

Measurement of the Pion Polarizability with COMPASS

Stefan Huber
for the COMPASS collaboration

Physik Department E18 - Technische Universität München

CIPANP 2015

2015/05/22



Bundesministerium
für Bildung
und Forschung

 Motivation

Pion structure as fundamental test of QCD (via χ PT)

Quantities describing the charged pion:

- charge known
- scattering length known
- polarisability let's see

 Motivation

Pion structure as fundamental test of QCD (via χ PT)

Quantities describing the charged pion:

- charge **known**
- scattering length **known**
- polarisability **let's see**

 Motivation

Pion structure as fundamental test of QCD (via χ PT)

Quantities describing the charged pion:

- charge **known**
- scattering length **known**
- polarisability **let's see**



Motivation

Pion structure as fundamental test of QCD (via χ PT)

Quantities describing the charged pion:

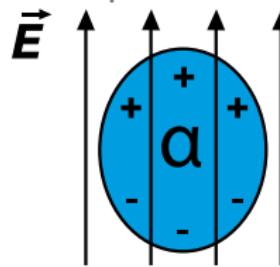
- charge **known**
- scattering length **known**
- polarisability **let's see**

Consider π^- in a strong EM-field ($\approx 300\text{kV/fm}$)

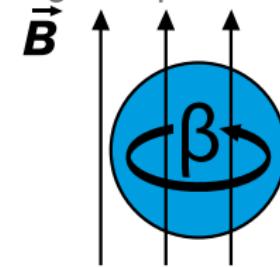
Lowest order correction to point-like structure

Rigidity against deformation

electric polarizability α



magnetic polarizability β

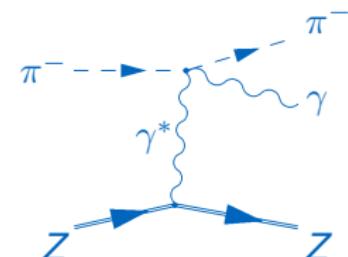
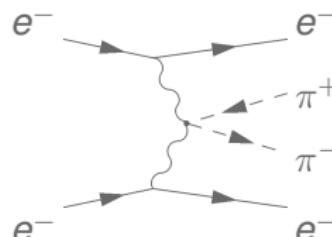
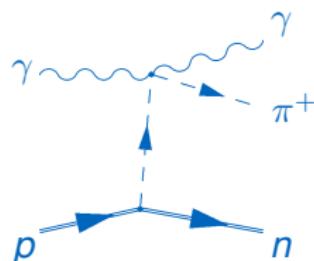


χ PT prediction: $\alpha_\pi - \beta_\pi = 5.7 \pm 1.0 \times 10^{-4} \text{ fm}^3$

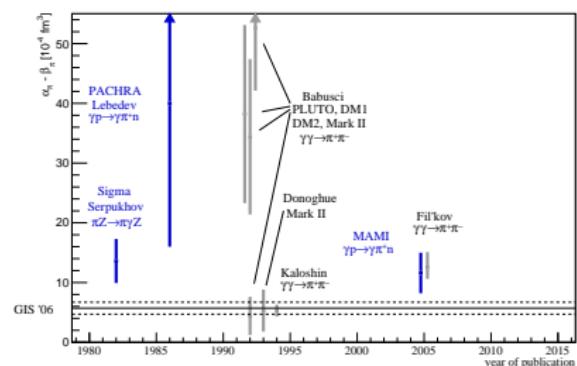
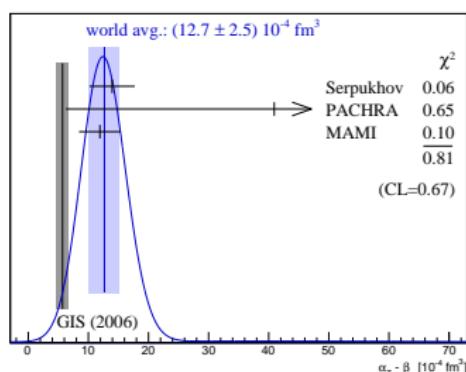
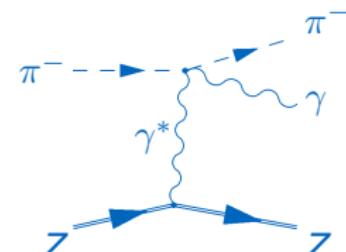
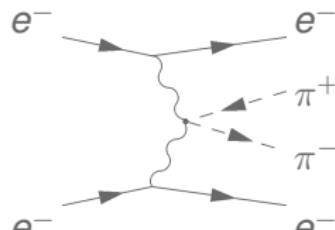
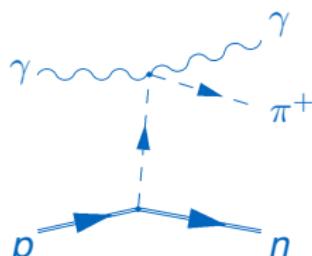
$$\alpha_\pi \approx -\beta_\pi$$

