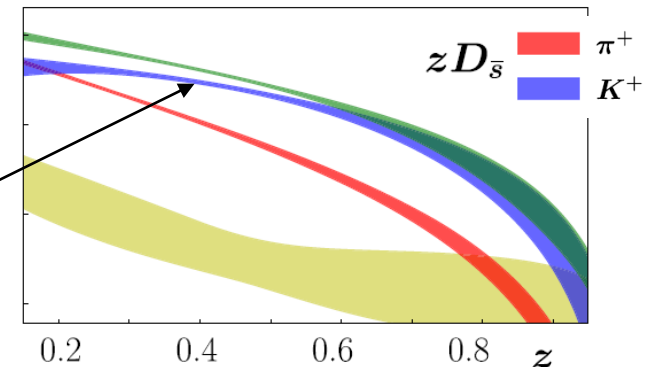
Also **simultaneous/ iterative fits of PDFs & FFs:**

Ex: **Borsa, Sasso, Stratmann, PRD96 (2017)**

& **JAM20-sidis, PRD104 (2021) 016015**

SIA + SIDIS data : strong preference for smaller strange to nonstrange PDF ratio, and enhanced  $D_s^K$

→ worth revisiting  $\Delta s(x)$  extraction from SIDIS data



# $R_K = M(K^-) / M(K^+)$ kaon multiplicity ratio at high $z$

$\mu p \rightarrow \mu' K X$

**Motivation:** High  $z$  region not studied so far

Most experimental and theoretical uncertainties cancel in ratio

**Simple estimation at LO**, proton target

with assumptions ( $D_{unf}$  neglected...):

and assuming  $s = \bar{s}$ ,

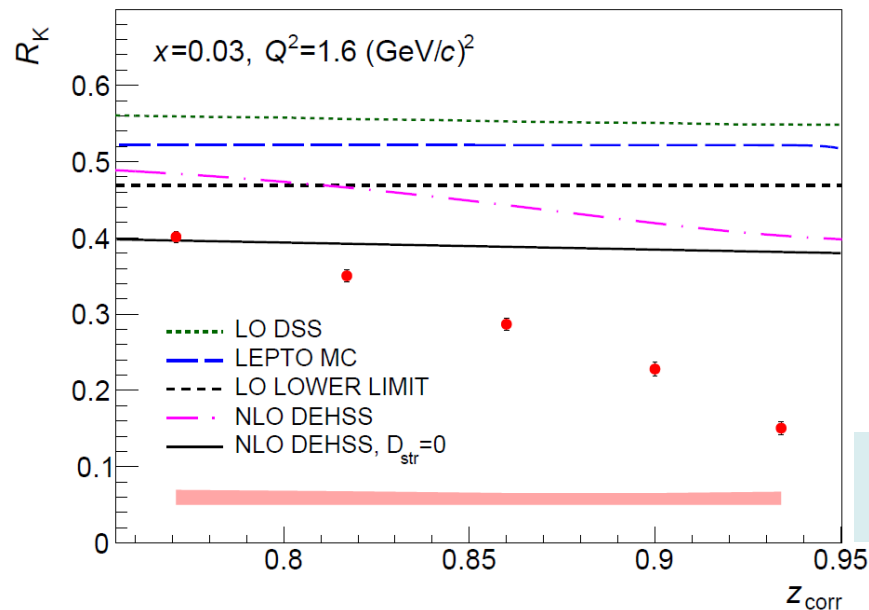
→  $R_K$  **lower bound** driven by light quarks:

$$R_K = \frac{4\bar{u}D_{fav} + sD_{str}}{4uD_{fav} + \bar{s}D_{str}}$$

$$R_K > \frac{\bar{u}}{u} \quad \text{for a proton target}$$

$$R_K > \frac{\bar{u} + \bar{d}}{u + d} \quad \text{for a deuteron target}$$

In contradiction with data:



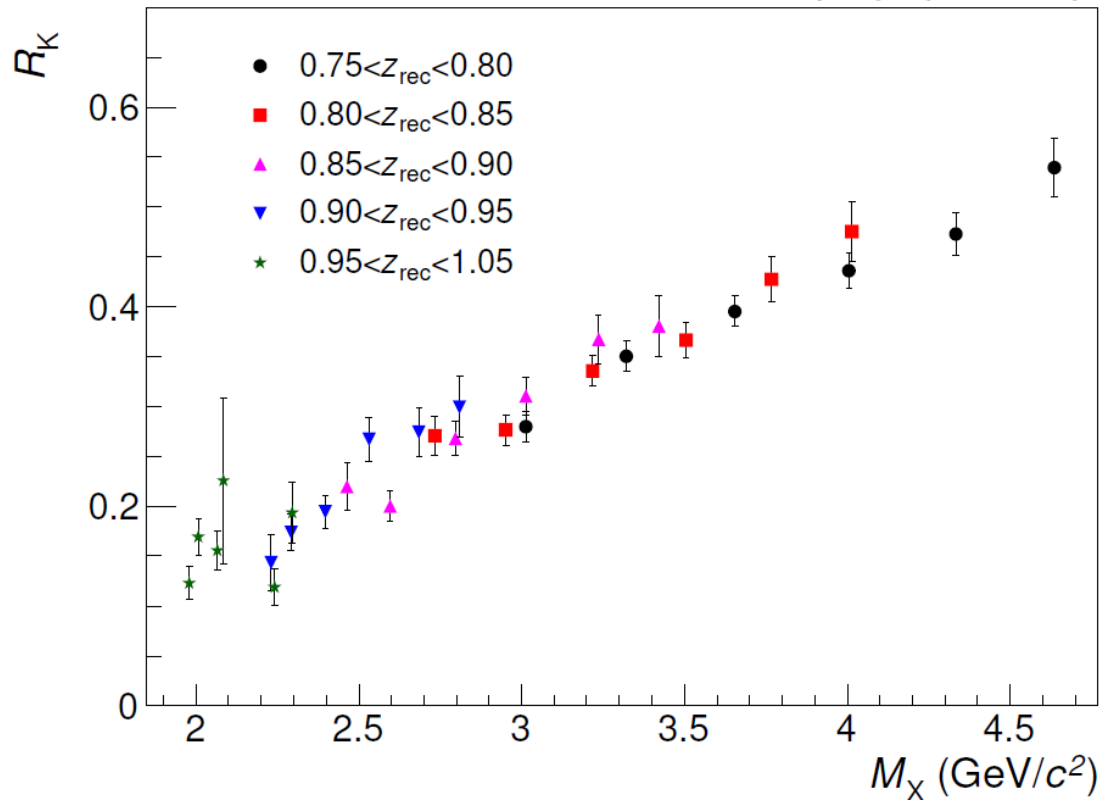
$M(K^-) / M(K^+)$  ratio well below expectations at high  $z$

