



*Measurement of the  
charged pion polarisability  
at COMPASS*

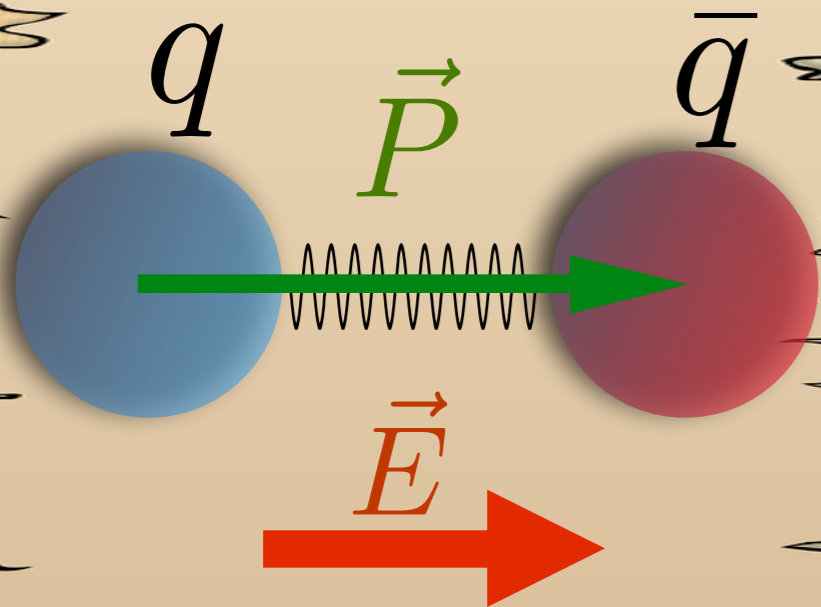


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on behalf of the COMPASS collaboration*



*Vienna, 23.07.2015*

# Polarizabilities of hadrons



$$\vec{P} = \alpha_X \vec{E}$$

$$\vec{\mu} = \beta_X \vec{H}$$

The electric and magnetic polarizabilities of a hadron are the quantities characterizing the rigidity of QCD system

$$H = \dots -(\alpha_X E^2 + \beta_X H^2)/2$$

**Compton amplitude:**

$$A(\gamma X \rightarrow \gamma X) = \dots$$

$$\dots + \alpha_\pi \omega_1 \omega_2 \hat{e}_1 \cdot \hat{e}_2 +$$

$$+ \beta_\pi \omega_1 \omega_2 (\hat{e}_1 \times \hat{q}_1) (\hat{e}_2 \times \hat{q}_2)$$

**PDG data:**

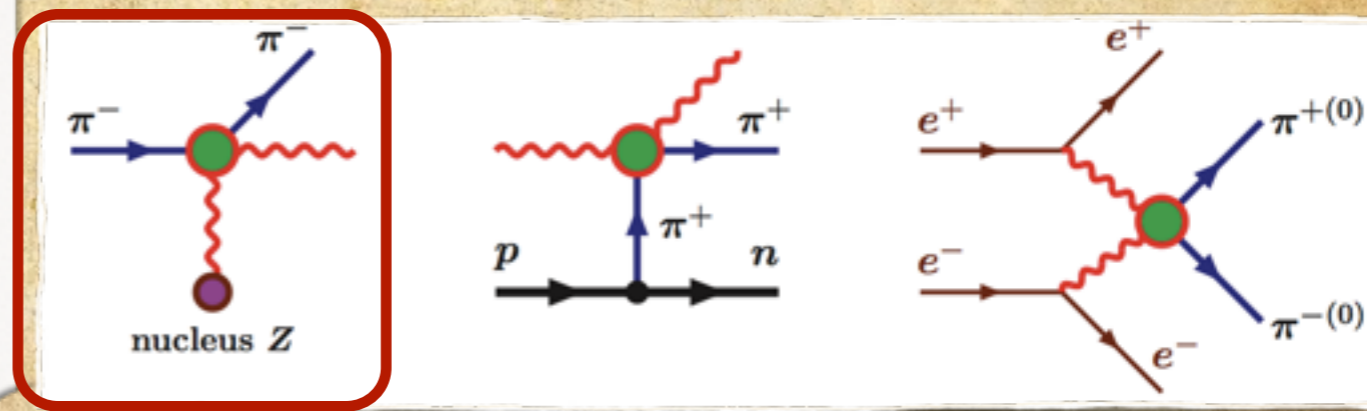
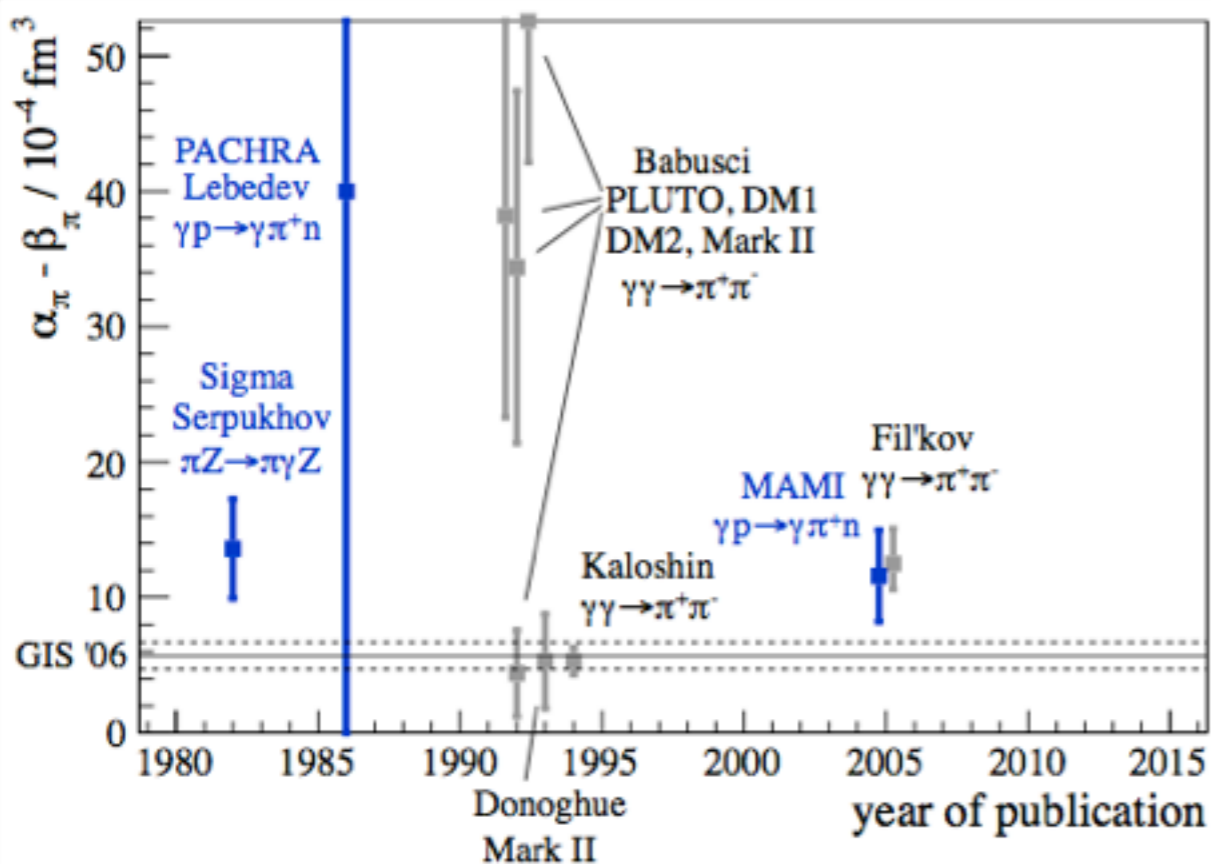
	$\alpha_X, 10^{-4} \text{ fm}^3$	$\beta_X, 10^{-4} \text{ fm}^3$
$p$	$12.0 \pm 0.6$	$1.9 \mp 0.6$
$n$	$12.5 \pm 1.7$	$2.7 \mp 1.8$

$\pi, K?$

# Expectations and results for $a_\pi, \beta_\pi$

Model	Parameter	$10^{-4} \text{ fm}^3$
$\chi$ PT (2-loops)	$a_\pi - \beta_\pi$	$5.7 \pm 1.0$
	$a_\pi + \beta_\pi$	$0.16$

