

Spin Density Matrix Elements in Exclusive Muoproduction of ρ^0 and ω Mesons at COMPASS



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on behalf of the COMPASS Collaboration

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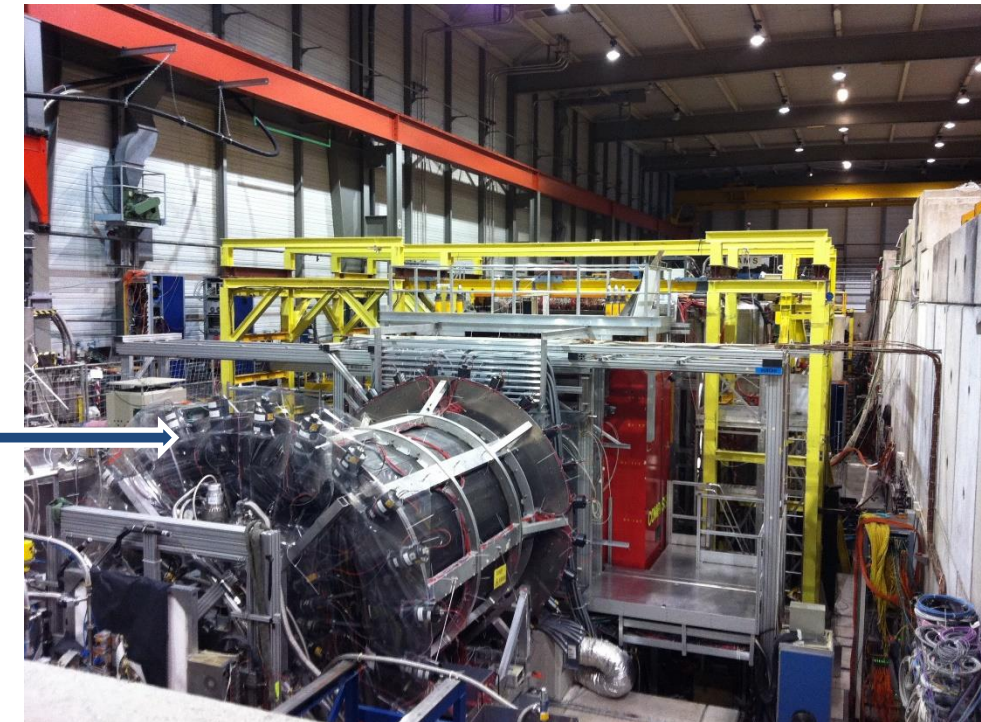
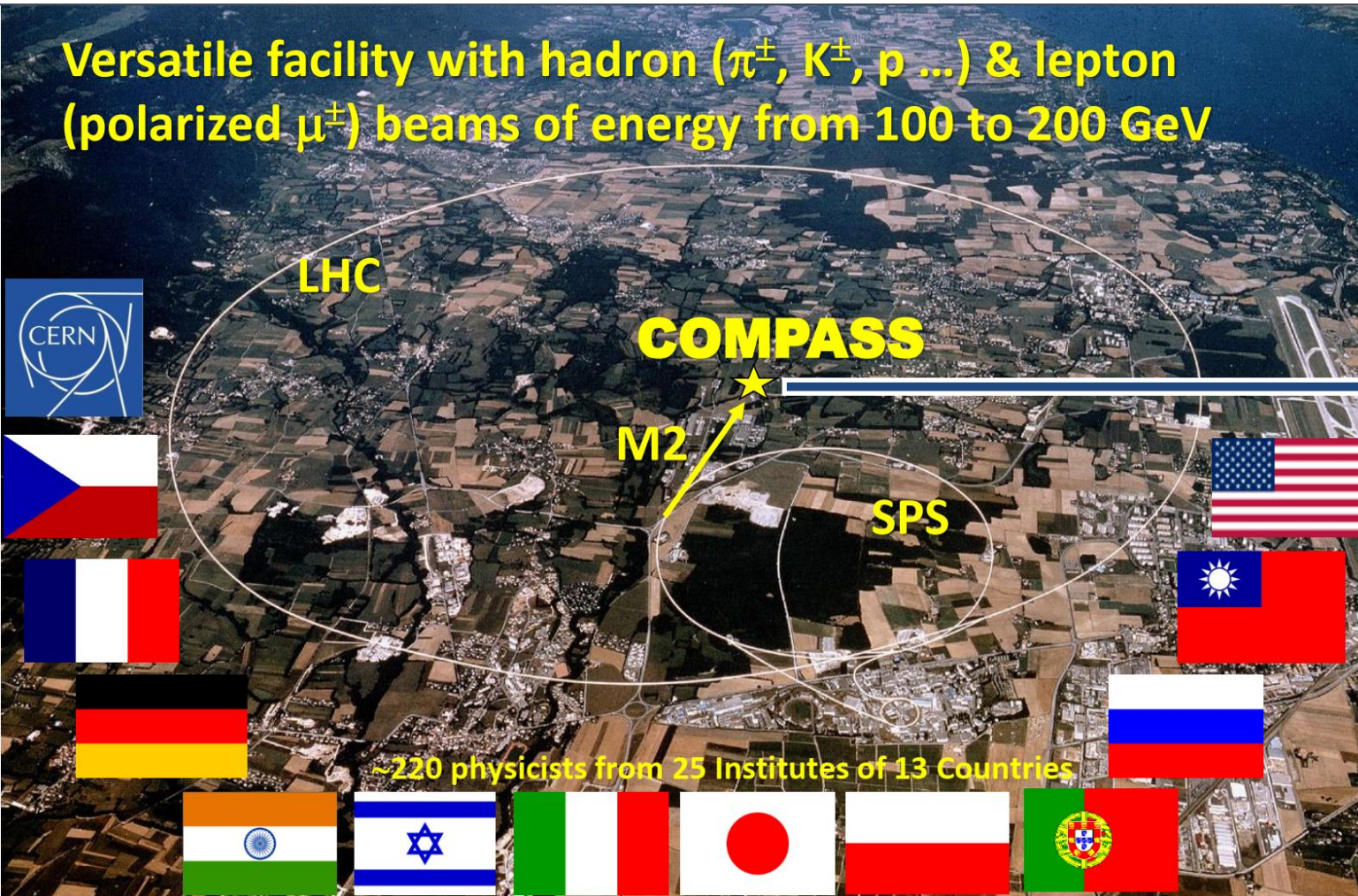
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COMPASS Experiment

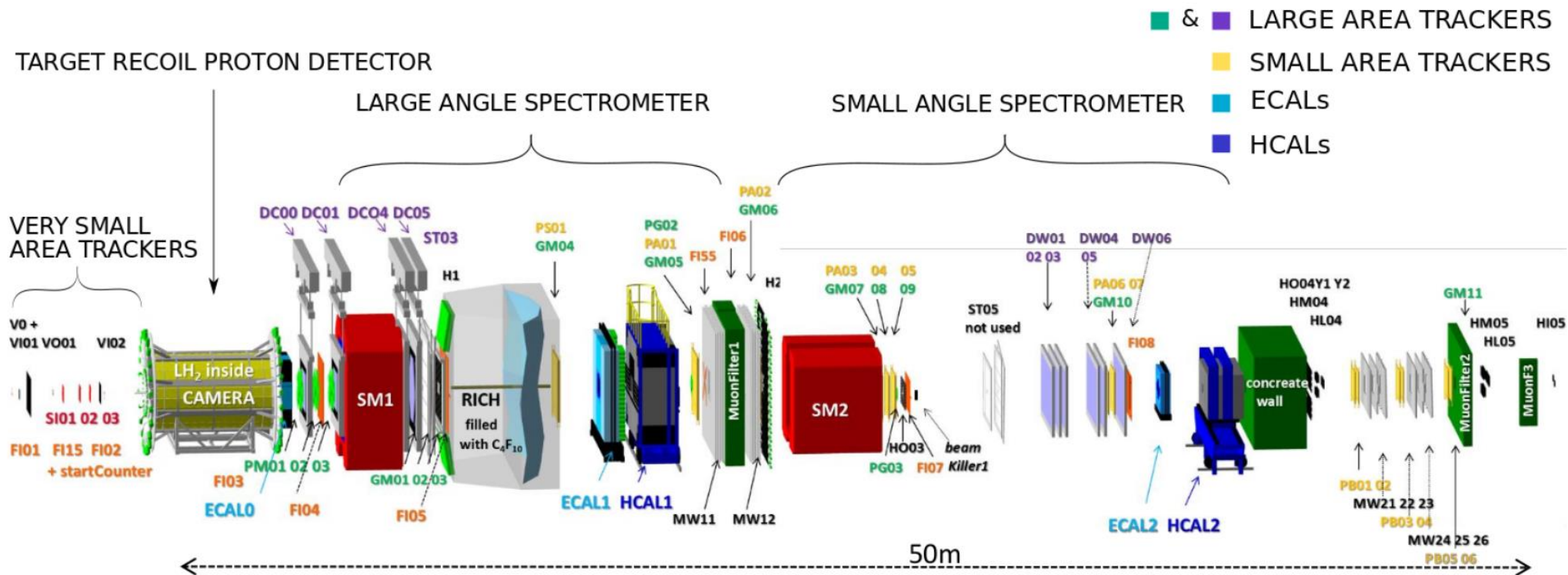
COmmon **M**uon **P**roton **A**pparatus for **S**tructure and **S**pectroscopy

Versatile facility with hadron (π^\pm , K^\pm , p ...) & lepton (polarized μ^\pm) beams of energy from 100 to 200 GeV



data taking 2002 – 2022 & longitudinally, transversely or unpolarized targets

COMPASS Experiment – setup and data



NIMA 577 (2007)
455–518
&
NIMA 779 (2015)
69

μ^+ , μ^- beams
- data separately
polarization $\sim \pm 80\%$
energy 160 GeV

Exclusive Muoproduction



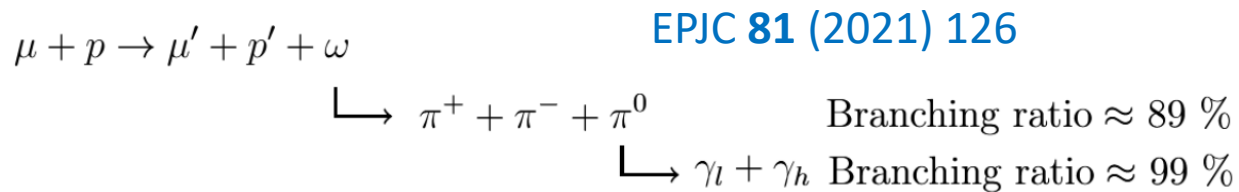
2.5m long LH_2 target

results in this talk: data from 2012 pilot run (4 weeks)

Hard Exclusive Meson Production (HEMP)

Selection

Common selection: $1 < Q^2 < 10 \text{ (GeV}/c)^2$, $W > 5 \text{ GeV}/c^2$, $0.01 < p_T^2 < 0.5 \text{ (GeV}/c)^2$, $0.1 < y < 0.9$
 Recoil proton detector not included in selection



$0.1 < M_{\gamma\gamma} < 0.17 \text{ GeV}$, $0.71 < M_{\pi^+\pi^-\pi^0} < 0.86 \text{ GeV}$

topology:

