



Newest COMPASS results on longitudinal and transverse nucleon spin structure

Stefano Levorato INFN Trieste
on behalf of the COMPASS collaboration

- The COMPASS experiment at CERN
- Longitudinal asymmetries in DIS
- Hadron multiplicities in SIDIS
- The Structure of the Nucleon (SIDIS): Transversity and TMD
- Unpolarized SIDIS

A selection of the many available results!

Common Muon Proton Apparatus for Structure and Spectroscopy

main task:
study of hadron structure
and spectroscopy

data taking
since 2002

participants:
~240 scientists
28 institutions from
12 countries

LHC

COMPASS

SPS

COMPASS



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LHC

Rich and diversified physics programme :

- Nucleon structure with 160 GeV μ
- Hadron Spectroscopy with 190 GeV π

On transversely, longitudinally polarized target,
LH₂ or nuclei targets:

Measurement of elicity, transversity, Λ , GPD,
meson spectroscopy π, K polarizabilities

Not all covered in this talk !!!

COMPASS





2002	nucleon structure with	160 GeV μ	L&T	polarised deuteron target
2003	nucleon structure with	160 GeV μ	L&T	polarised deuteron target
2004	nucleon structure with	160 GeV μ	L&T	polarised deuteron target
2005	<i>CERN accelerators shut down</i>			
2006	nucleon structure with	160 GeV μ	L	polarised deuteron target
2007	nucleon structure with	160 GeV μ	L&T	polarised proton target
2008	<i>hadron spectroscopy</i>	190 GeV π		
2009	<i>hadron spectroscopy</i>	190 GeV π		
2010	nucleon structure with	160 GeV μ	T	polarised proton target
2011	nucleon structure with	190 GeV μ	L	polarised proton target
2012	Primakoff & DVCS / SIDIS test			
2013	<i>CERN accelerators shut down</i>			
2014	Test beam Drell-Yan process with π beam and T polarised proton target			
2015	Drell-Yan process with π beam and T polarised proton target			
2016	DVCS / SIDIS with μ beam and unpolarised proton target			
2017	DVCS / SIDIS with μ beam and unpolarised proton target			



the COMPASS spectrometer

- high energy beams
- large angular acceptance
- broad kinematical range

two stages spectrometer

- Large Angle Spectrometer (SM1)
- Small Angle Spectrometer (SM2)

variety of tracking detectors

to cope with different particle flux from $\theta = 0$ to $\theta \approx 200$ mrad with a good azimuthal acceptance

calorimetry, μ ID

RICH

SM1

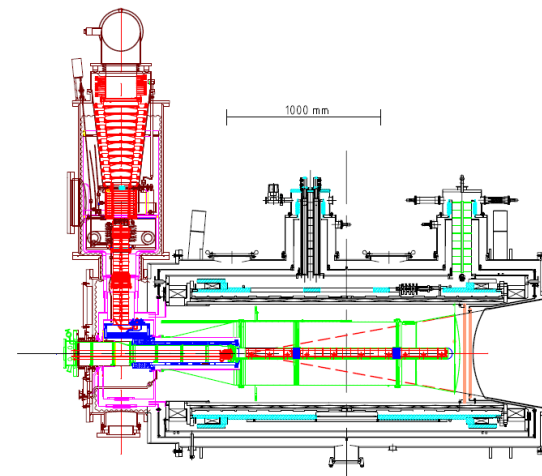
SM2

~ 50 m

Polarised Target

Spectrometer NIMA 577 (2007) 455

μ beam



- Two/three target cells, oppositely polarized
- 180 mrad geometrical acceptance
- 2.5T solenoid field
- Low temperature 50mK
- Regular polarization reversals by field rotation
- ${}^6\text{LiD}$ (Longitudinal deuteron polarization: 50%)
- NH_3 (Longitudinal proton polarization: 90%)



Longitudinal polarization

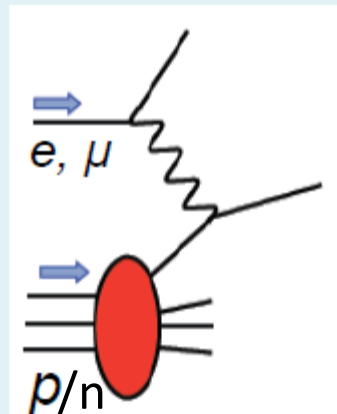


Transverse polarization





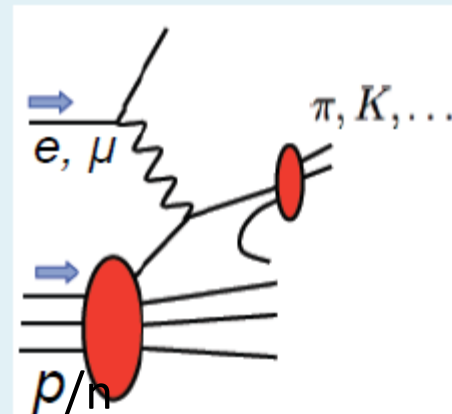
- The COMPASS experiment at CERN
 - Longitudinal asymmetries in DIS
 - Pion and Kaon multiplicities
 - The Structure of the Nucleon : Transversity and TMD
 - Unpolarized SIDIS
- A selection of the many available results!



DIS:

$$\Delta q + \Delta \bar{q}$$

$$\Delta g \text{ (From } Q^2 \text{ evolution of } g_1 \text{)}$$



SIDIS:

$$\Delta q, \Delta \bar{q}$$

$$\Delta g$$

DIS variables

- Photon virtuality: $Q^2 = -q^2$
- Bjorken scaling variable: $x = \frac{Q^2}{2 \cdot P \cdot q}$
- Relative photon energy: $y = \frac{E - E'}{E}$

SIDIS variables

$$z = \frac{P \cdot P_h}{P \cdot q} =_{LAB} \frac{E_h}{E - E'}$$

Hadron transverse momentum p_T^h




Helicity measurement in DIS process

$$S_N = \frac{1}{2} = \frac{1}{2} \Delta \Sigma + \Delta G + L_q + L_g$$

$$\Delta \Sigma(Q^2) = \int_0^1 dx [\Delta u + \Delta \bar{u} + \Delta d + \Delta \bar{d} + \Delta s + \Delta \bar{s}](x, Q^2)$$

$$\Delta G(Q^2) = \int_0^1 dx \Delta g(x, Q^2)$$

Helicity PDFs: $\Delta q(x, Q^2) =$ 

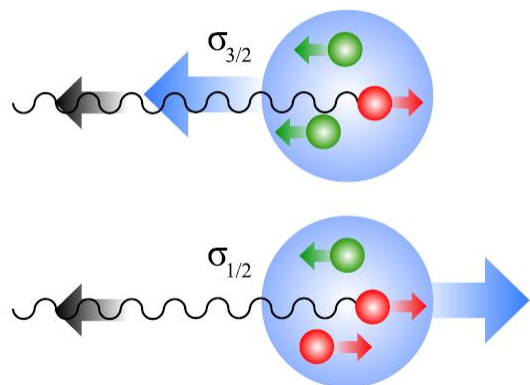
The goal is the determination of $\Delta q(x, Q^2)$, ΔG



► **Inclusive cross section**

$$\frac{d^2\sigma}{d\Omega dE'} \sim \underbrace{c_1 F_1(x, Q^2) + c_2 F_2(x, Q^2)}_{\text{spin independent}} + \underbrace{c_3 g_1(x, Q^2) + c_4 g_2(x, Q^2)}_{\text{spin dep. structure functions}}$$

$$g_1(x, Q^2) = \frac{1}{2} \sum_q e_q^2 \Delta q(x) \approx A_1(x, Q^2) \cdot F_1(x, Q^2)$$



Absorption of polarised photons

$$\sigma_{1/2} \sim q^+ \quad \sigma_{3/2} \sim q^-$$

$$q(x) = q^+(x) + q^-(x)$$

$$\Delta q(x) = q^+(x) - q^-(x)$$

$q(x)$ = Quark momentum DF

$\Delta q(x)$ = Difference in DF of quarks with spin parallel or antiparallel to the nucleon's spin in a longitudinally polarized nucleon;

$$A_1(x, Q^2) = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}} \stackrel{\text{LO}}{=} \frac{\sum_q e_q^2 \Delta q(x, Q^2)}{\sum_q e_q^2 q(x, Q^2)}$$

$$A_{\text{exp}} = \frac{N_u - N_d}{N_u + N_d}$$



Final sample: 135 million events

Data at $E = 160$ GeV (from 2002–2004) published [PLB 647 \(2007\) 8](#)

Data at $E = 160$ GeV (from 2006)

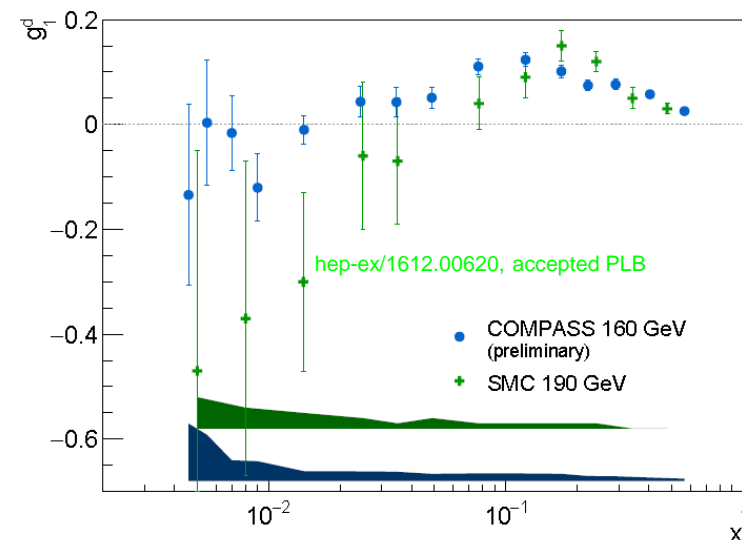
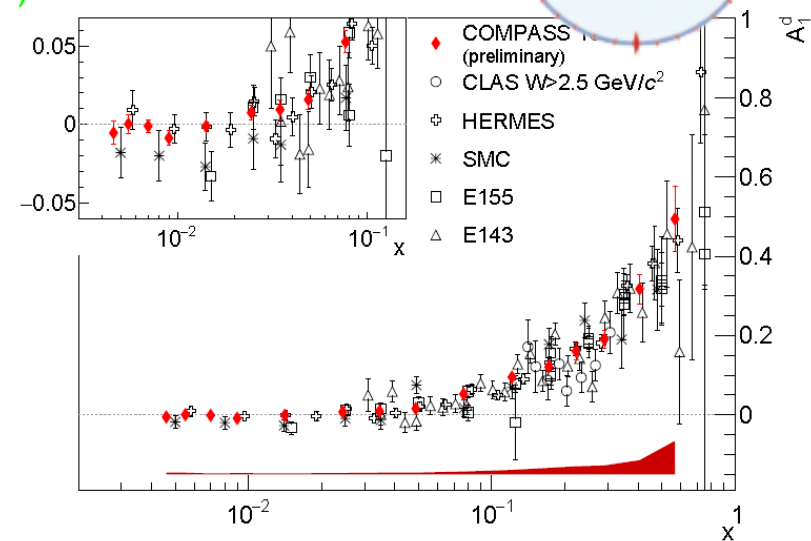
- Good agreement with world data
- Small statistical uncertainty at low x
- Compatible with zero at low x

