



Archaeological Museum of Thessaloniki

Recent experimental results on hadron structure, GPDs and TMDs



G.K. Mallot



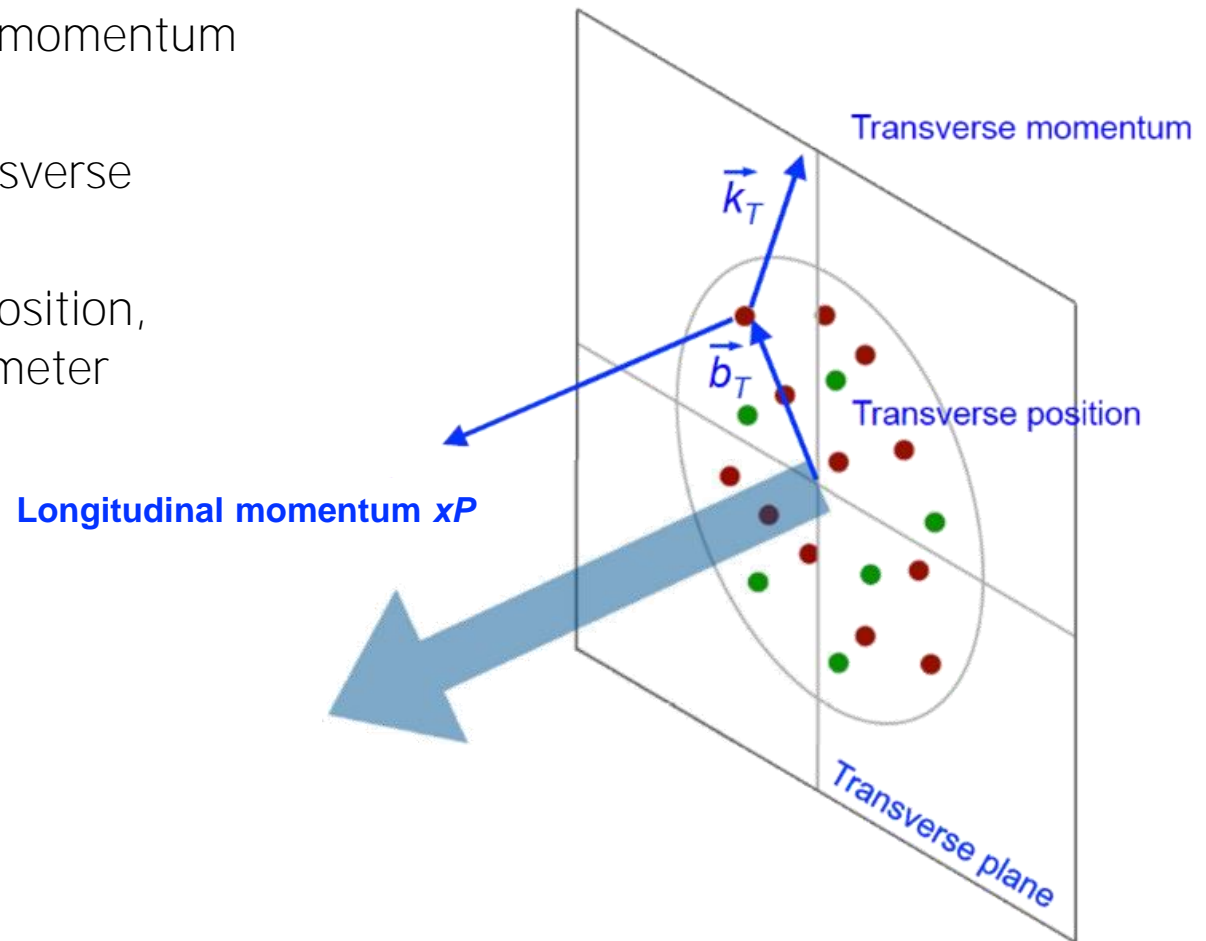
Outline

- Introduction
- spin-independent PDFs
- spin-dependent PDFs
 - inclusive DIS
 - semi-inclusive DIS
 - gluon polarisation
- TMDPDFs
- GPDs
- Outlook

A parton in a hadron

Relative position and motion characterised by 5 dimensions

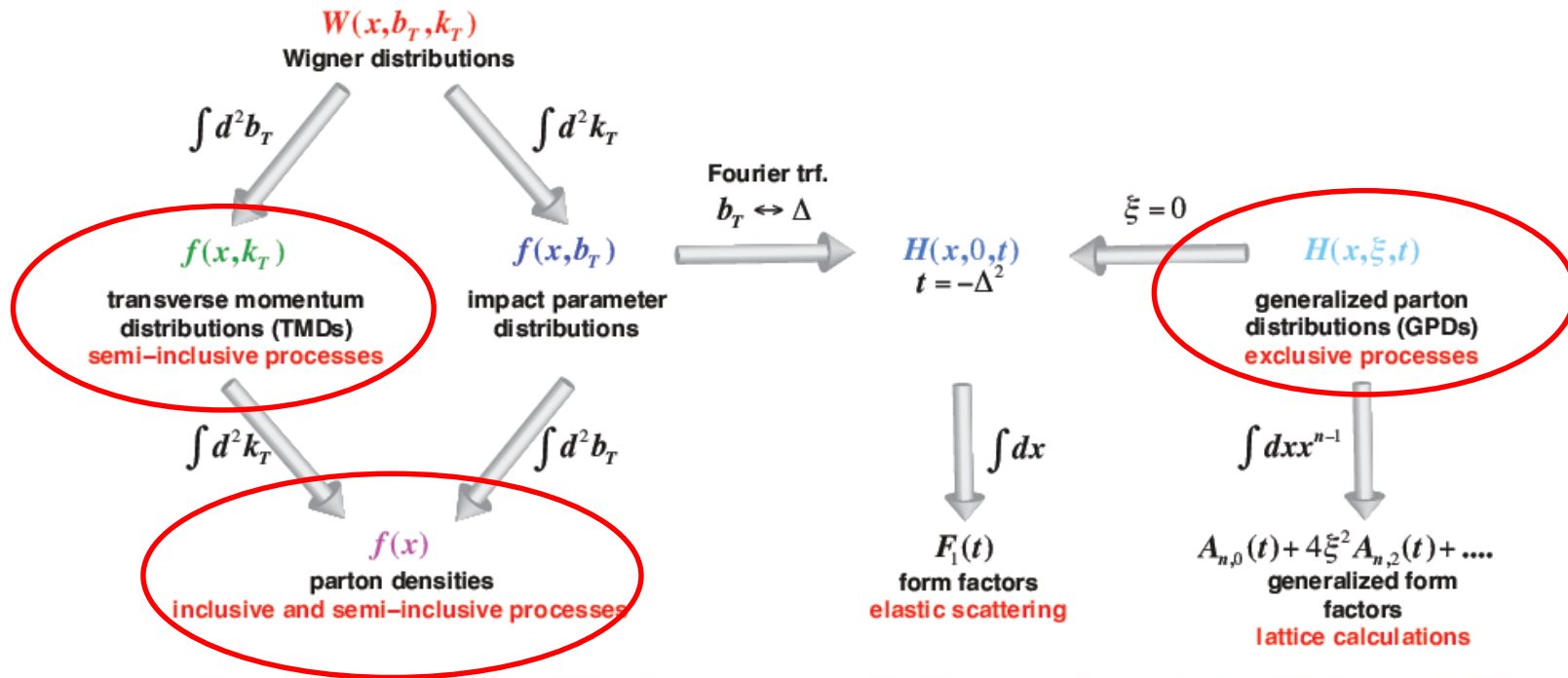
- x longitudinal momentum fraction
- \vec{k}_T intrinsic transverse momentum
- \vec{b}_T transverse position, impact parameter



Family tree of parton distributions

momentum space

coordinate space



confined motion of a parton in a hadron needs 2 scales:

- soft scale k_T or t
- hard scale of the probe Q^2

k_T -integrated Parton Distribution Functions

Three twist-2 PDFs

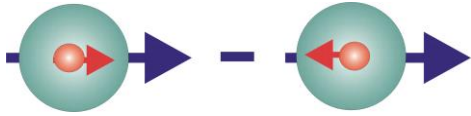
$q(x)$
 $f_1^q(x)$

A green sphere representing a nucleon with a small red dot in the center, representing a quark or gluon.

unpolarised PDF

quark/gluon with momentum xP in a nucleon

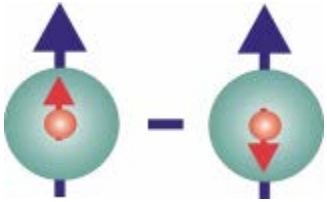
$\Delta q(x)$
 $g_1^q(x)$

Two green spheres representing nucleons. The left one has a red dot with a red arrow pointing right, and a blue arrow pointing right. The right one has a red dot with a red arrow pointing left, and a blue arrow pointing right. A minus sign is between them.

helicity PDF

quark/gluon with spin parallel to the nucleon spin in a longitudinally polarised nucleon

$\Delta_T q(x)$
 $h_1^q(x)$

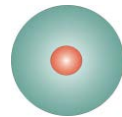
Two green spheres representing nucleons. The left one has a red dot with a red arrow pointing up, and a blue arrow pointing up. The right one has a red dot with a red arrow pointing down, and a blue arrow pointing up. A minus sign is between them.

transversity PDF

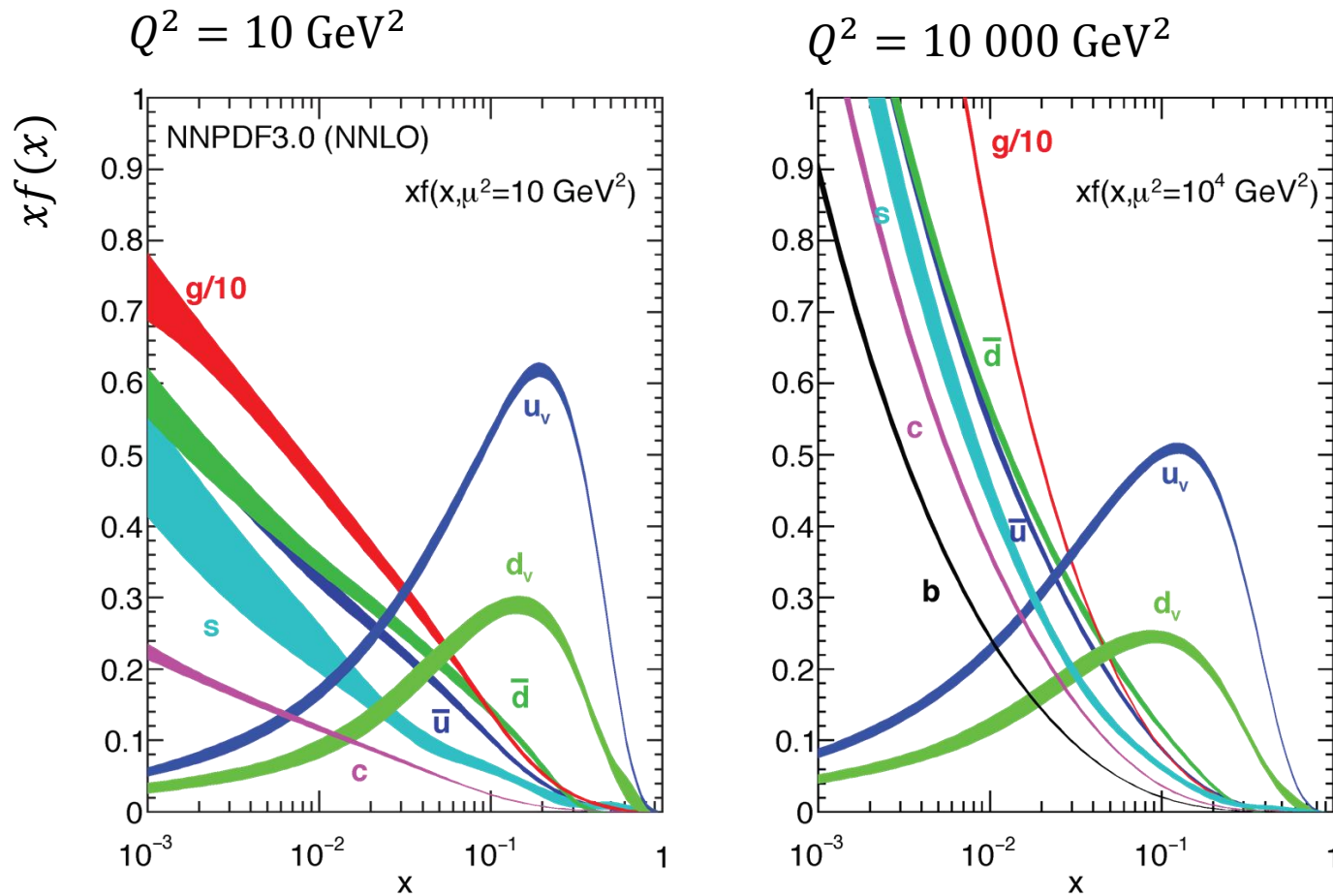
quark with spin parallel to the nucleon spin in a transversely polarised nucleon

unpolarized PDFs

$$q(x, Q^2) = \vec{q}(x, Q^2) + \overleftarrow{q}(x, Q^2)$$



PDFs: Example NNPDF3.0

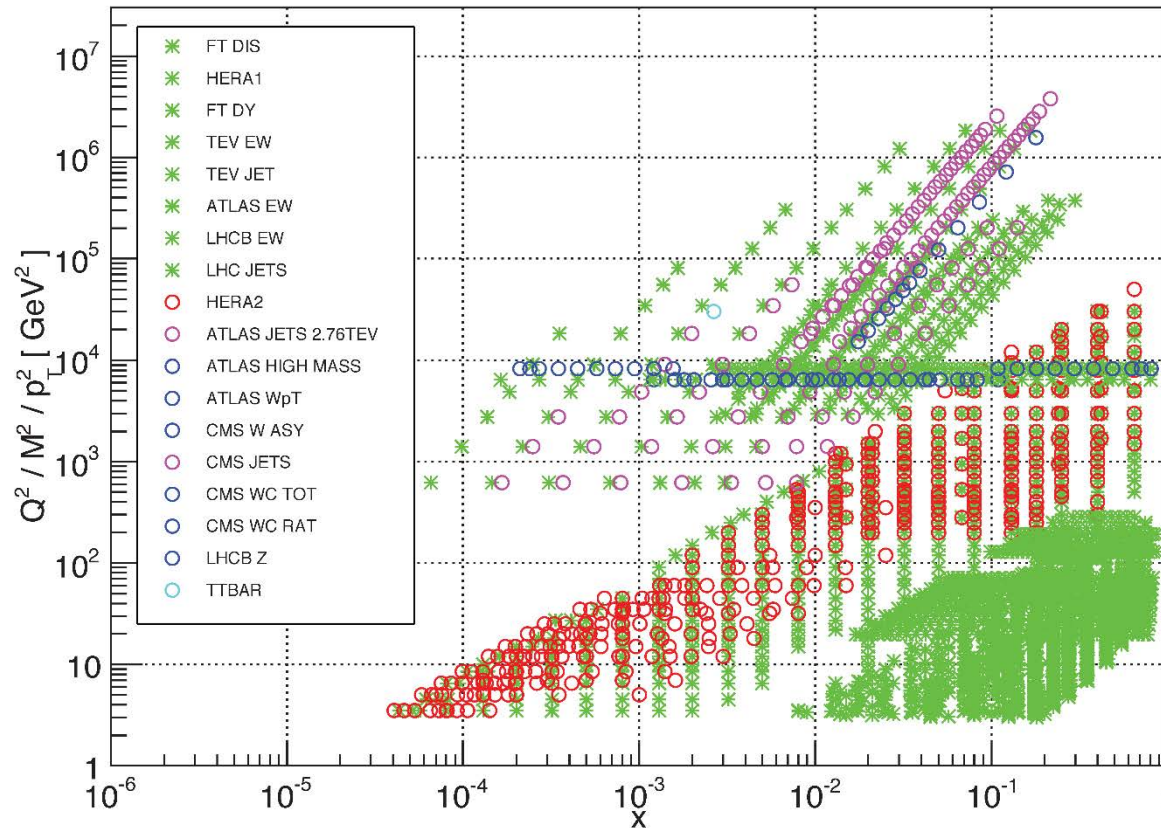


JHEP 04 (2015) 040

- Neural network approach NNLO (also LO, NLO)

Data used in NNPDF3.0

NNPDF3.0 NLO dataset



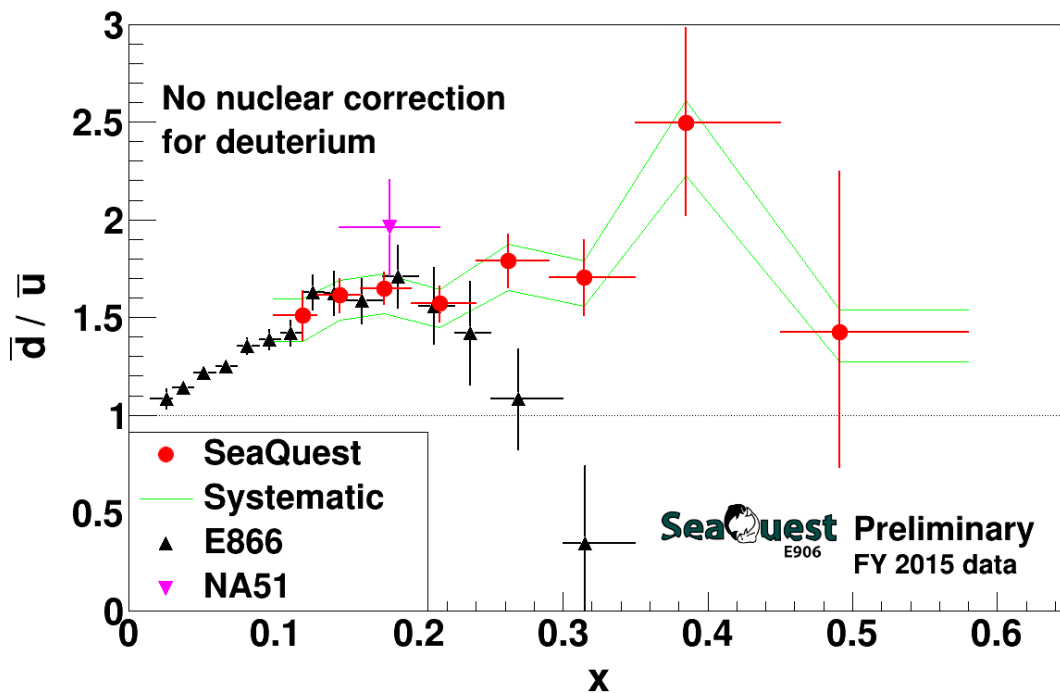
$W^2 \geq 12.5 \text{ GeV}^2$
 $Q^2 \geq 3.5 \text{ GeV}^2$
no HT

exp. data:
NMC, SLAC,
BCDMS,
Chorus,
NuTeV, Zeus,
H1,
DY E605/E866,
CDF, D0,
Atlas, CMS,
LHCb