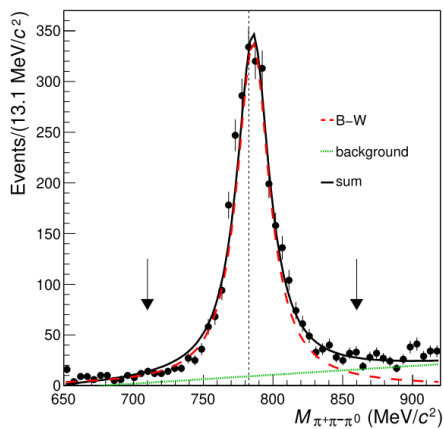
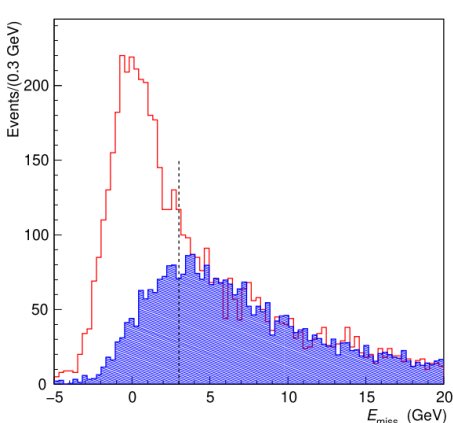
scattered muon + two hadrons with opposite charges

+ two neutral clusters in calorimeters

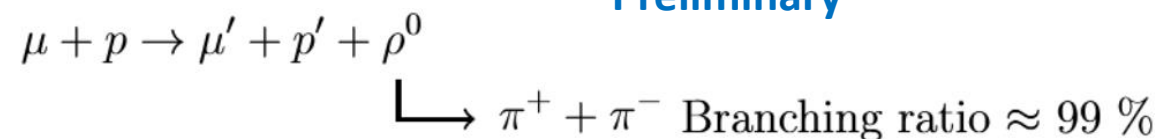
event yield: 3060 events

$|E_{\text{miss}}| < 3 \text{ GeV}$

$$E_{\text{miss}} = \frac{M_X^2 - M^2}{2M}$$



Preliminary



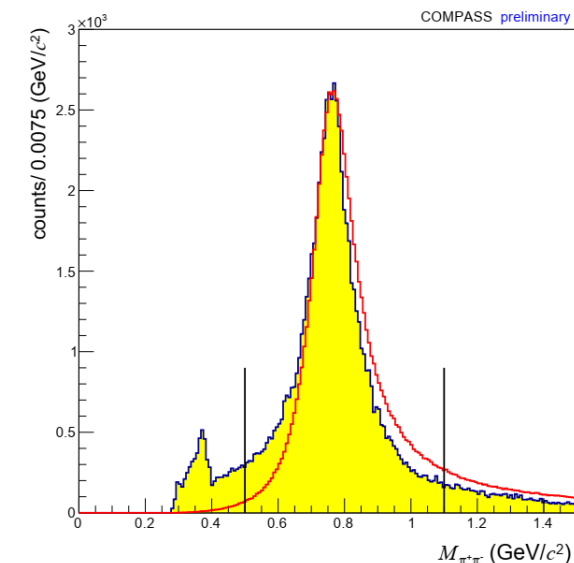
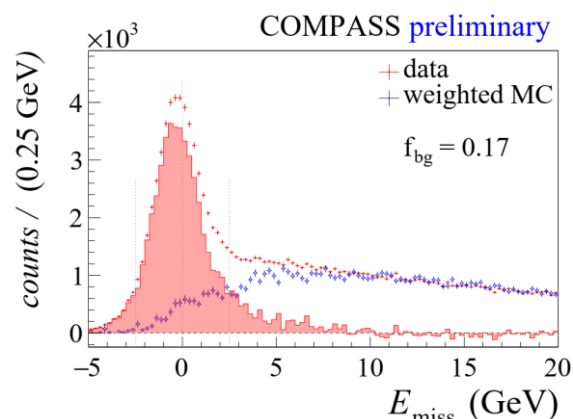
$0.5 < M_{\pi^+\pi^-} < 1.1 \text{ GeV}$

topology:

scattered muon + two hadrons with opposite charges

event yield: 52257 events

exclusivity: $|E_{\text{miss}}| < 2.5 \text{ GeV}$



Vector meson spin-density matrix

$$\rho_{\lambda_V \lambda'_V} = \frac{1}{2N} \sum_{\lambda_\gamma \lambda'_\gamma \lambda_N \lambda'_N} F_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N} \mathcal{Q}_{\lambda_\gamma \lambda'_\gamma}^{U+L} F_{\lambda'_V \lambda'_N \lambda'_\gamma \lambda_N}^*$$

photon spin density matrix ($\mu \rightarrow \mu' + \gamma^*$); calculable on QED

$$\mathcal{Q}_{\lambda_\gamma \lambda'_\gamma}^{U+L} = \mathcal{Q}_{\lambda_\gamma \lambda'_\gamma}^U + P_b \mathcal{Q}_{\lambda_\gamma \lambda'_\gamma}^L$$

- ❖ F helicity amplitudes describe transitions $\lambda_\gamma, \lambda_N \rightarrow \lambda_V, \lambda'_N$, depend on W, Q^2, p_T^2
- ❖ $\rho_{\lambda_V \lambda'_V}$ decomposes into 9 matrices $\rho_{\lambda_V \lambda'_V}^\alpha$ corresponding to different photon polarization states ($\alpha=0-3$ transverse, $\alpha=4$ longitudinal, $\alpha=5-8$ interference amplitudes)
- ❖ if not possible to separate long. and transv. photon contributions, SDMEs are defined:

$$r_{\lambda_V \lambda'_V}^{04} = (\rho_{\lambda_V \lambda'_V}^0 + \epsilon R \rho_{\lambda_V \lambda'_V}^4) (1 + \epsilon R)^{-1}, \quad r_{\lambda_V \lambda'_V}^\alpha = \begin{cases} \rho_{\lambda_V \lambda'_V}^\alpha (1 + \epsilon R)^{-1}, & \alpha = 1, 2, 3, \\ \sqrt{R} \rho_{\lambda_V \lambda'_V}^\alpha (1 + \epsilon R)^{-1}, & \alpha = 5, 6, 7, 8. \end{cases}$$

$R = d\sigma_L/d\sigma_T$ diff. longitudinal-to-transverse cross-section ratio of virtual photons and ϵ is the virtual-photon polarization parameter

↓
23 SDMEs

Vector Meson SDMEs and GPDs

- ❖ access to helicity amplitudes F allows:

- ❖ test of s-channel helicity conservation SCHC ($\lambda_\gamma = \lambda_V$)

- ❖ decomposition into Natural (N) and Unnatural (U) Parity Exchange (NPE/UPE)

in Regge framework: NPE $J^P = (0^+, 1^-, \dots)$ (pomeron, ρ , ω , $a_2 \dots$); UPE $J^P = (0^-, 1^+, \dots)$ (π , $a_1 \dots$)

- ❖ quantify the role of transitions with helicity flip

$$F_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N} = T_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N} + U_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N}$$

- ❖ determination of the longitudinal-to-transverse cross-section ratio

- ❖ test of GPD models

like SCHC-violating transitions $\gamma_T \rightarrow V_L$ to test sensitivity to GPDs with helicity-flip of „active“ quark (transversity GPDs)

- ❖ GPDs in HEMP: 4 chiral-even

$H^q(x, \xi, t)$	$E^q(x, \xi, t)$	For Vector Meson
$\tilde{H}^q(x, \xi, t)$	$\tilde{E}^q(x, \xi, t)$	For Pseudo-Scalar Meson

4 chiral-odd or transversity (not in DVCS)

$H_T^q(x, \xi, t)$	$E_T^q(x, \xi, t)$	$\bar{E}_T^q = 2 \tilde{H}_T^q + E_T^q$
$\tilde{H}_T^q(x, \xi, t)$	$\tilde{E}_T^q(x, \xi, t)$	

- universality of GPDs, quark flavor filter,

additional non-perturbative term from meson wave function, insights into reaction mechanism

Experimental access to SDMEs

- ❖ through angular distribution

K. Schilling and G. Wolf,
Nucl. Phys. B **61**, 381(1973)

$$\mathcal{W}^{U+L}(\Phi, \phi, \cos \Theta) = \mathcal{W}^U(\Phi, \phi, \cos \Theta) + P_b \mathcal{W}^L(\Phi, \phi, \cos \Theta)$$

- ❖ decomposition into 23 terms with different angular dependences

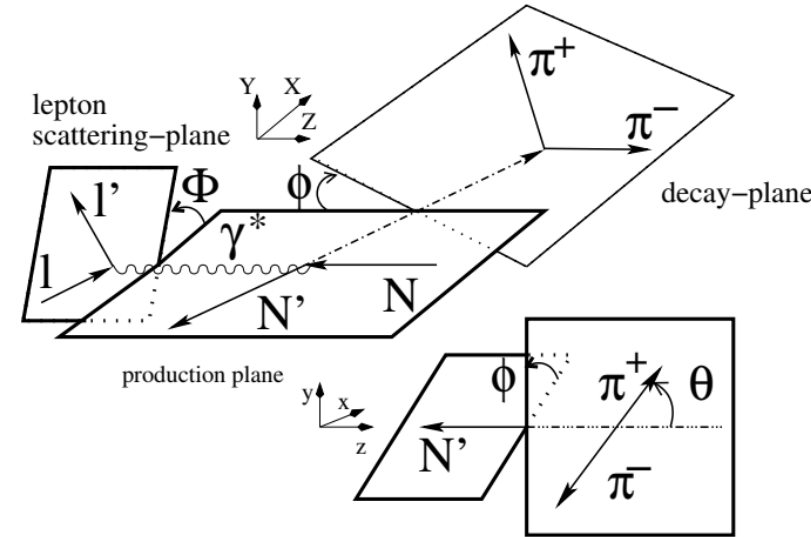
- ❖ 15 unpolarized - \mathcal{W}^U and 8 polarized - \mathcal{W}^L

- ❖ extraction of SDMEs:

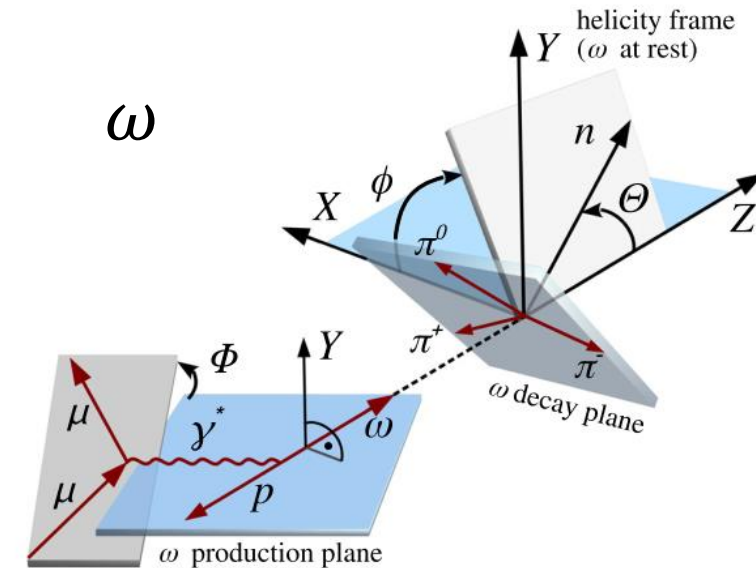
- ❖ Unbinned Maximum Likelihood fit to experimental function $\mathcal{W}(\mathcal{R}, \Phi, \phi, \cos \Theta)$, \mathcal{R} is set of 23 SDMEs
 - ❖ total acceptance
 - ❖ fraction of background f_{bg}
 - ❖ angular distribution of background

$$\mathcal{W}^{U+L}(\mathcal{B}, \Phi, \phi, \cos \Theta)$$

ρ_0



ω



Results

$1 < Q^2 < 10$ (GeV/c)²
 $5 < W < 17$ GeV/c²
 $0.01 < p_T^2 < 0.5$
 (GeV/c)²

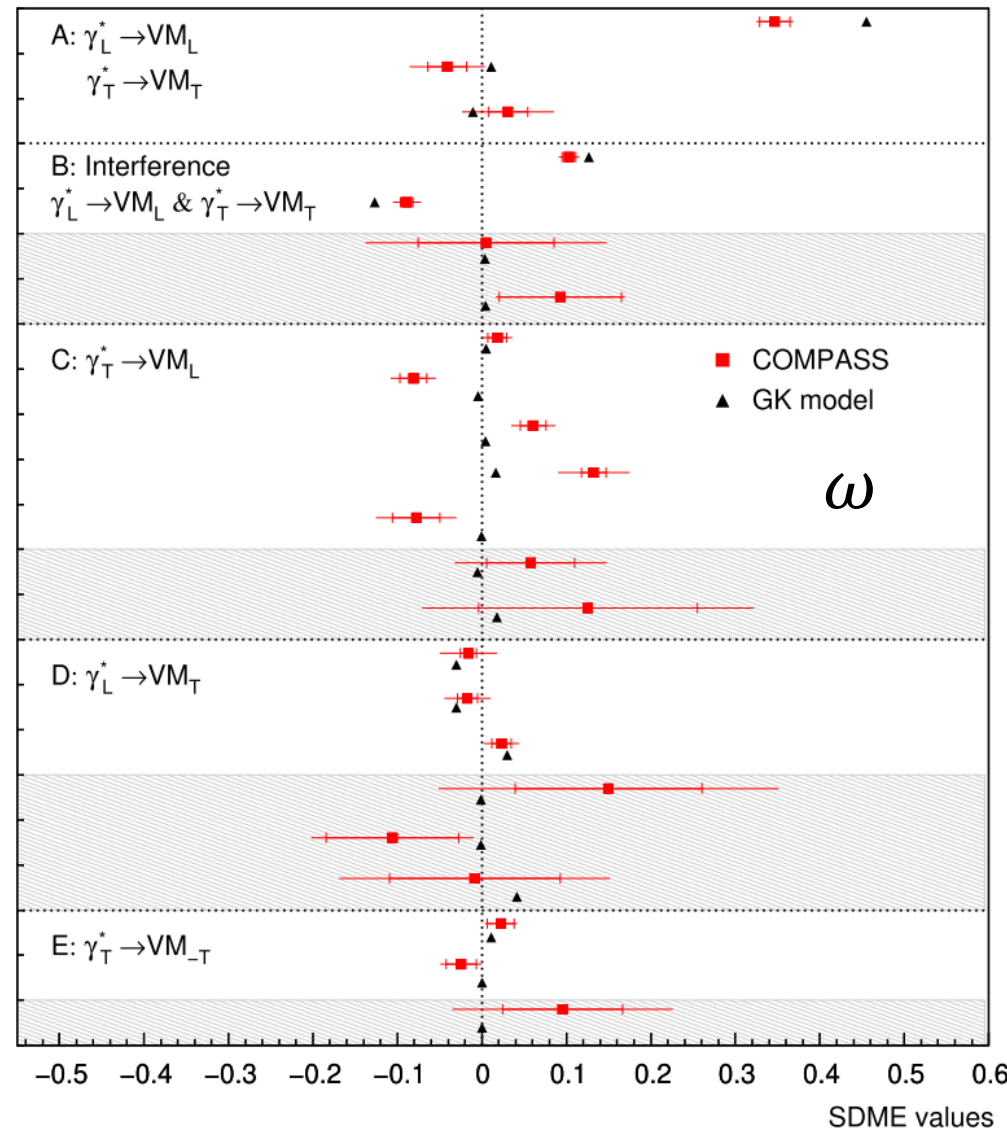
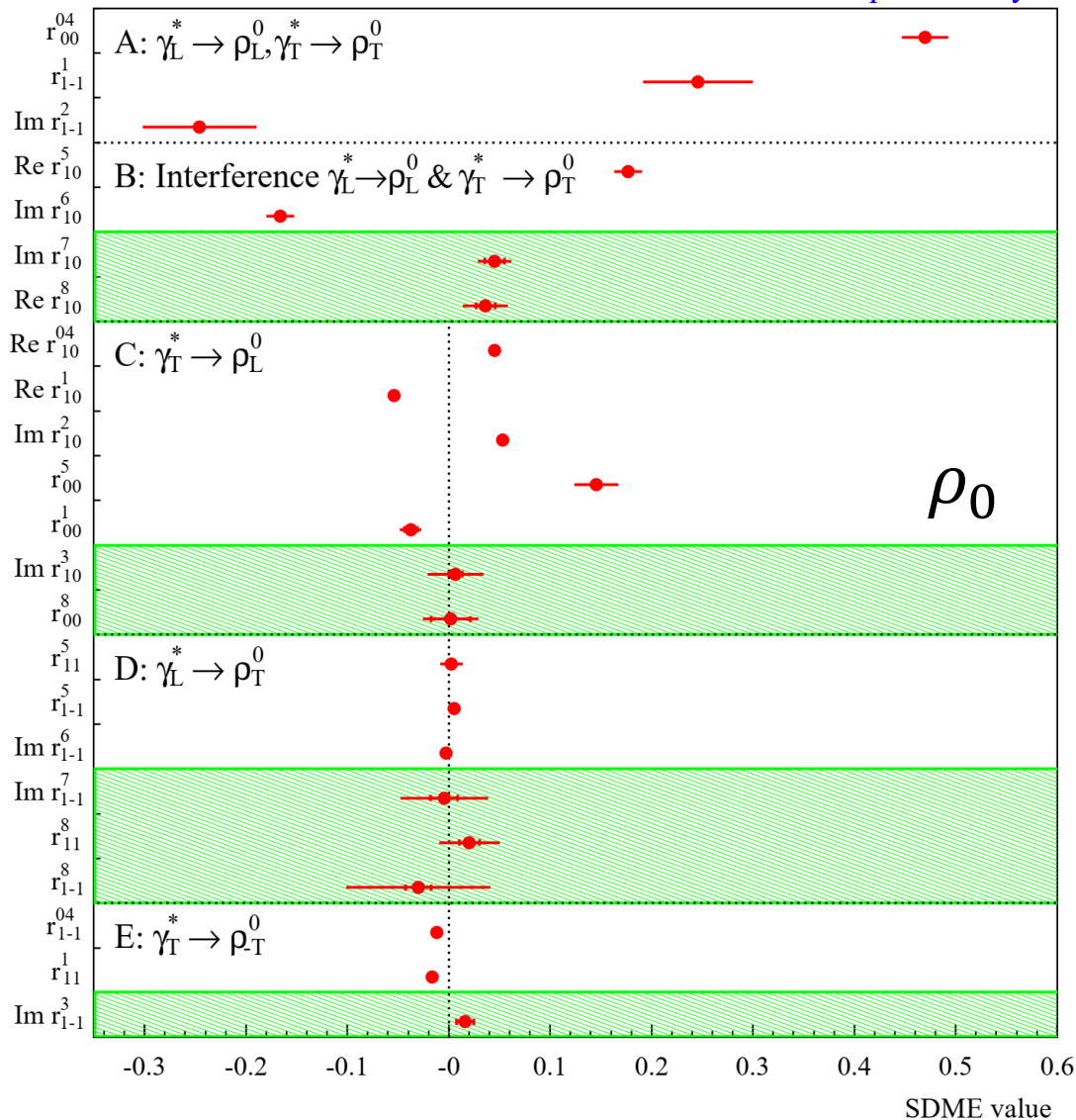
A, B, C, D, E classes corresponding to different helicity transitions

shaded areas show SDMEs related to beam polarization

GK model:
 EPJA 50 (2014) 146 parameters
 constrained mostly by HERMES results for ρ^0 and ω

COMPASS preliminary

EPJC 81 (2021) 126



Results - SCHC

❖ SCHC implies:

$$r_{1-1}^1 + \text{Im } r_{1-1}^2 = 0 \quad \text{OK}$$

$$\text{Re } r_{10}^5 + \text{Im } r_{10}^6 = 0 \quad \text{OK}$$

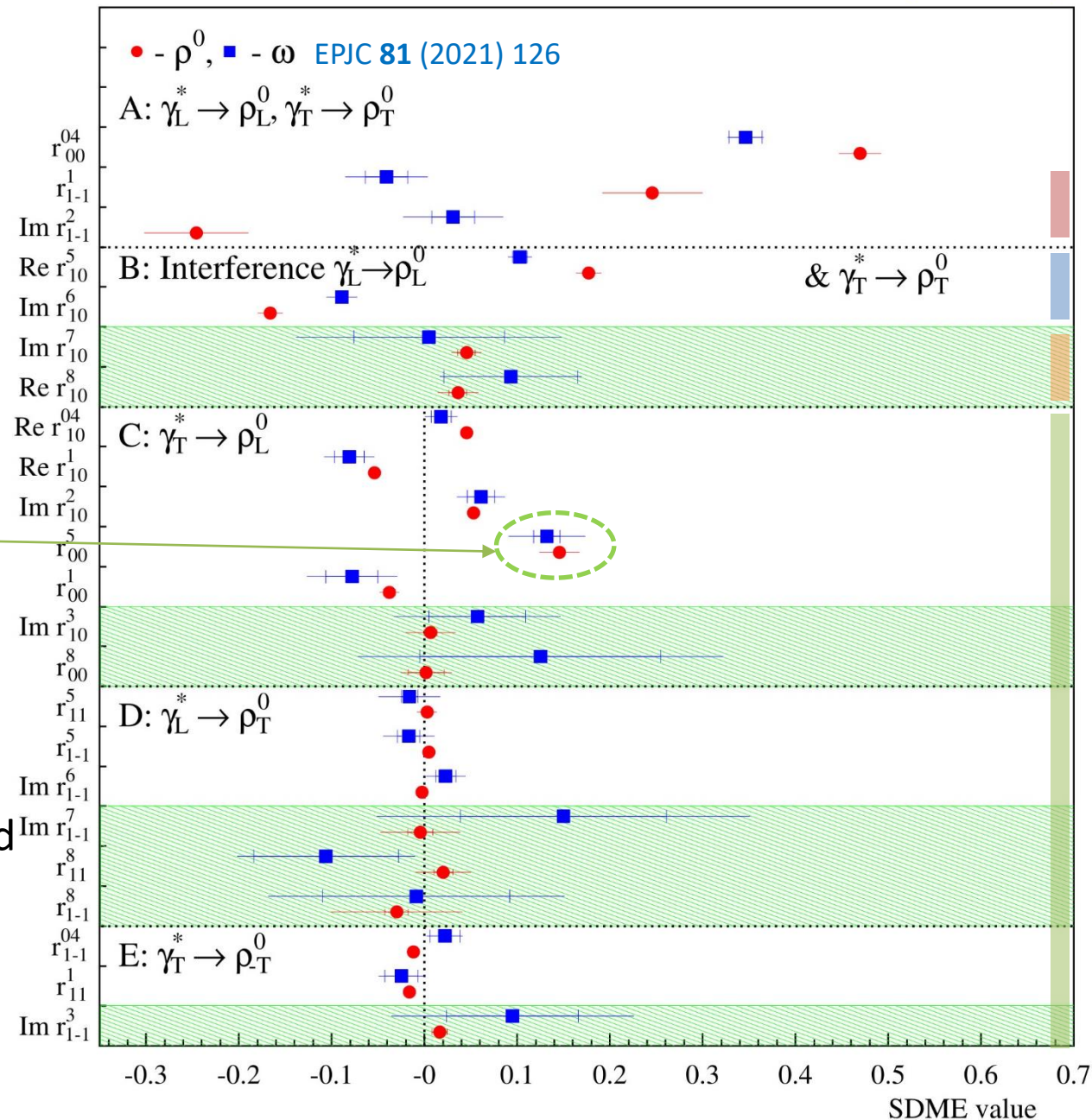
$$\text{Im } r_{10}^7 + \text{Re } r_{10}^8 = 0 \quad \text{OK}$$