# M(K<sup>-</sup>)/ M(K<sup>+</sup>) Results vs missing mass $M_X$

High  $z$  kaon  $\rightarrow$  reduced phase space for other particles

Study missing mass behaviour

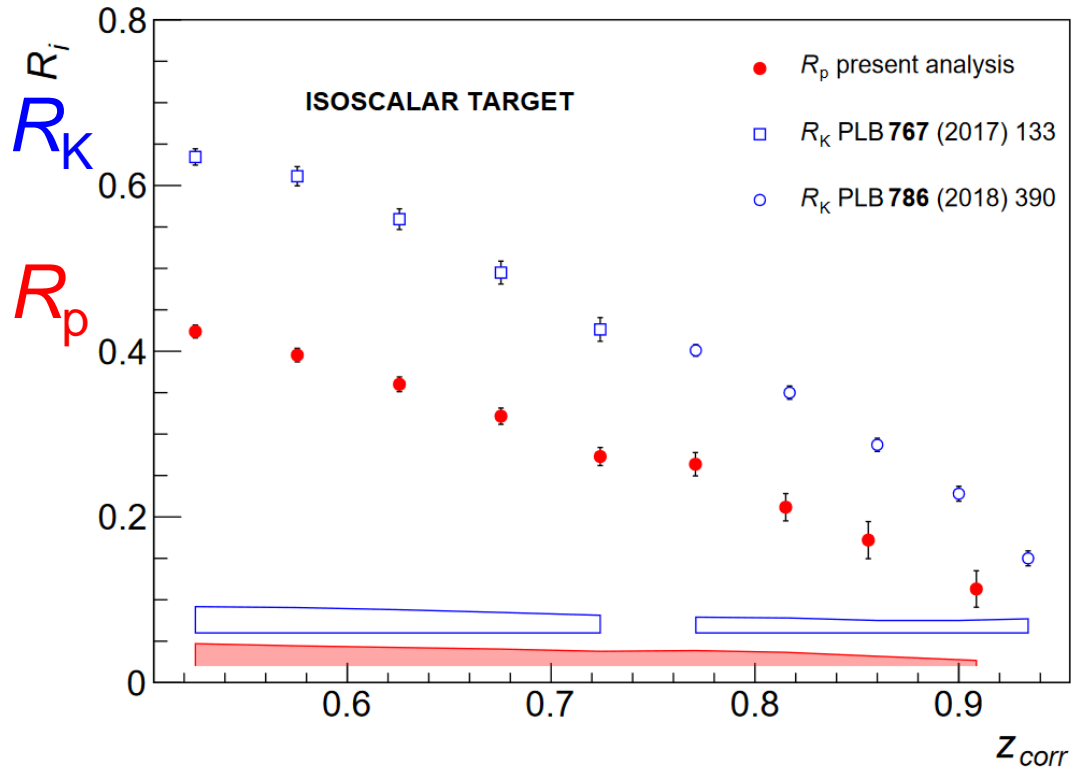
$$M_X = \sqrt{M_p^2 + 2M_p v(1-z) - Q^2(1-z)^2}$$



- **M(K<sup>-</sup>)/ M(K<sup>+</sup>) shows unexpected strong rise with  $M_X$**
- **Suggests to take into account the available phase space for hadronisation, in the formalism**

$$R_p = M(\bar{p}) / M(p)$$

Stronger suppression of  $\bar{p}$  vs  $p$ ,  
compared to  $K^-$  vs  $K^+$ .



PLB 807 (2020) 135600

# Transverse Momentum Dependent distributions

## TMDs

↑ spin of the nucleon  
 ↑ spin of the parton  
 ↗  $k_T$  of the parton

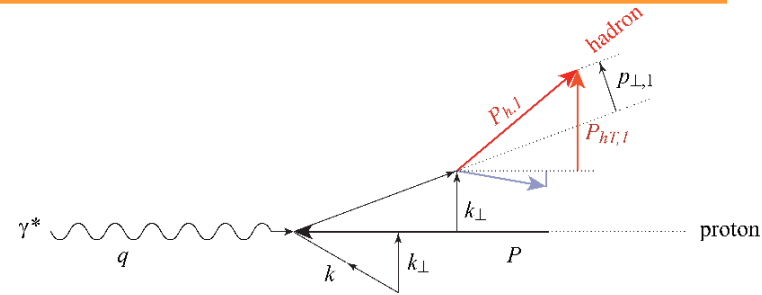
		Quark		
		U	L	T
Nucleon	U	 number density $f_1^{q,g}(x, k_T^2)$		 Boer-Mulders $h_1^{\perp q,g}(x, k_T^2)$
	L		 Helicity $g_{1L}^{q,g}(x, k_T^2)$	 worm-gear L $h_{1L}^{\perp q,g}(x, k_T^2)$
	T	 Sivers $f_{1T}^{\perp q,g}(x, k_T^2)$	 Kotzinian-Mulders worm-gear T $g_{1T}^{\perp q,g}(x, k_T^2)$	 Transversity $h_1^{q,g}(x, k_T^2)$ Pretzelosity $h_{1T}^{\perp q,g}(x, k_T^2)$

# Transverse Momentum Dependent distr. : TMDs

Importance of hadron transverse momentum  $p_T$ :

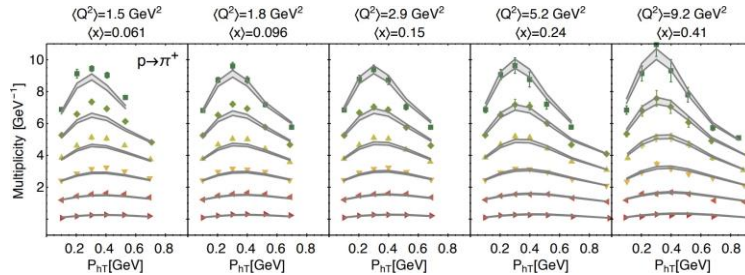
$P_T$  dependence results from:

- intrinsic  $k_\perp$  of the quarks
- $p_\perp$  generated in the quark fragmentation

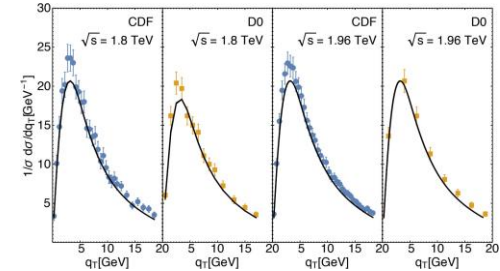


Global analyses of SIDIS, Drell-Yan and Z production data with TMD  $Q^2$  evolution

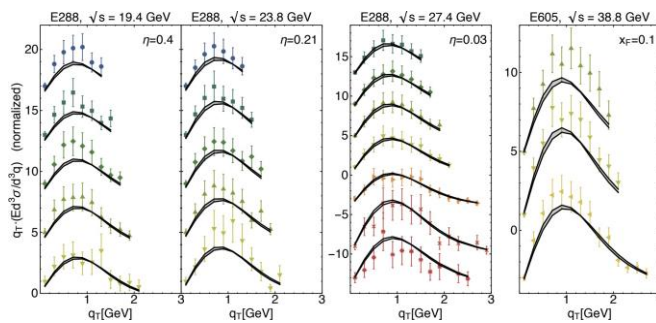
SIDIS multiplicity (example)



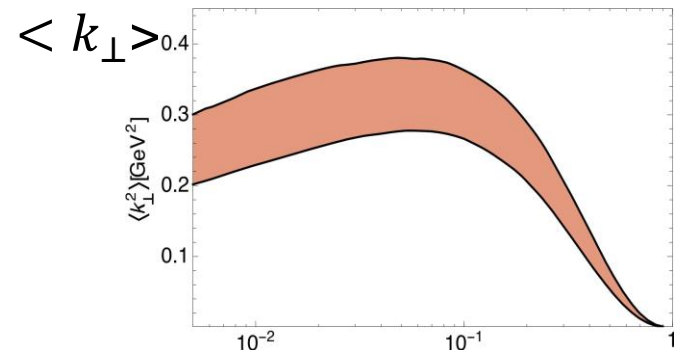
Z production



Drell-Yan cross section



Transverse momentum distribution



A. Bacchetta et al., JHEP06 (2017) 081 X

# TMDs- Collins and Sivers functions (SIDIS)

- Access via **SIDIS**, transversely polarized target

$$\mu p^\uparrow \rightarrow \mu h^{+/-} X$$

- Measure simultaneously several azimuthal asymmetries, out of which :

- Collins: Outgoing hadron direction & quark transverse spin
- Sivers: Nucleon spin & quark transverse momentum  $k_T$

at LO: **Collins**  
quark transverse spin distr.

$$A_{\text{Coll}} = \frac{\sum_q e_q^2 \cdot x \cdot h_1^q \otimes H_{1q}^\perp}{\sum_q e_q^2 \cdot x \cdot q \otimes D_{1q}^h}$$

Collins TMD fragmentation function, depends on spin, and hadron  $p_T$

**Sivers**

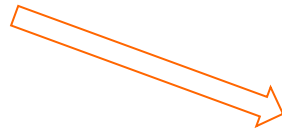
Unpolarized quark fragmentation function

$$A_{\text{Siv}} = \frac{\sum_q e_q^2 \cdot f_{1Tq}^\perp \otimes D_q^h}{\sum_q e_q^2 \cdot q \otimes D_q^h}$$



