



Virtues and challenges of precision spectroscopy :  
A new axial-vector meson  
and  
a look behind the scenery of light meson decays

Stephan Paul  
for the COMPASS collaboration  
TUM

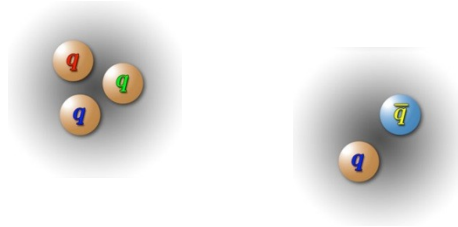


# Brief Overview

- Introduction
- Data-set and PWA analysis
  - Method and Analysis Model
  - Results
    - Light meson resonances revisited
    - A new meson  $a_1(1420)$
- How to observe decay dynamics
  - Example:  $\pi\pi$  S-wave extraction ‘
    - Role of  $f_0(980)$
- Radiative meson-decays
- Conclusions
- Left out: Central production, Photo production,  $\eta\pi$ ,  $\eta'\pi$ ,  $\eta\eta\pi$ ..

- **Hadron: colour neutral** system of quarks

- Baryon (qqq)
- Meson (q $\bar{q}$ )



- At small energy scales

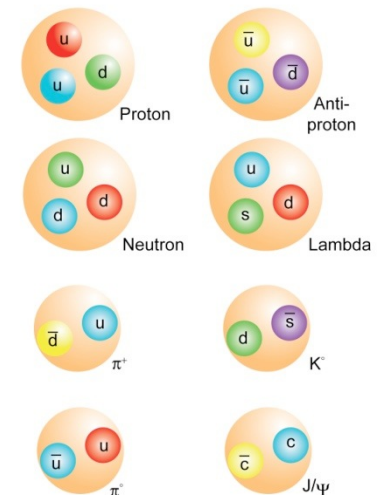
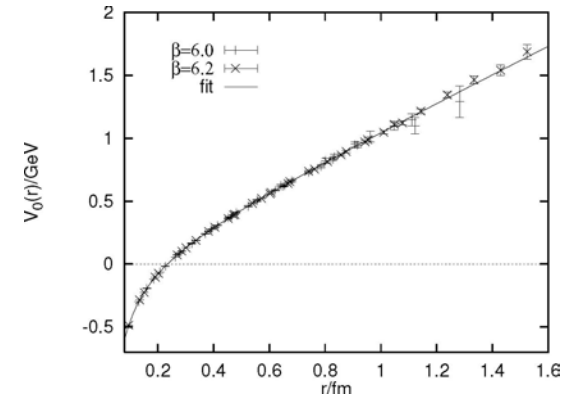
- QCD not analytically solvable
- Effective degrees of freedom: **constituent quarks**

Coupling **quarks** with **gluon field** (99% of p-mass)

$$m_u = m_d = 310 \text{ MeV}/c^2 ; m_s = 485 \text{ MeV}/c^2$$

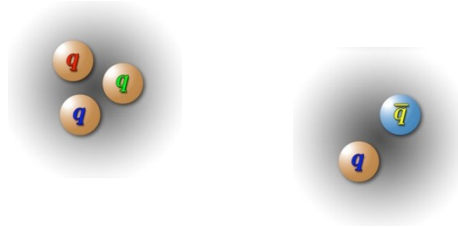
Use effective potential

- Use **symmetries** flavour, spin, colour  
build ‚Periodic table‘ of hadrons



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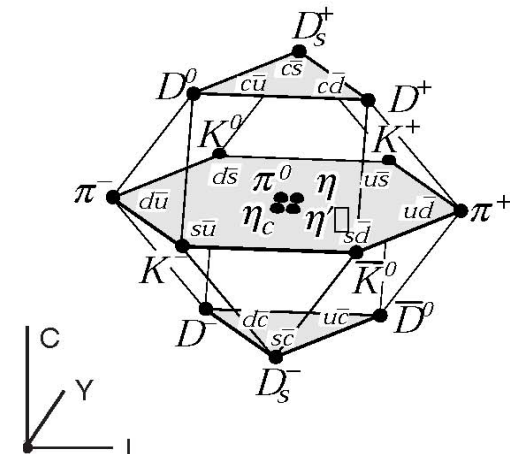
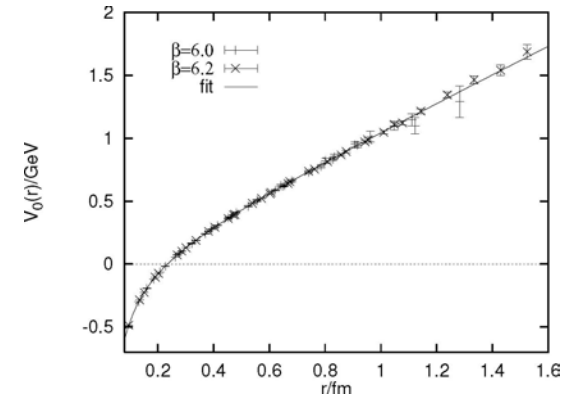
Use effective potential

- Use symmetries flavour, spin, colour build 'Periodic table' of hadrons
- Classify into multiplets

Hadron masses are sum of quark masses

- Use hyperfine-interaction (spin-spin interaction) mass spectrum surprisingly well described

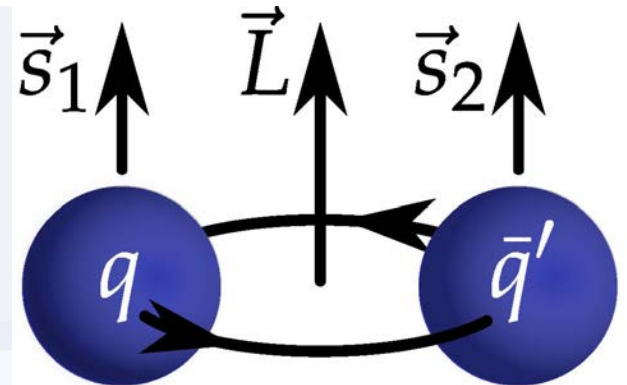
- effective  $q\bar{q}$  potential



## Spin-Parity selection rules for bound $q\bar{q}'$ system

- Quark spins couple to total **intrinsic spin  $S$**   
 $S = 0$  (singlet) or  $S=1$  (triplet)
- Relative **orbital angular momentum  $L$**  couples with total **spin  $S$**  to  $J$

Meson spin:  $\vec{J} = \vec{L} + \vec{S}$





# Constituent Quark Model Mesons



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Meson spin:  $\vec{J} = \vec{L} + \vec{S}$

- Isospin:  $I = 1$  for u,d quarks,  $I=0$  for other quarks

$$I_z(\text{u}) = 1/2$$

$$I_z(\text{d}) = -1/2$$

light Mesons:  $I = 0$  or  $1$

other Mesons:  $I = 0$  or  $1/2$

- Parity:  $P = (-1)^{L+1}$
- Charge conjugation:  $C = (-1)^{L+S}$
- G-parity:  $G = C \cdot e^{i\pi I_z} = (-1)^{I+L+S}$



# Constituent Quark Model II Mesonen



- **Allowed**  $J^{PC}$  combinations:

$L = 0 \rightarrow$  pseudo-scalar  $0^{-+}$ , Vector  $1^{--}$

$L = 1 \rightarrow$  scalar  $0^{++}$ , axial-vector  $1^{+-}$ ,  $1^{++}$  and tensor  $2^{++}$

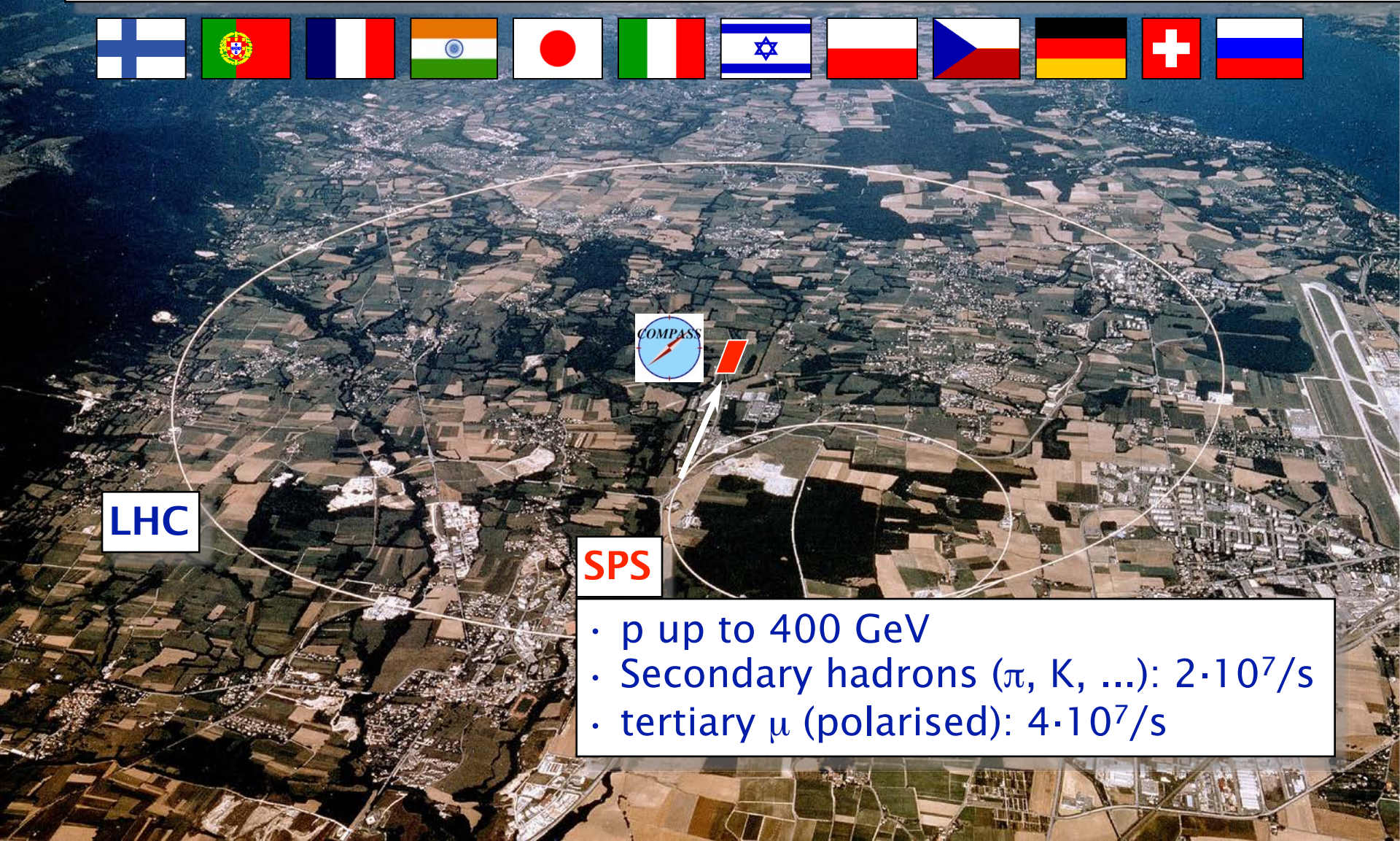
- **Forbidden**  $J^{PC}$  combinations:  $0^{--}$ ,  $0^{+-}$ ,  $1^{-+}$ ,  $2^{+-}$ ,  $3^{+-}$  .....
- Same quantum numbers mix



# COMPASS am CERN



COmmon Muon and Proton Apparatus for Structure and Spectroscopy



LHC

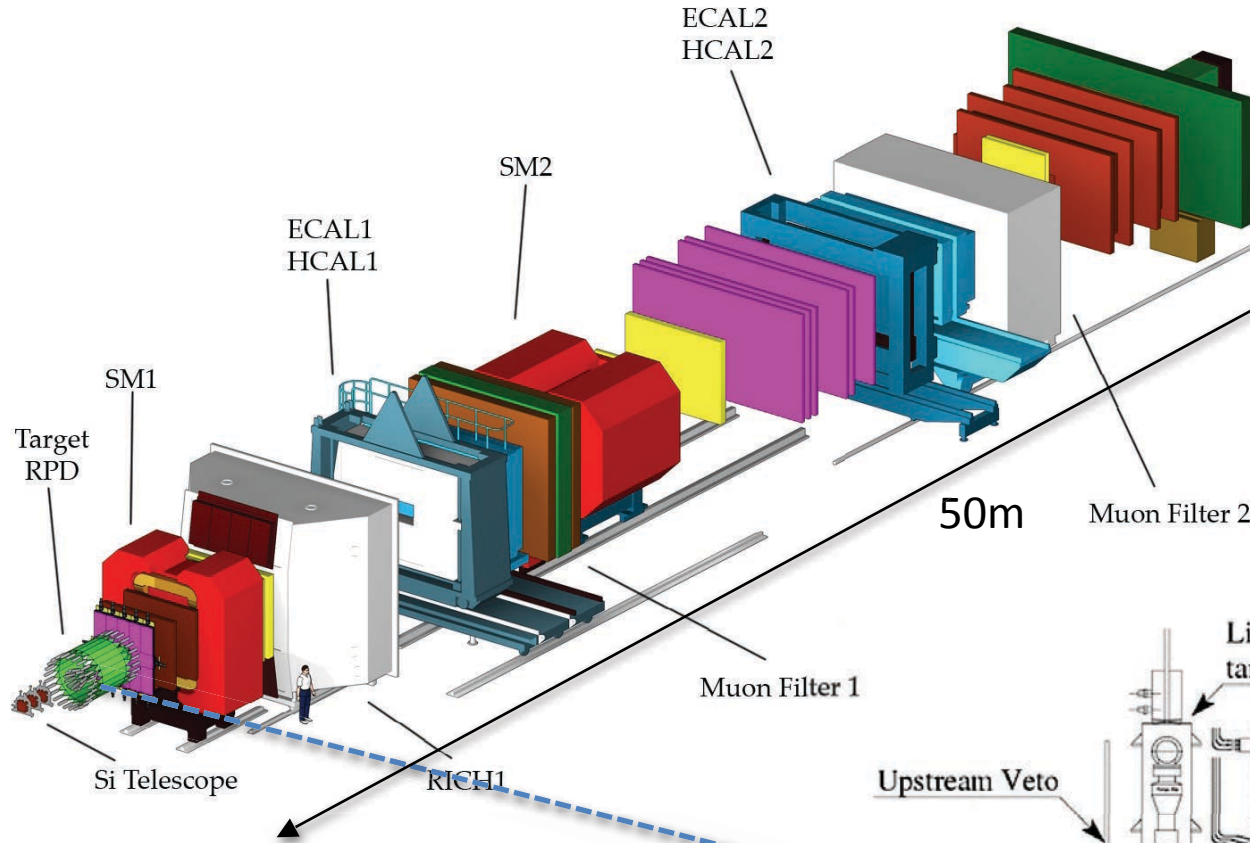
SPS

- p up to 400 GeV
- Secondary hadrons ( $\pi$ , K, ...):  $2 \cdot 10^7/s$
- tertiary  $\mu$  (polarised):  $4 \cdot 10^7/s$





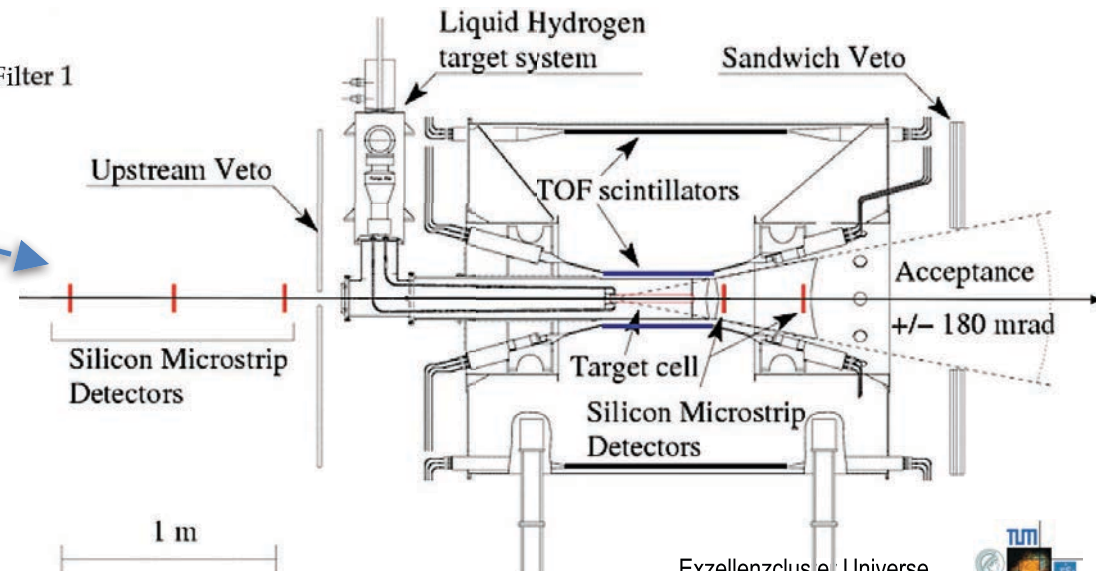
# The COMPASS Experiment



CERN SPS

Hadron beam:

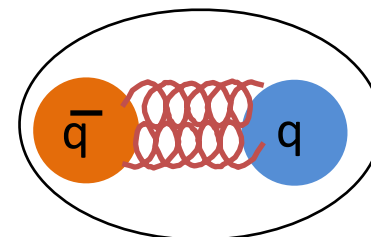
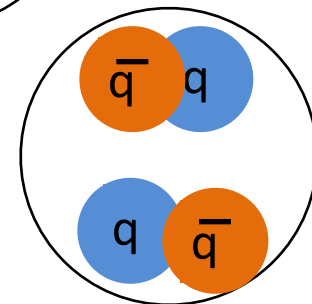
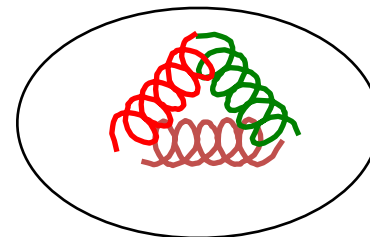
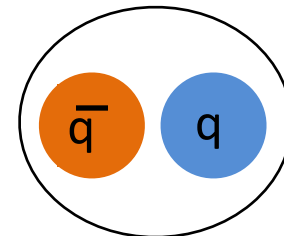
- 190 GeV/c  $\pi$ , K,  $\rho$
- $5 \cdot 10^7$  particles/SPS-spill
- 60 days data taking 2008
- **Trigger:** RPD hit, beam veto