all elements of classes C, D, E should be 0

- ❖ not observed in class C – transition $\gamma_T^* \rightarrow \rho_L^0$
- ❖ possible GPD interpretation **Goloskokov and Kroll, EPJC 74 (2014) 2725:**
- ❖ contribution of amplitudes depending on chiral-odd (“transversity”) GPDs $H_T, \bar{E}_T = 2\tilde{H}_T + E_T$

$$r_{00}^5 \sim \text{Re} \left[\langle \bar{E}_T \rangle_{LT}^* \langle H \rangle_{LL} + \frac{1}{2} \langle H_T \rangle_{LT}^* \langle E \rangle_{LL} \right]$$

- ❖ first term dominates, r_{00}^5 essentially probes \bar{E}_T



Results – Helicity-Flip NPE Amplitudes ρ^0

❖ described as $\tau_{ij} = \frac{|T_{ij}|}{\mathcal{N}}$

$$\tau_{01} \approx \sqrt{\epsilon} \frac{\sqrt{(r_{00}^5)^2 + (r_{00}^8)^2}}{\sqrt{2r_{00}^{04}}}$$

$$\gamma_T^* \rightarrow \rho_L^0$$

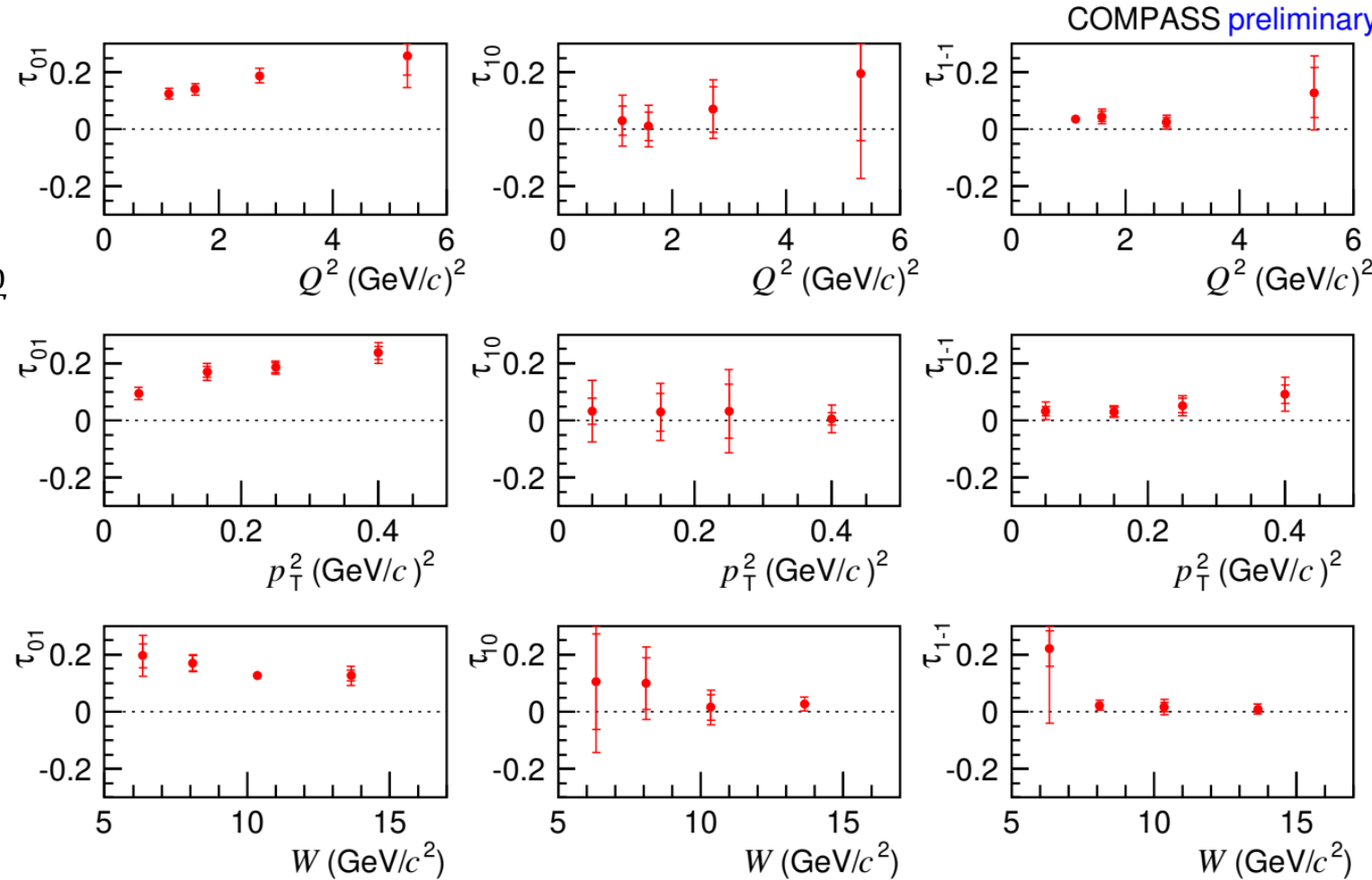
$$\tau_{10} = \frac{\sqrt{(r_{11}^5 + \text{Im}\{r_{1-1}^6\})^2 + (\text{Im}\{r_{1-1}^7\} - r_{11}^8)^2}}{\sqrt{2(r_{1-1}^1 - \text{Im}\{r_{1-1}^2\})}}$$

$$\gamma_L^* \rightarrow \rho_T^0$$

$$\tau_{1-1} = \frac{\sqrt{(r_{11}^1)^2 + (\text{Im}\{r_{1-1}^3\})^2}}{\sqrt{r_{1-1}^1 - \text{Im}\{r_{1-1}^2\}}}$$

$$\gamma_T^* \rightarrow \rho_{-T}^0$$

❖ only τ_{01} significantly differs from 0, consistent with SCHC violation in C, D, E



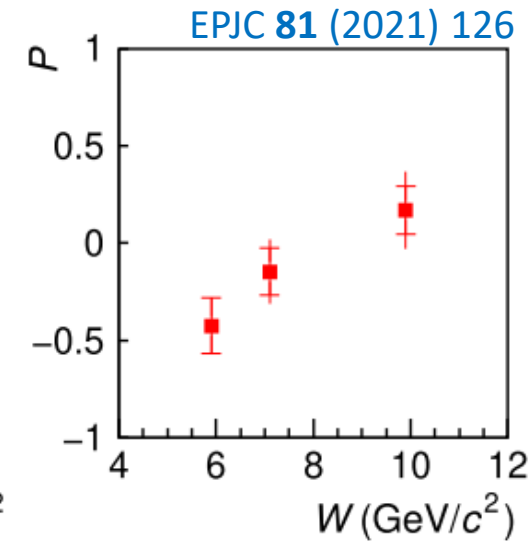
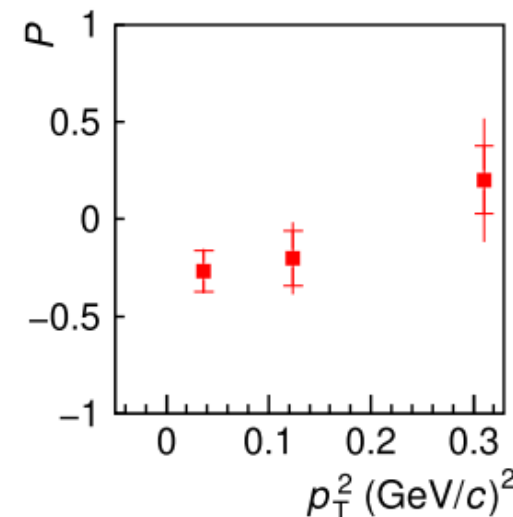
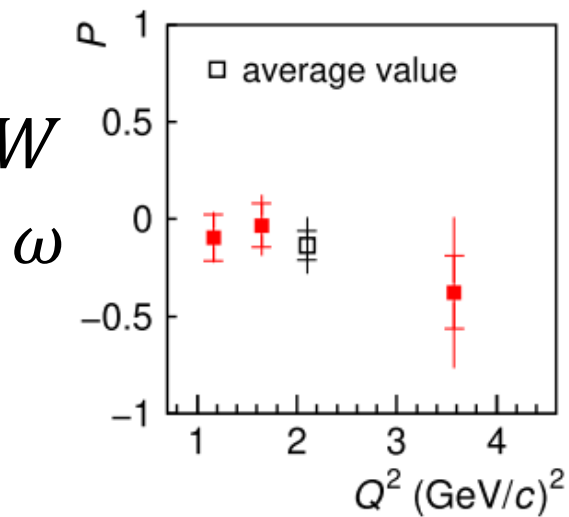
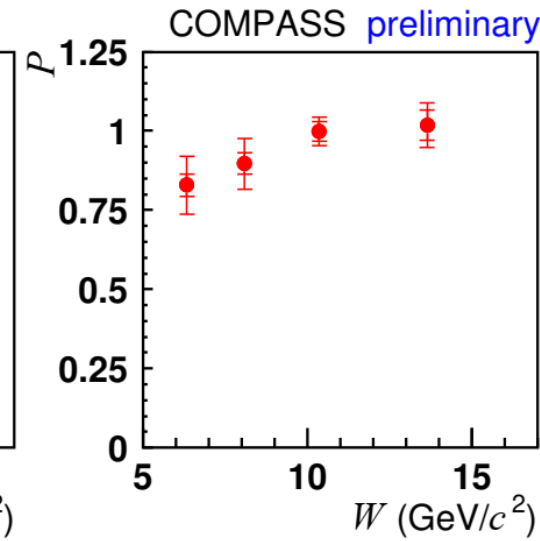
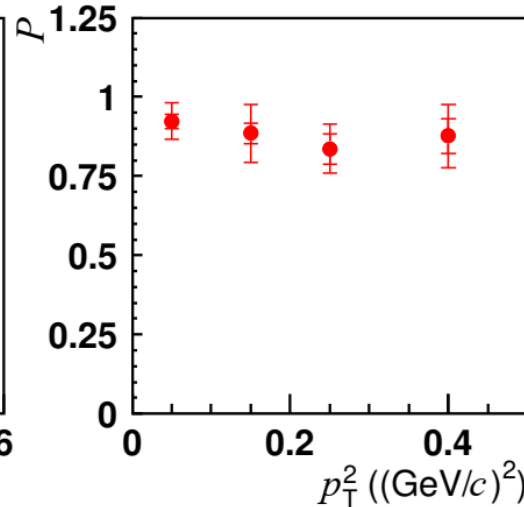
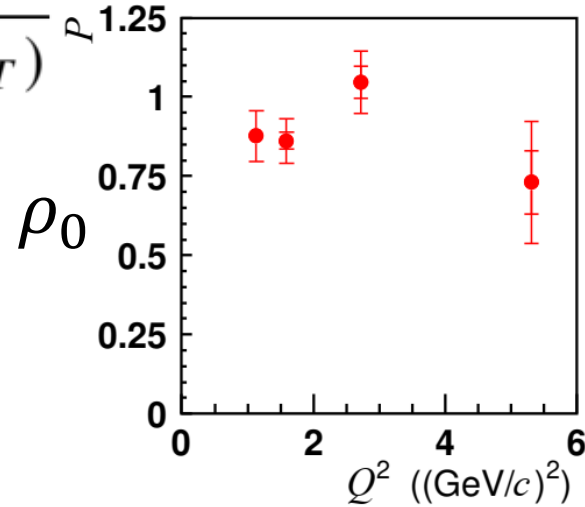
Results – NPE to UPE asymmetry

