

# Measurement of $q_T$ -weighted transverse-spin-dependent azimuthal asymmetries at COMPASS


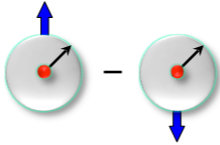
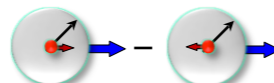
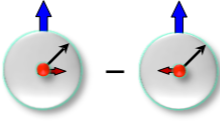
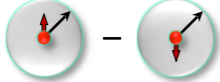
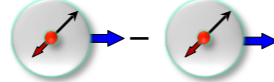
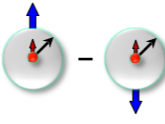
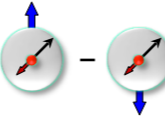


Riccardo Longo  
On behalf of the COMPASS Collaboration

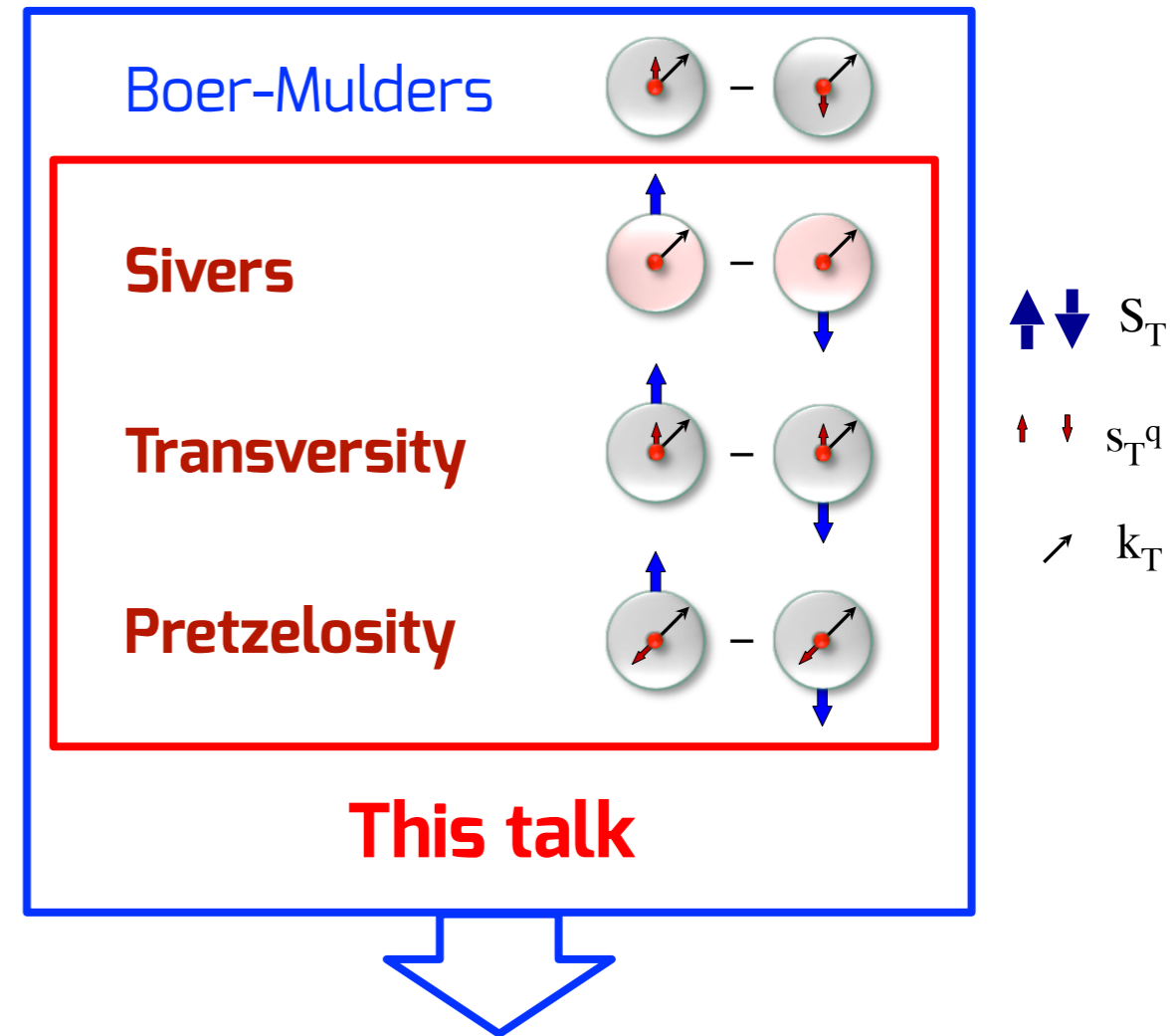


# Transverse Momentum Dependent PDFs

In the leading order QCD parton model nucleon spin-structure can be parametrized in terms of 8 *twist-2* quark intrinsic transverse momentum ( $k_T$ ) dependent TMD PDFs.

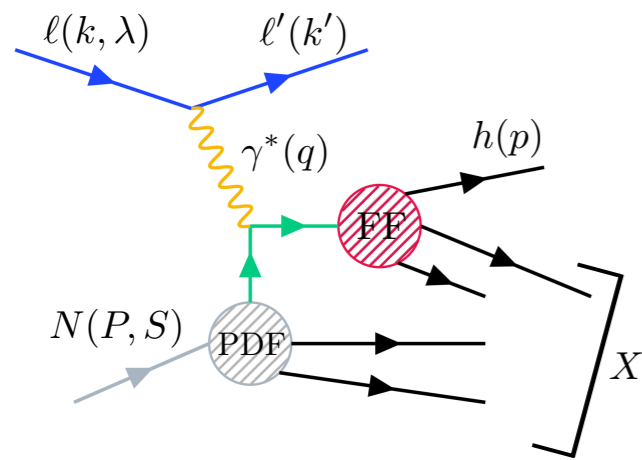
		Nucleon Polarization		
		U	L	T
Quark Polarization	U	 $f_1^q(x, \mathbf{k}_T^2)$ Number Density		 $f_{1T}^{q\perp}(x, \mathbf{k}_T^2)$ Sivers
	L		 $g_1^q(x, \mathbf{k}_T^2)$ Helicity	 $g_{1T}^{q\perp}(x, \mathbf{k}_T^2)$ Worm-Gear T
	T	 $h_1^{q\perp}(x, \mathbf{k}_T^2)$ Boer-Mulders	 $h_{1L}^{q\perp}(x, \mathbf{k}_T^2)$ Worm-Gear L	 $h_{1T}^q(x, \mathbf{k}_T^2)$ Transversity  $h_{1T}^{q\perp}(x, \mathbf{k}_T^2)$ Pretzelosity

 Nucleon   
  Nucleon spin   
  quark   
  quark spin   
   $k_T$



TMD PDFs can be accessed through measurement of target spin (in)dependent azimuthal asymmetries both in SIDIS and Drell-Yan

# Probing nucleon structure via SIDIS and Drell-Yan



**SIDIS on transversely polarized nucleons**  
COMPASS 2007, 2010

$$\mu + p^\uparrow \rightarrow \mu' + h + X$$

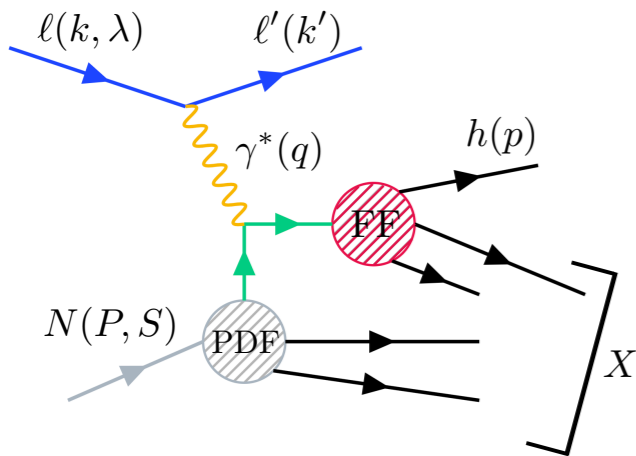
- Access to convolutions of TMD PDFs and Fragmentation Functions (FFs):

$$A_{\lambda S}^{mod} \longrightarrow F_{\lambda S}^{mod} \longrightarrow PDF_p \otimes FF_h$$

$$F_{UU}^{\cos \phi_h}, F_{UU}^{\cos 2\phi_h} \longrightarrow h_{1,p}^\perp \quad F_{UT,T}^{\sin(\phi_h - \phi_S)} \propto f_{1T,p}^\perp \otimes D_{1,q}^h$$

$$F_{UT}^{\sin(\phi_H + \phi_S)} \propto h_{1,p} \otimes H_1^{\perp,h} \quad F_{UT}^{\sin(3\phi_h - \phi_S)} \propto h_{1T,p}^\perp \otimes H_1^{\perp,h}$$

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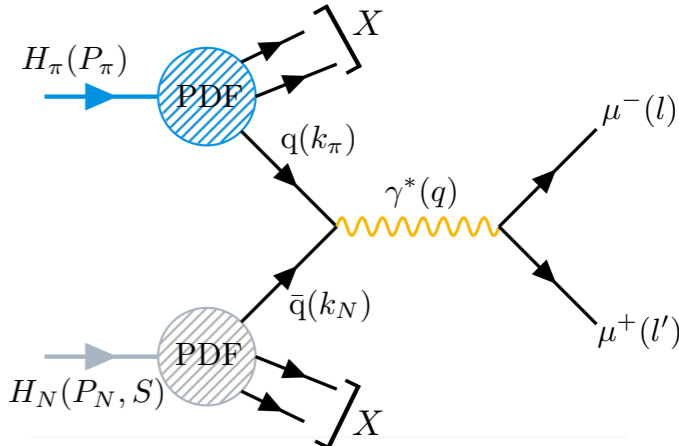
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**Pion induced polarized Drell-Yan**  
 COMPASS 2015, 2018

$$\pi^- + p^\uparrow \rightarrow \mu^+ \mu^- + X$$



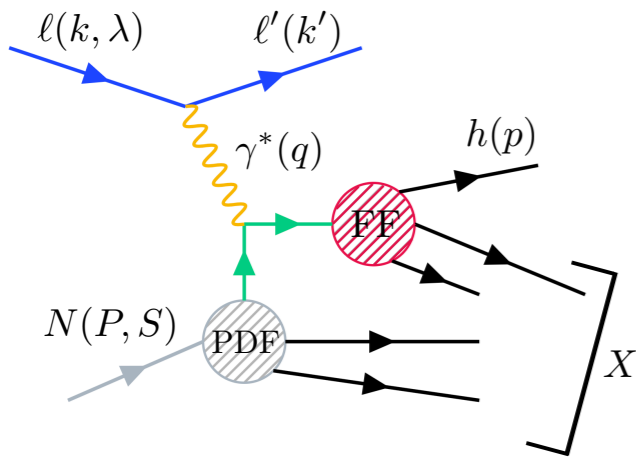
- Access to convolutions of TMD PDFs;

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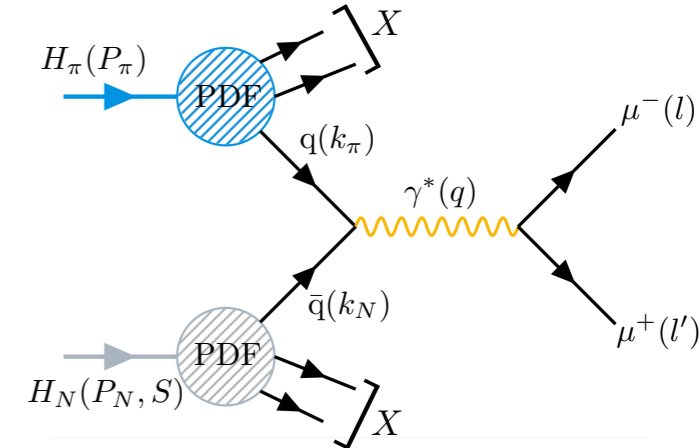


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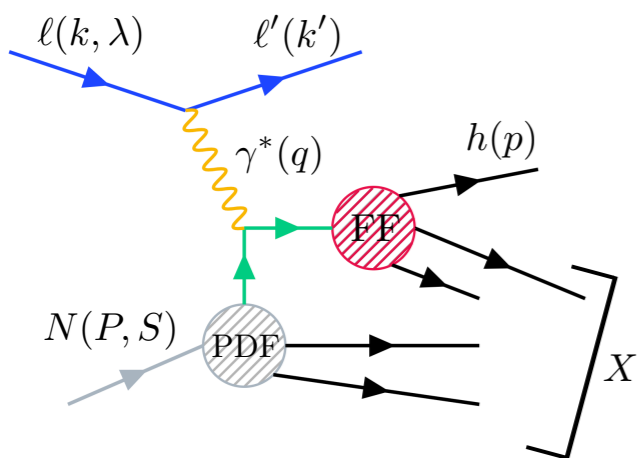
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**Universality in the TMD-QCD parton model approach**

$$h_{1,p}^{SIDIS} = h_{1,p}^{DY}$$

$$h_{1T,p}^{SIDIS} = h_{1T,p}^{DY}$$

# Probing nucleon structure via SIDIS and Drell-Yan

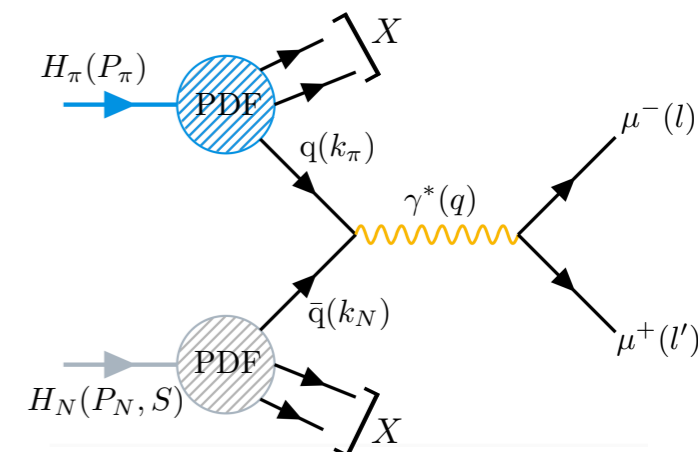


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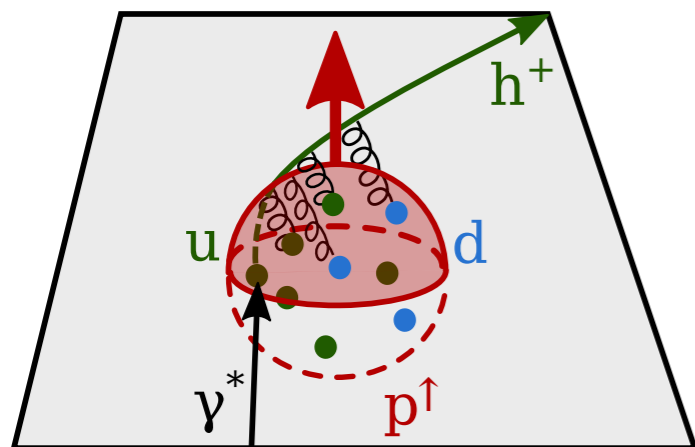
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Drawings courtesy of J. Matoušek



