



From Pions to Kaons - Hadron Spectroscopy from COMPASS to AMBER

Mathias Wagner
on behalf of the COMPASS collaboration
and COMPASS++/AMBER

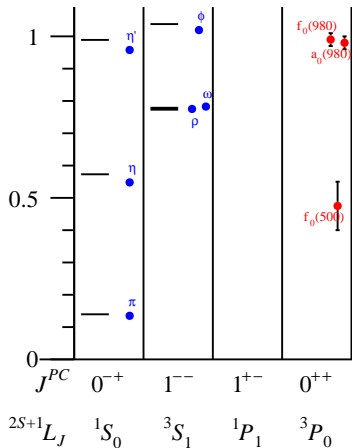
HISKP, Bonn University

June 25, 2019
at the IWHSS19 Aveiro

supported by BMBF

- Motivation
- The COMPASS experiment
- 3π PWA
- Freed-isobar analysis
- Exotic $\pi_1(1600)$
- RF-separated kaon beam
- Conclusion & outlook

Why Hadron Spectroscopy?

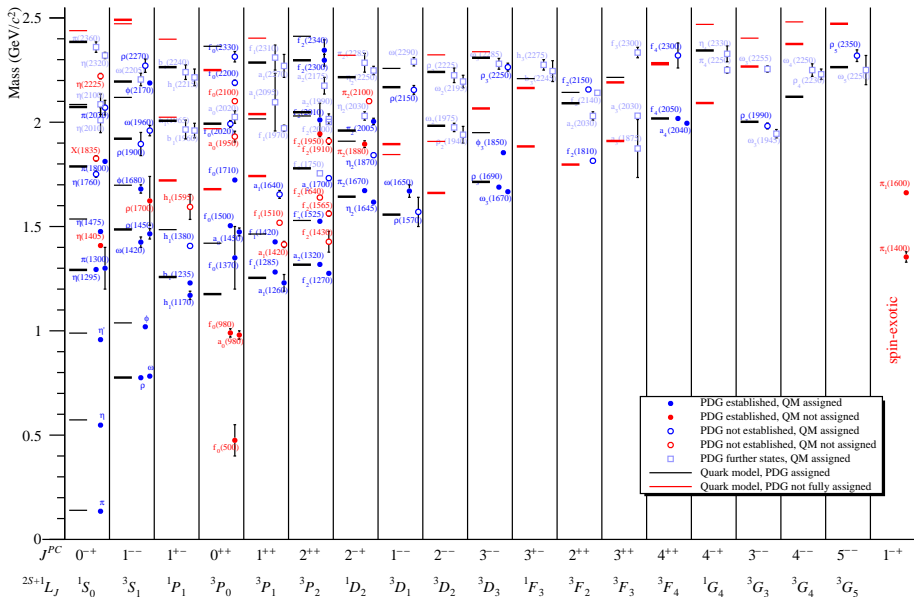


— QM pred., PDG assigned

● QM assigned, ● QM not assigned

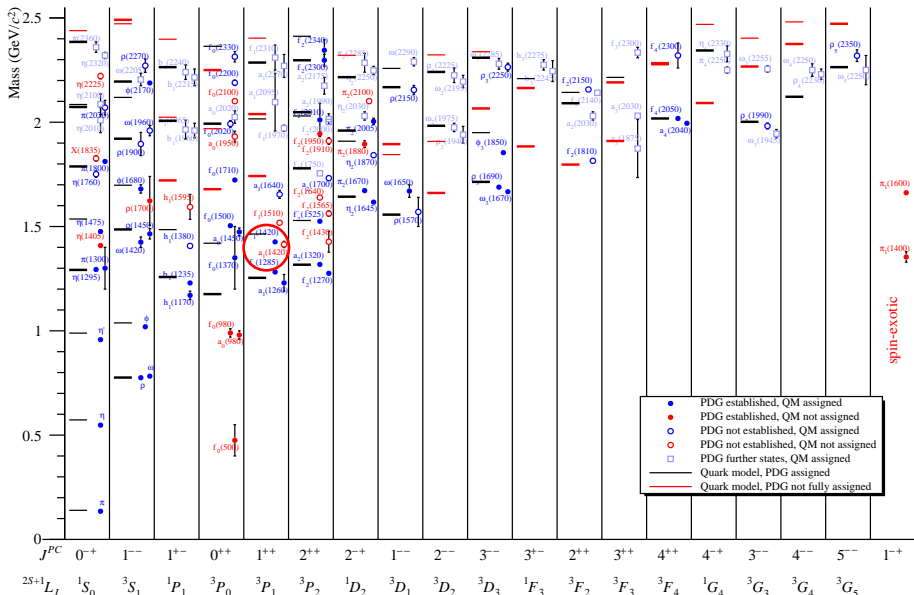
Motivation

[To be published in Progress in Particle and Nuclear Physics]



