

Recent Measurements of Transverse Spin Asymmetries

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Transverse Structure of the Nucleon



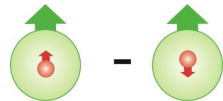
Transverse Structure of the Nucleon

in the GPM the information is encoded in the **TMD PDFs** which describe the correlations between transverse momentum and spin of quarks and nucleon spin

8 at twist 2 for each q

		nucleon		
		U	L	T
quark	U	f_1		f_{1T}^\perp
	L		g_1	g_{1L}
	T	h_1^\perp	h_{1L}^\perp	h_1

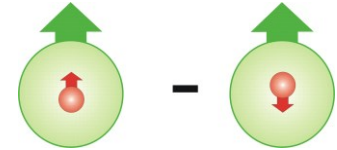
3 of them survive after integration over transverse momenta *collinear*

- **number density** f_1^q 
 q , well known
- **helicity** g_1^q 
 Δq , known
- **transversity** h_1^q 
 $\Delta_T q$, new

ALL OF EQUAL IMPORTANCE !

Transversity PDF

- proposed in '77 (Ralston & Soper)
- different properties than helicity
 - chiral-odd, cannot be measured in inclusive DIS
 - no contribution from the gluons
 - first moment: tensor charge
- first ideas on possible measurements in the 90s (Collins, ...)
- first measurements in 2005



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	T	h_1^\perp	h_{1L}^\perp	h_1 h_{1T}^\perp

other **5 new PDFs** which vanish when integrating over transverse momentum: all of great interest and ~ unknown

two of them are T-odd

Boer-Mulders h_1^\perp

parton transverse spin \leftrightarrow
parton transverse momentum

Sivers f_{1T}^\perp

nucleon transverse spin \leftrightarrow
parton transverse momentum

nucleon transverse spin \leftrightarrow parton transverse momentum

- requires final/initial state interactions to survive time-reversal invariance
- time-reversal invariance implies:

$$f_{1T}^\perp|_{\text{SIDIS}} = -f_{1T}^\perp|_{\text{DY}} \quad \dots \text{ to be checked, new experiments}$$

Transverse Structure of the Nucleon

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quark	U	f_1		f_{1T}^\perp	
	L		g_1	g_{1L}	
	T	h_1^\perp	h_{1L}^\perp	h_1	h_{1T}^\perp

how to measure these new PDFs?

either chiral-odd

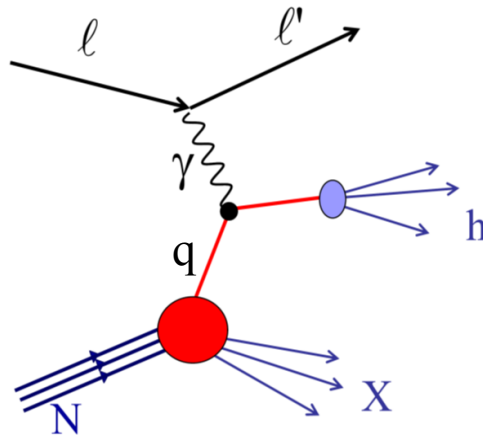
or vanishing when integrating over transverse momentum

→ not in DIS

accessing transversity and TMD PDFs

they can be accessed through different processes

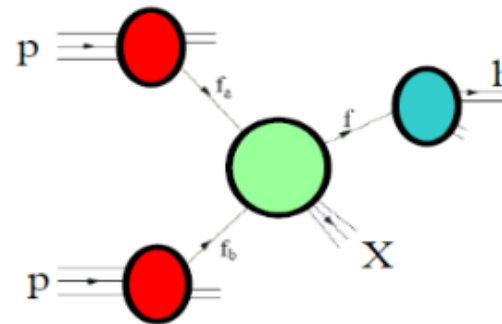
SIDIS



hard polarised pp scattering

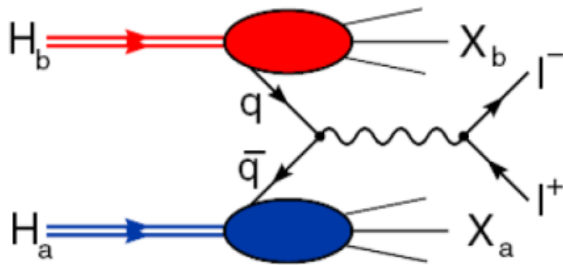
HERMES
COMPASS
Jefferson Lab

what we know today comes from these measurements



RHIC

not easy to disentangle different effects

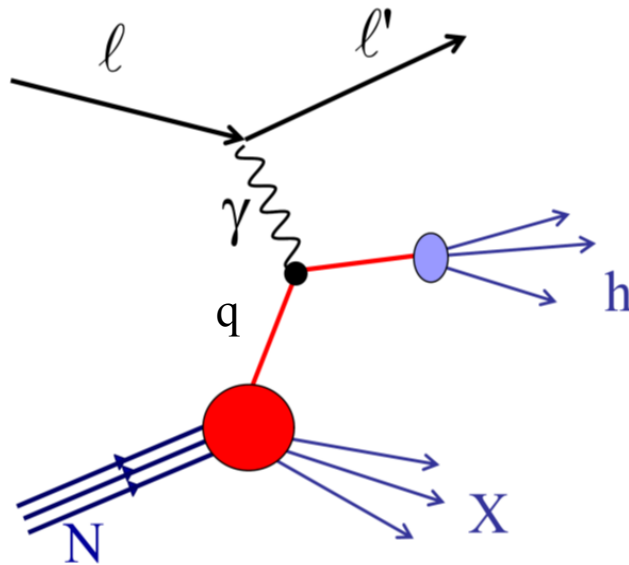


Drell-Yan

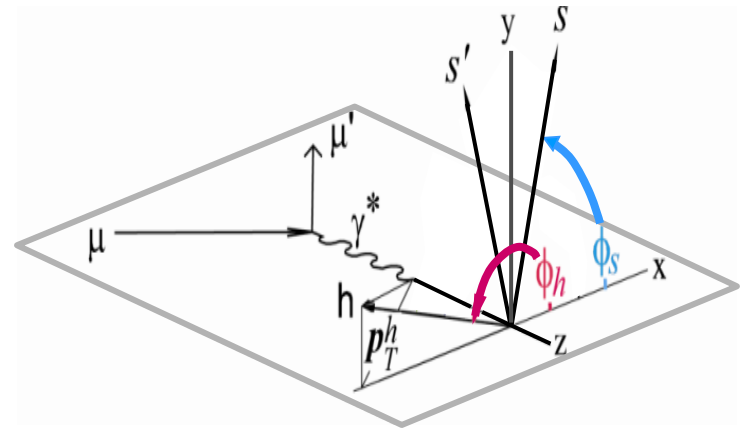
no polarised data (yet !)

why SIDIS

a simple process, a special tool



$$x, Q^2; \quad z, P_T^h, \quad \phi_h, \phi_S$$



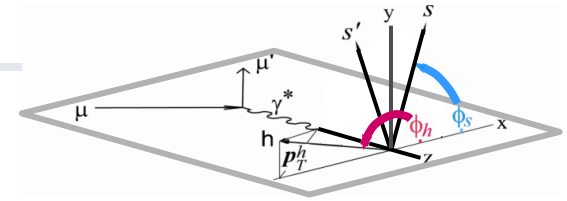
$$d\sigma^{\ell p \rightarrow \ell h X} \sim \sum_q e_q^2 f_q(x, \mathbf{k}_\perp) \cdot d\sigma^{\ell q \rightarrow \ell q} \cdot D_q^h(z, \mathbf{p}_T)$$

p, n, d targets , final state particle identification
 → flavor separation

**all the TMD PDFs appear in the cross-section
 and the different effects can be disentangled**

why SIDIS

cross-section



$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right.$$

$$+ \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h}$$

$$+ S_{\parallel} \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[\sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right]$$

$$+ |S_{\perp}| \left\{ f_{IT}^{\perp} D_I \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \right.$$

$$+ \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)}$$

$$+ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \left. \left. \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \right.$$

$$+ |S_{\perp}| \lambda_e \left\{ g_{IT}^{\perp} D_I \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \right.$$

$$\left. \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},$$

18 structure functions
14 azimuthal modulations

azimuthal asymmetries

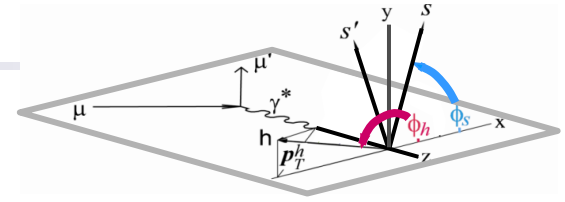
fi Sivers

$$A_{Siv} \approx \frac{\sum_q e_q^2 \mathbf{f}_{1T}^{\perp q} \otimes D_1^q}{\sum_q e_q^2 f_1 \otimes D_1^q}$$

- the Fragmentation Functions must be well known
- convolutions on transverse momenta
crucial to know them!

why SIDIS

cross-section



$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right.$$

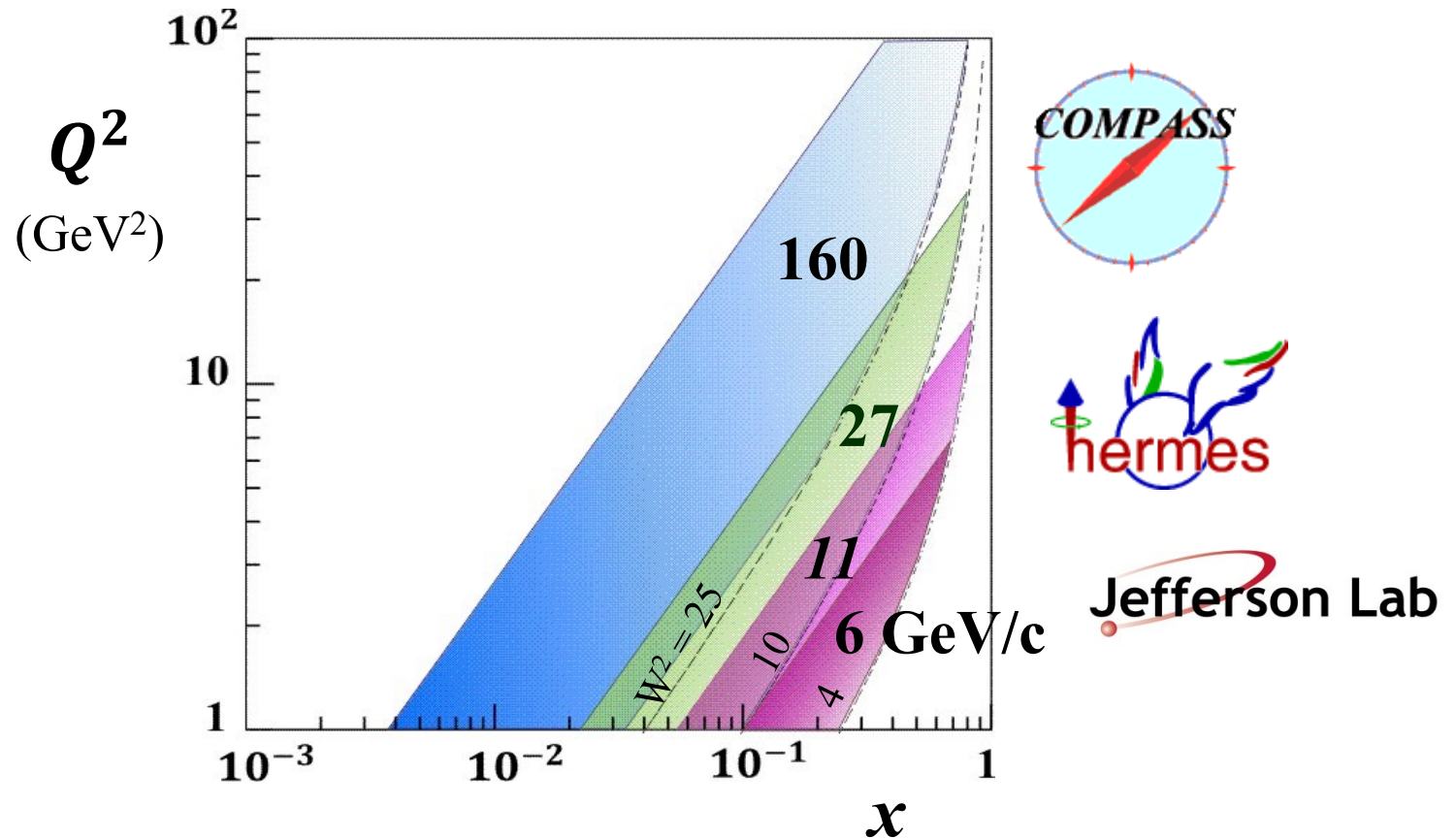
$$+ \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h}$$

$$+ S_{\parallel} \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[\sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right]$$

$$+ |S_{\perp}| \left[\begin{aligned} & f_{IT}^{\perp} D_I \left(\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\ & + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\ & + \left. h_I H_I^{\perp} \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \right. \\ & + |S_{\perp}| \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\ & \left. \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\}, \end{aligned}$$

results

from HERMES, COMPASS and Jefferson Lab experiments



some selected results only ...

Sivers asymmetry

amplitude of the modulation in $\phi_h - \phi_S$ $A_{UT}^{\sin(\phi_h - \phi_S)}$

2004: first evidence for non-zero values on proton
compatible with zero on deuteron

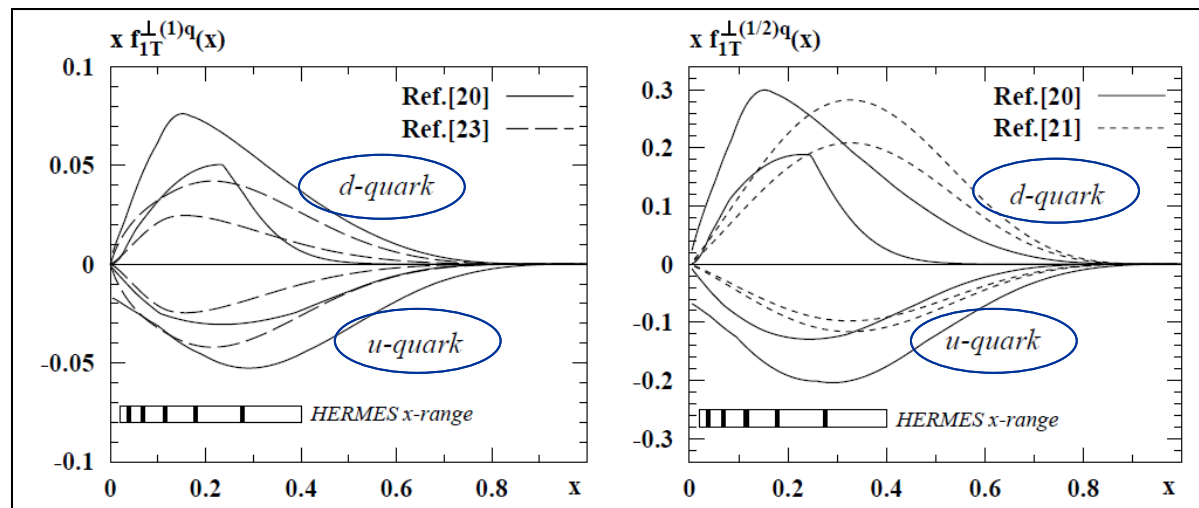


data well described by theory

first extractions
of the Sivers function

M. ANSELMINO¹, M. BOGLIONE¹, J. C. COLLINS², U. D'ALELIO³,
A. V. EFREMOV⁴, K. GOEKE⁵, A. KOTZINIAN¹, S. MENZEL⁵, A. METZ⁵,
F. MURGIA³, A. PROKUDIN¹, P. SCHWEITZER⁵, W. VOGELSANG^{6,7}, F. YUAN⁷
proceedings of Transversity2005 hep-ph/0511017

~ opposite
u- d- quark
contributions

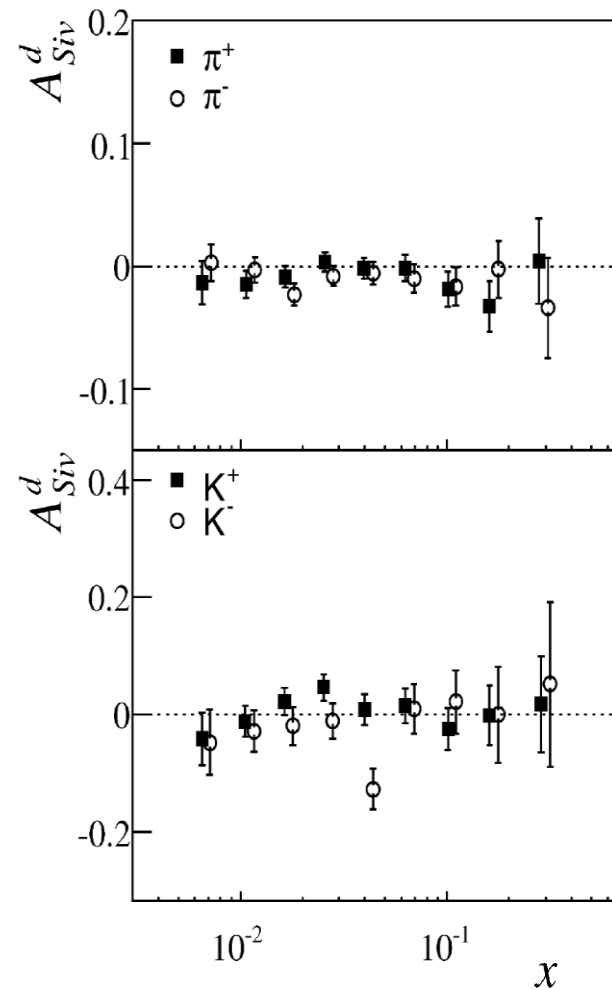
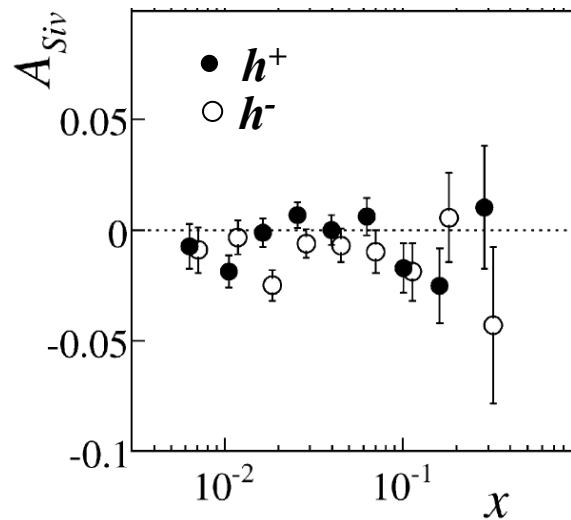


