

Extraction of the t-dependence of the pure DVCS x-section

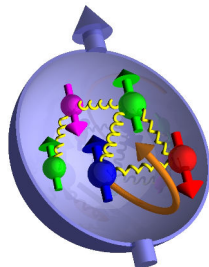
P. Jörg (ALU Freiburg)

on behalf of the COMPASS Collaboration

DIS2016 - Hamburg, 13/04/2016



The Spin Puzzle

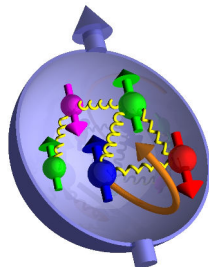


$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + \mathcal{L}$$

(Jaffe&Manohar Nucl.Phys.B337 (1990))

- $\frac{1}{2}\Delta\Sigma \sim 0.15$ well known from DIS/SIDIS
- $\Delta G \sim 0.2$ known from DIS/pp
- \mathcal{L} unknown

The Spin Puzzle



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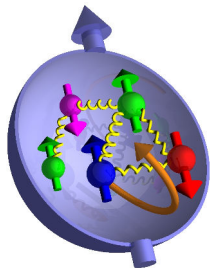
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The **Ji sum rule** connects the Generalized Parton Distributions (GPDs) H and E , measured in exclusive reactions, with the total angular momentum $J^{q,g}$, e.g.

$$J^q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^{+1} x [H^q + E^q] dx$$

(Phys.Rev.Lett.78 (1997))

The Spin Puzzle

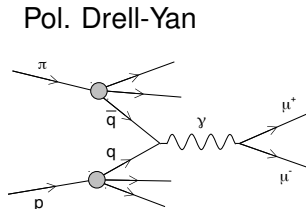
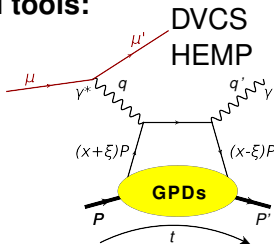
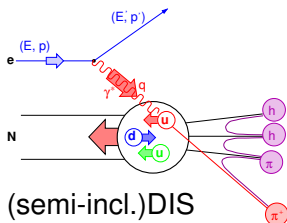


$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + \mathcal{L}$$

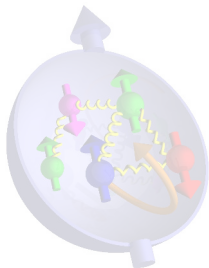
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COMPASS experimental tools:



The Spin Puzzle



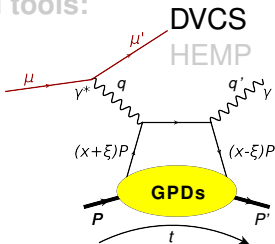
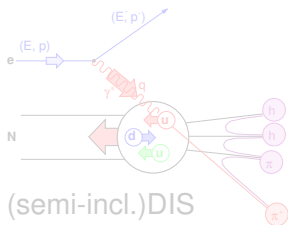
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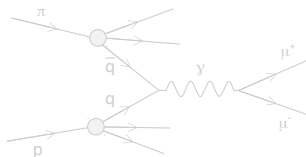
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This talk:

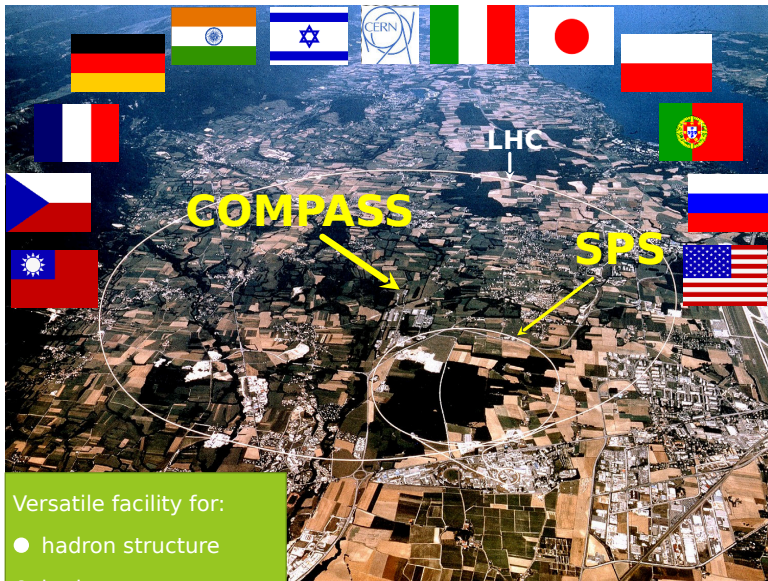
COMPASS experimental tools:



Pol. Drell-Yan



The COMPASS Experiment

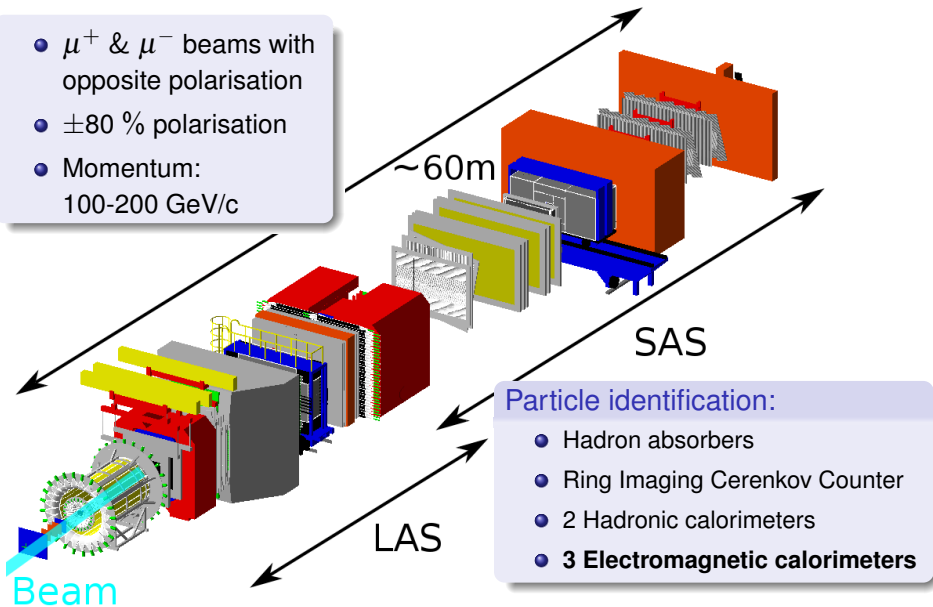


Versatile facility for:

- hadron structure
- hadron spectroscopy

The COMPASS II Spectrometer

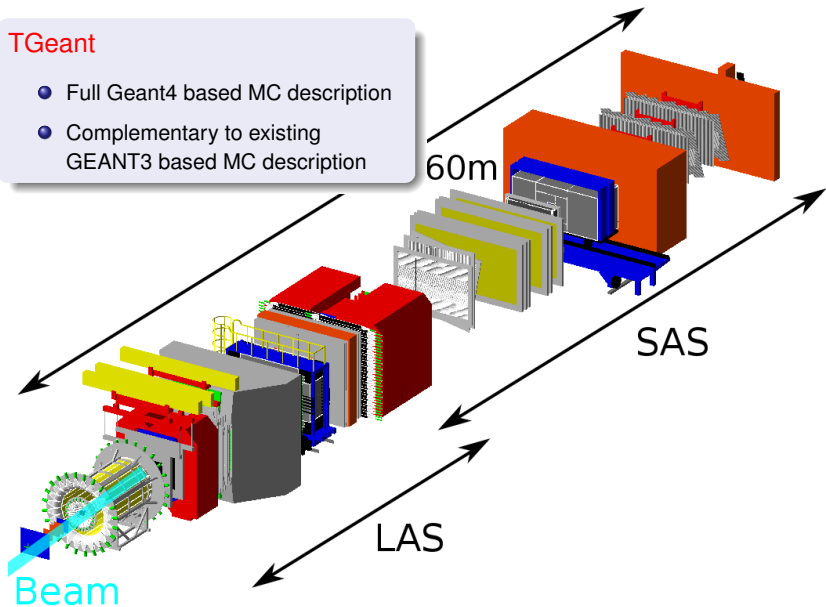
- μ^+ & μ^- beams with opposite polarisation
- $\pm 80\%$ polarisation
- Momentum: 100-200 GeV/c