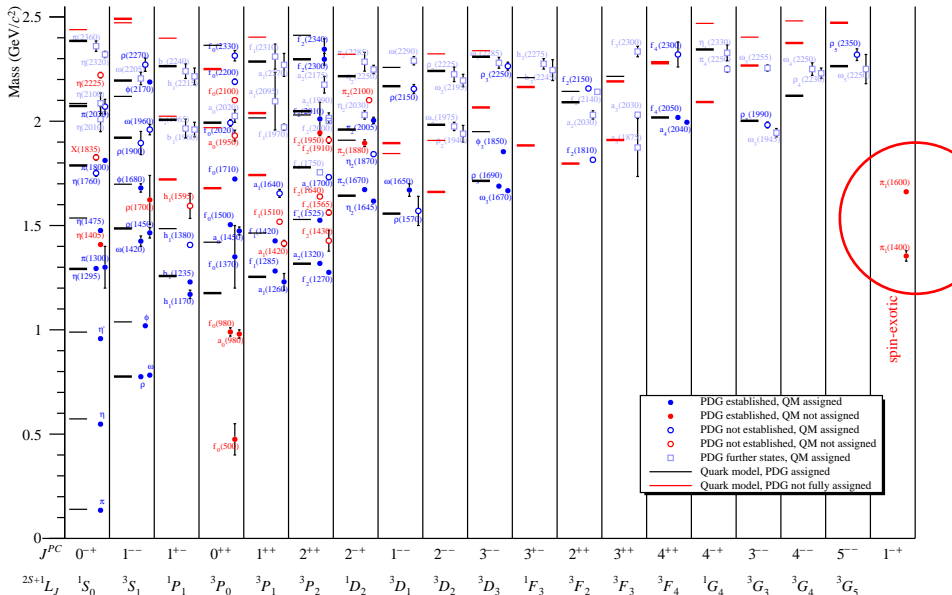
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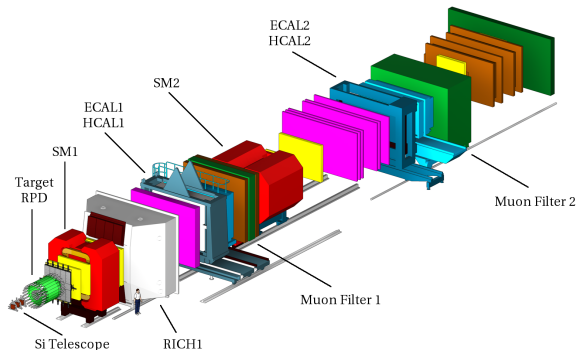
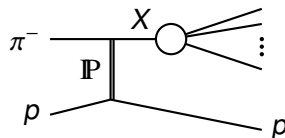


The COMPASS Experiment

The COMPASS Experiment

- Secondary hadron beam, mostly π^- ($\sim 97\%$)

- $E_{\text{beam}} = 190 \text{ GeV}$
- Liquid hydrogen target (40 cm)
- $\pi^- + p \rightarrow \pi^- + \pi^- + \pi^+ + p$
- $\pi^- + p \rightarrow \eta^{(\prime)} + \pi^- + p$

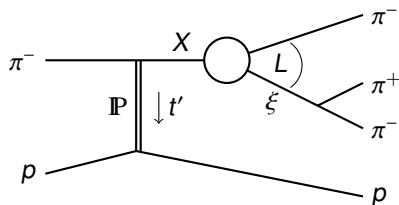


[COMPASS, NIM A779, 69-115 (2015)]

COMPASS

3π PWA

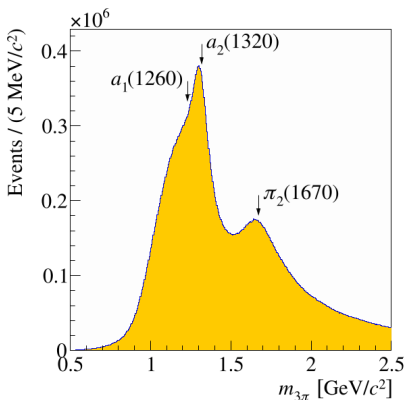
- Isobar model: $X^- \rightarrow \pi^- + \xi^0 \rightarrow \pi^- + \pi^+ + \pi^-$
- Data binned in 100 $m_{3\pi}$ and 11 $t' = |t| - |t|_{\min}$ slices
- PWA with 88 waves [COMPASS, PRD **95**, 032004 (2017)]



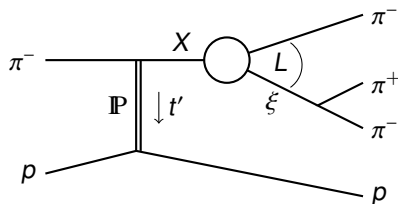
\mathbb{P} : Pomeron

X : Resonance with J^{PC}

ξ : Isobar



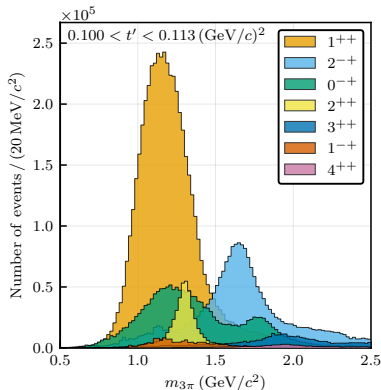
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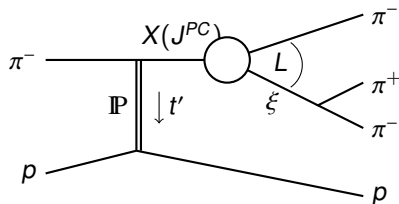


[To be published in Progress in Particle and Nuclear Physics]

