

# Light Scalar Mesons in Central Production at COMPASS

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for the  
COMPASS Collaboration

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Großgeräte der physikalischen  
Grundlagenforschung





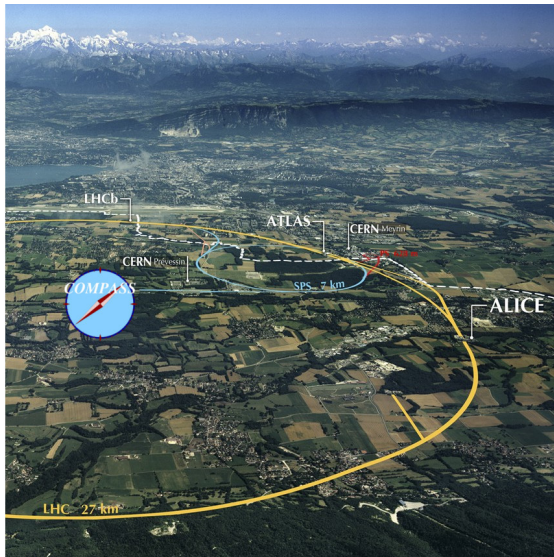
Light Scalar Mesons

Central Production

Partial-Wave Analysis

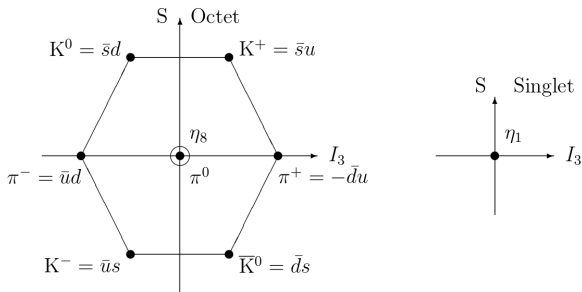
$t$ -Dependent Analysis

Interpretation





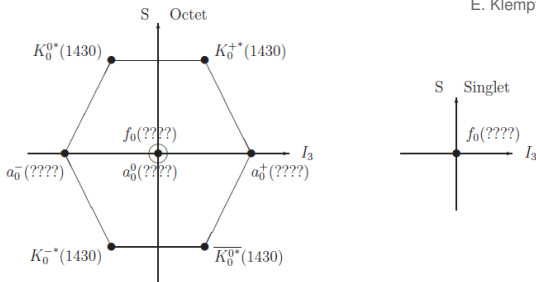
- Flavour SU(3): Mesons are grouped into  $3 \otimes 3 = 8 \oplus 1$  nonets



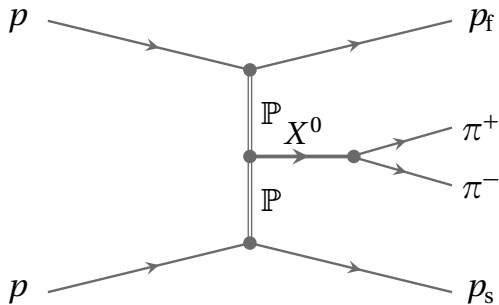


- Flavour SU(3): Mesons are grouped into  $3 \otimes 3 = 8 \oplus 1$  nonets
- Scalar isoscalar mesons ( $I^G J^{PC} = 0^+ 0^{++}$ ):  
 $f_0(500)$ ,  $f_0(980)$ ,  $f_0(1370)$ ,  $f_0(1500)$ ,  $f_0(1710)$ , ...

'ground state nonet of scalar mesons as most physicists in the field would agree upon'  
 E. Klempt [arXiv:hep-ex/0101031]



- **Super-numerous  $f_0$  states** not understood by constituent quark models  
 $\Rightarrow$  Mixing with **Glueballs?**



$$pp \rightarrow p_{\text{fast}} X p_{\text{slow}}$$

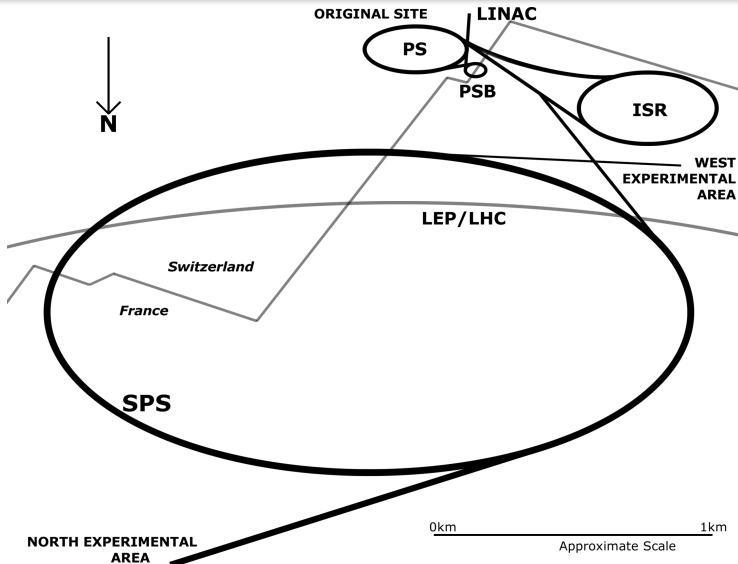
- Proton beam impinging on proton target, both **stay intact** and are detected
- Double-Pomeron production of meson system (**gluon-rich environment**)
- Decay into two pseudoscalar mesons ( $\pi^+ \pi^-$ ,  $\pi^0 \pi^0$ ,  $K^+ K^-$ ,  $\eta \eta$ , ..)



