

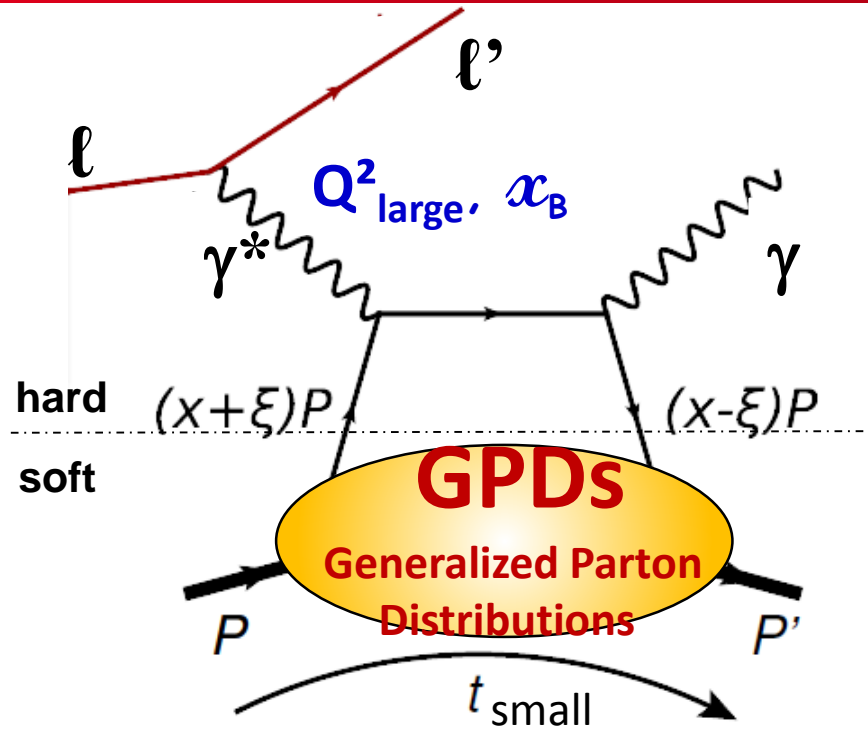
# Status and Prospects of the Experimental Investigation on GPDs

Nicole d'Hose, CEA Université Saclay-Paris



Electron Ion Collider user meeting 2017  
18-22 July, Trieste, Italy

# Deeply virtual Compton scattering (DVCS) and DVMP



D. Mueller *et al*, Fortsch. Phys. 42 (1994)

X.D. Ji, PRL 78 (1997), PRD 55 (1997)

A. V. Radyushkin, PLB 385 (1996), PRD 56 (1997)

DVCS:  $l p \rightarrow l' p' \gamma$

the golden channel

because it interferes with  
the Bethe-Heitler process

also meson production

$l p \rightarrow l' p' \pi, \rho$  or  $\phi$  or  $J/\psi \dots$

The GPDs depend on the following variables:

$x$ : average long. momentum

$\xi$ : long. mom. difference  $\simeq x_B / (2 - x_B)$

$t$ : four-momentum transfer  
related to  $b_{\perp}$  via Fourier transform

The variables measured in the experiment:

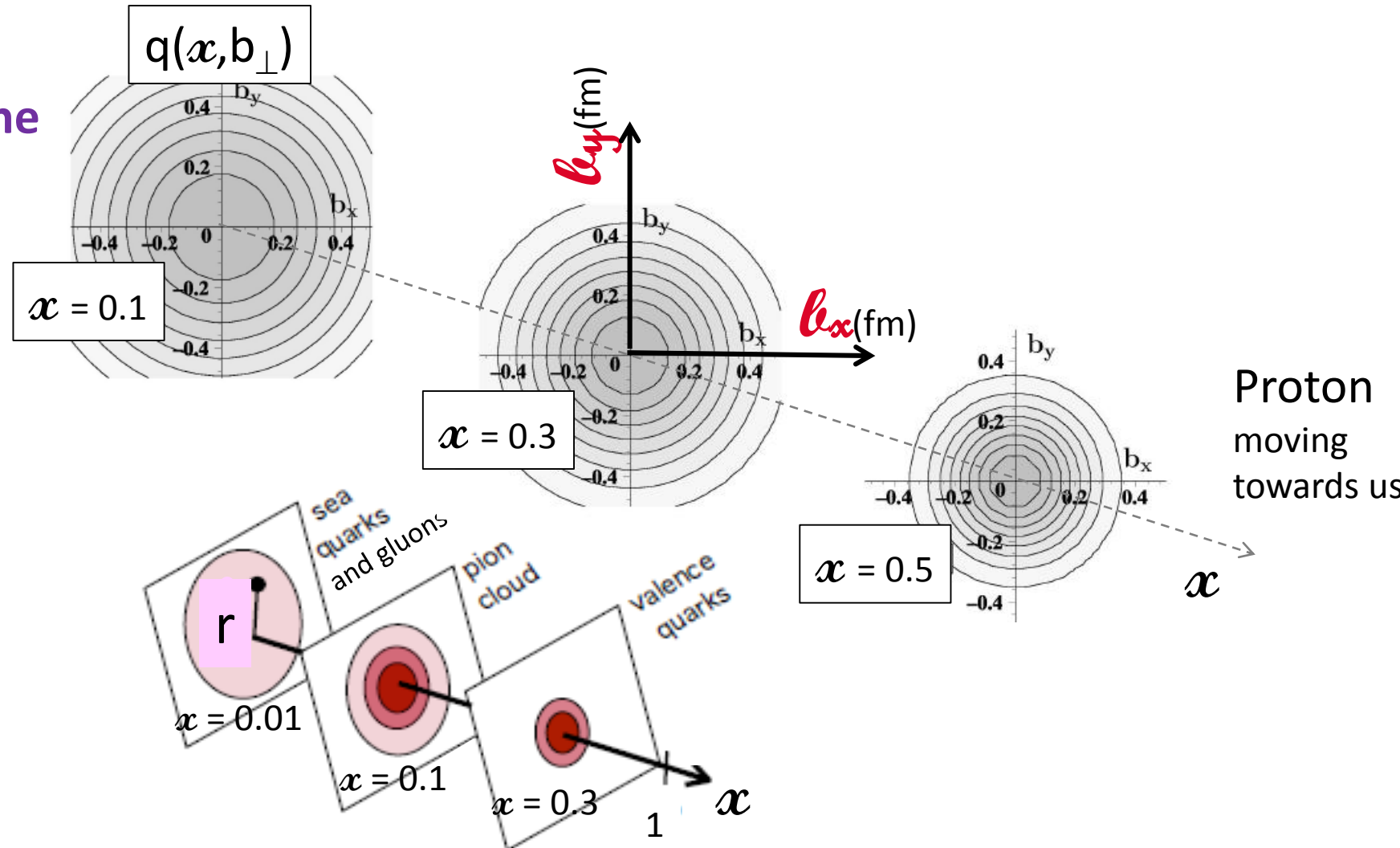
$E_{\ell}, Q^2, x_B \sim 2\xi / (1 + \xi),$

$t$  (or  $\theta_{\gamma^* \gamma}$ ) and  $\phi$  ( $l l'$  plane /  $\gamma \gamma^*$  plane)

# GPDs and 3D imaging

M. Burkardt, PRD66(2002)

mapping in the transverse plane  
Impact parameter distribution



Correlation between the spatial distribution of partons  
and the longitudinal momentum fraction

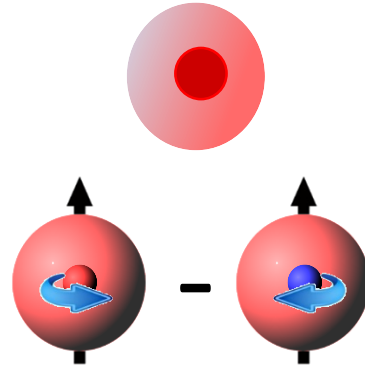
# GPDs and Energy-Momentum Tensor and Confinement

GPDs can provide an experimental answer by exploiting their equivalence to the gravitational form factors of the nucleon energy-momentum-tensor (fundamental nucleon properties)

$$H^q(x, \xi, t) \xrightarrow{t \rightarrow 0} q(x) \text{ or } f_1(x)$$

"Elusive"

$$E^q(x, \xi, t) \leftrightarrow f_{1T}(x, k_T)$$



Sivers: quark  $k_T$  & nucleon transv. spin

mass & energy  
distribution

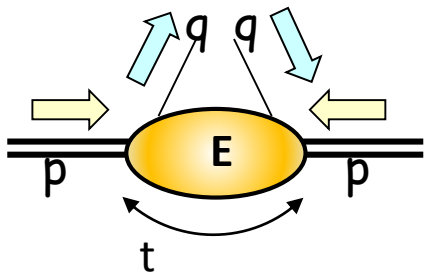
$$\int dx x H^q(x, \xi, t) = A^q(t) + \frac{4}{5} \xi^2 d_1^q(t)$$

$$\int dx x E^q(x, \xi, t) = B^q(t) - \frac{4}{5} \xi^2 d_1^q(t)$$

Angular momentum distribution      Force & Pressure distribution

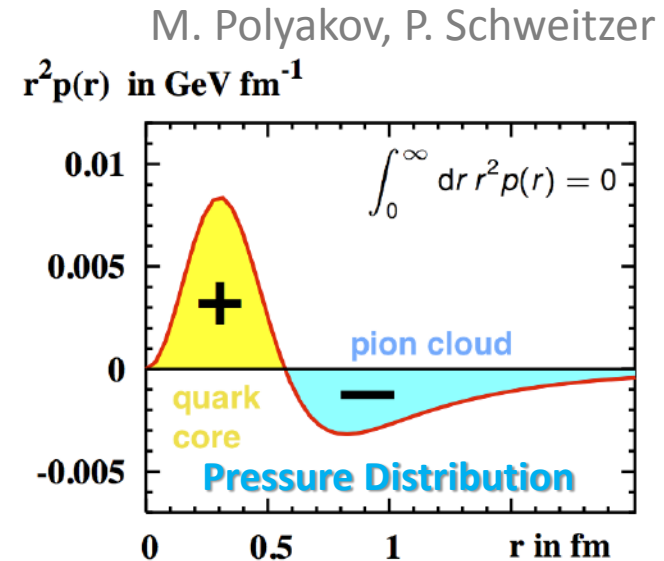
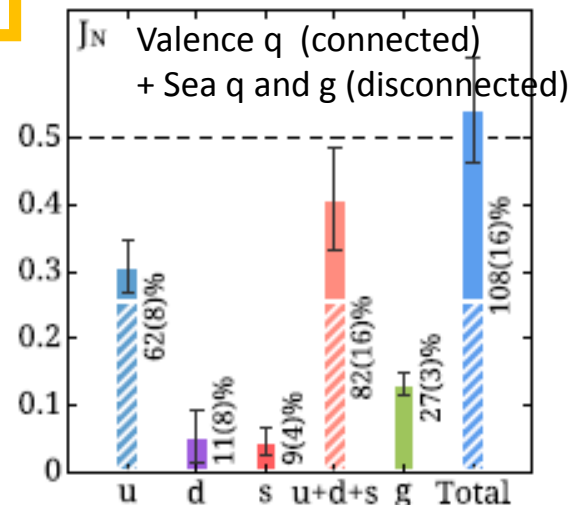
$$2J^q = \lim_{t \rightarrow 0} \int x (H^q(x, \xi, t) + E^q(x, \xi, t)) dx$$

Ji sum rule: PRL78 (1997) cited 1504 times

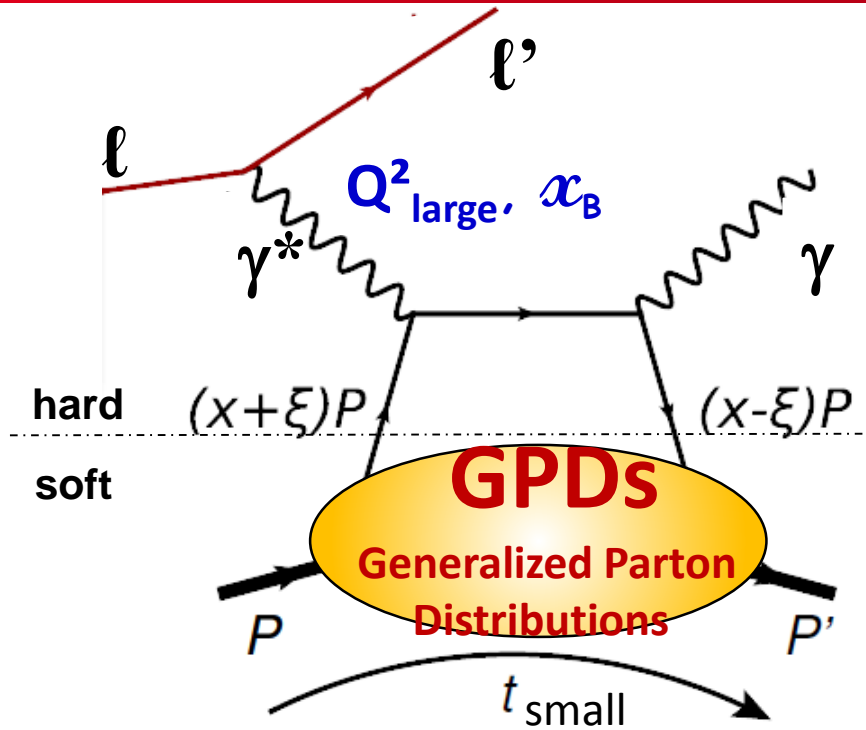


## Relation to OAM

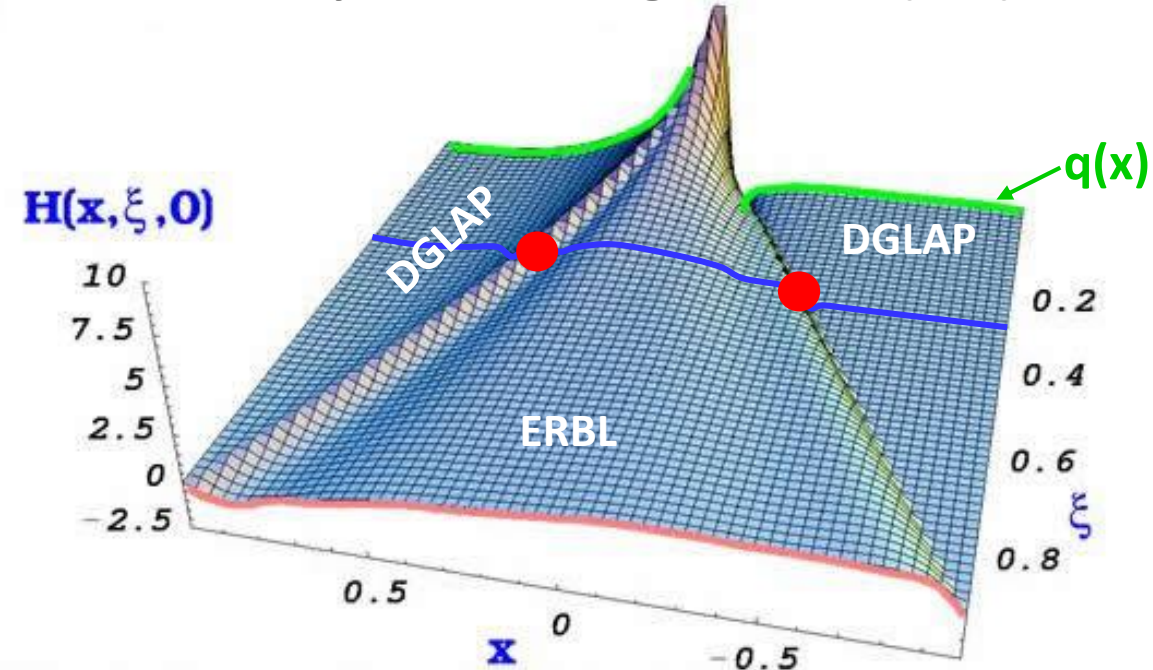
Lattice ArXiv:1706.02973  
 Alexandrou et al.  
 $\frac{1}{2} \Delta \Sigma = 0.20$   
 $L^q = 0.21$   
 $J^g = 0.13$



# Deeply virtual Compton scattering (DVCS)



From Goeke, Polyakov, Vanderhaeghen, PPNP47 (2001)



The amplitude DVCS at LT & LO in  $\alpha_s$ :