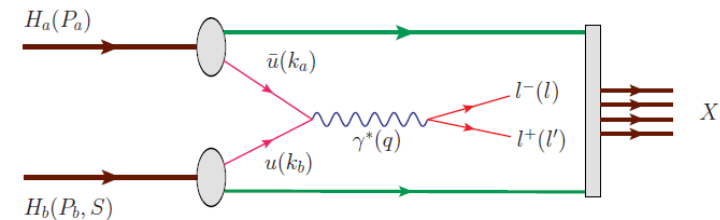
- other PDF sets: ABM12, CJ15, CT14, JR14, HERA-PDF2.0, MMHT14, JAM (→ [W. Melnitchouk, Mon. 11:30](#))

Asymmetry of light quark sea \bar{d}/\bar{u}

- first observed 1991 by NMC as violation of Gottfried sum rule
- NA51@CERN, E866@FNAL
- new preliminary results from  @FNAL
- ~25% of anticipated data

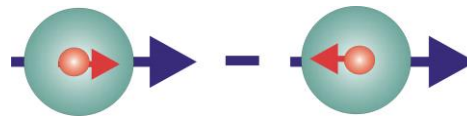


Drell-Yan: 120 GeV
 $p \rightarrow \text{LH}_2 / \text{LD}_2 / \text{C} / \text{Fe} / \text{W}$

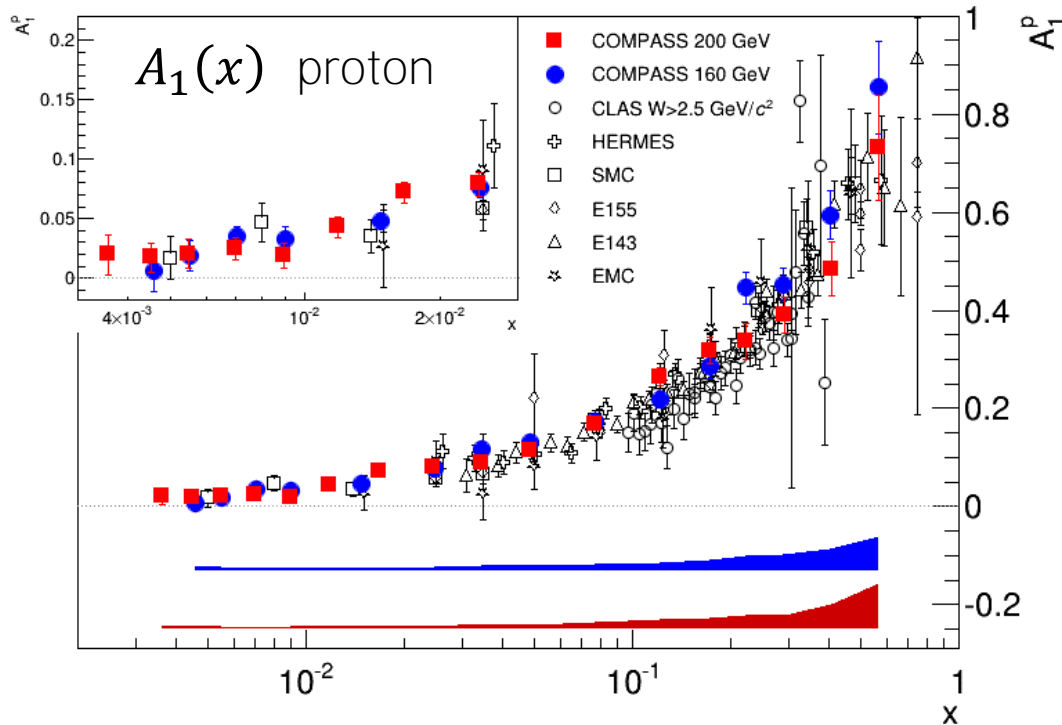


Helicity distributions

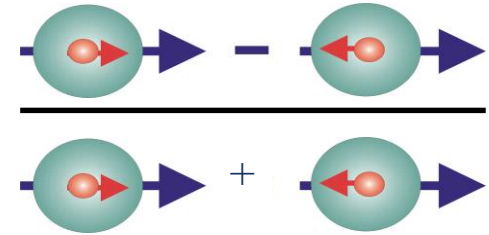
$$\Delta q(x, Q^2) = \vec{q}(x, Q^2) - \overleftarrow{q}(x, Q^2)$$



World data on proton A_1 spin asymmetry

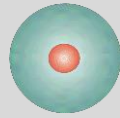


PLB 753 (2016) 18

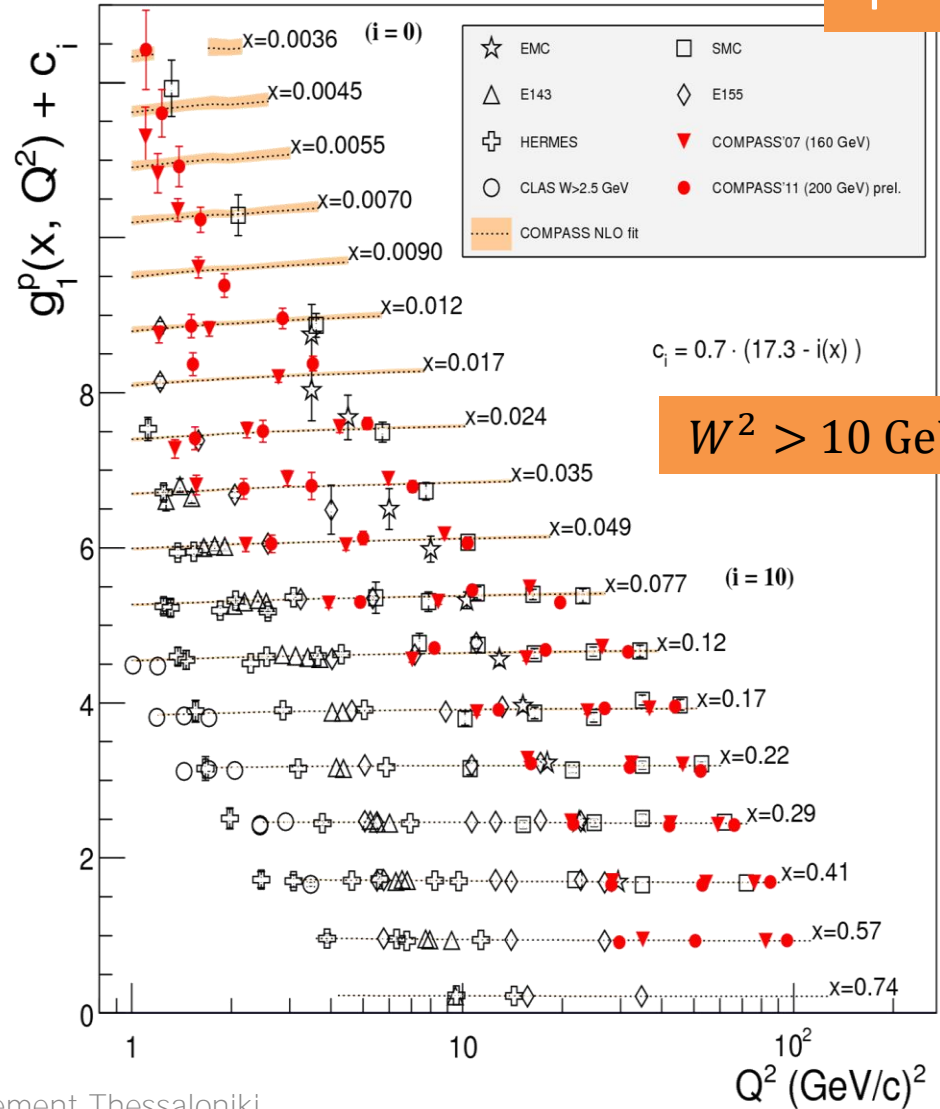
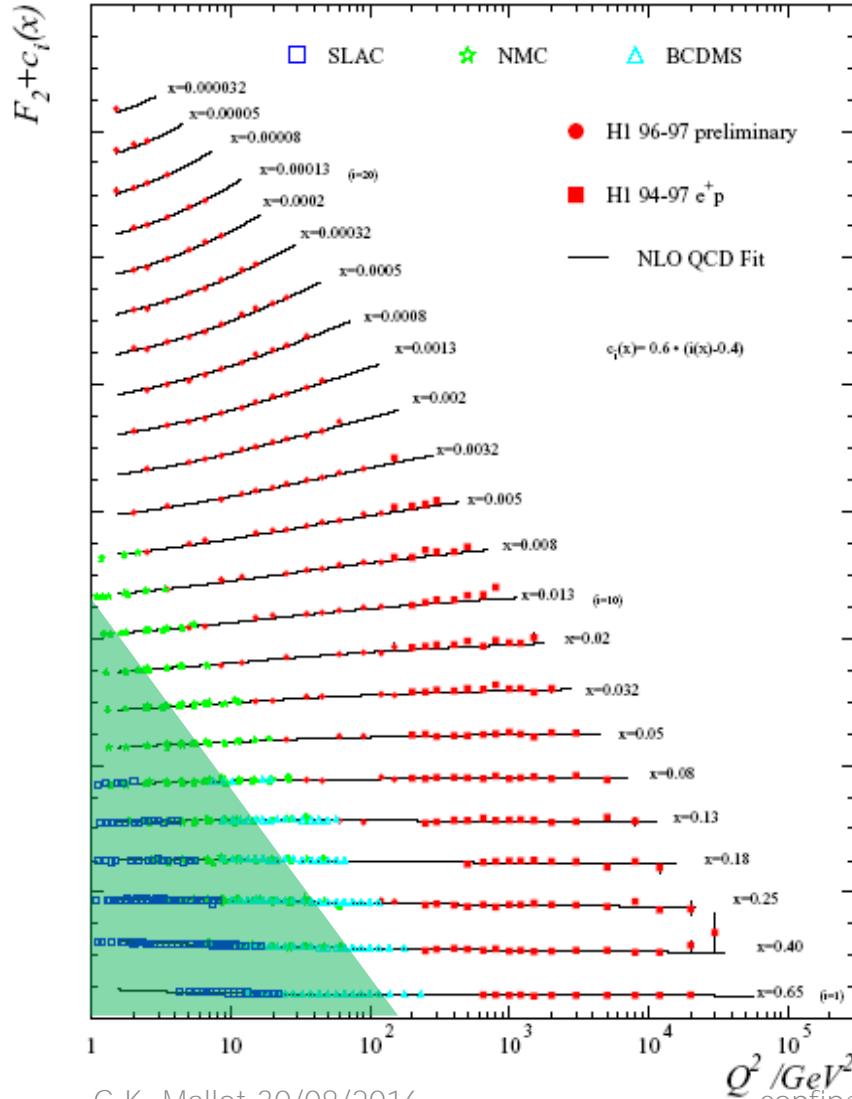
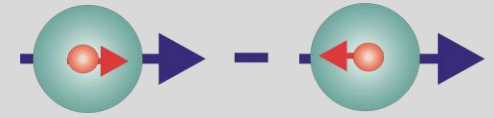


$$A_1(x, Q^2) = \frac{\sum_q e_q^2 \Delta q(x, Q^2)}{\sum_q e_q^2 q(x, Q^2)} = \frac{g_1(x, Q^2)}{F_1(x, Q^2)}$$

$$F_2(x, Q^2)$$

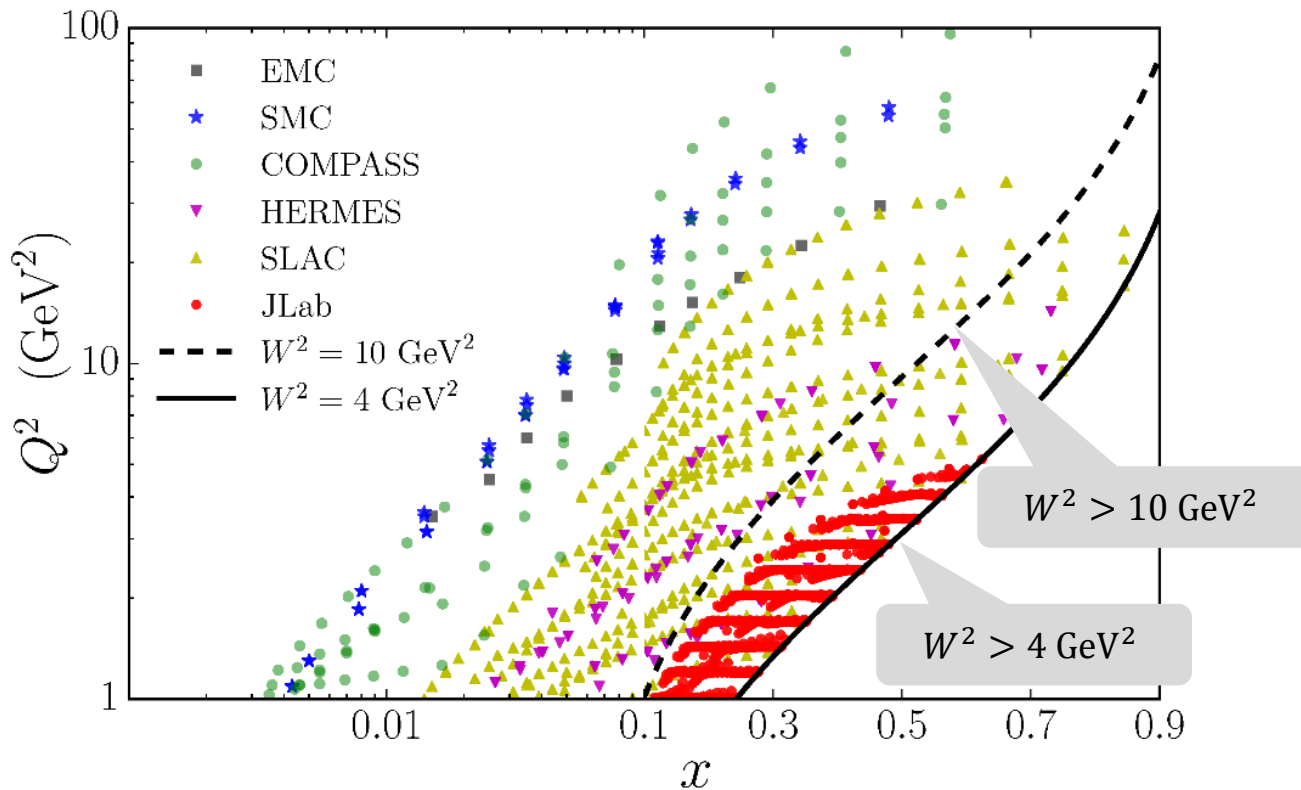


$$g_1(x, Q^2)$$

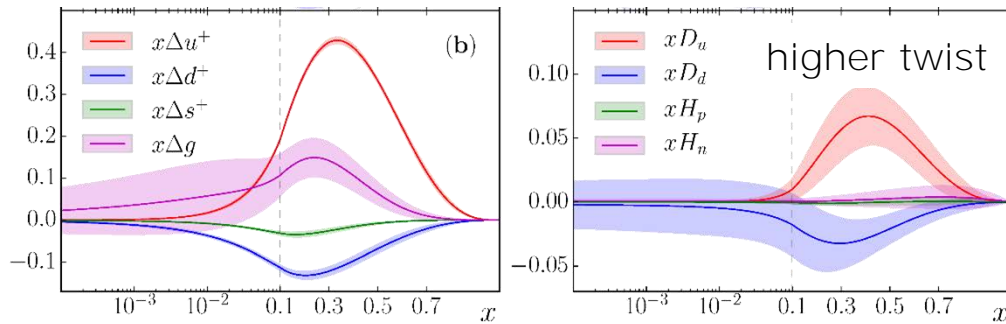


JAM15 – a new PDF fit to inclusive data

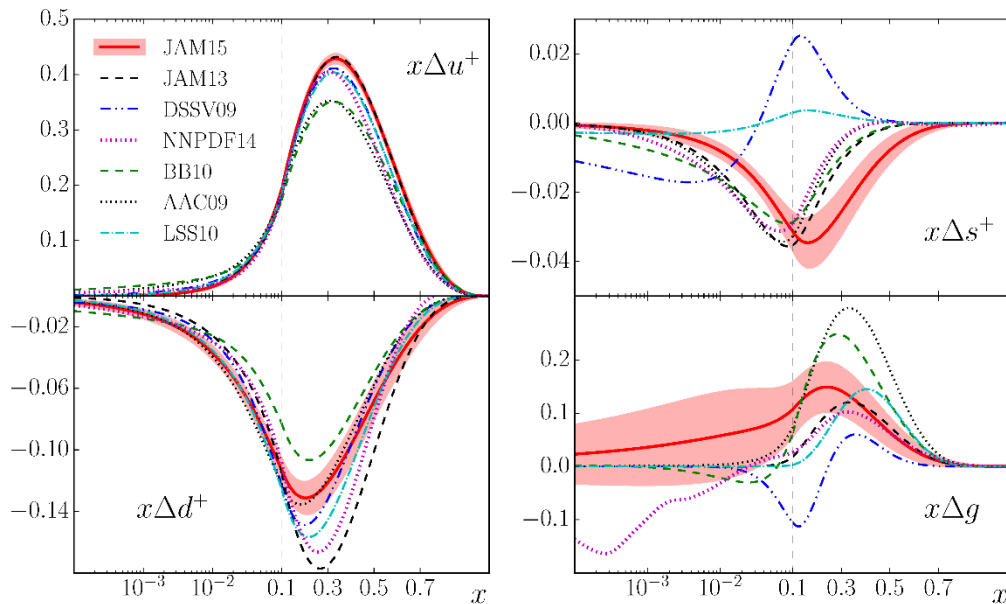
- includes precise low $W^2 > 4 \text{ GeV}^2$ JLAB data
- only inclusive data, 2515 data points vs 854 for $W^2 > 10 \text{ GeV}^2$



