

Exclusive Reactions at High Momentum Transfer An Experimental Point of View

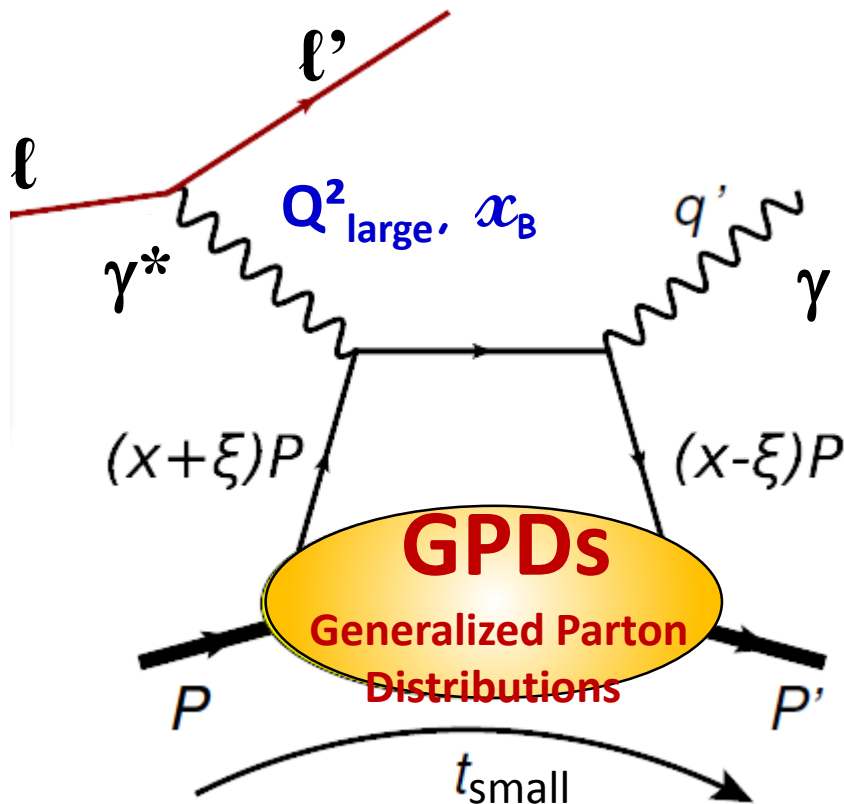
Nicole d'Hose – CERN & CEA Saclay



Photonuclear Reactions
Gordon Research Conference

Holderness, 10 August 2016

Deeply virtual Compton scattering (DVCS)



D. Mueller *et al*, Fortsch. Phys. 42 (1994)

X.D. Ji, PRL 78 (1997), PRD 55 (1997)

A. V. Radyushkin, PLB 385 (1996), PRD 56 (1997)

DVCS: $\ell p \rightarrow \ell' p' \gamma$

the golden channel

because it interferes with
the Bethe-Heitler process

also meson production

$\ell p \rightarrow \ell' p' \pi, \rho$ or ϕ or $J/\psi \dots$

The GPDs depend on the following variables:

x : average long. momentum

ξ : long. mom. difference $\simeq x_B / (2 - x_B)$

t : four-momentum transfer
related to b_\perp via Fourier transform

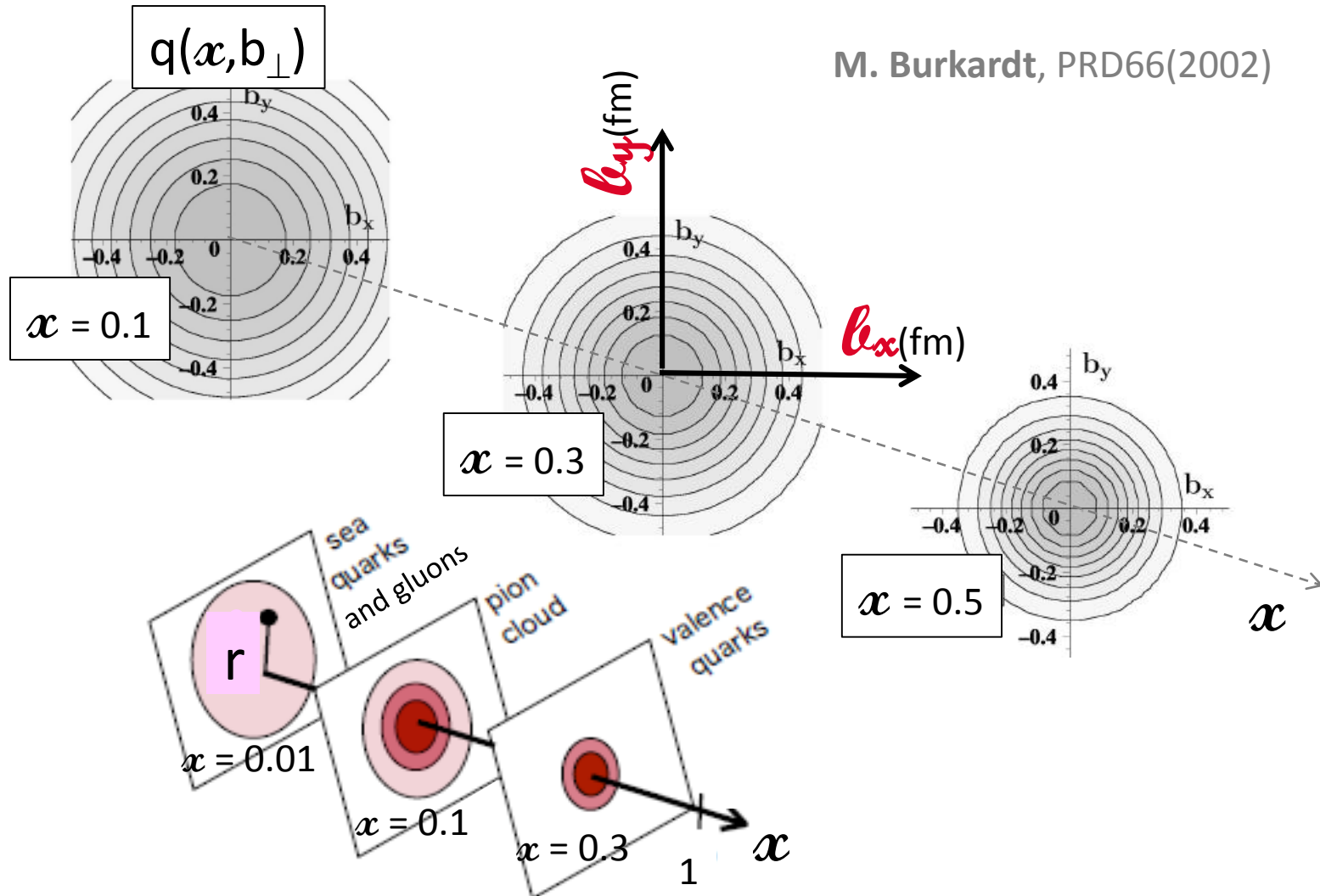
The variables measured in the experiment:

$E_\ell, Q^2, x_B \sim 2\xi / (1 + \xi),$
 t (or $\theta_{\gamma^* \gamma}$) and ϕ

3D imaging: mapping in the transverse plane

Proton
moving
towards us

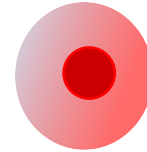
M. Burkardt, PRD66(2002)



Correlation between the spatial distribution of partons
and the longitudinal momentum fraction

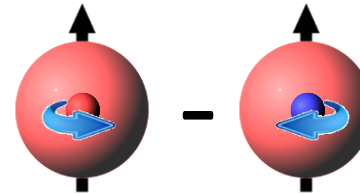
The 2 most famous GPDs

$$H(x, \xi, t) \xrightarrow{t \rightarrow 0} q(x) \text{ or } f_1(x)$$



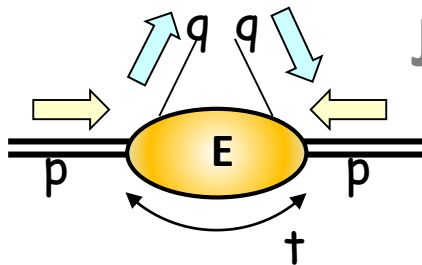
"Elusive"

$$E(x, \xi, t) \longleftrightarrow f_{1T}^\perp(x, k_T)$$



Sivers: quark k_T & nucleon transv. Spin

$$2J^q = \lim_{t \rightarrow 0} \int x (H^q(x, \xi, t) + E^q(x, \xi, t)) dx$$



Ji sum rule: PRL78 (1997) cited 1404 times

Relation to OAM

$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + \mathcal{L}$$

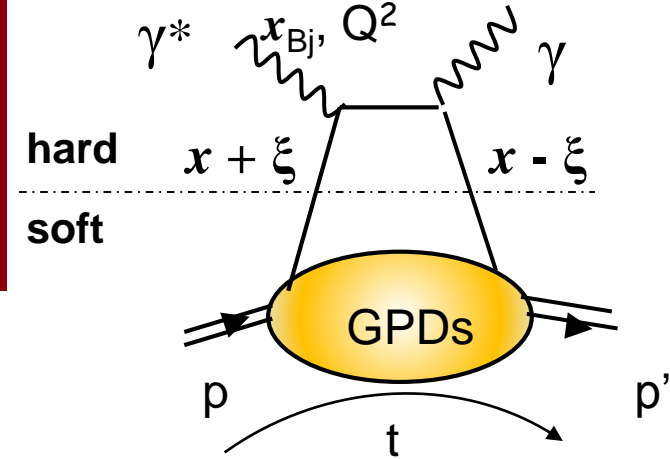
Jaffe and Manohar
NPB337 (1990)

$\frac{1}{2} \Delta\Sigma \sim 0.15$ well know from DIS/SIDIS

$\Delta G \sim 0.2$ known from SIDIS/pp

\mathcal{L} unknown

Compton Form Factors are measured in DVCS

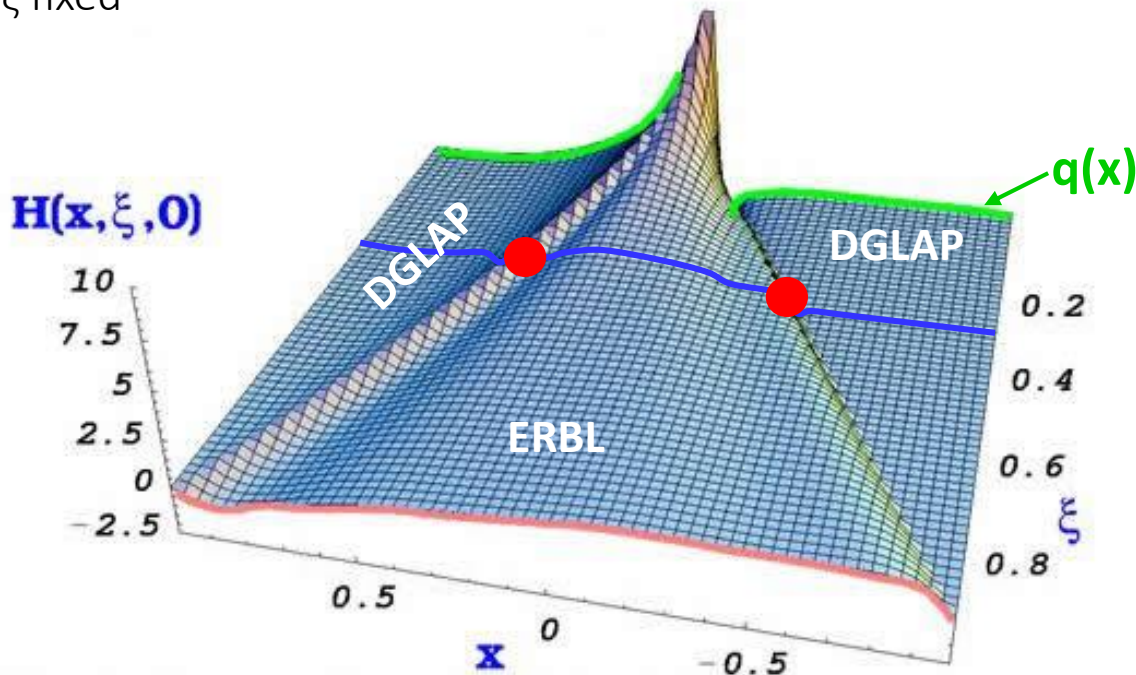


The amplitude DVCS at LT & LO in α_s :

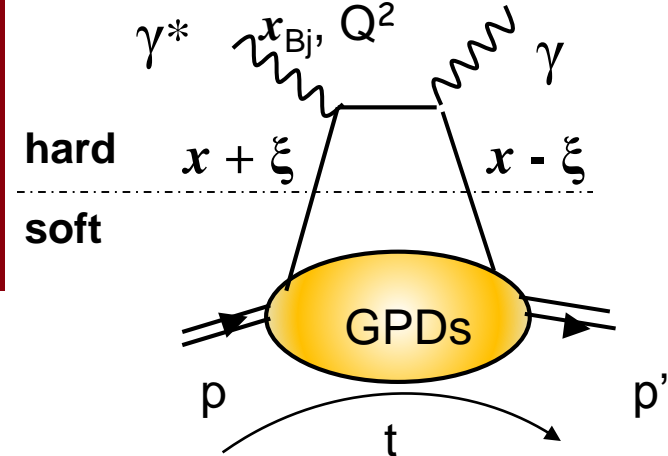
$$\mathcal{H} = \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi + i\epsilon} = \mathcal{P} \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi} - i \pi H(x = \pm \xi, \xi, t)$$