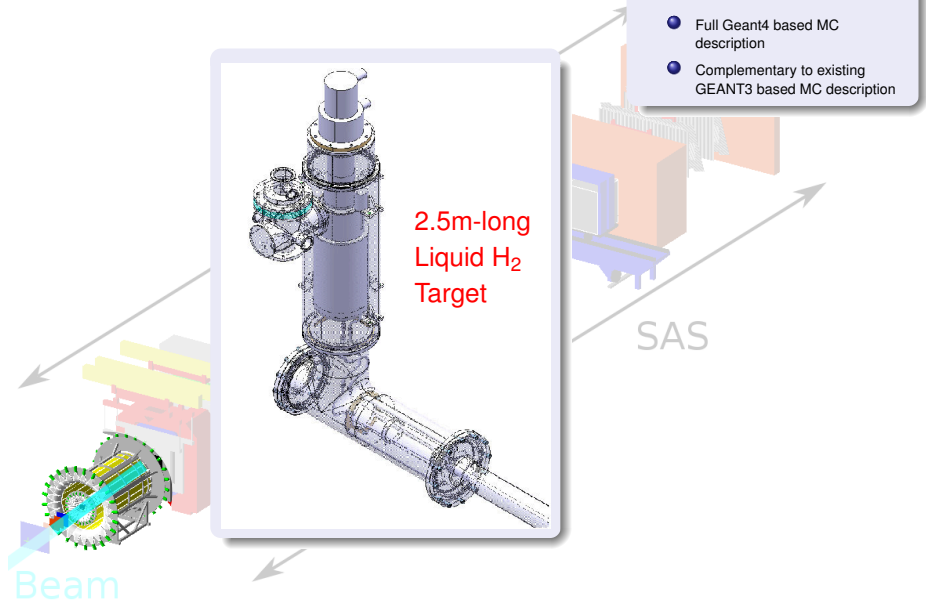
Upgrades for the DVCS Program

TGeant

- Full Geant4 based MC description
- Complementary to existing GEANT3 based MC description



Upgrades for the DVCS Program

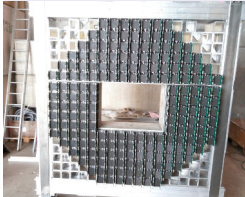
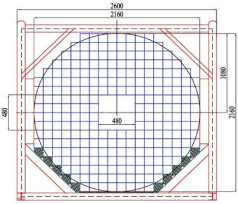


Upgrades for the DVCS Program

ECAL0 Calorimeter

Shashlyk modules + MAPD readout

$\sim 2 \times 2 \text{ m}^2$, ~ 2200 ch.

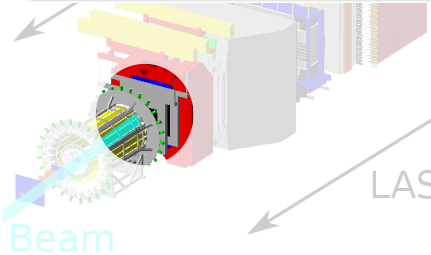


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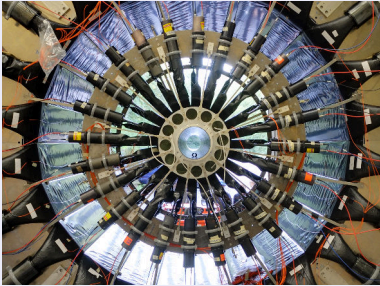
2.5m-long
Liquid H₂
Target



Upgrades for the DVCS Program

Target ToF System

24 inner & outer scintillators
1 GHz SADC readout
Goal: **310 ps** ToF resolution



TGeant

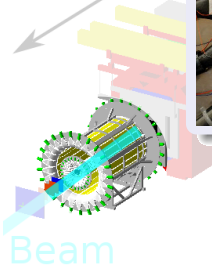
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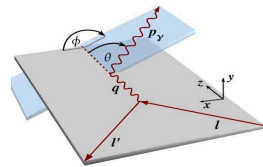
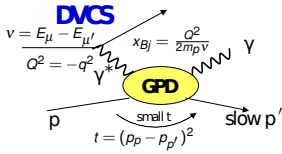
2.5m-long
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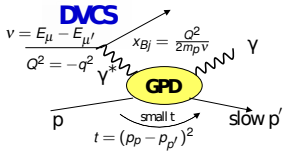
ECAL0 Calorimeter

Shashlyk modules + MAPD readout
~ 2 x 2 m², ~2200 ch.



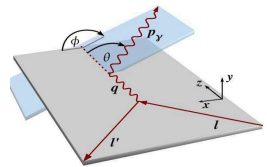
LAS

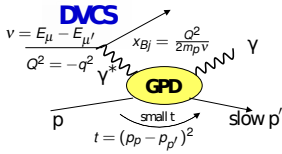




$$d\sigma \propto |T_{DVCS}|^2$$

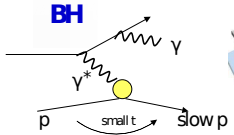
bilinear combination of GPDs





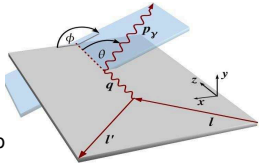
$$d\sigma \propto \underbrace{|T_{DVCS}|^2}_{\text{bilinear combination of GPDs}}$$

bilinear combination of GPDs



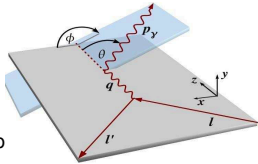
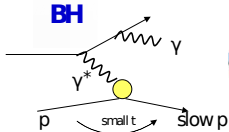
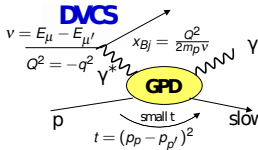
$$+ \underbrace{|T_{BH}|^2}_{\text{known to 1 \%}}$$

known to 1 %

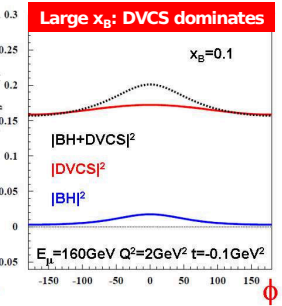
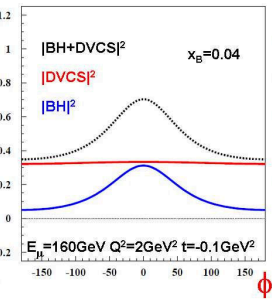
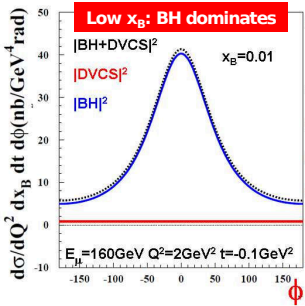


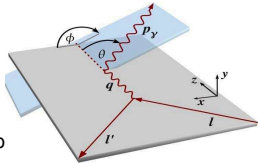
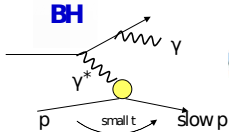
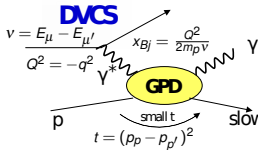
$$+ \underbrace{\text{interference term}}_{\text{linear combination of GPDs}}$$

linear combination of GPDs

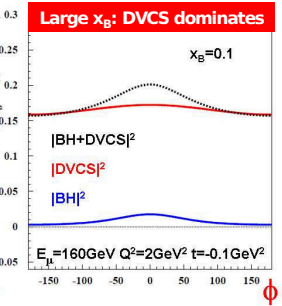
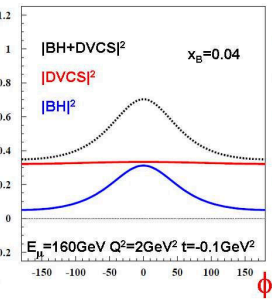
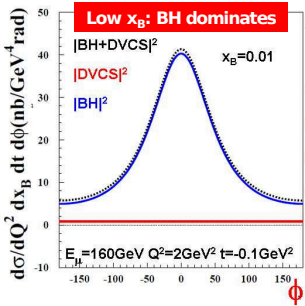


$$d\sigma \propto \underbrace{|T_{DVCS}|^2}_{\text{bilinear combination of GPDs}} + \underbrace{|T_{BH}|^2}_{\text{known to 1 \%}} + \underbrace{\text{interference term}}_{\text{linear combination of GPDs}}$$

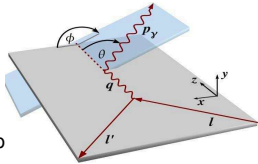
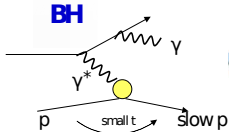
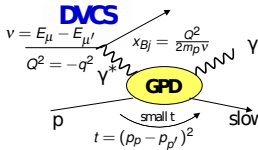