JAM15 – a new PDF fit to inclusive data



- $q^+ = q + \bar{q}$
- $Q^2 = 1 \text{ GeV}^2$
- very significant higher twist terms
- improvements for strange quarks and gluon at large x



PRD 93 (2016) 074005

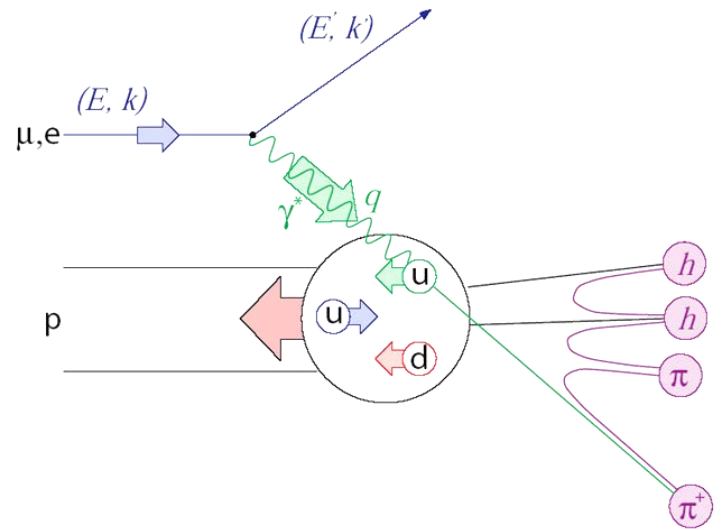
Beyond inclusive: Semi-inclusive DIS results

- additional hadron observed in FS

$$A_1^h = \frac{\sum_q e_q^2 g_1^q(x, Q^2) D_{1q}^h(z, Q^2)}{\sum_q e_q^2 f_1^q(x, Q^2) D_{1q}^h(z, Q^2)}$$

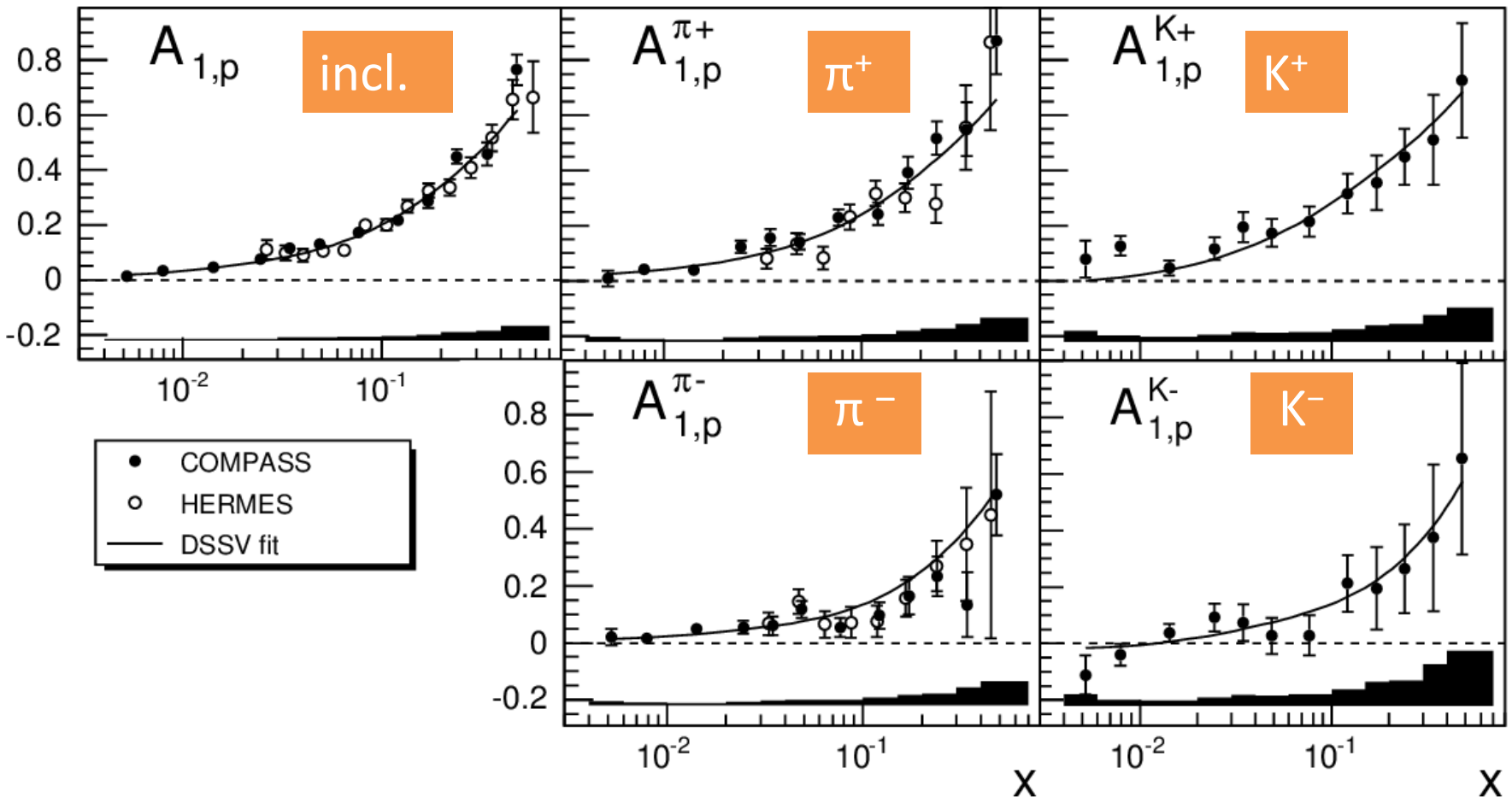
- gives access to flavour information via the fragmentation functions D

$$z = E_h/\nu$$



Incl. & semi-incl. A_1

- Compass and Hermes data for proton
- similar data for deuteron





Hadron multiplicity data and FF

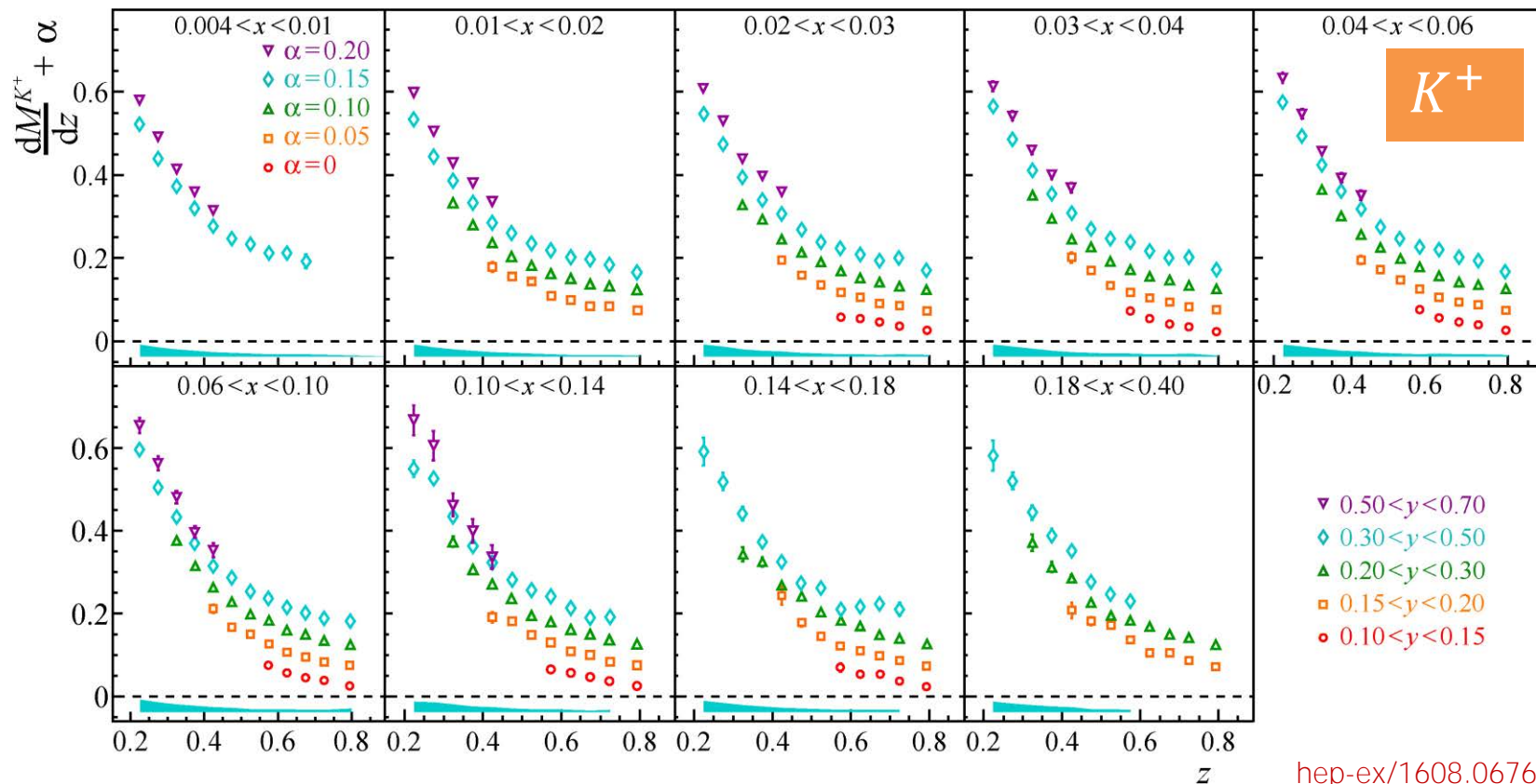
- Fragmentation functions not well enough known, in particular for the strange quark
- limit the determination of strange PDF
- new charged pion and kaon multiplicity data in 3-dimensional bins (x, y, z) from isoscalar target (${}^6\text{LiD}$) by COMPASS

hep-ex/1604.02695
hep-ex/1608.06760

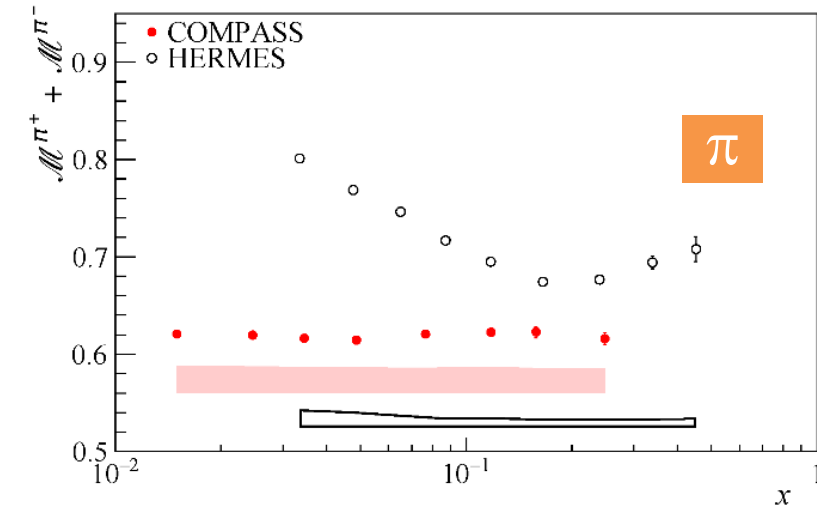
$$\frac{dM^K(x, y, z)}{dz} = \frac{1}{N^{\text{DIS}}(x, y)} \frac{dN^K(x, y, z)}{dz} \frac{1}{A(x, y, z)}$$

Charged kaon multiplicities

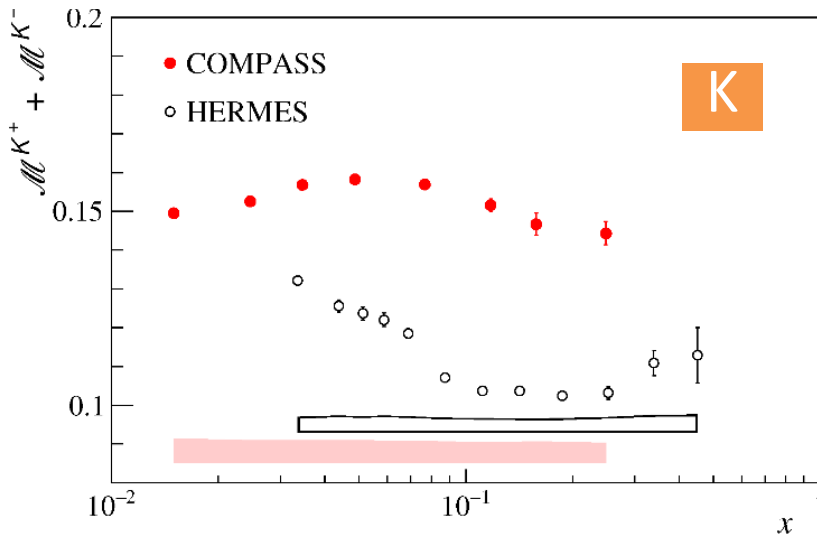
- data for positive and negative pion and kaons



Pion and kaon multiplicities



hep-ex/1604.02695



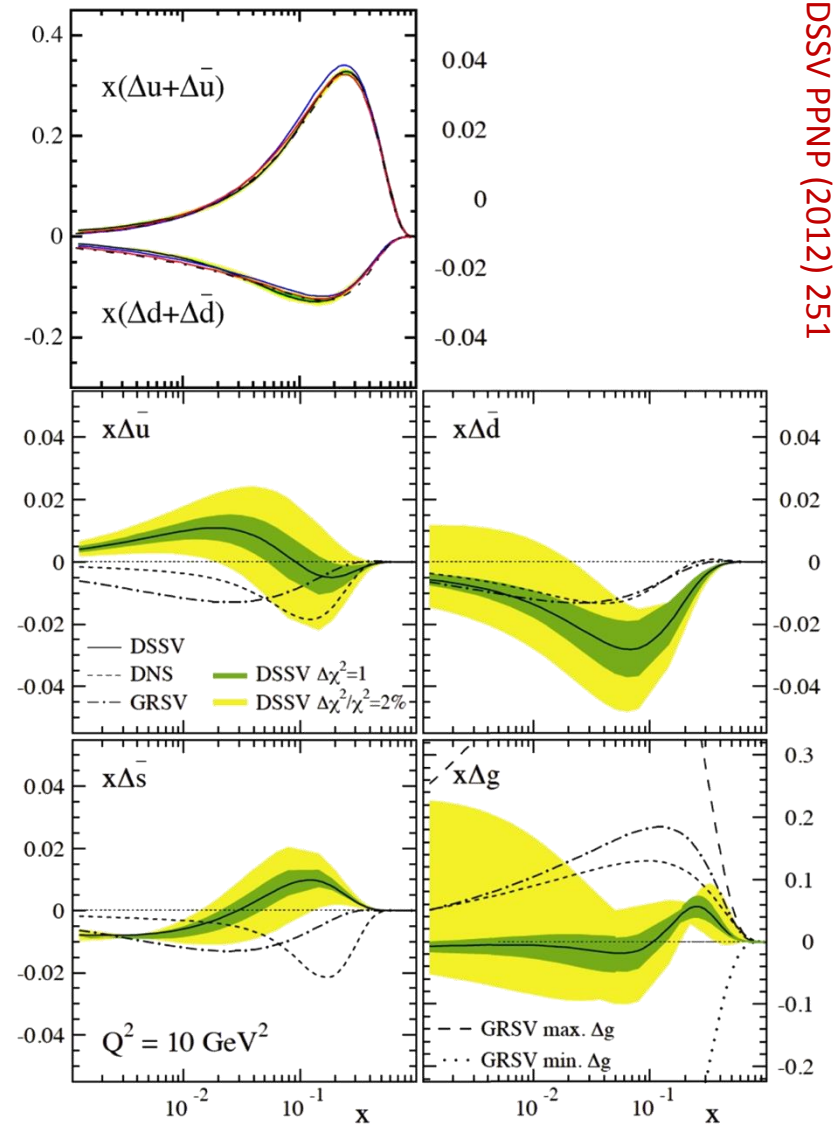
hep-ex/1608.06760

- isoscalar target, int. over z, p_T, Q^2
- discrepancies in multiplicities between Hermes and COMPASS
- similar, but not identical kinematics
- ratio π^+/π^- ok, K^+/K^- differs $\sim 20\%$
- being investigated
- new data:
impact on FF \rightarrow strange PDF in next global fits

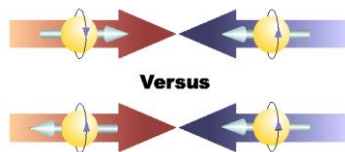
Hermes K: PRD 89 (2014) 097101; π : PRD 87 (2013) 074029

Status of PDFs: global analyses (e.g. DSSV)