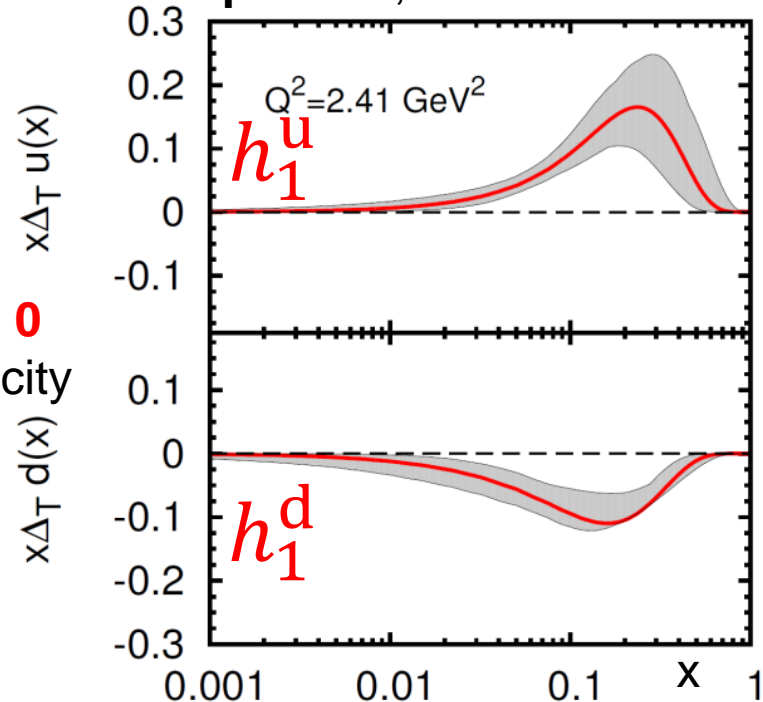
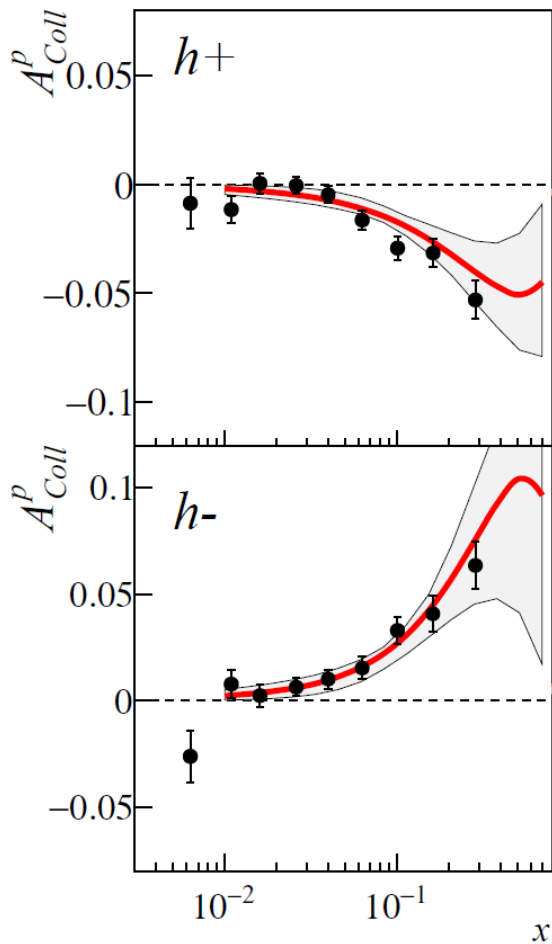
# TMDs, Collins asymmetry $\rightarrow$ Transversity $h_1$

- Large signal for proton target.  
(compatible with zero for deuteron target)
- Same signal strength seen by HERMES and COMPASS, although different  $Q^2$  (times 4)



Several combined analyses of polarized SIDIS data  
**HERMES p**, **COMPASS p and d**, and **BELLE FF**