Gasser, Ivanov, Sainio, Nucl. Phys. B 745 (2006) obtained by relating to $\pi^+ \rightarrow e^+ \nu_e \gamma$

Previous Measurements of $\alpha_\pi - \beta_\pi$



Previous Measurements of $\alpha_\pi - \beta_\pi$



χ PT prediction: $\alpha_\pi - \beta_\pi = 5.7 \pm 1.0 \times 10^{-4} \text{ fm}^3$

Gasser, Ivanov, Sainio, Nucl. Phys. B 745 (2006)

$$\alpha_\pi \approx -\beta_\pi$$

Pion Compton Scattering

$\pi^- \gamma \rightarrow \pi^- \gamma$ X-Section

$$\frac{d\sigma_{\pi\gamma}}{d\Omega_{cm}} = \frac{\alpha^2(s^2 z_+^2 + m_\pi^4 z_-^2)}{s(sz_+ + m_\pi^2 z_-)^2} - \frac{\alpha m_\pi^3 (s - m_\pi^2)^2}{4s^2(sz_+ + m_\pi^2 z_-)} \cdot \textcolor{red}{P}$$

$$\textcolor{red}{P} = z_-^2(\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+(\alpha_\pi + \beta_\pi)$$

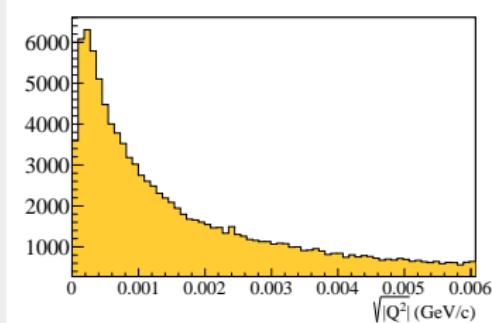
$$z_\pm = 1 \pm \cos \theta_{cm}$$

COMPASS: $\pi^- \text{Ni} \rightarrow \pi^- \text{Ni} \gamma$

Related to $\pi\gamma \rightarrow \pi\gamma$ by Weizäcker-Williams Approximation

$$\frac{d\sigma}{ds dQ^2 d\Omega_{CM}} \propto \frac{Q^2 - Q_{min}^2}{Q^4} \cdot \frac{d\sigma_{\pi\gamma}}{d\Omega_{CM}}$$

⇒ Smallest momentum transfers
 $Q^2 \approx 10^{-5} \text{ GeV}^2/\text{c}^2$





Primakoff reactions

COMPASS: $\pi^- \text{Ni} \rightarrow \pi^- \text{Ni} \gamma$

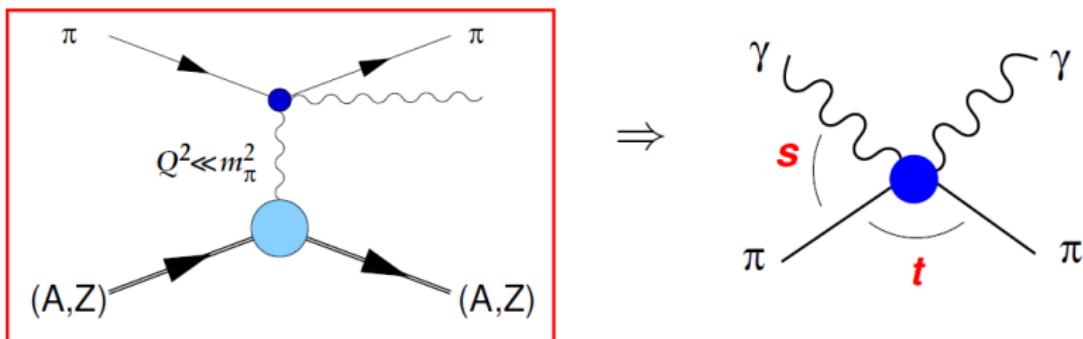
Related to $\pi\gamma \rightarrow \pi\gamma$ by Weizäcker-Williams Approximation

$$\frac{d\sigma}{ds dQ^2 d\Omega_{\text{CM}}} \propto \frac{Q^2 - Q_{\min}^2}{Q^4} \cdot \frac{d\sigma_{\pi\gamma}}{d\Omega_{\text{CM}}}$$