Sivers asymmetry

final results on
deuteron



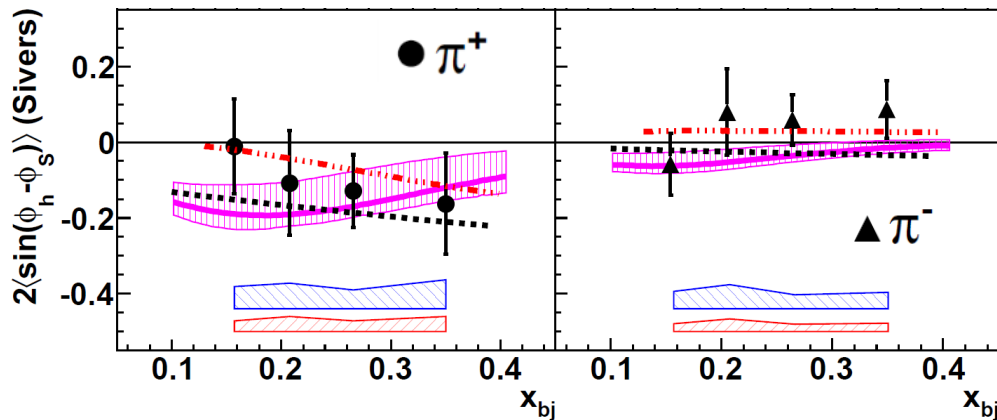
2002-2004 data
NPB765 2007, PLB673 2009



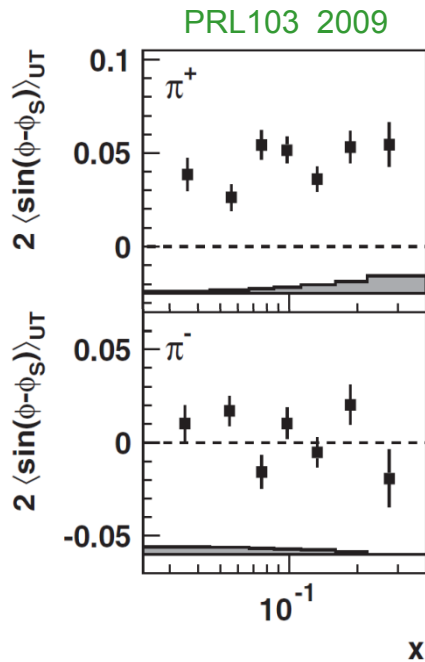
and neutron

Jefferson Lab

Hall A PRL107, 2011



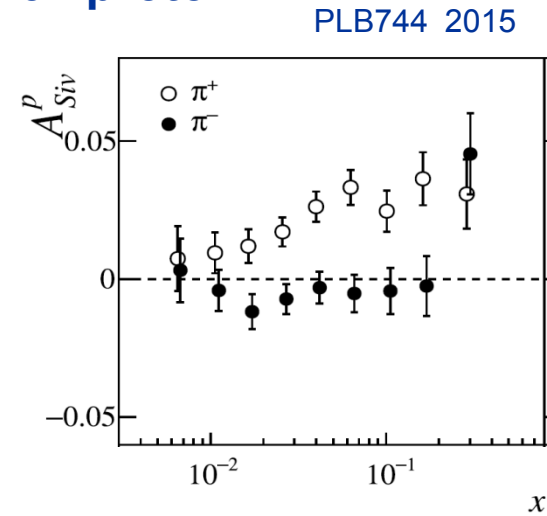
Sivers asymmetry



1D final results on **proton**



$z > 0.2$



- clearly positive for π^+ down to $x \sim 10^{-2}$

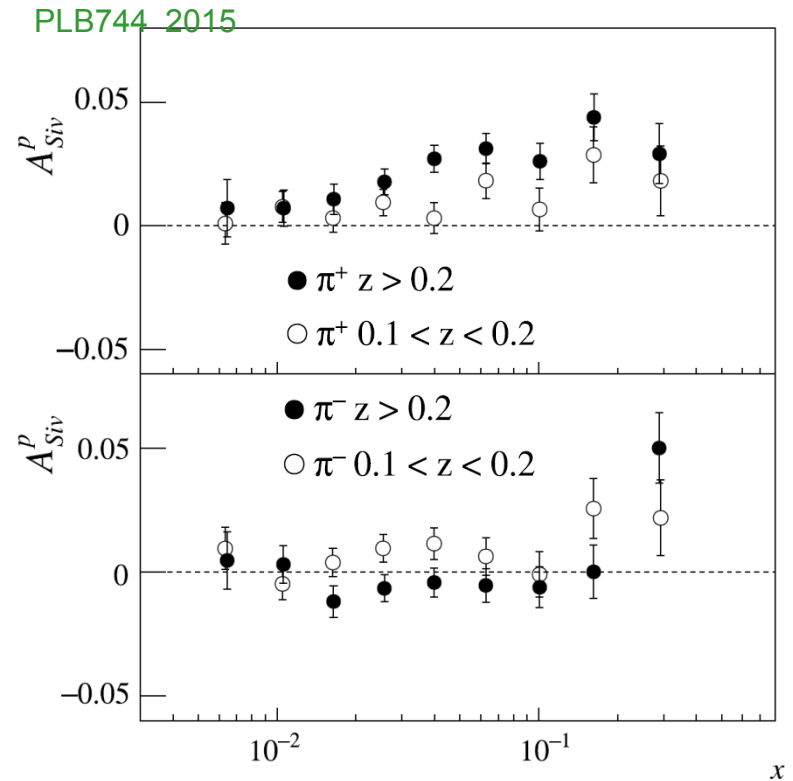
Sivers asymmetry

already published:

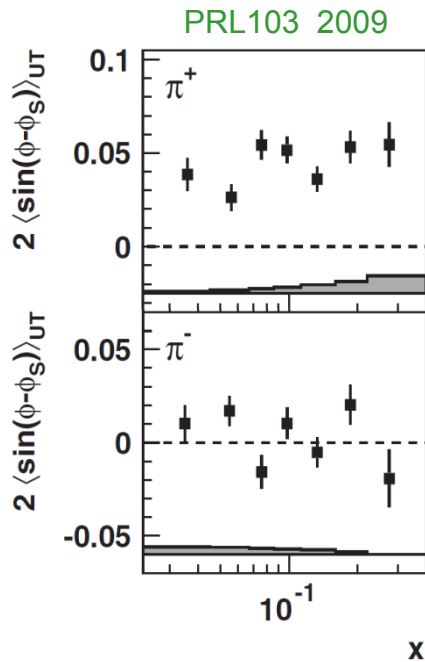
TSA vs z and p_T in different x ranges
vs x and p_T in different z ranges
vs x and z in different p_T ranges

or in extended kinematical ranges

low z / low y



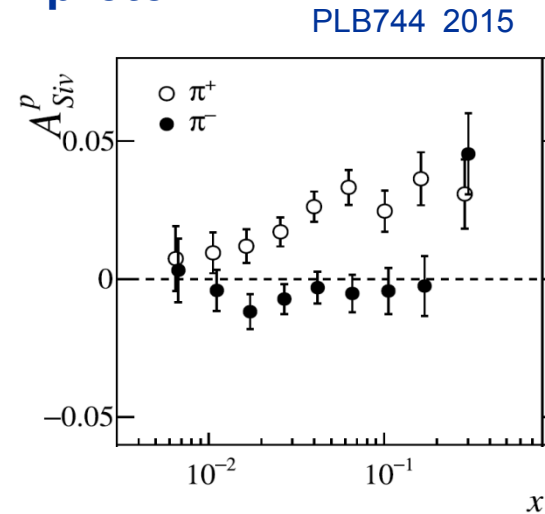
Sivers asymmetry



final results on **proton**



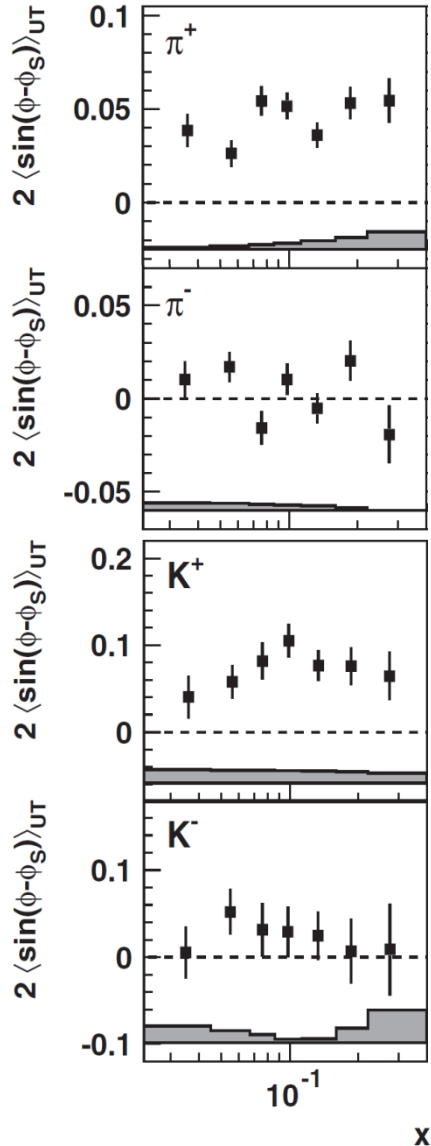
$z > 0.2$



- clearly positive for π^+ down to $x \sim 10^{-2}$

Sivers asymmetry

PRL103 2009

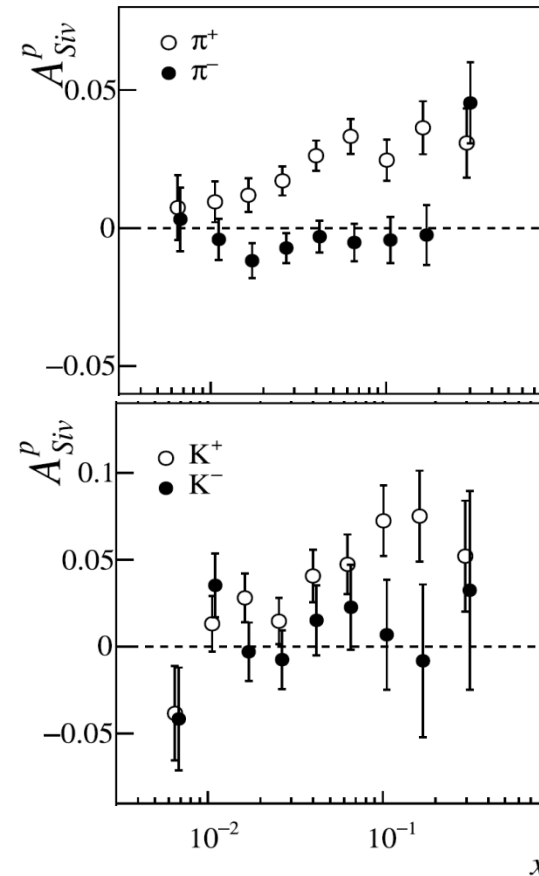


final results on proton



$z > 0.2$

PLB744 2015



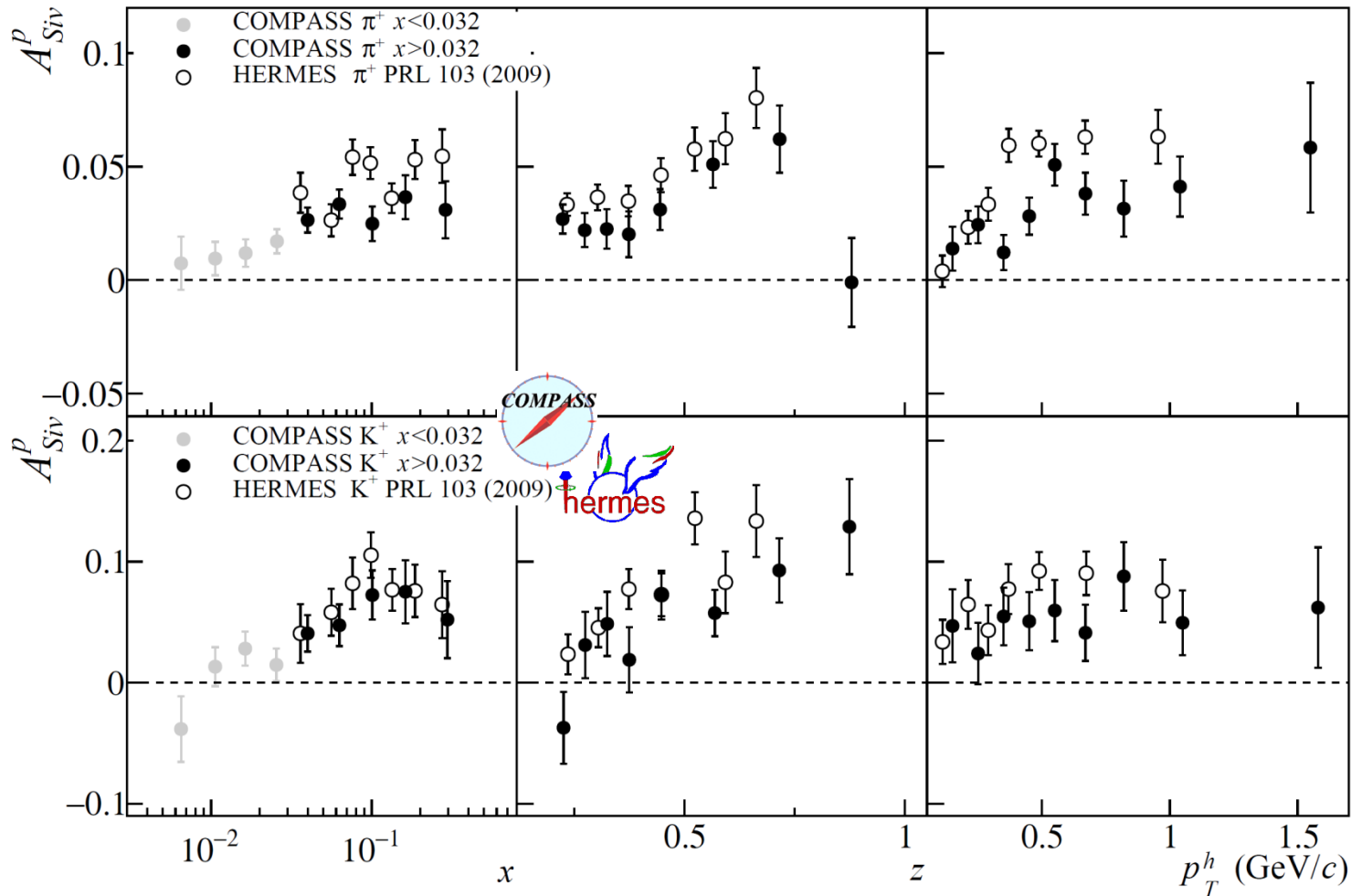
- clearly positive for π^+ down to $x \sim 10^{-2}$
- K^+ asymmetries larger than π^+ asymmetries

Sivers asymmetry

final results on proton for positive particles



vs

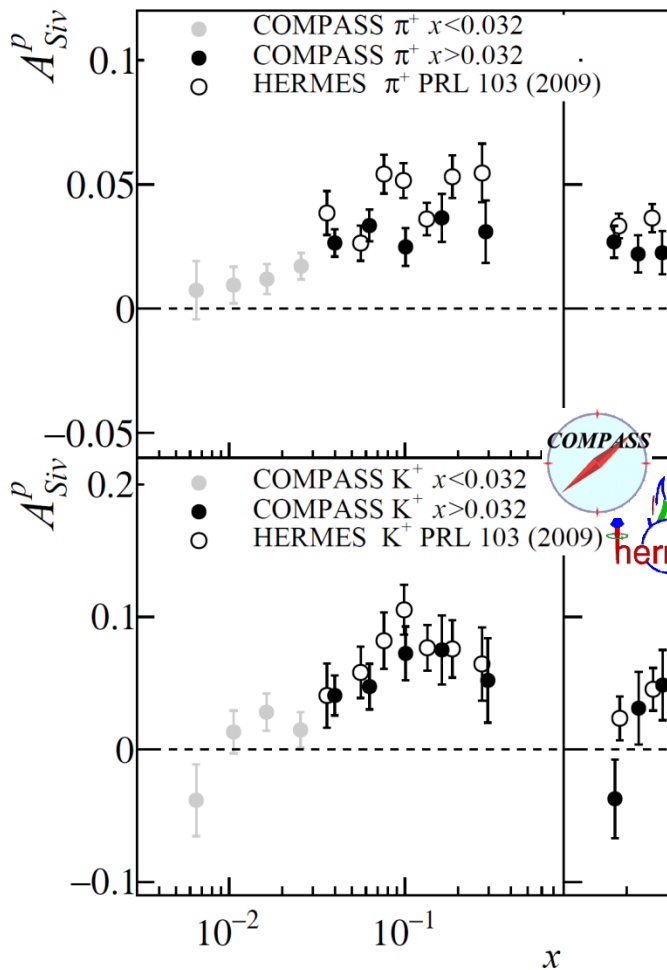


Sivers asymmetry

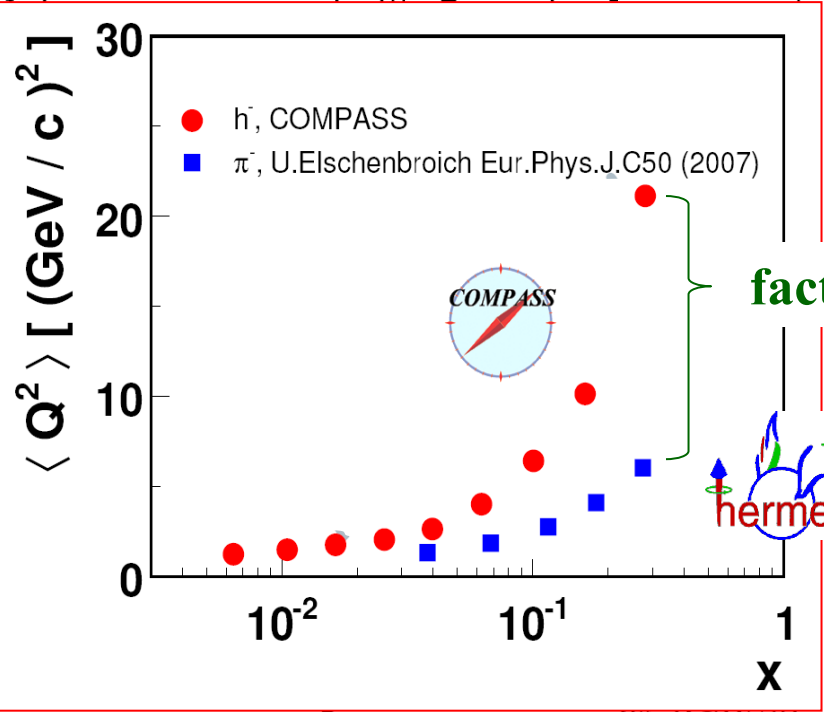
final results on proton for positive particles



vs



HERMES asymmetries larger than COMPASS asymmetries
 Q^2 evolution of TMDs ?



TMDs evolution

a lot of work in the last few years
still ongoing

new extractions from existing SIDIS data
and predictions for SIDIS experiments at different energies
and polarised Drell-Yan experiments

from small to very large Q^2 dependence

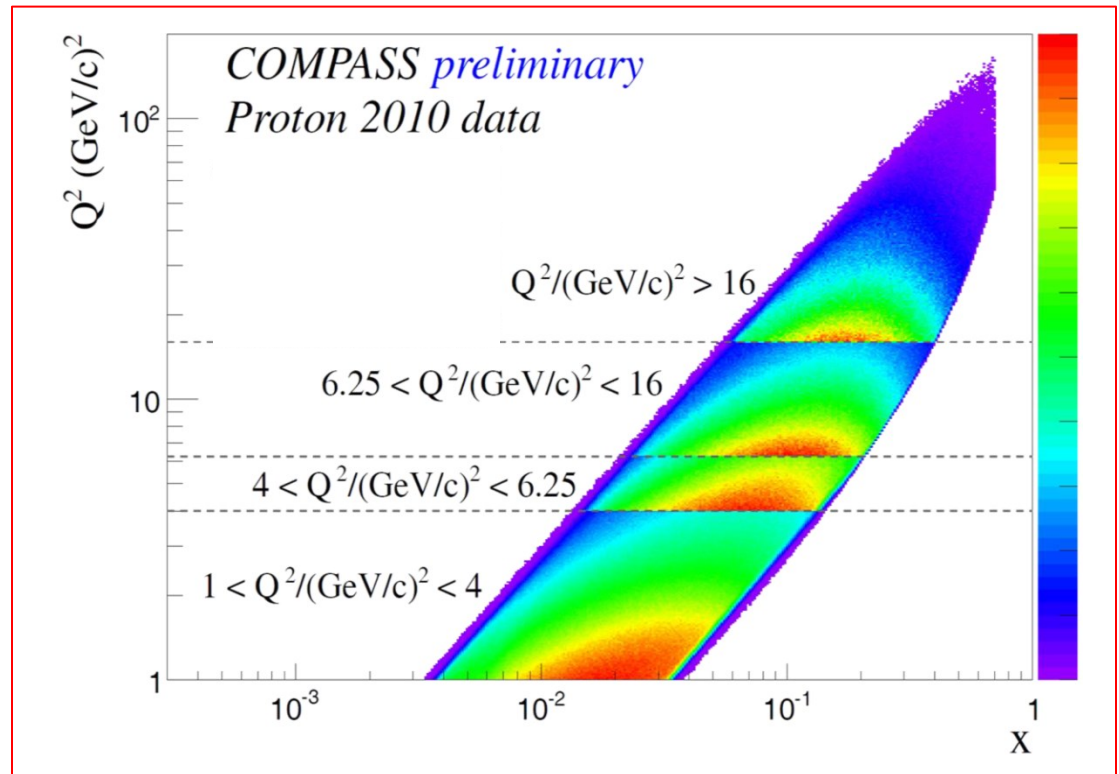
multidimensional analysis

Sivers asymmetry



COMPASS has measured the TSA in the 4 Q^2 ranges of the “future” Drell-Yan experiment

Transversity 2014



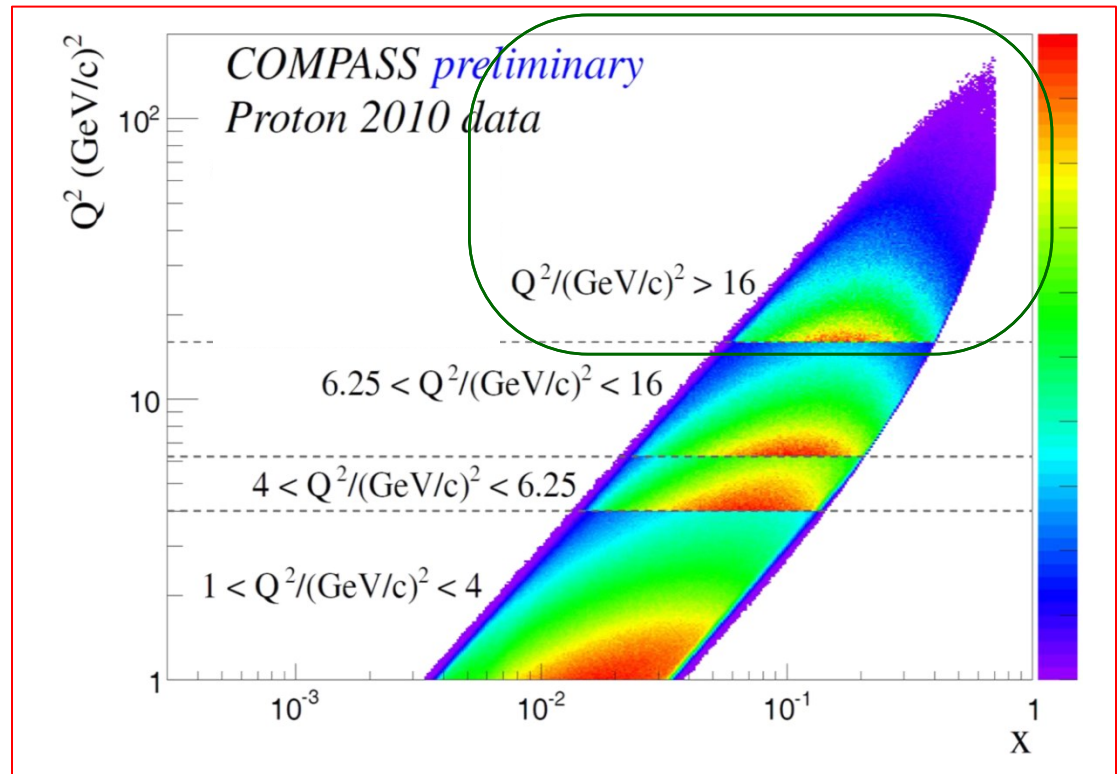
Sivers asymmetry



COMPASS has measured the TSA in the 4 Q^2 ranges of the “future” Drell-Yan experiment