Data	Reaction	Parameter	$[10^{-4} \text{ fm}^3]$
Serpukhov ( $\alpha_\pi + \beta_\pi = 0$ )	$\pi Z \rightarrow \pi Z \gamma$	$\alpha_\pi$	$6.8 \pm 1.4 \pm 1.2$
Serpukhov ( $\alpha_\pi + \beta_\pi \neq 0$ )		$\alpha_\pi + \beta_\pi$	$1.4 \pm 3.1 \pm 2.8$
		$\beta_\pi$	$-7.1 \pm 2.8 \pm 1.8$
Lebedev	$\gamma N \rightarrow \gamma N \pi$	$\alpha_\pi$	$20 \pm 12$
Mami A2	$\gamma p \rightarrow \gamma \pi^+ n$	$\alpha_\pi - \beta_\pi$	$11.6 \pm 1.5 \pm 3.0 \pm 0.5$
PLUTO	$\gamma\gamma \rightarrow \pi^+ \pi^-$	$\alpha_\pi$	$19.1 \pm 4.8 \pm 5.7$
DM1	$\gamma\gamma \rightarrow \pi^+ \pi^-$	$\alpha_\pi$	$17.2 \pm 4.6$
DM2	$\gamma\gamma \rightarrow \pi^+ \pi^-$	$\alpha_\pi$	$26.3 \pm 7.4$
Mark II	$\gamma\gamma \rightarrow \pi^+ \pi^-$	$\alpha_\pi$	$2.2 \pm 1.6$
Combined fit: MARK II, VENUS, ALEPH, TPC/2 $\gamma$ , CELLO, BELLE (L. Fil'kov, V. Kashevarov)	$\gamma\gamma \rightarrow \pi^+ \pi^-$	$\alpha_\pi - \beta_\pi$	$13.0^{+2.6}_{-1.9}$
		$\alpha_\pi + \beta_\pi$	$0.18^{+0.11}_{-0.02}$
Combined fit: MARK II, Crystal Ball (A. Kaloshin, V. Serebryakov)	$\gamma\gamma \rightarrow \pi^+ \pi^-$	$\alpha_\pi - \beta_\pi$	$5.25 \pm 0.95$



*At the moment experimental uncertainty for pion polarizabilities is too high. New experiments are needed!*

# Pion polarizabilities and cross section

$$\frac{d\sigma}{ds dt dQ^2} = \frac{Z^2 \alpha}{\pi(s - m_\pi^2)} \cdot F_{\text{eff}}^2(Q^2) \cdot \frac{Q^2 - Q_{\text{min}}^2}{Q^4} \cdot \frac{d\sigma_{\pi\gamma}}{dt}$$

$$Q_{\text{min}} = (s - m_\pi^2)/2E_{\text{beam}}$$

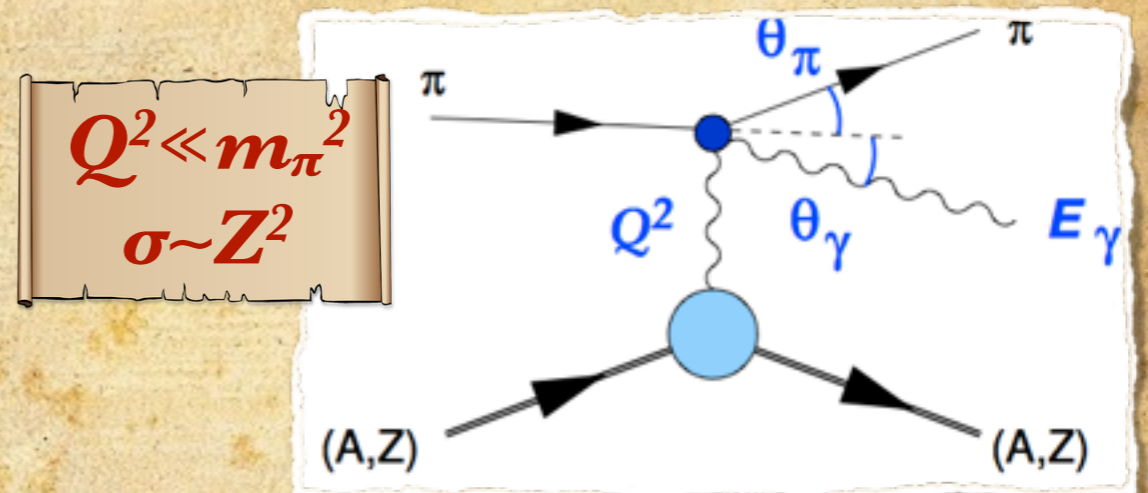
Compton cross section:

$$\frac{d\sigma_{\pi\gamma}}{d\Omega_{\text{cm}}} = \frac{\alpha^2(s^2 z_+^2 + m_\pi^4 z_-^2)}{s(sz_+ + m_\pi^2 z_-)^2} - \frac{\alpha m_\pi^3 (s - m_\pi^2)^2}{4s^2(sz_+ + m_\pi^2 z_-)} \cdot \mathcal{P}$$

$$z_\pm = 1 \pm \cos \theta_{\text{cm}}$$

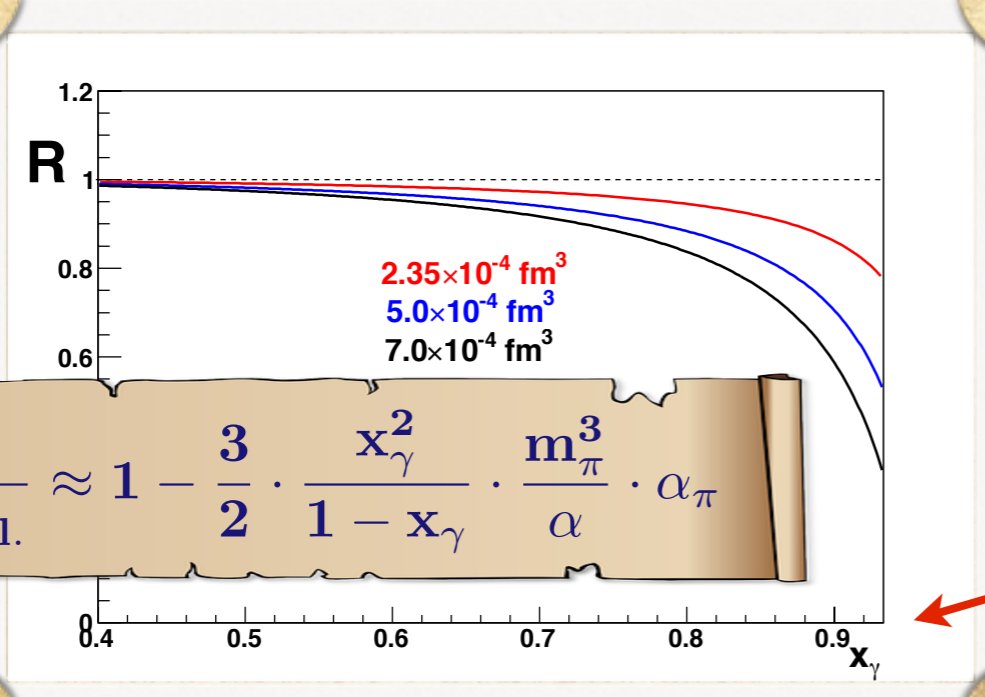
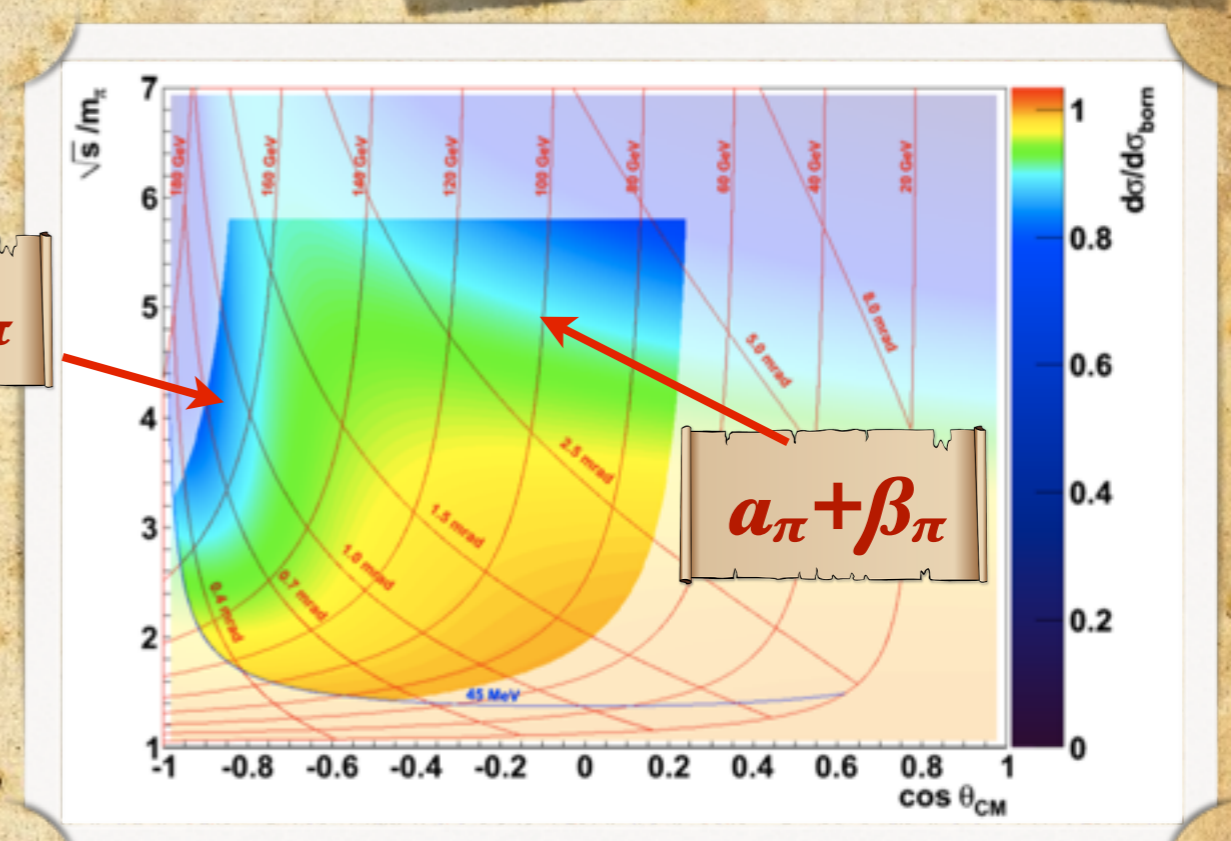
$$\mathcal{P} = z_-^2(\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+^2(\alpha_\pi + \beta_\pi)$$