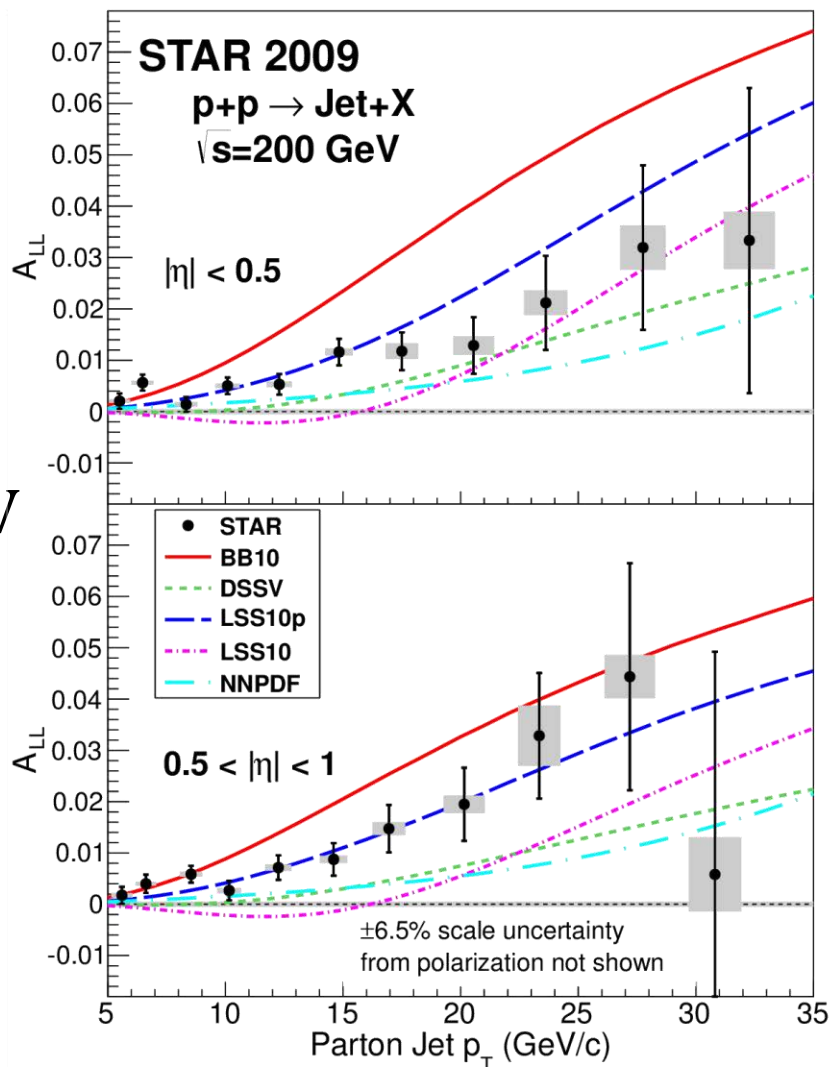
- data: DIS, SIDIS, pp
- latest update DSSV14++ with STAR jet data
PRL 113 (2014) 012001
- DSS fragmentation functions, new COMPASS data not yet included
- most uncertain: $\Delta g(x)$



STAR single jet asymmetry A_{LL}

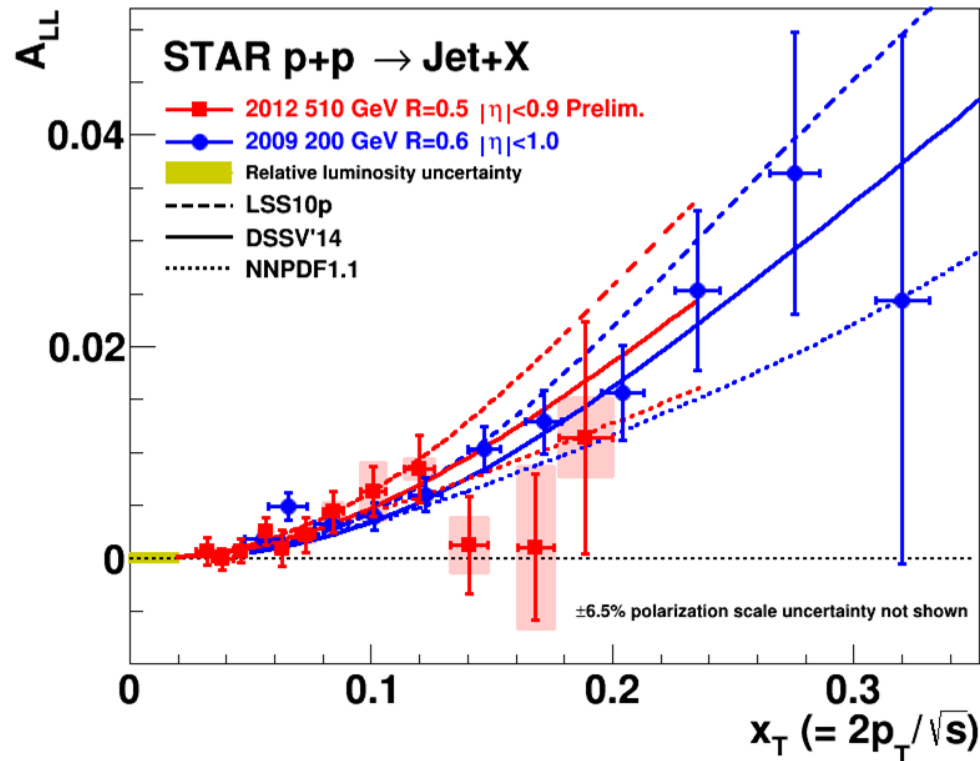


- $A_{LL} \propto \Delta g$
- no fragmentation function
- $pp \rightarrow \text{jet} + X @ \sqrt{s} = 200 \text{ GeV}$
- 2009 data, mid rapidity
- A_{LL} in good agreement with LSS10p (pos. Δg)



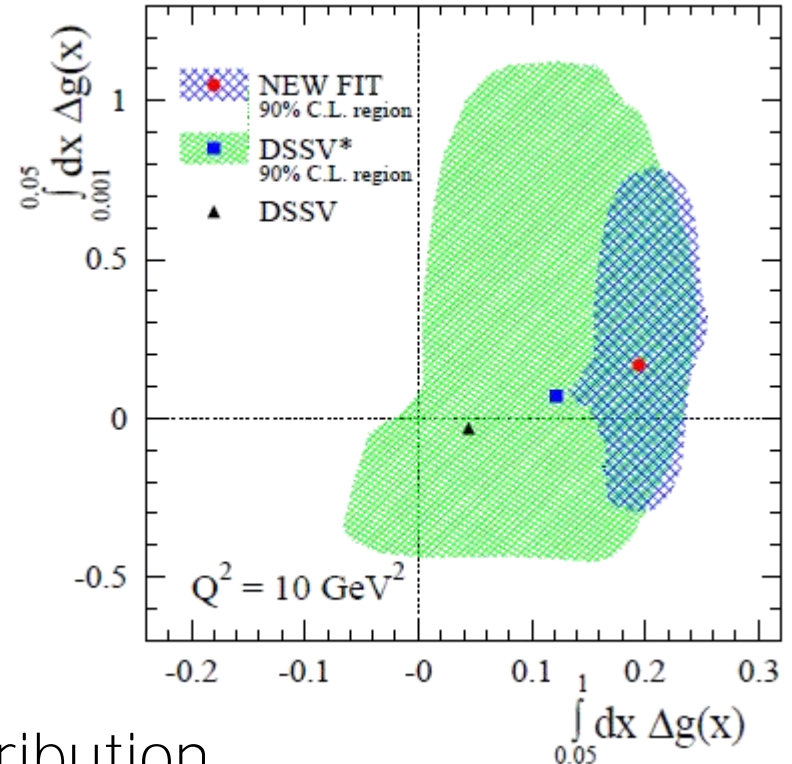
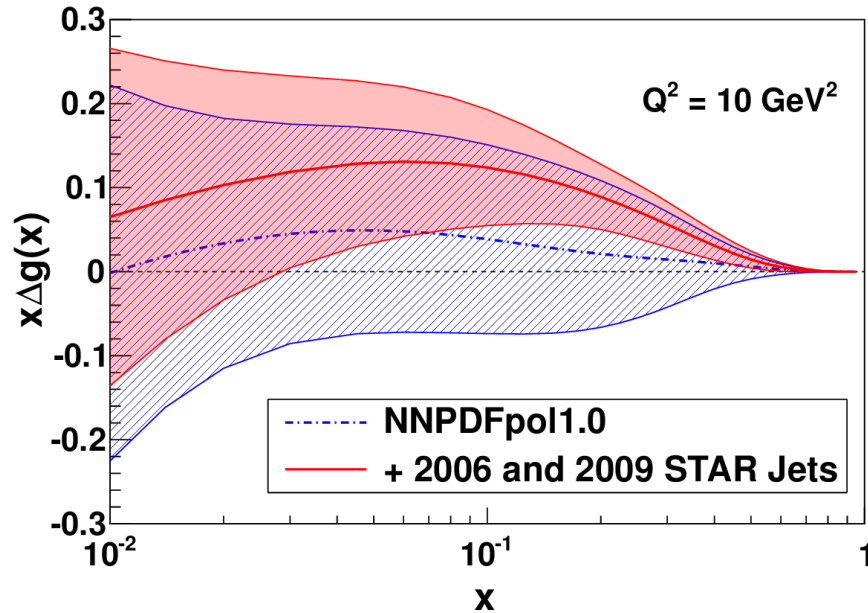
PRL 115 (2015) 092002

STAR single jet asymmetry A_{LL}



- prelim. 2012 data, $\sqrt{s} = 510$ GeV, lower x
- agree with 2009 data and LSS10p and DSSV14
- DSSV14 includes 2009 data

Impact of Star jet data



- big impact on pol. gluon distribution
- $\int_{0.05}^1 \Delta g(x) dx \simeq 0.20$
- need data at small x

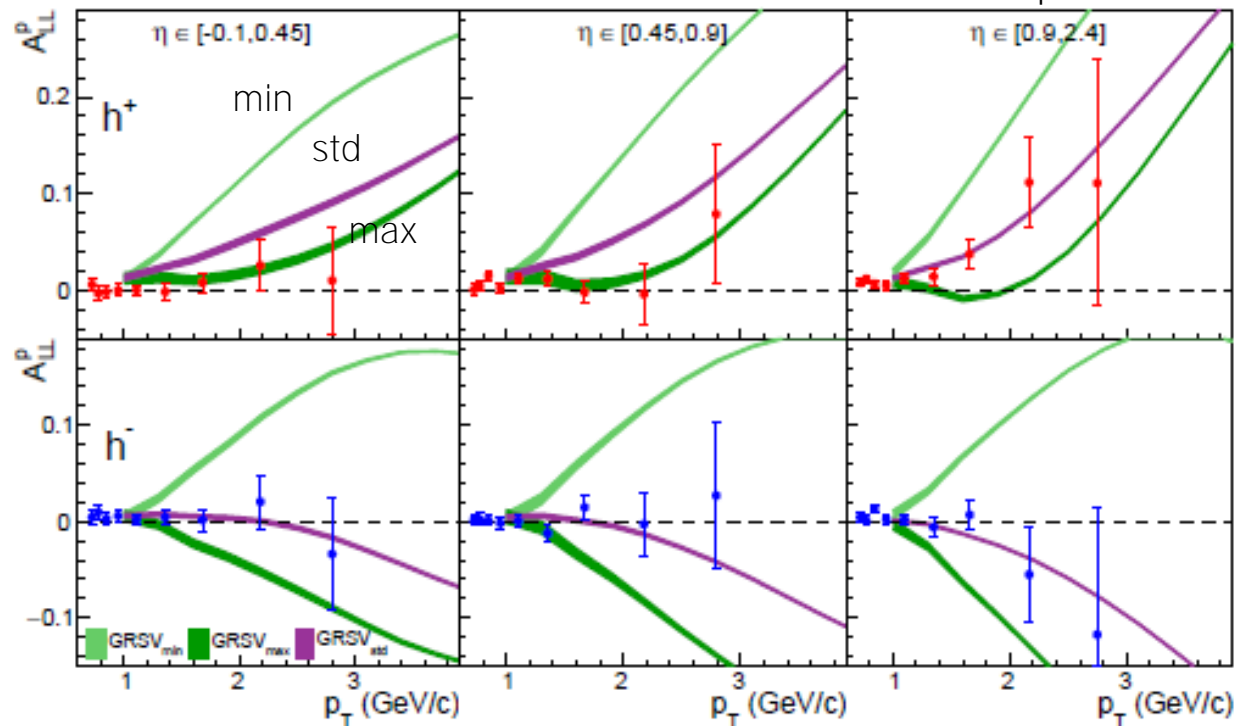
$\Delta g/g$ from single hadron (NLO)

- quasi-real photoproduction of single hadrons, à la RHIC π^0 prod.
- calc. by group of Vogelsang, agreement for unpolarised case
- caveat: NNL resummation **missing for polarised case**

$$\eta_{cms} = -\ln\left(\tan\frac{\theta}{2}\right) - \frac{1}{2}\ln\left(\frac{2E}{M}\right)$$

proton

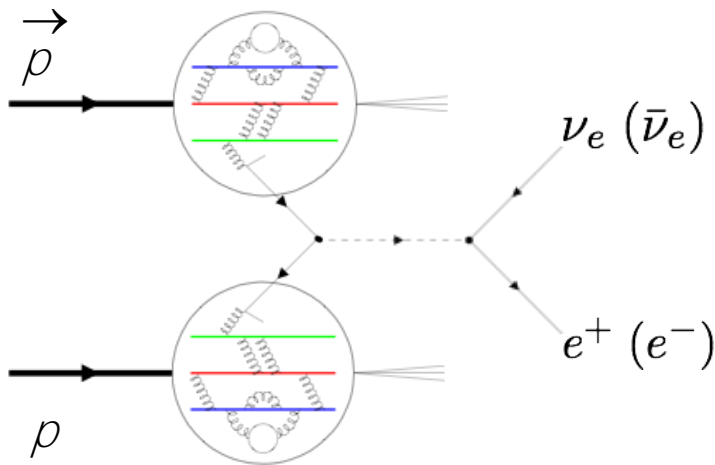
- 3 bins of pseudorapidity η
- FF important, using DSS (2015), agree best with meas. multiplicities
- data prefer **positive** gluon polarisation as suggested by recent RHIC data
- same seen in LO analysis of $Q^2 > 1 \text{ GeV}^2$
hep-ex/1512.05053



W production & antiquark polarisation

- $\vec{p}p$ collisions at 250 GeV+ 250 GeV
- $u_L \bar{d}_R \rightarrow W^+$ and $\bar{u}_R d_L \rightarrow W^-$
- parity-violating long. SSA:
- sensitive to antiquark polarisation

$$A_L = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-}$$



signature: high p_T lepton
 $\eta_e = -\ln \left[\tan \left(\frac{\theta}{2} \right) \right]$

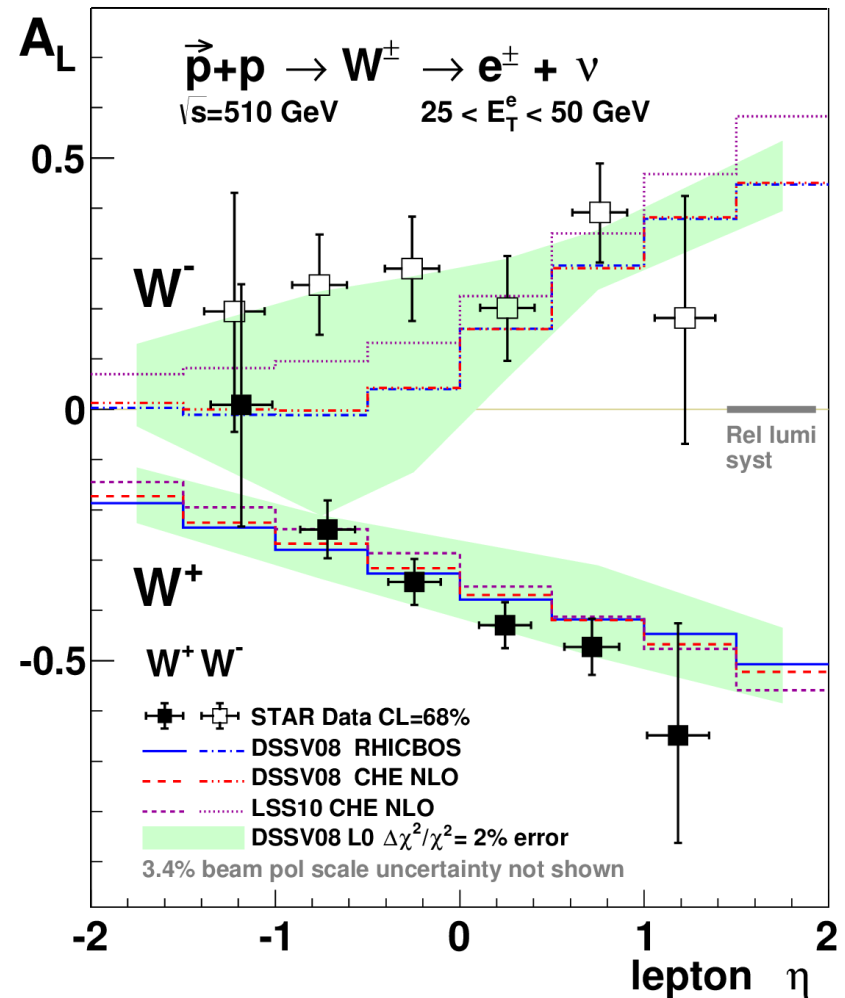
W production in pp



- run 11+12, $|\eta_e| < 1.2$
- A_L larger than expected for W^- @ $\eta < 0$
- indication for a sizable, positive up antiquark polarization
- $0.05 < x < 0.2$
- New Phenix W data