“golden” range: $Q^2 > 16 \text{ GeV}^2$

Transversity 2014

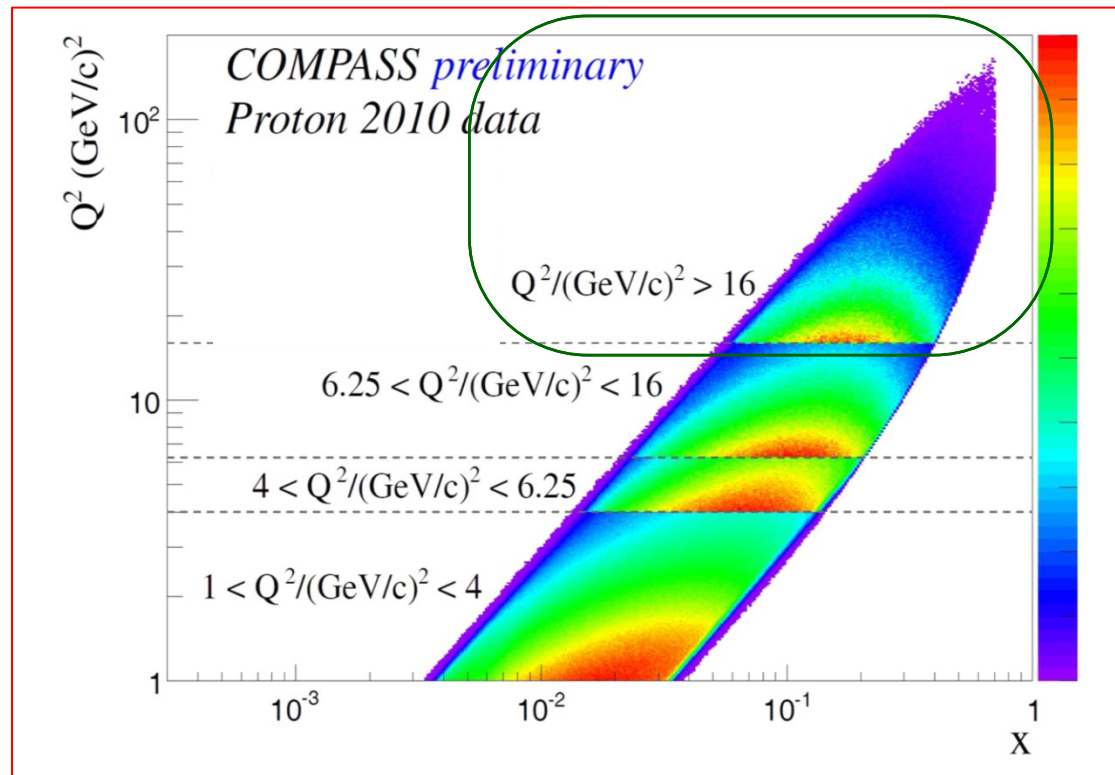
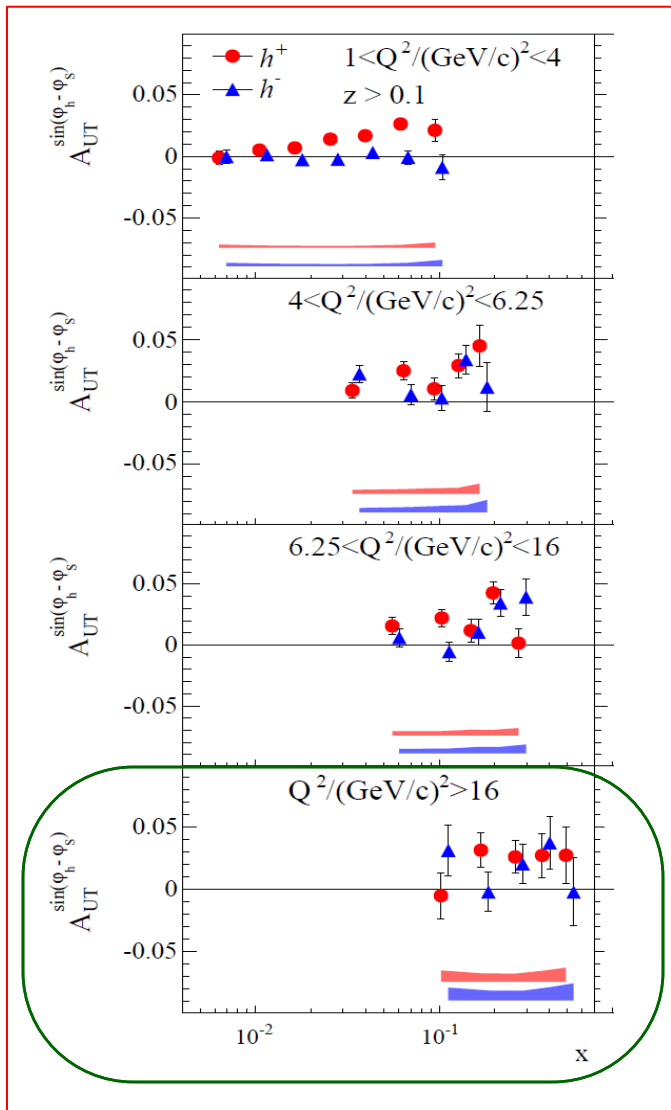


Sivers asymmetry

COMPASS has measured the TSA in the 4 Q^2 ranges of the “future” Drell-Yan experiment

“golden” range: $Q^2 > 16 \text{ GeV}^2$

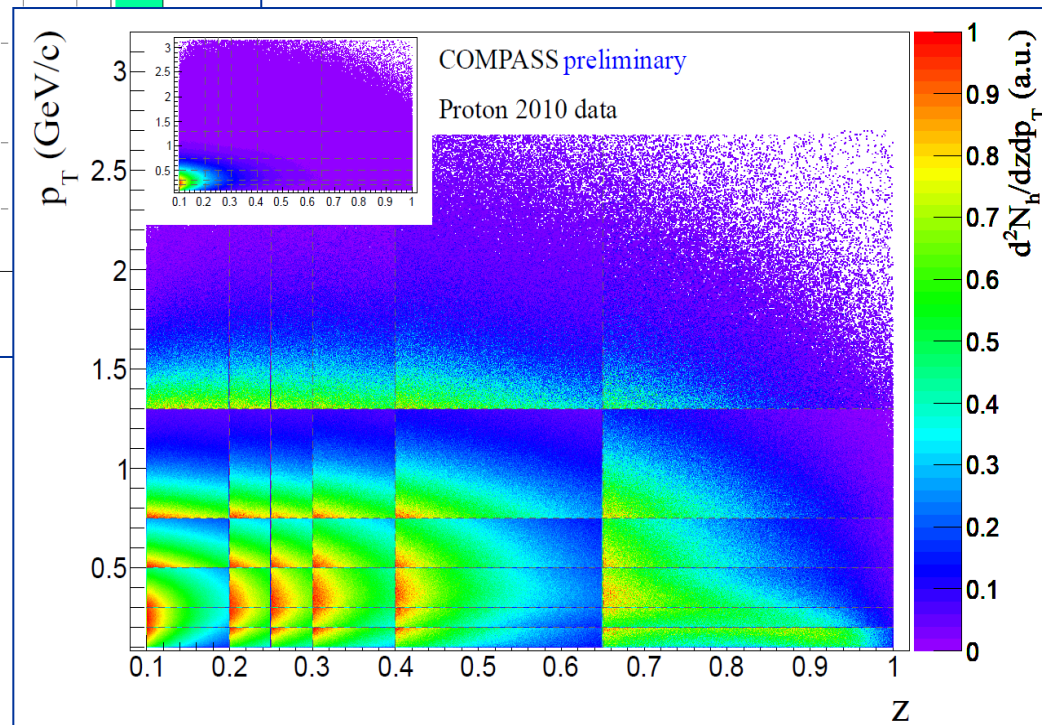
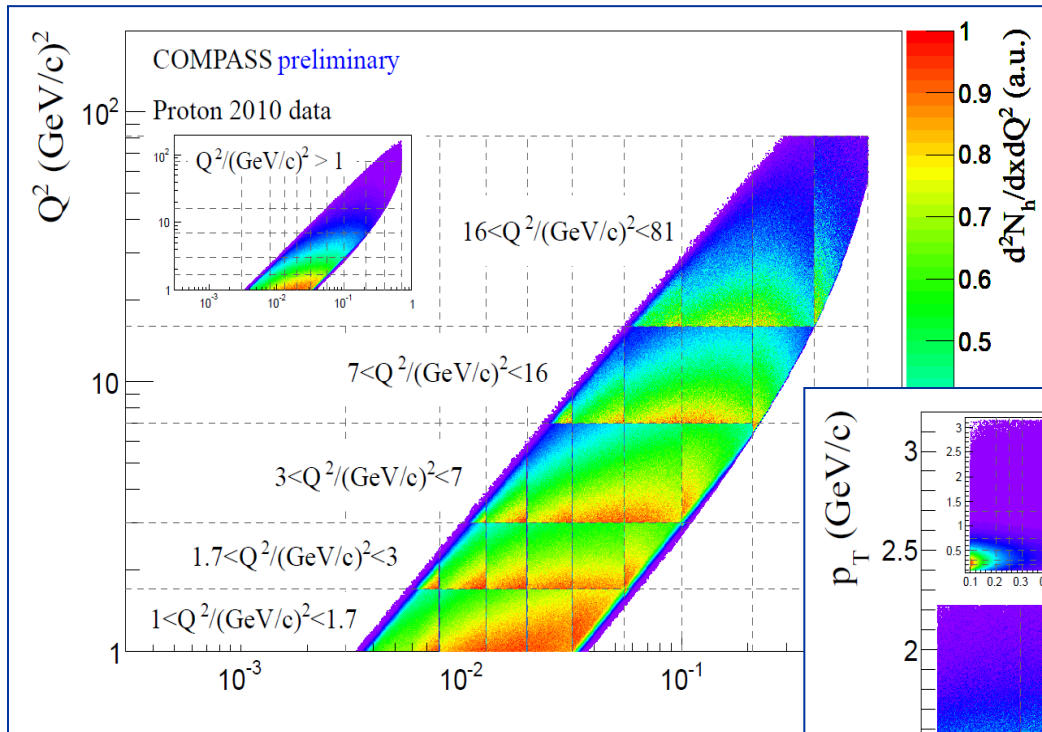
Transversity 2014



clearly positive
test of change of sign feasible

Sivers asymmetry

complete multidimensional measurements



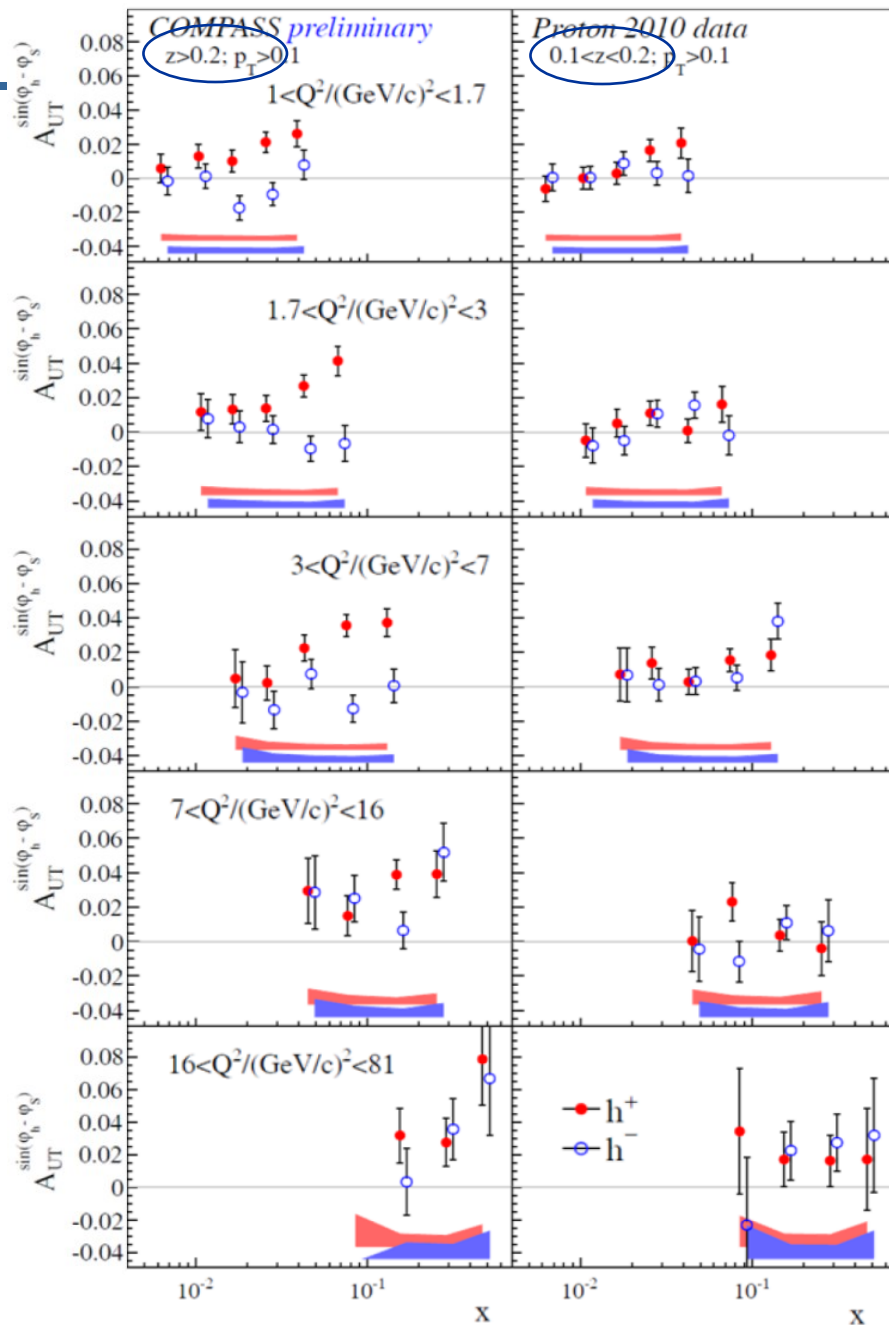
optimised x - Q^2
 z - p_T binning

Sivers asymmetry

complete multidimensional measurements



SPIN2014



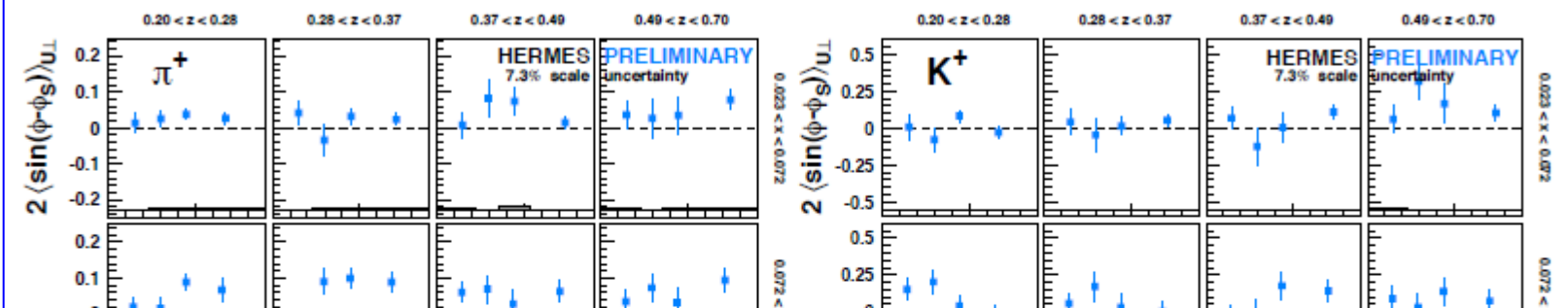
Sivers asymmetry



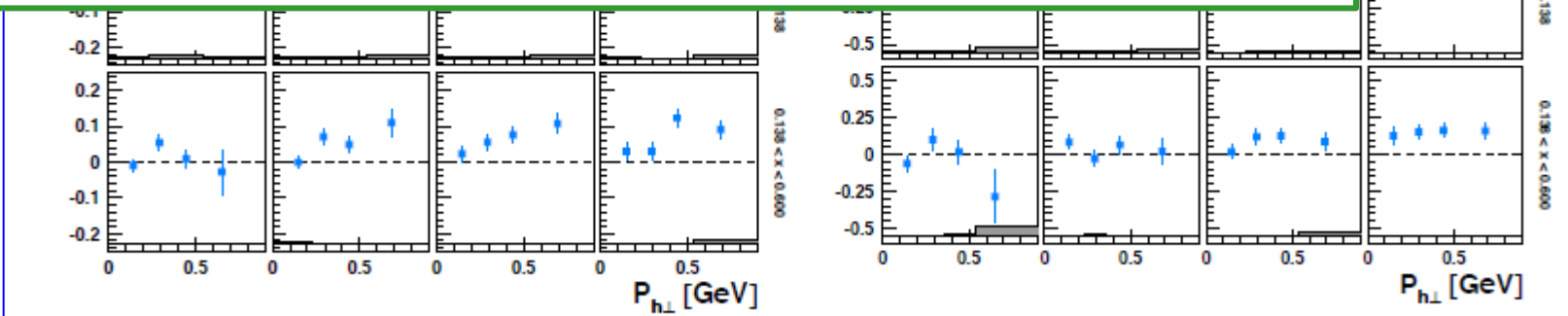
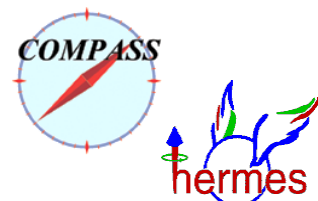
Sivers asymmetries: 3D



$$\sigma_{UT} \propto f_{1T}^{\perp q} \otimes D_1^q$$



- preliminary results produced for all TSA
- these data allow for useful tests of results from integrated 1D asymmetries



- > K^+ amplitudes are larger than π^+ in most kinematic regions
- role of sea quarks

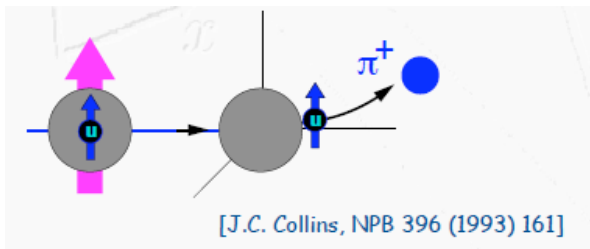
Collins asymmetry

Collins asymmetry

amplitude of the modulation in $\phi_h + \phi_S - \pi$

$$A_{Coll} \approx \frac{\sum_q e_q^2 h_1^q \otimes H_{1q}^\perp}{\sum_q e_q^2 f_1^q \otimes D_q}$$

convolution of transversity with the chiral-odd Collins FF

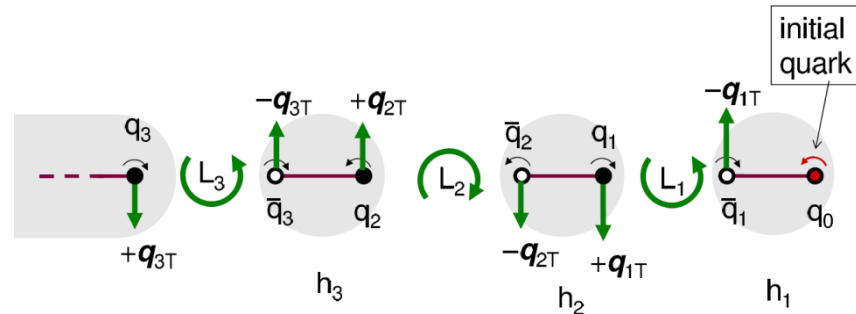


G. Schnell

correlation between transverse spin of the fragmenting quark and transverse momentum of hadrons

Classical String + 3P_0 mechanism of Collins effect

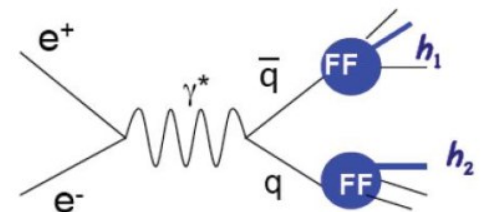
Artru, Czyzewski, Yabuki ZP C73 1997



can be (has been) accessed in

$$e^+ e^- \rightarrow q \bar{q} \rightarrow h_1 h_2 X$$

Collins FF \otimes Collins FF



Collins asymmetry

amplitude of the modulation in $\phi_h + \phi_S - \pi$

$$A_{Coll} \approx \frac{\sum_q e_q^2 h_1^q \otimes H_{1q}^\perp}{\sum_q e_q^2 f_1^q \otimes D_q}$$