Real part **Imaginary part**

t, ξ fixed



Compton Form Factors are measured in DVCS



The amplitude DVCS at LT & LO in α_s :

$$\mathcal{H} = \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi + i\varepsilon} = \mathcal{P} \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi} - i \pi H(x = \pm \xi, \xi, t)$$

t, ξ fixed

Real part **Imaginary part**

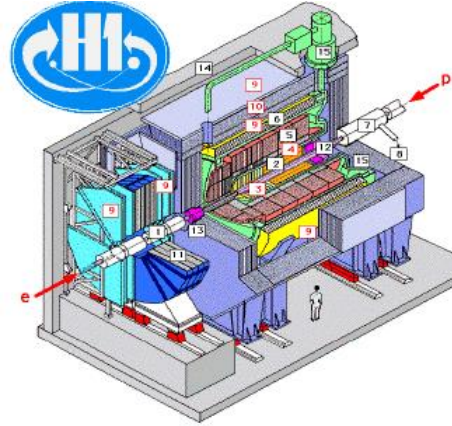
$$\mathcal{Re} \mathcal{H}(\xi, t) = \mathcal{P} \int dx \frac{\mathcal{Im} \mathcal{H}(x, t)}{x - \xi} + \mathcal{D}(t)$$

Im part measured in
Single Spin measurements:
Beam Spin or **Target Spin Asym**

\mathcal{D} term related to the Energy-Momentum Tensor :
Polyakov, PLB 555 (2003) 57-62

Real part measured in
Unpolarized x- sect,
Beam Charge Asymmetry,
or **Double Spin Asymmetries**

The past and future experiments



Collider mode e-p forward fast proton

HERA: H1 and **ZEUS**

Polarised 27 GeV e-/e+

Unpolarized 920 GeV proton

~ Full event reconstruction

Fixed target mode slow recoil proton

HERMES: Polarised 27 GeV e-/e+

Long, Trans polarised p, d target

Missing mass technique

2006-07 with recoil detector



Jlab: Hall A, C, CLAS High lumi, polar. 6 & **12 GeV e-**

Long, (Trans) polarised p, d target

Missing mass technique



COMPASS @ CERN: Polarised **160 GeV μ^+/μ^-**

p target, (Trans) polarised target

with recoil detection



The measurement of t

$$t = (p-p')^2 = (q-q')^2$$

$$|t|_{\min} \sim m_p^2 x_B^2 / (1-x_B) \quad \text{if } x_B/Q \ll 1$$

Fixed target mode slow recoil proton

with forward outgoing photon ($\theta_{\gamma^*\gamma}$ in the Lab)

$$t = (q-q')^2 = -Q^2 - 2 E_\gamma (v - q \cos \theta_{\gamma^*\gamma}) = \frac{-Q^2 - 2 v (v - q \cos \theta_{\gamma^*\gamma})}{1 + 1/m_p (v - q \cos \theta_{\gamma^*\gamma})}$$

with recoiling proton

$$t = (p-p')^2 = 2m_p (m_p - E_p)$$

Better resolution at small t

But $|t|_{\min \text{ exp}}$ to escape target cell to be detected

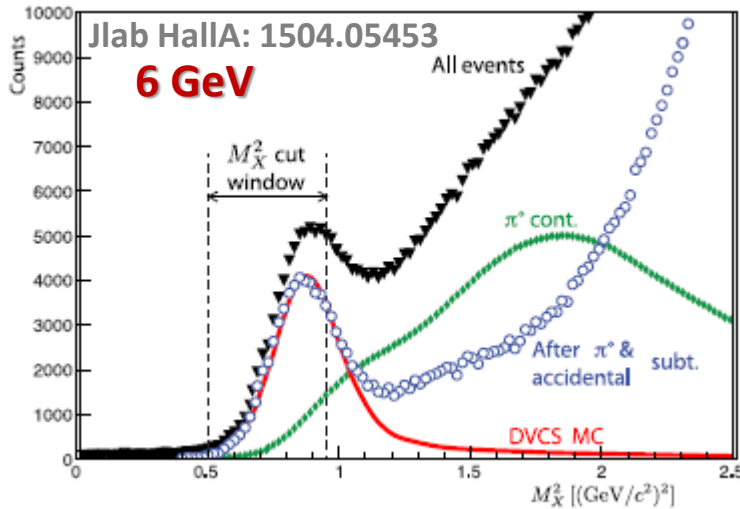
Collider mode e-p forward fast proton

$t = (p-p')^2$ need detection of the fast proton at forward angle close to the beam
with dedicated detectors as « Roman Pot »

Ex: Jlab	$x_B = 0.3$	$ t _{\min} \sim 0.1 \text{ GeV}^2$	$ t _{\min \text{ exp}} \sim 0.1 \text{ GeV}^2$
COMPASS	$x_B = 0.01$	$ t _{\min} \sim 10^{-4} \text{ GeV}^2$	$ t _{\min \text{ exp}} \sim 0.06 \text{ GeV}^2$
EIC	$x_B = 0.0001$	$ t _{\min} \sim 10^{-8} \text{ GeV}^2$	we need to measure very small $ t $

Exclusivity : $\ell p \rightarrow \ell + \gamma + p$

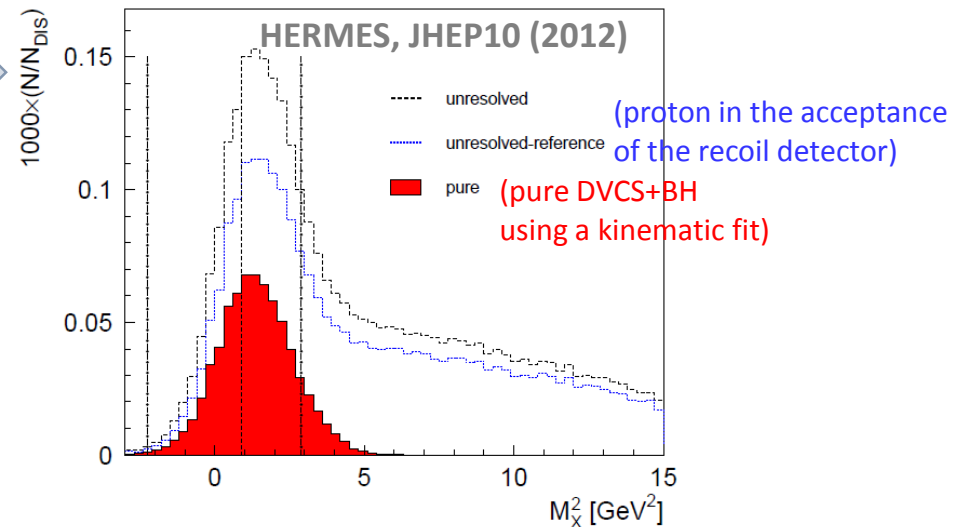
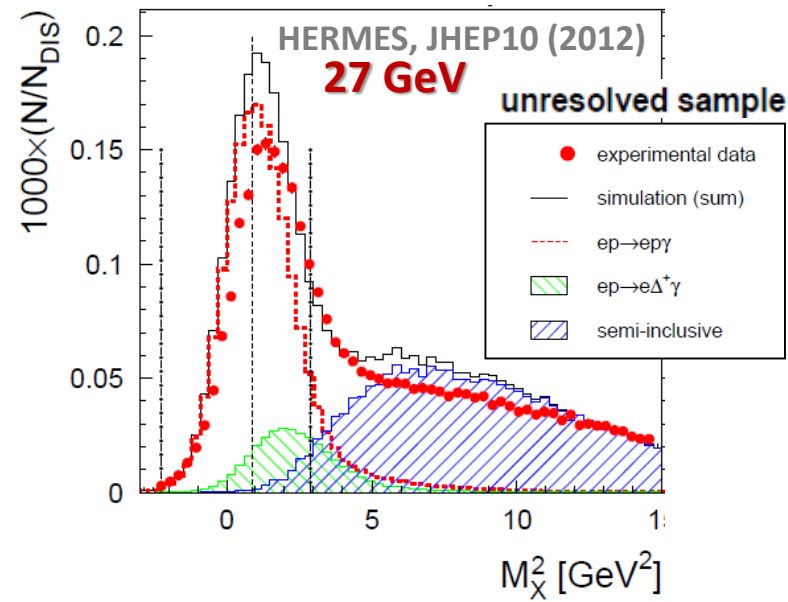
$M_x^2 = (P_\ell + P_p - P_{\ell'} - P_\gamma)^2$ ΔM_x^2 increases with the beam energy !



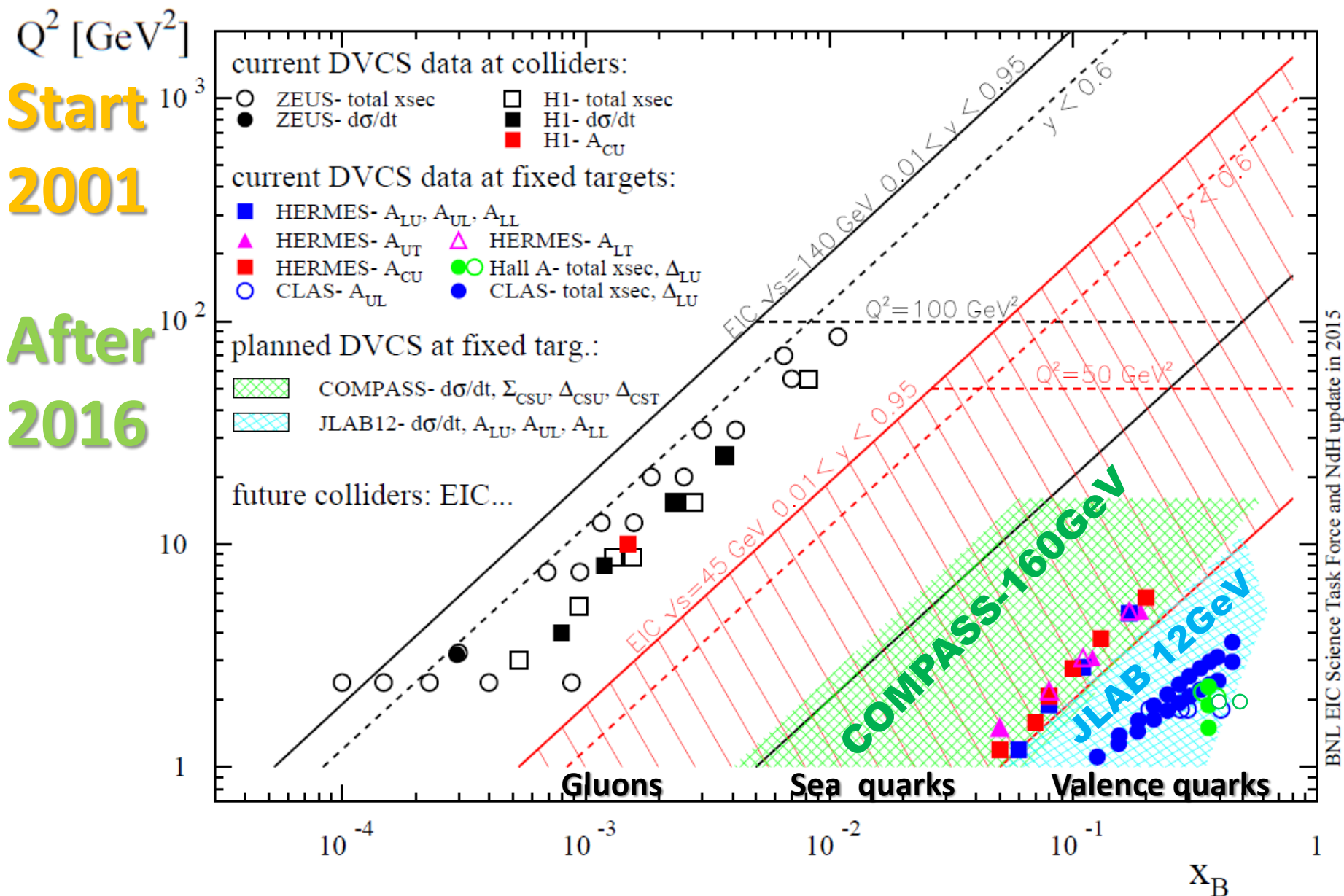
$\ell p \rightarrow \ell' + \gamma (+p')$ for DVCS + BH

Contamination from π^0 decay:

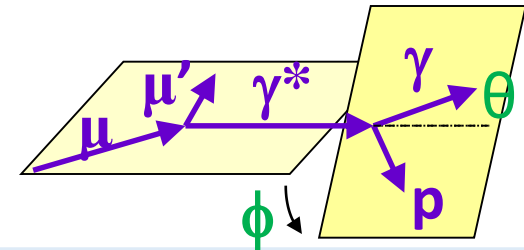
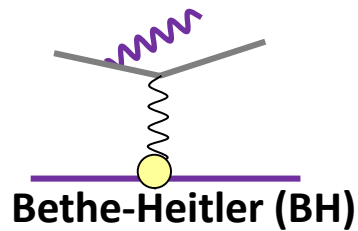
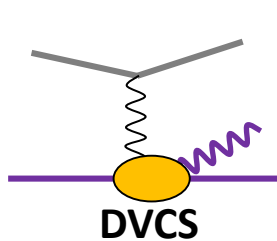
- $\ell p \rightarrow \ell' + \gamma (+\Delta^+)$ associated DVCS + BH
- $\ell p \rightarrow \ell' + \gamma (+\gamma + p')$ exclusive π^0
- $\ell p \rightarrow \ell' + \gamma (+\gamma + p' + \dots)$ SIDIS π^0



