

Spin of the nucleon: The COMPASS programme, present and future

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on behalf of the COMPASS Collaboration



International School of Nuclear Physics
Probing Hadron Structure with Lepton and Hadron Beams

Erice-Sicily
September 16-24, 2015



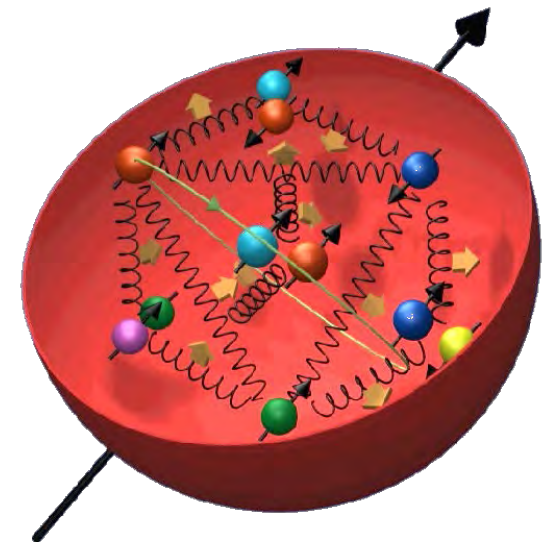
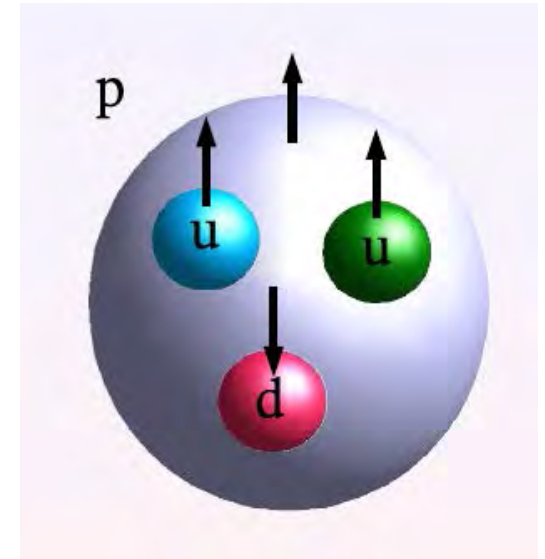
Outline

- Introduction
- Experiment
- Longitudinal spin: DIS results
- Longitudinal spin: SIDIS results
- COMPASS-II
- Add-on: Physics with hadrons beams

- Not covered (→ F. Bradamante):
 - transverse spin, TMDs
 - hadron multiplicities and fragmentation functions

1. Introduction: nucleon spin

- Nucleon
 - 3 valence quarks
 - sea quark-antiquark pairs
 - gluons
- Spin
 - quark/antiquark spins
 - gluon spins
 - orbital angular momentum



Spin: Static Quark Model

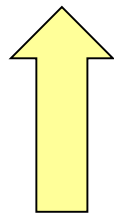
- notation: $\Delta q = q^+ - q^-$
- Proton: $\Delta u = \frac{4}{3}$ $\Delta d = -\frac{1}{3}$ $\Delta s = 0$ (in \hbar)

$$\Delta\Sigma = \Delta u + \Delta d + \Delta s = 1$$

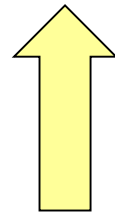
- EMC 1988: $\Delta\Sigma \approx 0.12$ "spin crisis"
- Now: $\Delta\Sigma \approx 0.30$
- Quark spins do not dominantly carry the nucleon spin

Where is the proton spin?

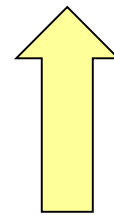
$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L_z$$



small



smallish,
sign?



unknown,
quark & gluon

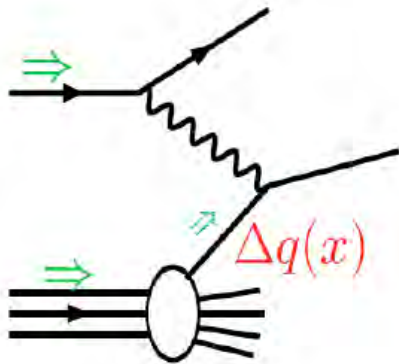
in infinite-momentum frame

Tools to study the partonic nucleon structure

Factorisation of hard interaction and nonperturbative nucleon structure/fragmentation:

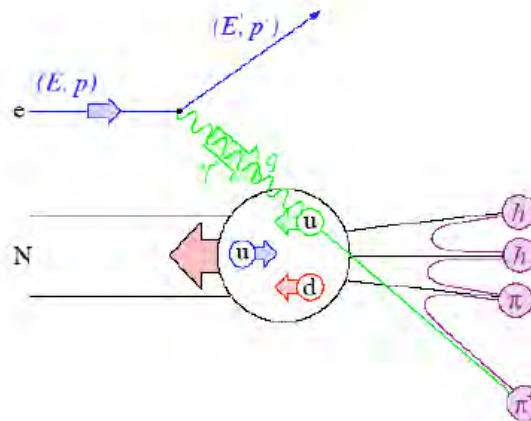
- PDF parton distribution functions
- FF fragmentation functions

DIS



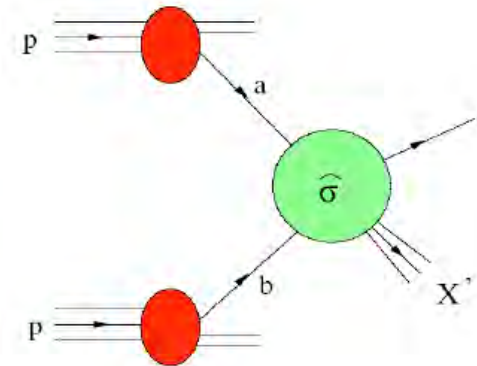
PDF

SIDIS



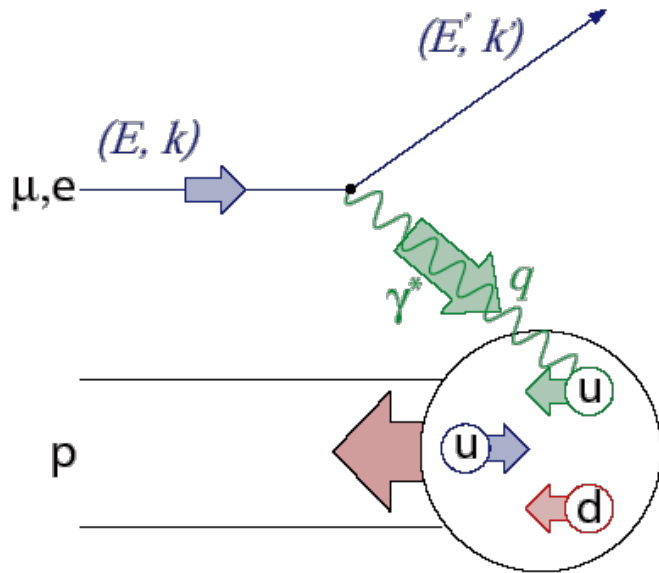
PDF \otimes FF

pp



PDF \otimes PDF

Deep inelastic scattering



$$Q^2 = -(k - k')^2 \stackrel{lab}{=} 4EE' \sin^2 \frac{\vartheta}{2}$$

$$P \cdot q \stackrel{lab}{=} M\nu = M(E - E')$$

$$P \cdot k \stackrel{lab}{=} ME$$

$$x \stackrel{lab}{=} \frac{Q^2}{2M\nu} = \frac{-q^2}{2P \cdot q}$$

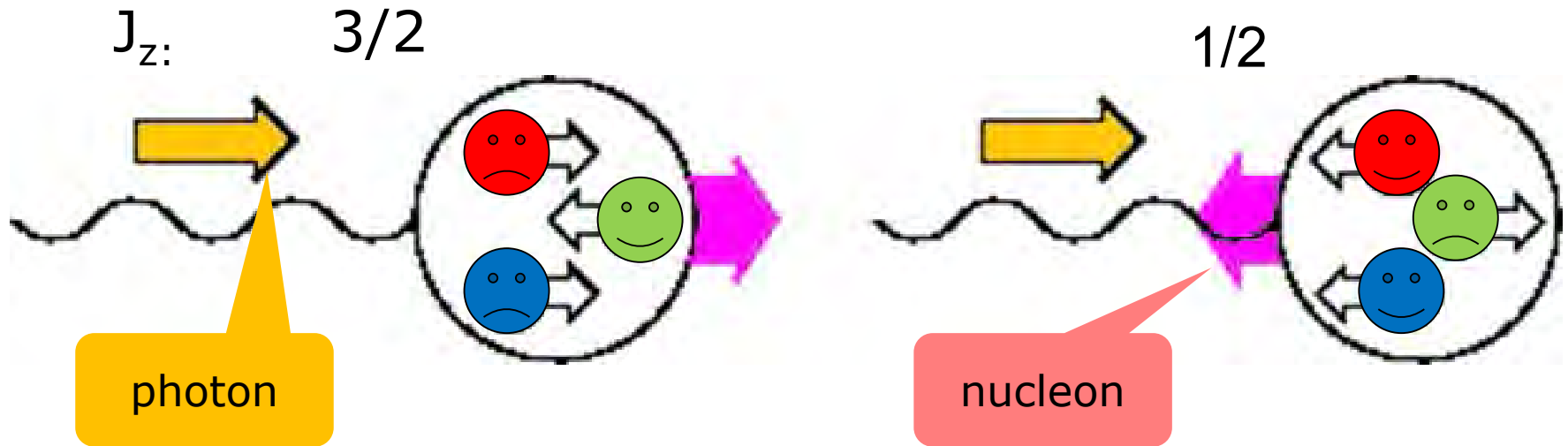
$$y \stackrel{lab}{=} \frac{\nu}{E} = \frac{P \cdot q}{P \cdot k}$$

$$0 \leq x, y \leq 1$$

Bjorken-x: fraction of longitudinal momentum carried by the struck quark in infinite-momentum frame (Breit)



Structure Function asymmetry

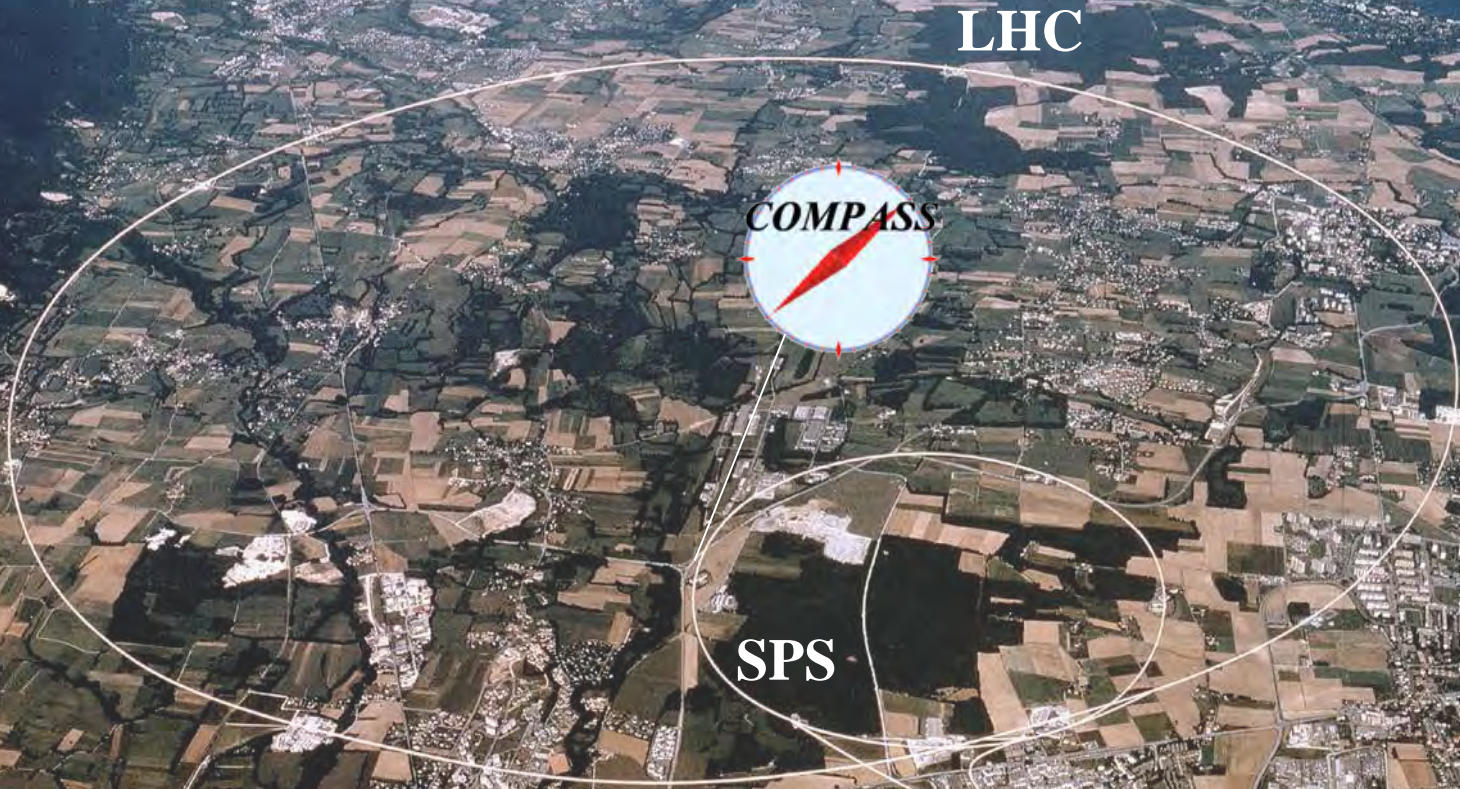


Measure longitudinal **double-spin** x-sect. asymmetries

$$A_1(x, Q^2) = \frac{\sum_q e_q^2 \Delta q(x, Q^2)}{\sum_q e_q^2 q(x, Q^2)} = \frac{g_1(x, Q^2)}{F_1(x, Q^2)}$$

2. The COMPASS experiment

COmmon Muon and Proton Apparatus for Structure and Spectroscopy"



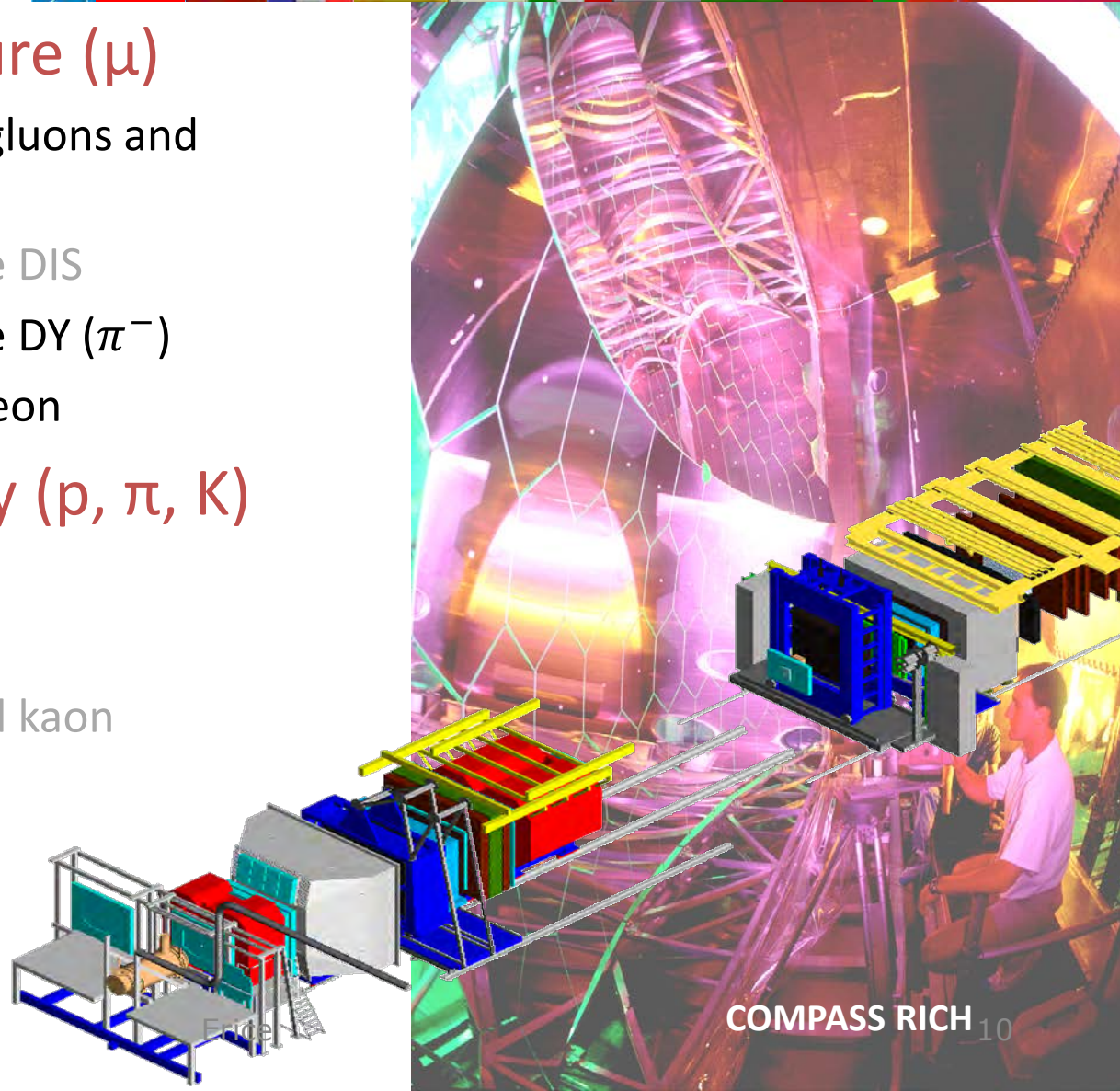


COMPASS: QCD structure of hadrons

data taking since 2002



- nucleon spin-structure (μ)
 - helicity distributions of gluons and quarks
 - transverse spin structure DIS
 - transverse spin structure DY (π^-)
 - 3D structure of the nucleon
- hadron spectroscopy (ρ , π , K)
 - light mesons, glue-balls
 - exotic mesons
 - polarisability of pion and kaon
- members:
 - 220 physicists,
13 countries