# Central Production at CERN



Technische Universität München

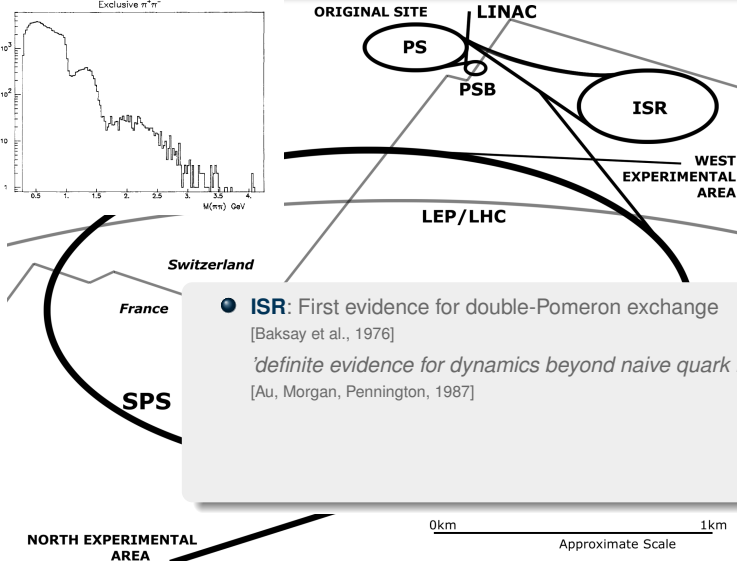
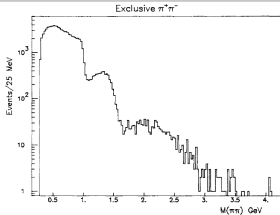




# Central Production at CERN



Technische Universität München

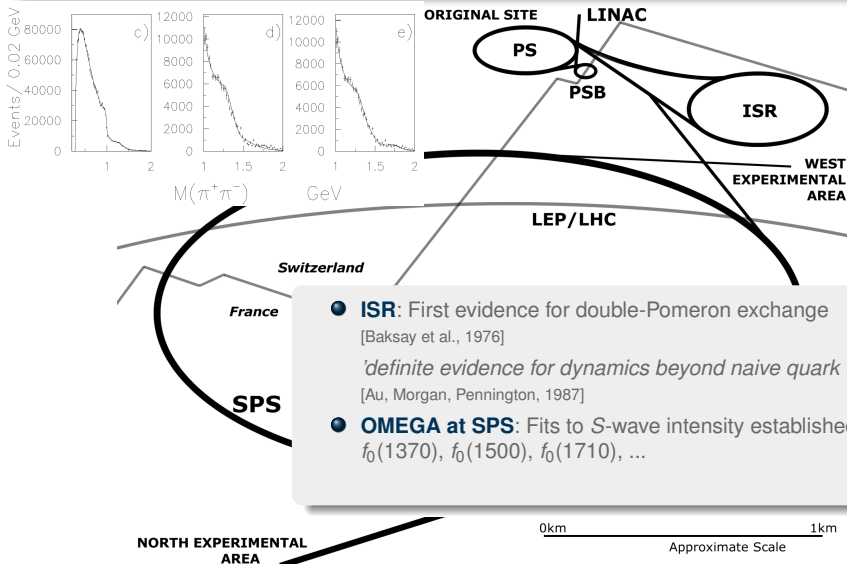


● **ISR**: First evidence for double-Pomeron exchange [Baksay et al., 1976]  
*'definite evidence for dynamics beyond naive quark model'* [Au, Morgan, Pennington, 1987]

0km 1km  
 Approximate Scale



# Central Production at CERN



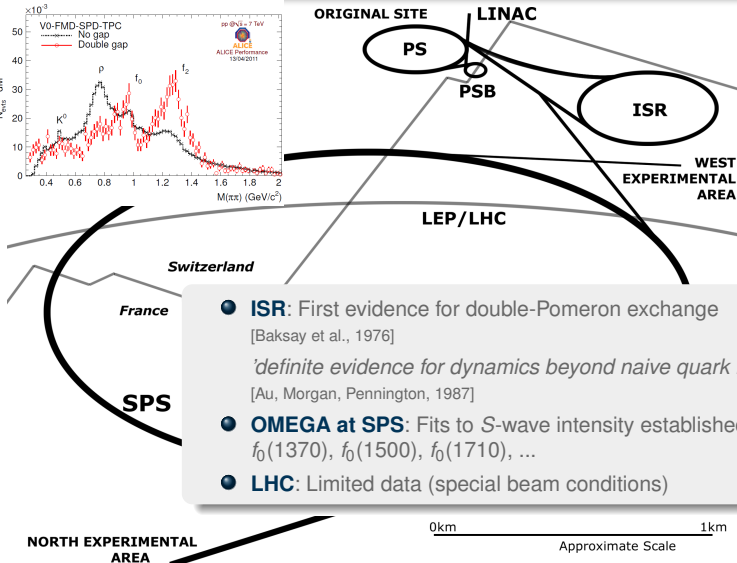
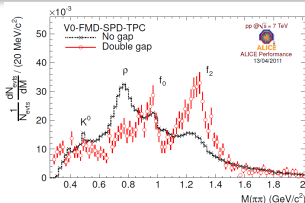