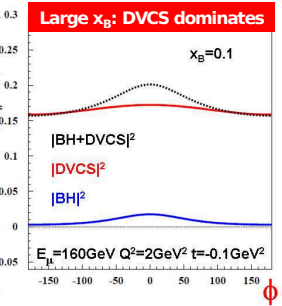
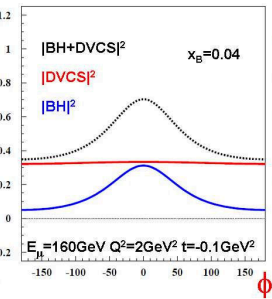
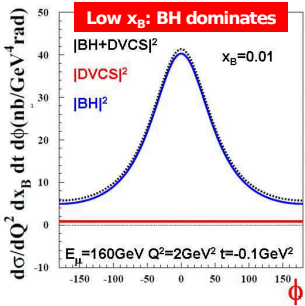
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reference yield of
 almost pure
 Bethe-Heitler

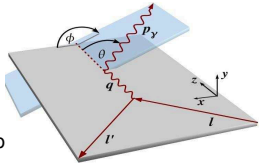
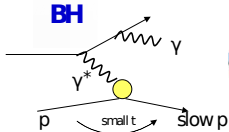
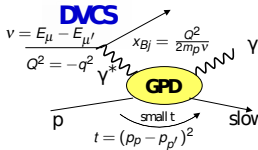


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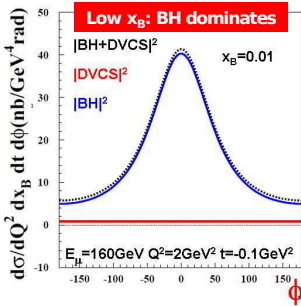


reference yield of almost pure Bethe-Heitler

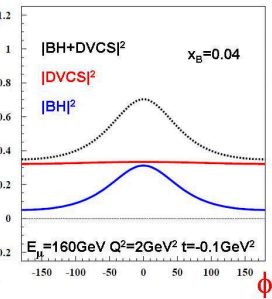
Study DVCS with:
 $\text{Re}(T^{DVCS})$ & $\text{Im}(T^{DVCS})$
 via $(d\sigma^{+\leftarrow} \pm d\sigma^{-\rightarrow})$



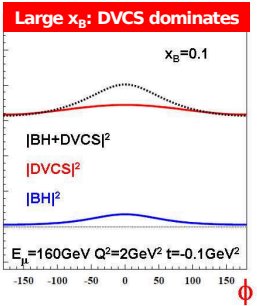
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reference yield of almost pure Bethe-Heitler



Study DVCS with: $\text{Re}(T^{DVCS})$ & $\text{Im}(T^{DVCS})$ via $(d\sigma^{+\leftarrow} \pm d\sigma^{-\rightarrow})$



Transverse Imaging: $d\sigma^{DVCS}/dt$ via $(d\sigma^{+\leftarrow} + d\sigma^{-\rightarrow})$

Transverse Nucleon Imaging at $x_{Bj} > 0.03$

- Measure $S_{CS,U} = (d\sigma^{+\leftarrow} + d\sigma^{-\rightarrow})$ $S_{CS,U} \propto d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + e_{\mu} P_{\mu} \text{Im } I$

note:

$$d\sigma_{unpol}^{DVCS} \propto c_0^{DVCS} + c_1^{DVCS} \cos \phi_{\gamma^* \gamma} + c_2^{DVCS} \cos 2\phi_{\gamma^* \gamma}$$

$$\text{Im } I \propto s_1^I \sin \phi_{\gamma^* \gamma} + s_2^I \sin 2\phi_{\gamma^* \gamma}$$

Transverse Nucleon Imaging at $x_{Bj} > 0.03$

- Measure $S_{CS,U} = (d\sigma^{+\leftarrow} + d\sigma^{-\rightarrow})$
- Subtract Bethe-Heitler (BH)

$$S_{CS,U} \propto d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + e_{\mu} P_{\mu} \text{Im } I$$

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Transverse Nucleon Imaging at $x_{Bj} > 0.03$

- Measure $S_{CS,U} = (d\sigma^{+\leftarrow} + d\sigma^{-\rightarrow})$
- Subtract Bethe-Heitler (BH)
- Integrate over $\phi_{\gamma^* \gamma}$

$$S_{CS,U} \propto d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + e_{\mu} P_{\mu} \text{Im } I$$

$$S_{CS,U} \propto d\sigma_{unpol}^{DVCS} + e_{\mu} P_{\mu} \text{Im } I$$

$$S_{CS,U} \propto c_0^{DVCS}$$

⇒ PURE DVCS CONTRIBUTION

note:

$$d\sigma_{unpol}^{DVCS} \propto c_0^{DVCS} + \cancel{c_1^{DVCS} \cos \phi_{\gamma^* \gamma}} + \cancel{c_2^{DVCS} \cos 2\phi_{\gamma^* \gamma}}$$

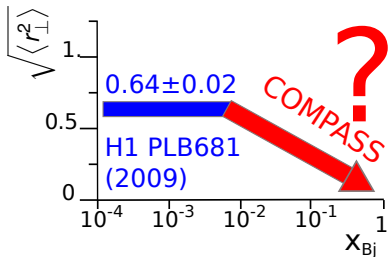
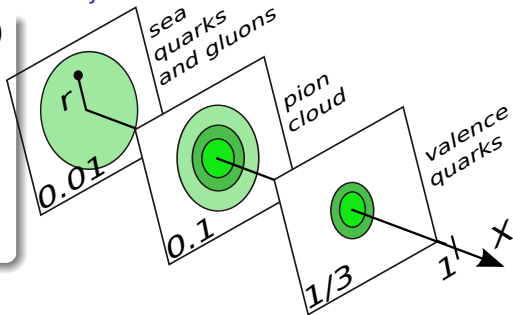
$$\text{Im } I \propto \cancel{s_1' \sin \phi_{\gamma^* \gamma}} + \cancel{s_2' \sin 2\phi_{\gamma^* \gamma}}$$

Transverse Nucleon Imaging at $x_{Bj} > 0.03$

- Measure $S_{CS,U} = (d\sigma^{+\leftarrow} + d\sigma^{-\rightarrow})$
- Subtract Bethe-Heitler (BH)
- Integrate over $\phi_{\gamma^*\gamma}$

$$\frac{d\sigma^{DVCS}}{d|t|} \propto e^{-B|t|}; \quad \langle r_{\perp}^2 \rangle \sim 2B(x_{Bj})$$

at small x_{Bj}

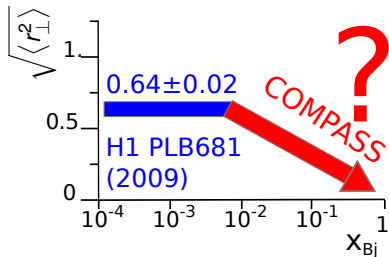
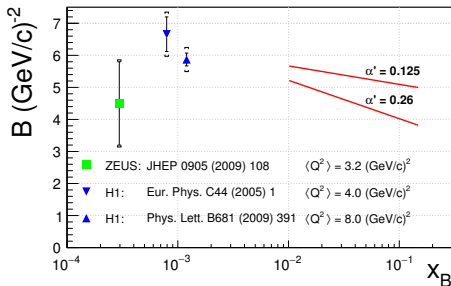
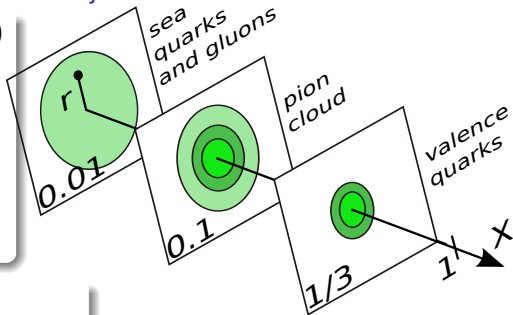


Transverse Nucleon Imaging at $x_{Bj} > 0.03$

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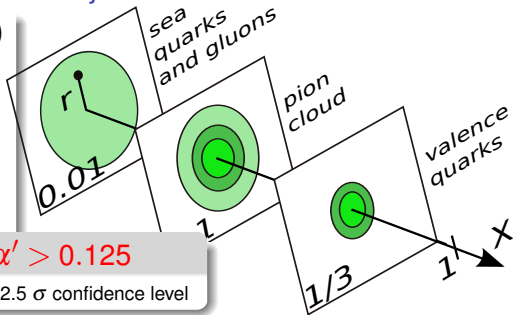