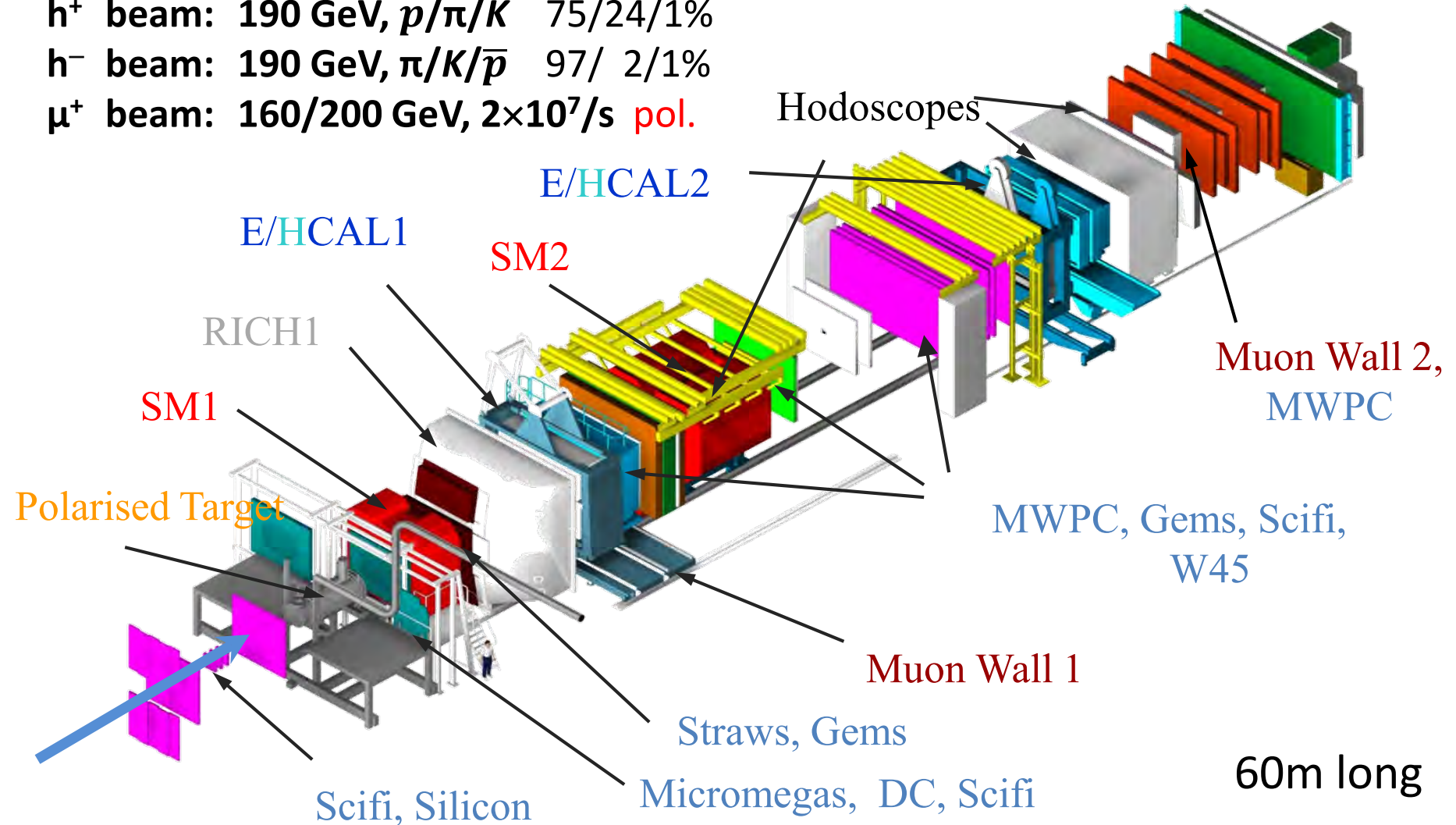


COMPASS spectrometer

h^+ beam: 190 GeV, $p/\pi/K$ 75/24/1%

h^- beam: 190 GeV, $\pi/K/\bar{p}$ 97/ 2/1%

μ^+ beam: 160/200 GeV, $2 \times 10^7/s$ pol.



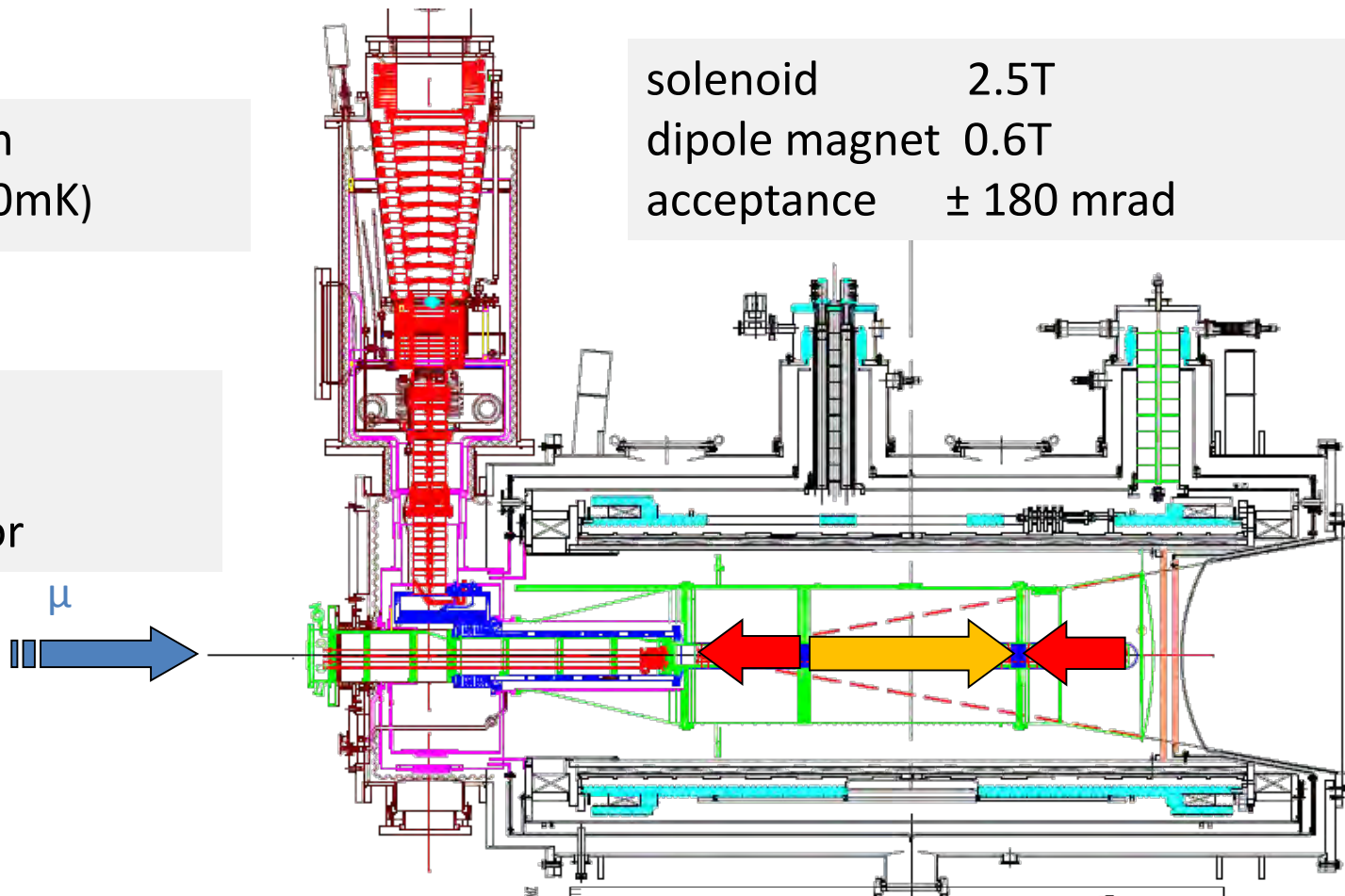
Polarized target system



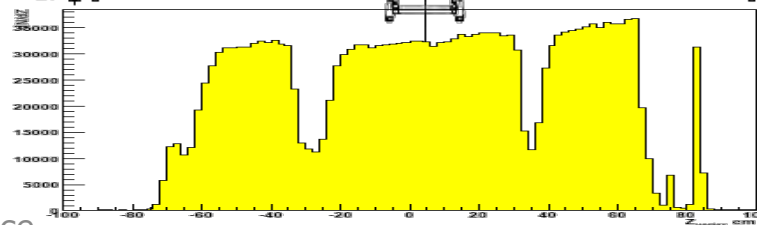
$^3\text{He} - ^4\text{He}$ dilution refrigerator ($T \sim 50\text{mK}$)

$^6\text{LiD}/\text{NH}_3$ (d/p)
50/90% pol.
40/16% dil. factor

solenoid 2.5T
dipole magnet 0.6T
acceptance ± 180 mrad

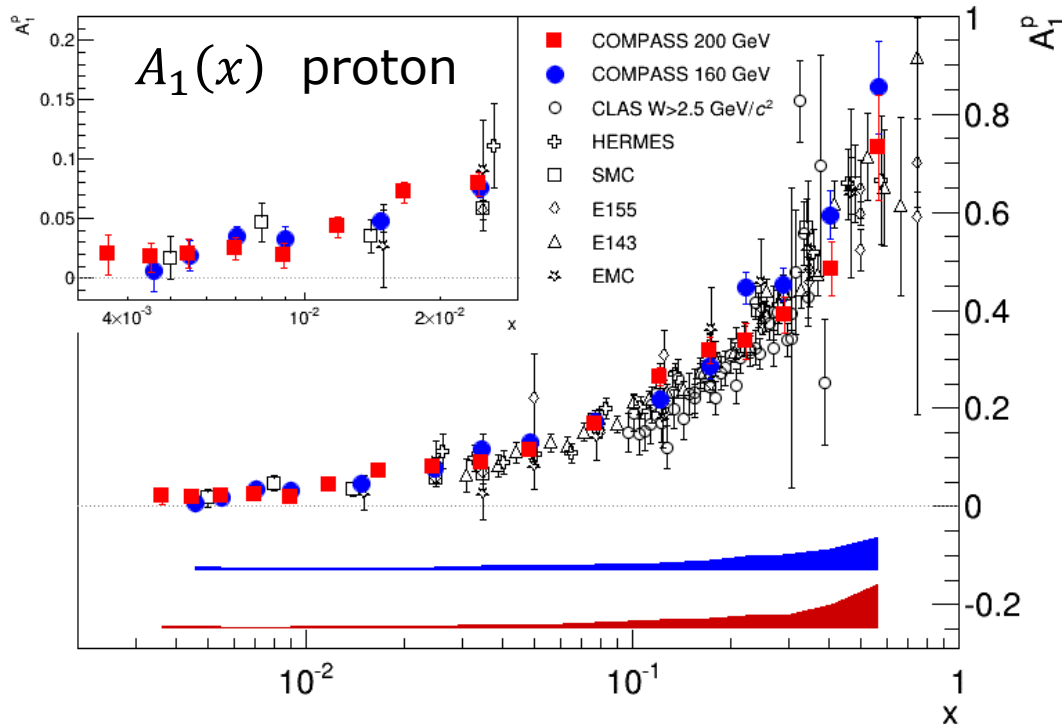


Reconstructed interaction vertices

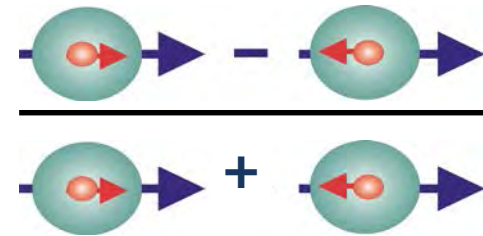


3. Longitudinal spin: DIS results

g_1 and PDFs

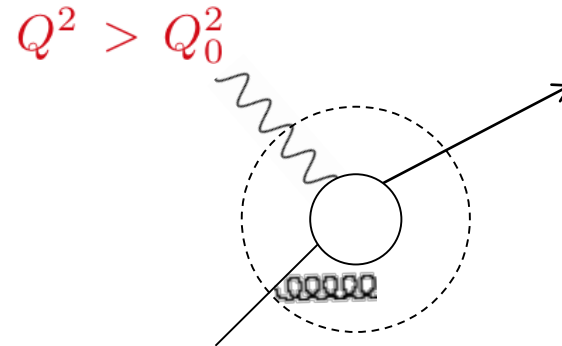
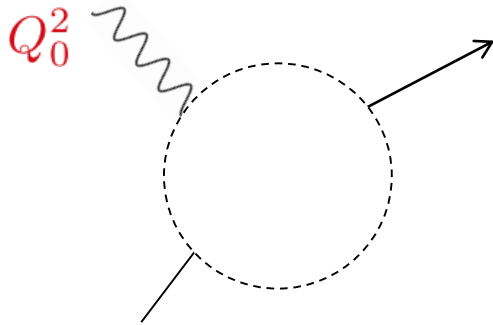


x : Bjorken x , fraction of nucleon mom. carried by struck quark in inf. mom. frame



$$A_1(x, Q^2) = \frac{\sum_q e_q^2 \Delta q(x, Q^2)}{\sum_q e_q^2 q(x, Q^2)} = \frac{g_1(x, Q^2)}{F_1(x, Q^2)}$$

Scaling violations (gluons)



- with increasing Q^2 more and more details are resolved
- quarks/gluons **split** and produce more partons
- the 'new' partons have **smaller x-Bjorken**
- PDFs and SFs became functions of Q^2 : $P(x) \rightarrow P(x, Q^2)$
- this Q^2 evolution is calculable in perturbative **QCD**, if the PDFs $P(x, Q_0^2)$ are known at some Q_0^2 (**DGLAP equations**)
- the x dependence is not described in pQCD
- The scaling violations depend on the gluon distribution