$$P = \frac{d\sigma_T^N(\gamma_T^* \rightarrow V_T) - d\sigma_T^U(\gamma_T^* \rightarrow V_T)}{d\sigma_T^N(\gamma_T^* \rightarrow V_T) + d\sigma_T^U(\gamma_T^* \rightarrow V_T)}$$

$$= \frac{2r_{1-1}^1}{1 - r_{00}^{04} - 2r_{1-1}^{04}}$$

❖ ρ_0 NPE dominance
NPE \rightarrow GPDs E, H

❖ ω NPE \approx UPE on average
UPE dominance at small W
and p_T^2
UPE \rightarrow GPDs \tilde{E}, \tilde{H}
+ pion pole (dominant)



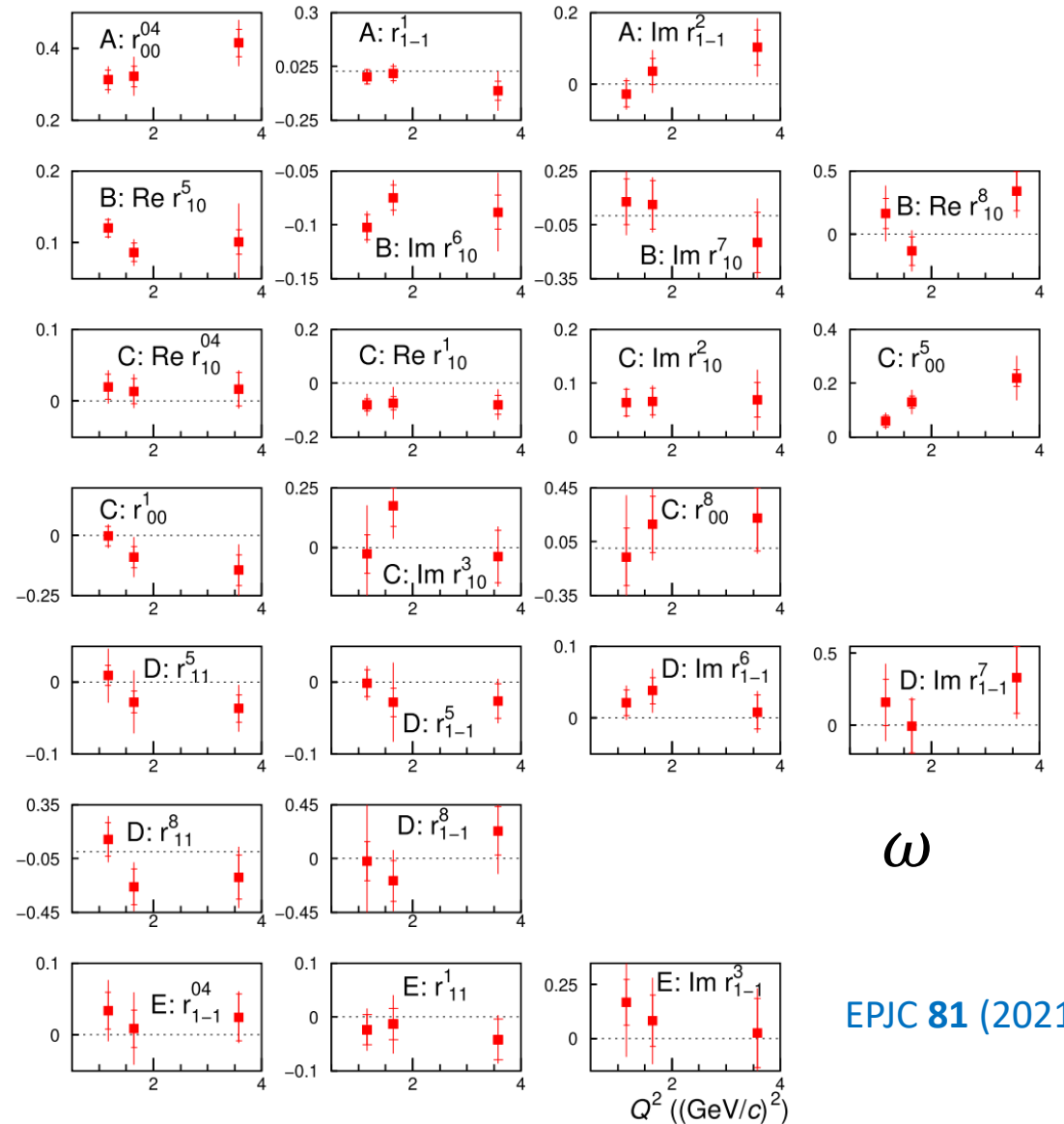
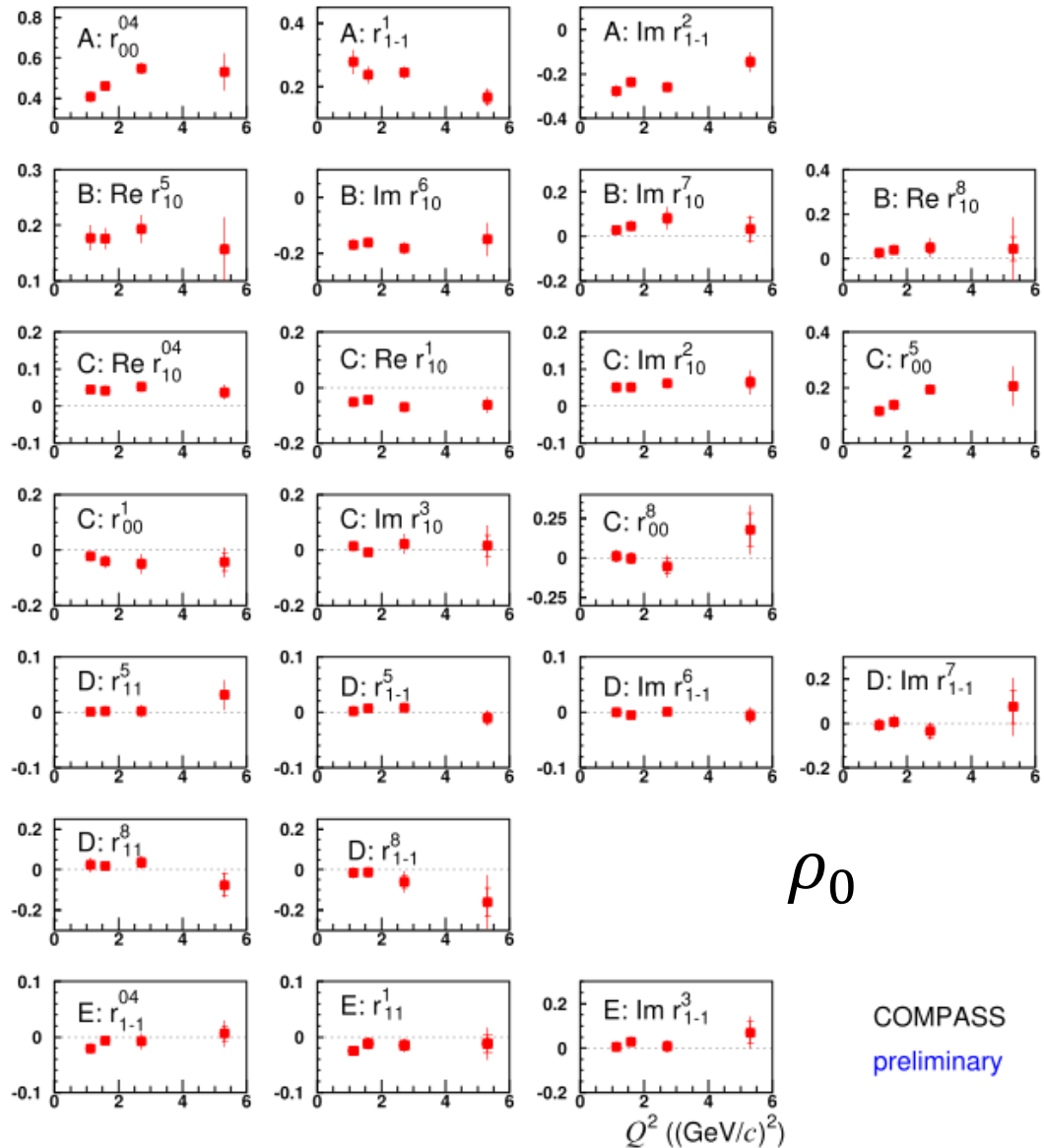
Summary and outlook