$h_1^u > 0$  and  $h_1^d < 0$   
 Smaller than helicity

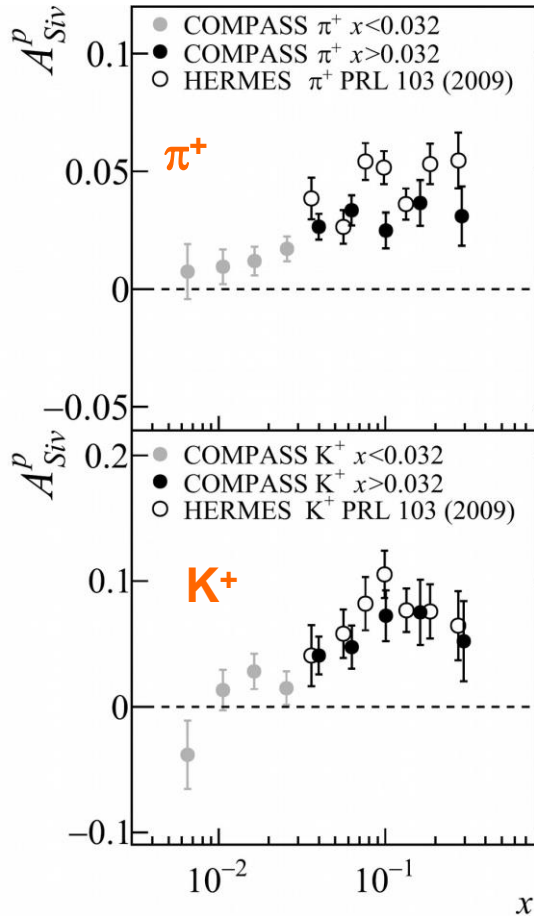


NB: asymmetries also measured for  $\pi$  and K

**HERMES PLB 693(2010)**  
**COMPASS PLB 744 (2015)**

# TMDs, Sivers asymmetry $\rightarrow$ Sivers function

Correlation between Nucleon spin & quark transverse momentum  $k_T$



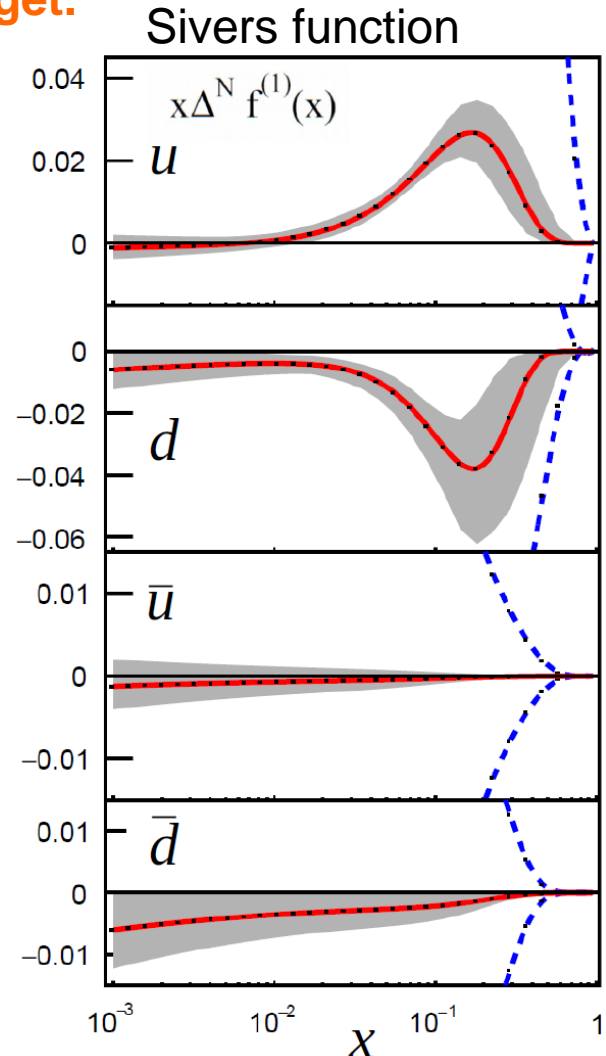
**Large signal with proton target.**

Was measured compatible with zero on deuteron

**Compared to COMPASS, HERMES (smaller  $Q^2$ ) has larger signal**



**HERMES PRL 103 (2009)**  
**COMPASS PLB 744 (2015)**



**Anselmino et al., JHEP04 (2017)046**

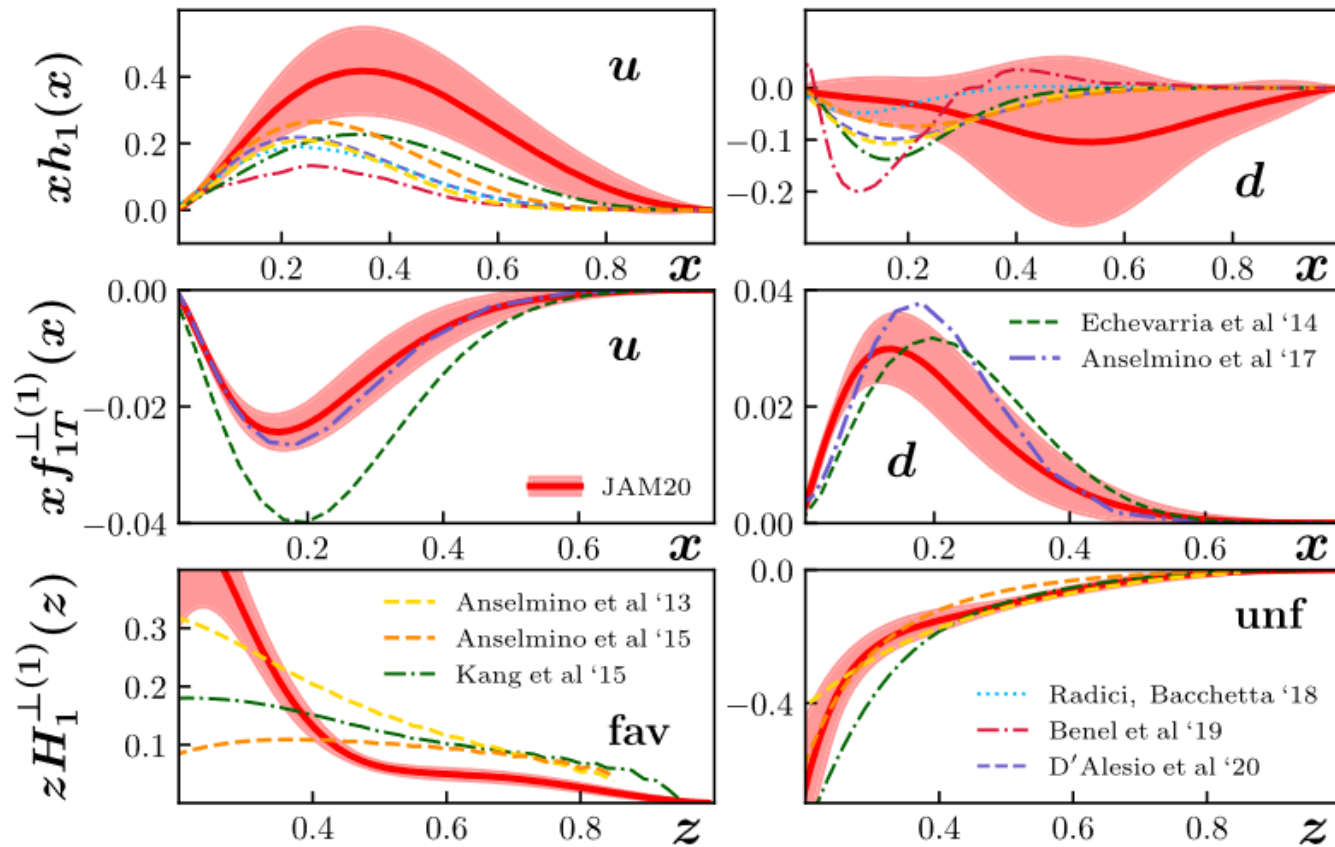
# TMDs Collins & Sivers. Recent global fits

Many global analyses of SIDIS, Drell-Yan, pp and e+e- .

Great progress: theoretical developments, large data sets, uncertainty studies

JAM20, Etchevaria et al., Anselmino et al., Radici, Bacchetta, Kang et al., D'Alesio et al., Boglione et., Bury et al. ..

e.g.:

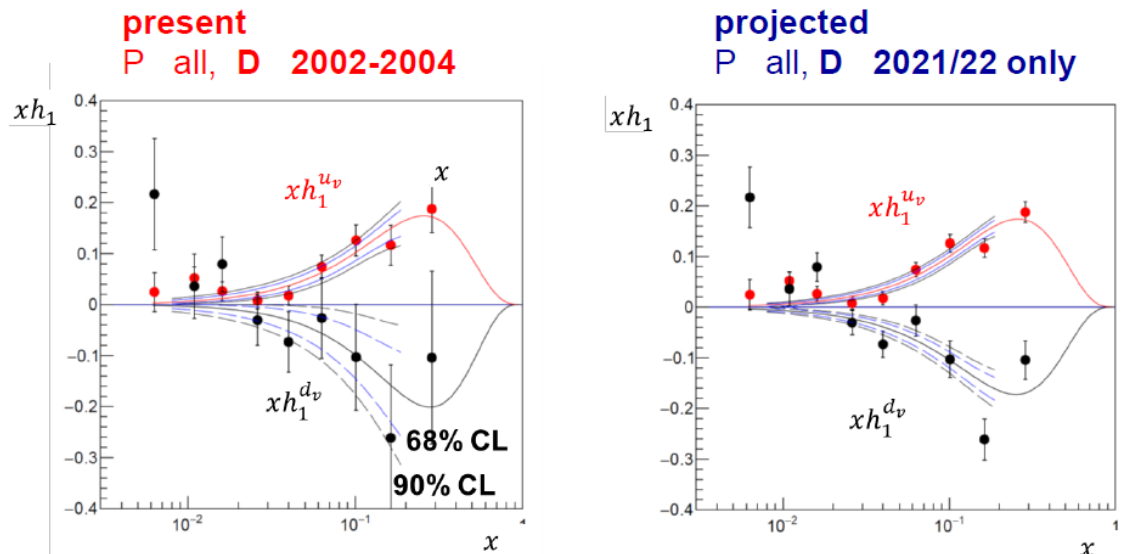


JAM20, PRD102, 054002 (2020)

# TMDs, Transversity $h_1$ / tensor charge

More data on deuteron needed

COMPASS projection for 2022 data, pol. 6LiD :



	$\delta_u = \int_{\Omega_x} dx h_1^{uv}(x)$	$\delta_d = \int_{\Omega_x} dx h_1^{dv}(x)$	$g_T = \delta_u - \delta_d$
Present	$0.201 \pm 0.032$	$-0.189 \pm 0.108$	$0.390 \pm 0.087$
Projected	$0.201 \pm 0.019$	$-0.189 \pm 0.040$	$0.390 \pm 0.044$

With 2022 data, expect improvement on uncertainties by factors of :  $\sim 2$  (u),  $\sim 3$  (d)