Transverse Nucleon Imaging at $x_{Bj} > 0.03$

- Measure $S_{CS,U} = (d\sigma^{+\leftarrow} + d\sigma^{-\rightarrow})$
- Subtract Bethe-Heitler (BH)
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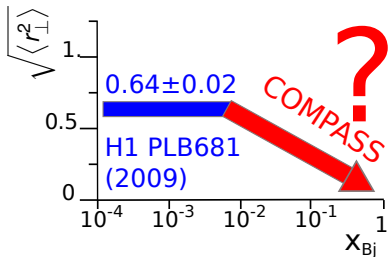
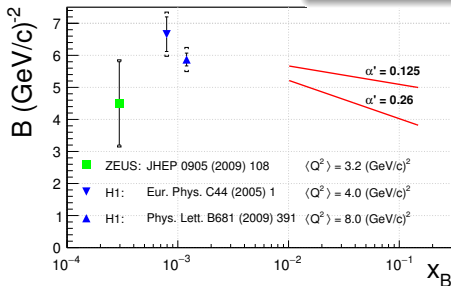
$$\frac{d\sigma^{DVCS}}{d|t|} \propto e^{-B|t|}; \quad \langle r_{\perp}^2 \rangle \sim 2B(x_{Bj})$$

at small x_{Bj}



Measure $\alpha' > 0.125$

with more than 2.5σ confidence level



2012 Pilot Run - 20 days

ECAL2

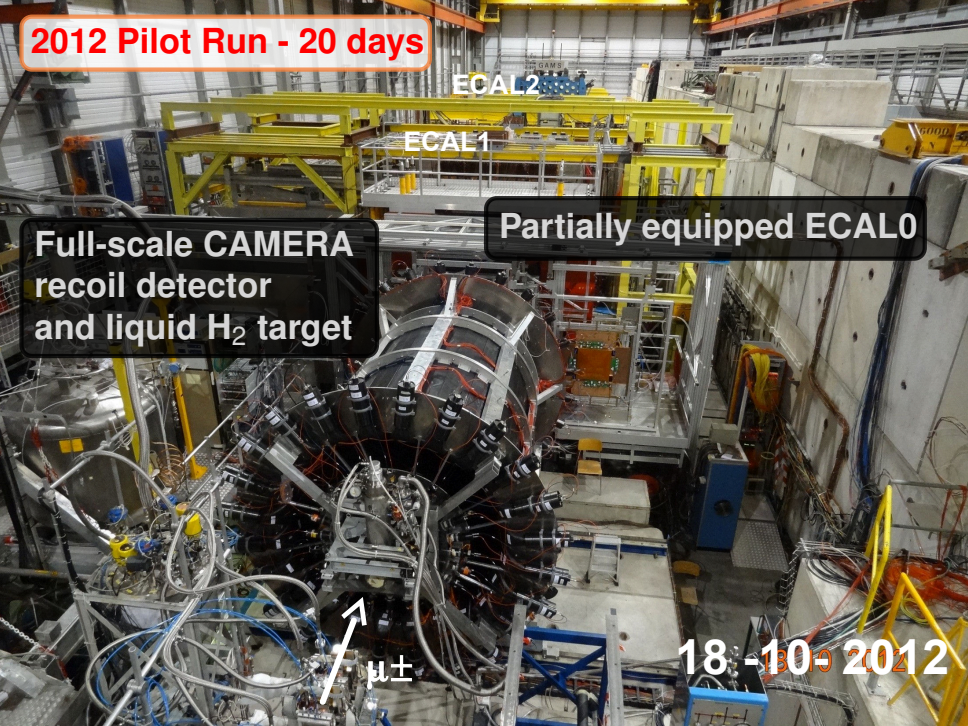
ECAL1

**Full-scale CAMERA
recoil detector
and liquid H₂ target**

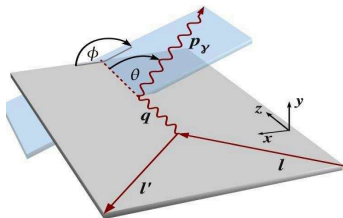
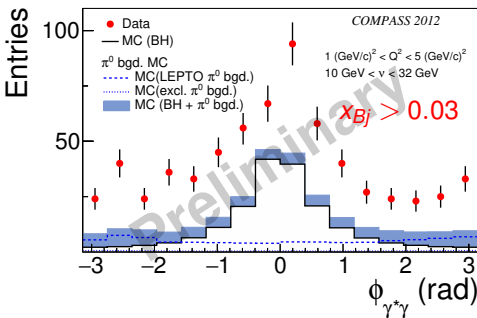
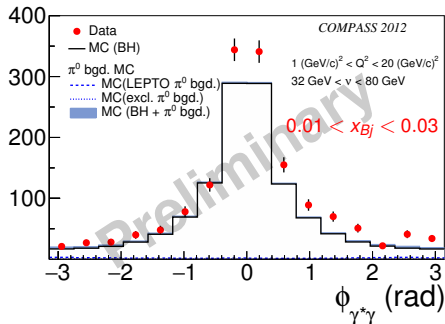
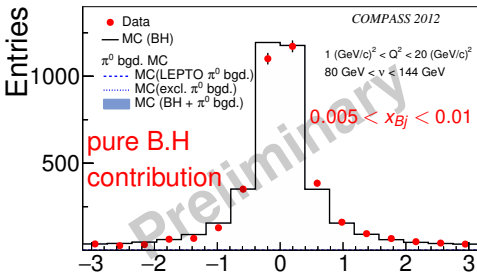
Partially equipped ECAL0

$\mu\pm$

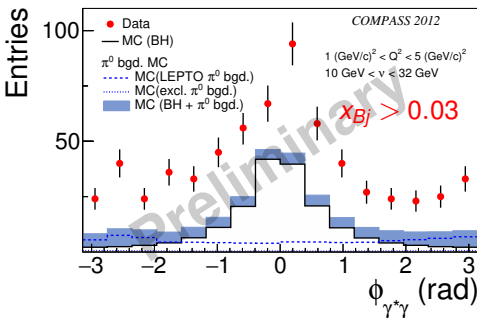
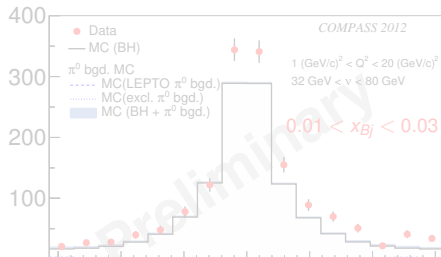
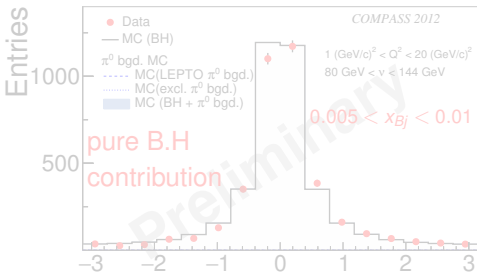
18-10-2012



Exclusive γ Azimuthal Distributions



Exclusive γ Azimuthal Distributions



- Exclusive γ event selection
- π^0 bgd. estimation
- Kinematic fit
- Acceptance corrections
- Cross-section ($\gamma^*p \rightarrow \gamma p$)



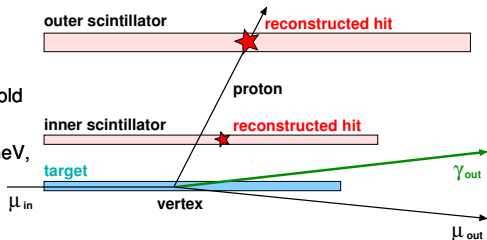
Exclusive Photon Events Selection

Reconstructed interaction vertex in **target volume**

One single photon above DVCS production threshold

$1 \text{ (GeV/c)}^2 < Q^2 < 5 \text{ (GeV/c)}^2$, $10 \text{ GeV} < \nu < 32 \text{ GeV}$,

$0.08 \text{ (GeV/c)}^2 < t < 0.64 \text{ (GeV/c)}^2$



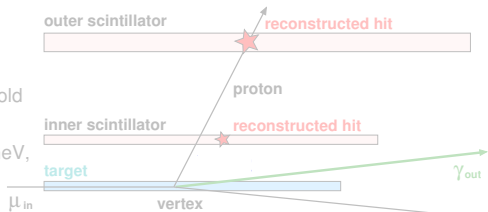
Exclusive Photon Events Selection

Reconstructed interaction vertex in **target volume**

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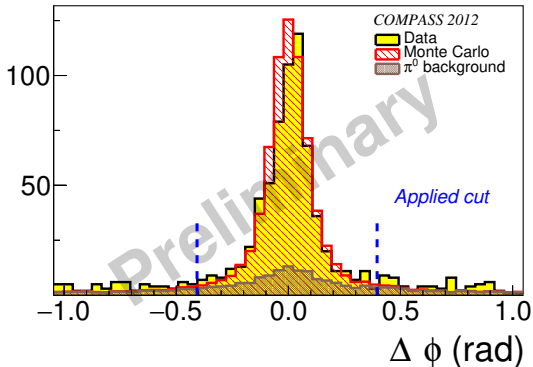
$0.08 \text{ (GeV/c)}^2 < t < 0.64 \text{ (GeV/c)}^2$



Exclusivity conditions:

- $\Delta\phi = \phi_{meas}^{proton} - \phi_{reco}^{proton}$
- Vertex pointing (Δz)
- Transv. momentum balance:
 $\Delta p_{\perp} = p_{\perp,meas}^{proton} - p_{\perp,reco}^{proton}$
- Four-momentum balance:
 $M_X^2 = (p_{\mu_{in}} + p_{p_{in}} - p_{\mu_{out}} - p_{p_{out}} - p_{\gamma})^2$