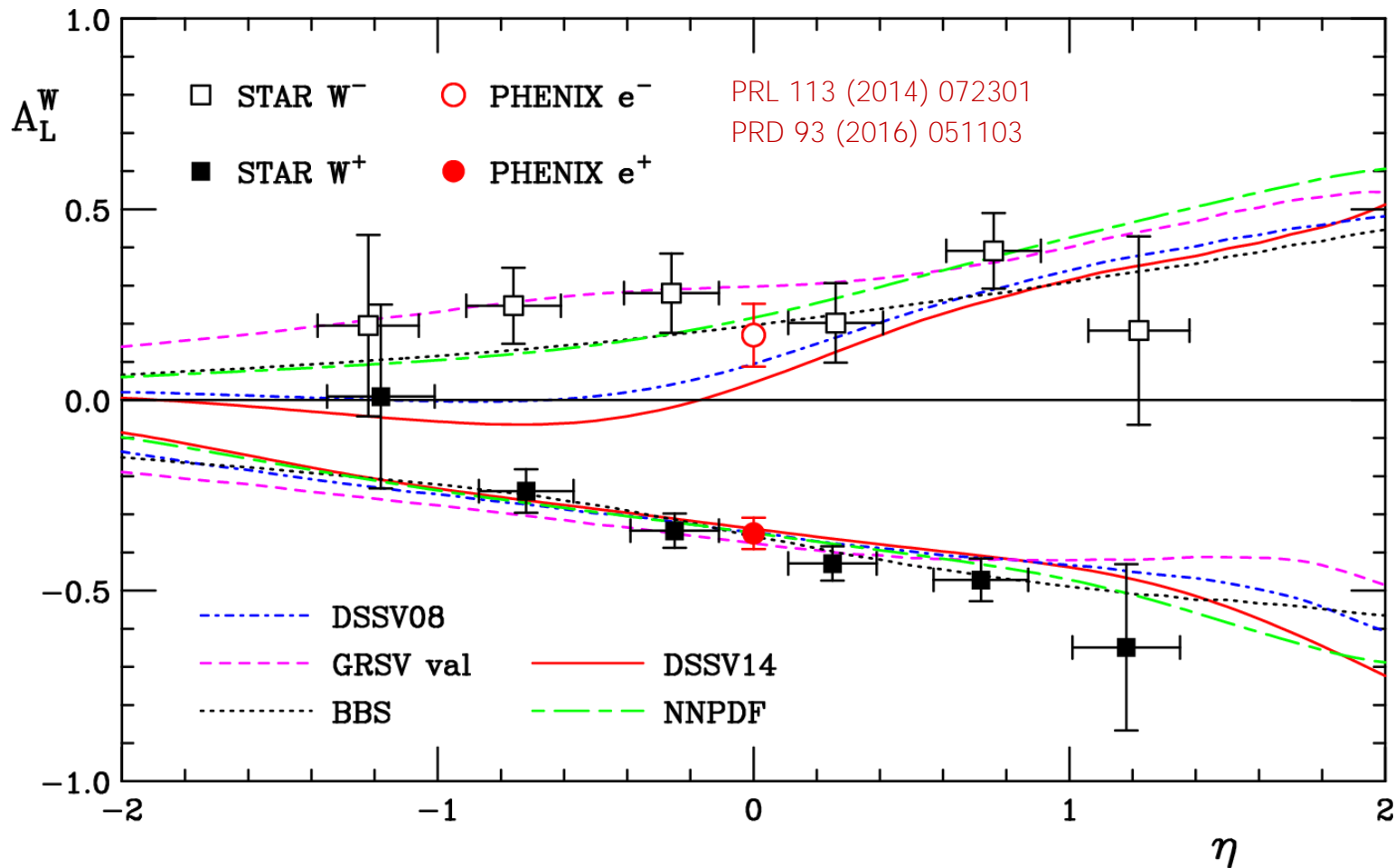
PRD 93 (2016) 051103

$$A_L^{W^-} = \frac{\Delta\bar{u}}{\bar{u}} \quad \frac{1}{2} \left(\frac{\Delta\bar{u}}{\bar{u}} - \frac{\Delta d}{d} \right) \quad -\frac{\Delta d}{d}$$



PRL 113 (2014) 072301
















W production in pp



Ringer, Vogelsang: PRD 91 (2015) 094033

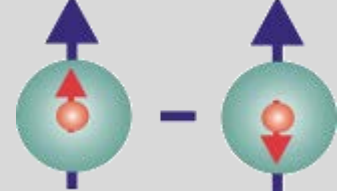
Best agreement for W^- with GRSV val
with sizable positive $\Delta\bar{u}$

TMD distributions

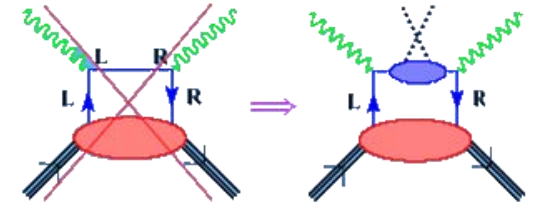
		nucleon polarization		
		U	L	T
quark polarization	U	f_1  number density		f_{1T}^\perp  -  <i>Sivers</i>
	L		g_1  -  helicity	g_{1T}  -  <i>worm-gear</i>
	T	h_1^\perp  -  <i>Boer-Mulders</i>	h_{1L}^\perp  -  <i>worm-gear</i>	h_1  -  <i>transversity</i> h_{1T}^\perp  -  <i>Pretzelosity</i>

- 8 TMD PDFs at leading twist
- 3 non-vanishing k_T -integrated PDFs: f_1 , g_1 , h_1
- Azim. asym. with different angular modulations in ϕ_h and ϕ_S
- TMDFF

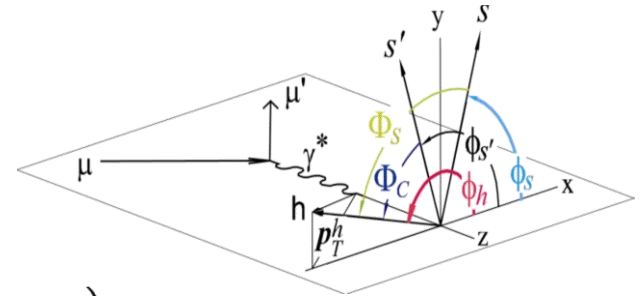
Transversity h_1



- chiral-odd \rightarrow vanishes in DIS \rightarrow SIDIS



- leads to azimuthal modulation in the Collins angle $\phi_C = \phi_h + \phi_S - \pi$
($-\pi$ used by COMPASS)



- amplitude

$$A_{\text{Coll}}^h \propto \frac{\sum_q e_q^2 h_1^q(x) \otimes H_1^{\perp h/q}(z, p_T)}{\sum_q e_q^2 f_1^q(x) D^{h/q}(z)}$$

- Collins fragmentation function $H_1^{\perp}(z, p_T)$ from e^+e^-
- convolution (\otimes) over intrinsic transverse momentum k_T
- product for 2-hadron asymmetries coupled to IFF $H_1^{\otimes}(z, M_h^2)$

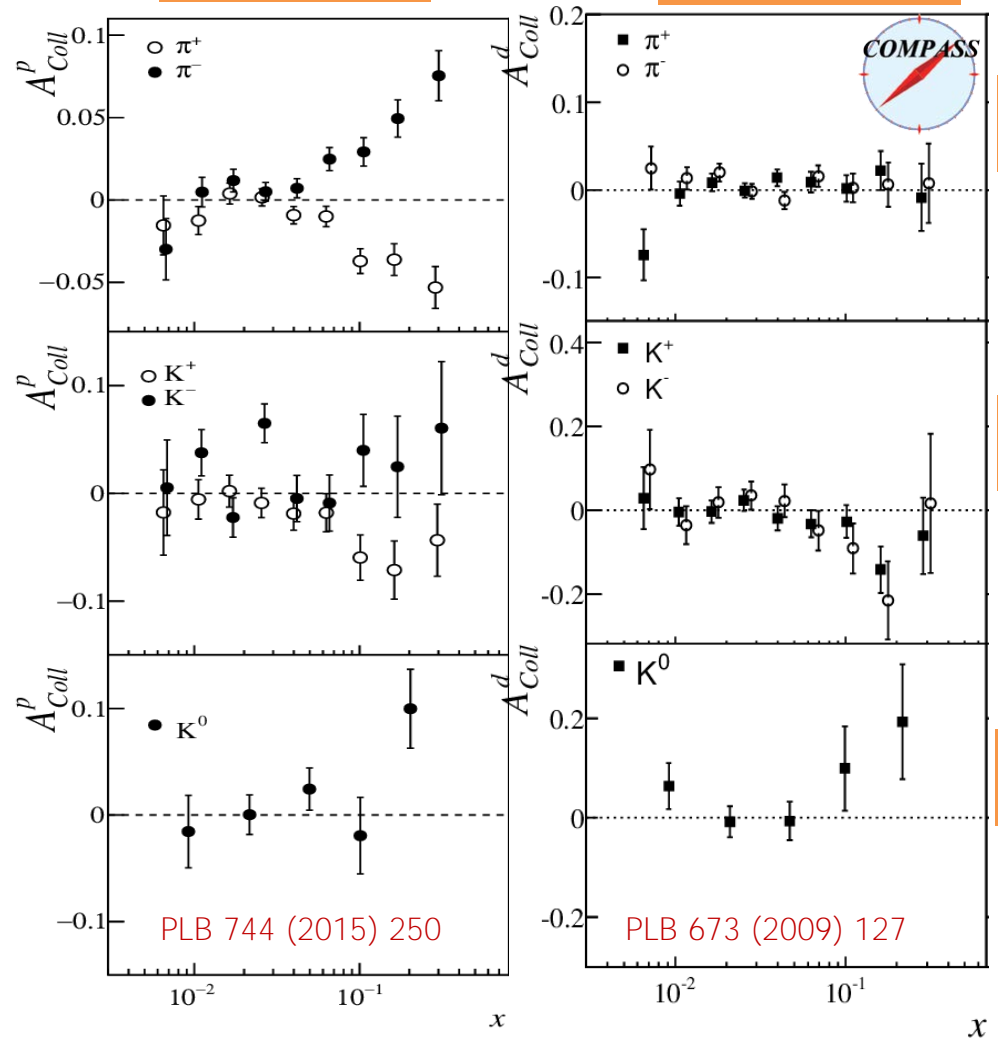
Collins asymmetry for proton & deuteron

- first proton data from Hermes
PRL 94 (2005) 012002
- sizable for proton
- mirror symmetry π^+ and π^-
- small for deuteron
- di-hadron asym. are similar, collin. factorisation $h_1 \times H_1^x$

PLB 736 (2014) 124

proton

deuteron



π^\pm

K^\pm

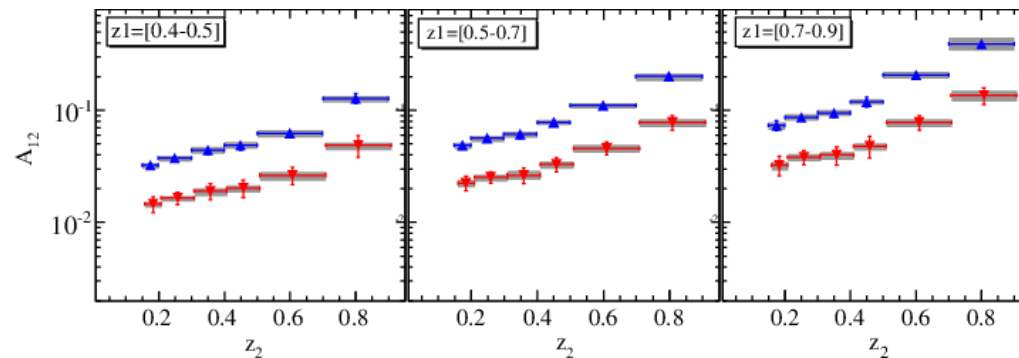
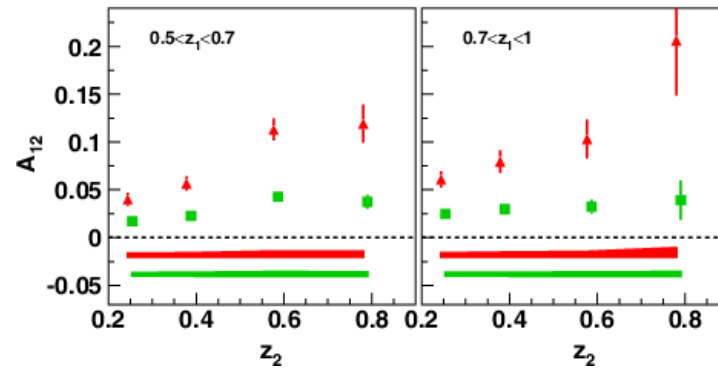
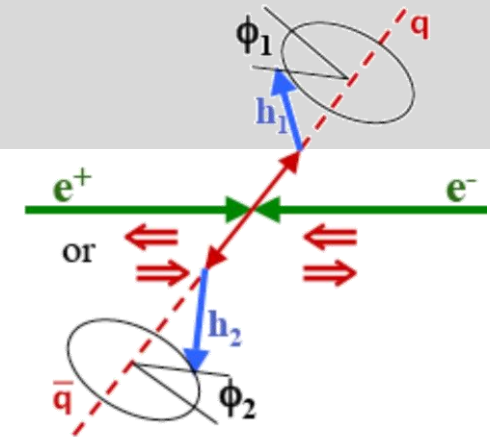
K^0

Collins FF from e^+e^-

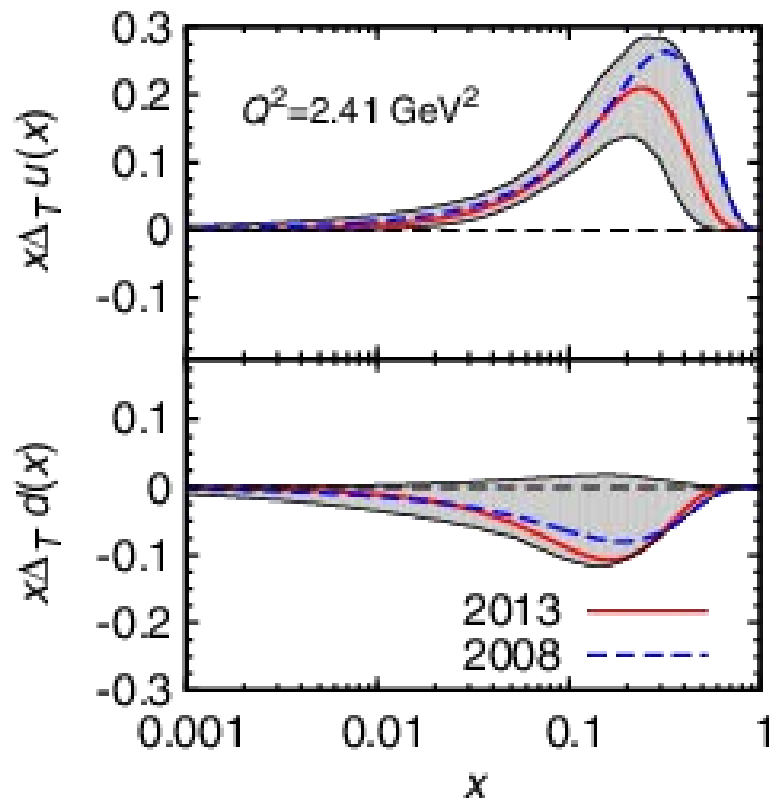
- $\propto H_1^\perp \otimes H_1^\perp$
- Belle, Babar, BESIII

Belle: PRD 90 (2012) 052003
 Babar: PRD 90 (2014) 052003
 BESIII: PRL116 (2016) 042001

- clear signals



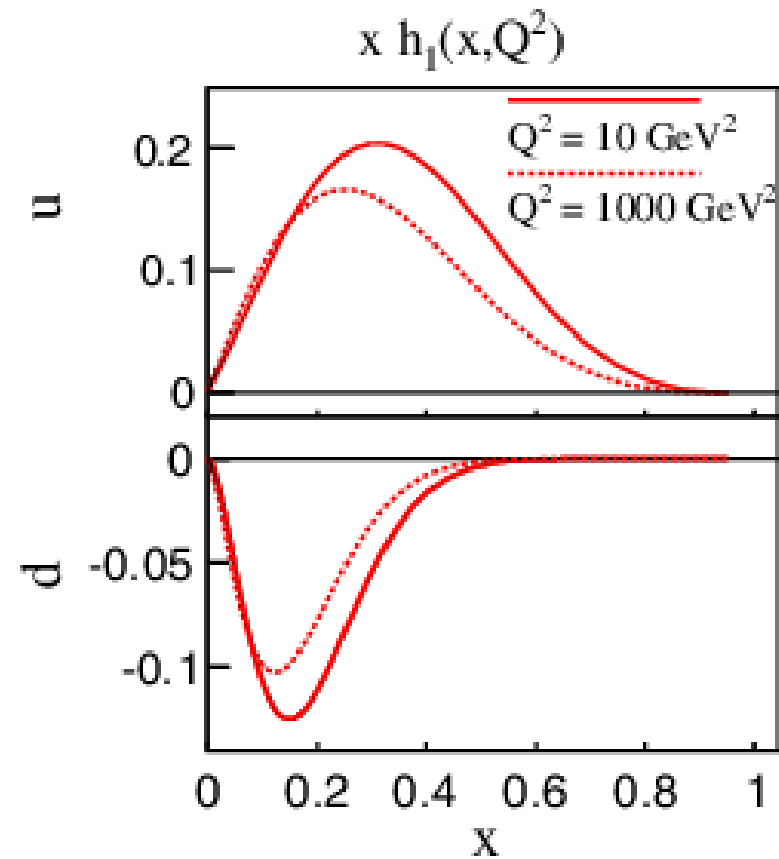
Determination of h_1 from SIDIS & e^+e^-



Anselmino et al.,
PRD 87 (2013) 094019

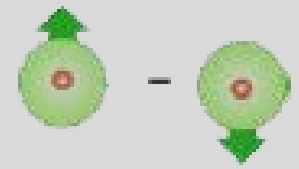
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Kang et al.,
PRD 91 (2015) 071501(R)

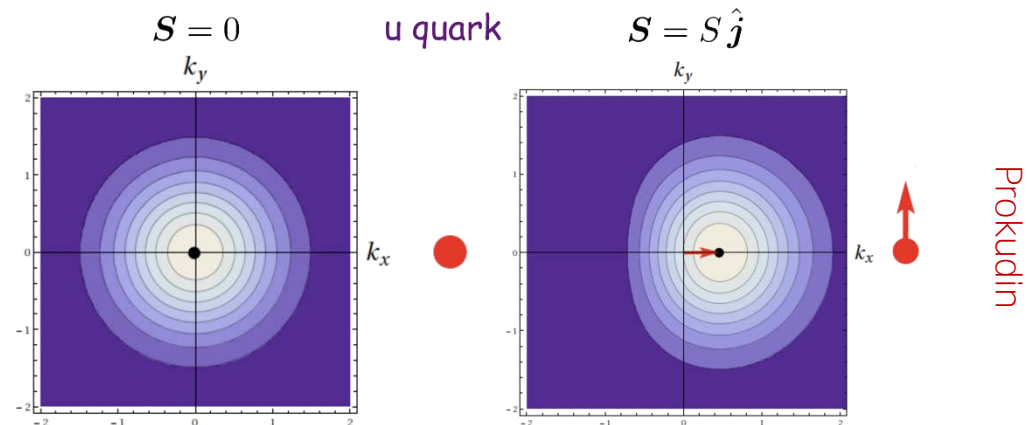
Sivers TMD f_{1T}^\perp



- azim. asym. in $\phi_{Siv} = \phi_h - \phi_S$

$$A_{Siv}^h \propto \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, k_T) \otimes D_1^{h/q}(z, p_T)}{\sum_q e_q^2 f_1^q(x, k_T) \otimes D_1^{h/q}(z, p_T)}$$