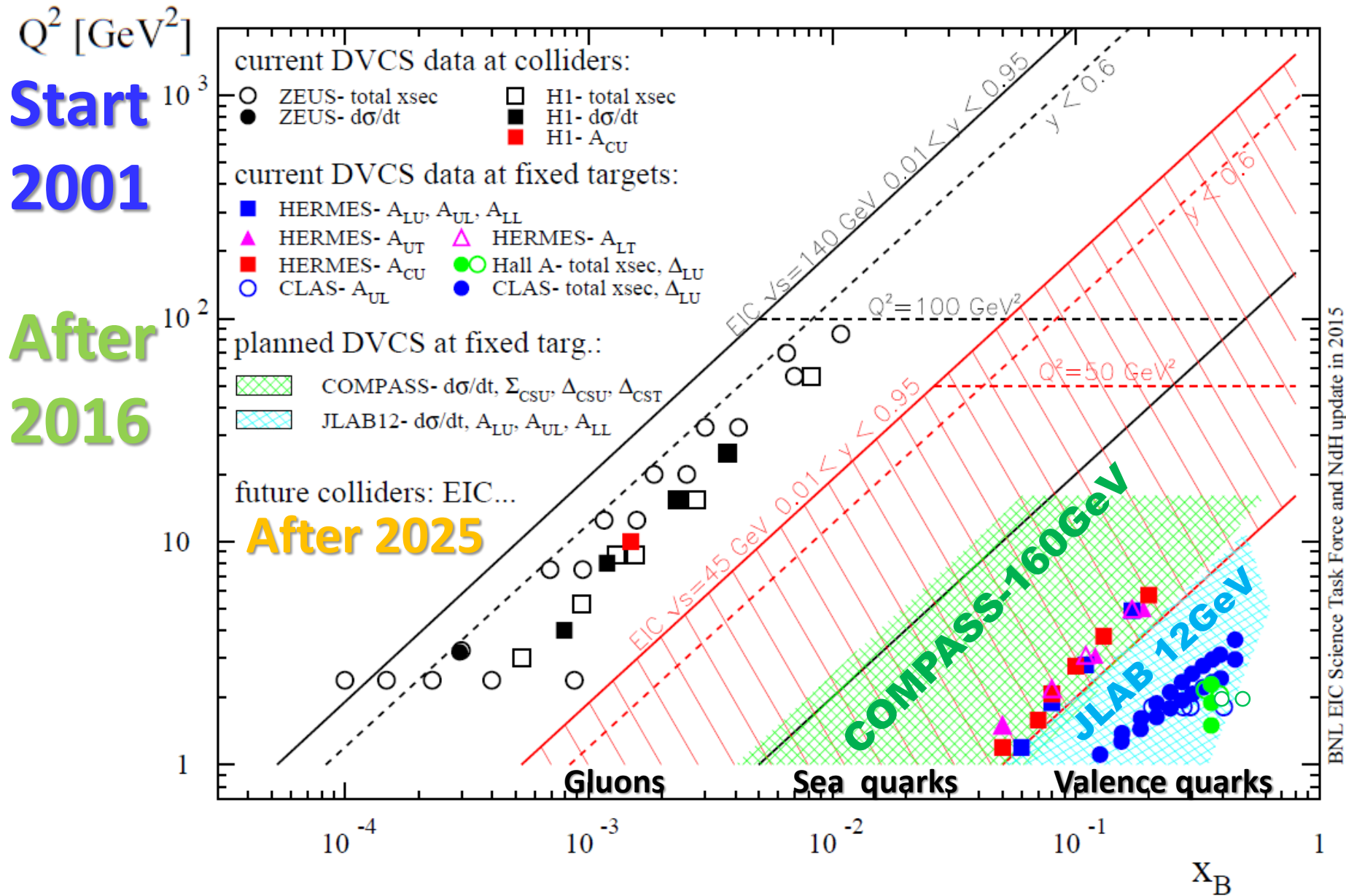
$$\mathcal{H} = \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi + i\epsilon} = \mathcal{P} \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi} - i \pi H(x = \pm \xi, \xi, t)$$

Real part      Imaginary part

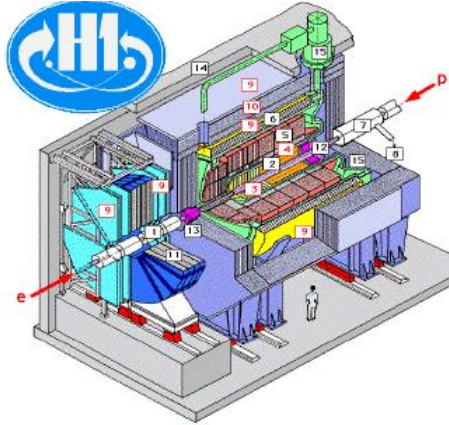
$t, \xi$  fixed

$$\text{Re } \mathcal{H}(\xi, t) = \mathcal{P} \int dx \frac{\text{Im } \mathcal{H}(x, t)}{x - \xi} + d(t)$$

# The past and future DVCS experiments



# The past and present experiments



## Collider mode e-p forward fast proton

**HERA: H1** and **ZEUS**

Polarised **27 GeV** e-/e+

Unpolarized **920 GeV** proton

~ Full event reconstruction

Examples for EIC

## Fixed target mode slow recoil proton

**HERMES:** Polarised **27 GeV** e-/e+

Long, Trans polarised p, d target

Missing mass technique

2006-07 with recoil detector

**Jlab: Hall A, C, CLAS** High lumi, polar. **6 & 12 GeV** e-

Long, (Trans) polarised p, d target

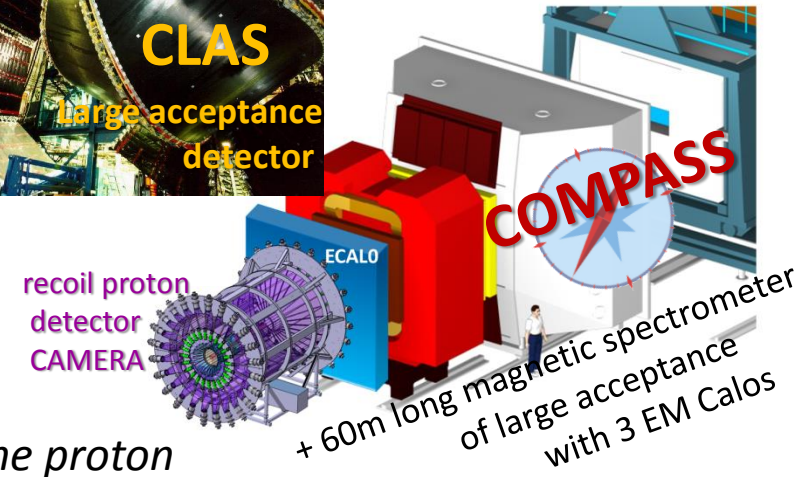
Missing mass technique (A,C) and complete detection (CLAS)

**COMPASS @ CERN:** Polarised **160 GeV**  $\mu^+/\mu^-$

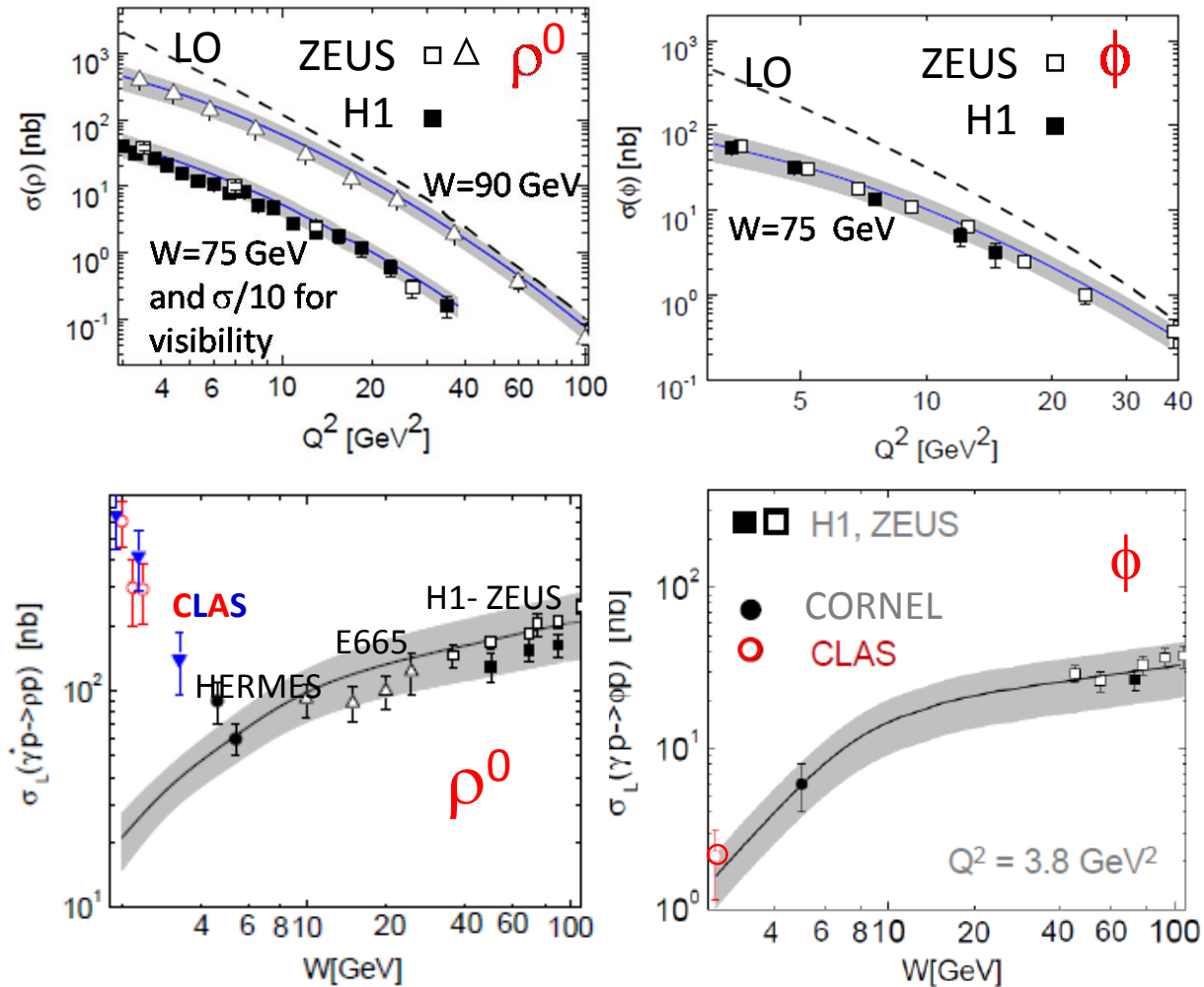
p target, (Trans) polarised target

with recoil detection

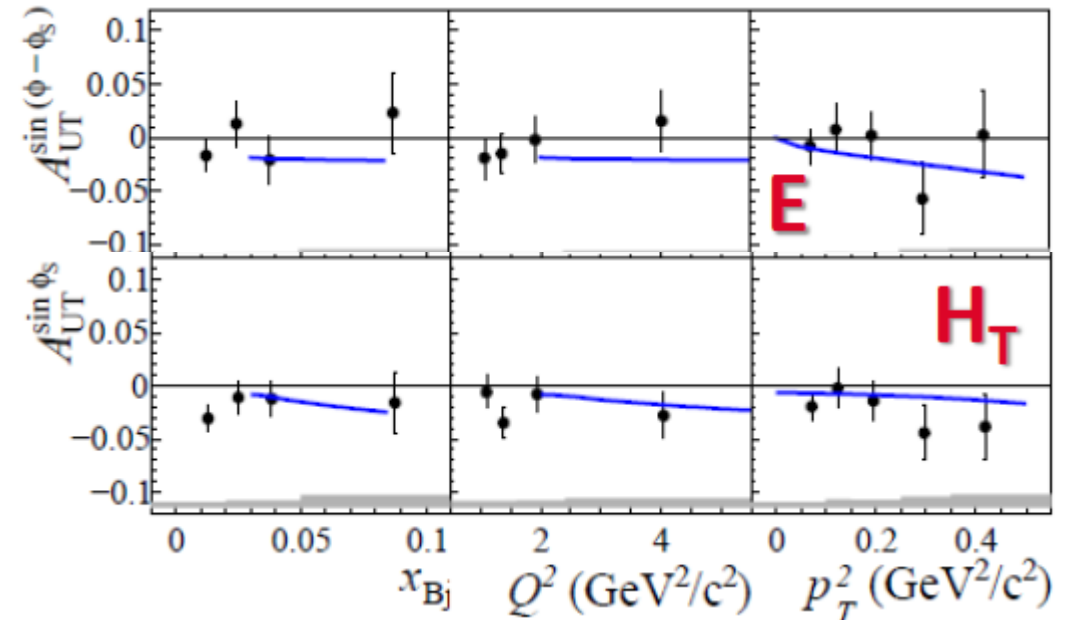
*Rejection of background: SIDIS, exclusive  $\pi^0$ /DVCS, dissociation of the proton*



# Exclusive Meson production for GPD models



$\rho^0 (\rightarrow \pi^+\pi^-)$  production at COMPASS with Transversely Polarized Target



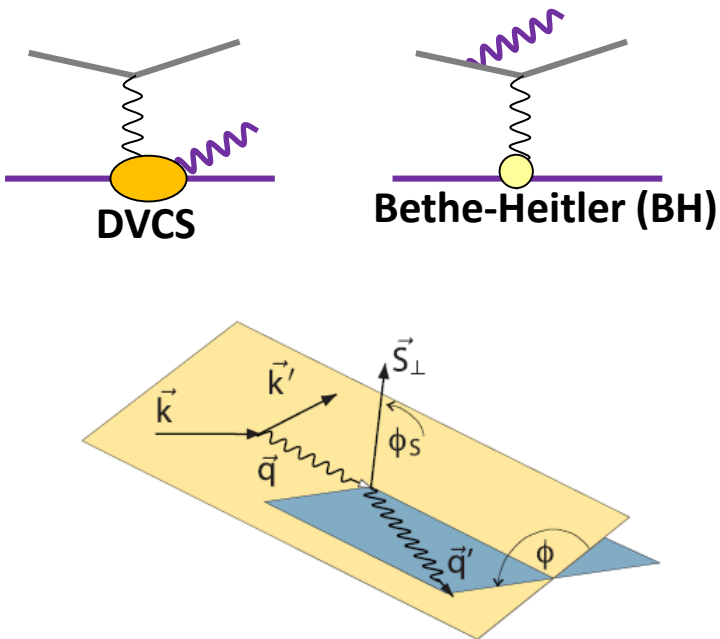
**GK** Goloskokov, Kroll, EPJC42,50,53,59,65,74 GPD model constrained by HEMP at small  $x_B$  (or large  $W$ )

dominant (longitudinal)  $\gamma_L^* p \rightarrow M p$  and transv. polar.  $\gamma_T^* p \rightarrow M p$

quark and gluon contributions (GPDs **H**, **E**, **H<sub>T</sub>**) and beyond leading twist

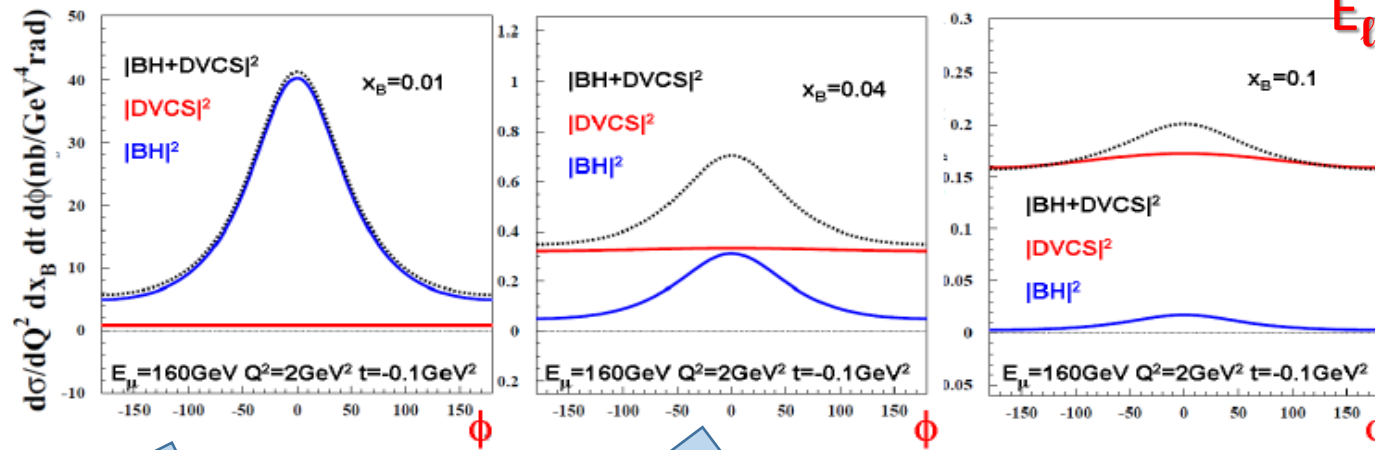


# DVCS and Impact of the beam energy



$$d\sigma \propto |T^{BH}|^2 + \text{Interference Term} + |T^{DVCS}|^2$$

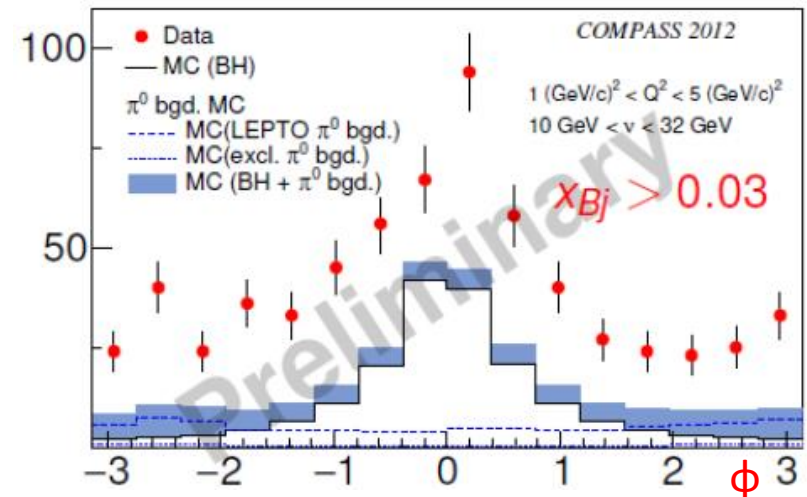
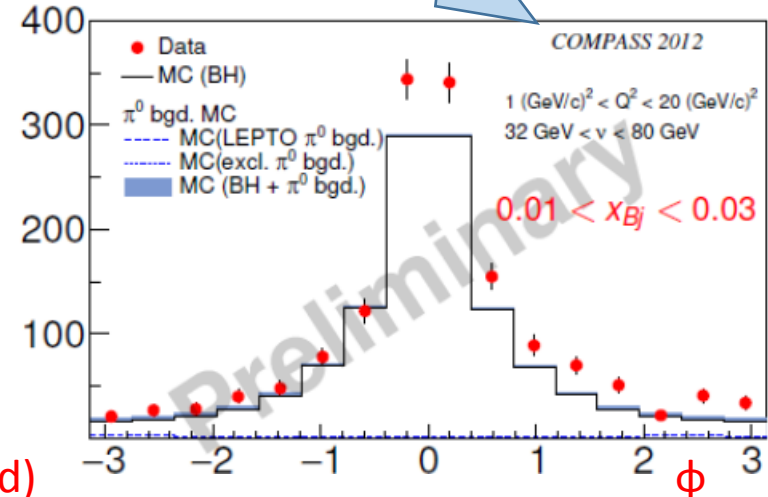
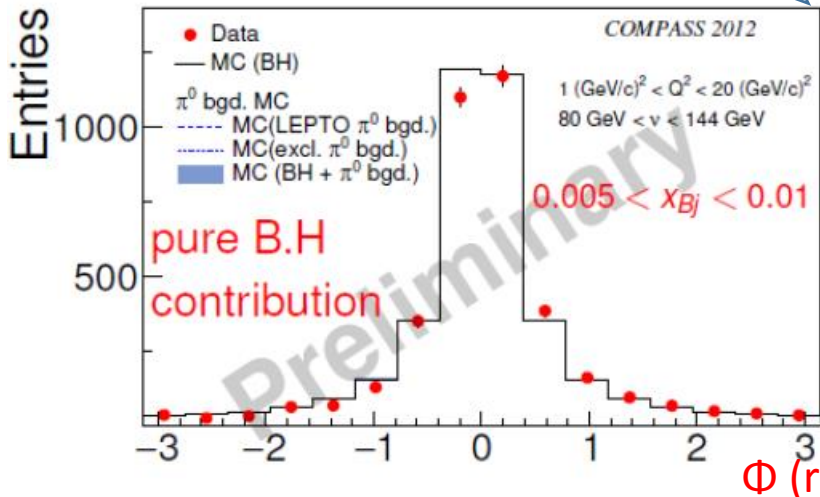
$E_\mu = 160 \text{ GeV}$