- $$g_1^d(x, Q^2) = \frac{F_2^d(x, Q^2)}{2x(1+R(x, Q^2))} A_1^d(x, Q^2)$$

- F_2 from SMC [PRD 58 \(1998\) 11201](#)

- R1998 [PLB 452 \(1999\) 194](#)
used with improvements

Good agreement $A_1^d(x)$ and of $g_1^d(x)$ with world data
 $g_1^d(x)$ compatible with zero at lowest measured values of x ,
 contrary to hints from SMC

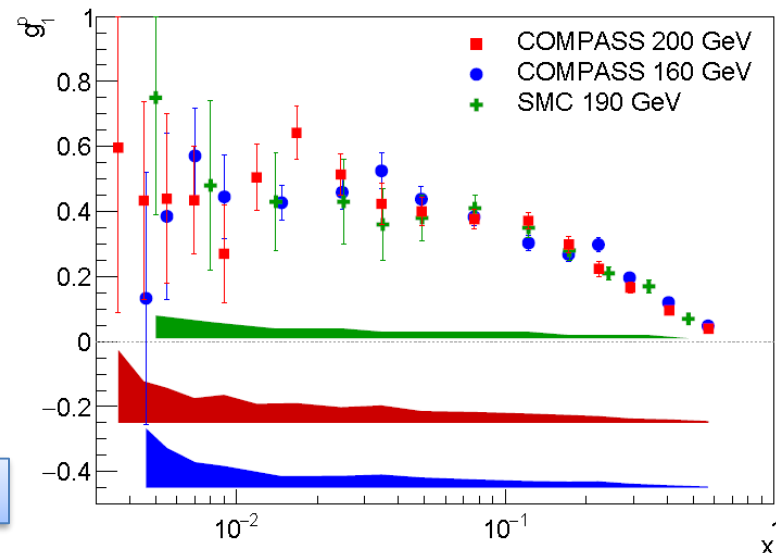
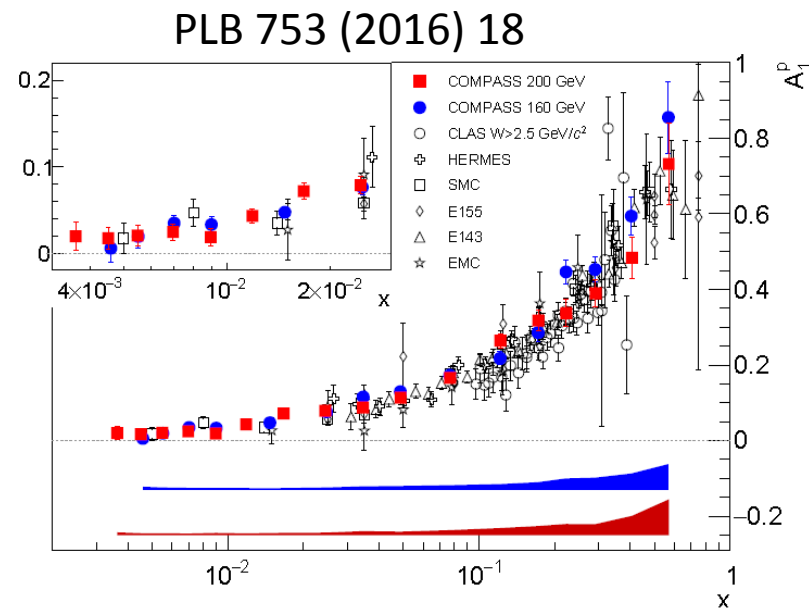


Final sample: 85 million events @ 160 GeV
+ 77 million events @ 200 GeV

- 2007 results already published
PLB 690 (2010) 466
- Increased beam energy in 2011
160 GeV \rightarrow 200 GeV
- Higher Q^2 and lower x reached
- ^{14}N correction applied
- Good agreement

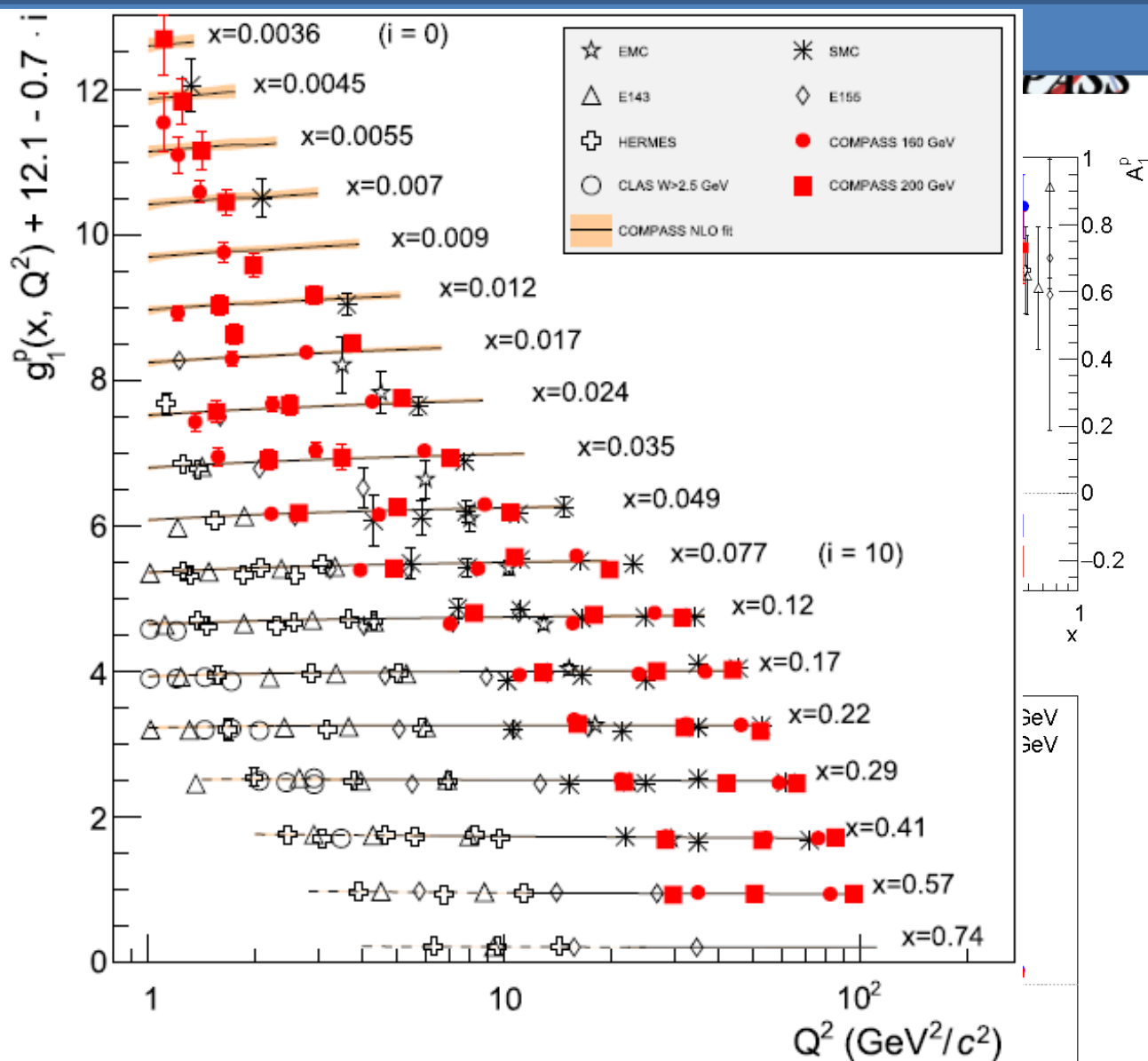
$$g_1^p(x, Q^2) = \frac{F_2^p(x, Q^2)}{2x(1+R(x, Q^2))} A_1^p(x, Q^2)$$

$g_1^p(x)$ clearly positive at lowest measured values of x



Final sample: 85 million + 77 million events @ 2

- 2007 results already published in PLB 690 (2010) 466
- Increased beam energy from 160 GeV → 200 GeV
- Higher Q^2 and lower x
- ^{14}N correction applied
- Good agreement with previous data
- $g_1^p(x, Q^2) = \frac{F_2^p}{2x(1-x)}$



From COMPASS data alone (and a_8 from PRD 82 (2010) 114018):

$$a_0(Q_2 = 3 \text{ (GeV/c)}_2) = 0.320 \pm 0.02_{\text{stat}} \pm 0.04_{\text{syst}} \pm 0.05_{\text{evol}}$$