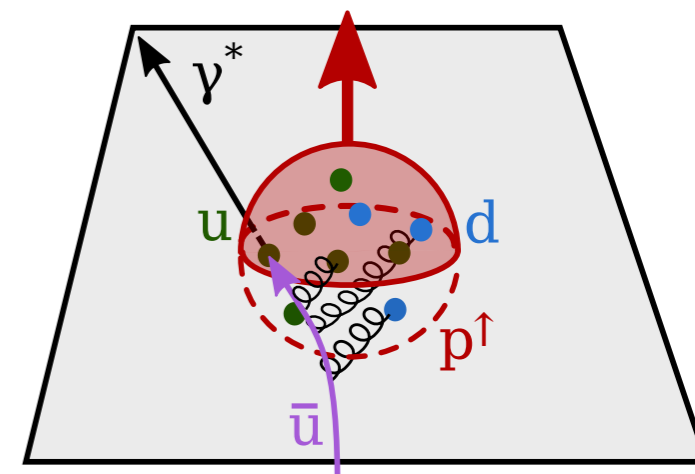
Sivers effect in SIDIS (as described by [M. Burkardt, Nucl.Phys. A735 (2004) 185])

**Universality in the TMD-QCD parton model approach**

$$f_{1T,p}^\perp_{SIDIS} = -f_{1T,p}^\perp_{DY}$$

$$h_{1,p}^\perp_{SIDIS} = -h_{1,p}^\perp_{DY}$$

Predicted **sign-change** for Sivers and Boer-Mulders functions



Sivers effect in Drell-Yan Described in the same manner

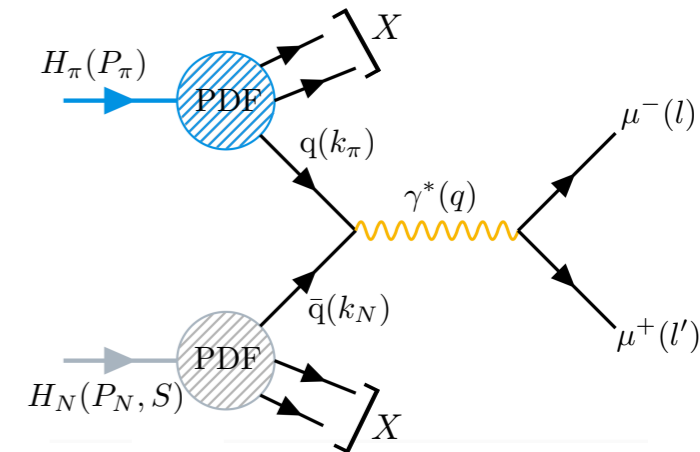
# Drell-Yan cross-section

General leading order QCD parton model expression of the Single Polarized DY cross-section

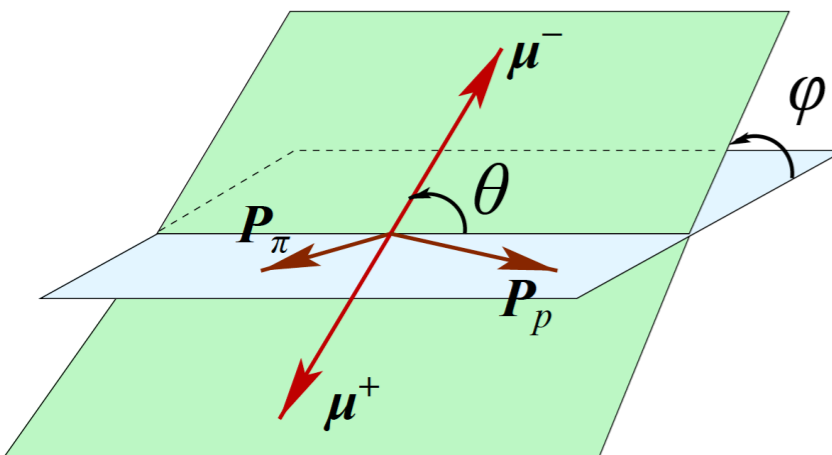
$$\frac{d\sigma_{DY}}{dx_\pi dx_N dq_T^2 d\varphi_S d\cos\theta d\varphi} = C_0 \left\{ (1 + \cos^2\theta) F_U^1 + \sin^2\theta \cos 2\varphi F_U^{\cos 2\varphi} \right. \\ \left. + |\mathbf{S}_T| \left[ (1 + \cos^2\theta) \sin\varphi_S F_T^{\varphi_S} \right. \right. \\ \left. \left. + \sin^2\theta \sin(2\varphi + \varphi_S) F_T^{\sin(2\varphi + \varphi_S)} \right. \right. \\ \left. \left. + \sin^2\theta \sin(2\varphi - \varphi_S) F_T^{\sin(2\varphi - \varphi_S)} \right] \right\}$$

Pion induced polarized Drell-Yan  
COMPASS 2015, 2018

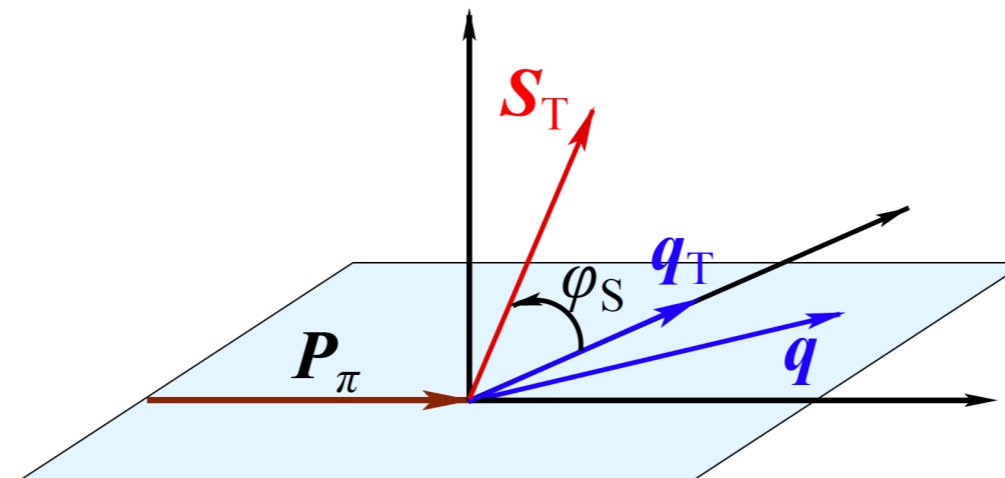
$$\pi^- + p^\uparrow \rightarrow \mu^+ \mu^- + X$$



Collins - Soper frame



Target rest frame

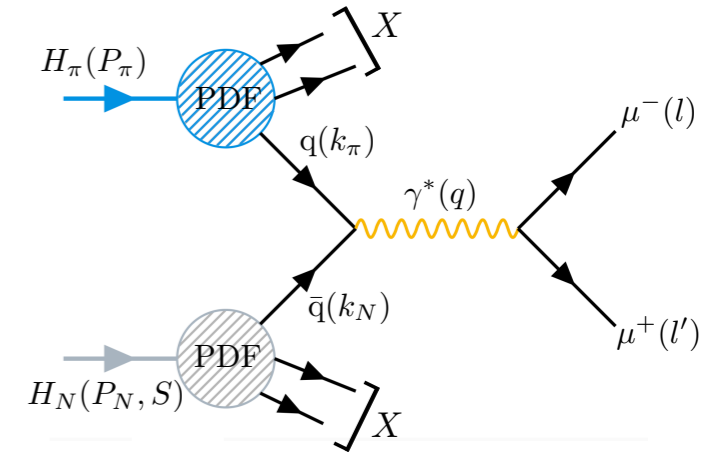
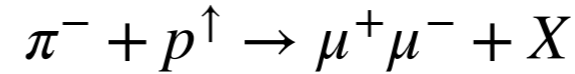


$\mathbf{q}_T$ : transverse momentum of the virtual photon in the target rest frame

# Drell-Yan cross-section

Each structure function  $F_X^{[\text{mod}]}$  can be interpreted in terms of convolutions of TMD PDFs of beam and target hadrons;

Pion induced  
polarized Drell-Yan  
COMPASS 2015, 2018



$$F_U^1 = -\mathcal{C} \left[ f_{1,\pi} f_{1,p} \right], \quad \text{Number densities}$$

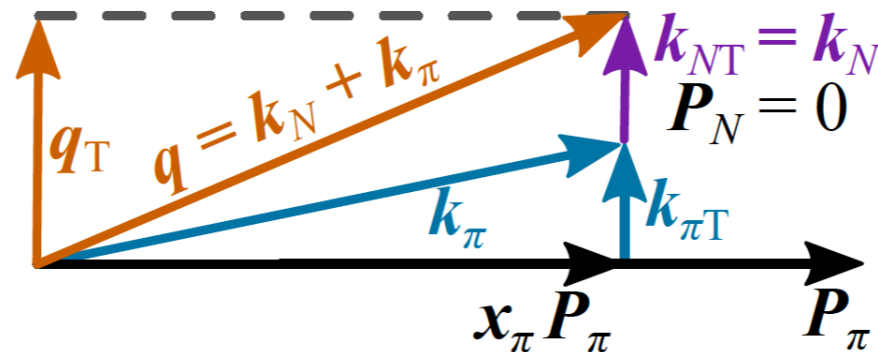
$$F_U^{\cos 2\varphi} = -\mathcal{C} \left[ \frac{2(\mathbf{q}_T \cdot \mathbf{k}_{\pi T})(\mathbf{q}_T \cdot \mathbf{k}_{pT}) - q_T^2(\mathbf{k}_{\pi T} \cdot \mathbf{k}_{pT})}{q_T^2 M_\pi M_p} h_{1,\pi}^\perp h_{1,p}^\perp \right], \quad \text{Boer Mulders functions}$$

$$F_T^1 = F_T^{\sin \varphi_S} = -\mathcal{C} \left[ \frac{\mathbf{q}_T \cdot \mathbf{k}_{pT}}{q_T M_p} f_{1,\pi} f_{1T,p}^\perp \right], \quad \text{Number density of the pion, Sivers of the proton}$$

$$F_T^{\sin(2\varphi+\varphi_S)} = -\mathcal{C} \left[ \left( \frac{(\mathbf{q}_T \cdot \mathbf{k}_{pT}) [2(\mathbf{q}_T \cdot \mathbf{k}_{\pi T})(\mathbf{q}_T \cdot \mathbf{k}_{pT}) - q_T^2(\mathbf{k}_{\pi T} \cdot \mathbf{k}_{pT})]}{q_T^3 M_\pi M_p^2} - \frac{k_{pT}^2(\mathbf{q}_T \cdot \mathbf{k}_{\pi T})}{2q_T M_\pi M_p^2} \right) h_{1,\pi}^\perp h_{1T,p}^\perp \right], \quad \begin{array}{l} \text{Boer Mulders of the pion} \\ \text{Pretzelosity of the proton} \end{array}$$

$$F_T^{\sin(2\varphi-\varphi_S)} = -\mathcal{C} \left[ \frac{\mathbf{q}_T \cdot \mathbf{k}_{\pi T}}{q_T M_\pi} h_{1,\pi}^\perp h_{1,p} \right] \quad \begin{array}{l} \text{Boer Mulders of the pion} \\ \text{Transversity of the proton} \end{array}$$

The convolution  $\mathcal{C}$  of the TMDs runs over the intrinsic transverse momenta



Transverse momenta in the target rest frame



# Transverse Spin Asymmetries in Drell-Yan

- Transverse Spin Asymmetries (TSAs):

See talk by B.Parsamyan

$$A_T^{\sin \Phi}(x_\pi, x_N, q_T^2) = \frac{F_T^{\sin \Phi}(x_\pi, x_N, q_T^2)}{F_U^1(x_\pi, x_N, q_T^2)} = \frac{\mathcal{C} \left[ \omega(\mathbf{k}_{\pi T}, \mathbf{k}_{p,T}) f_\pi f_p \right]}{\mathcal{C} \left[ f_{1,\pi} f_{1,p} \right]}, \quad \Phi = \varphi_S, 2\varphi_{CS} \pm \varphi_S$$

- To solve the convolution over intrinsic transverse momenta one has to assume a given dependence of the TMD on  $k_T$  (e.g. Gaussian).

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- To solve the convolution over intrinsic transverse momenta one has to assume a given dependence of the TMD on  $k_T$  (e.g. Gaussian).
- Example: **Sivers asymmetry** integrated over  $q_T$  in the Gaussian model

First  $\mathbf{k}_T^2$  moment of the Sivers function  $f_{1T,p}^{\perp(1)q}(x_N) = \int d^2\mathbf{k}_T \left( \frac{k_T^2}{2M^2} \right) f_{1T,p}^{\perp(1)q}(x_N, k_T^2)$

$$A_T^{\sin \varphi_S}(x_\pi, x_N) \stackrel{\text{Gauss.}}{=} -a_G \frac{\sum_q e_q^2 \left[ f_{1,\pi}^{\bar{q}}(x_\pi) f_{1T,p}^{\perp(1)q}(x_N) + (q \leftrightarrow \bar{q}) \right]}{\sum_q e_q^2 \left[ f_1^q(x_\pi) f_1^{\bar{q}}(x_N) + q \leftrightarrow \bar{q} \right]} \approx -a_G \frac{f_{1,T}^{\perp(1)u}(x_N)}{f_{1,p}^u(x_N)}$$

$$a_G = \frac{\sqrt{\pi} M_p}{\sqrt{\langle \mathbf{k}_{\pi T} \rangle^2 + \langle \mathbf{k}_{pT} \rangle^2}}$$

Gaussian factor

Neglecting sea quarks contribution

$\pi^- = |\bar{u}d\rangle$   
 $p = |uud\rangle$

# $q_T$ -weighted TSAs in Drell-Yan

- To avoid making assumptions on the  $\mathbf{k}_T$  dependence of the TMDs, a popular solution is to weight the structure functions with the transverse momentum of the virtual photon ( $\mathbf{q}_T$ ).