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- **ISR:** First evidence for double-Pomeron exchange [Baksay et al., 1976]  
*'definite evidence for dynamics beyond naive quark model'* [Au, Morgan, Pennington, 1987]
- **OMEGA at SPS:** Fits to  $S$ -wave intensity established  $f_0(1370)$ ,  $f_0(1500)$ ,  $f_0(1710)$ , ...
- **LHC:** Limited data (special beam conditions)

0km 1km

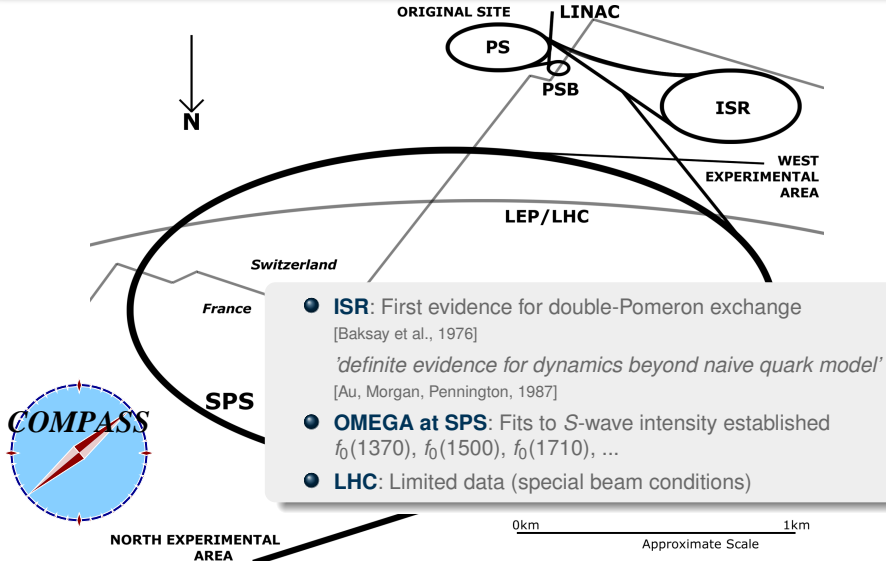
Approximate Scale



# Central Production at CERN



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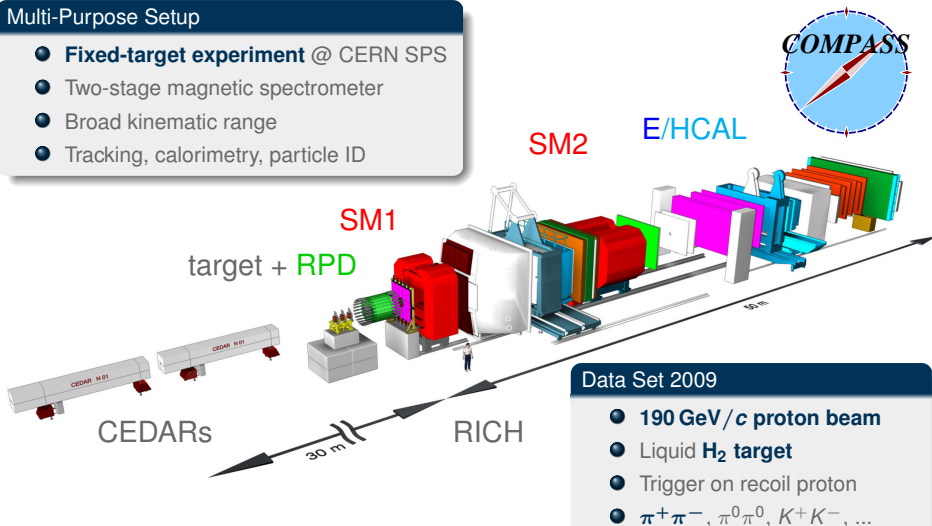




# The COMPASS Experiment

## Multi-Purpose Setup

- **Fixed-target experiment @ CERN SPS**
- Two-stage magnetic spectrometer
- Broad kinematic range
- Tracking, calorimetry, particle ID

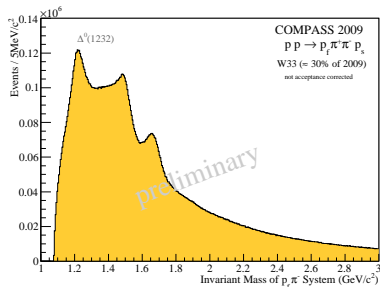
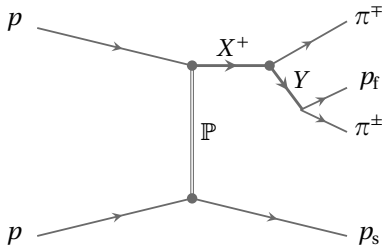