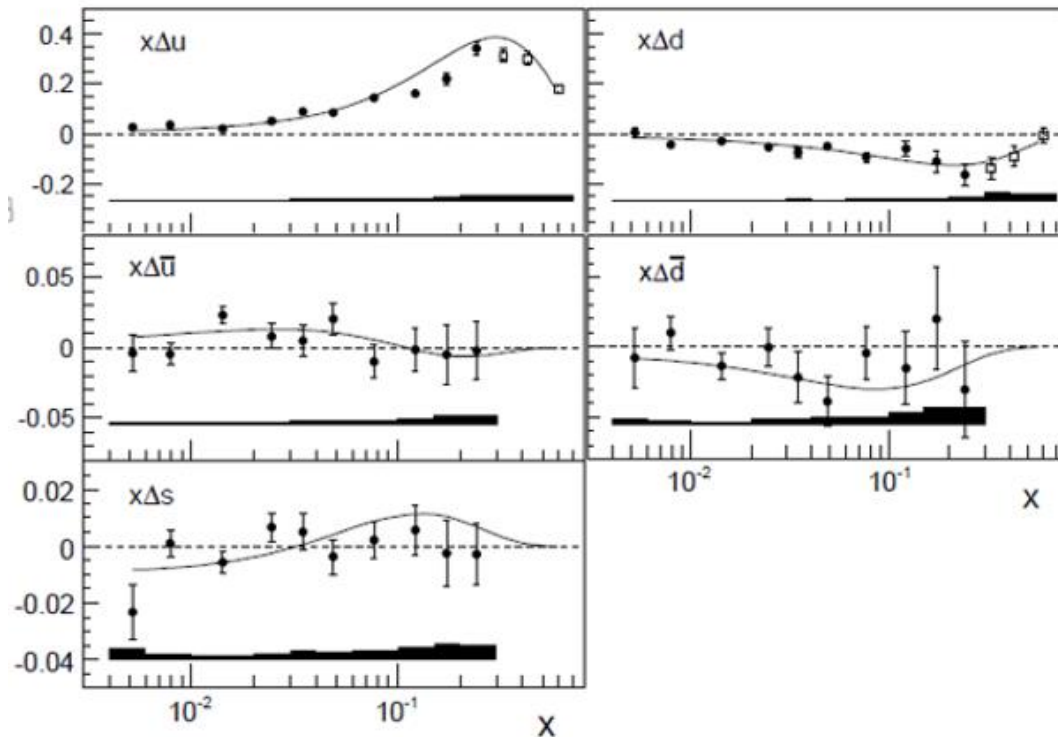
(consistent with value from the COMPASS NLO QCD fit of world data).

In MS identified with total contribution of quark helicities to the nucleon spin



To perform flavor separation SIDIS is needed

$$A_1^h = \frac{\sum_q e_q^2 \Delta q(x) \int D_q^h(z) dz}{\sum_q e_q^2 q(x) \int D_q^h(z) dz}$$



PLB 693 (2010) 227

→ Results for Δs depend very much on the strange quark FFs used

Basic concept

▶ measured:

$$A_1^d, A_{1d}^{K^\pm}, A_{1d}^{\pi^\pm}, A_1^p, A_{1p}^{K^\pm}, A_{1p}^{\pi^\pm}$$

▶ determined:

$$\Delta u, \Delta \bar{u}, \Delta d, \Delta \bar{d}, \Delta s = \Delta \bar{s}$$

▶ inputs:

unpol. LO PDFs (MRST04)
LO FFs (DSS)

▶ curves: DSSV param.

▶ results: $\Delta s \geq 0$??



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- **Hadron multiplicities**
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A selection of the many available results!



Fragmentation functions (FF, D_q^h) describe parton fragmentation into hadrons → needed in analyses which deal with a hadron(s) in the final state

In Leading Order QCD D_q^h describes probability density for a quark of flavour q to fragment into hadron of type h

SIDIS data are crucial to understand quark fragmentation process

Hadron multiplicities can be expressed in terms of parton distribution functions (pdfs) and fragmentation functions (FFs), in **LO pQCD** this reads:

$$\frac{dM^h(x, z, Q^2)}{dz} = \frac{\sum_q e_q^2 q(x, Q^2) D_q^h(z, Q^2)}{\sum_q e_q^2 q(x, Q^2)}$$

quark pdfs
quark to hadron FFs

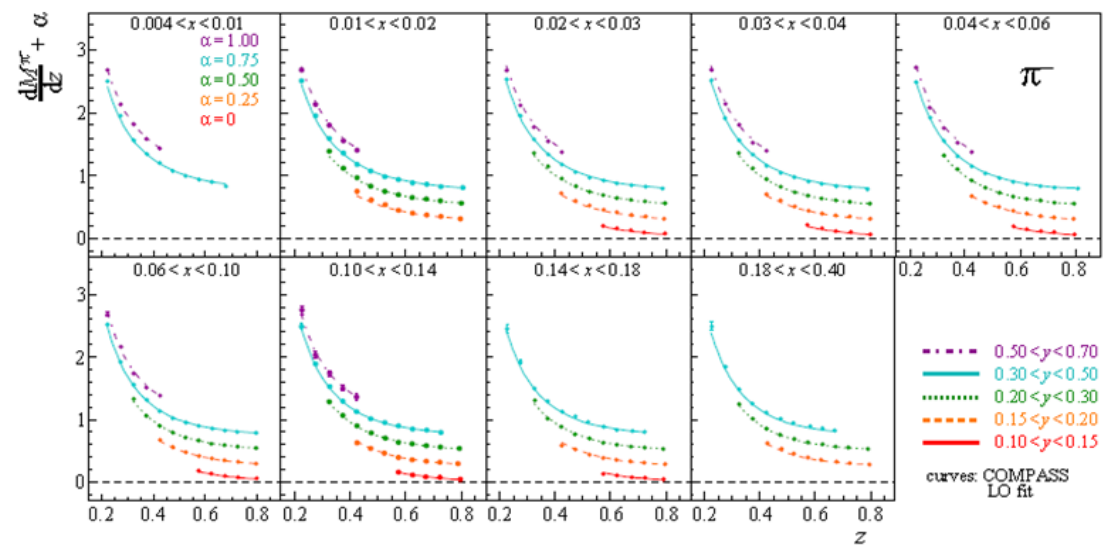
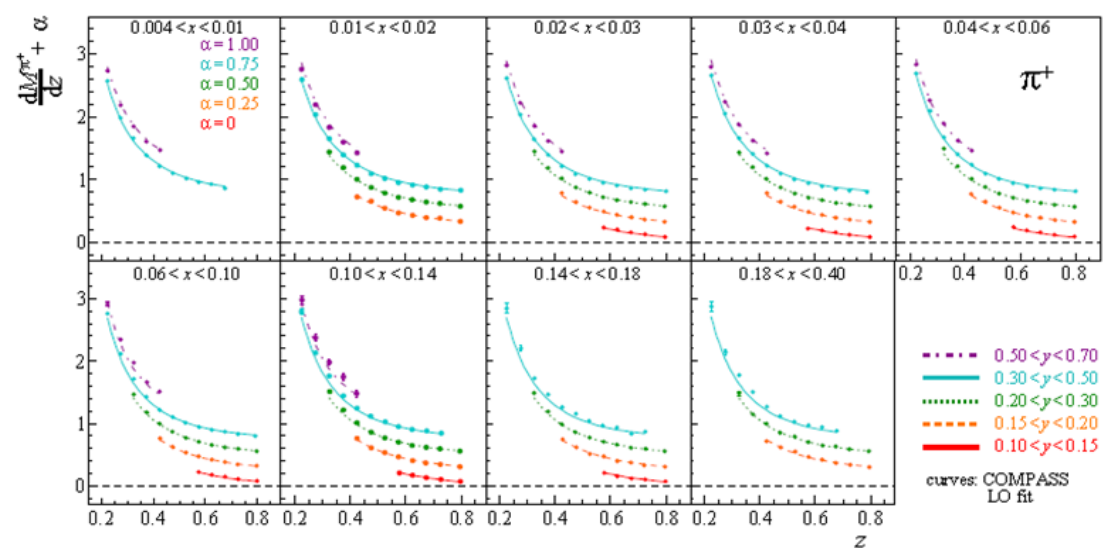
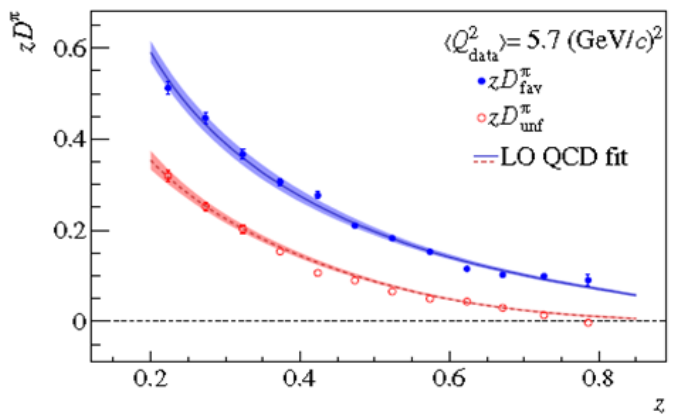