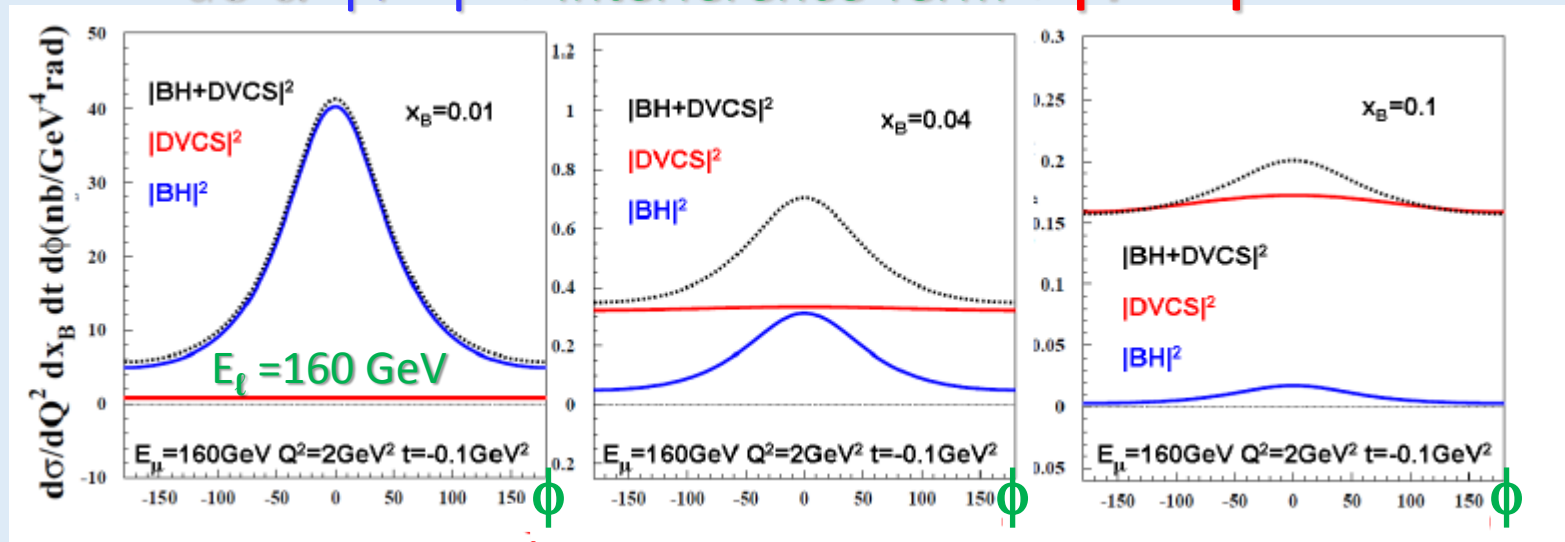
The past and future DVCS experiments



Impact of the beam energy for DVCS



$$d\sigma \propto |T^{BH}|^2 + \text{Interference Term} + |T^{DVCS}|^2$$



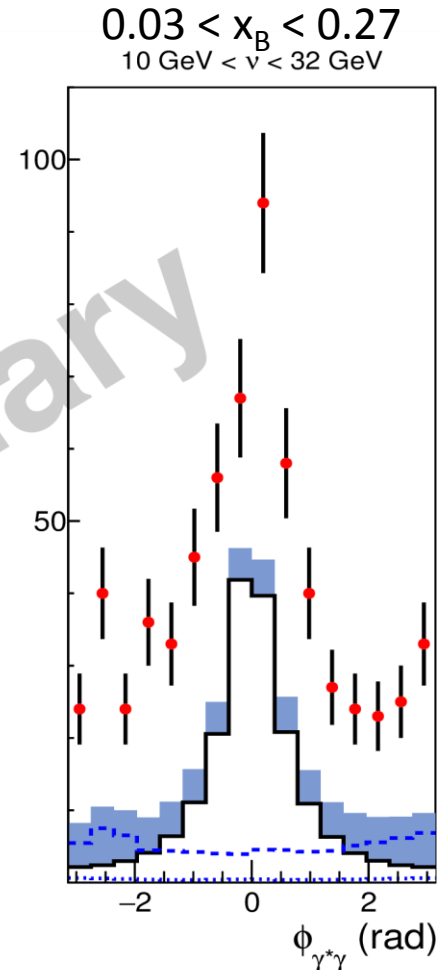
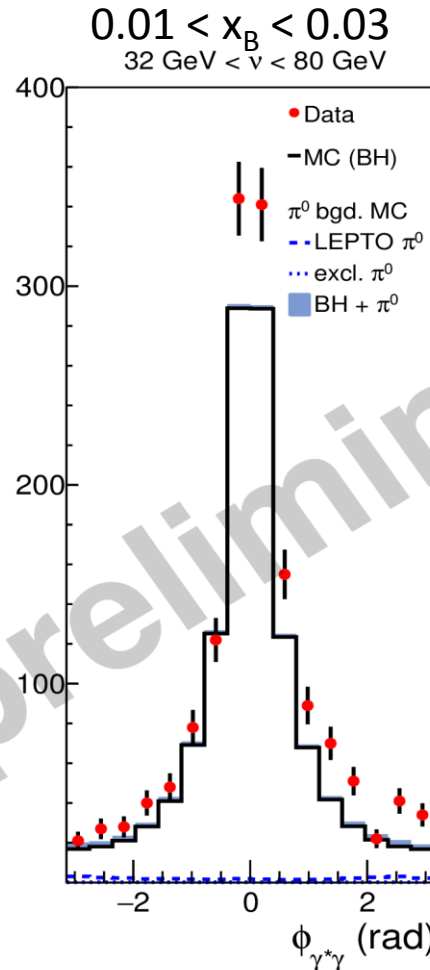
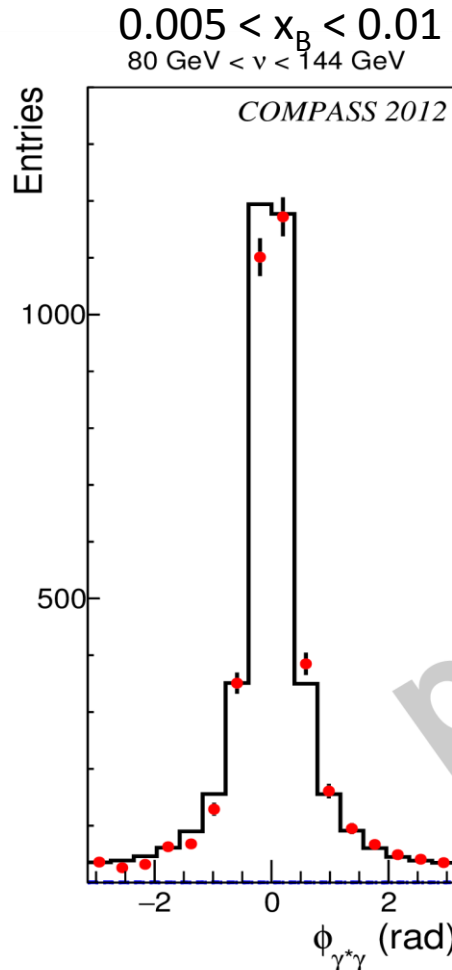
BH dominates
Reference yield

DVCS ampl. via interference
Jlab, HERMES, H1, COMPASS

DVCS dominates - Study of $d\sigma^{DVCS}/dt$
Only for H1, ZEUS, COMPASS

DVCS and BH contributions @ COMPASS

μ^+ and μ^-
160 GeV



Pilot run in 2012

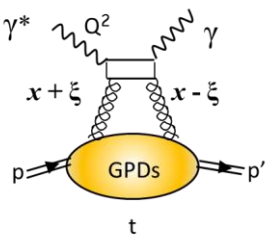
- ✓ Dominant Bethe-Heitler process clearly visible at small x_{Bj}
- ✓ Maximum π^0 background (from exclusive and SIDIS π^0 production) estimated in blue
- ✓ The data at large x_{Bj} show an excess compared to BH+Background (for pure DVCS)

COMPASS is taking DVCS data during 2 years (2016 and 2017)

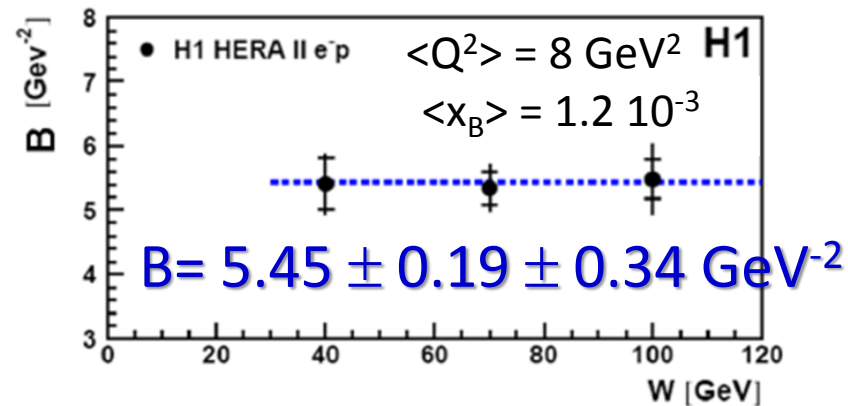
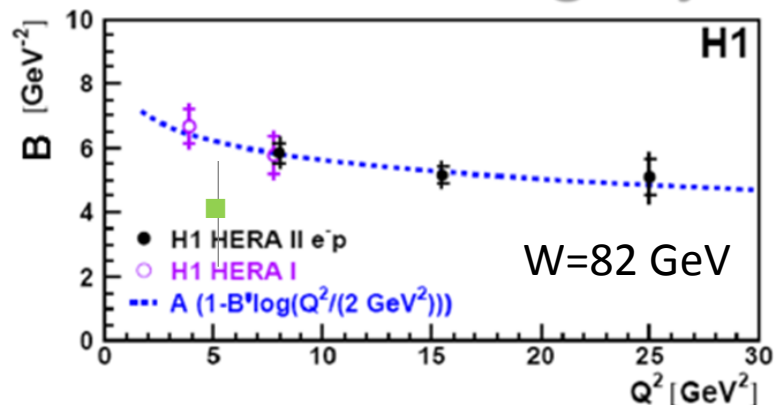
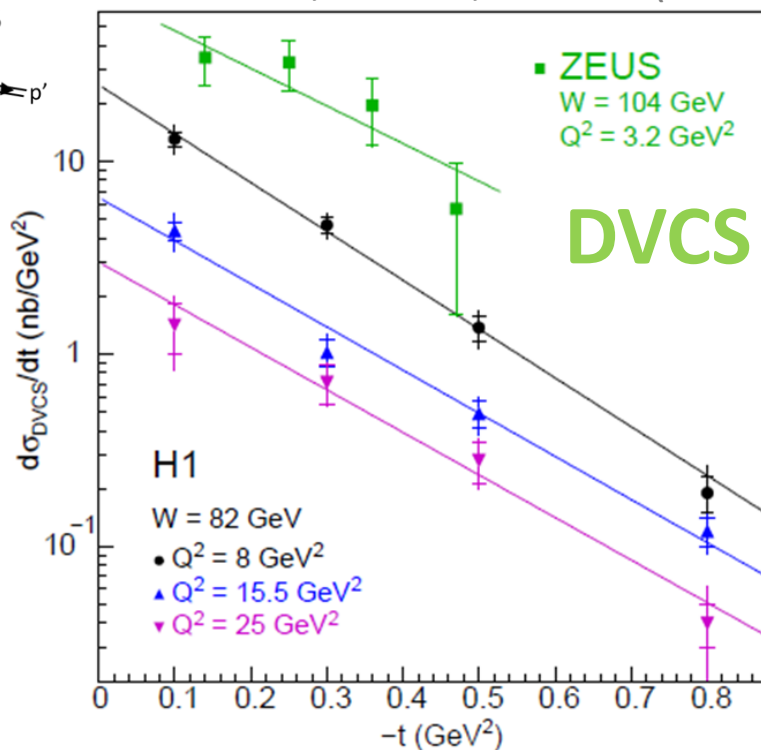
Gluon imaging @ HERA

$$d\sigma^{\text{DVCS}}/dt = e^{-B|t|}$$

B is related to the transversed size of the scattering objects



Aaron et al., H1 Coll, PLB659 (2008)