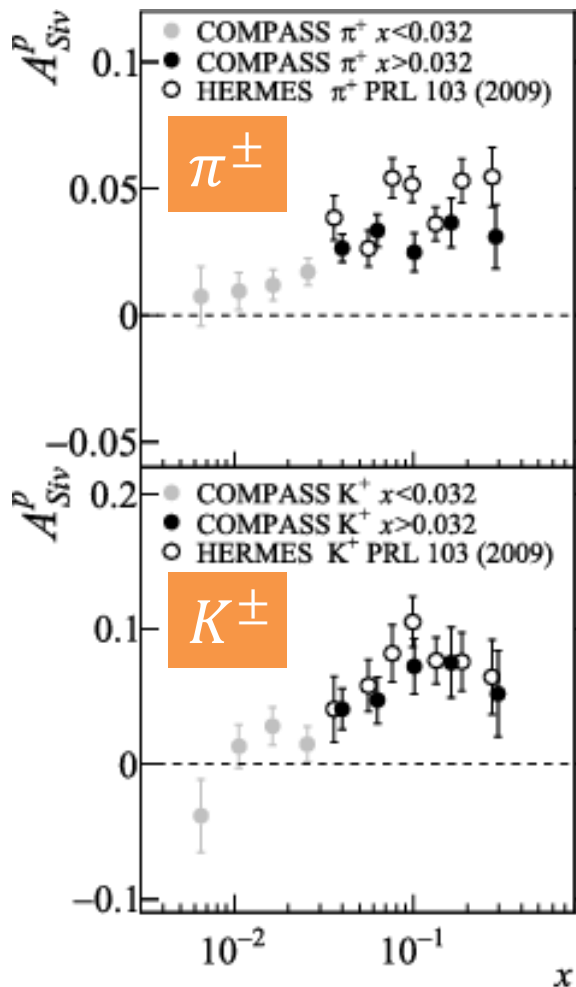
- if non-zero \rightarrow orbital angular momentum
- induces distortions in the PDF of polarized nucleons



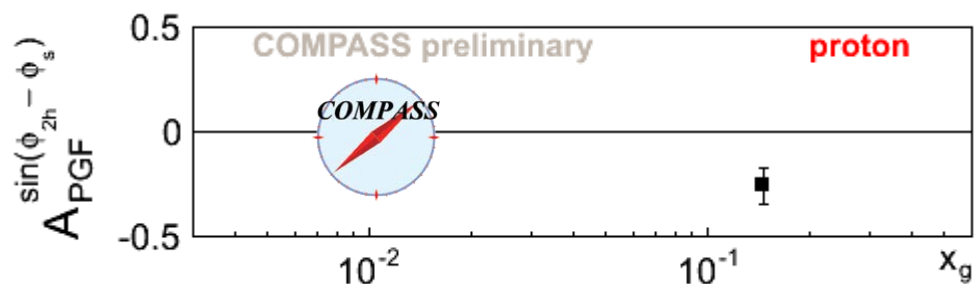
Sivers asymmetry



proton



- sizable for proton
- Hermes vs Compass: some Q^2 evolution
- Sivers small for deuteron
- gluon: indication from 2h



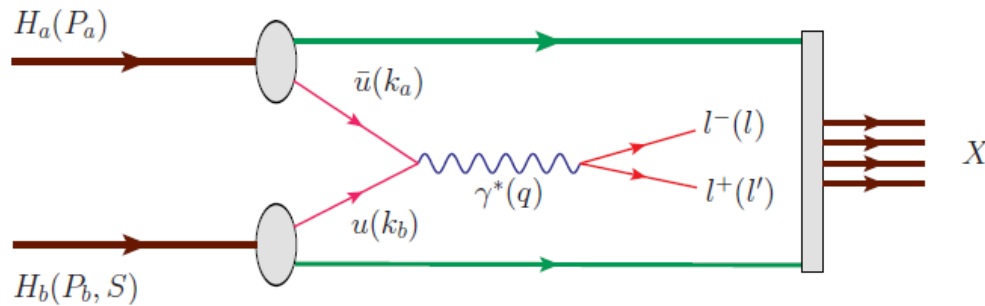
A. Szabelski, DIS2016

Hermes: PRL 103 (2009) 152002

COMPASS: PLB 744 (2015) 250

G.K. Mallot 30/08/2016

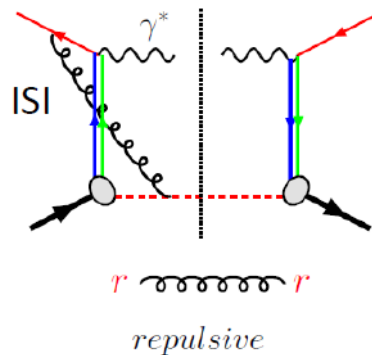
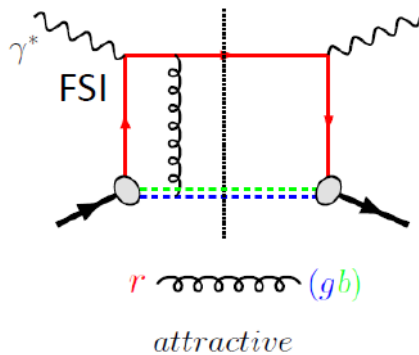
Restricted universality in SIDIS and **pol.** DY



T-odd TMDs:

'gauge link changes sign for T-odd TMD', restricted universality of T-odd TMDs

J.C. Collins, PLB536 (2002) 43



Compass measures SIDIS and DY with same spectrum.

$$f_{1T}^\perp|_{\text{DIS}} = \color{red}{-} f_{1T}^\perp|_{\text{DY}}$$

Sivers

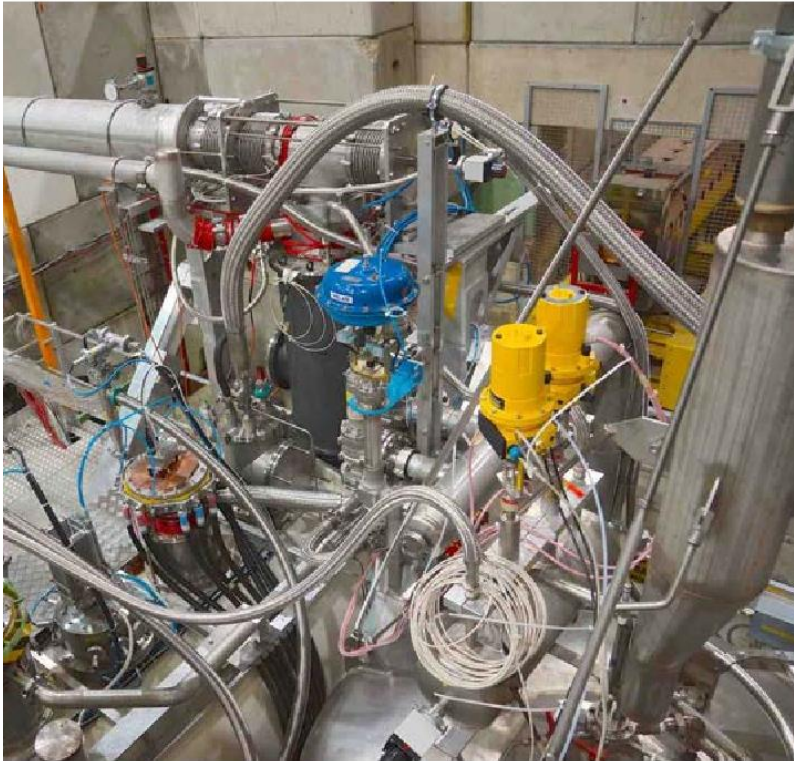
$$h_1^\perp|_{\text{DY}} = \color{red}{-} h_1^\perp|_{\text{DIS}}$$

Boer-Mulders

- important prediction, needs to be verified: COMPASS, FNAL, RHIC?

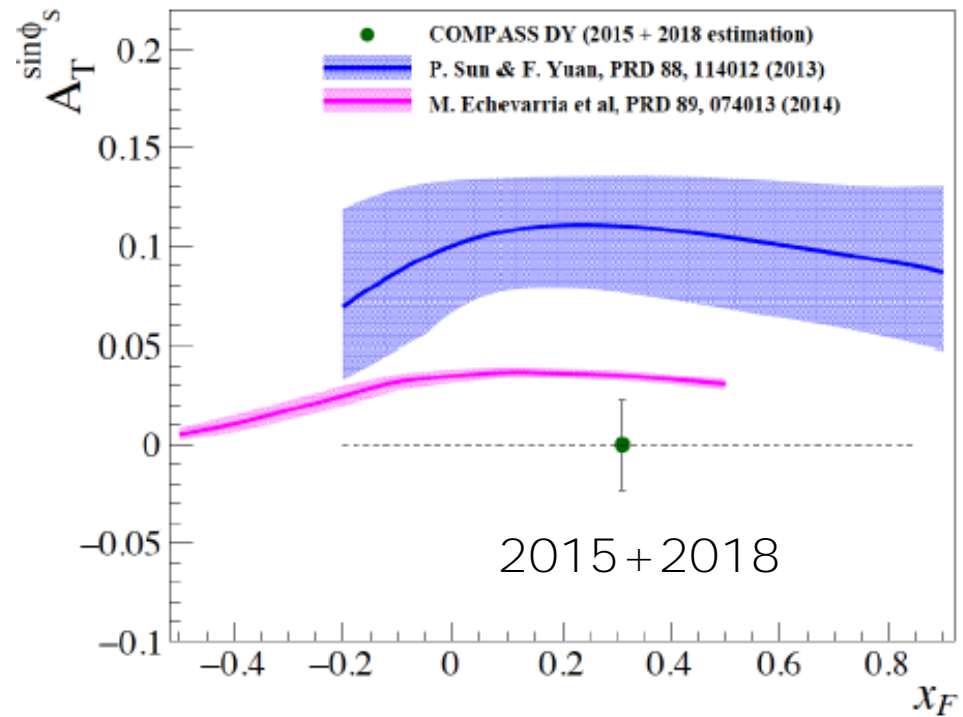
COMPASS polarized DY

- first results at Spin2016



- Predictions vary strongly, due to different TMD evolution
- 2015: uncertainty ~ 0.04

→ Longo: Thu 17:30

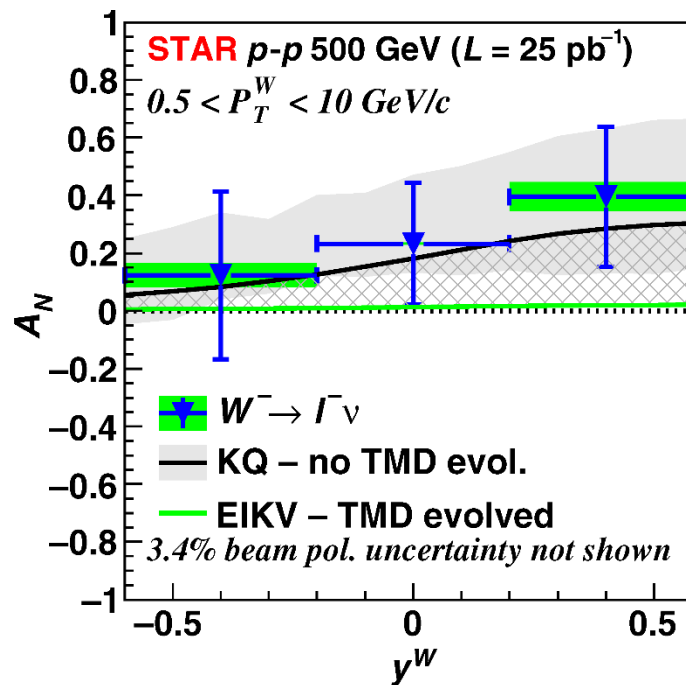
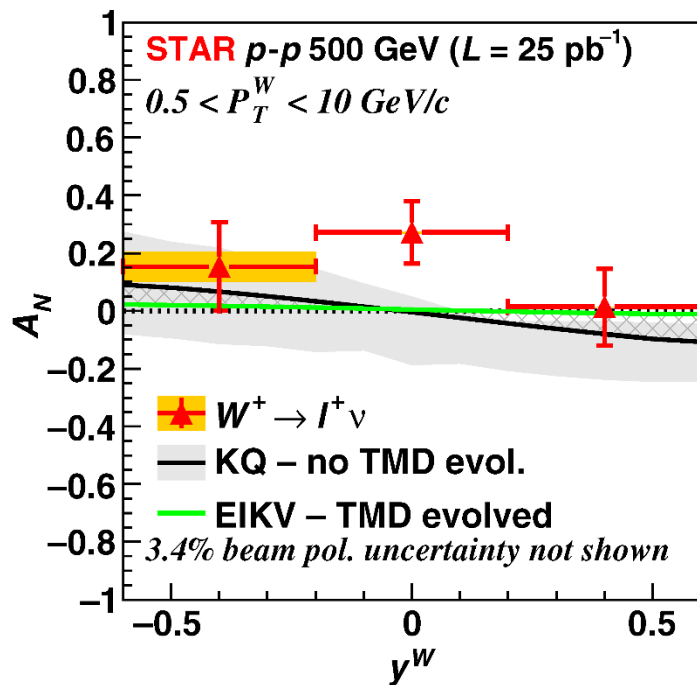


2015+2018

$$x_F = x_\pi - x_p$$

- Fermilab, RHIC, ...

Sivers in W production



PRL 116, 132301 (2016)

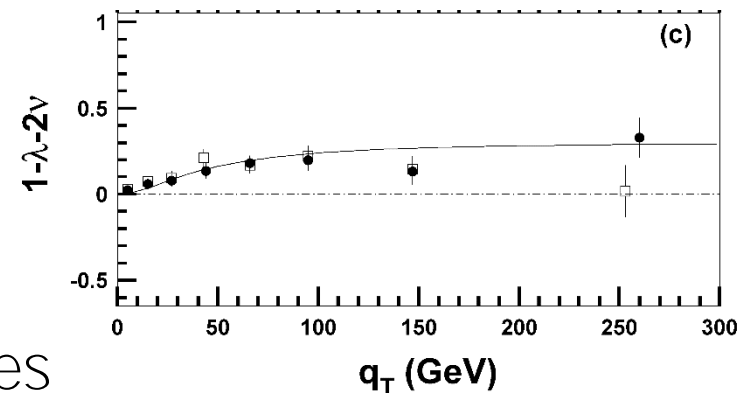
- 2011 data, 25 pb^{-1}
- no TMD evolution: clear preference for sign change!
- with EIKV TMD evolution: no sizable Sivers effect
- need more data

Boer-Mulders in Drell-Yan?

$$\frac{dN}{d\Omega} = \frac{3}{4\pi} \frac{1}{\lambda + 3} \left[1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi \right]$$

- Lam-Tung relation $1 - \lambda - 2\nu = 0$
- new CMS data: $pp \rightarrow ZX \rightarrow \mu\bar{\mu}X$ violate Lam-Tung relation
- Boer-Mulders TMD h_1^\perp contr. to $\cos 2\phi$ modulation?
- misalignment of $q\bar{q}$ and hadron planes do to gluon emission causes modification of Lam-Tung relation

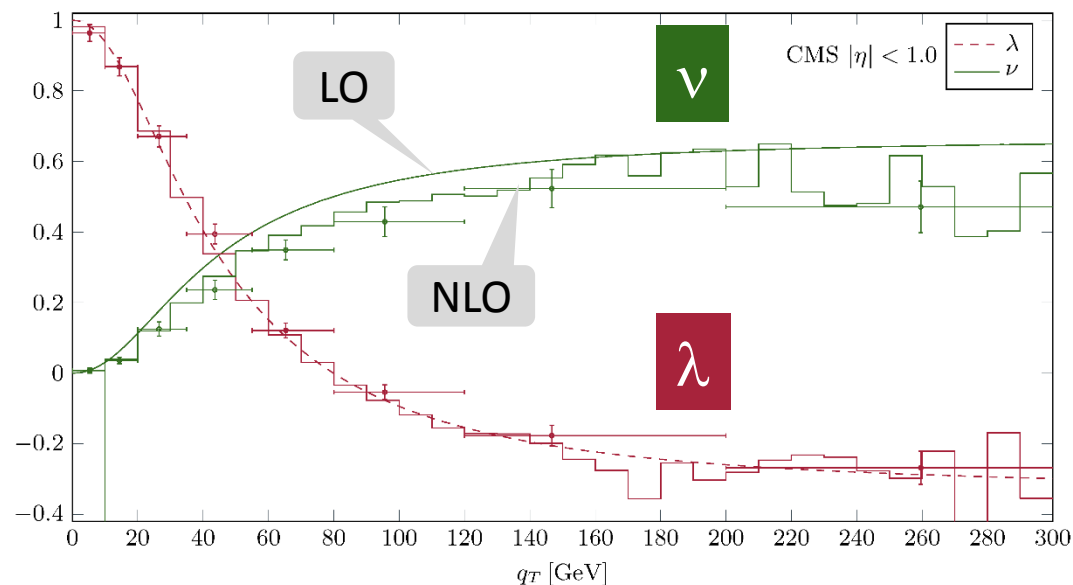
CMS, PLB 750 (2015) 154



Peng et al., PLB 758 (2016) 384

Boer-Mulders in DY?

- NLO calculations describe DY data well!