COMPASS extracted π^\pm multiplicities

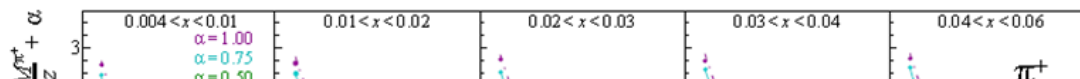
Results published in
PLB 764 (2017) 001

COMPASS performed LO fit,
using HKNS FF programme

Results agrees with world FFs.
As expected $D_{fav} > D_{unf}$



COMPASS extracted π^\pm

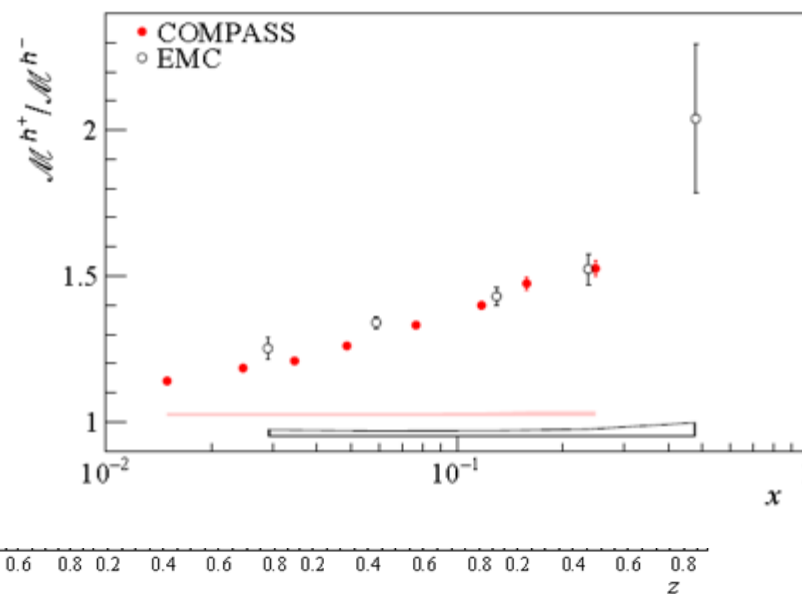
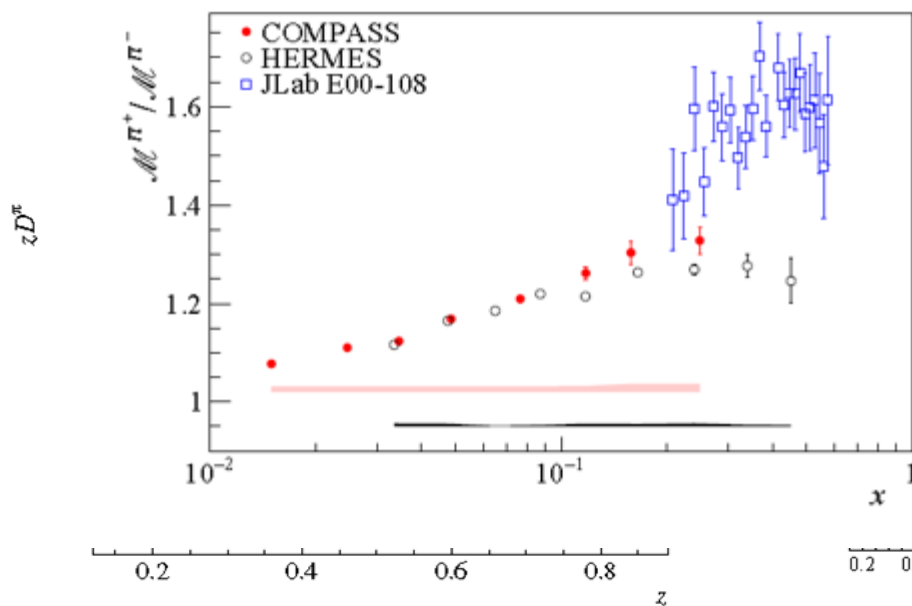


The ratio of π^+/π^- is interesting to study due to significant cancellation of experimental systematic errors

Here, a good agreement between HERMES and COMPASS

Difference between HERMES and JLab likely explained by different W

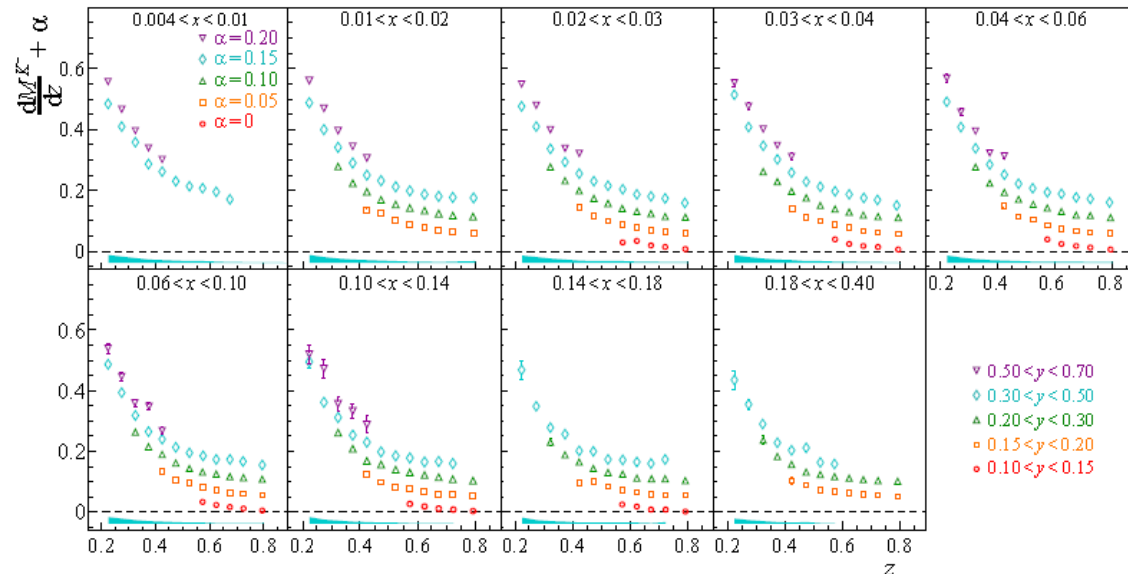
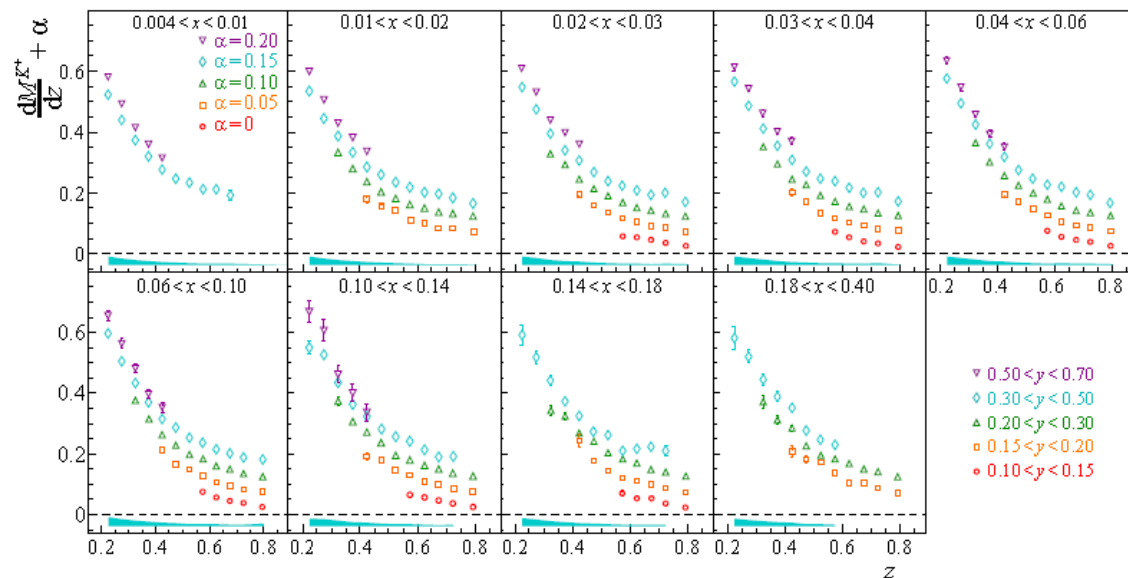
Good agreement between COMPASS and EMC data for unidentified hadrons



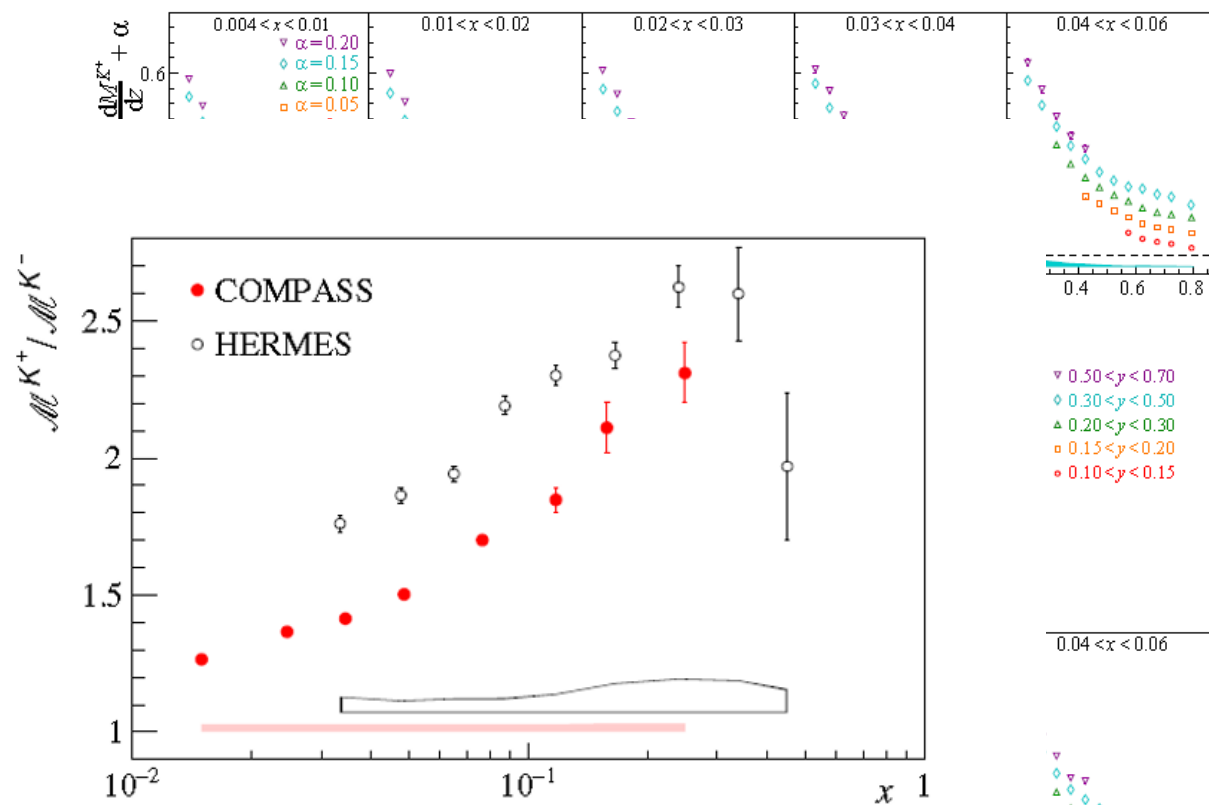
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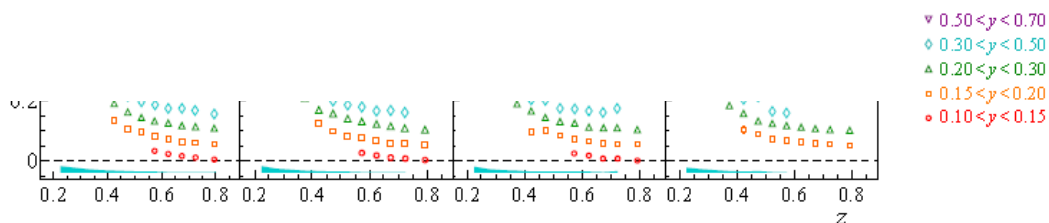
- COMPASS extracted Kaon multiplicities
- More than 620 data points
- Recently published in [PLB 767 \(2017\) 133](#)