Simplest case:  $\alpha_\pi = -\beta_\pi$



$$Q^2 \ll m_\pi^2$$

$$\sigma \sim Z^2$$



$$R = \frac{\sigma}{\sigma_{\text{p.l.}}} \approx 1 - \frac{3}{2} \cdot \frac{x_\gamma^2}{1 - x_\gamma} \cdot \frac{m_\pi^3}{\alpha} \cdot \alpha_\pi$$

$x_\gamma$  - relative energy of emitted photon in Lab system

# The COMPASS experiment

**COMPASS** (**CO**mmun **M**uon **P**roton **A**pparatus for **S**tructure and **S**pectroscopy) is the fixed target experiment on the secondary beam of Super Proton Synchrotron at CERN



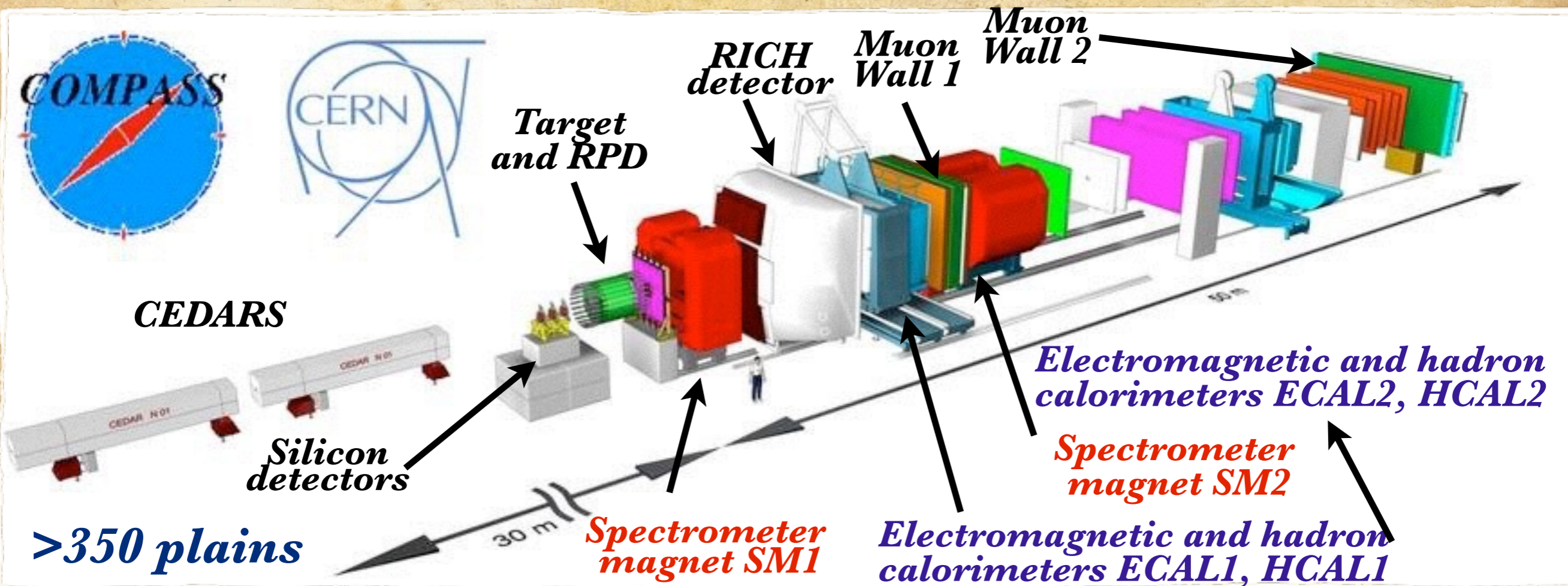
The purpose of this experiment is the study of hadron structure and hadron spectroscopy with high intensity muon and hadron beams.

1996 - Proposal  
2002-2015 - Physical data taking

13 countries,  
24 institutions,  
~220 physicists



# The COMPASS setup



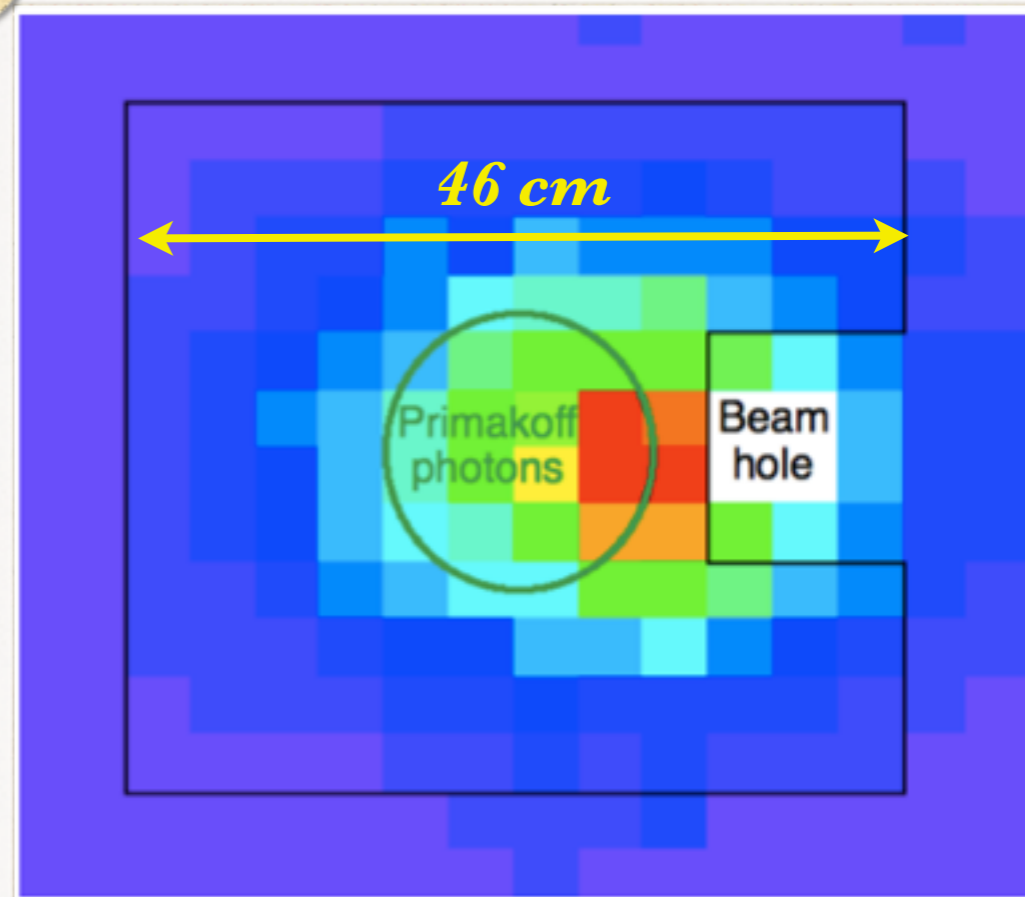
- CEDAR detectors for beam particle identification
- Precise silicon detectors to measure small scattering angles
- Magnetic spectrometer for pion momentum measurement
- Electromagnetic calorimeter with good energy and spacial resolution for photon detection
- Muon identification system
- Possibility to use pion and muon beams of the same momentum