2004: non-zero values on proton



first evidence that both h_1 and Collins FF different from zero

compatible with zero on deuteron



first e+e- measurements from Belle

“global” fits

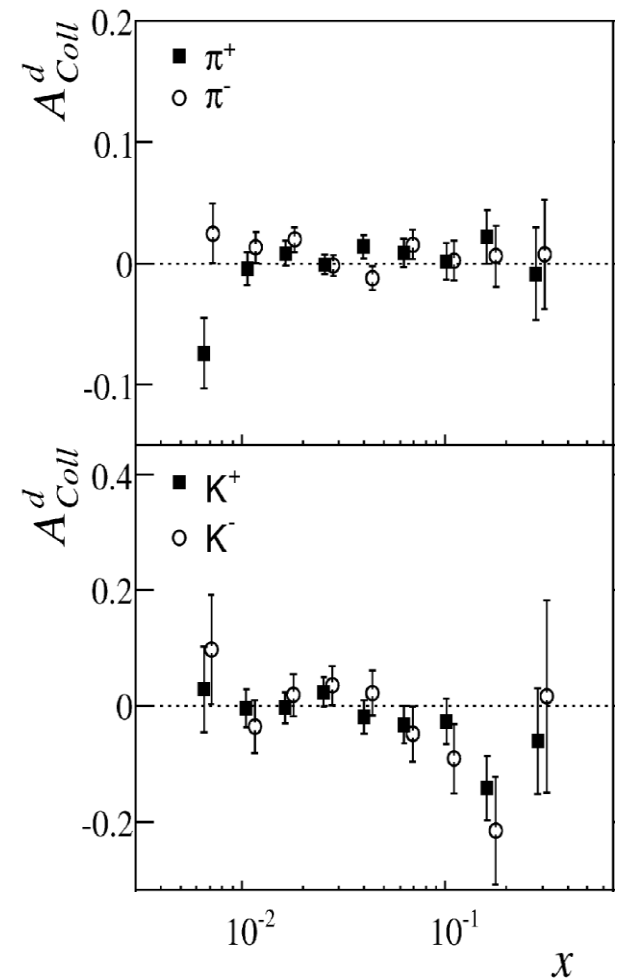
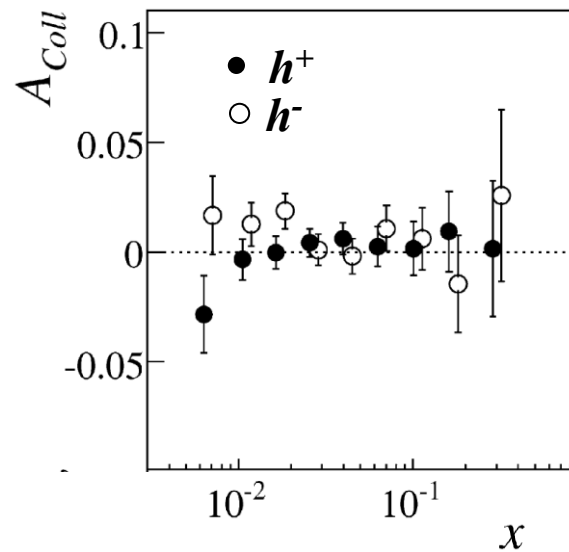
→ first extractions of h_1 and Collins FF

Collins asymmetry

final results on
deuteron



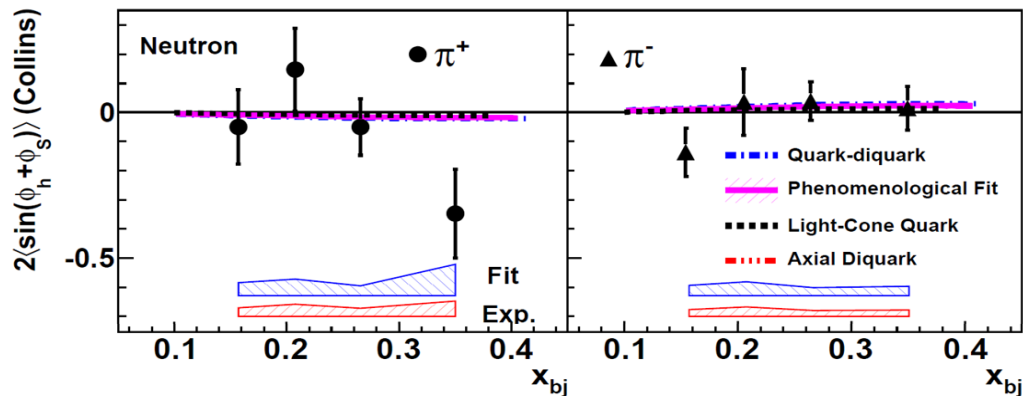
2002-2004 data
NPB765 2007, PLB673 2009



and neutron

Jefferson Lab

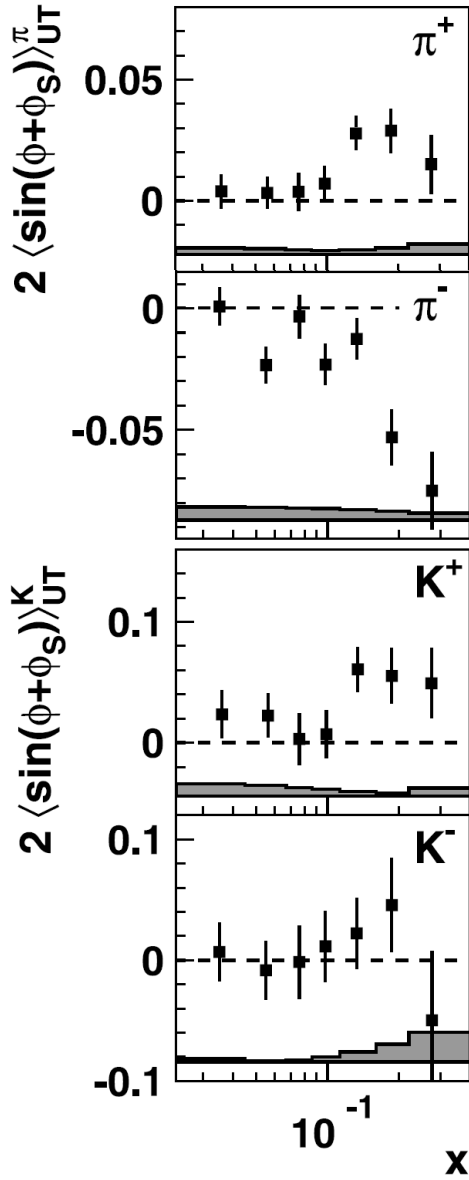
Hall A PRL107, 2011



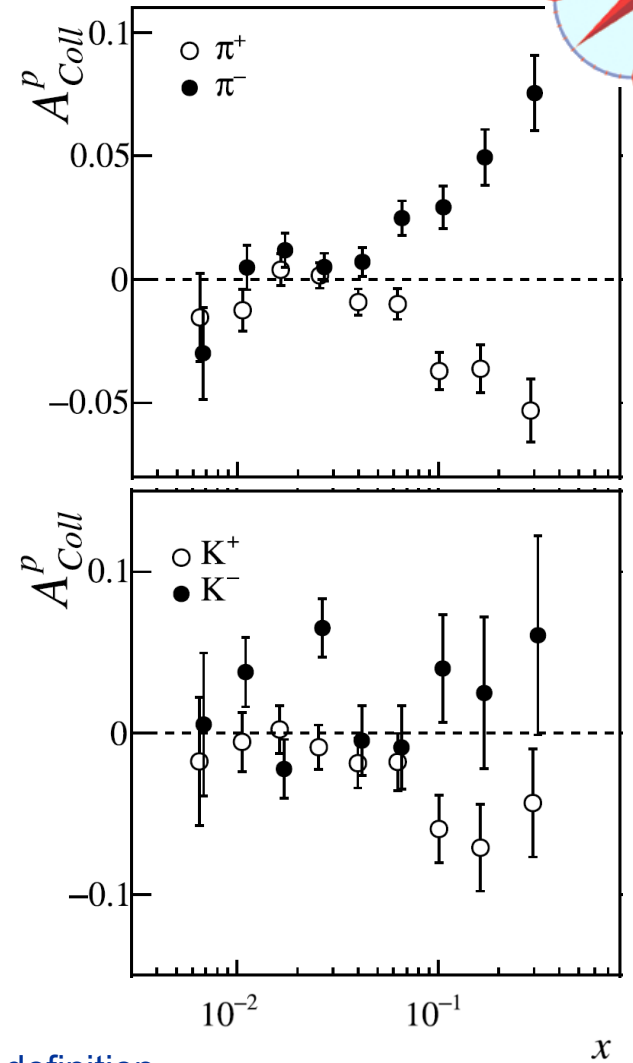
Collins asymmetry

PLB693 2010

1D final results on **proton**



PLB744 2015



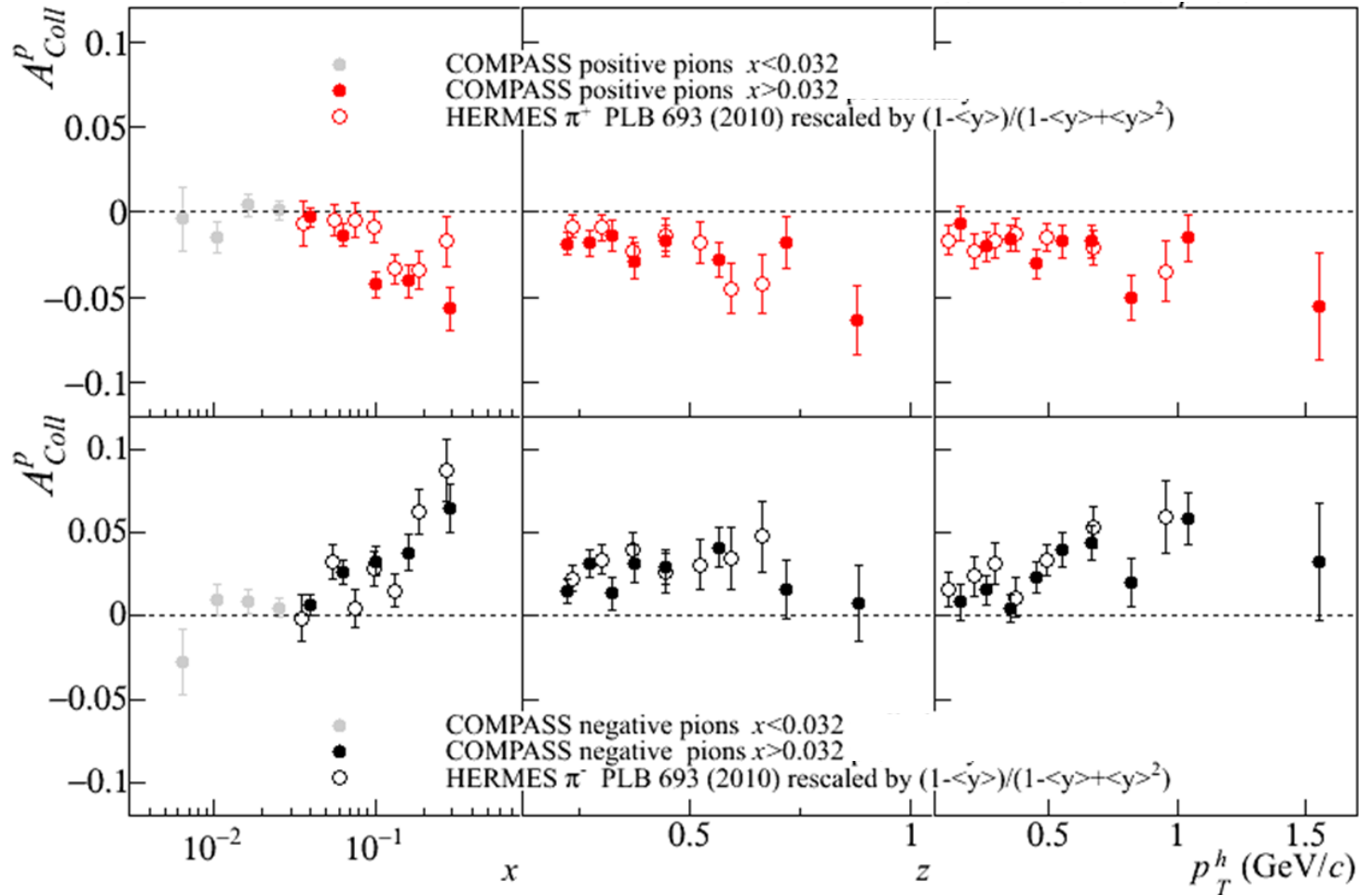
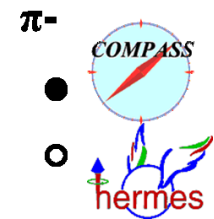
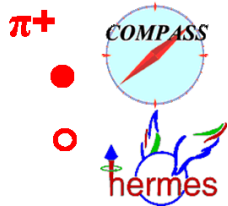
phase π in Collins angle definition

Anna Martin



Collins asymmetry

charged pions

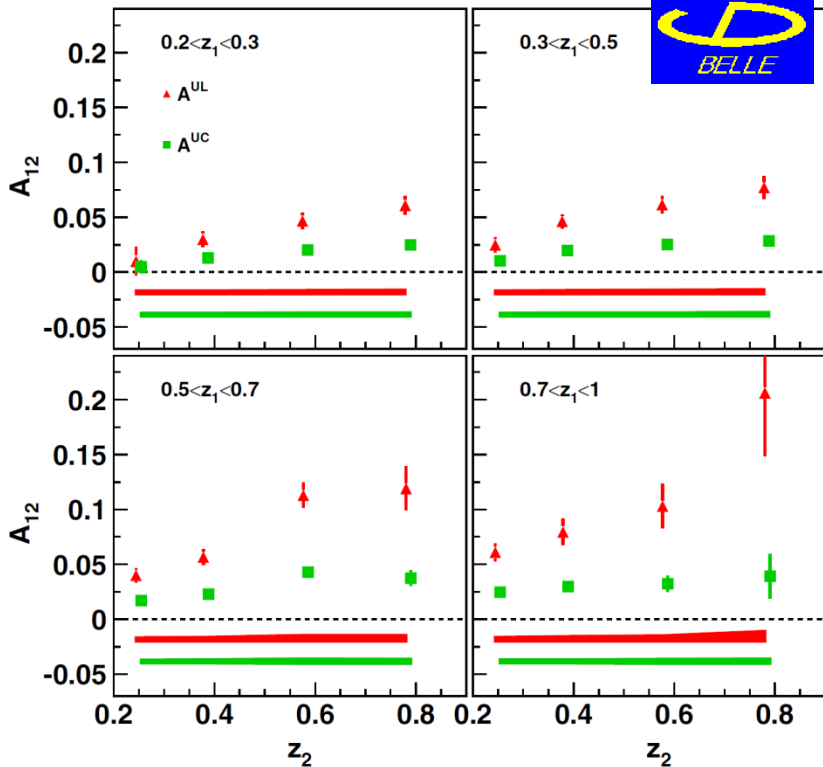


Q² evolution of Collins FF?

Collins FF

Collins FF

PRD78, 2008 PRD86, 2012

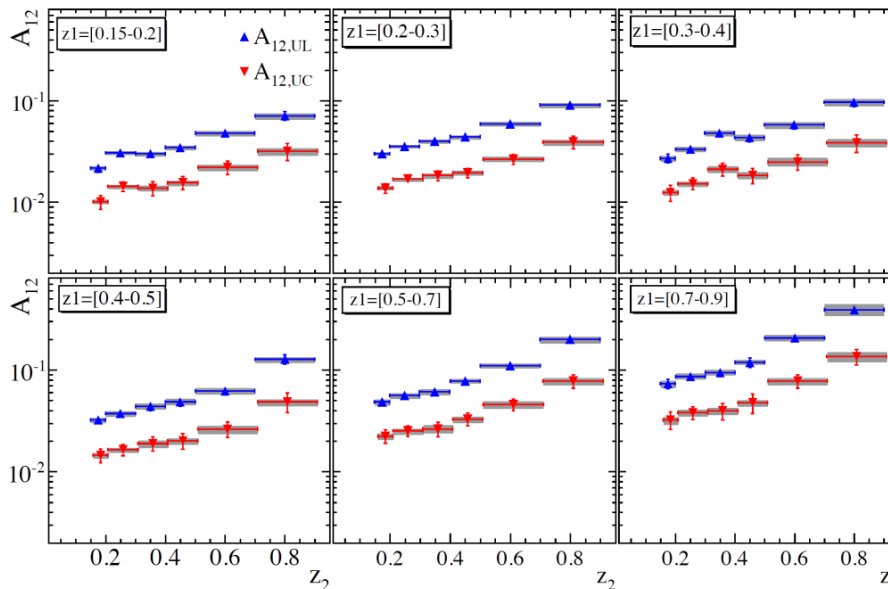


Unlike-sign couples / Like-sign couples
 Unlike-sign couples / All charges

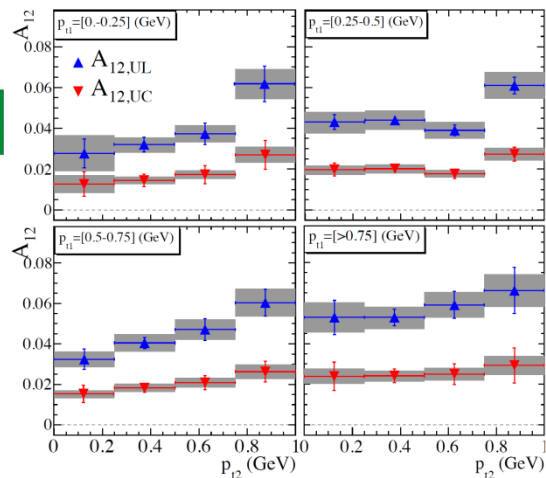


$\sqrt{s}=10.58$ GeV

PRD90 2014



$(z_1, z_2, p_{t1}, p_{t2})$



Collins FF

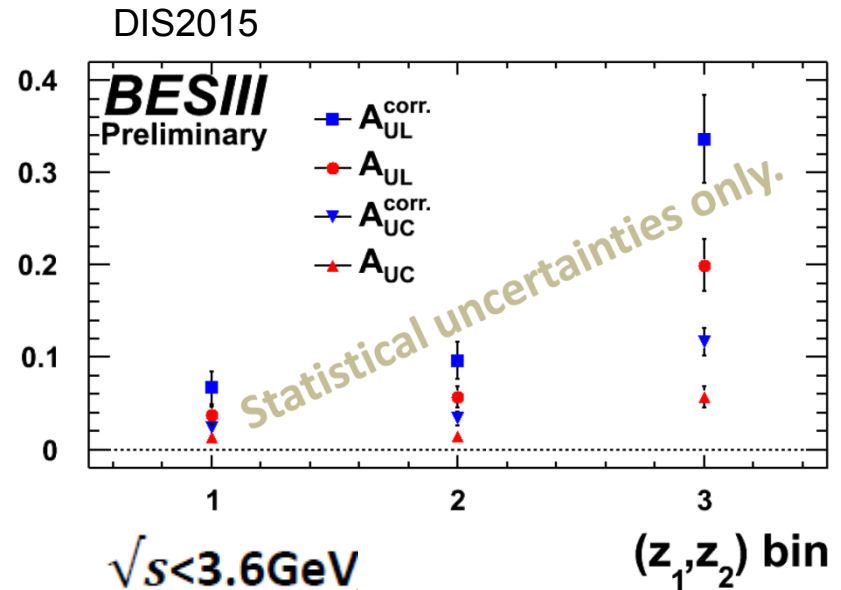
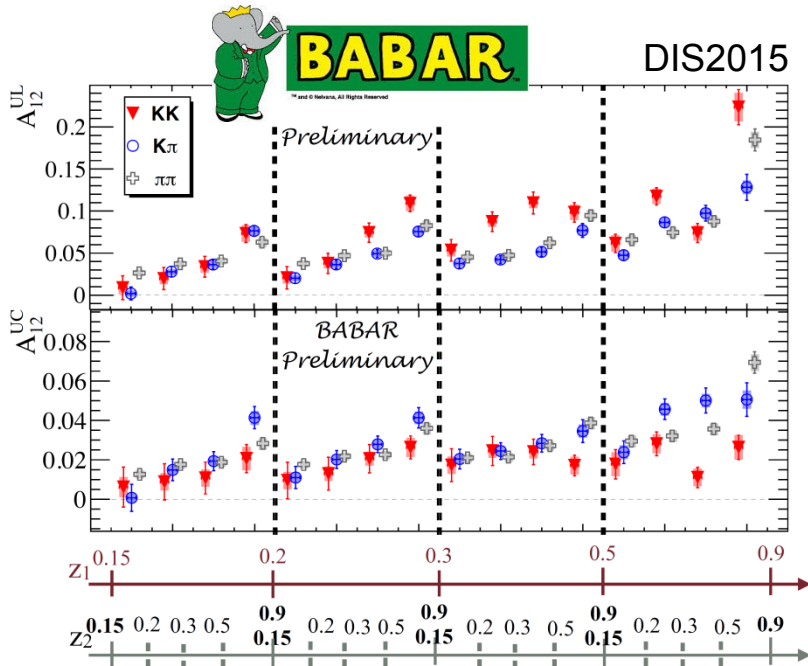
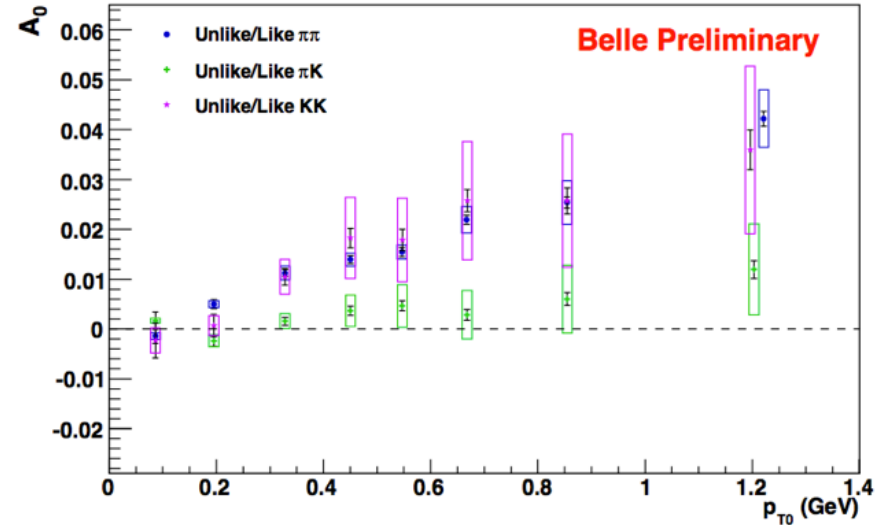