Lambertsen, Vogelsang
PRD 93 (2016) 114013

CMS, PLB 750 (2015) 154

$\sqrt{s} = 8 \text{ TeV}$
 $81 \text{ GeV} < Q < 101 \text{ GeV}$

- Need more data to establish a possible BM contribution
→ COMPASS, SeaQuest, LHC, RHIC?

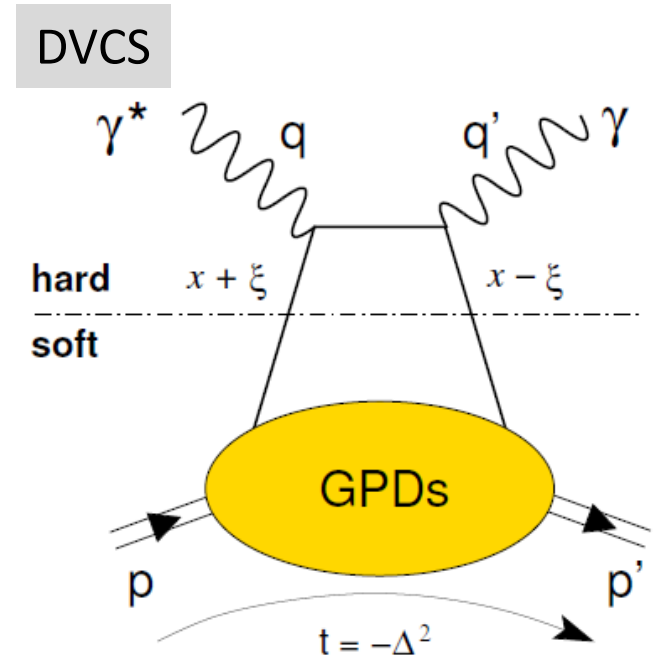
Generalised parton distributions

Generalized PDF's

- Correlating **transverse spatial** and **longitudinal momentum** degrees of freedom

$$H(x, \xi, t, Q^2); \quad Q^2 \text{ large, } t \text{ small}$$

- meas. 4 dim diff x-sect: x, Q^2, t, ϕ
- DVCS, hard exclusive meson prod.

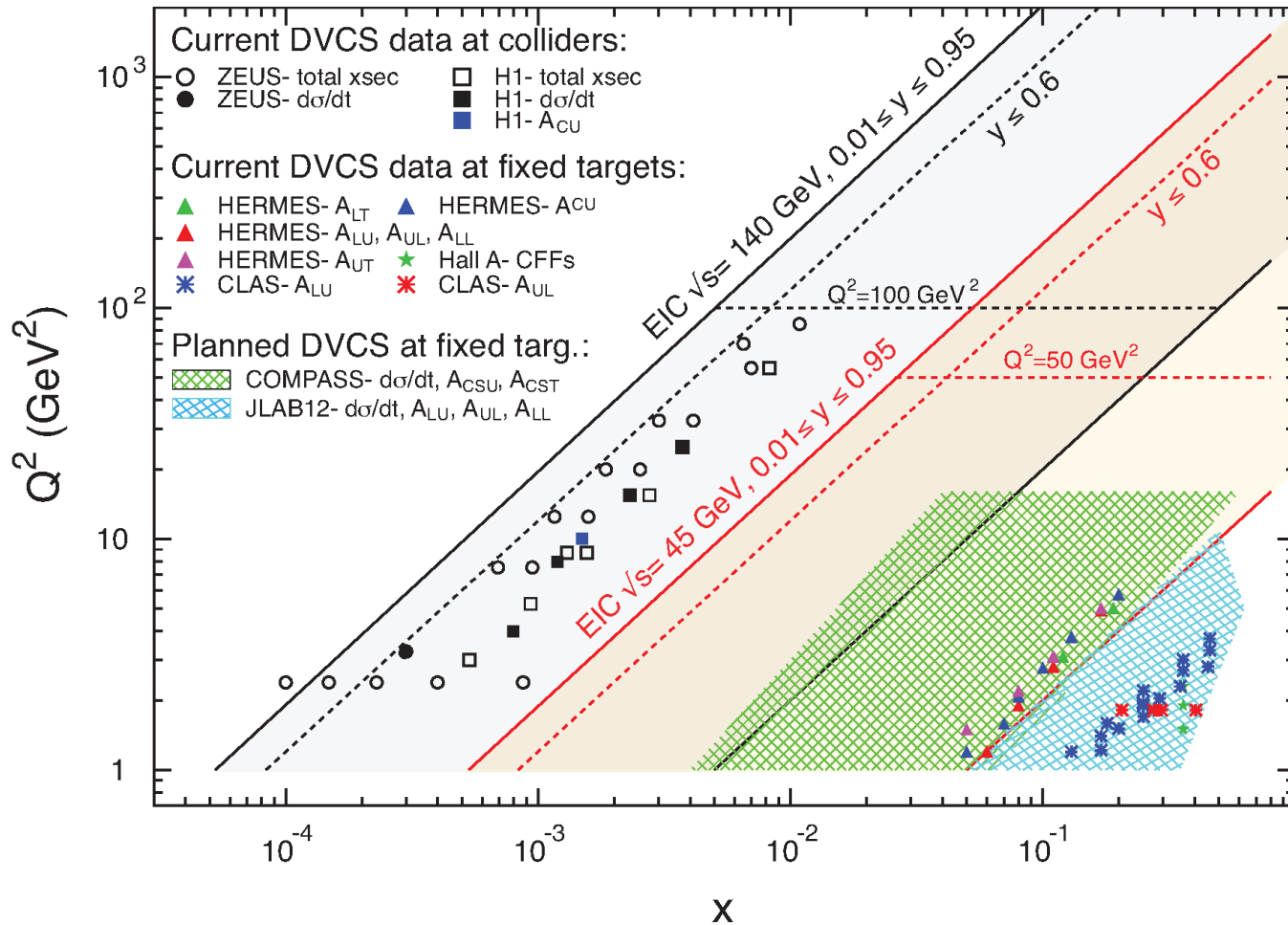


Ji's sum rule for total orbital momentum:

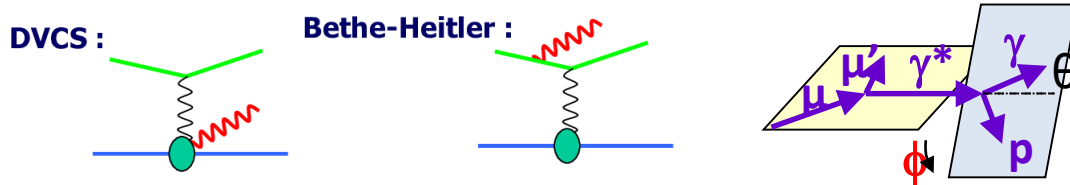
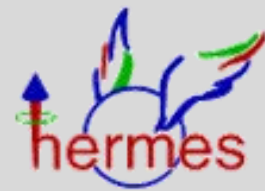
$$J^f(Q^2) = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x \left[H^f(x, \xi, t, Q^2) + E^f(x, \xi, t, Q^2) \right]$$

X.-D. Ji, PRL 78 (1997) 610

DVCS: experimental kinematic ranges

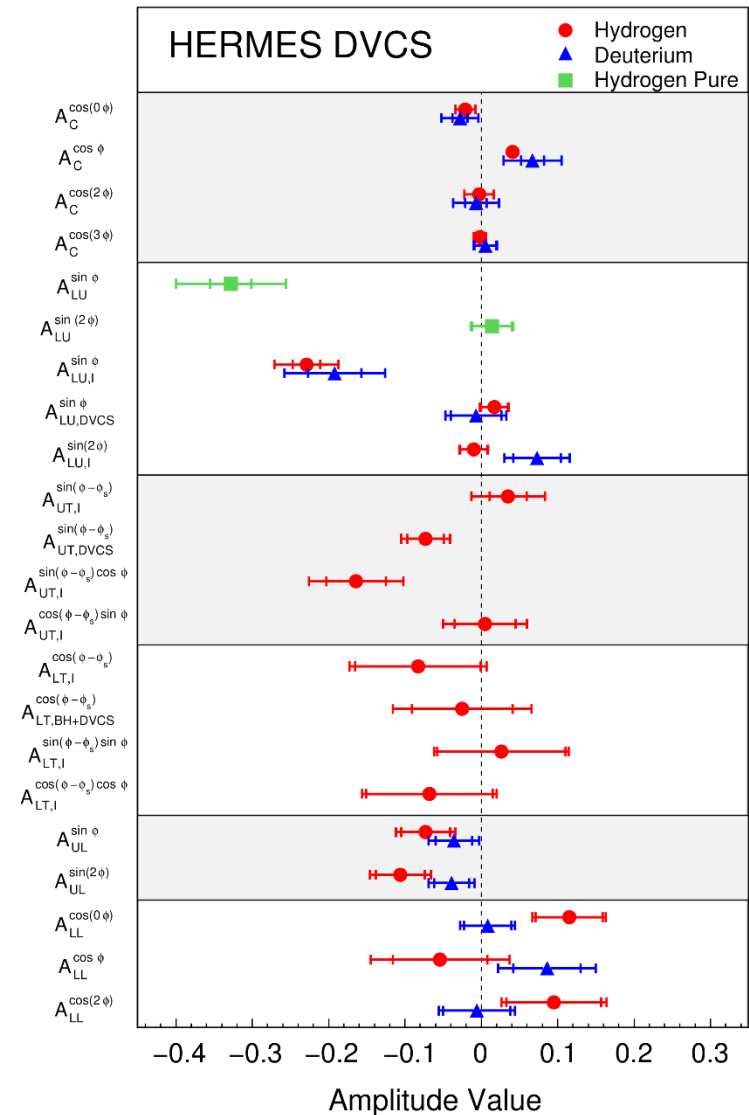


Deeply virtual Compton scattering

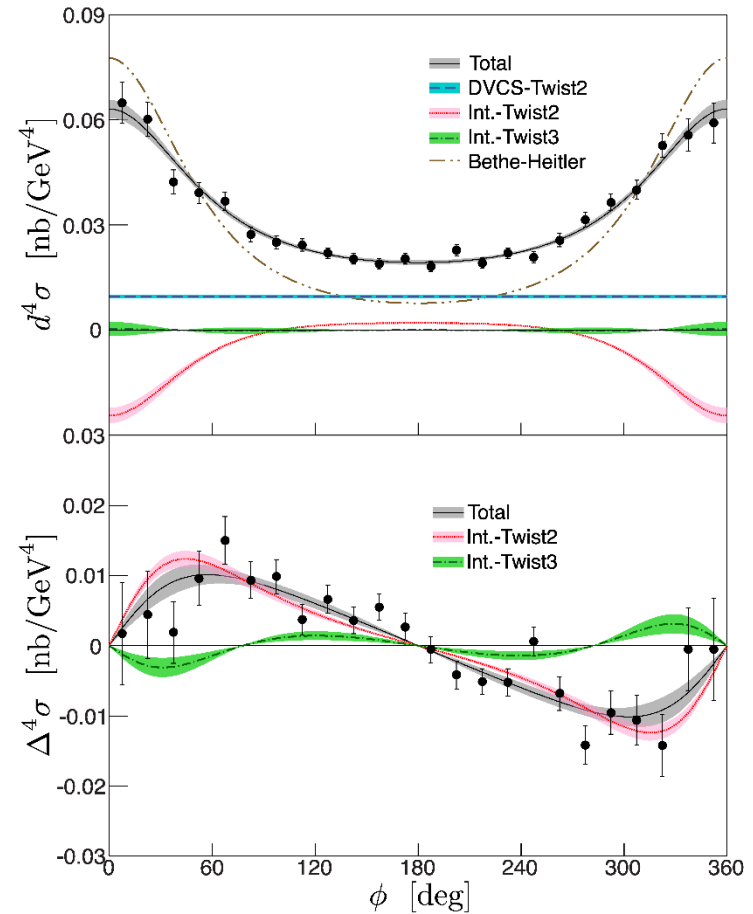


- cross-section depend on lepton charge e_ℓ and pol. P_ℓ , and on target pol. S
- contributions with different azimuthal dependence from:

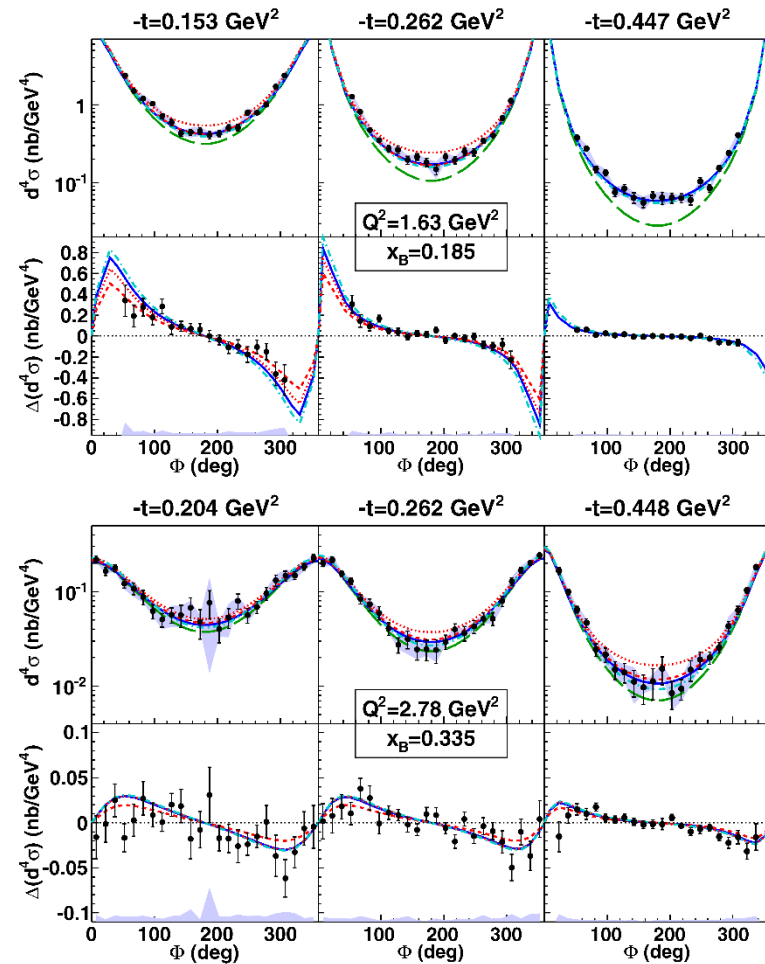
BH	interference	DVCS
$d\sigma(lp \rightarrow l\gamma p) \sim$		
$d\sigma_{UU}^{BH}$	$+ e_\ell d\sigma_{UU}^I$	$+ d\sigma_{UU}^{DVCS}$
$+ P_\ell S_L d\sigma_{LL}^{BH}$	$+ e_\ell P_\ell S_L d\sigma_{LL}^I$	$+ P_\ell S_L d\sigma_{LL}^{DVCS}$
$+ P_\ell S_T d\sigma_{LT}^{BH}$	$+ e_\ell P_\ell S_T d\sigma_{LT}^I$	$+ P_\ell S_T d\sigma_{LT}^{DVCS}$
	$+ e_\ell P_\ell d\sigma_{LU}^I$	$+ P_\ell d\sigma_{LU}^{DVCS}$
	$+ e_\ell S_L d\sigma_{UL}^I$	$+ S_L d\sigma_{UL}^{DVCS}$
	$+ e_\ell S_T d\sigma_{UT}^I$	$+ S_T d\sigma_{UT}^{DVCS}$



- final results of Hall-A E00-110
- unpol. x-sect and x-sect differences for beam pol.
- 588 bin ($x_B, Q^2, -t, \phi$)
- exp.:
 $-t = 0.32 \text{ GeV}^2, x=0.36$



- pol. proton (NH_3) target
- x-sect, TSA, BSA, DSA
- 164 bins ($x_B, Q^2, -t, \phi$)
- $1.0 < Q^2 < 4.6 \text{ GeV}^2$
- $0.10 < x_B < 0.58$
- $0.09 < -t < 0.52 \text{ GeV}^2$



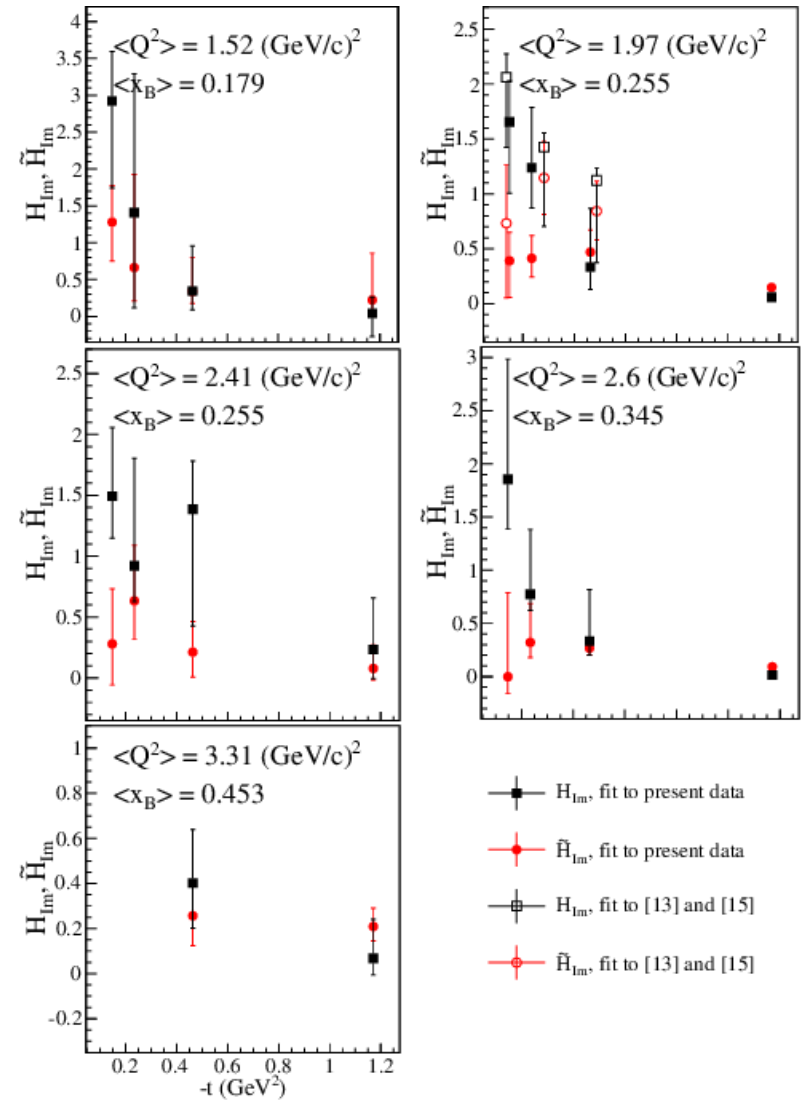
unpol.

beam
pol.