$$\langle r_{\perp}^2 \rangle \approx 2B$$

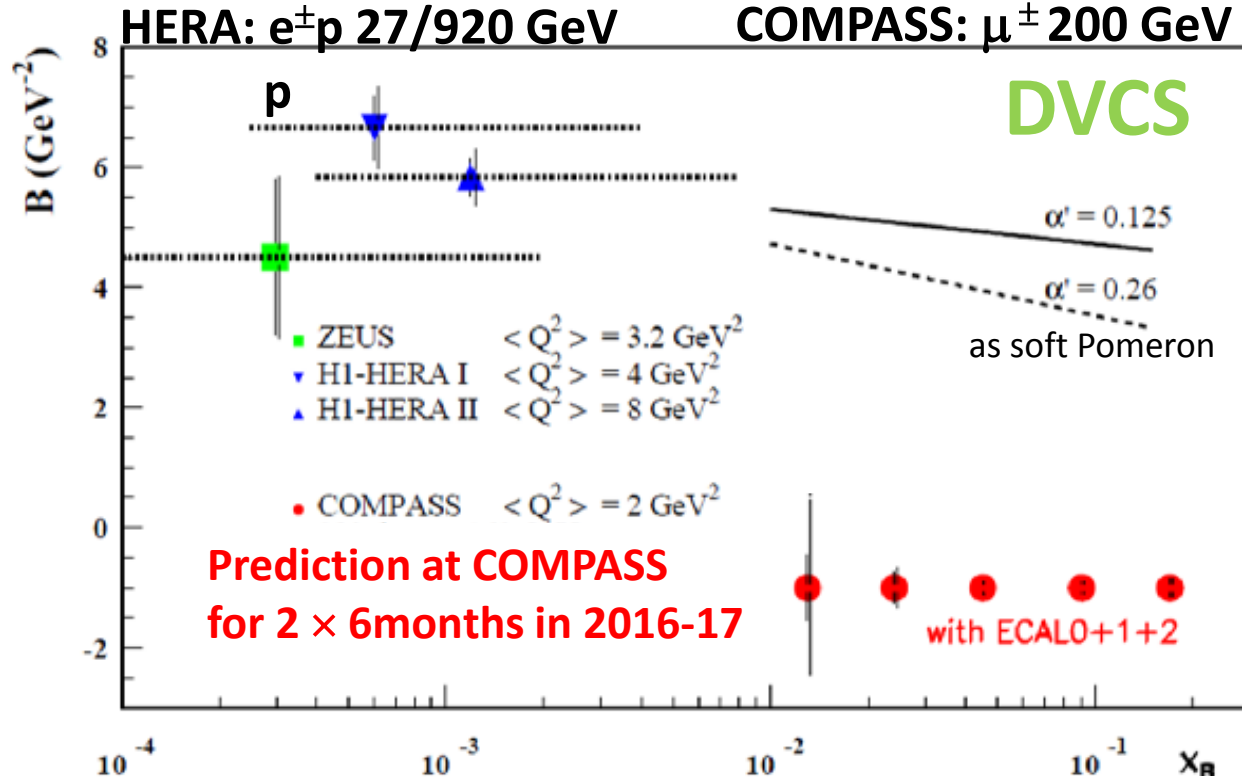
$$\sqrt{\langle r_{\perp}^2 \rangle} = 0.65 \pm 0.02 \text{ fm}$$

to be compared to

$$\sqrt{4 \frac{d}{dt} F_1^p} \Big|_{t=0} = 0.67 \pm 0.01 \text{ fm}$$

$$\sqrt{4 \frac{d}{dt} G_E^p} = 0.72 \pm 0.01 \text{ fm}$$

Sea quark imaging @ COMPASS



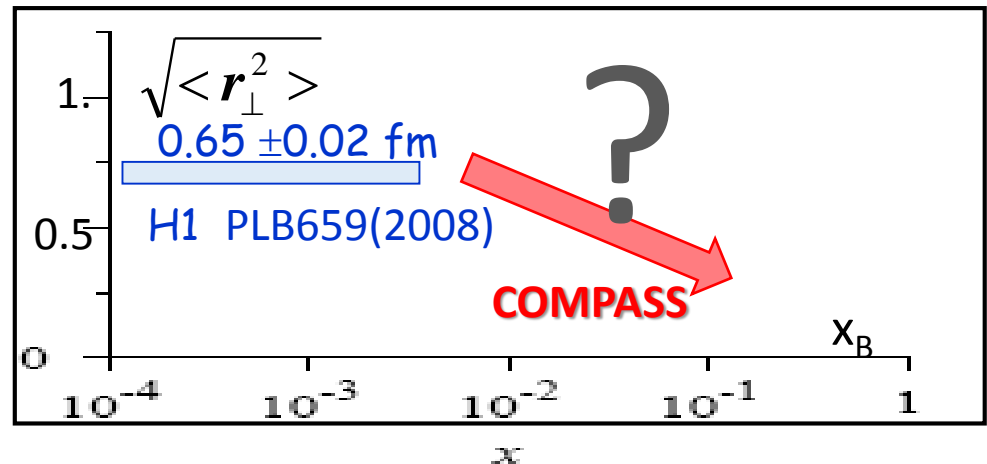
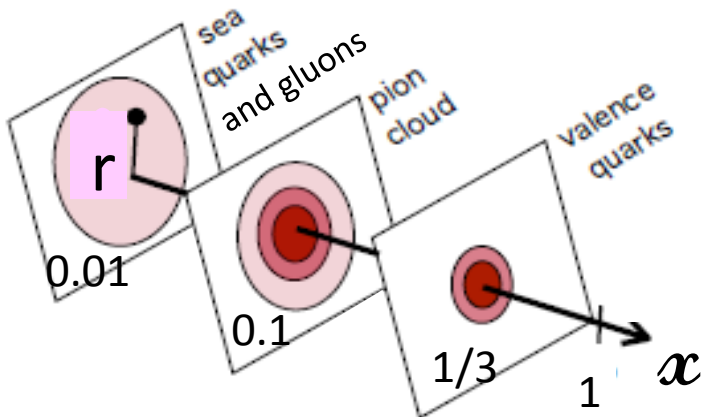
$$d\sigma^{\text{DVCS}}/dt = e^{-B|t|}$$

ansatz inspired by
Regge Phenomenology:

$$B(x_B) = b_0 + 2 \alpha' \ln(x_0/x_B)$$

α' slope of Regge traject

$$\langle r_\perp^2(x_B) \rangle \approx 2B(x_B)$$

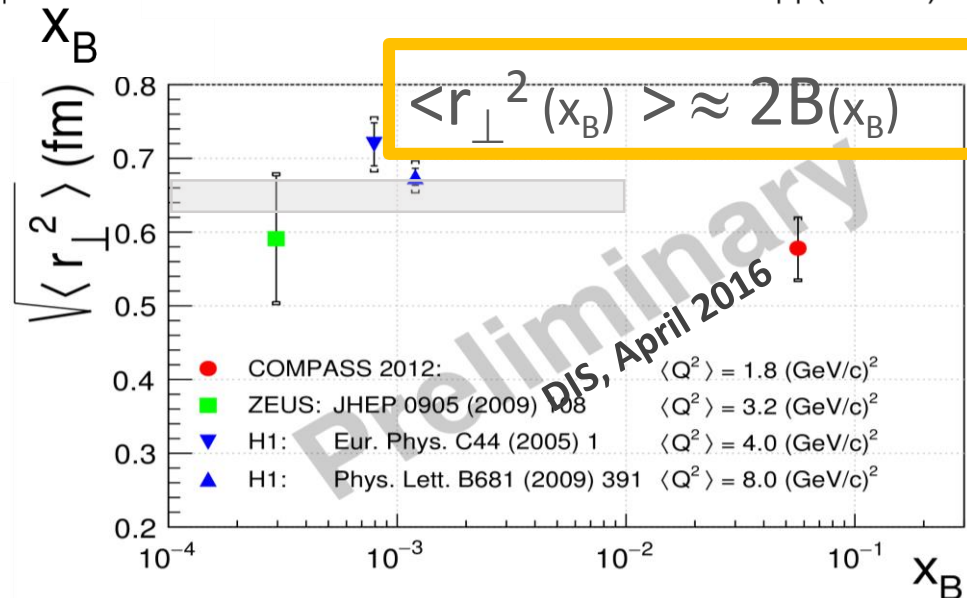
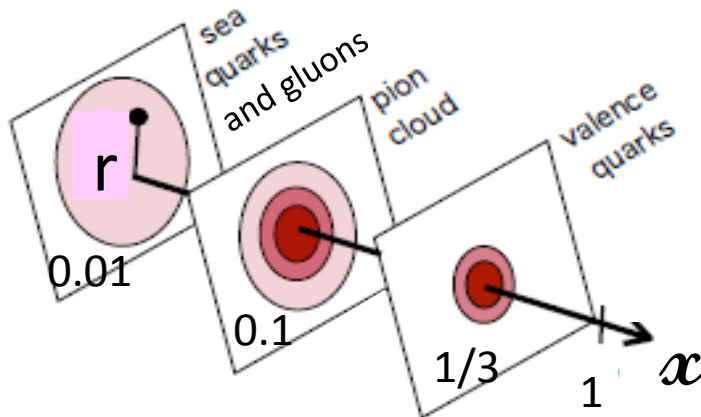
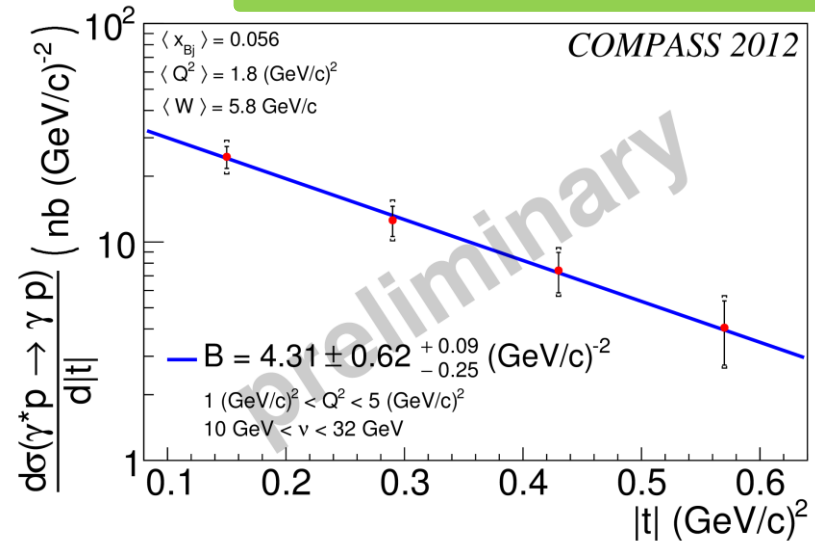
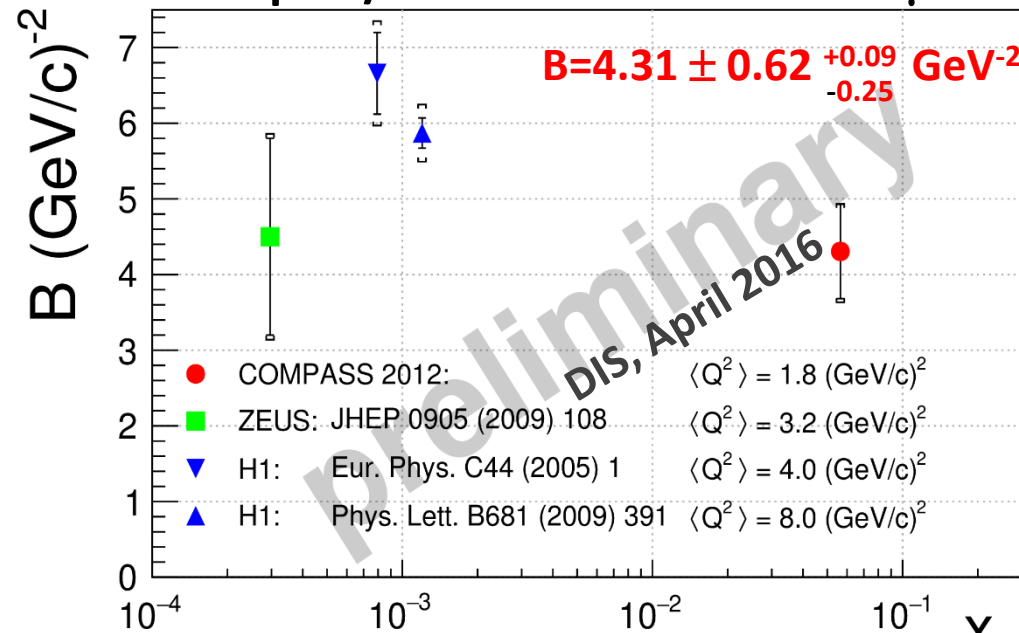


Sea quark imaging @ COMPASS

HERA: $e^\pm p$ 27/920 GeV

COMPASS: μ^\pm 200 GeV

$$d\sigma^{\text{DVCS}}/dt = e^{-B|t|}$$



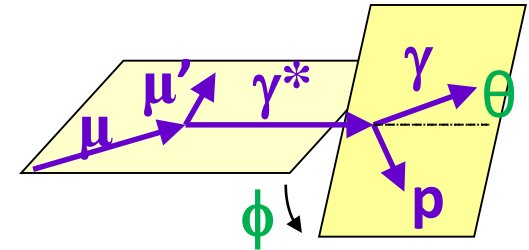
DVCS-BH interference on the proton

- Im DVCS with Beam Helicity Dependent X-sect.
- Re DVCS with Beam Charge Difference and Unpolarized X-section
- mainly constrains on the GPD H

Azimuthal dependence of BH+DVCS

$$\frac{d^4\sigma(\ell p \rightarrow \ell p \gamma)}{dx_B dQ^2 d|t| d\phi} = \underset{\text{Well known}}{d\sigma^{BH}} + \left(d\sigma_{unpol}^{DVCS} + P_\ell d\sigma_{pol}^{DVCS} \right) + (e_\ell \text{Re } I + e_\ell P_\ell \text{Im } I)$$

$$\begin{aligned} d\sigma^{BH} &\propto c_0^{BH} + c_1^{BH} \cos \phi + c_2^{BH} \cos 2\phi \\ d\sigma_{unpol}^{DVCS} &\propto c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi \\ d\sigma_{pol}^{DVCS} &\propto s_1^{DVCS} \sin \phi \\ \text{Re } I &\propto c_0^I + c_1^I \cos \phi + c_2^I \cos 2\phi + c_3^I \cos 3\phi \\ \text{Im } I &\propto s_1^I \sin \phi + s_2^I \sin 2\phi \end{aligned}$$