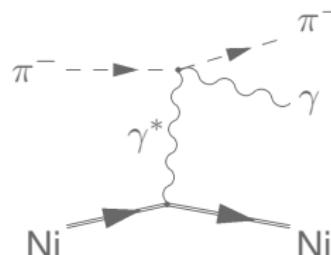
⇒ Smallest momentum transfers

$$Q^2 \approx 10^{-5} \text{ GeV}^2/c^2$$

Scattering on quasi real photons



Technique



Primakoff scattering on the Coulomb field of Ni nuclei

$$\frac{d\sigma_{\pi\gamma}}{dE_\gamma} = \frac{d\sigma_{\text{Born}}}{dE_\gamma} + \frac{d\sigma_{\text{pol}}}{dE_\gamma}$$

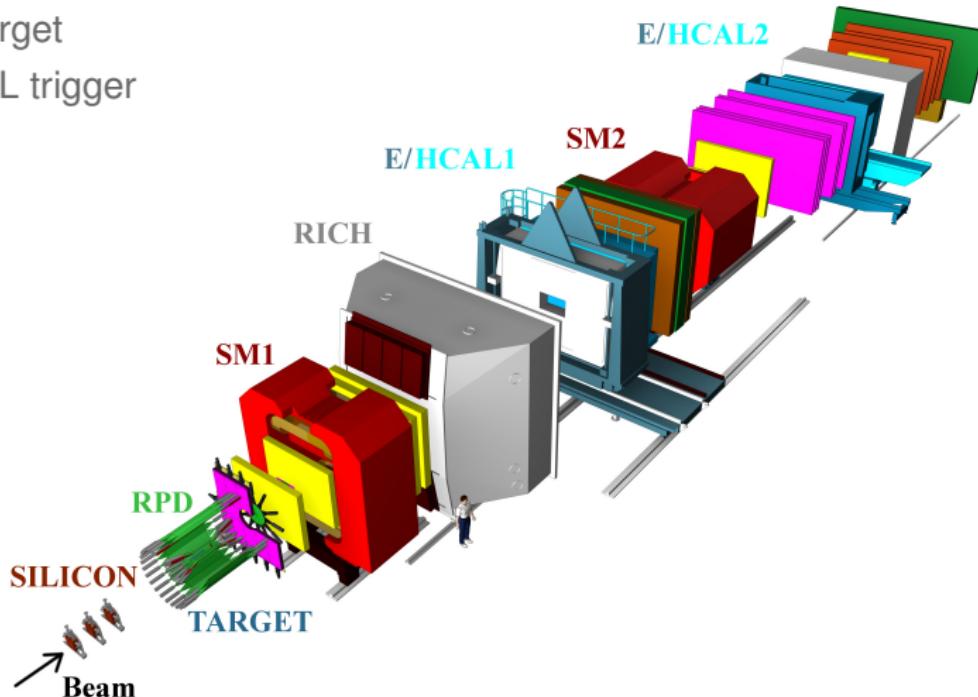
Cross-section ratio dependent on $x_\gamma = E_\gamma / E_{\text{beam}}$

$$R(x_\gamma) = \frac{N_{\text{data}}(x_\gamma)}{N_{\text{sim}}^{\text{born}}(x_\gamma)} \approx 1 + \frac{3}{2} \frac{m_\pi^3 x_\gamma}{\alpha_{em} (1 - x_\gamma)} \alpha_\pi$$