Naming scheme:

$$I^G(J^{PC})M^\varepsilon \xi \pi L$$

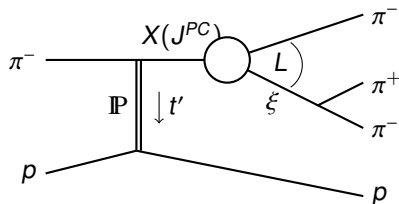
- $I^G = 1^-$
- $J \leq 6, M \in \{0, 1, 2\}$
- $PC = ++$ for $J \geq 1$,
 $PC = -+$ for $J \geq 0$
- 80 waves $\varepsilon = +$
- $L \leq 6$
- Isobars ξ :
 $(\pi\pi)_S, \rho(770), f_0(980),$
 $f_2(1270), f_0(1500), \rho_3(1690)$
fixed shape (Breit-Wigner)



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$1^-(1^{++})1^+ \rho\pi P$ -wave!

We have access to exotic mesons

- Maximize the likelihood function:

$$\mathcal{L} = \underbrace{\frac{N_e^N}{N!} \exp(-N_e)}_{\text{Prob. for } N \text{ events}} \prod_{k=1}^N \underbrace{\frac{I(\tau_k)}{N_e}}_{\text{Prob. for event } k},$$

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$$I(\tau) = |A(\tau)|^2 = \left| \sum_{JMLS} A_{LS}^{JM}(\tau) \right|^2$$

with the amplitude A separated in partial waves ($J^{PC} M^E \xi \pi L$):

$$A_{LS}^{JM}(\tau) = \underbrace{F_{LS}^{JM}(s_0, m_{3\pi}^2, t)}_{\text{const per } (m_{3\pi}, t')\text{-bin}} \cdot \Psi_{LS}^{JM}(m_{2\pi}^2, \Omega_X, \Omega_\xi)$$

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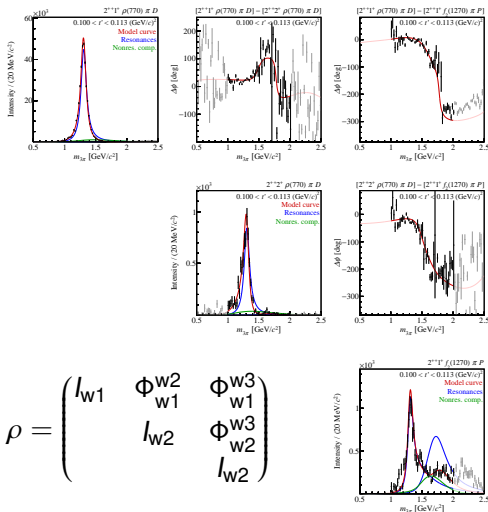
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- Extract the spin density matrix

$$\rho_{(LS)(L'S')}^{(JM)(J'M')} := F_{LS}^{JM} (F_{L'S'}^{J'M'})^* = \begin{pmatrix} I_{w1} & \Phi_{w1}^{w2} & \dots \\ (\Phi_{w1}^{w2})^* & I_{w2} & \dots \\ \dots & \dots & \dots \end{pmatrix}$$

Example: $a_2(1320)$

- $2^{++}1^+\rho\pi D$
- $2^{++}2^+\rho\pi D$
- $2^{++}1^+f_2(1270)\pi P$



$$\rho = \begin{pmatrix} I_{W1} & \Phi_{W1}^{W2} & \Phi_{W1}^{W3} \\ & I_{W2} & \Phi_{W2}^{W3} \\ & & I_{W2} \end{pmatrix}$$

[COMPASS, PRD **98** (2018) 092003]

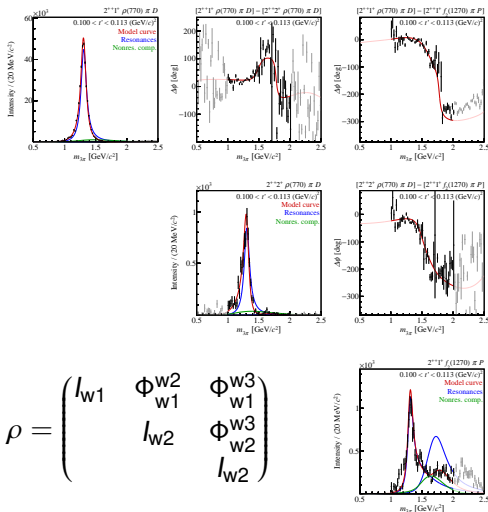
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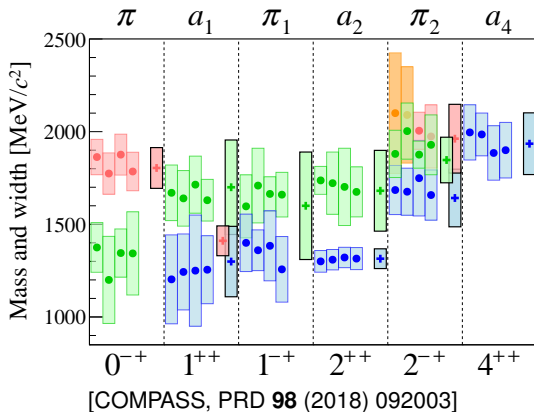
Parametrized by relativistic Breit-Wigner

$$\frac{m\Gamma}{m^2 - m_{3\pi}^2 - im\Gamma_{\text{tot}}(m_{3\pi})}$$

Good approximation if isolated resonance



[COMPASS, PRD **98** (2018) 092003]