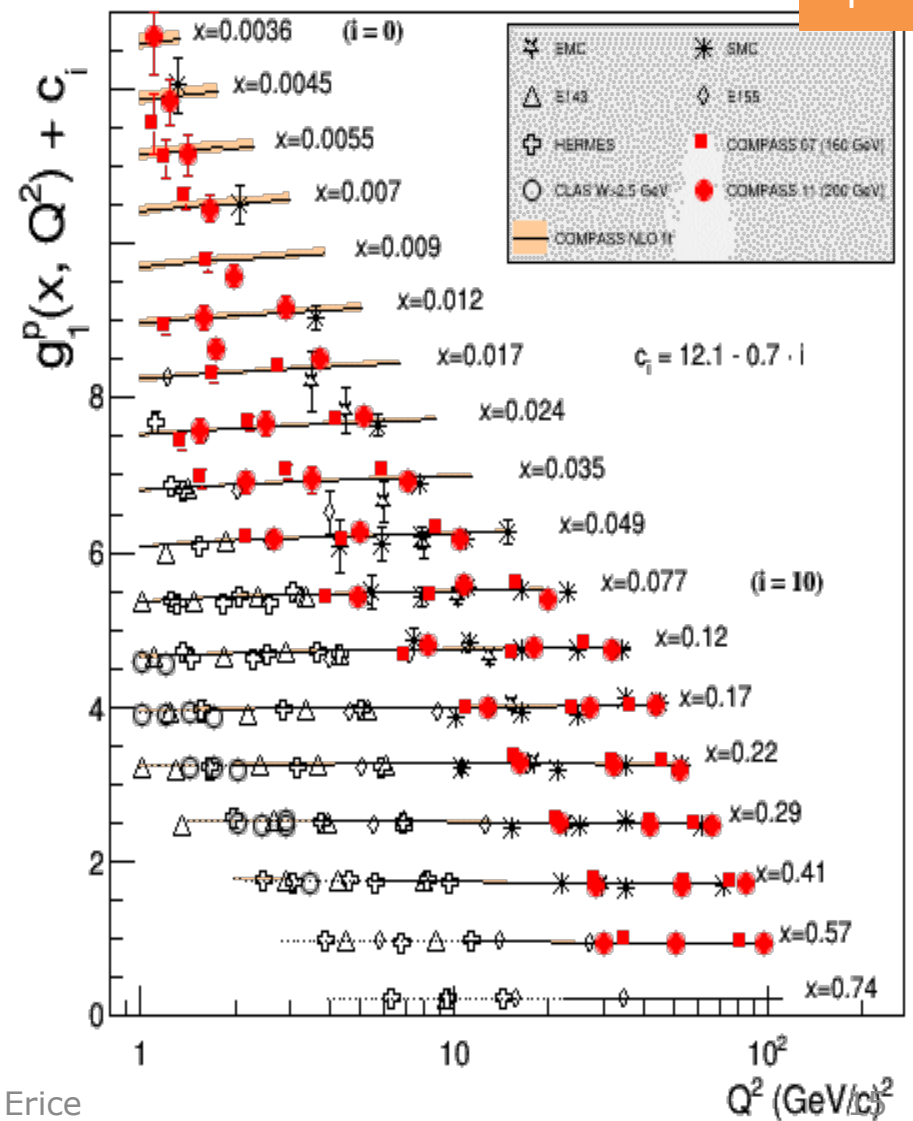
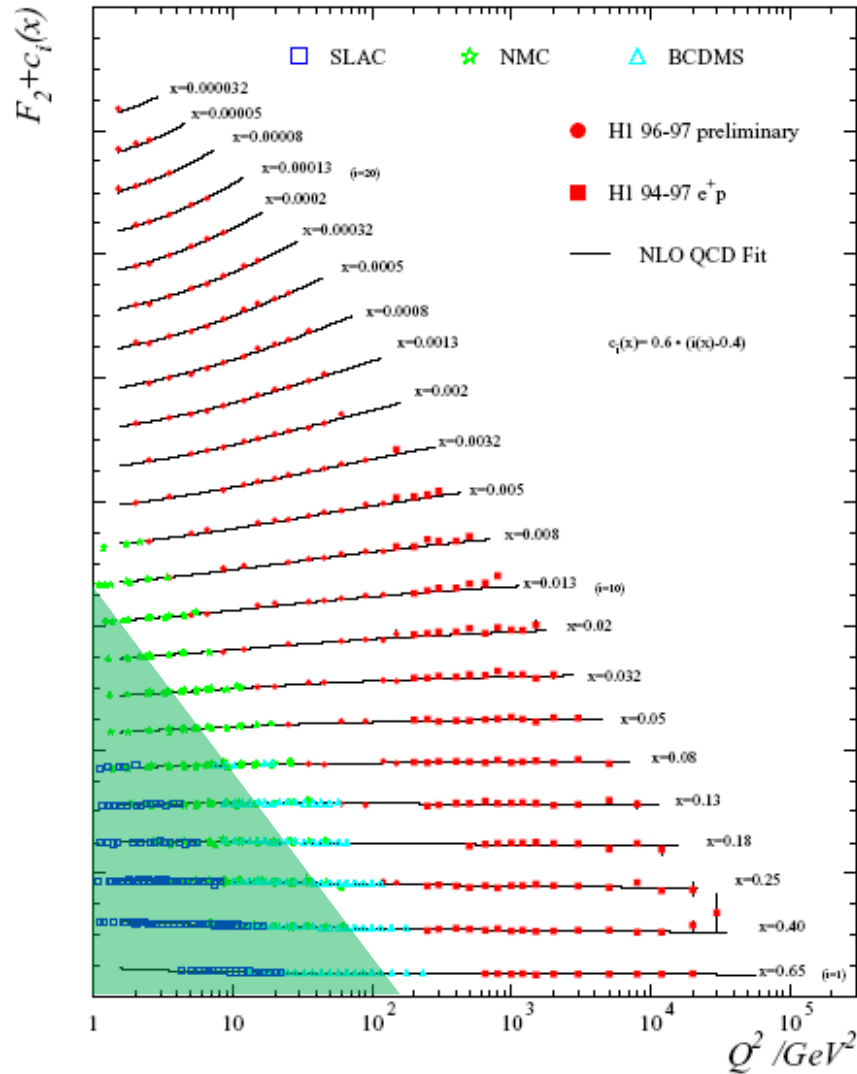
$$F_2(x, Q^2)$$



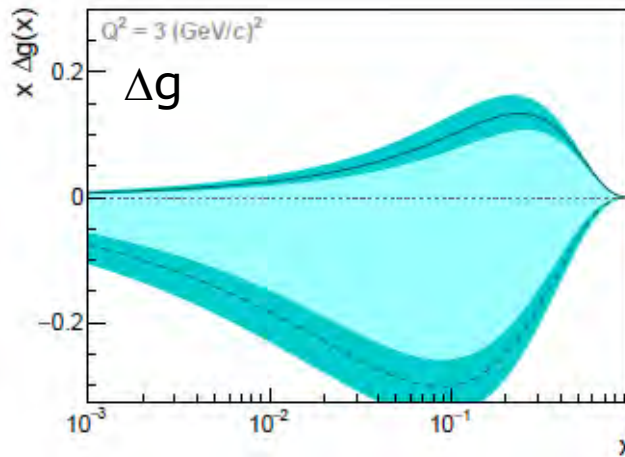
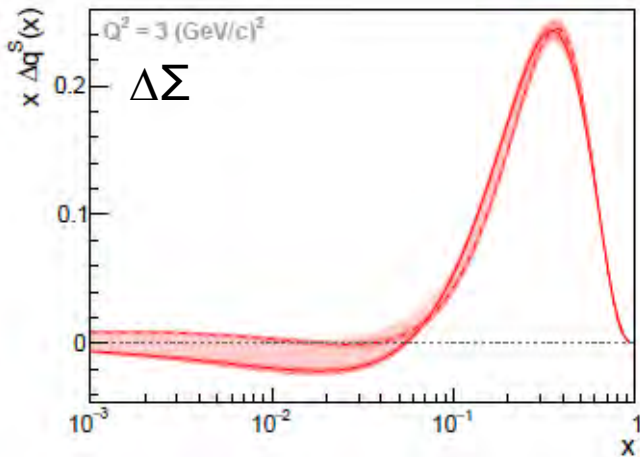
$$g_1(x, Q^2)$$



p



PDFs from NLO fit to world data



$$Q^2 = 3 \text{ GeV}^2$$

integrals:

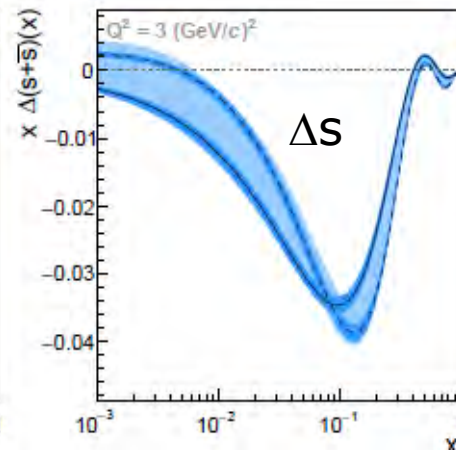
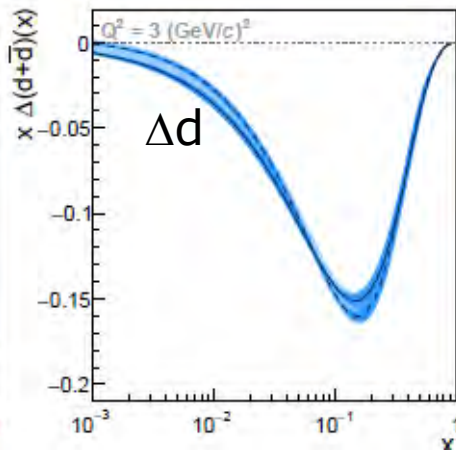
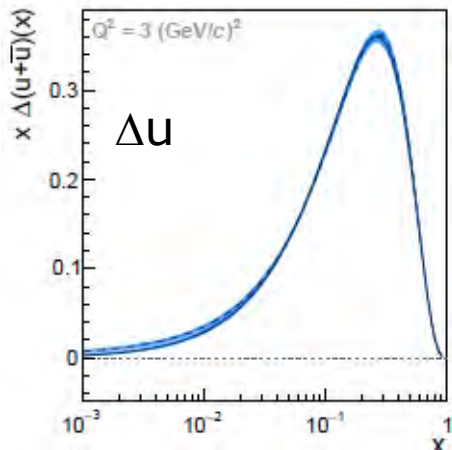
$$0.27 \leq \Delta\Sigma \leq 0.39$$

$$-1.6 \leq \Delta G \leq 0.5$$

$$0.82 \leq \Delta U \leq 0.85$$

$$-0.45 \leq \Delta D \leq -0.42$$

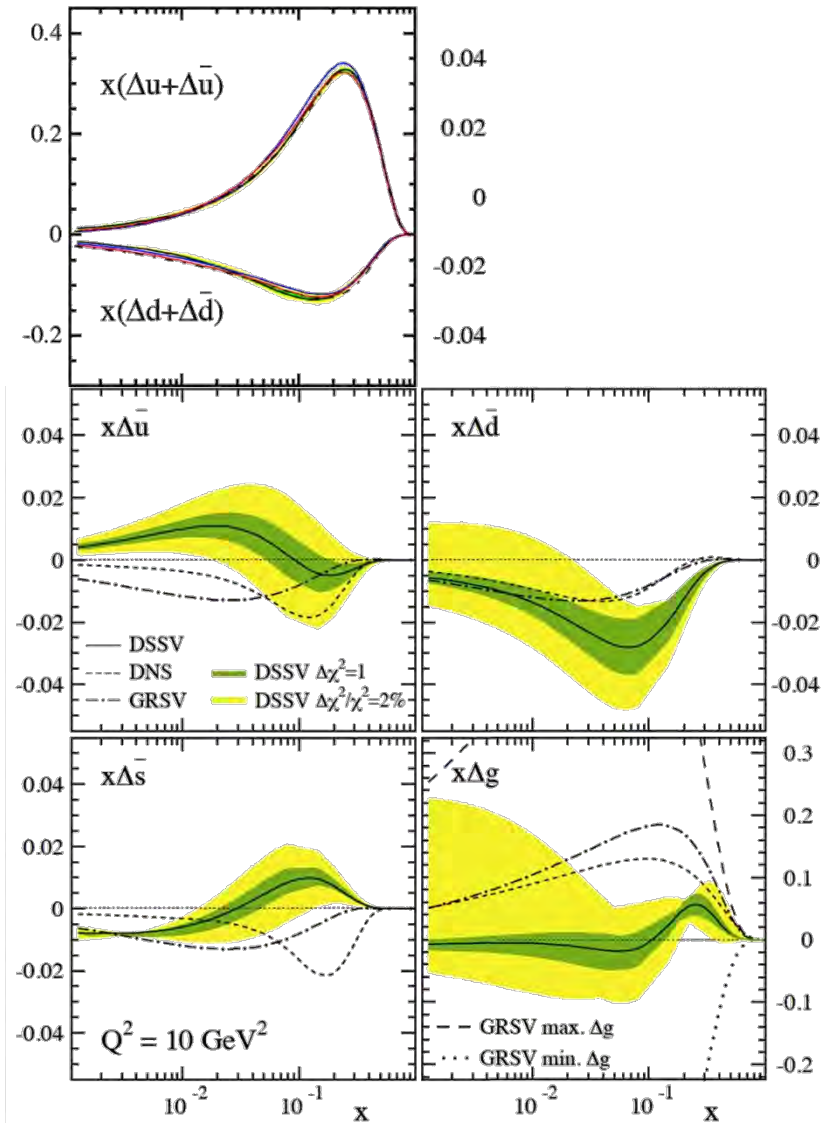
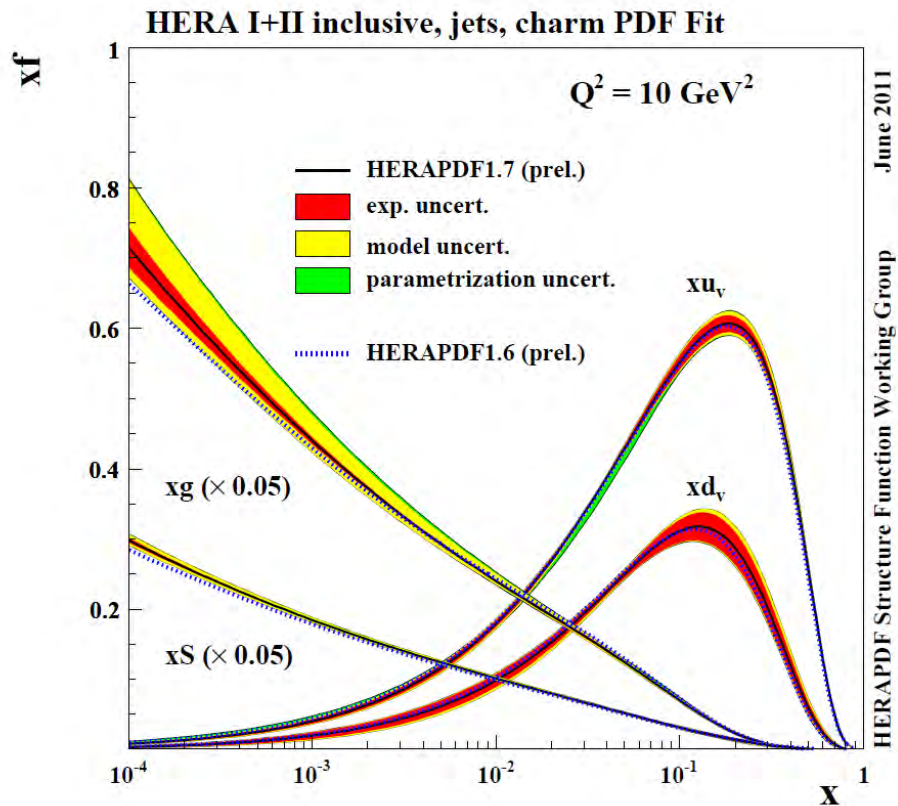
$$-0.11 \leq \Delta S \leq -0.08$$



using different
functional shapes
and Q_0^2

Status of PDFs: global analyses

unpolarised



Sum rules for g_1



- **first moment** Γ_1 of g_1 with $\Delta q = \int_0^1 \Delta q(x) + \Delta \bar{q}(x) dx$

$$\Gamma_1 = \int_0^1 g_1(x) dx \stackrel{\text{proton}}{=} \frac{1}{2} \left\{ \frac{4}{9} \Delta u + \frac{1}{9} \Delta d + \frac{1}{9} \Delta s \right\}$$

$$= \frac{1}{12} \underbrace{(\Delta u - \Delta d)}_{a_3} + \frac{1}{36} \underbrace{(\Delta u + \Delta d - 2\Delta s)}_{\sqrt{3}a_8} + \frac{1}{9} \underbrace{(\Delta u + \Delta d + \Delta s)}_{a_0}$$

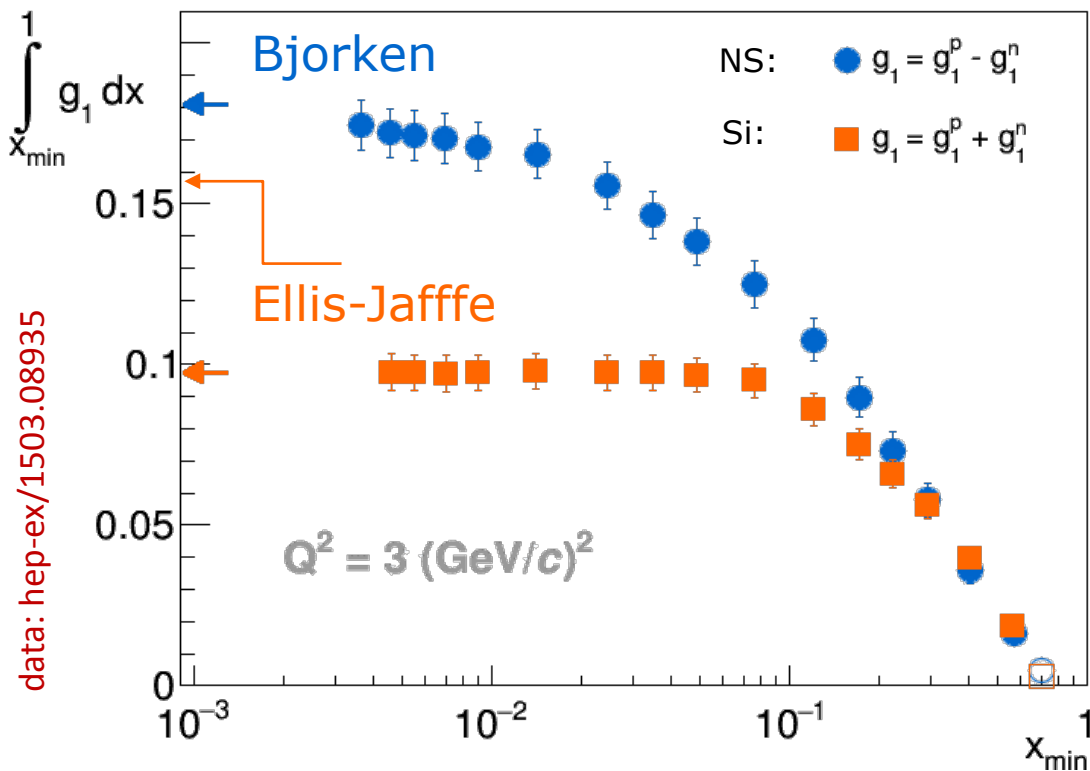
a_3 neutron decay

a_8 hyperon decay

$a_0 = \Delta \Sigma$

- **Bjorken sum rule:** $\Gamma_1^p - \Gamma_1^n = \frac{1}{6}(\Delta u - \Delta d)$ if wrong \Rightarrow QCD wrong but BJ: "worthless equation"
- **Ellis-Jaffe 'SRs' for p and n assume :** $\Delta s = 0$; $\Gamma_1 \Rightarrow \Delta u + \Delta d = \Delta \Sigma$