## Data Set 2009

- **190 GeV/c proton beam**
- **Liquid H<sub>2</sub> target**
- **Trigger on recoil proton**
- **$\pi^+\pi^-$ ,  $\pi^0\pi^0$ ,  $K^+K^-$ , ...**



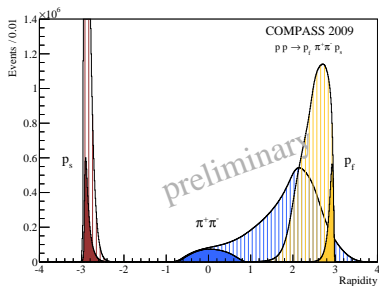
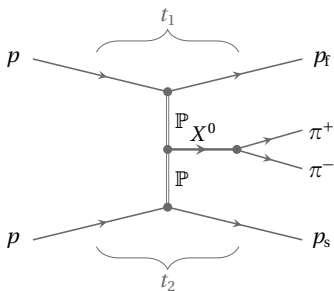
# Central Production of $\pi^+\pi^-$ System



- Baryon resonances in  $p_f \pi^\pm$  subsystems  
 → **Diffractive dissociation** of the beam proton as dominant process



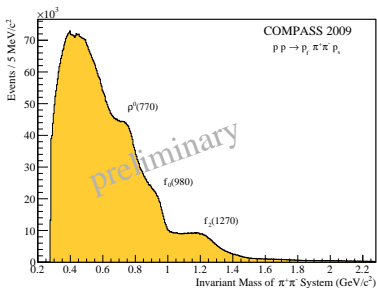
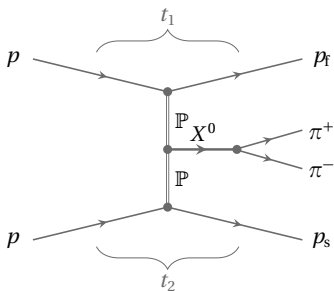
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- Separation between  $p_s$  and  $\pi^\pm$  by trigger on recoil proton  $p_s$



# Central Production of $\pi^+\pi^-$ System

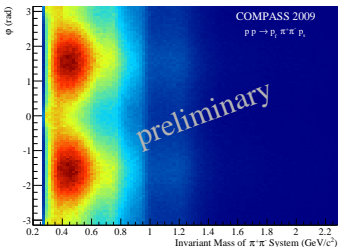
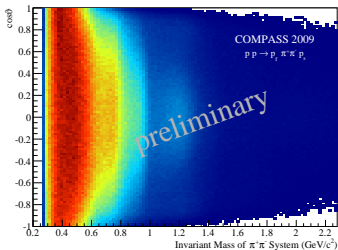


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- **Kinematic separation** between  $p_f$  and  $\pi^\pm$
- Separation between  $p_s$  and  $\pi^\pm$  by trigger on recoil proton  $p_s$
- $\rho(770)$  production → kinematic selection cannot isolate pure DPE sample

⇒ **Two-Body Partial-Wave Analysis (PWA)**

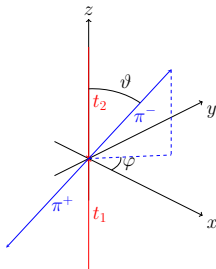


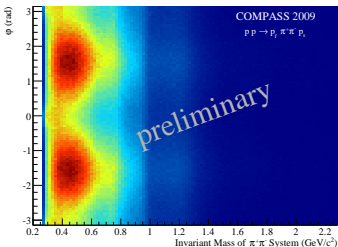
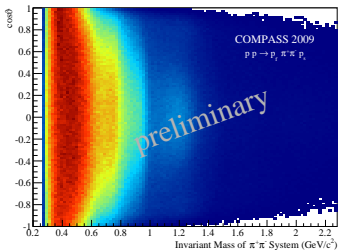
# Partial-Wave Analysis



$$X^0 \rightarrow \pi^+ \pi^-$$

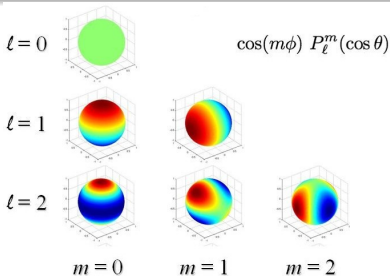
- **Assumption:** collision of two space-like exchange particles
- Decay of  $X^0$  fully described by  $M(\pi^+\pi^-)$ ,  $\cos \vartheta$  and  $\varphi$





$$X^0 \rightarrow \pi^+ \pi^-$$

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- Decay of  $X^0$  fully described by  $M(\pi^+ \pi^-)$ ,  $\cos \vartheta$  and  $\varphi$
- Decompose into complex-valued amplitudes (spherical harmonics) with definite spin and parity







Expand intensity  $I(\vartheta, \varphi)$  into partial-wave amplitudes in narrow mass bins ( $10 \text{ MeV}/c^2$ ):