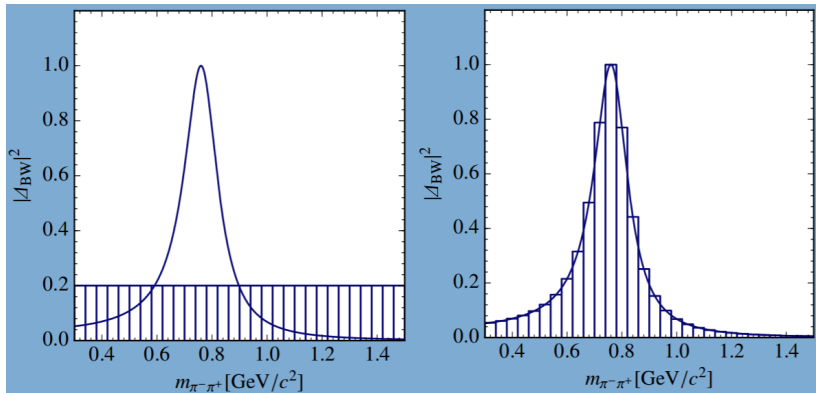


- previous measurements
- + COMPASS
- decay width
- color: different excitations

COMPASS

Freed-Isobar Analysis

- Not only slices in $m_{3\pi}$ and t' , but also in $m_{2\pi}$



[F. Krinner]

- Not only slices in $m_{3\pi}$ and t' , but also in $m_{2\pi}$
- Keep F and f as free complex fit parameters

$$A_{LS}^{JM}(\tau) = \underbrace{F_{LS}^{JM}(s_0, m_{3\pi}^2, t) \cdot f_S^\xi(m_{2\pi}^2)}_{\text{fixed per } (m_{3\pi}, t', m_{2\pi})\text{-bin}} Z_{LS}^{JM}(\Omega_{GJ}, \Omega_H)$$

- Freed partial waves include $[\pi\pi]_{0^{++}}$, $[\pi\pi]_{1^{--}}$, $[\pi\pi]_{2^{++}}$

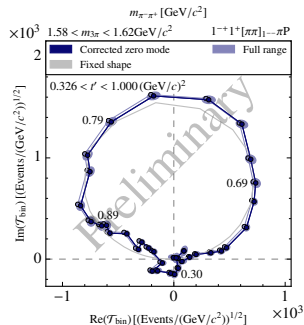
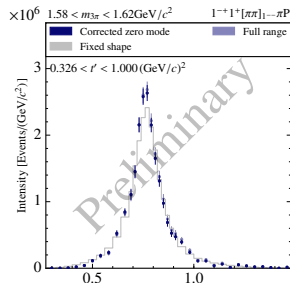
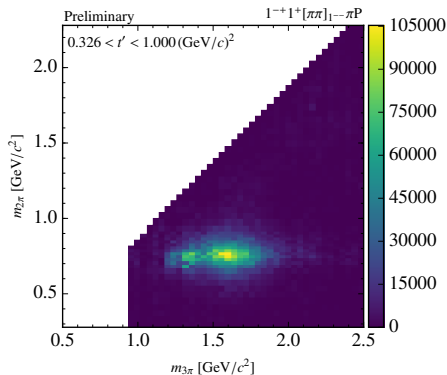
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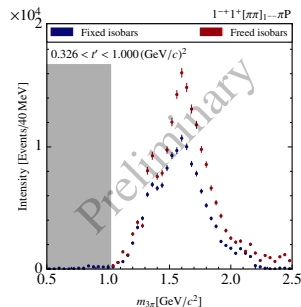
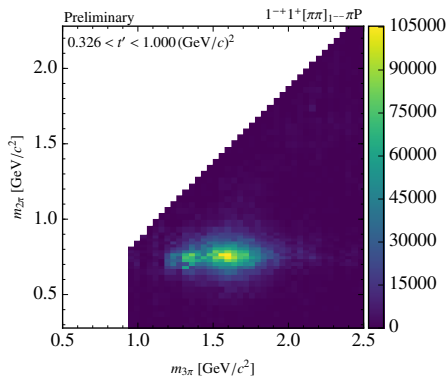
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What do we gain from this?

- Less model dependence during the PWA
- Enables to fit 2π spectrum
- Study rescattering effects \rightarrow collab. with C. Hanhart, B. Kubis





Signal not an artifact of fixed isobar shape!

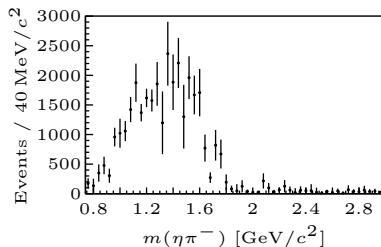
COMPASS

Exotic $\pi_1(1600)$

Two pseudo scalars \leadsto waves with odd L are spin-exotic

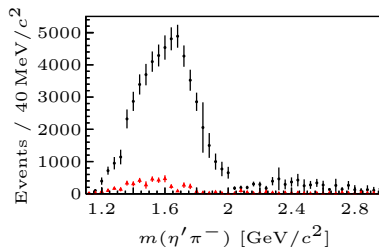
The π_1 is a puzzle!