Sum rules



$$\Gamma_1^{NS}(Q^2) = \frac{1}{6} \left| \frac{g_A}{g_V} \right| c_1^{NS}(Q^2)$$

Bjorken sum rule
verified to 9%

- BJ SR major contribution from small x
- EJ SR no contribution at small x

COMPASS data only: $|g_A/g_V| = 1.22 \pm 0.05 \text{ (stat.)} \pm 0.10 \text{ (syst.)}$

from neutron β decay: $|g_A/g_V| = 1.2723 \pm 0.0023$

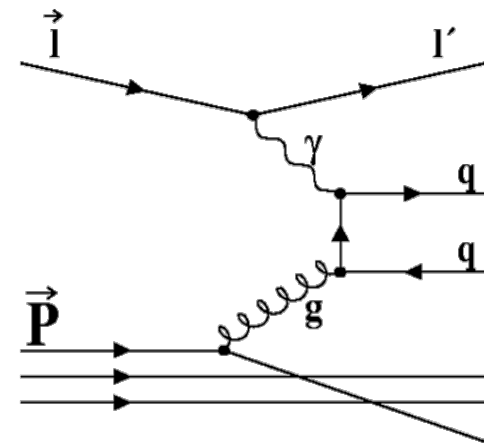
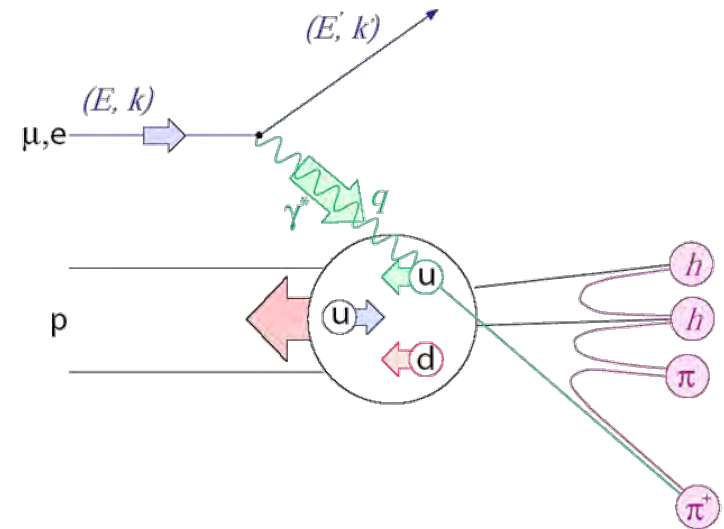
4. Longitudinal spin: SIDIS results

- additional hadron observed in FS

$$A_1^h = \frac{\sum_q e_q^2 g_1^q(x, Q^2) D_{1q}^h(z, Q^2)}{\sum_q e_q^2 f_1^q(x, Q^2) D_{1q}^h(z, Q^2)}$$

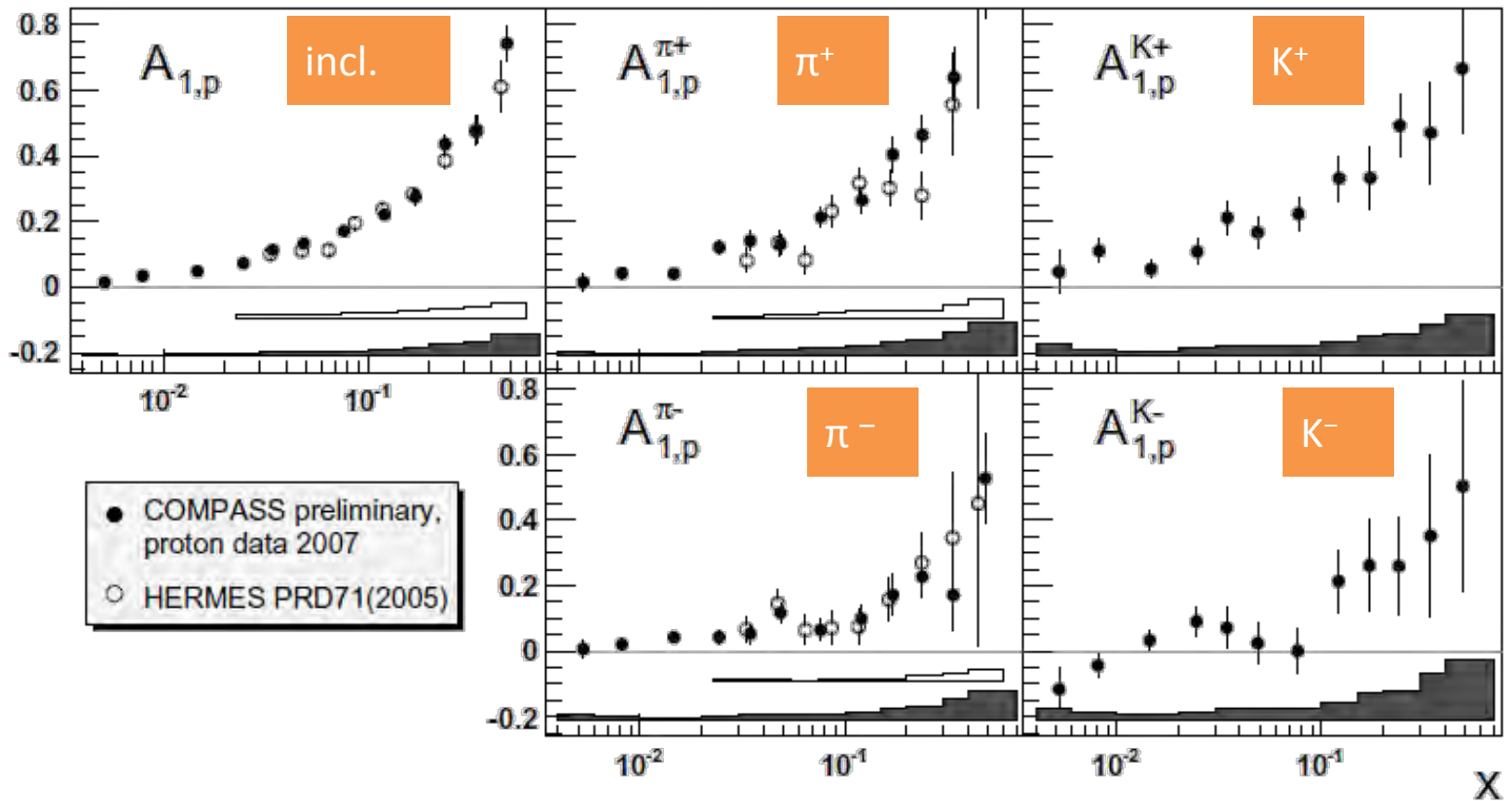
$$z = E_h/\nu$$

- gives access to flavour information via the fragmentation functions D
- photon–gluon fusion gives access to the gluon polarisation
- particularly interesting open charm production via $c\bar{c}$



Incl. & semi-incl. A_1

- proton

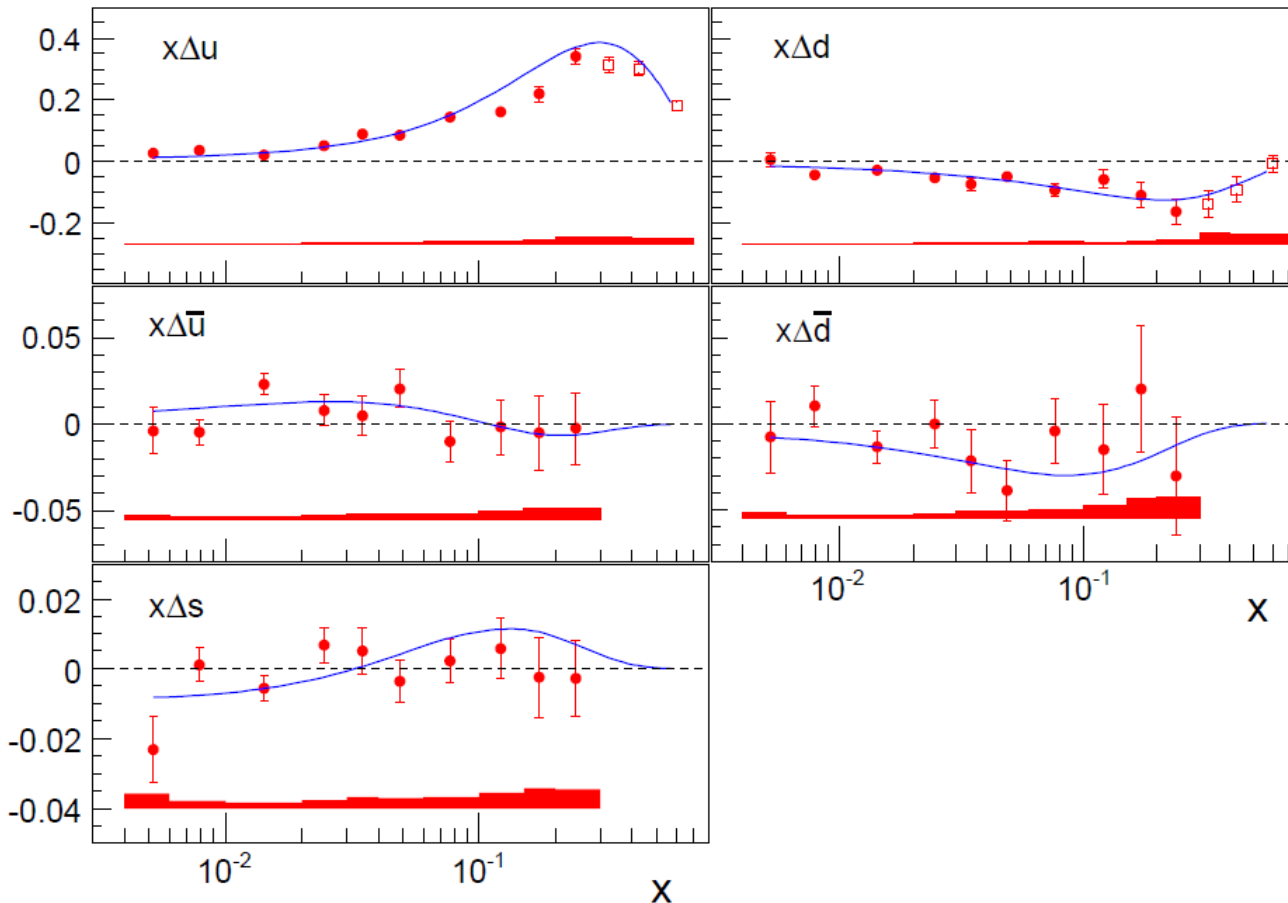


The role of quark flavours



LO analysis of 5p+5d asymmetries, DSS FF
Line: NLO DSSV not including these data

5-flavour fit,
assuming $\Delta s = \bar{\Delta} s$



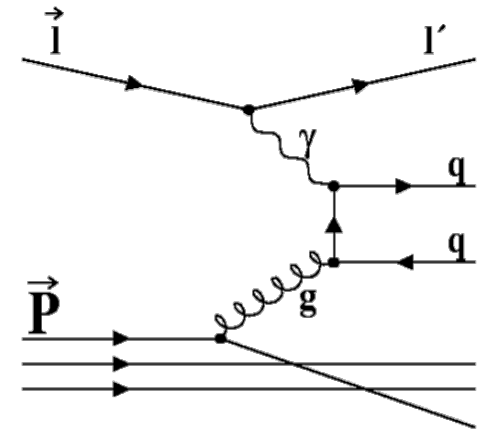
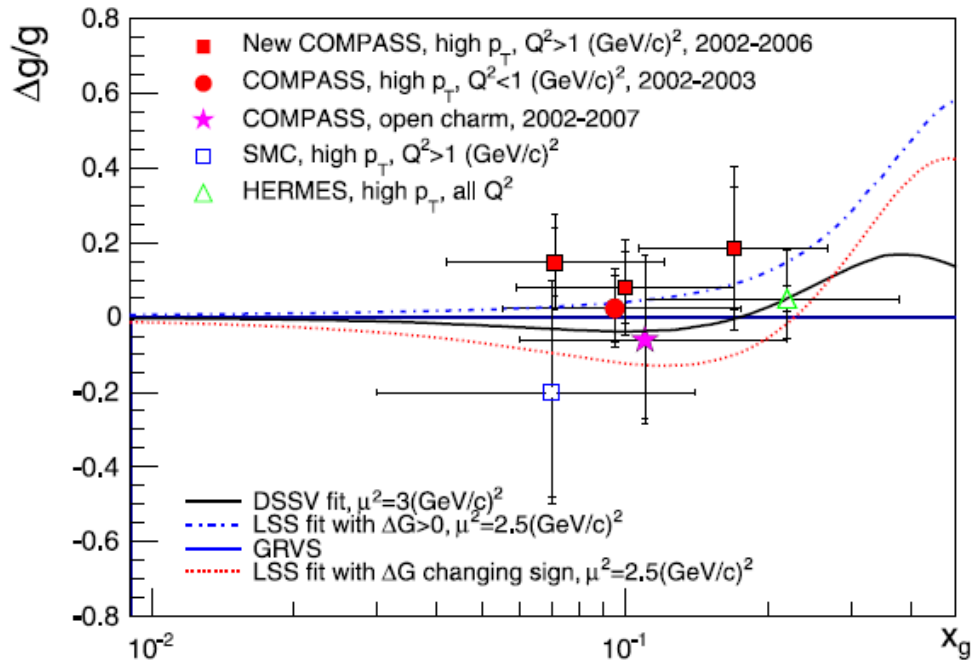
Data (LO analysis):



PLB693 (2010) 227

PRD80 (2009) 034030

$\Delta g/g$ from PGF (LO)

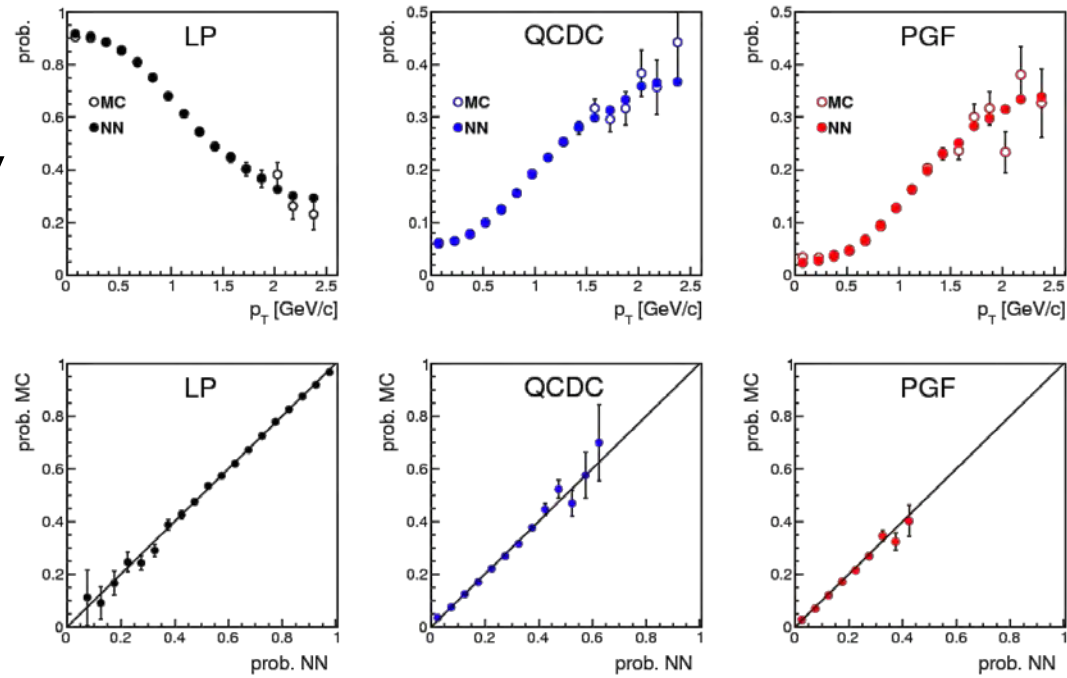
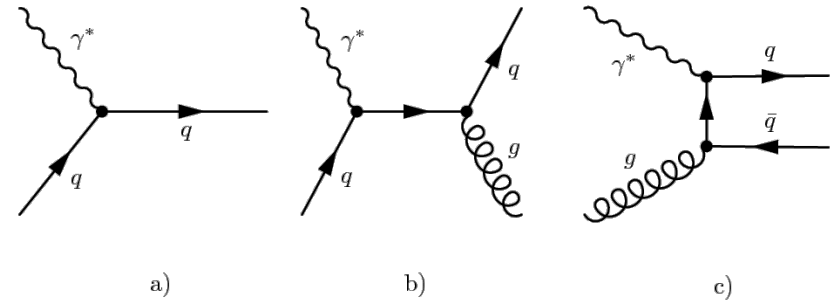