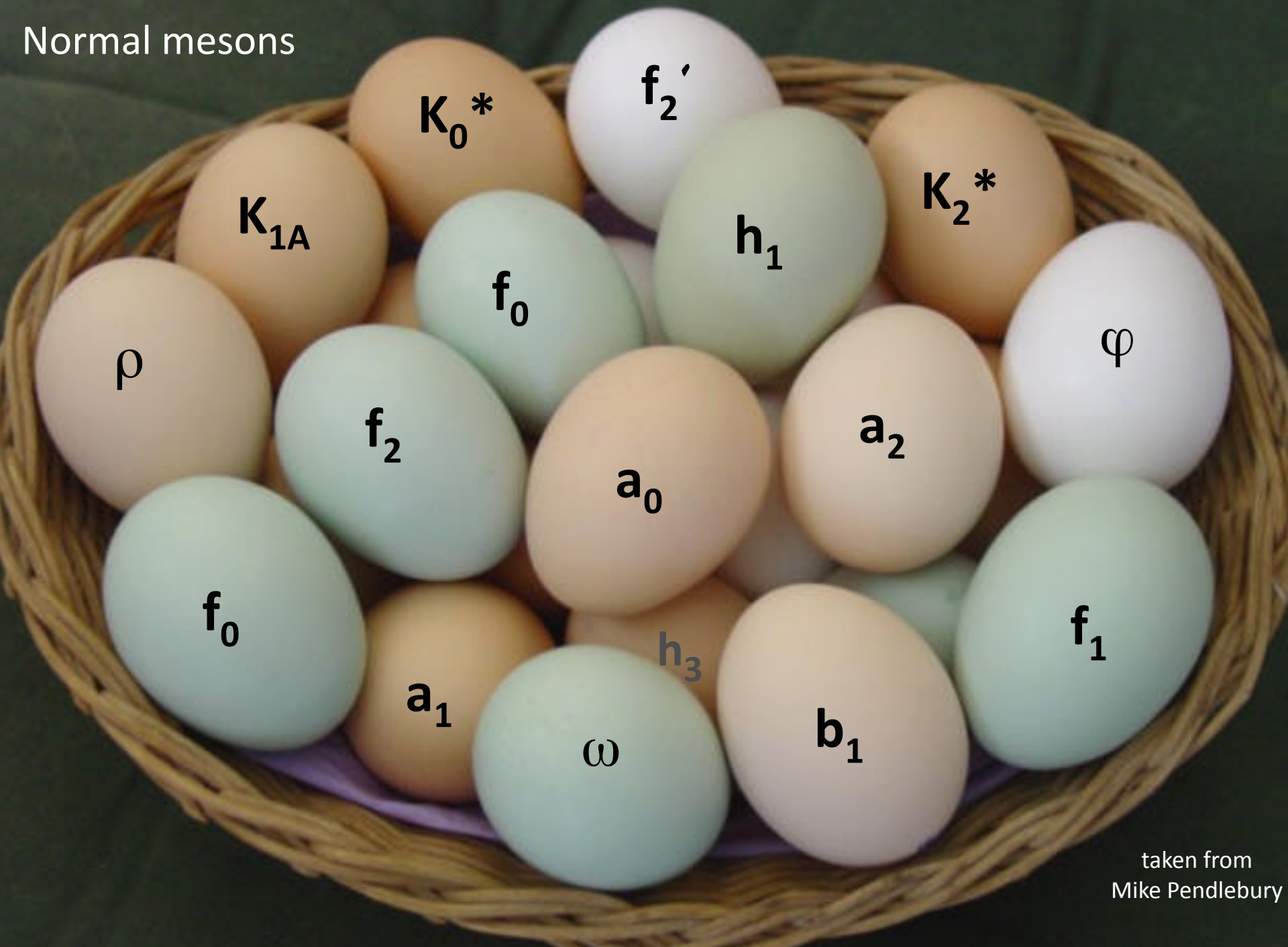


# Light Mesons, Quarks and Gluons

- **Quark model mesons** (u, d, s quarks)
- **Glueballs** (gluons and **no valence quarks**)
- **Multiquarks** (quark-antiquark pairs)
- **Hybrids** (quarks and gluonic excitation, which contribute to static properties)



Normal mesons



taken from  
Mike Pendlebury

**More Surprising States?**

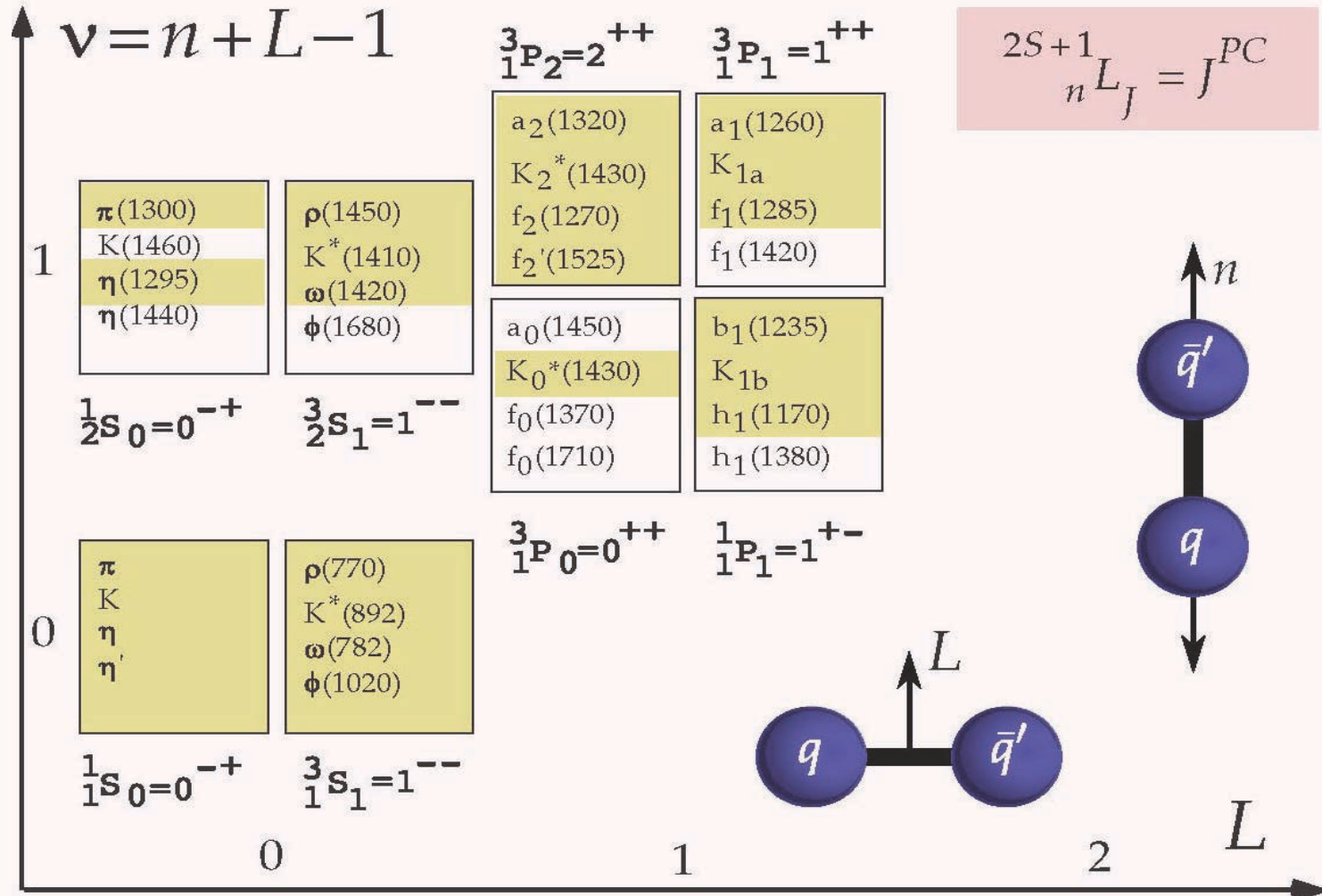


taken from  
Mike Pendlebury



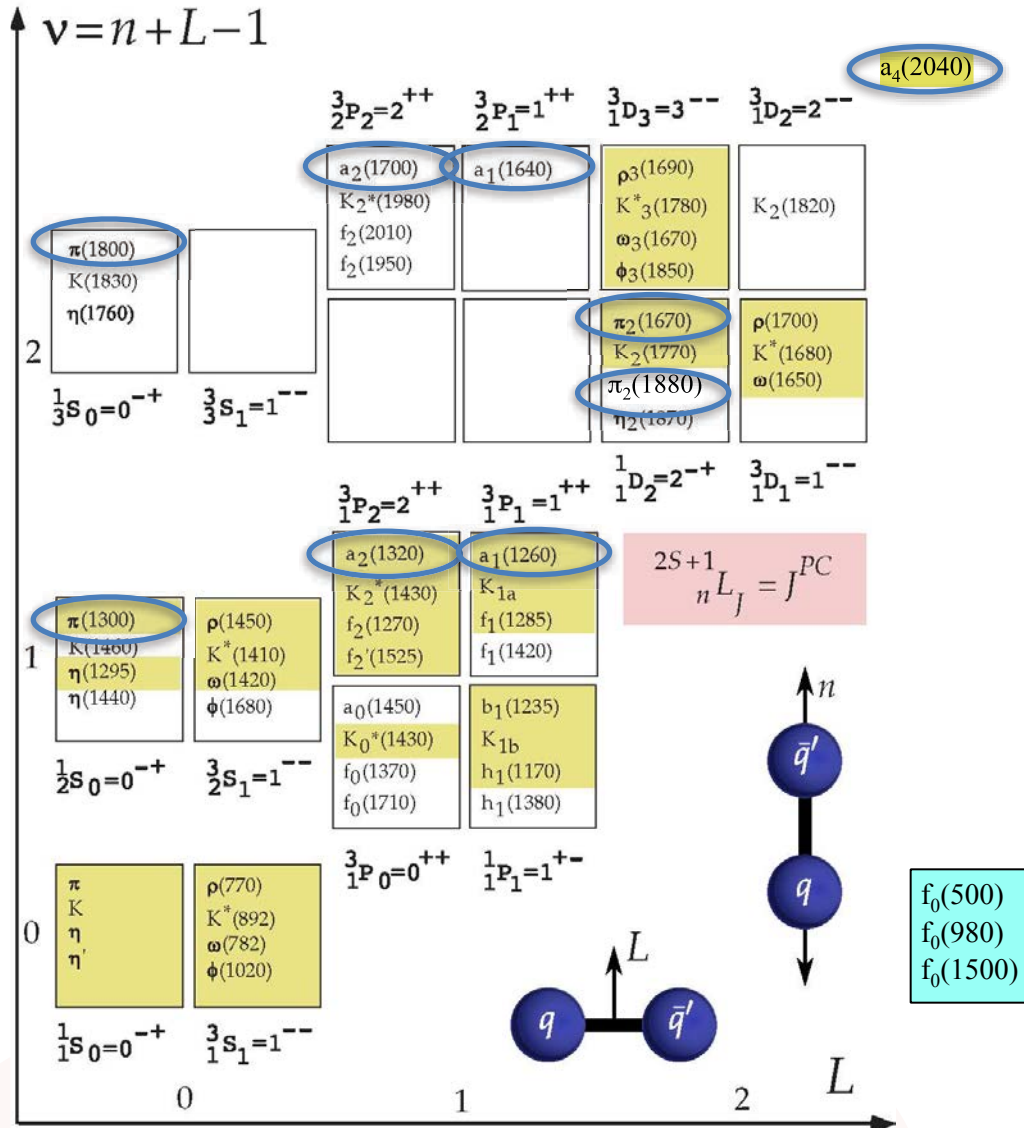
# Constituent Quarks and Mesons

Spectrum of light mesons:



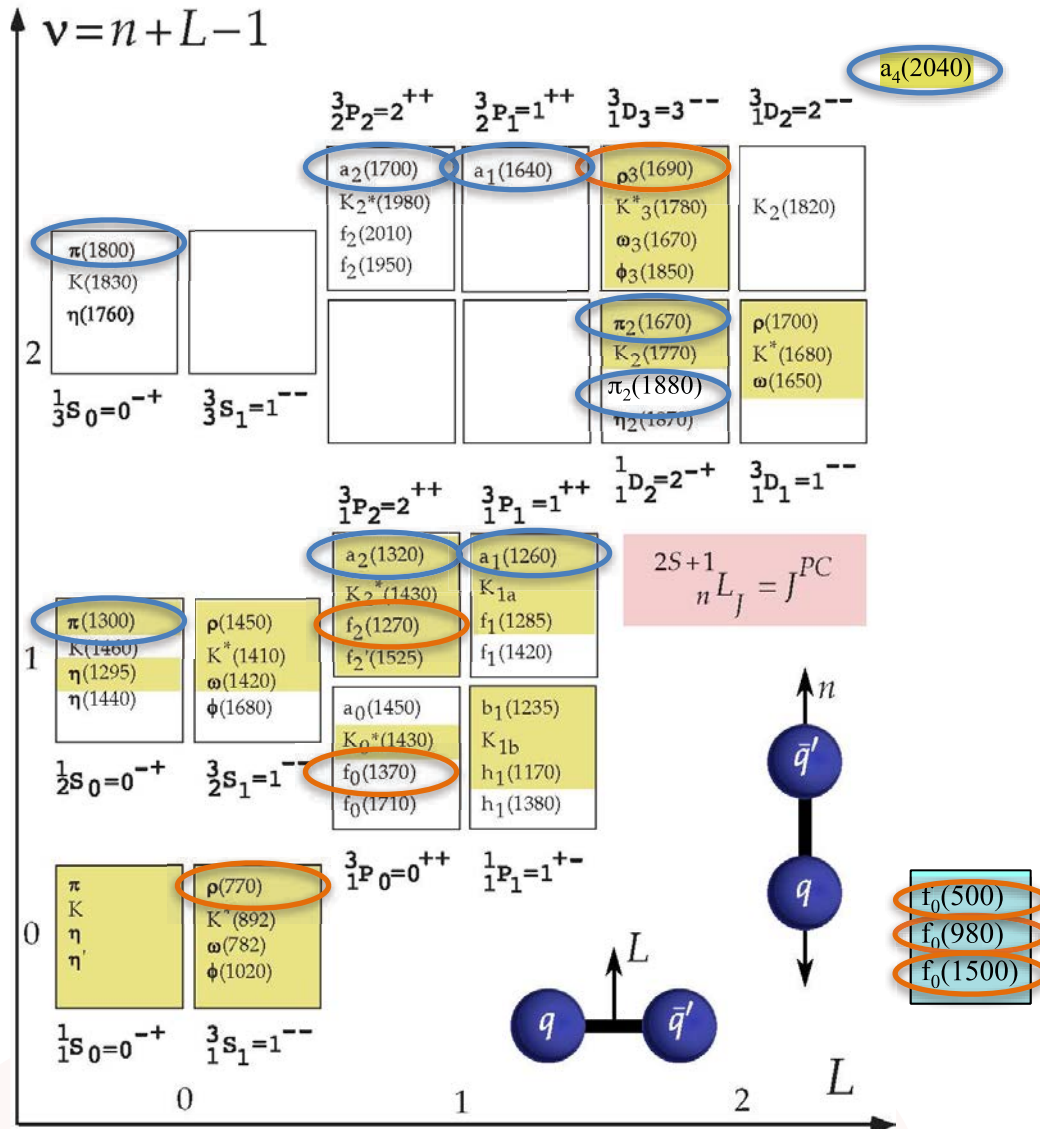


# Constituent Quarks and Mesons



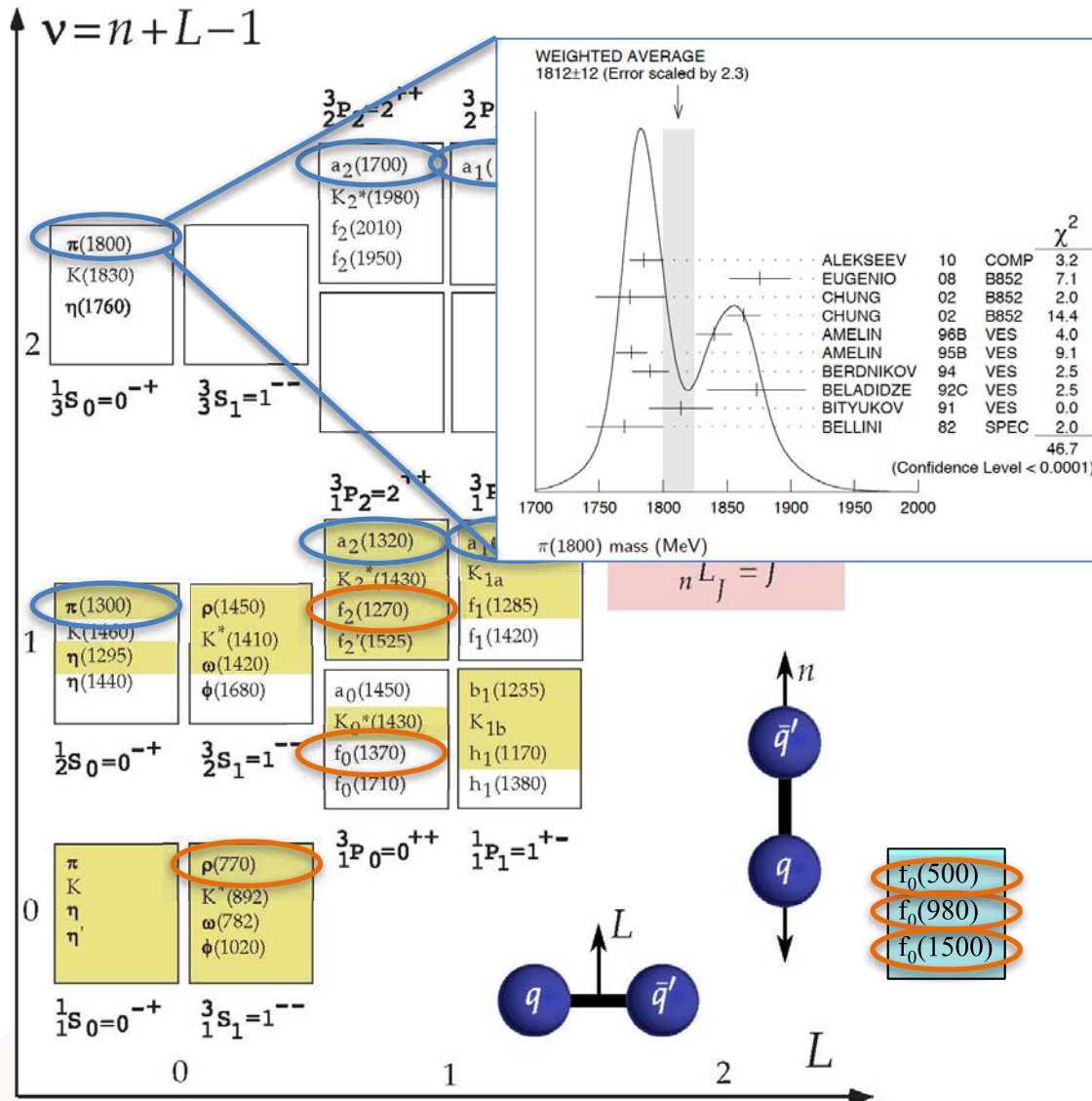


# Constituent Quarks and Mesons





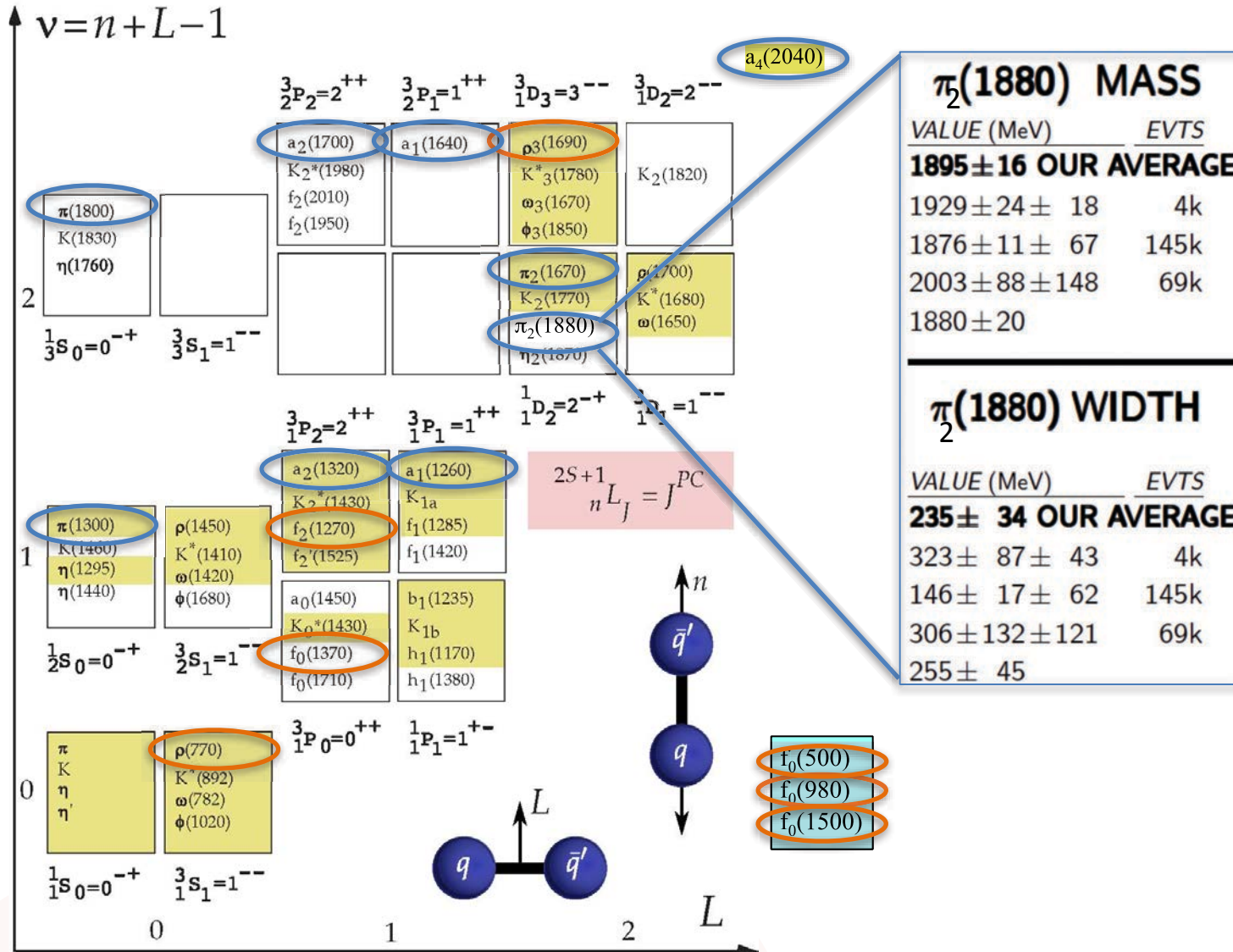
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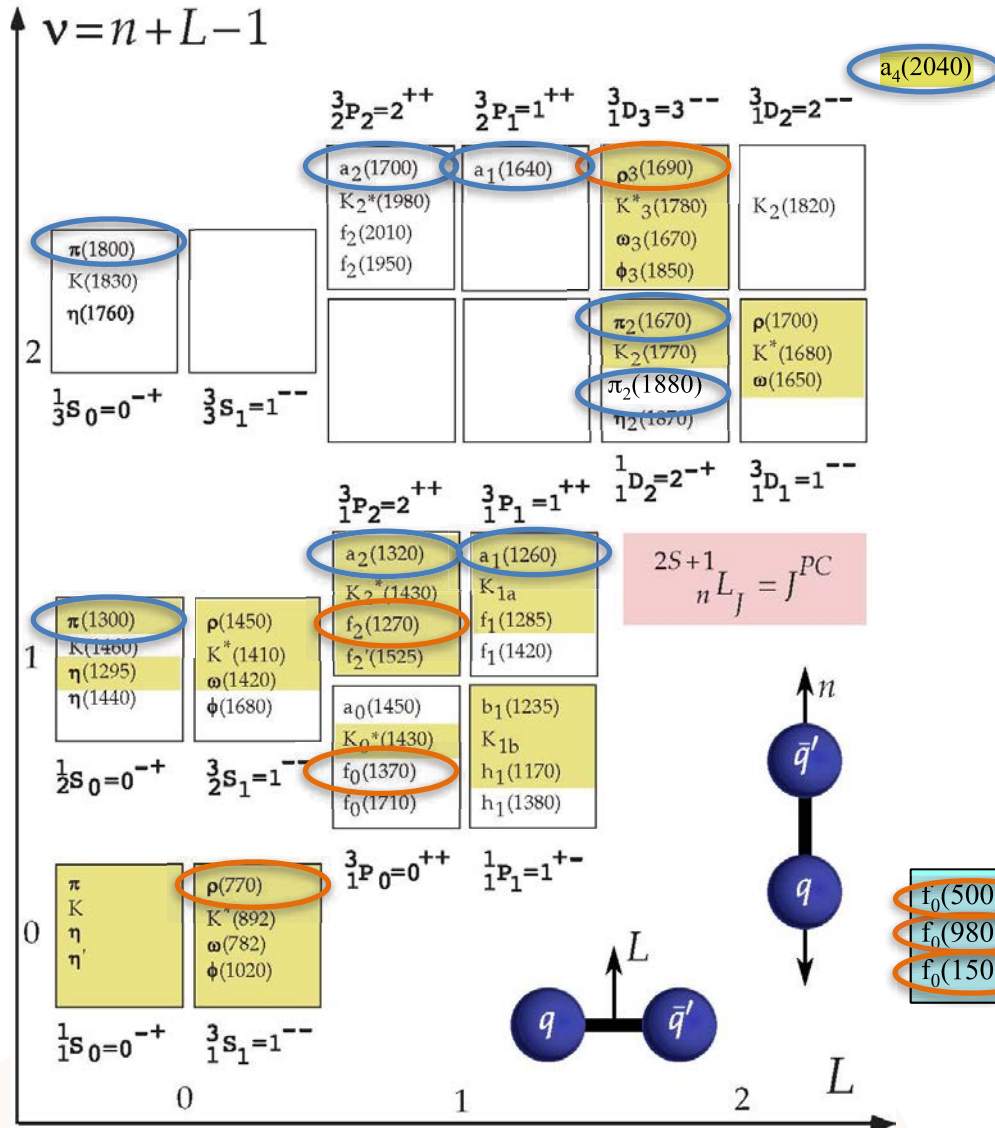


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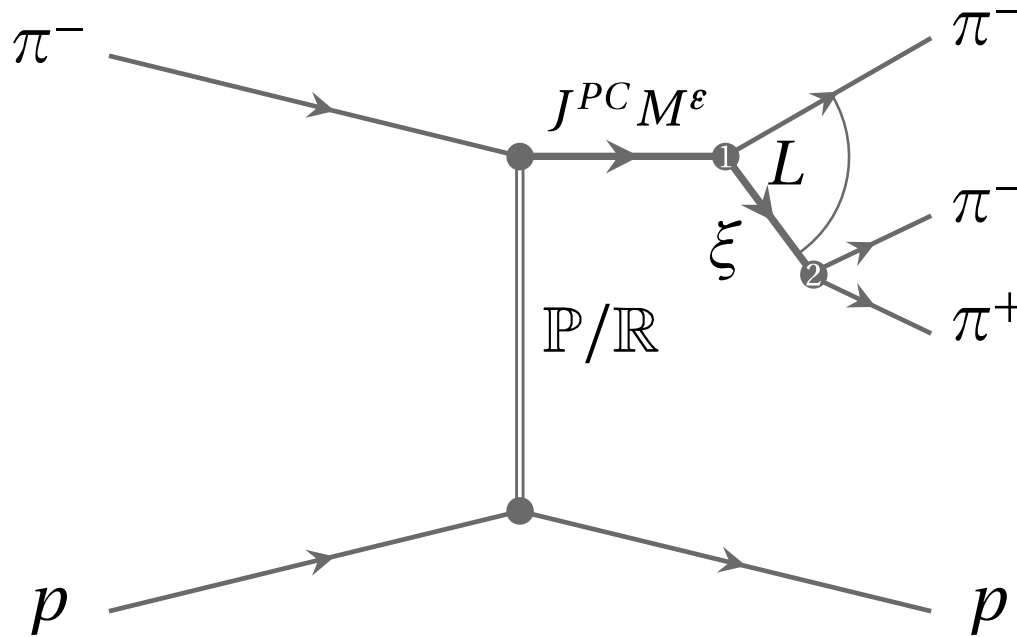
## Limits for light mesons

- many **missing/disputed** states in mass region  $m \sim 2 \text{ GeV}/c^2$
- **Identification** of heavy states **difficult**
  - broad states
  - large number
  - overlap + mixing





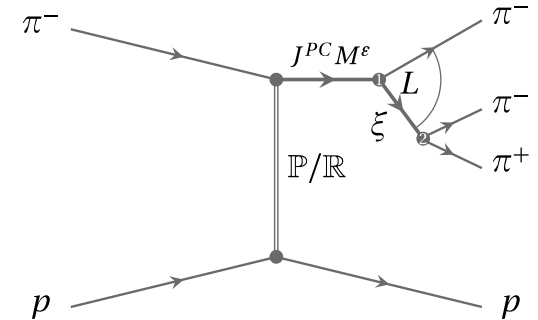
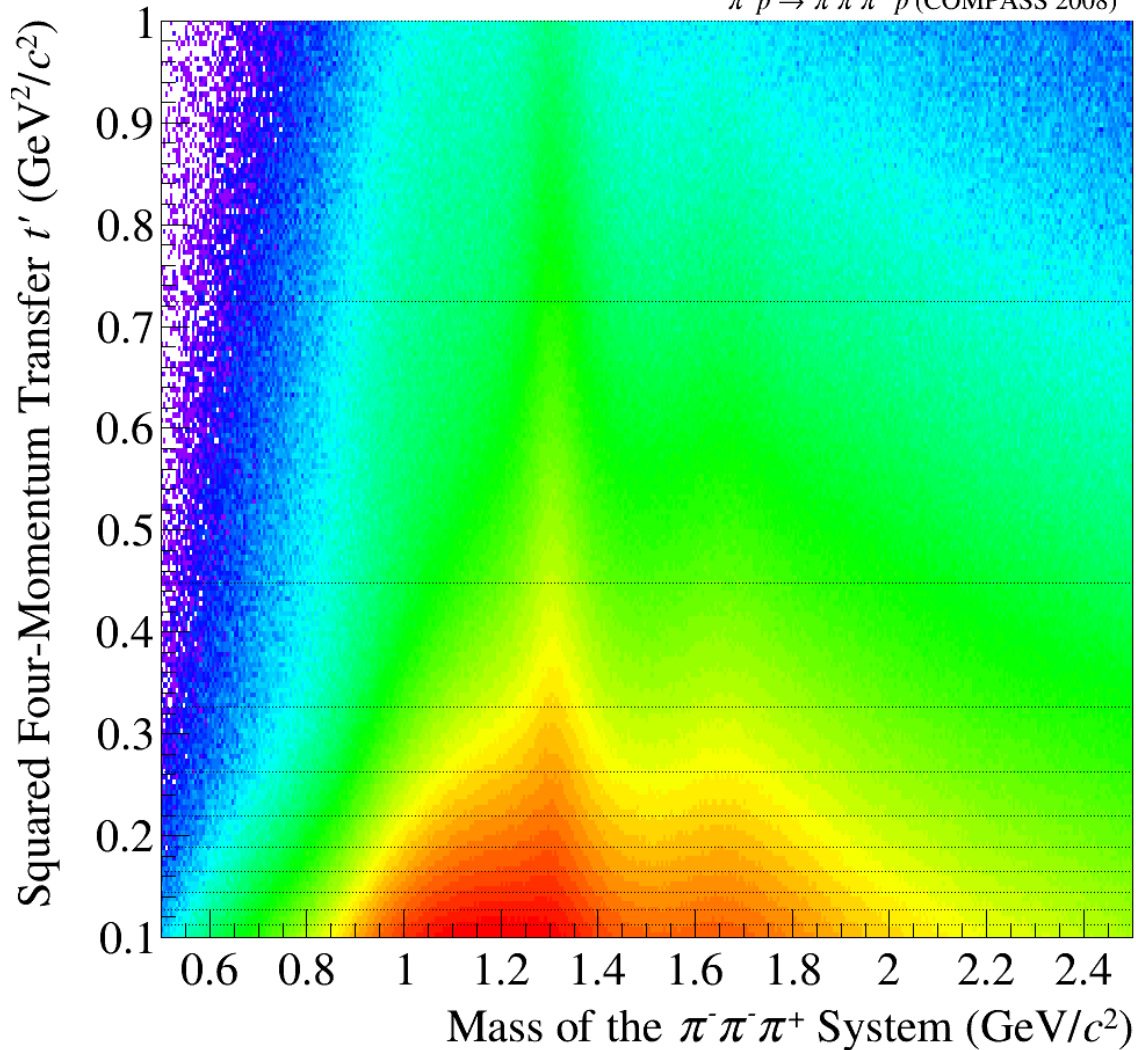
# Kinematics for today





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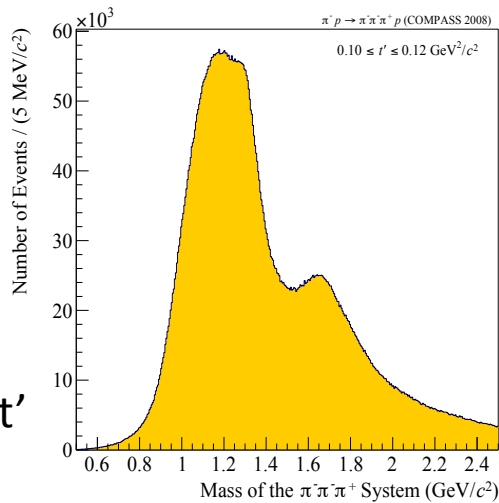
$\pi^- p \rightarrow \pi^- \pi^- \pi^+ p$  (COMPASS 2008)



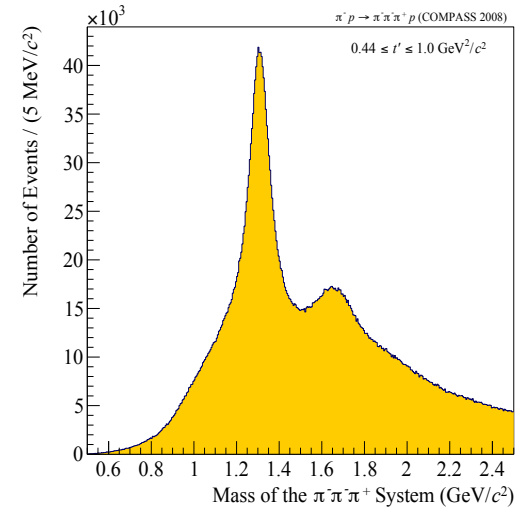
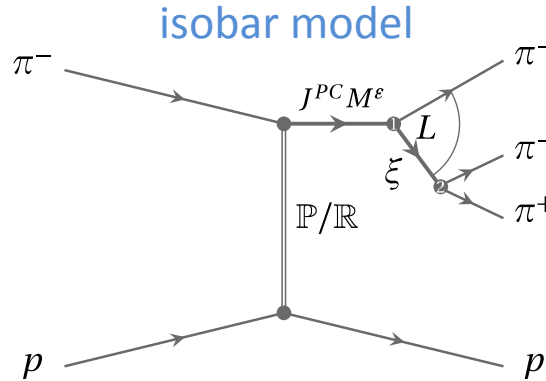
grid of  $t'$  used  
 $\Delta m: 20 \text{ MeV}/c^2$



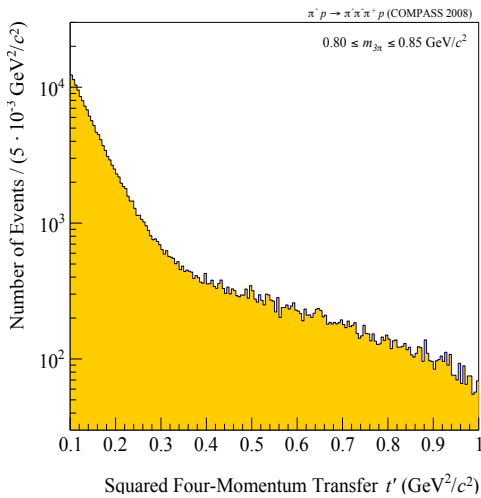
# Kinematics and Isobars



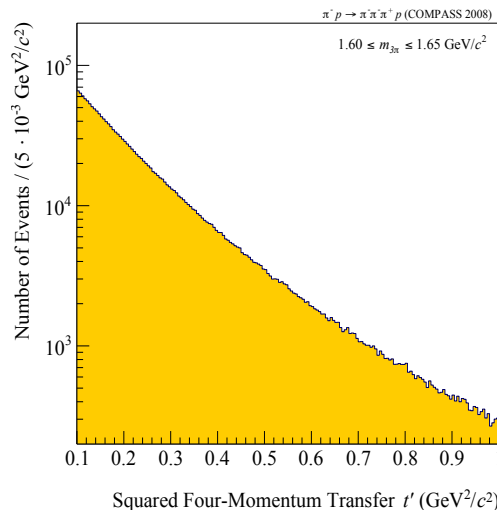
low  $t'$



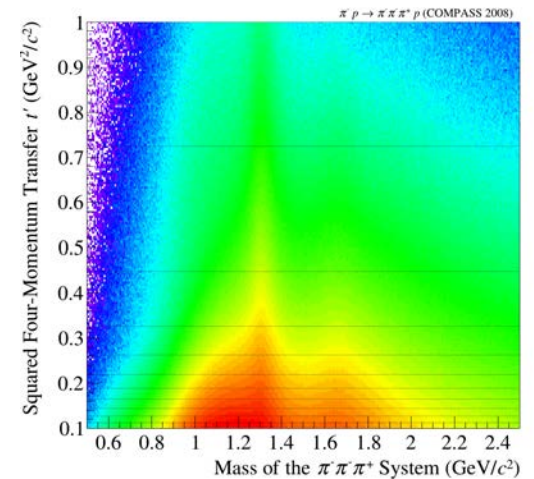
high  $t'$



$0.8 < m_{3\pi} < 0.85$



$1.6 < m_{3\pi} < 1.65$



grid of  $t'$  used

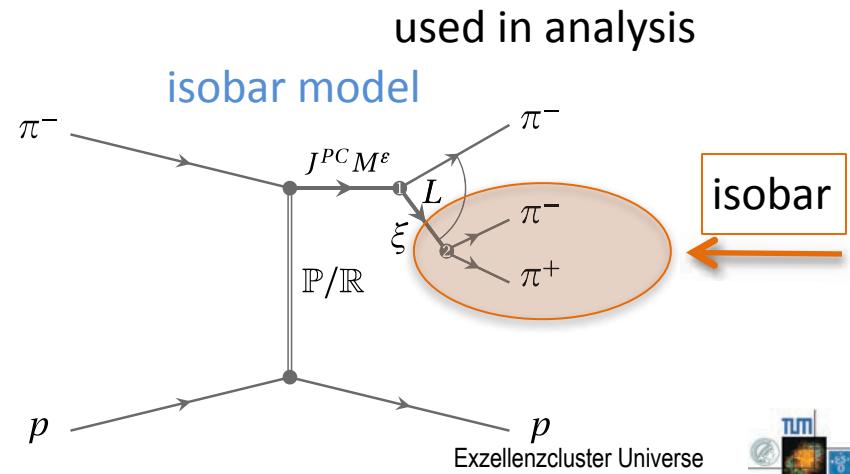
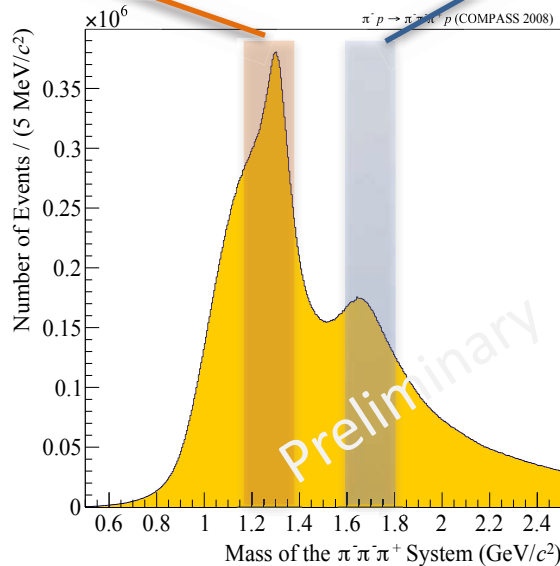
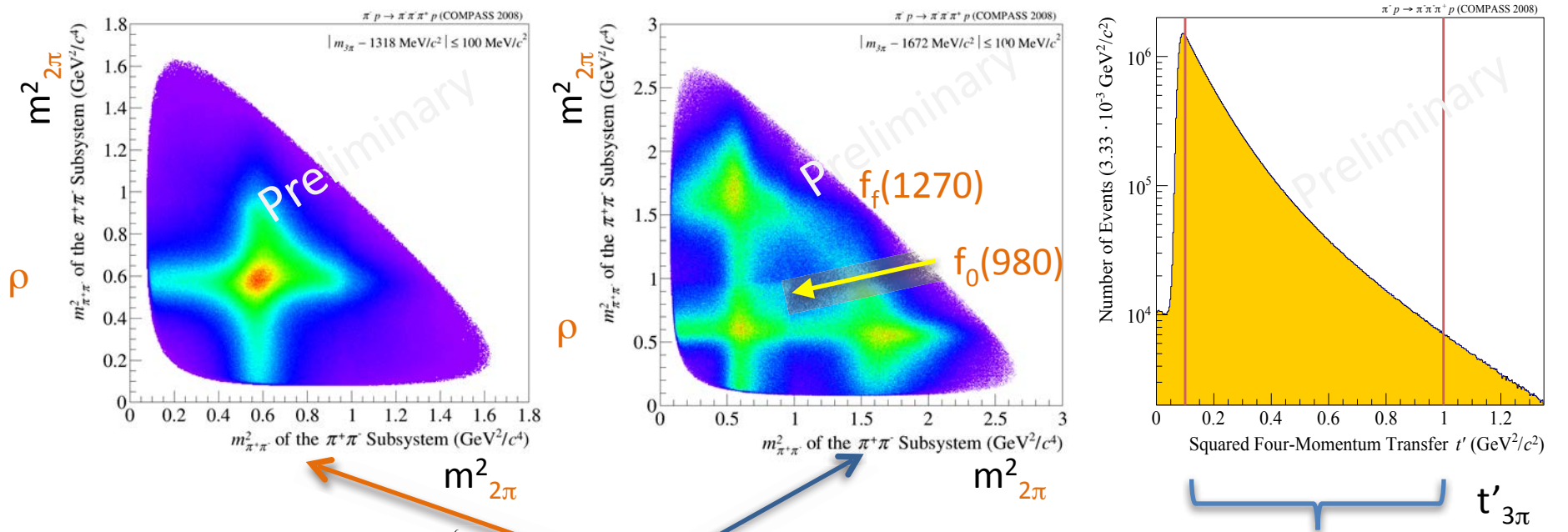
$\Delta m: 20 \text{ MeV}/c^2$   
 Exzellenzcluster Universe