$\eta\pi$ P-wave



@1400?

$\eta'\pi$ P-wave



@1600?

But: Fit not stable, strongly model dependent!

[COMPASS, PLB 740 (2015) 303]

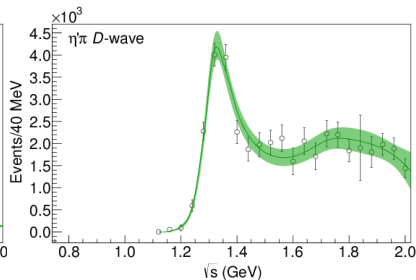
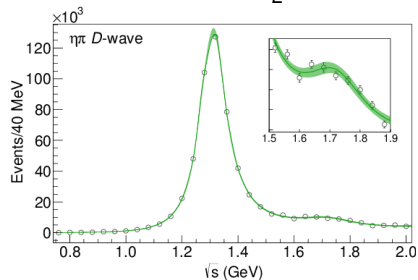
Improvement over simple Breit-Wigner fit:

- Unitary model (K -matrix approach)
- $\eta\pi$ and $\eta'\pi$ coupled-channel (N/D formalism)
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D -wave with a_2 and a_2'

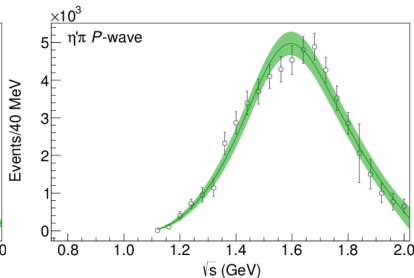
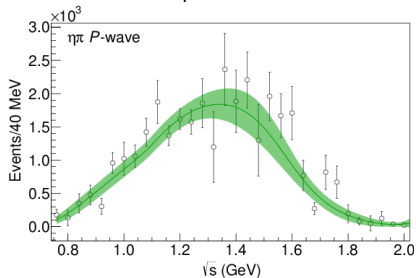


[JPAC, PRL 122, 042002 (2019)]

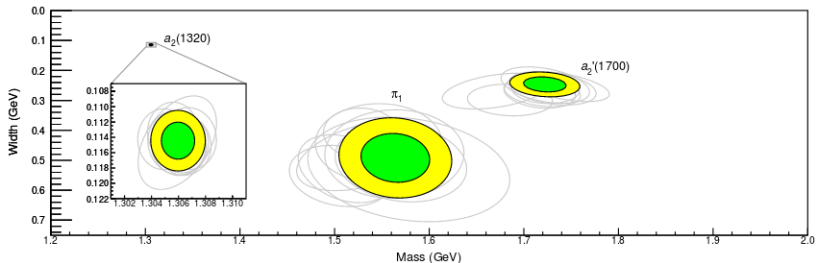
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P -wave with π_1



[JPAC, PRL 122, 042002 (2019)]

**Result:**

[JPAC, PRL 122, 042002 (2019)]

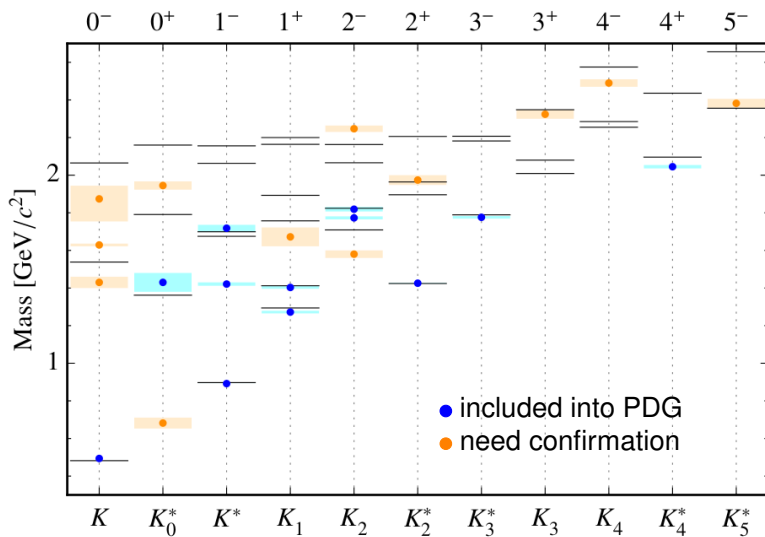
- 2 poles in D -wave: a_2 and a_2'
- Only 1 pole in P -wave: π_1 !

Poles	Mass (MeV)	Width (MeV)
$a_2(1320)$	$1306.0 \pm 0.8 \pm 1.3$	$114.4 \pm 1.6 \pm 0.0$
$a_2'(1700)$	$1722 \pm 15 \pm 67$	$247 \pm 17 \pm 63$
π_1	$1564 \pm 24 \pm 86$	$492 \pm 54 \pm 102$

COMPASS

Meson Spectrum of Excited Kaons

Meson Spectrum of Excited K



COMPASS Lol [arXiv:1808.00848v6, 25 Jan 2019]