- $Q^2 > 1 \text{ GeV}^2$
- $Q^2 < 1 \text{ GeV}^2$
- open charm (D mesons)

- gluon polarisation is much smaller than thought in the 1990s by many theorists (around $2\hbar$ [even up to $6\hbar$], axial anomaly); various methods
- confirmed by polarised pp at RHIC
- Δg still can make a substantial contribution to nucleon spin

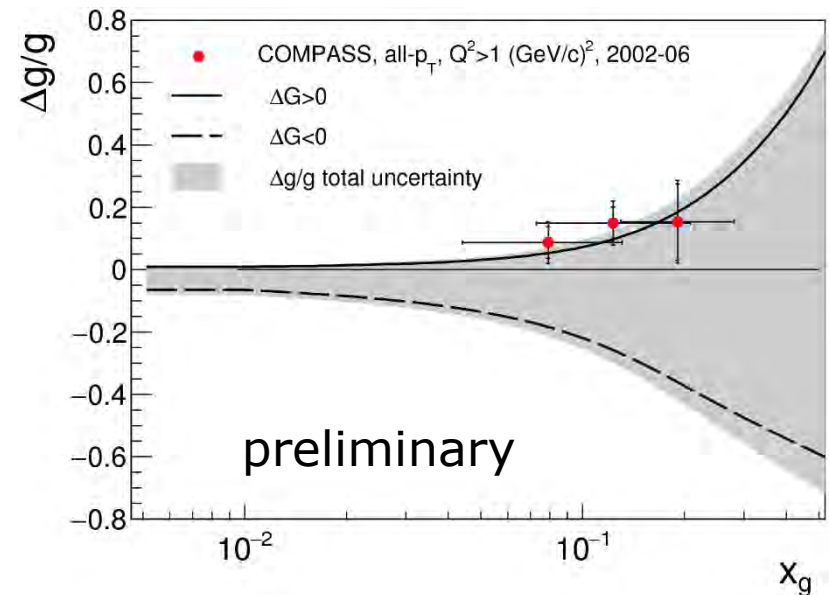
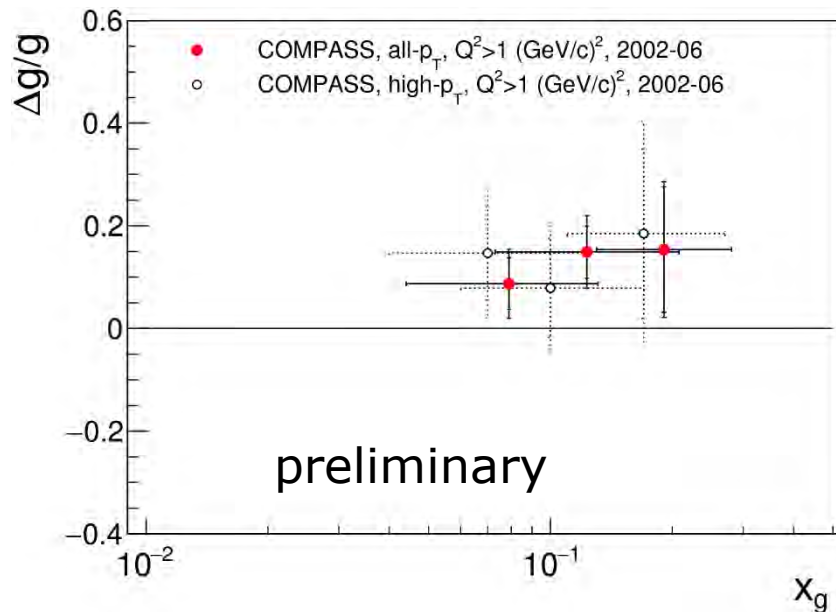
Gluon polarisation from PGF (LO)

- LO reanalysis of 2002-2004, 2006 deuteron data
- $Q^2 > 1 \text{ GeV}^2$
- novel method using events with any p_T and NN weights
- simultaneous determ. of leading order asym. reduces syst. uncertainty
- determination of $\Delta g(x)$ in 3 x ranges

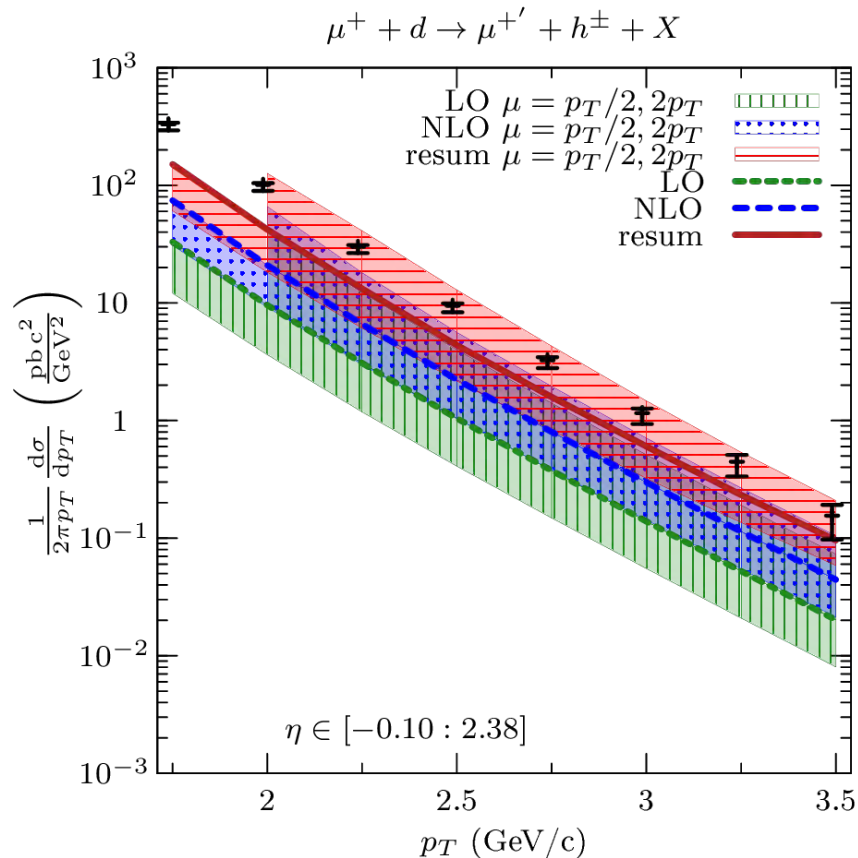


Gluon polarisation from PGF

- $\Delta g(x) = 0.113 \pm 0.038 \pm 0.036$ with $\langle x_g \rangle = 0.10$ at 3 GeV² prel.
- no x dependence visible
- error reduction factor: 1.6 stat, 1.8 syst
- positive $\Delta g(x)$ preferred



Spin independent cross-section



- semi-inclusive single hadron production
 - COMPASS kinematics
 - good agreement with NLL resummation
- ⇒ cross-section asymmetries can be used to determine the gluon polarisation
- ⇒ need NLL resummation for polarised case

De Florian, Pfeuffer, Schaefer, Vogelsang,
PRD 88 (2013) 014024

COMPASS, PRD 88 (2013) 091101

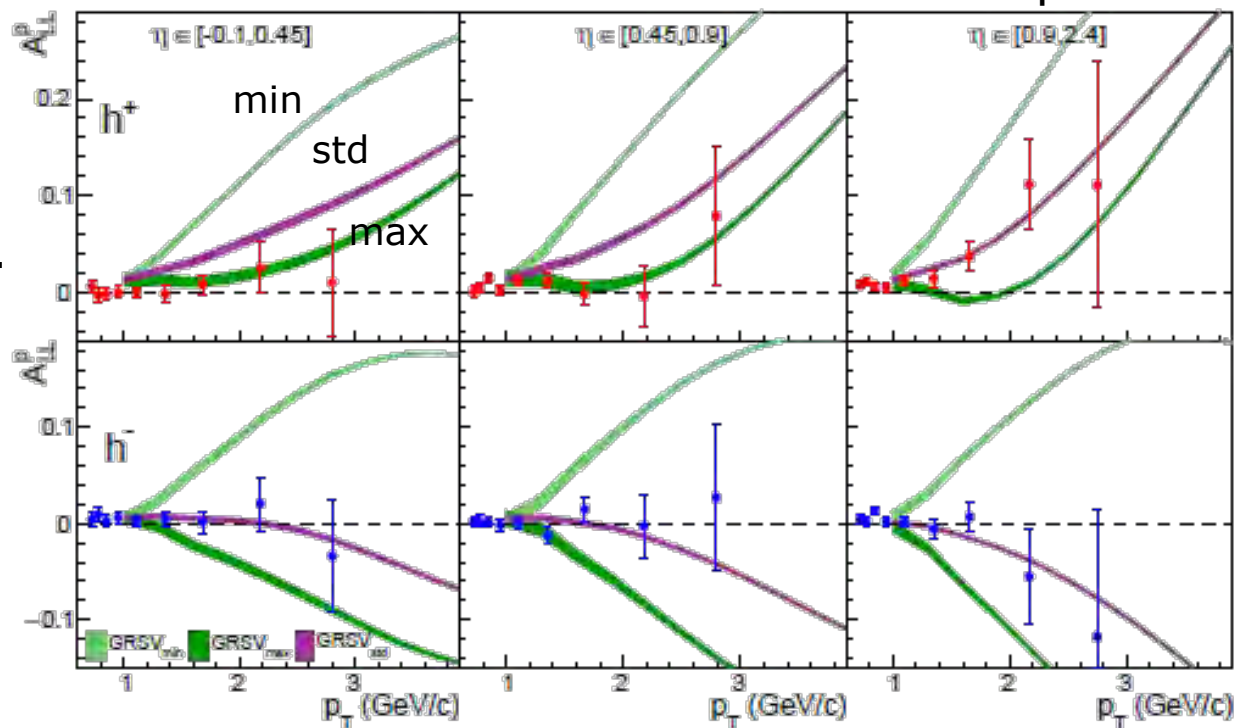
$\Delta g/g$ from single hadron (NLO)

- quasi-real photoproduction of single hadrons, à la RHIC π^0 prod.
- calc. by group of Vogelsang, agreement for unpolarised case
- caveat: NNL resummation **missing for polarised case**

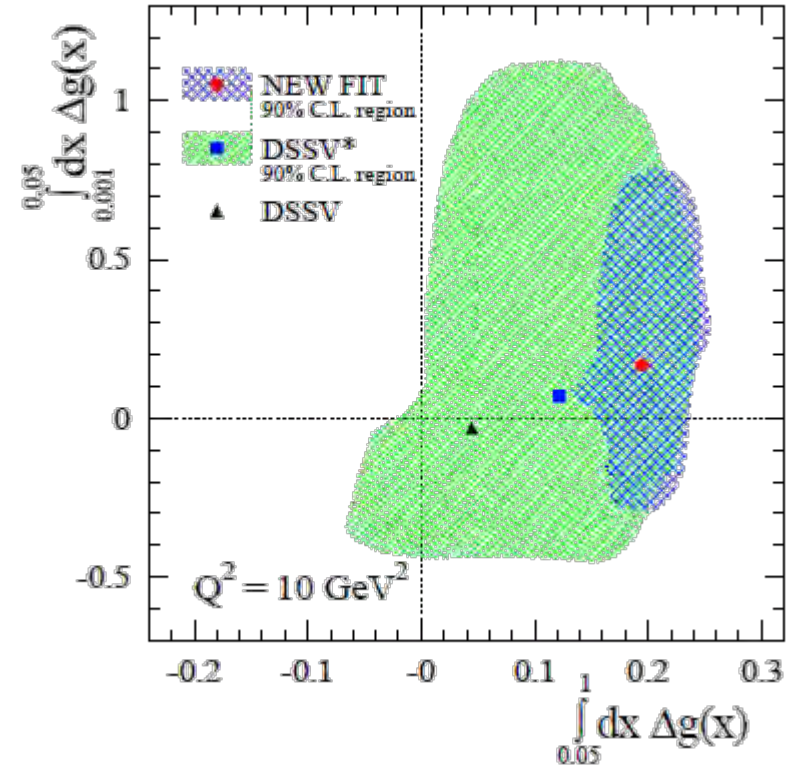
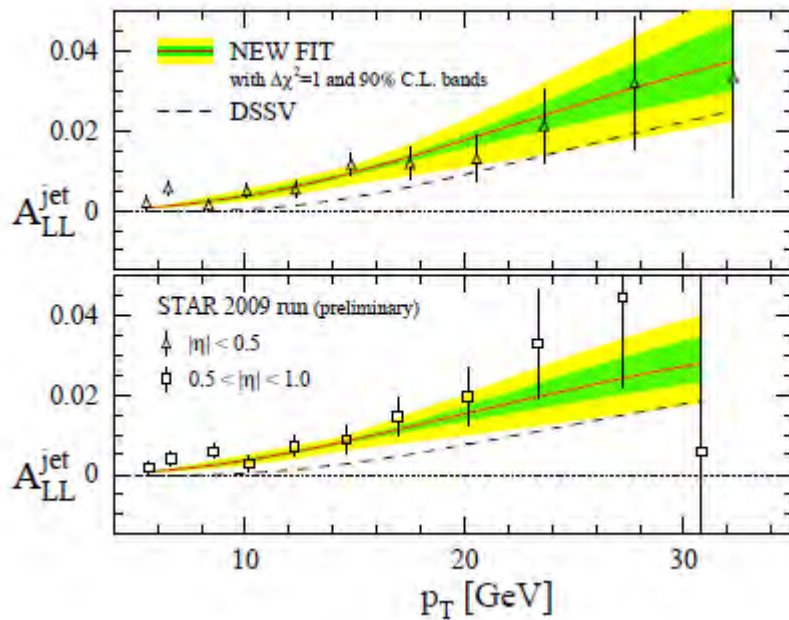
$$\eta_{cms} = -\ln\left(\tan\frac{\theta}{2}\right) - \frac{1}{2}\ln\left(\frac{2E}{M}\right)$$

proton

- 3 bins of pseudorapidity η
- FF important, using DSS (2015), agree best with meas. multiplicities
- data prefer **positive** gluon polarisation as also suggested by recent RHIC data



RHIC STAR jet data & new DSSV fit (2014)



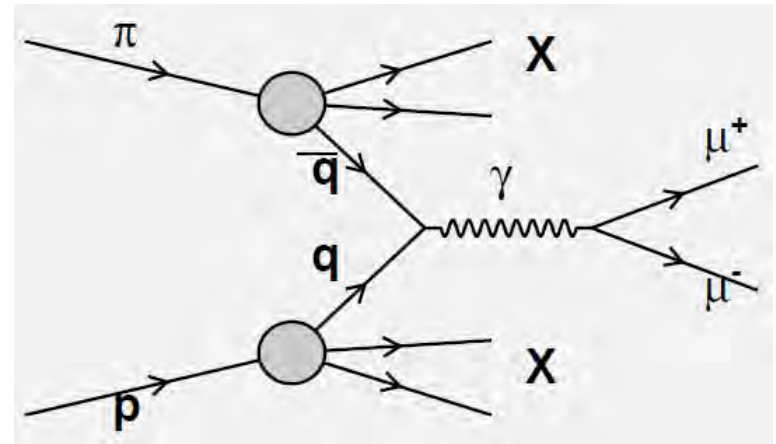
- clear preference for positive gluon distribution at $Q^2 = 10 \text{ GeV}^2$

5. COMPASS-II

- Pion (and kaon) polarizabilities 2012
 - TMD in $\pi^- + p$ transv. pol. Drell-Yan: 2015
 - Generalised Parton Distr. (GPD)
simult. unpol. SIDIS on proton: 2016/17
 - new option, under discussion 2018
-
- proposal and scientific approval 2010
 - first measurements 2012

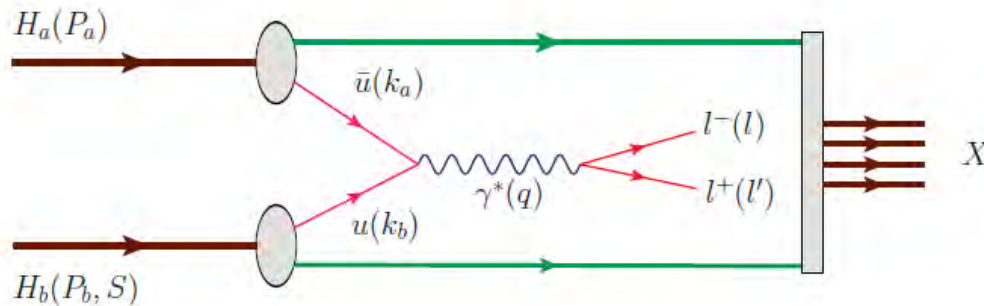
Drell–Yan Process

- No fragmentation function involved
- Convolution of two PDFs
- Best: pol. **antiproton–proton** (long-term)
- Simpler: **negative pion on proton**
- anti-u from neg. pion annihilates with proton u
- Transversely polarized proton target → access to transverse momentum dependent (TMD) PDFs like Sivers and Boer–Mulders functions → **F. Bradamante**
- Test of universality of PDFs, why interesting?