# First Impressions

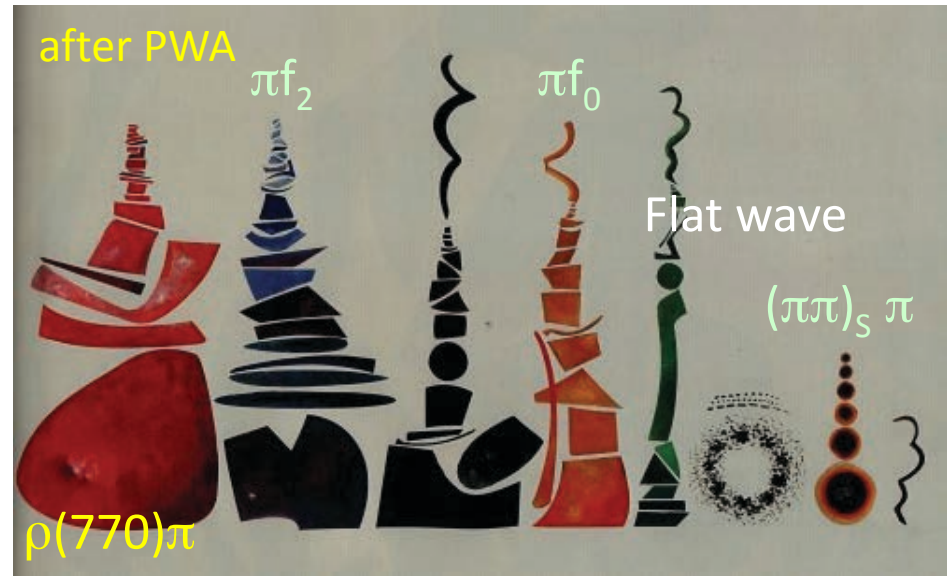
## Motivation for Isobar Model





# Partial wave analysis

inspired by M. Pennington





# Partial wave analysis

What is PWA ?

Describe population in 5-dimensional phase space in  $\pi\pi\pi$  by model

step 1

- Define a set of quantum numbers  $J^{PC}$
- Define a set of possible decay channels for each  $J^{PC}$   
 ( $X^- \rightarrow \text{isobar} + \pi; \text{isobar} \rightarrow \pi\pi$ ) : waves (waves used)
  - each such “wave” has a pre-determined population in phase space
  - each wave may have angular momentum  $J$  described by quantum number  $M$
- For each bin of 20 MeV/c<sup>2</sup> mass of  $\pi\pi\pi$ : determine which coherent combination of waves fits distribution best
- Obtain spin-density matrix

Mass independent fit

step 2

- Describe spin density matrix (submatrix), by model containing resonances and non-resonant contributions connecting all mass bins
- Determine resonance parameters

Mass dependent fit

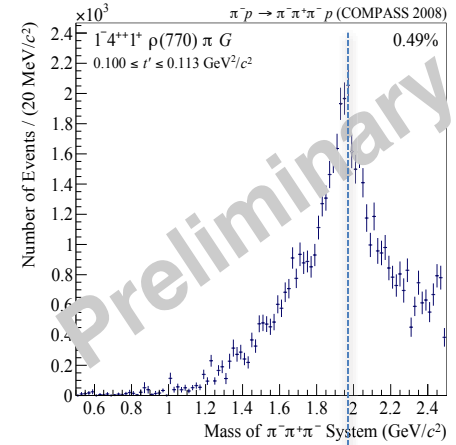
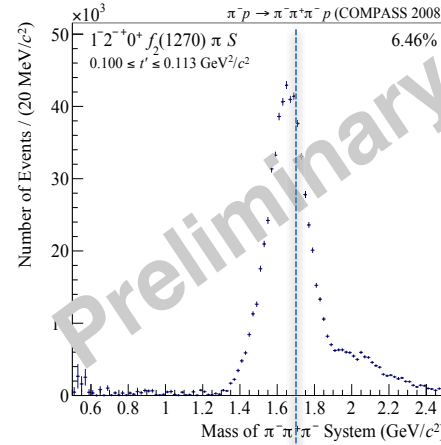
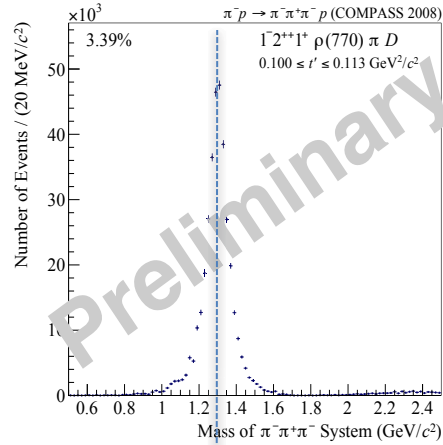
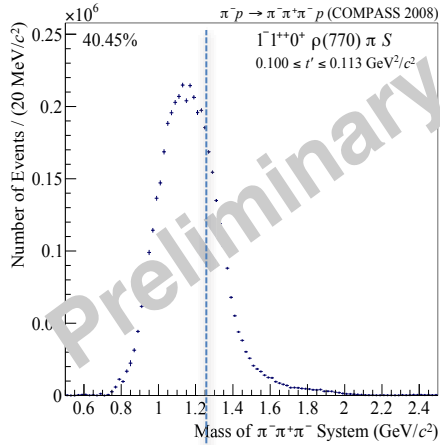




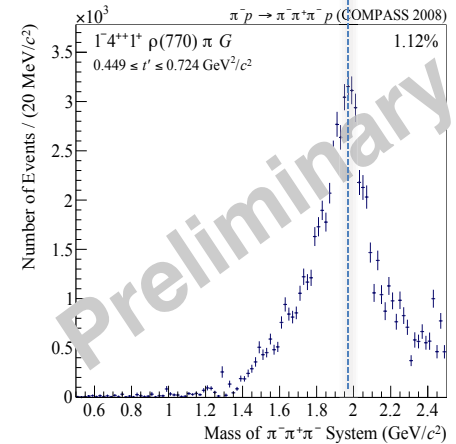
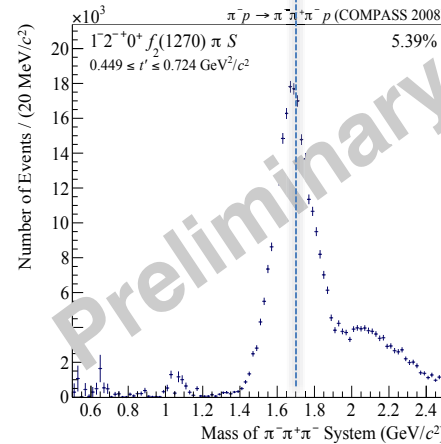
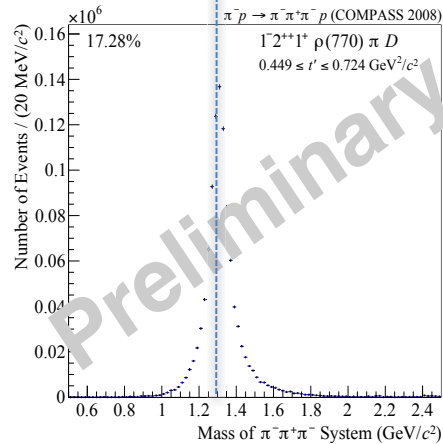
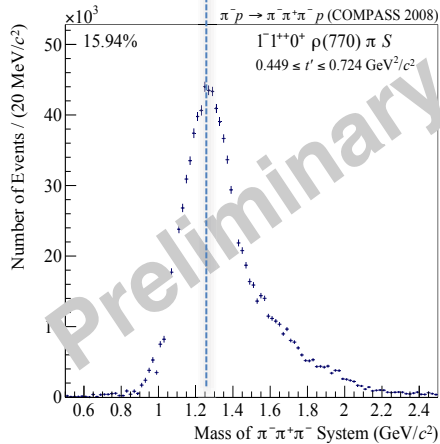


# t dependence of mass distributions

low t



high t



$1^{++}0^+ \rho \pi S$

$2^{++}1^+ \rho \pi D$

$2^{-+}0^+ f_2 \pi S$

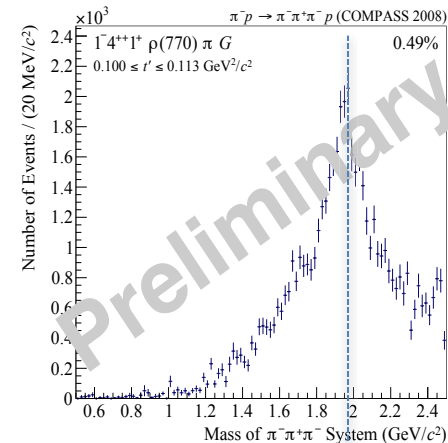
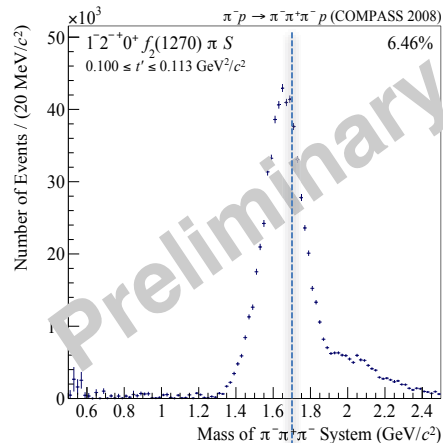
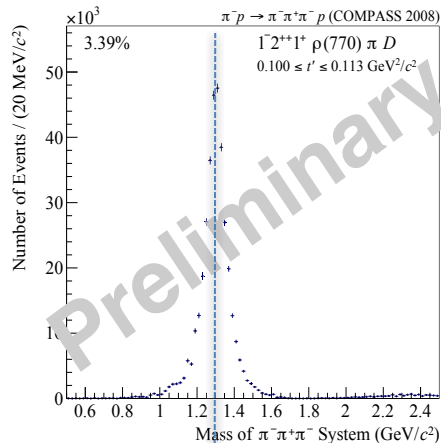
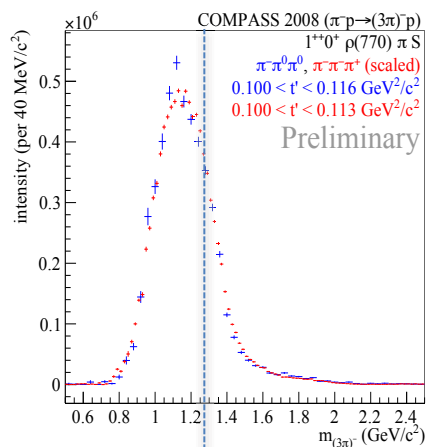
$4^{++}1^+ \rho \pi G$



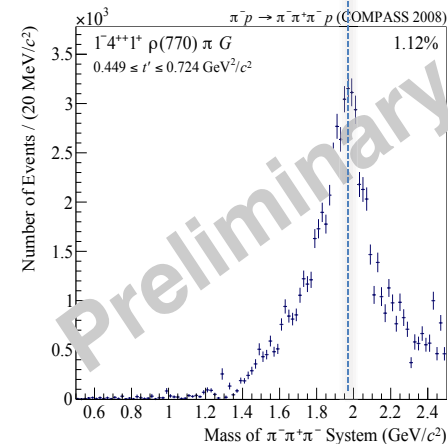
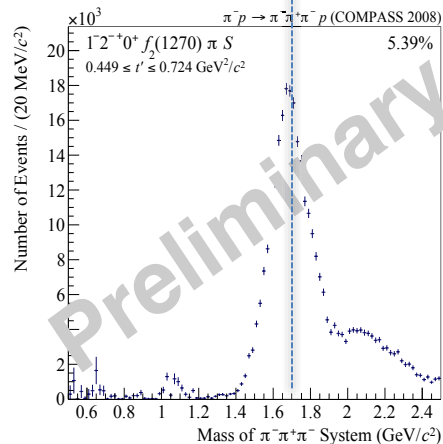
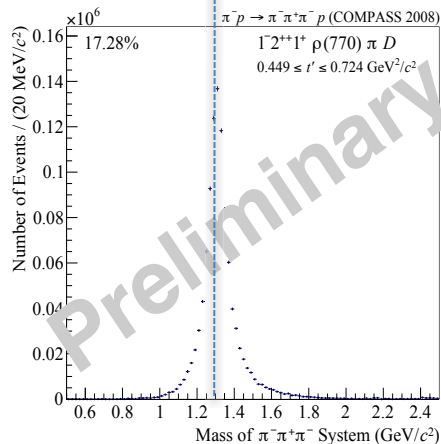
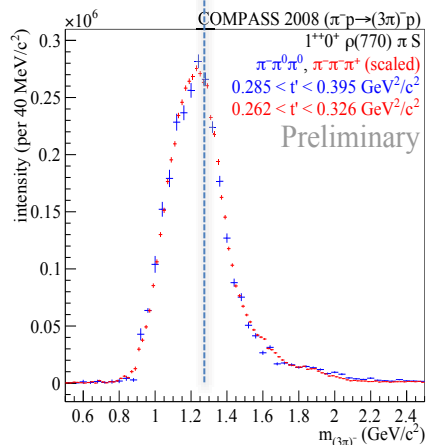