Twist-2 >>

■ Twist-3,

■ Twist-2
double helicity flip
for gluons

$$s_1^I = \text{Im } \mathcal{F} \quad c_1^I = \text{Re } \mathcal{F}$$

$$\mathcal{F} = F_1 \mathcal{H} + \xi (F_1 + F_2) \tilde{\mathcal{H}} - t/4m^2 F_2 \mathcal{E} \xrightarrow{\text{at small } x_B} F_1 \mathcal{H} \quad \text{for proton}$$

NB: to extract \mathcal{E} use a neutron (deuteron) target or a transversely pol. target
to extract $\tilde{\mathcal{H}}$ use a longitudinally polarized target

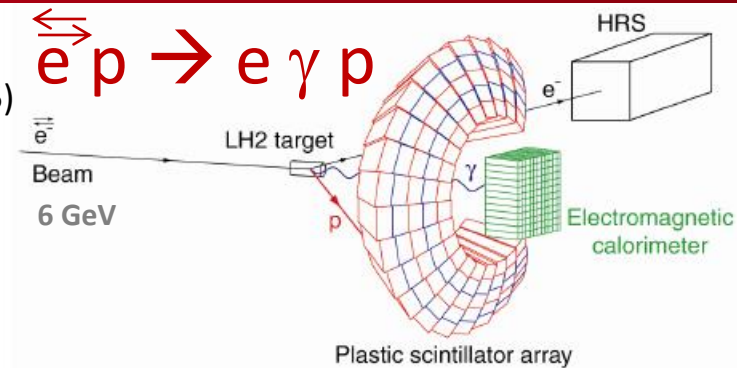
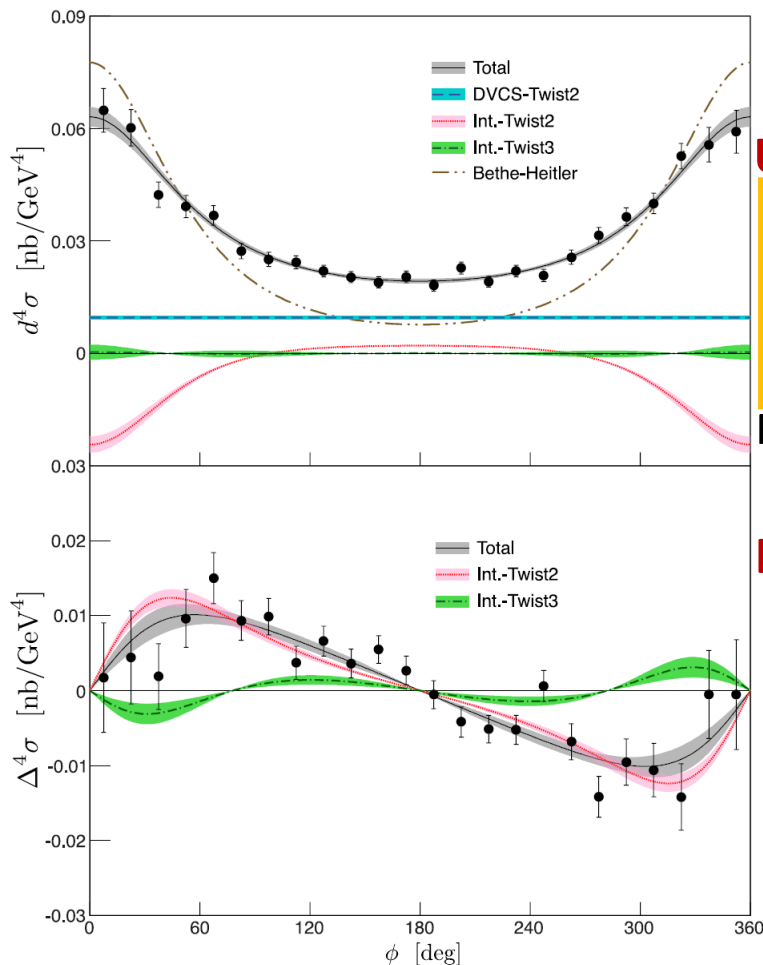
Beam Spin Sum and Diff of DVCS - HallA

E00-110 pioneer experiment with magnetic spectrometer

$x_B=0.36$ $Q^2=1.5, 1.9, 2.3 \text{ GeV}^2$ Defurne et al. PRC92, 055202 (2015)

$x_B=0.34, x_B=0.39$ $Q^2=2.1 \text{ GeV}^2$

$x_B=0.36, Q^2=2.3 \text{ GeV}^2, -t=0.32 \text{ GeV}^2$



Unpolarized cross section

$$\begin{aligned} d\sigma^{\leftarrow} + d\sigma^{\rightarrow} &\propto d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + \text{Re } I \\ &\rightarrow d\sigma^{BH} + \underbrace{c_0^{DVCS}}_{\text{cyan}} + \underbrace{c_0^I + c_1^I \cos \phi}_{\text{pink}} + \underbrace{c_2^I \cos 2\phi}_{\text{green}} \end{aligned}$$

Further separation \rightarrow need of different ε or beam energies

Helicity Dependent cross section

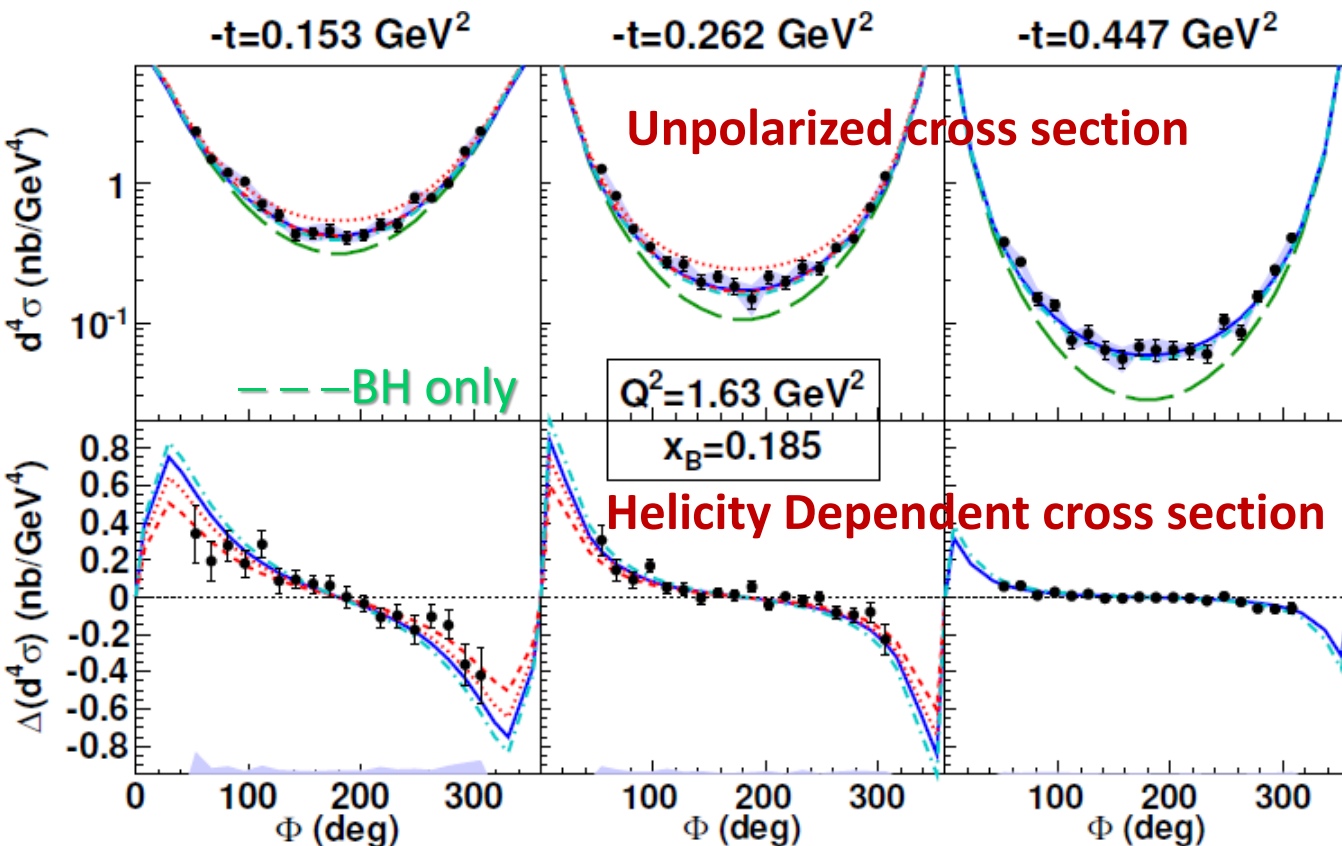
$$\begin{aligned} d\sigma^{\leftarrow} - d\sigma^{\rightarrow} &\propto d\sigma_{vol}^{DVCS} + \text{Im } I \\ &\rightarrow \underbrace{s_1^I \sin \phi}_{\text{pink}} + \underbrace{s_2^I \sin 2\phi}_{\text{green}} \end{aligned}$$

Beam Spin Sum and Diff of DVCS - CLAS

21 bins in (x_B, Q^2) or 110 bins (x_B, Q^2, t)

- Jo et al. PRL115, 212003 (2015)

$$\vec{e} p \rightarrow e \gamma p$$



models:

VGG Vanderhaeghen, Guichon, Guidal
PRL80(1998), PRD60(1999),
PPNP47(2001), PRD72(2005)
1st model of GPDs
constant evolution

KMS12 Kroll, Moutarde, Sabatié, EPJC73 (2013)
using the **GK** model
Goloskokov, Kroll,
EPJC42,50,53,59,65,74
for GPD adjusted on
the hard exclusive
meson production at
small x_B
“universality” of GPDs

KM10a — — — **KM10** Kumericki, Mueller, NPB (2010) 841

Flexible parametrization of the GPDs based on both a Mellin-Barnes representation and dispersion integral which entangle skewness and t dependences

Global fit on the world data ranging from H1, ZEUS to HERMES, JLab

Valence quark imaging at Jlab

Fit of 8 CFFs at L.O and L.T.

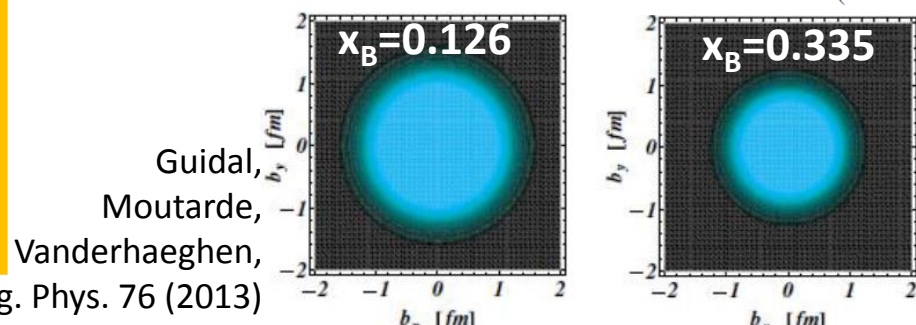
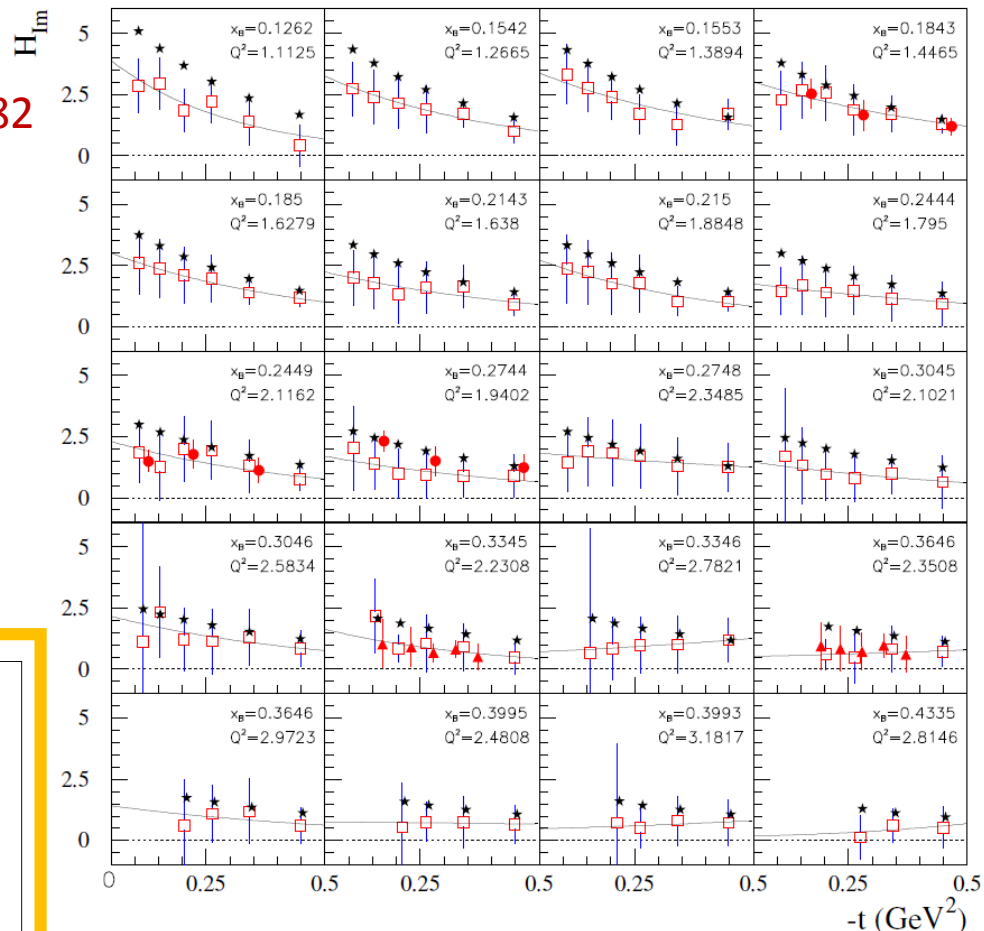
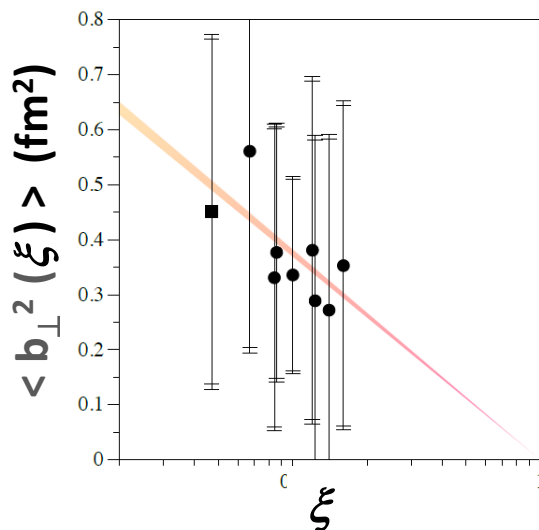
Dupré, Guidal, Vanderhaeghen, arXiv: 1606.0782

$$s_1^I = \text{Im } F_1 \mathcal{H}$$

- CLAS σ and $\Delta\sigma$
- ▲ HallA σ and $\Delta\sigma$
- CLAS A_{UL} and A_{LL}