- ❖ measured 23 SDMEs in HEMP ρ^0 and ω muoproduction
 - ❖ for kinematic range: $1 < Q^2 < 10$ (GeV/c)², $5 < W < 17$ GeV/c², $0.01 < p_T^2 < 0.5$ (GeV/c)²
 - ❖ with dependences on W, Q^2, p_T^2
- ❖ hypothesis of SCHC is violated for transitions $\gamma_T^* \rightarrow \rho_L^0$
 - ❖ in GPD framework described by contribution of chiral-odd "transversity" GPD
 - ❖ corresponding τ_{01} helicity-flip NPE amplitudes in ρ^0 observed with dependences on W, Q^2, p_T^2
 - ❖ observed also at other experiments HERMES, CLAS, H1 and ZEUS
- ❖ NPE dominant in $\rho^0 \Rightarrow$ role of GPDs E and H
- ❖ NPE \approx UPE in $\omega \Rightarrow$ role of GPDs $E, H, \tilde{E}, \tilde{H}$ and pion pole
- ❖ on-going analysis of 2016-17 data (~ 9 times larger statistics)

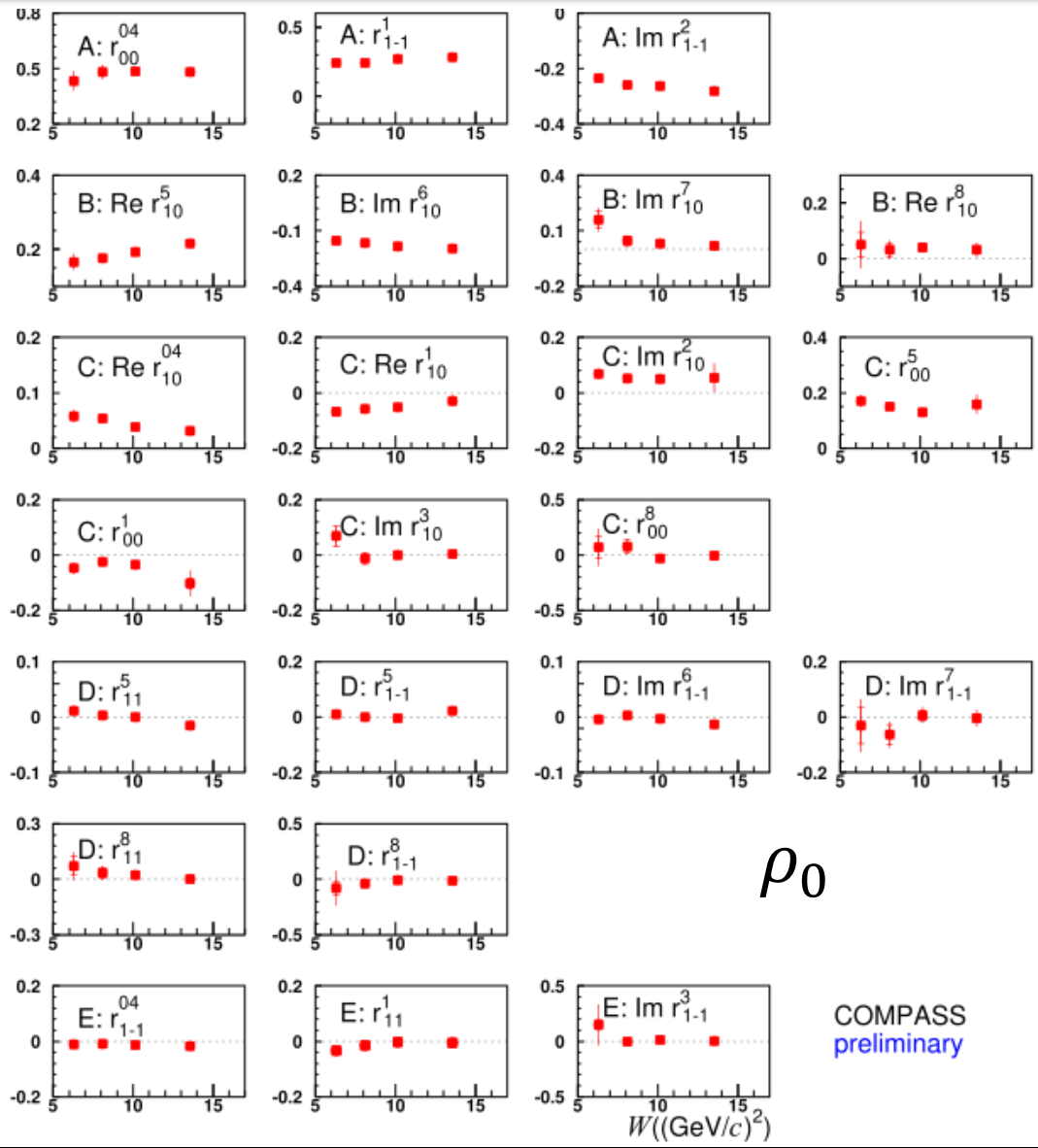
Thank you for your attention



SDMEs dependences

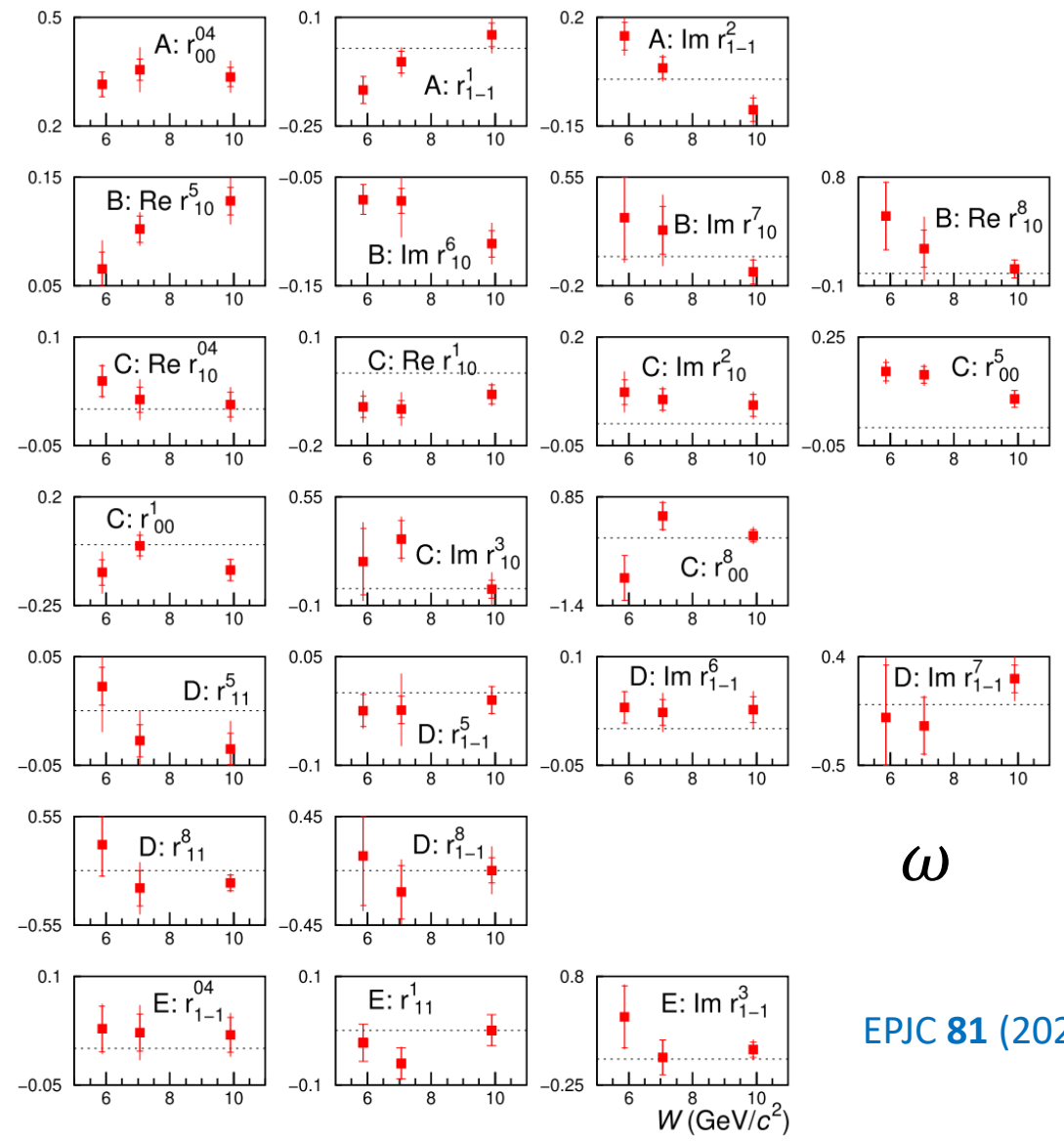


SDMEs dependences



ρ_0

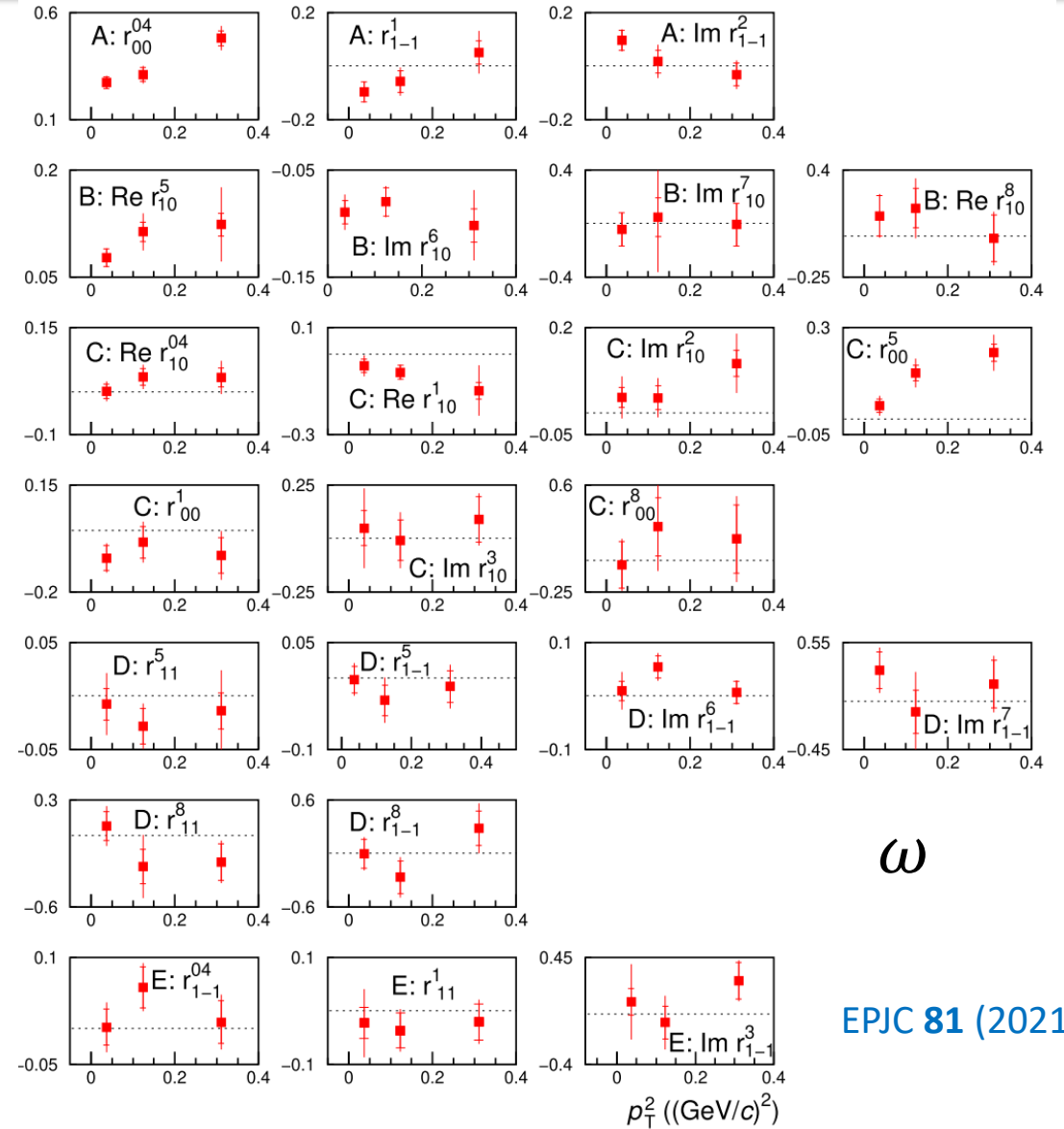
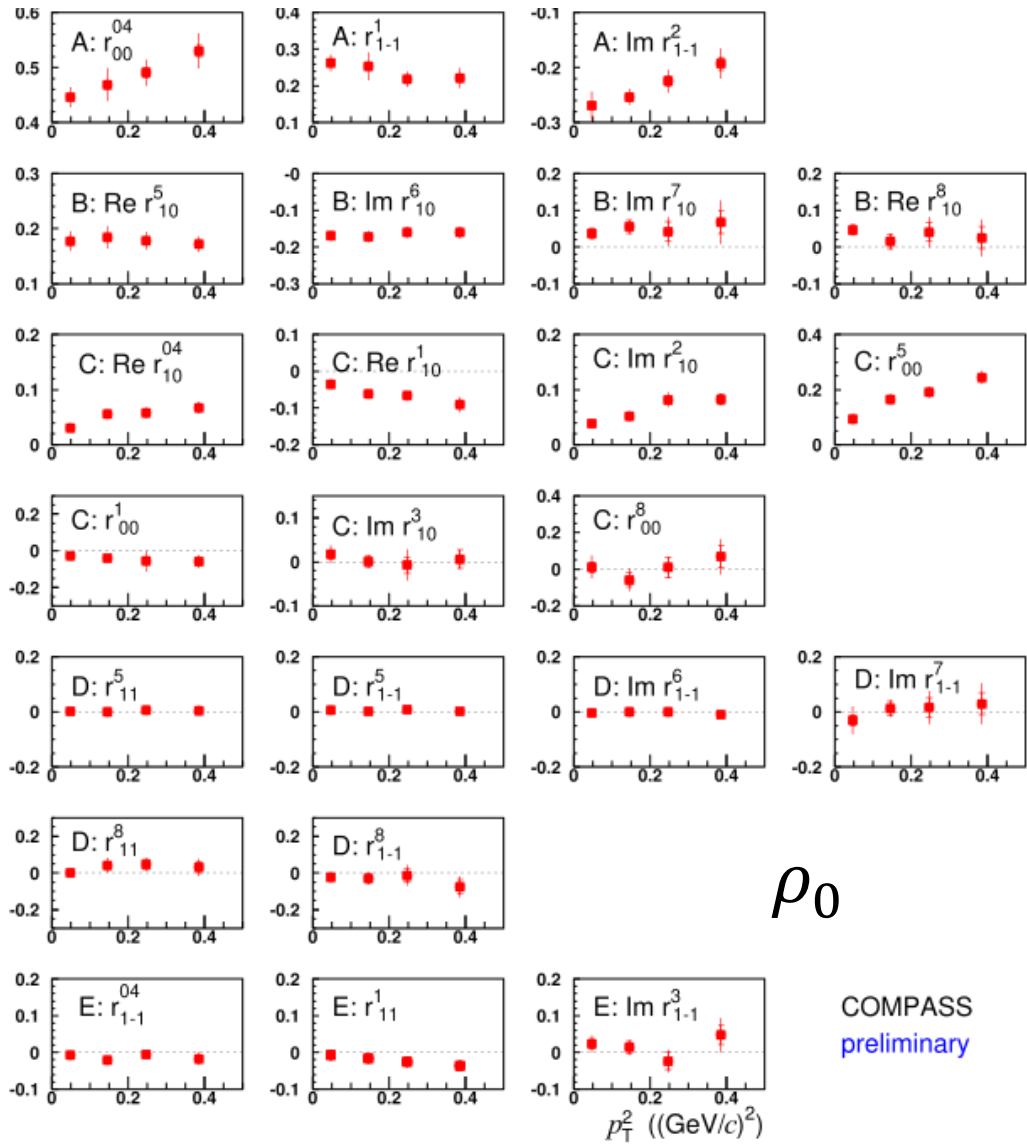
COMPASS
preliminary



ω

EPJC 81 (2021) 126

SDMEs dependences



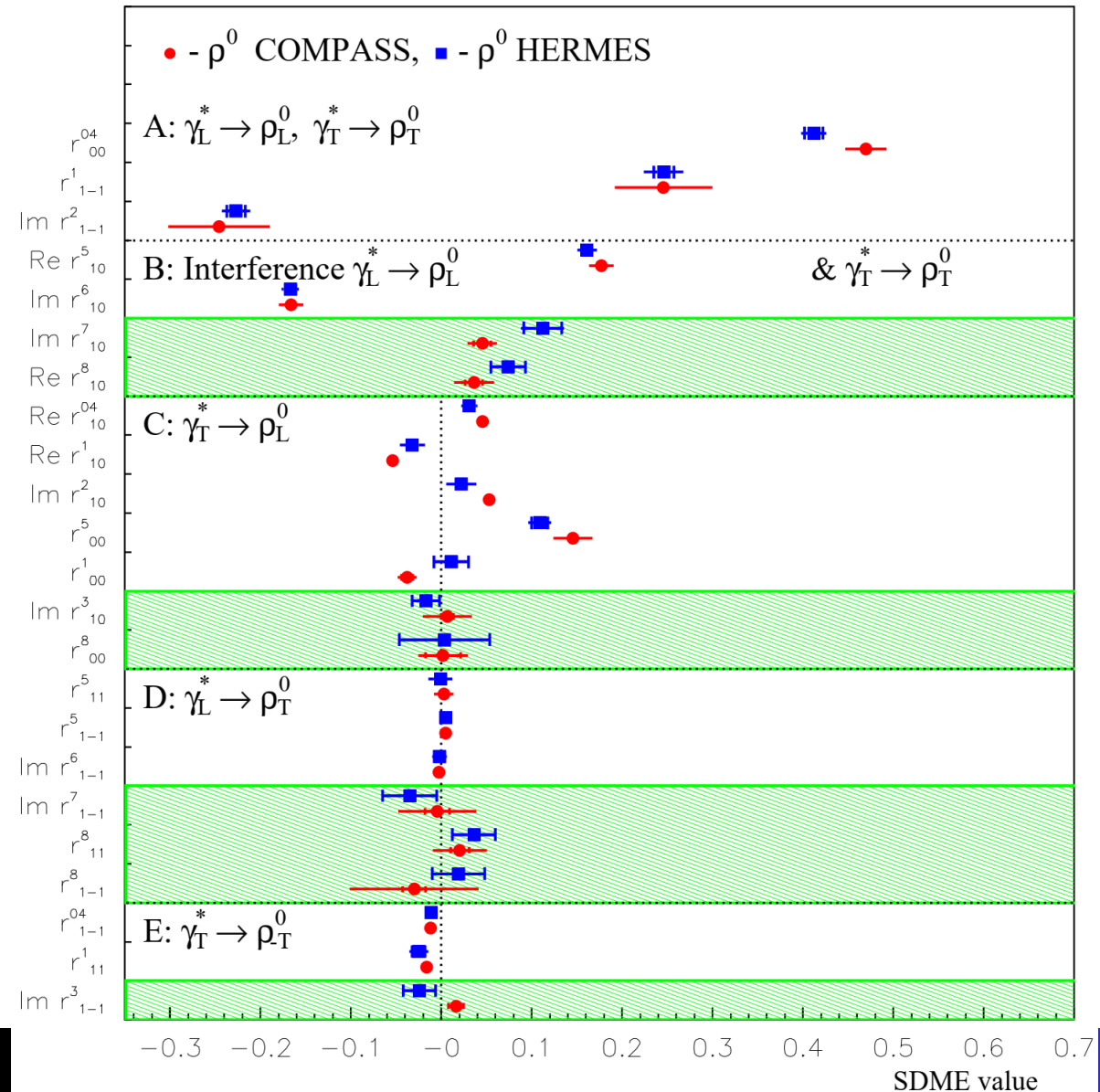
SDMEs comparison with HERMES

COMPASS preliminary

HERMES SDMEs results:

ω - EPJC **74** (2014) 3110,

ρ^0 - EPJC **62** (2009) 659–695



Unnatural Parity Exchange contribution ρ^0

$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1$$

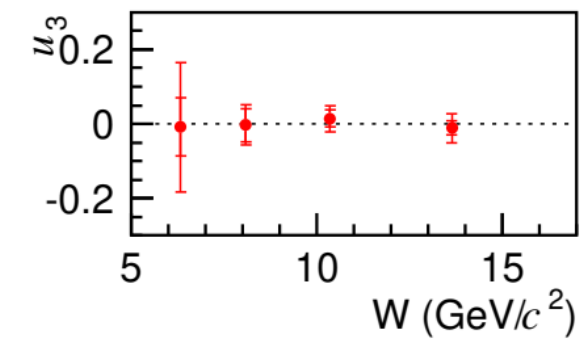
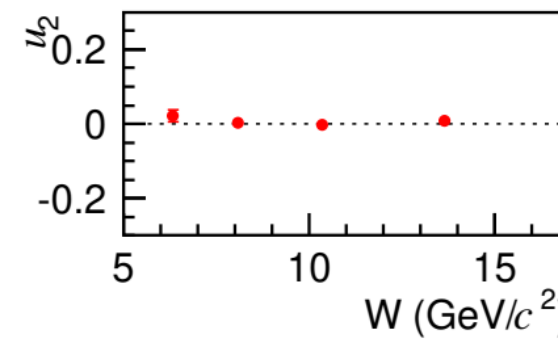
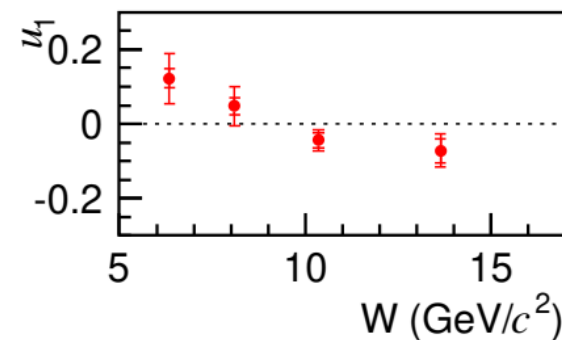
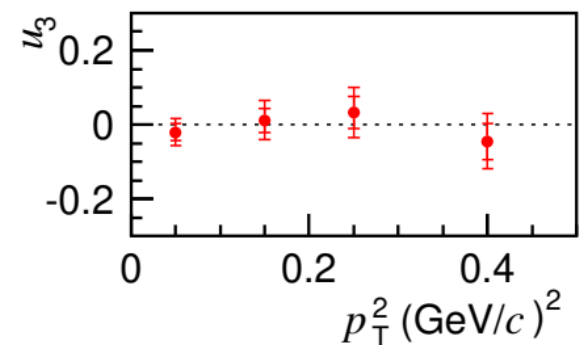
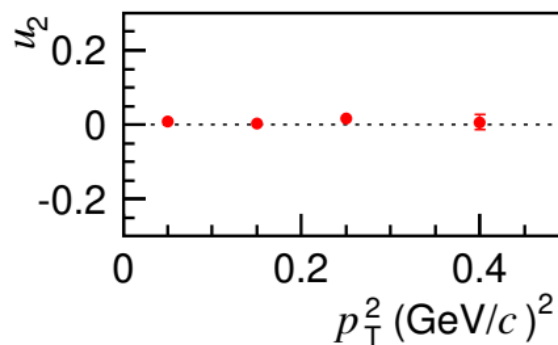
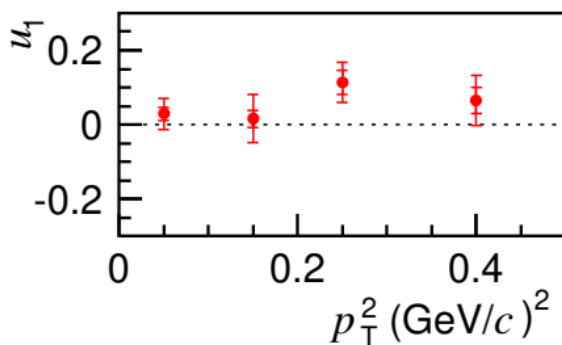
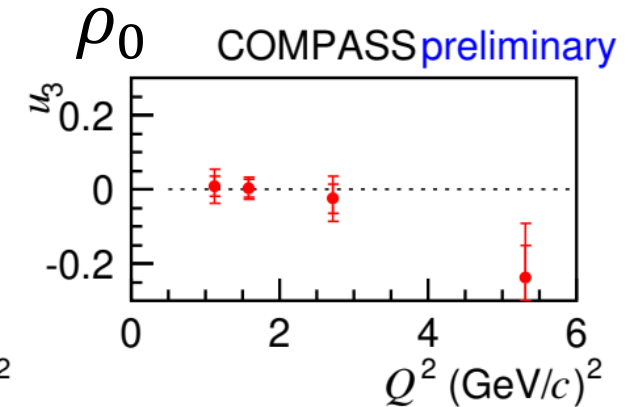
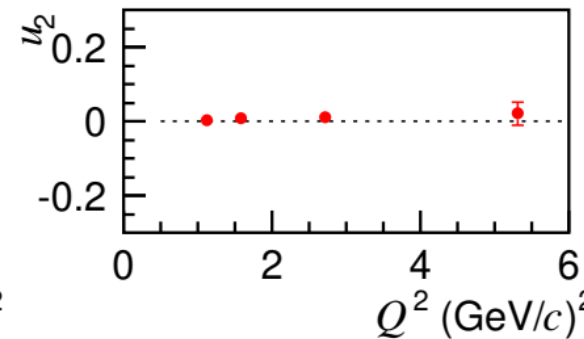
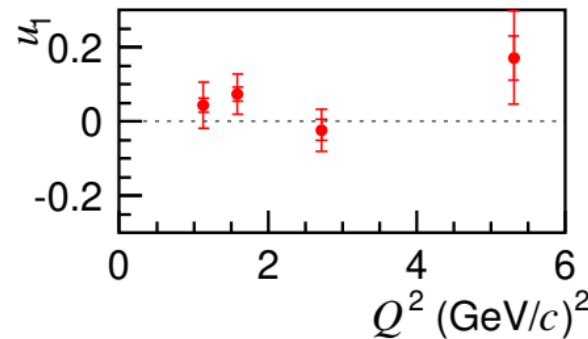
$$u_1 = \frac{\widetilde{\sum} 4\epsilon|U_{10}|^2 + 2|U_{11} + U_{-11}|^2}{\mathcal{N}}$$

$$u_2 = r_{11}^5 + r_{1-1}^5$$

$$u_3 = r_{11}^8 + r_{1-1}^8$$

$$u_2 + iu_3 = \sqrt{2} \frac{\widetilde{\sum} (U_{11} + U_{-11})U_{10}^*}{\mathcal{N}}$$

- ❖ numerator in u_1 depends only on UPE amplitudes $\rightarrow u_1 > 0$
- ❖ very small UPE contribution observed in ρ^0
- ❖ τ_{UPE}^2 0.03 averaged

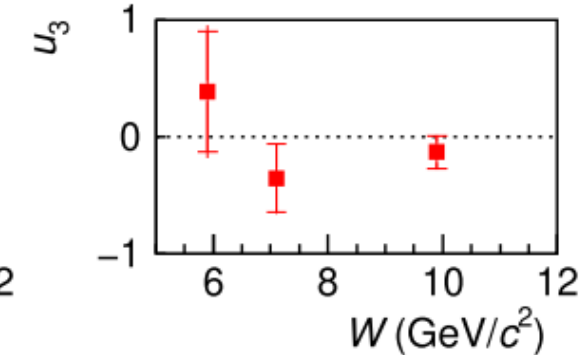
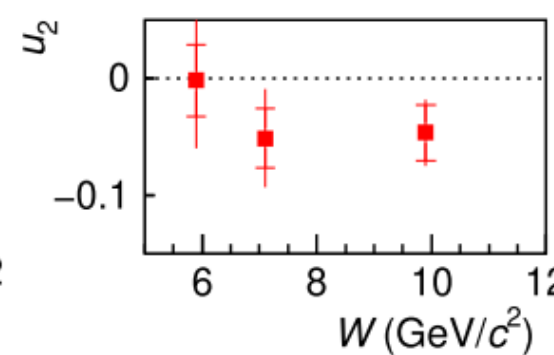
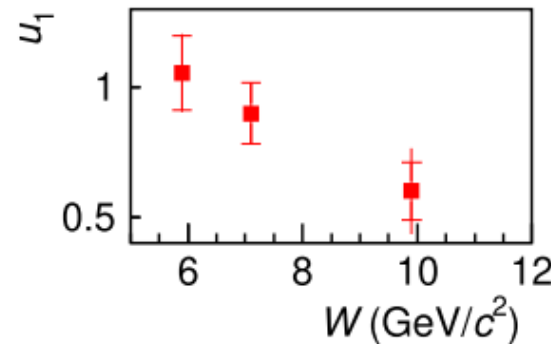
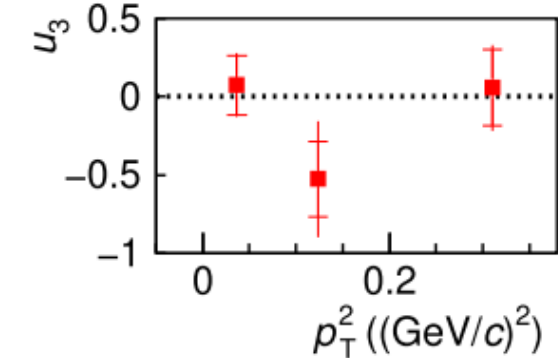
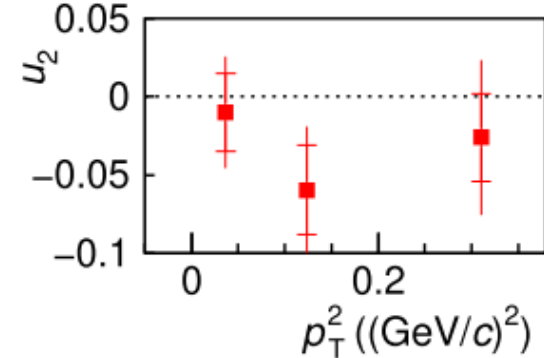
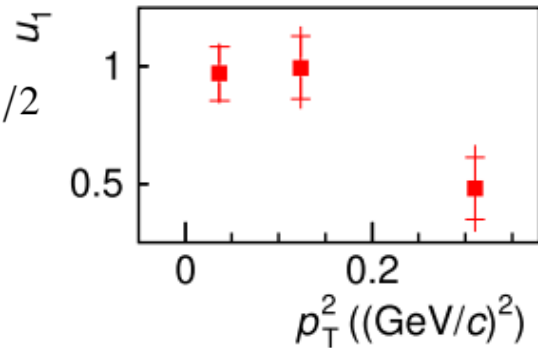
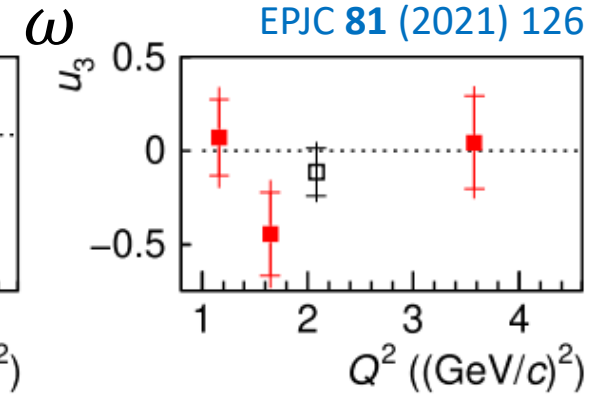
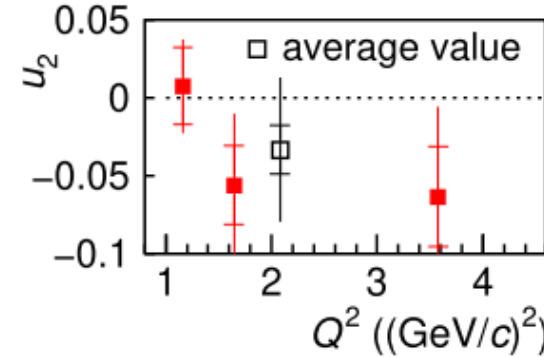
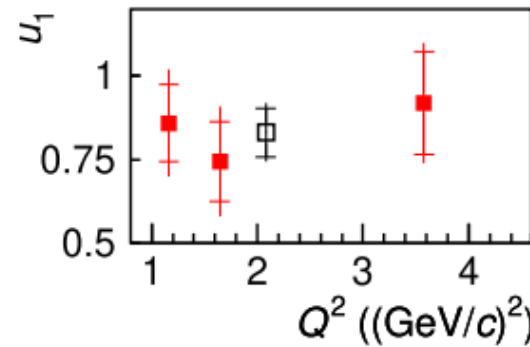


Unnatural Parity Exchange contribution ω

- ❖ ω large UPE contribution decreasing with increasing W in u_1
- ❖ u_2 and u_3 consistent with zero

$$\tau_{UPE}^2 = (2\epsilon|U_{10}|^2 + |U_{01}|^2 + |U_{1-1}|^2 + |U_{11}|^2) / \mathcal{N} \approx u_1 / 2$$

- ❖ UPE fractional contribution:
 $\tau_{UPE}^2 = 0.5 \rightarrow 0.3$



EPJC 81 (2021) 126