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$2^{++}1^+ \rho \pi D$

$2^{-+}0^+ f_2 \pi S$

$4^{++}1^+ \rho \pi G$



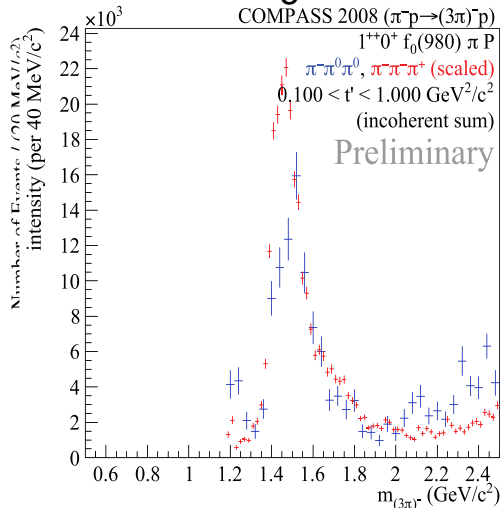
# More exotic families



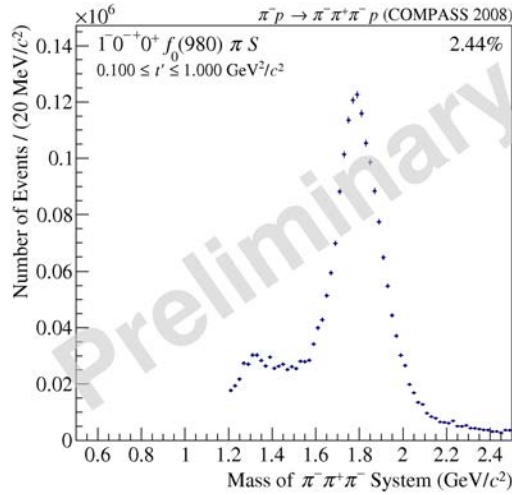


# Waves involving $f_0(980)$

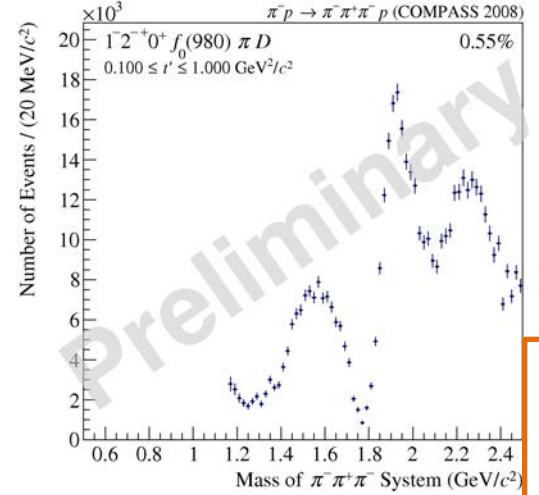
## $1^{++}0^+ f_0(980) \pi P$



## $0^{-+}0^+ f_0(980) \pi S$



## $2^{-+}0^+ f_0(980) \pi D$



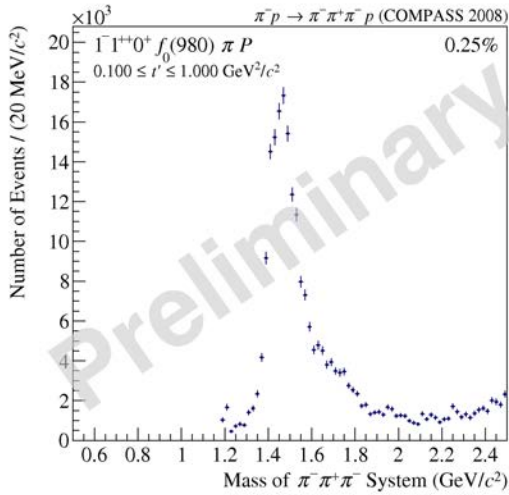
experts only

$\pi^- \pi^+ \pi^-$  and  $\pi^- \pi^0 \pi^0$

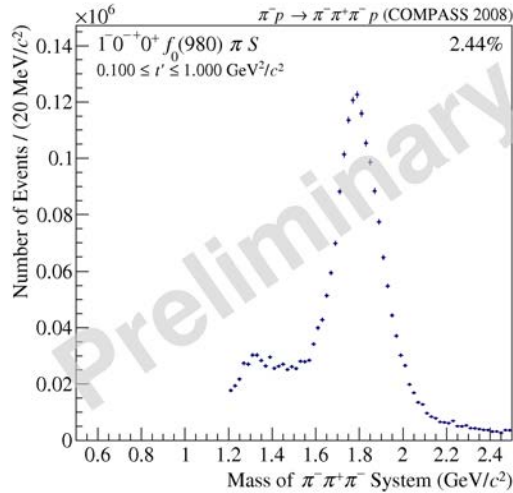


# Waves involving $f_0(980)$

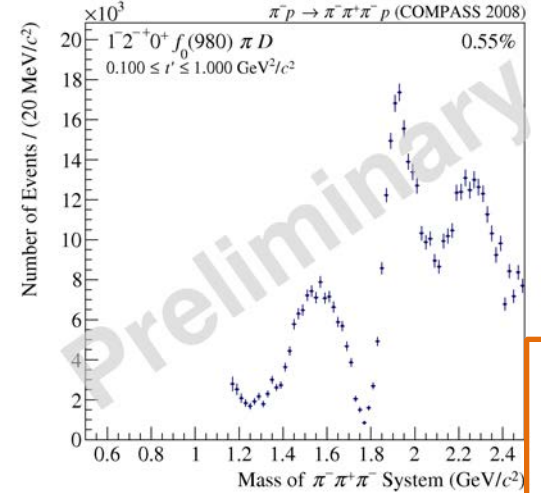
$1^{++}0^+ f_0(980) \pi P$



$0^{-+}0^+ f_0(980) \pi S$



$2^{-+}0^+ f_0(980) \pi D$



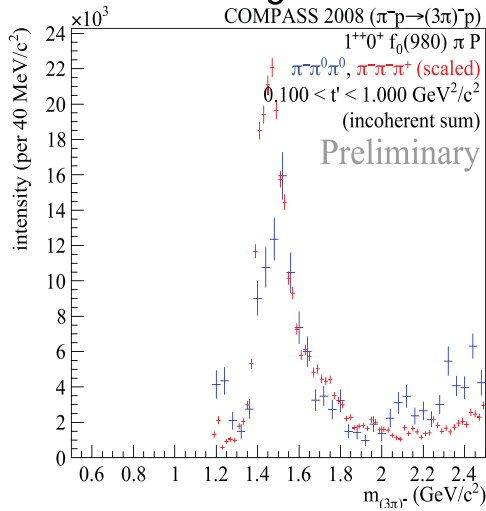
experts only

$\pi^- \pi^+ \pi^-$  and  $\pi^- \pi^0 \pi^0$

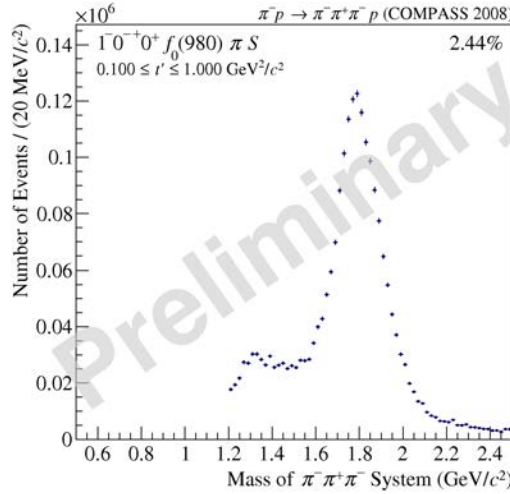


# Waves involving $[\pi\pi]_S$

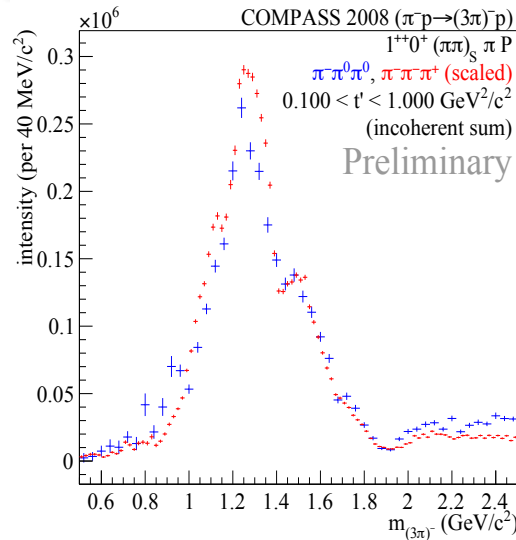
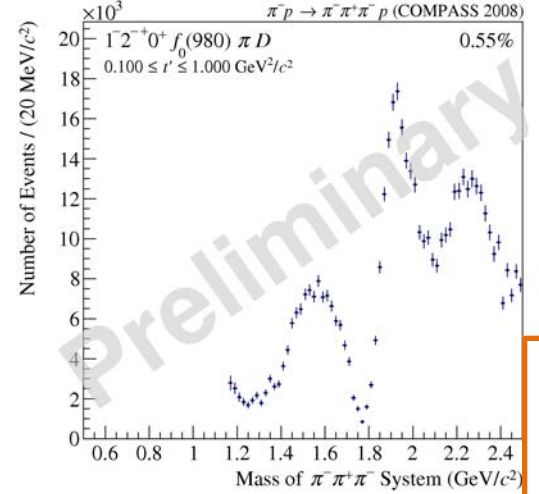
$1^{++}0^+ f_0(980) \pi P$



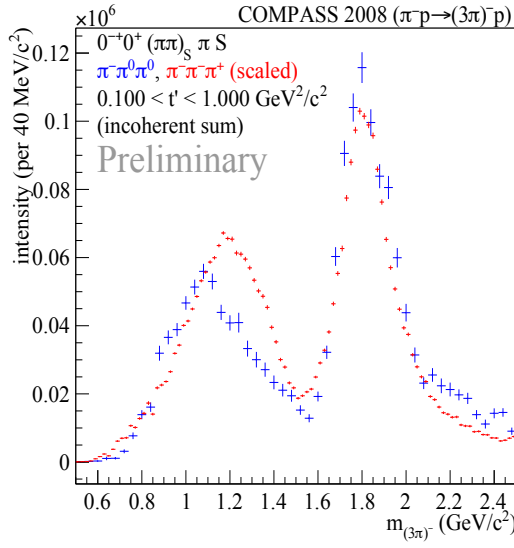
$0^{-+}0^+ f_0(980) \pi S$



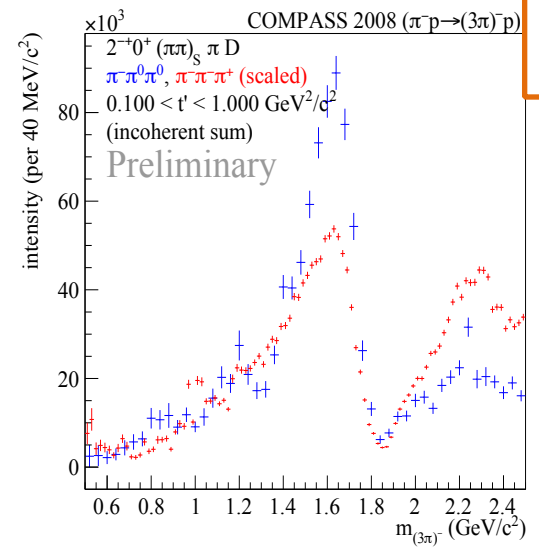
$2^{-+}0^+ f_0(980) \pi D$



$1^{++}0^+ [\pi\pi]_S \pi P$



$0^{-+}0^+ [\pi\pi]_S \pi S$



$2^{-+}0^+ [\pi\pi]_S \pi D$

experts only

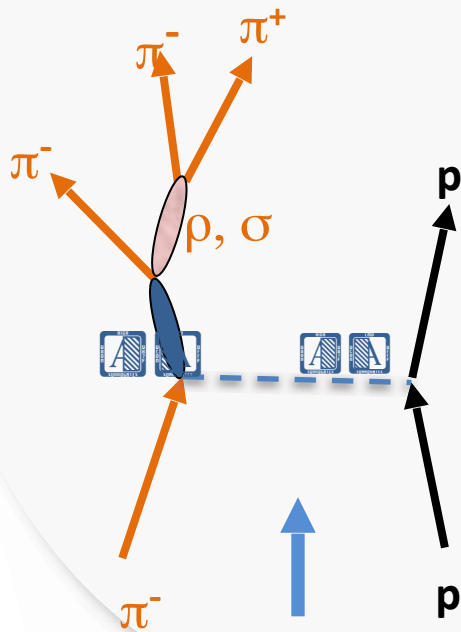
$\pi^- \pi^+ \pi^-$  and  $\pi^- \pi^0 \pi^0$

# Model for Spin Density Matrix

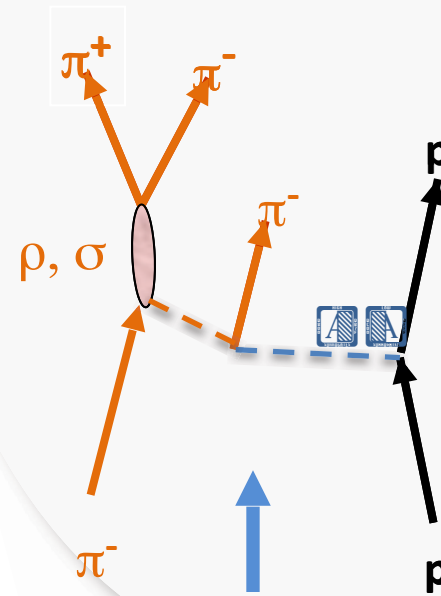
Describe the results obtained independently in different mass bins by a model

- select physics contributions
- fit to spin density matrix (not only to simple mass spectra)

## Resonance



## Deck



Two types of contributions



# Mass-dependent fit (simple)

Use only lowest  $M = 0, 1$  waves (so far)

This work: 4 waves

Model:

experts only

$2^{++} \quad 1^+ \rho \pi D$

$4^{++} \quad 1^+ \rho \pi G$

$1^{++} \quad 0^+ f_0(980) \pi P$

$J^{PC} M^\epsilon [isobar] \pi L$

2 resonances :  $a_2(1320)$  and  $a_2'$  + non resonant term

1 resonance :  $a_4(2040)$  + non resonant term

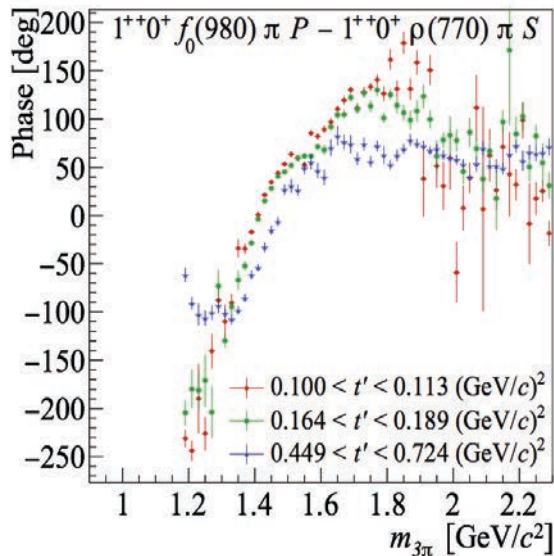
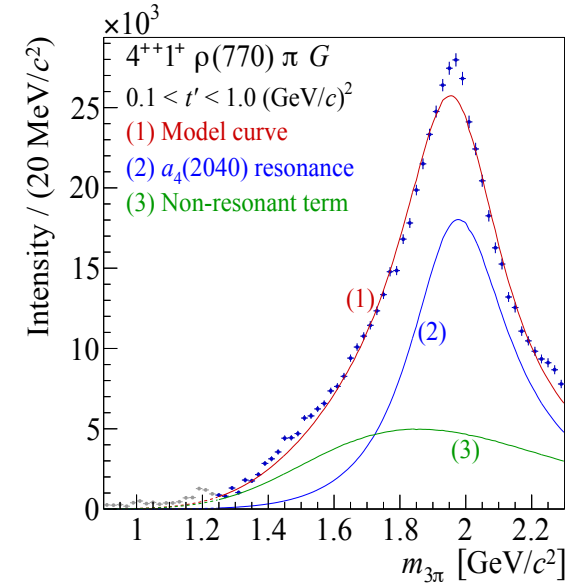
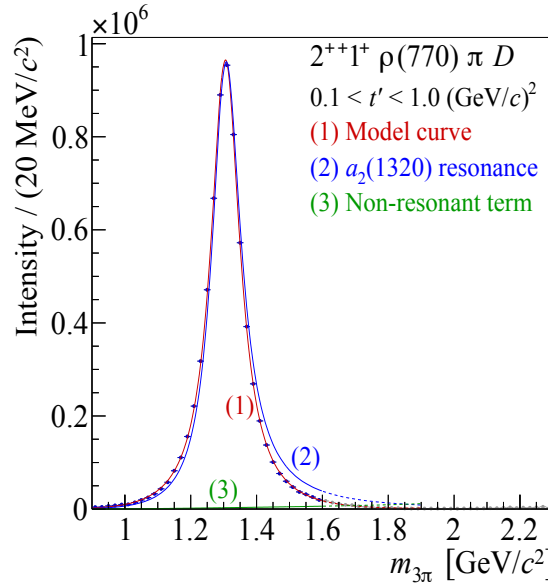
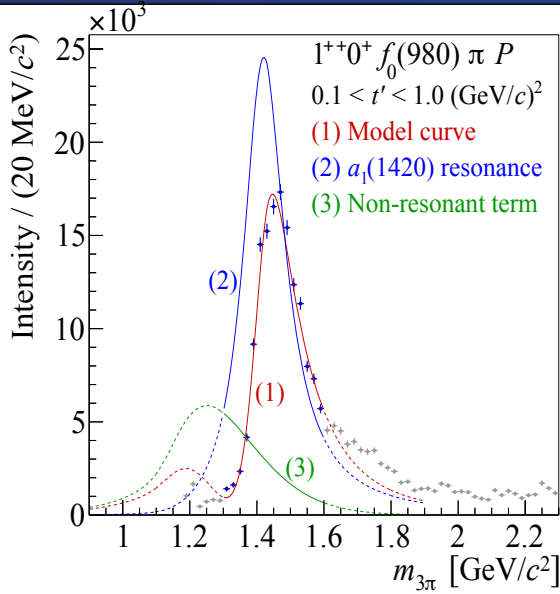
1 resonance :  $a_1(1420)$  + non resonant term

- 133 free parameters
- fix BW resonance parameter for all 11 bins of  $t'$



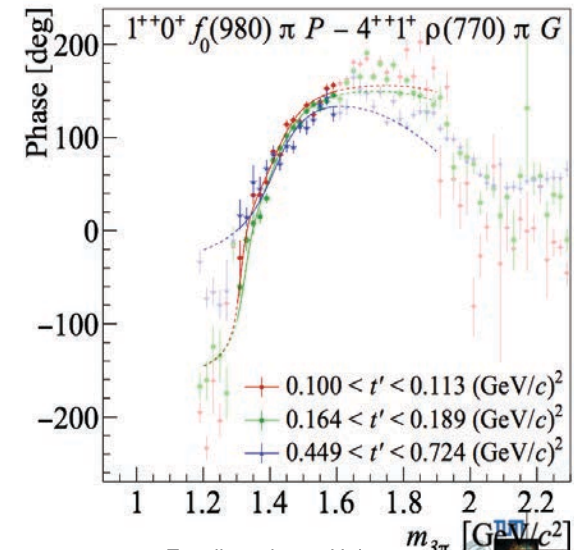


# New Observation: $a_1(1420)$



## Observation:

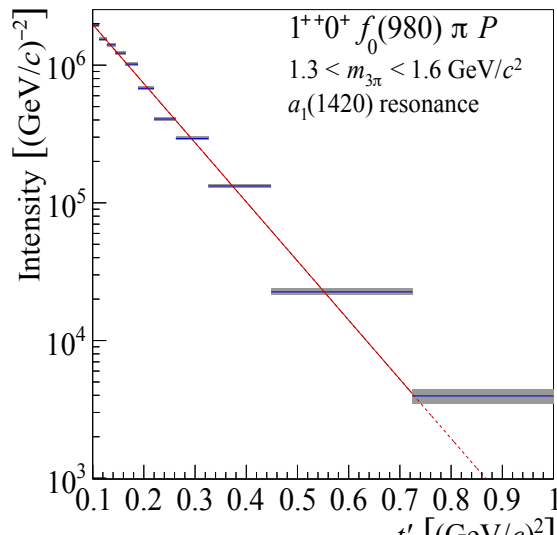
- Decay only :  $[f_0(980)] \pi P$
- Mass :  $1413 \pm 15 \pm 13 \text{ MeV}/c^2$
- Width:  $157 \pm 8 \pm 23 \text{ MeV}/c^2$





# $a_1(1420)$ and Production

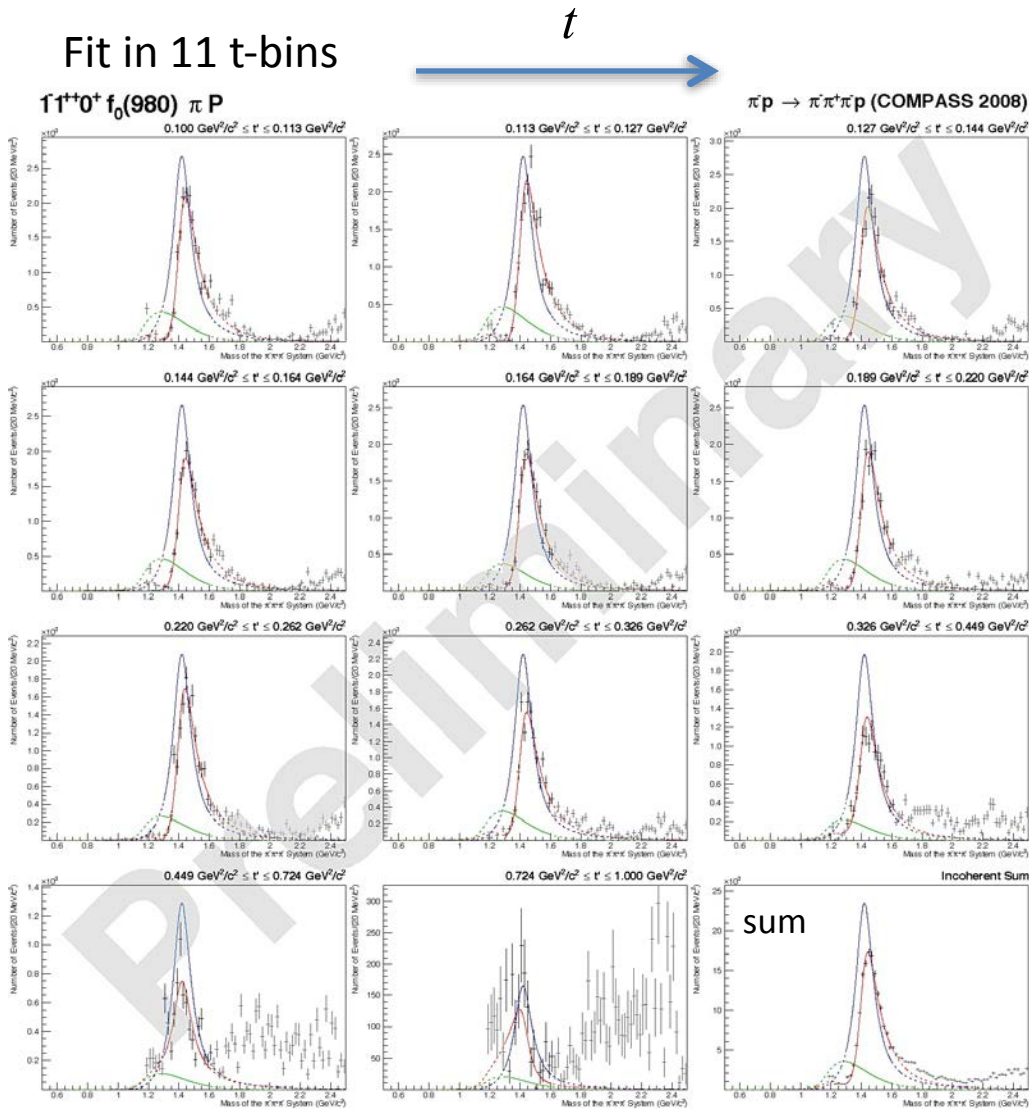
- Various explanations proposed for interpretation:
  - Dynamics
    - Interference of  $a_1(1260)$  with Deck amplitude ( $\Delta\phi = 180^\circ$  shifted by 100 MeV)
    - triangular anomaly coupling  $a_1(1260) \rightarrow KK^* \rightarrow KK\pi$  and  $KK \leftrightarrow f_0(980)$  ( $\Delta\phi = 90^\circ$ ) (see talk Mikhasenko)
    - Requires same  $t'$  dependence for  $a_1(1260)$  and  $a_1(1420)$
  - Molecular structure
    - Partner of  $f_1(1420)$