# TMDs, new approach: weighted asymmetries

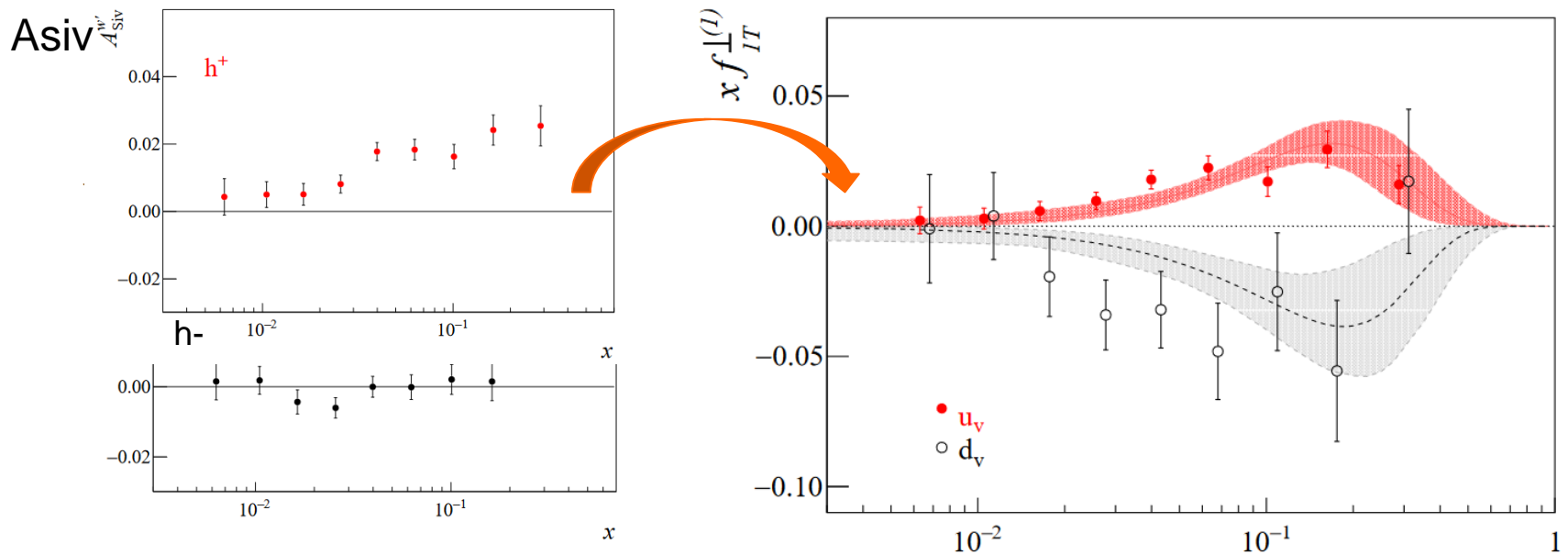
SIDIS, target transverse spin

$$A_{Siv}^{(p_T^h/zM)}(x, z) = 2 \frac{\sum_q e_q^2 f_{1T}^{\perp(1)q}(x) \cdot D_1^q(z)}{\sum_q e_q^2 f_1^q(x) \cdot D_1^q(z)},$$

Sivers asymmetry, with weight  $p_T/zM$   
No more convolution of TMDs and FFs  
but a product of integrals.

$$f_{1T}^{\perp(1)}(x, Q^2) = \int d^2k_T \frac{k_T^2}{2M^2} f_{1T}(x, k_T, Q^2).$$

→ extract first moment of Sivers  
without assumption on  $k_T$  dependence



Point by point extraction using  $h^+$  and  $h^-$  asym (NH3 target)<sup>x</sup>

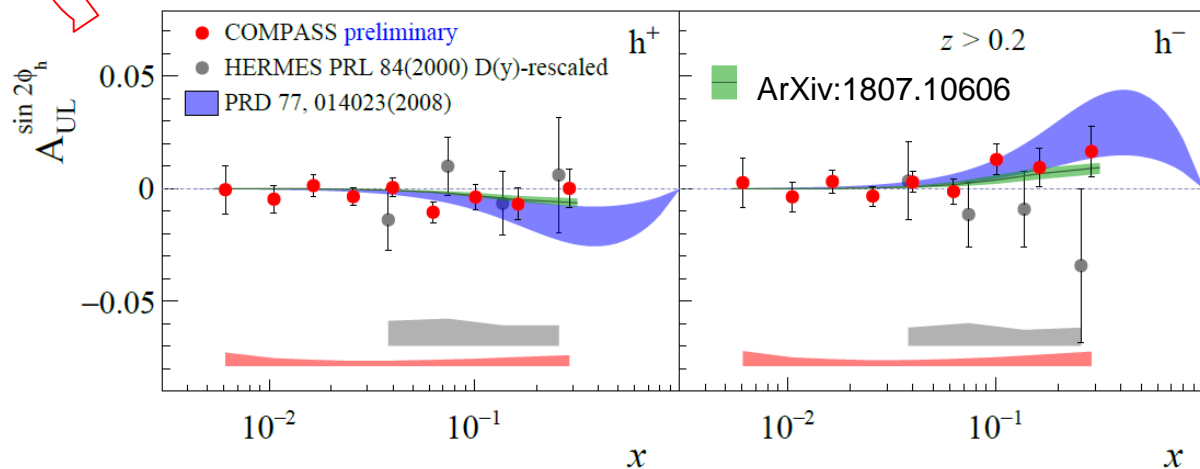
# TMDs, Target spi-dnependent azimuthal asymmetries

## Leading twist asymmetries

LO LSA/TSA	twist-2: PDF $\otimes$ FF	
$A_{UL}^{\sin(2\phi_h)}$	$h_{1L}^{\perp q} \otimes H_{1q}^{\perp h}$	
$A_{LL}$	$g_{1L}^q \otimes D_{1q}^h$	<i>g1</i>
$A_{UT}^{\sin(\phi_h - \phi_S)}$	$f_{1T}^{\perp q} \otimes D_{1q}^h$	<i>Sivers</i>
$A_{UT}^{\sin(\phi_h + \phi_S - \pi)}$	$h_1^q \otimes H_{1q}^{\perp h}$	<i>Collins</i>
$A_{UT}^{\sin(3\phi_h - \phi_S)}$	$h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$	<i>Pretzelosity: (deviation of spin density from spherical shape)</i>
$A_{LT}^{\cos(\phi_h - \phi_S)}$	$g_{1T}^q \otimes D_{1q}^h$	

Results on TMDs are characterised by an unprecedented precision, covering a wider kinematic range and many observables.

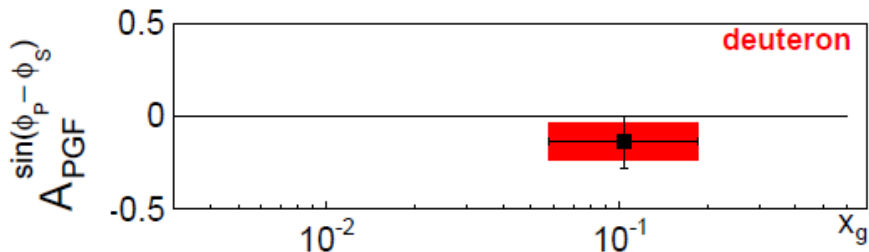
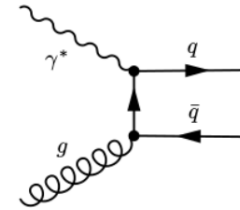
## Example $A_{UL}(x)$



# TMDs, Sivers gluon

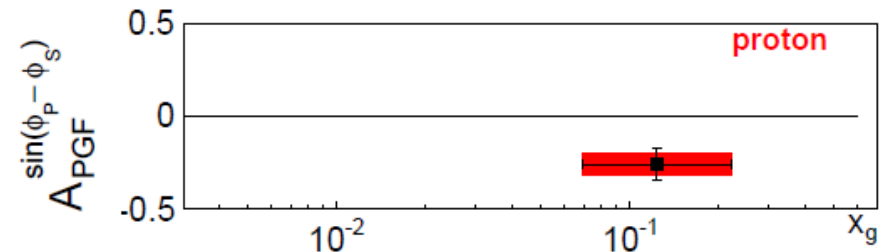
Sivers asymmetry:  
**correlation between nucleon transverse spin  
 & parton transverse momentum.**