Entries



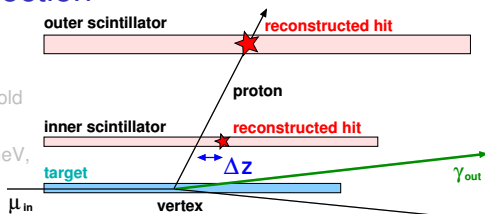
Exclusive Photon Events Selection

Reconstructed interaction vertex in **target volume**

One single photon above DVCS production threshold

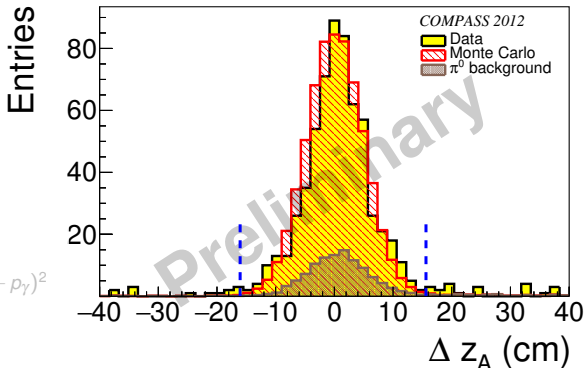
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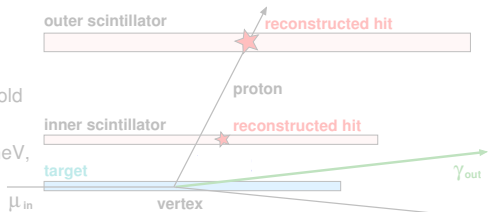
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Exclusivity conditions:

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- Vertex pointing (Δz)

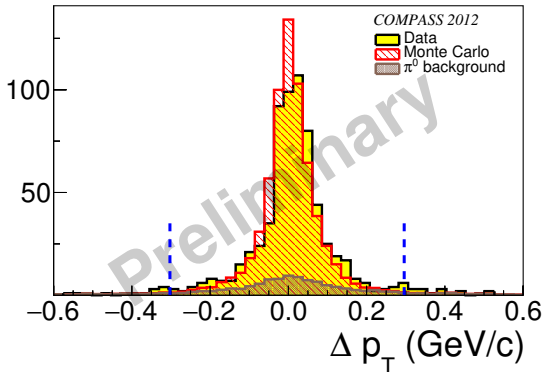
- Transv. momentum balance:

$$\Delta p_{\perp} = p_{\perp,meas}^{proton} - p_{\perp,reco}^{proton}$$

- Four-momentum balance:

$$M_X^2 = (p_{\mu_{in}} + p_{p_{in}} - p_{\mu_{out}} - p_{p_{out}} - p_{\gamma})^2$$

Entries



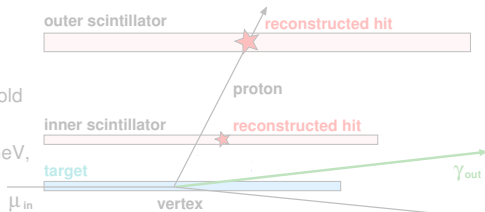
Exclusive Photon Events Selection

Reconstructed interaction vertex in **target volume**

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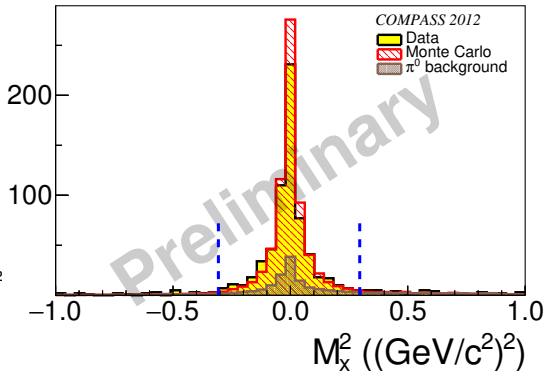
Exclusivity conditions:

- $\Delta\varphi = \varphi_{meas}^{proton} - \varphi_{reco}^{proton}$
- Vertex pointing (Δz)
- Transv. momentum balance:
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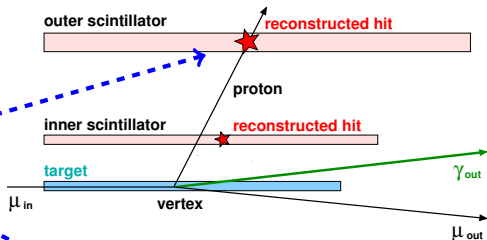
Entries



Exclusive Photon Events Selection

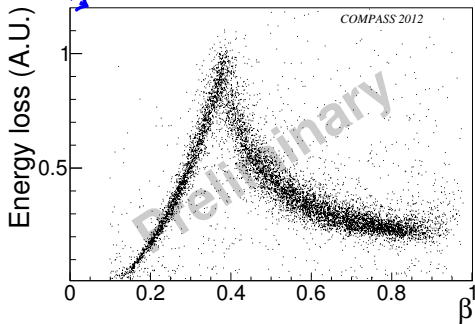
Signal amplitude in outer scintillators vs. β of recoiling particle

Proton signature clearly visible after all exclusivity conditions



Exclusivity conditions:

- $\Delta\phi = \phi_{meas}^{proton} - \phi_{reco}^{proton}$
- Vertex pointing (Δz)
- Transv. momentum balance:
 $\Delta p_{\perp} = p_{\perp,meas}^{proton} - p_{\perp,reco}^{proton}$
- Four-momentum balance:
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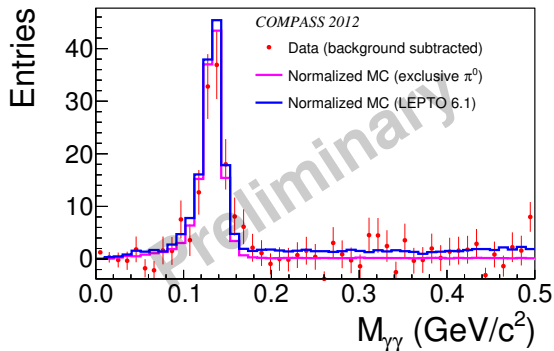


π^0 Background Estimation

Major background source for exclusive photon events

Two cases:

- **Visible** (both γ detected, easy to reject)
- **Invisible** (one γ “lost”, estimated with MC)



$M_{\gamma\gamma}$ distribution
("Visible" π^0)

„Exclusive“ γ ($E_\gamma > 4, 5, 10$ GeV / Ecal0,1,2)
+ one γ below energy threshold

Semi inclusive LEPTO MC

or

exclusive

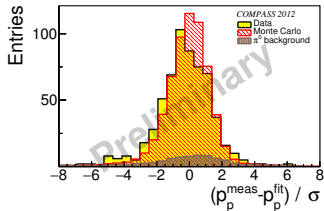
HEPGen++ MC
(Golosgokov & Kroll model)

π^0 contribution normalized to
 $M_{\gamma\gamma}$ peak from real data

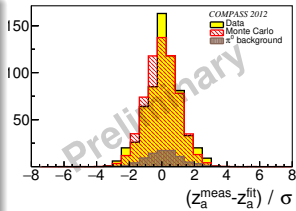
Kinematically constrained fit

- constrained χ^2 minimisation with NDF=9
- full 4-momentum conservation of the reaction $\mu p \rightarrow \mu p \gamma$
- vertex constraints for μ, μ' and p' included in the fit

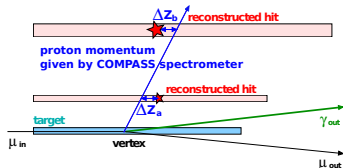
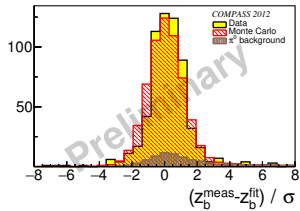
⇒ most accurate determination of t