Important components

coMmon Muon Proton Apparatus for Structure and Spectroscopy

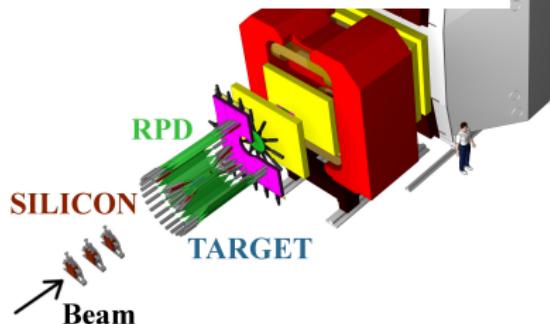
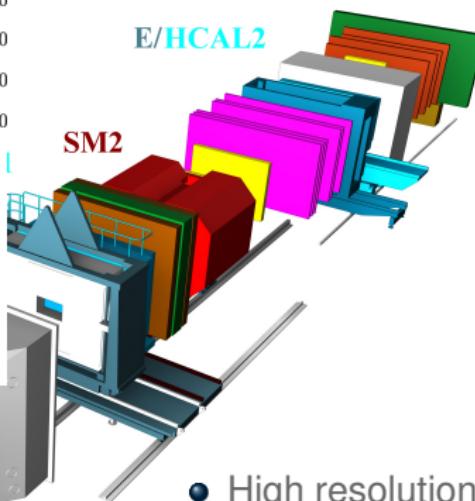
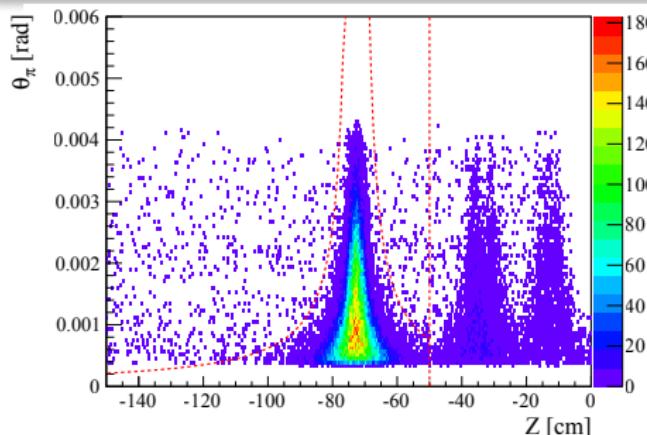
- π^- and μ^- Beams
- Ni target
- ECAL trigger





Important components

co
mmon Muon Proton Apparatus for Structure and Spectroscopy

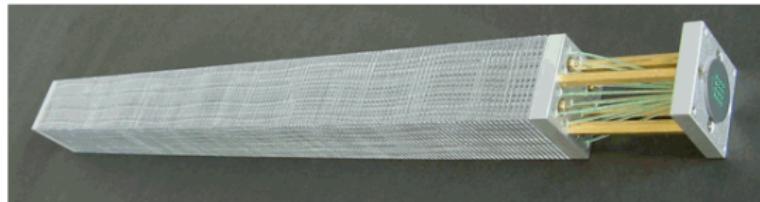


- High resolution vertexing
- Precise Calorimetry
- Calibrations/Alignment

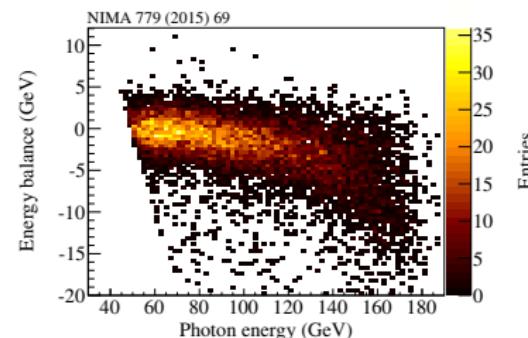
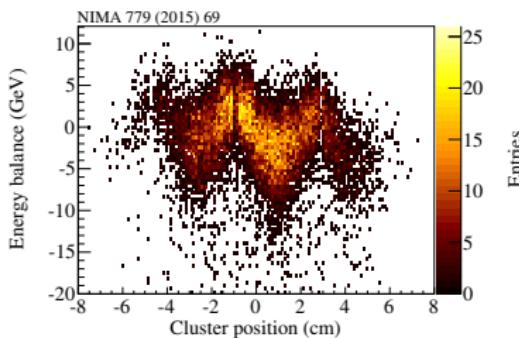