$\pi\pi \Rightarrow$ non-zero asymmetries,
increase with z_1, z_2

$\pi K \Rightarrow$ asymmetries compatible
with zero

$KK \Rightarrow$ non-zero asymmetries,
increase with z_1, z_2

Transversity2014



Transversity

simultaneous fit of HERMES p, COMPASS p & d, and Belle data
parametrisations of Transversity and Collins functions

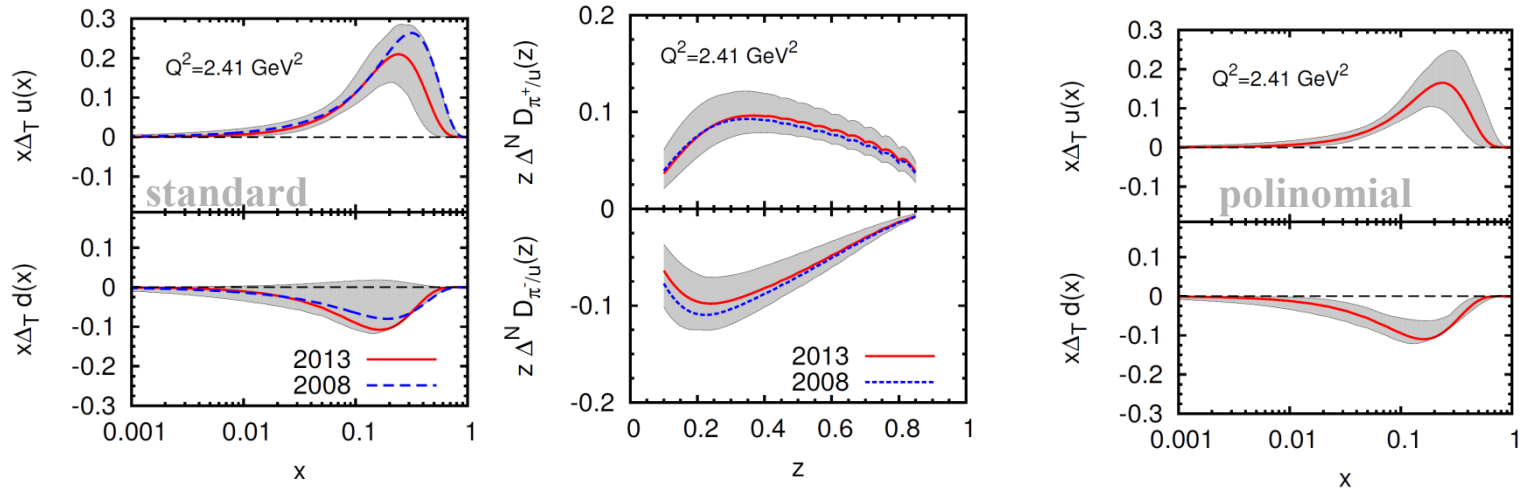
very good χ^2

Transversity

simultaneous fit of HERMES p, COMPASS p & d, and Belle data
 parametrisations of Transversity and Collins functions

very good χ^2

Anselmino
 et al.,
 PRD87 2013



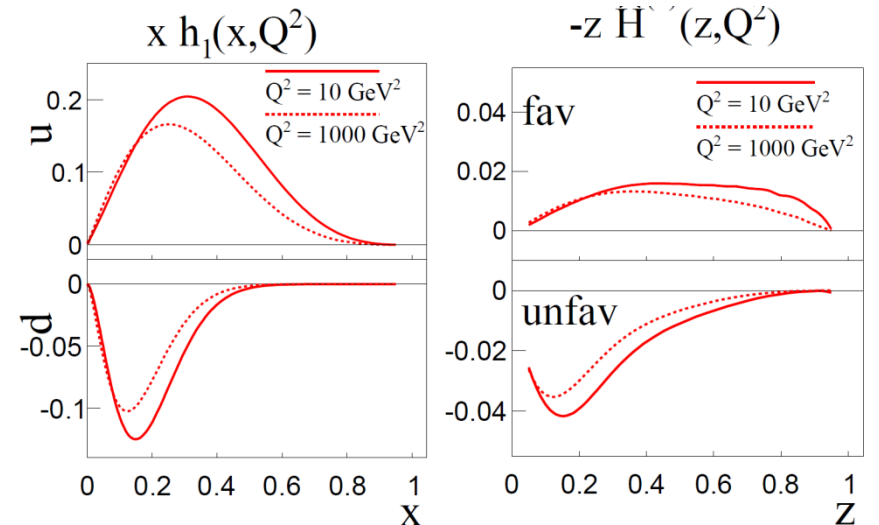
- $\delta u = 0.39^{+0.18}_{-0.12}$
- $\delta d = -0.25^{+0.30}_{-0.10}$
- ▲ $\delta u = 0.31^{+0.16}_{-0.12}$
- ▲ $\delta d = -0.27^{+0.10}_{-0.10}$

Kang et al, PRD91 2015

$$\delta u^{[0.0065, 0.35]} = +0.30^{+0.12}_{-0.08}$$

$$\delta d^{[0.0065, 0.35]} = -0.20^{+0.28}_{-0.11}$$

higher order corrections, xz

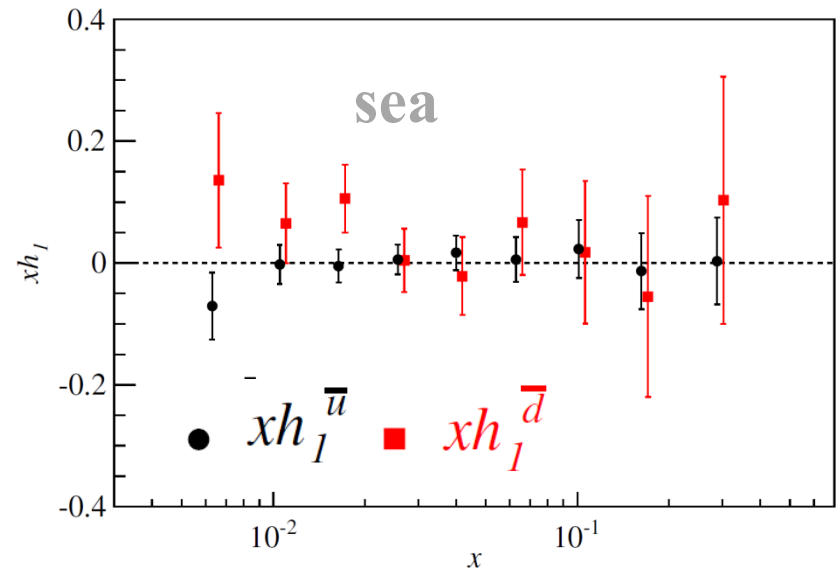
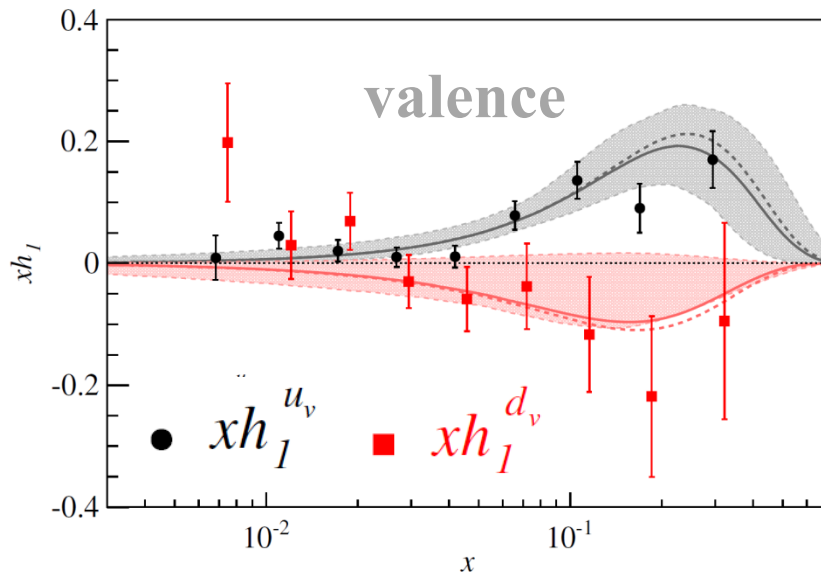


Transversity

from **COMPASS p & d** and **Belle** data, **point by point extraction**

- evolution: the same for Collins and unpolarised FF
- convolution on k_T neglected

Martin Bradamante Barone PRD91 2015



curves
from Anselmino et al.,
PRD87 2013

Transversity

alternative channels to access transversity in SIDIS

- **Λ production**, measurement of transverse polarisation
difficult: low statistics (see COMPASS d)
- **hadron pair production**, measurement of the di-hadron asymmetry
easier / done

dihadron asymmetry

independent channel to access transversity in SIDIS off transversely polarised nucleons

Collins

$$A_{Coll} \approx \frac{\sum_q e_q^2 \mathbf{h}_1^q \otimes H_{1q}^\perp}{\sum_q e_q^2 f_1^q \otimes D_q}$$

“Collins FF”

Belle Babar

dihadron

$$A_{RS} \approx \frac{\sum_q e_q^2 \mathbf{h}_1^q \cdot H_q^\angle}{\sum_q e_q^2 f_1^q \cdot D_q^{2h}}$$

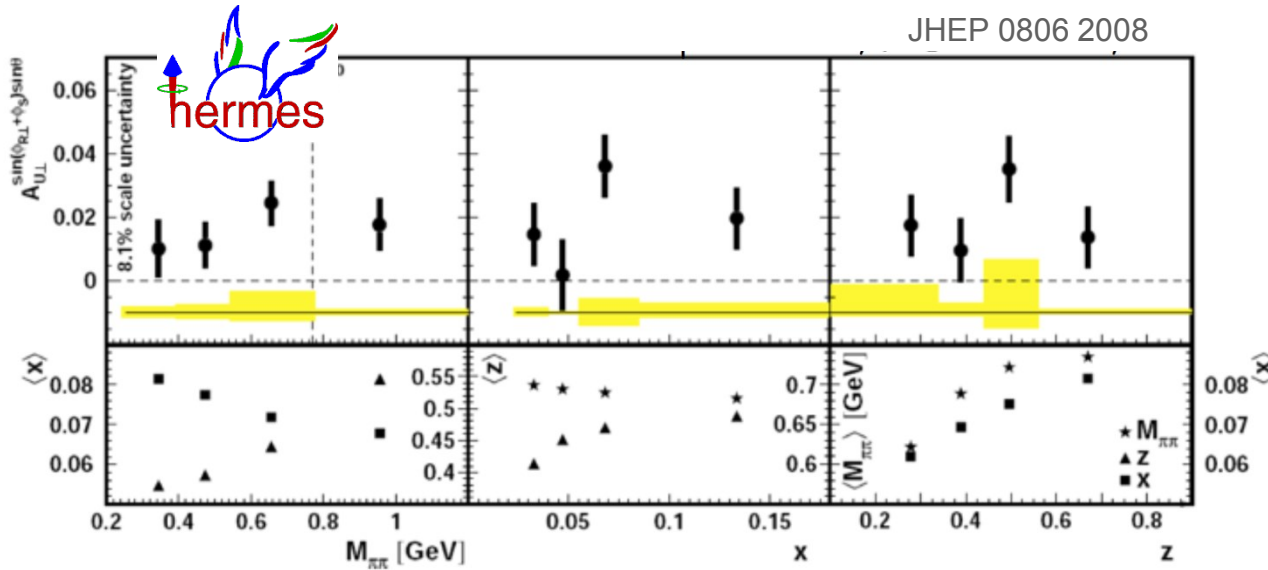
“Interference / Di-hadron FF”

Belle Babar

“spin independent di-hadron FF”

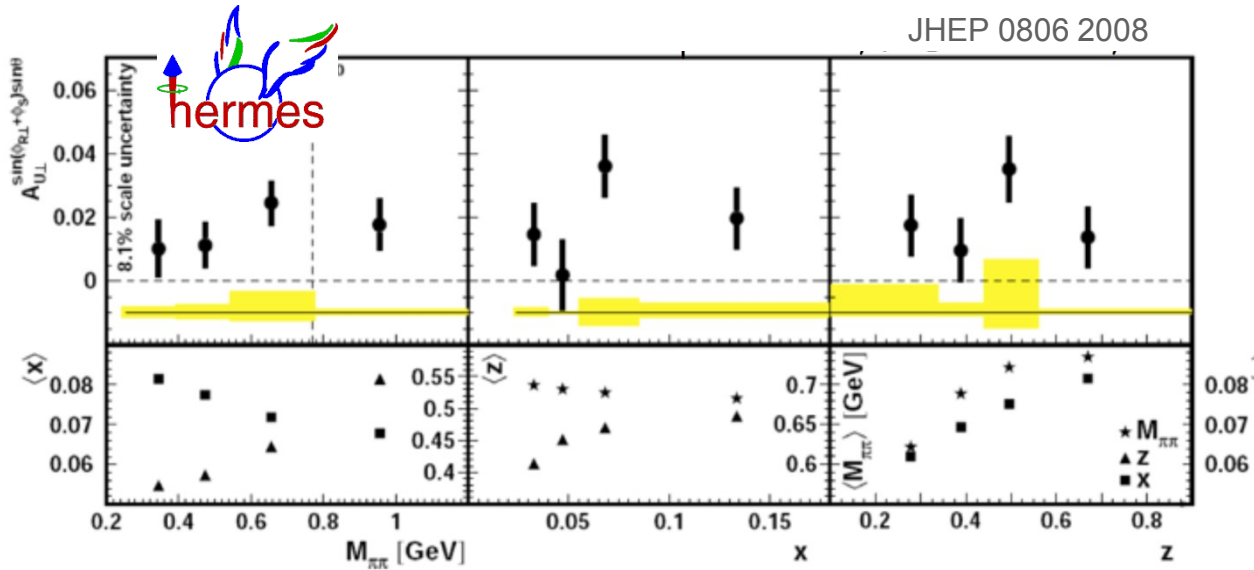
being measured at Belle Babar COMPASS

dihadron asymmetry



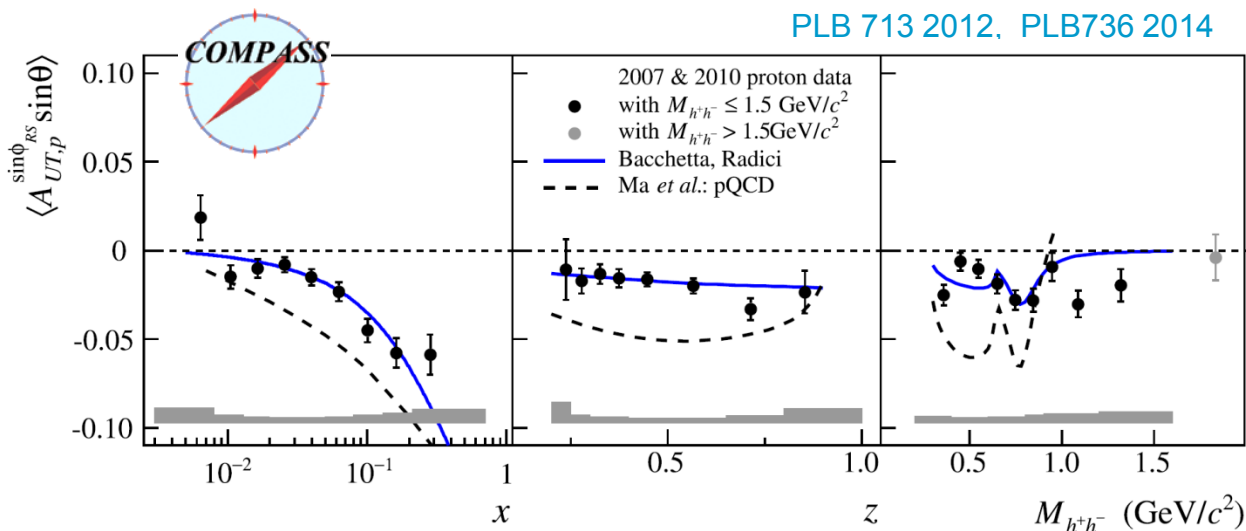
HERMES proton
 first evidence for
 non-zero dihadron FF,
 same sign of Collins
 asymmetry for π^+

dihadron asymmetry



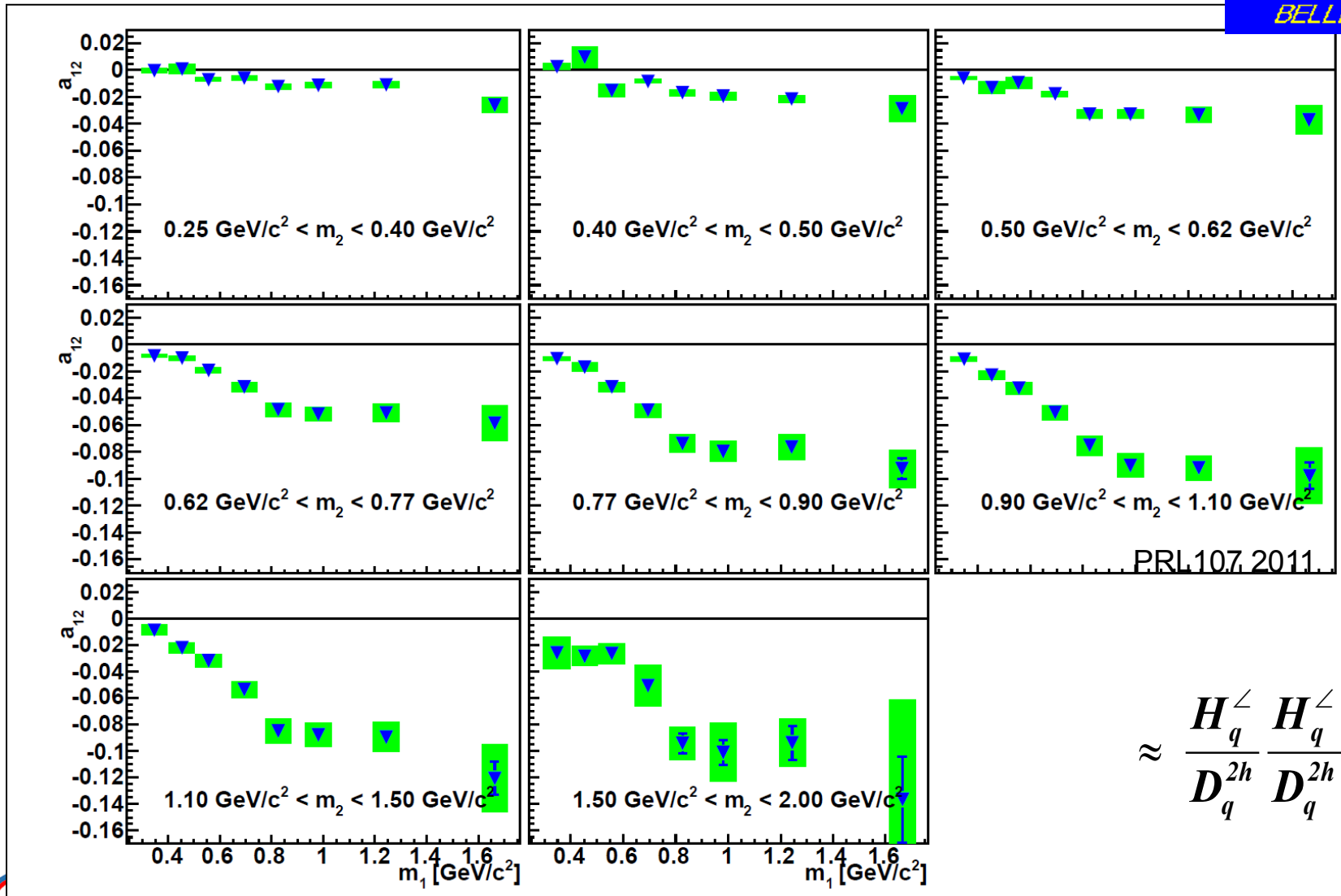
HERMES proton
 first evidence for
 non-zero dihadron FF,
 same sign of Collins
 asymmetry for π^+