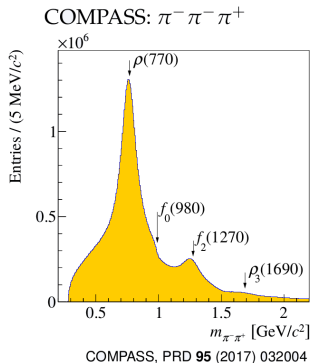
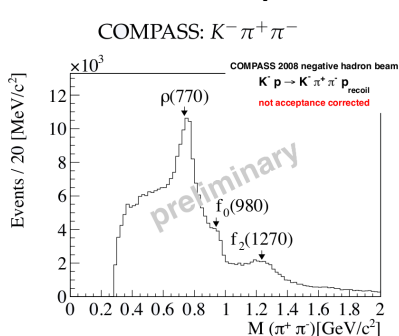
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- Only 2.5 % K^- fraction in beam
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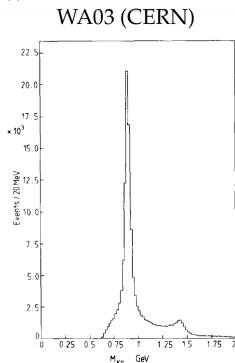
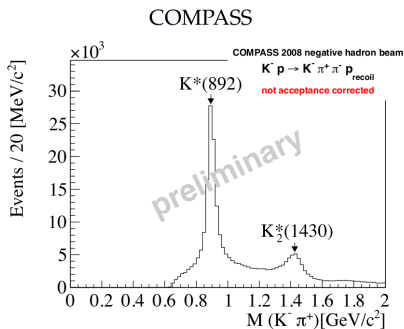
Comparison $\pi\pi$ for $K \leftrightarrow \pi$:



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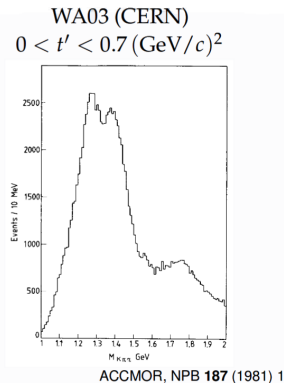
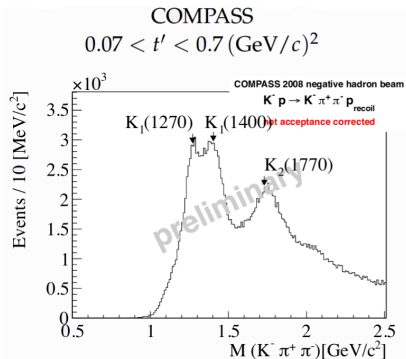


ACCMOR, NPB 187 (1981) 1

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Comparison $K\pi\pi$:



COMPASS++/AMBER

Apparatus for Meson and Baryon
Experimental Research

Improve our knowledge
of the spectrum
of excited Kaons

What do we need?

- Clean, high-intensity K beam
- 10x more statistics than currently available

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- PWA in (m, t) -bins
- Freed-isobar analysis \rightarrow study $K\pi$
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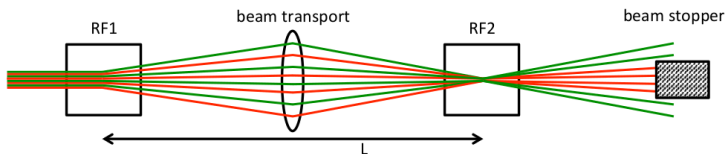
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How can we achieve this?

COMPASS++/AMBER

RF-Separated Kaon Beam

- First employed at CERN in the 1960s

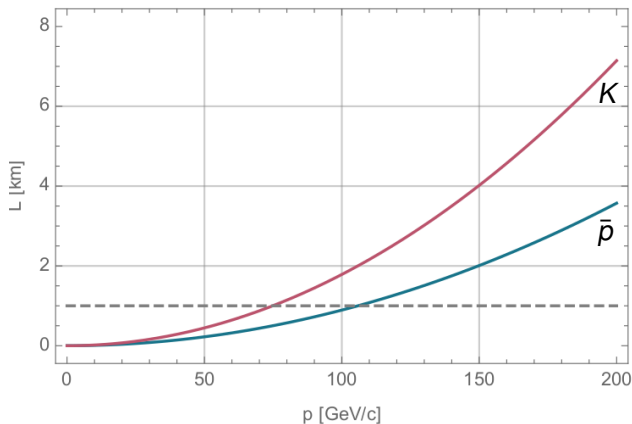


COMPASS Lol [arXiv:1808.00848v6, 25 Jan 2019]

- Two dipole RF-cavities at frequency f and phase φ
- Different particles at same beam momentum have phase difference:

$$\Delta\Phi = 2\pi \frac{Lf}{c} \left(\frac{m_1^2 - m_2^2}{2p^2} \right)$$

$$\Delta\Phi_{p\pi} = 2\pi \quad \Rightarrow \quad \Delta\Phi_{K\pi} \approx \pi/2$$



COMPASS Lol [arXiv:1808.00848v6, 25 Jan 2019]

Beam line limit $L = 1.1$ km yields $p_{\max} \sim 75$ GeV/c (for fixed f)
 \leadsto high enough forward boost, recoil proton angle sufficiently large

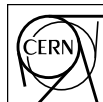
Pions:

- 3π PWA improved mass and width parameters
- Freed-isobar analysis further removes model dependence from PWA, independent of the isobar shape
- Enables fits to 2π subsystems, rescattering effects
- Coupled-channel analysis of $\eta^{(\prime)}\pi$ yields precise $\pi_1(1600)$ pole position \Rightarrow Puzzle solved!