[A. Kotzinian & P. Mulders, PLB 406 (1997) 373]

[A. Efremov et al., Phys.Lett. B612 (2005) 233]

[A. Sissakian et al., Eur.Phys.J. C46 (2006) 147]

[Z. Wang et al., Phys.Rev. D95 (2017) 094004]

- Sivers** example:

$$A_T^{\sin \phi_S}(x_\pi, x_N, q_T^2) = \frac{F_T^{\sin \phi_S}(x_\pi, x_N, q_T^2)}{F_U^1(x_\pi, x_N, q_T^2)} = - \frac{\mathcal{C} \left[ \frac{\mathbf{q}_T \cdot \mathbf{k}_{pT}}{q_T M_p} f_{1,\pi} f_{1T,p}^\perp \right]}{\mathcal{C} \left[ f_{1,\pi} f_{1,p} \right]}$$

- Integration of  $F_U^1$  over  $d^2 \mathbf{q}_T$  can be solved w/o assumptions

$$\int d^2 \mathbf{q}_T F_U^1 = \int d^2 \mathbf{q}_T \mathcal{C} \left[ f_{1,\pi} f_{1,p} \right] = \frac{1}{N_c} \sum_q e_q^2 \left[ f_{1,\pi}^{\bar{q}}(x_\pi) f_{1,p}^q(x_p) + (q \leftrightarrow \bar{q}) \right]$$

- Applying the weight  $\frac{q_T}{M_p}$  the integral can be solved w/o assumptions

$$\int d^2 \mathbf{q}_T \frac{q_T}{M_p} F_T^{\sin \phi_S} = - \int d^2 \mathbf{q}_T \frac{q_T}{M_p} \mathcal{C} \left[ \frac{\mathbf{q}_T \cdot \mathbf{k}_{pT}}{q_T M_p} f_{1,\pi} f_{1T,p}^\perp \right] = - \frac{2}{N_c} \sum_q e_q^2 \left[ f_{1,\pi}^{\bar{q}}(x_\pi) f_{1T,p}^{\perp(1)q}(x_p) + (q \leftrightarrow \bar{q}) \right]$$

# $q_T$ -weighted TSAs in Drell-Yan

- $q_T$ -weighted TSAs represent a **direct measurement** of TMD PDFs  $k_T^2$ -moments;
- By  $q_T$ -weighting we are able to access **products**, not convolutions;
- For Drell-Yan pairs originated in  $\pi^- + p$  collisions and in the valence quark region, one can neglect sea quarks
- $q_T$ -weighted Sivers asymmetry

$$A_T^{\sin \varphi_S \frac{q_T}{M_p}}(x_\pi, x_N) = -2 \frac{\sum_q e_q^2 [f_{1,\pi}^{\bar{q}}(x_\pi) f_{1T,p}^{\perp(1)q}(x_p) + (q \leftrightarrow \bar{q})]}{\sum_q e_q^2 [f_{1,\pi}^{\bar{q}}(x_\pi) f_{1,p}^q(x_p) + (q \leftrightarrow \bar{q})]} \approx -2 \frac{f_{1T}^{\perp(1)u}(x_N)}{f_{1,p}^u(x_N)}$$

- $q_T$ -weighted asymmetry induced by proton Transversity and pion Boer-Mulders function

$$A_T^{\sin(2\varphi - \varphi_S) \frac{q_T}{M_\pi}}(x_\pi, x_N) \approx -2 \frac{h_{1,\pi}^{\perp(1)\bar{u}}(x_\pi) h_{1,p}^{\perp u}(x_N)}{f_1^{\bar{u}}(x_\pi) f_{1,p}^u(x_N)}$$

- $q_T$ -weighted asymmetry induced by proton Pretzelosity and pion Boer-Mulders function

$$A_T^{\sin(2\varphi + \varphi_S) \frac{q_T^3}{2M_p M_\pi}}(x_\pi, x_N) \approx -2 \frac{h_{1,\pi}^{\perp(1)\bar{u}}(x_\pi) h_{1T,p}^{\perp(2)u}(x_N)}{f_1^{\bar{u}}(x_\pi) f_{1,p}^u(x_N)}$$

# The COMPASS collaboration



• SPS North Area

• Fixed target experiment

• First data taking in 2002

## Phase I

- 2002 – 2011
- Hadron spectroscopy
- Nucleon spin structure (L/T P/D Targets)

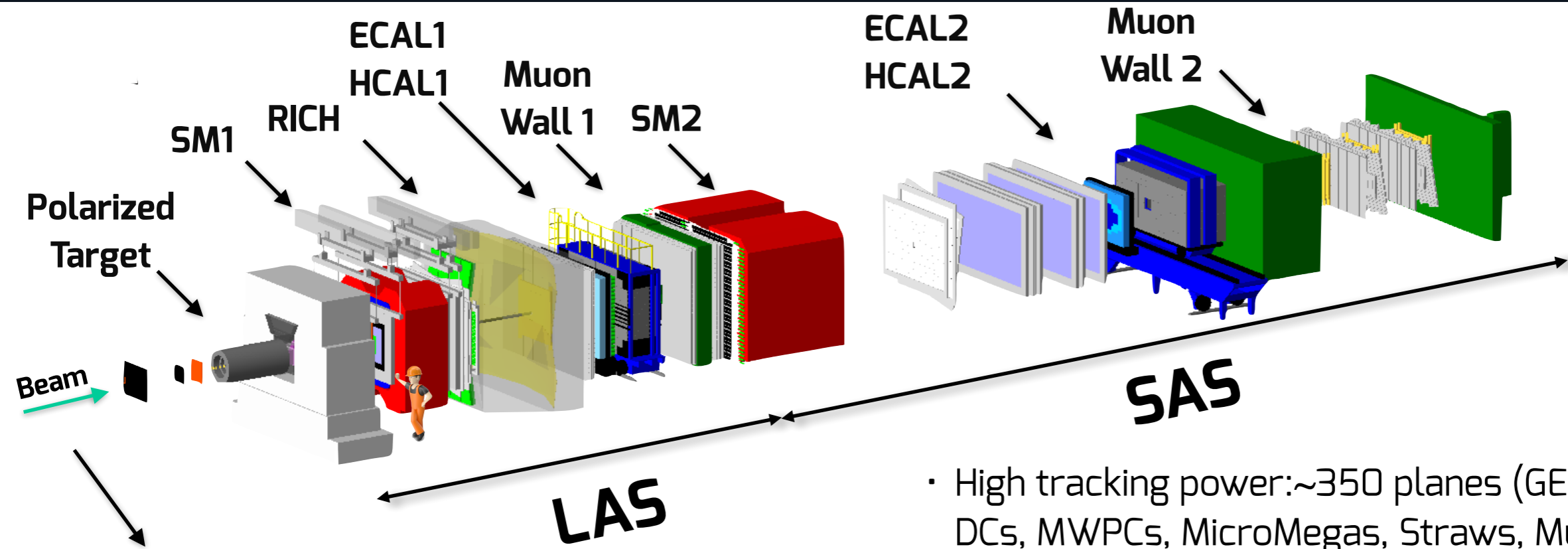
See talk by M.Stolarski

## Phase II

- 2012 – 2018
- Primakoff + DVCS pilot run (2012)
- **Drell-Yan (2015, 2018)**
- DVCS + Unpolarized SIDIS(2016-2017)
- T-polarized SIDIS (D target) (2021)

See talks by  
B.Parsamyan,  
A.Martin  
J.Matoušek,  
N.Pierre,  
A.Vidon,  
A. Moretti

# Drell-Yan measurements at COMPASS



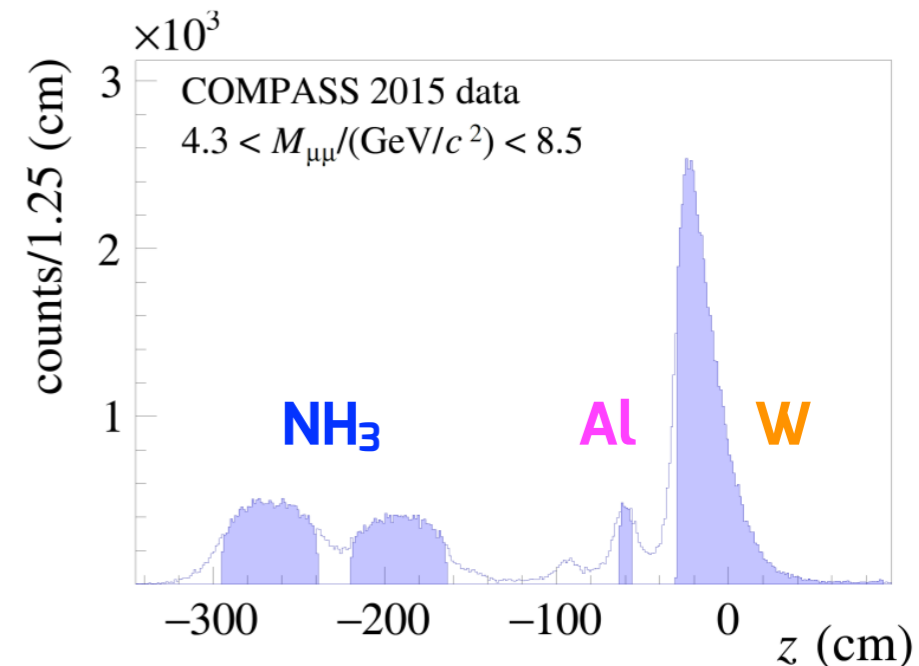
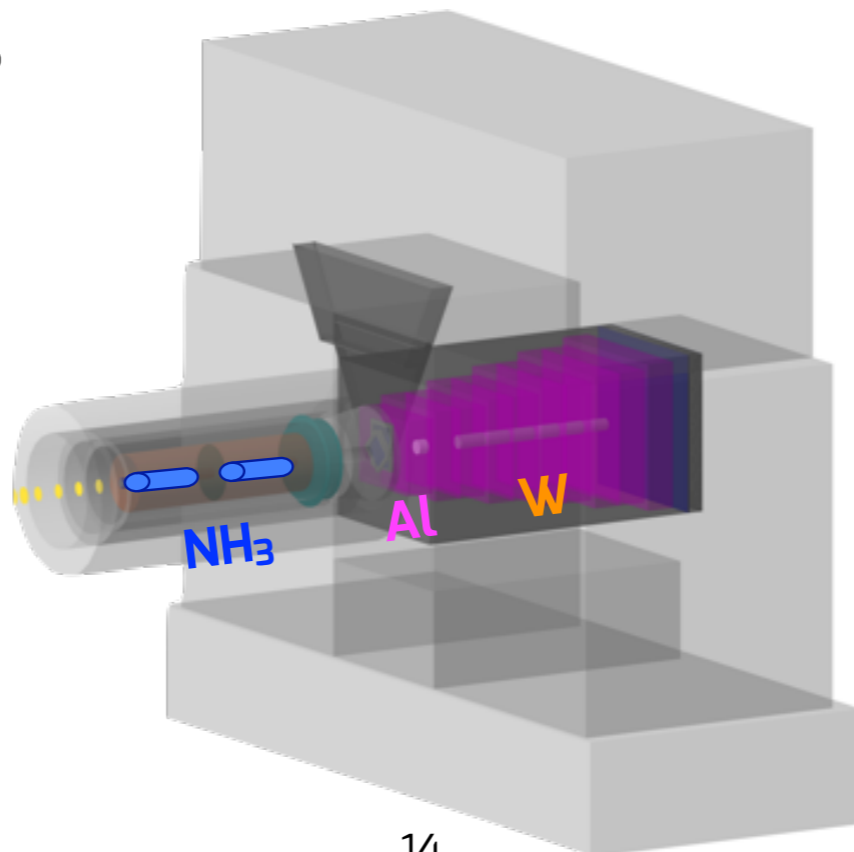
- High tracking power: ~350 planes (GEMs, SciFis, DCs, MWPCs, MicroMegas, Straws, Muon Walls...)

$\pi^-$  beam

- $P_{\pi^-}$  : 191 GeV/c, intensity  $10^8 \pi^-/s$

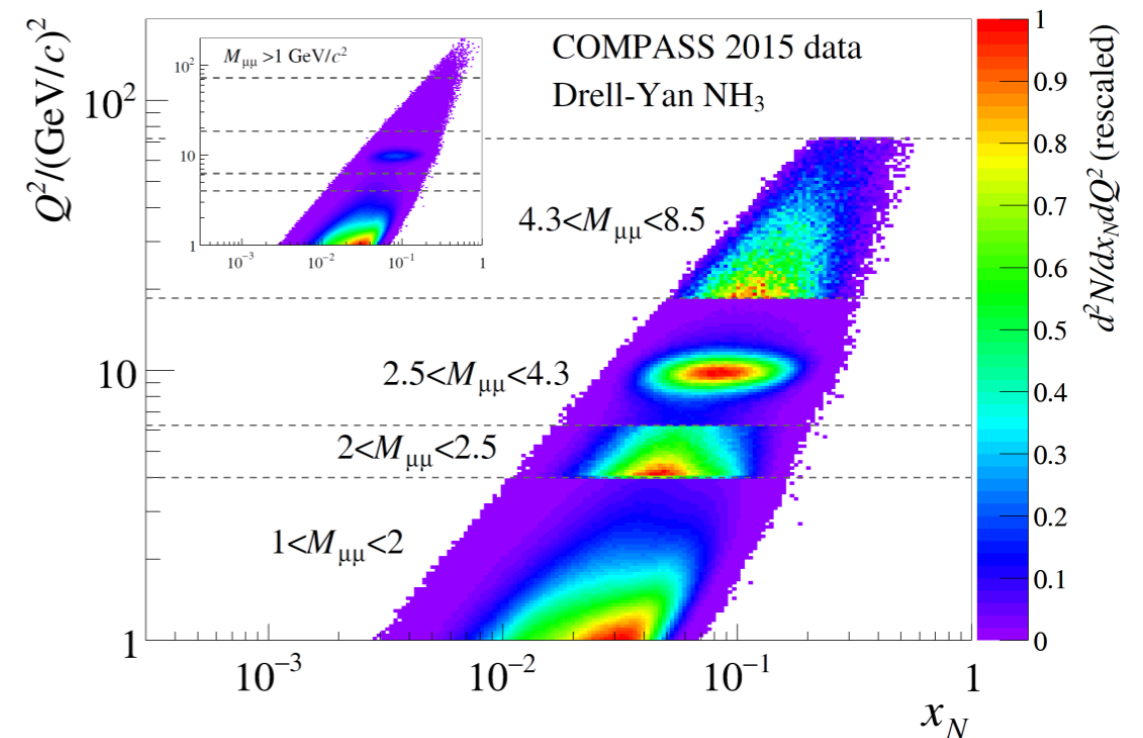
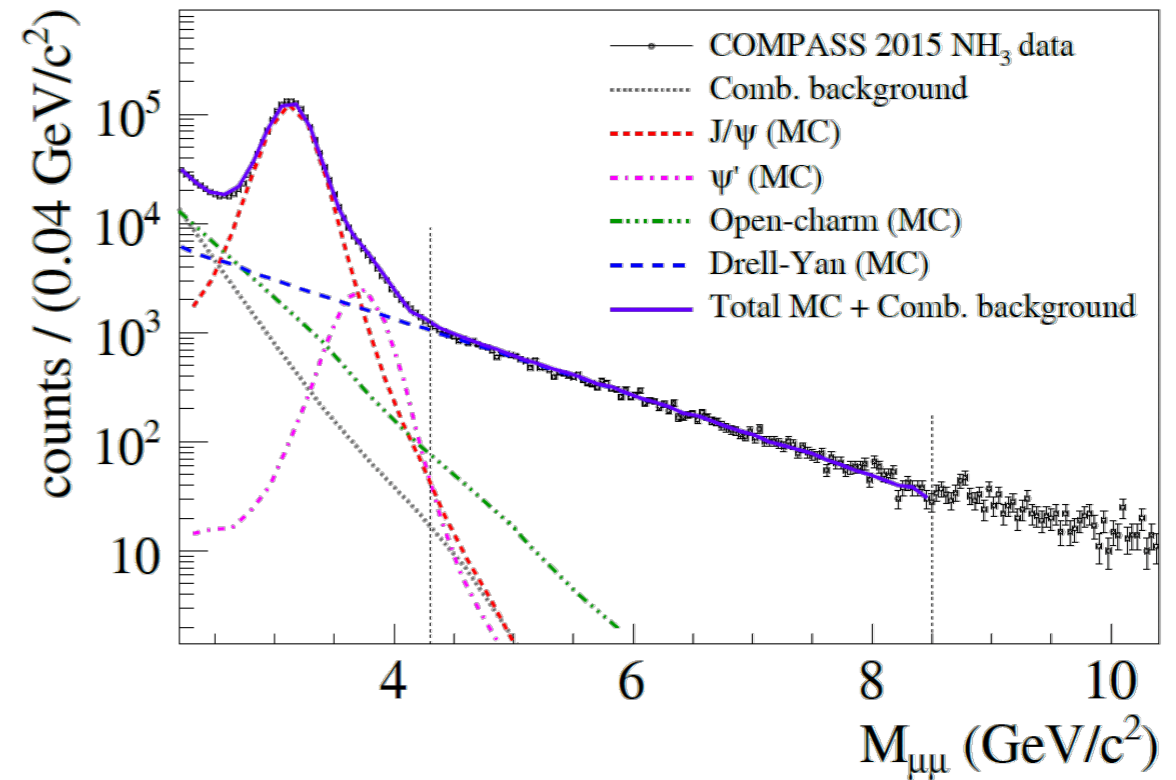
Target	# of cells	Polarization
NH <sub>3</sub>	2	T, ~73 % (2015)
		T, ~75 % (2018)