- At present: slope difference  $\Delta b$  is 2 units
- Uncertainty in extraction of resonance in  $1^{++} \rho\pi$  S-wave gives uncertainty for  $b_{a_1(1260)}$



# Mass dependent fits $a_1(1420)$



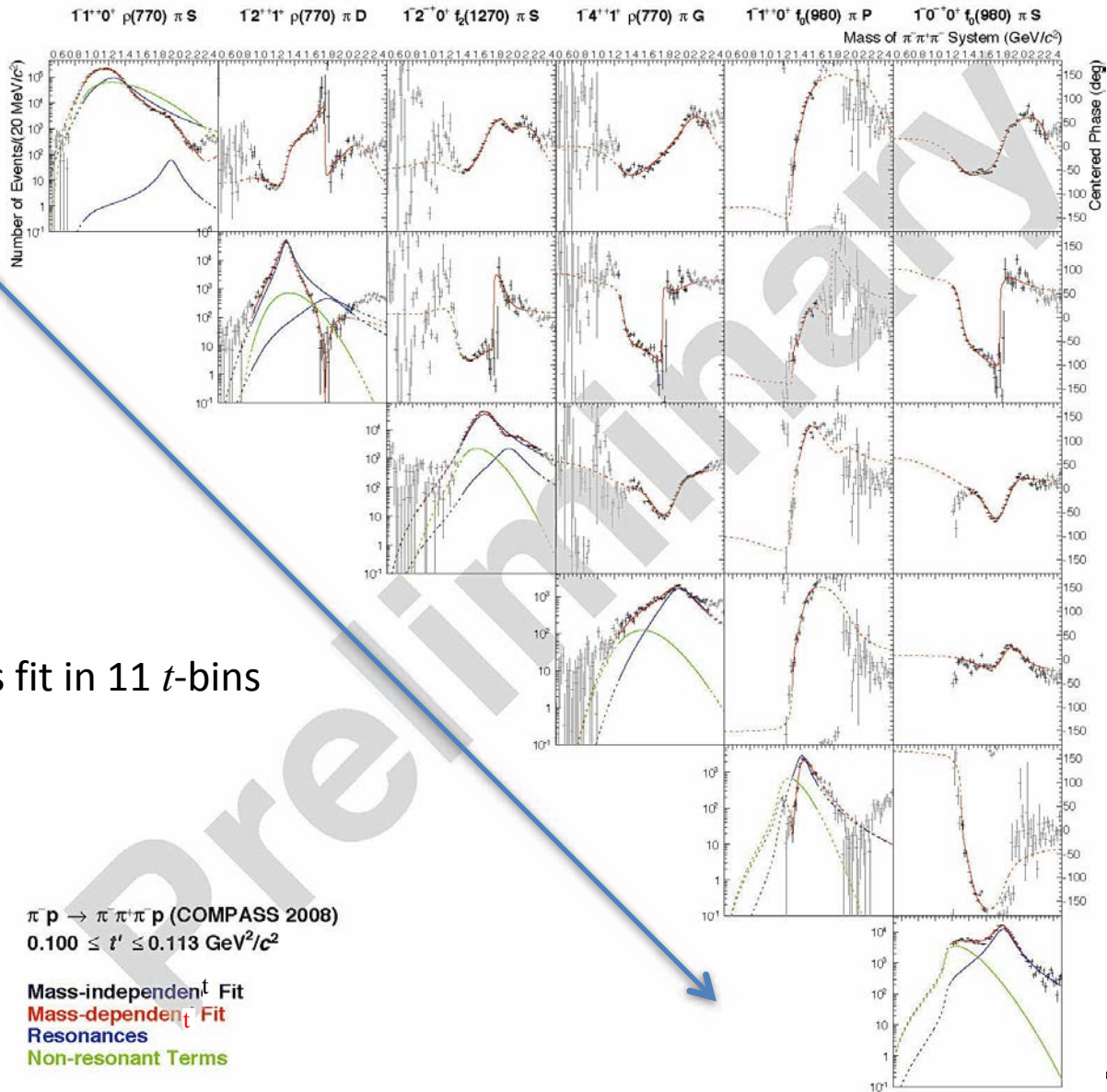
$1^{++}0^+ f_0(980) \pi P$



**NEW**



# COMPASS "Holography"



Reference waves

Interferometry

simultaneous fit in 11  $t$ -bins

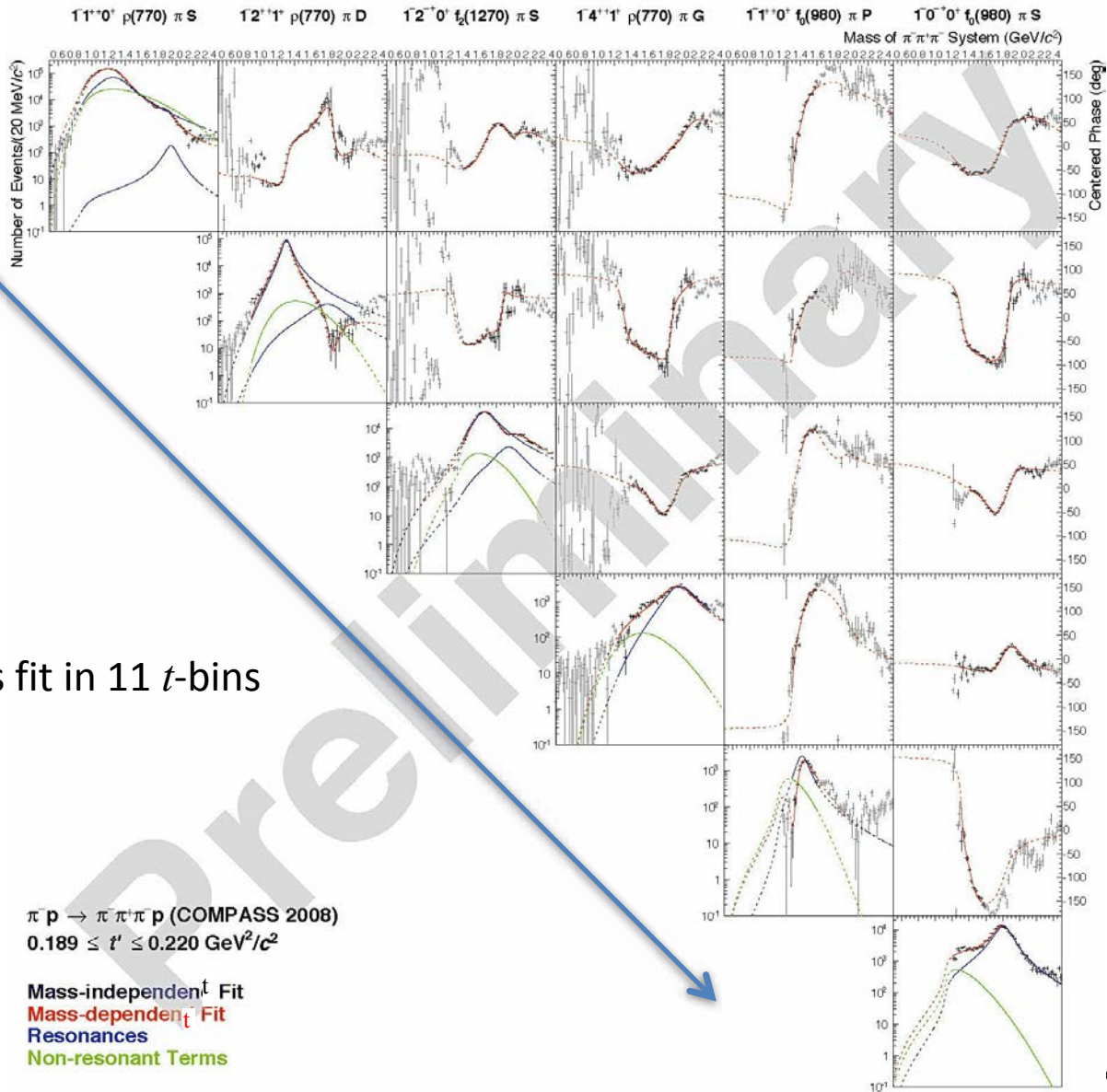
$\pi^+ p \rightarrow \pi^+ \pi^+ \pi^- p$  (COMPASS 2008)  
 $0.100 \leq t' \leq 0.113 \text{ GeV}^2/c^2$

Mass-independent  $\dagger$  Fit  
 Mass-dependent  $\ddagger$  Fit  
 Resonances  
 Non-resonant Terms





# COMPASS "Holography"



Reference waves

Interferometry

simultaneous fit in 11  $t$ -bins

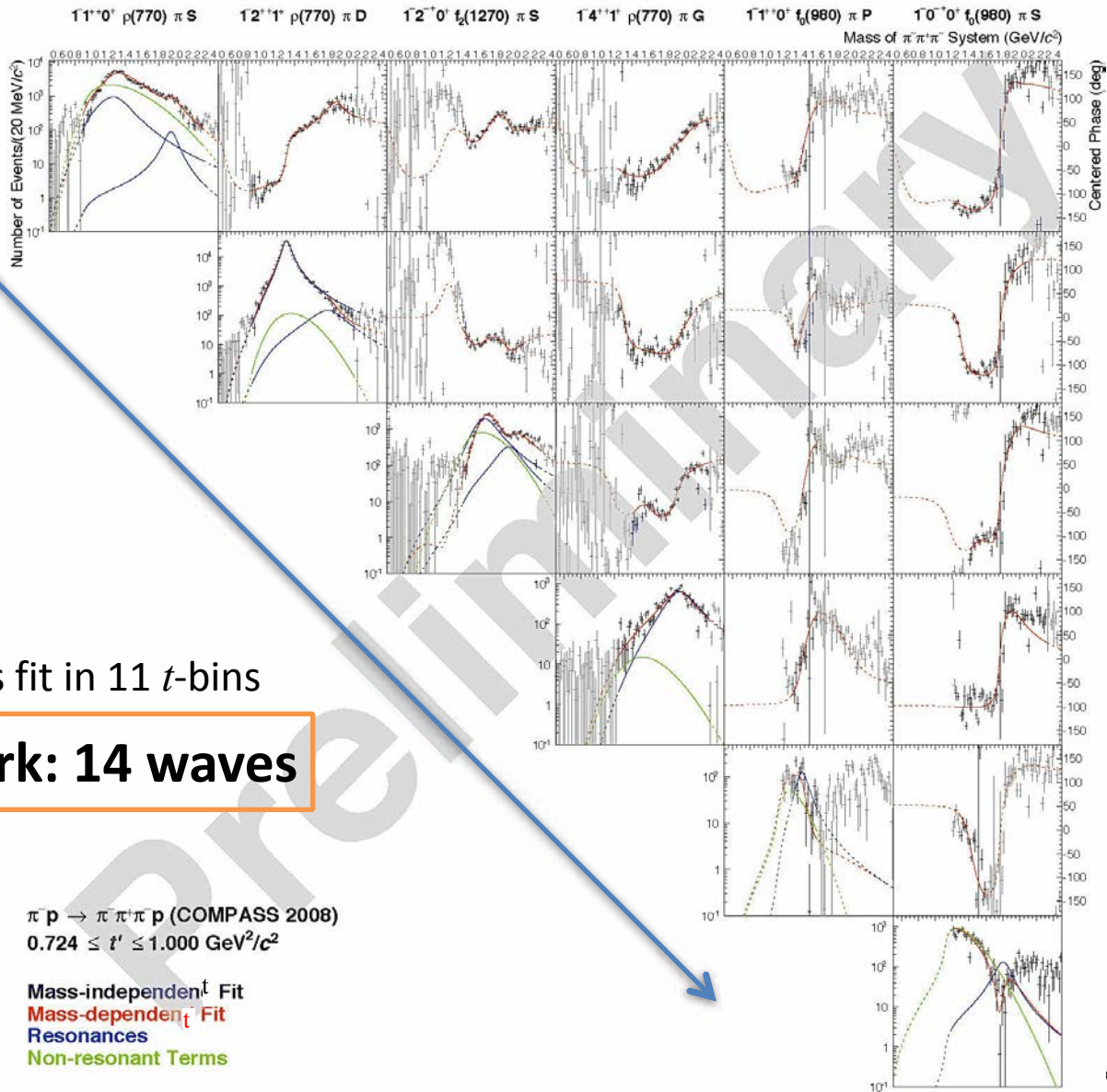
$\pi^+ p \rightarrow \pi^+ \pi^+ \pi^- p$  (COMPASS 2008)  
 $0.189 \leq t' \leq 0.220 \text{ GeV}^2/c^2$

Mass-independent  $t'$  Fit  
 Mass-dependent  $t'$  Fit  
 Resonances  
 Non-resonant Terms





# COMPASS "Holography"



Reference waves

Interferometry

simultaneous fit in 11  $t$ -bins

latest work: 14 waves

$\pi^+ p \rightarrow \pi^+ \pi^+ \pi^- p$  (COMPASS 2008)  
 $0.724 \leq t' \leq 1.000 \text{ GeV}^2/c^2$

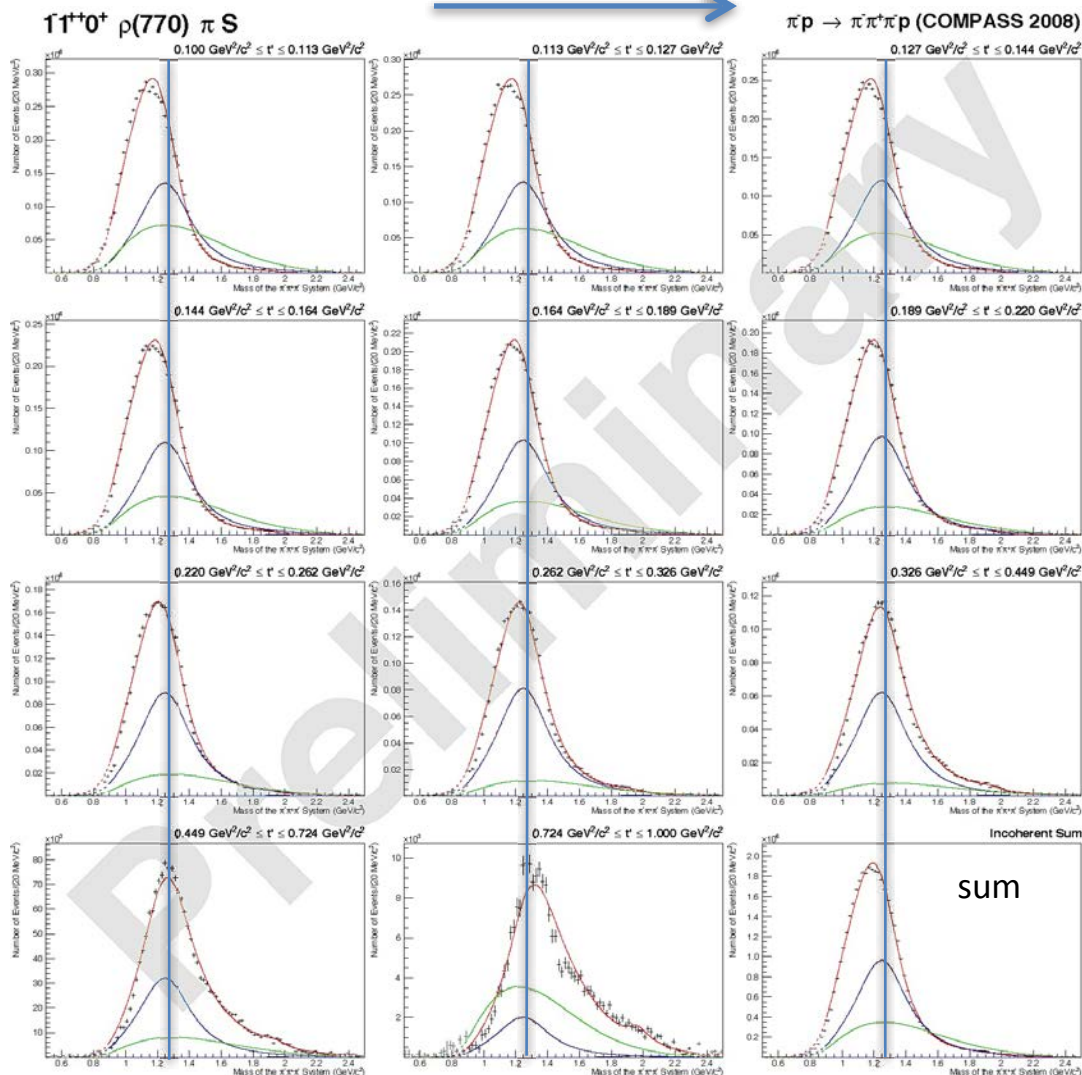
Mass-independent  $t'$  Fit  
 Mass-dependent  $t'$  Fit  
 Resonances  
 Non-resonant Terms



# Mass dependent fits

Fit in 11 t-bins

$t$



Strongly t-dependent spectral shape around  $a_1(1260)$

$1^{++}0^+ \rho \pi S$

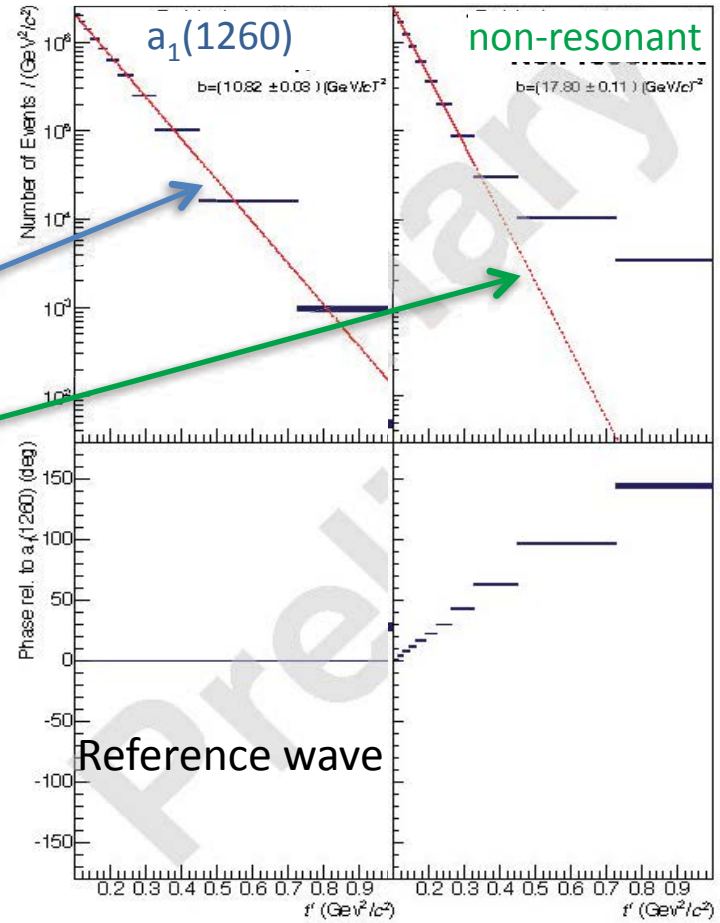
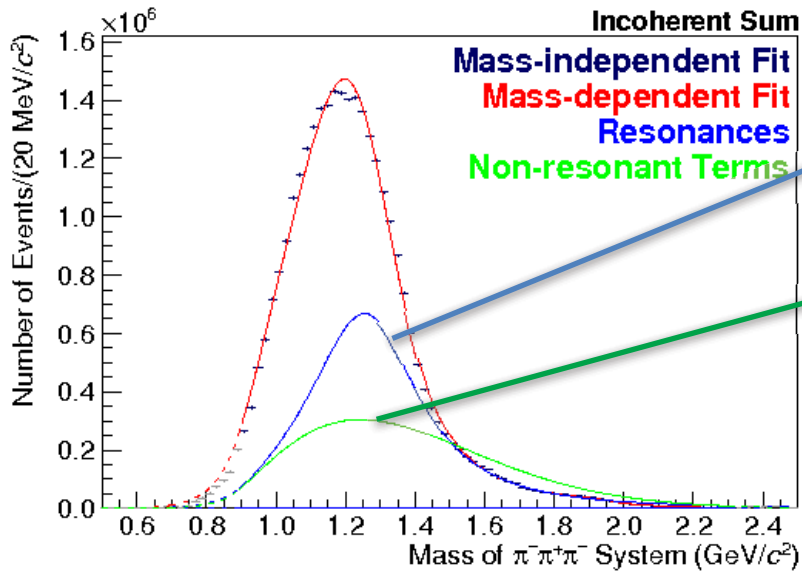
$J^{PC} M^\epsilon [isobar] \pi L$