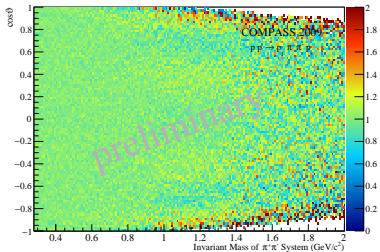
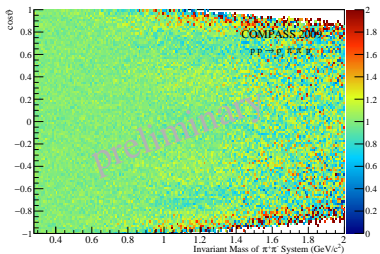
$$I(\vartheta, \varphi) = \left| \sum_{LM} T_{LM} Y_M^L(\vartheta, \varphi) \right|^2$$

- Quantum-mechanical interference between amplitudes with same  $|i\rangle$  and  $|f\rangle$
- **Complex-valued transition amplitudes  $T_{LM}$** , no assumption on mass-dependence
- Significant contributions only from  $L = S, P, D$  and  $M \leq 1$

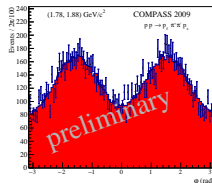
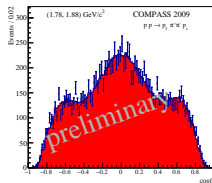
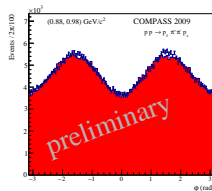
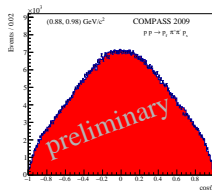
⇒ **Maximum Likelihood Fit in Mass Bins**



# Evaluation of the Fit Quality



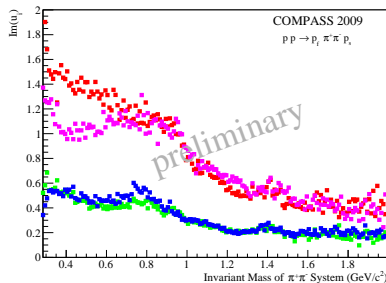
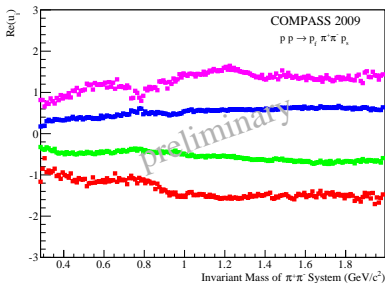
$$I(\vartheta, \varphi) = \left| \sum_{LM} T_{LM} Y_M^L(\vartheta, \varphi) \right|^2$$





- 8 mathematically ambiguous solutions result in the same angular distribution
- Analytical computation via method of **Barrelet Zeros**

S.-U. Chung, [Phys. Rev. D 56 (1997), 7299]



- Real (left) and imaginary (right) part of polynomial roots
- Well separated, imaginary parts do not cross the real axis

⇒ Solutions can be uniquely identified and linked from mass bin to mass bin



# Ambiguities in the $\pi\pi$ Systems

## $\pi^+\pi^-$ System

- 8 different solutions can be calculated analytically
- Differentiation requires additional input (e.g. behaviour at threshold, physics content)

## $\pi^0\pi^0$ System

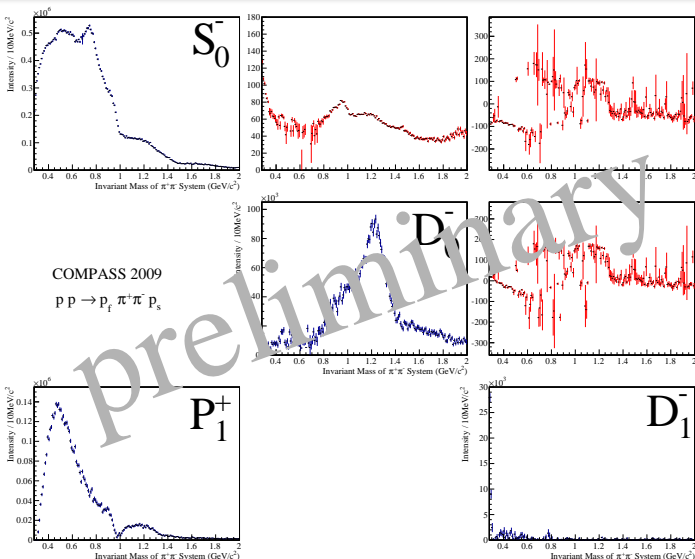
- Identical particles, only even waves allowed
- Reduces number of ambiguities to 2