Important components

It's all about resolution



COMPASS calorimeter cell

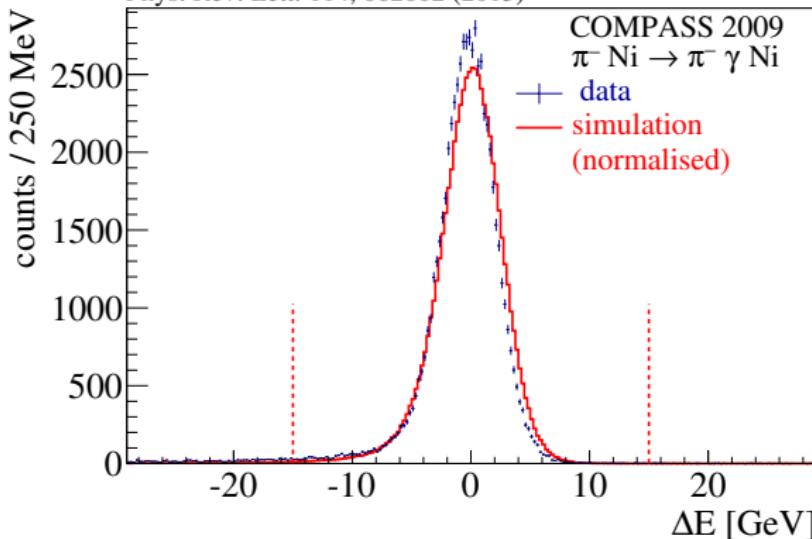


Position dependend energy calibrations necessary

Selection of $\pi\gamma \rightarrow \pi\gamma$ events

$$\Delta E = E_\gamma + E_{\pi^-} - E_{beam}$$

Phys. Rev. Lett. 114, 062002 (2015)

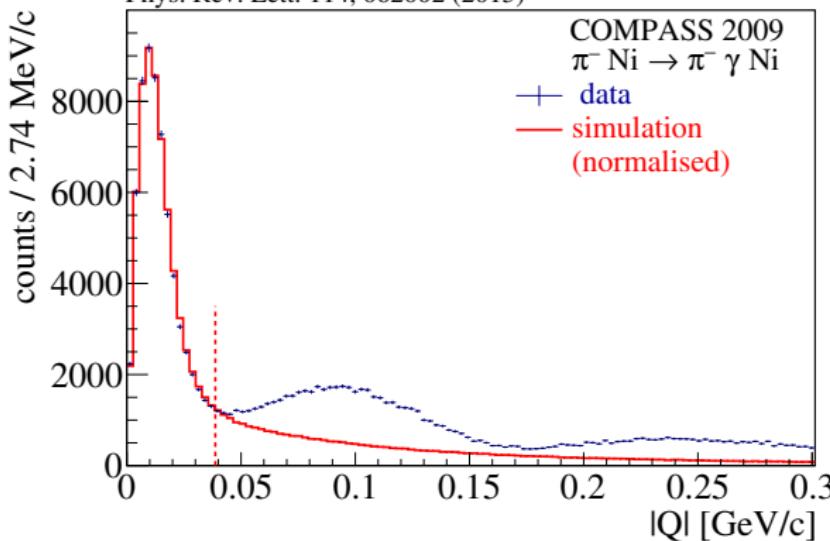


About 60 000 **exclusive** events

Four-Momentum transfer

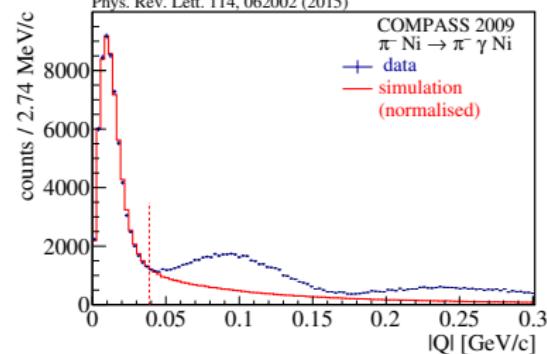
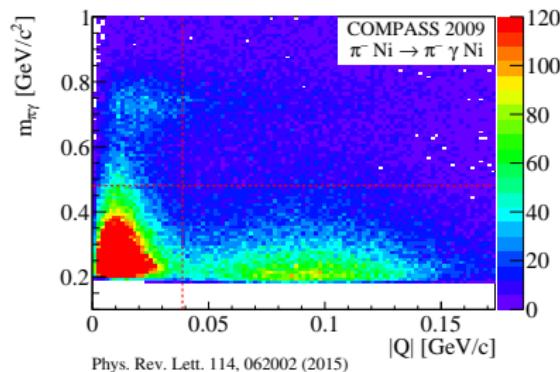
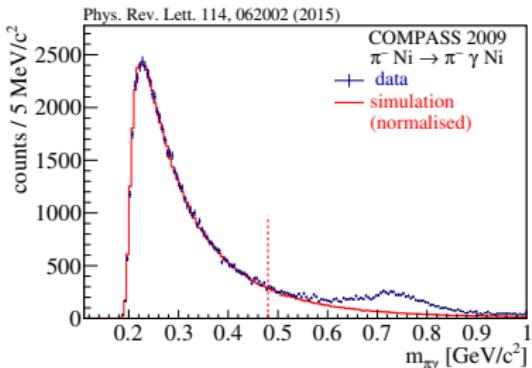
$$|Q| = \sqrt{|Q^2|}$$