PLB 713 2012, PLB736 2014



COMPASS
 deuteron:
 compatible with zero
 proton:
 same sign and shape
 slightly higher
 than Collins asymmetry
 for h^+

dihadron FF

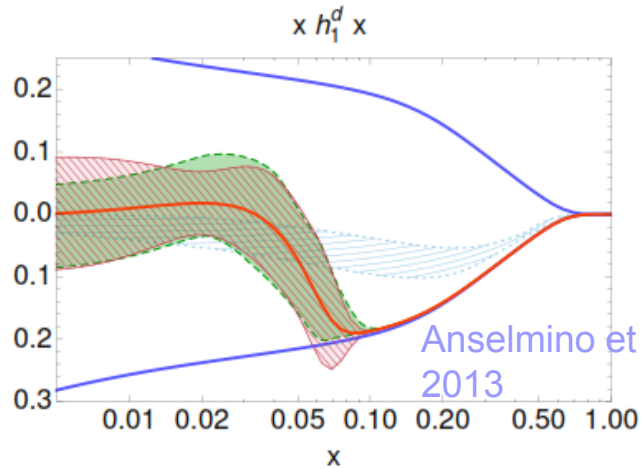
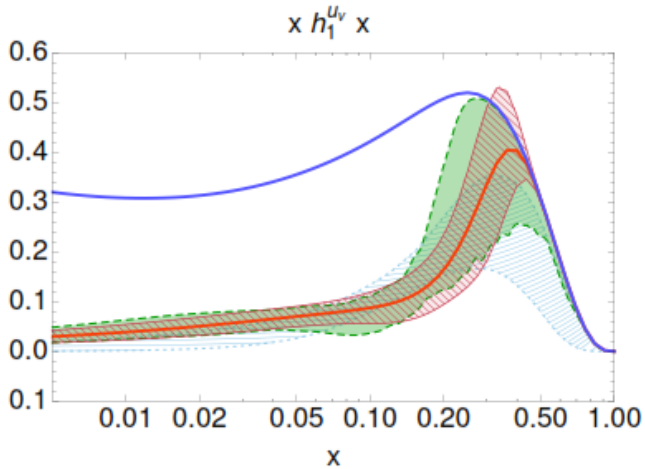
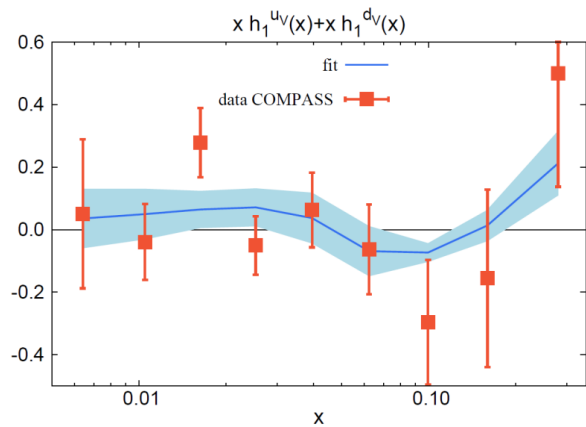
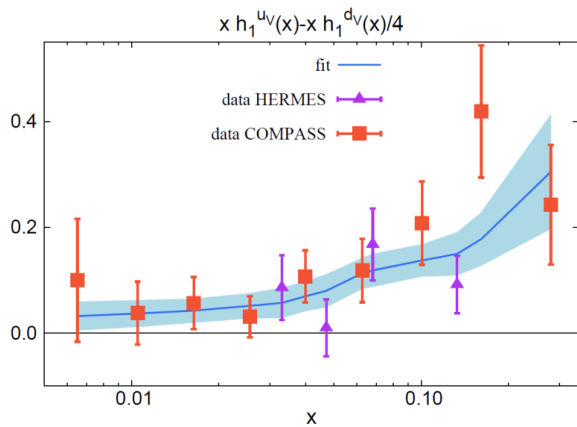


$$\approx \frac{H_q^\angle}{D_q^{2h}} \frac{H_q^\angle}{D_q^{2h}}$$

Transversity from 2h asymmetries

Bacchetta Courtoy Radici JHEP 1303 2013

D_q^{2h} from PYTHIA HERMES p, COMPASS p and d, Belle data
 → linear combinations of transversity for u and d valence quark
 fit with parametrisations → transversity PDFs



flexible

Anselmino et al
2013

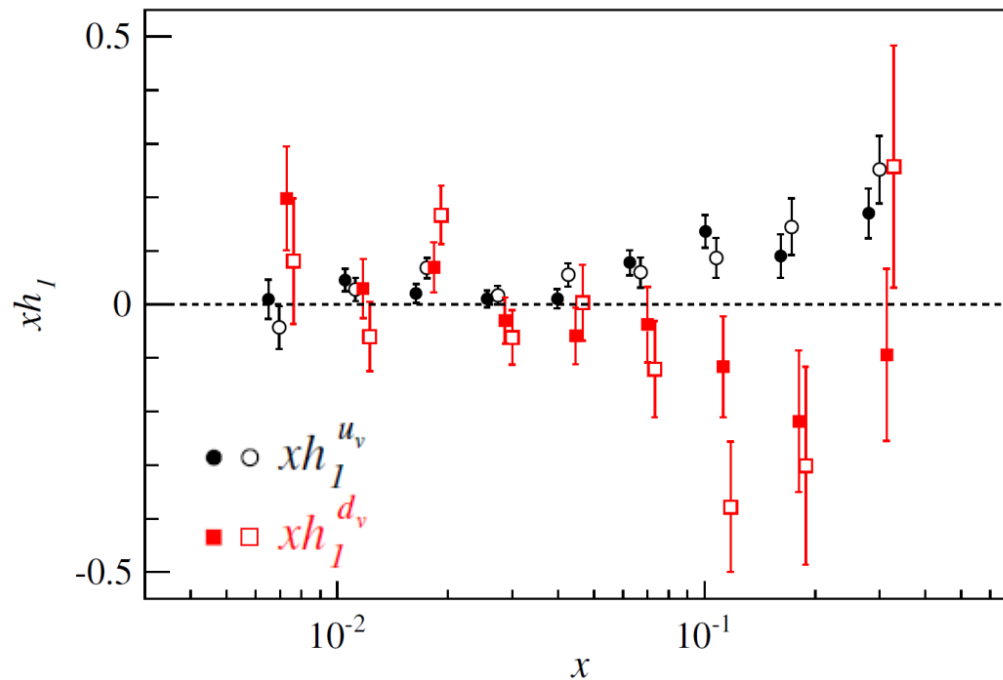
Transversity from 2h asymmetries

also possible: point-to-point extraction

one can use directly the COMPASS p and d data, and the Belle data (plus some “reasonable” assumptions) to evaluate the analysing power

advantages:

- no MC nor parametrisation is needed
- the same technique used for the Collins asymmetries



open points: dihadron
closed points: Collins

further confirmation that k_T is not so relevant in this case

Martin Bradamante Barone
PRD91 2015

dihadron asymmetry - new ideas

dihadron asymmetry - new ideas

Gliske, Bacchetta, Radici PRD90 2014, P.R.D91 2015

new partial wave expansion for fragmentation functions

- it gives a consistent framework for fragmentation into final states of any polarization
- shows that the two-hadron SIDIS cross sections, at any twist, can be derived from single-hadron SIDIS cross section
- two-hadron SIDIS cross section is given up to subleading twist, including the dependence upon the transverse momentum of involved particles

$$D_1 = \sum_{\ell=0}^{\ell_{\max}} \sum_{m=-\ell}^{\ell} P_{\ell,m}(\cos \vartheta) \cos(m(\phi_{R_\perp} - \phi_p)) \\ \times D_1^{|\ell,m\rangle}(z, M_h, |\mathbf{p}_T|),$$

$$H_1^\perp = \sum_{\ell=0}^{\ell_{\max}} \sum_{m=-\ell}^{\ell} P_{\ell,m}(\cos \vartheta) e^{im(\phi_{R_\perp} - \phi_p)} \\ \times H_1^{\perp|\ell,m\rangle}(z, M_h, |\mathbf{p}_T|),$$

not easy ...
→ HERMES

dihadron asymmetry - new ideas

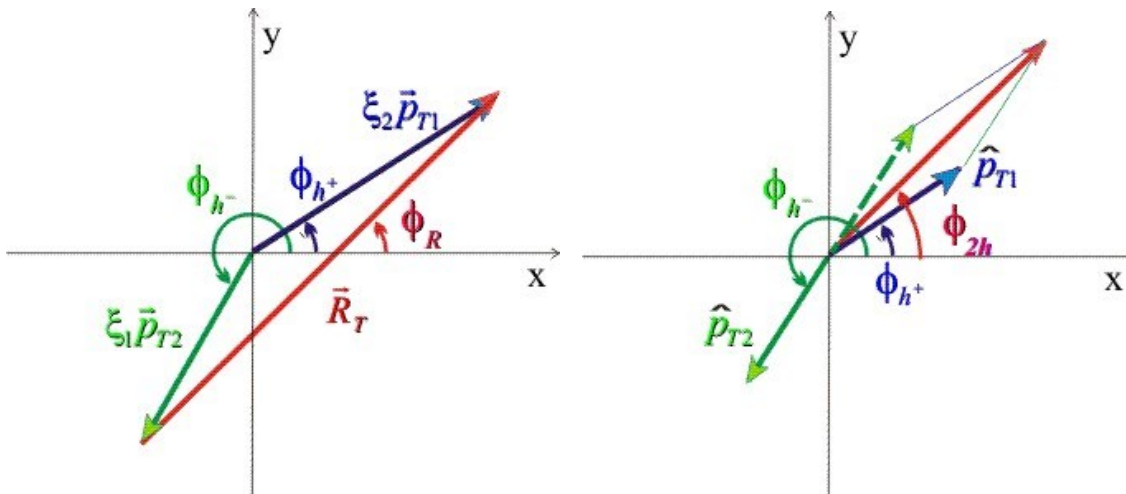
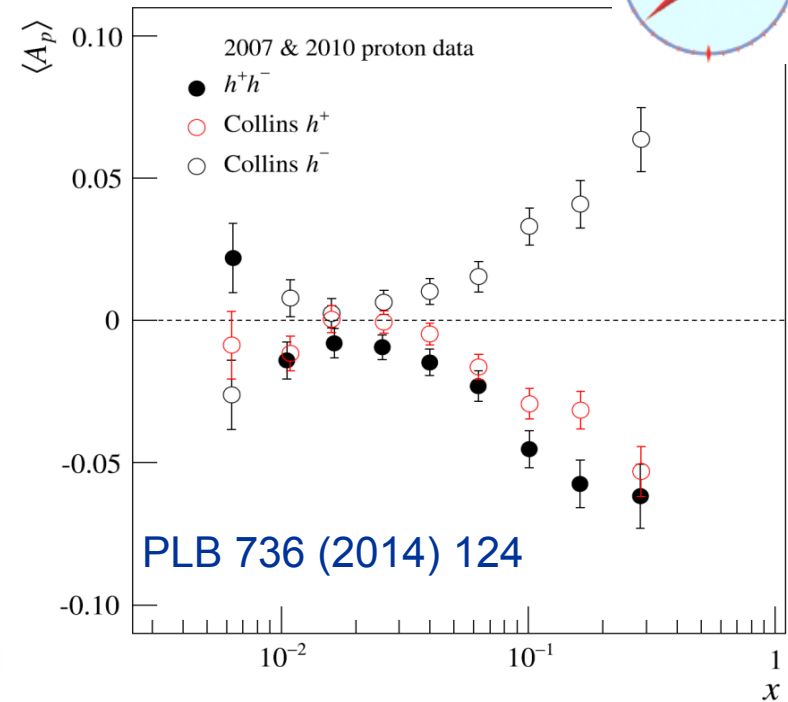
interplay between dihadron and single hadron asymmetries



known intriguing results

- Collins asymmetry for h^+ and for h^-
“mirror symmetry”
- dihadron asymmetry
only somewhat larger than h^+ Collins

→ first studies of the correlations between the relevant azimuthal angles and the corresponding asymmetries $\phi_R \sim \phi_{2h}$



hints for a common origin
of the Collins FF and DiFF
Como 2013, DSpin2013, PLB736 2014

interplay between single hadron and dihadron asymmetries



new: Collins like and di-hadron asymmetries vs $\Delta\phi = \phi_1 - \phi_2$
 using the events with at least 2 oppositely charged hadrons (2h sample):

Transversity2014, SPIN2014

the asymmetries are expected to be specular and maximum at $\Delta\phi \simeq \pi$

analytical calculations:

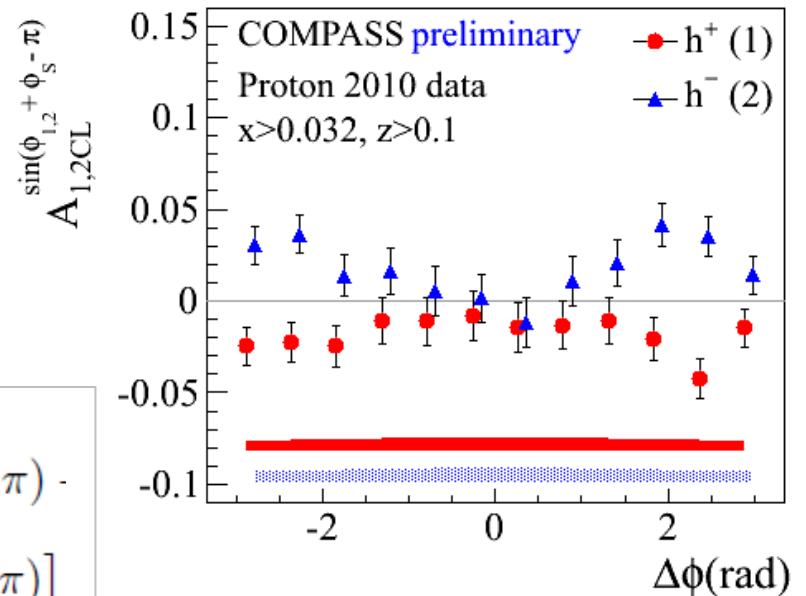
A. Kotzionian, PRD91 2015

$$\frac{d\sigma^{h_1 h_2}}{d\phi_1 d\phi_2 d\phi_S} = \sigma_U^{h_1 h_2} + S_T \left[\sigma_{C1}^{h_1 h_2} \sin(\phi_1 + \phi_S - \pi) \cdot \right. \\ \left. + \sigma_{C2}^{h_1 h_2} \sin(\phi_2 + \phi_S - \pi) \right]$$



$$A_{CL1}^{\sin(\phi_1 + \phi_S - \pi)} = \frac{1}{D_{NN}} \frac{\sigma_{C1}^{h_1 h_2} + \sigma_{C2}^{h_1 h_2} \cos \Delta\phi}{\sigma_U^{h_1 h_2}}$$

$$A_{CL2}^{\sin(\phi_2 + \phi_S - \pi)} = \frac{1}{D_{NN}} \frac{\sigma_{C2}^{h_1 h_2} + \sigma_{C1}^{h_1 h_2} \cos \Delta\phi}{\sigma_U^{h_1 h_2}}$$



good agreement with data if

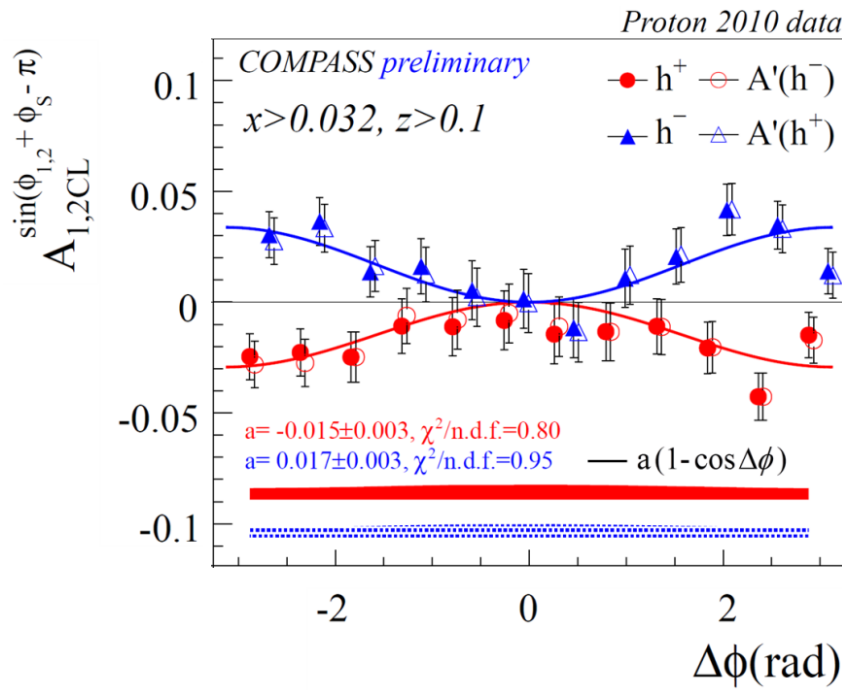
$$\sigma_{C1}^{h_1 h_2} = -\sigma_{C2}^{h_1 h_2}$$

interplay between single hadron and dihadron asymmetries



$$\sigma_{C1}^{h_1 h_2} = -\sigma_{C2}^{h_1 h_2} \quad \Rightarrow \quad \begin{cases} A_{CL1}^{\sin(\phi_1 + \phi_S - \pi)} = \frac{1}{D_{NN}} \frac{\sigma_{C1}^{h_1 h_2}}{\sigma_U^{h_1 h_2}} \cdot (1 - \cos \Delta\phi) \\ A_{CL2}^{\sin(\phi_2 + \phi_S - \pi)} = -A_{CL1}^{\sin(\phi_1 + \phi_S - \pi)} \end{cases}$$

mirror symmetry



interplay between single hadron and dihadron asymmetries



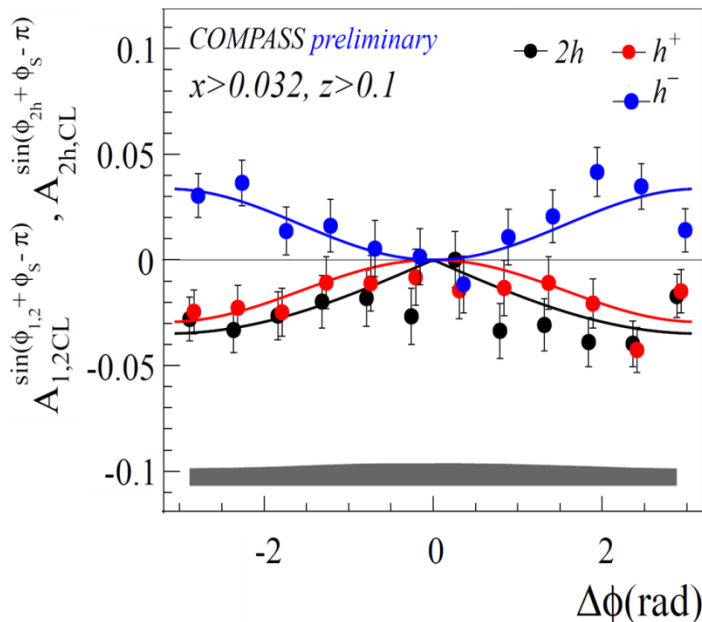
$$\sigma_{C1}^{h_1 h_2} = -\sigma_{C2}^{h_1 h_2} \quad \Rightarrow \quad \left\{ \begin{array}{l} A_{CL1}^{\sin(\phi_1 + \phi_S - \pi)} = \frac{1}{D_{NN}} \frac{\sigma_{C1}^{h_1 h_2}}{\sigma_U^{h_1 h_2}} \cdot (1 - \cos \Delta\phi) \\ A_{CL2}^{\sin(\phi_2 + \phi_S - \pi)} = -A_{CL1}^{\sin(\phi_1 + \phi_S - \pi)} \end{array} \right.$$

mirror symmetry

rewriting the cross-section in terms of ϕ_{2h} and $\Delta\phi$ one easily obtains

$$A_{2h,CL}^{\sin(\phi_{2h} + \phi_S - \pi)} = \frac{1}{D_{NN}} \frac{\sigma_{C1}^{h_1 h_2}}{\sigma_U^{h_1 h_2}} \cdot \sqrt{2(1 - \cos \Delta\phi)}$$

a very simple relationship between dihadron and single hadron asymmetries in the 2h sample



in agreement with data

ratio of the integrals: $4/\pi$
slightly larger than h^+

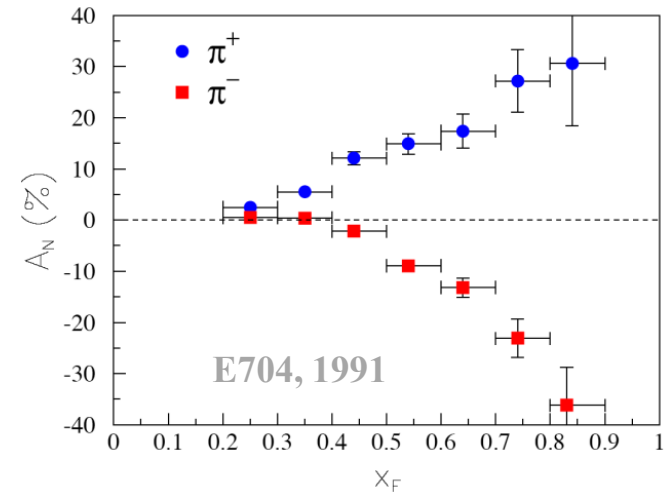
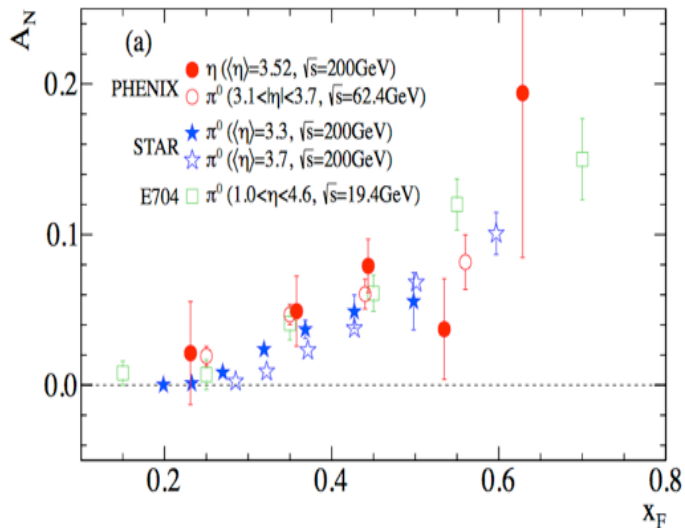
it would be interesting to perform the corresponding studies in e^+e^-