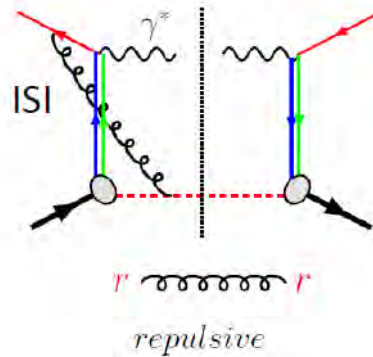
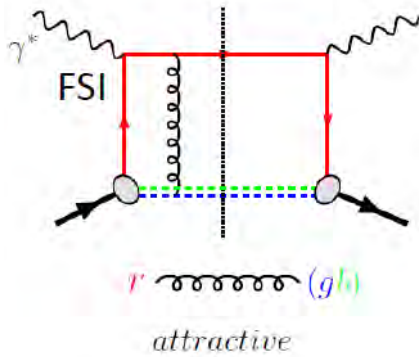


$$\sigma^{DY} \propto f_{\bar{u}|\pi^-} \otimes f_{u|p}$$

Restricted universality in SIDIS and **pol.** DY



T-odd TMD



'gauge link changes sign for T-odd TMD', restricted universality of T-odd TMDs

J.C. Collins, PLB536 (2002) 43

$$f_{1T}^\perp \Big|_{DY} = - f_{1T}^\perp \Big|_{DIS} \quad \text{and} \quad h_1^\perp \Big|_{DY} = - h_1^\perp \Big|_{DIS}$$

Sivers

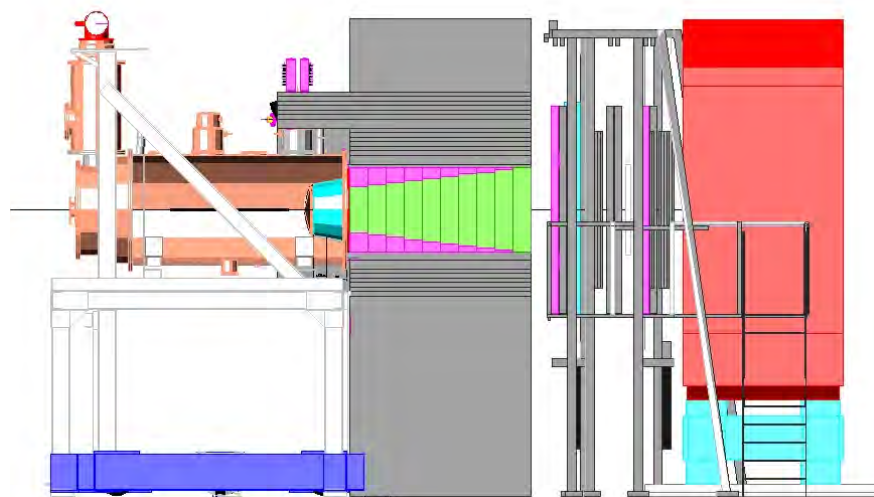
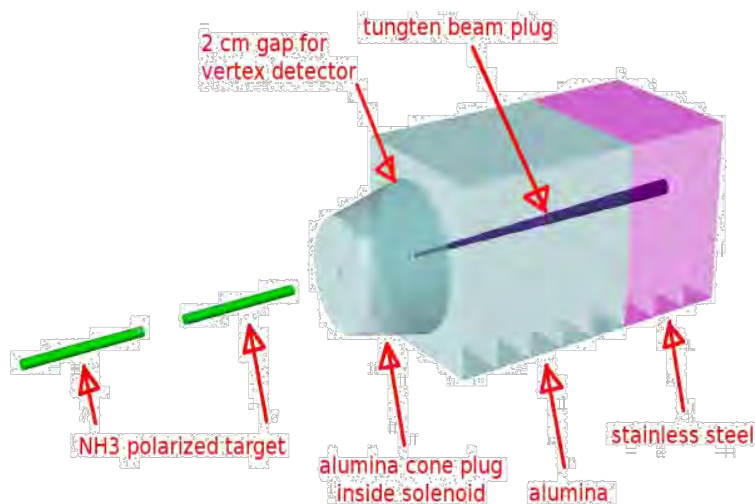
$$h_1^\perp \Big|_{DY} = - h_1^\perp \Big|_{DIS}$$

Boer-Mulders

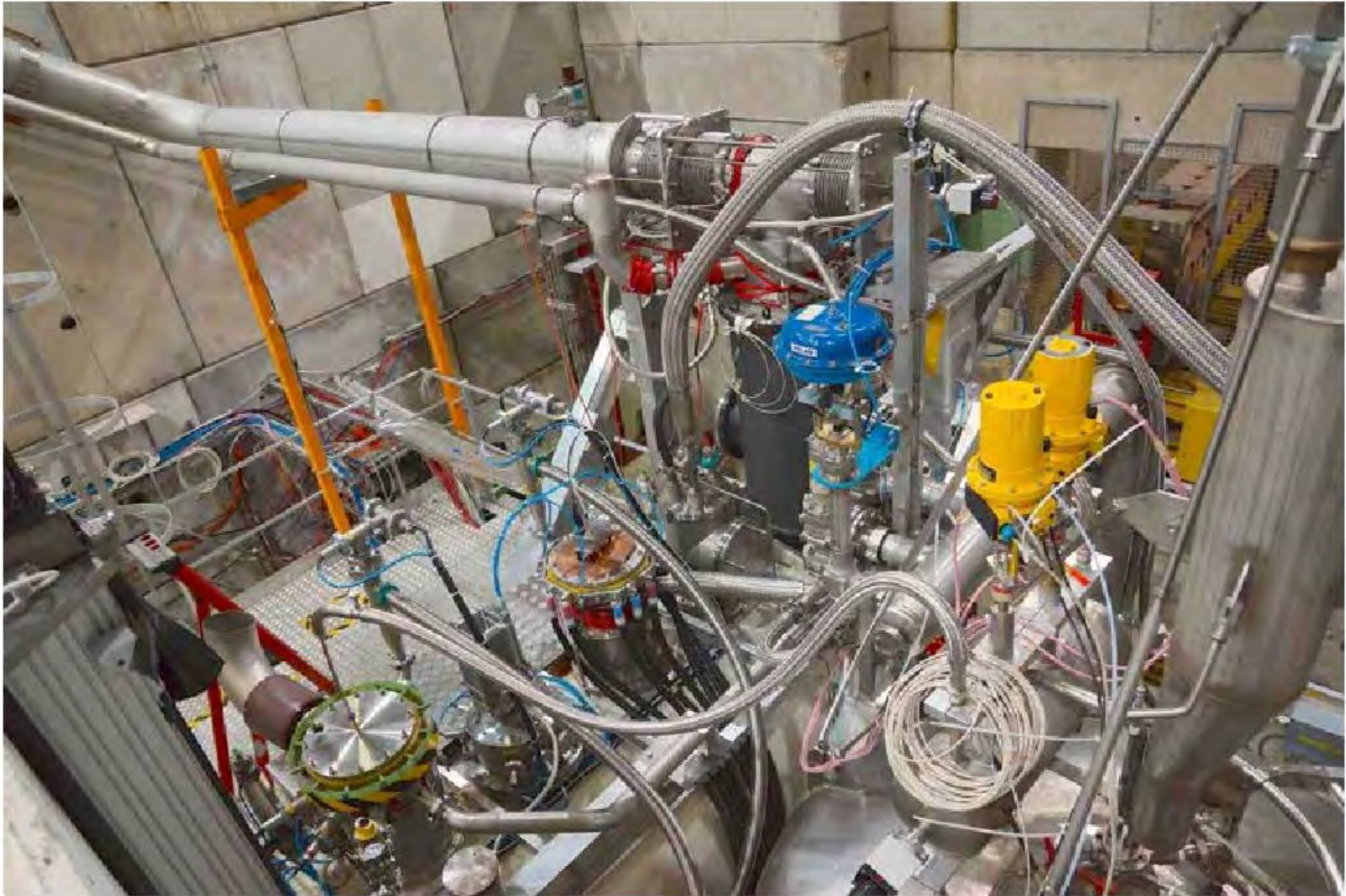
- important prediction, needs to be verified

COMPASS-II Polarised Drell-Yan

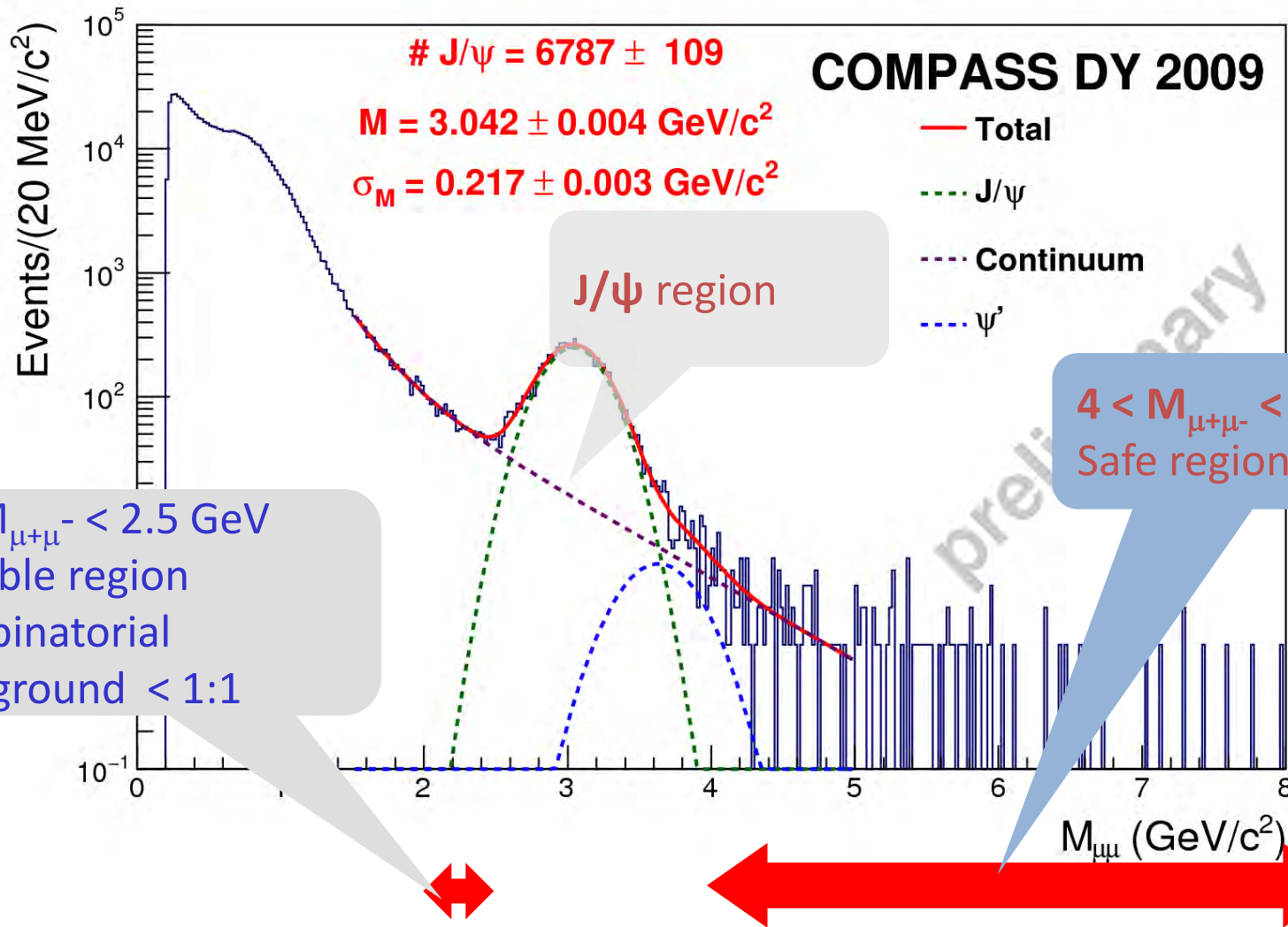
- First ever polarized Drell-Yan experiment
- 190 GeV/c π^- beam on transv. pol. proton target
- Access to transversity, the T-odd Sivers and Boer-Mulders TMDs



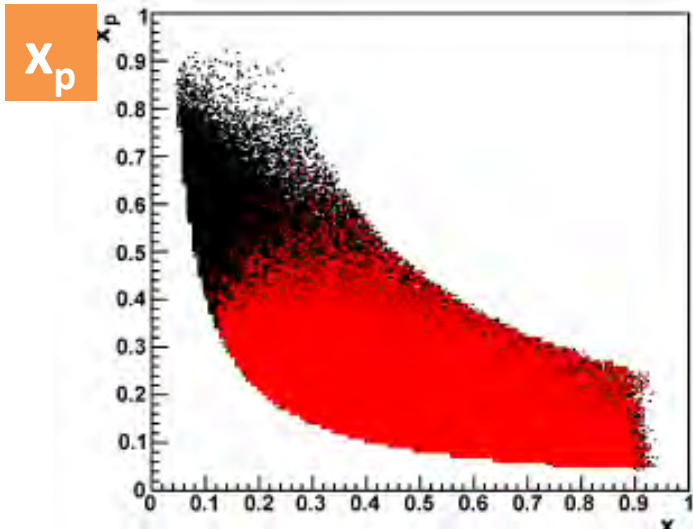
2015 run: polarised target



Drell–Yan muon pair mass regions

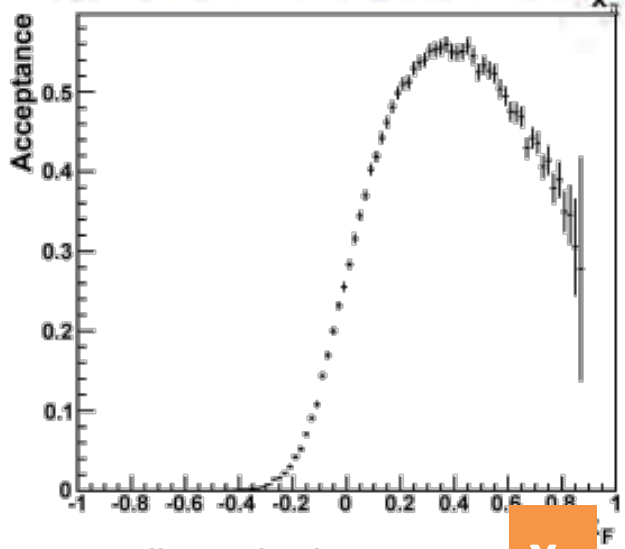


COMPASS polarized DY, projections HMR



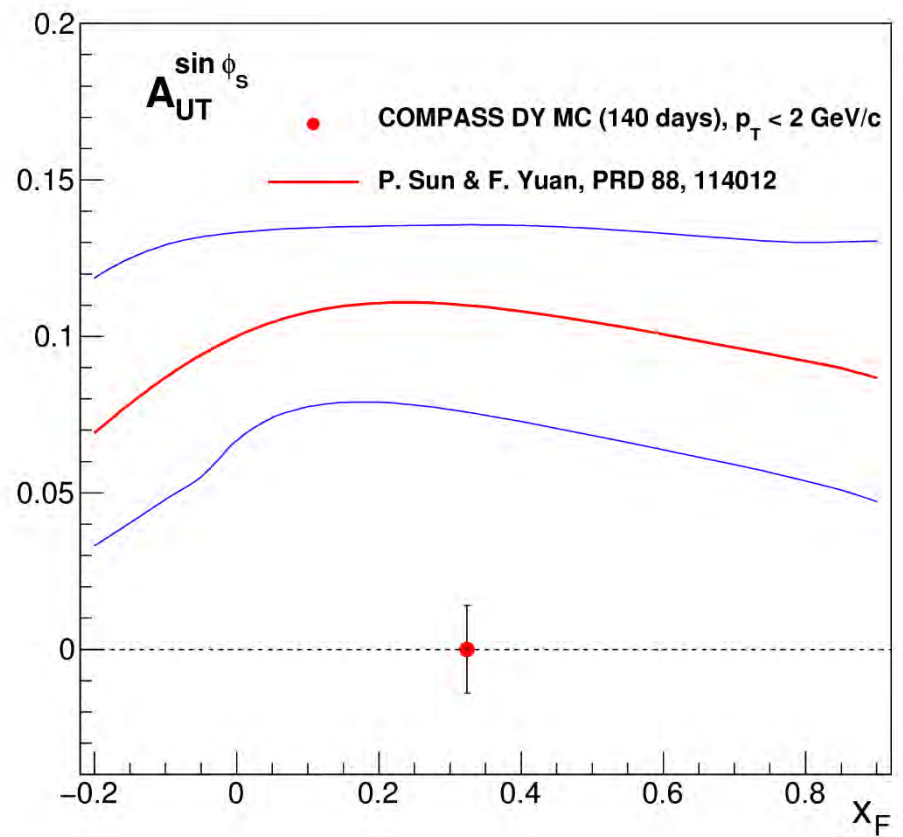
x_p

x_π



x_F

Predictions vary strongly, e.g.