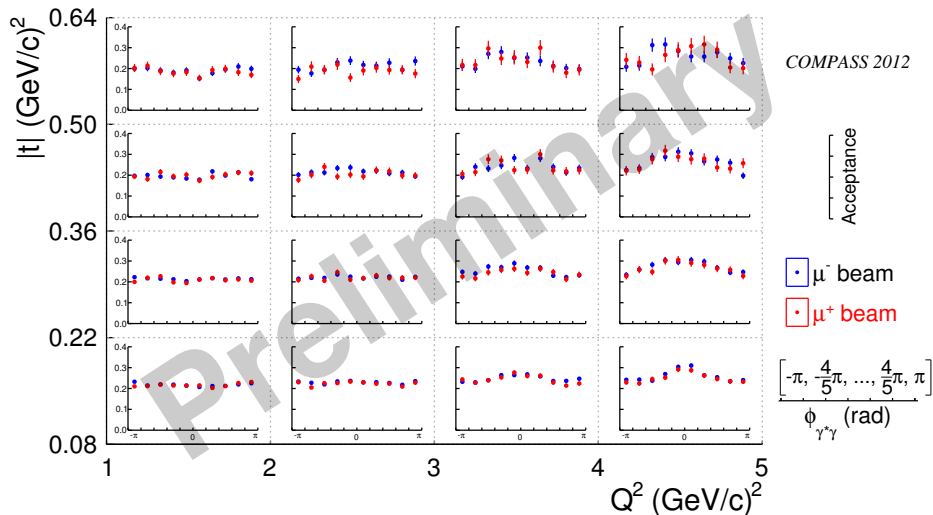
recoil proton
momentum



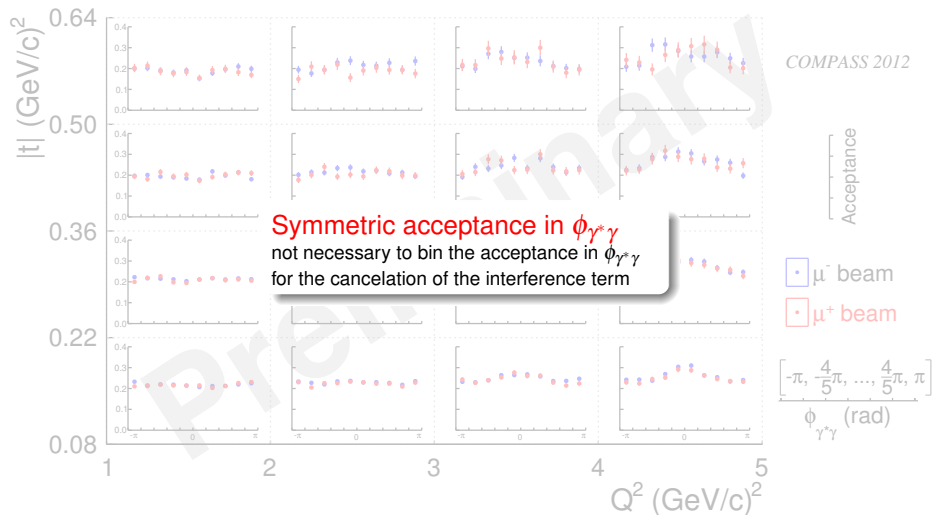
recoil proton
direction



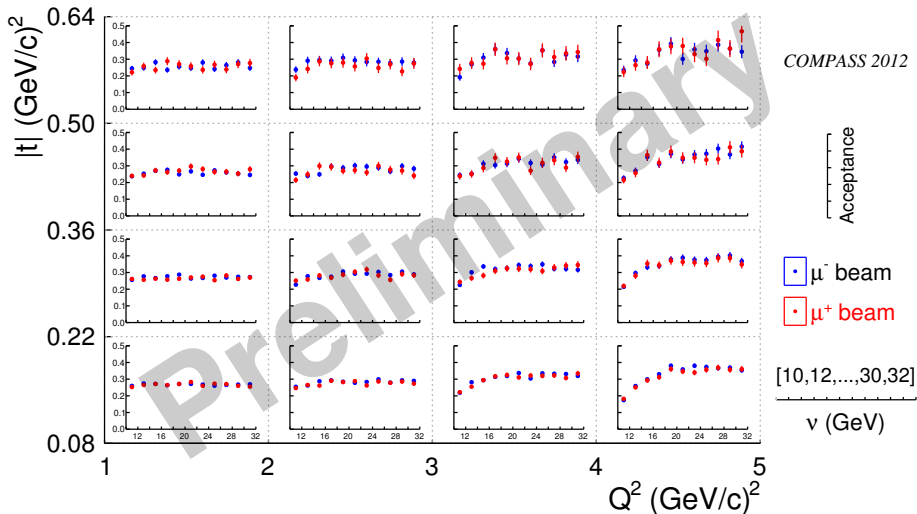
COMPASS acceptance for DVCS



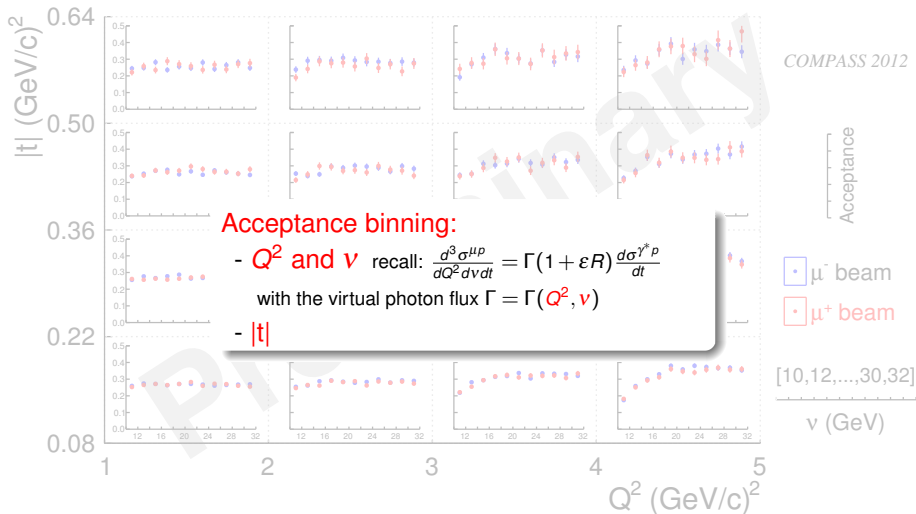
COMPASS acceptance for DVCS



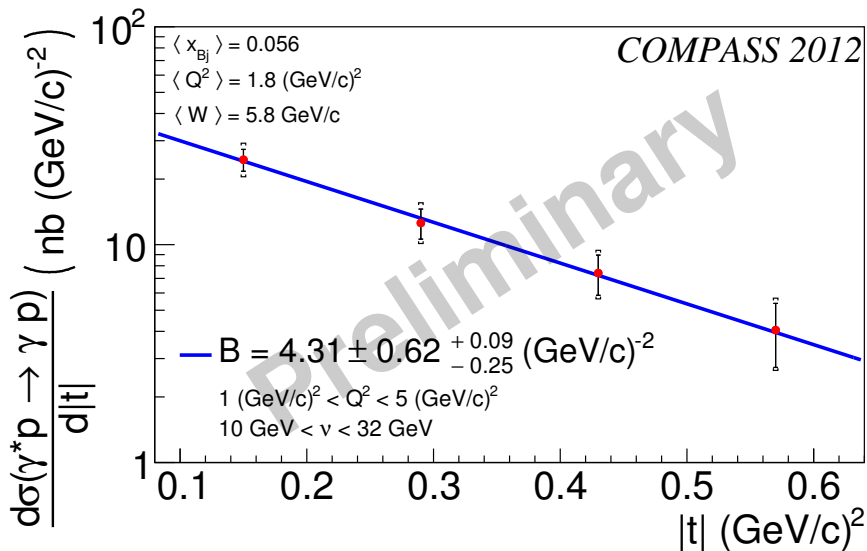
COMPASS acceptance for DVCS



COMPASS acceptance for DVCS

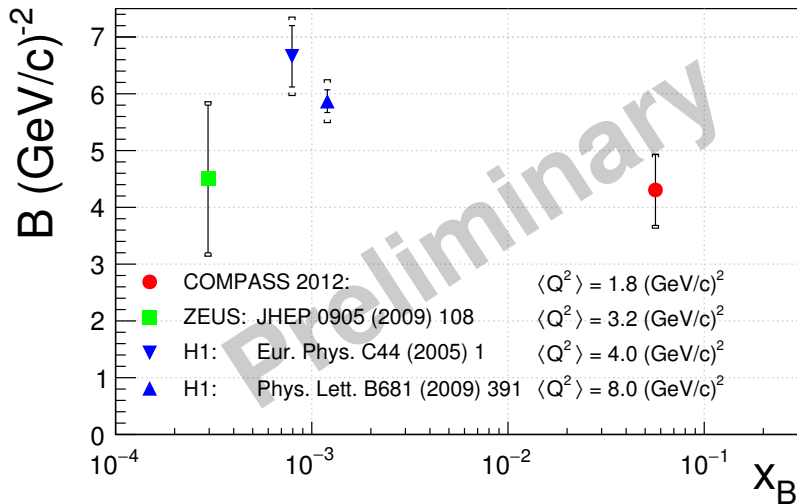


DVCS x-section and t-slope extraction

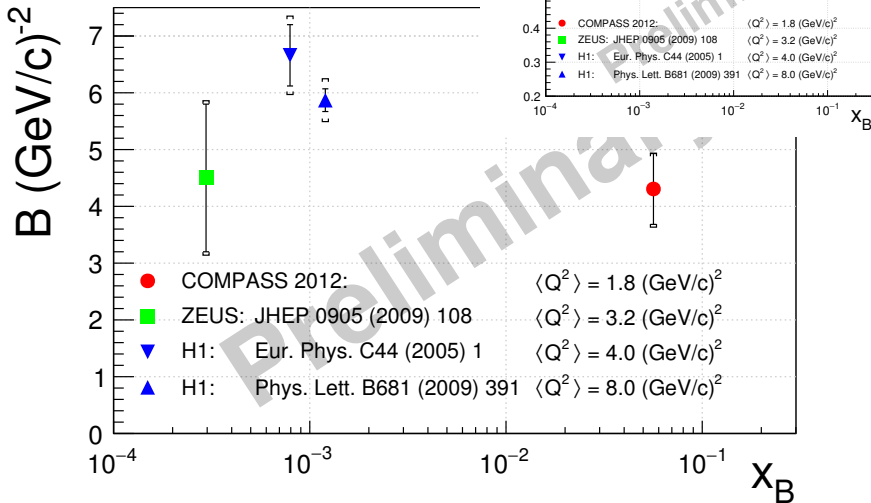


Comparison with HERA results

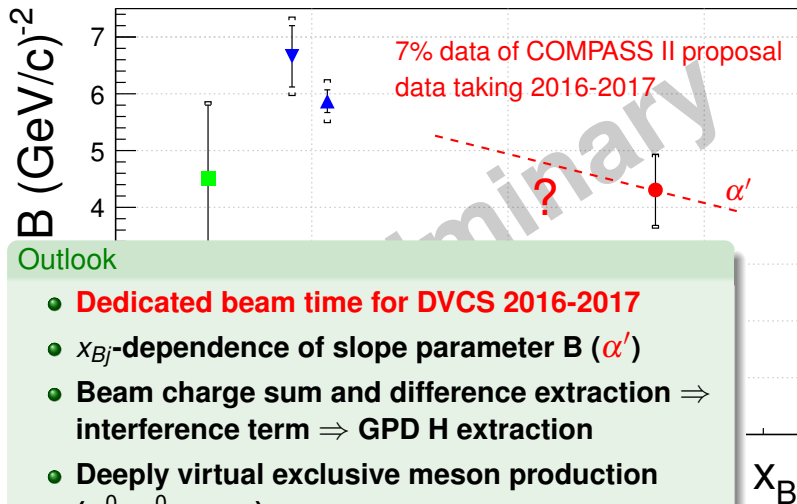
Model independent result



Comparison with HERA results



Comparison with HERA results



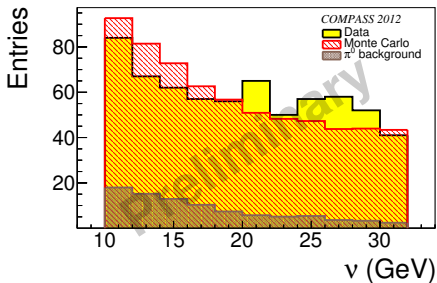
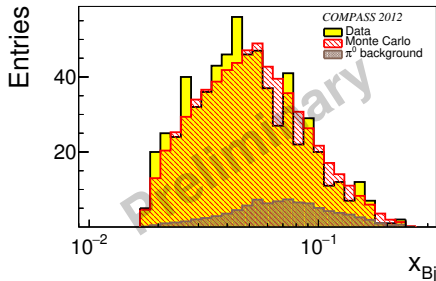
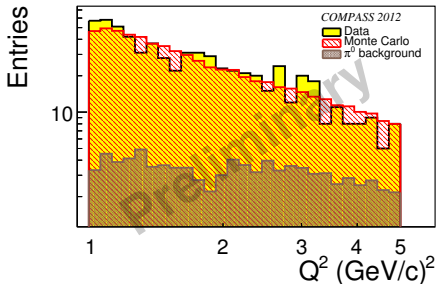
Outlook

- **Dedicated beam time for DVCS 2016-2017**
- x_{Bj} -dependence of slope parameter B (α')
- **Beam charge sum and difference extraction** \Rightarrow interference term \Rightarrow **GPD H extraction**
- **Deeply virtual exclusive meson production** ($\pi^0, \rho^0, \omega, \dots$)

Thank you for your attention

Thank you for your attention

Kinematic distributions