Transversity in pp

Transversity in pp

inclusive pion production $p^\uparrow p \rightarrow \pi X$

one of the most famous measurements
and one of the motivations for the last
20 years of studies of transverse spin
effects



large spin effects confirmed at RHIC
still not clear how large is the
contribution of transversity

Drell-Yan:

convolution of u and \bar{u} (d and \bar{d}) transversity distributions \rightarrow difficult

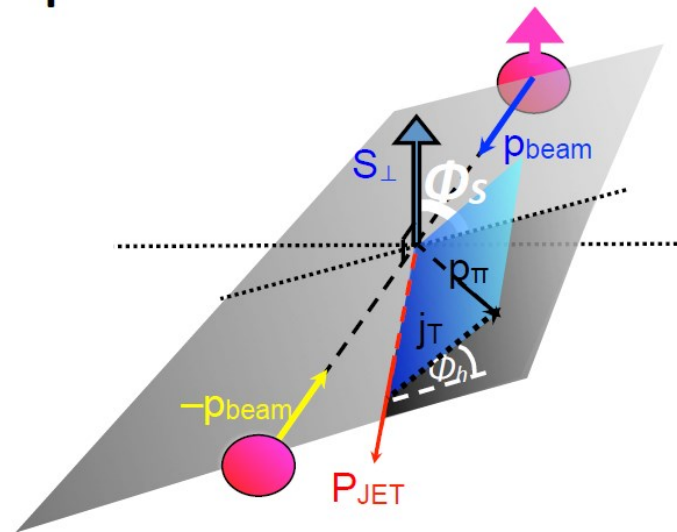
still ...

Transversity in pp

hadrons inside a jet

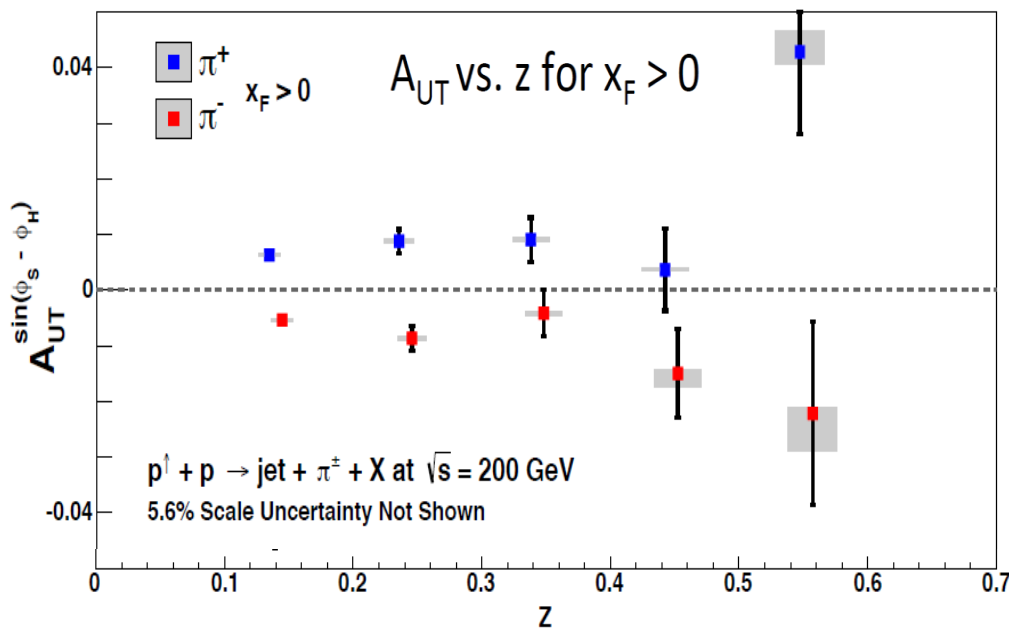
Collins asymmetry

$$\phi_C = \phi_S - \phi_H$$



STAR Preliminary

SPIN2014



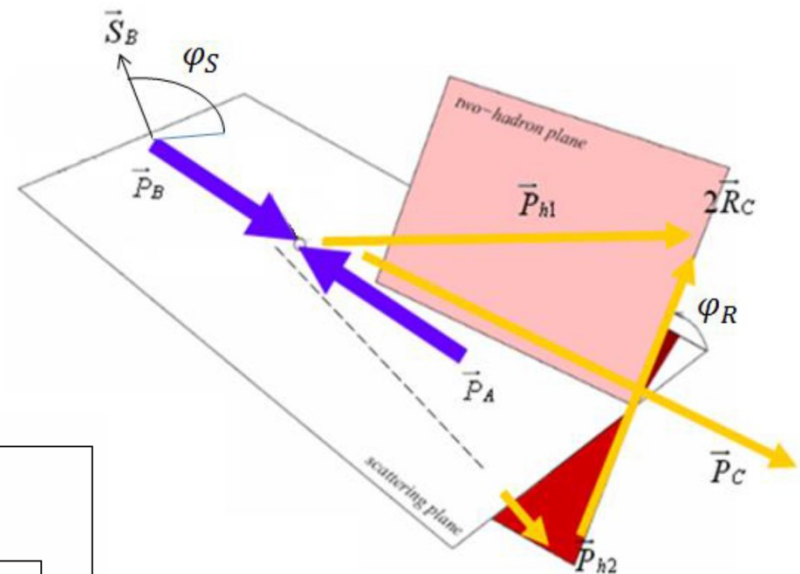
“ the first statistically significant non-zero Collins asymmetries measured in hadronic collisions ”

Transversity in pp

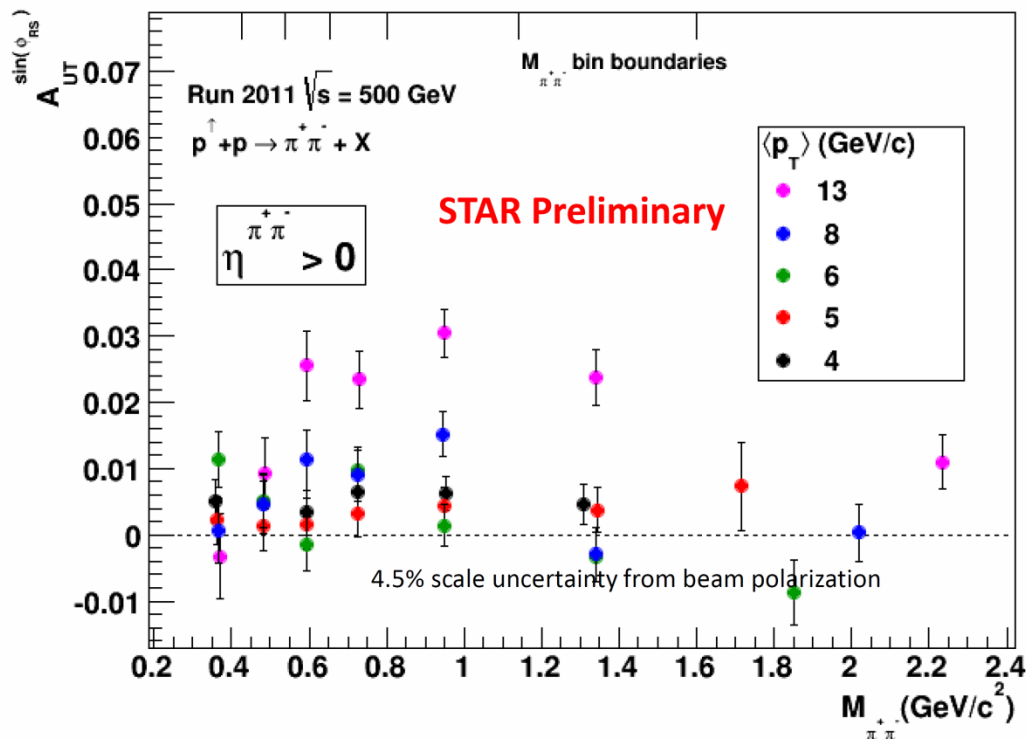
hadrons inside a jet

di-hadron asymmetry

$$\varphi_{RS} = \varphi_S - \varphi_R$$



SPIN2014



“results are at much higher Q^2 and sample a different mixture of quark flavors than SIDIS”
 complementary input

other SIDIS transverse spin asymmetries

$$\begin{aligned}
 & + |S_{\perp}| \left[\overset{f_{1T}^{\perp} D_1}{\sin(\phi_h - \phi_S)} \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & \quad + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & \quad \left. + \overset{h_1 H_1^{\perp}}{\sqrt{2\varepsilon(1+\varepsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)}} \right] \\
 & + |S_{\perp}| \lambda_e \left[\sqrt{1 - \varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1 - \varepsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} \right. \\
 & \quad \left. + \sqrt{2\varepsilon(1 - \varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \Bigg\},
 \end{aligned}$$

**all of them (and more ...) have been measured on p / d / n by
COMPASS, HERMES, JLab**

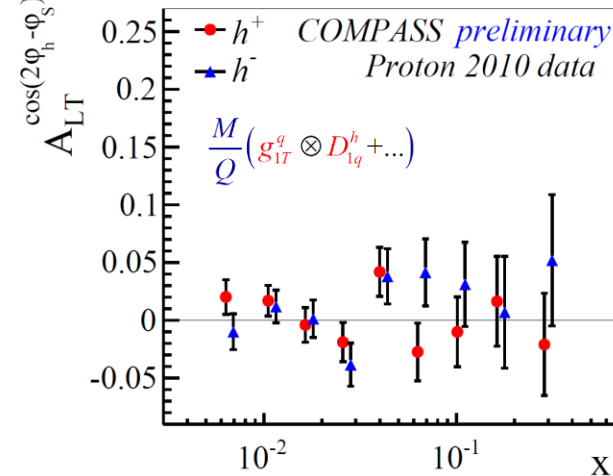
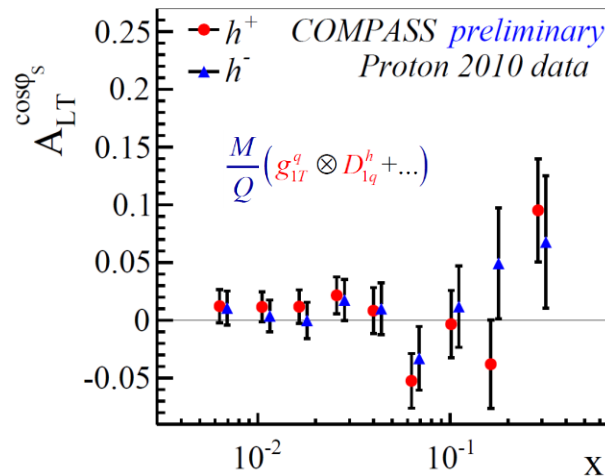
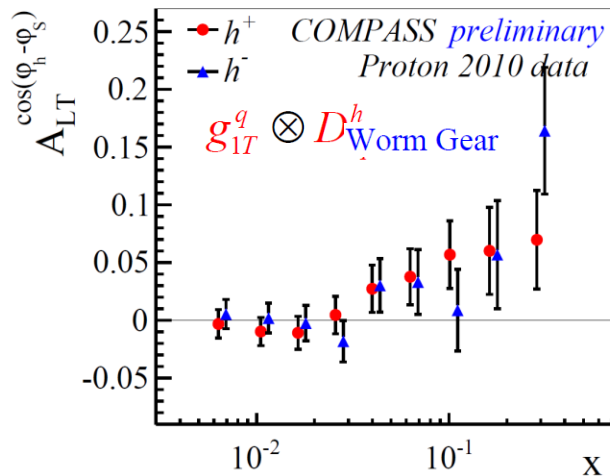
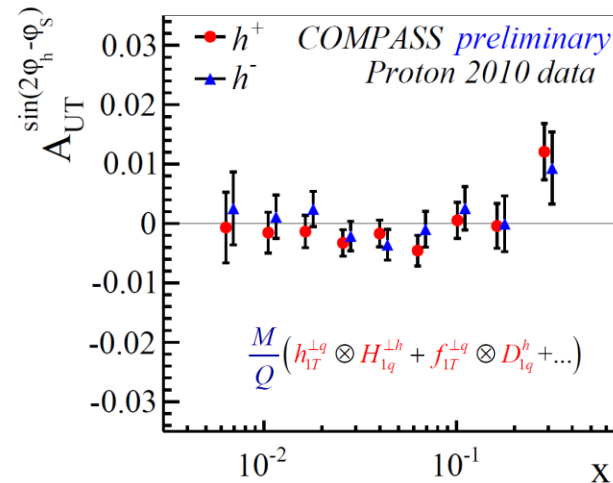
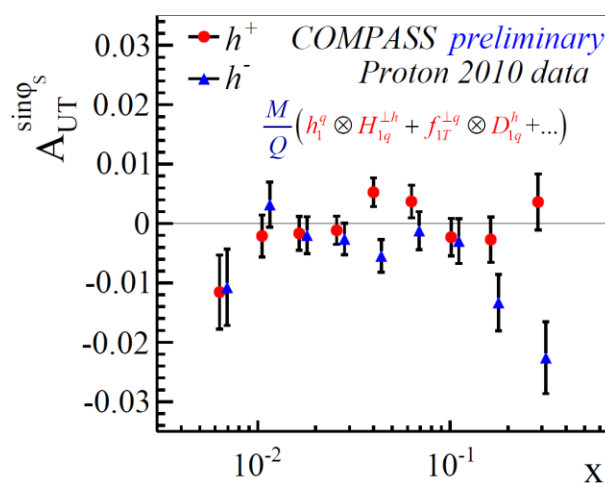
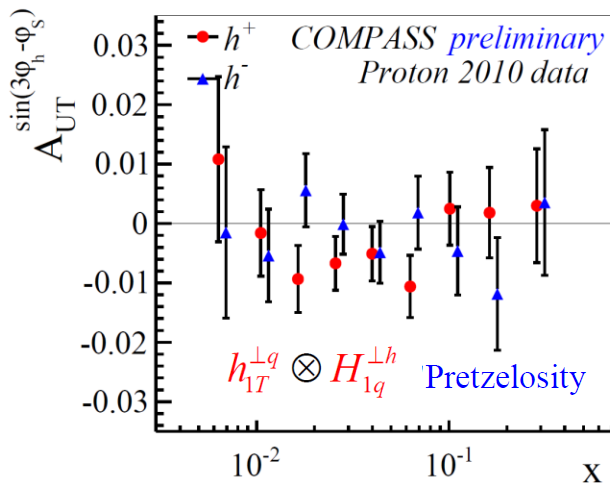
***preliminary results for multidimensional analysis also
produced at COMPASS and HERMES (SPIN2014)***

other SIDIS transverse spin asymmetries

measured on p (HERMES, COMPASS)
d (COMPASS) and n (JLab)

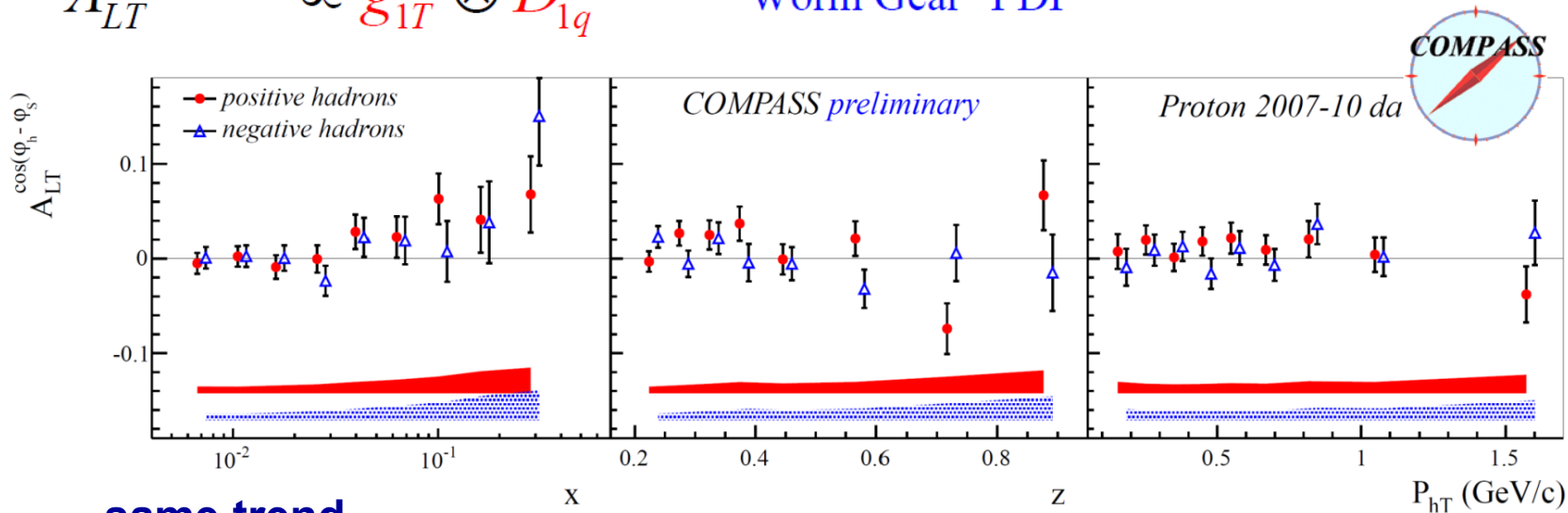


proton

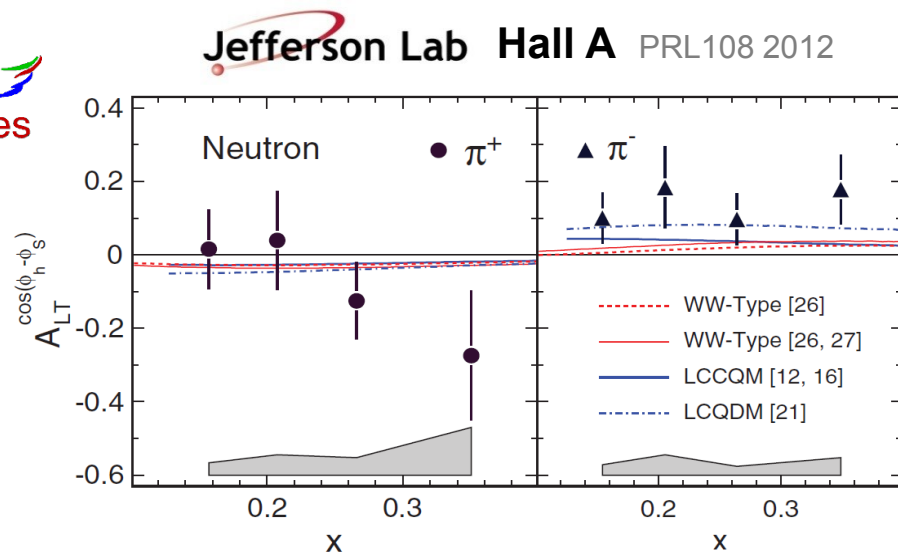
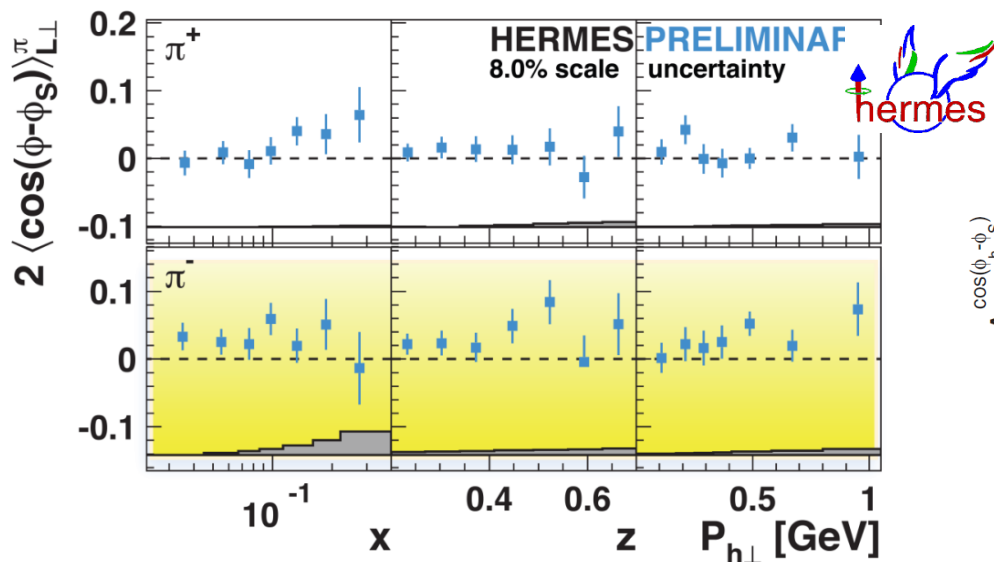


other SIDIS transverse spin asymmetries

$$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h \quad \text{"Worm Gear" PDF}$$