- COMPASS extracted Kaon multiplicities
- More than 620 data
- Recently published in *PLB* 767 (2017) 133



There are large differences observed between COMPASS and HERMES for the multiplicity ratio (which agrees for π case)





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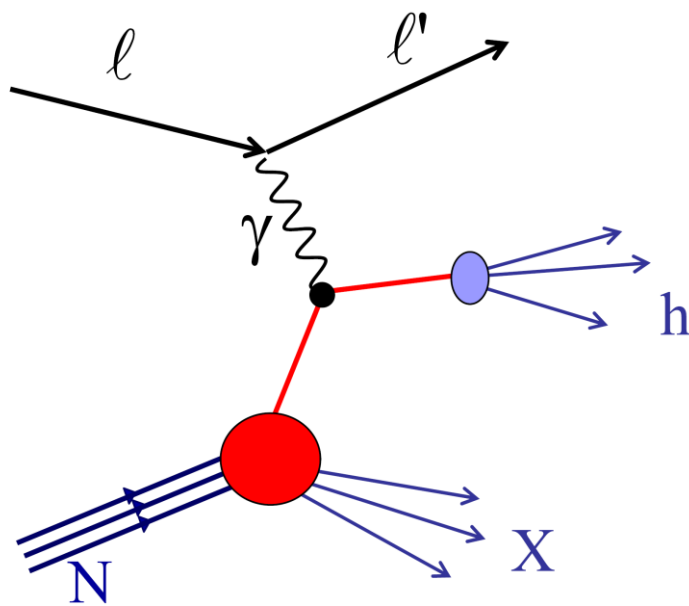
Taking into account the quark intrinsic transverse momentum k_T , at leading order other 6 TMD PDFs are needed for a full description of the nucleon structure

		nucleon polarisation			
		U	L	T	
quark polarisation	U	f_1 number density q		f_{1T}^\perp - Sivers	$\Delta_0^T q$
	L		g_1 - helicity Δq	g_{1T} -	
	T	h_1^\perp - Boer Mulders	h_{1L}^\perp -	h_1 - transversity h_{1T}^\perp -	$\Delta_T q$

SIDIS gives access to all of them



hard interaction of a lepton with a nucleon via virtual photon exchange

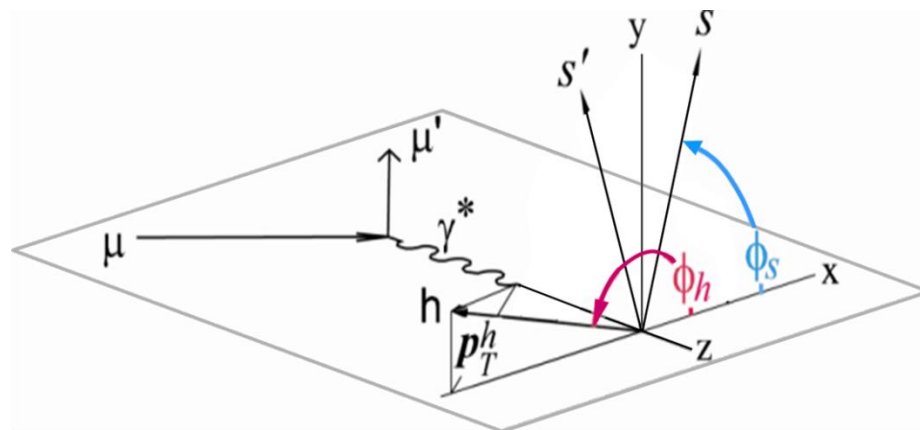


$$x = \frac{Q^2}{2P \cdot q} \quad y = \frac{P \cdot q}{P \cdot \ell} =_{LAB} \frac{E - E'}{E}$$

$$Q^2 = -q^2 \quad W^2 = (P + q)^2$$

$$z = \frac{P \cdot P_h}{P \cdot q} =_{LAB} \frac{E_h}{E - E'}$$

$$\sigma^{lN \rightarrow lhX} \propto \sum_q f(x) \otimes \sigma^{lq \rightarrow lq} \otimes D_q^h(z)$$





$$\begin{aligned}
 \frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = & \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right. \\
 & + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \\
 & + S_{\parallel} \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[\sqrt{1-\varepsilon^2} \right. \\
 & + |S_{\perp}| \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \\
 & \left. \left. + |S_{\perp}| \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \right. \right. \\
 & \left. \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},
 \end{aligned}$$

14 independent azimuthal modulations

amplitudes of the modulations
 → TMD PDFs



$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right.$$

$$+ \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h}$$

$$+ S_{\parallel} \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[\sqrt{1-\varepsilon^2} \right.$$

$$+ |S_{\perp}| \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \right.$$

$$\left. \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},$$

14 independent azimuthal modulations

amplitudes of the modulations
→ TMD PDFs

SIDIS

- allows to disentangle the effects related to the different TMD PDFs and to access all of them
- by identifying the final state hadrons and using different targets allows for flavour separation
→ *very powerful tool*

all the amplitudes (AA) have been measured in COMPASS



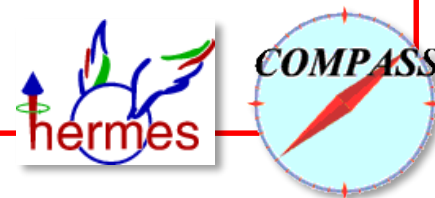
some SIDIS results on

TRANSVERSITY and TMD PDFs

MAJOR RESULT:

in the past 10 years 2 of these new PDF's have been measured
and shown to be different from zero

by COMPASS and HERMES



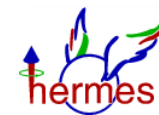
the Transversity PDF amplitude of the sine modulation in $\phi_h + \phi_s - \pi$
Collins asymmetry $\sim h_1 \otimes H_1^\perp$

the Sivers PDF amplitude of the sine modulation in $\phi_h - \phi_s$
Sivers asymmetry $\sim f_{1T}^\perp \otimes D_1$

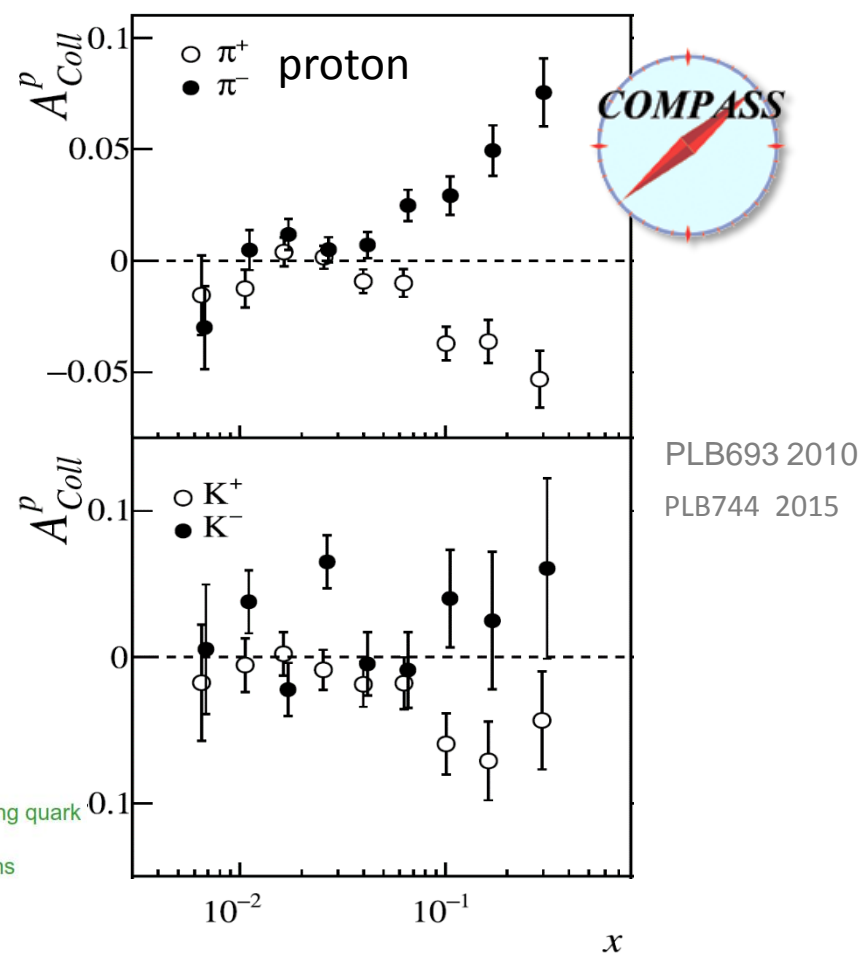
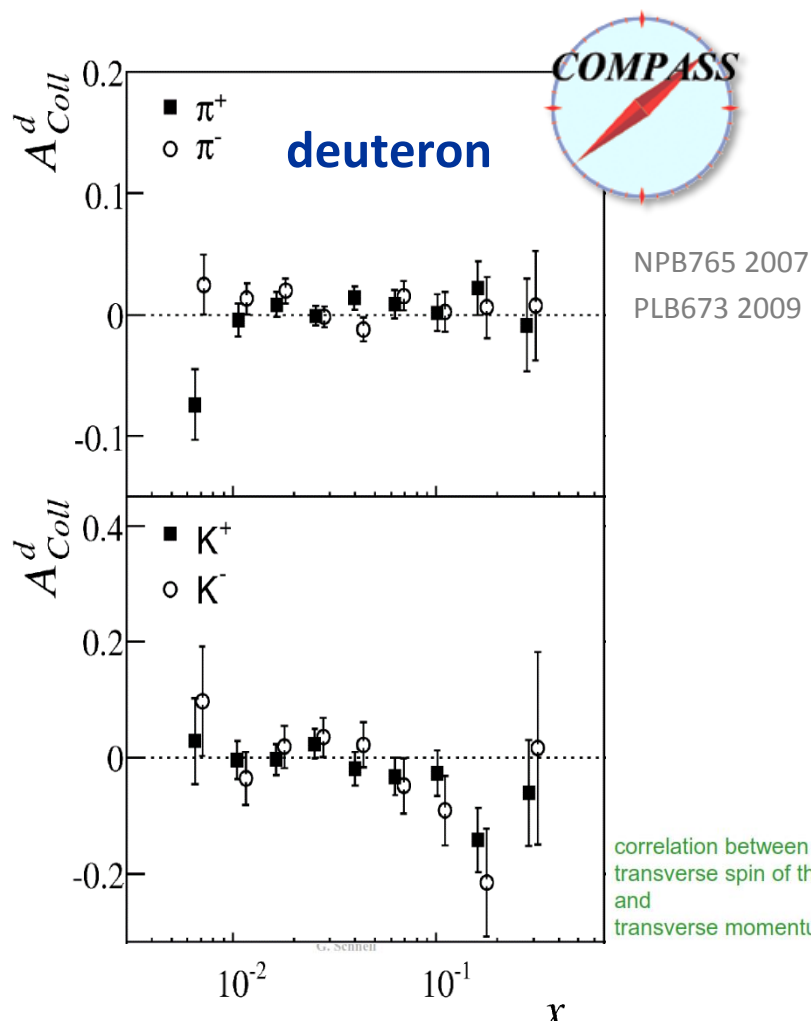
**A STEP TOWARDS
THE 3-D STRUCTURE OF THE NUCLEON**