Q^2 and ν (resp. x_{Bj}) after kinematic fit!

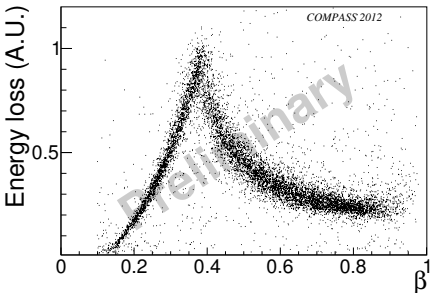
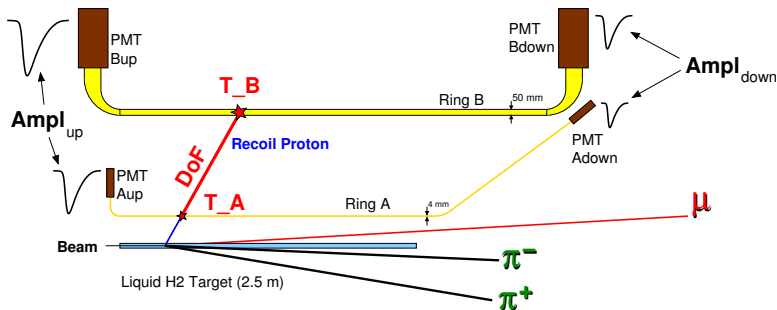
Monte Carlo prediction (the sum is shown)

-(DVCS/BH): based on phenomenological model of DVCS x-section*

$-\pi^0$: parametrisation* linked to Golosgov & Kroll + LEPTO (shown separately)

*HEPGen++: Andrzej Sandacz, Christopher Regali

Recoil particle Measurement in CAMERA



$$E_{loss} \sim \sqrt{Ampl_{up} * Ampl_{down}}$$

$$TOF \rightarrow (t_{up} + t_{down})_{A,B}$$

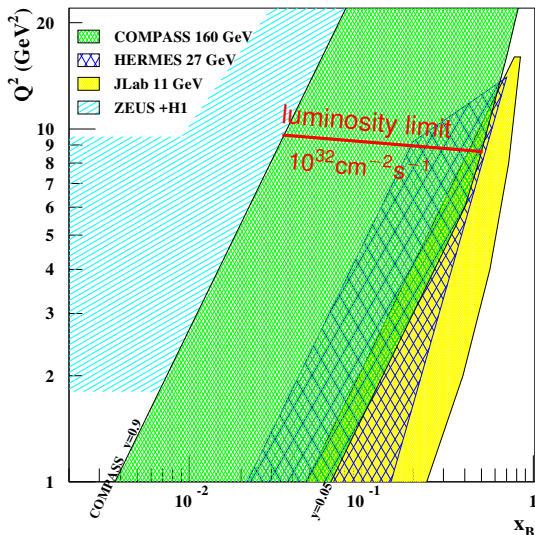
$$z \rightarrow t_{up} - t_{down}$$

Count rates: > 5 MHz in ring A

~1 MHz in ring B

What Makes COMPASS Unique?

COMPASS covers the unexplored region between collider (H1+Zeus) and low-energy fixed target (Hermes+JLab) experiments

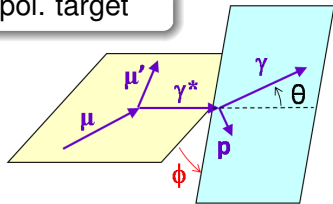
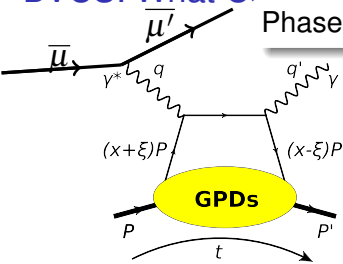


- μ^+ and μ^- beams
- momentum: 100 – 190 GeV/c
- beam polarization: 80 %
opposite for μ^+ and μ^-
- coverage of intermediate x_B
 - low x_B : **pure BH**
useful for normalization
 - high x_B : **DVCS predominant**

~> **unexplored region between
ZEUS+H1 and HERMES+JLab**

DVCS: What Can We Learn?