- 2015 ~4 months of data taking;
- 2018 ~5 months of data taking;
- The NH<sub>3</sub> target polarization was **reversed** after each week;



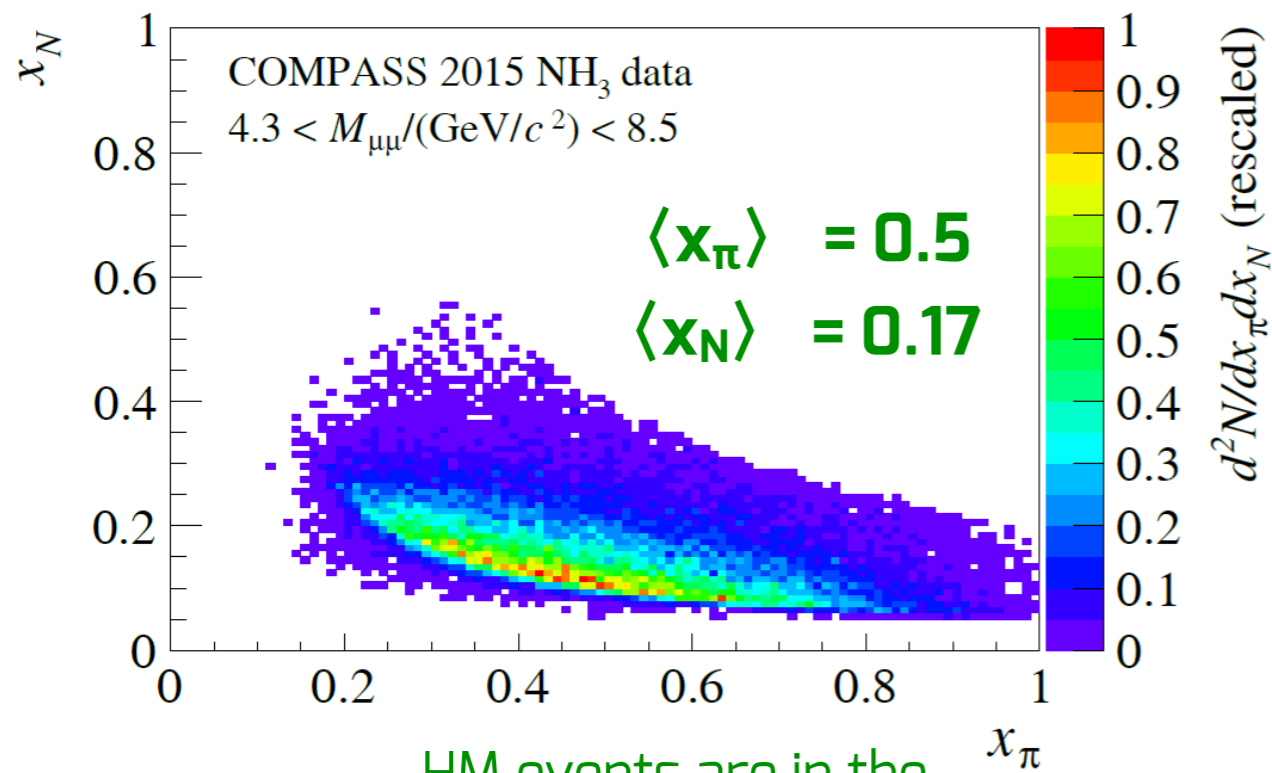
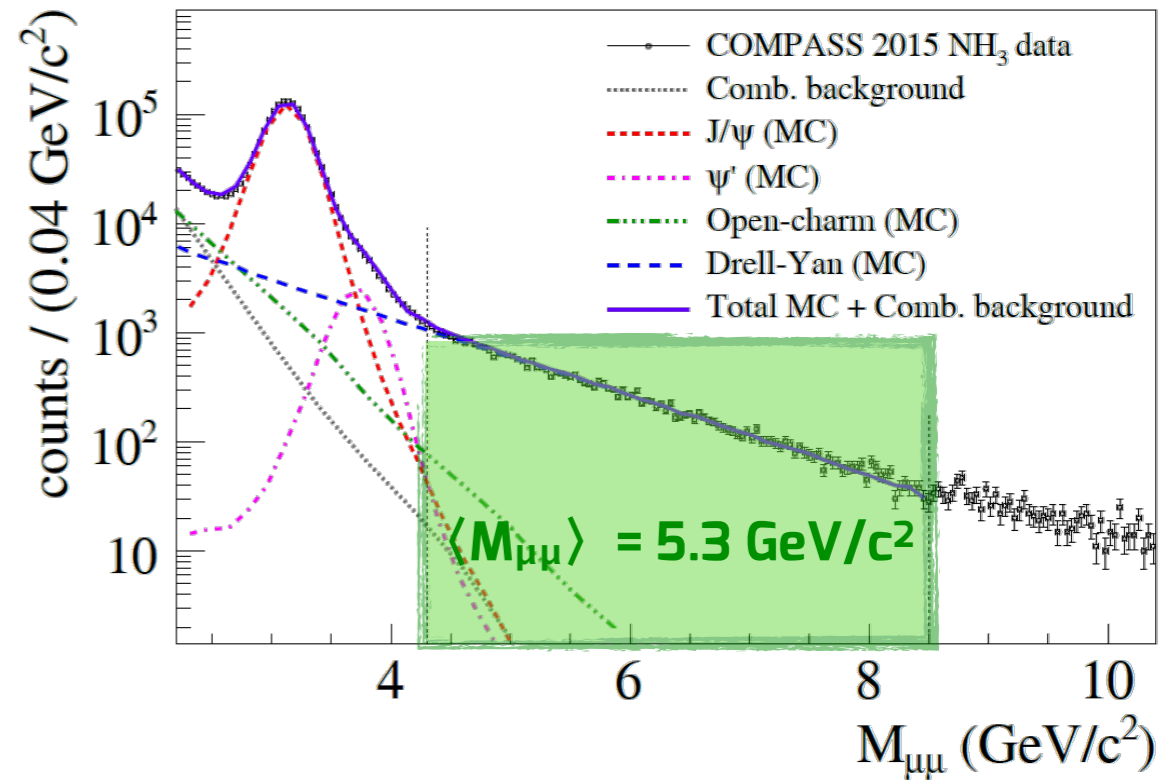
# Drell-Yan measurements at COMPASS

- I.  $1 < M_{\mu\mu}/(\text{GeV}/c^2) < 2$ , “Low mass”
  - Large background contamination
- II.  $2 < M_{\mu\mu}/(\text{GeV}/c^2) < 2.5$ , “Intermediate mass”
  - High DY cross section.
  - Still low DY-signal/background ratio.
- III.  $2.5 < M_{\mu\mu}/(\text{GeV}/c^2) < 4.3$ , “Charmonia mass”
  - Strong  $J/\psi$  signal  $\rightarrow$  Studies of  $J/\psi$  physics.
  - Good signal/background.
- IV.  $4.3 < M_{\mu\mu}/(\text{GeV}/c^2) < 8.5$ , “High mass”
  - Beyond  $J/\psi$  and  $\psi'$  peak, background  $< 4\%$ .
  - Valence quark region  $\rightarrow$  Largest asymmetries!
  - Low DY cross-section