# Trigger



**TRIGGER = (BC & ECAL2)**  
**!SW !BK1 !BK2**

Trigger name	ECAL2 threshold, GeV	Scale factor	Rate, kHz
Primakoff 1	~40	2	~20
Primakoff 2	~60	1	



# Event selection

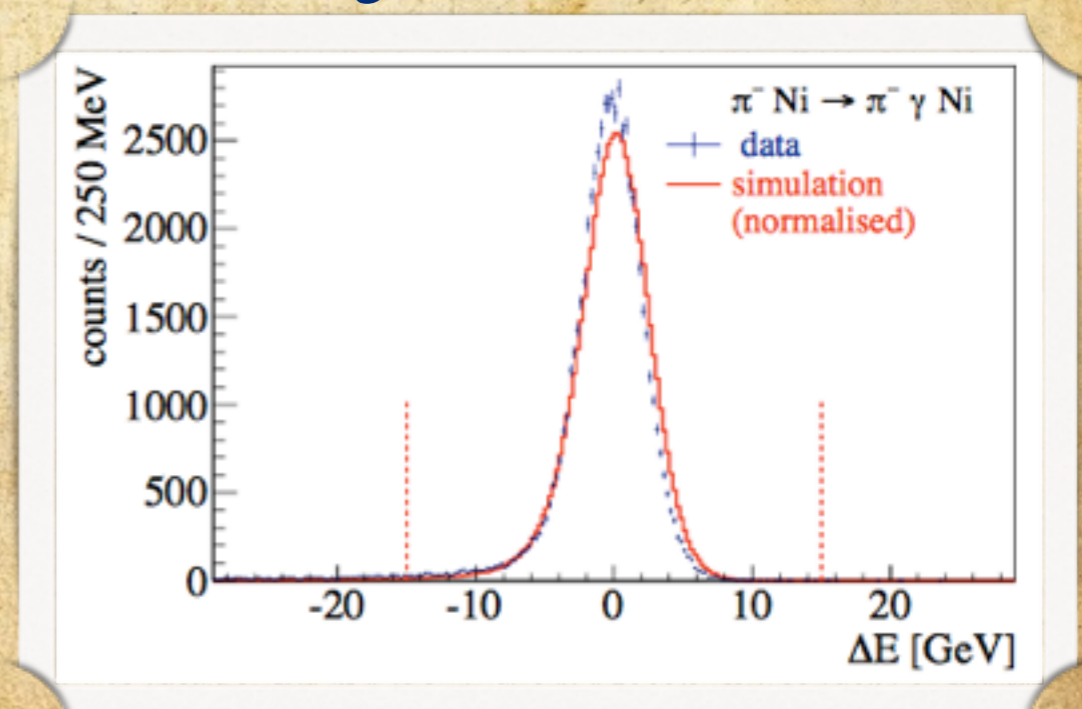
- *Primakoff1, Primakoff2 triggers*
- *1 vertex with 1 outgoing negative track*
- *No other tracks*
- *Beam track is parallel to the nominal beam axis*
- *Scattered track is not muon*
- *No activity in RPD*
- *Exactly 1 neutral cluster in ECAL2 ( $E > 2$  GeV)*
- *Beam particle is pion (CEDAR)*
- *Exclusivity cut on the level  $\pm 15$  GeV to reject events with missed particles in the final state*

- *Parallel analysis of three channels*

$$\pi^- Ni \rightarrow \pi^- Ni \gamma$$

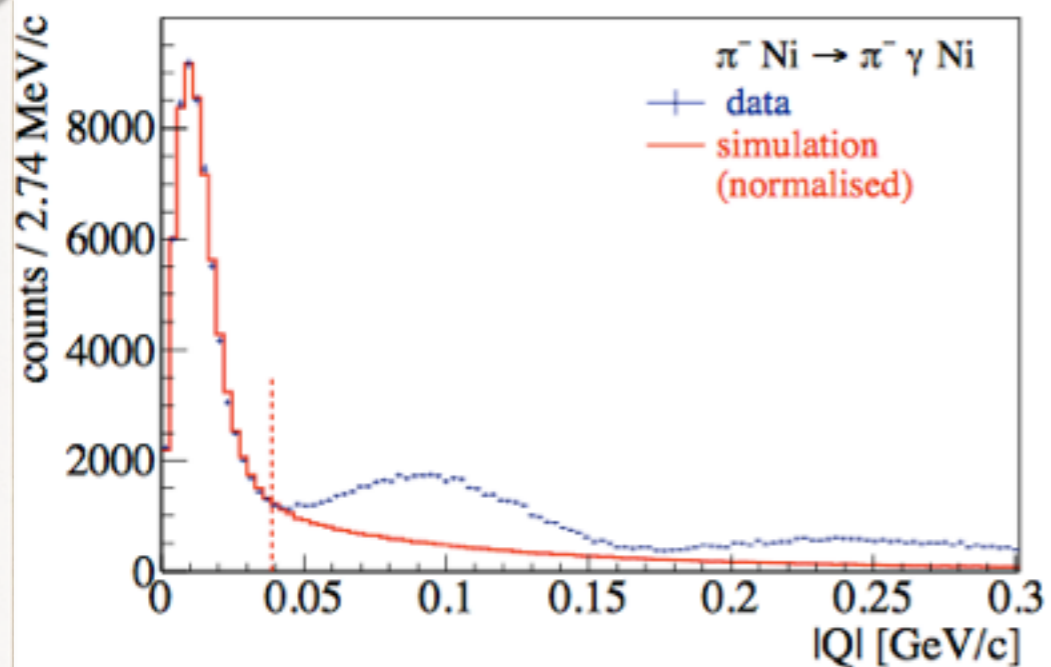
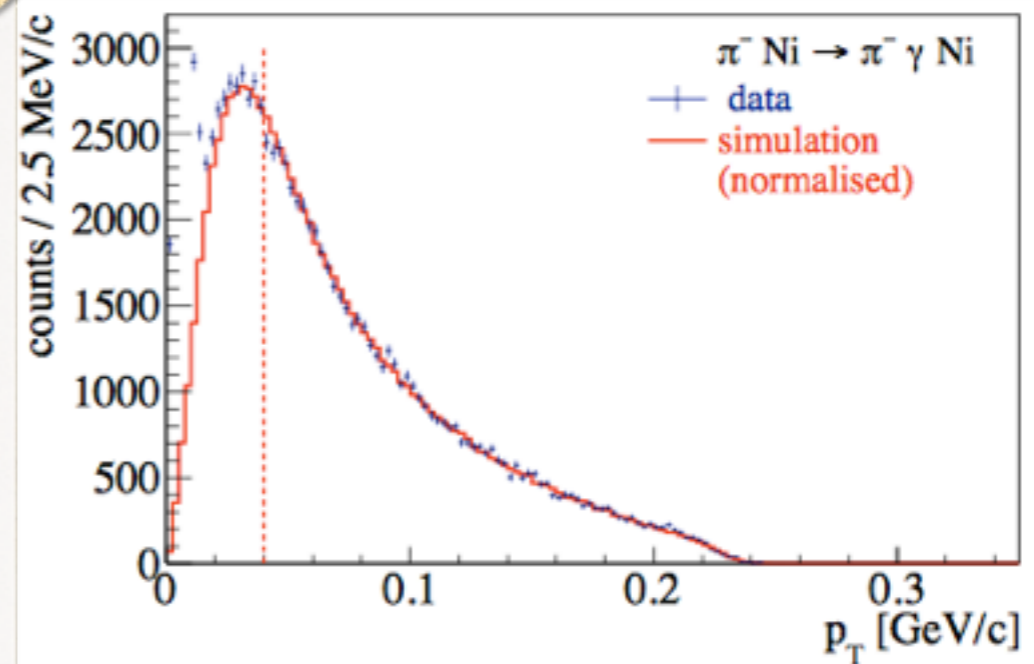
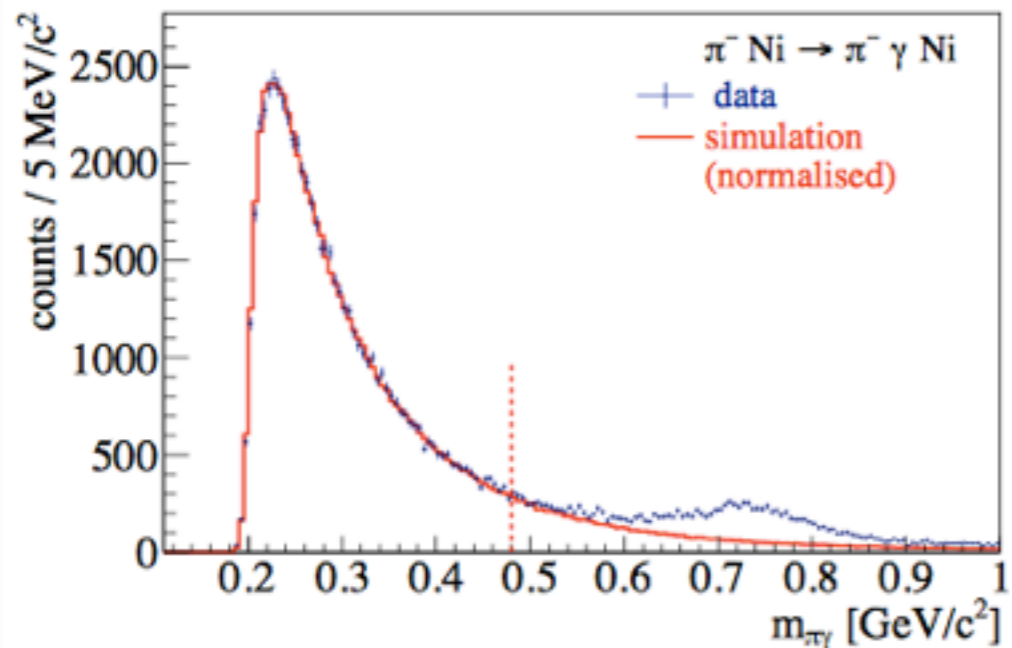
$$\mu^- Ni \rightarrow \mu^- Ni \gamma$$