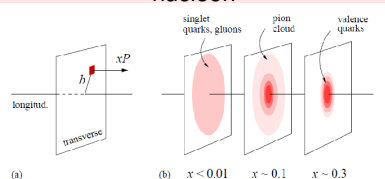
Phase 1: Polarized beam, unpol. target



DVCS dominance at large x_B

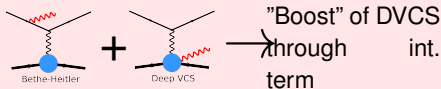
BH/DVCS interf. at intermediate x_B

x_B -dependent transv. size of nucleon



r_{\perp} parameter from slope of $d\sigma^{DVCS}/dt$

Interference between BH and DVCS

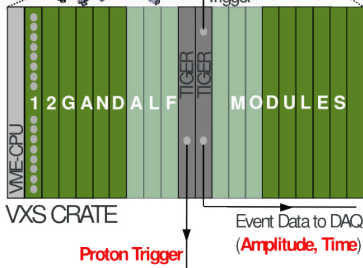
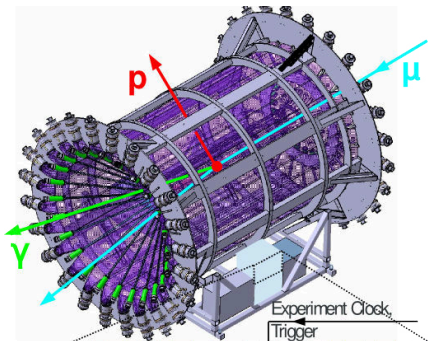


Measurement of $Re\mathcal{H}(\xi, t)$ and $Im\mathcal{H}(\xi, t)$ via ϕ -modulation of cross section

- $Re\mathcal{H}(\xi, t) = P \int dx H(x, \xi, t)/(x - \xi)$
- $Im\mathcal{H}(\xi, t) = H(x = \xi, \xi, t)$

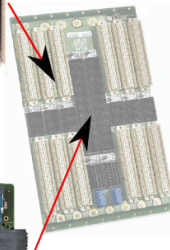
Exp. constrain to GPD H

CAMERA Readout



GANDALF

Virtex-5 VSX95
8 channels
1 GS/s
12 bit resolution

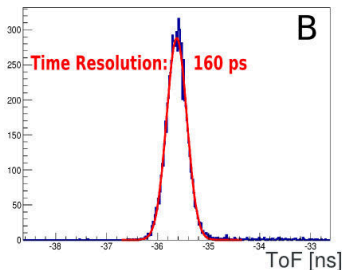
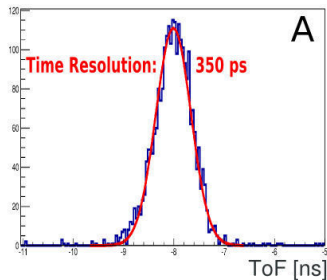


TIGER

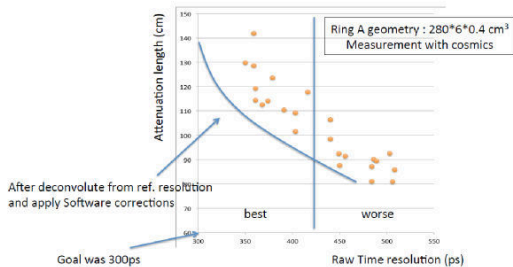
Virtex-6 VLX365
onBoard GPU
2x SFP+
COM Express



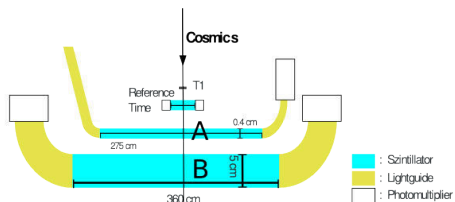
Time Resolutions Measured with Cosmics



Ring A - performances

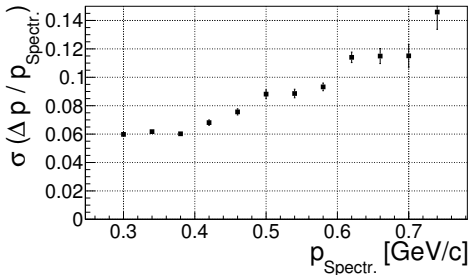


At length better than 200 cm was expected

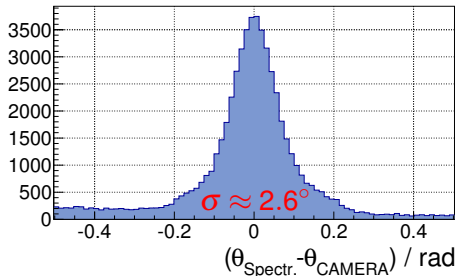


Summary of Present CAMERA Performances

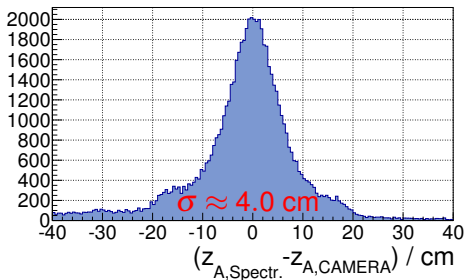
momentum resolution



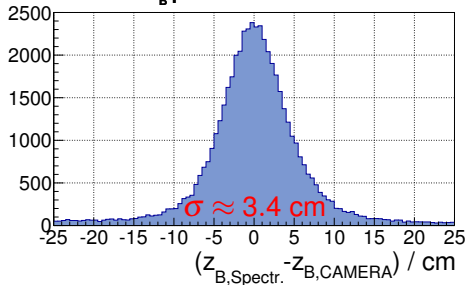
polar angle resolution



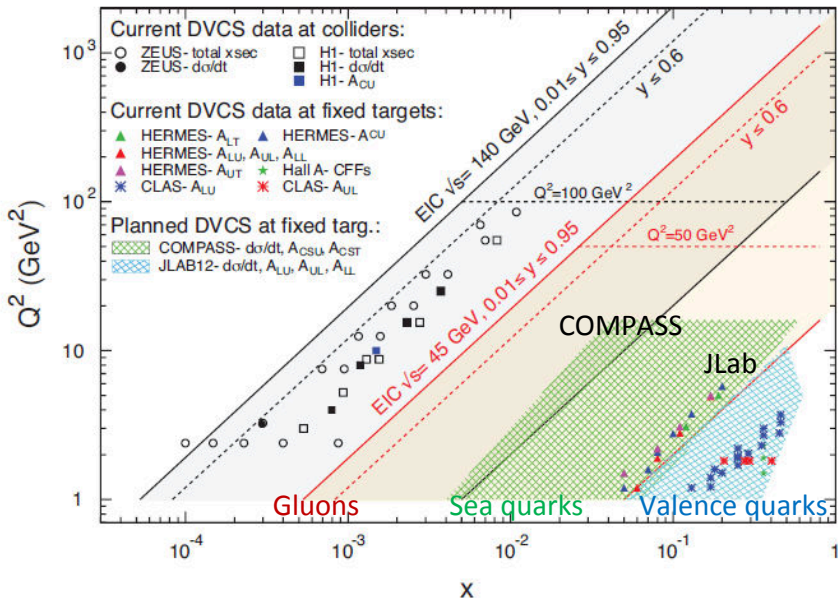
z_A position resolution



z_B position resolution



Past, Present and Future GPD Experiments



Measurements of DVCS and BH Cross-sections

cross-sections on proton for $\mu^{+\downarrow}$, $\mu^{-\uparrow}$ beam with opposite charge & spin (\mathbf{e}_μ & \mathbf{P}_μ)

$$d\sigma_{(\mu p \rightarrow \mu p \gamma)} = d\sigma^{\text{BH}} + d\sigma^{\text{DVCS}}_{\text{unpol}} + \mathbf{P}_\mu d\sigma^{\text{DVCS}}_{\text{pol}} \\ + \mathbf{e}_\mu a^{\text{BH}} \Re \mathbf{A}^{\text{DVCS}} + \mathbf{e}_\mu \mathbf{P}_\mu a^{\text{BH}} \text{Im} \mathbf{A}^{\text{DVCS}}$$

Charge & Spin Difference and Sum:

$$\mathcal{D}_{CS,U} \equiv d\sigma(\mu^{+\downarrow}) - d\sigma(\mu^{-\uparrow}) \propto c_0^{\text{Int}} + c_1^{\text{Int}} \cos \phi \quad \text{and} \quad c_{0,1}^{\text{Int}} \sim F_1 \Re \mathcal{H} \\ \mathcal{S}_{CS,U} \equiv d\sigma(\mu^{+\downarrow}) + d\sigma(\mu^{-\uparrow}) \propto d\sigma^{\text{BH}} + c_0^{\text{DVCS}} + K \cdot s_1^{\text{Int}} \sin \phi \quad \text{and} \quad s_1^{\text{Int}} \sim F_1 \text{Im} \mathcal{H}$$

$$c_1^{\text{Int}} \propto \Re (F_1 \mathcal{H} + \xi (F_1 + F_2) \tilde{\mathcal{H}} - t/4m^2 F_2 \mathcal{E})$$

NOTE: ✓ dominance of \mathcal{H} with a proton target
at COMPASS kinematics
✓ only leading twist and LO