$t$



# Example for $t$ -dependence

$\pi\pi\pi$  COMPASS 2008



Intensities

Phases

$$1^{++}0^+\rho\pi S$$

$$J^PC M^\epsilon [\textit{isobar}] \pi L$$

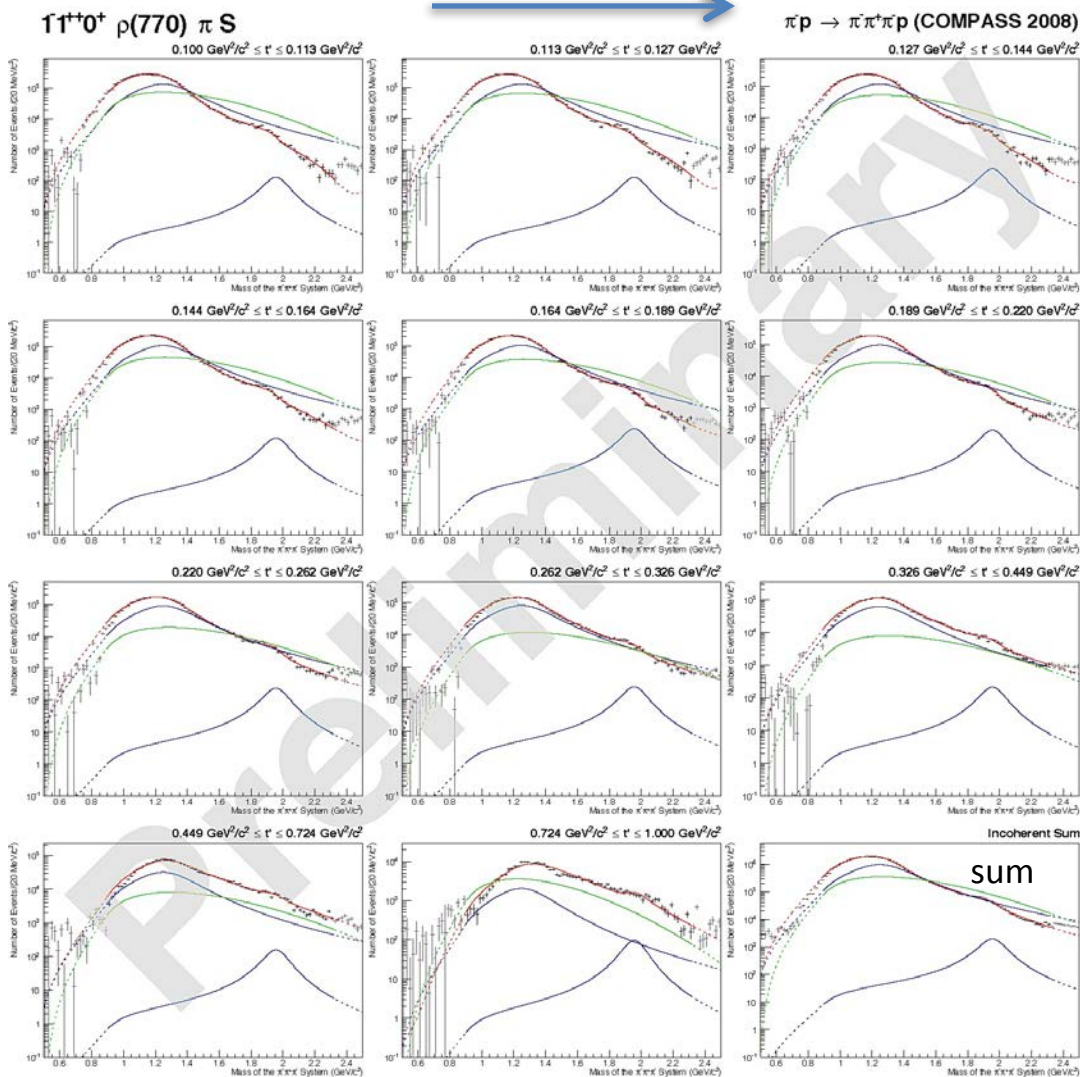




# Mass dependent fits

Fit in 11 t-bins

$t$



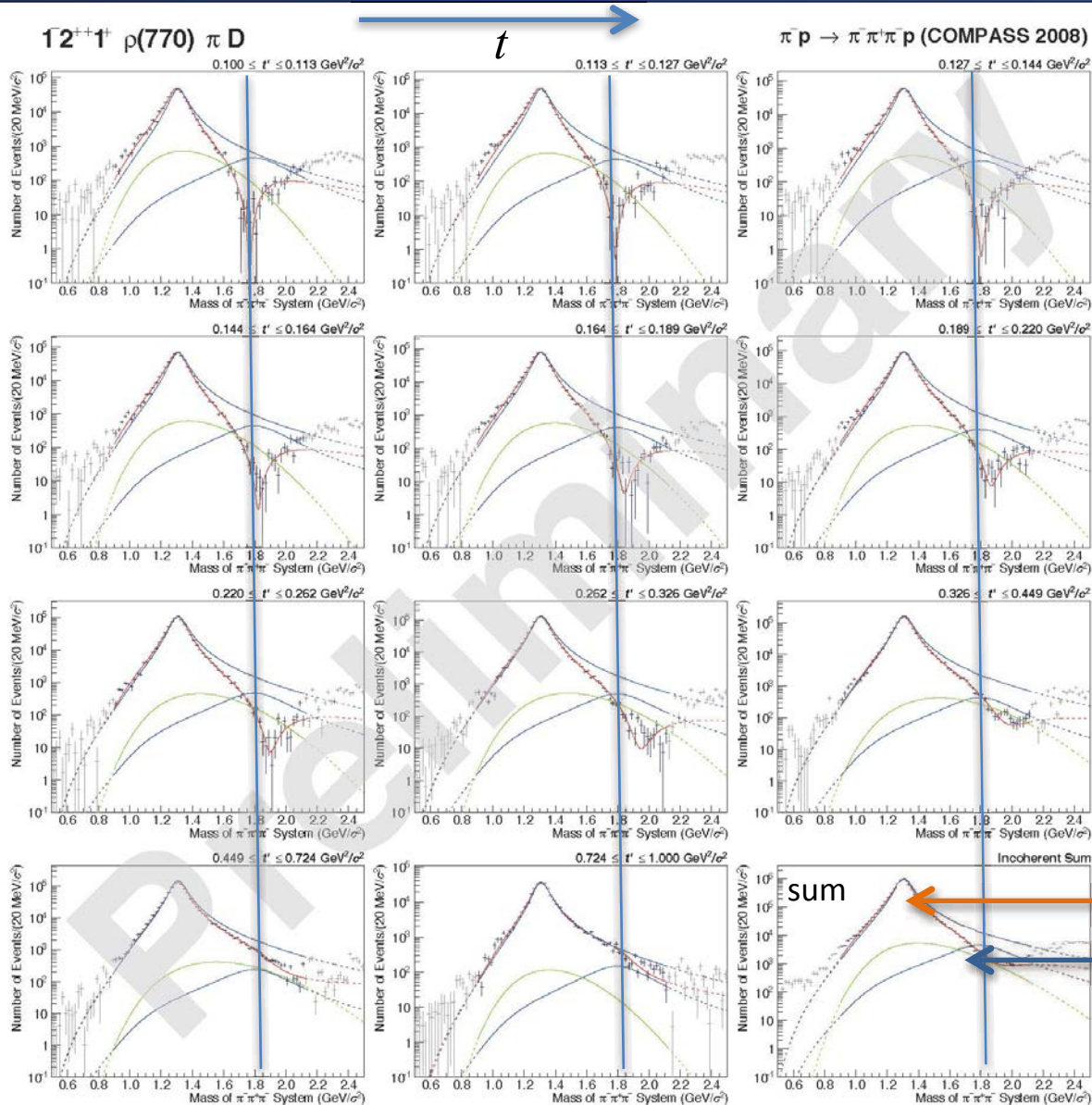
Second high-mass  $a_1'$  resonance visible

$1^{++}0^+ \rho \pi S$

$t$



# Mass dependent fits $a_2(1320)$



Strongly  $t$ -dependent interference effects  
 high-mass  $a_2'$



$a_2(1320)$   
 $a_2'$





# What about the building blocks

- We have solved a puzzle – but were the building blocks correct ?



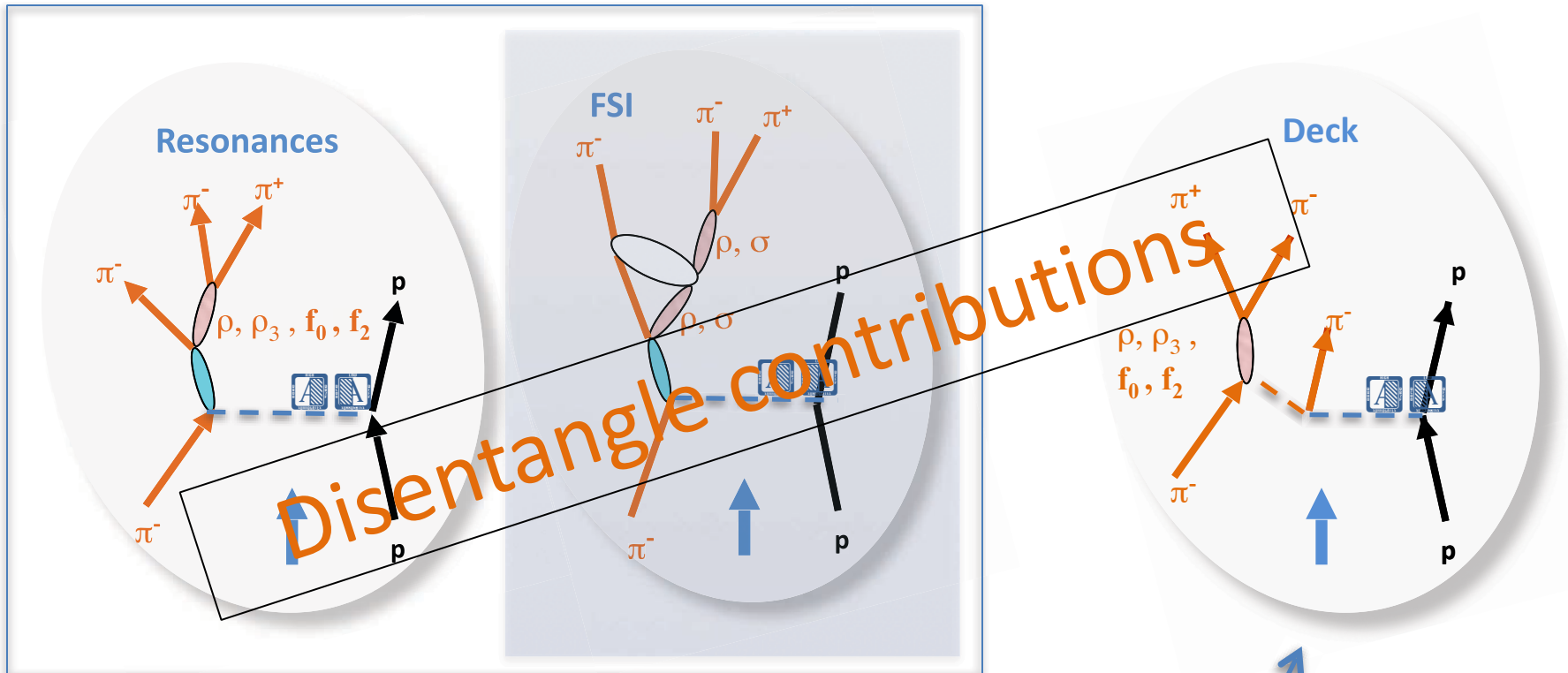


# What about the building blocks

- We have solved a puzzle – but were the building blocks correct ?



# New Paths to Meson Decays



- Select  $J^{PC}$  via PWA
- For each  $J^{PC}$  and mass-bin in  $3\pi$  :
  - determine composition and shapes of  $2\pi$  isobars
  - complex couplings
  - non-resonant contributions (via  $t$ -dependence)



# Isobars: $[\pi\pi]_S^*$

Phys. Rev. D35 1633, Au, Morgan, Pennington

continuum -  $[\pi\pi]_S$

$f_0(980)$

fixed functional form – variable intensity/phase (2 parameters)



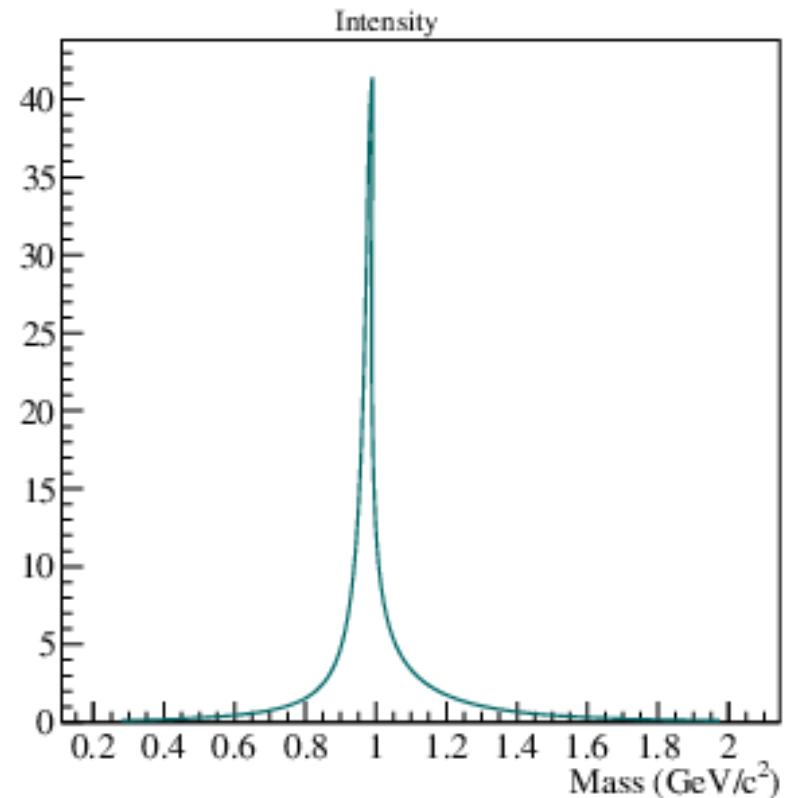
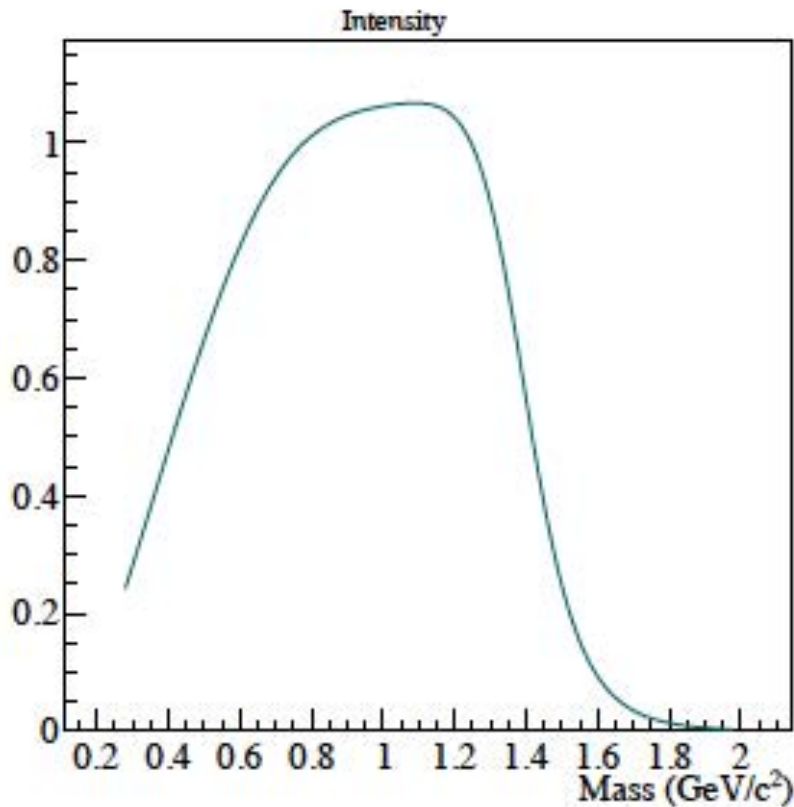
# Isobars: $[\pi\pi]^*_S$

Phys. Rev. D35 1633, Au, Morgan, Pennington

continuum -  $[\pi\pi]_S$

$f_0(980)$

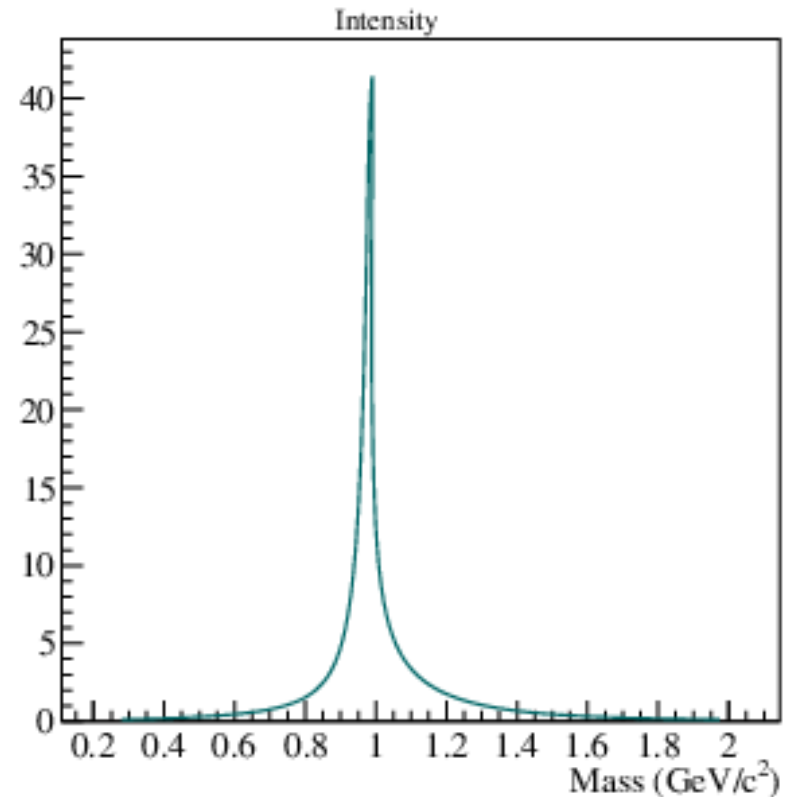
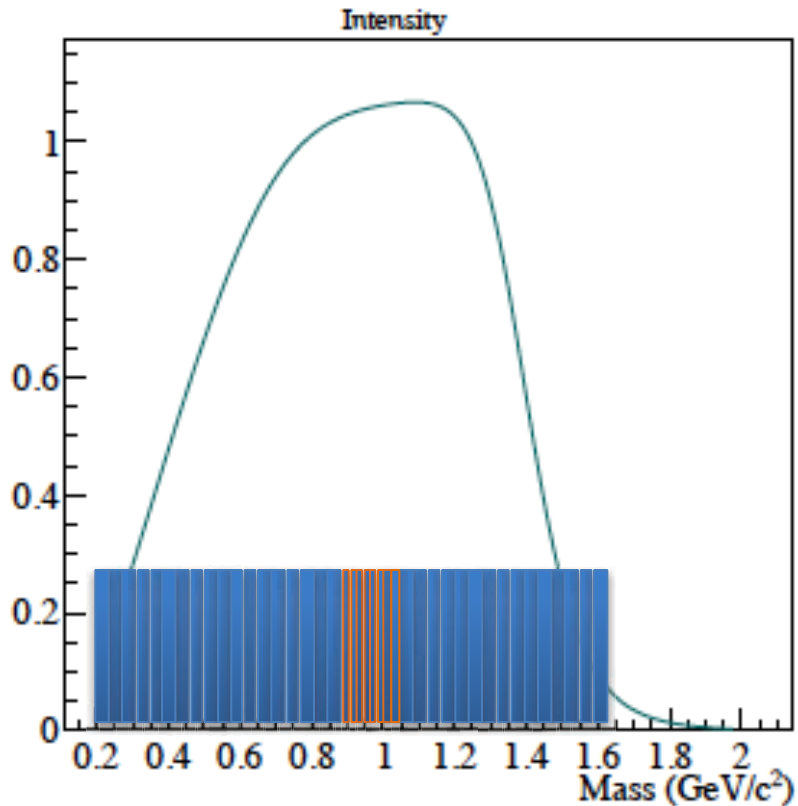
fixed functional form – variable intensity/phase (2 parameters)