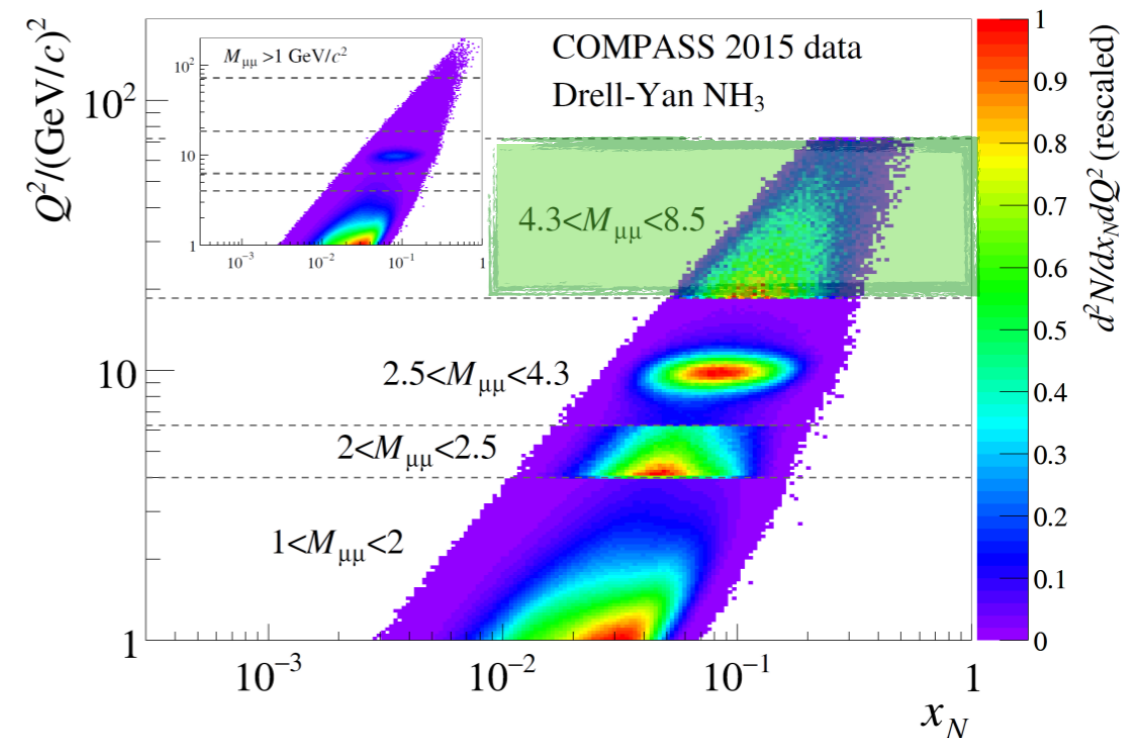


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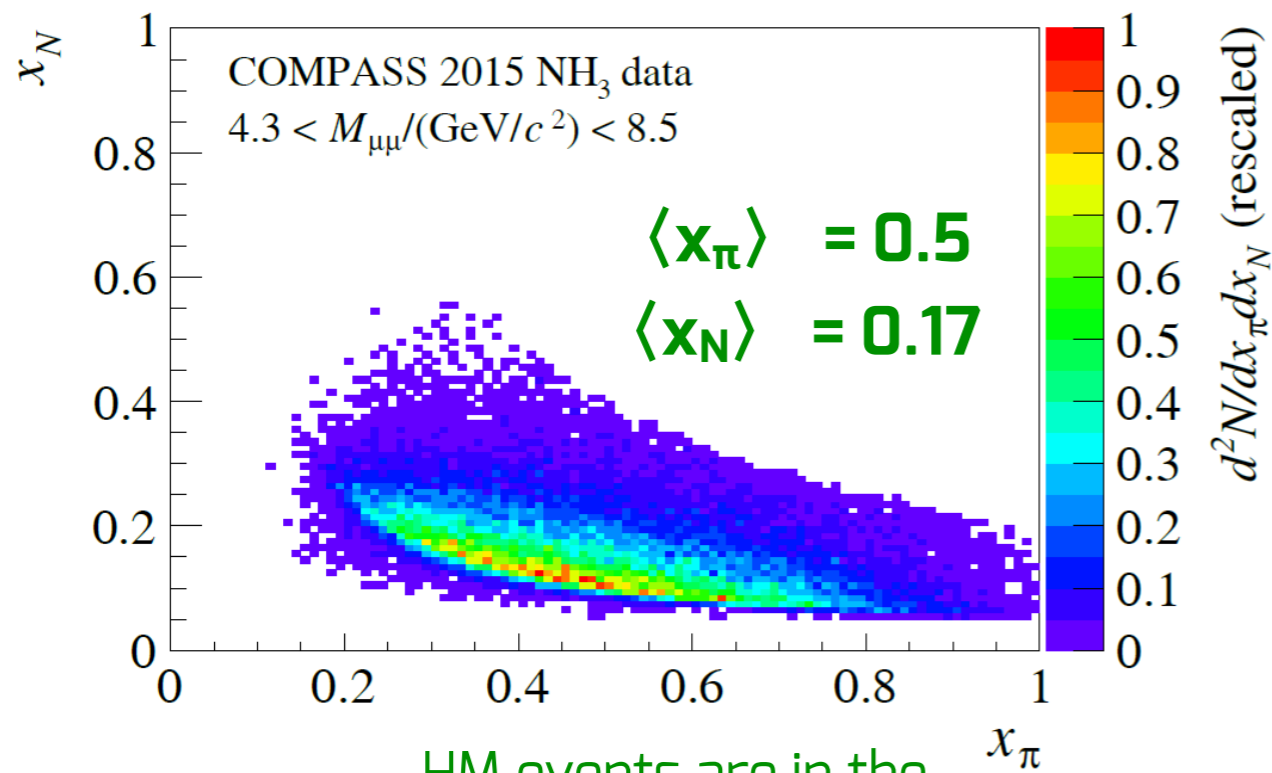
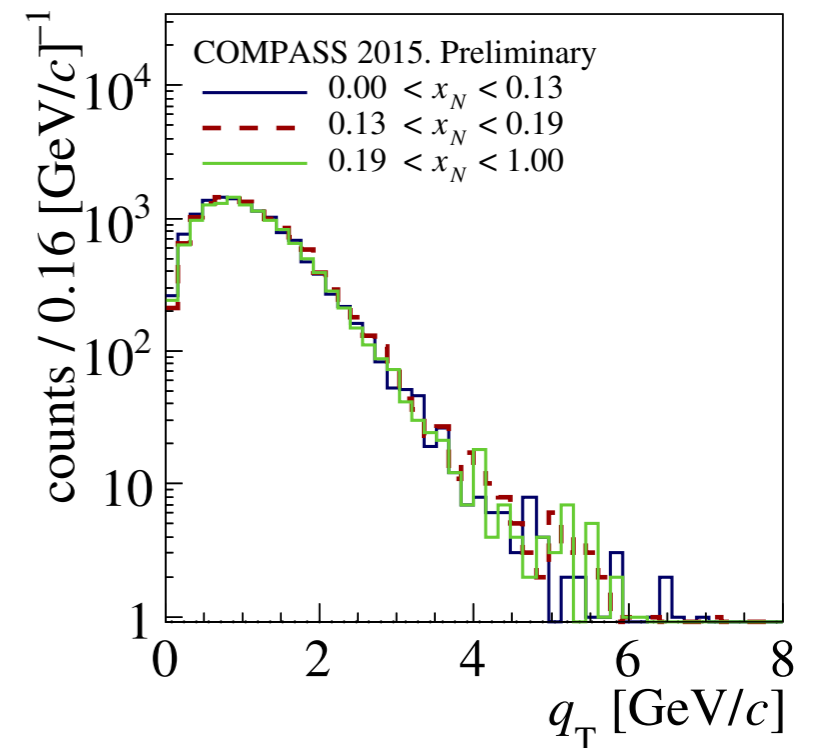
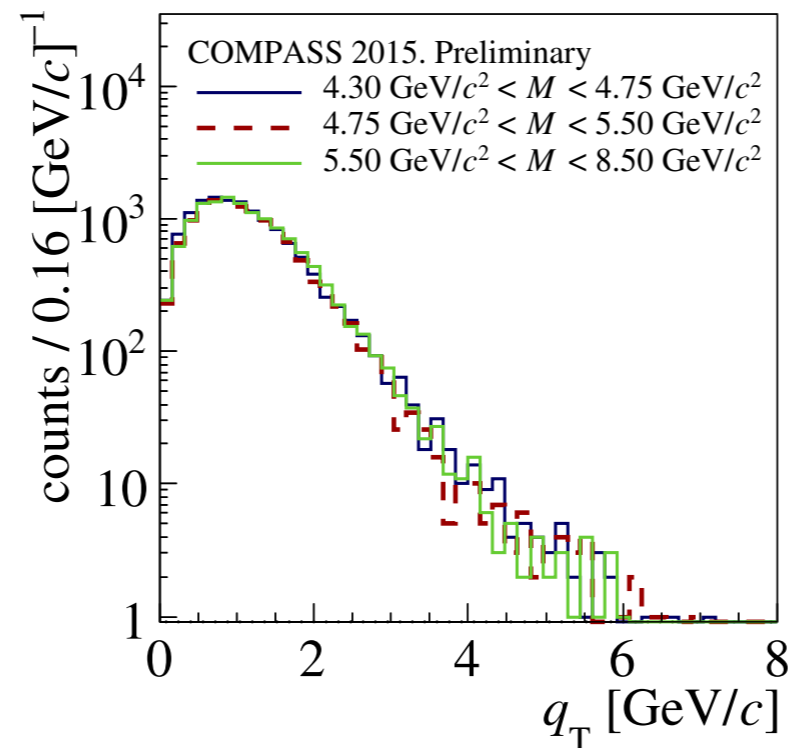
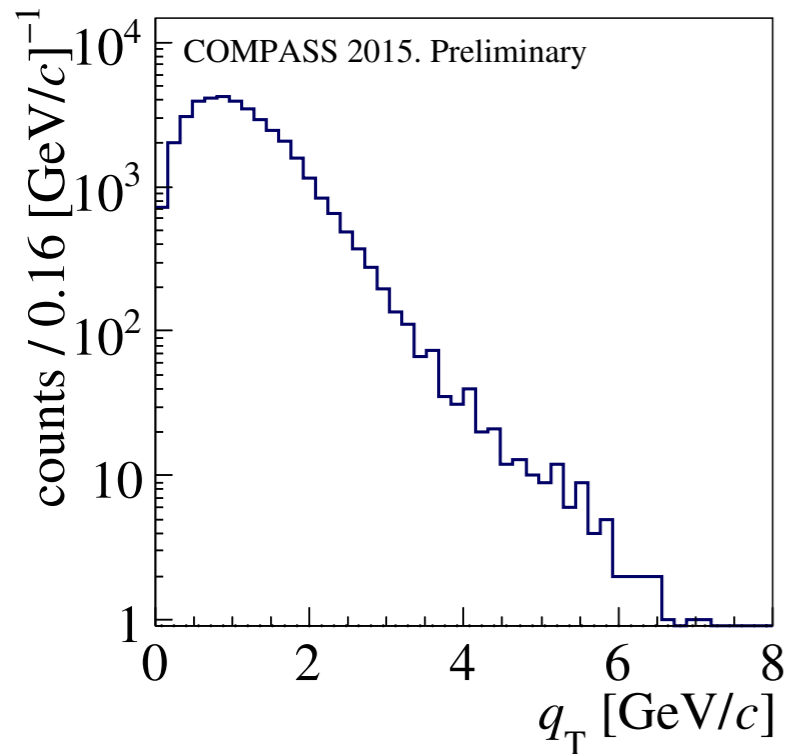


HM events are in the valence quark region

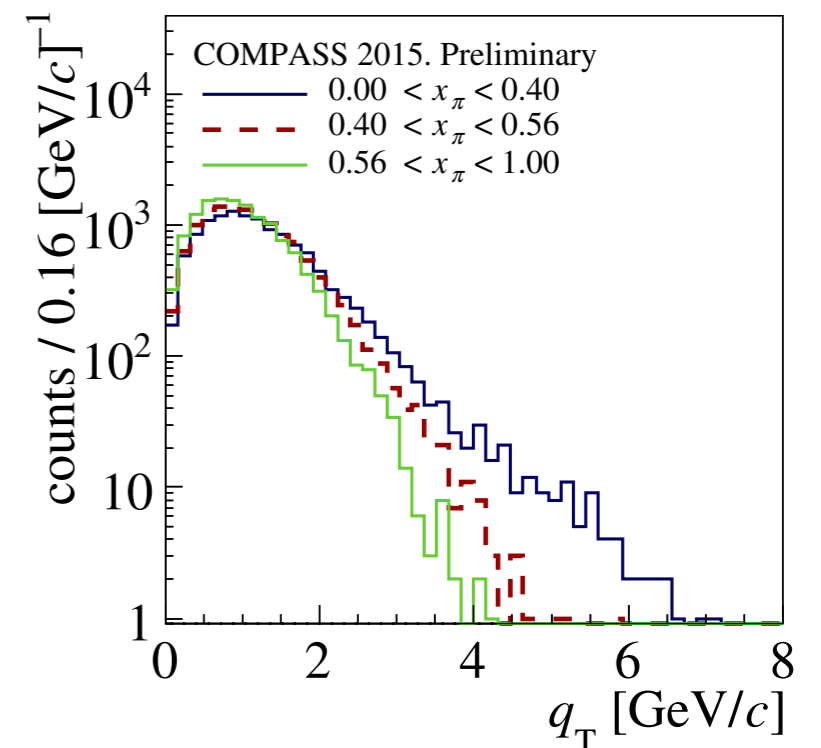




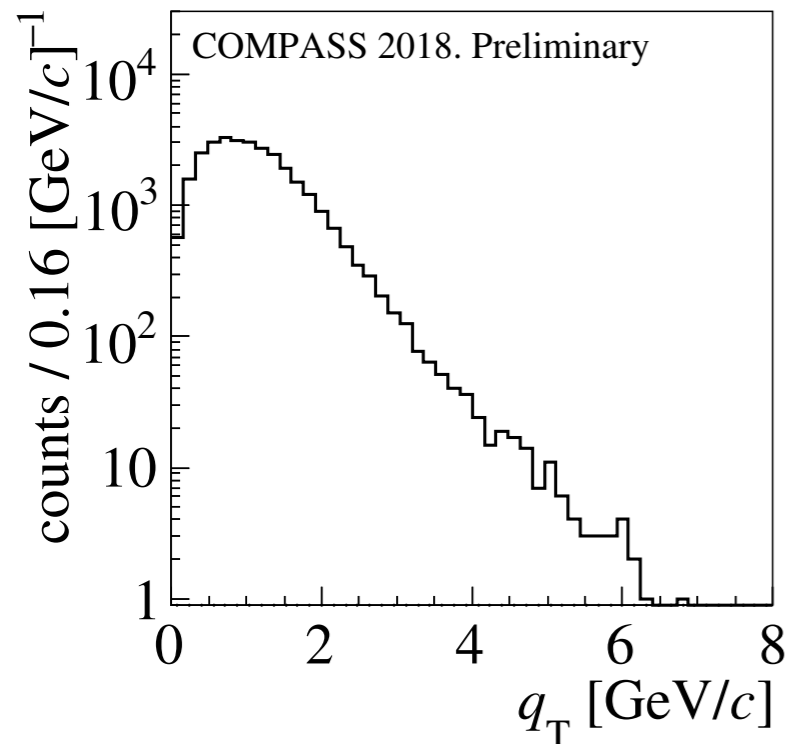
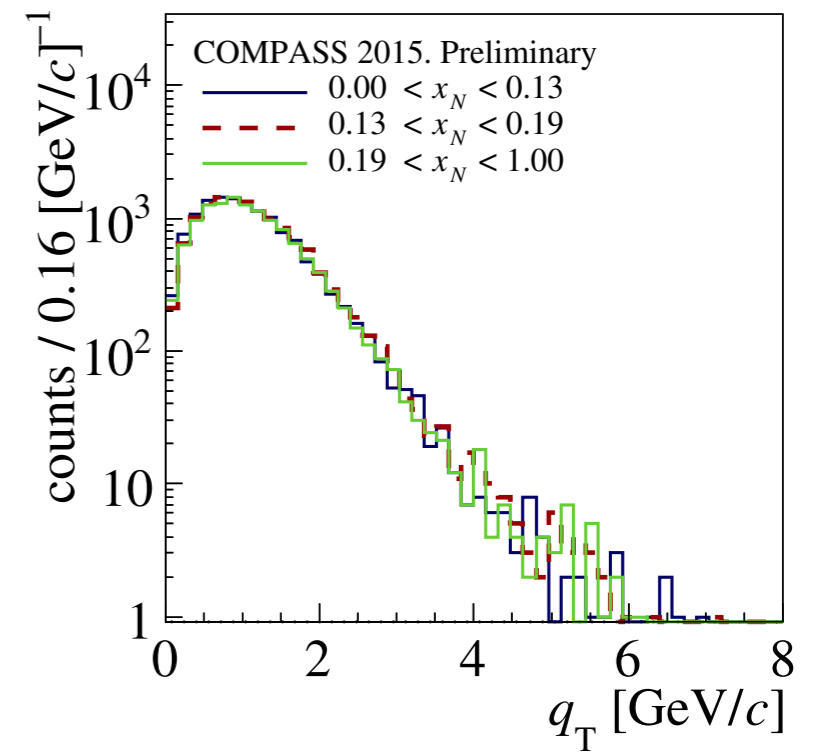
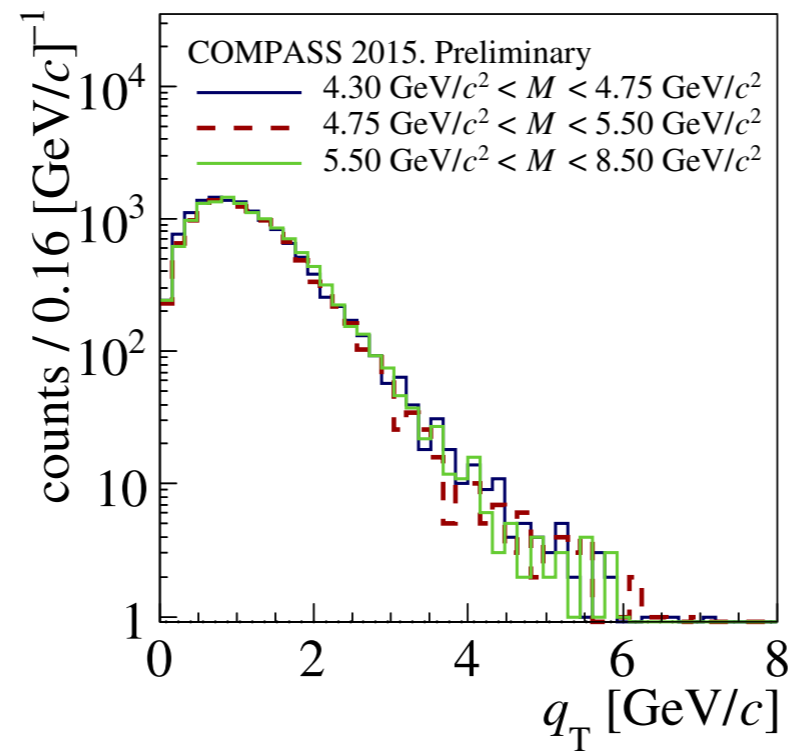
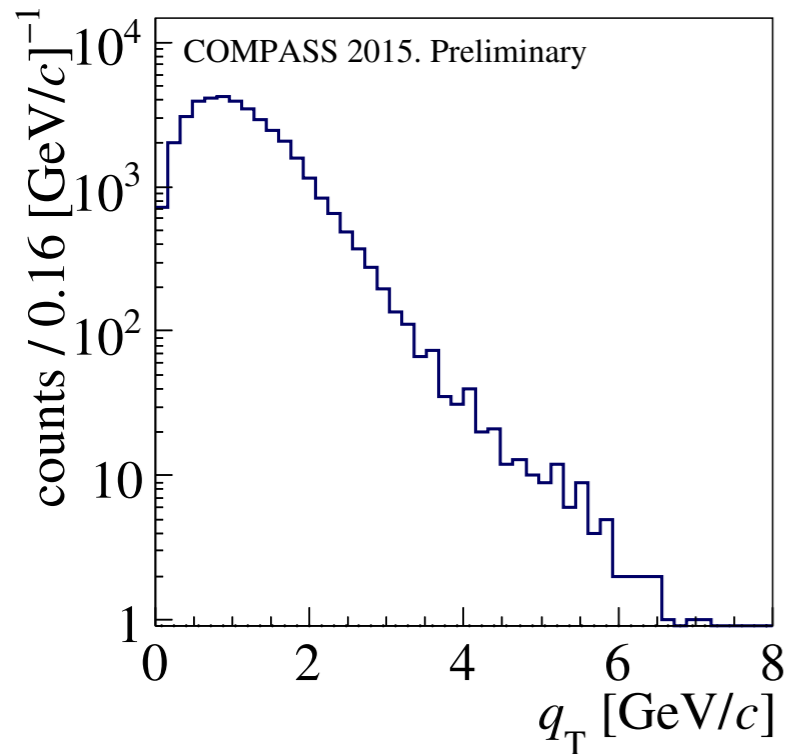
# Drell-Yan measurements at COMPASS