Kaons:

- Limited data set of $K^- + p \rightarrow K^- \pi^+ \pi^- + p_{\text{recoil}}$

EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH



CERN-SPSC-2019-003
SPSC-I-250
January 28, 2019

Letter of Intent:**A New QCD facility at the M2 beam line of the CERN SPS*****COMPASS++[†]/AMBER[‡]**

*email: NQF-M2@cern.ch

[†]Common Muon Proton Apparatus for Structure and Spectroscopy

[‡]Apparatus for Meson and Baryon Experimental Research

[arXiv:1808.00848v6, 25 Jan 2019]

RF-separated K beam for spectroscopy

- Only way to achieve a high-intensity K beam
- Same quantum leap as for π expected
- Knowledge exists for π , can easily be adapted to K
- Nowhere else possible at this high intensity and energy

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RF-separated K beam will also give insight in:

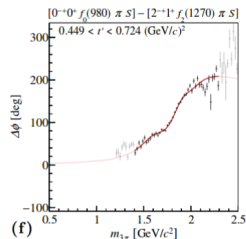
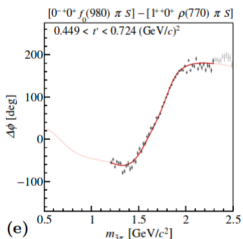
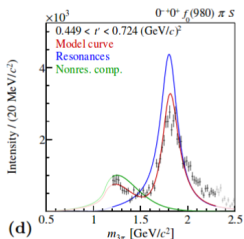
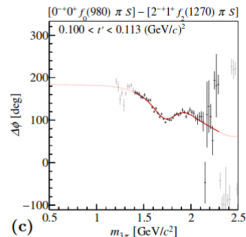
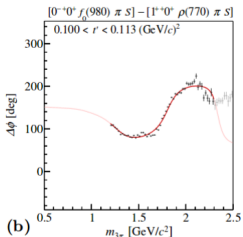
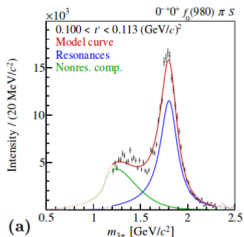
- Kaon valence-quark distribution
(Drell-Yan \rightarrow [Marco Meyer, yesterday 12:10](#))
- Separation of valence- and sea-quark contribution
(K^\pm cross-section asymmetry \rightarrow [Yann Bedfer, today 15:00](#))
- Study of gluon content inside the kaon via J/ψ and prompt photon production
- Kaon polarizability (Primakoff)

Also possible: RF-separated \bar{p} beam

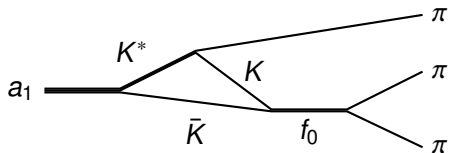
- Spin structure of the nucleon
- Drell-Yan with high-intensity antiproton beam

Thank you for your
attention!

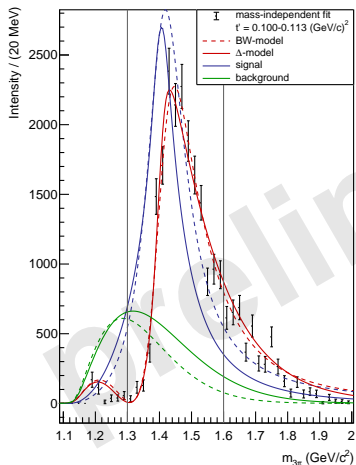
Back-Up



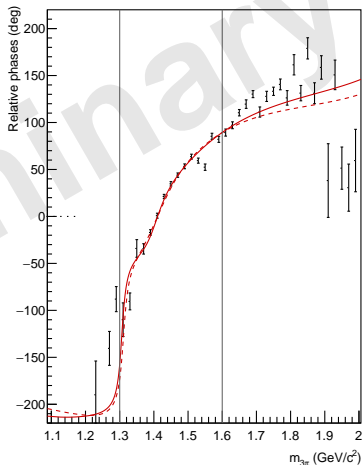
[COMPASS, PRD 98 (2018) 092003]



$f_0\pi P$ - intensity



$\rho\pi S - f_0\pi P$ - phase



Probability to measure N events:

$$P(N; N_e) = \frac{N_e^N}{N!} \exp(-N_e)$$

with expected events

$$N_e = \int I(\tau) \zeta(\tau) d\tau$$

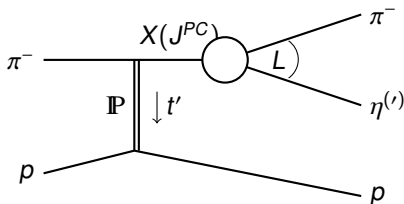
with the kin. variables chosen as $\tau = (s_0, m_{3\pi}^2, t, \Omega_{GJ}, m_{2\pi}^2, \Omega_H)$.