BH dominates  
Reference yield

DVCS ampl. via interference  
Jlab, HERMES,  
H1, COMPASS

DVCS dominates - Study of  $d\sigma^{DVCS}/dt$   
Only for H1, ZEUS, COMPASS

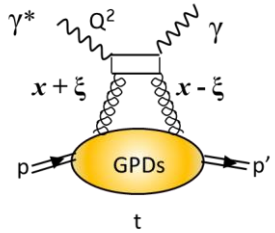


**Study of t-dependence of  
the pure DVCS cross-section ( $\gamma^* p \rightarrow \gamma p$ )**

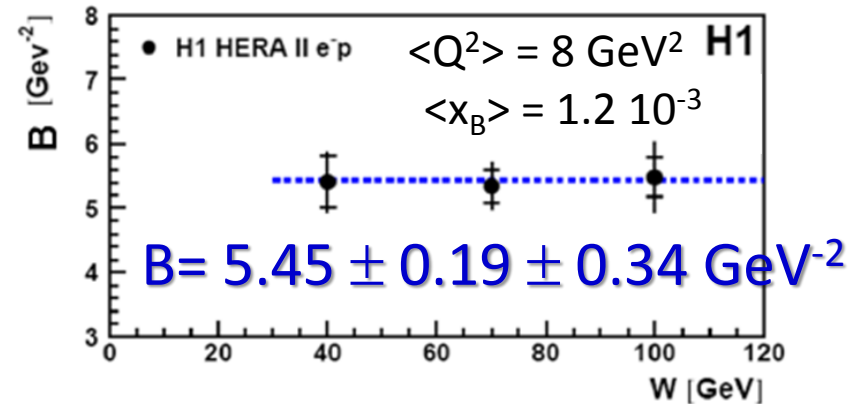
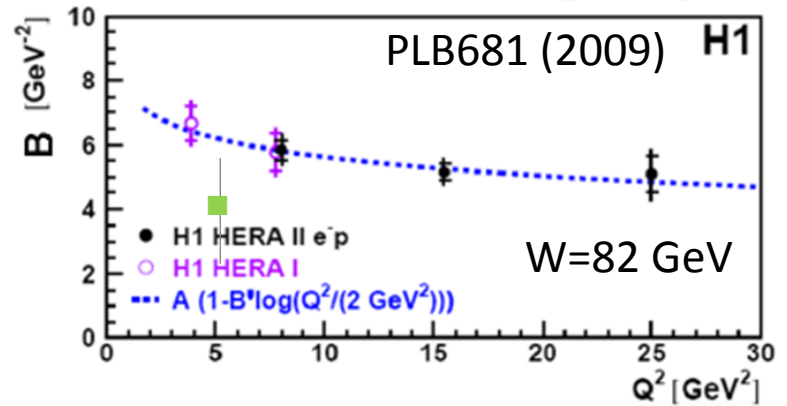
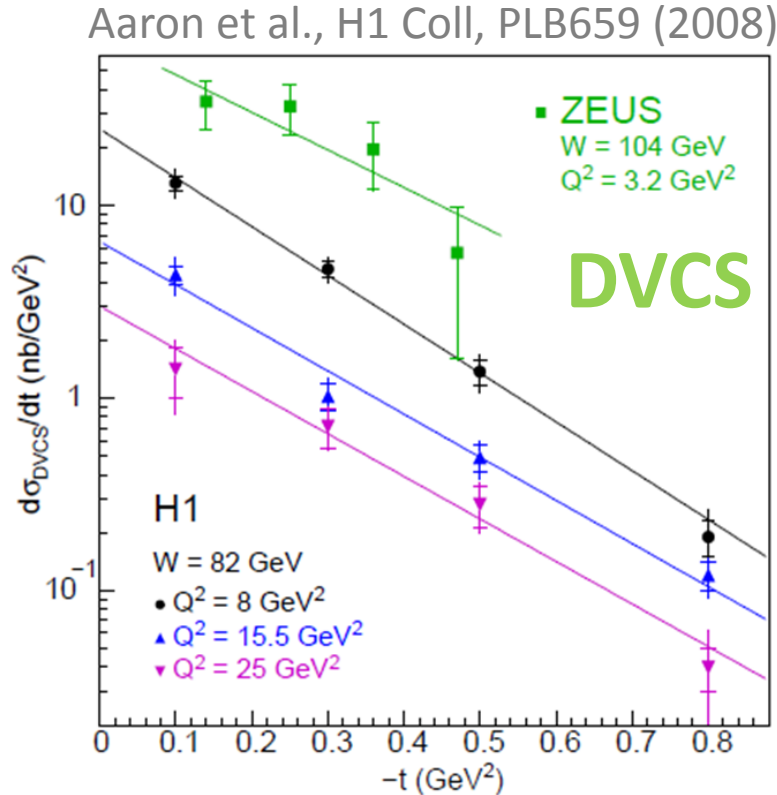
# Gluon imaging @ HERA

$$d\sigma^{DVCS}/dt = e^{-B|t|}$$

B is related to the transversed size of the scattering objects



ZEUS-H1  
Data collected  
1995-2007



$$\langle r_{\perp}^2 \rangle \approx 2B$$

$$\sqrt{\langle r_{\perp}^2 \rangle} = 0.65 \pm 0.02 \text{ fm}$$

to be compared to

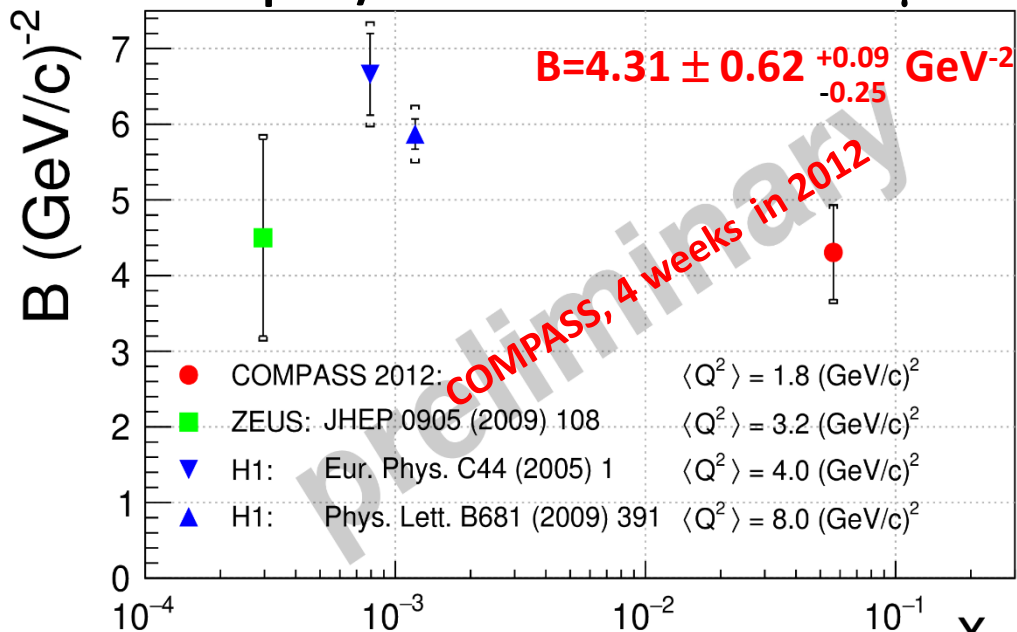
$$\sqrt{4 \frac{d}{dt} F_1^p} \Big|_{t=0} = 0.67 \pm 0.01 \text{ fm}$$

not to

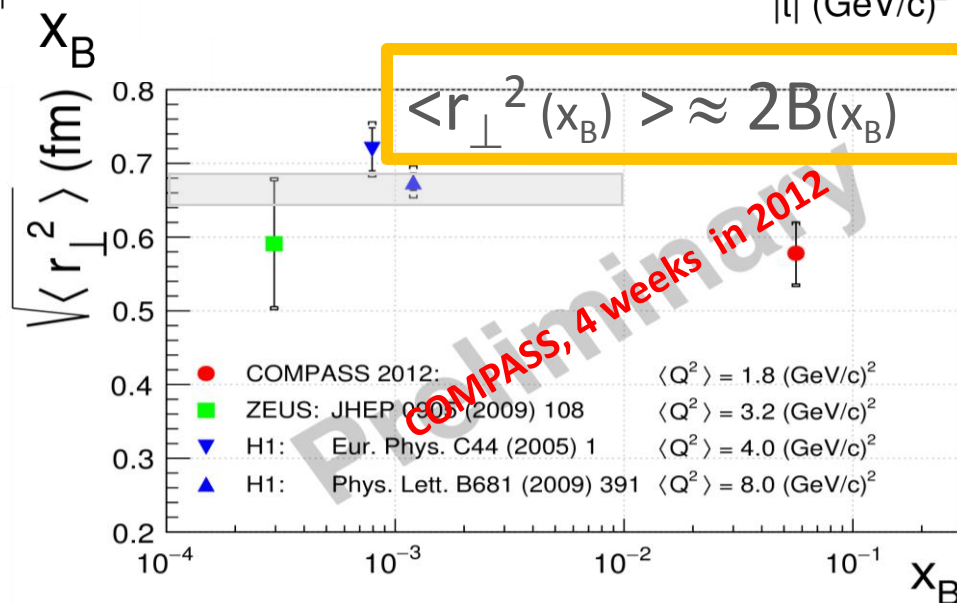
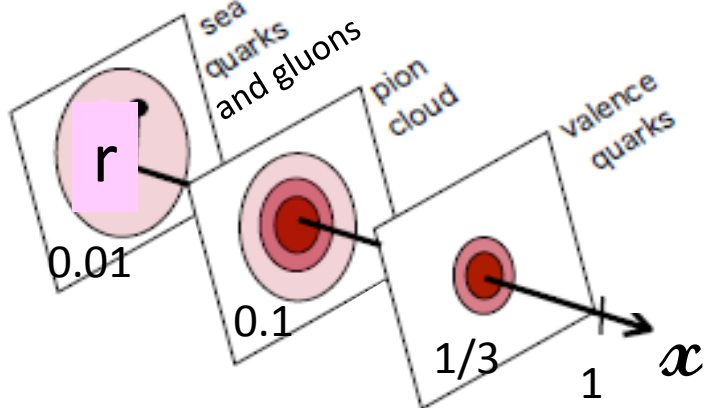
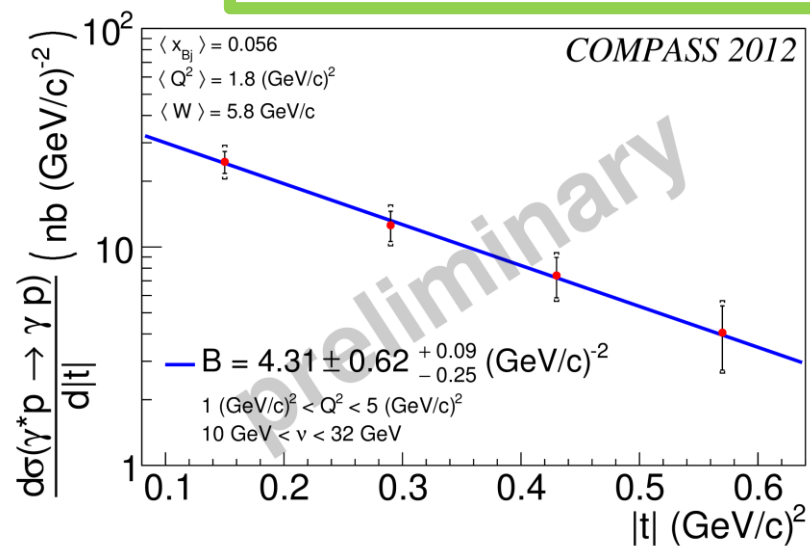
$$\sqrt{4 \frac{d}{dt} G_E^p} = 0.72 \pm 0.01 \text{ fm}$$

# Sea quark imaging @ COMPASS

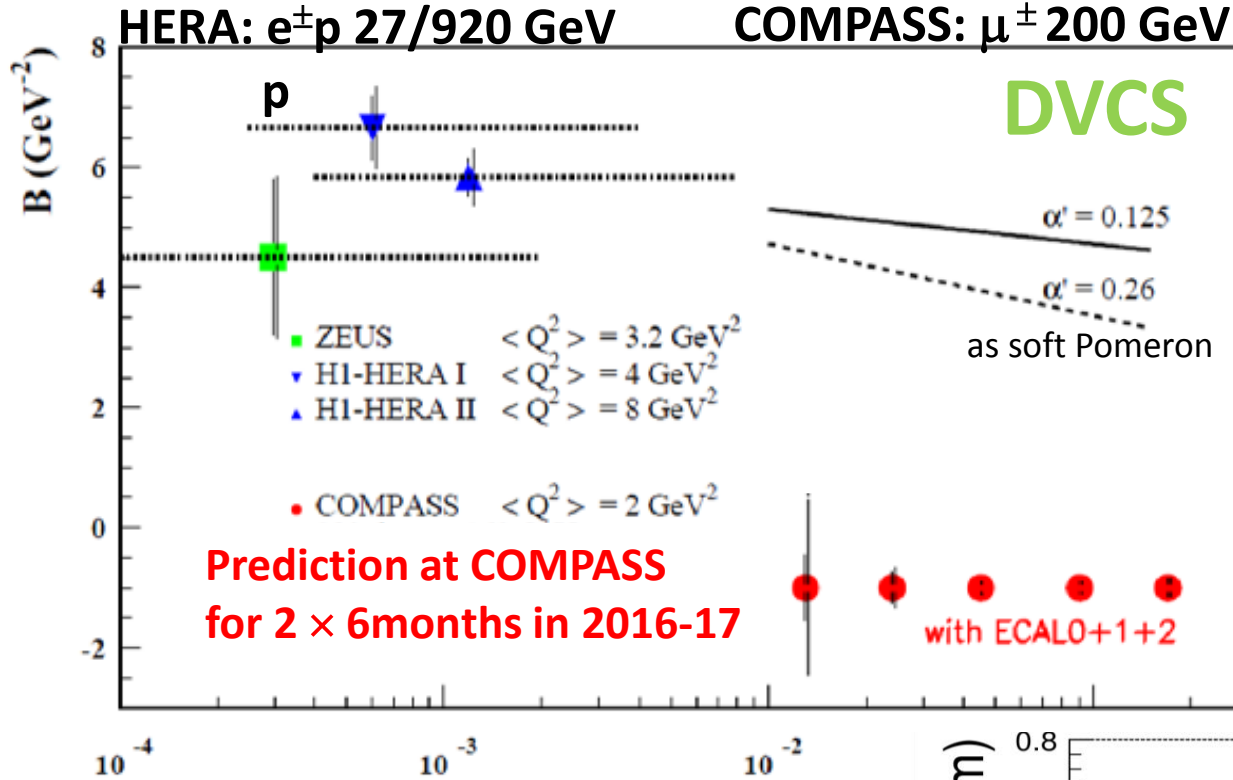
HERA:  $e^\pm p$  27/920 GeV      COMPASS:  $\mu^\pm$  200 GeV