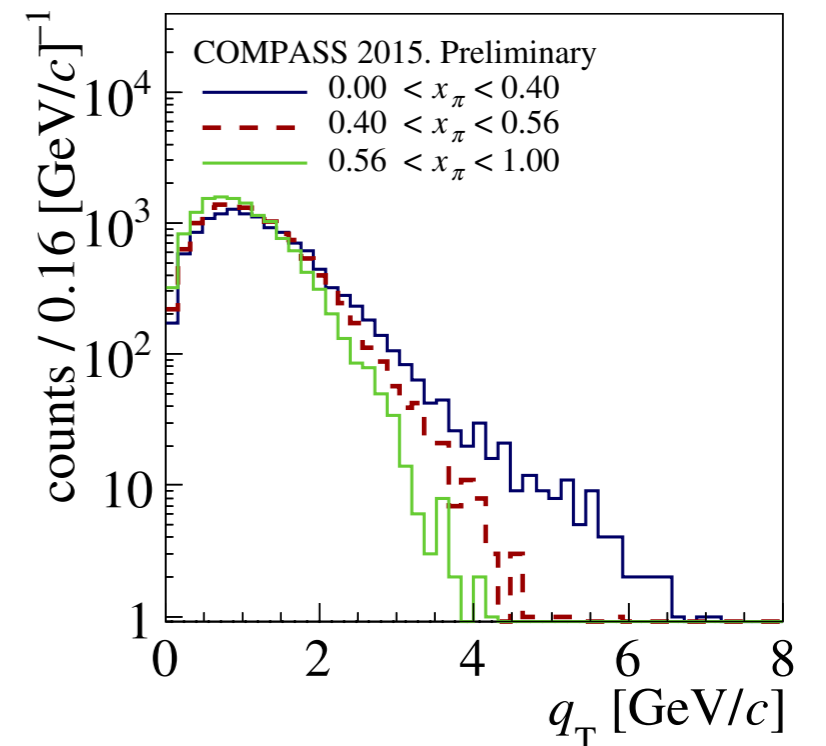
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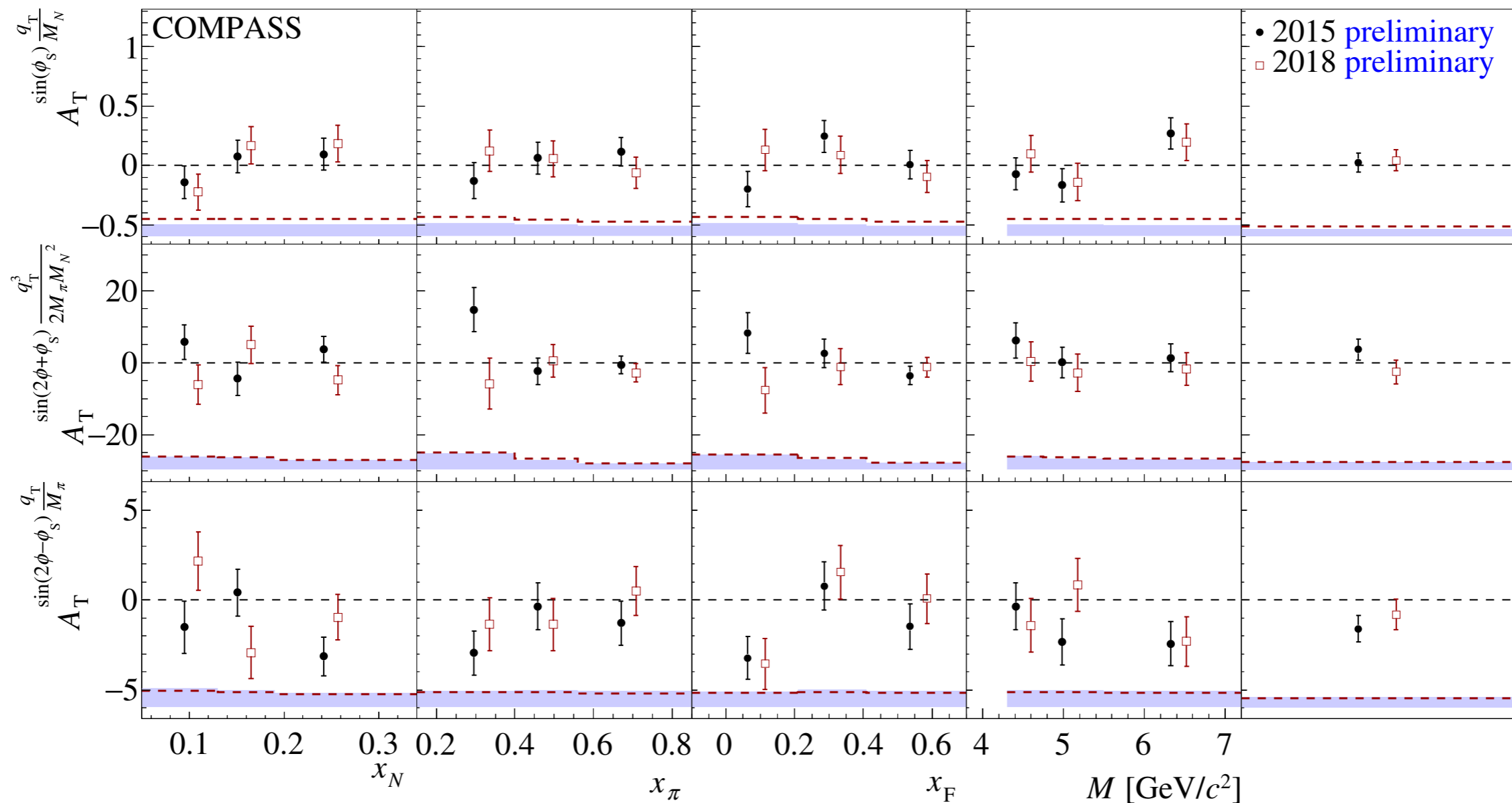
# Drell-Yan measurements at COMPASS



The  $q_T$  distribution of selected HM events is fully compatible in the two years (2015-2018).

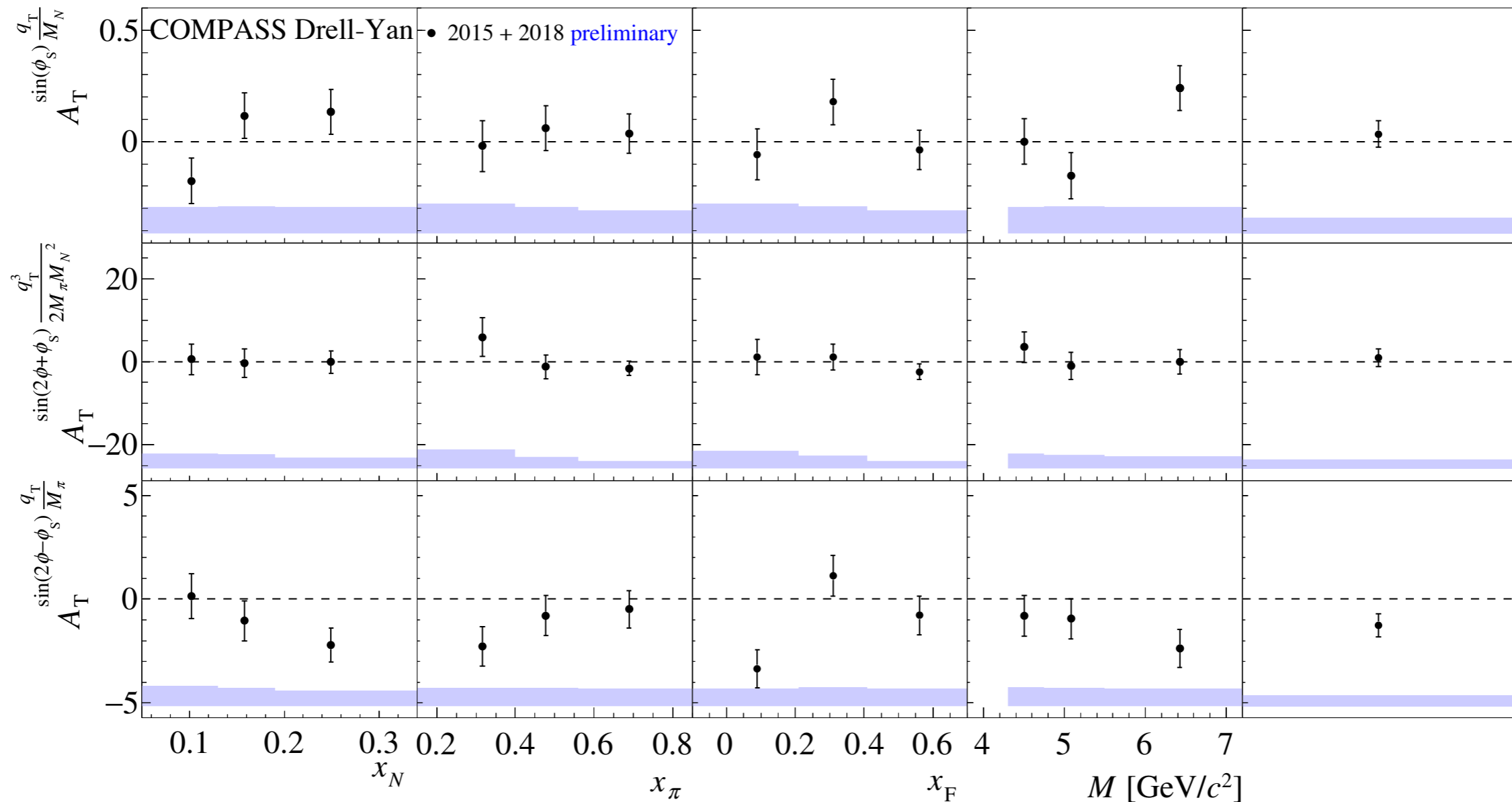


# $q_T$ weighted asymmetries: 2015 vs 2018



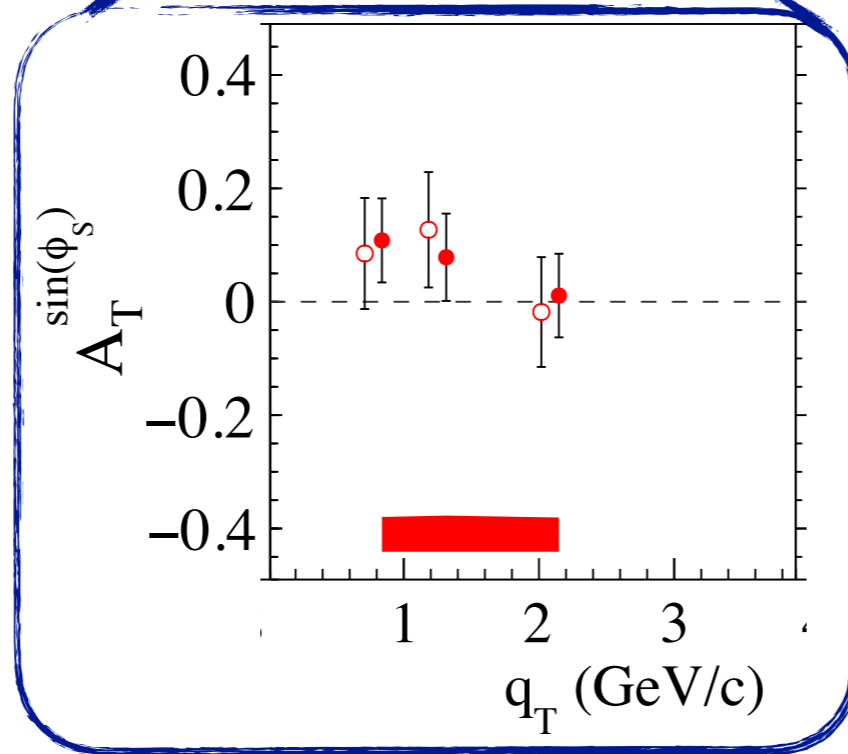
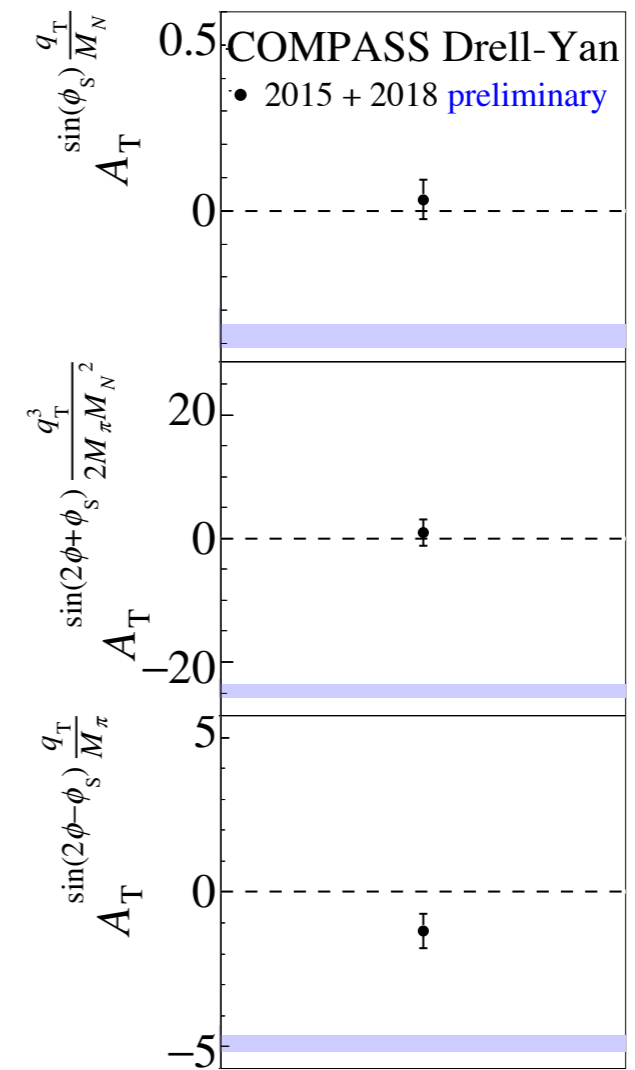
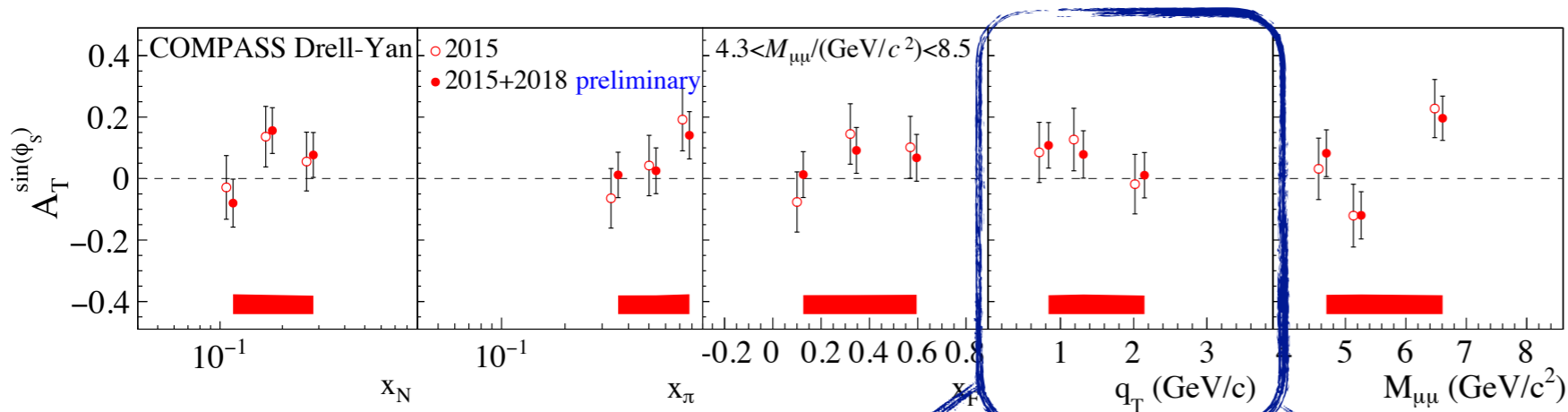
- The  $q_T$ -weighted asymmetries extracted in the **HM range** from the COMPASS Drell Yan data collected in 2015 and 2018 (**~50%**) ;
- Additional uncertainties of about 5 % from the polarization and 8 % from dilution factor calculation have to be added to the systematic errors in both the years.