PRL 115 (2015) 212003
PRD 91 (2015) 052014

- determine the imaginary part of CFF H_{Im} and \tilde{H}_{Im} of GPDs \mathcal{H} and $\tilde{\mathcal{H}}$
- most sensitive to \tilde{H}_{Im}

$$F_{Im}(\xi, t) = -\frac{1}{\pi} \Im \mathcal{F}(\xi, t) = [F(\xi, \xi, t) \mp F(-\xi, \xi, t)]$$

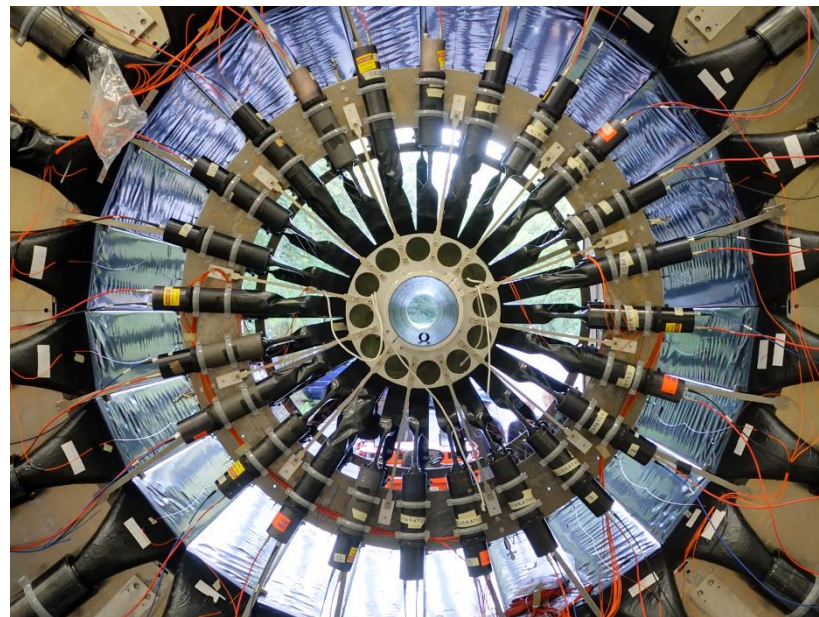
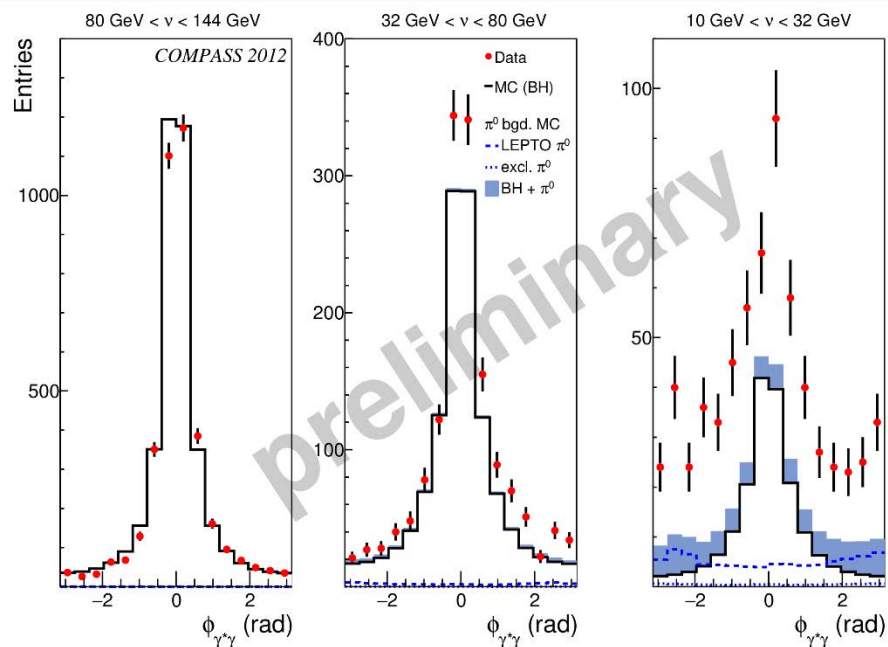


COMPASS DVCS



- GPD data 2012 (pilot), 2016–2017
- liquid hydrogen target
- 3 bin in $\nu \sim 1/x$

- 160 GeV muon beam
- CAMERA recoil detector



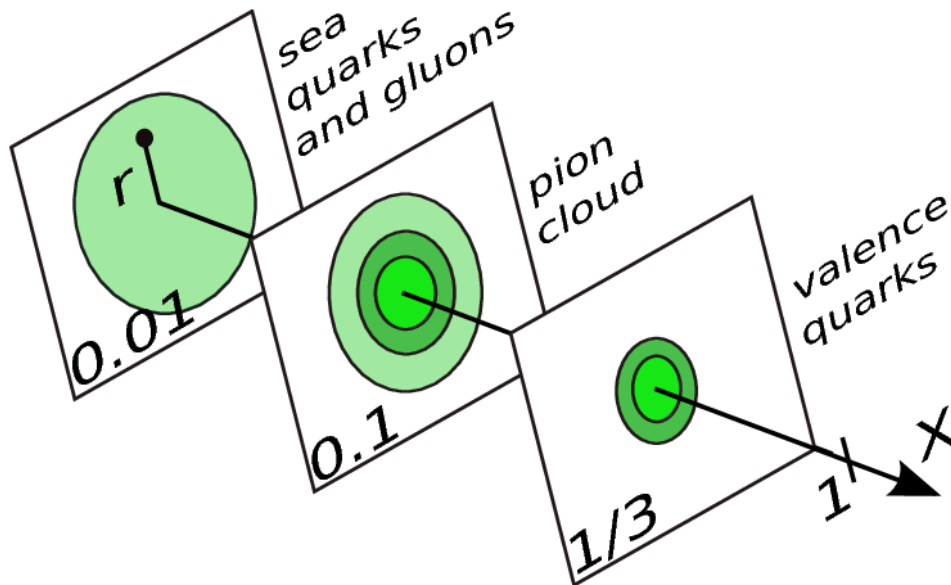


Transverse proton size

- The distance $\langle r_{\perp}^2 \rangle$ between struck quark and spectator c.m. given by t -slope of DVCS cross-section σ_0 (as function of x_B , LO)

$$\frac{d\sigma_0^{\text{DVCS}}}{dt} \propto \exp(-B(x_B)|t|)$$

$$\langle r_{\perp}^2(x_B) \rangle \approx 2B(x_B)$$

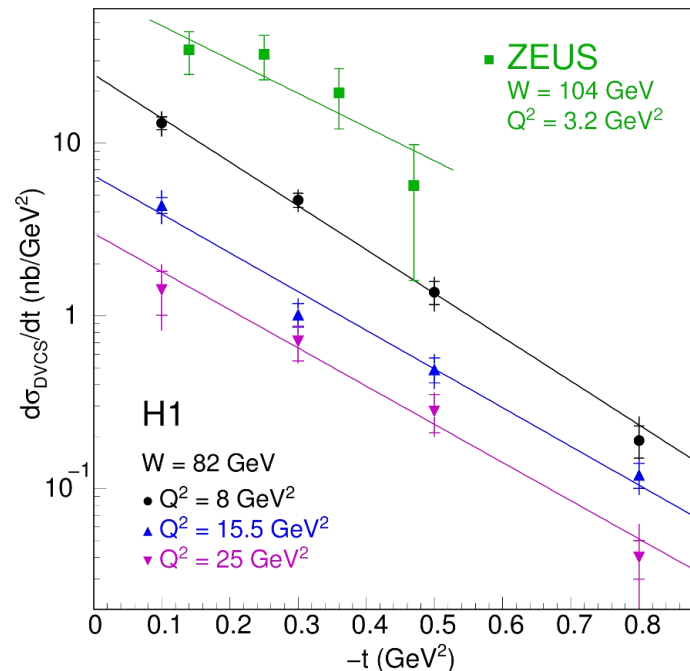
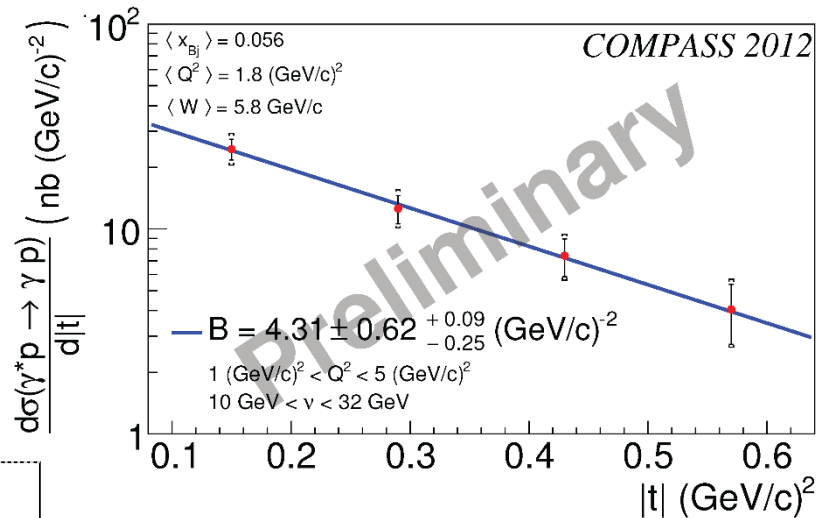
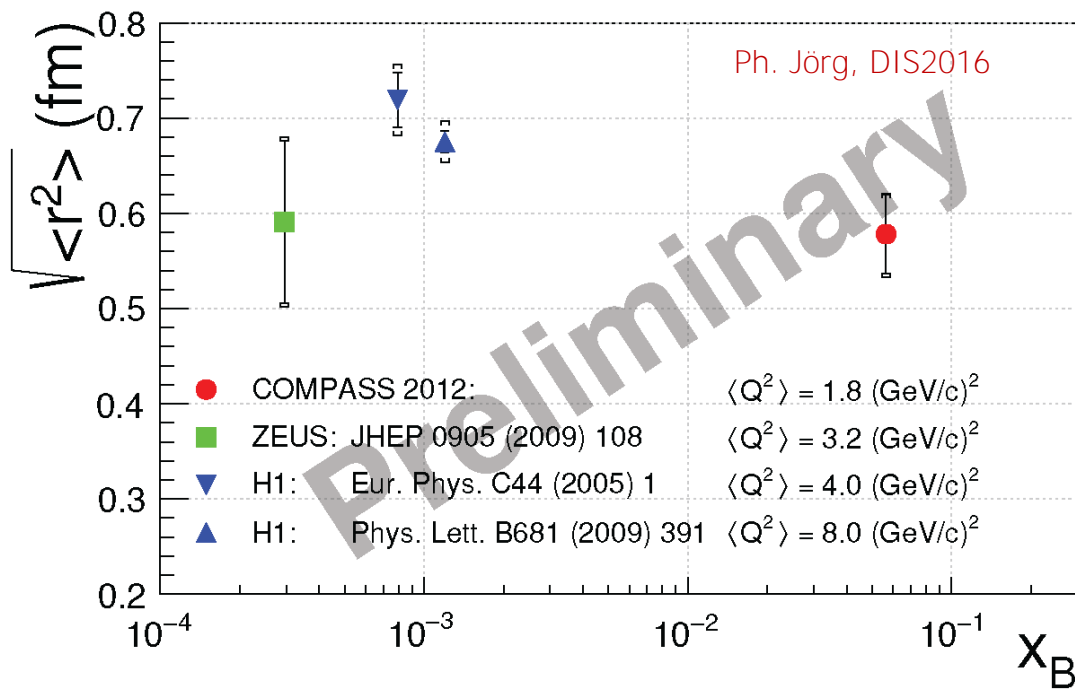


- Transverse size as function of x_B
- Expect log. dependence



t slope and transverse proton size

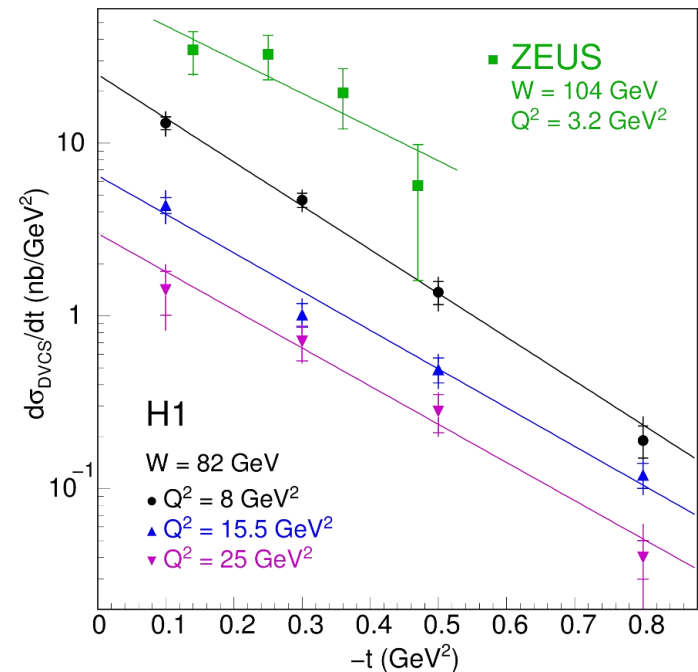
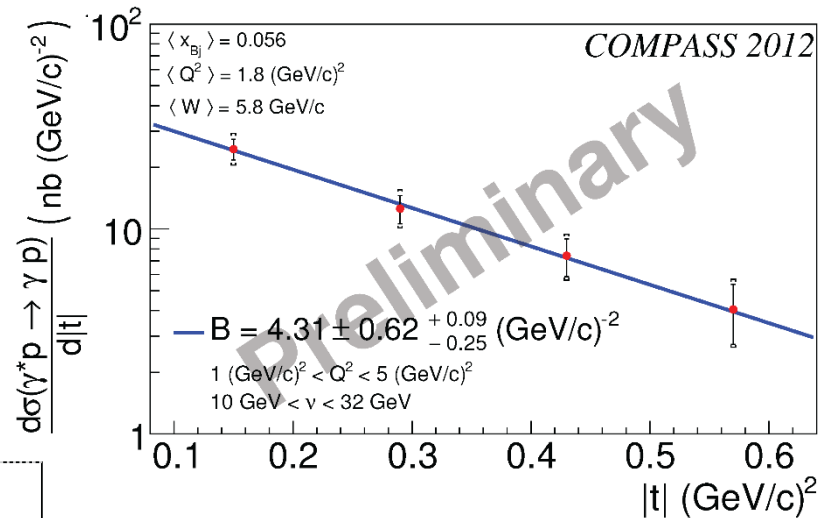
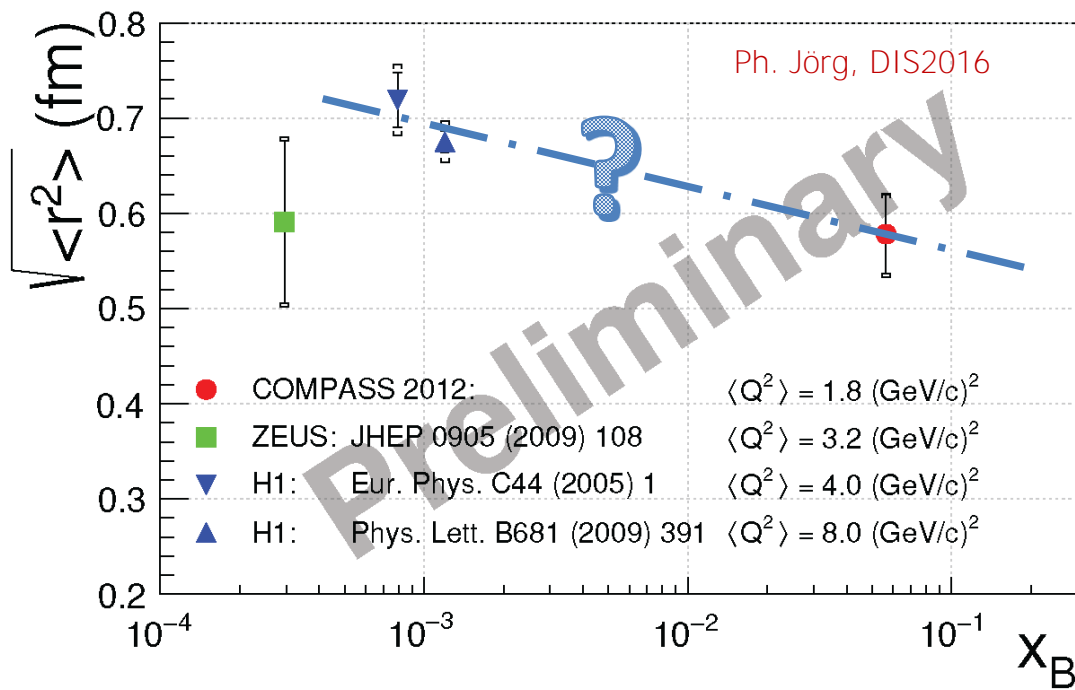
- model independent
- 2012 pilot run data only
- 2016/17 data: several x_B bins, higher precision





t slope and transverse proton size

- model independent
- 2012 pilot run data only
- 2016/17 data: several x_B bins, higher precision



Outlook

- a wealth of new data
- gluon polarisation likely to be positive at $x \cong 0.2$, need low x_g data
- multilicities and FF to be clarified, in particular for kaons/strange quarks, impact PDF determination
- measure the sign change of T-odd TMDs in DY and SIDIS!
- new data coming up JLab 6/12, RHIC, COMPASS, JPARC and eventually EIC