Phys. Rev. Lett. 114, 062002 (2015)



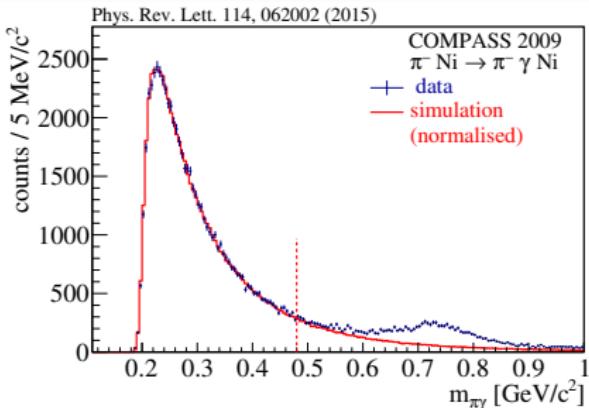
Primakoff production distinguishable from strong interaction
by cut on $Q^2 < 1.5 \cdot 10^{-3} \text{ GeV}^2/\text{c}^2$

Backgrounds in the Pion measurement



- Background coming from mis-identified π^0
- Background from strong interaction

Background coming from mis-identified π^0

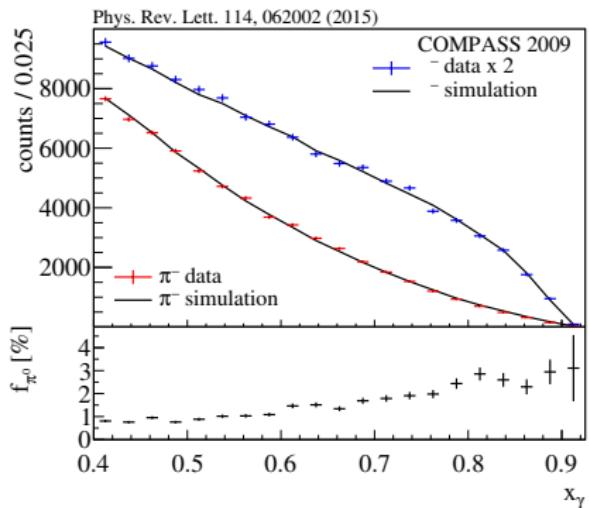
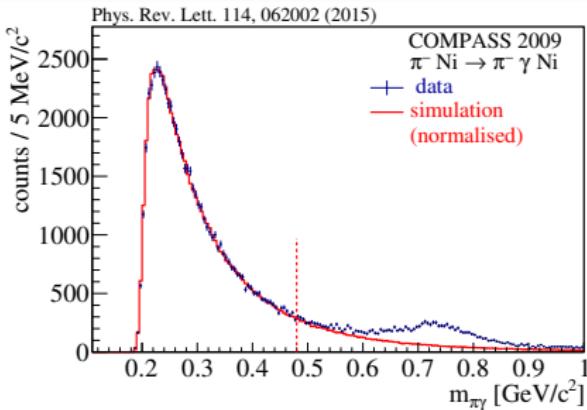


Background fraction

Beam kaon content

- Decay: $K^- \rightarrow \pi^- \pi^0$
- Determine mis-identification probability
- Scale by $\pi^- \text{Ni} \rightarrow \pi^- \text{Ni} \pi^0$

Background coming from mis-identified π^0

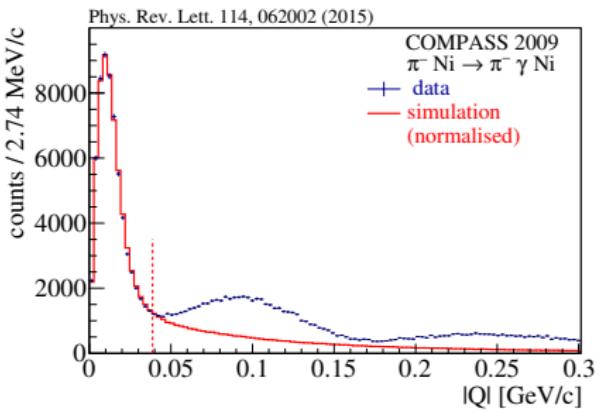


Background fraction

Beam kaon content

- Decay: $K^- \rightarrow \pi^- \pi^0$
- Determine mis-identification probability
- Scale by $\pi^- \text{Ni} \rightarrow \pi^- \text{Ni} \pi^0$