$$\pi^- Ni \rightarrow \pi^- Ni \pi^0 \rightarrow \pi^- Ni \gamma \gamma$$





# Kinematic cuts

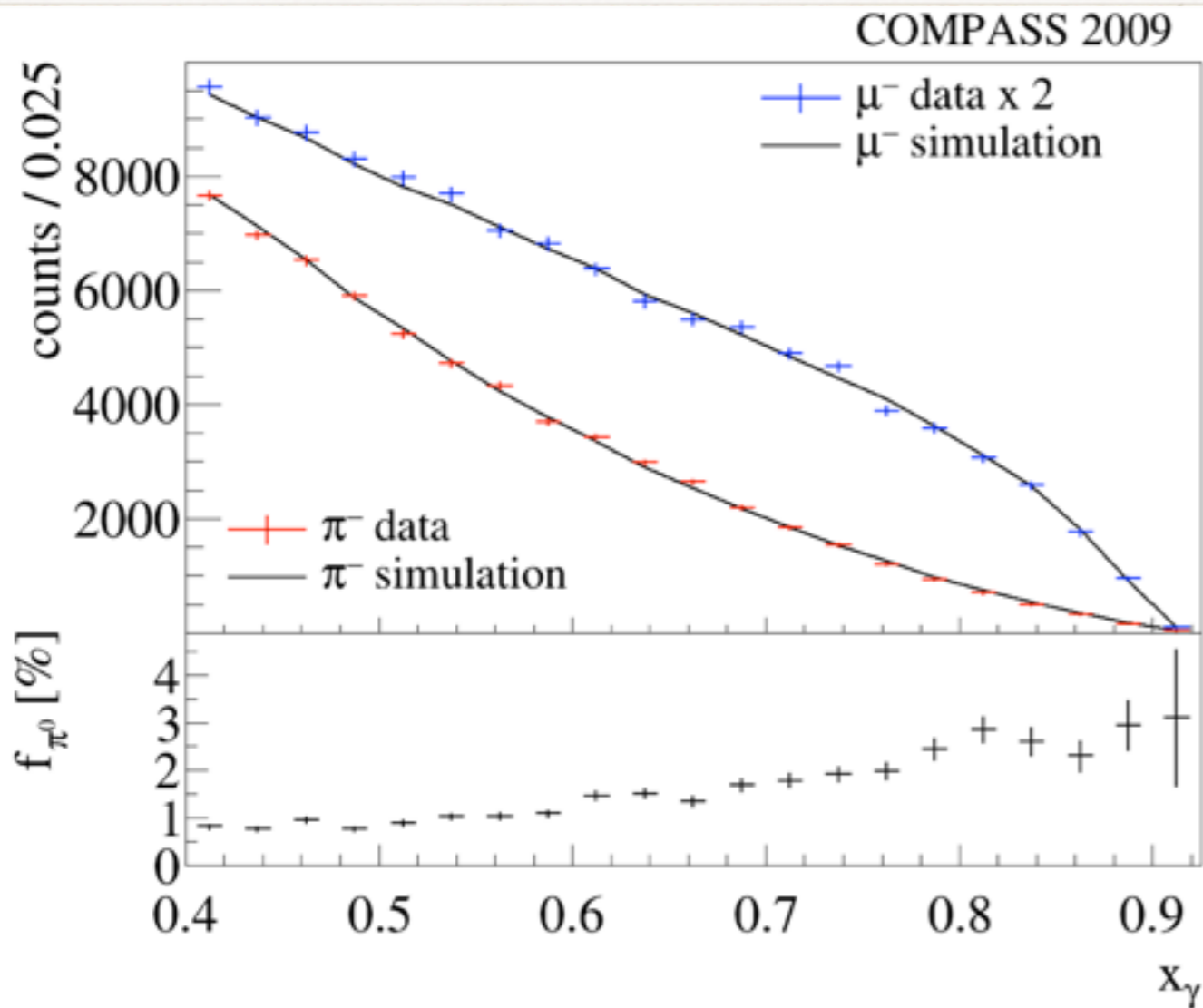


*$p_T$ -cut to reject low  $p_T$  region related with multiple scattering in the material*

*$M_{\pi\gamma} < 3.5 m_\pi$  to suppress  $\rho$ -meson production and decay to  $\pi\pi^0$*

*$Q^2 < 1.5 \times 10^{-3} (\text{GeV}/c)^2$  to reject  $\pi\gamma$  state production via strong interaction*

# The measured $x_\gamma$ distributions



Main background:  
 $\pi^- Ni \rightarrow \pi^- Ni \pi^0 \rightarrow \pi^- Ni \gamma \gamma$