$$\sim h_1 \otimes H_1^\perp$$

2004: first evidence for non-zero Collins asymmetry on p from HERMES



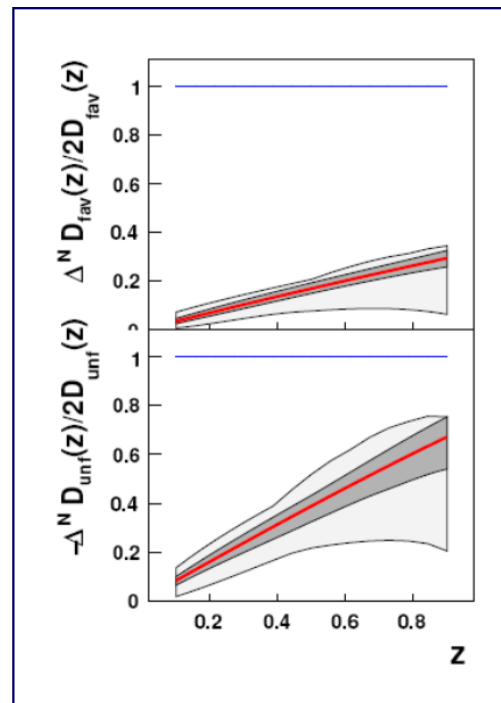
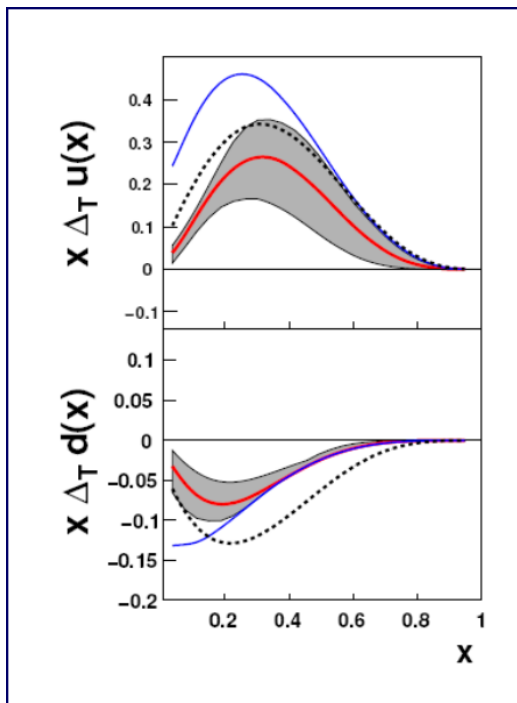
final COMPASS results





M. Anselmino et al., Nucl. Phys. Proc. Suppl. 2009

fit to HERMES p, COMPASS d, Belle e+e- data



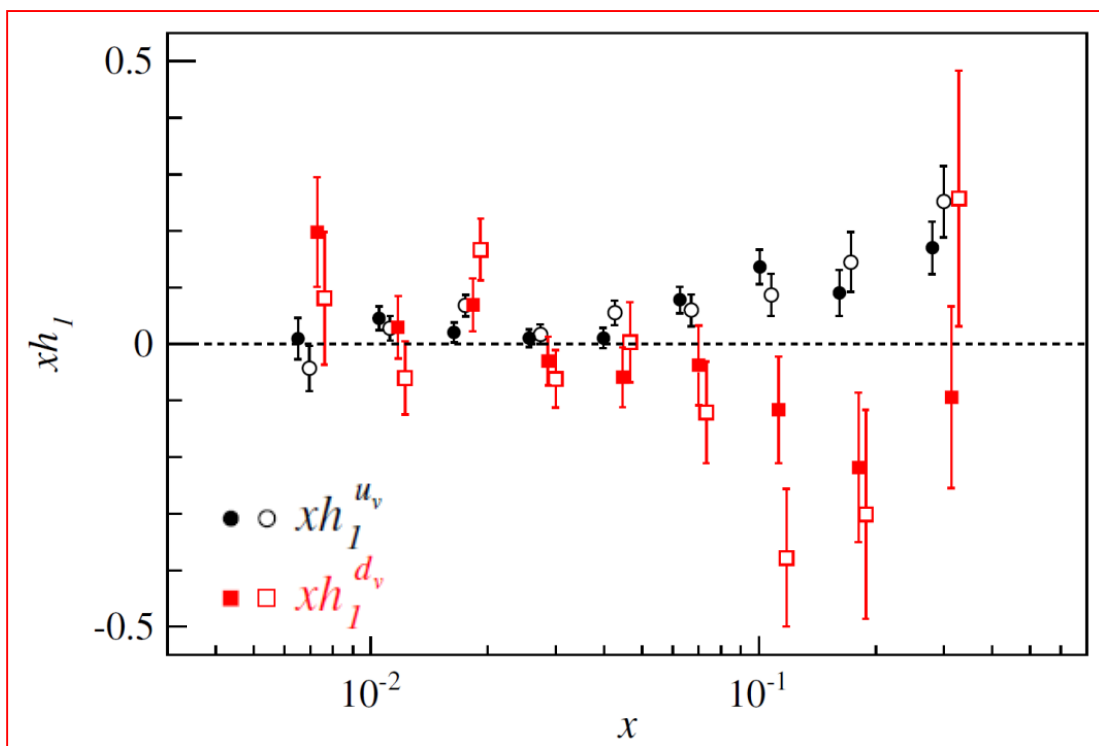
But it is not the only way →



point by point extraction

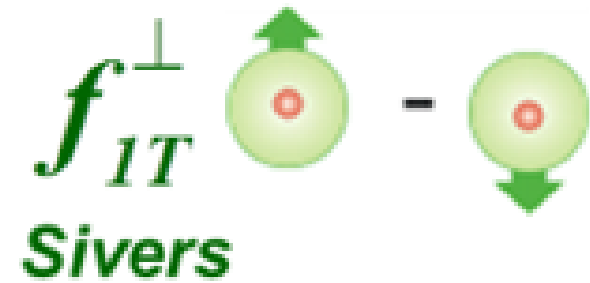
Directly use of the COMPASS p and d asymmetries, and the Belle data to evaluate the analyzing power (with some “reasonable” assumptions)