Measured in SIDIS with transversely polarized target,  
 (already done for quarks), now for **gluons** from  
 azimuthal asymmetry for **PGF process**



$$A_{PGF}^{Siv,d} = -0.14 \pm 0.15(\text{stat.}) \pm 0.10(\text{syst.})$$

$$\langle x_g \rangle = 0.13$$



$$A_{PGF}^{Siv,p} = -0.26 \pm 0.09(\text{stat.}) \pm 0.06(\text{syst.})$$

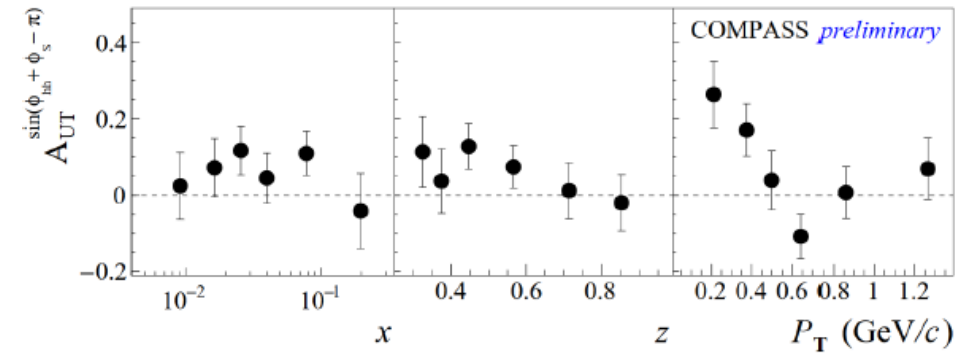
$$\langle x_g \rangle = 0.15$$

**COMPASS Phys. Lett. B 772, 854 (2017).**

# TMDs, $\rho^0$

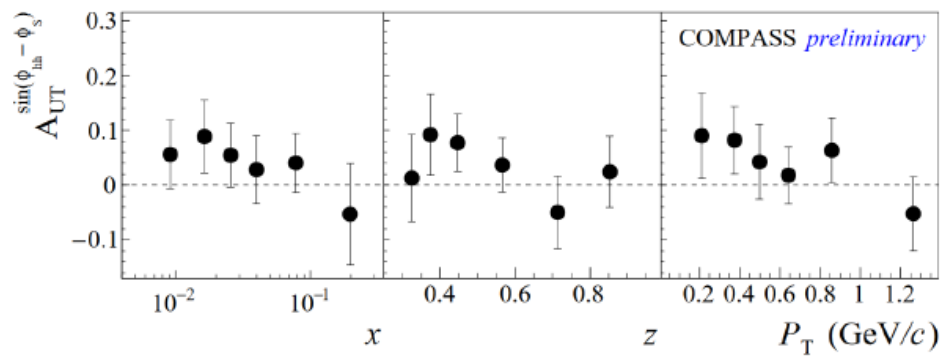
## $\rho^0$ COMPASS first Collins and Sivers measurement

A. Moretti SPIN21



### $\rho^0$ Collins

positive asymmetry  
opposite to  $\pi^+$ , as expected from models  
large at small  $p_T$



### $\rho^0$ Sivers

positive asymmetry,  
similarly to  $\pi^+$ , as expected



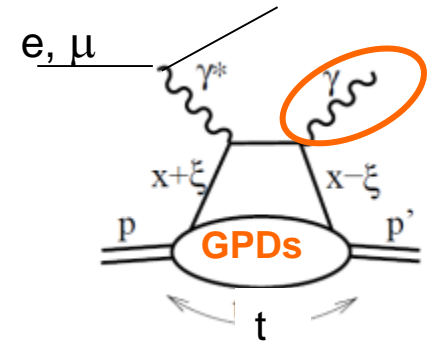
# GPDs - Generalized Parton Distributions

Physics goals:

- 3D mapping of nucleon
- access to Orbital Angular Momentum

160 GeV  $\mu$  beam

$\mu p \rightarrow \mu' p \gamma$



Determine 4 GPDs : **H, E,  $\tilde{H}$ ,  $\tilde{E}$**  (Re and Im parts)  
via 'exclusive' processes: DVCS ( $\gamma$ ) and DVMP ( $\rho, \omega, \phi$ )

DVCS interferes with Bethe-Heitler process

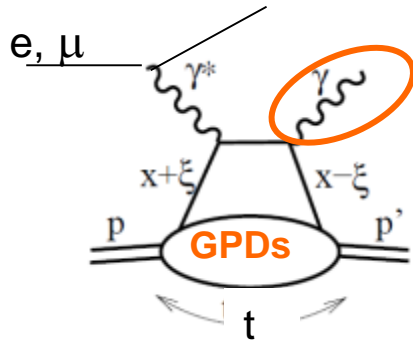
→ Can use interference terms or pure DVCS production  
with appropriate combinations of beam sign and polarization.

**Way to it:**

- Collect very large sample of data, for various observables and several kinematic variables
- Global analyses to extract 4x2 Compton Form Factors **CFFs**
- Deconvolutions to finally access **GPDs**.

# DVCS- t-slope of Cross-section (COMPASS)

$\mu^{+/-} p \rightarrow \mu p \gamma$



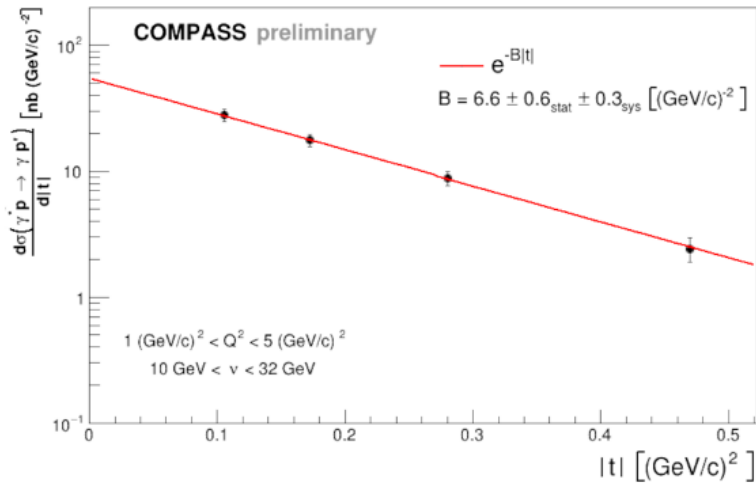
Measurement of proton transverse size vs  $x_B$

$$\sigma^{\text{DVCS}}/dt \sim \exp^{-B|t|}$$

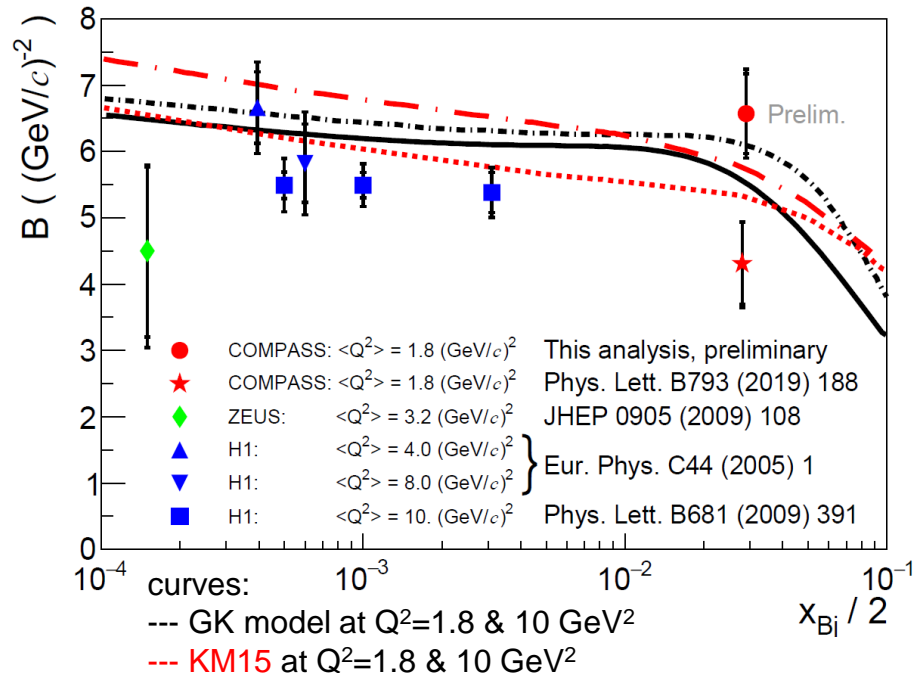
$$B(x_B) = \frac{1}{2} \langle r_{\perp}^2(x_B) \rangle$$

Combining data from  $\mu^+$  and  $\mu^-$  beams  
measure t-slope of DVCS cross section  
→ x dependence of transverse size of the nucleon

New preliminary COMPASS result:



2016 data :prelim. result  
3 x more stat. expected from 2017 data

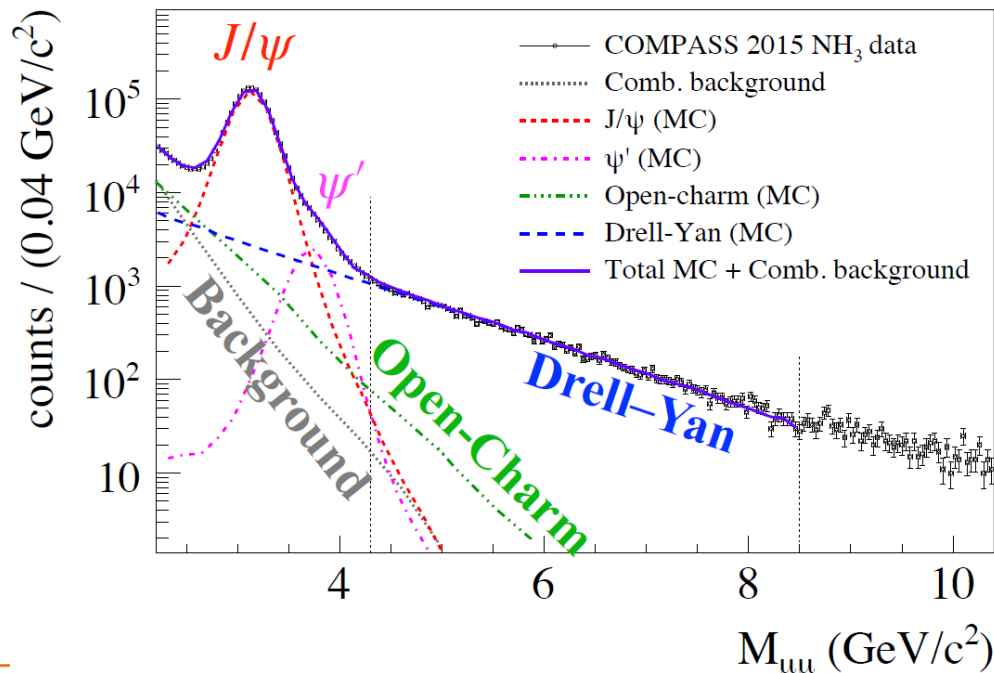
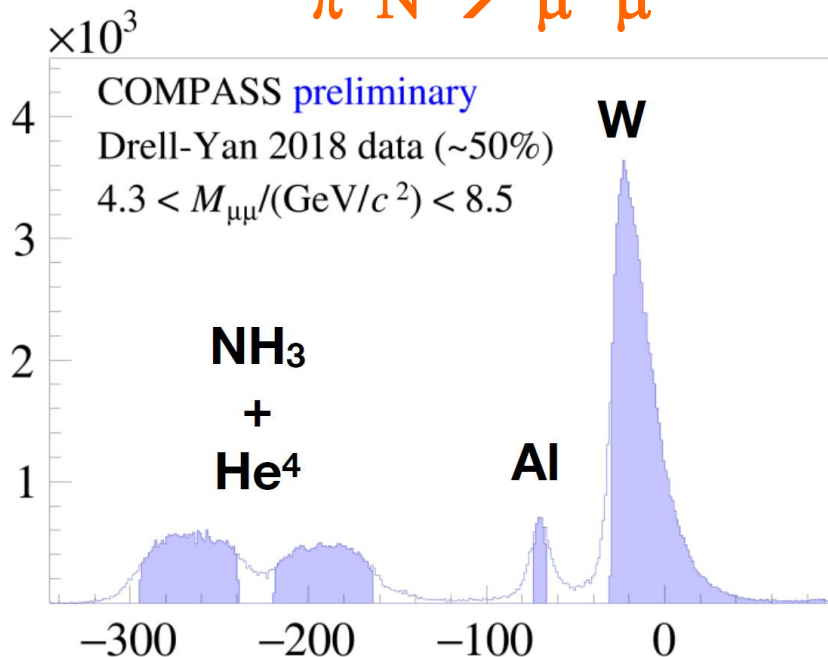


See SPIN 2021, J.Giarra talk

# Drell-Yan and $J/\psi$ from $\pi$ induced dimuon production



190 GeV  $\pi$  beam



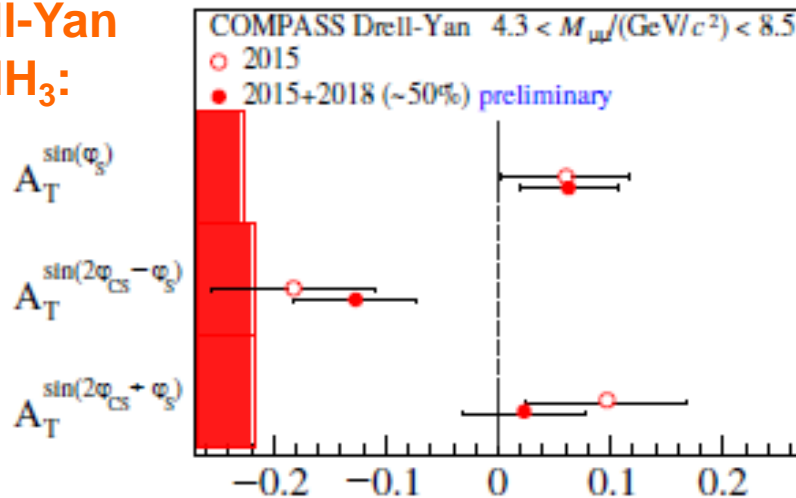
**Drell-Yan** : - polarized  $\text{NH}_3$  target  $\rightarrow$  results on TMDs (SIDIS/DY sign change)  
 - W target  $\rightarrow$  Lam-Tung relation study

**$J/\psi$  production** high statistics data:

- $J/\psi$  TSA and cross-section analysis in progress
- study production mechanism, two processes:
  - q-qbar annihilation  $\rightarrow$  quark TMDs
  - g g fusion  $\rightarrow$  gluon TMDs
- search for  $J/\psi$  pairs

# TMDs in polarized Drell-Yan

$\pi$  induced Drell-Yan on polarized  $\text{NH}_3$ :



$\pi N \rightarrow \mu^+ \mu^-$

Sivers  $\sim 1\sigma$  above zero

Transversity  $\sim 2\sigma$  below zero

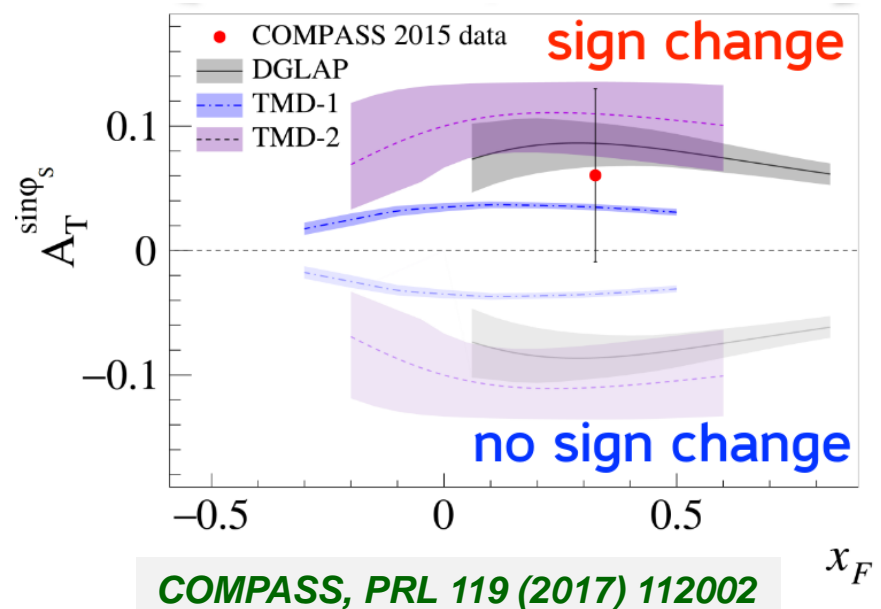
Pretzelosity  $\sim 1\sigma$  above zero