# $q_T$ weighted asymmetries: 2015+2018



- The  $q_T$ -weighted asymmetries extracted in the **HM range** from the combined 2015-2018 Drell Yan data samples. For 2018, only **50%** of the data have been used.
- Additional uncertainties of about 5 % from the polarization and 8 % from dilution factor calculation have to be added to the systematic errors.

# $q_T$ weighted asymmetries: 2015+2018



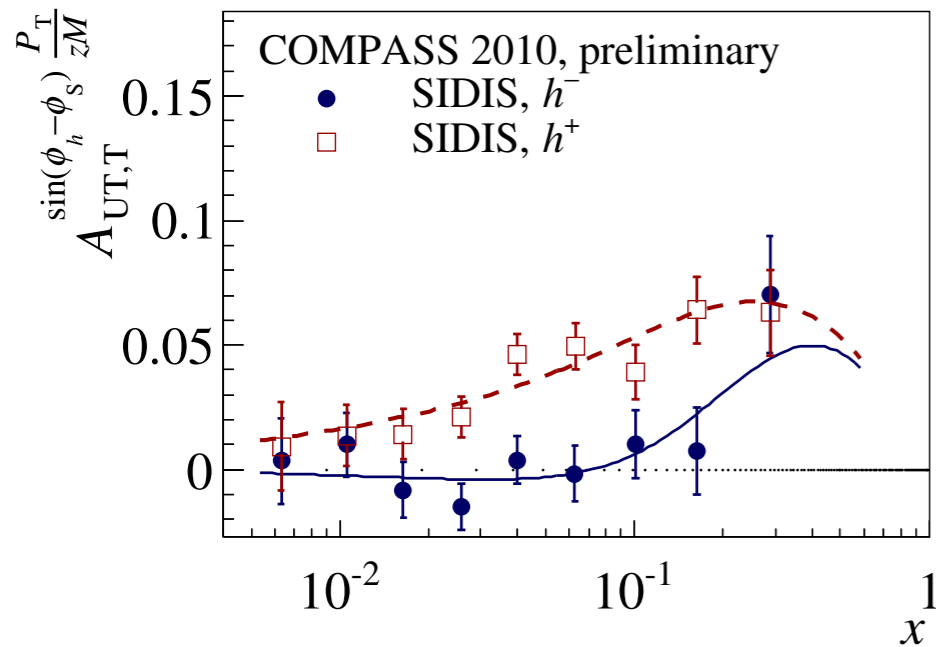
- Standard Sivers TSA smaller in the last  $q_T$  bin;

- The  $q_T$ -weighted asymmetries extracted from the combined 2015-2018 Drell Yan data samples. For **2018**, only **50%** of the data have been used.
- Additional uncertainties of about 5 % from the polarisation and 8 % from dilution factor calculation have to be added to the systematic errors.

# $p_T$ weighted asymmetries in SIDIS

COMPASS

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- COMPASS has also measured the  $p_T$  weighted TSAs in SIDIS;
- Alternative way to compare TMD PDFs from SIDIS and DY;

• Siverson TSA in SIDIS

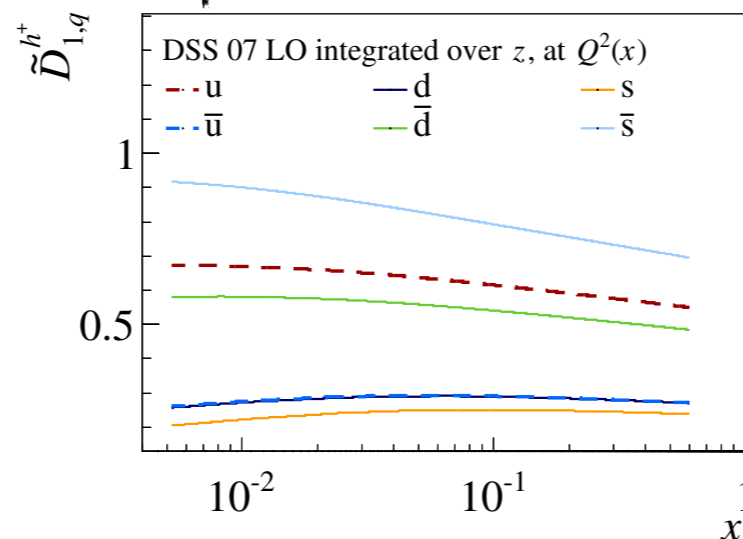
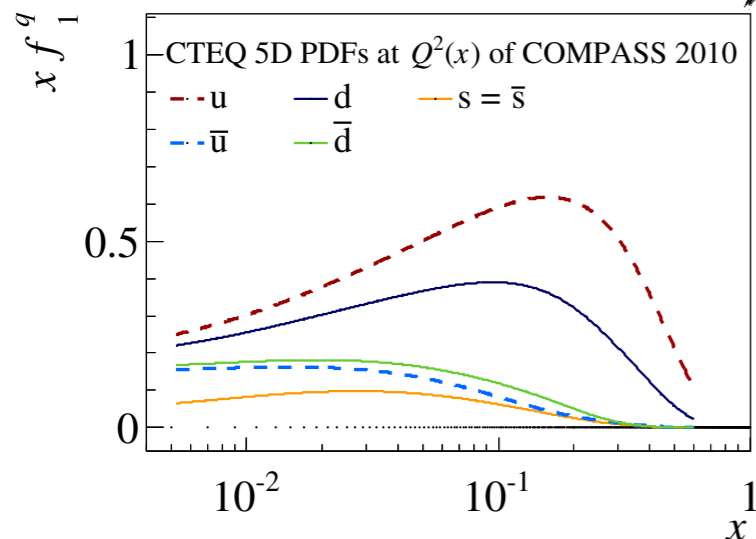
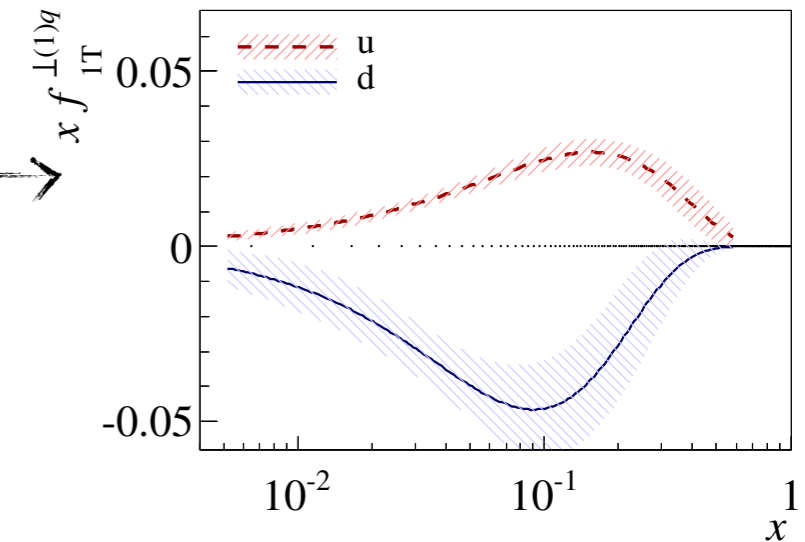
$$A_{UT}^{\sin(\phi_h - \phi_S)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

• Siverson wTSA in SIDIS

$$A_{UT}^{\sin(\phi_h - \phi_S)} \frac{P_T}{zM} \propto f_{1T}^{\perp q(1)} \times D_{1q}^h$$

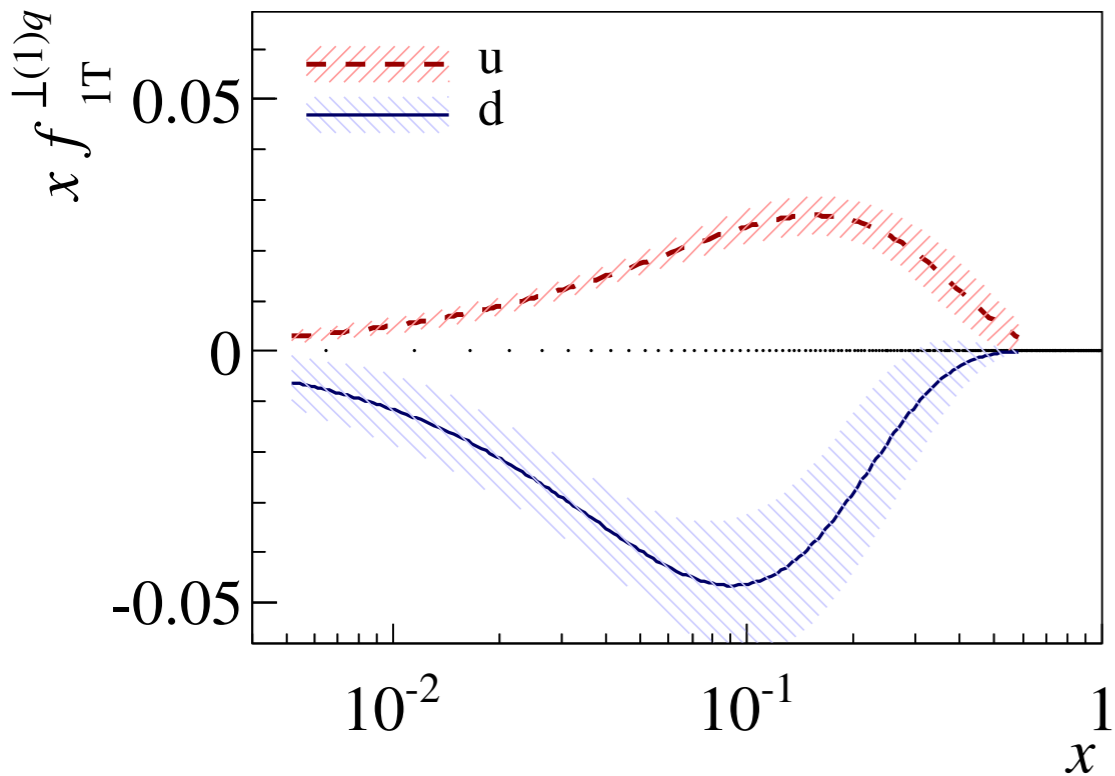
$$A_{UT}^{\sin(\phi_h - \phi_S)} \frac{P_T}{zM}(x, z) = 2 \frac{\sum_q e_q^2 f_{1T}^{\perp q(1)}(x) D_1^q(z)}{\sum_q e_q^2 f_1^q(x) D_1^q(z)}$$

$$x f_{1T}^{\perp(1)q}(x) = a_q x^{b_q} (1-x)^{c_q}$$



1<sup>st</sup>  $k_T^2$ -moment of the Siverson function at  $Q^2 = Q_{SIDIS}^2(x)$

# Weighted asymmetries: from SIDIS to DY



1<sup>st</sup>  $k_T^2$ -moment of the Sivers function from SIDIS data at  $Q^2 = Q_{SIDIS}^2(x)$

- Preliminary 2015 results, full data sample;
- Preliminary 2018 results, 50% of the sample;
- Ongoing analysis;
- What about the other asymmetries?

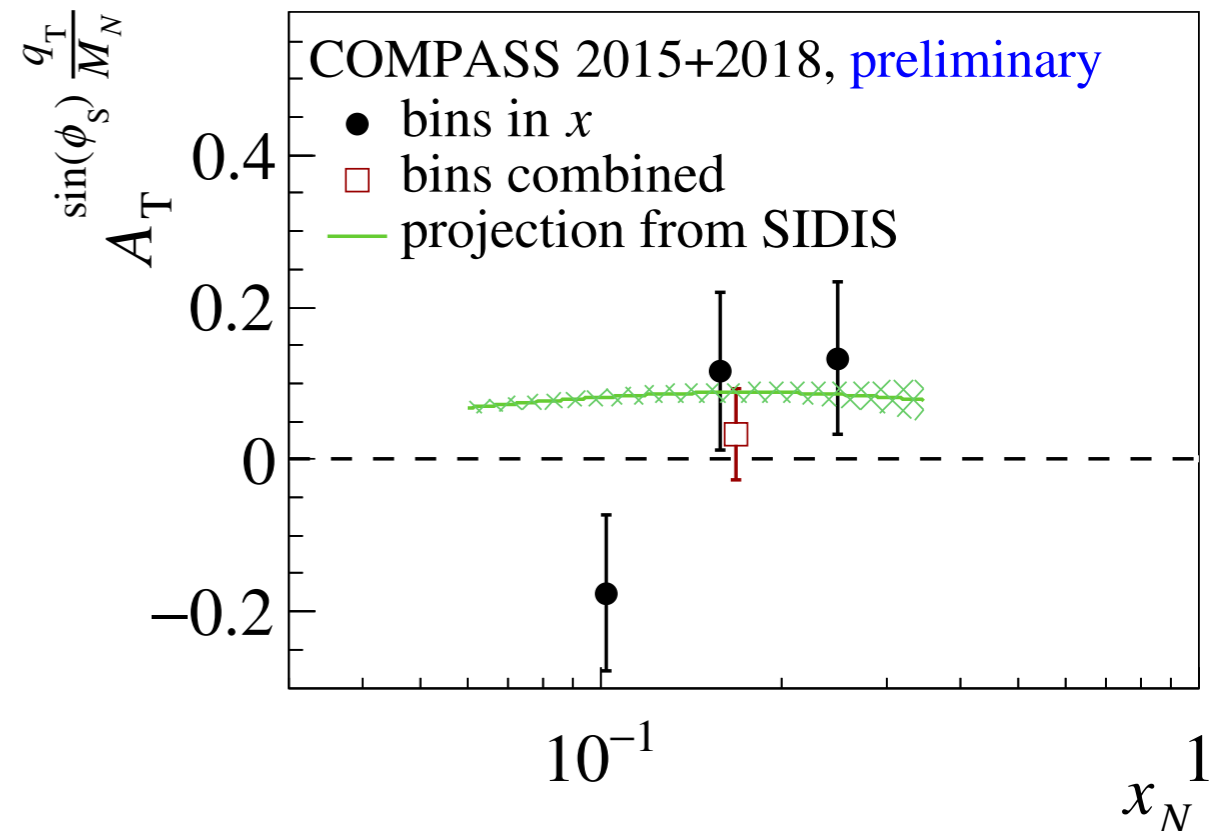
Assuming:

- $u$  quark dominance

$$A_T^{\sin \phi_S \frac{q_T}{M_N}} \sim \frac{f_{1T,p}^{\perp u(1)}}{f_{1,p}^u}$$