★ VGG model
— Fit $A e^{-B'|t|}$

$$\langle b_{\perp}^2 \rangle \approx 4 B'$$



Guidal,
Moutarde,
Vanderhaeghen,

Rept. Prog. Phys. 76 (2013)

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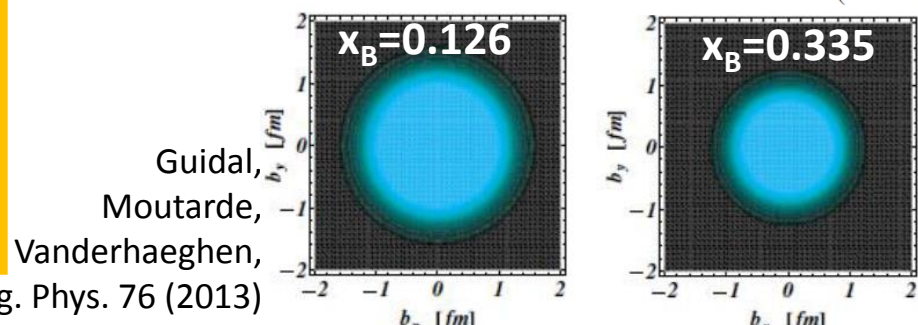
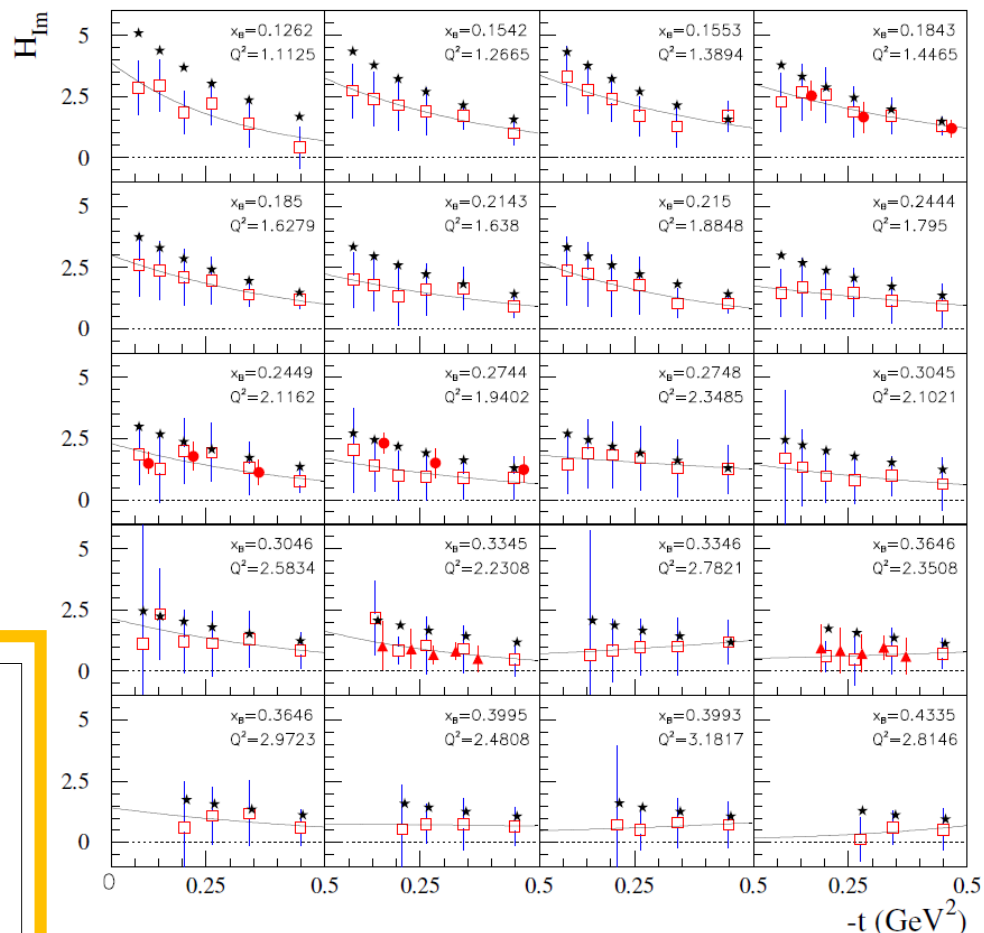
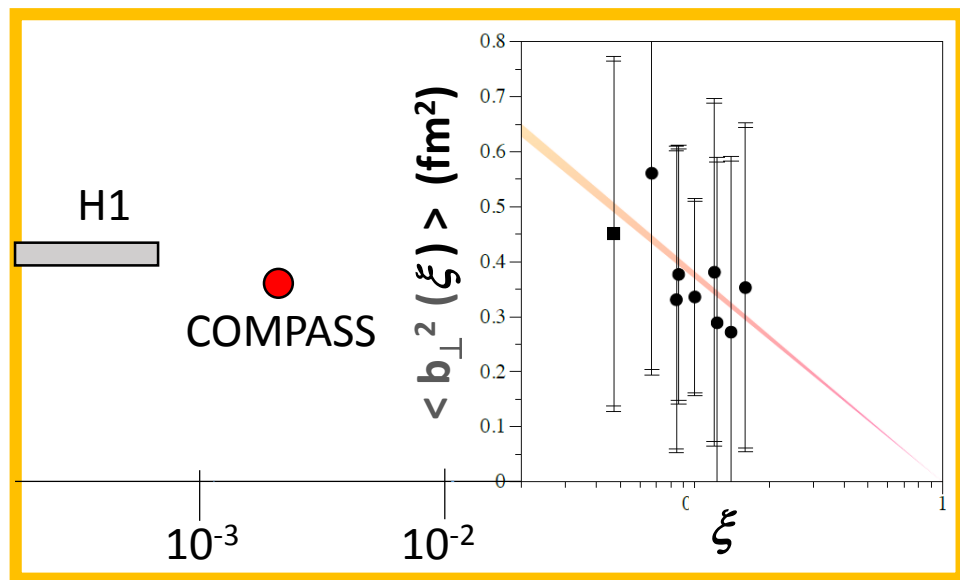
Dupré, Guidal, Vanderhaeghen, arXiv: 1606.071

$$s_1^I = \text{Im } F_1 \mathcal{H}$$

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— Fit $A e^{-B'|t|}$

$$\langle b_{\perp}^2 \rangle \approx 4 B'$$



Guidal, Moutarde, Vanderhaeghen, Rept. Prog. Phys. 76 (2013)

Future Beam Spin Sum and Diff @JLab12

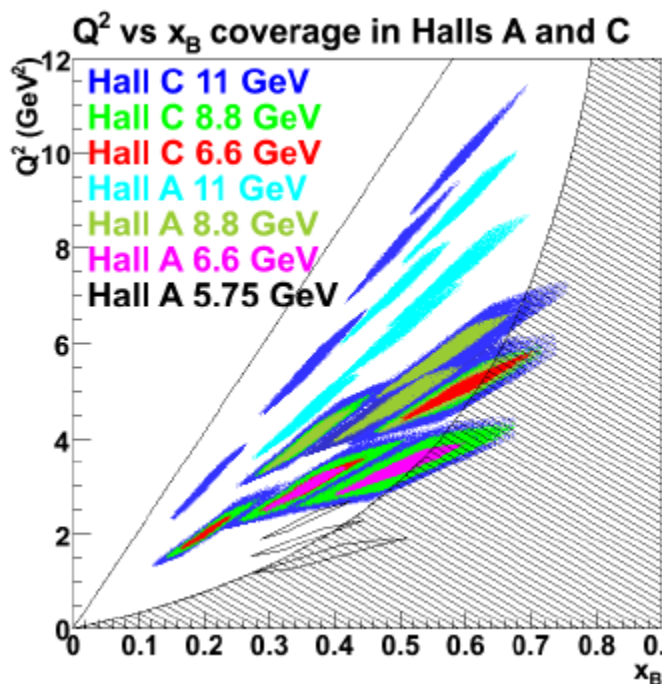
with high resolution magnetic spectrometer+ Calorimeter in Halls A and C