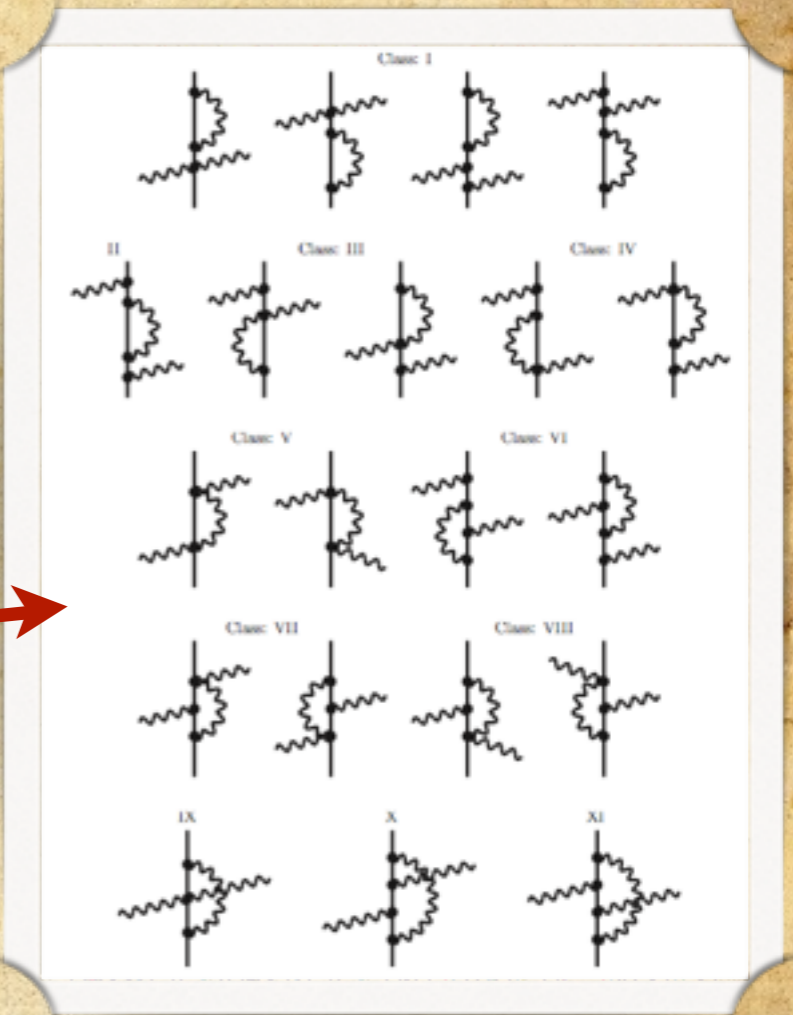
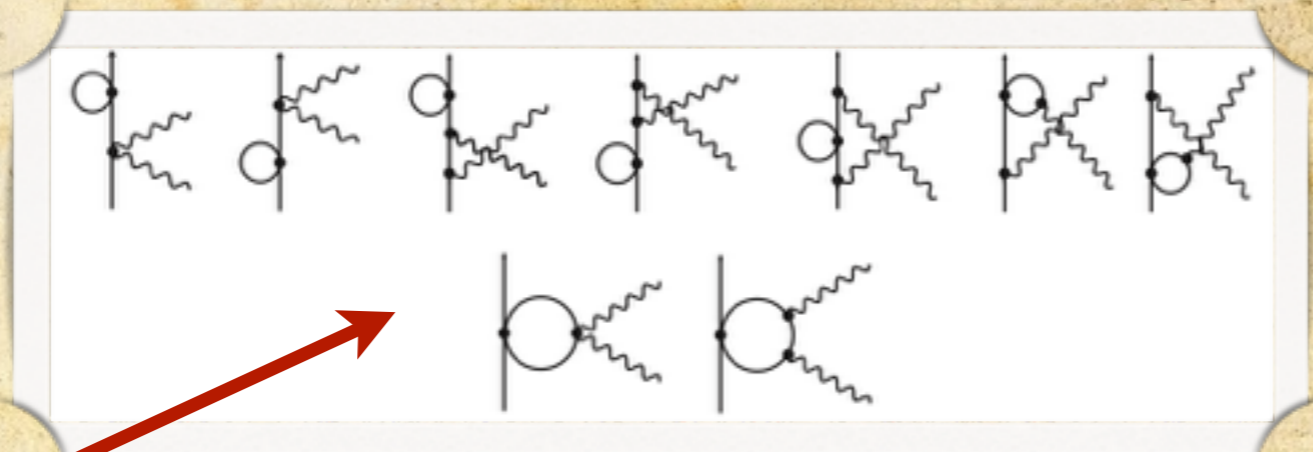
$\gamma$  lost

single cluster  
in ECAL2

Kaon decay  $K^- \rightarrow \pi^- \pi^0$   
out of the target was  
the reference process

Fraction of mis-reconstructed  $\pi^- \pi^0$  events in  $\pi^- \gamma$  sample from kaon decay was used to estimate contribution  $f_{\pi^0}$  of  $\pi^0$  background

# Corrections



*applied*

- *pion rescattering*
- *radiative corrections (Compton vertex)*
- *form factor of the Ni nucleus*

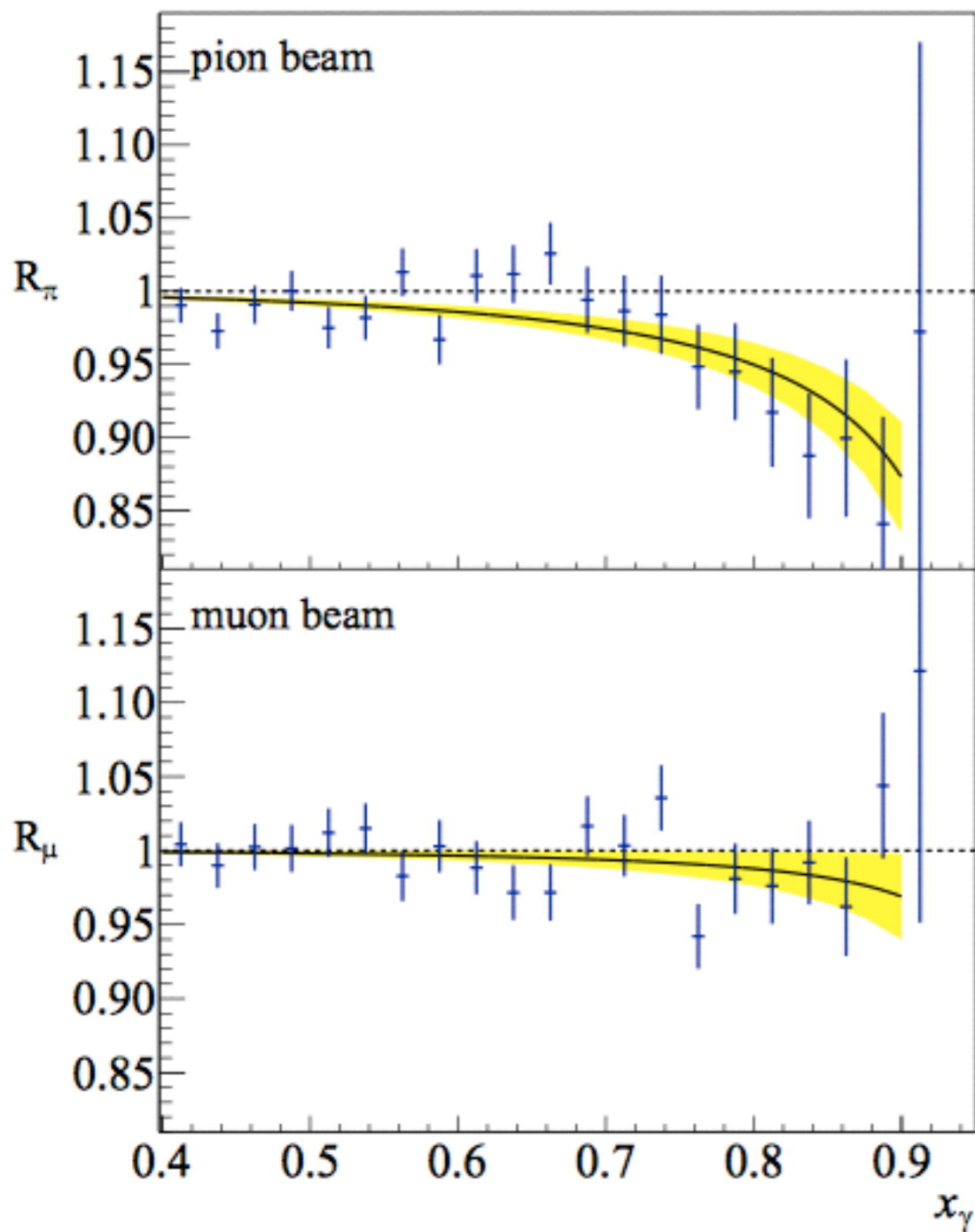
*put to systematics*

- *High Z effects ( $Z\alpha=0.2$ )*
- *Nuclear charge screening by atomic electrons*

# The COMPASS result



2009



Source of uncertainty	Estimated magnitude [ $10^{-4} \text{ fm}^3$ ]
Determination of tracking detector efficiency	0.5
Treatment of radiative corrections	0.3
Subtraction of $\pi^0$ background	0.2
Strong interaction background	0.2
Pion-electron elastic scattering	0.2
Contribution of muons in the beam	0.05
Quadratic sum	0.7