# Isobars: $[\pi\pi]^*_S$

replaced by ONE  $[\pi\pi]^*_S$  histogram with n-bins  
( $2n$  parameters determined by fit)

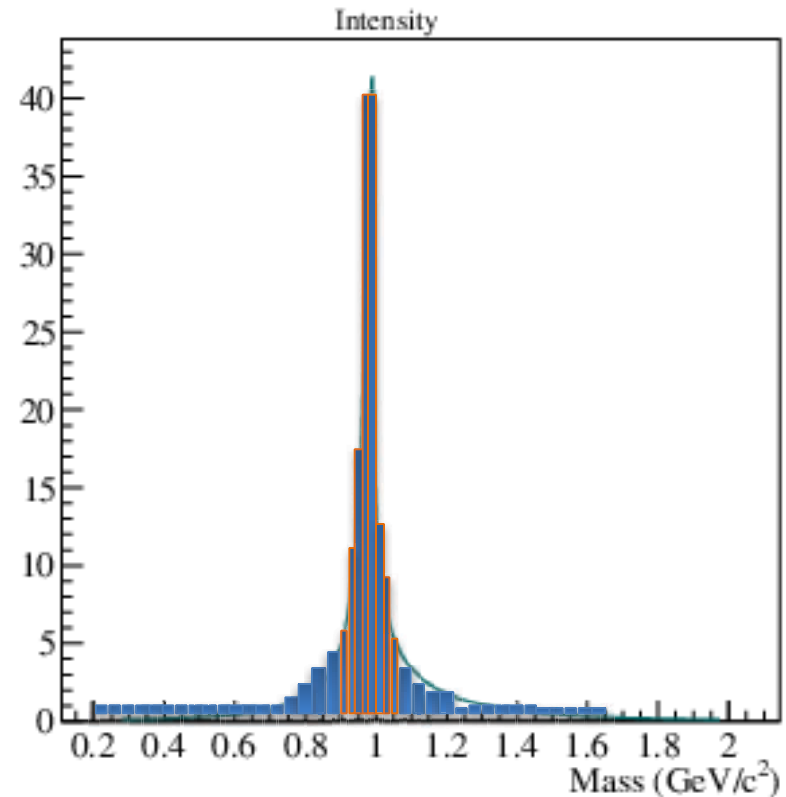
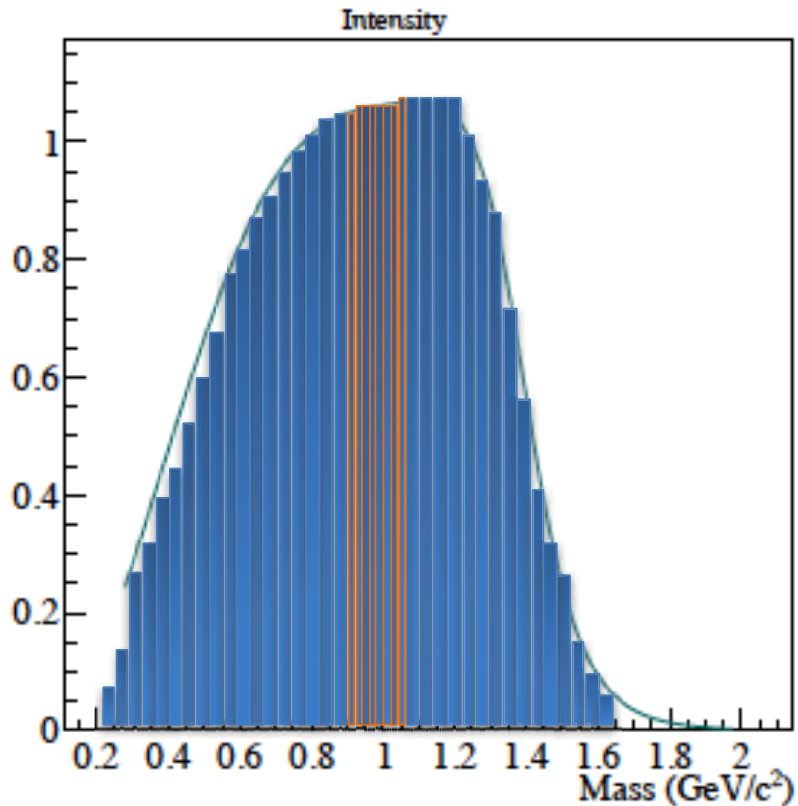






# Isobars: $[\pi\pi]^*_S$

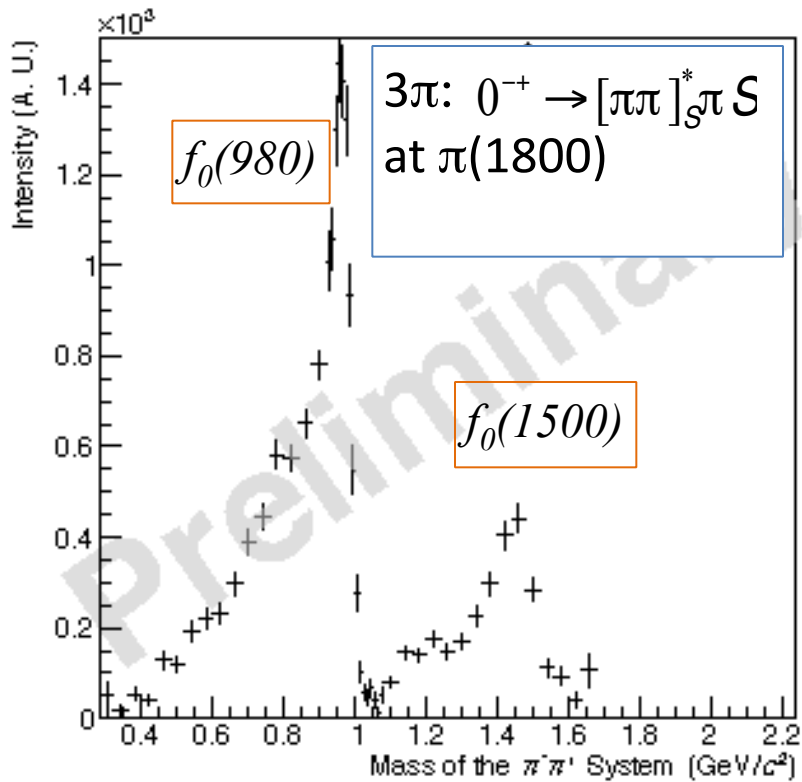
replaced by ONE  $[\pi\pi]^*_S$  histogram with n-bins  
( $2n$  parameters determined by fit)





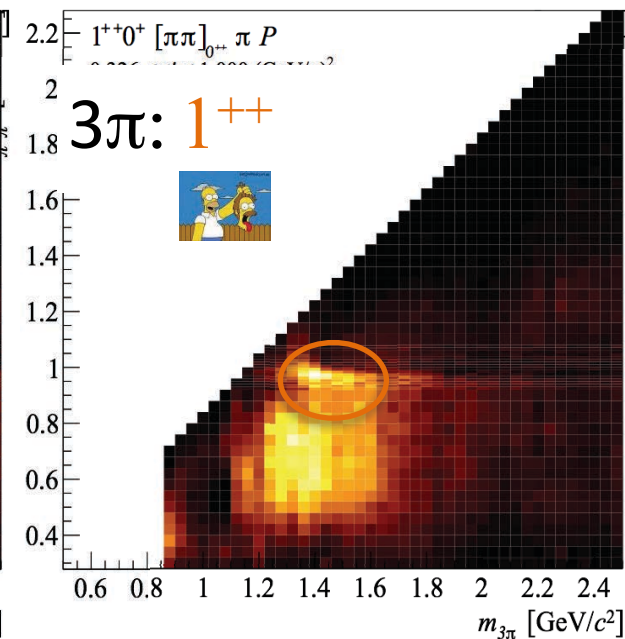
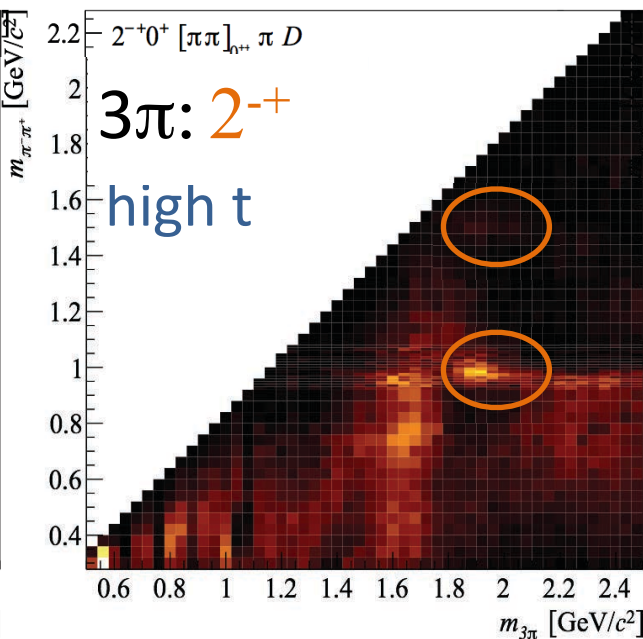
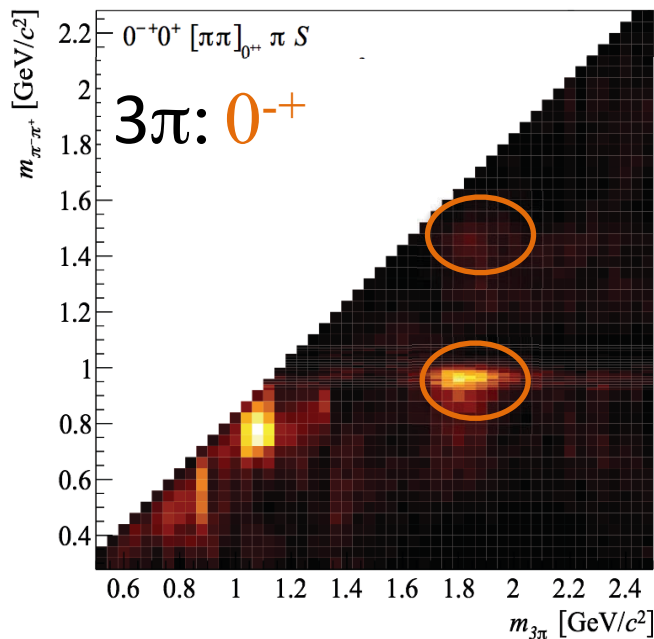
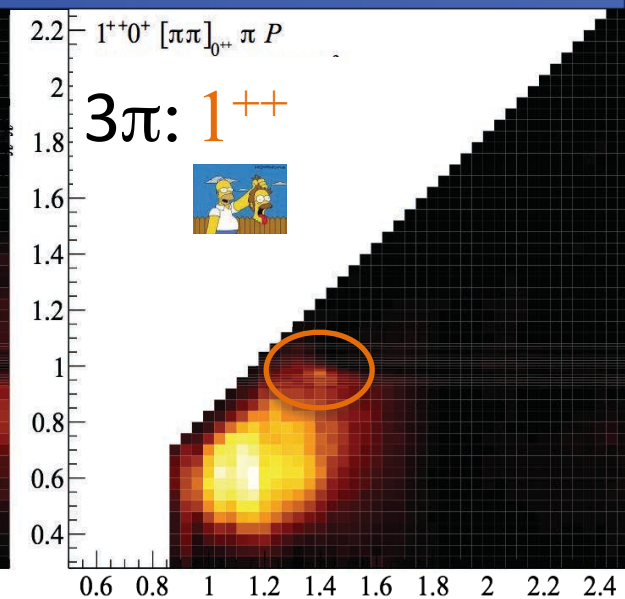
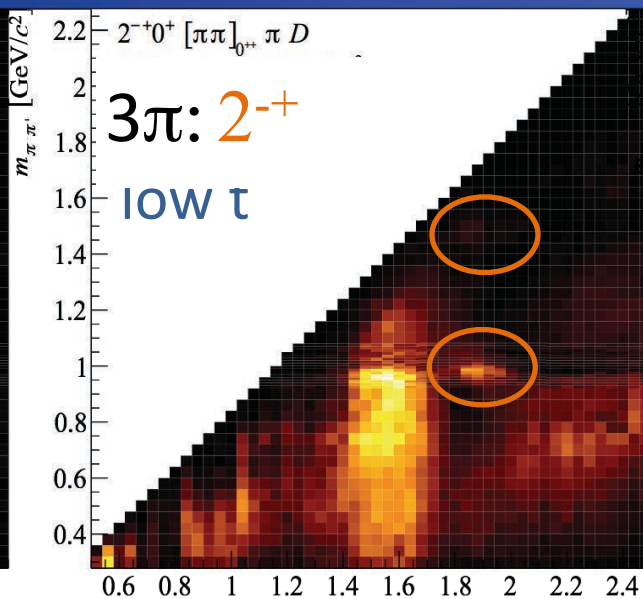
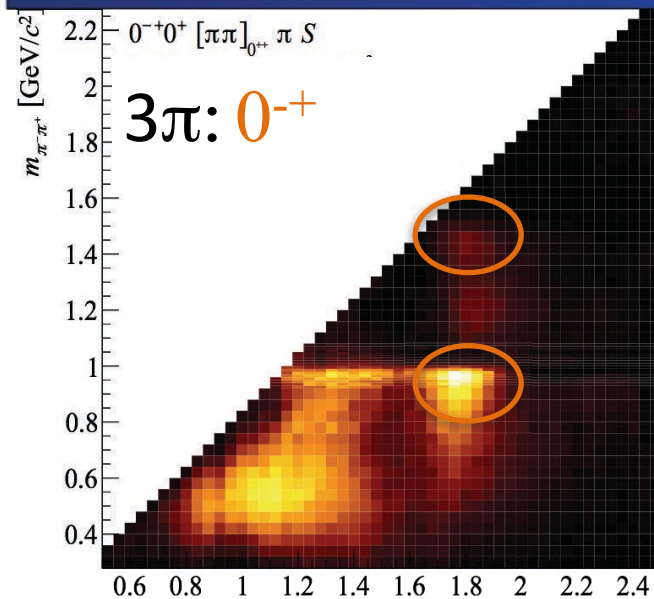
# Isobars: $[\pi\pi]^*_S$

replaced by ONE  $[\pi\pi]^*_S$  histogram with n-bins  
(2n parameters determined by fit)





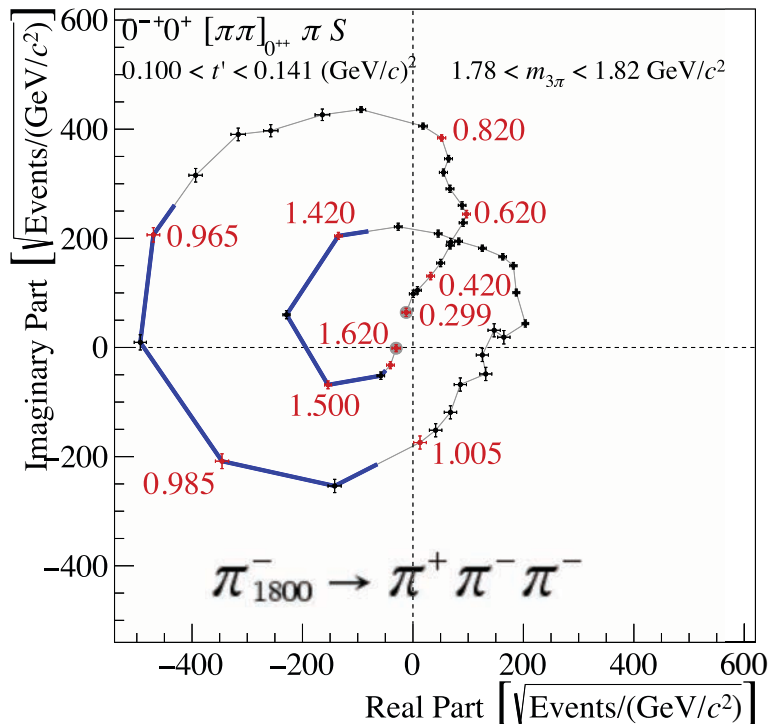
# Correlation: $m_{2\pi}(0^{++})$ vs $m_{3\pi}(J^{PC})$





# What about $\pi\pi$ S-wave phase shifts ?

- Extracting  $\pi\pi$  S-wave phase shifts : **not trivial**
  - Additional phases arise from
    - Deck effect (non-resonant)
    - $3\pi$  phase w.r.t to reference
    - Phase due to „third“  $\pi$  (rescattering effect)





# Summary

- Establish **new “2D” fit** method to perform PWA in  $m_{3\pi}$  and  $t$ 
  - Allows to “**separate**” non-resonant and resonant production
  - Cleaner access to resonances

- Find **new iso-vector** state  $a_1(1420)$

- $M_{a_1(1420)} = 1412-1422 \text{ MeV}/c^2$  ,  $\Gamma_{a_1(1420)} = 130-150 \text{ MeV}/c^2$
- (exclusive) decay into  $f_0(980)\pi$  in relative P-wave



- **Nature of  $a_1(1420)$  ?**

Isospin partner of  $f_1(1420)$  (considered to be exotic) ?

Dynamically generated through  $a_1(1260) \leftrightarrow KK^* \leftrightarrow f_0(980)\pi$  channel ?

Interference of  $a_1(1260)$  with non resonant amplitudes ?



# Summary – Analyses Concepts

- Developed **new methods** to establish shape of isobar-spectrum
  - **first application**:  $[\pi\pi]_S^*$ :
    - Shows **strong dependence** on  $m_{3\pi}$  and on  $J^{PC}$  of **mother wave**
    - Reveals information on **scalar isobars** (measure **phases in decays**)
  - Extend to “all” isobaric systems

**Open Path to Dalitz-plot analysis** using PWA  
from PWA identified states

Needs **high statistics !!**

- **New mindset** for analysis : include production **amplitudes** (non-resonant)
- Include **relativistic effects** into amplitudes
- **New (CPU intensive)** methods to determine **systematics** on resonance parameters