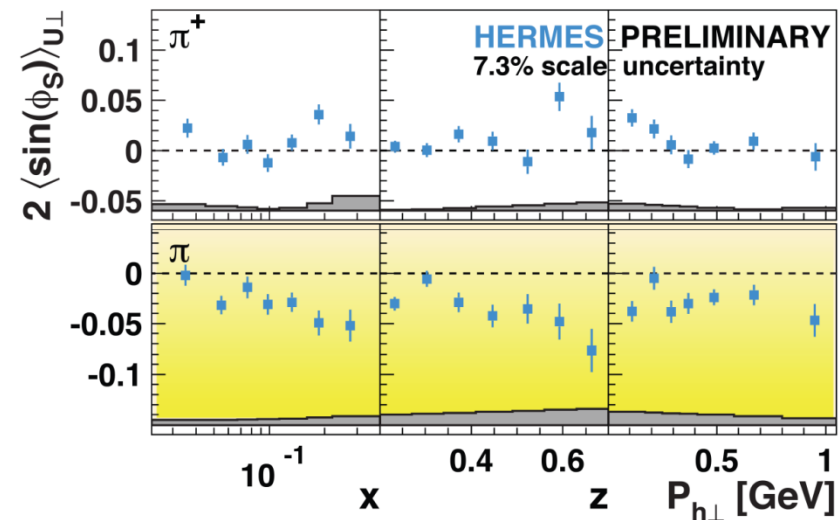
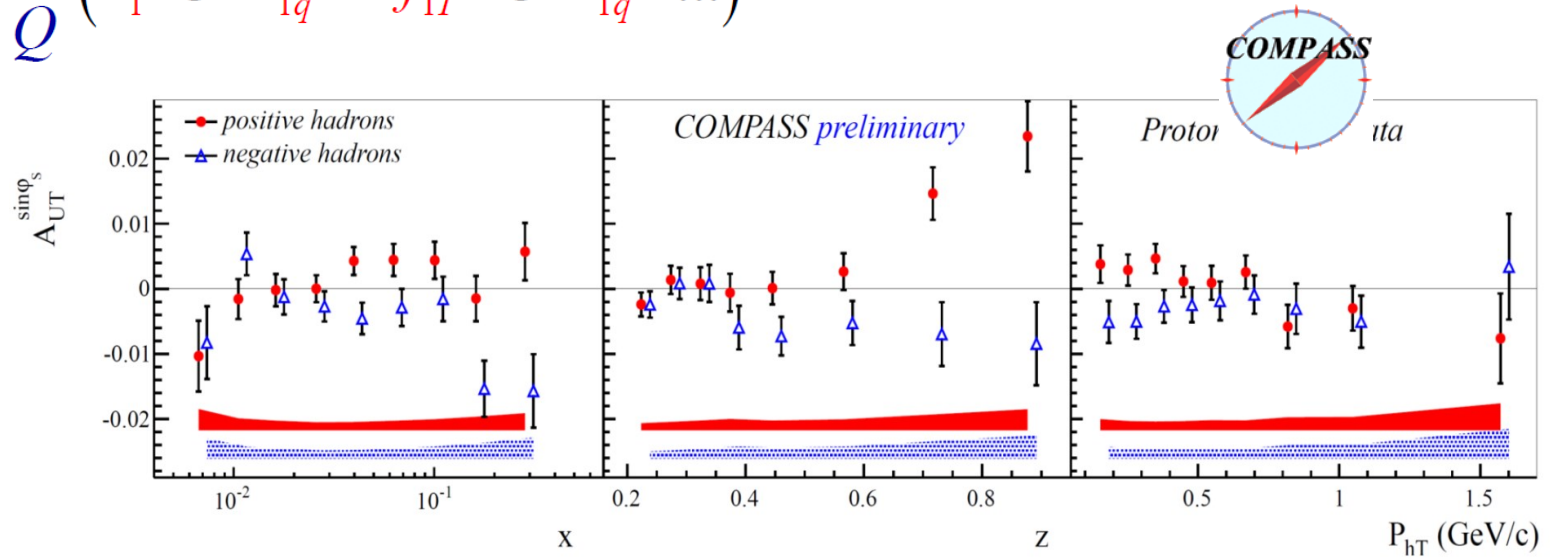


same trend



other SIDIS transverse spin asymmetries

$$A_{UT}^{\sin\phi_s} \propto \frac{M}{Q} \left(h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$



considerably larger at HERMES
as expected

Glue Sivers function



Gluon Sivers function

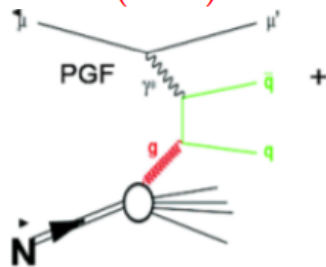


1. measurement of the “Sivers” asymmetry in $lp \rightarrow l' hh X$

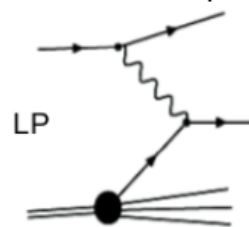
$$\phi_P - \phi_S, \quad P = p_1 + p_2$$

2. extraction of the asymmetries for **Photon-Gluon Fusion**,
Leading Process and QCD Compton using NN trained on MC data

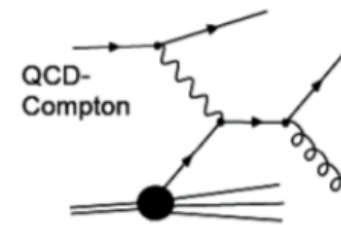
photon-gluon fusion
(PGF)



Leading process (LP)-
main DIS process



QCD Compton

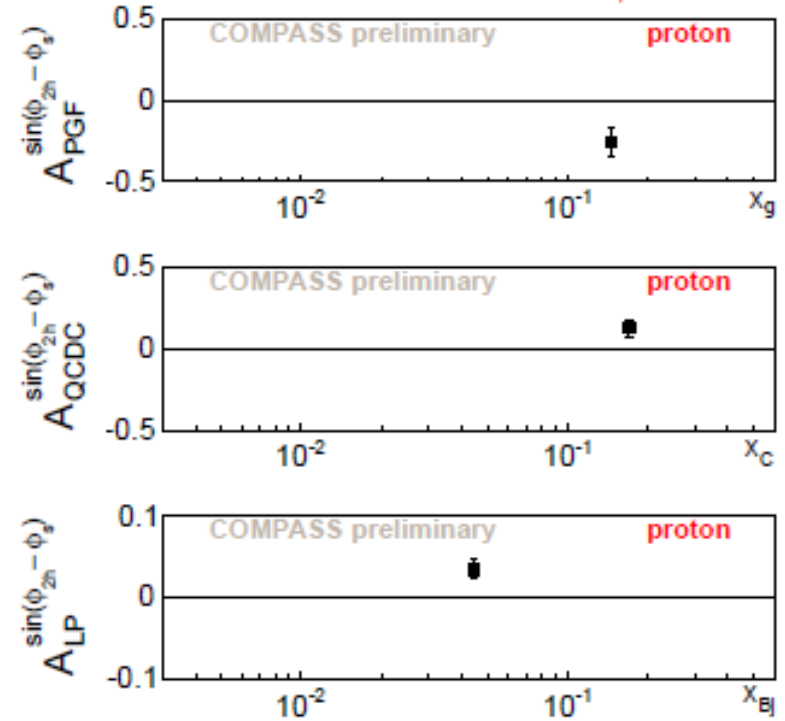
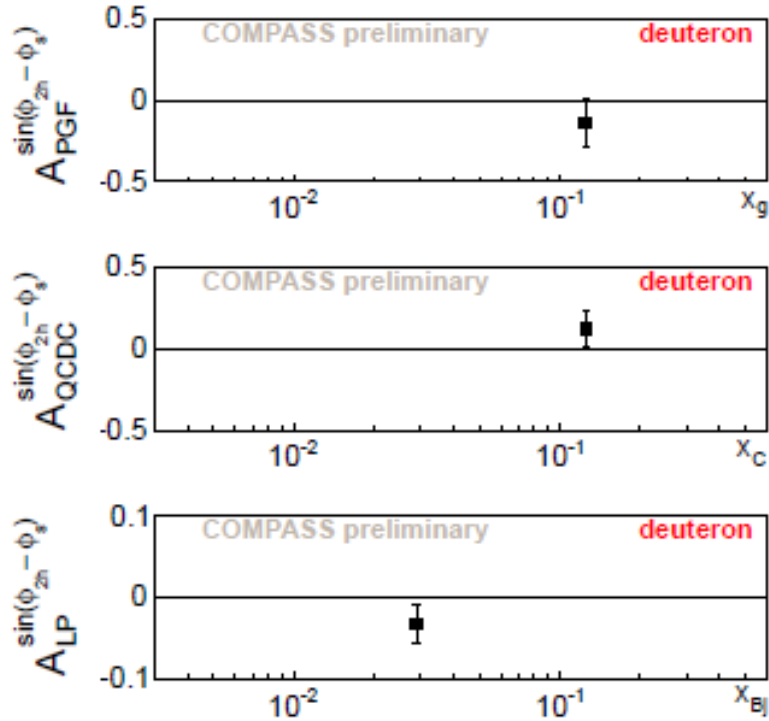


the sample with PGF events is enhanced by selecting DIS events with at
least 2 hadrons with large p_T ($p_{T1} > 0.7$, $p_{T2} > 0.4$ GeV/c)

Gloun Sivers function



QNP2015



deuteron $A_{PGF}^{\sin(\phi_{2h} - \phi_s)} = -0.14 \pm 0.15(stat.) \pm 0.06(syst.)$ $\langle x_G \rangle = 0.13$

proton $A_{PGF}^{\sin(\phi_{2h} - \phi_s)} = -0.26 \pm 0.09(stat.) \pm 0.08(syst.)$ $\langle x_G \rangle = 0.15$

TSA A_N in $lp \rightarrow hX$ processes

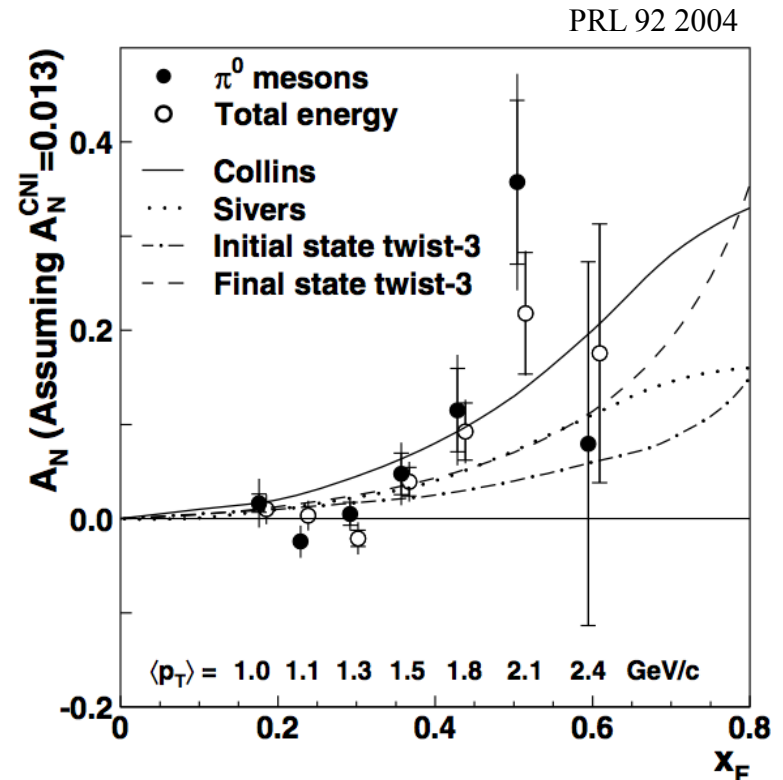
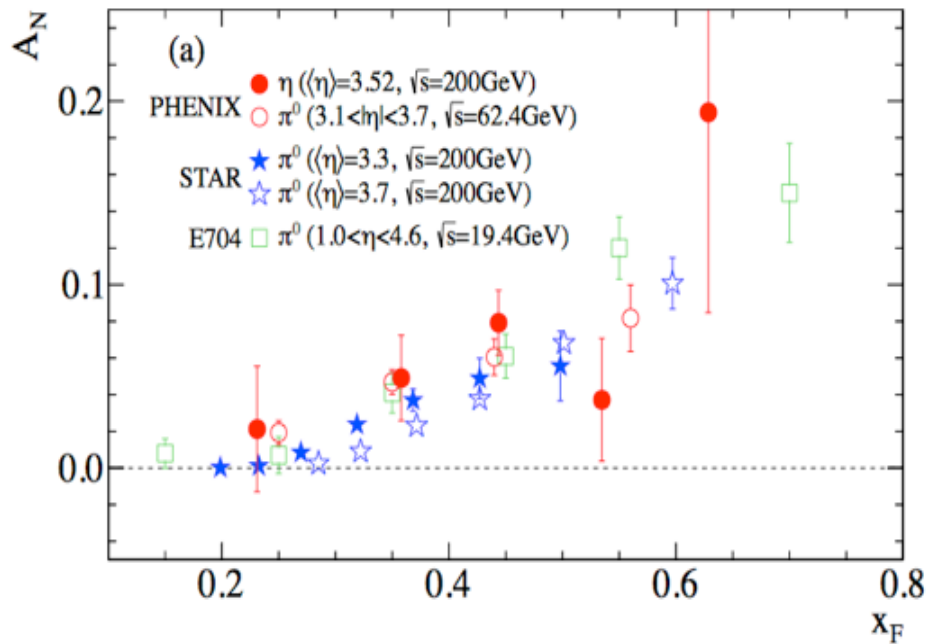
TSA A_N in $lp \rightarrow hX$ processes

motivation:

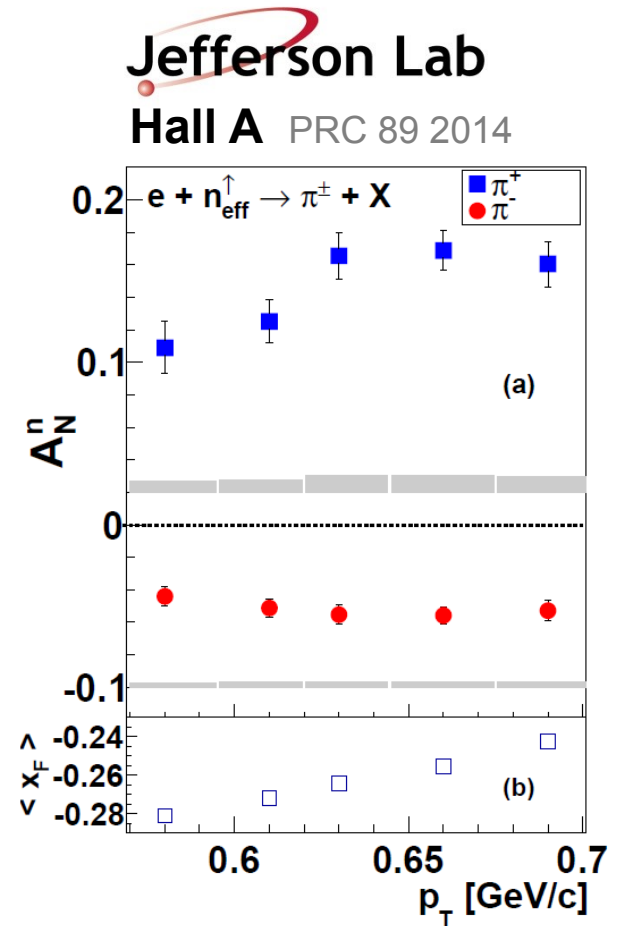
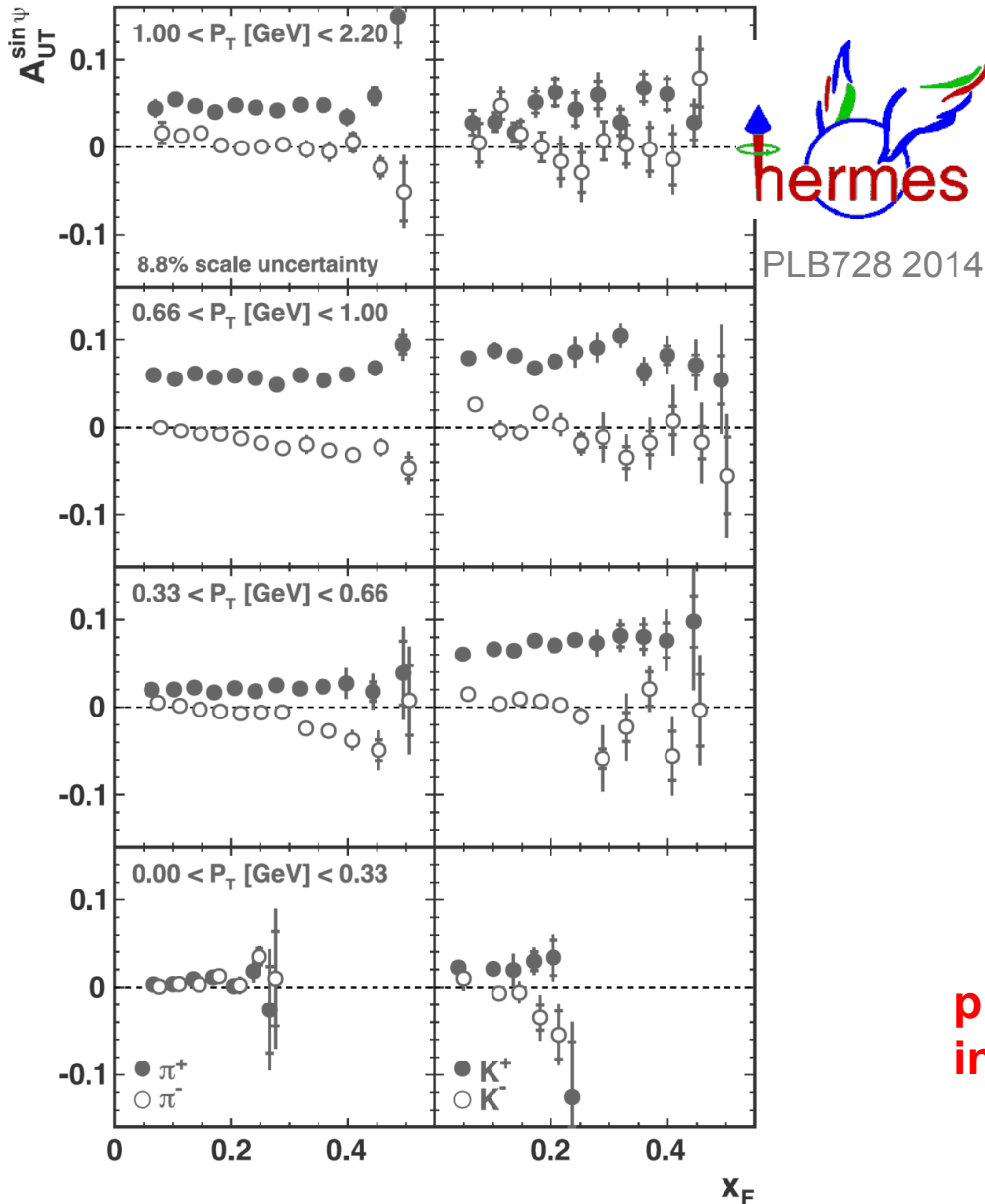
direct test of the validity of the TMD factorization in $lp \rightarrow hX$

→ understanding TSA in $pp^\uparrow \rightarrow hX$

M. Anselmino et al PRD 81 2010



TSA A_N in $lp \rightarrow hX$ processes



phenomenological interpretation
in progress

summary

many new SIDIS results, not all easy to explain

**the SIDIS data collected in so far are unique
and the analysis are not yet over**

more information is still hidden in the data and has to be extracted
from SIDIS at COMPASS, HERMES, JLab experiments
pp at RHIC
e⁺e⁻ at Belle / Babar / BES

**while waiting for the results of the new complementary measurements
and experiments**
at COMPASS too!