advantage: *no Monte Carlo nor parametrization is needed*



open points: di hadron
closed points: Collins

A. Martin F. B. V. Barone
PRD91 2015

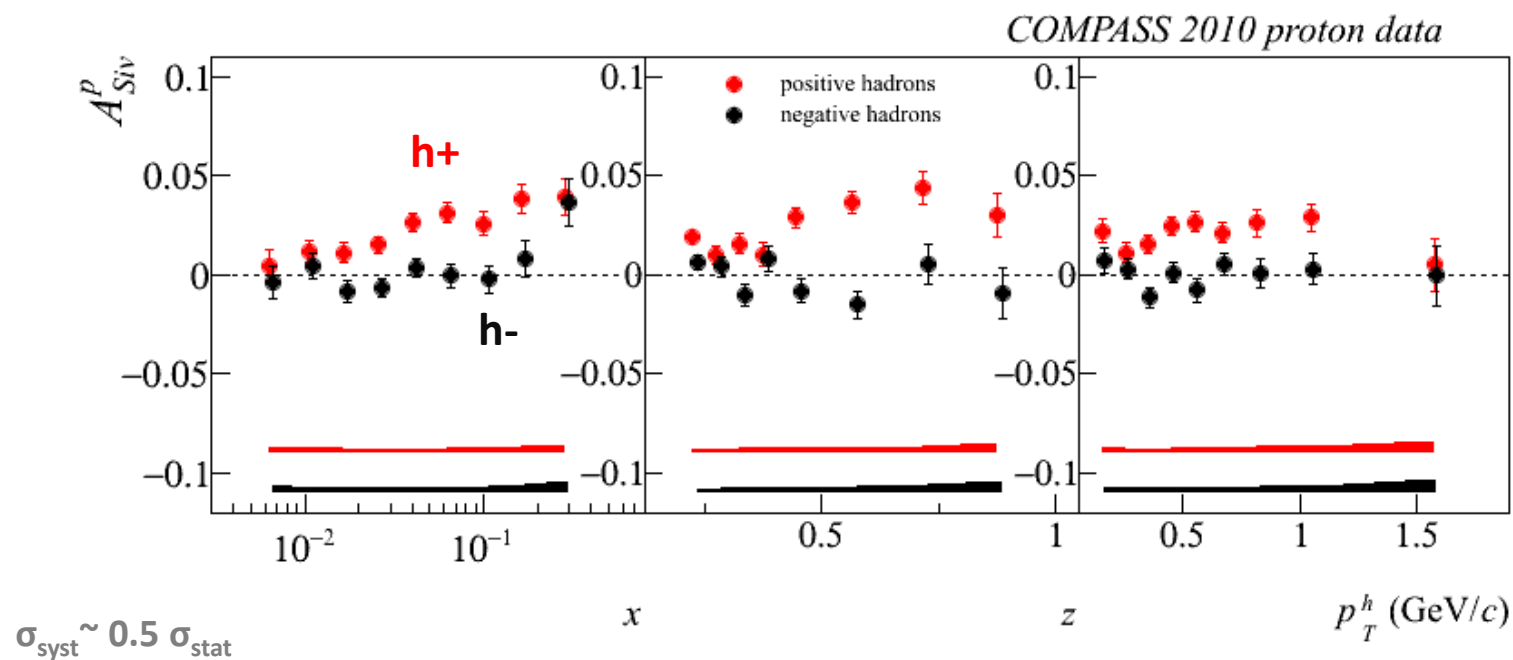


Sivers asymmetry

correlation between the nucleon transverse polarization and the quark transverse momentum k_{\perp}



charged hadrons 2010 data



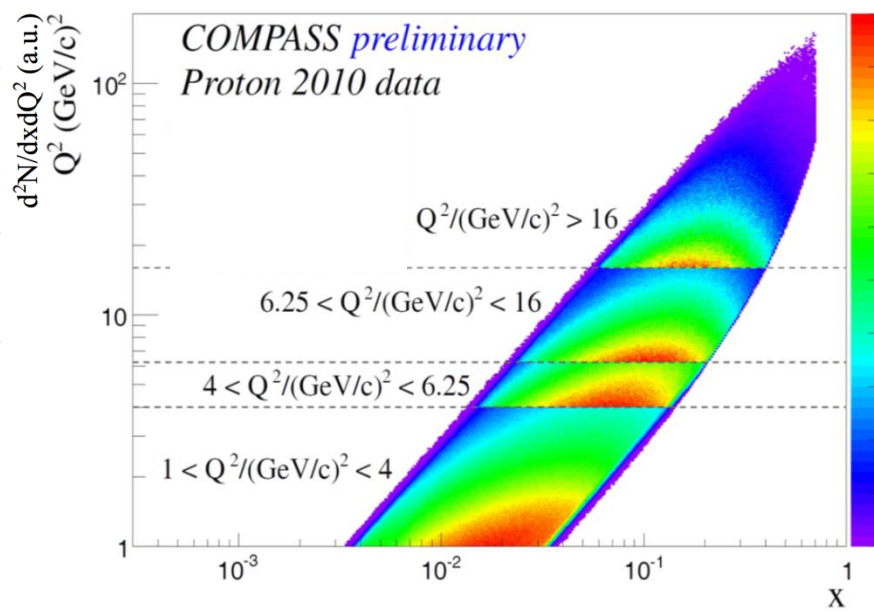
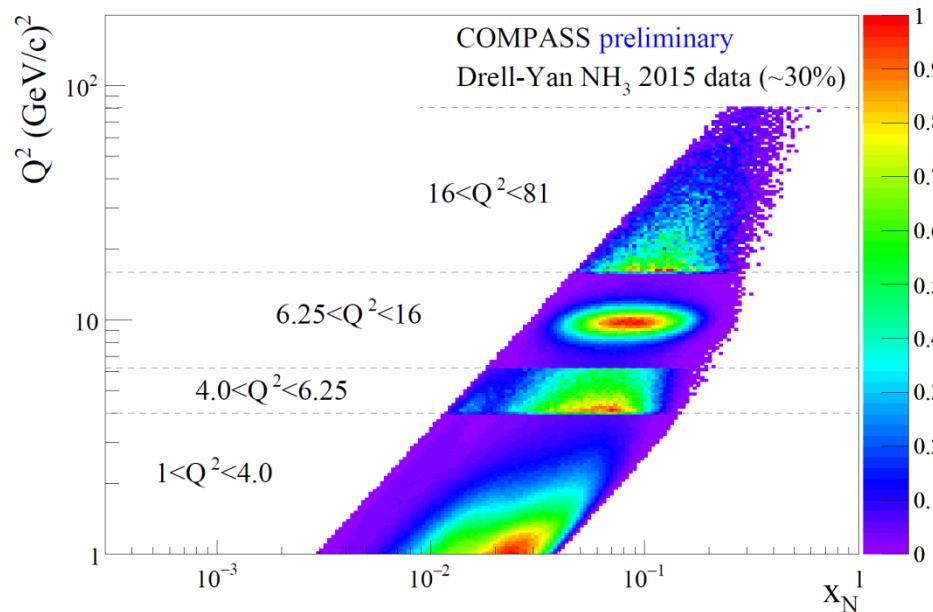
clear evidence for a positive signal for h^+ , which extends to small x



COMPASS has measured the TSA in the 4 Q^2 ranges of the Drell-Yan experiment

Drell-Yan
190 GeV pion beam

SIDIS
160 muon beam



fundamental prediction pQCD
sign change between Sivers TMD
measured in SIDIS and in Drell-Yan