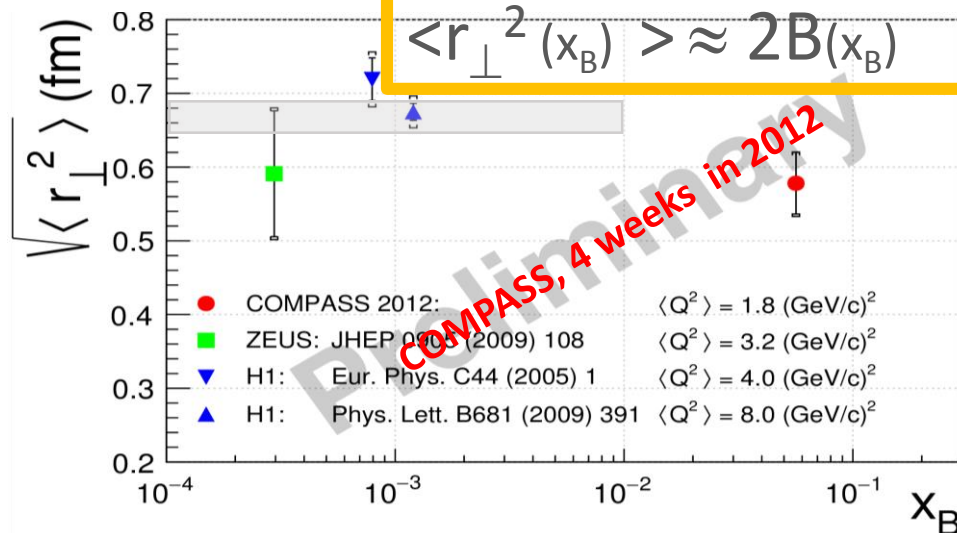
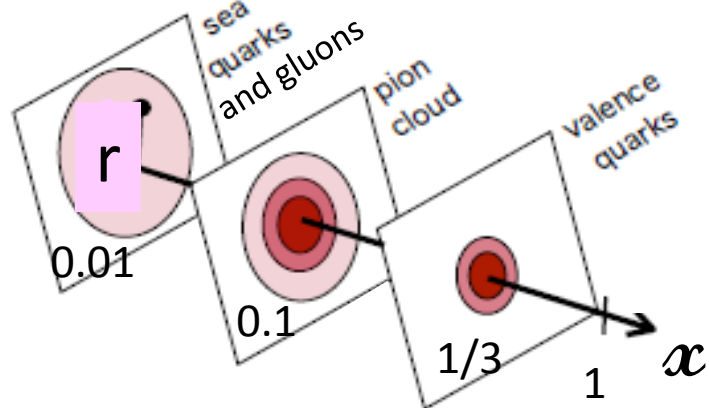
$$d\sigma^{\text{DVCS}}/dt = e^{-B|t|}$$



# Sea quark imaging @ COMPASS



$$d\sigma^{\text{DVCS}}/dt = e^{-B|t|}$$



# **Study of DVCS-BH interference**

# A complete set of observables for DVCS

Results on the proton

## Asymmetry measurements

HERMES 27 GeV provided a complete set of observables

1995: start of data taking

2001: 1<sup>st</sup> DVCS publication as CLAS & H1

2007: end of data taking

2012: still important publications

*JHEP 07 (2012) 032*  $A_C A_{LU}$

*JHEP10(2012) 042*  $A_{LU}$

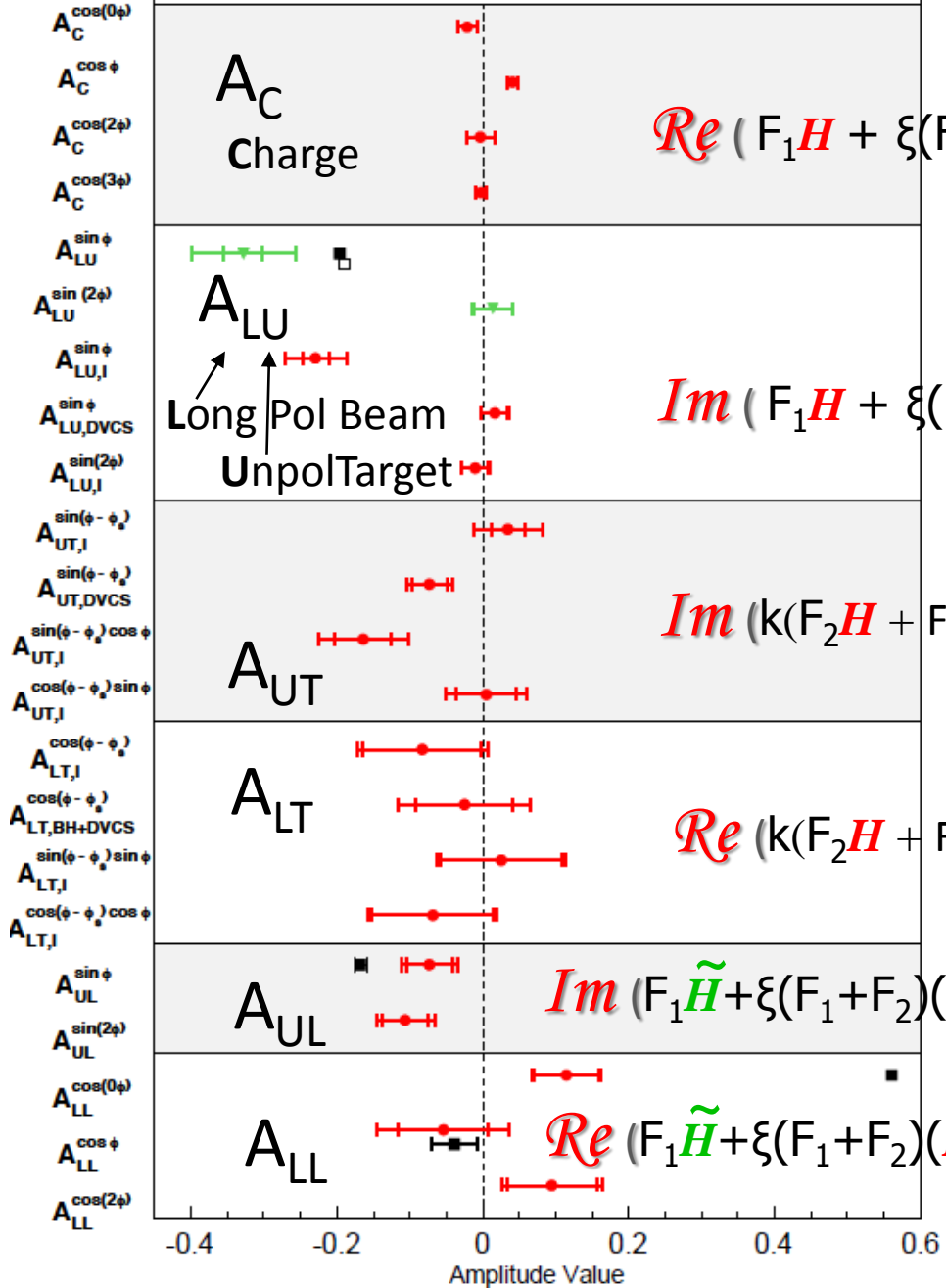
*with recoil detection (2006-7)*

+ 1998-2017 JLAB 6 GeV

Very precise data

### DVCS asymmetries

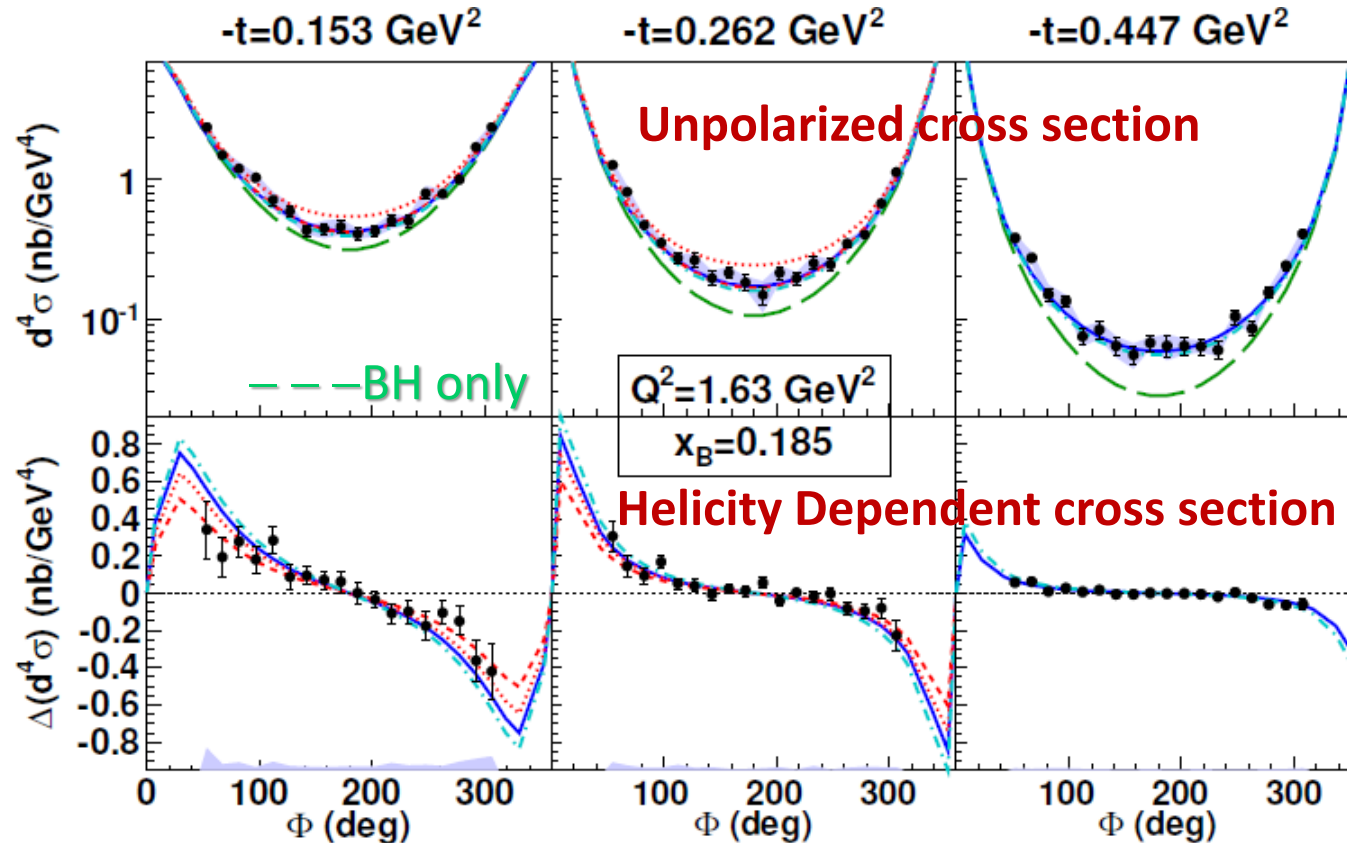
- HERMES Hydrogen
- ▼ HERMES Hydrogen Pure
- CLAS (eg1-dvcs)
- CLAS (e1-dvcs)



# Beam Spin Sum and Diff of DVCS - CLAS

21 bins in  $(x_B, Q^2)$  or 110 bins  $(x_B, Q^2, t)$

3 months data taken in 2005 - Jo et al. PRL115, 212003 (2015)



models:

**VGG** Vanderhaeghen, Guichon, Guidal  
PRL80(1998), PRD60(1999), PPNP47(2001), PRD72(2005)  
1st model of GPDs  
constant evolution

**KMS12** Kroll, Moutarde, Sabatié, EPJC73 (2013)  
using the **GK** model  
Goloskokov, Kroll, EPJC42,50,53,59,65,74  
for GPD adjusted on the hard exclusive meson production at small  $x_B$

“**universality**” of GPDs

**KM10a** --- **KM10** ..... Kumericki, Mueller, NPB (2010) 841

Flexible parametrization of the GPDs based on both a Mellin-Barnes representation and dispersion integral which entangle skewness and  $t$  dependences

**Global fit on the world data ranging from H1, ZEUS to HERMES, JLab**



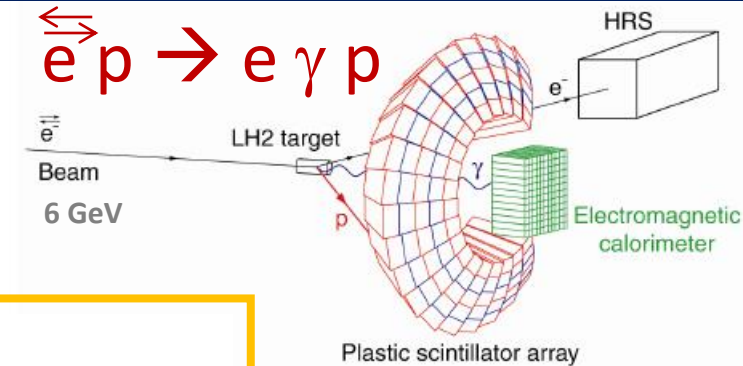
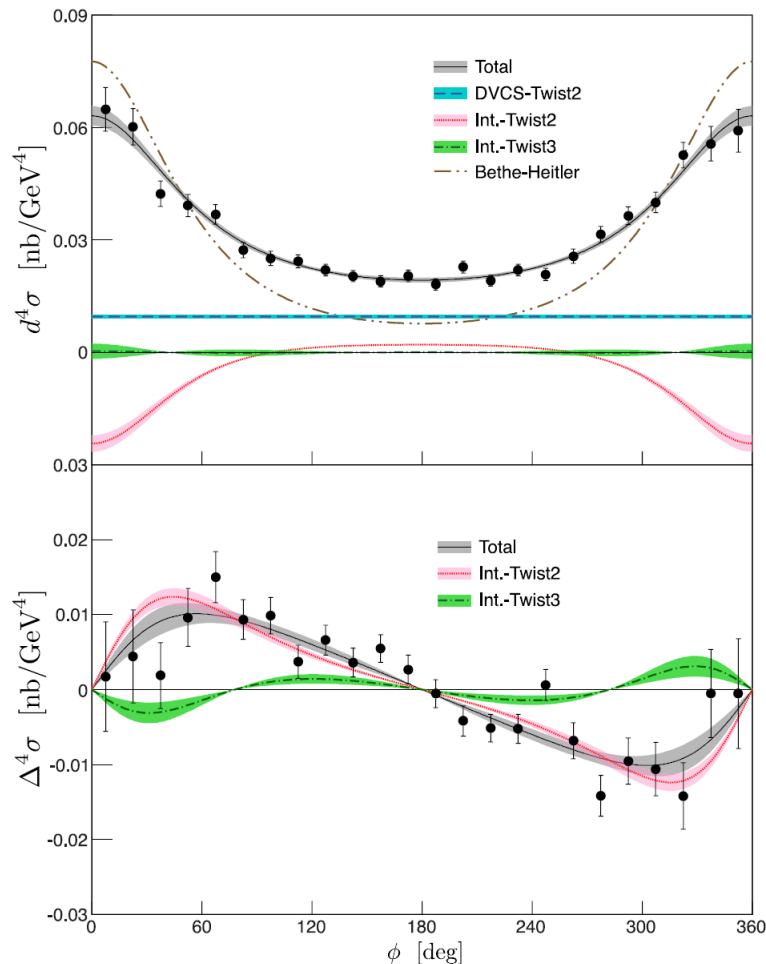
# Beam Spin Sum and Diff of DVCS - HallA

E00-110 pioneer experiment in 2004 with magnetic spectrometer

$x_B=0.36$   $Q^2= 1.5, 1.9, 2.3 \text{ GeV}^2$  Defurne et al. PRC92, 055202 (2015)

$x_B=0.34, x_B=0.39$   $Q^2= 2.1 \text{ GeV}^2$

$x_B=0.36, Q^2= 2.3 \text{ GeV}^2, -t= 0.32 \text{ GeV}^2$



## Unpolarized cross section

$$d\sigma^{\leftarrow} + d\sigma^{\rightarrow} \propto d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + \text{Re } I$$

$$\rightarrow d\sigma^{BH} + \underbrace{c_0^{DVCS}} + \underbrace{c_0^I + c_1^I \cos \phi} + \underbrace{c_2^I \cos 2\phi}$$

## Helicity Dependent cross section

$$d\sigma^{\leftarrow} - d\sigma^{\rightarrow} \propto d\sigma_{pol}^{DVCS} + \text{Im } I$$

$$\rightarrow \underbrace{s_1^I \sin \phi} + \underbrace{s_2^I \sin 2\phi}$$

Further separation with different beam energies (2010 data)

2 solutions: higher-twist  
or next-to-leading order

arXiv:1703.09442 submitted to

# Valence quark imaging at Jlab and HERMES

Fit of 8 CFFs at L.O and L.T.