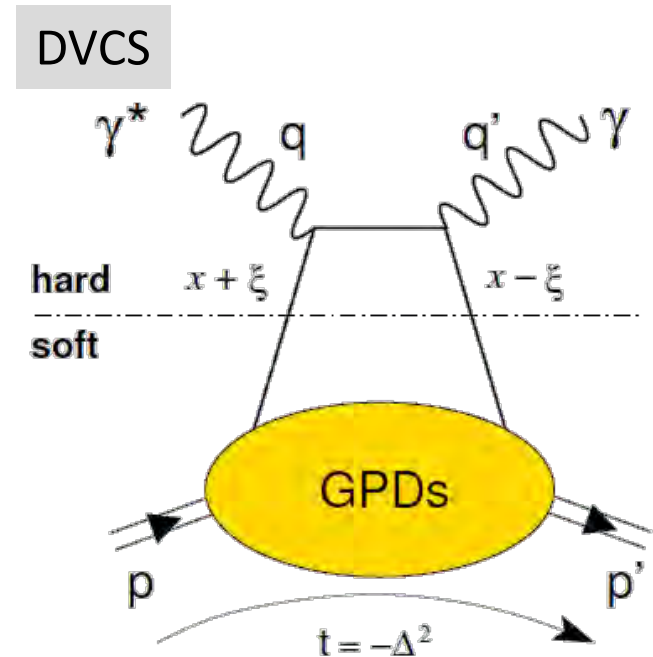
$x_F = x_\pi - x_p$

Generalized PDF's

- Correlating **transverse spatial** and **longitudinal momentum** degrees of freedom
- PDFs and elastic FF as limiting cases
- $H, \tilde{H} \rightarrow f_1, g_1$ for $\xi \rightarrow 0$;
- $H(E)$ for nucleon helicity (non)conservation
- **exclusive** processes like DVCS, HEMP (vector & pseudoscalar)

$$H(x, \xi, t, Q^2); \quad Q^2 \text{ large, } t \text{ small}$$

$$H^f, E^f, \tilde{H}^f, \tilde{E}^f \text{ with } f = q, g$$

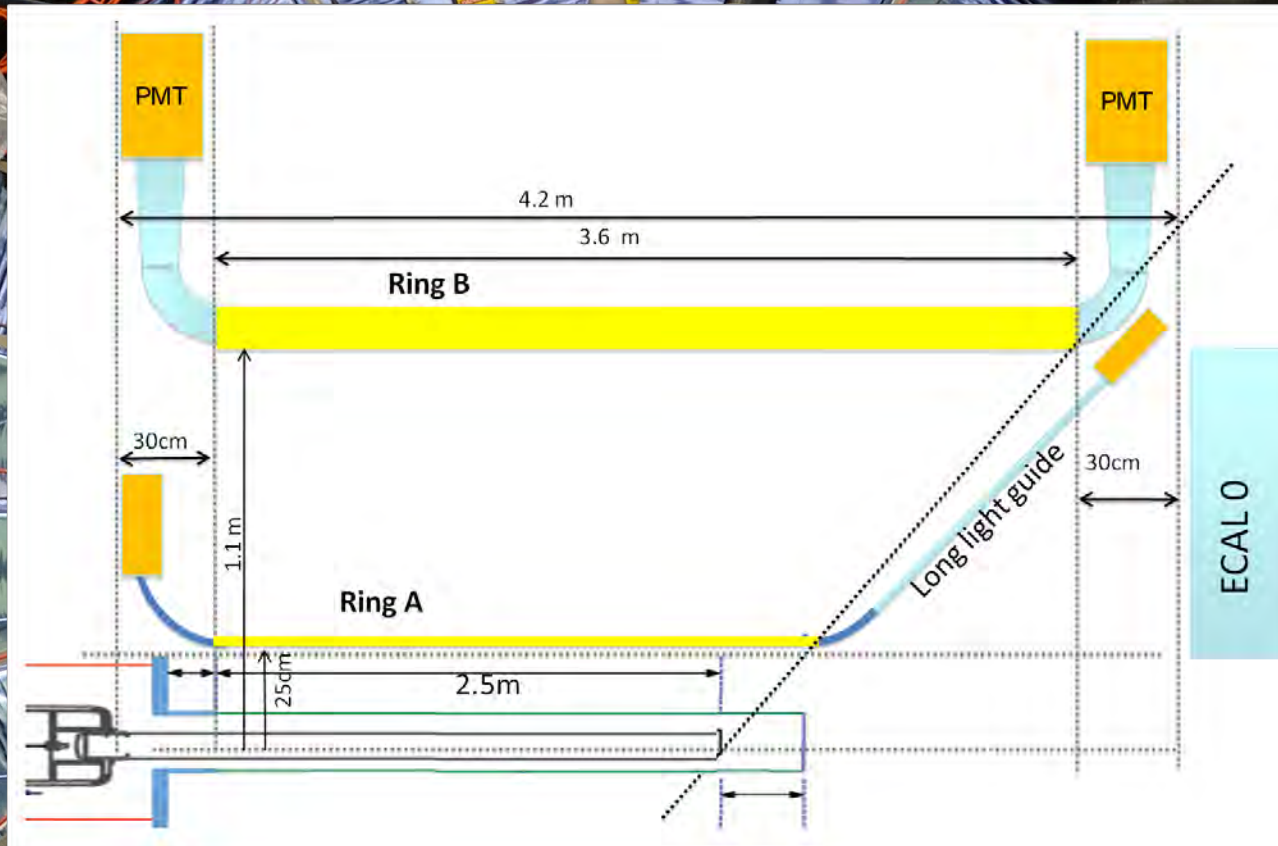


Total orbital momentum:

$$J^f(Q^2) = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x \left[H^f(x, \xi, t, Q^2) + E^f(x, \xi, t, Q^2) \right]$$

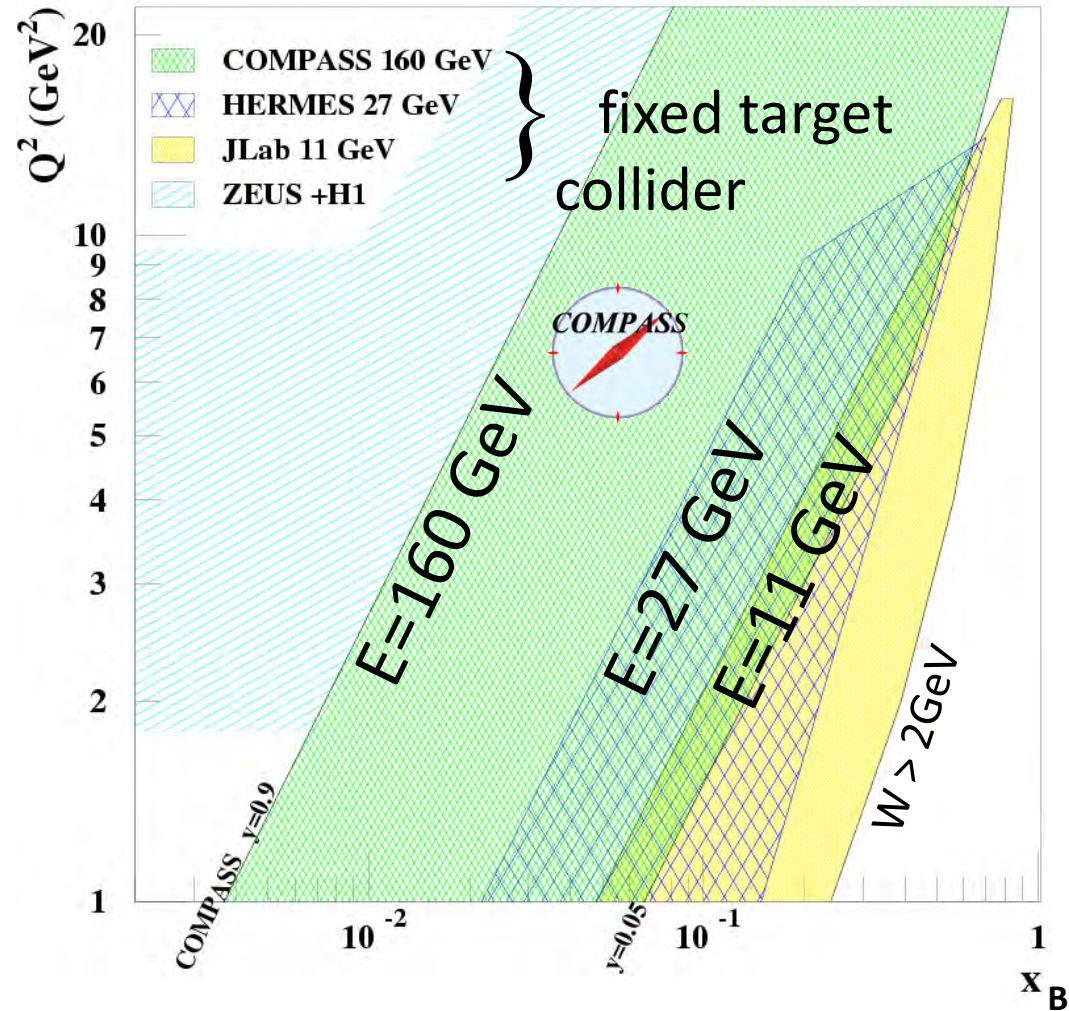
X.-D. Ji, PRL 78 (1997) 610

Camera detector for exclusivity



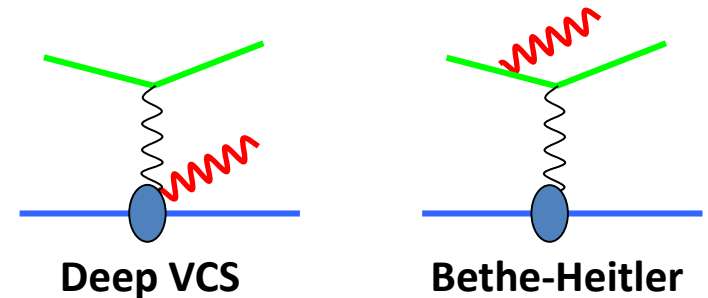
DVCS

- DVCS is the cleanest process to determine GPDs
- need a world-wide effort
- global analysis over large kinematic range mandatory
- COMPASS-II: bridges HERA to JLAB 11 GeV kinematics



DVCS–Bethe-Heitler interference /

- DVCS can be separated from BH and constrain the GPD H e.g. using different charge & spin (e_μ & P_μ) cross section combinations of the μ beam



- Note: μ^\pm beams have opposite polarisation at COMPASS

$$d\sigma^{\mu p \rightarrow \mu p \gamma} = d\sigma^{\text{BH}} + d\sigma_0^{\text{DVCS}} + P_\mu d\Delta\sigma^{\text{DVCS}} + e_\mu \text{Re } I + P_\mu e_\mu \text{Im } I$$

Charge & Spin sum and difference:

$$\mathcal{S} = d\sigma^{\leftarrow+} + d\sigma^{\rightarrow-} = 2(d\sigma^{\text{BH}} + d\sigma_0^{\text{DVCS}} + \text{Im } I)$$

$$\mathcal{D} = d\sigma^{\leftarrow+} - d\sigma^{\rightarrow-} = 2(d\sigma_0^{\text{DVCS}} + \text{Re } I)$$

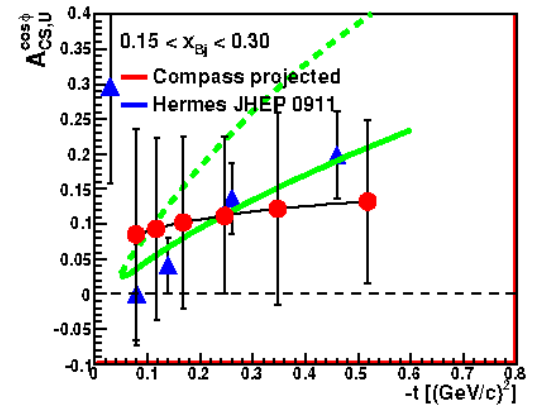
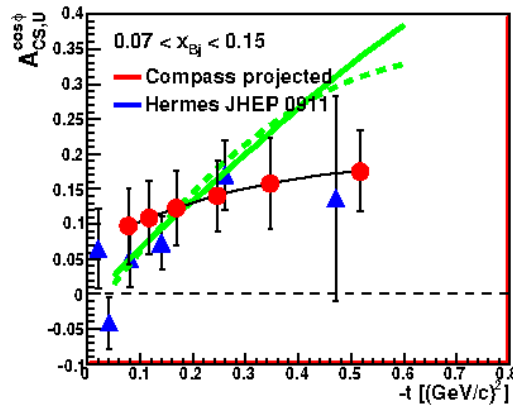
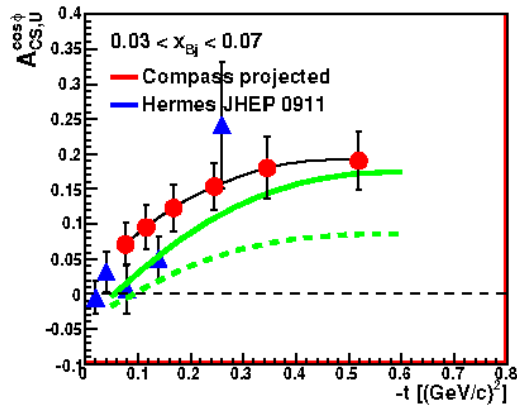
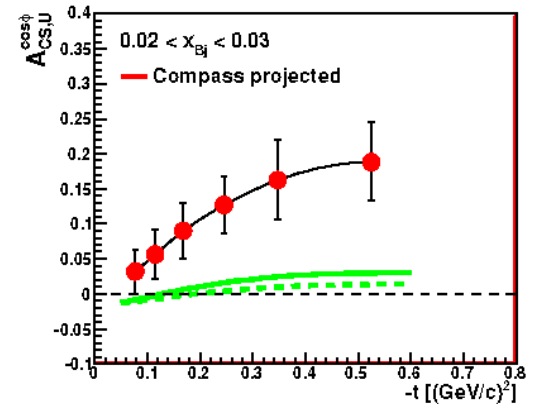
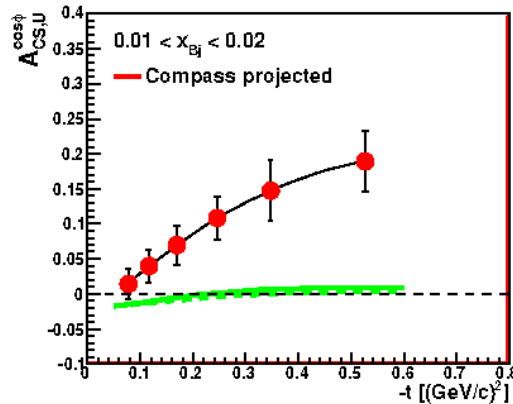
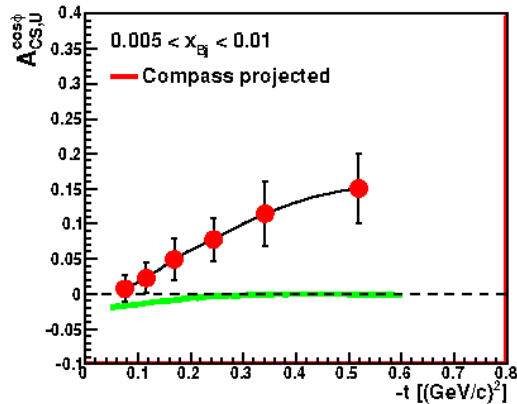
$\text{Im } I$ and $\text{Re } I$ related to

$$H(x = \xi, \xi, t)$$

$$\mathcal{P} \int dx H(x, \xi, t) / (x - \xi)$$

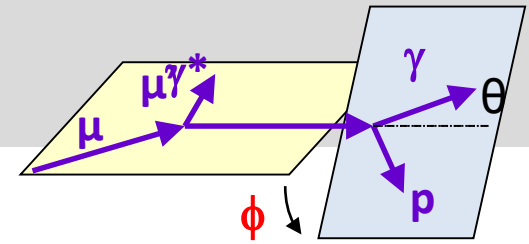
Projection for beam charge-and-spin asym.