Next Talk by Robert Heitz

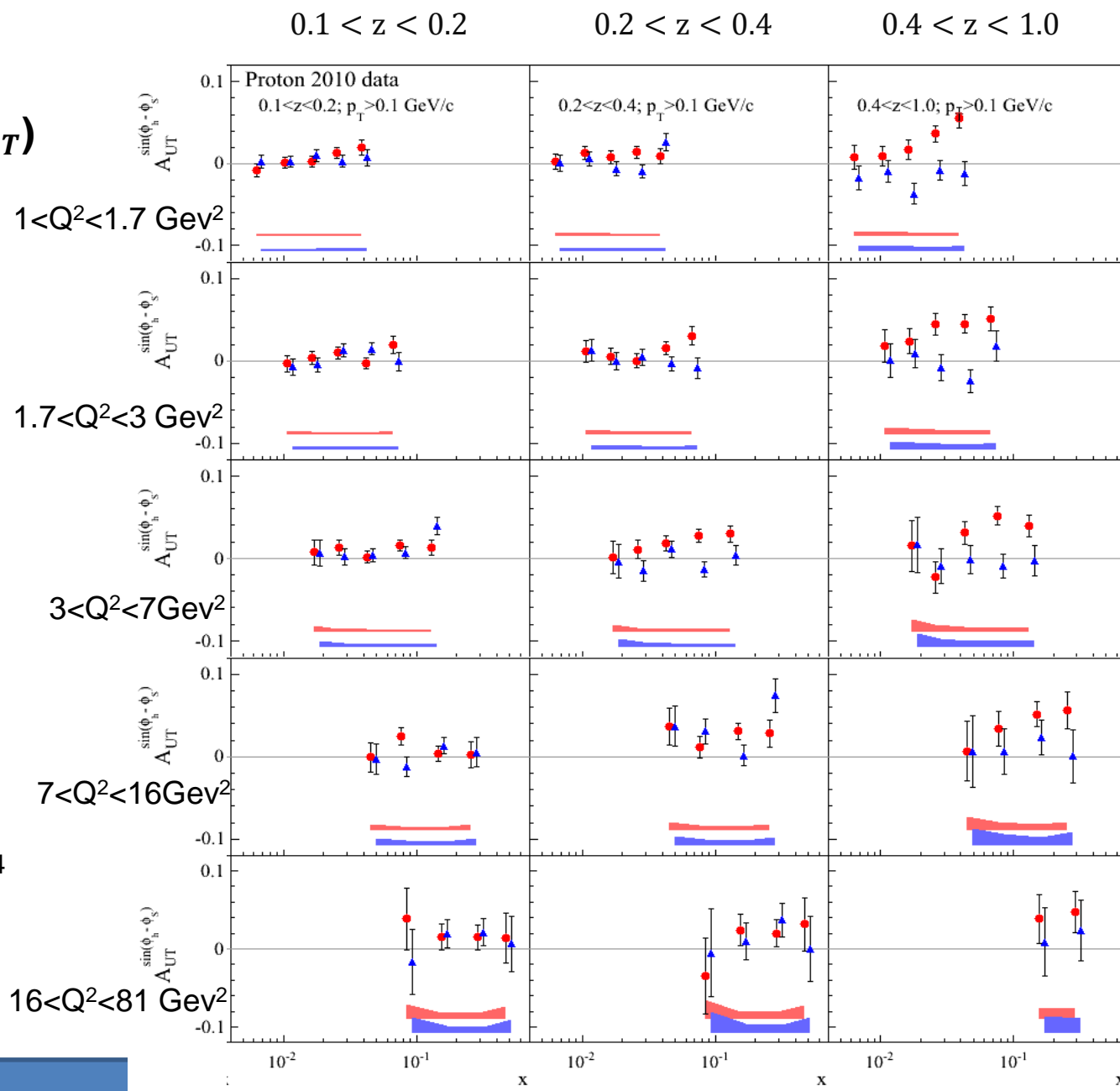
multiD ($x, Q^2; z, P_T$) analysis

an example:
Sivers
 asymmetry

$P_T > 0.1 \text{ GeV}/c$



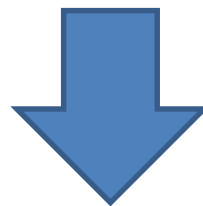
SPIN2014





Compute the Siverts Asymmetry by weighting the spin dependent part by

$$w = P_T/zM$$



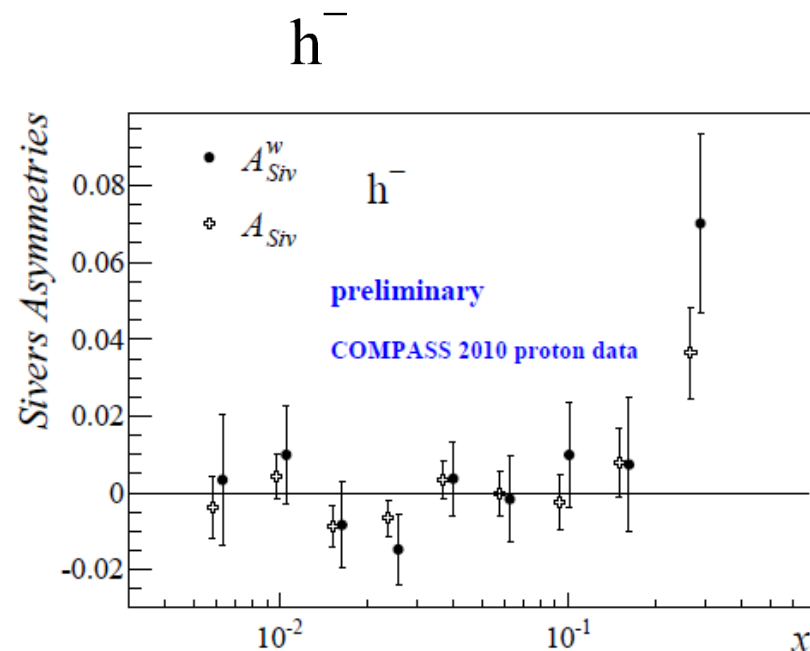
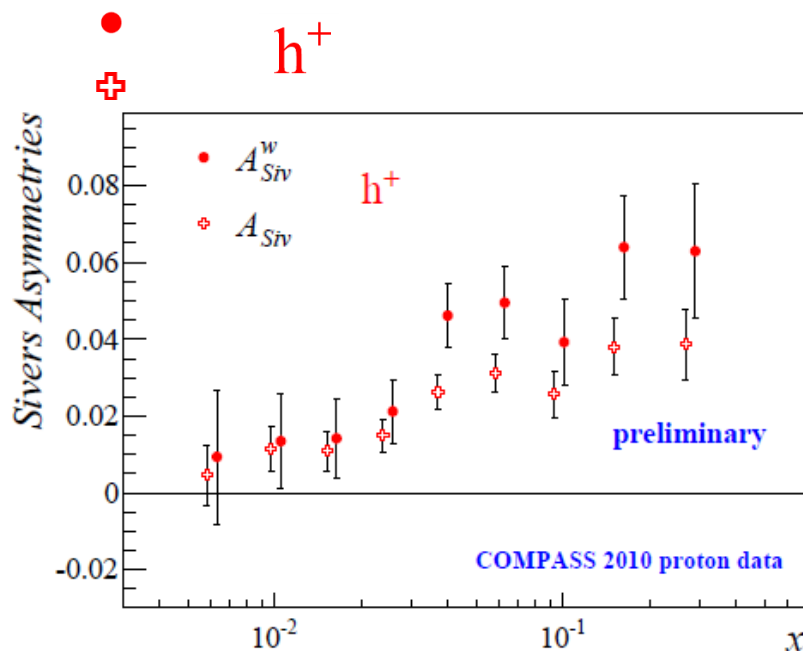
Direct access to the first moment of the Siverts asymmetry!



$$A_{Siv}^w(x) = \frac{\sigma_{Siv}^w}{\sigma_U} = 2 \frac{\sum_q e_q^2 x f_{1T}^{\perp(1)q}(x) \int D_{1q}(z) dz}{\sum_q e_q^2 x f_1^q(x) \int D_{1q}(z) dz}$$



$$w = P_T/zM \quad A_{Siv}^w(x) = \frac{\sigma_{Siv}^w}{\sigma_U} = 2 \frac{\sum_q e_q^2 x f_{1T}^{\perp(1)q}(x) \int D_{1q}(z) dz}{\sum_q e_q^2 x f_1^q(x) \int D_{1q}(z) dz}$$



assuming u dominance
and for π^+

$$A_{Siv}^w(x) \simeq 2 \frac{x f_{1T}^{\perp(1)u}(x)}{x f_1^u(x)}$$

$A_{Siv}^w(x)$ SPIN2016, arXiv:1702.00621
 $A_{Siv}^w(x)$ PLB717 (2012) 383



- The COMPASS experiment at CERN
- Longitudinal asymmetries in DIS
- Hadron multiplicities
- The Structure of the Nucleon : Transversity and TMD
- **Unpolarized SIDIS**
A selection of the many available results!

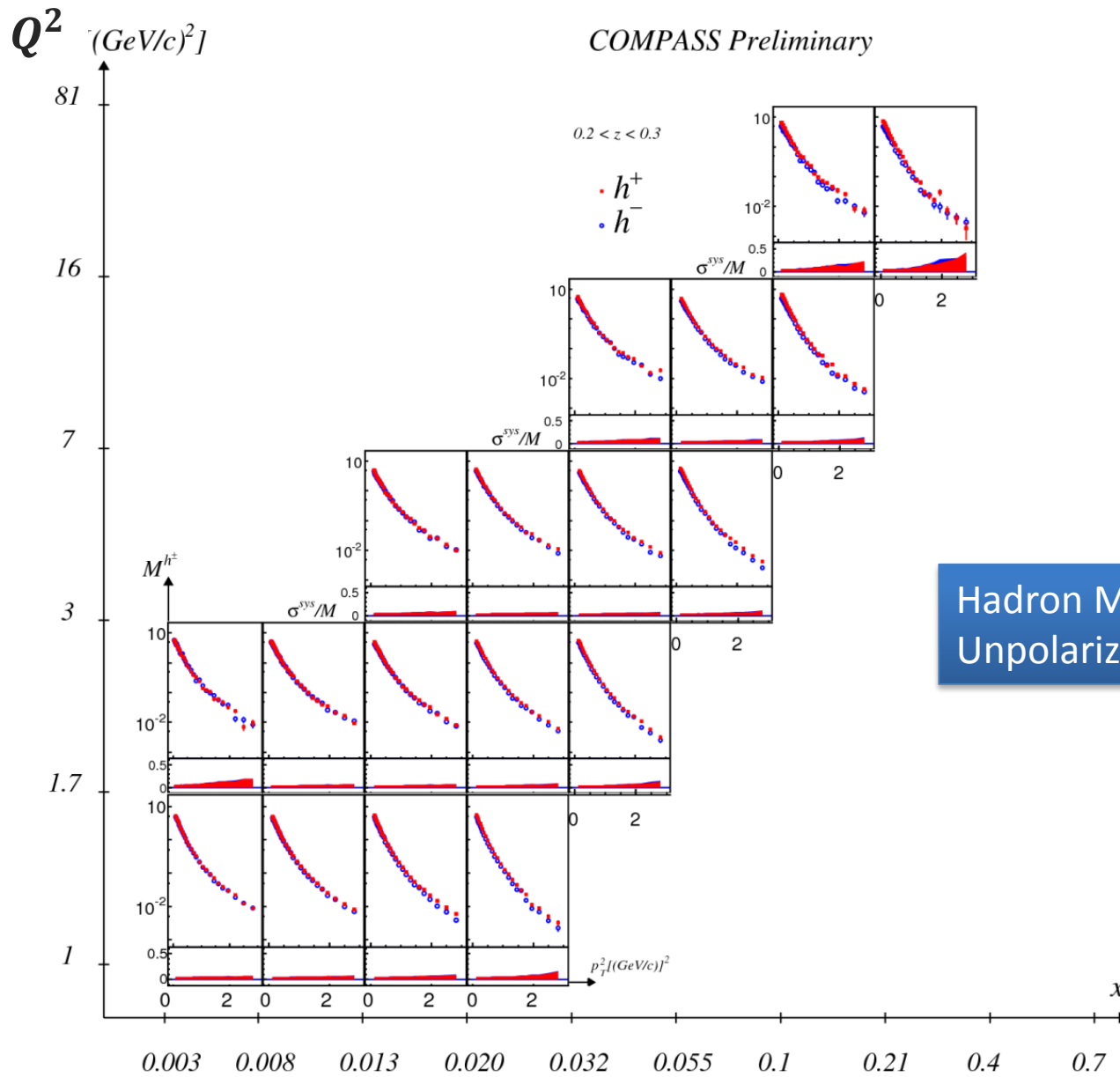


Relevance for TMDs:

- the cross-section **dependence on p_{Th}** comes from:
 - intrinsic k_T of the quarks
 - p_{\perp} generated in the quark fragmentation

$$\langle p_{Th}^2 \rangle = \langle p_{\perp}^2 \rangle + z^2 \langle k_T^2 \rangle$$

COMPASS
has produced results
on ${}^6\text{LiD}$ ($\sim d$) from
2004/6 data



Hadron Multiplicities from Unpolarized SIDIS

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- the **azimuthal modulations** in the unpolarized cross-sections comes from:
 - intrinsic k_T of the quarks
 - Boer-Mulders PDF

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2004 data

combined analysis should allow to disentangle the different effects

COMPASS

- Is measuring these observables in SIDIS on LH_2 in parallel with DVCS

SIDIS gave and is giving fundamental contributions to the study of the nucleon structure.

The COMPASS contribution is remarkable:

- Longitudinal spin structure → structure function, helicity PDFs
- Transverse spin and momentum structure
 - Sivers, transversity, Collins functions different from zero

to progress further

- comparison with different processes, from Drell-Yan to pp hard scattering
- more from SIDIS
 - new precise measurements at new facilities with different energies
JLab12, EIC
 - COMPASS can still do a lot in the “consolidation” phase from existing data,
with the LH2 data and hopefully in the future d↑

still a long way, a lot to be learned, and a lot of fun!