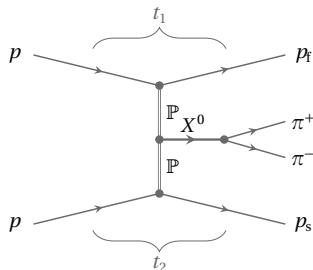
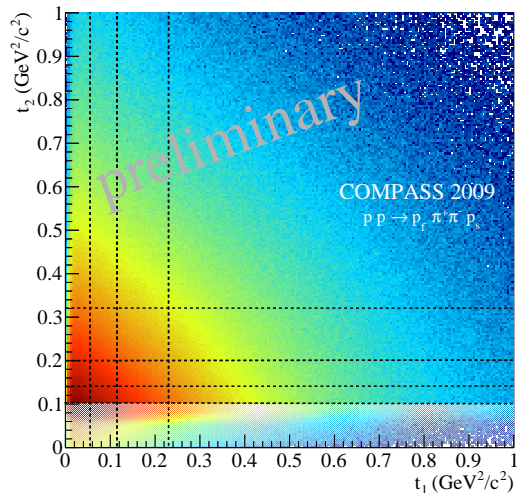
## Combination of $\pi\pi$ Systems

- Consistent picture of the reaction, measured with different parts of experimental setup



# $\pi^+\pi^-$ System: Physical Solution

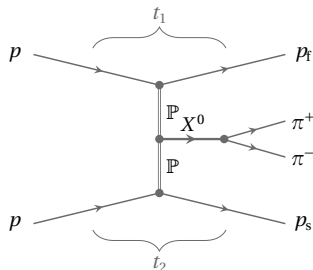
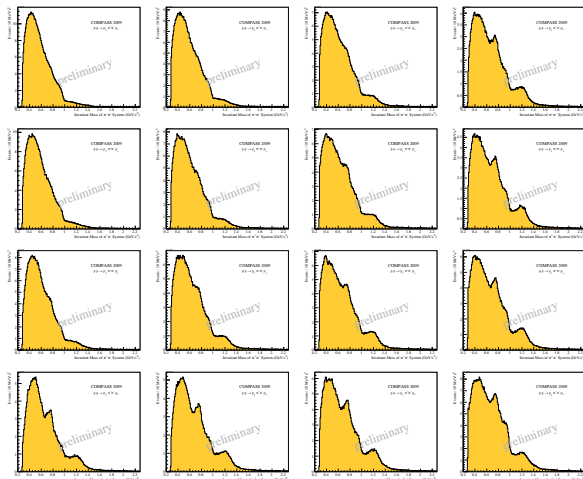




- Disregarded  $t_2 < 0.1 \text{ GeV}^2/c^2$  due to trigger inefficiency
- $4 \times 4$  bins with approximately equal #events ( $\approx 3 \cdot 10^5$ )
- Not symmetric in  $t_{1,2}$ !



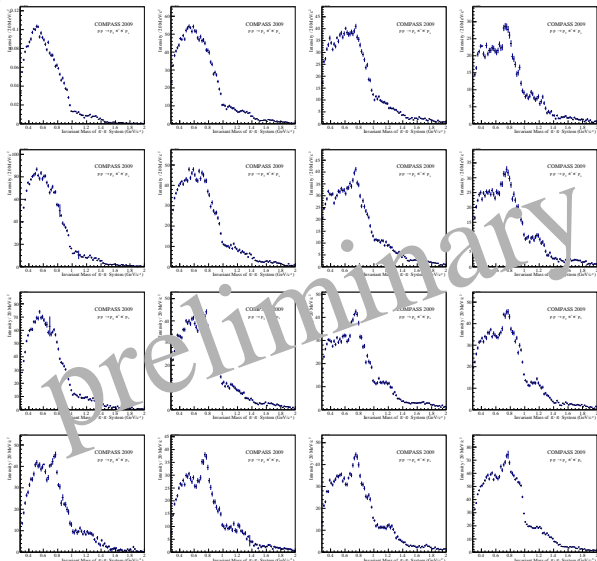
# $t$ -Dependent Analysis



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- $4 \times 4$  bins with approximately equal #events ( $\approx 3 \cdot 10^5$ )
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# Fit to the $\pi^+\pi^-$ System:

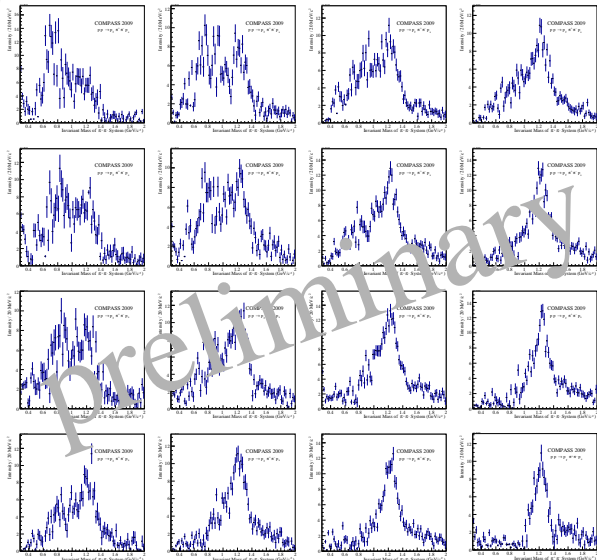

 $t_1 \Rightarrow$ 
 $S_0^-$ 
 $t_2$ 


- Pure S-wave for low  $t_{1,2}$





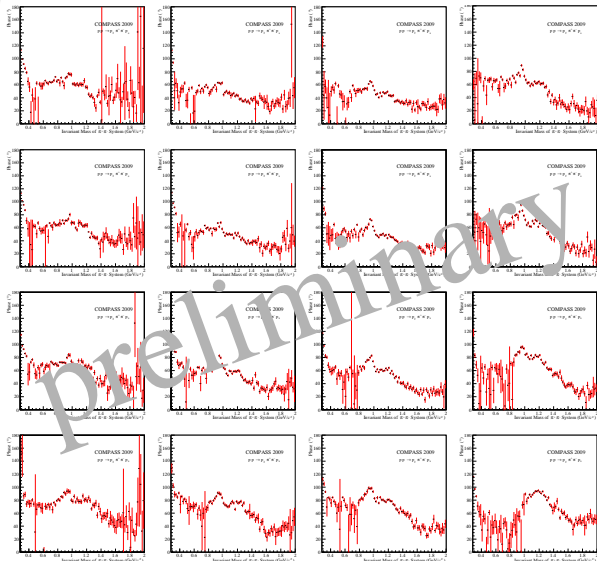
# Fit to the $\pi^+\pi^-$ System:


 $t_1 \Rightarrow$ 
 $D_0^-$ 
 $t_2$ 
 $\Downarrow$ 

- Pure S-wave for low  $t_{1,2}$
- Production of  $f_2(1270)$  increases with  $t_{1,2}$



# Fit to the $\pi^+\pi^-$ System:


 $t_1 \Rightarrow$ 

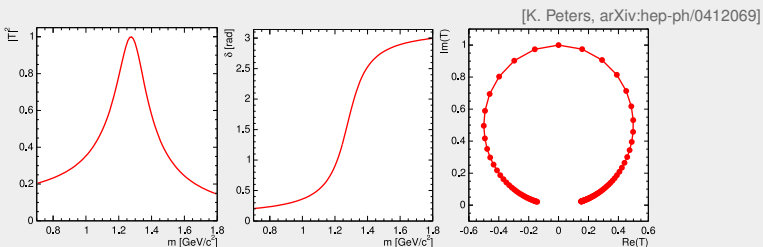
$$S_0^- - D_0^-$$

 $t_2$ 


- Pure S-wave for low  $t_{1,2}$
- Production of  $f_2(1270)$  increases with  $t_{1,2}$
- Phase approx. stable  $\Rightarrow t$ -dependence of production mechanisms



## Resonance: Relativistic Breit-Wigner Function



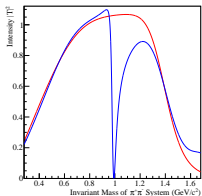
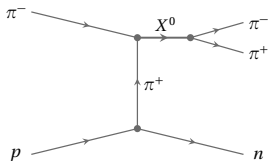
## Non-Resonant Contribution

Phase-space with exponential damping (phenomenological)

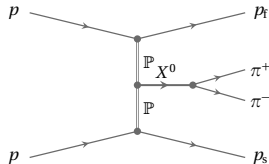
- Sum with complex-valued coefficient (**strength + phase**) for each component



# Unitarity Constraints

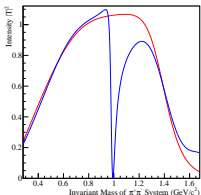
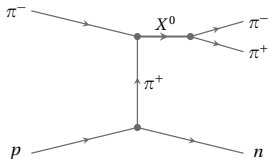


- **Watson theorem** relates phase of prod. processes
- M solution from Au, Morgan, Pennington Phys. Rev. D 35 (1987) 1633
- $\pi\pi$  ampl. vanishes near threshold (Adler zero)



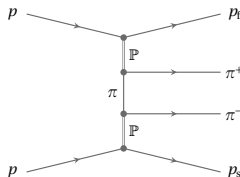


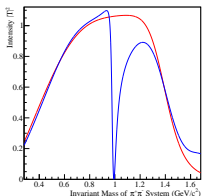
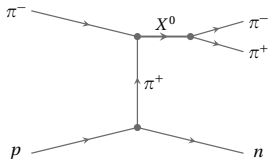
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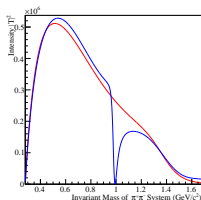
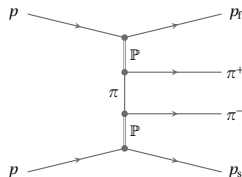
$$\mathbb{T}_{\text{red}} = \frac{\mathbb{T}}{s - s_0}$$





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$$\mathbb{T}_{\text{red}} = \frac{\mathbb{T}}{s - s_0}$$



- First fit of  $S$ -wave amplitude **with interference** to  $D$ -wave
- **Constrain** masses below 1 GeV/ $c$  with  $\pi\pi$  scattering data
- Interpretation with mass dependent parametrisation **on it's way!**



## COMPASS is a unique experiment to study **Light Mesons in Central Production**

- **Large samples of precision data** for many final states
- **Novel analysis schemes** provide insight in hadron dynamics
  - $t$ -dependent analysis distinguishes between production mechanisms
  - Interference of  $S$ - and  $D$ -waves helps to identify resonant components
- **Consistent picture of scalar sector** through combination of different approaches