Exp. 2010: run E07-007

Now 2015: Hall A

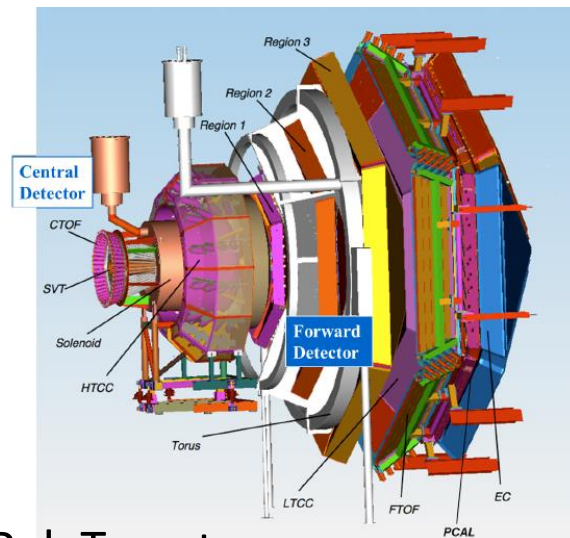
~2018: Hall C

Different beam energies for a Rosenbluth-like DVCS²/Interf. separation

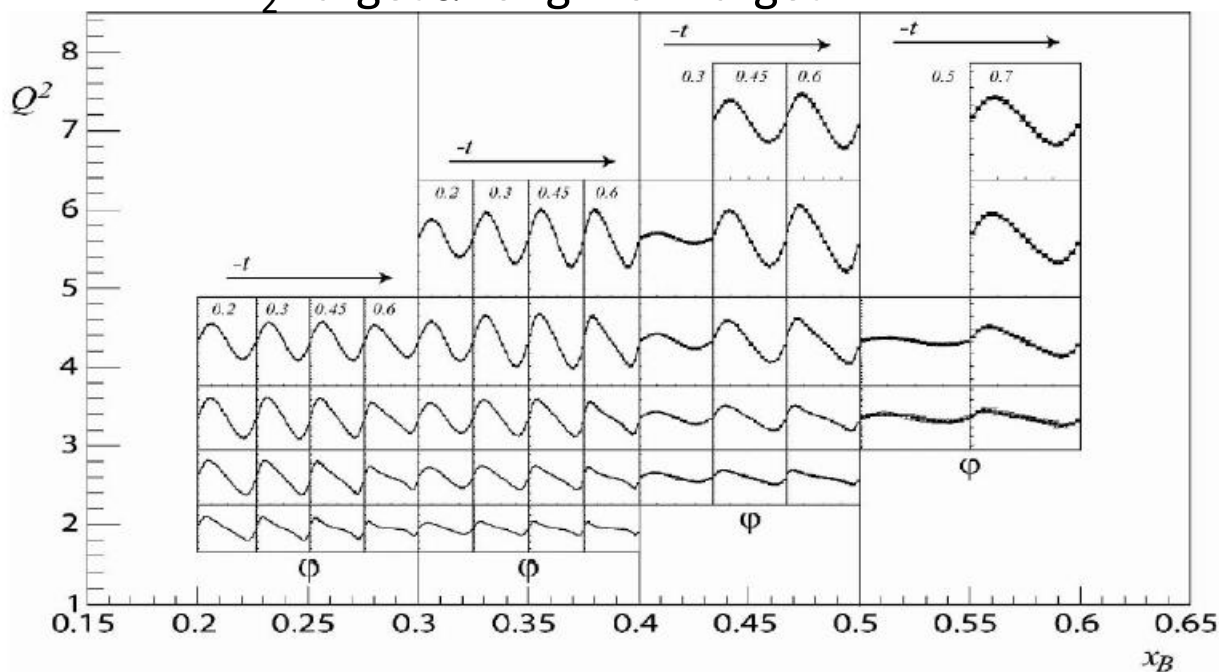


with CLAS12
In 2016

E12-06-119

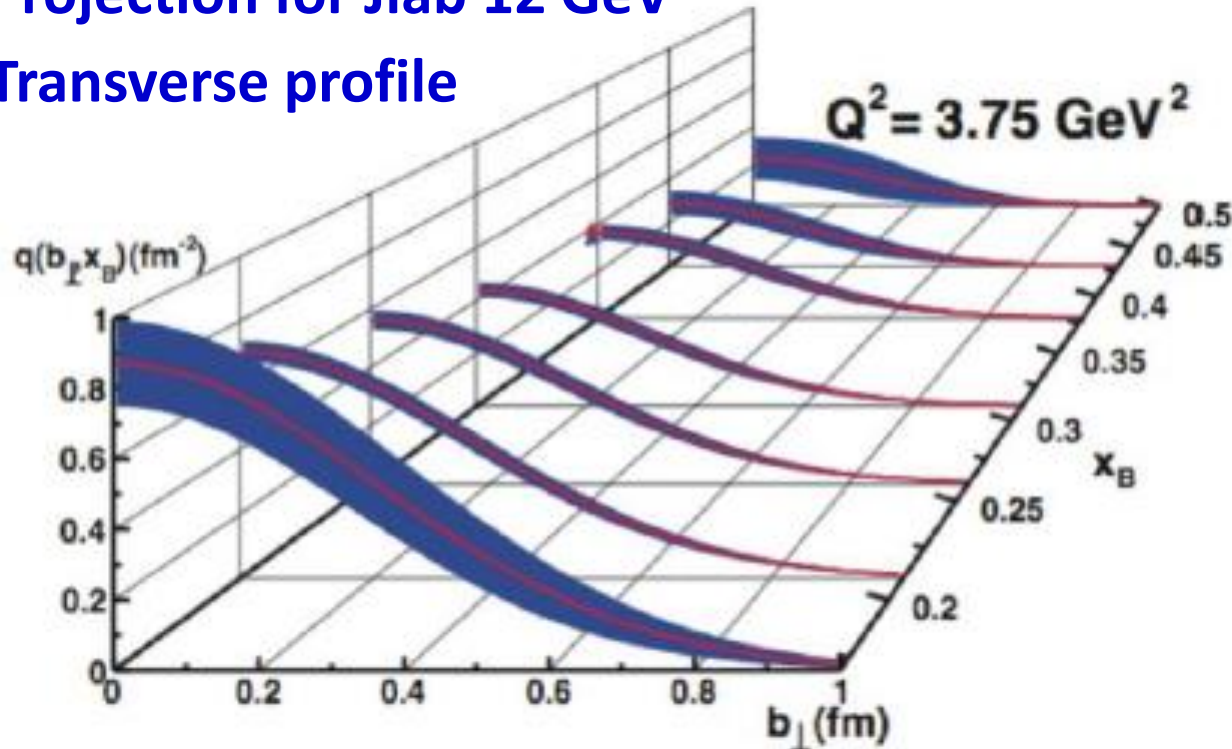


LH₂ Target & Long. Pol. Target



Future Beam Spin Sum and Diff @JLab12

Projection for Jlab 12 GeV
Transverse profile



Dudek et al., EPJA48 (2012)

The 2015 Long Range Plan for Nuclear Science

Beam Charge and Spin Diff. @ COMPASS

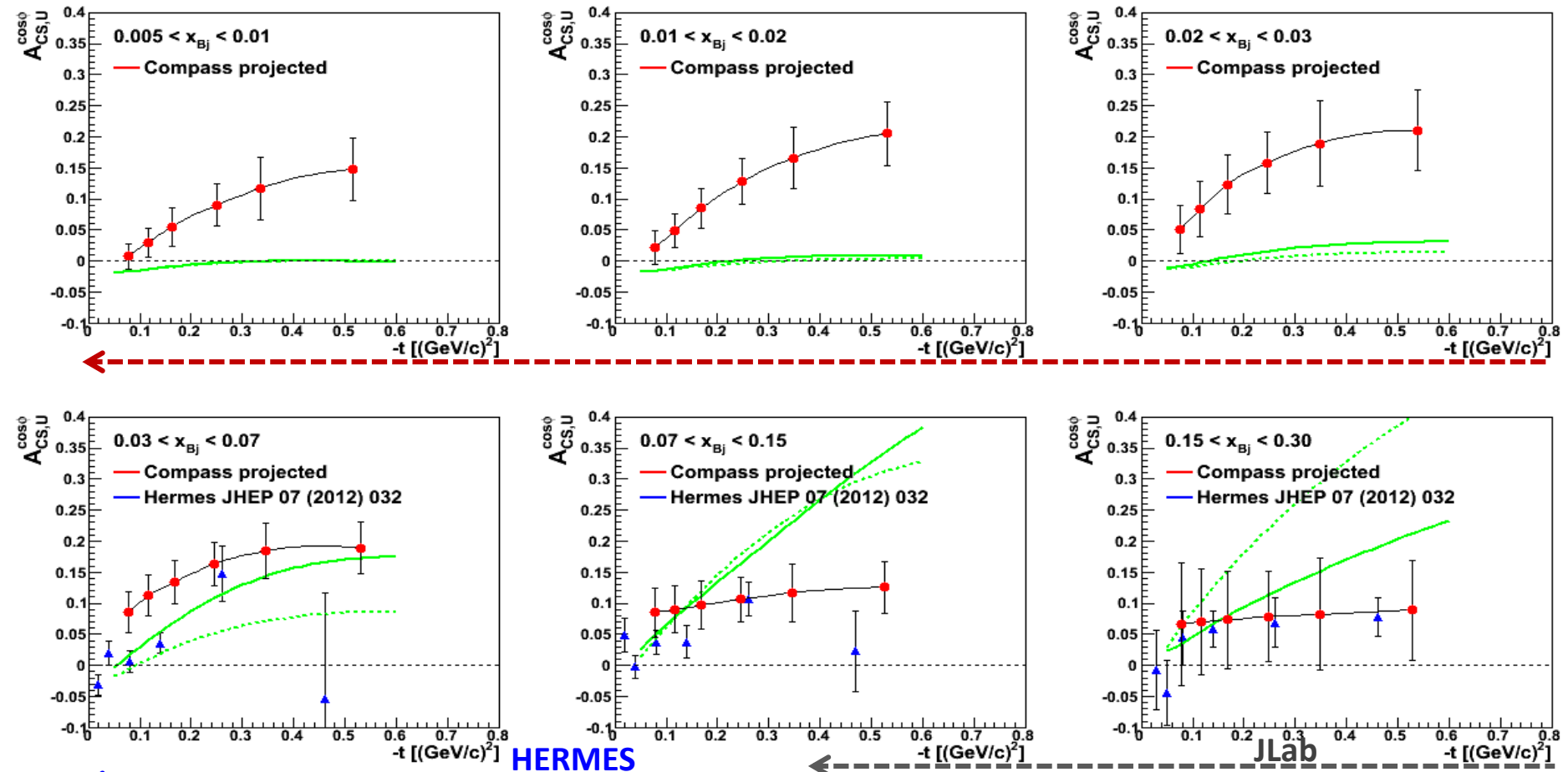
$$c_1^I = \text{Re } F_1 \mathcal{H}$$

Predictions with
VGG and **D.Mueller KM10**

$\text{Re } \mathcal{H} > 0$ at H1

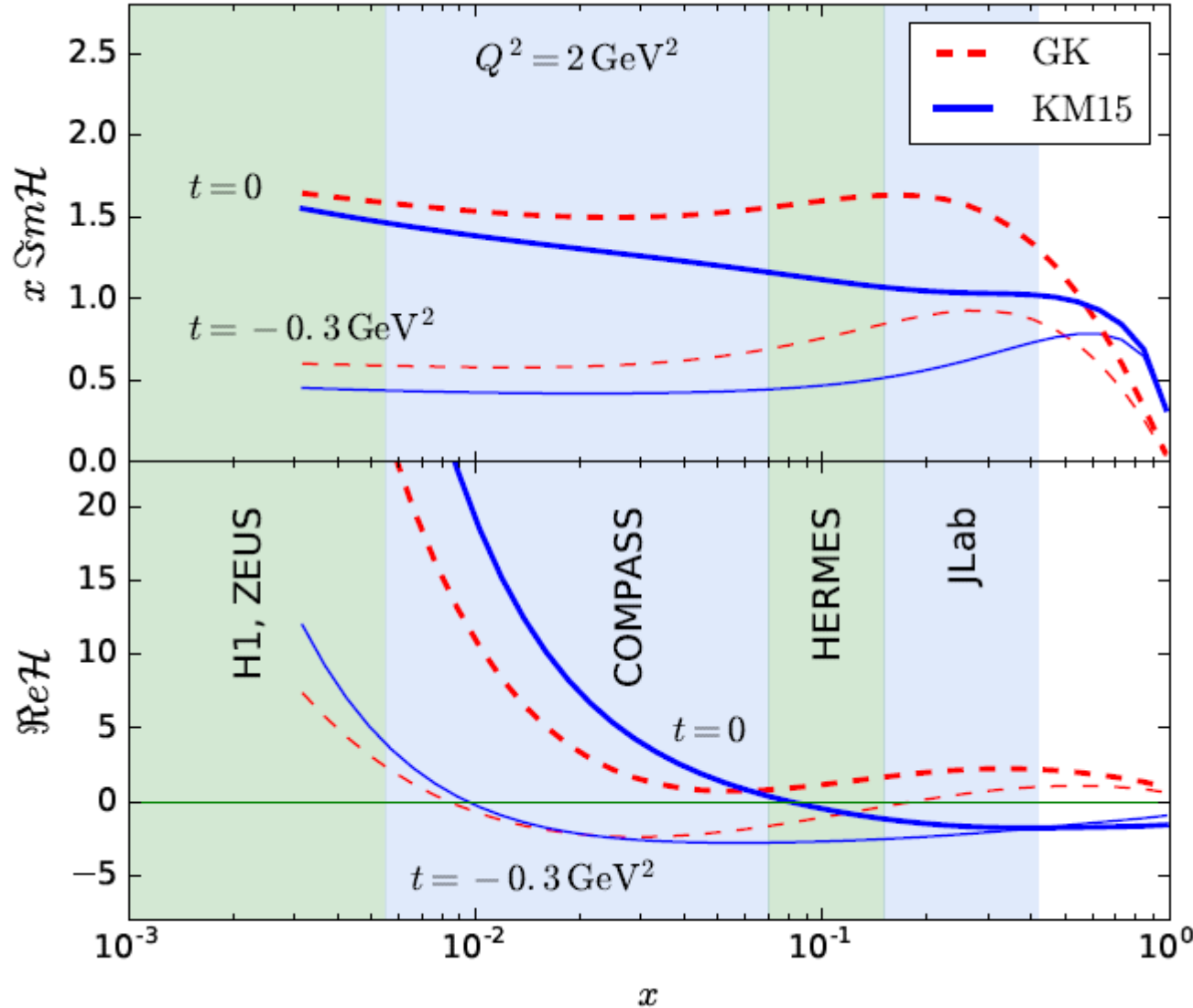
< 0 at HERMES

Value of x_B for the node?



COMPASS 2 years of data $E_\mu = 160 \text{ GeV}$ $1 < Q^2 < 8 \text{ GeV}^2$

Impact of DVCS @ COMPASS in global analysis ?



Im H

Is it rather
well known ?

Re H linked
to the *D term*
is still poorly
constrained

KM15 K Kumericki and D Mueller [arXiv:1512.09014v1](https://arxiv.org/abs/1512.09014v1)

GK S.V. Goloskokov, P. Kroll, EPJC53 (2008), EPJA47 (2011)

Hunting the GPD E, holy grail for OAM

$$\vec{\ell} d \rightarrow \ell n \gamma (p)$$

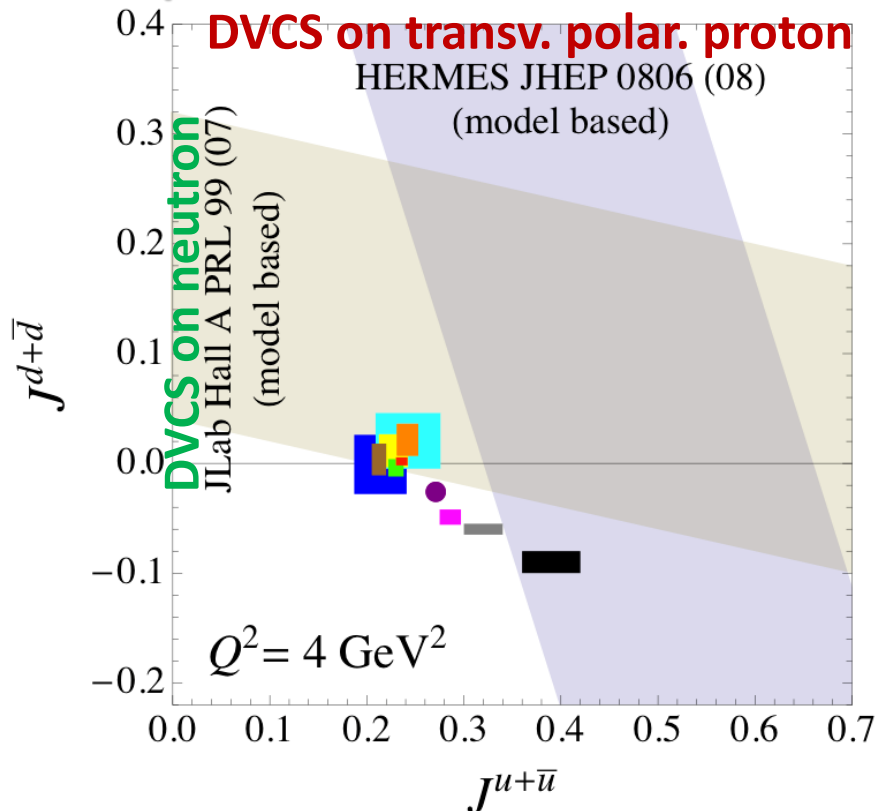
$$\Delta\sigma_{LU} \sim \text{Im} (F_{1n} \mathcal{H} - F_{2n} \mathcal{E})$$

$$\vec{\ell} p^{\uparrow} \rightarrow \ell p \gamma$$

$$\Delta\sigma_{UT} \sin(\phi - \phi_s) \cos \phi = \text{Im} (F_2 \mathcal{H} - F_1 \mathcal{E})$$

$$\Delta\sigma_{LT} \sin(\phi - \phi_s) \cos \phi = \text{Re} (F_2 \mathcal{H} - F_1 \mathcal{E})$$