Probability to find measured event at given kinematics:

$$P_k(\tau_k) = \frac{I(\tau_k)}{N_e}$$

Maximize likelihood: $\mathcal{L} = \frac{N_e^N}{N!} \exp(-N_e) \prod_{k=1}^N \frac{I(\tau_k)}{N_e}$

Or minimize: $-\log \mathcal{L} = \underbrace{\int I(\tau) \zeta(\tau) d\tau}_{\text{acceptance with MC}} - \underbrace{\sum_{k=1}^N \log(I(\tau_k))}_{\text{real data}}$



simpler: angular dependence \rightarrow spherical harmonics

$$J = L, P = (-1)^L, C = +1 \quad \Rightarrow \quad J^{PC} = 1^{-+}, 2^{++}, (3^{-+}), 4^{++}, \dots$$

giving access to $\pi_1, a_2, (\pi_3)$ and a_4

[arXiv:1810.04171v2 [hep-ph] 16 Jan 2019]

N/D formalism:

$$A_i^J(s) \sim \sum_k n_k^J(s) [D^J(s)^{-1}]_{ki}$$

n_k^J effective expansion in Chebyshev polynomials

$$D^J = \begin{pmatrix} \eta\pi \rightarrow \eta\pi & \eta\pi \rightarrow \eta'\pi \\ \eta'\pi \rightarrow \eta\pi & \eta'\pi \rightarrow \eta'\pi \end{pmatrix}$$

containing right-hand cuts constrained by unitarity

$$D_{ki}^J(s) = [K^J(s)^{-1}]_{ki} - \frac{s}{\pi} \int_{s_k}^{\infty} ds' \frac{\rho N_{ki}^J(s')}{s'(s' - s - i\varepsilon)}$$

effective description of left-hand singularities via

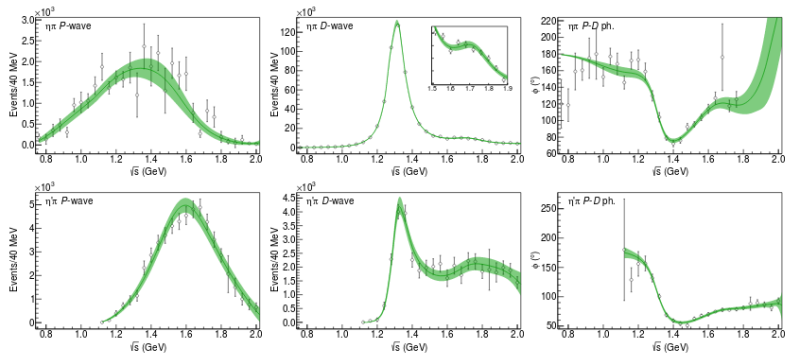
$$\rho N_{ki}^J(s') = \delta_{ki} \frac{\lambda^{J+1/2}(s', m_{\eta^{(\prime)}}^2, m_{\pi}^2)}{(s' + s_L)^{2J+1+\alpha}}$$

($s_L = 1 \text{ GeV}^2, \alpha = 2$) and standard K -matrix parametrization

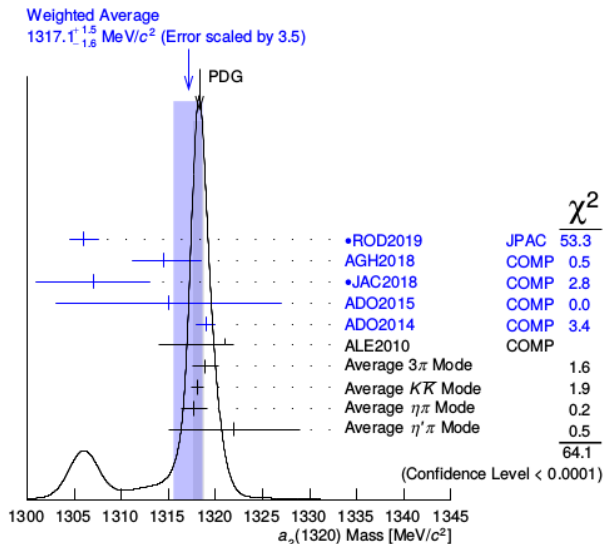
$$K_{ki}^J(s) = \sum_R \frac{g_k^{J,R} g_i^{J,R}}{m_R^2 - s} + c_{ki}^J + d_{ki}^J s$$

2 poles in D -wave, 1 pole in P -wave (c and d are symmetric)

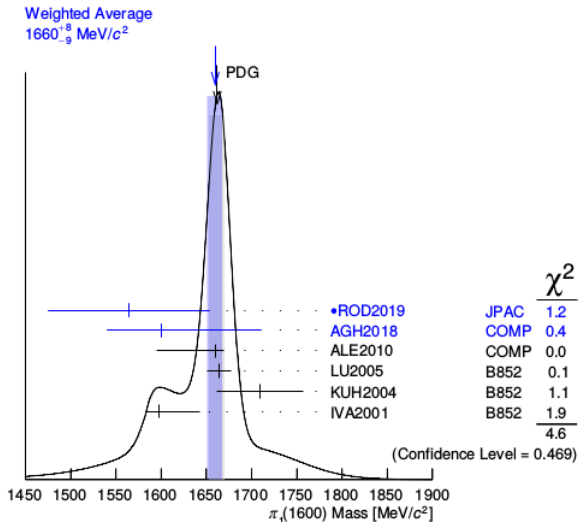
pole in $K \rightsquigarrow$ zero in $D \rightsquigarrow$ pole in a



[JPAC, PRL 122, 042002 (2019)]



[To be published in Progress in Particle and Nuclear Physics]



[To be published in Progress in Particle and Nuclear Physics]