Background coming from strong interaction



Background fraction

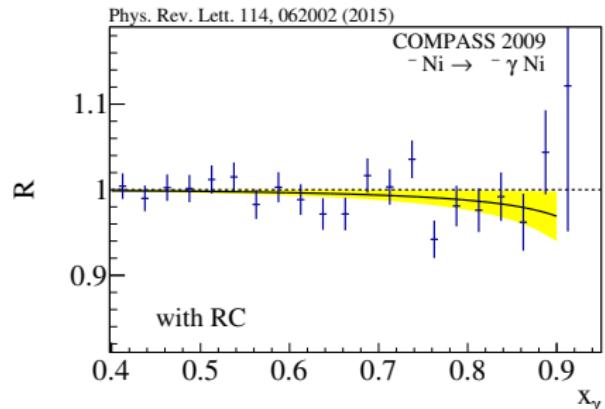
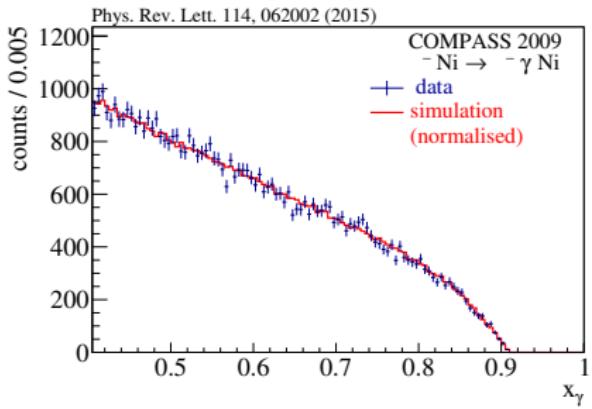
- Fit with Primakoff-peak shape, diffractive pattern and interference term
- Take into account resolution
- Indications for negative interference
- Result statistically limited \Rightarrow systematic error



Muon control measurement

Unique Feature

- Switching between π^- and μ^- beams
- Background free reaction of point-like particle
- Allows control of systematic effects

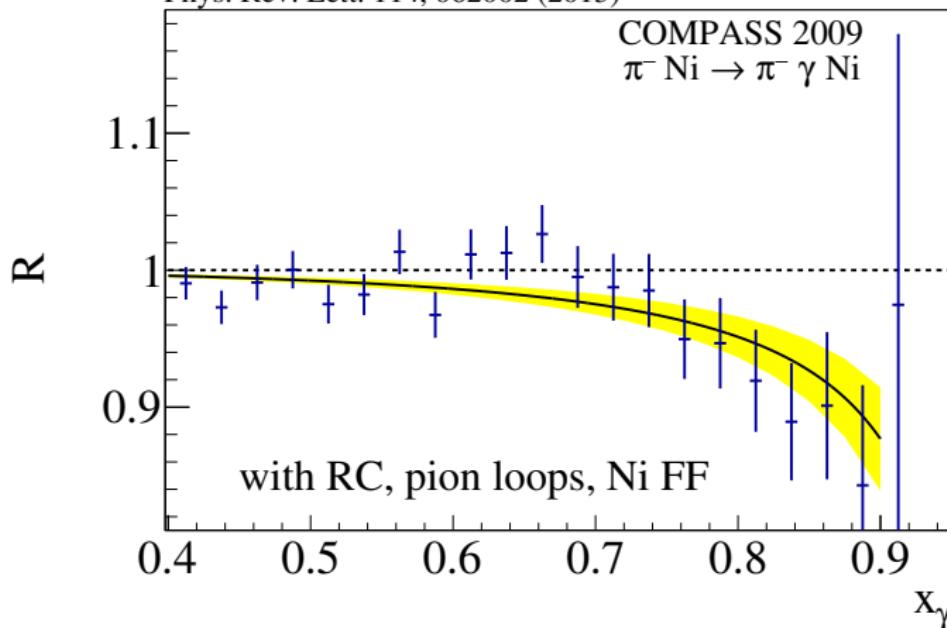


False polarizability for Muons compatible with point-like structure

$$\alpha_\mu^{\text{false}} = (0.5 \pm 0.5_{\text{stat}}) \times 10^{-4} \text{ fm}^3$$