Dupré, Guidal, Vanderhaeghen, PRD95, 011501(R)(2017)

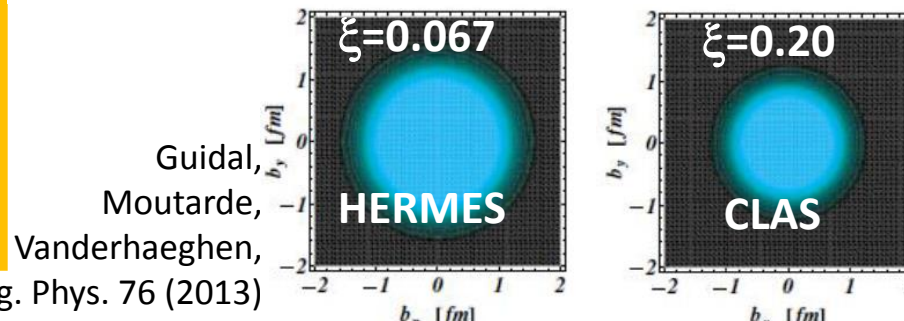
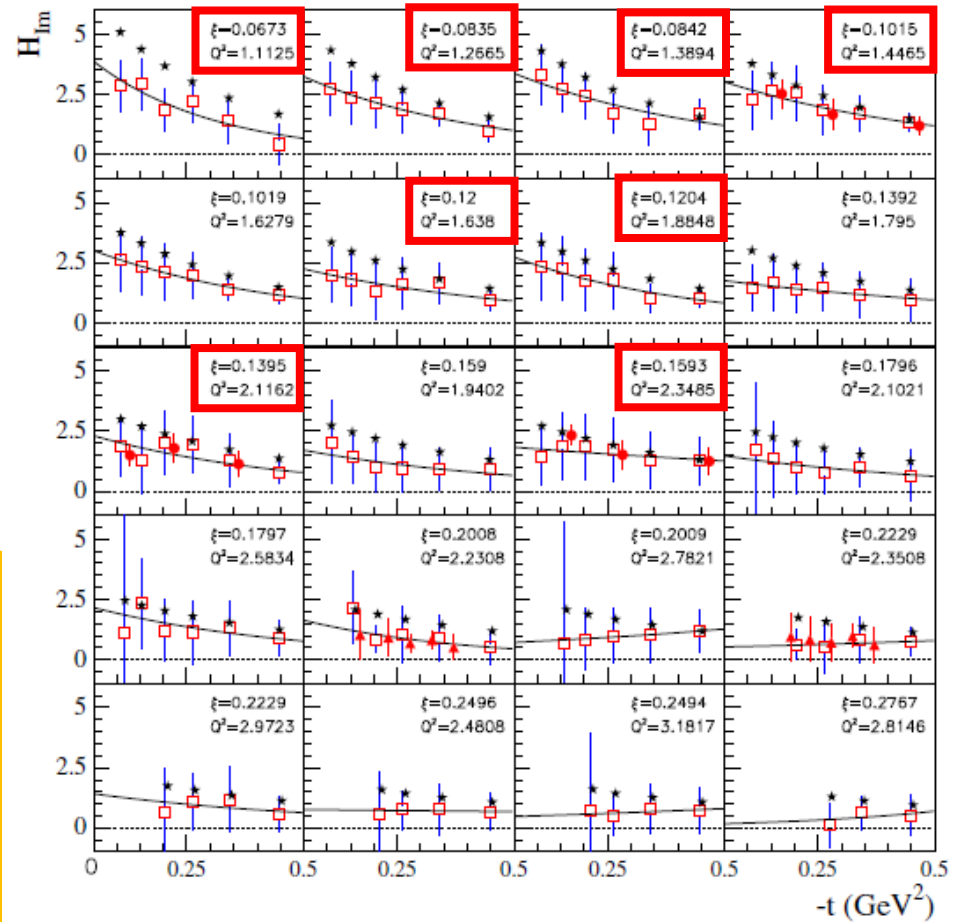
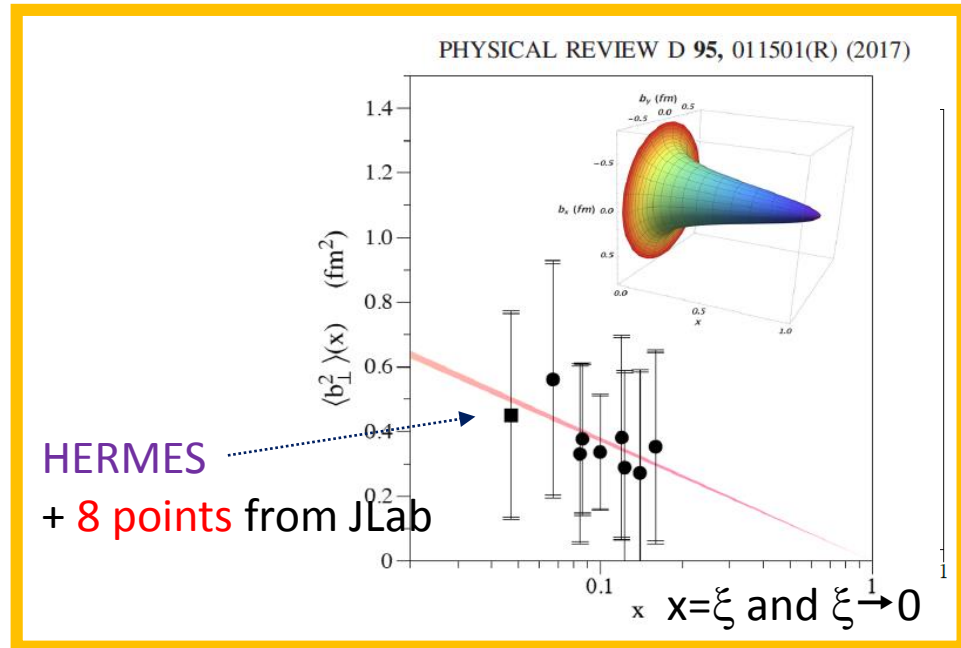
Dupré, Guidal, Nicolai, Vanderhaeghen, arXiv: 1704.07330

$$s_1^I = \text{Im } F_1 \mathcal{H}$$

- CLAS  $\sigma$  and  $\Delta\sigma$
- ▲ HallA  $\sigma$  and  $\Delta\sigma$
- CLAS  $A_{UL}$  and  $A_{LL}$
- ★ VGG model

— Fit  $A e^{-B'|t|}$

$$\langle b_{\perp}^2 \rangle \approx 4 B'$$

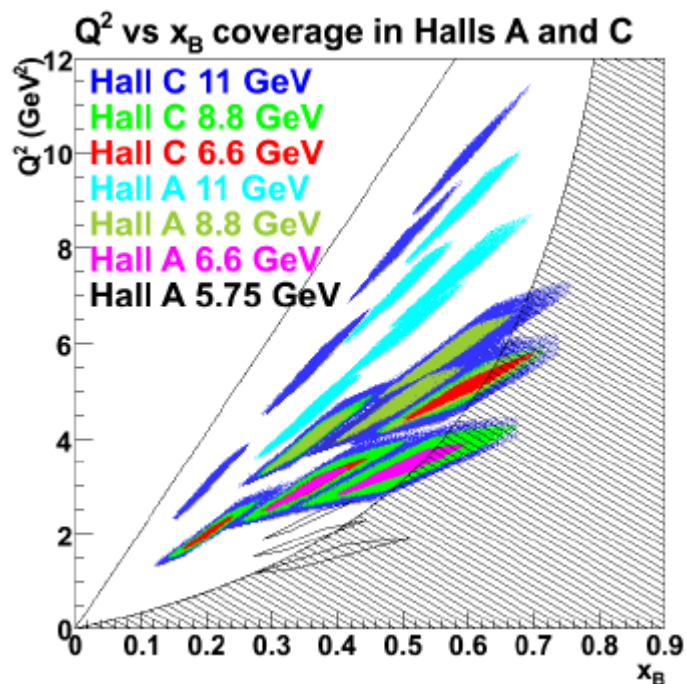


# Future Beam Spin Sum and Diff @JLab12

with high resolution magnetic spectrometer  
+ Calorimeter in Halls A and C

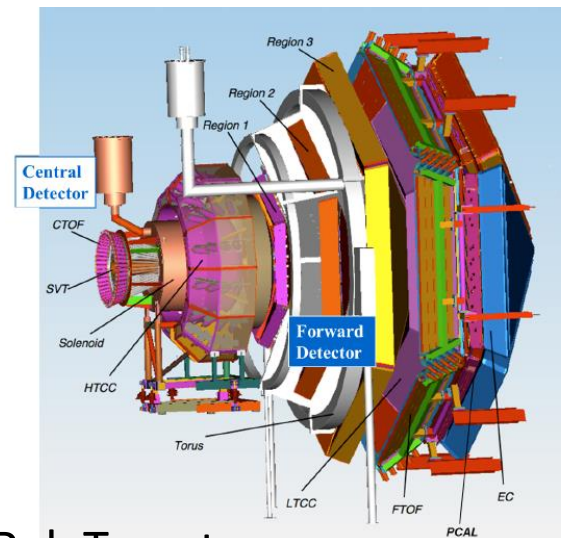
Exp. 2010: run E07-007  
2016-17: Hall A: E12-06-119  
~2018: Hall C: E12-13-010

Different beam energies for a  
Rosenbluth-like DVCS<sup>2</sup>/Interf. separation

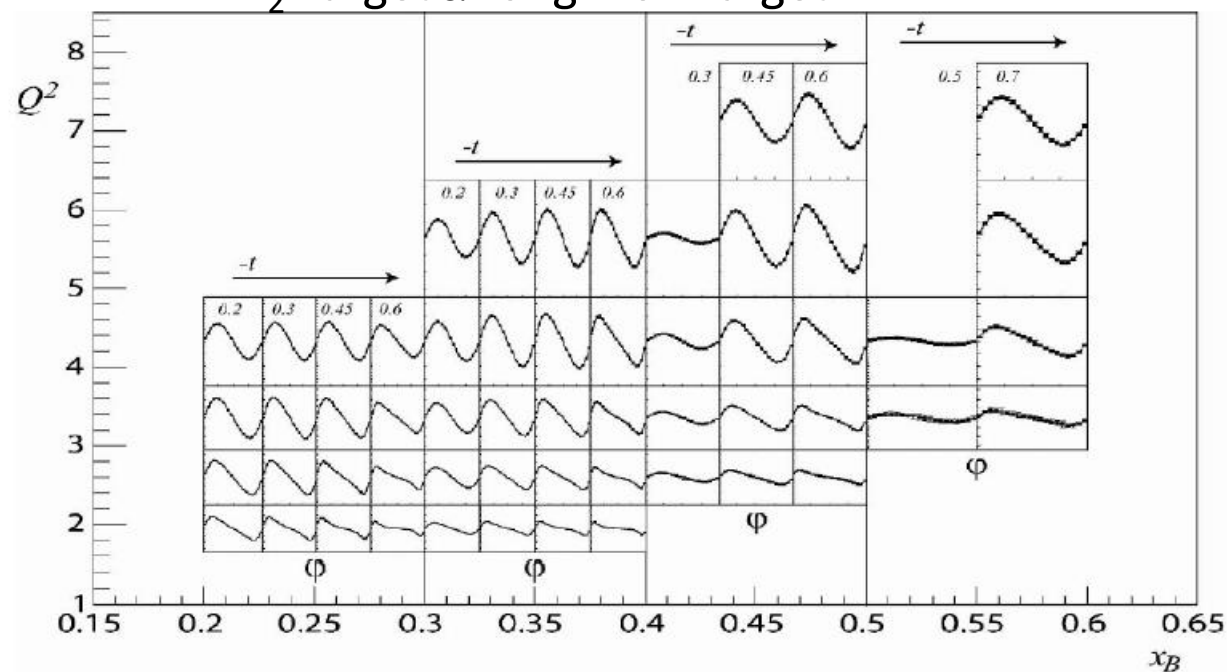


with CLAS12  
In 2017

E12-06-119



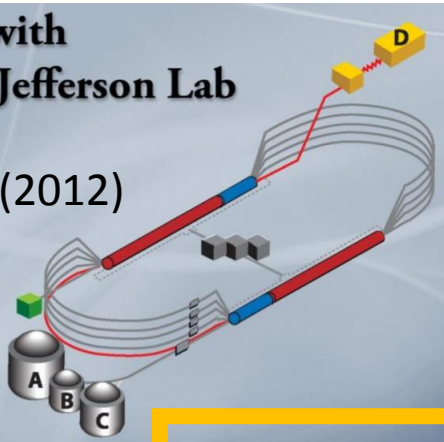
LH<sub>2</sub> Target & Long. Pol. Target



# Future Beam Spin Sum and Diff @JLab12

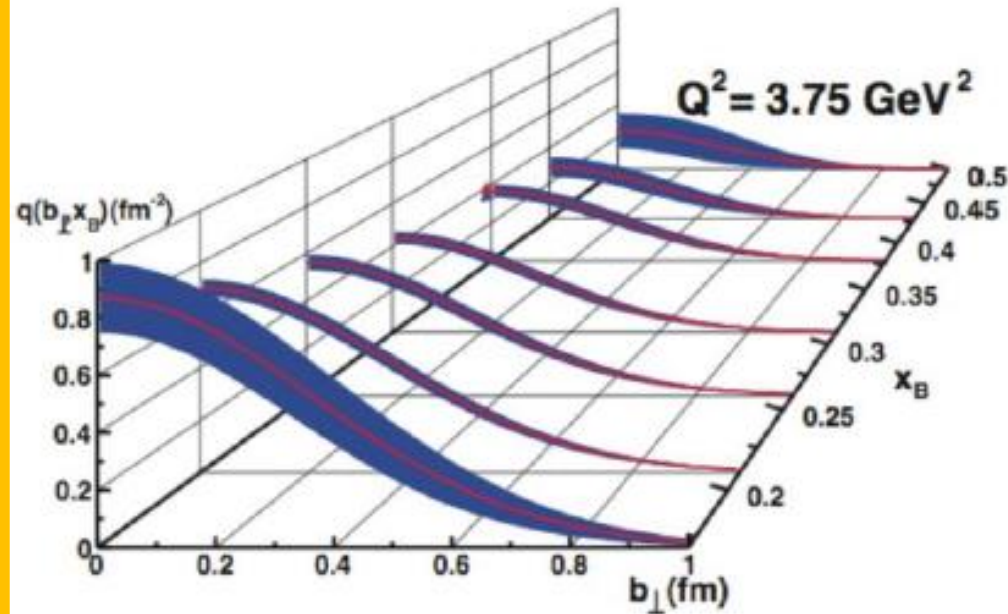
Physics Opportunities with the 12 GeV Upgrade at Jefferson Lab

Dudek et al., EPJA48 (2012)



## Projection for Jlab 12 GeV

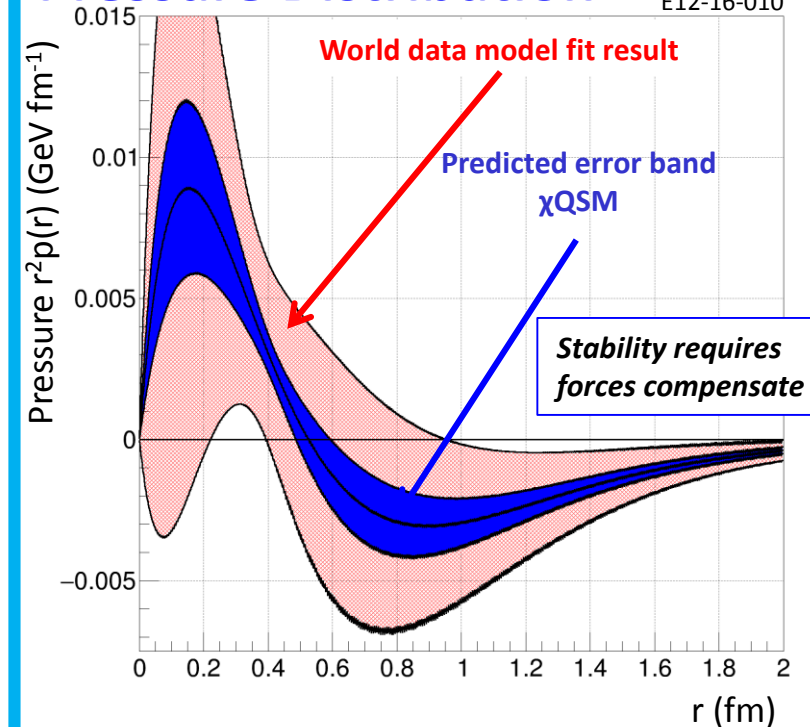
### Transverse profile



### Pressure Distribution

E12-06-119

E12-16-010



REACHING FOR THE HORIZON

The Site of the Wright Brothers' First Airplane Flight

The 2015  
LONG RANGE PLAN  
for NUCLEAR SCIENCE

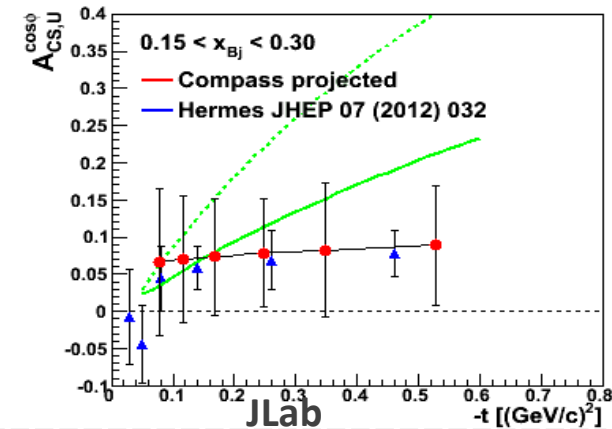
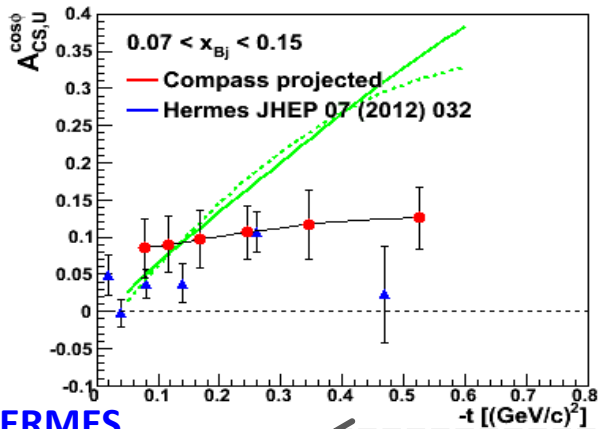
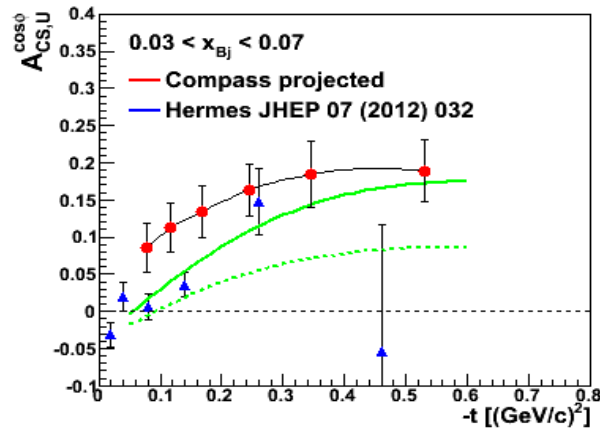
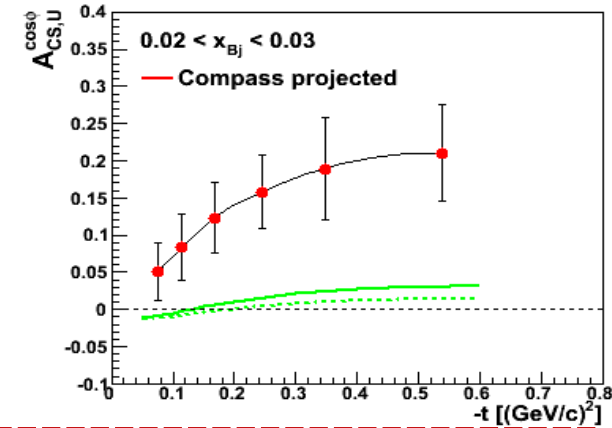
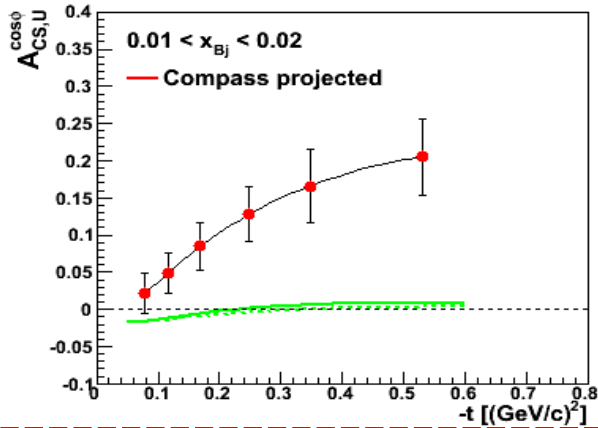
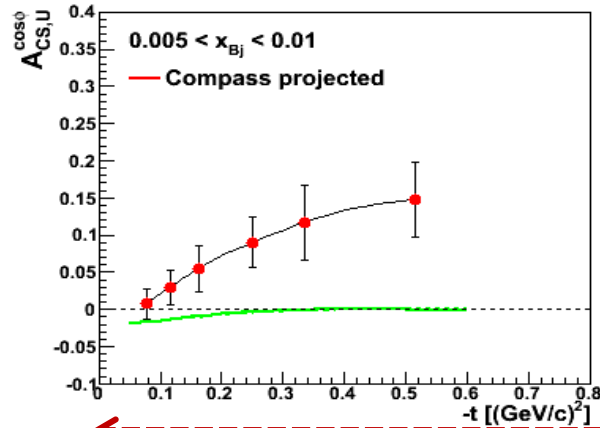


# Beam Charge and Spin Diff. @ COMPASS

$$c_1^I = \text{Re } F_1 \mathcal{H}$$

Predictions with  
VGG and D.Mueller KM10

$\text{Re } \mathcal{H} > 0$  at H1  
 $< 0$  at HERMES  
Value of  $x_B$  for the node?