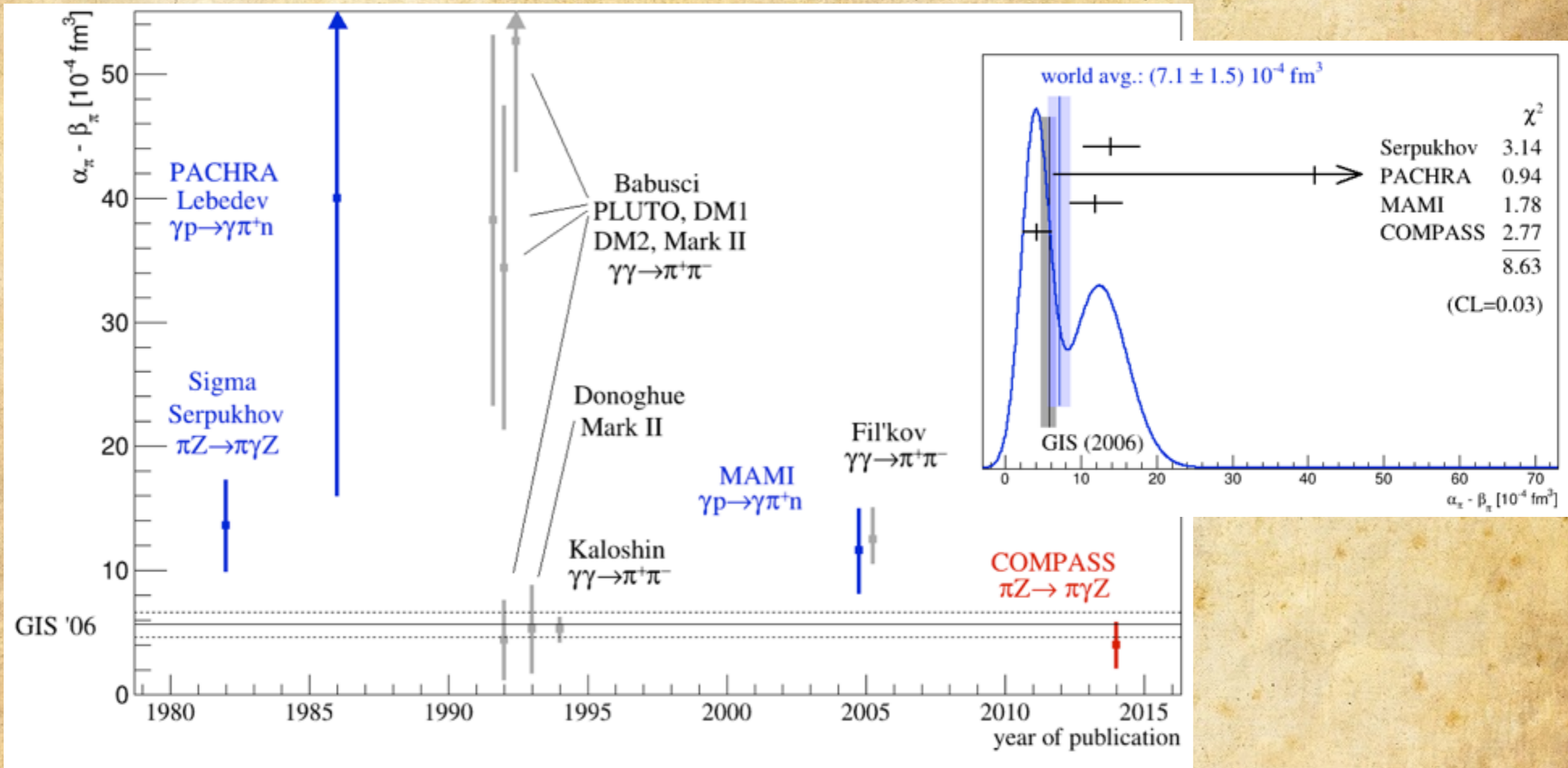
Under assumption  $a_\pi = -\beta_\pi$ :

$$a_\pi = (2.0 \pm 0.6_{stat} \pm 0.7_{syst}) \times 10^{-4} \text{ fm}^3$$

*Phys. Rev. Lett.* 114 (2015) 06002

Protvino:  $a_\pi = -\beta_\pi = (6.8 \pm 1.4_{stat} \pm 1.2_{syst}) \times 10^{-4} \text{ fm}^3$ ,  $\chi\text{PT}$ :  $a_\pi \approx 2.8 \times 10^{-4} \text{ fm}^3$

# Pion polarizabilities and COMPASS



2009

**COMPASS preliminary result for pion polarizability is the most precise among dedicated measurements**

# Summary

● **The COMPASS experiment performed the most precise dedicated measurement of pion polarizability  $a_\pi$  under assumption  $a_\pi + \beta_\pi = 0$  basing on the data of 2009 year.**

● **The result is:**

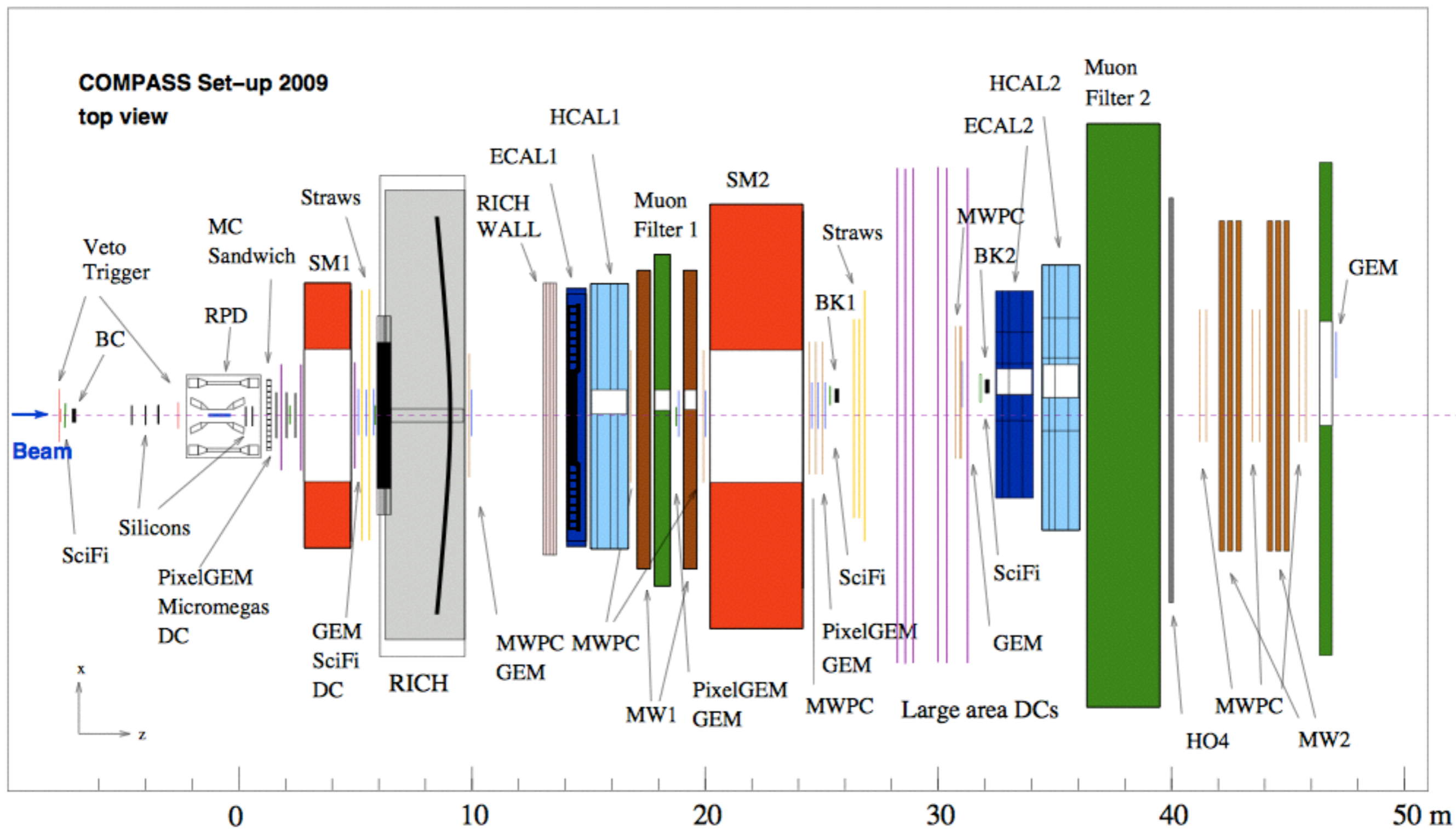
$$a_\pi = (2.0 \pm 0.6_{stat} \pm 0.7_{syst}) \times 10^{-4} \text{ fm}^3$$