## COMPASS is a unique experiment to study **Light Mesons in Central Production**

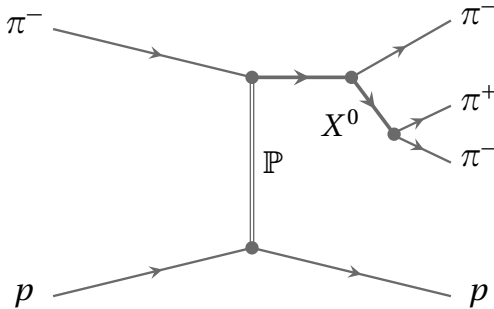
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Thank you for your attention!





# Subsystem in Diffractive Dissociation



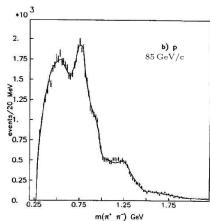
**See F. Krinner's Presentation!**



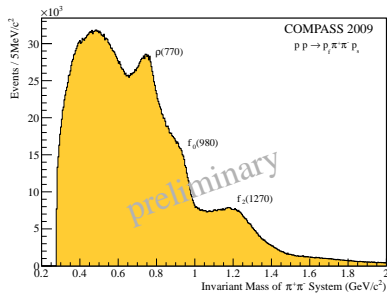
## Backup Slides



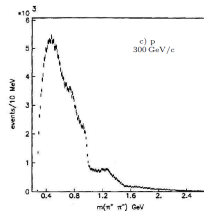
T.A. Armstrong et al. [Z. Phys. C51 (1991)]



$$\sqrt{s} = 12.7 \text{ GeV}/c^2$$

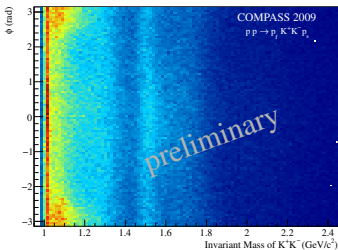
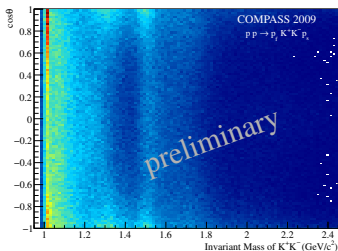


$$\sqrt{s} = 18.9 \text{ GeV}/c^2$$

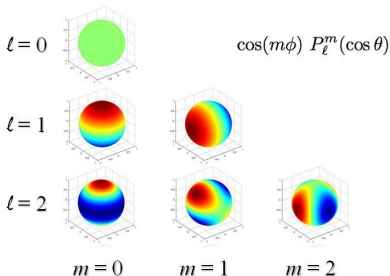


$$\sqrt{s} = 23.7 \text{ GeV}/c^2$$

- Production of  $\rho(770)$  disappears rapidly with increasing  $\sqrt{s}$
- Low-mass enhancement and  $f_0(980)$  remain practically unchanged  
→ characteristic for  $s$ -independent Pomeron-Pomeron scattering
- Kinematic selection cannot single out pure DPE sample

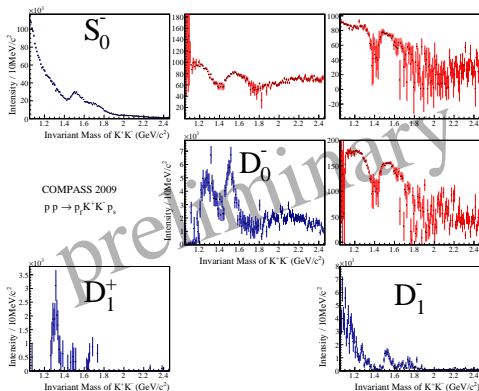

 $X \rightarrow K^+ K^-$ 

- **Assumption:** collision of two space-like exchange particles ( $\mathbb{P}, \mathbb{R}$ )
- Decay of  $X^0$  fully described by  $M(K^+ K^-)$ ,  $\cos(\vartheta)$  and  $\varphi$
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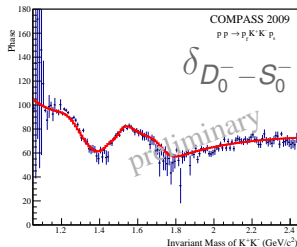
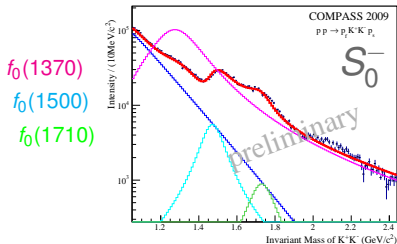
# Fit to the $K^+K^-$ System



- Similar partial-wave analysis of  $K^+K^-$ -system
- Odd waves do not play a significant role above the  $\phi(1020)$ -mass  
 $\Rightarrow$  Reduction of ambiguities



# Mass-Dependence of $K^+K^-$



BW contributions  
non-resonant contribution  
coherent sum

Interference of S and D

distinguish resonances from  
non-resonant contribution