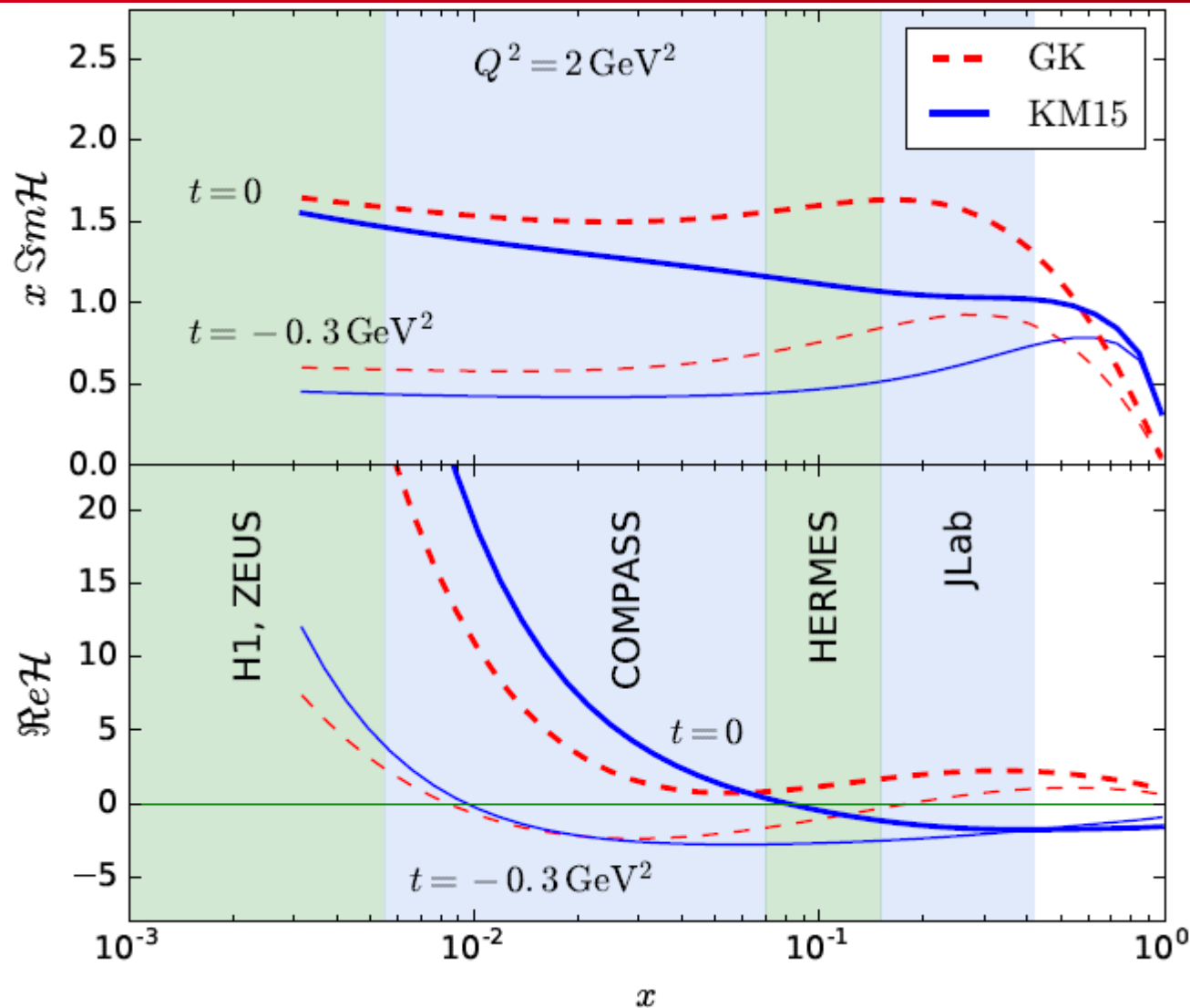


COMPASS 2 years of data  $E_\mu = 160 \text{ GeV}$   $1 < Q^2 < 8 \text{ GeV}^2$

HERMES

JLab

# Present knowledge of the GPD $H$ in global analysis



$\text{Im} H$   
is rather  
well known

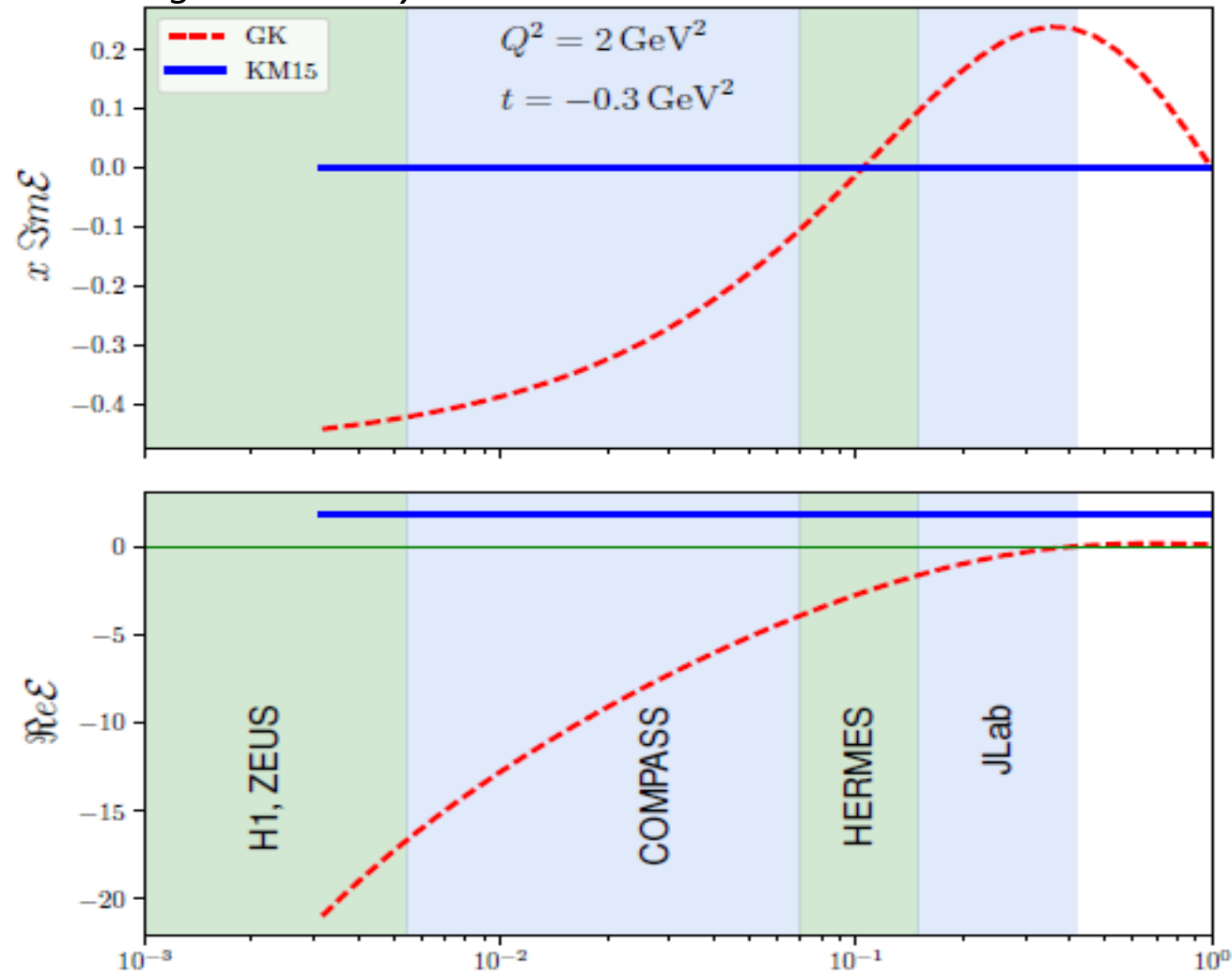
$\text{Re} H$  linked  
to the *d* term  
is still poorly  
constrained

**KM15** K Kumericki and D Mueller [arXiv:1512.09014v1](https://arxiv.org/abs/1512.09014v1)

**GK** S.V. Goloskokov, P. Kroll, EPJC53 (2008), EPJA47 (2011)

# Present knowledge of the GPD E in global analysis

Figure made by D. Mueller and K. Kumericki



$\text{Im} \mathcal{E}$   
is rather unknown

$\text{Re} \mathcal{E}$   
is rather unknown

**KM15** K Kumericki and D Mueller [arXiv:1512.09014v1](https://arxiv.org/abs/1512.09014v1)

**GK** S.V. Goloskokov, P. Kroll, EPJC53 (2008), EPJA47 (2011)

# GPD E at Jlab 11 GeV with CLAS12

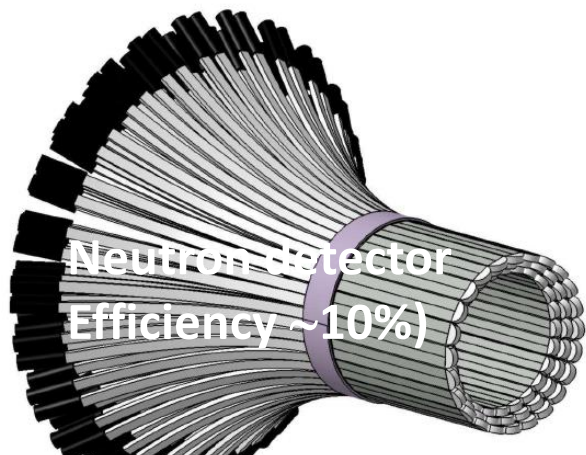
Exp E12-11-003: DVCS on the neutron

Exp E12-12-010: DVCS on a transversely polarized HD-Ice target Pol H = 60% Pol D = 35%

$$\Delta\sigma_{LU}^{\sin\phi} = \text{Im} (F_{1n}\mathcal{H} + \xi(F_{1n} + F_{2n})\tilde{\mathcal{H}} + t/4m^2 F_{2n}\mathcal{E})$$

$$\Delta\sigma_{UT}^{\sin(\phi-\phi_s)\cos\phi} = -t/4m^2 \text{Im} (F_{2p}\mathcal{H} - F_{1p}\mathcal{E})$$

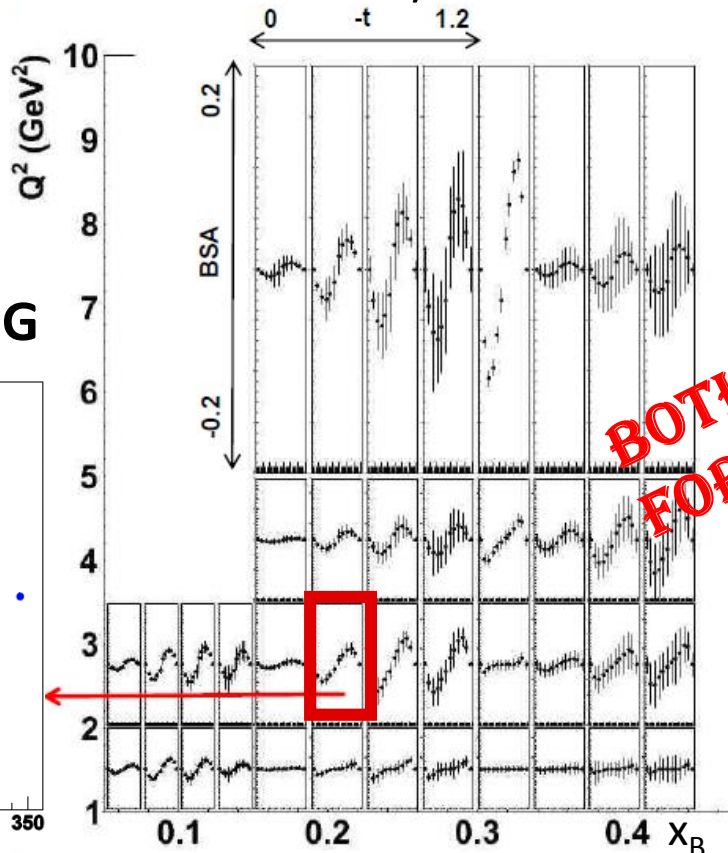
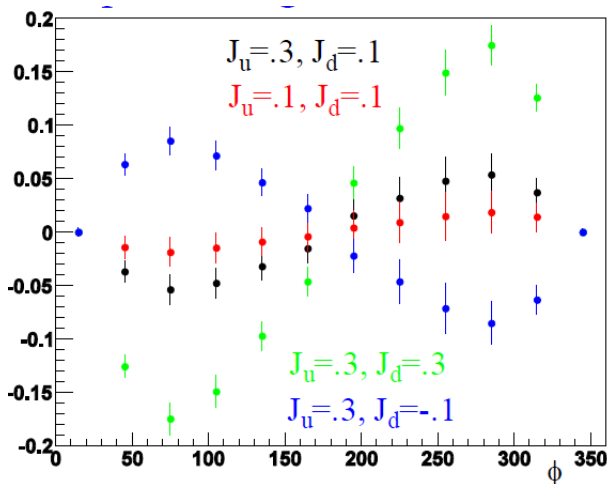
$$\Delta\sigma_{LT}^{\sin(\phi-\phi_s)\cos\phi} = -t/4m^2 \text{Re} (F_{2p}\mathcal{H} - F_{1p}\mathcal{E})$$



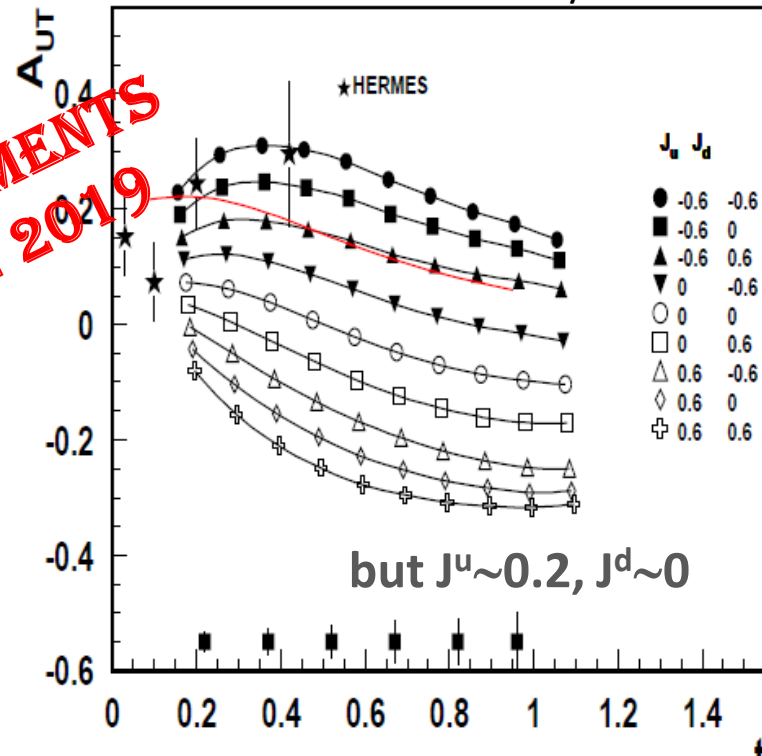
90 days on LD2 target  
Lumi =  $10^{35} \text{ cm}^{-2} \text{ s}^{-1}/\text{nucleon}$

110 days on HD-Ice target  
Lumi =  $5 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}/\text{nucleon}$