**published in *PRL* 114 (2015) 06002**



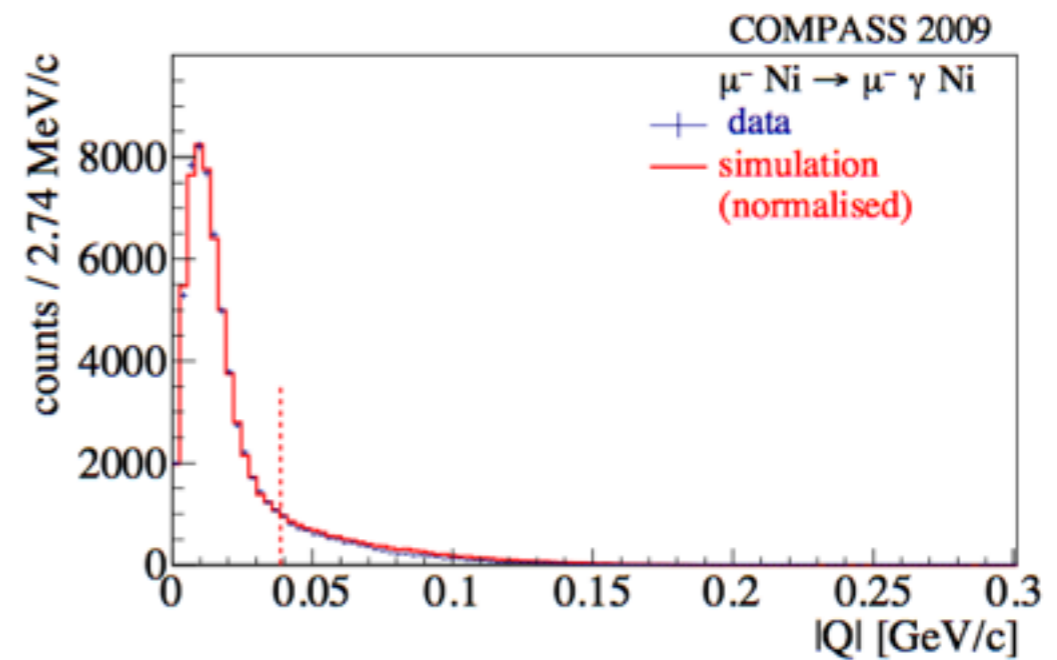
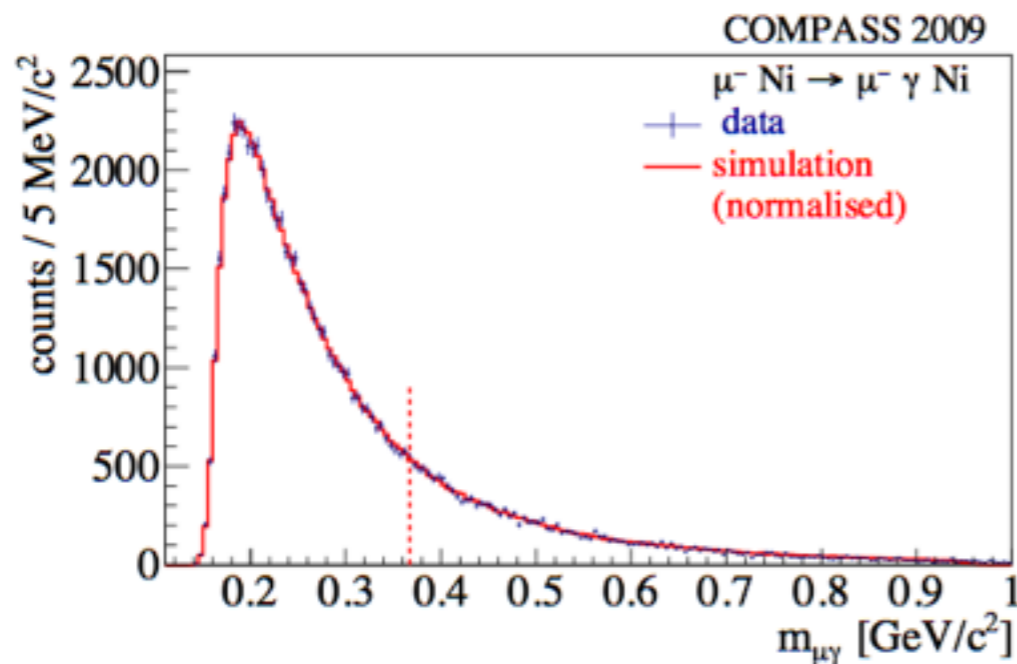
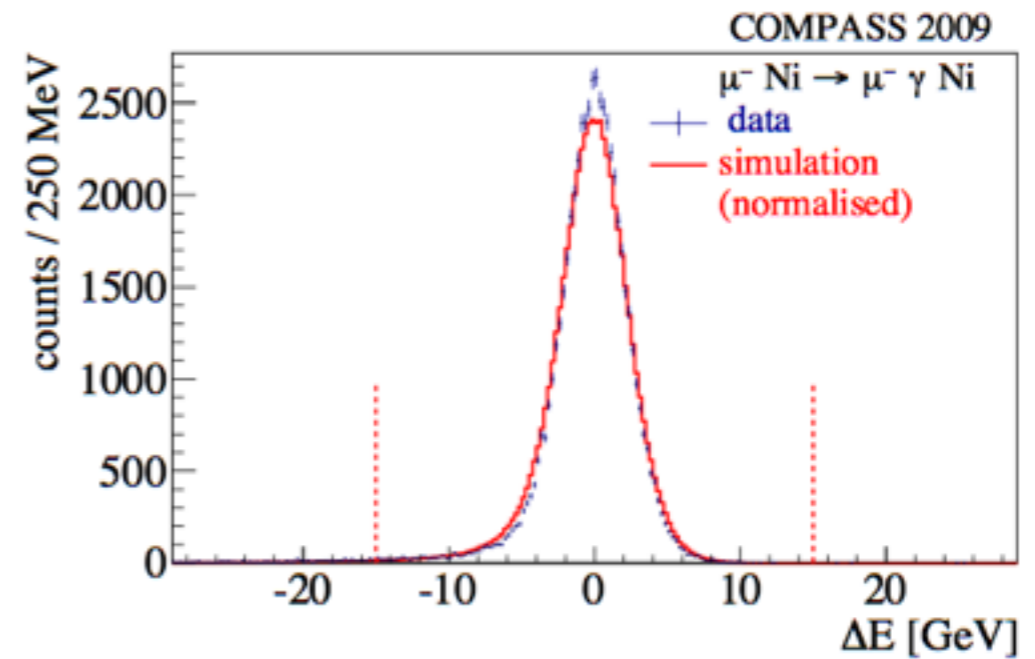
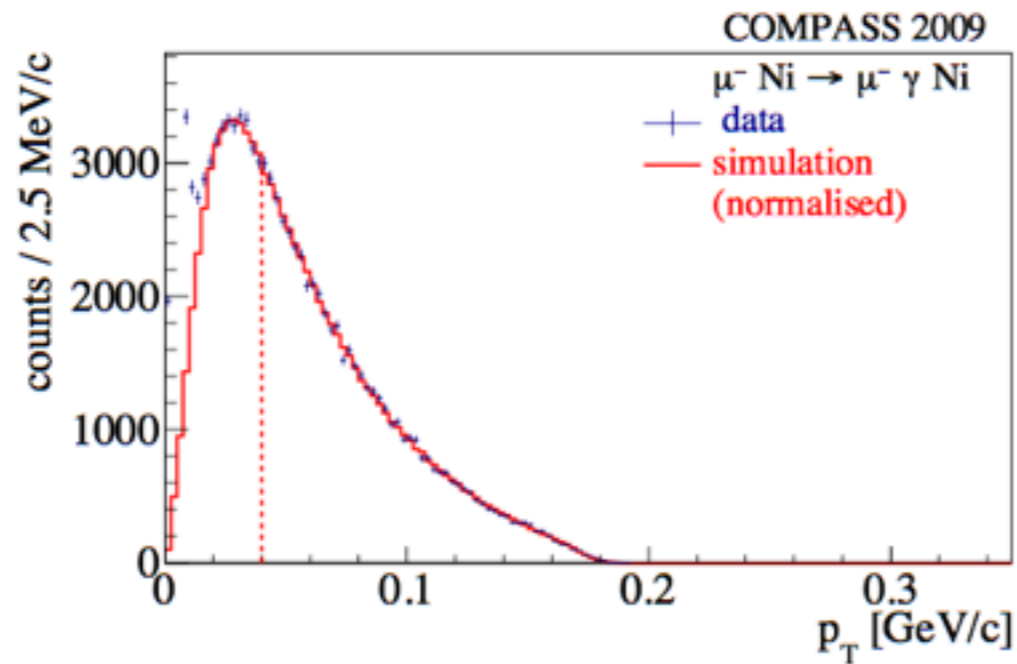
● **COMPASS Primakoff data of 2012 still are under analysis and new results for pion (**and kaon**) polarizabilities are expected**

# Backup slides



# Muon data

The same selection + muon beam momentum measurement





# Backup slides

## Polarisability and Loop Contributions $z=-1.0$