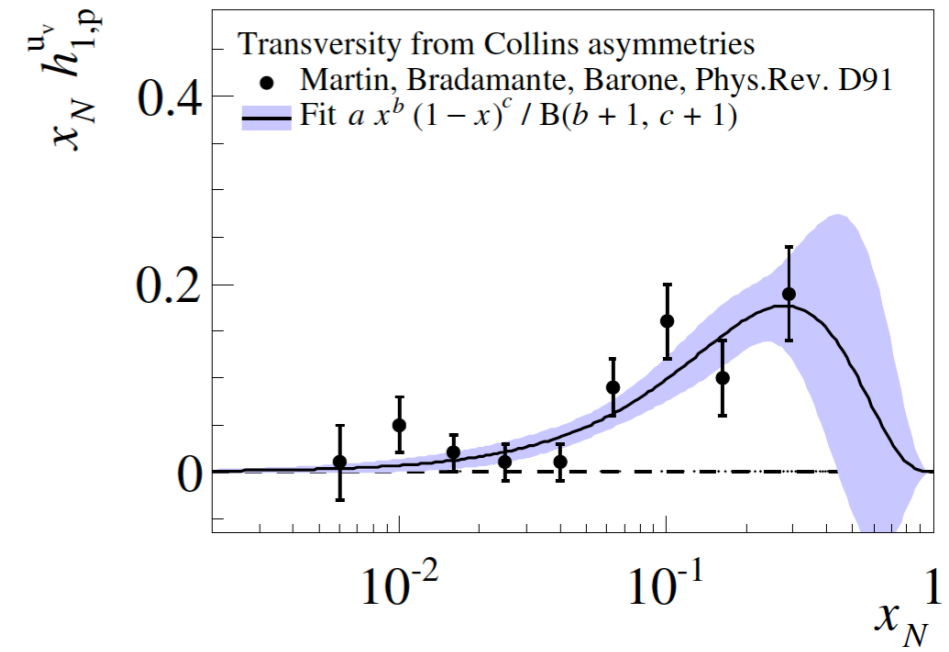
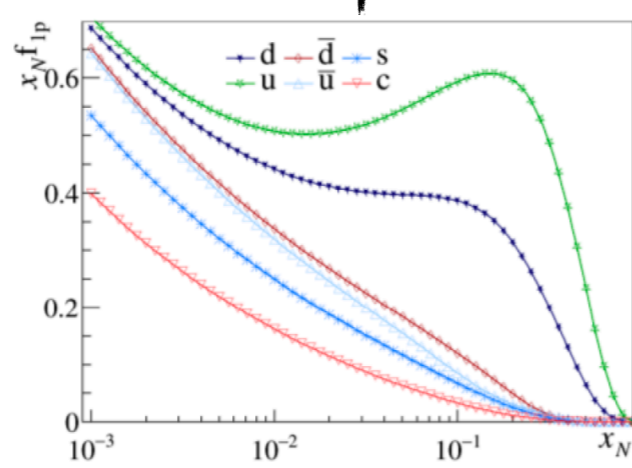
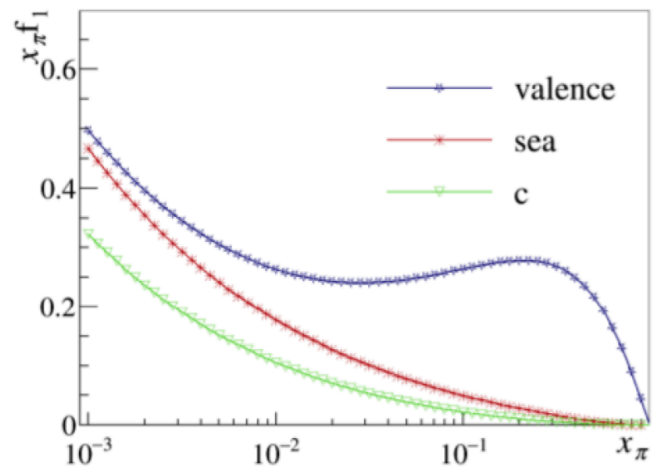
- No  $Q^2$  evolution for Sivers
- Sivers sign-change

$$f_{1T,p}^{\perp u}|_{SIDIS} = -f_{1T,p}^{\perp u}|_{DY}$$



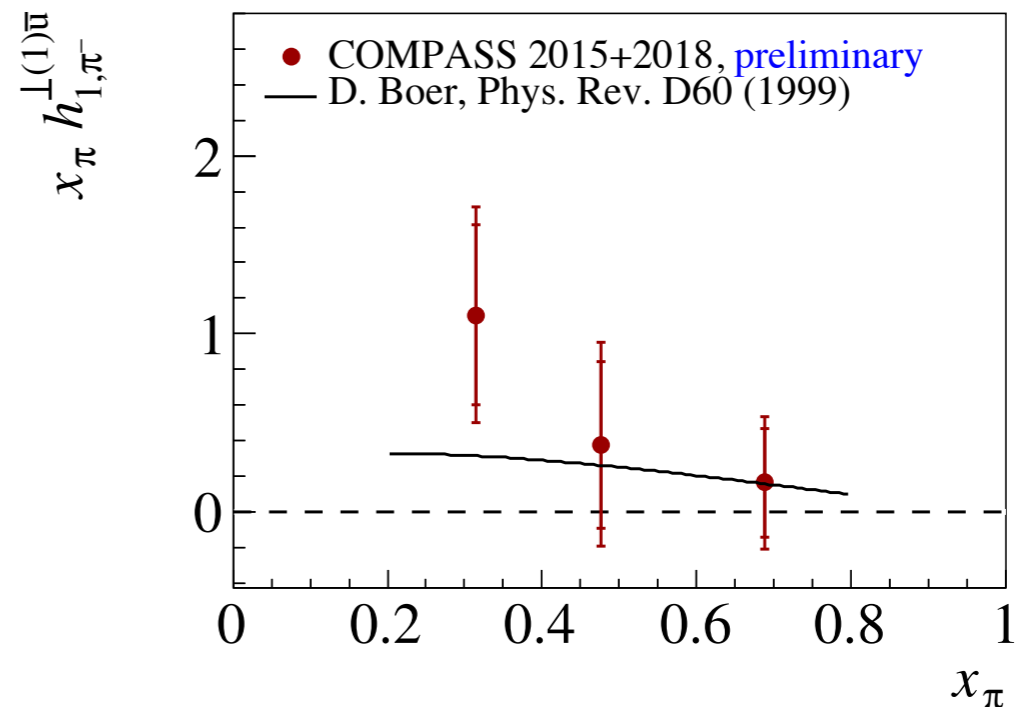
# First $k_T$ -moment of pion Boer-Mulders

$$A_T^{\sin(2\varphi - \varphi_S) \frac{q_T}{M_\pi}}(x_\pi, x_N) \approx -2 \frac{h_{1,\pi}^\perp(1) \bar{u}(x_\pi) h_{1,p}^u(x_N)}{f_1^{\bar{u}}(x_\pi) f_{1,p}^u(x_N)}$$



- Assuming:
- $u$  quark dominance
  - no  $Q^2$  evolution

- Different pion PDFs tested (GRV-Pi, JAM);
- Transversity from different asymmetries (Collins, Dihadron);





# Conclusions

- COMPASS is investigating the TMD PDFs in SIDIS and DY also using weighted asymmetries;
- $q_T$ -weighted asymmetries in Drell-Yan have been extracted from the full 2015 dataset and from  $\sim 50\%$  of 2018 data;
- 2018 analysis is ongoing, final results are expected to be released by autumn;



**Thank you for your  
attention!**

*This research is part of the Blue Waters sustained-petascale computing project, which is supported by the National Science Foundation (awards OCI-0725070 and ACI-1238993) and the state of Illinois. Blue Waters is a joint effort of the University of Illinois at Urbana-Champaign and its National Center for Supercomputing Applications. This work is also part of the "Mapping Proton Quark Structure using Petabytes of COMPASS Data" PRAC allocation supported by the National Science Foundation (award number OCI [1713684](#)).*

**BLUE WATERS**

# BACKUP SLIDES

# Extraction of qT-weighted asymmetries

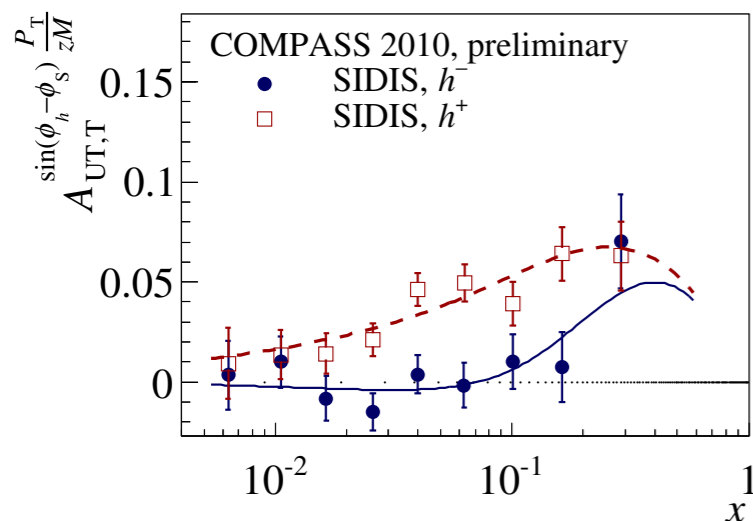
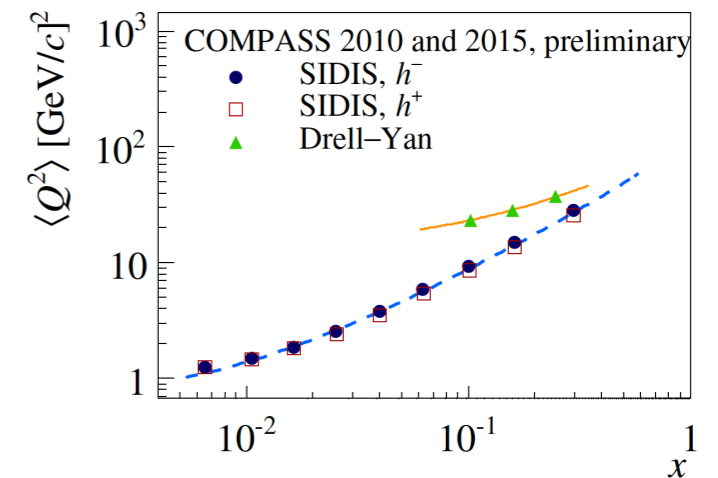
- SIDIS events as function of  $x$ , standard event selection,  $z > 0.2$ ;
- Neglecting the Sivers function of the sea quarks we can write

$$A_{\text{UT},\text{T},h^\pm}^{\sin(\phi_h - \phi_S)} \frac{P_{\text{T}}}{zM} (x, Q^2) = 2 \frac{\frac{4}{9} f_{1\text{T}}^{\perp(1)\text{u}}(x, Q^2) \tilde{D}_{1,\text{u}}^{h^\pm}(Q^2) + \frac{1}{9} f_{1\text{T}}^{\perp(1)\text{d}}(x, Q^2) \tilde{D}_{1,\text{d}}^{h^\pm}(Q^2)}{\sum_{q=\text{u,d,s},\bar{\text{u}},\bar{\text{d}},\bar{\text{s}}} e_q^2 f_1^q(x, Q^2) \tilde{D}_{1,q}^{h^\pm}(Q^2)},$$

- For the first  $k_{\text{T}}^2$ -moment of Sivers we use a parametrization

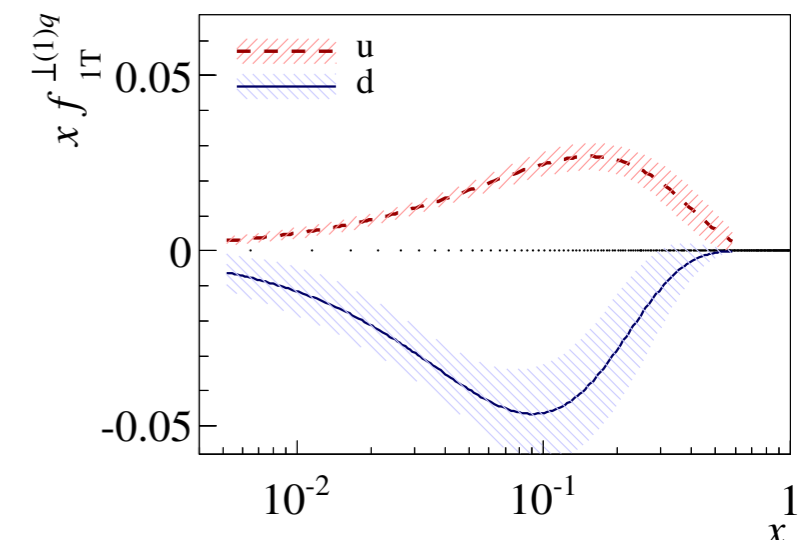
$$x f_{1\text{T}}^{\perp(1)q}(x) = a_q x^{b_q} (1-x)^{c_q}$$

- PDFs and FFs from global fit results  
[CTEQ, Eur.Phys.J. C12 (2000) 375]  
[D. de Florian et al., Phys.Rev. D75 (2007) 114010],  
collinear evolution with  $Q^2 = \langle Q^2 \rangle (x)$ .



- Asymmetries are simultaneously fitted for  $h^+$  and  $h^-$

- Error bands  $1 \sigma$ , only statistical error of the data and the fit



# 1st moment of the pion BM: assumptions

$$\begin{aligned}
 A_T^{\sin(2\phi - \phi_S) \frac{q_T}{M_\pi}}(x_\pi, x_N) &= -2 \frac{\sum_q e_q^2 [h_{1,\pi}^{\perp(1)\bar{q}}(x_\pi) h_{1,p}^q(x_N) + (q \leftrightarrow \bar{q})]}{\sum_q e_q^2 [f_{1,\pi}^{\bar{q}}(x_\pi) f_{1,p}^q(x_N) + (q \leftrightarrow \bar{q})]} \\
 &\approx -2 \frac{e_u^2 h_{1,\pi}^{\perp(1)\bar{u}}(x_\pi) h_{1,p}^u(x_N)}{\sum_{q=u,d,s} e_q^2 [f_{1,\pi}^{\bar{q}}(x_\pi) f_{1,p}^q(x_N) + (q \leftrightarrow \bar{q})]} \\
 &\approx -2 \frac{h_{1,\pi}^{\perp(1)\bar{u}}(x_\pi) h_{1,p}^u(x_N)}{f_{1,\pi}^{\bar{u}}(x_\pi) f_{1,p}^u(x_N)},
 \end{aligned}$$

- Transversity: we utilize a point-by-point extraction from COMPASS data. The  $Q^2$  of the transversity obtained in this way is different from point to point. It raises with  $x_N$  and in our range of 0.1 : 0.3 it lies between 8 and 23 (GeV/c)<sup>2</sup>
- We have neglected the difference with respect to the Drell-Yan kinematics.
- Two set of transversity from the article:
  - From the Collins asymmetries using the TMD formalism with the Gaussian assumption;
  - Based on dihadron asymmetries, which can be described in collinear formalism;

$$h_{1,p}^u(x_N) = a \frac{x_N^b (1 - x_N)^c}{B(b + 1, c + 1)}$$

Assumptions:

- Boer Mulders and Transversity of sea quarks are zero. For transversely what's available is indeed compatible with 0. For BM is a full assumption.
- We consider only u, d and s quarks in the denominator.

If we go further and we neglect also the d and s, we get the last formula (Differences <= 4%)

Final errors take into account only the statistical uncertainties of transversity PDF and the uncertainty of the weighted asymmetry.