 Fit to the data

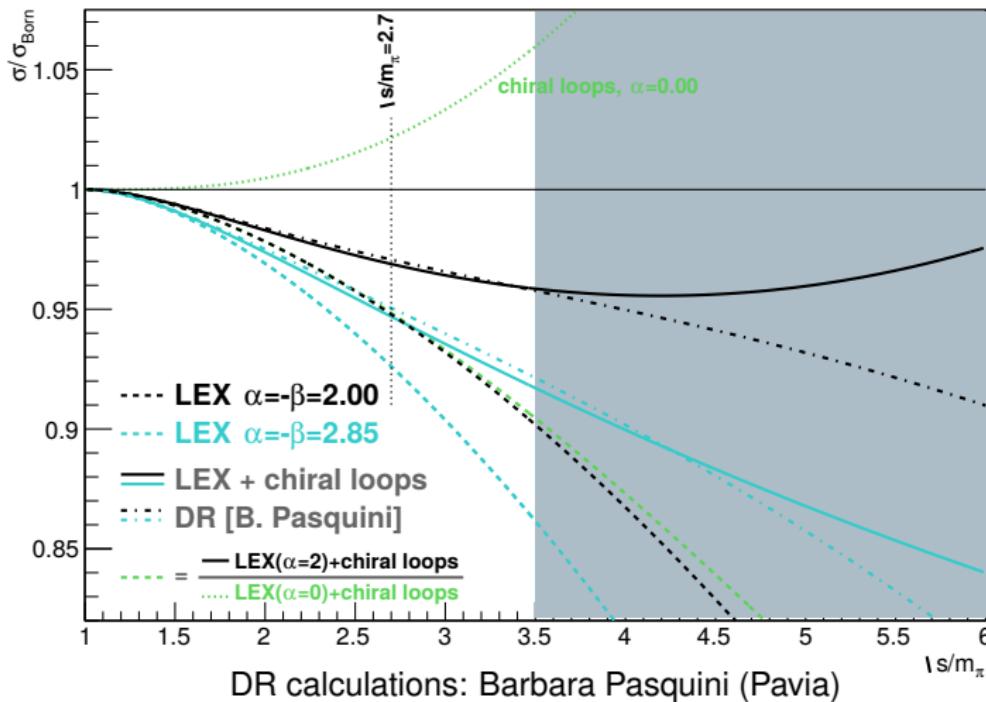
Phys. Rev. Lett. 114, 062002 (2015)



$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}}) \times 10^{-4} \text{ fm}^3$$

Validity of the chiral expansion

Polarisability and Loop Contributions $z=-1.0$

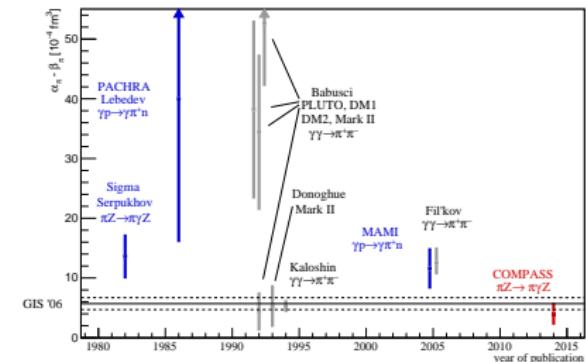
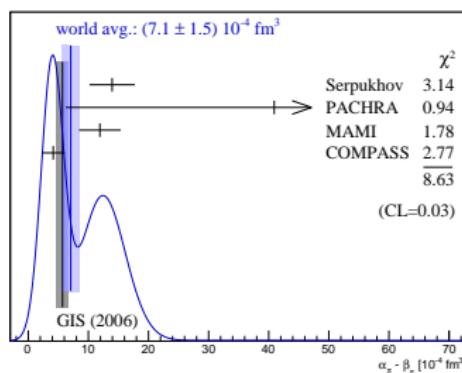


 Systematic uncertainties

Source of uncertainty	Estimated magnitude [10^{-4} fm 3]
Determination of tracking detector efficiency	0.5
Treatment of radiative corrections	0.3
Subtraction of π^0 background	0.2
Strong interaction background	0.2
Pion-electron elastic scattering	0.2
Contribution of muons in the beam	0.05
Quadratic sum	0.7

Result

- COMPASS result:
 $\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst.}}) \times 10^{-4} \text{ fm}^3$
- Assumption: $\alpha_\pi = -\beta_\pi$
- In tension with previous measurements
- Measurement in agreement with χ PT prediction
- Most precise determination of π^- -polarizability



 Conclusion

- COMPASS result:
 $\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst.}}) \times 10^{-4} \text{ fm}^3$
 - Strong constraints on previous experiments
 - In tension with previous measurements
 - Measurement in agreement with χ PT prediction
 - Published in Phys. Rev. Lett. 114, 062002 (2015)
-
- Bigger data set from 2012
 - Separate measurement of α_π, β_π
 - Kaon polarizabilities