Amplitude of $\cos \phi$ modulation of $A_{CS,U}^{\cos \phi} \equiv \frac{d\sigma^{++} - d\sigma^{--}}{d\sigma^{++} + d\sigma^{--}} = \frac{D_{CS,U}}{S_{CS,U}}$

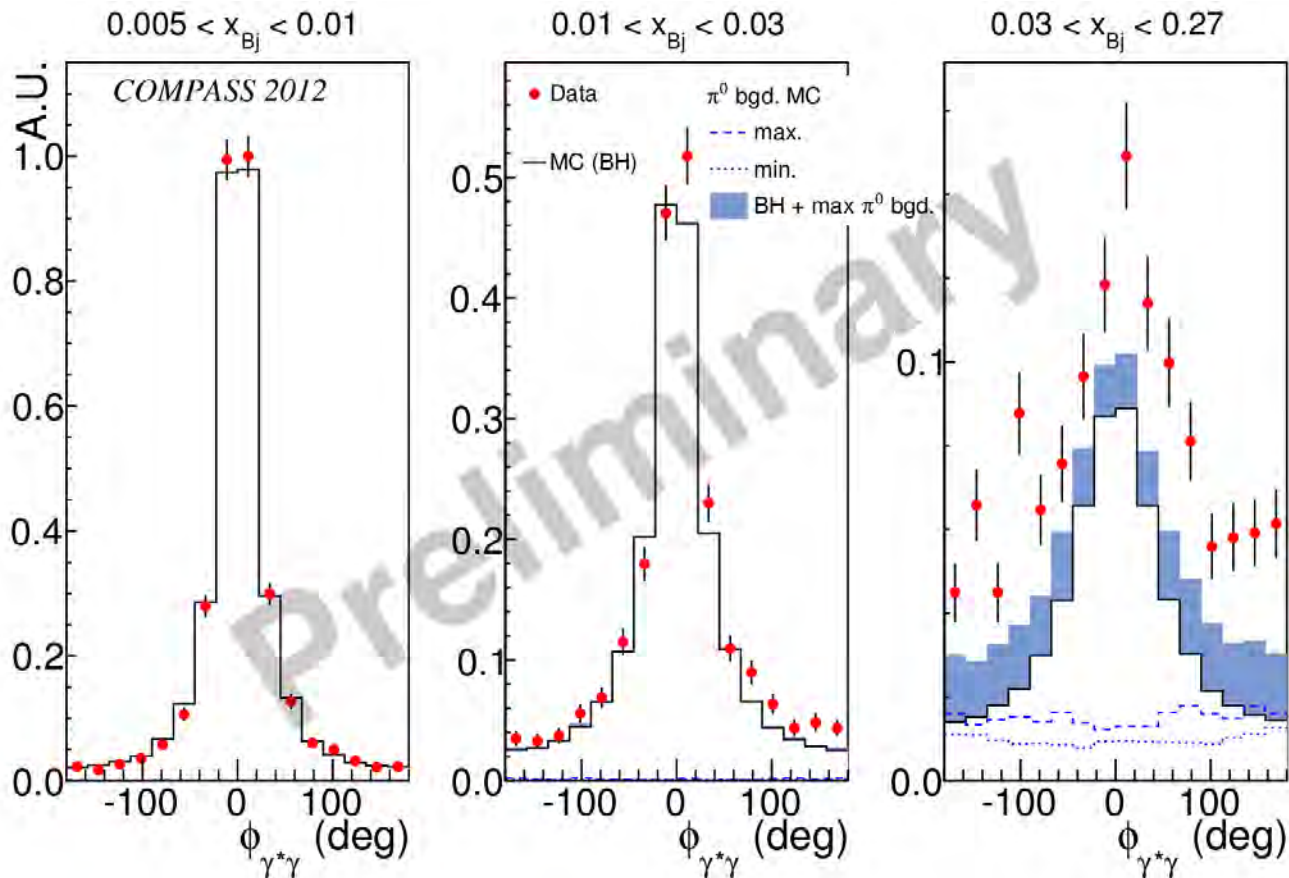


— fits by Kumericki, Mueller

BH vs DVCS data

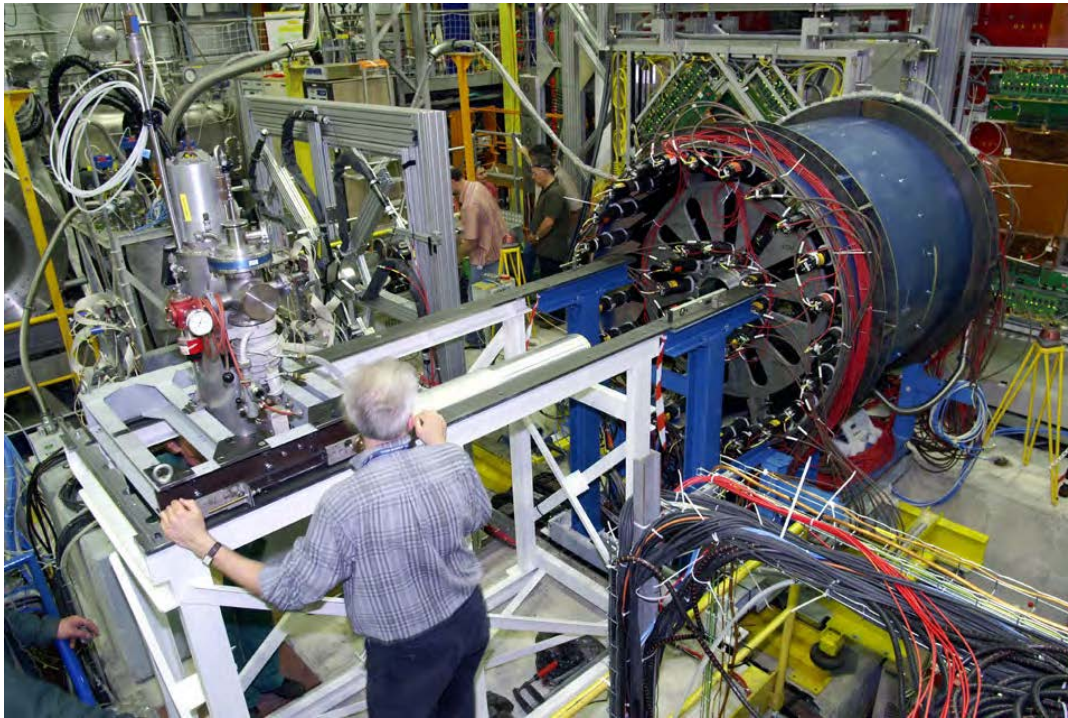


- Test runs in 2012 long LH target
- Clear DVCS signal, BH (- - - -) can subtracted



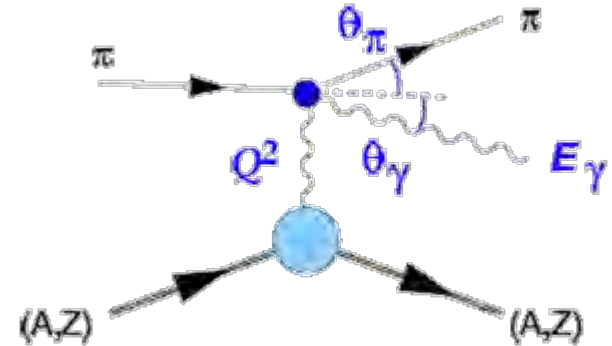
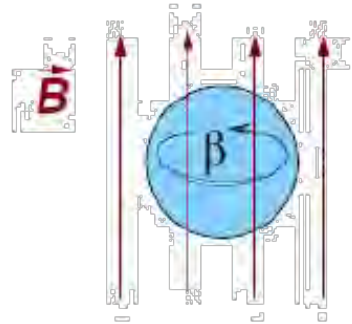
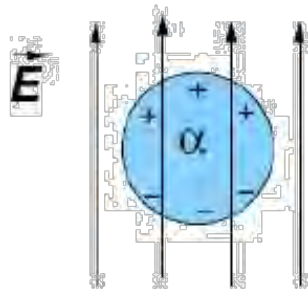
Add-on: Physics with hadron beams

- Proton, pion (and kaon) beams
- hydrogen, nickel and lead targets



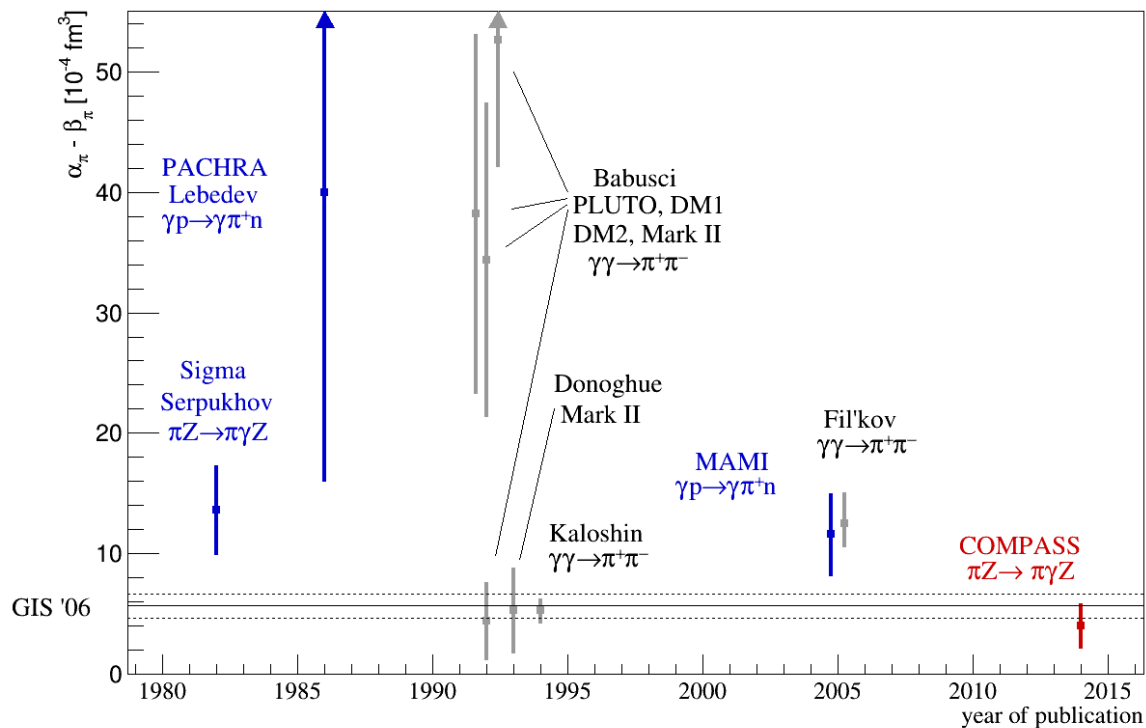
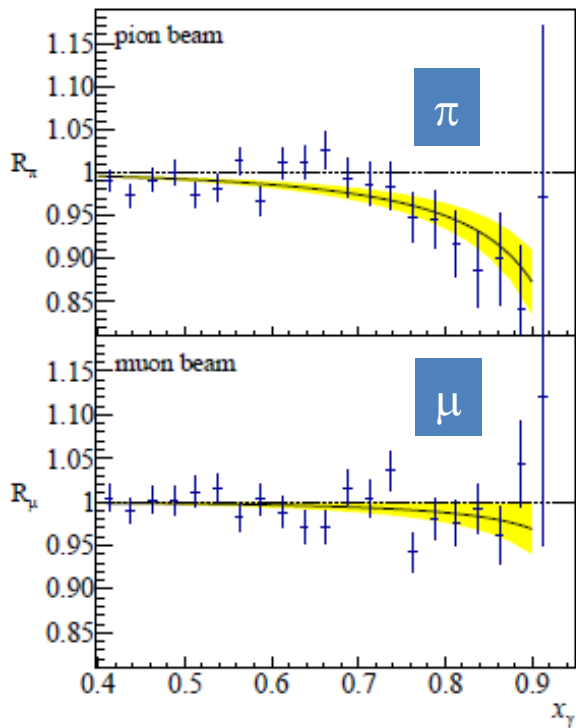
Inserting the liquid hydrogen target in the recoil detector

Pion el. & magn. polarisability



- deformation of a pion in el. & magn. fields
- prediction by chiral perturbation theory (χ PT)
 $\alpha + \beta \simeq 0$
- pion polarisability measured via Primakoff scattering of pion in em. field of nucleus (Ni)
- control measurement using muons
- previously confused exp. situation

Pion polarisability

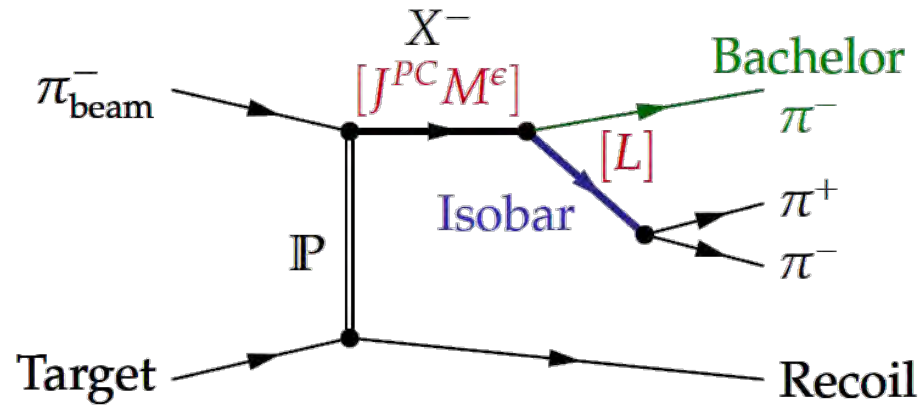


- predictions by χ PT: $\alpha = (2.9 \pm 0.5) \cdot 10^{-4} \text{ fm}^3$
- exp with $\alpha + \beta = 0$ $\alpha = (2.0 \pm 0.6 \pm 0.7) \cdot 10^{-4} \text{ fm}^3$
- pion is very stiff!
PRL 114 (2015) 062002

Neue Zürcher Zeitung : da schwabbelt nichts

PWA of $\pi^-p \rightarrow \pi^- \pi^+ \pi^- p$

- **Isobar model:**



X decay is chain of successive two-body decays

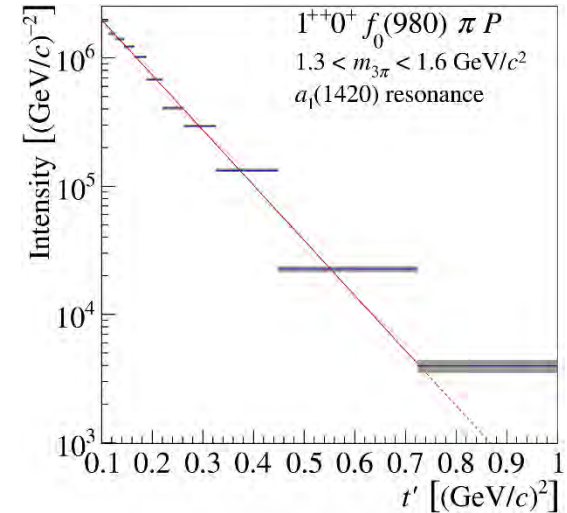
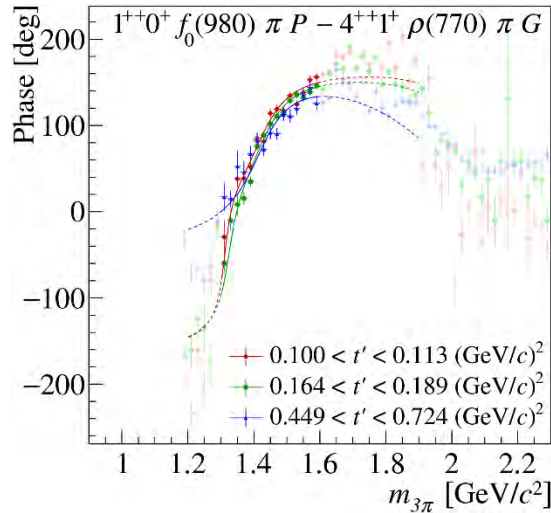
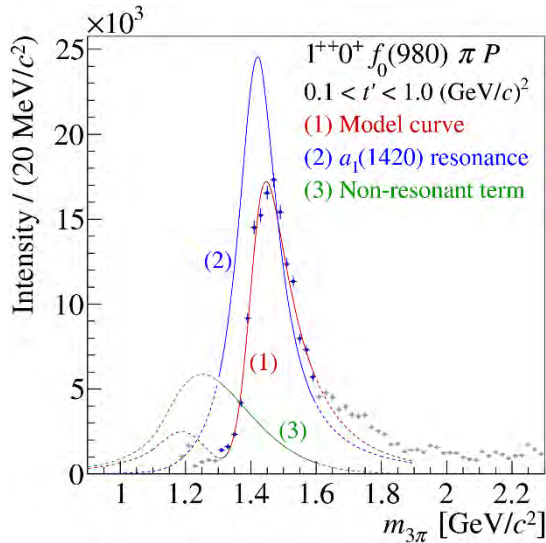
- **Analysis:**

- Partial wave analysis (PWA) in mass bins with 88 waves labelled $J^{PC} M^E$ Isobar L in 11 t' bins
- fit of spin-density matrix for major waves as function of mass
- unprecedented statistical precision

- **Discovery of $a_1(1420)$**

- 46 million events in $0.5 \text{ GeV} < m_{3\pi} < 2.5 \text{ GeV}$ bin
- unexpected narrow axial-vector state found
- [PRL 115 \(2015\) 082001](#)

$a_1(1420)$ in $1^{++}0^+ f_0(980) \pi P$ wave



- **state of unknown nature**

- tetra-quark state
- triangular diagram in $a_1(1260) \rightarrow K^* \bar{K}$; $K^* \pi$ and $K \bar{K} \rightarrow f_0(980)$
- ...

Summary and outlook



- A wealth of data from a decade of COMPASS-I
 - longitudinally polarised DIS and SIDS:
 - spin puzzle: first measurement of small gluon polarisation
 - PDFs, flavour separated quark distributions, BJ sum rule
 - transverse and unpolarised data → Bradamante
 - pion polarisability and other tests of chiral perturbation theory
 - a new quality of spectroscopy data, huge data sets
- Exciting new experiments of COMPASS-II
 - polarised DY, GPDs via DVCS and HEMP, SIDIS with LH2
- What's next? COMPASS-III?
 - until the advent of EIC the CERN COMPASS facility with the versatile M2 beam line remains unique.
 - physics case for 2021-202x after CERN LS2 being built up.
- **New Collaborators and ideas welcome!**

Thank you!