Model prediction using VGG



**BOTH EXPERIMENTS FORESEEN IN 2019**





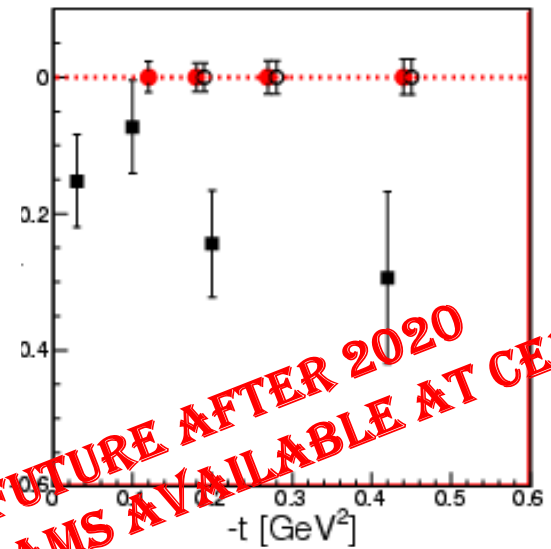
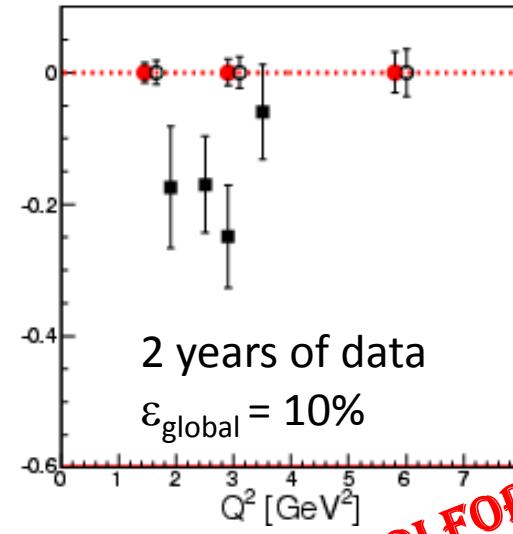
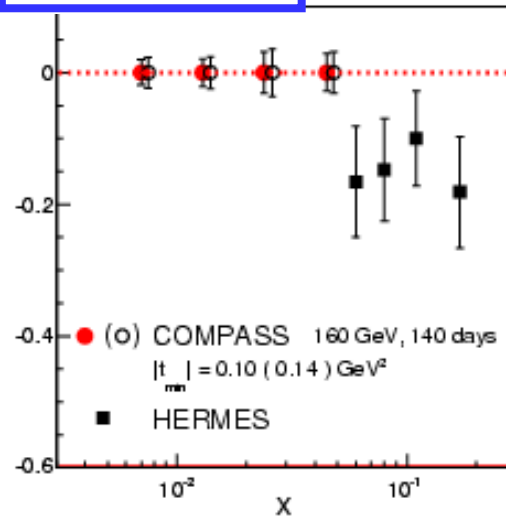
# GPD E at COMPASS 160 GeV with $\mu^+$ and $\mu^-$

$$\mathcal{D}_{CS,T} \equiv \sigma_T(\mu^{+\downarrow}) - \sigma_T(\mu^{-\uparrow})$$

$$\propto \text{Im}(\mathbf{F}_2 \mathcal{H} - \mathbf{F}_1 \mathbf{E}) \sin(\phi - \phi_s) \cos \phi$$

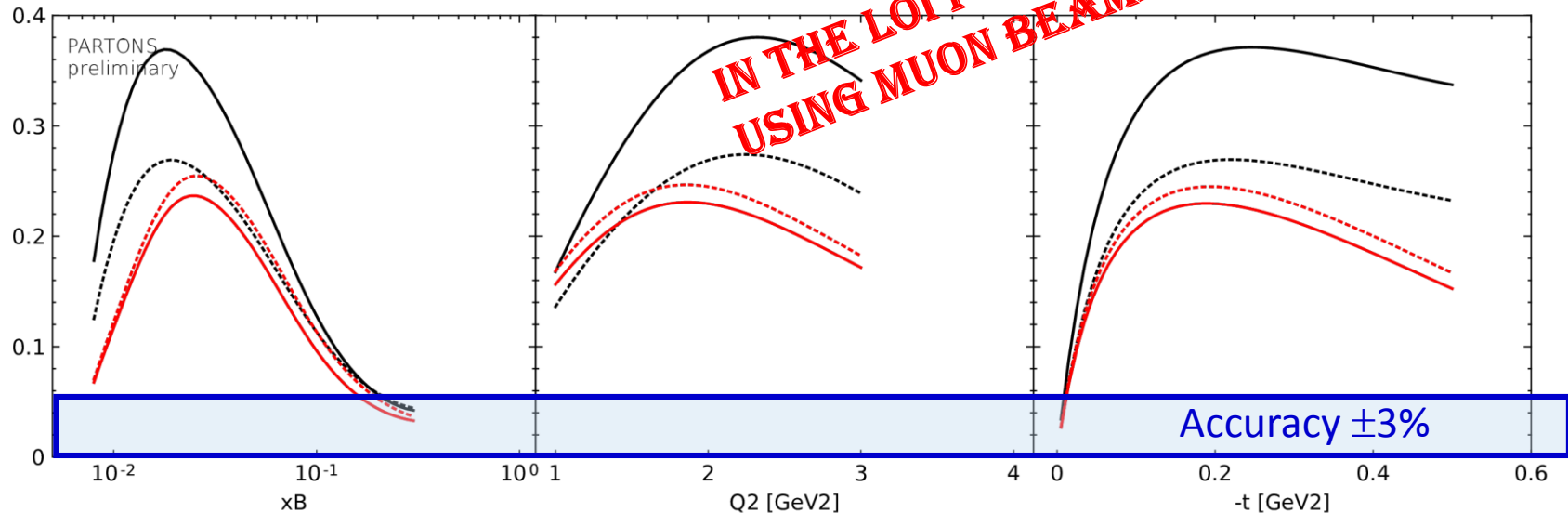
$$A_{CS,T}^{\sin(\phi - \phi_s) \cos \phi}$$

DVCS on a 1.2m long transversely polarized  $\text{NH}_3$  target

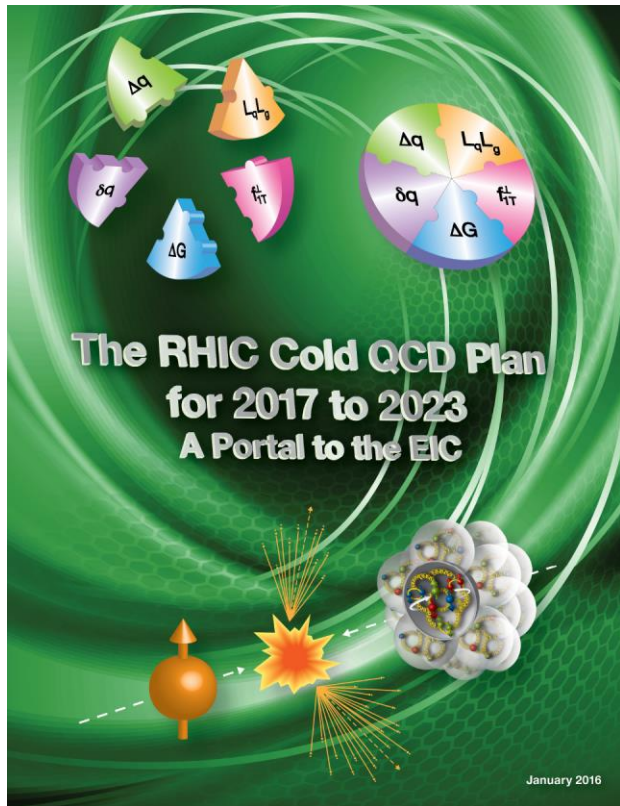


From Pawel Sznajder  
 Using the PARTONS code  
 Formalism at LO

- GK and CFFs@LO
- - - Idem with GPDs E = 0
- VGG and CFFs@LO
- - - Idem with GPDs E = 0



# GPD $E_{\text{gluon}}$ at RHIC in 2017 and 2023



## 2.3.1 Run-2017, Run-2023 and Opportunities with a Future Run at 500 GeV

### *Ultra Peripheral Collisions to access the Generalized Parton Distribution $E_{\text{gluon}}$*

Two key questions, which need to be answered to understand overall nucleon properties like the spin structure of the proton, can be summarized as:

- How are the quarks and gluons, and their spins distributed in space and momentum inside the nucleon?
- What is the role of orbital motion of sea quarks and gluons in building the nucleon spin?

..... RHIC, with its capability to collide transversely polarized protons at  $\sqrt{s}=500$  GeV, has the unique opportunity to measure  $A_N$  for exclusive  $J/\psi$  in ultra-peripheral  $p^\uparrow+p$  collisions (UPC) [99]. The measurement is at a fixed

$Q^2$  of 9 GeV<sup>2</sup> and  $10^{-4} < x < 10^{-1}$ . A nonzero asymmetry would be the first signature of a non-zero GPD  $E$  for gluons, which is sensitive to spin-orbit correlations and is intimately connected with the orbital angular momentum carried by partons in the nucleon and thus with the proton spin puzzle. Detecting one of the scattered polarized protons in “Roman Pots” (RP) ensures an elastic process. ....

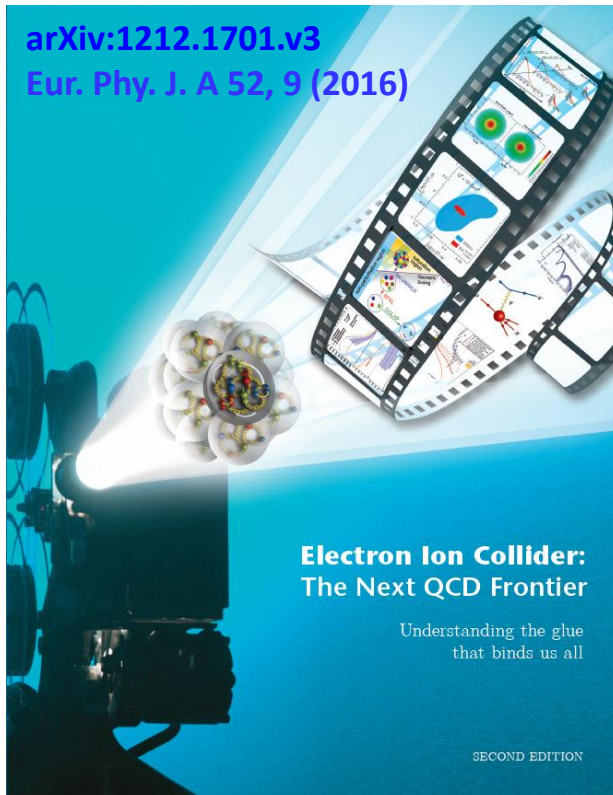
**11k  $J/\psi$  in 2017 ( $p^\uparrow p$  @ 510 GeV) and 13k in 2023 ( $p^\uparrow Au$  @ 200 GeV)  
Important input for the photoproduction of  $J/\psi$  at EIC**

# Key measurements for imaging partons with EIC

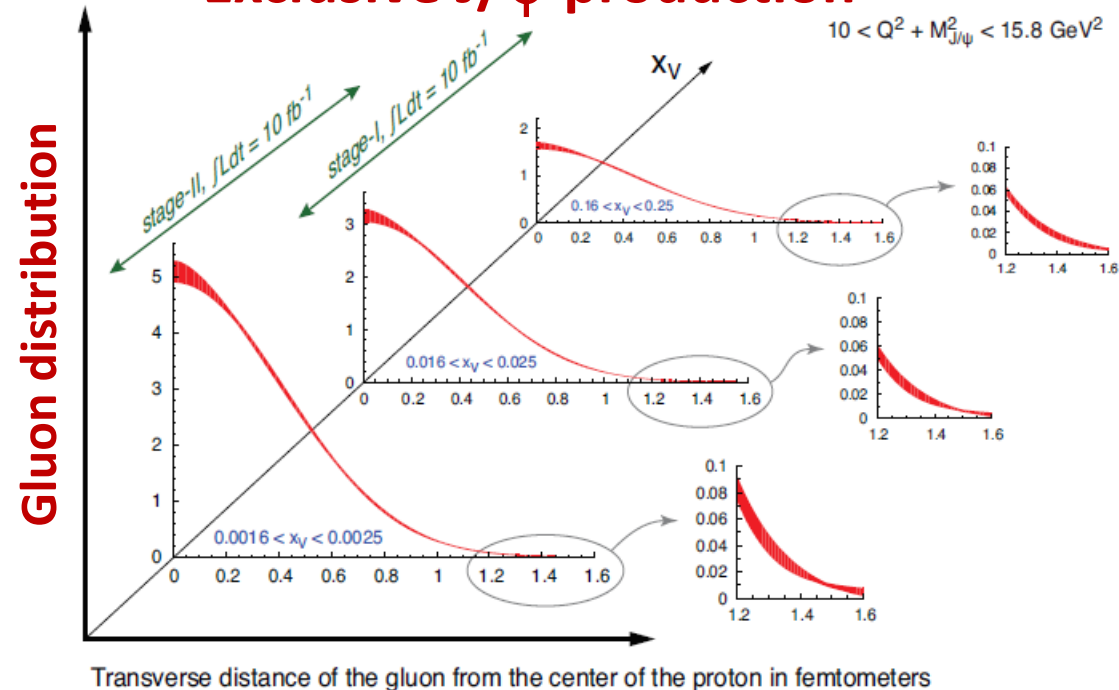
Stage 2  
Ee=20 GeV Ep=250 GeV

Stage 1  
Ee=5 GeV Ep=100 GeV

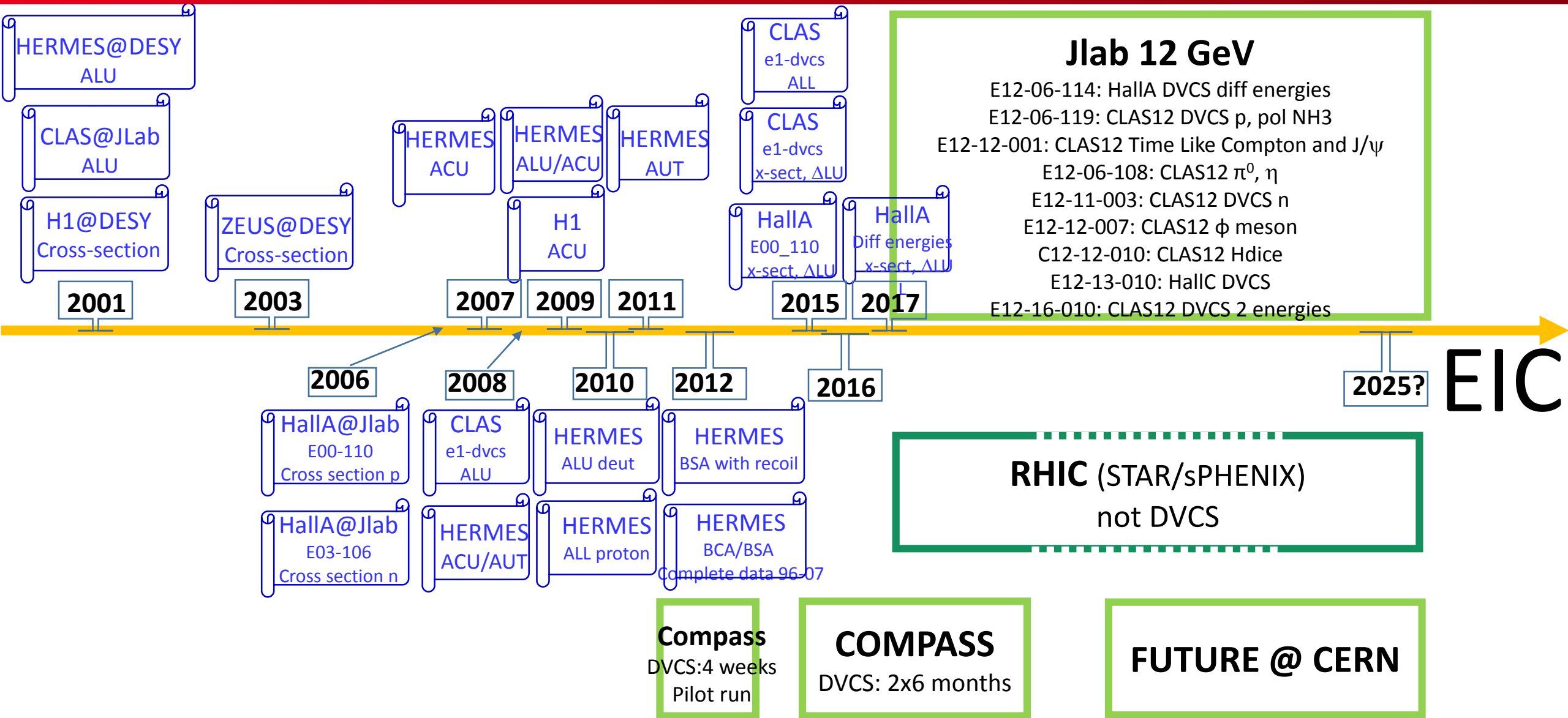
Deliverables	Observables	What we learn	Requirements
GPDs of sea quarks and gluons	DVCS and $J/\Psi, \rho^0, \phi$ production cross section and polarization asymmetries	transverse spatial distrib. of sea quarks and gluons; total angular momentum and spin-orbit correlations	$\int dt L \sim 10$ to $100 \text{ fb}^{-1}$ ; Roman Pots; polarized $e^-$ and $p$ beams; wide range of $x_B$ and $Q^2$ ;
GPDs of valence and sea quarks	electroproduction of $\pi^+, K$ and $\rho^+, K^*$	dependence on quark flavor and polarization	range of beam energies; $e^+$ beam valuable for DVCS