**Sivers function:**

- Non-vanishing orbital angular momentum
- Process dependence expected :

**Sign change between SIDIS and Drell-Yan**

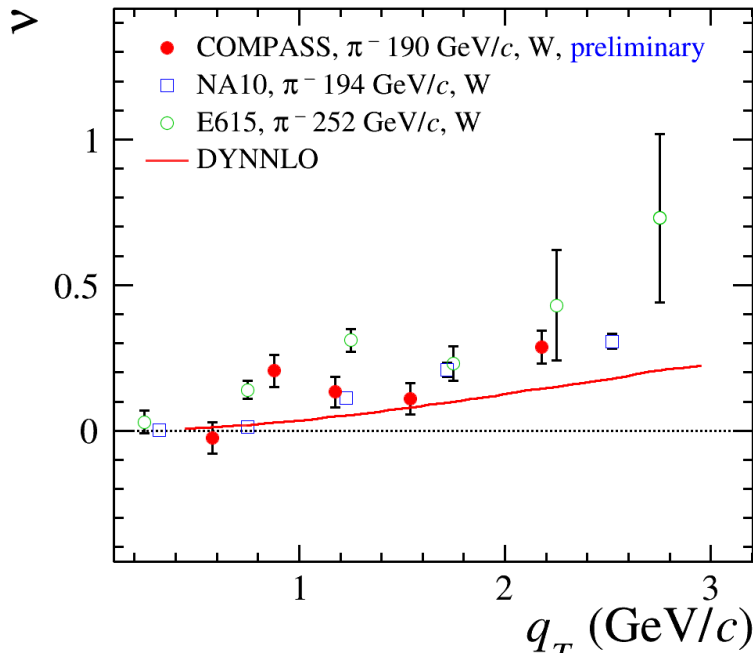
both measured in COMPASS at similar hard scale



# Preliminary results on Lam-Tung relation

$\pi$  induced Drell-Yan, W target.  $\pi W \rightarrow \mu^+ \mu^-$

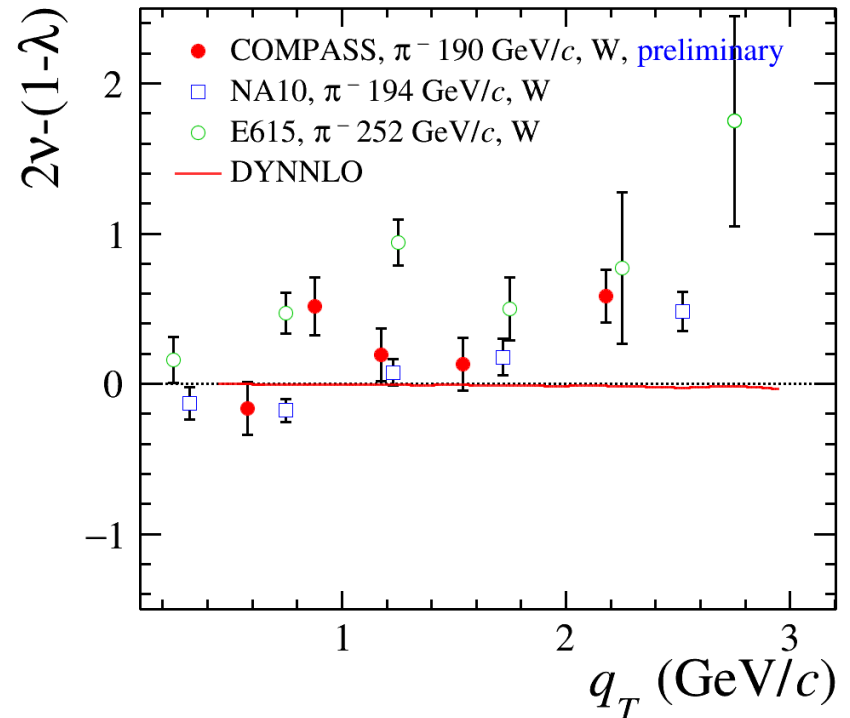
$$\frac{d\sigma}{d\Omega} \propto \frac{3}{4\pi} \frac{1}{\lambda + 3} \left[ 1 + \lambda \cos^2 \theta_{CS} + \mu \sin 2\theta_{CS} \cos \varphi_{CS} + \frac{\nu}{2} \sin^2 \theta_{CS} \cos 2\varphi_{CS} \right] \text{ at LO}$$



Data deviate from pQCD calculation  
 $\rightarrow$  Presence of non-zero TMD Boer-Mulders contribution

Lam-Tung violation quantity  $2\nu - (1-\lambda)$

Non zero  $\cos 2\varphi$  dependence



- Possible violation of Lam-Tung relation
- $\cos 2\varphi$  dependence
- Results compatible with previous data

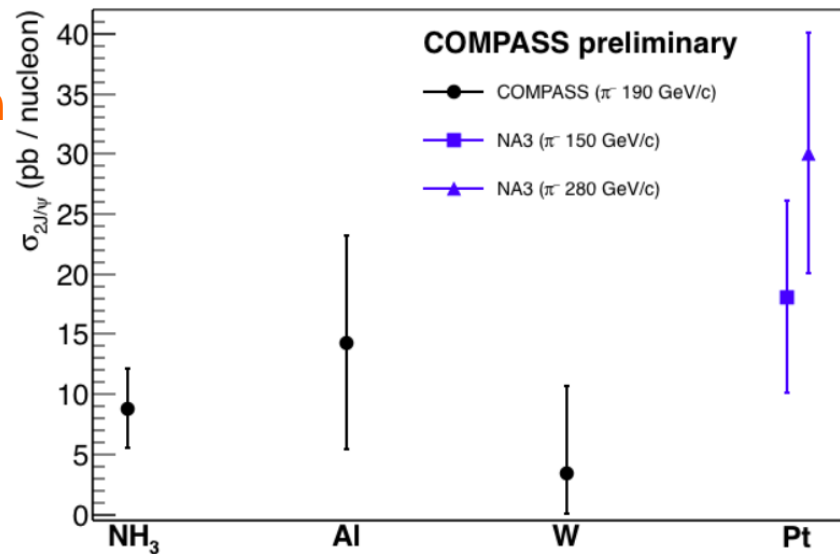
# J/ψ pair production in π –N collisions

## Search for J/ψ pairs

Goals:

- investigate possible intrinsic charm
- search for  $T_{4c}$  states

**2-J/ψ cross-section estimation for NH<sub>3</sub>, Al and W targets:**  
(25, 4 and 21 events)



See Qat 2021, A. Gridin talk

**Result consistent with single parton scattering (SPS) mechanism:**

$$q \bar{q} \rightarrow 2 J/\psi$$
$$g g \rightarrow 2 J/\psi$$

**No sign of intrinsic charm**  $d u c \bar{c} c \bar{c}$

# Summary –

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## Gluon and quark contribution to nucleon spin

**Gluon**  $\Delta G/G=0.1$  at  $x=0.1$  (photon gluon fusion process) agrees with RHIC  $\int \Delta G \sim 0.2$   
Unknown contribution at low  $x$

**Quarks** :  $\frac{1}{2} \Delta \Sigma \sim 0.15$  from global QCD fit of  $g_1$  world data; agrees with Lattice QCD  
**Flavor decomposition** from SIDIS, down to  $x \sim 0.004$ .

## Quark Fragmentation functions:

High  $z$  data for  $K^-/K^+$  and  $p\bar{b}/p$  hadron multiplicity ratios

- Data disagree with current NLO QCD calculations **at high  $z$  and low  $\nu$**
- Unexpected rise of ratio  $M(K^+) / M(K^-)$  with missing mass, suggesting to take into account the available phase space for hadronisation in formalism.

## Transverse Momentum Dependent parton distributions

Extensive and precise results on all azimuthal asymmetries  
Global analyses

**GPDs** via DVCS: b slope prelim. result

Many data coming and promising framework for global analyses.

**Polarized Drell-Yan** First ever measurement  $\rightarrow$  Sivers asymmetry (sign change vs SIDIS)  
Angular distributions: TMDs, Lam-Tung relation...