Model dependent extraction of J^u and J^d



- Goloskokov & Kroll, EPJ C59 (09) 809
- Diehl et al., EPJ C39 (05) 1
- Guidal et al., PR D72 (05) 054013
- Liuti et al., PRD 84 (11) 034007
- Bacchetta & Radici, PRL 107 (11) 212001
- LHPC-1, PR D77 (08) 094502
- LHPC-2, PR D82 (10) 094502
- QCDSF, arXiv:0710.1534
- Wakamatsu, EPJ A44 (10) 297
- Thomas, PRL 101 (08) 102003
- Thomas, INT 2012 workshop

Dudek et al., EPJA48 (2012)

LATTICE QCD

Future program - under discussion at COMPASS - selected at JLab12 as
 "High impact" experiments (CLAS 12 + neutron detector + HDice or ND₃ target)

Look for other GPDs: the chiral-odd H_T and \bar{E}_T

$e p \rightarrow e \pi^0 p$

$$\frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[\left(\frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

$$\frac{d\sigma_L}{dt} = \frac{4\pi\alpha}{k'} \frac{1}{Q^6} \left\{ (1 - \xi^2) |\langle \tilde{H} \rangle|^2 - 2\xi^2 \text{Re} [\langle \tilde{H} \rangle^* \langle \tilde{E} \rangle] - \frac{t'}{4m^2} \xi^2 |\langle \tilde{E} \rangle|^2 \right\} \approx \text{only a few \% of } \frac{d\sigma_T}{dt}$$

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha}{2k'} \frac{\mu_\pi^2}{Q^8} \left[(1 - \xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2 \right]$$

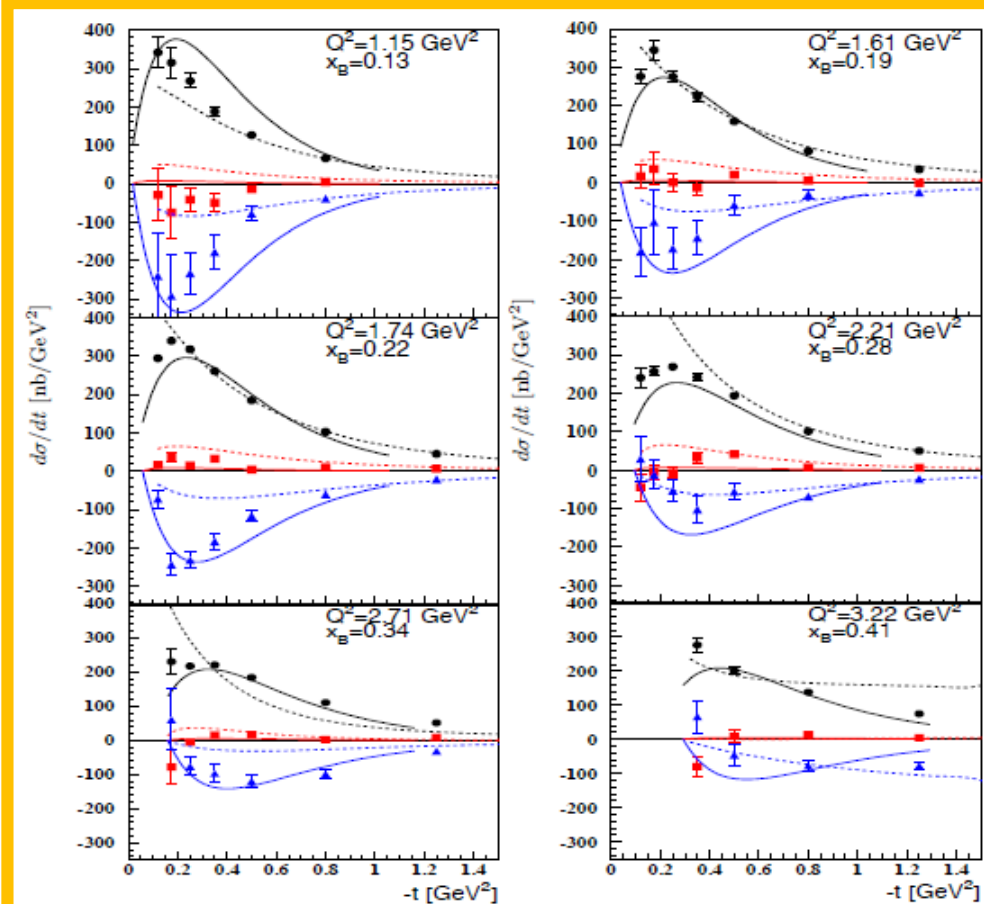
$$\frac{\sigma_{LT}}{dt} = \frac{4\pi\alpha}{\sqrt{2}k'} \frac{\mu_\pi}{Q^7} \xi \sqrt{1 - \xi^2} \frac{\sqrt{-t'}}{2m} \text{Re} [\langle H_T \rangle^* \langle \tilde{E} \rangle]$$

$$\frac{\sigma_{TT}}{dt} = \frac{4\pi\alpha}{k'} \frac{\mu_\pi^2}{Q^8} \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2$$

Large impact of \bar{E}_T
clearly visible in σ_{TT}
and in the dip at small t of σ_T

solid lines : **GK** EPJA47 (2011)

Dotted lines: **GHL** JPG:NPP39 (2012)



CLAS Coll, Bedlinskiy et al., PRC90(2014)2-025205

Look for other GPDs: the chiral-odd H_T and \bar{E}_T

$e p \rightarrow e \pi^0 p$

$$\frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[\left(\frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

$$\frac{d\sigma_L}{dt} = \frac{4\pi\alpha}{k'} \frac{1}{Q^6} \left\{ (1-\xi^2) |\langle \tilde{H} \rangle|^2 - 2\xi^2 \text{Re} [\langle \tilde{H} \rangle^* \langle \tilde{E} \rangle] - \frac{t'}{4m^2} \xi^2 |\langle \tilde{E} \rangle|^2 \right\} \ll \frac{d\sigma_T}{dt} \quad \text{Confirmation -Hall A}$$

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha}{2k'} \frac{\mu_\pi^2}{Q^8} \left[(1-\xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2 \right]$$

$$\frac{\sigma_{LT}}{dt} = \frac{4\pi\alpha}{\sqrt{2}k'} \frac{\mu_\pi}{Q^7} \xi \sqrt{1-\xi^2} \frac{\sqrt{-t'}}{2m} \text{Re} [\langle H_T \rangle^* \langle \tilde{E} \rangle]$$

$$\frac{\sigma_{TT}}{dt} = \frac{4\pi\alpha}{k'} \frac{\mu_\pi^2}{Q^8} \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2$$

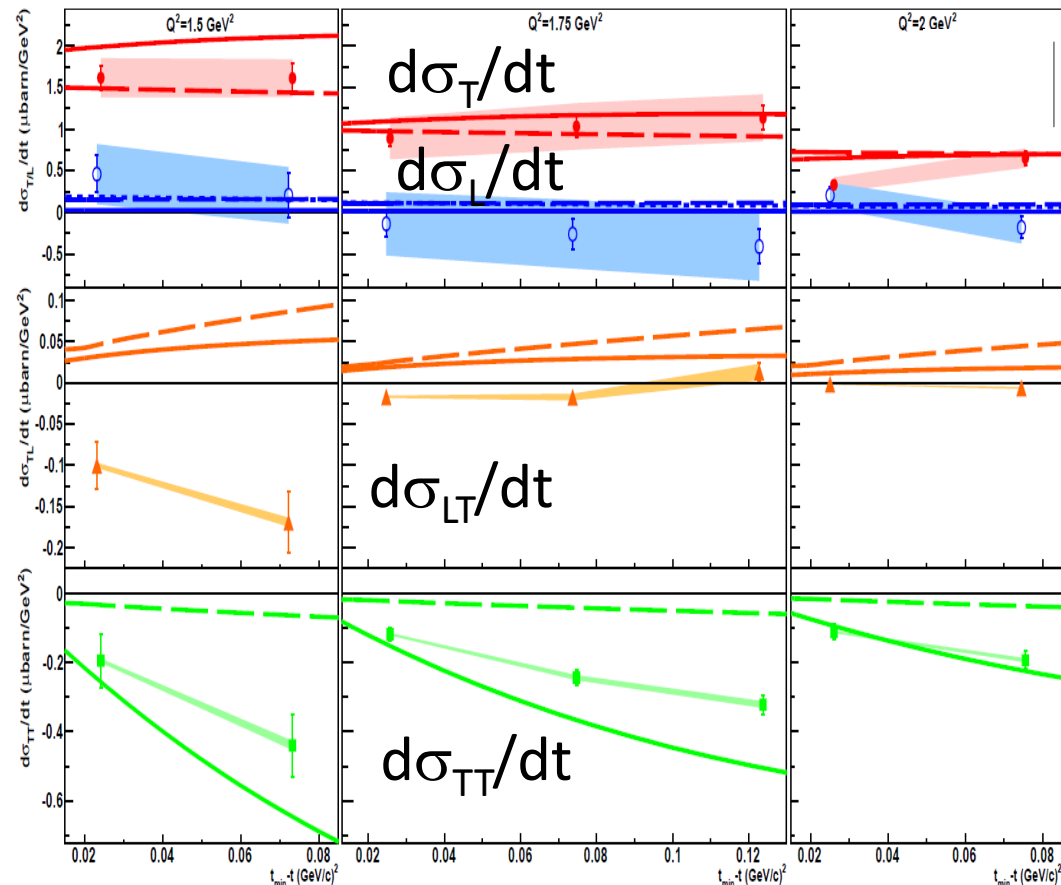
Large impact of \bar{E}_T
clearly visible in σ_{TT}
and in the dip at small t of σ_T

Hall A: σ_L and σ_T separation

Defurne et al. ArXiv:1608.01003

solid lines : **GK** EPJA47 (2011)

Dashed lines: **GHL** JPG:NPP39 (2012)



Only selected results.

A large effort on ρ , ω , ϕ , J/Ψ , π^0 ,

Prospects for Time-like Compton Scattering and Double DVCS.

Precise Data in a large kinematic domain are necessary.

A large theoretical effort:

- to extract the GPD information from the experiments
- to still improve the GPD models

GPD programs with DVCS, HEMP (from light mesons to J/Ψ) are a priority for COMPASS (CERN) @ 200GeV, JLab @ 12GeV and for a future electron-proton collider

Transverse imaging at COMPASS

$d\sigma^{\text{DVCS}}/dt \sim \exp(-B|t|)$

$$B(x_B) = \frac{1}{2} \langle r_{\perp}^2(x_B) \rangle$$

distance between the active quark
and the center of momentum of spectators

Transverse size of the nucleon

mainly dominated by $H(x, \xi=x, t)$

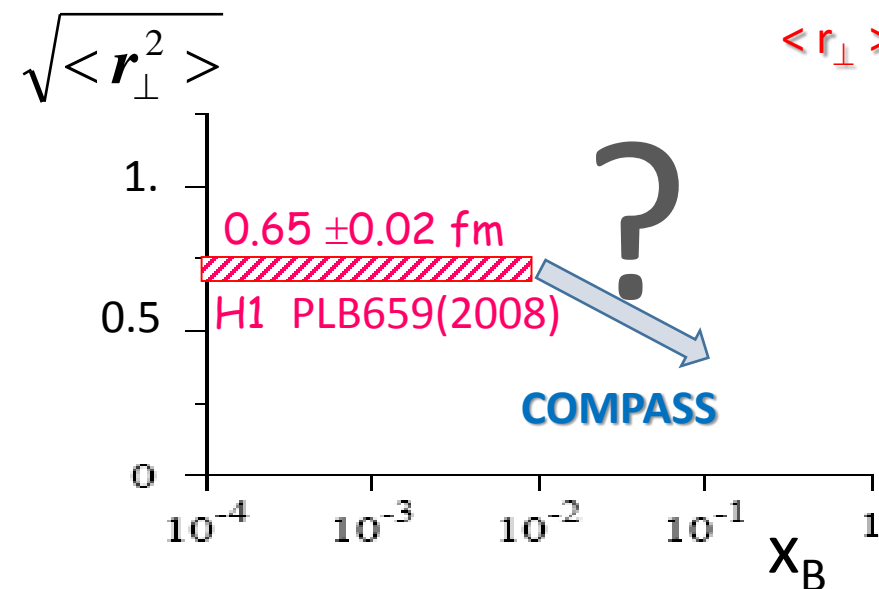
$$\text{related to } \frac{1}{2} \langle b_{\perp}^2(x_B) \rangle$$

distance between the active quark
and the center of momentum of the nucleon

Impact Parameter Representation

$$q(x, b_{\perp}) \leftrightarrow H(x, \xi=0, t)$$

$$\langle r_{\perp} \rangle \sim \langle b_{\perp} \rangle / (1-x)$$



Note $0.65 \text{ fm} = \sqrt{2/3} \times 0.8 \text{ fm}$