## Exclusive $J/\psi$ production



# DVCS publications and data taking over the years

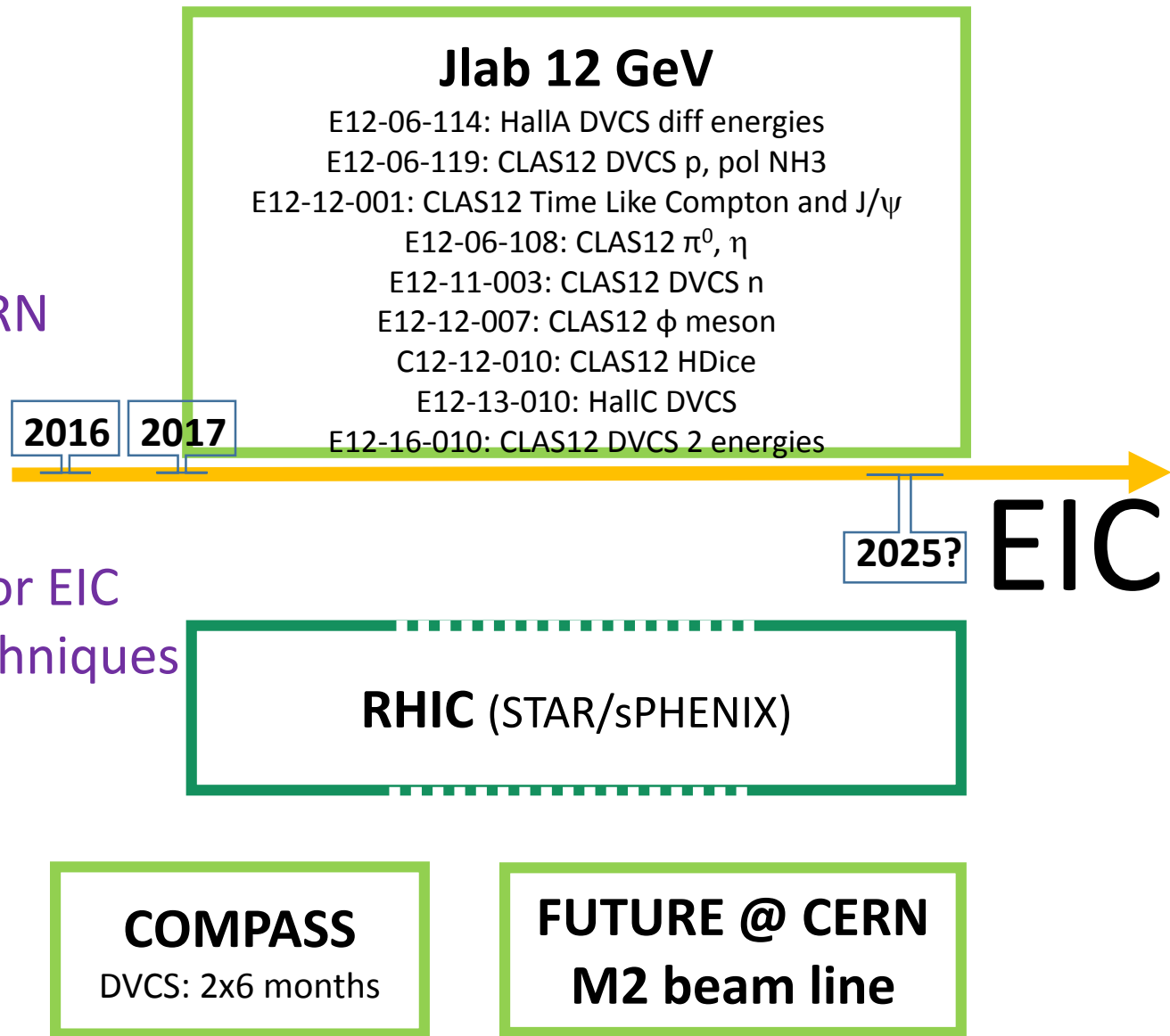


# Conclusions

Jlab 12 GeV will perfectly investigate the valence quarks at large  $x_B$

COMPASS with high energy muon beams at CERN and RHIC will provide first results of sea quarks and gluons at small  $x_B$

All these facilities are physics opportunities prior EIC  
- to preserve knowledge on state of the art techniques  
- to prepare the next generation of leading new experiments at EIC

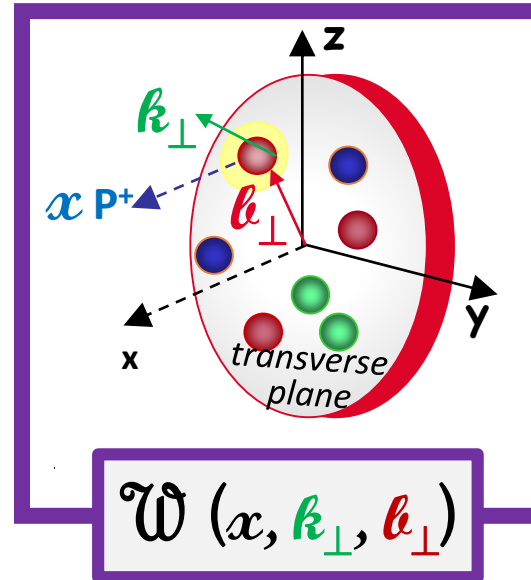
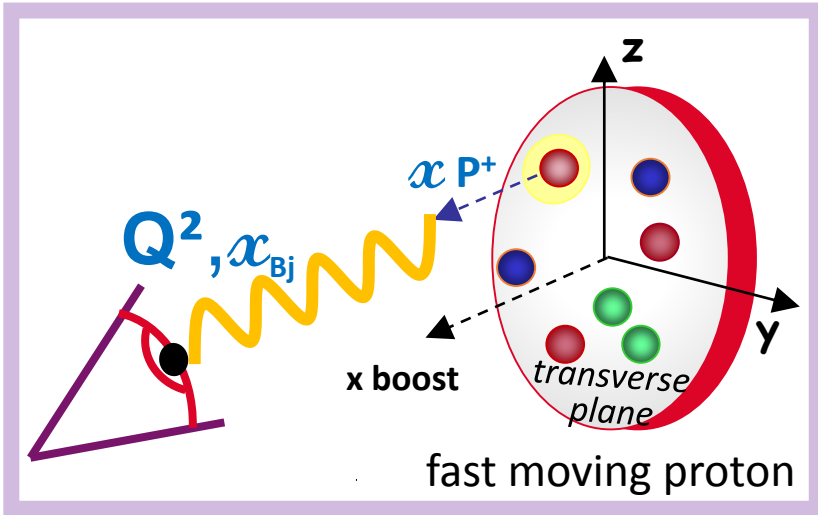




# Proton picture: 1D

→ 1+2D

Ji, PRL91 (2003), Belitsky, Ji, Yuan, PRD69 (2004)  
Lorcé et al, JHEP1105 (2011)



Quantum tomography of the nucleon



The Wigner functions offer unprecedented insight into confinement and chiral symmetry breaking

Parton Distribution Functions PDFs ( $x$ )

Longitudinal momentum

$$q(x) \text{ or } f_1^q(x)$$

Longitudinal spin

$$\Delta q(x) = \vec{q}(x) - \overleftarrow{q}(x)$$

Transverse spin

$$\Delta_T q \text{ or } h_1(x)$$

$$\int dk_{\perp}$$

Transverse momentum

8 TMDs ( $x, k_{\perp}$ )

accessible in SIDIS and Drell-Yan

Transverse position

Impact param.  $q(x, l_{\perp})$

8 GPDs ( $x, \xi, t$ )

accessible

in **exclusive reactions**

**DVCS**: Deeply Virtual Compton Scattering

**HEMP**: Hard Exclusive Meson Production

$$\int dx$$

Form Factors

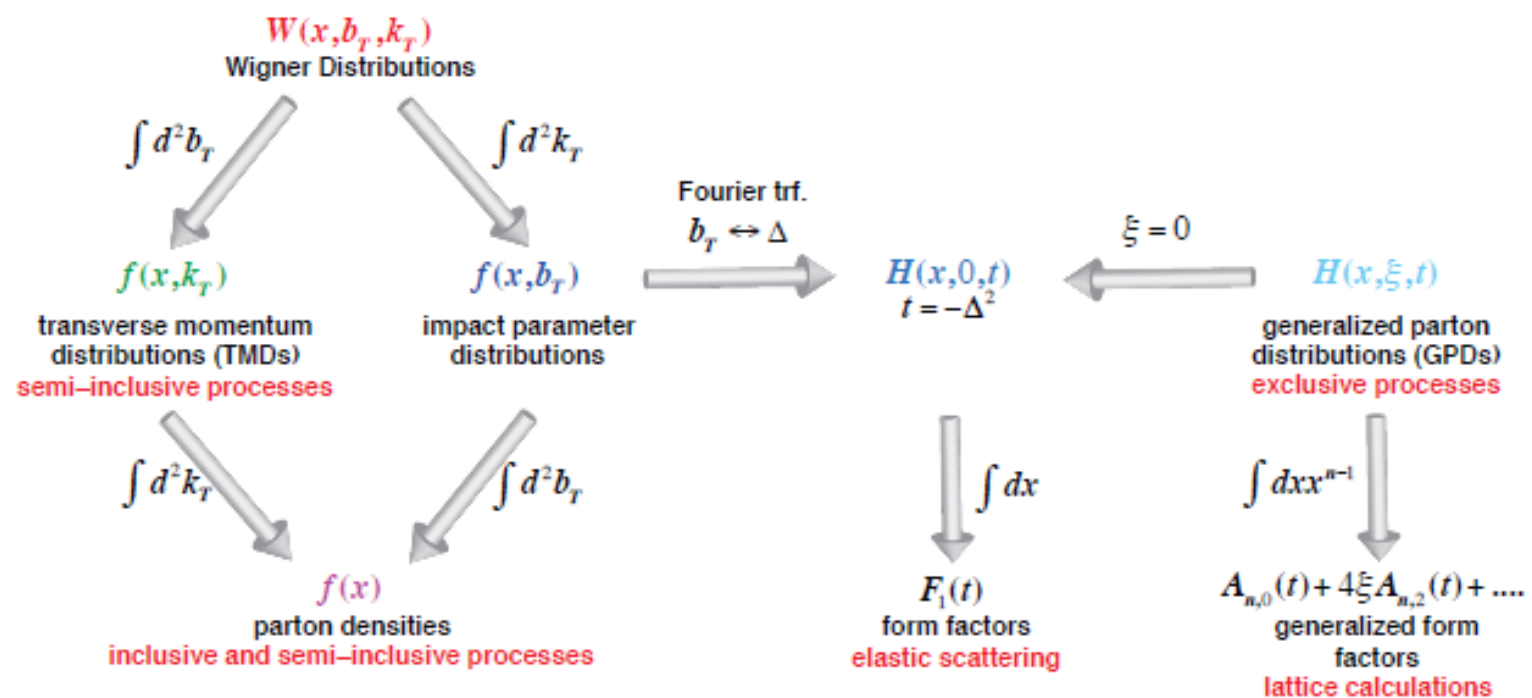
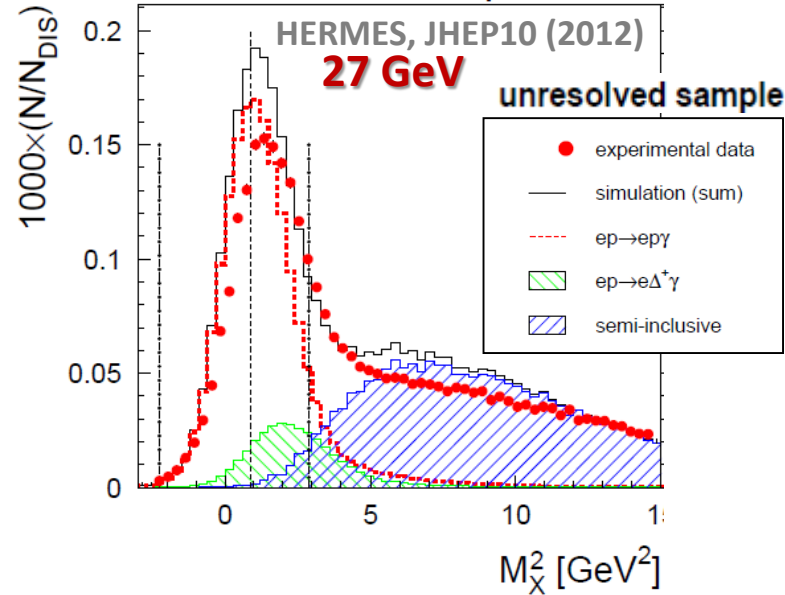
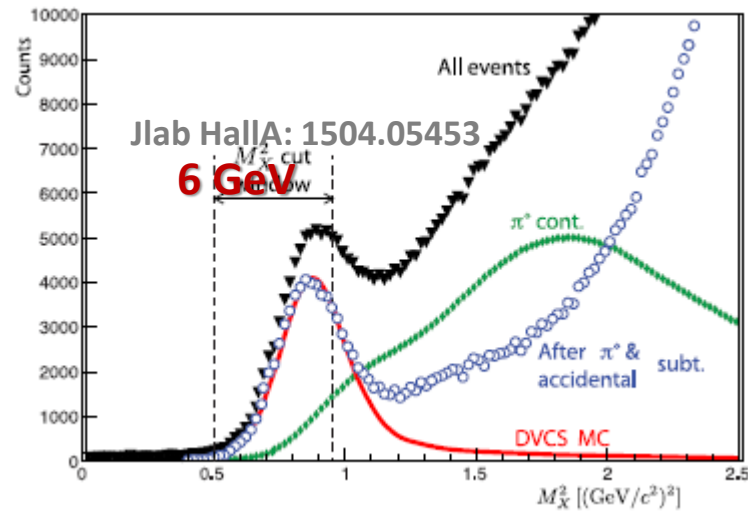


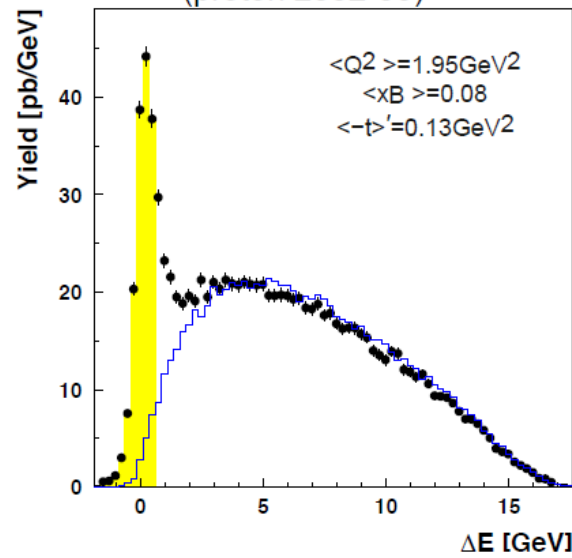
Figure 2.2: Connections between different quantities describing the distribution of partons inside the proton. The functions given here are for unpolarized partons in an unpolarized proton; analogous relations hold for polarized quantities.



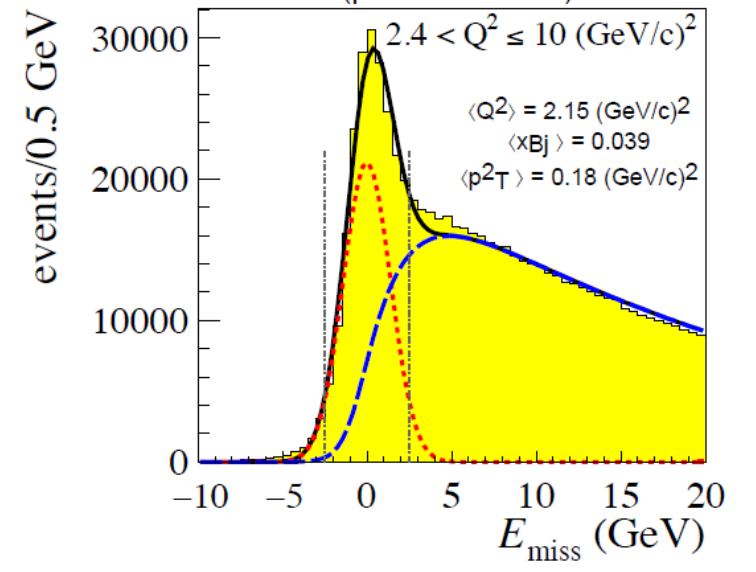
# Exclusivity : $\ell p \rightarrow \ell + \gamma \text{ (or } \rho^0) + p$



HERMES exclusive  $\rho^0$   
 (proton 2002-05)



COMPASS exclusive  $\rho^0$   
 (proton 2007/10)



$$M_x^2 = (P_\ell + P_p - P_\ell' - P_\gamma)^2$$

$\Delta M_x^2$  increases  
 with the beam energy !

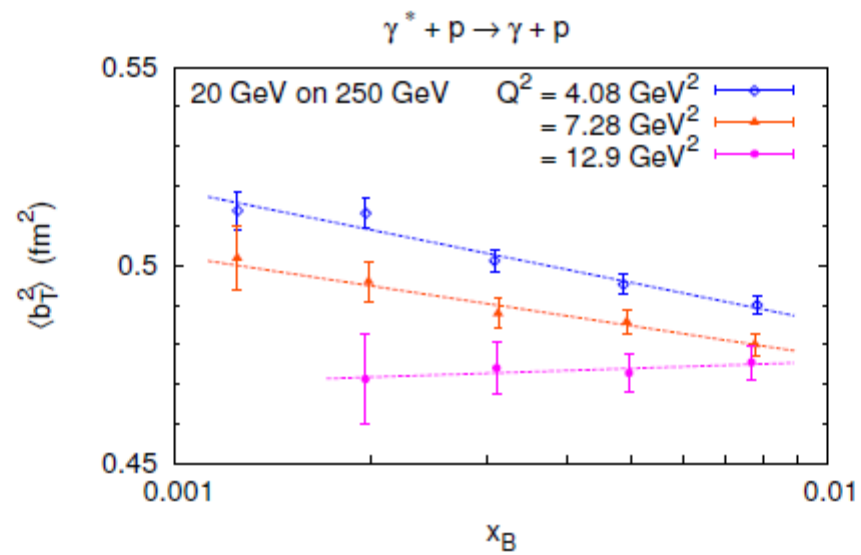


Figure 2.22: Average values of  $b_T^2$  obtained from the DVCS cross section in different bins of  $x_B$  and  $Q^2$ . The assumed luminosity is as for the left panels of figure [2.21](#).